



上海交通大學

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# Constrain Massive Cluster Formation with SDSS

Ying Zu (祖颖)

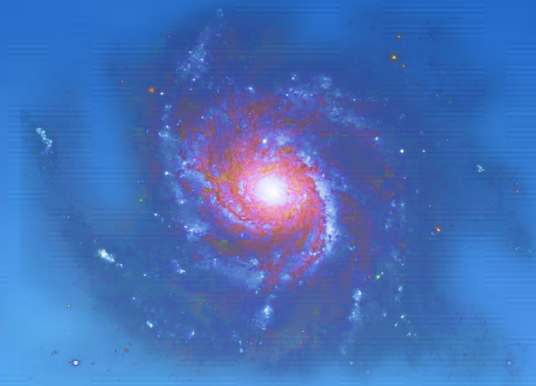
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Rachel Mandelbaum (CMU), Weiguang Cui (Madrid)





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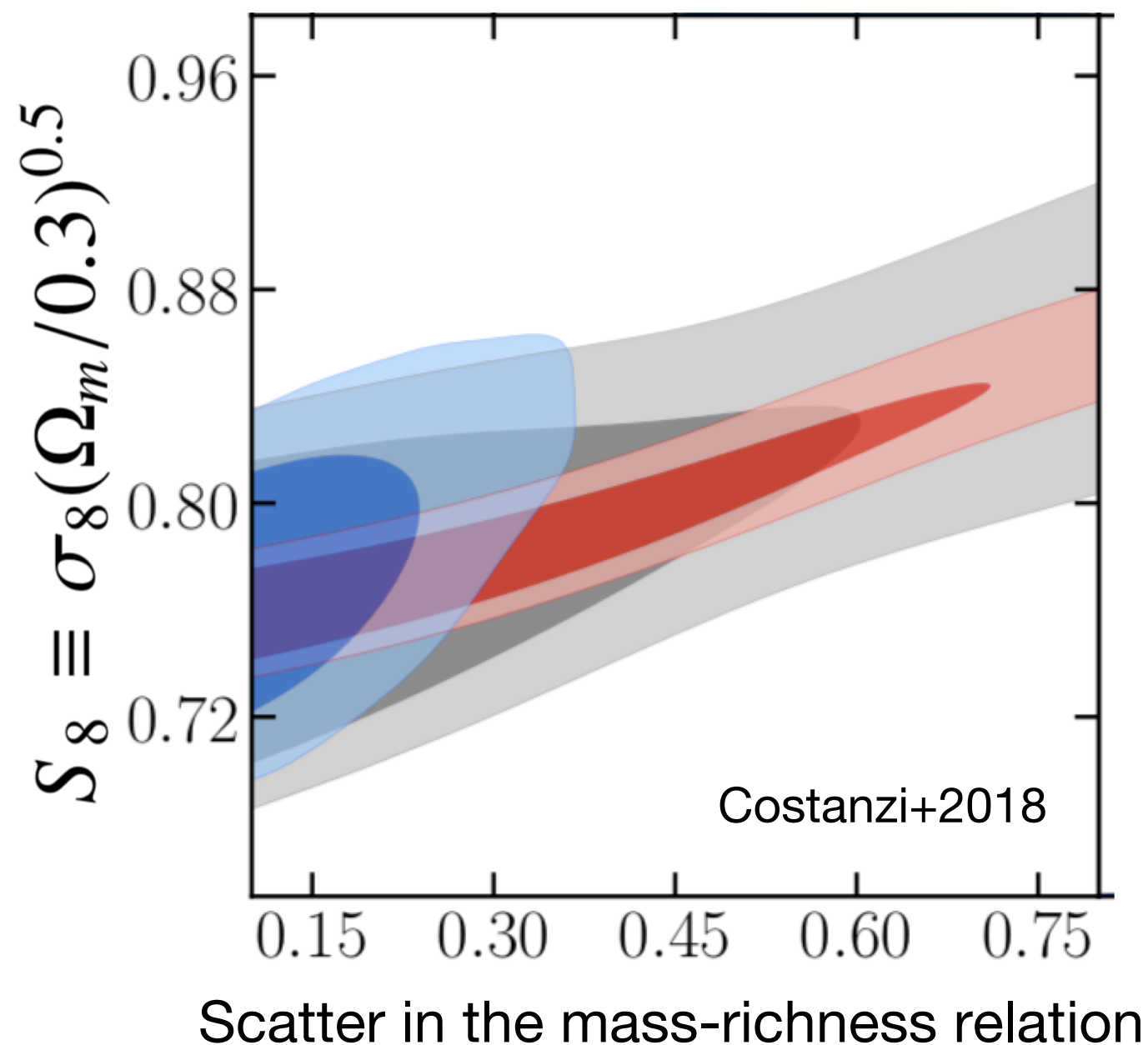
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# Cluster cosmology: mass-observable relation

The scatter in the mass-observable relation is THE most important source of systematic uncertainty in cluster cosmology.  
(observables: richness,  $L_x$ ,  $T_x$ , SZ, etc)

