



Cosmological imprints of string axions in plateau

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I.Soda & Y.U.(1710.00305)

N. Kitajima, I.Soda, & Y.U.(in progress)

Collaboration in C01

Triggered at annual meeting of 2017

Axions (or ALPs) from string theory

Superstring theory in compact 6D



4D low energy EFT + Axions + Moduli

Wide mass ranges → Probe of exDim



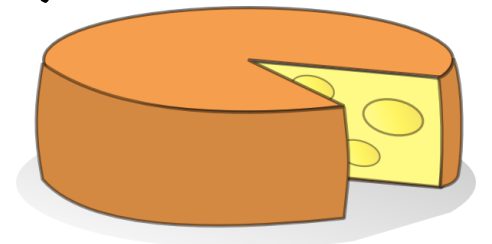
DM candidate (Fuzzy DM)

Wu et al.(00), ...

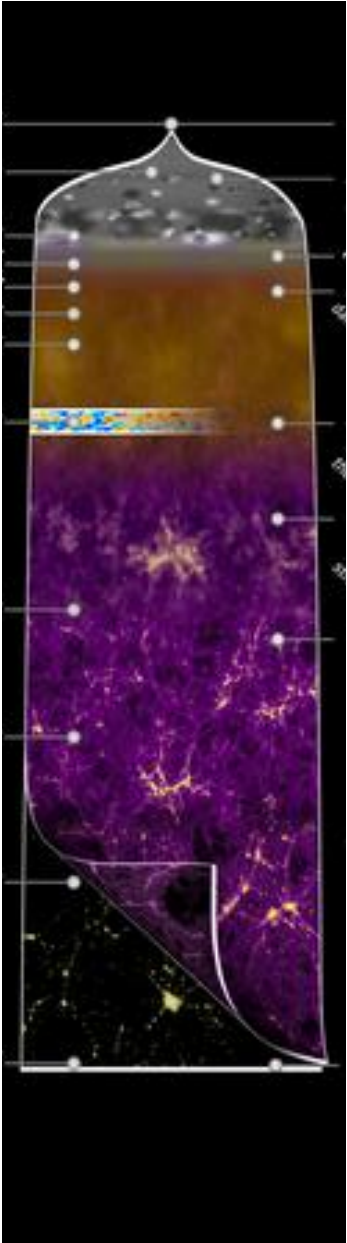
ex. Large Volume Scenario

Conlon et al. (05)

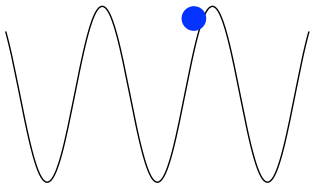
Predicts light mass axions



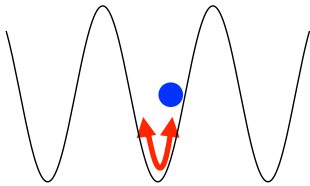
Dreamy bottom-line story



← Onset of oscillation
 ← Equal time



$$H \gg m$$



$$H \ll m$$

~ DM

who are you?



© Can Stock Photo

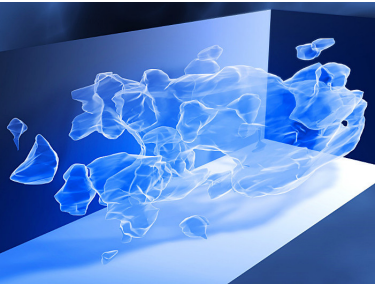


image credit NASA, ESA, R. Massay

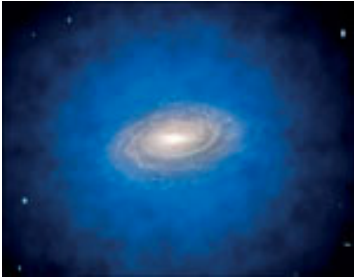
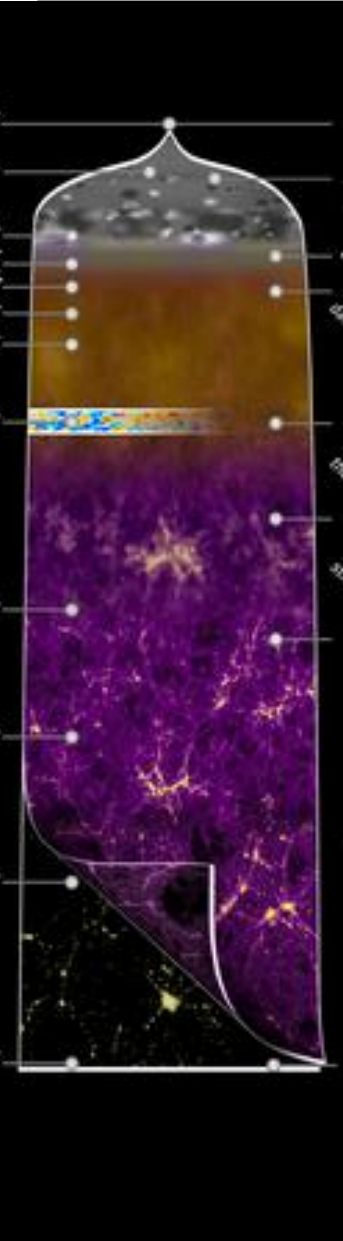
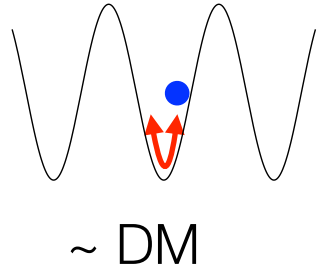


