

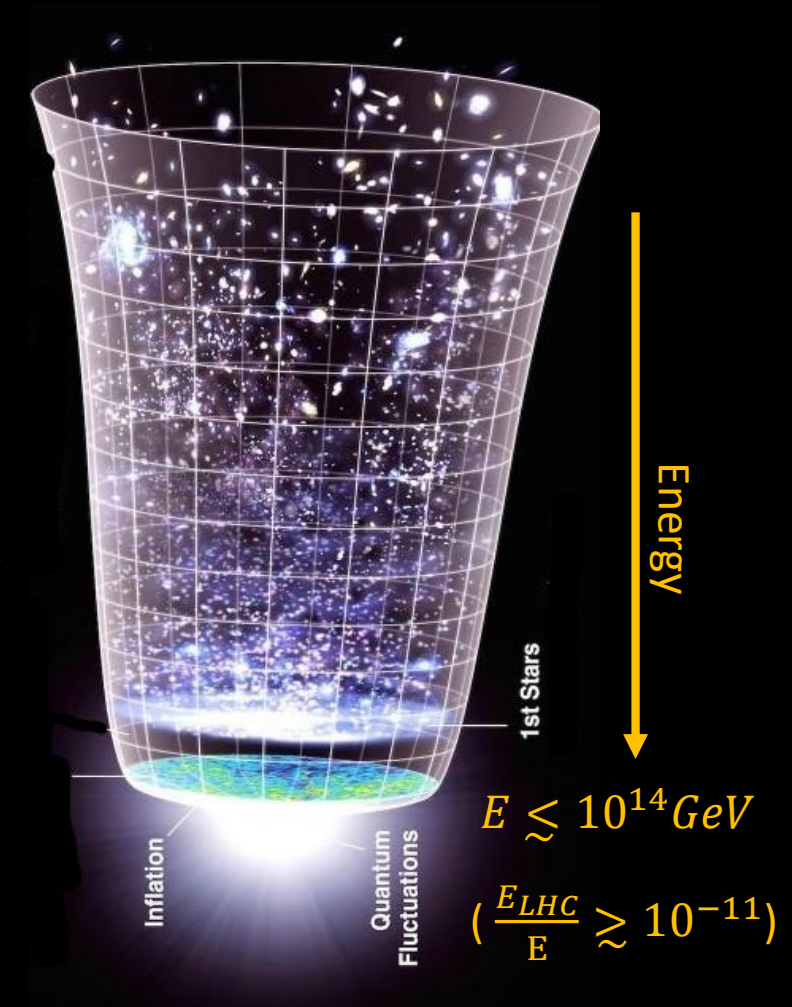
Particle Production & Gravitational Waves with $SU(2)$ Gauge Fields in Inflation

Azadeh Maleknejad

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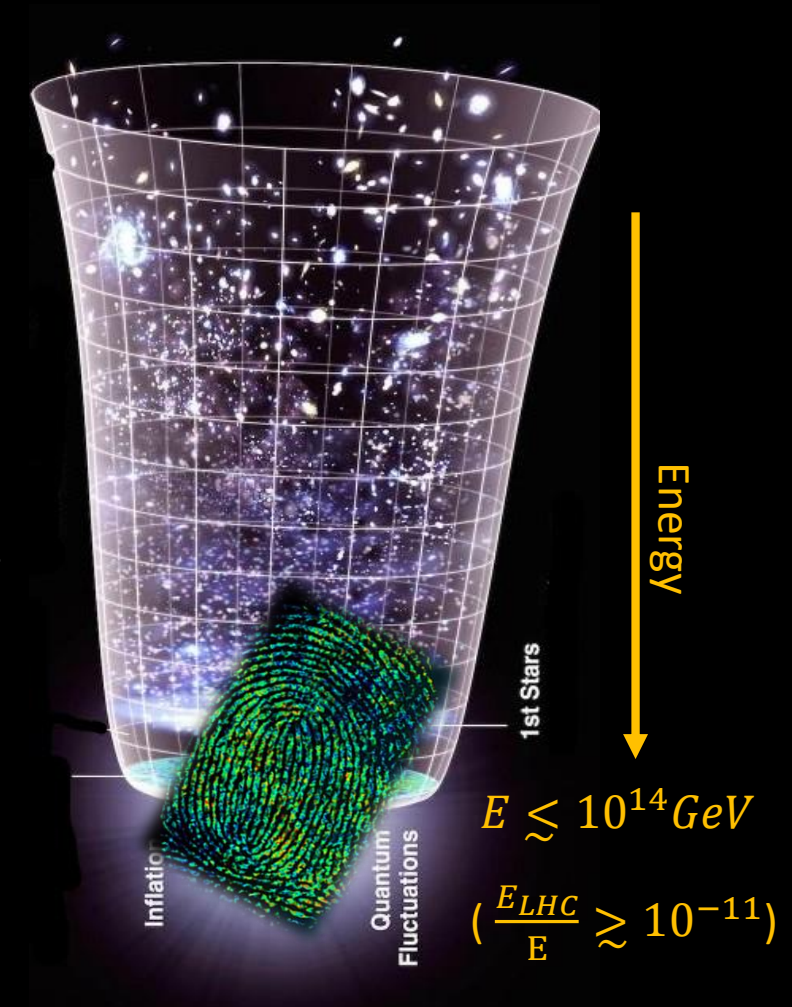
Motivation

- Inflation: Universe at highest observable energy!
- **Gauge field** theories, Abelian or non-Abelian, are the widely accepted framework for particle physics beyond SM.
- The **Primordial gauge fields** in the physics of inflation **compatible** with the FRW symmetries?



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Non-Abelian Gauge fields in Inflation?