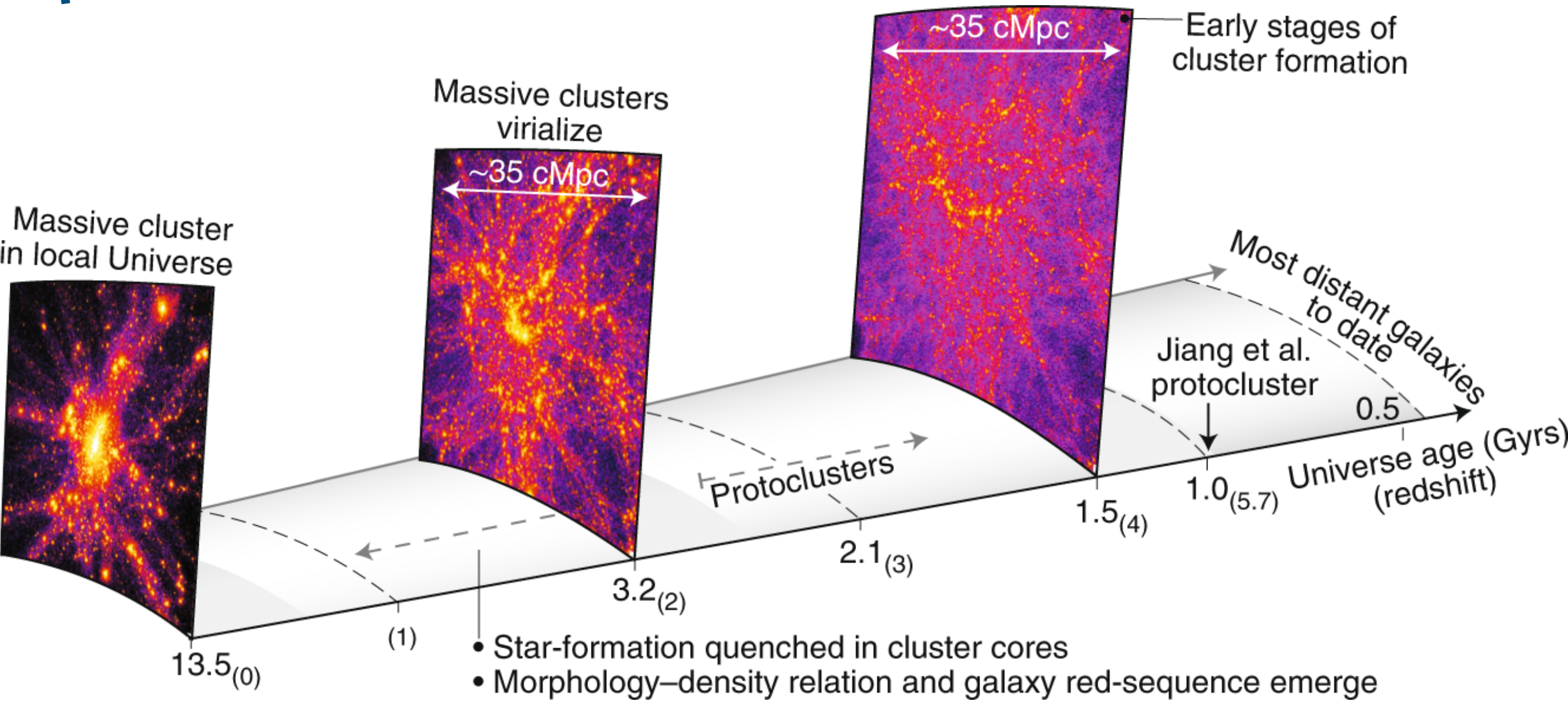


*More from Hendrik,  
Elisabeth, Miyatake,  
and Chiaki's talks*

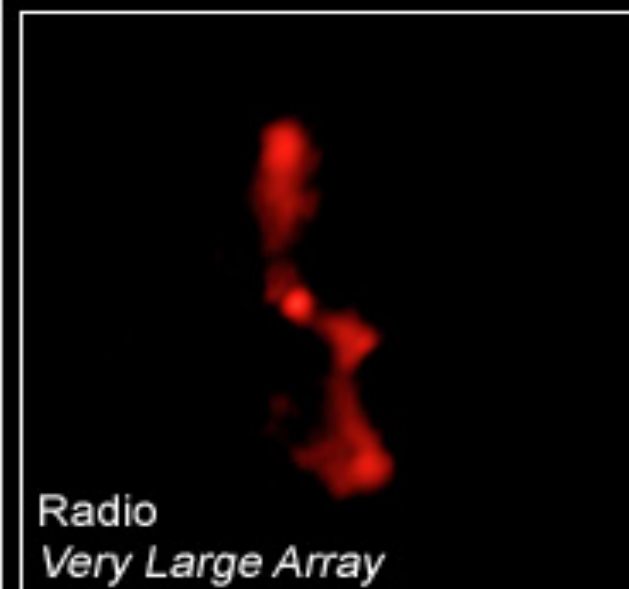
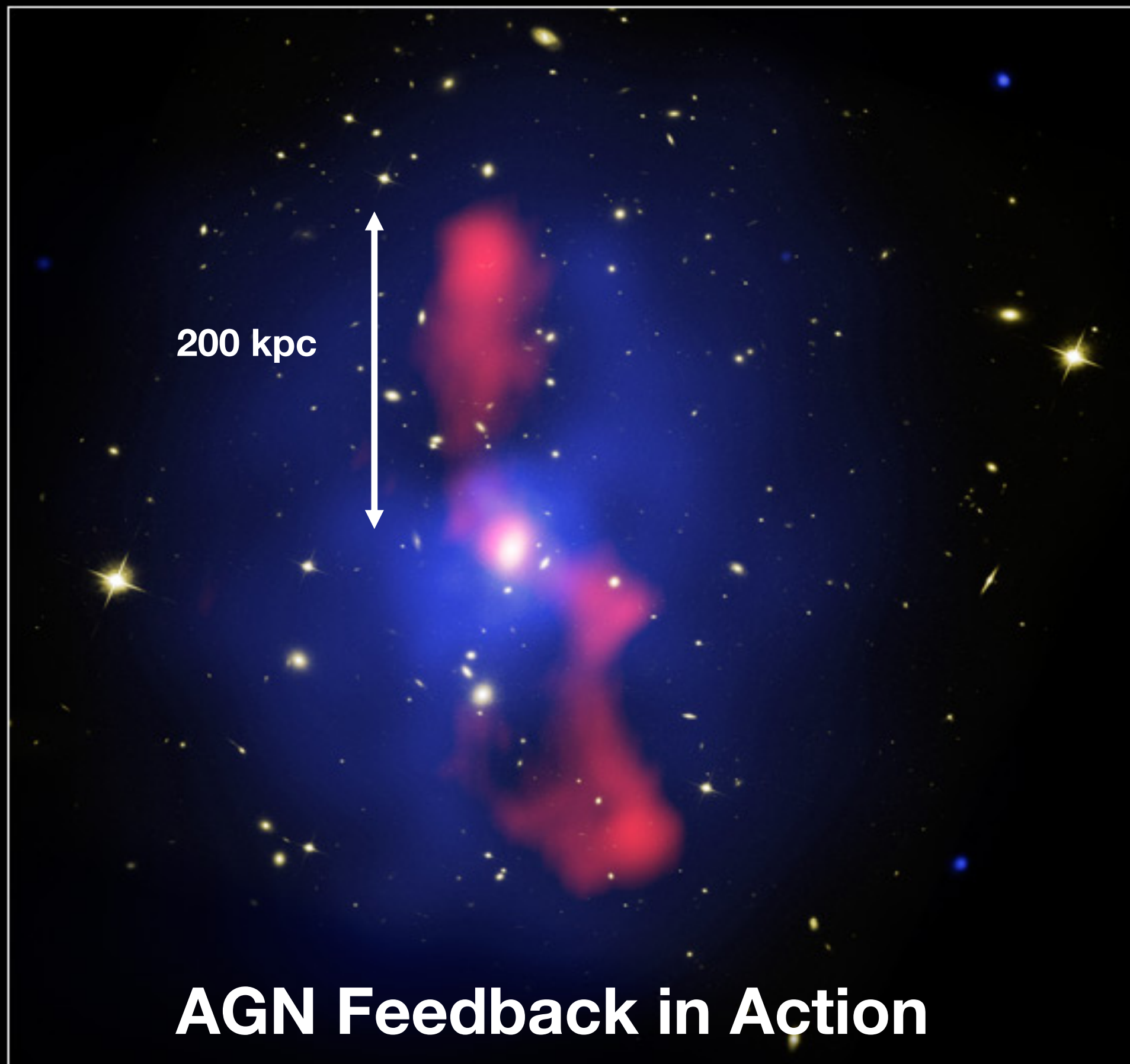