image credit ESO

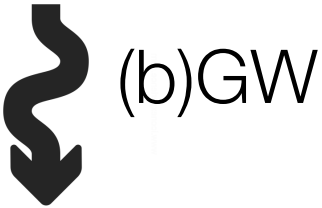
Dreamy bottom-line story



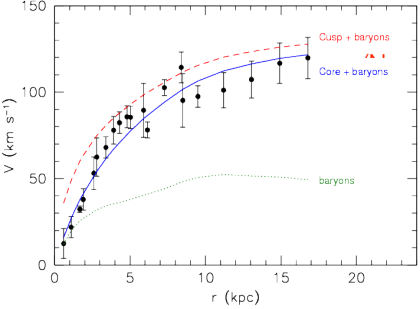
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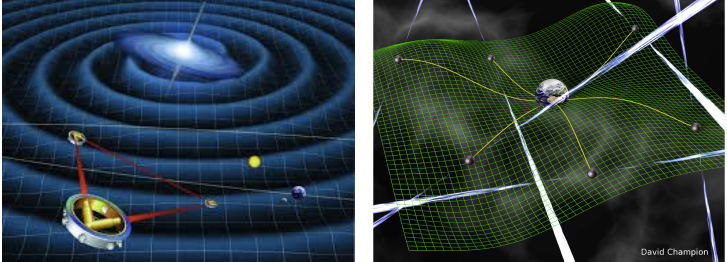
$\phi(t)$ → inst. $\delta\phi(t, x)$
 turbulence



if $\Omega_C \sim \Omega_{\text{axion}}$



~~axion~~
~~bio-marker~~

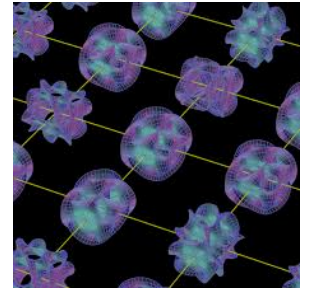


implications to small scales issues?

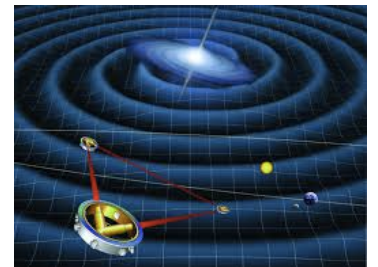
Why it's fun?

Three perspectives

i) Probe of string axiverse: New window
w/some luck



ii) GW emission, new observational tool.



©LISA

iii) Based on basic physics
Kolmogorov turbulence



©V.Gogh

Scalar potential of axion

continuous shift sym.

$$\phi \rightarrow \phi + c$$

—————→
NP effects
e.g. instanton effects

$$\phi \rightarrow \phi + 2\pi n/f$$

$$n \in \mathbf{Z}$$

$$V(\phi) \sim \Lambda^4 \cos\phi/f$$

Potential can be more flatten than $\cos\phi/f$

i) Superposition of multiple cosine terms

e.g., alignment mechanism

Kim, Nilles, & Peloso (04)

ii) Non-minimal coupling w/gravity

→ α attractor model

Kallosh & Linde + (13, 14, ...)

~~iii) Dilute instanton gas approximation~~

Dubovski et al. (10), Nomura, Watari & Yamazaki (17)

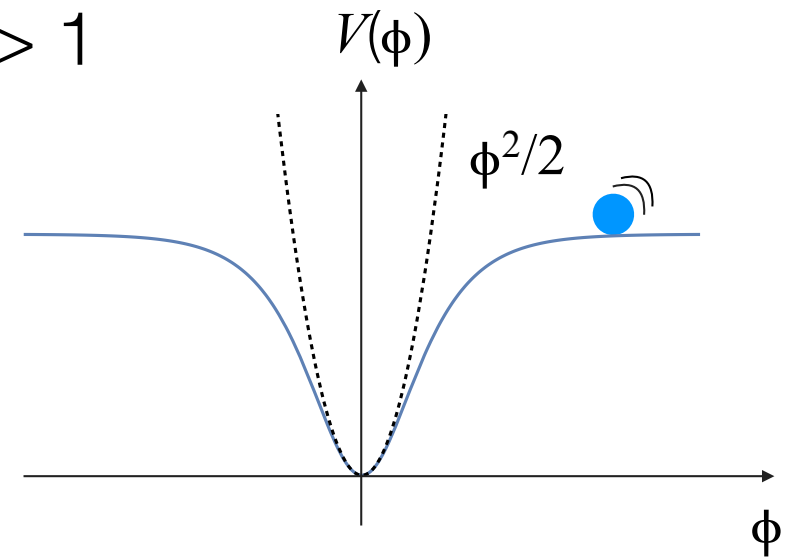
Outline of the story

Soda & Y.U.(17)

Kitajima, Soda & Y.U.(in prep.)

1. Axion slowly rolls down

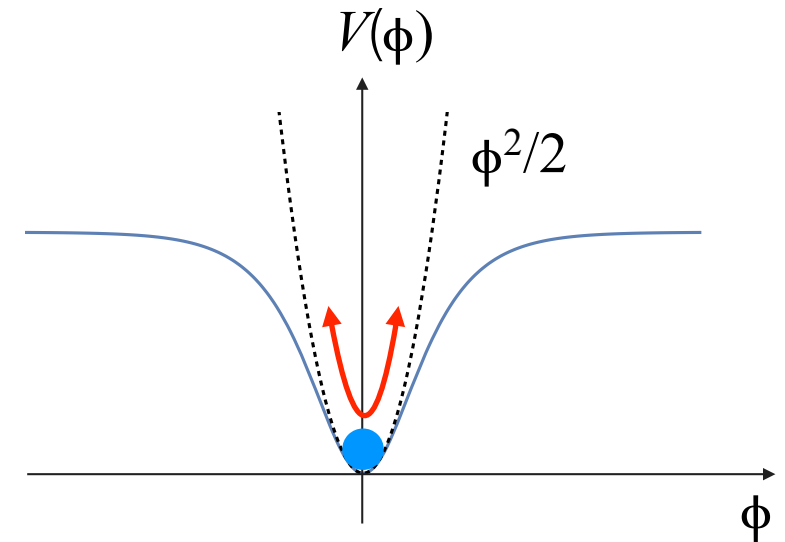
$$H_{osc}/m \gg 1$$



Outline of the story

1. Axion slowly rolls in plateau
2. Onset of oscillation $H_{osc}/m < 1$
Especially w/plateau
(or $\cos\phi/f$ w/fine tuned IC)

