Recent Updates on fiTQun, a New Event Reconstruction Algorithm for Water Cherenkov Detectors

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Introduction

- fiTQun: New Super-K event reconstruction algorithm
 - Can be applied to any Hyper-K detector configuration straightforwardly
- A maximum likelihood fitter
 - Using the charge and time information from the PMTs, fit particle track parameters by maximizing the likelihood function:

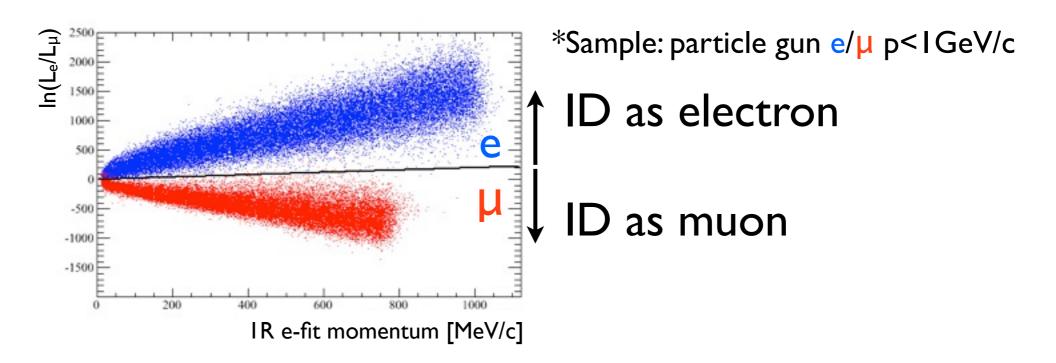
$$L(\mathbf{x}) = \prod_{i} \Pr(i \text{unhit} | \mathbf{x}) \prod_{i} \Pr(i \text{hit} | \mathbf{x}) f_q(q_i | \mathbf{x}) f_t(t_i | \mathbf{x})$$

Unhit probability Hit probability Charge likelihood Time likelihood

 All parameters (vertex, direction, momentum etc.) are fit simultaneously

PID/Number of Rings

- Distinguish between different event topologies by making a cut on the best-fit likelihood ratio:
 - e.g. One-ring e/μ separation by cutting on the likelihood ratio of IR-e and IR-μ hypotheses



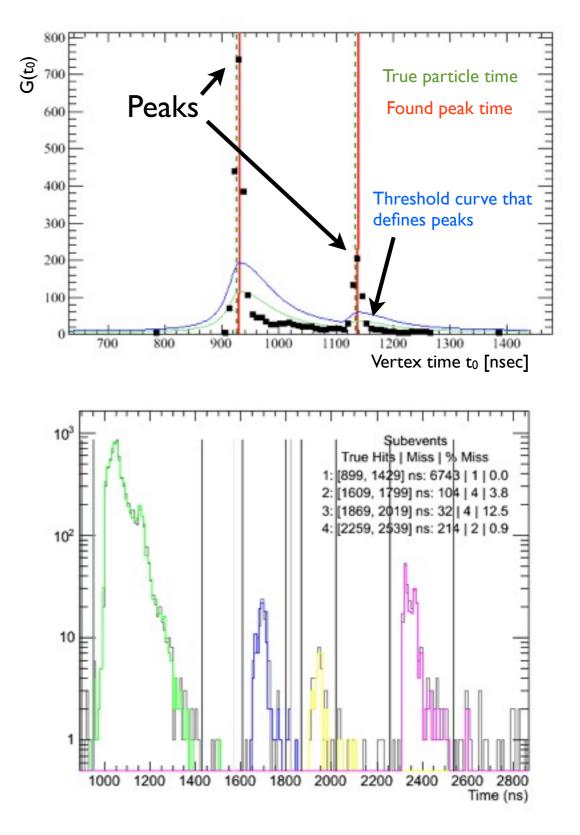
• Separation of e/π^0 , μ/π^+ , and number of ring determination are done in a similar manner

Current features (New since Aug.)

- Subevent algorithm Count and fit decay electrons
 - Peak finder, time clustering
 - In-gate decay charge masking & fitting
- One ring fit (e, μ , π^+)
 - Reduced fit failures by improving parameter seeding
- π^0 fit Further seeding optimization
- Multi-ring fit & Ring counting
 - 2/3/4 ring fits with all possible combinations of e/µ/ π^+ rings

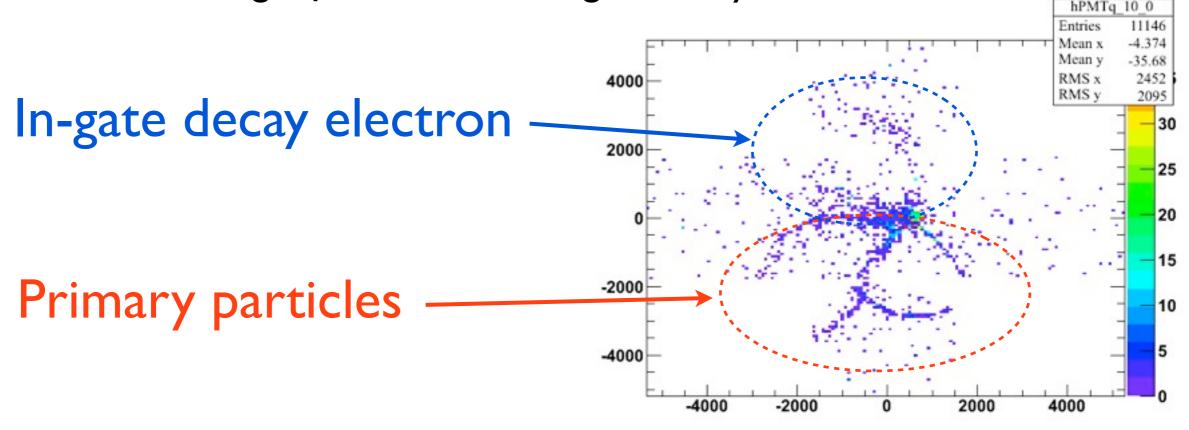
Peak Finder & Clustering

- Peak finder
 - Determine the number and time of subevents (primary particles, decay electrons) in an event
 - Use TOF-corrected hit time
- Time clustering (spliTChan)
 - Separate subevents into different time windows in raw hit time, so that they can be fitted independently



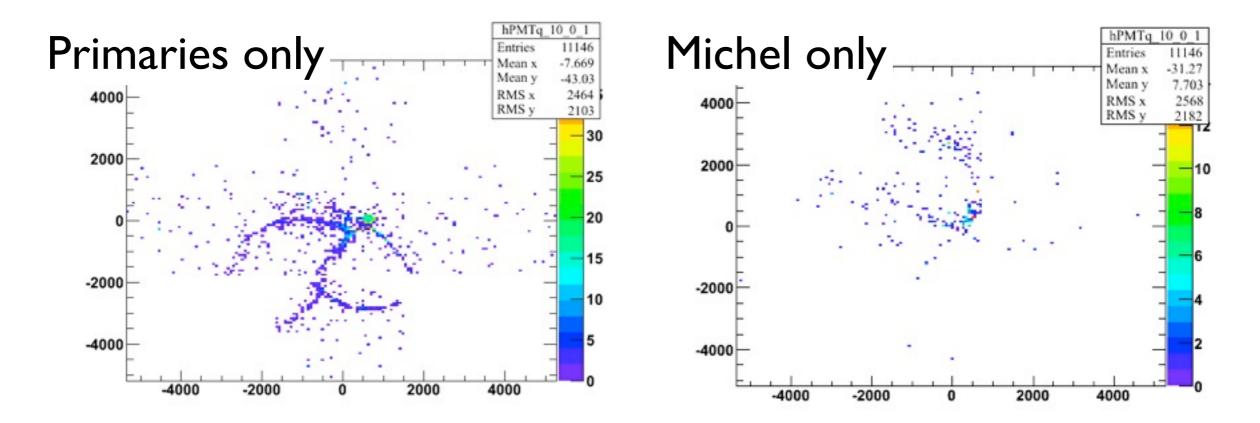
In-gate Decays

- Some clusters have multiple subevents
 - e.g. when decay happens early (in-gate decays)
- Hits from multiple subevents are present in the same time window
 - Primary particle momentum is overestimated
 - Due to charge from in-gate decay electrons
- ~1/6 of single- μ events have in-gate decays

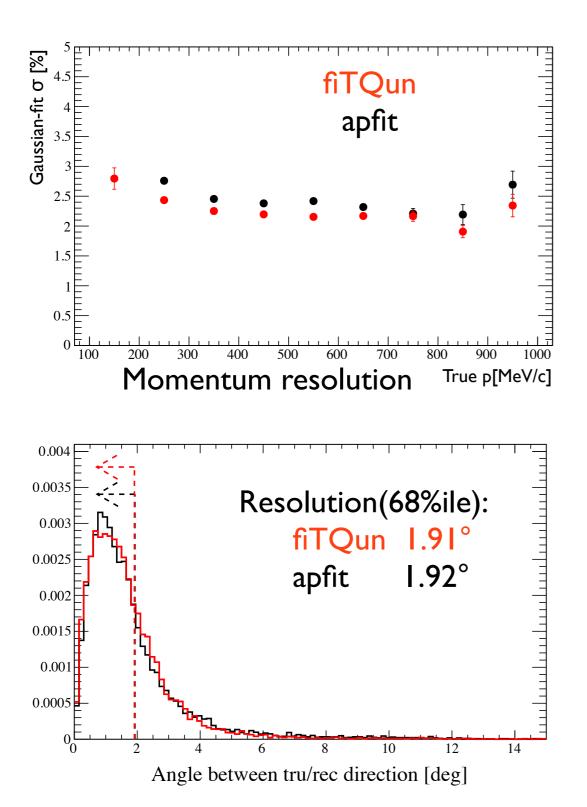


Charge Masking & Fitting In-gates

- Fit each in-gate subevent found by the peak finder by masking out hits that are not caused by the subevent
 - Masking suppresses the momentum overestimation
- Vertex, direction and momentum is reconstructed for ALL decay electrons that are found by the peak finder



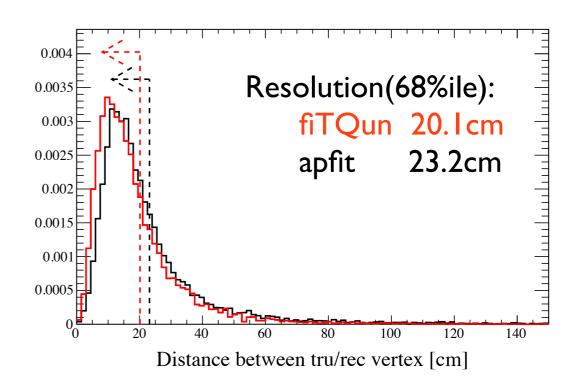
Single Muon Fit Resolution



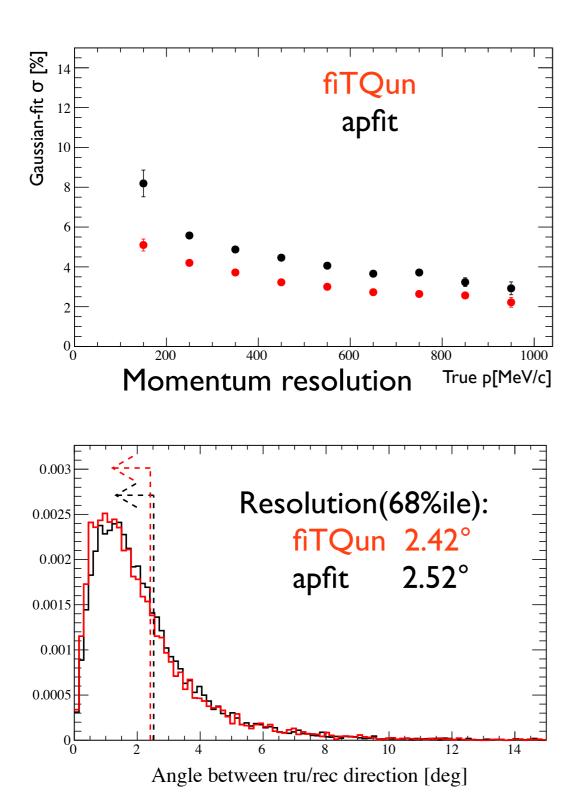
*Sample information: T2K ν_μ CCQE, fully contained, true fiducial volume, one-ring events

Better momentum and vertex resolution compared to apfit

**Nuclear de-excitation γ's, decay electrons are present in this sample

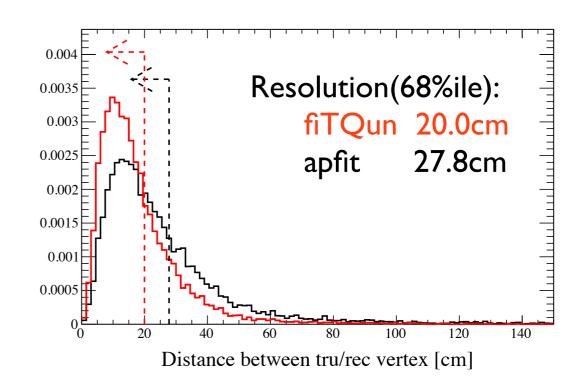


Single Electron Fit Resolution

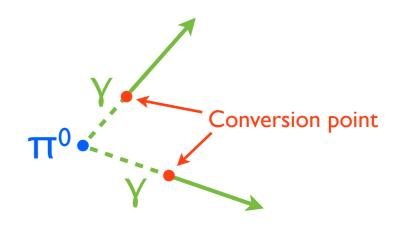


*Sample information: T2K v_e CCQE, fully contained, true fiducial volume, one-ring events