The story started in 2011

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- Respecting gauge symmetry

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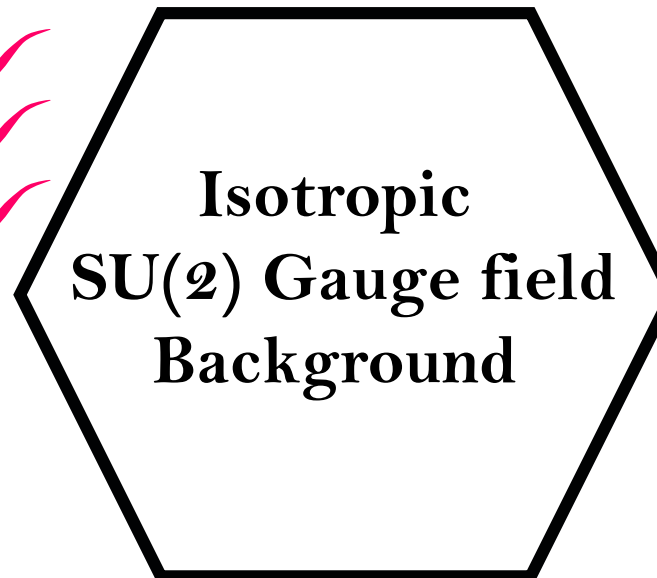
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- Breaking the conformal symmetry ✓
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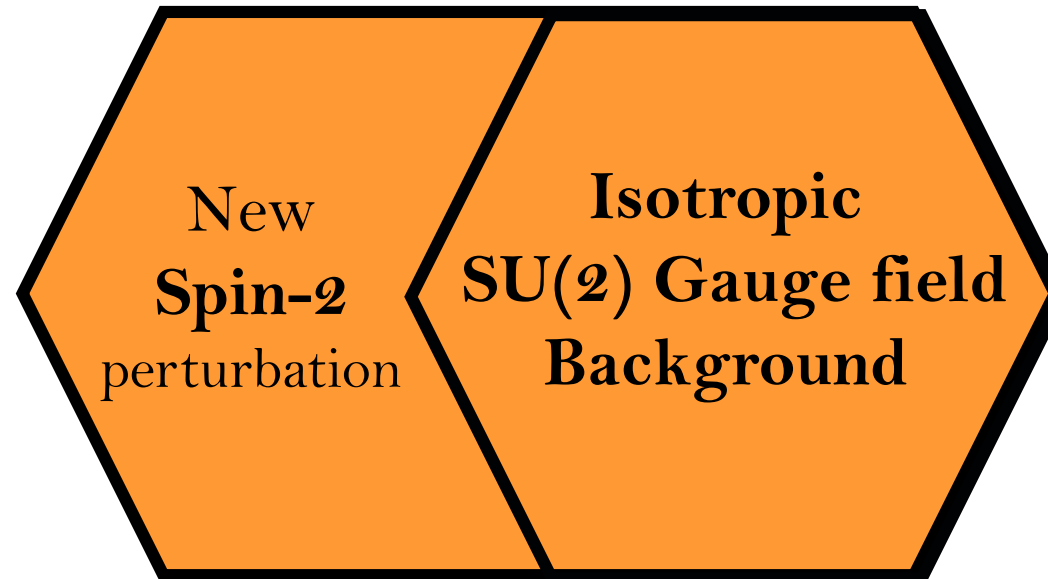
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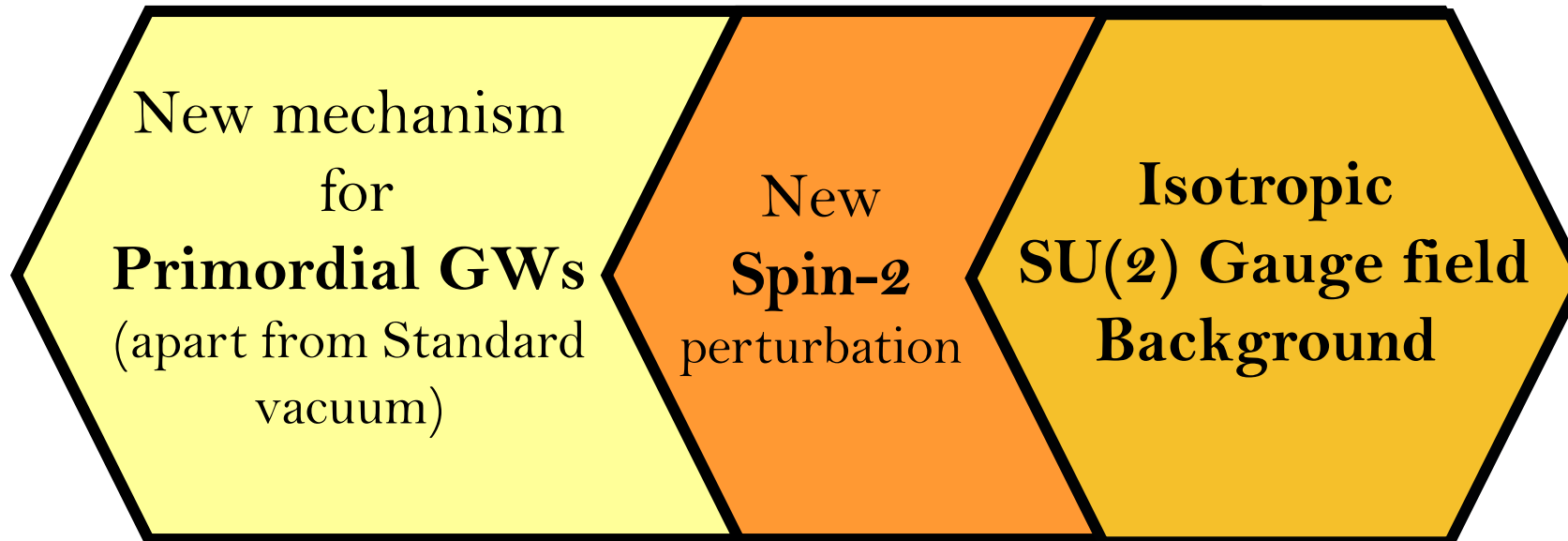
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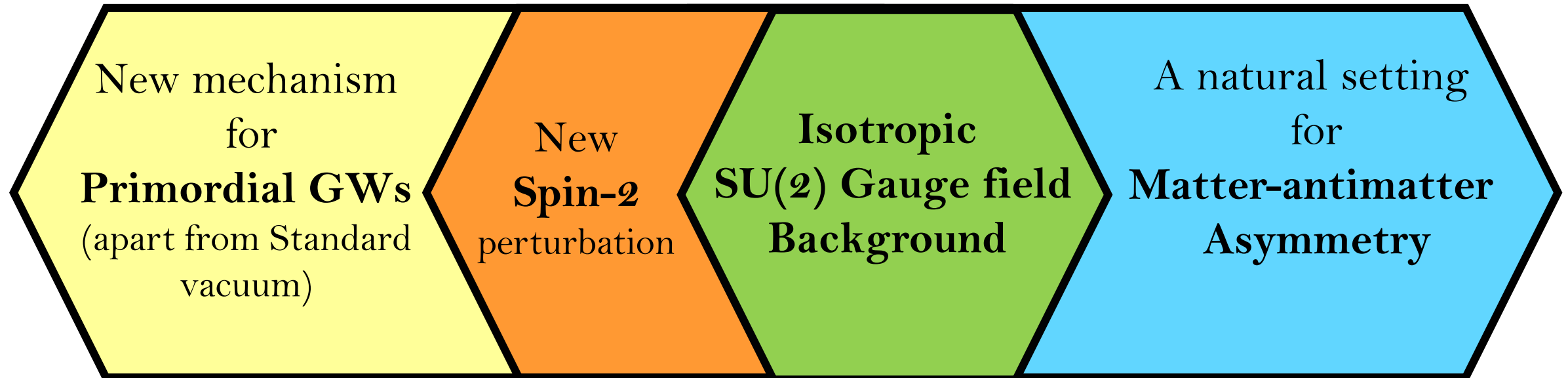
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Turns out that my **setup is much Smarter than me!**