You can *marginalize over  
marching-learn*

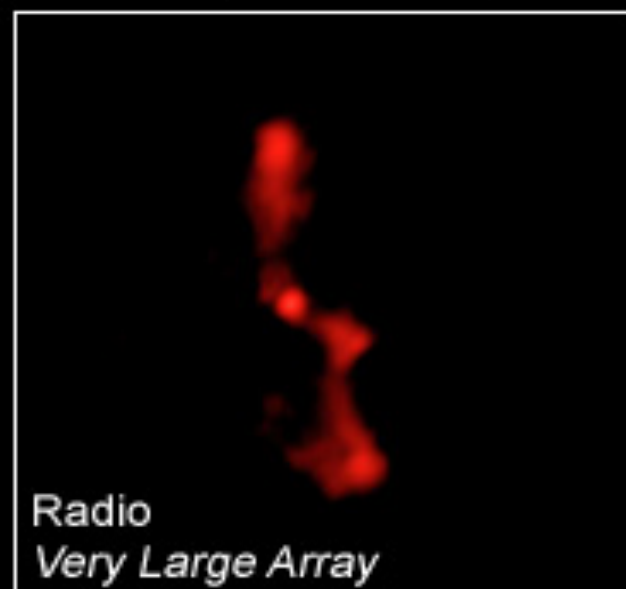
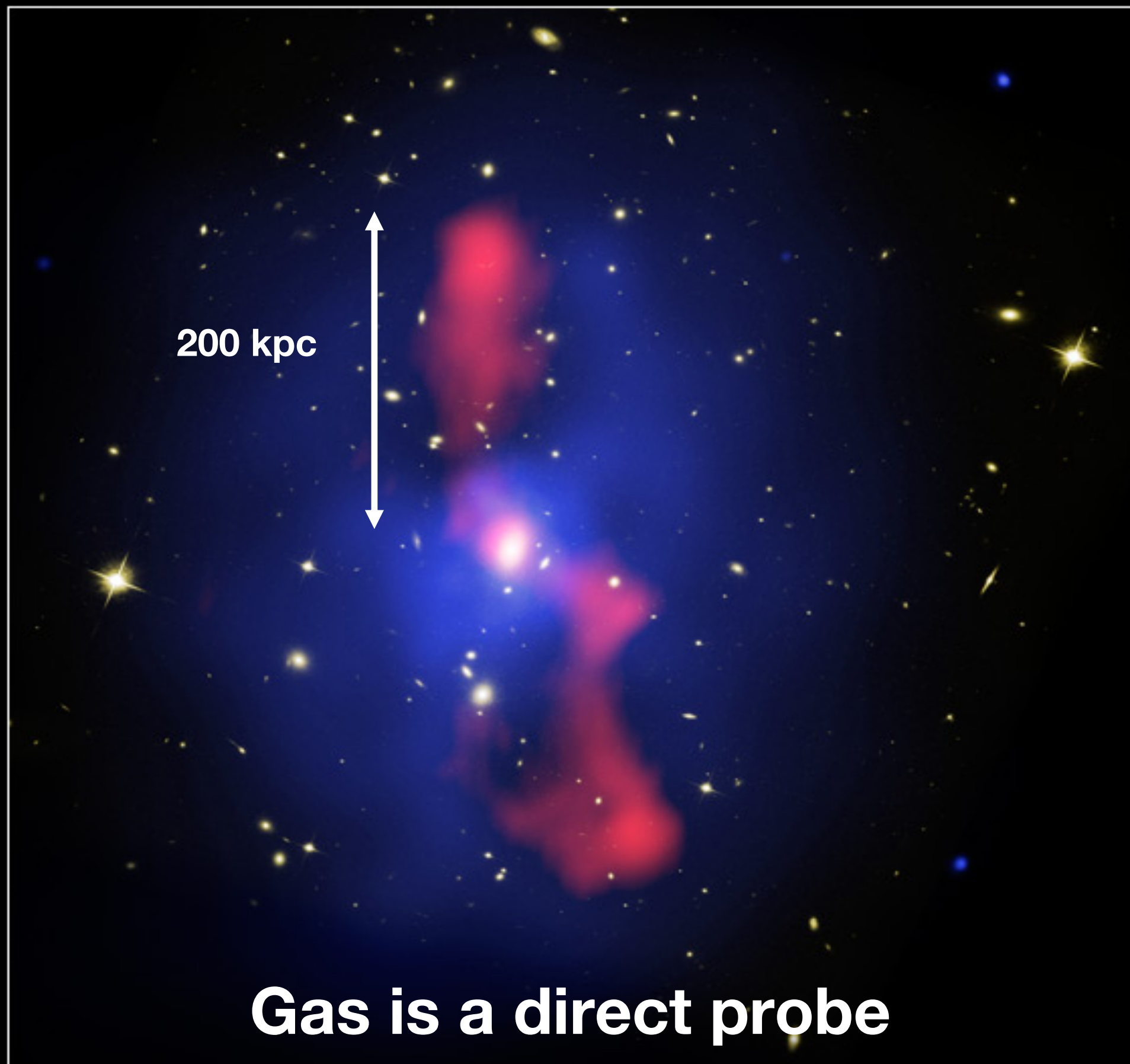
or solve for the **astrophysics**





