EFFECT OF DARK ENERGY PERTURBATION ON COSMIC VOIDS FORMATION (SUBMITTED TO MNRAS...)

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Dark Energy

The condition for the acceleration

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3}(\bar{\rho} + 3\bar{P}) > 0 \implies w_{\rm DE} = \frac{\bar{P}}{\bar{\rho}} < -\frac{1}{3}$$

Planck 2015,

Dark Energy

 $w = -1.019^{+0.075}_{-0.080}$ *Planck* TT, TE, EE+lowP+lensing+ext.

- Cosmological Constant
 Quintessence
 k-essence
 etc...

How do we distinguish dark energy models?

The large scale structure and void

✓ The effect of dark energy should be imprinted on large scale structures.

 ✓ Voids are low matter density regions.
 → They are one of the "largest" structures (~10s Mpc)
 → They are regarded as "clean" objects to observe the effect of DE.

(Weygaert, 2014)

✓ Our aim

To investigate effects of DE models on void properties



credit:SDSS



Dark Energy and Cosmic Voids

Previous works

• Shape(ellipticity)

Park & Lee (2007), Lee & Park (2009), Lavaux & Wandelt (2010) Biswas et al. (2010), Bos et al. (2012)

- Size distribution (Sheth & Weygaert, (2004)) Pisani et al. (2015)

Our work

- Allow DE to be perturbed spatially $(c_s^2 < 1)$
- Focusing on size (isolated void, distribution)

Set up

- Our set up
 - Isolated
 - Spherical
 - Top-hat(bucket) profile

- Voids in real
 - Not isolated
 - Not spherical
 - Smooth density profile





Set up

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calculation set up

$$\begin{split} \Omega_{\mathrm{m},0} &= 0.3\\ \Omega_{\mathrm{de},0} &= 0.7\\ H_0 &= 70 \; [\mathrm{km/s/Mpc}]\\ \delta_{\mathrm{m},i} &= -5.0 \times 10^{-4}\\ \delta_{\mathrm{DE},i} &\propto \delta_{\mathrm{m},i}\\ 0 &\leq c_s^2 < 1\\ w \neq -1 \end{split}$$

Evolution equations (comoving coordinate:Basse et al. (2011))

$$\begin{aligned} \frac{X''}{X} + \mathcal{H}\frac{X'}{X} &= -\frac{4\pi G}{3}a^2 \left[\bar{\rho}_{\rm m}\delta_{\rm m}^{\rm TH} + \bar{\rho}_{\rm de}\delta_{\rm de}^{\rm TH} + 3\delta P_{\rm de}^{\rm TH}\right]\\ \text{where } X &= \frac{R}{a}, \ (') = \frac{d}{d\tau} = a\frac{d}{dt}, \ \mathcal{H} = aH\\ \text{matter } M &= \frac{4\pi}{3}\bar{\rho}_{\rm m}(1+\delta_{\rm m}^{\rm TH})R^3 = \text{constant}\\ & & & & & \\ & & & \\ & & & \\ & & & \\ \end{pmatrix} \delta_{\rm m}^{\rm TH} = (1+\delta_{\rm m,i}^{\rm TH})\left[\frac{X_i}{X}\right]^3 - 1\\ \text{dark energy} \begin{bmatrix} \rho_{\rm de}' + 3\mathcal{H}(\rho_{\rm de} + P_{\rm de}) + \nabla \cdot \left[(\rho_{\rm de} + P_{\rm de})\vec{v}_{\rm de}\right] = 0\\ \vec{v}_{\rm de}' + \mathcal{H}\vec{v}_{\rm de} + (\vec{v}_{\rm de} \cdot \nabla)\vec{v}_{\rm de} + \frac{\nabla P_{\rm de} + \vec{v}_{\rm de}\dot{P}_{\rm de}}{\rho_{\rm de} + P_{\rm de}} + \nabla\phi = 0\\ \nabla^2\phi &= 4\pi Ga^2 \left[\bar{\rho}_{\rm m}\delta_{\rm m}^{\rm TH} + \bar{\rho}_{\rm de}\delta_{\rm de}^{\rm TH} + 3\delta P_{\rm de}^{\rm TH}\right] \end{aligned}$$

Results for an isolate void



Effects of various sound speed on the evolution of void radius. For w = -0.9, small value of sound speed promotes the evolution, while for w=-1.3 it suppresses the evolution. At a = 1, the maximum deviation is around 0.1%

Dark Energy perturbation in Fourier space



Void size function

Void size function: Sheth & Weygaert (2004)

$$\frac{dn}{dR} = (1+\delta_m)^{1/3} \frac{3}{4\pi R_L^3} f(\nu, \delta_v, \delta_c) \frac{d\nu}{dR_L}$$

$$f(\nu) \approx \sqrt{\frac{2}{\pi}} \exp\left(-\frac{\nu^2}{2}\right) \exp\left(-\frac{|\delta_v|}{\delta_c}\frac{\mathcal{D}^2}{4\nu^2} - 2\frac{\mathcal{D}^4}{\nu^4}\right)$$



$$\nu = \frac{|\delta_v|}{\sigma(R_L)} \qquad \mathcal{D} = \frac{|\delta_v|}{\delta_c + \delta_v} \qquad \delta_c = 1.69$$

$$\sigma^2(R_L) = \int \frac{k^2 dk}{2\pi^2} \tilde{W}(kR_L) P(k)$$
DE perturbation CAMB(Lewis et al. 2000)





Sheth & Weygaert (2004)

Formation of voids

• Void shell crossing condition (EdS model): Blumenthal et al. (1992)

$$\delta R = \frac{\delta R_i}{2|\delta_{\mathrm{m},i}|} (\cosh \theta - 1) \left(1 - \frac{\partial \ln |\delta_{\mathrm{m},i}|}{\partial \ln R_i} \left[1 + \frac{3}{2} \frac{\sinh \theta \cdot (\sinh \theta - \theta)}{(\cosh \theta - 1)^2} \right] \right)$$
$$\delta R = 0 \Rightarrow \delta_{\mathrm{m,sc}} \simeq -0.8$$



variance (a=1)

For w = -0.9 dark energy perturbation enhances the variance while it suppresses for w = -1.3



Results for void abundance (a=1)



Effects of various sound speed on the evolution of void radius.

For w = -0.9, small value of sound speed increases the number of large voids, while for w=-1.3 it decreases.

At R = 30 Mpc, the maximum deviation is around 20%

Summary

- we characterize dark energy in terms of its constant equation of state and sound speed.
- For calculation, we adopt spherical model for an isolate void and excursion set theory for void abundance.
- The maximum deviation from homogeneous dark energy model is about 0.1 % at present time for the isolate void
- When w=-0.9 dark energy perturbation works to promote the evolution of void radius while for w= -1.3 it works opposite direction.
- For void abundance, the maximum deviation is more than 20% at the void radius of 30 Mpc.
- At large scale, in case of w=-0.9 dark energy perturbation increases the number of voids, while w =-1.3, it decreases.