Since 2011, many aspects and different realization of non-Abelian gauge fields in inflation have been studied.

Here is an incomplete list of colleagues and friends that contribute to the better understanding of this setup.

A.M., P. Adshead, M. Wyman, M. Peloso, M.M. Sheikh-Jabbari,
J. Soda, E. Dimastrogiovanni, E. Komatsu, A. Agrawal, T. Fujita,
E. Sfakianakis, M. Noorbala, R. Caldwell, K. Lozanov, B. Thorne,
M. Hazumi, N. Katayama, M. Shiraishi, J. Bielefeld, C.
Devulder, N. A. Maksimova, R. Namba, I. Obata, V. Domcke, Y.
Ema, K. Mukaida, R. Sato and ...

SU(2) Gauge fields and Inflation

- **Gauge-flation** A. M. and M. M. Sheikh-Jabbari, Phys. Lett. B723 (2013) [*arXiv:1102.1513*]
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$$S_{Gf} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{4} F^2 + \frac{\kappa}{384} (F \tilde{F})^2 \right)$$

- **Chromo-natural** P. Adshead, M. Wyman, Phys. Rev. Lett.(2012) [*arXiv:1202.2366*]

$$S_{Cn} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{4} F^2 - \frac{1}{2} \left(\partial_\mu \chi \right)^2 - \mu^4 \left(1 + \cos\left(\frac{\chi}{f}\right) \right) - \frac{\lambda}{8f} \chi F \tilde{F} \right)$$

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- Inspired by them, several different models with SU(2) fields have been proposed and studied.

An incomplete list of models with SU(2) gauge field:	α_H	α_s
1. A. M. and M. M. Sheikh-Jabbari, Phys. Lett. B723 (2013) [arXiv:1102.1513]	0	0
2. P. Adshead, M. Wyman, Phys. Rev. Lett.(2012) [arXiv:1202.2366]	0	0
3. A. M. JHEP 07 (2016) 104 [arXiv:1604.03327]	0	0
4. C. M. Nieto and Y. Rodriguez Mod. Phys. Lett. A31 (2016) [arXiv:1602.07197]	1	0
5. E. Dimastrogiovanni, M. Fasiello, and T. Fujita JCAP 1701 (2017) [arXiv:1608.04216]	0	1
6. P. Adshead, E. Martinec, E. I. Sfakianakis, and M. Wyman JHEP 12 (2016) 137 [arXiv:1609.04025]	1	0
7. P. Adshead and E. I. Sfakianakis JHEP 08 (2017) 130 [arXiv:1705.03024]	1	0
8. R. R. Caldwell and C. Devulder Phys. Rev. D97 (2018) [arXiv:1706.03765]	0	0
-	1	1

- These models can be represented in the unified form

$$S = \alpha_H \underbrace{S_H(A_\mu, H)}_{\text{Higgs sector (mass for gauge field)}} + \alpha_s \underbrace{S_s(\chi)}_{\text{Scalar inflaton (spectator SU(2))}} + S_A(A_\mu, \varphi)$$

Higgs sector
(mass for gauge field)

Scalar inflaton
(spectator SU(2))