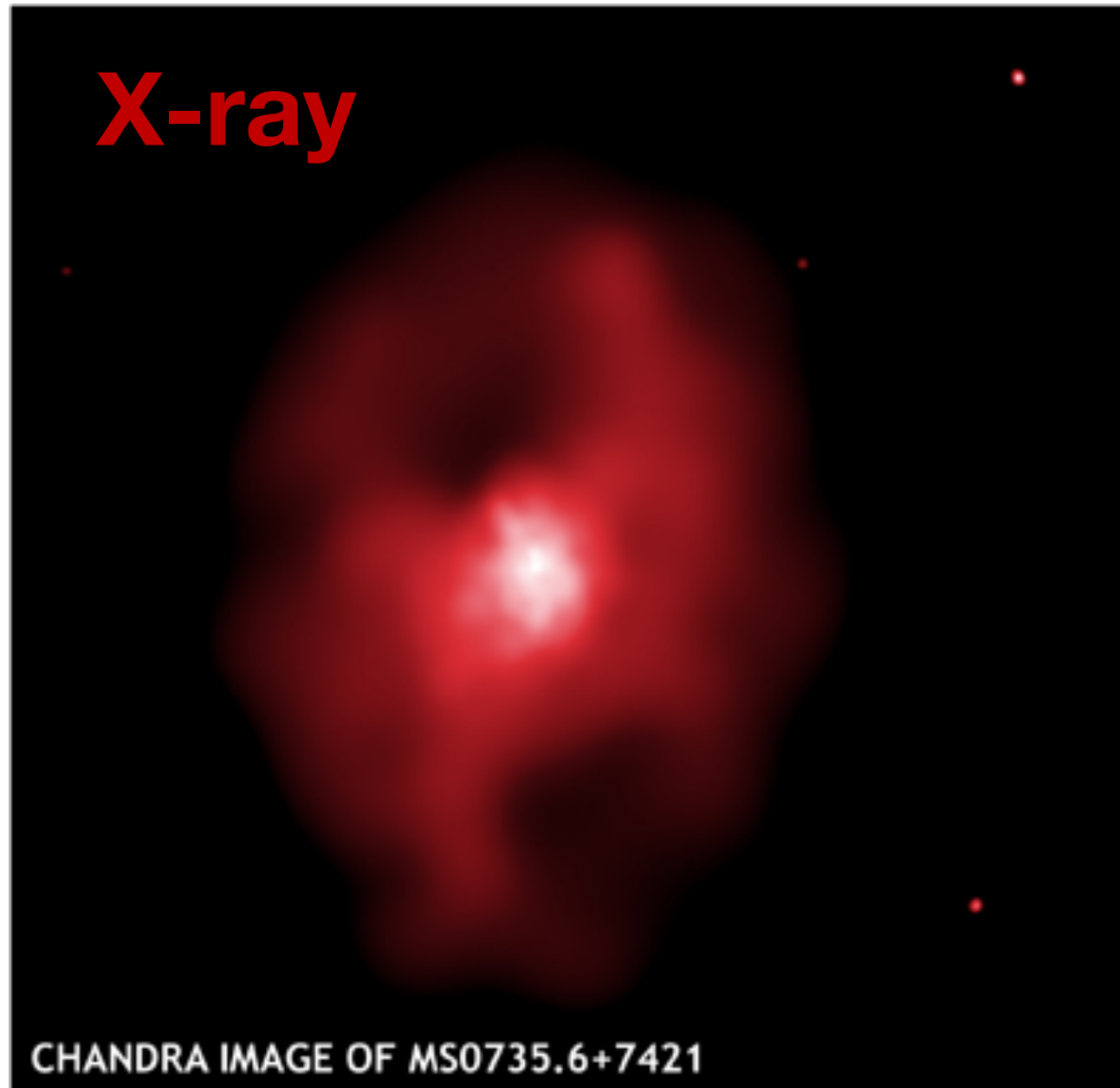




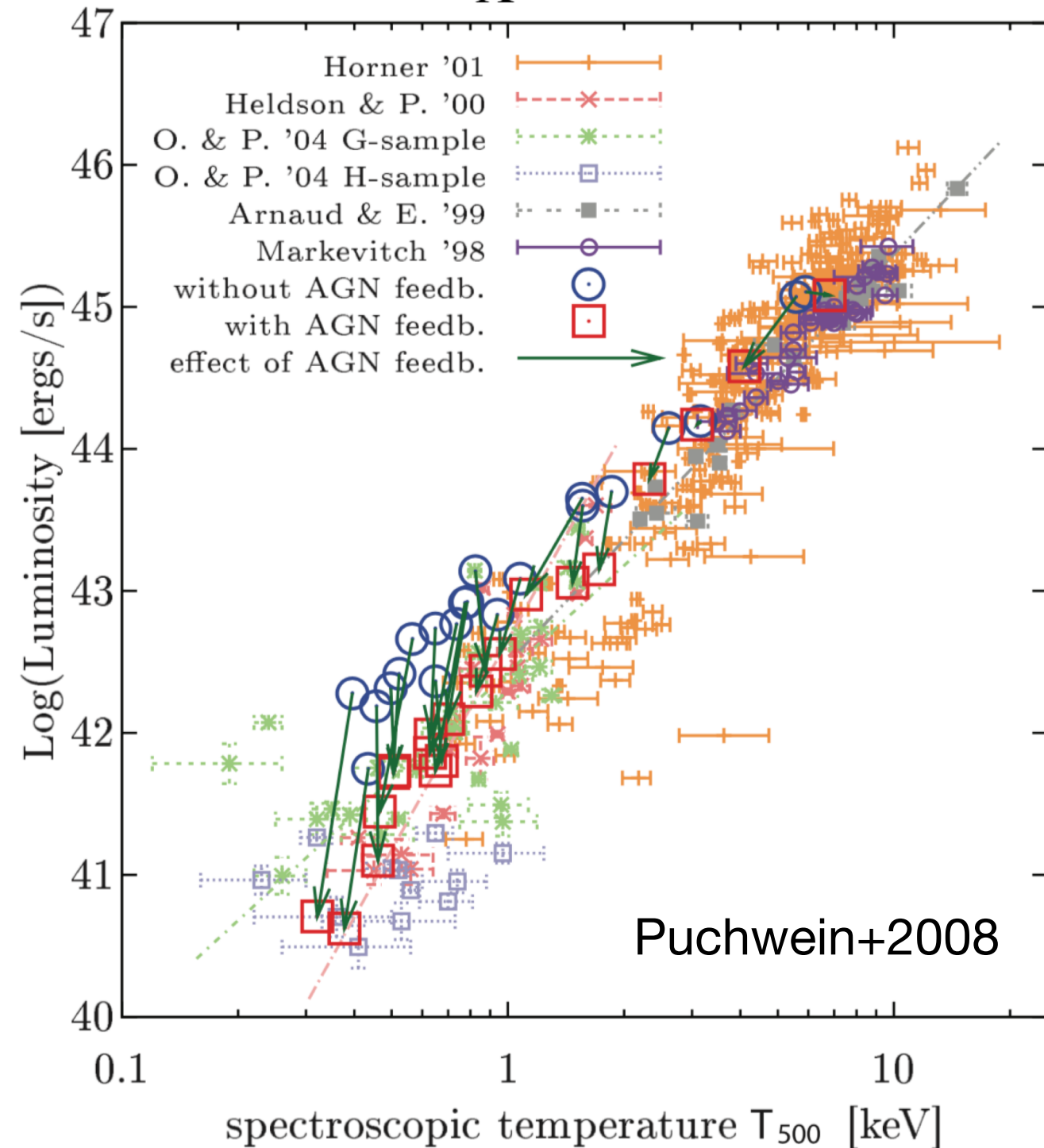




# You can use X-ray gas to constrain