$$H_{osc}/m \ll 1$$

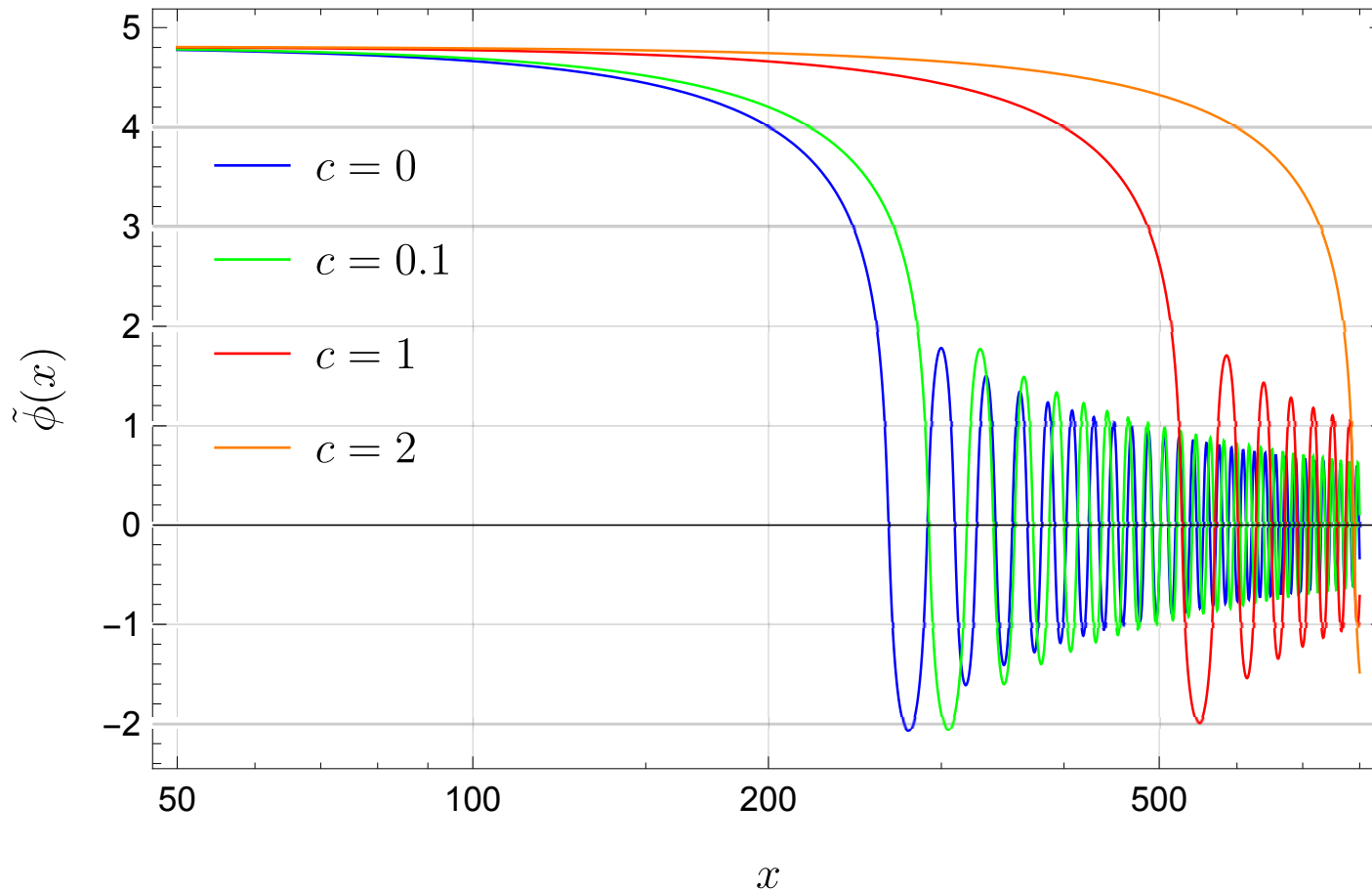


Background evolution

$$V(\phi) = \frac{(m_a f)^2}{2} \frac{(\tanh \frac{\phi}{f})^2}{1 + c(\tanh \frac{\phi}{f})^2}$$

RD

Soda & Y.U.(17)



$x = m/H$

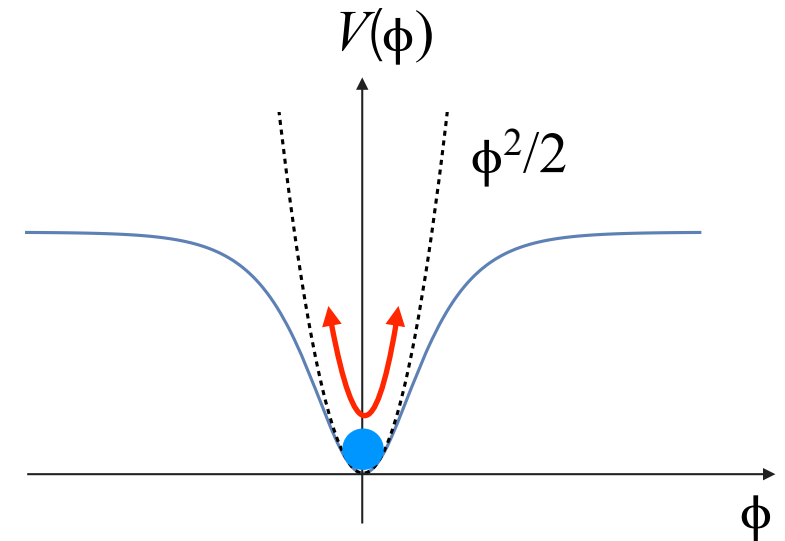
Onset of oscillation is not $m \sim H$, but delayed!

Outline of the story

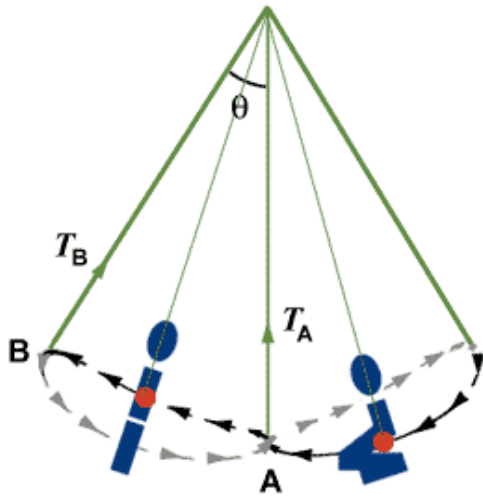
1. Axion slowly rolls in plateau
2. Onset of oscillation $H_{osc}/m < 1$
3. Exponential growth due to PR

if $H_{osc}/m \ll 1$

No disturbance due to cosmic exp.