S_A is either S_{Gf} (Gauge-flation) or S_{Cn} (Chromo-natural with an arbitrary potential)

$$\alpha_H = \begin{cases} 0 \\ 1 \end{cases} \quad \text{Higgsed (massive SU(2))}$$

$$\alpha_s = \begin{cases} 0 \\ 1 \end{cases} \quad \text{Spectator SU(2)}$$

A. M. and E. Komatsu, [arXiv:1808.09076]

- The unified action for the inflation models with an SU(2) gauge field

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Higgs sector
(mass for gauge field)

Scalar inflaton
(spectator SU(2))

S_A is either S_{Gf} (Gauge-flation) or S_{Cn} (Chromo-natural with an arbitrary potential)

- Due to the SU(2) gauge field with a non-zero VEV, they all share these features

I. The FRW friendly VEV solution $A_\mu^a(t) = \begin{cases} 0 & \mu = 0 \\ a(t)\psi(t)\delta_i^a & \mu = i \end{cases}$

II. New Spin-2 field $\delta A_i^a(t, \vec{x}) = B_{ij} \delta_i^a + \text{scalar \& vector fields}$

SU(2) Gauge fields and Inflation

- It starts in 2011 $A_\mu = A_\mu^a T_a$ $[T_b, T_c] = i \epsilon_{abc} T_a$

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i) SU(2) gauge fields are FRW friendly: (respect isotropy & homogeneity)

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ii) Breaking conformal symmetry & respecting the gauge symmetry

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- iii) Extra spin-2 degrees of freedom:

$$\delta A_i^a(t, \vec{x}) = \underbrace{\delta S_i^a}_{\text{Scalar and vector d.o.f}} + \overbrace{B_{ij}}^{\text{Spin-2 field}} \delta_i^a$$

Scalar and vector d.o.f

- iv) Spin-2 field breaks Parity & coupled linearly with gravity waves

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 Chiral primordial Gravitational waves

Spin-2 Particle Production & Chiral Gravity waves

- Spin-2 field $\delta A_i^a(t, \vec{x}) = B_{ij}(t, \vec{x}) \delta_i^a$ is governed by (δ_c and $\frac{m^2}{H^2}$ are two positive, order 10, given by BG fields)

$$B_{\pm}'' + \underbrace{\left[k^2 \mp \delta_c k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a} \right]}_{\omega_{\sigma}^2(\tau, k) \text{ effective frequency}} B_{\pm} \approx 0$$

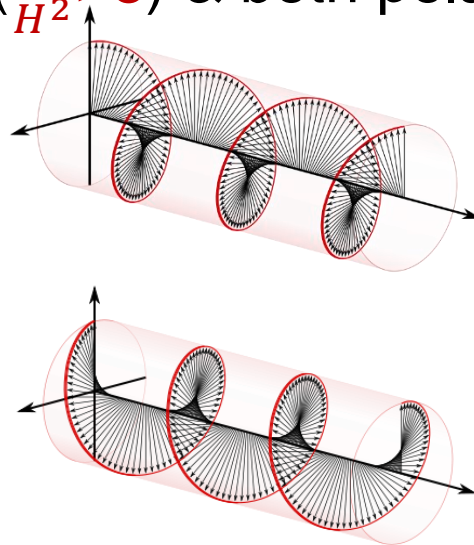
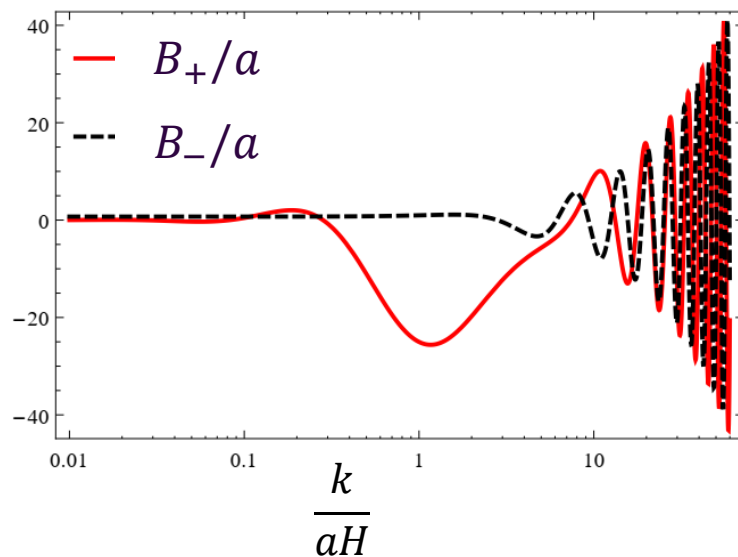
$\omega_{\sigma}^2(\tau, k)$ effective frequency

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- Polarization B_+ has a short time of particle production before horizon crossing.
- Polarization B_- is (almost) always very close to its vacuum state, negligible pair production.
- The B_{\pm} fields are massive ($\frac{m^2}{H^2} > 8$) & both polarizations decay after horizon crossing.