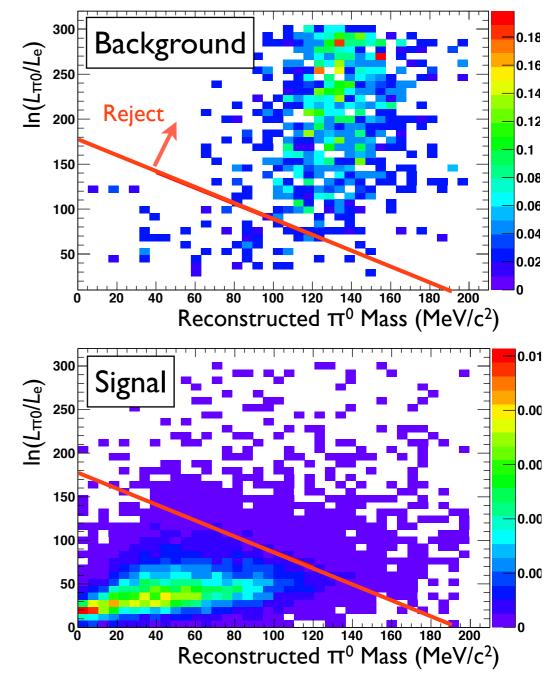
More significant resolution improvement for electrons



π⁰ Fitter

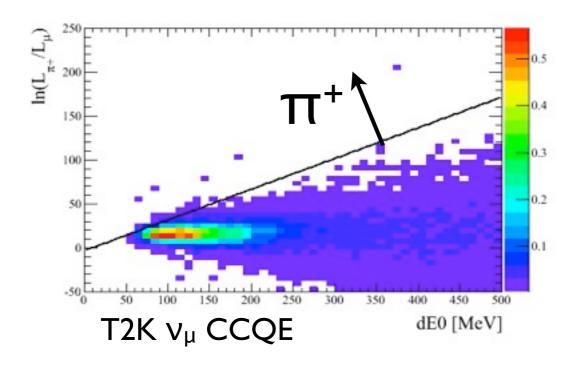


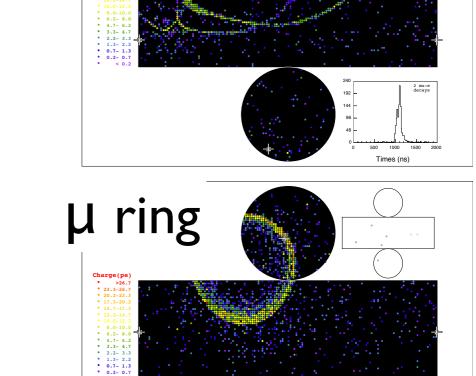
- Dedicated π^0 fitter
 - Fit the two decay Y rings, considering Y conversion length
- Able to find low energy γ ring well
- Provides significant improvement of π^0 background rejection for T2K v_e appearance
 - Make a cut using likelihood ratio of π^0 and I-ring electron hypothesis
 - π^0 background reduced to <1/3 compared to standard V_e selection

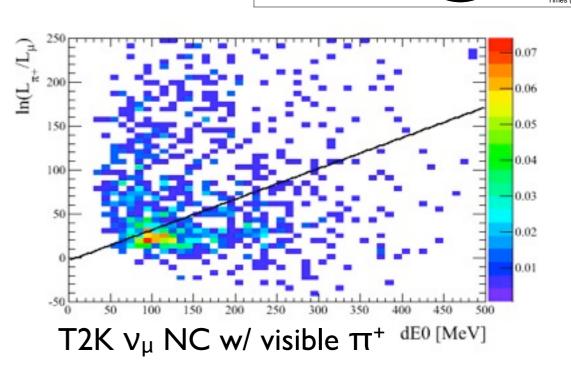


π^+ Fitter

- π⁺ often hadronically interacts with nuclei
 - Produces sharp, hollow rings
- Fit the π⁺ rings, with an additional fit parameter which characterizes the thickness of the ring
- μ/π^+ separation seen in the likelihood ratio to one-ring μ fit



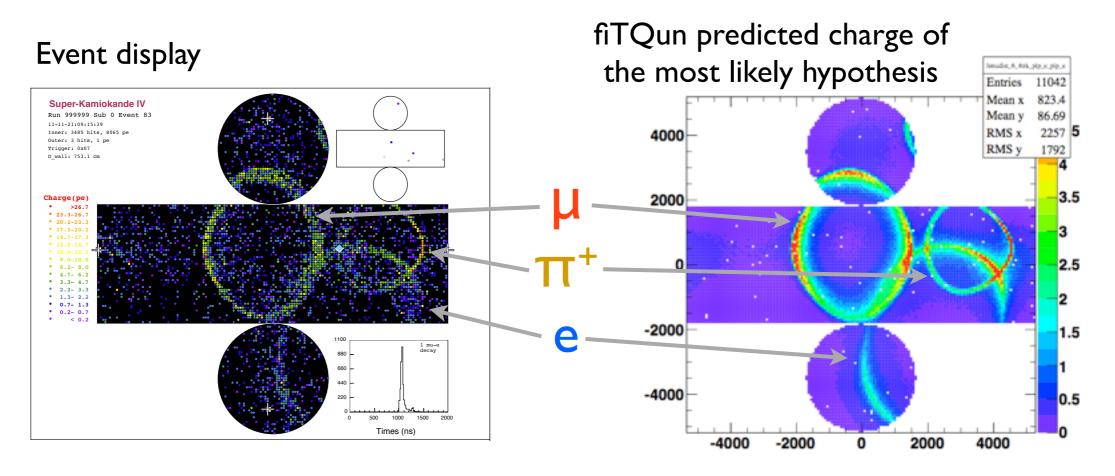




 π^+ ring

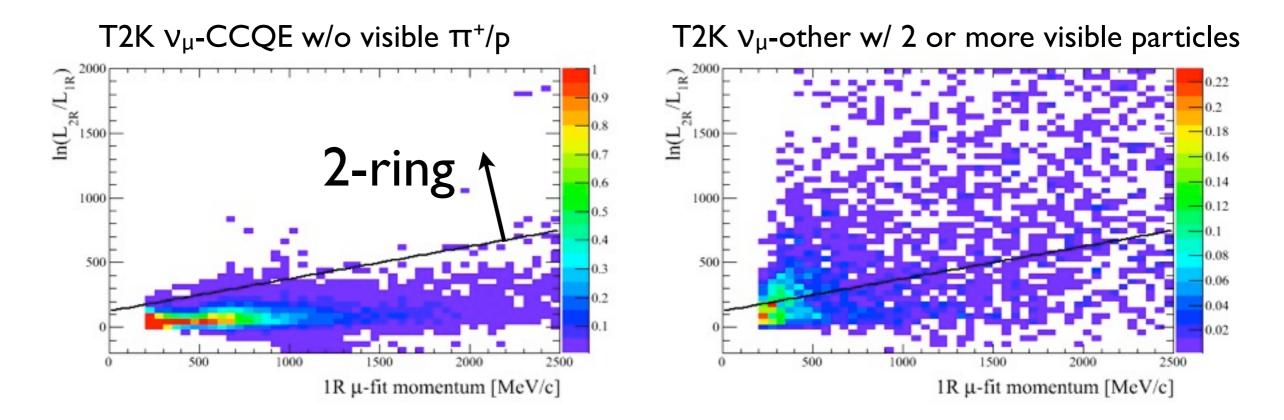
Multi-Ring Fitter

- Construct multi-ring hypotheses by combining I-ring framework
- Multi-ring fitter fit up to four rings, using e & π^+ rings
 - π⁺ hypothesis covers µ-ring as well, since µ produces similar charge pattern as π⁺, with a ring filled inside
- Accept the hypothesis with the best likelihood to PID each ring



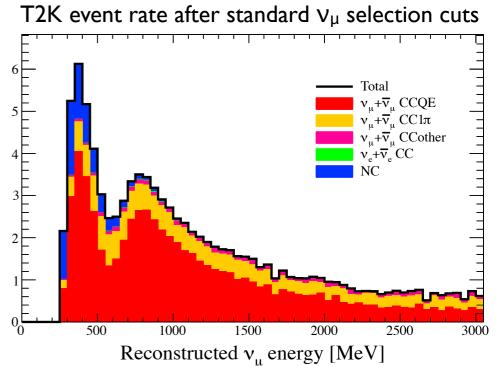
Ring counting

- To determine the number of rings, make a cut on the likelihood ratio between best-fit n-ring and (n+1)-ring hypotheses
 - e.g. One-ring cut is done by cutting on the likelihood ratio of I-ring and 2-ring hypotheses



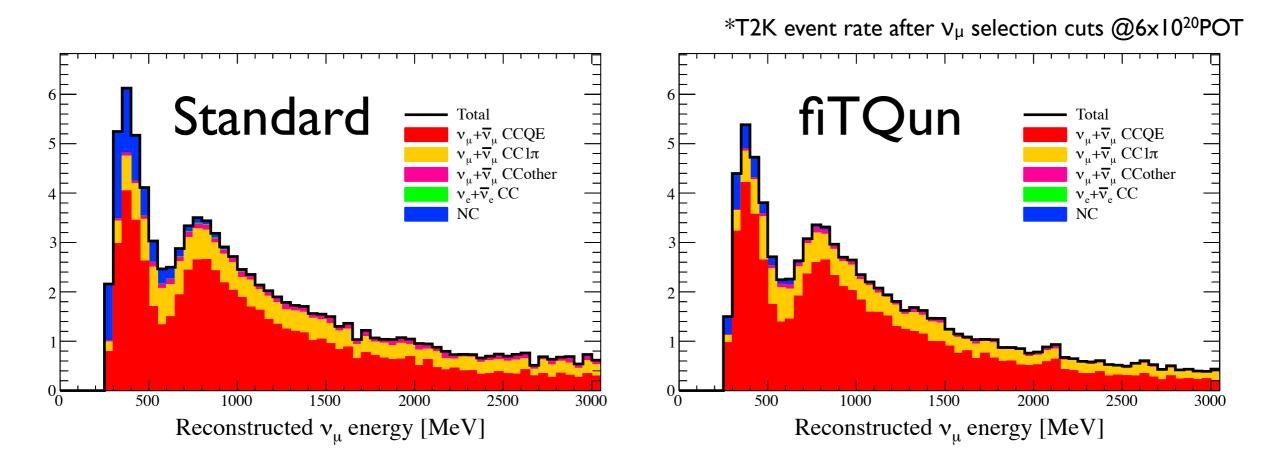
Improving T2K ν_{μ} Disappearance

- Main backgrounds are v_{μ} CCI π and NC
- Around 600MeV(oscillation dip), about half of the entries are backgrounds, filling up the dip
- One of the largest systematics come from NC selection efficiency



- >100% error assigned to NC events in published analyses
- Reducing NC backgrounds is crucial for a precise measurement
 - Most background are due to π^+ ring mis-identified as muon
- Use fiTQun π^+ fitter to reduce π^+ backgrounds

Standard vs. fiTQun v_{μ} selection



Reduction rate to
standard selection: $V_{\mu} + \overline{V}_{\mu}$ CCQE4.8% $V_{\mu} + \overline{V}_{\mu}$ CCI π 21.5% $V_{\mu} + \overline{V}_{\mu}$ CCoth.53.7% $V_e + \overline{V}_e$ CC92.1%NC61.2%

- Significant reduction of NC background by π^+ cut
- Large CC non-QE reduction by fiTQun 1-ring cut
- Signal efficiency loss is mostly at >3GeV
 - fiTQun efficiency is higher at <IGeV
- Signal purity 60.6%→69.3%

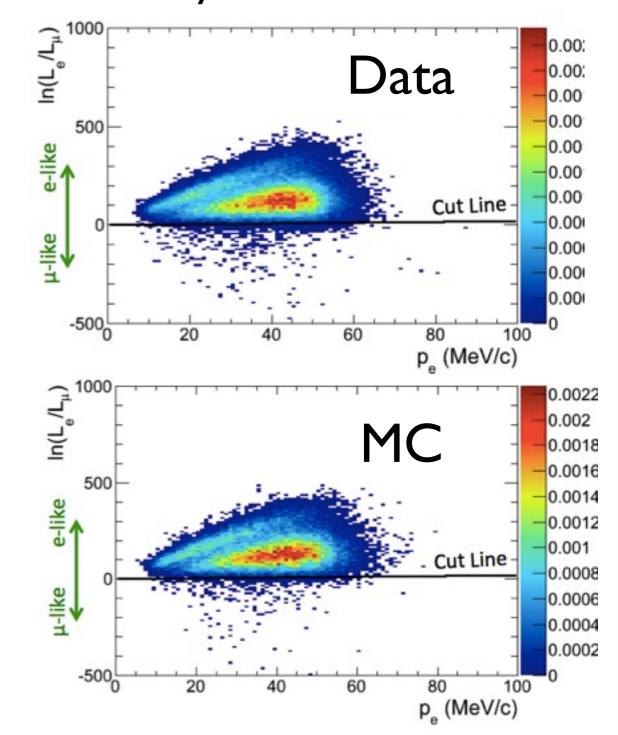
Fitting complex event topologies

- The multi-ring fitter is applicable to event topologies that are relevant to proton decay and atmospheric V
- e.g. for proton decay:
 - e+e+e fit for e⁺+ π^0 , e+e+ π^+ fit for π^0 + π^+
- fiTQun multi-ring fitter is sensitive to dim rings in the presence of bright rings
 - Improve signal efficiency from current analyses
- Background reduction by new particle hypotheses, better particle identification and improved resolution
- One can also easily construct arbitrary analysis-specific event hypotheses multi-ring fitter result can be used as a seed
 - Imposing kinematic constraints potentially improves power

Validation Using SK Data

- Data/MC agreement has been studied using SK control sample:
 - Stopping cosmic-ray muons & decay electrons
 - Atmospheric neutrino
 - Hybrid π⁰
- Reasonable agreement seen in various distributions
 - Currently studying the sources of discrepancies
 - Simulation of light reflections, nuclear de-excitation γ etc.