Parametric resonance



Repeat: Up & Down in a half of osc. period

→ Periodic ext. force

→ Enhancing the amplitude

“Parametric resonance instability”

Mathieu equation

$$\frac{d^2}{dx^2} \tilde{\varphi} + (A - 2q \cos 2x) \tilde{\varphi} = 0$$

resonance band

$$A \sim n^2$$

ex. First band

$$\tilde{\varphi} \propto e^{\gamma x}$$

$$\gamma \simeq q/2$$

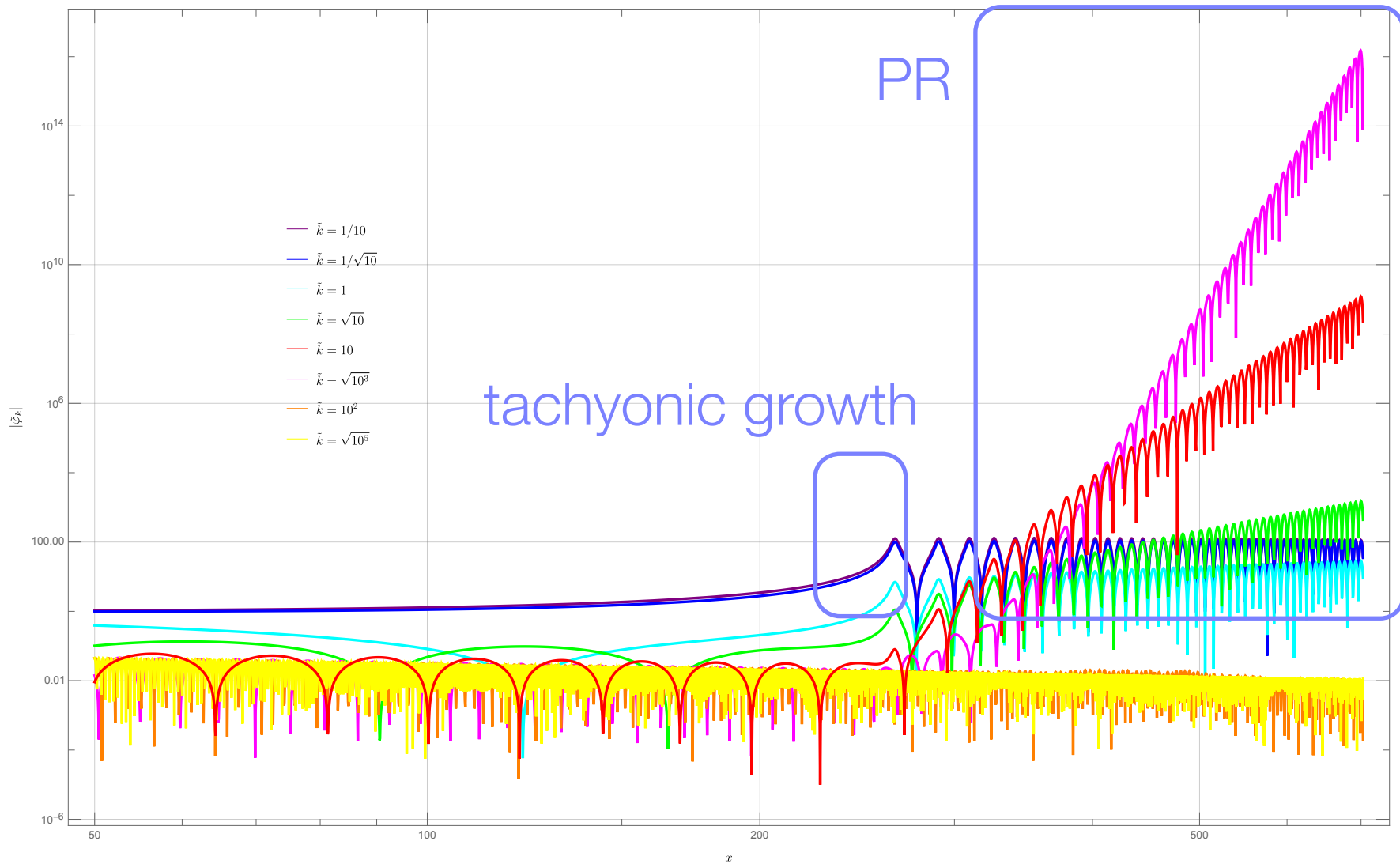
Energy transfer

$$\phi(t) \longrightarrow \delta\phi(t, x)$$

Linear perturbation

Soda & Y.U.(17)