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$\omega_{\sigma}^2(\tau, k)$ effective frequency

- due to the derivative interaction, $\omega_{\sigma}^2(\tau, k)$ is
- 1) chiral
- 2) violates adiabaticity conditions for a short period before horizon exit.

$$\left(\frac{\partial_{\tau} \omega_{+}(\tau, k)}{\omega_{+}^2(\tau, k)} \right)^2 \ll 1 \quad \text{and} \quad \frac{\partial_{\tau}^2 \omega_{+}(\tau, k)}{\omega_{+}^3(\tau, k)} \ll 1$$

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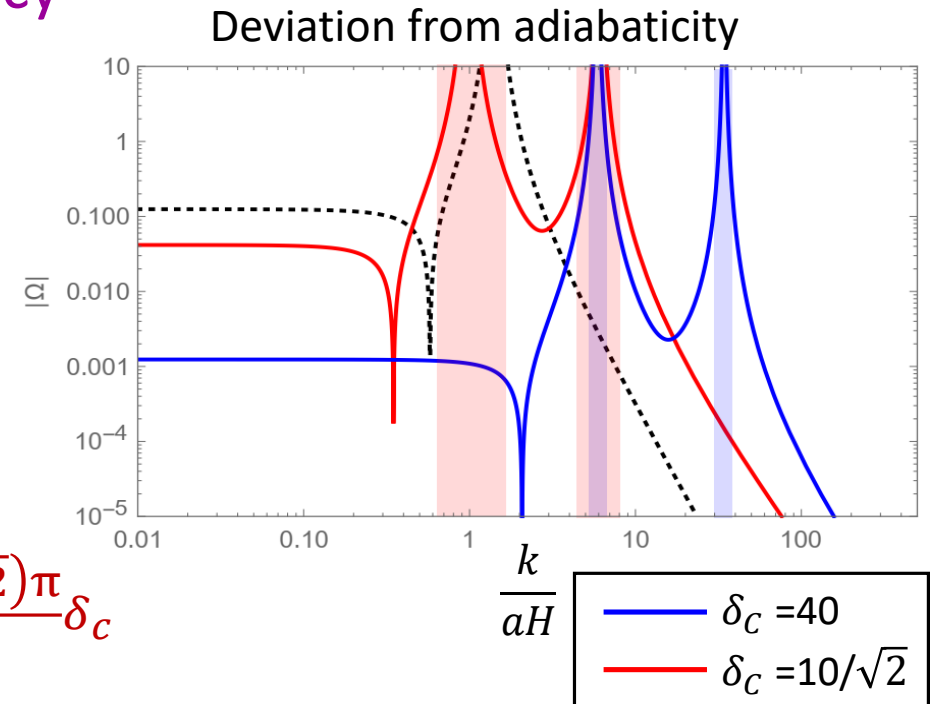
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Chiral particle production $n_B \sim \frac{H^3}{6\pi^2} \delta_c^3 e^{\frac{(2-\sqrt{2})\pi}{2} \delta_c}$



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- That sourced the Gravity waves $\delta g_{ij}(t, \vec{x}) = a h_{ij}(t, \vec{x})$ as $(h_{ij} \equiv a \gamma_{ij})$

$$h_{\pm}'' + \left[k^2 - \frac{a''}{a} \right] h_{\pm} \approx \underbrace{\frac{2\psi}{M_{Pl}} \mathcal{H}^2 \Pi_{\pm}[B_{\pm}]}_{\text{Anisotropic stress}}$$

Anisotropic stress

Linear in B_{\pm}

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The efficiency of the coupling of B_{\pm} to GWs is proportional to the VEV of the SU(2) gauge field.

Anisotropic stress
Linear in B_{\pm}

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- Gravitational waves have two uncorrelated terms



$$h_{\pm} = \underbrace{h_{\pm}^{vac}}_{\substack{\text{Vacuum} \\ \text{GWs} \\ \text{unpolarized}}} \\ h_+^{vac} = h_-^{vac}$$

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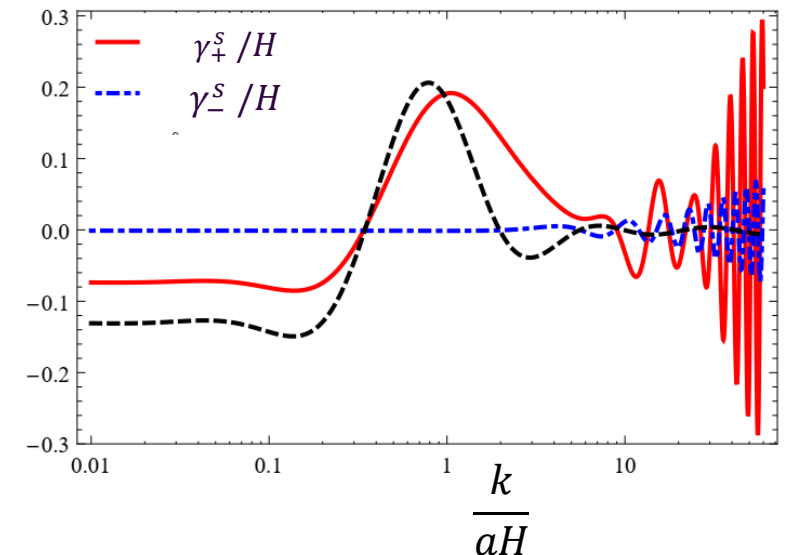
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$$h_{\pm} = h_{\pm}^{vac} + h_{\pm}^s$$

The ratio of the power spectra of sourced to vacuum gravitational waves is

$$\frac{P_T^s}{P_T^{vac}} = \frac{\langle \gamma_+^s \gamma_+^s \rangle}{\langle \gamma_+^{vac} \gamma_+^{vac} \rangle} \Big|_{-k\tau \ll 1} \simeq \left(\frac{\psi}{M_{Pl}} \right)^2 \left(\frac{n_B}{H^3} \right) \frac{3\pi^3 |\mathcal{A}_+|^2 |\kappa|}{(|\kappa| + \sqrt{|\kappa|^2 - |\mu|^2})^3}$$

Spin-2 Particle Production & Chiral Gravity waves

In the presence of the primordial SU(2) gauge fields

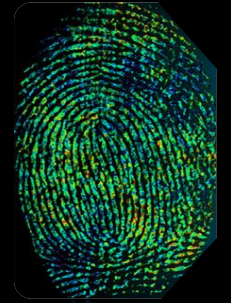
- i) The tensor power spectrum is not entirely specified by the **scale of inflation!**
- ii) Sizable tensor to scalar ratio without large field = **violation of Lyth bound!**
- iii) The tensor power spectrum is partially chiral and **parity odd correlations**
 $\langle TB \rangle$ and $\langle EB \rangle$ are non-zero!