Decay-e PID likelihood



Adapting fiTQun for Hyper-K

- Interfacing fiTQun with WCSim(Blair Jamieson)
 - First check fitter response with SK geometry
- The modularized design of fiTQun allows relatively easy adaptation to Hyper-K
- Other than the scattered light calculation, fiTQun runs properly on any detector geometry
- Start by approximating scattered light using the existing machinery for SK(assume cylindrical tank)
- As tank geometry becomes ready in WCsim, generate new scattering table which allows precise calculation of scattered light in HK

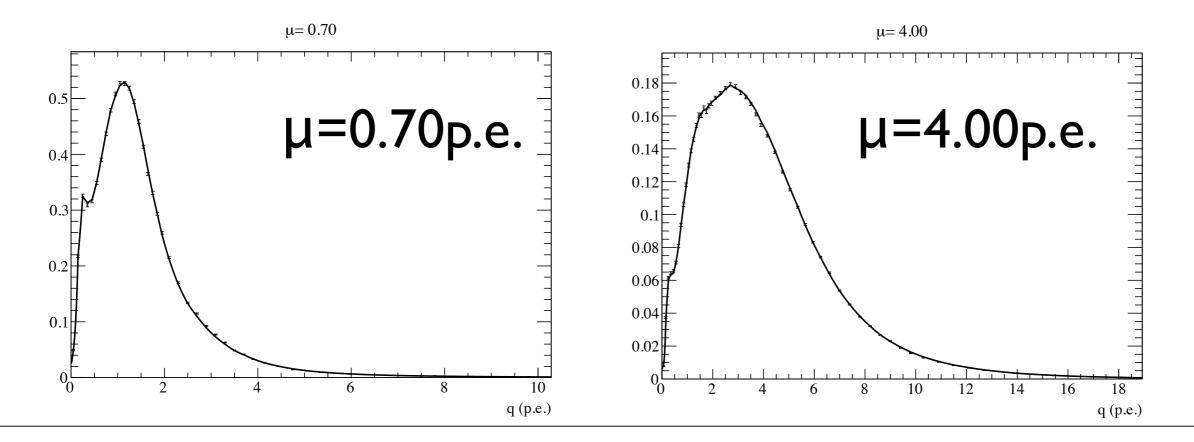
Summary

- fiTQun demonstrates improved particle identification performance and resolutions compared to the existing SK reconstruction framework
 - New particle hypothesis such as π^+
- Significant background reduction is expected in various high-energy physics studies at SK/HK
- Functions that are essential for T2K, atmospheric V and proton decay analyses are now all available
- Validation using SK control sample is ongoing
- Started modifying the code to support Hyper-K

Backup

Charge Likelihood

- Given the mean # of p.e.'s liberated at i-th PMT...
 - Hit/unhit prob. \rightarrow Poisson prob.+corrections
 - Charge likelihood: $f_q(q|\mu)$
 - Probability of observing charge q given mean μ



Predicted Charge µ

- Expected number of photoelectrons liberated at each PMT, given track parameters X
 - $P_{\rm hit}, f_q, f_t$: functions of μ
- For direct light, predicted charge is:

 $\mu^{\rm dir} = \Phi(p) \int dsg(p, s, \cos\theta) \Omega(R) T(R) \epsilon(\eta)$ Light yield Solid angle subtended by PMT PMT angular acceptance

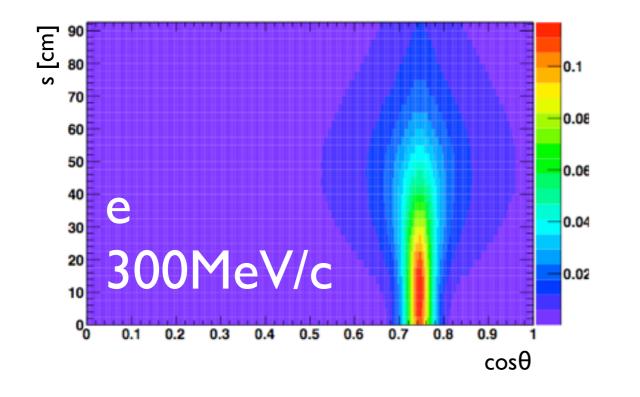
- s: Distance particle traveled along the track *R, θ , η are functions of s
- Scattered/reflected light is also treated separately

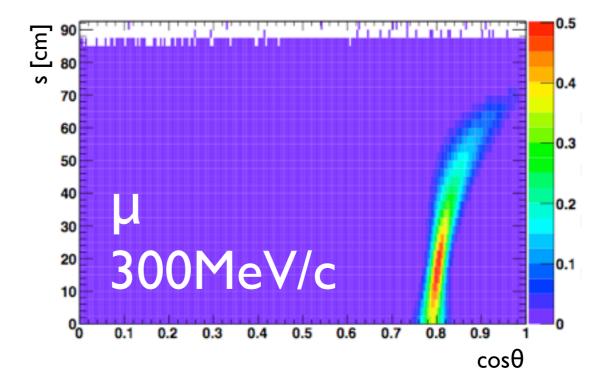
PMT

Cherenkov Emission Profile

$$\mu^{\text{dir}} = \Phi(p) \int ds g(p, s, \cos \theta) \Omega(R) T(R) \epsilon(\eta)$$

- Fraction of photons emitted in direction $\boldsymbol{\theta}$
- Profiles are different between particle types
 - Creates different charge patterns



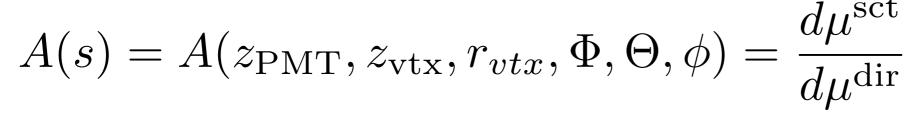


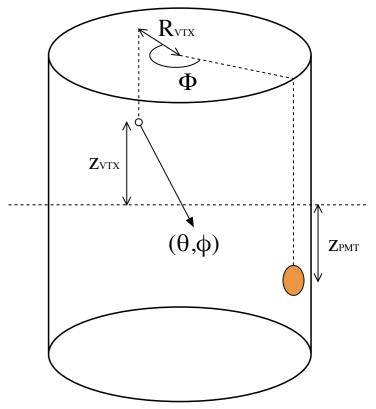
PMT

Scattered Light

$$\mu^{\text{sct}} = \Phi(p_0) \int ds \rho(s) \Omega(s) T(s) \epsilon(s) A(s)$$

Scattering table:





- Ratio of scattered light to direct light
- Using SKDETSIM, shoot 3MeV/c electrons(point-like Cherenkov source) randomly, and fill a 6-D histogram
 - Multiple scattering was turned off
- Linearly interpolate at run time

Parabolic approximation

Integral is CPU-intensive

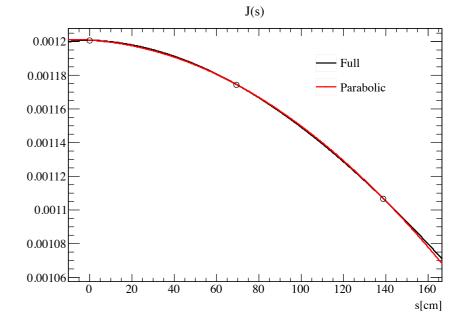
$$\mu^{\rm dir} = \Phi(p) \int ds g(s) \Omega(s) T(s) \epsilon(s)$$

Acceptance factors $J(s) = \Omega(s)T(s)\epsilon(s)$ vary slowly as a function of s

Approximate it by parabola, perform the integral in advance

$$\mu^{\text{dir}} = \Phi(p) \int dsg(s) (j_0 + j_1 s + j_2 s^2)$$

= $\Phi(p) (I_0 j_0 + I_1 j_1 + I_2 j_2)$

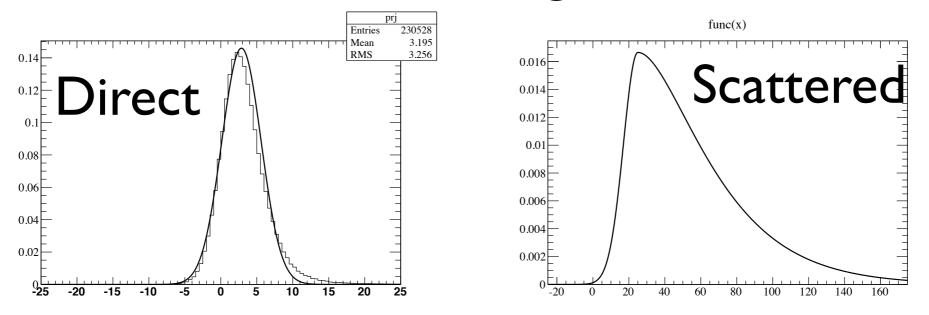


500cm

Determine j_n , read off the integral values I_n from table Similar thing is done for scattered light

Time Likelihood

 Make primitive time likelihood functions separately for direct and scattered light



• Based on the relative strength of direct/scattered light, time PDF is constructed on the fly:

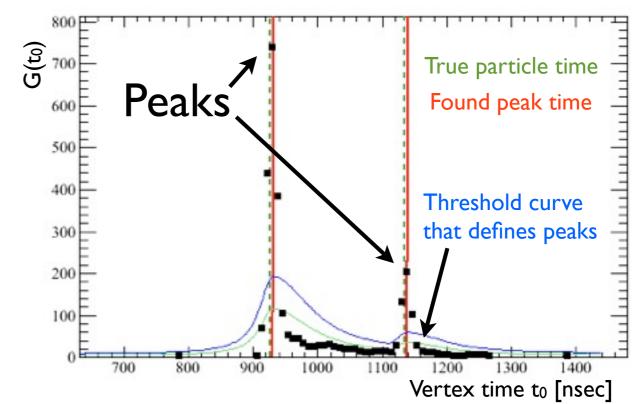
$$f_t(t_c) = w \cdot f_t^{\text{dir}}(t_c) + (1 - w) \cdot f_t^{\text{sct}}(t_c)$$
$$w = \frac{1 - e^{-\mu_{\text{dir}}}}{1 - e^{-\mu_{\text{dir}}}e^{-\mu_{\text{sct}}}} \qquad \textbf{t_c: corrected time}$$

Counting decays: Peak Finder

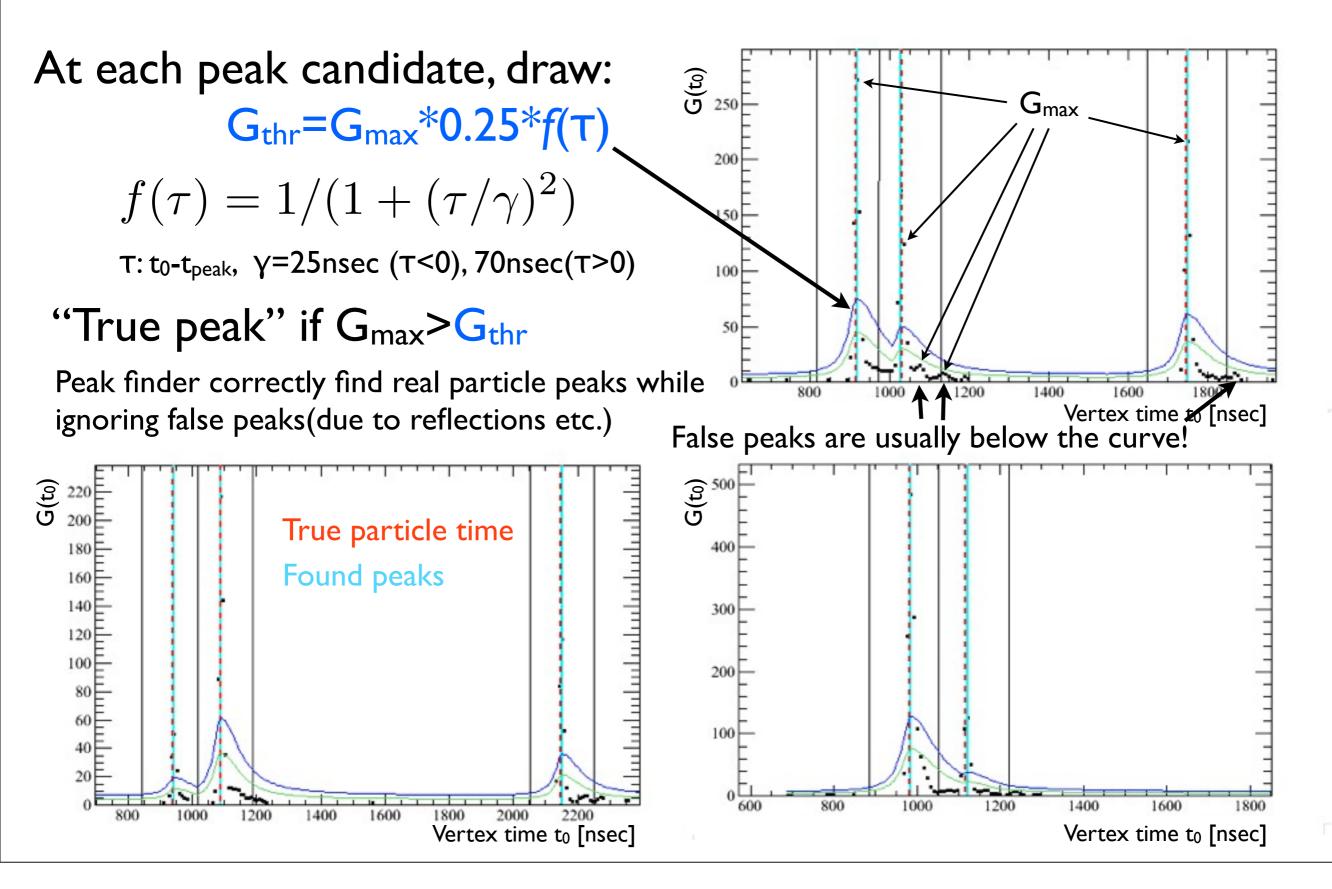
- Provides with the number and time of decay e's in an event
- Hit-time based vertex goodness:

$$G(\mathbf{x}, t_0) = \sum_{\text{hit}} \exp(-(T_{\text{res}}^i/\sigma)^2/2) \qquad T_{\text{res}}^i = t_{\text{hit}}^i - t_0 - |\mathbf{R}_{\text{PMT}}^i - \mathbf{x}|/c_n$$