PR in $k_r/(a_{osc} m) \sim O(1)$, $k_r/(a_{osc} H) \gg 1$

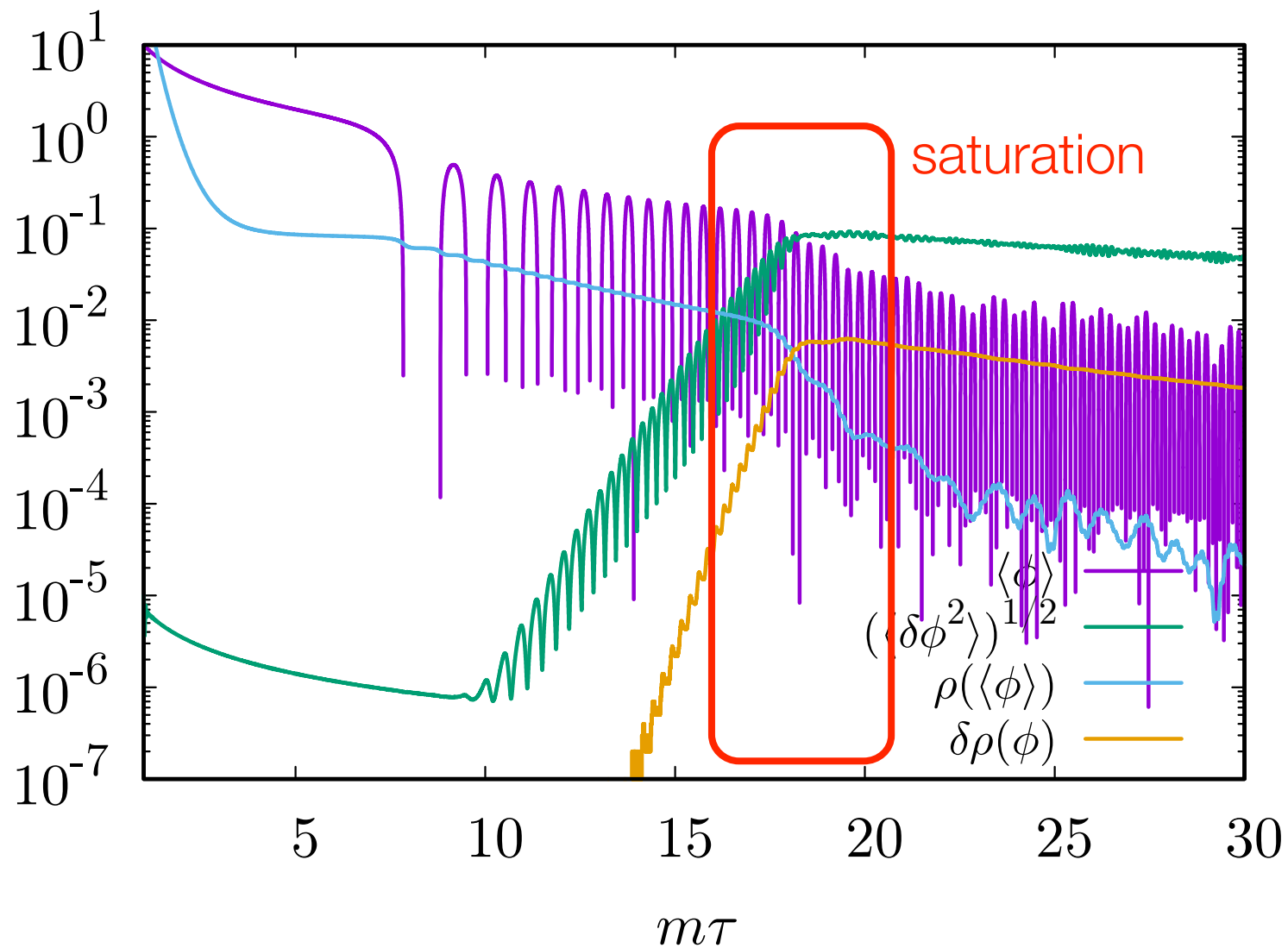


$$\tilde{k} = k/(a_i m)$$

Energy transfer

Kitajima, Soda & Y.U.(in prep.)

Lattice simulation $N_{\text{grid}}=(128)^3$

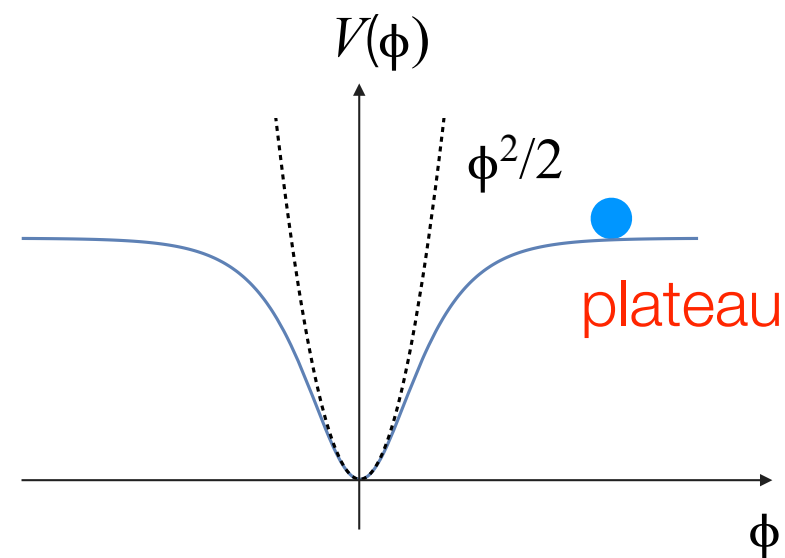


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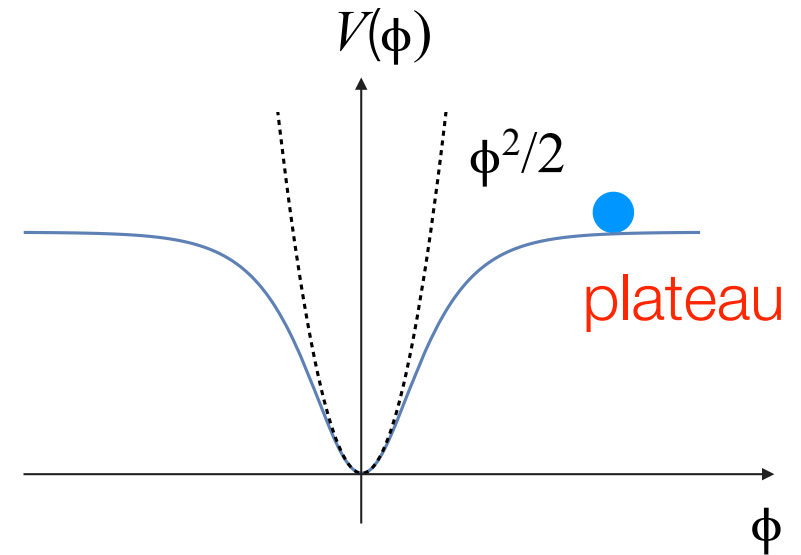


4. Rescattering \rightarrow PR becomes inefficient *eg. Kofman, Linde, Starobinsky*

$$\frac{\delta\phi}{\phi}, \frac{\delta\rho}{\rho} \sim O(1)$$

Outline of the story

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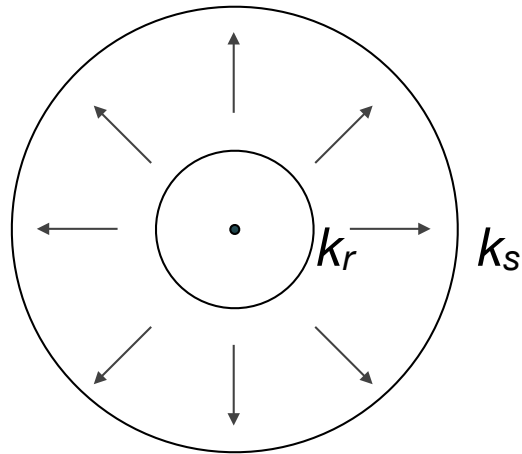
5. Kolmogorov turbulence \rightarrow GW emission