- Gravitational waves have two uncorrelated terms

$$h_{\pm} = h_{\pm}^{vac} + h_{\pm}^s$$

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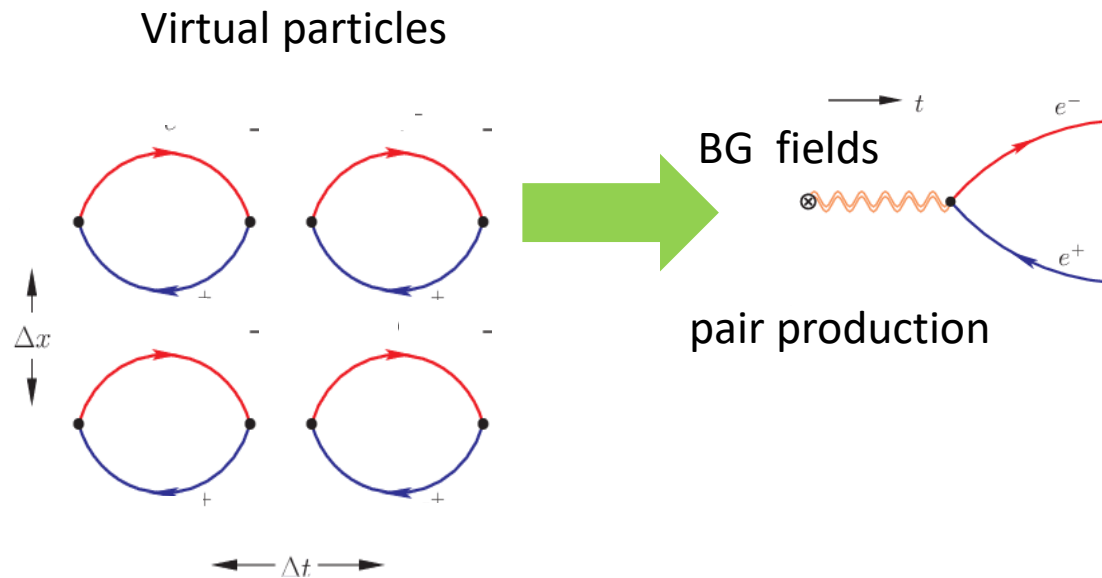


Schwinger Particle Production

- Charged scalar fields coupled to the SU(2) gauge field BG

$$S_{\text{matter}} = \int d^4x \sqrt{-g} \left[(\mathbf{D}_\mu \varphi)^\dagger \underbrace{\mathbf{D}^\mu \varphi}_{\text{red bracket}} - m^2 \varphi^\dagger \varphi \right]$$

$$\mathbf{D}_\mu \varphi = (\mathbf{I}_{2 \times 2} \nabla_\mu + i g_A \mathbf{A}_\mu) \varphi$$

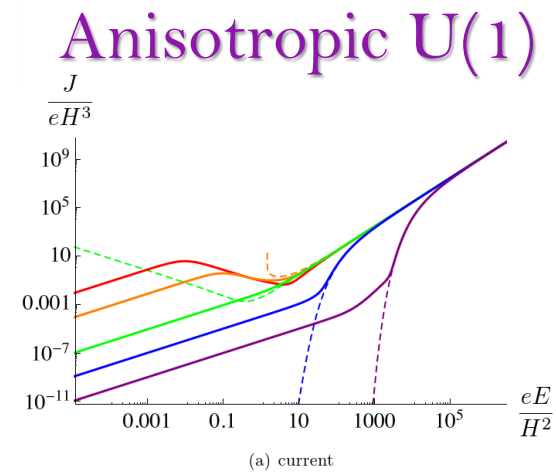
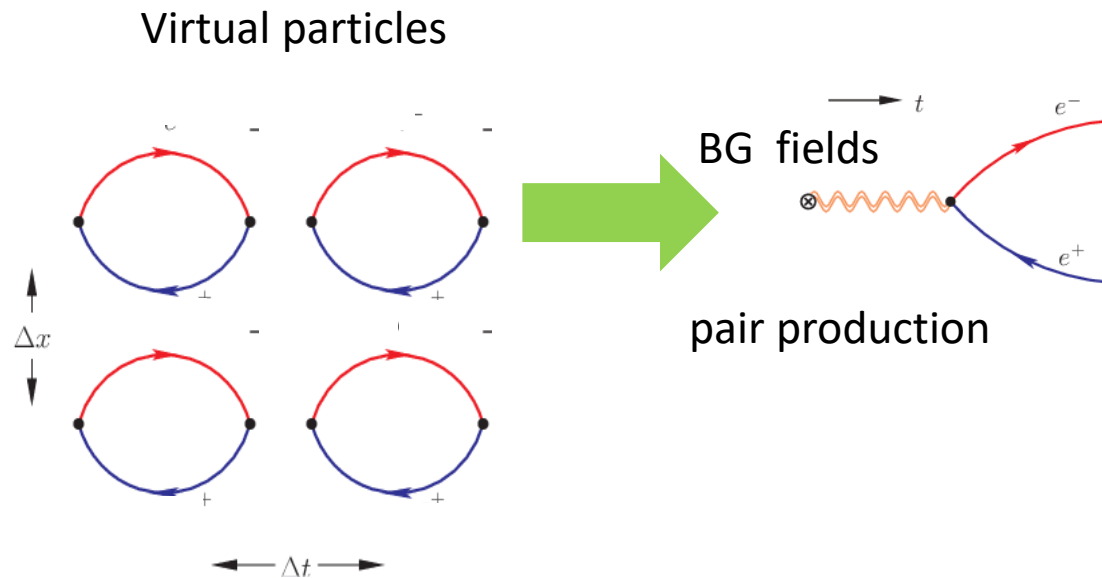