- G is large for correct vertex position \boldsymbol{x} and time t_0
- fiTQun vertex pre-fitter fit \mathbf{x} , t_0 by maximizing $G(\mathbf{x}, t_0)$
- Using the pre-fitter vertex, scan trough t₀ evaluating the goodness, and search for peaks of G(t₀) that correspond to particle time

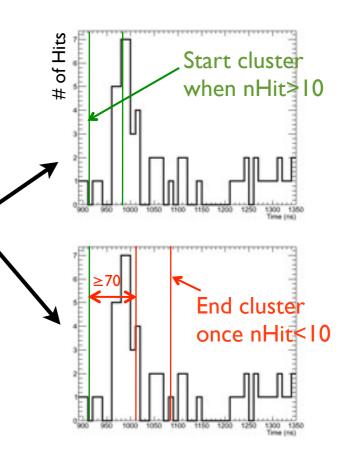


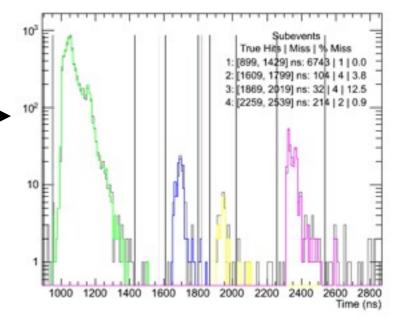
True Peak Selection



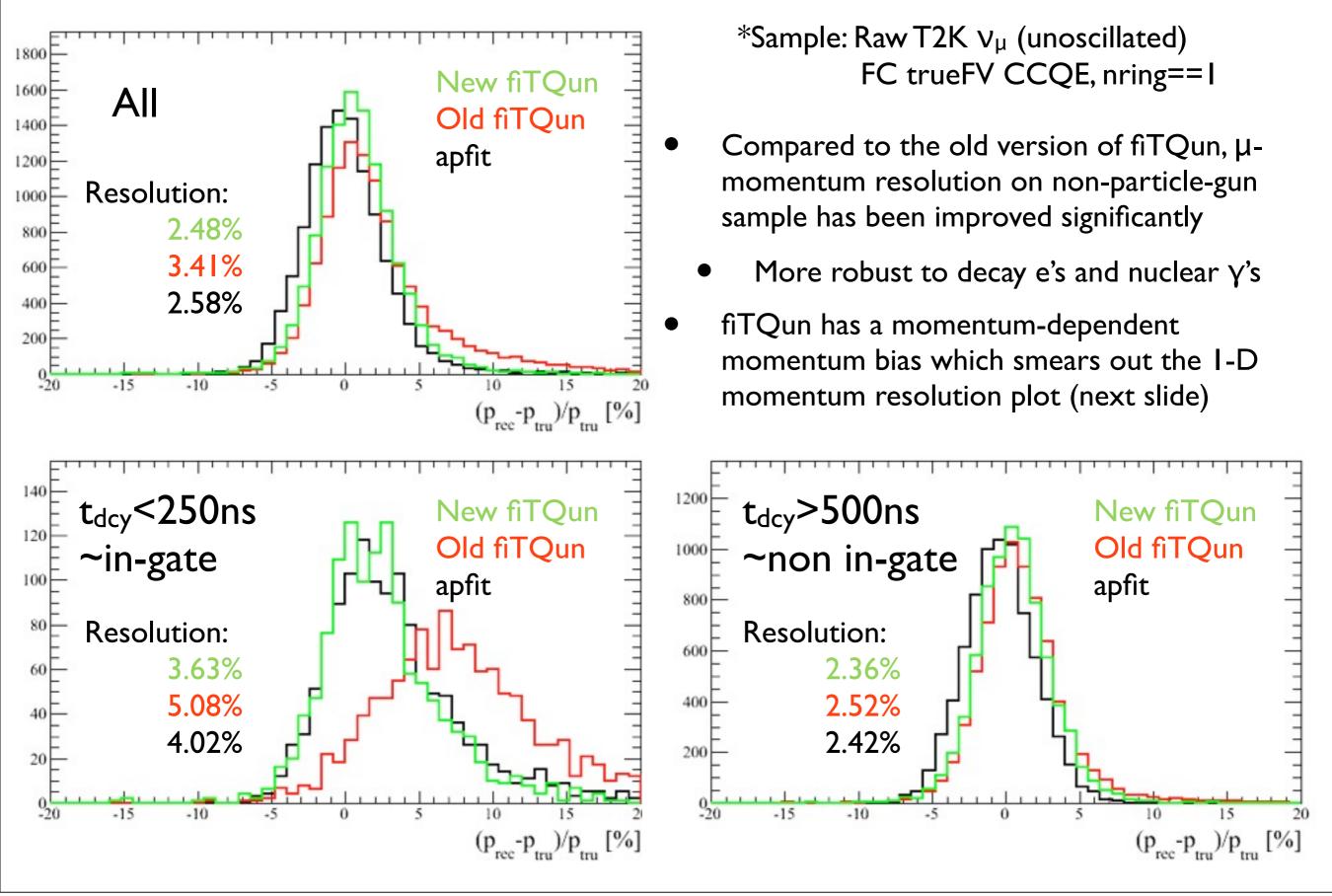
Clustering algorithm(spliTChan)

- Scan through the raw hit-time distribution(by sliding a 70ns window) and look for clusters of hits
- Separate sub-events(primary particles, decay electrons) into different time windows, so that they can be fitted independently
- Can identify and isolate most particles that are well separated in time

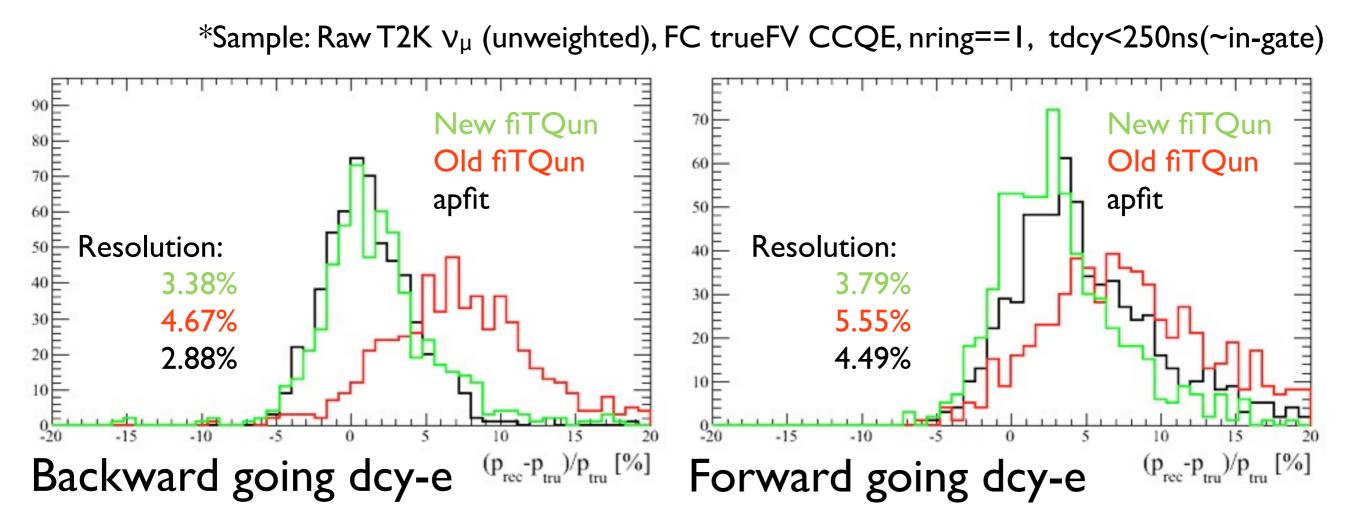




$CCQE \ \mu \ momentum \ resolution$



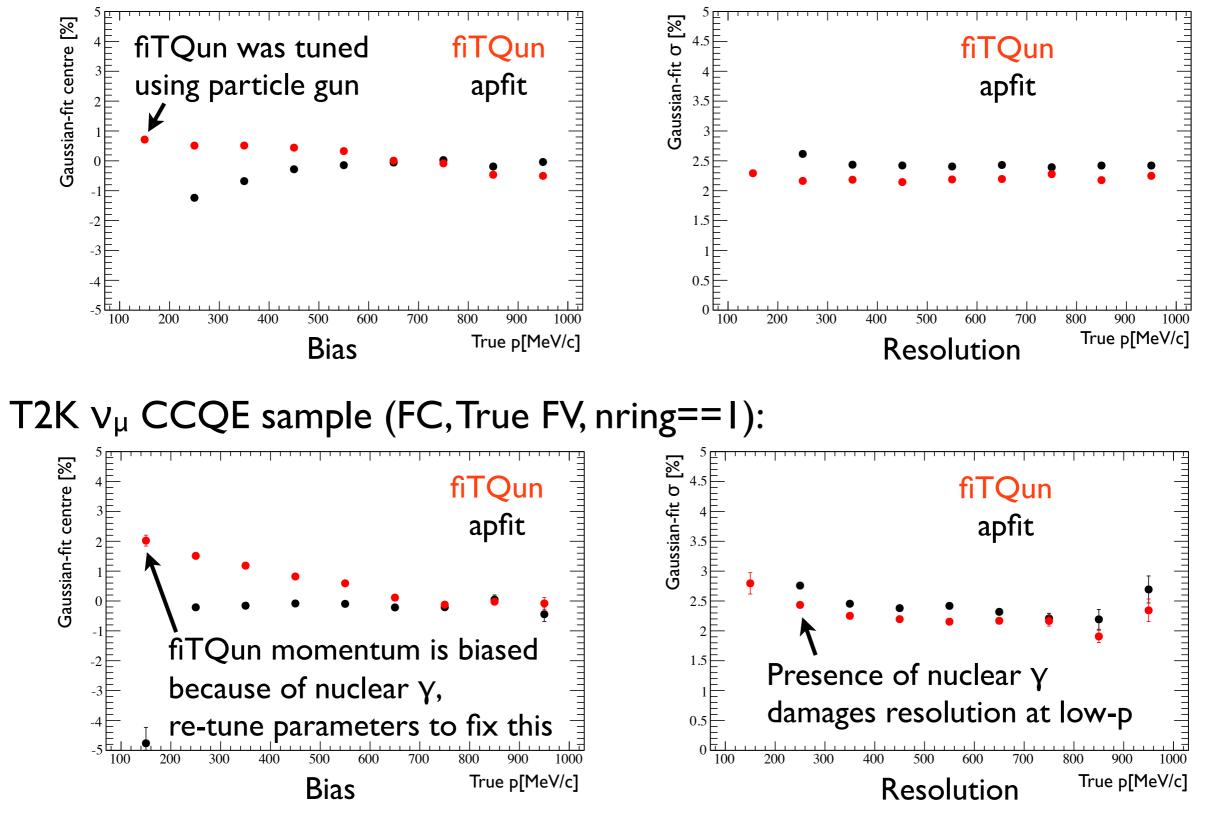
Overlapping charge



- Hits caused by direct light from Michel's are masked
- When charge from Michel rings overlap with primary rings, those additional charge wouldn't be removed by the masking
 - Momentum gets overestimated \rightarrow tail on the right side
- Reflected light from Michel's also causes some overestimation