AGN feedback



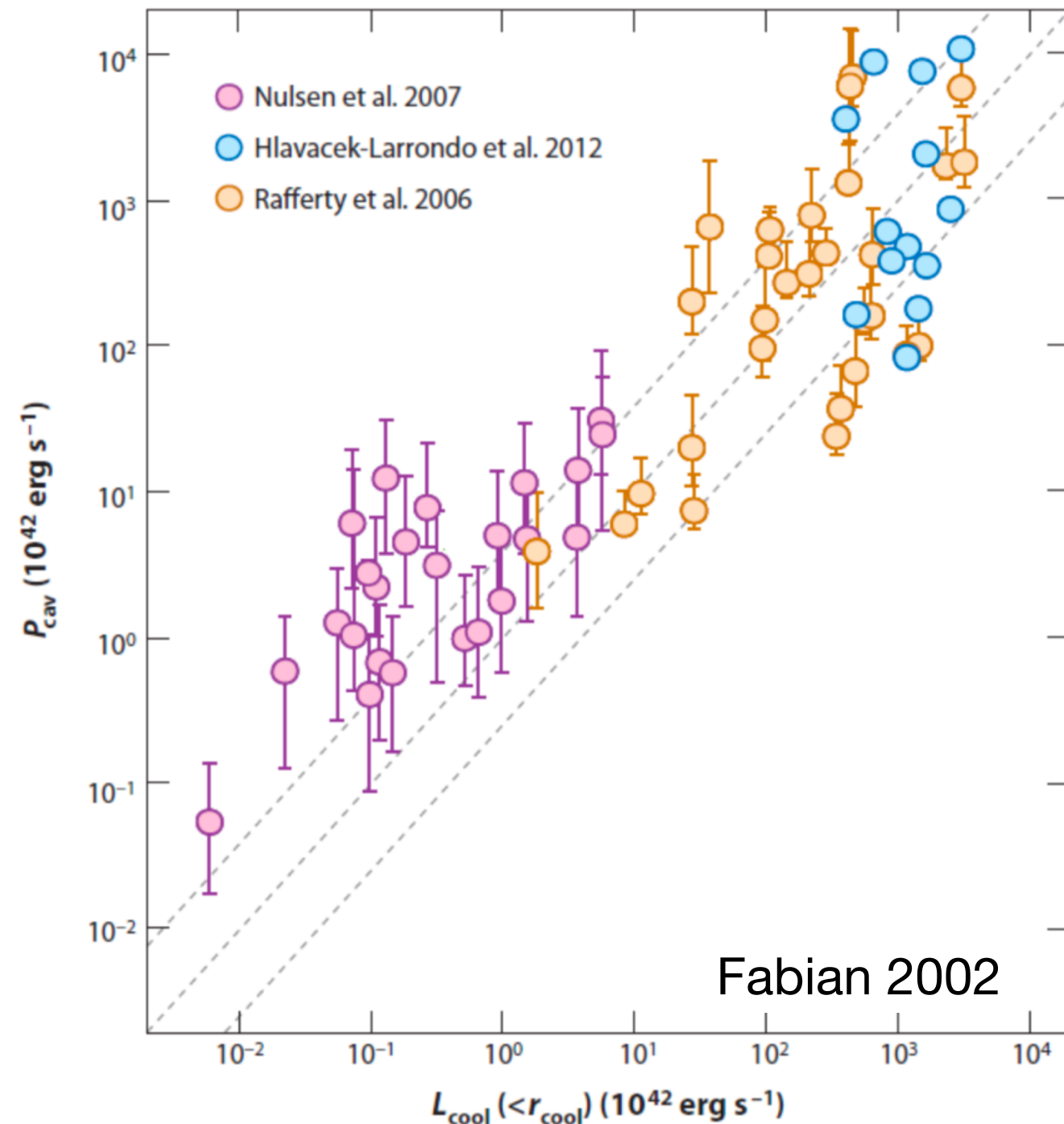
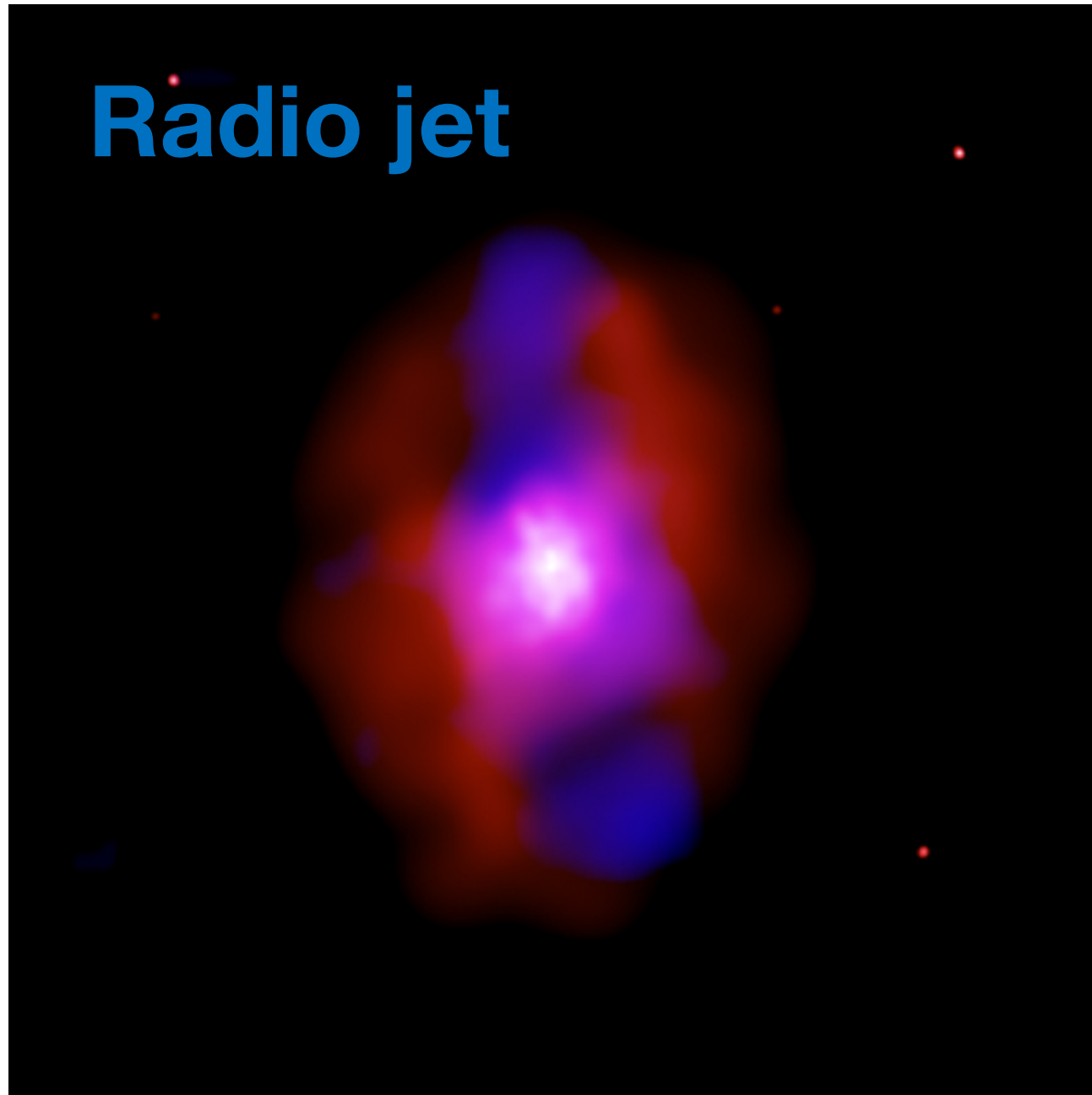
## *The $L_X$ - $T$ Relation*