Micha & Tkachev (02,04)

Kolmogorov turbulence

stationary turbulence: source k_r (IR) \rightarrow sink k_r (UV)

in k-space

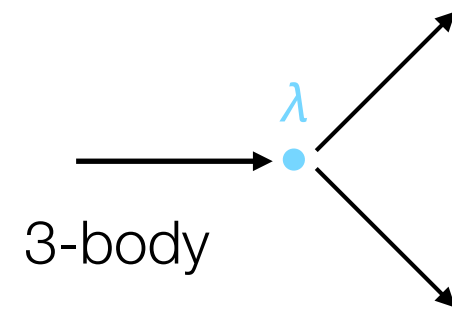
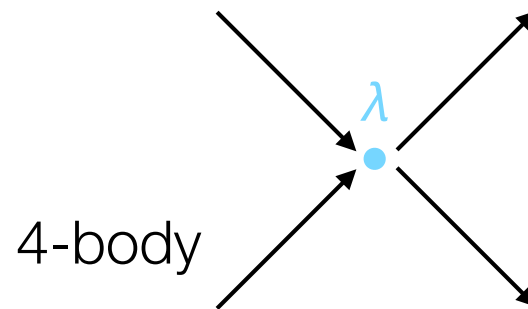


kinetic theory

$$\frac{dn_k}{dt} = \underline{I_k[n]}$$

Collision integral

take $\lambda\phi^4$ theory, now w/ $\phi(t)$



assump: const. flux in k for massless ϕ

Micha & Tkachev (02,04)

$$\frac{dn}{d\ln k} = k^3 n(k) \propto k^{3-s}$$

$$s = 5/3$$

for 4-body

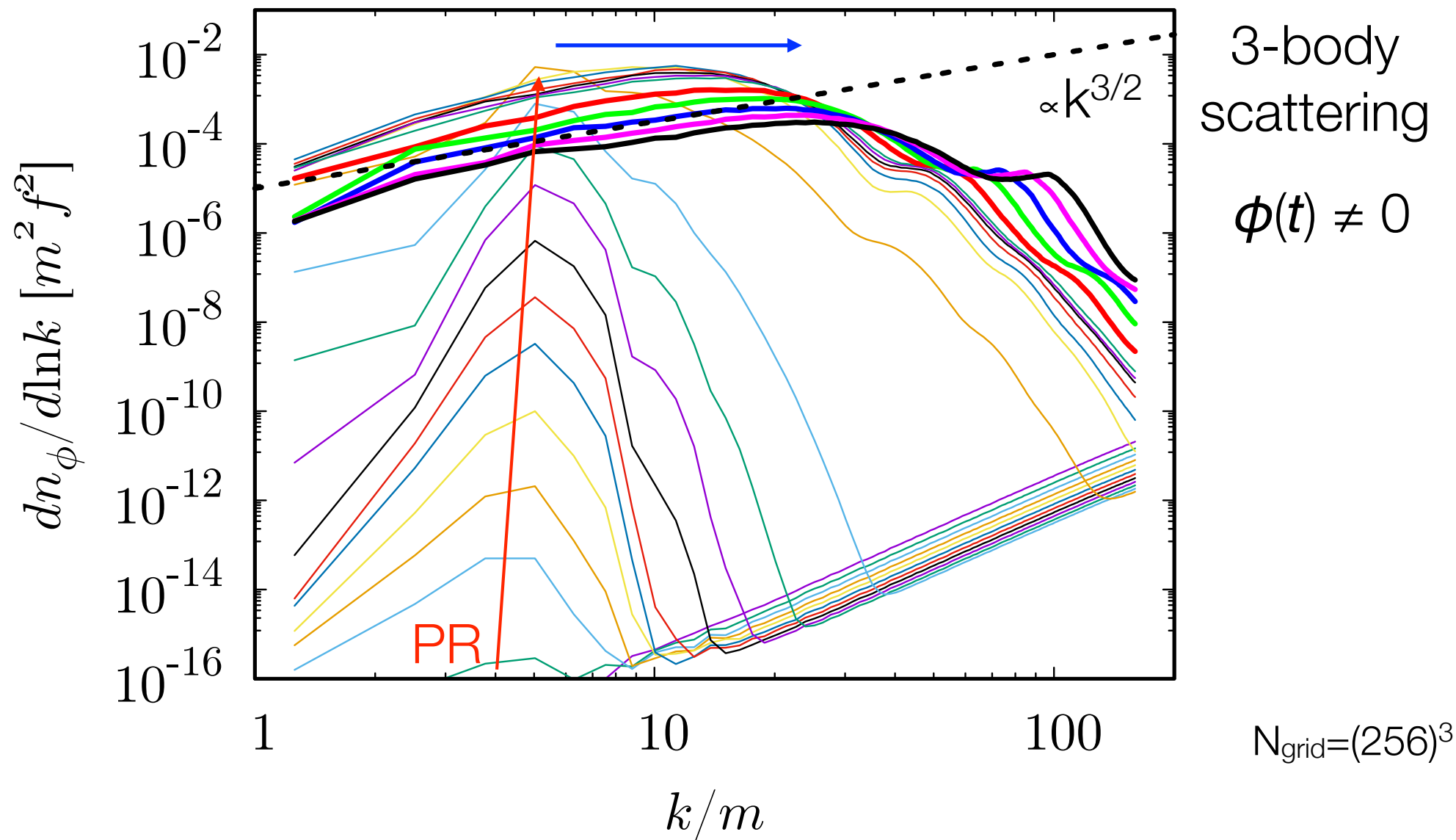
$$s = 3/2$$

for 3-body

Lattice simulation

Kitajima, Soda, Y.U. (in preparation)