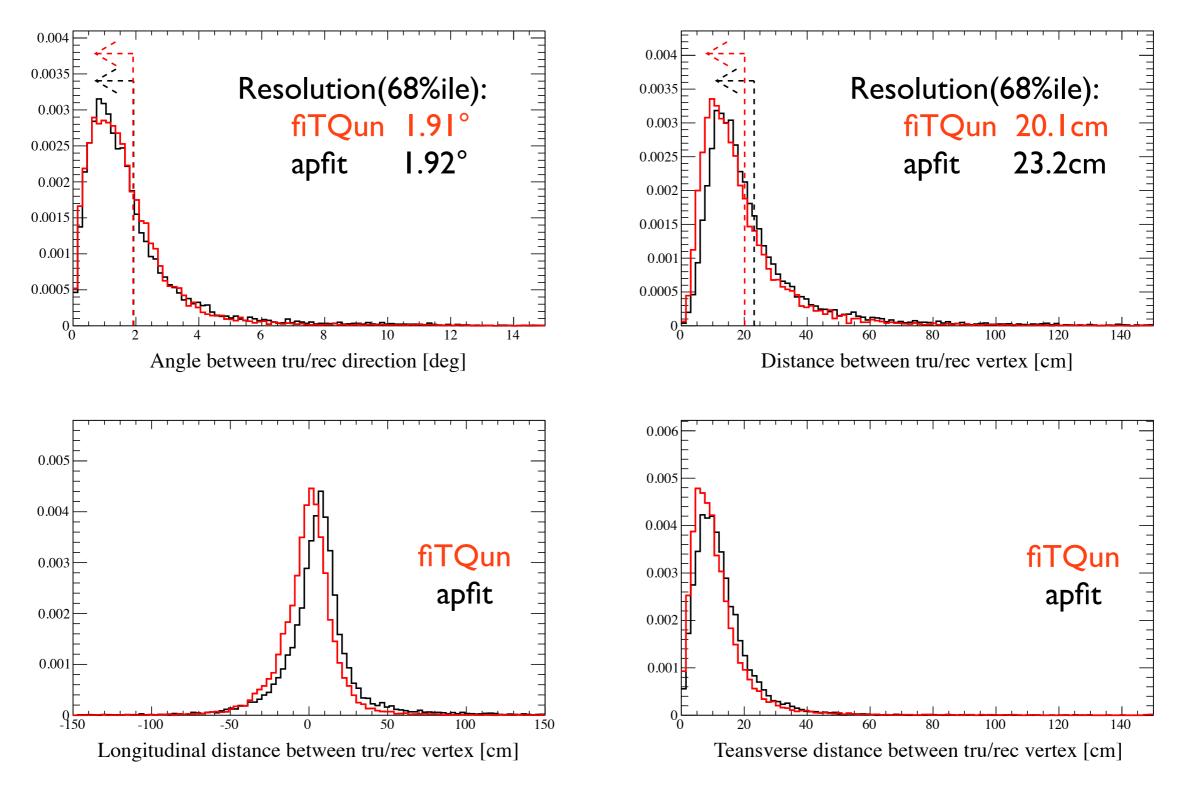
Muon momentum resolution

Muon particle gun sample (FC, True FV, nring==1):



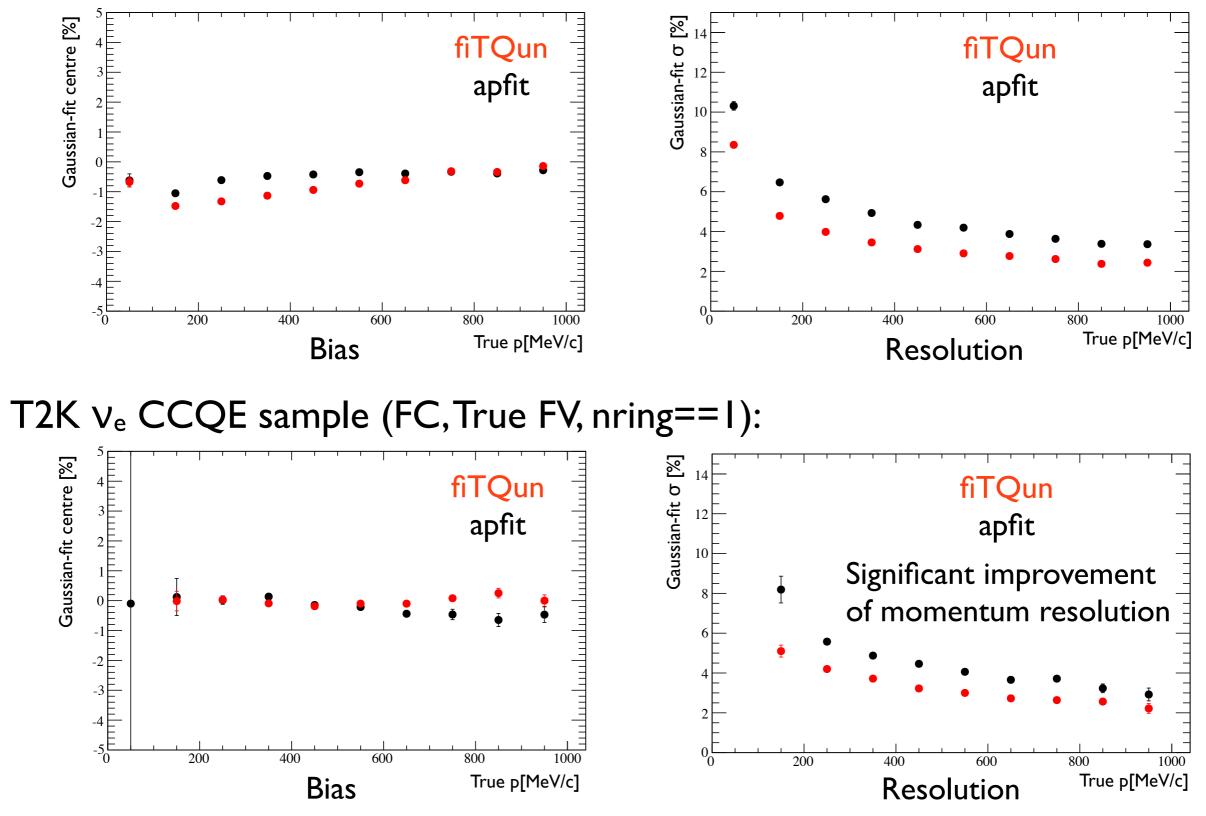
Muon vertex/direction resolution

T2K v_{μ} CCQE sample (FC, True FV, nring==1):



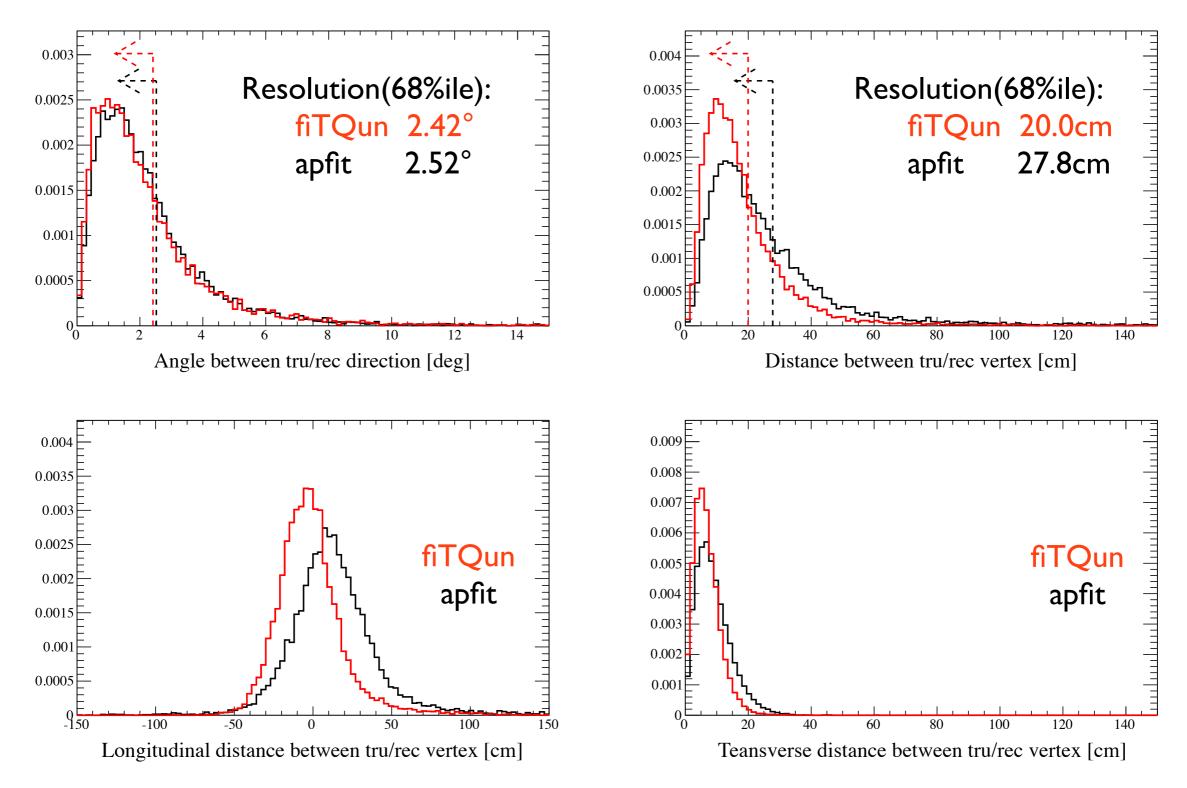
Electron momentum resolution

Electron particle gun sample (FC, True FV, nring==1):



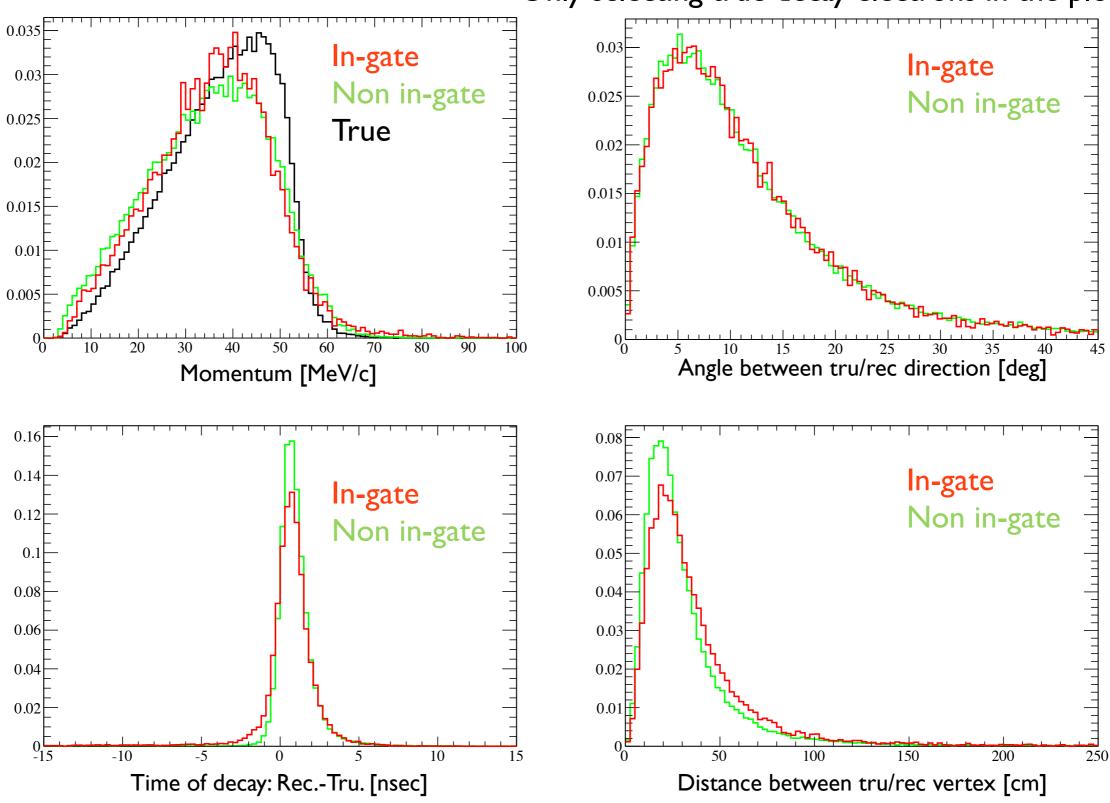
Electron vertex/direction resolution

T2K v_e CCQE sample (FC, True FV, nring==1):



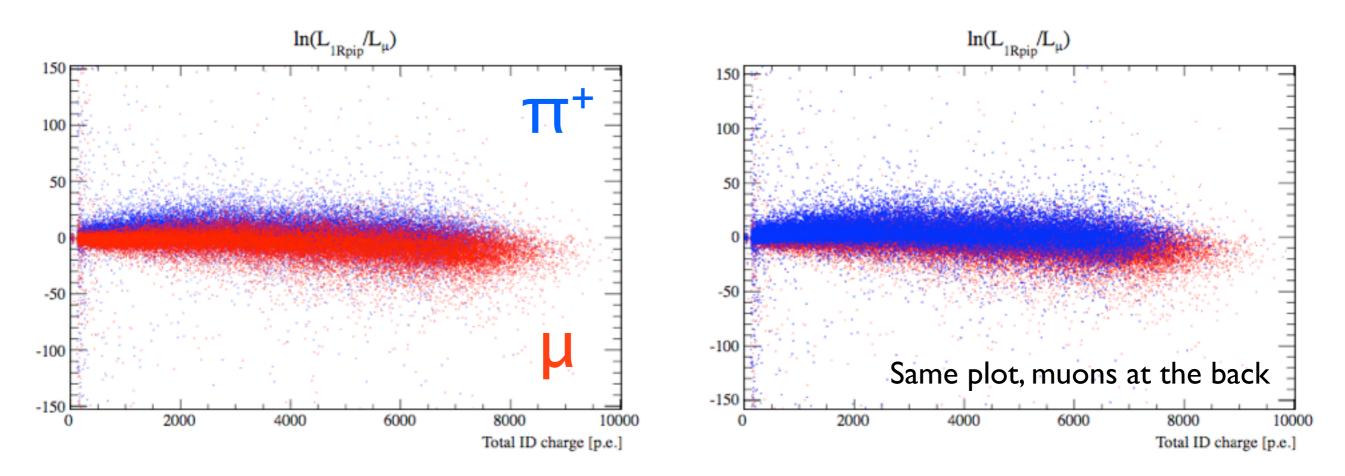
Decay electron reconstruction

*Sample: Raw (unweighted) T2K ν_{μ} , FC, True FV Only selecting true decay electrons in the plots