# You can use Radio to constrain AGN feedback

## Jet Heating Power vs. Cooling luminosity

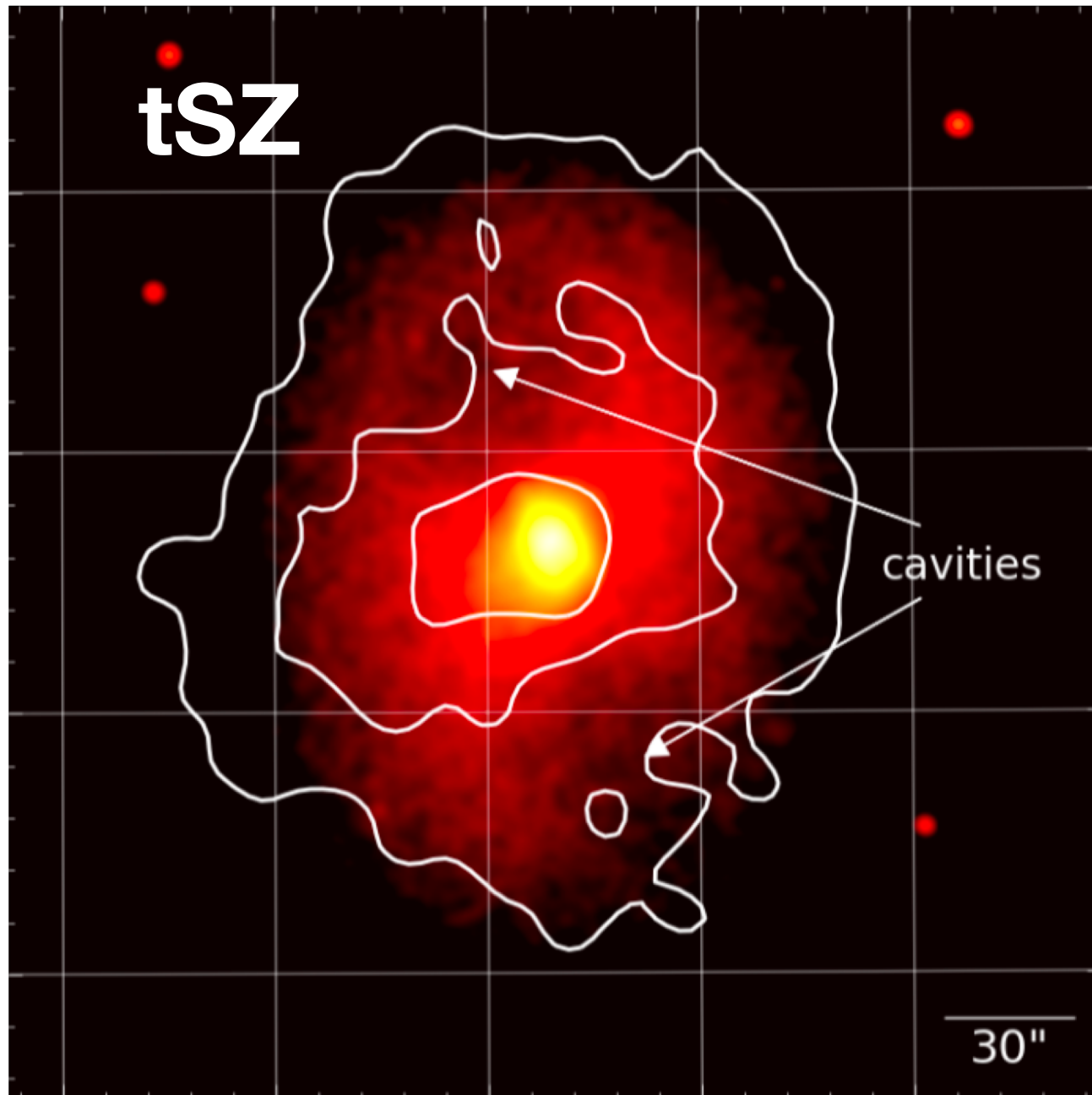
Radio jet



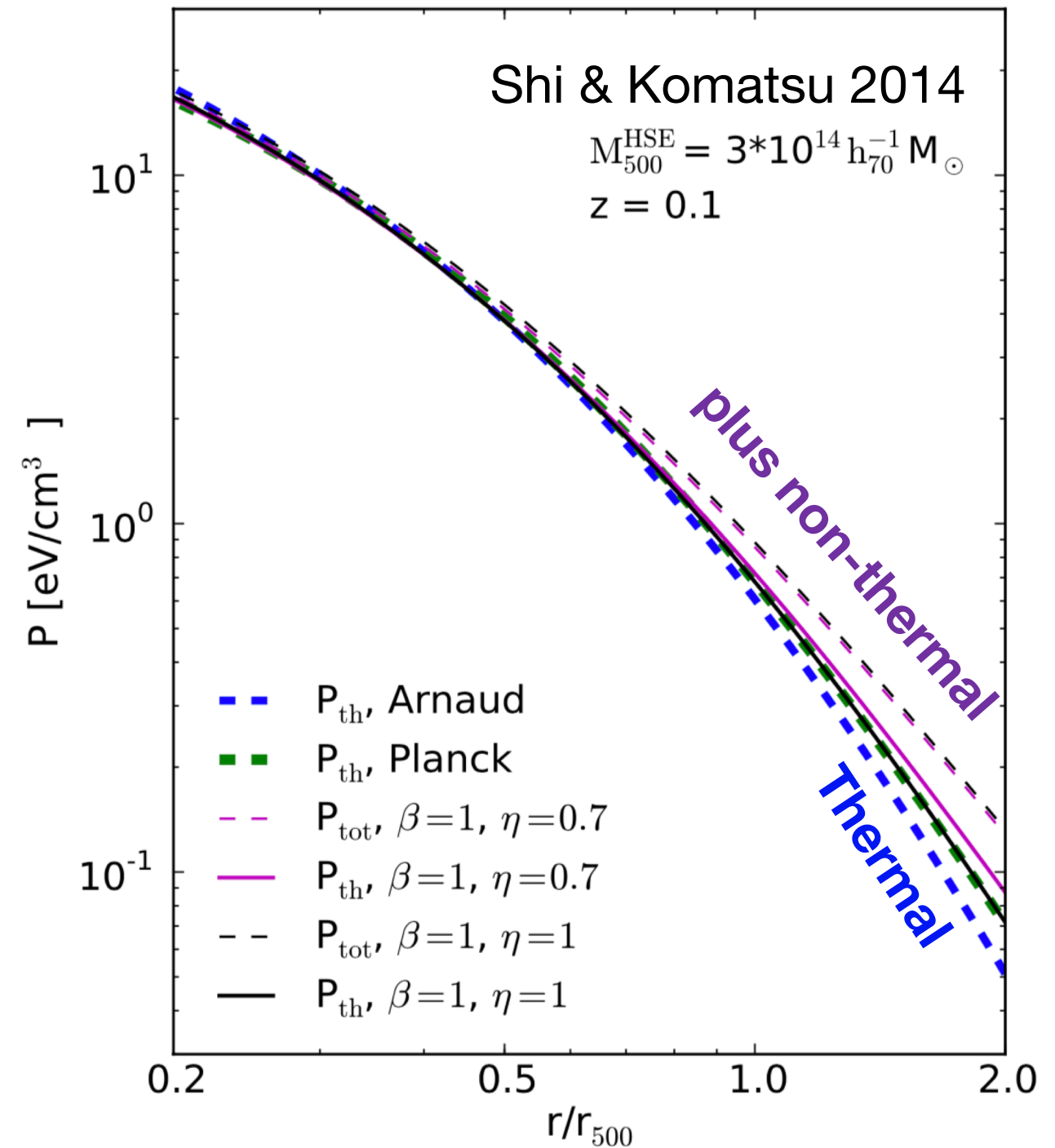


# You can also use Sunyaev Zeldovich effect

## Analytical