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$$\mathbf{D}_\mu \varphi = (\mathbf{I}_{2 \times 2} \nabla_\mu + i g_A \mathbf{A}_\mu) \varphi$$



Schwinger Particle Production

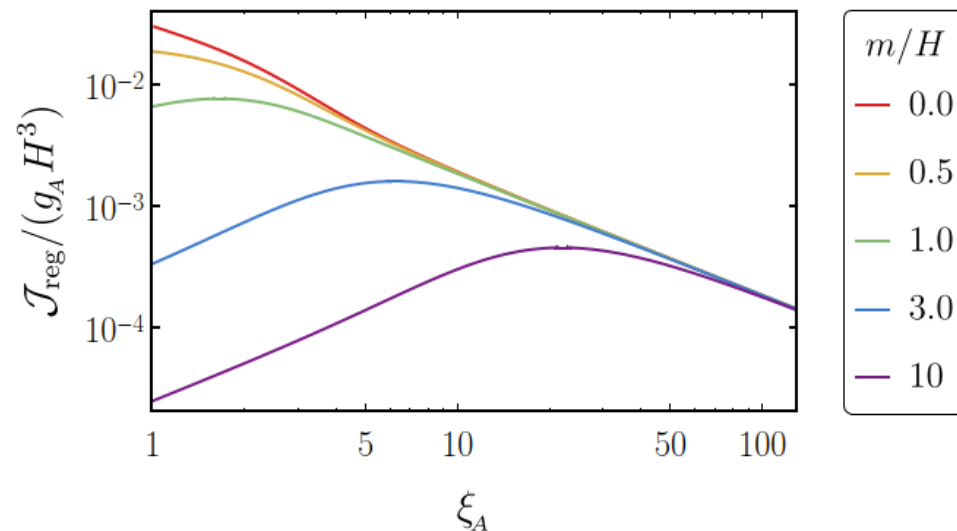
- Charged scalar fields coupled to the SU(2) gauge field BG

$$S_{\text{matter}} = \int d^4x \sqrt{-g} \left[(\mathbf{D}_\mu \varphi)^\dagger \underbrace{\mathbf{D}^\mu \varphi}_{\text{induced current}} - m^2 \varphi^\dagger \varphi \right]$$

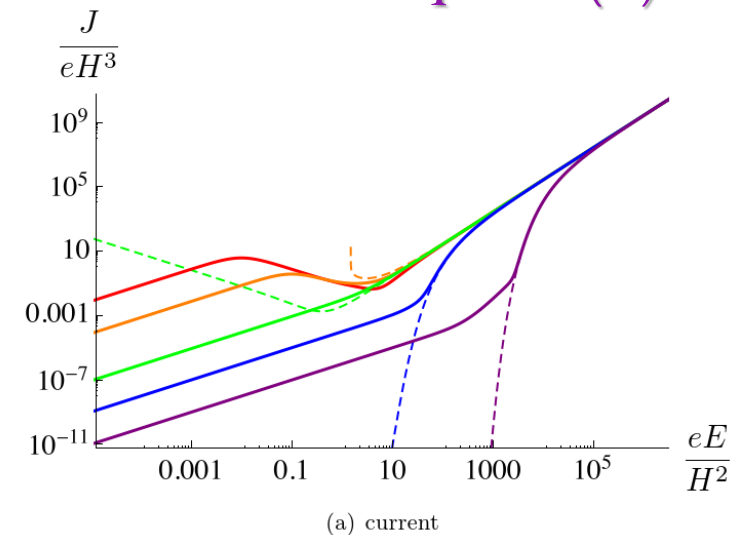
$$\mathbf{D}_\mu \varphi = (\mathbf{I}_{2 \times 2} \nabla_\mu + i g_A \mathbf{A}_\mu) \varphi$$

The induced current

Isotropic SU(2)



Anisotropic U(1)



Schwinger Particle Production

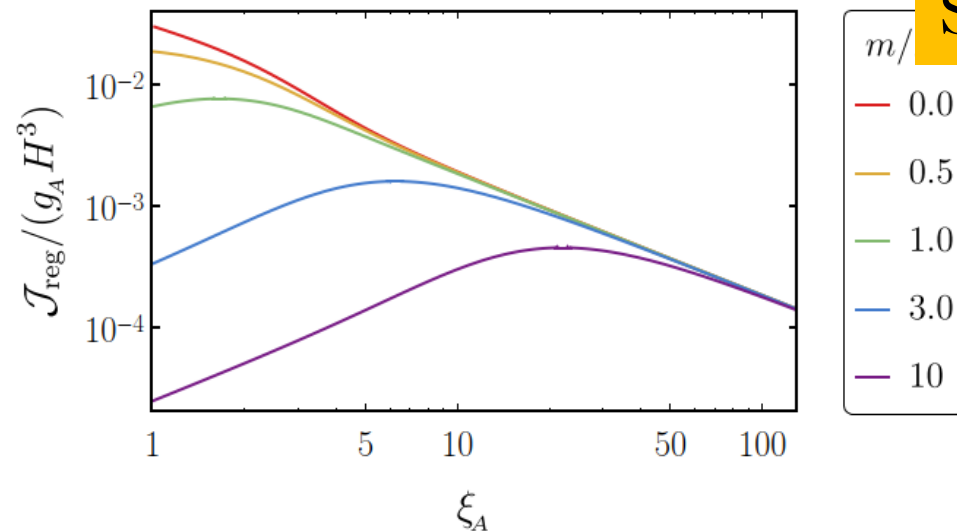
- Charged scalar fields coupled to the SU(2) gauge field BG

$$S_{\text{matter}} = \int d^4x \sqrt{-g} \left[(\mathbf{D}_\mu \varphi)^\dagger \underbrace{\mathbf{D}^\mu \varphi}_{\text{induced current}} - m^2 \varphi^\dagger \varphi \right]$$