μ/π^+ separation, w/o kink

- Apply straight-track π^+ hypothesis to both π^+ & μ samples, p<1GeV/c
- When hadronic interaction is turned off, only slight separation of $\pi^+\!/\mu$ is seen



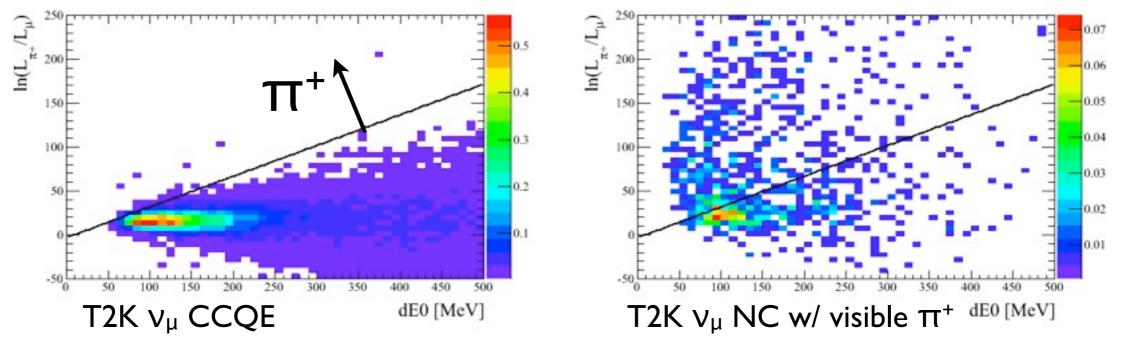
Upstream track π⁺ Fitter

• π^+ track often has a kink due to hadronic interactions with nuclei

 dE_0

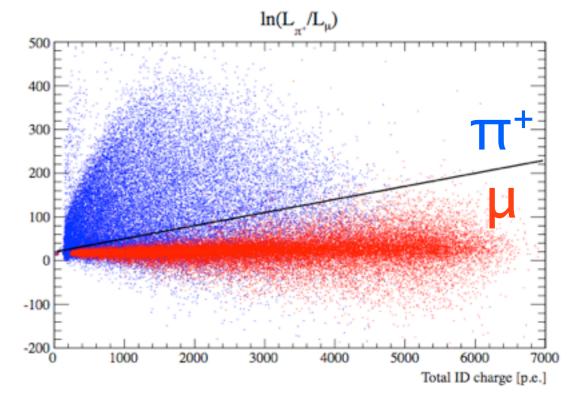
Downstre Track

- Produces sharp, hollow upstream ring
- Fit the upstream track 8 parameter fit
 - Additional parameter dE₀: energy lost before the kink
 - Characterizes the thickness of the ring
- μ/π^+ separation seen in the likelihood ratio to 1-ring μ fit

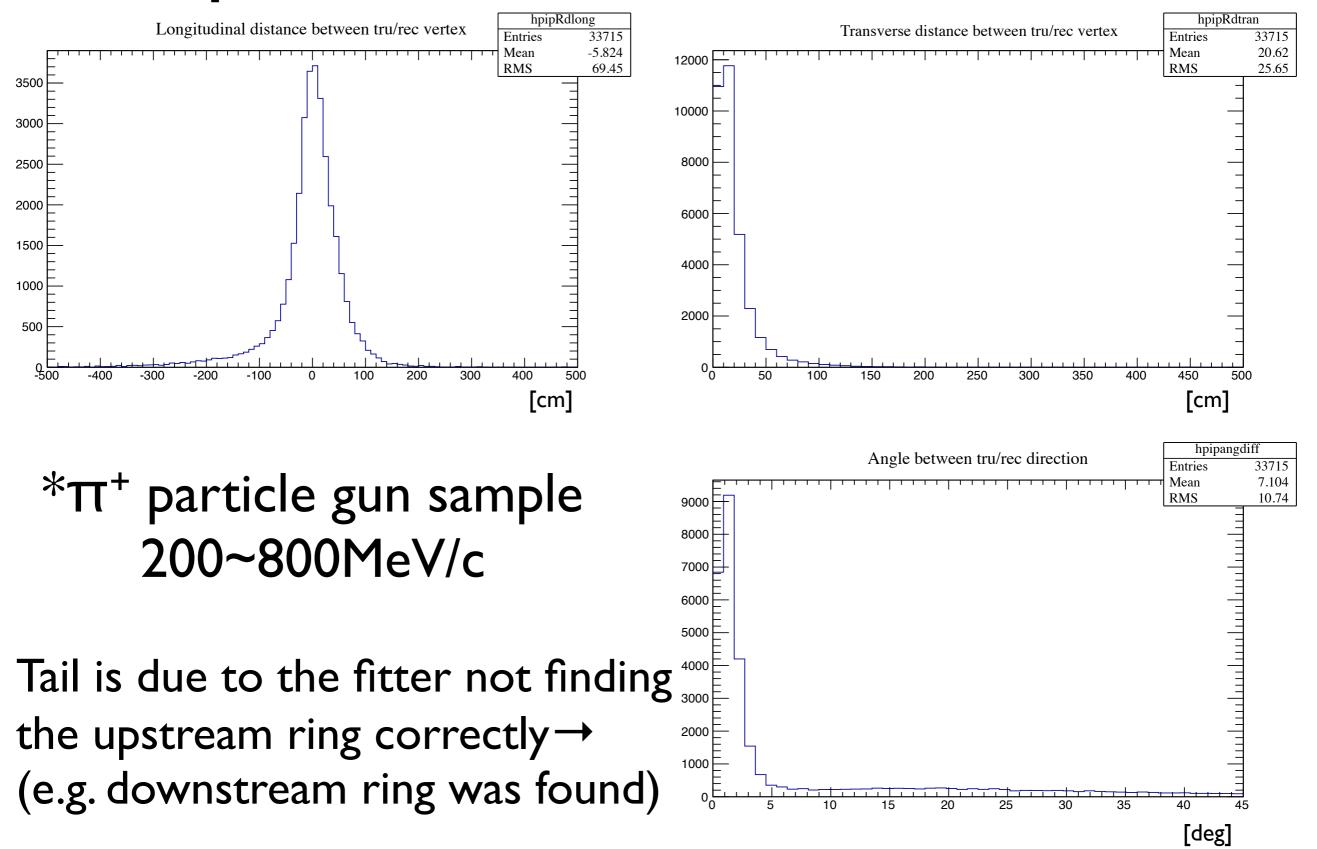


Upstream track π^+ Fitter

- μ and π^+ produce similar charge pattern, since the mass of the two are similar
- Difference is seen since π^+ makes the kink, producing hollow rings, while such thing rarely happens for μ
- Apply both IR μ and upstream π^+ fits
- Make a line cut on the likelihood ratio
 - Since the underlying charge pattern is similar, the upstream π⁺ hypothesis reproduces muon rings, simply by adjusting the dE₀ parameter
 - Always $\ln(L_{\pi^+}/L_{\mu}) > \approx 0$

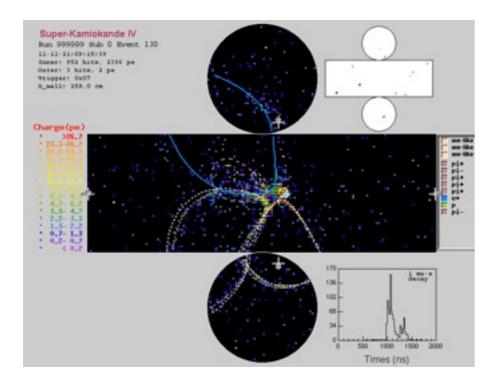


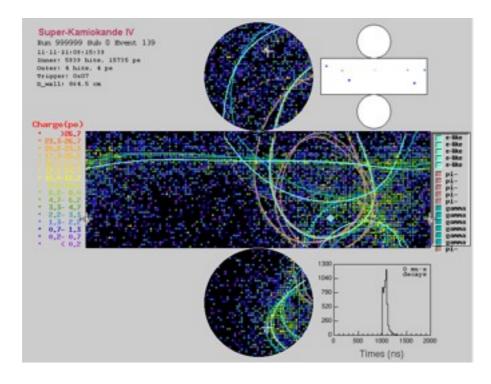
Upstream π^+ fitter resolution



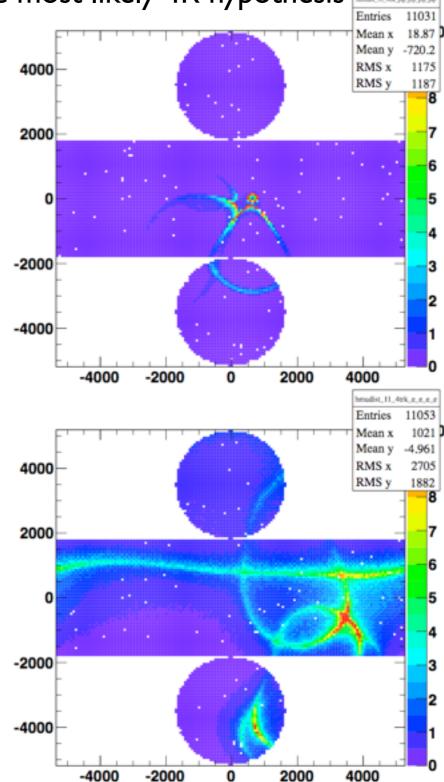
$MR \ Fit \ Event \ Displays \quad *{\tt T2K-SK \ MC \ v_{\mu} \ multi-ring \ events} \\$

Event display



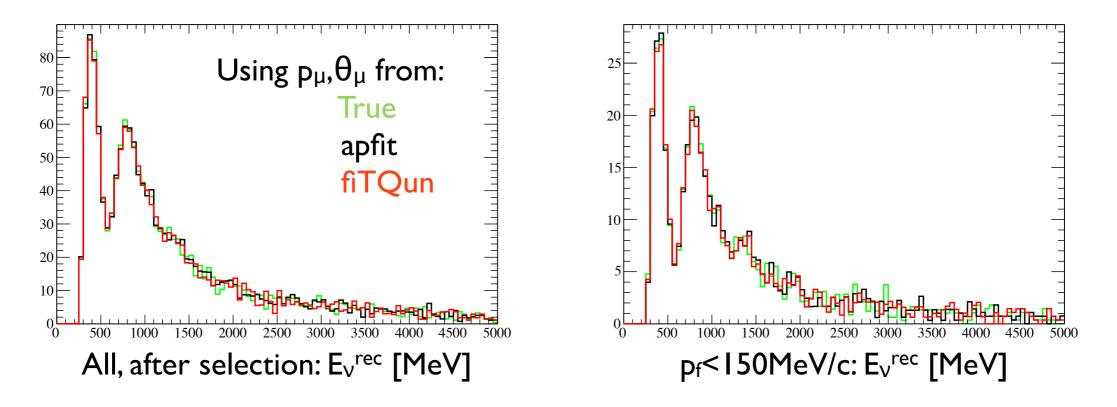


fiTQun predicted charge of the most likely 4R hypothesis



Reconstructed v_{μ} energy (QE formula)

*Sample:T2K ν_{μ} CCQE, maximal osc., after standard ν_{μ} selection cuts



- E_v^{rec} resolution is limited by the fermi motion of target neutrons, not the resolution of p_μ , θ_μ reconstruction
- Both apfit/fiTQun resolution is sufficiently good for E_{ν} reconstruction, no difference is seen between the two