model for non-thermal pressure



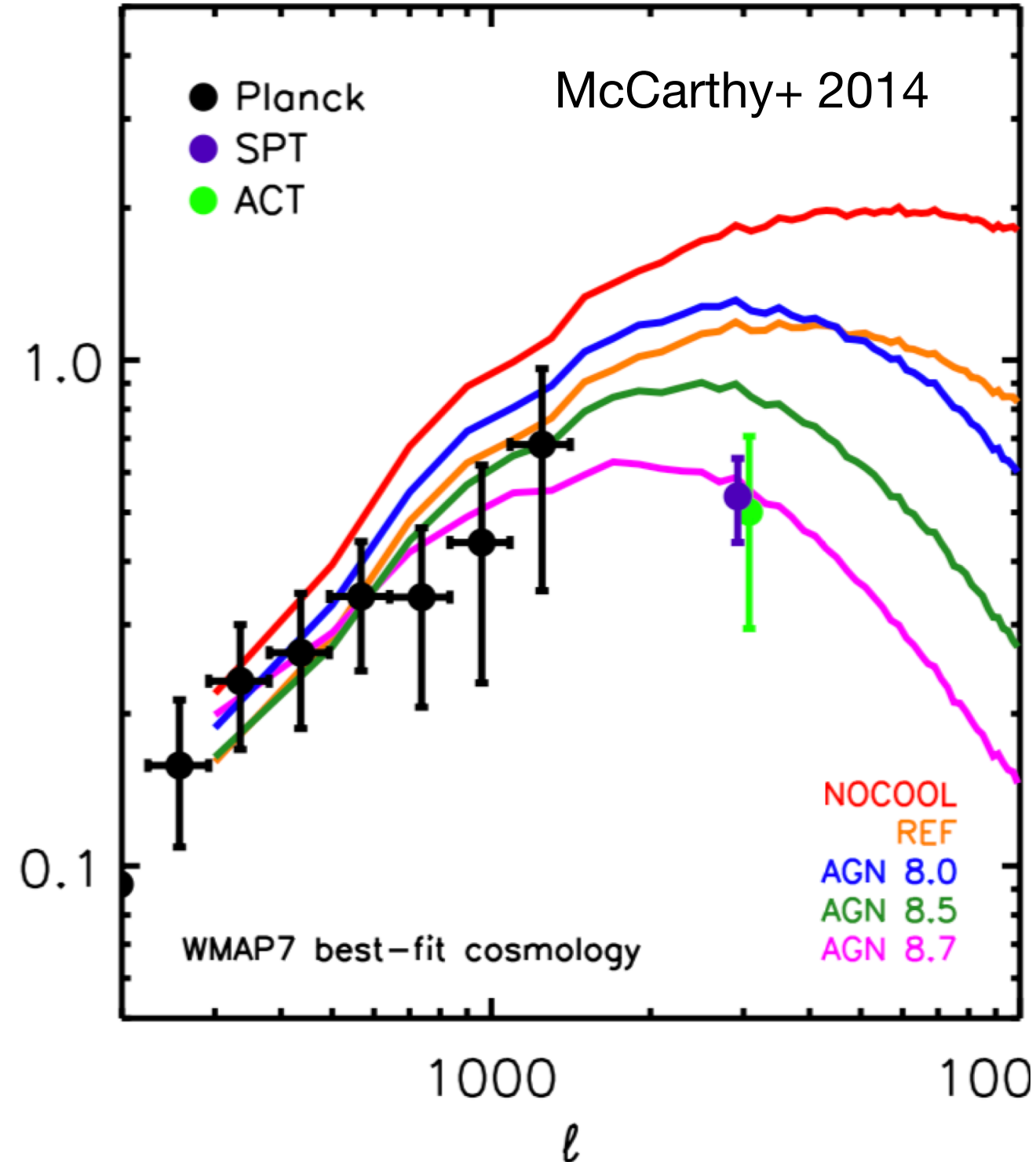
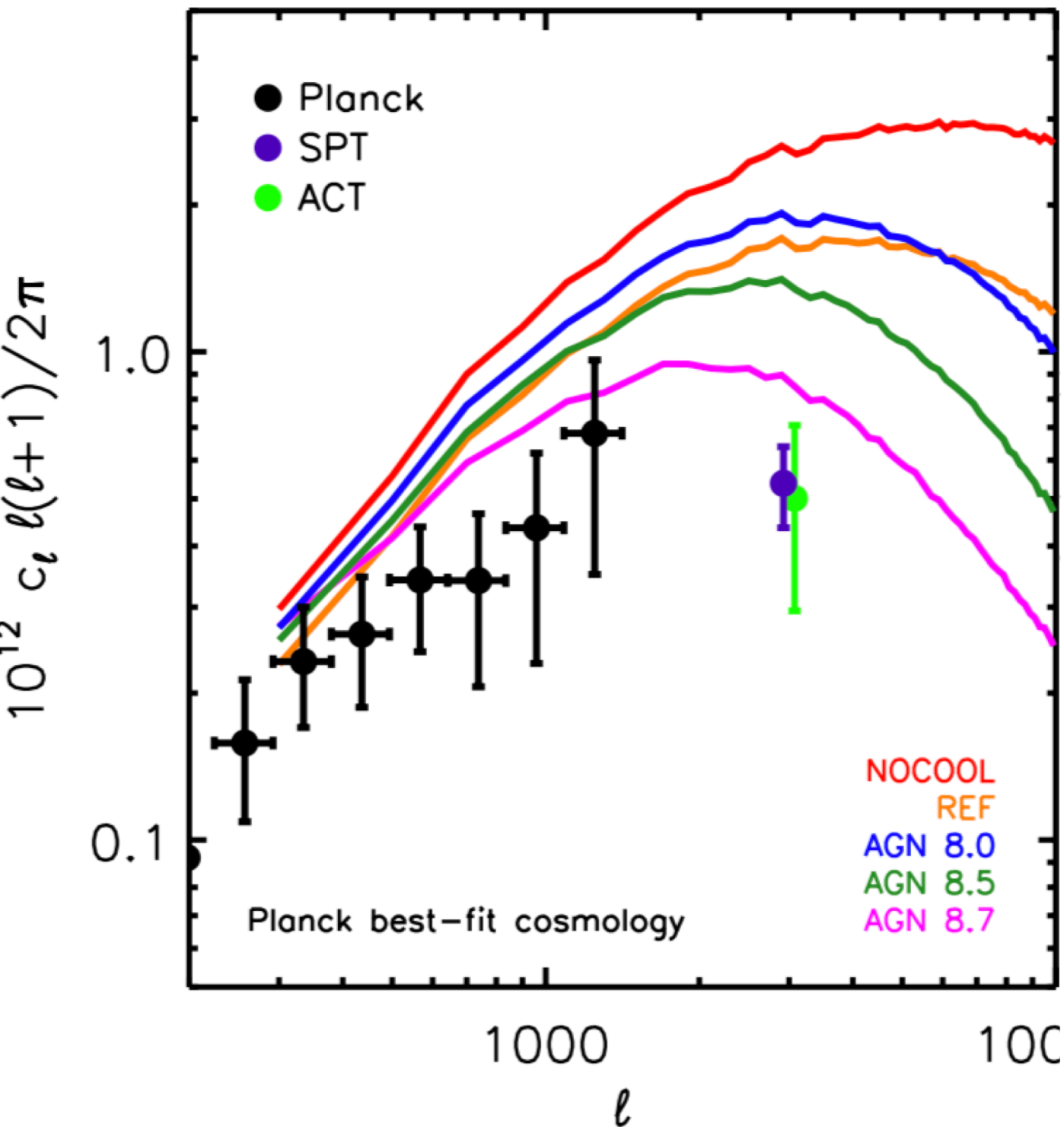
Abdulla et. al. 2018



# AGN feedback favors WMAP7 over Planck?

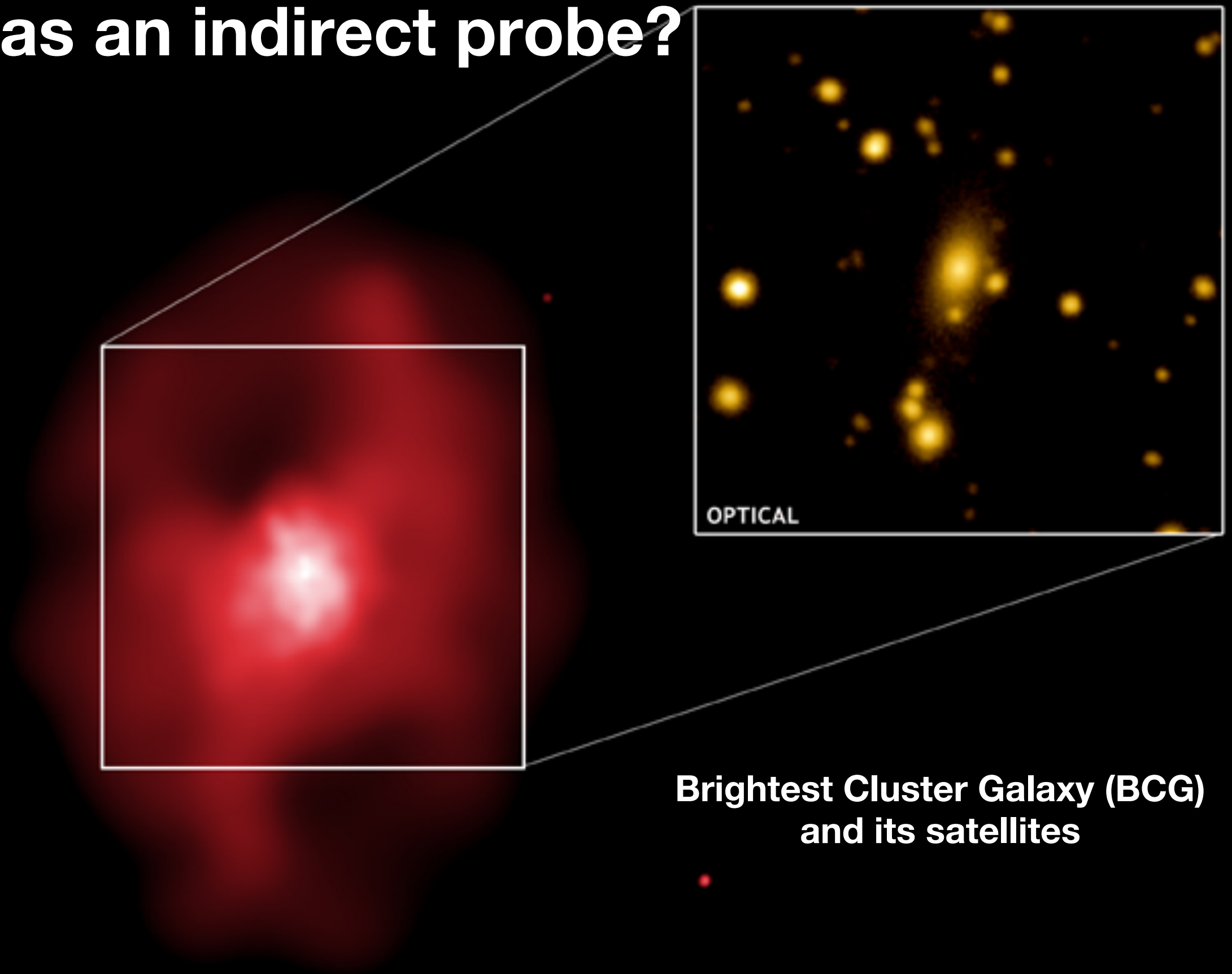
Nobody likes Planck ...