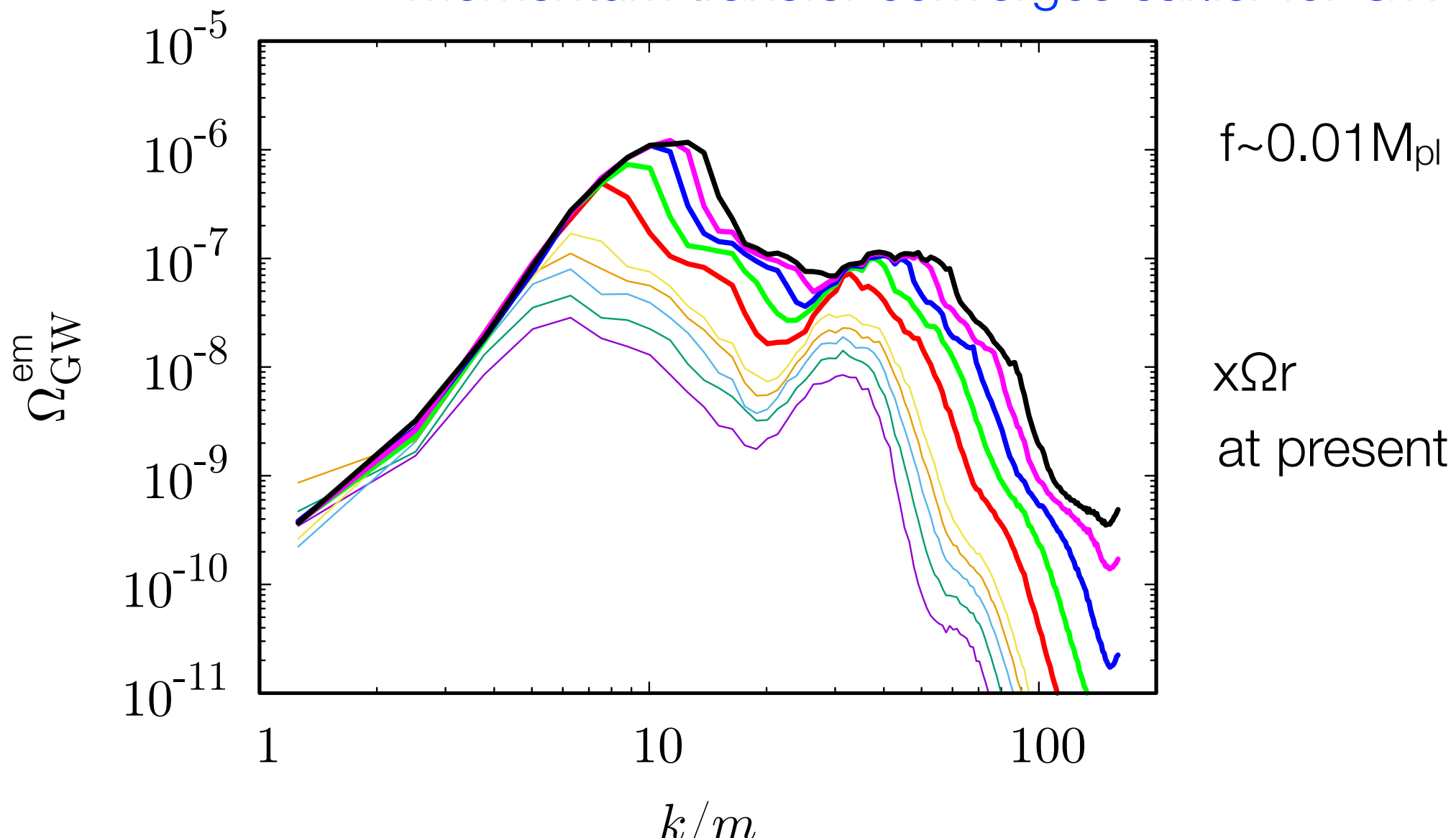
Momentum trans due to turbulence



GW spectrum

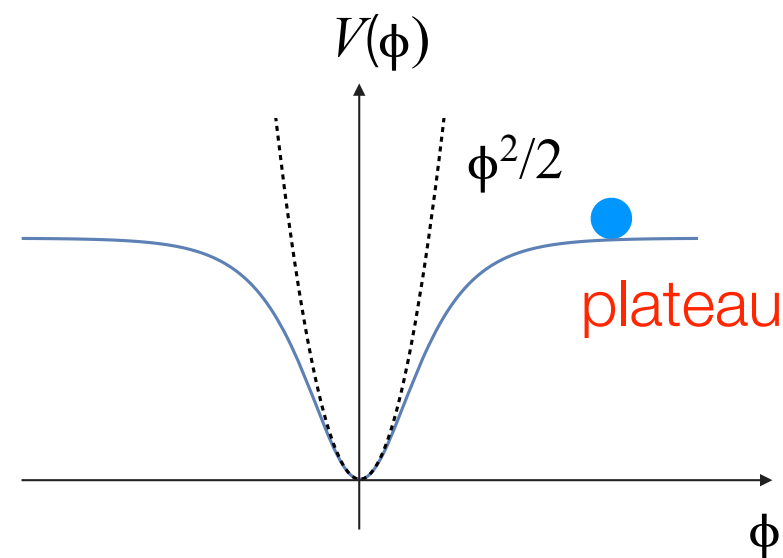
Kitajima, Soda, Y.U. (in preparation)

momentum transfer converges earlier for GW



Outline of the story

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if $H_{osc}/m < 1$

No disturbance due to cosmic exp.

4. Rescattering \rightarrow PR becomes inefficient *eg. Kofman, Linde, Starobinsky*

5. Momentum transfer due to turbulence \rightarrow GW emission

Micha & Tkachev (02,04)

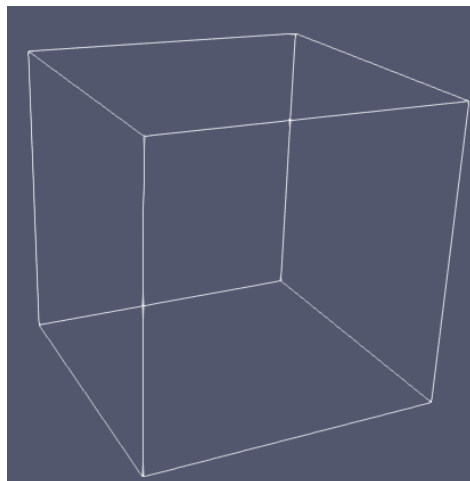
6. GW& ϕ decoupled, Oscillon/I-ball formation

Kasuya+(03), Amin + (10, 12, 17), Zhou(13), Antusch +(17), Kawasaki+(17), ...