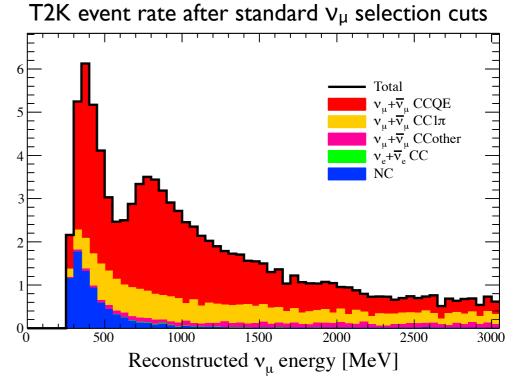
T2K ν_{μ} selection

- Standard cuts: FC, FV, I-ring, μ-like, _μ^{rec}>200MeV/c, n_{dcy}<=1

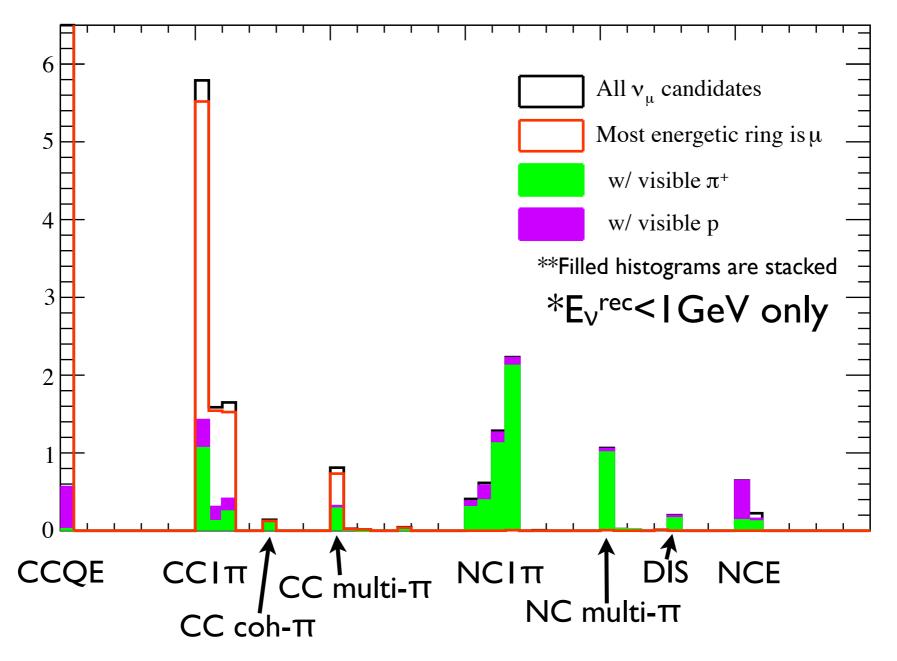
- Main backgrounds are v_{μ} CCI π and NC
- Around 600MeV(oscillation dip), about half of the entries are backgrounds, filling up the dip
- One of the largest systematics come from NC selection efficiency
 - I00% PID error assigned to NC in previous analysis
- Reducing NC background improves θ_{23} , Δm^2_{23} sensitivity

*In the following slides, osc. parameters are:

$sin^2 2\theta_{12}$	0.8704		
$sin^2 2\theta_{23}$	1.0		
$sin^2 2\theta_{13}$	0.1		
δ _{CP}	0		
Δm^2_{21}	7.6x10 ⁻⁵ eV ²		
Δm^{2}_{32}	2.4x10 ⁻³ eV ²		
Hierarchy	Normal		



ν_{μ} backgrounds by NEUT mode



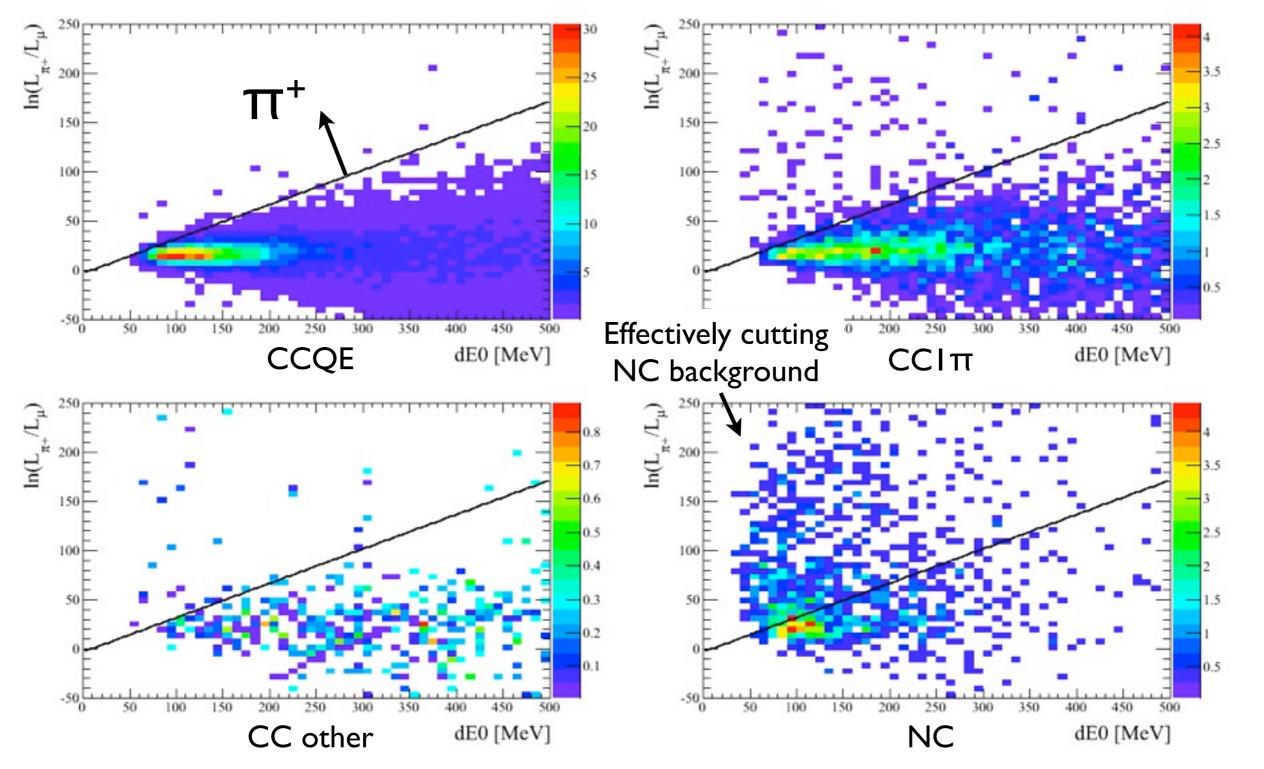
- For most CC backgrounds, μ is the most energetic ring
- NC backgrounds are mostly due to π^+ rings, mis-ID'd as μ
- NCE background is largely from proton rings

fiTQun ν_{μ} selection

- Use fiTQun upstream π^+ fitter to reduce π^+ backgrounds
 - Take the best-fit likelihood ratio of I-ring μ fit and upstream π^+ fit
 - π^+ 's favour π^+ hypothesis over μ hypothesis
 - Thin ring, small $dE_0 \rightarrow \mu$ -fit can't reproduce the ring
 - μ 's almost equally favour μ and π^+ hypotheses
 - π^+ fit returns large dE₀ \rightarrow emulates μ -like ring
 - Make a line cut in dE₀ In($L_{\pi+}/L_{\mu}$) space
- To select I-ring events, compare the best-fit likelihood values of I-ring and 2-ring hypotheses
- We can now make all the V_{μ} selection cuts using fiTQun variables only:
 - I-ring, μ-like(vs. e-like), μ-like (vs. π⁺-like), IRμ-FV, p_μ^{rec}>200MeV/c, n_{dcy}<=I

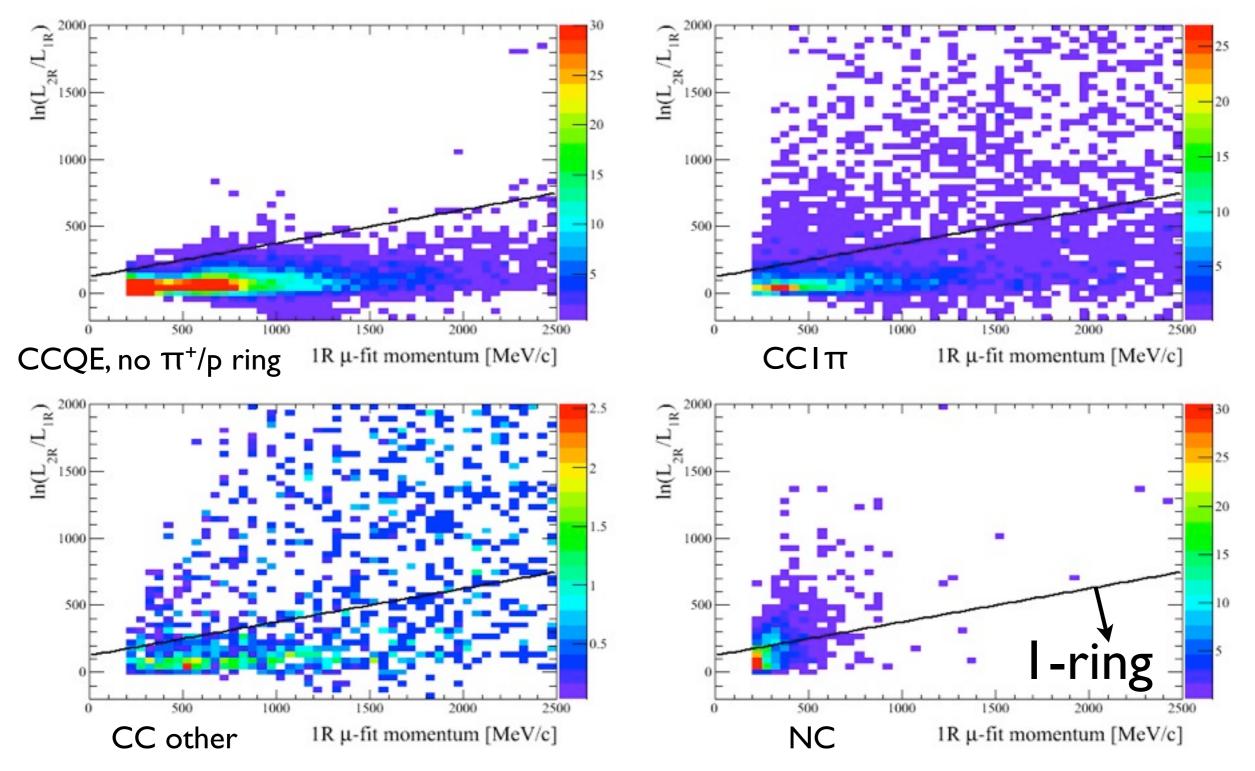
π^+ rejection cut

*T2K ν_{μ} , all fiTQun ν_{μ} cuts, except the IR cut and π^{+} cut, are applied



One-ring cut

*T2K ν_{μ} , all fiTQun ν_{μ} cuts, except the IR cut and π^{+} cut, are applied



Selection efficiencies

*T2K event rate @ $6x10^{20}$ POT, after each v_{μ} selection cut, w/ 3-flvr. osc.