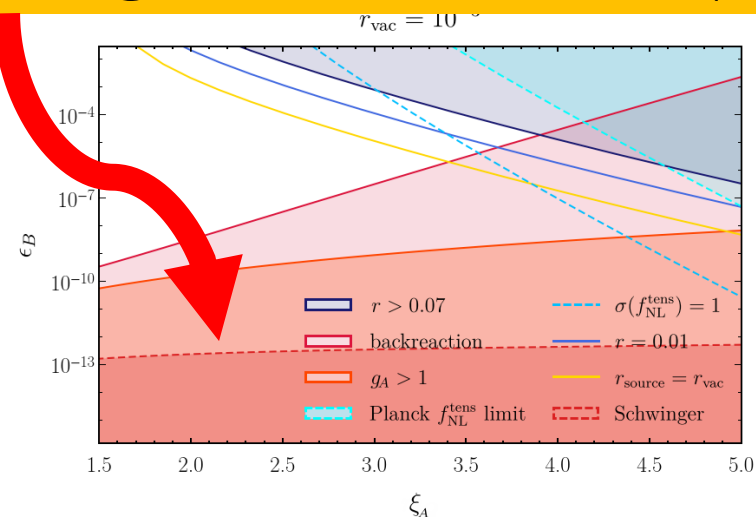
$$\mathbf{D}_\mu \varphi = (\mathbf{I}_{2 \times 2} \nabla_\mu + i g_A \mathbf{A}_\mu) \varphi$$

The induced current

Isotropic SU(2)



Unlike U(1) case! Negligible Schwinger effect for Iso. SU(2)



In the presence of the primordial SU(2) gauge fields

- i) The tensor power spectrum is not entirely specified by the scale of inflation!
- ii) Sizable tensor to scalar ratio without large field.
- iii) The tensor power spectrum is partially chiral and parity odd correlations

$\langle TB \rangle$ and $\langle EB \rangle$ are non-zero!

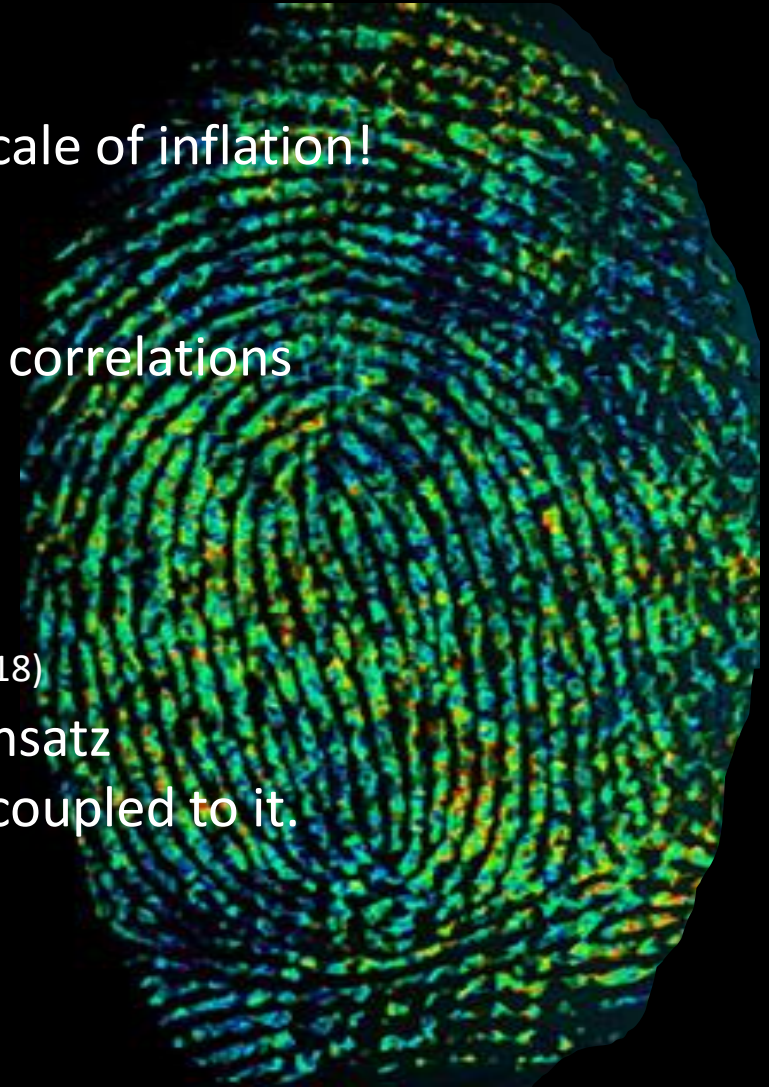
- iv) Possible large tensor non-Gaussianity.

Aniket Agrawal, Tomohiro Fujita, Eiichiro Komatsu, JCAP 1806 (2018) & Phys.Rev. D97 (2018)

- v) Unlike U(1) gauge fields, the SU(2) field in the FRW friendly ansatz does not receive any sizable backreaction from charged fields coupled to it.

- vi) Naturally explains the matter asymmetry in our Universe!

A. M. Phys. Rev. D (2014) & JCAP 1612 (2016)





Thank You!