Oscillon formation

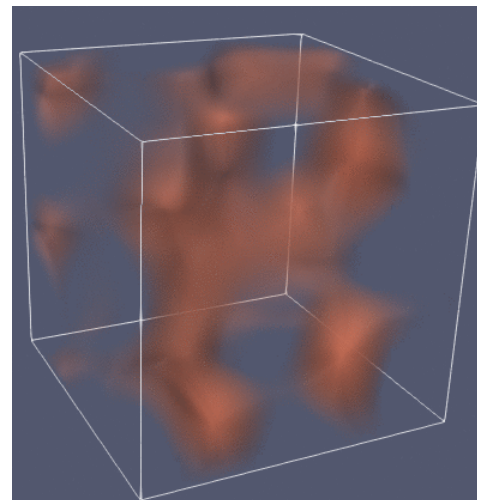
Kitajima, Soda, Y.U. (in preparation)

$a \sim a_0$



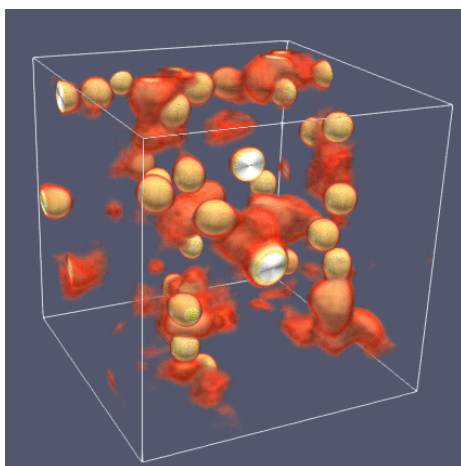
$a \sim 20 a_0$

rescattering



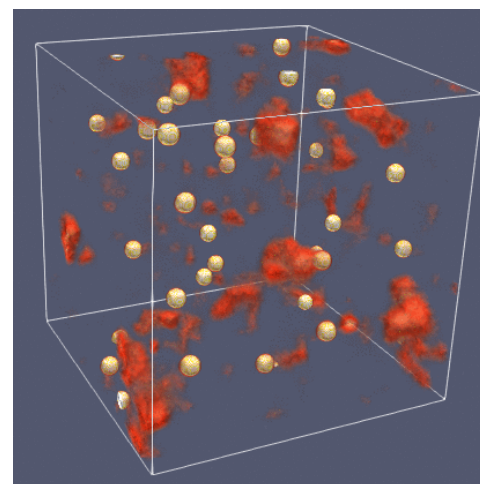
$a \sim 35 a_0$

turbulence



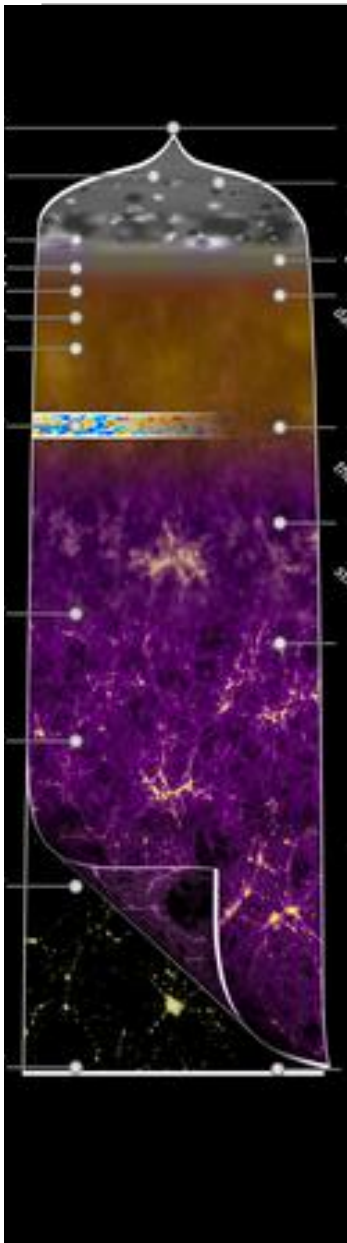
$a \sim 90 a_0$

oscillon

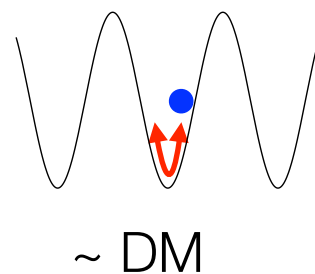


$N_{\text{grid}}=(128)^3$

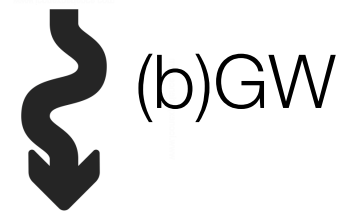
Summary/Future issues



← Onset of oscillation
 ← Equal time

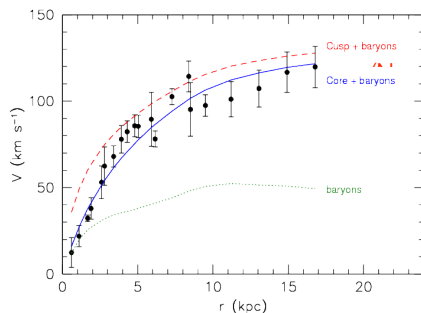


$\phi(t)$ → $\delta\phi(t, x)$
 PR turbulence

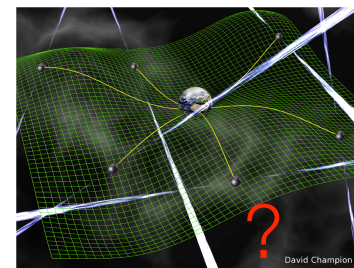


(b)GW
 ongoing project

if $\Omega_c \sim \Omega_{\text{axion}}$ future project



axion-marker



nHz?
 or lower

implications to small scales issues?