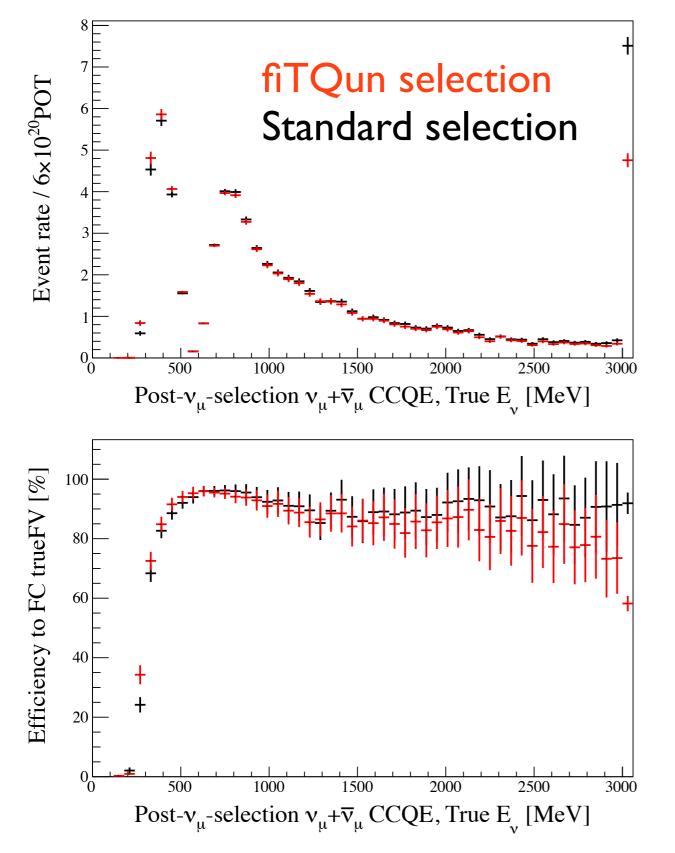
Standard selection

Signal purity: **60.6%**

fiTQun
selection
Signal purity:
69.3 %

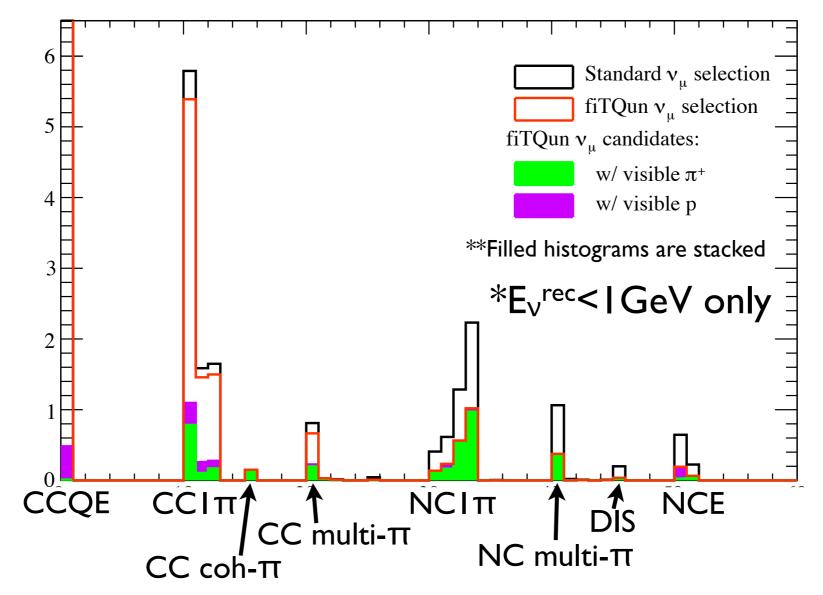
@ 6x10 ²⁰ POT	ν_{μ} + $\overline{\nu}_{\mu}$ CCQE	ν_{μ} + $\overline{\nu}_{\mu}$ CCI π	ν_{μ} + $\overline{\nu}_{\mu}$ CC oth.	$v_e + \overline{v}_e CC$	NC
FC trueFV	81.83	68.06	87.82	38.88	102.74
FCFV	78.09	67.36	88.26	38.63	86.26
I-ring	73.72	39.73	18.25	30.04	24.95
µ-PID	72.46	38.50	16.03	0.29	8.21
pµ ^{rec} >200MeV/c	71.86	38.40	16.02	0.29	7.98
N _{dcy} <=1	71.03	28.93	9.32	0.29	7.63
Efficiency [%]	86.8	42.5	10.6	0.7	7.4
@ 6x10 ²⁰ POT	ν_{μ} + $\overline{\nu}_{\mu}$ CCQE	ν_{μ} + $\overline{\nu}_{\mu}$ CCI π	ν_{μ} + $\overline{\nu}_{\mu}$ CC oth.	$v_e + \overline{v}_e CC$	NC
FC trueFV	81.83	68.06	87.82	38.88	102.74
FCFV	80.57	65.58	72.11	35.01	91.61
I-ring	73.09	33.67	12.50	29.42	42.07
μ -PID(w/ π^+ cut)	70.14	30.81	8.01	0.02	3.41
pµ ^{rec} >200MeV/c	68.38	30.61	7.97	0.02	3.07
N _{dcy} <=I	67.62	22.71	4.32	0.02	2.96
Efficiency [%]	82.6	33.4	4.9	0.1	2.9
Reduction rate to std. sel. [%]	4.8	21.5	53.7	92.1	61.2

Signal efficiency comparison



- Around the oscillation dip, signal efficiency of fiTQun selection is not worse compared to standard selection
 - Efficiency is higher at lower energy (<600MeV)
- Signal loss by fiTQun selection is mostly in the high-energy tail region (>3GeV)

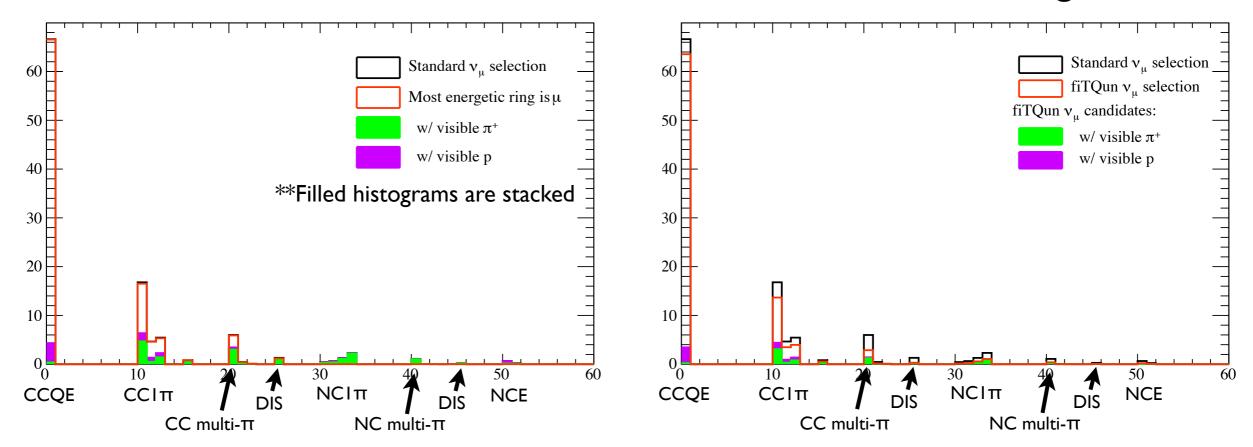
fiTQun ν_{μ} selection: backgrounds



- Significant reduction of NC backgrounds; π^+ 's are properly identified
- Single proton ring events are mostly rejected by π^+ cut, large reduction of NCE background
 - Proton hypothesis only partially implemented now, could work even better
- CC background reduction by π^+ cut(for events w/ invisible μ) and I-ring cut
 - Reduction by I-ring cut is seen more in the higher energy region(not included in this plot)

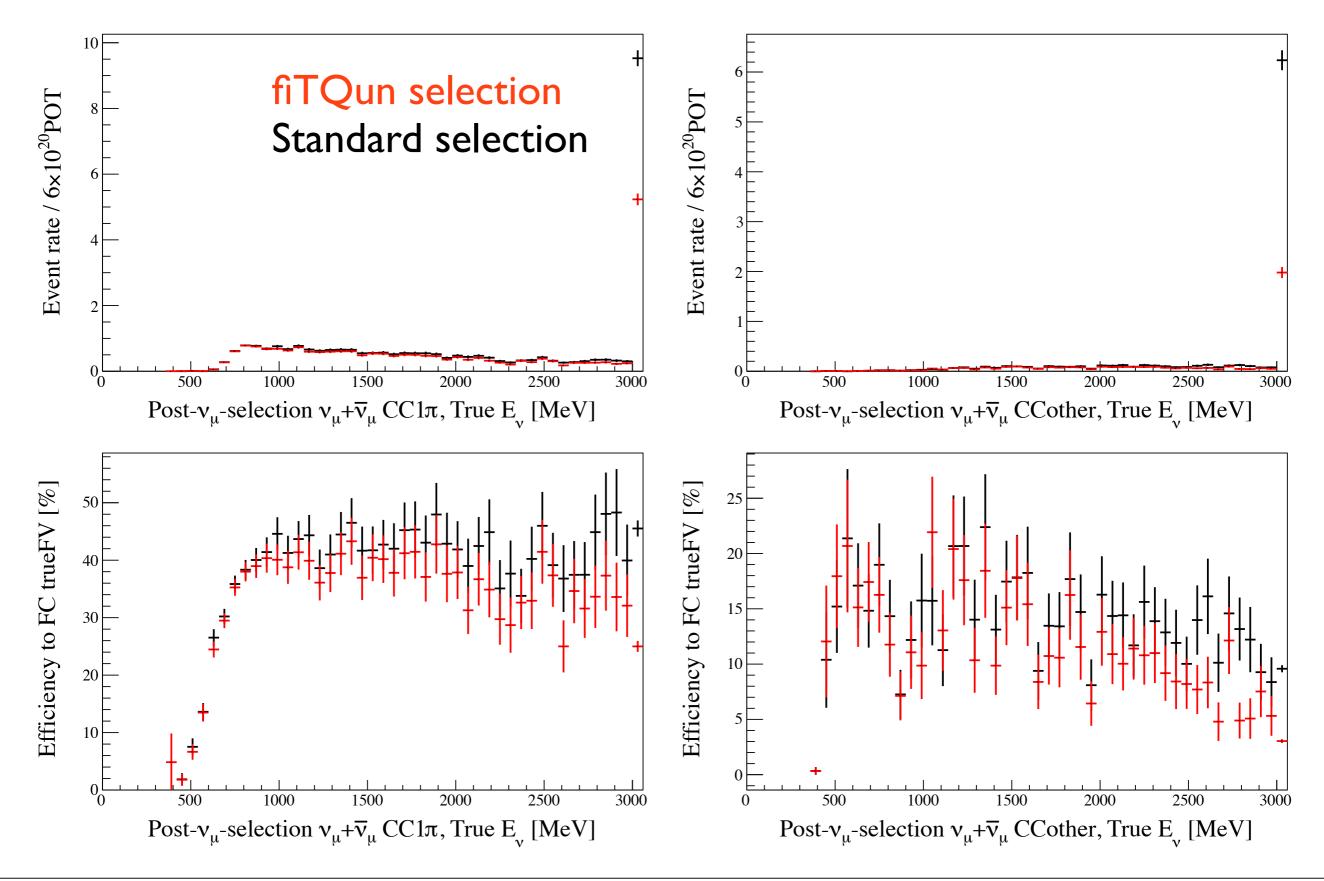
Including higher energy events...

*Includes full range of E_v^{rec}

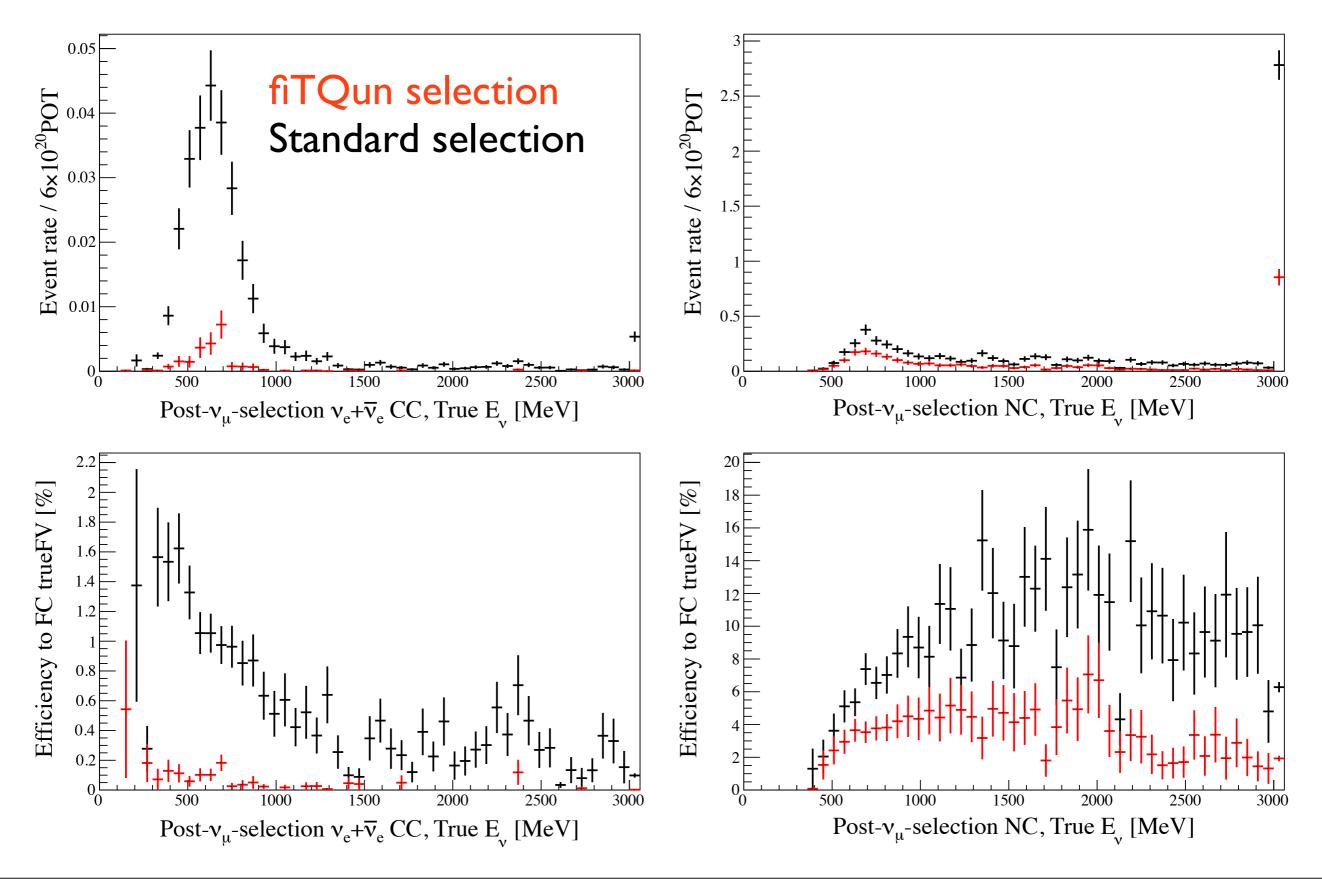


- Larger CC background reduction for higher energy events
 - Multi-ring fitter is sensitive to darker rings in the presence of bright rings
 - fiTQun I-ring cut rejects π^+/p rings which are missed by apfit I-ring cut
- CCQE efficiency loss is mainly in the higher energy region
 - Need to optimize the the I-ring cut criterion to maximize sensitivity, balancing background rejection and signal efficiency

v_{μ} selection efficiencies



v_{μ} selection efficiencies



Processing time

- Effort was made to reduce CPU time
 - IR fit takes ~40% less time now compared to older versions
- Overall, fiTQun requires x3~5 more CPU time compared to apfit+POLfit
 - Depends on the type of event (# of hits/rings/sub-events etc.)
 - fiTQun uses all PMTs while apfit, in general, uses hit PMTs only
- Difference between apfit tends to get smaller for more complex event topology

Average time per event apfit+POLfit [sec]		fiTQun					
	Total	Sub-evt+1R	π ⁰	CM π⁰	MR		
e particle gun 0-500MeV/c	52.1	229.7	33.1	26.0	33.5	137.2	
π ⁰ particle gun 0-500MeV/c	84.4	256.4	37.0	34.3	26.8	158.3	

*Measured on SciNet GPC