TSZ angular power spectra





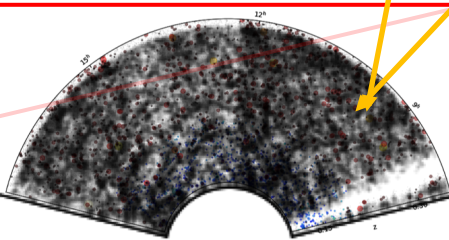
# Optical as an indirect probe?



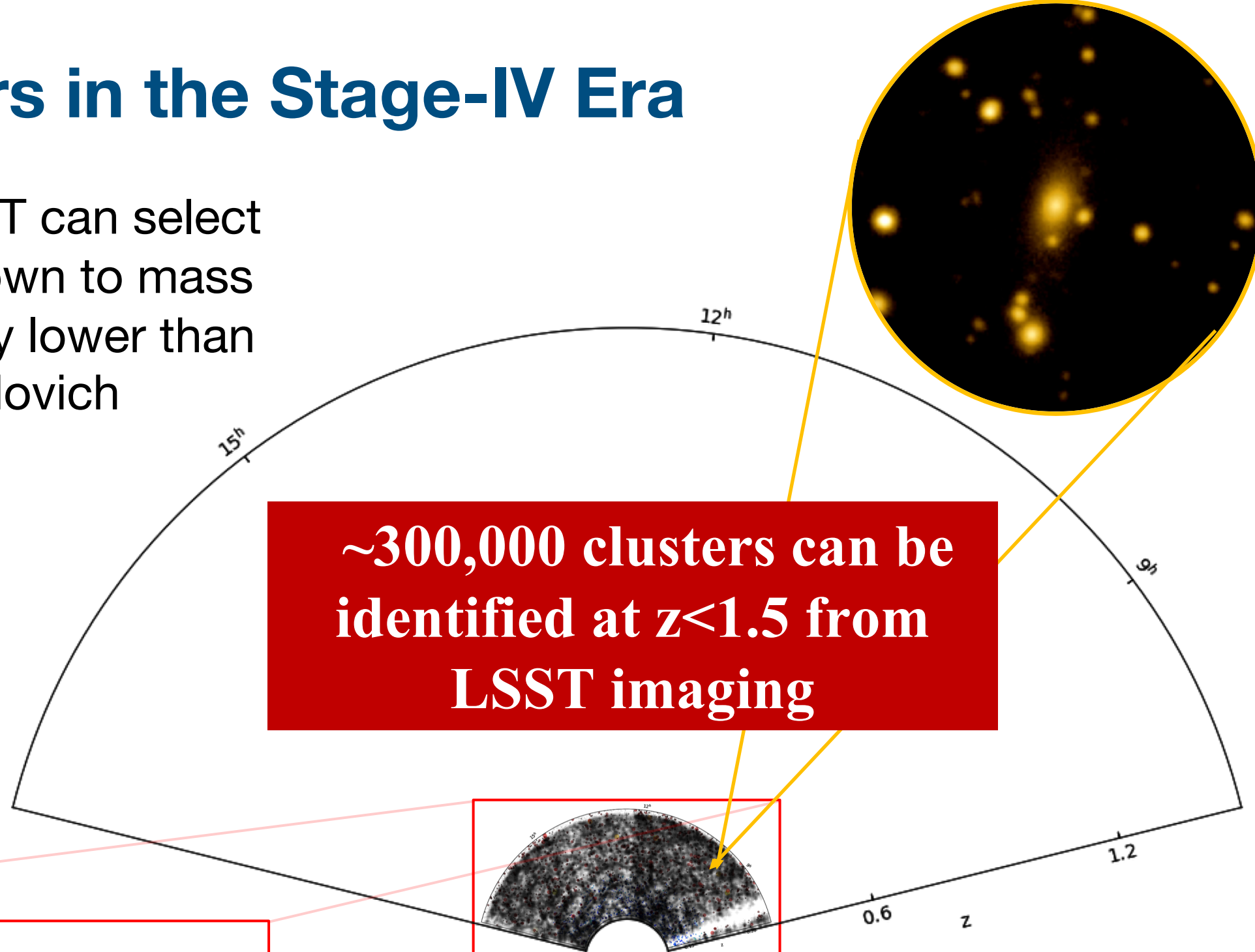
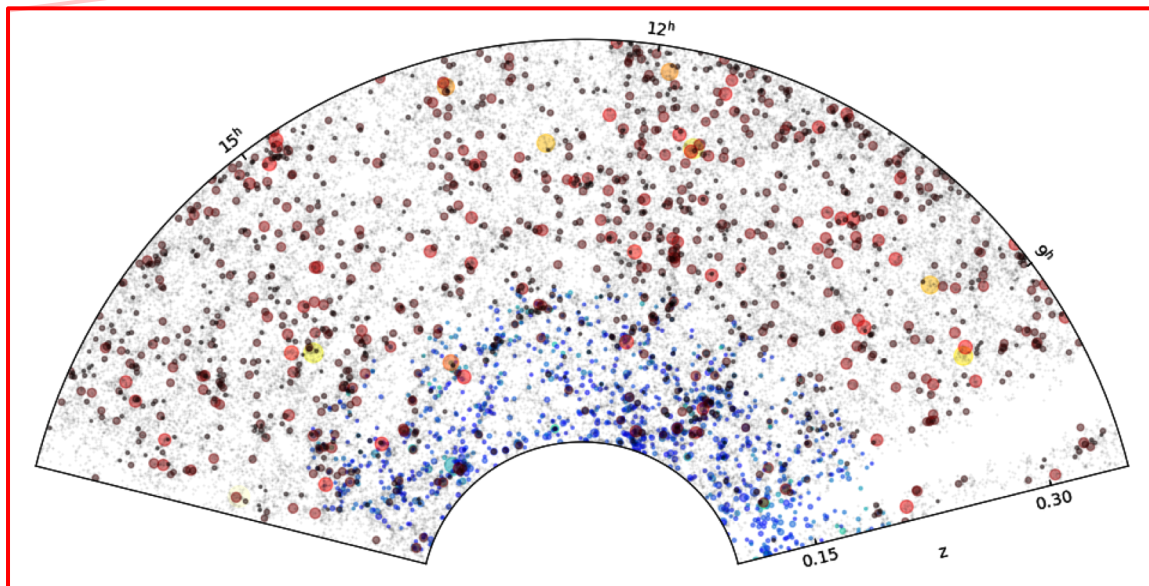
# Optical Clusters in the Stage-IV Era

Optical+NIR from LSST can select clusters ( $z \sim 0.5-1.5$ ) down to mass thresholds significantly lower than X-ray or Sunyaev-Zeldovich detection.

**$\sim 300,000$  clusters can be identified at  $z < 1.5$  from LSST imaging**

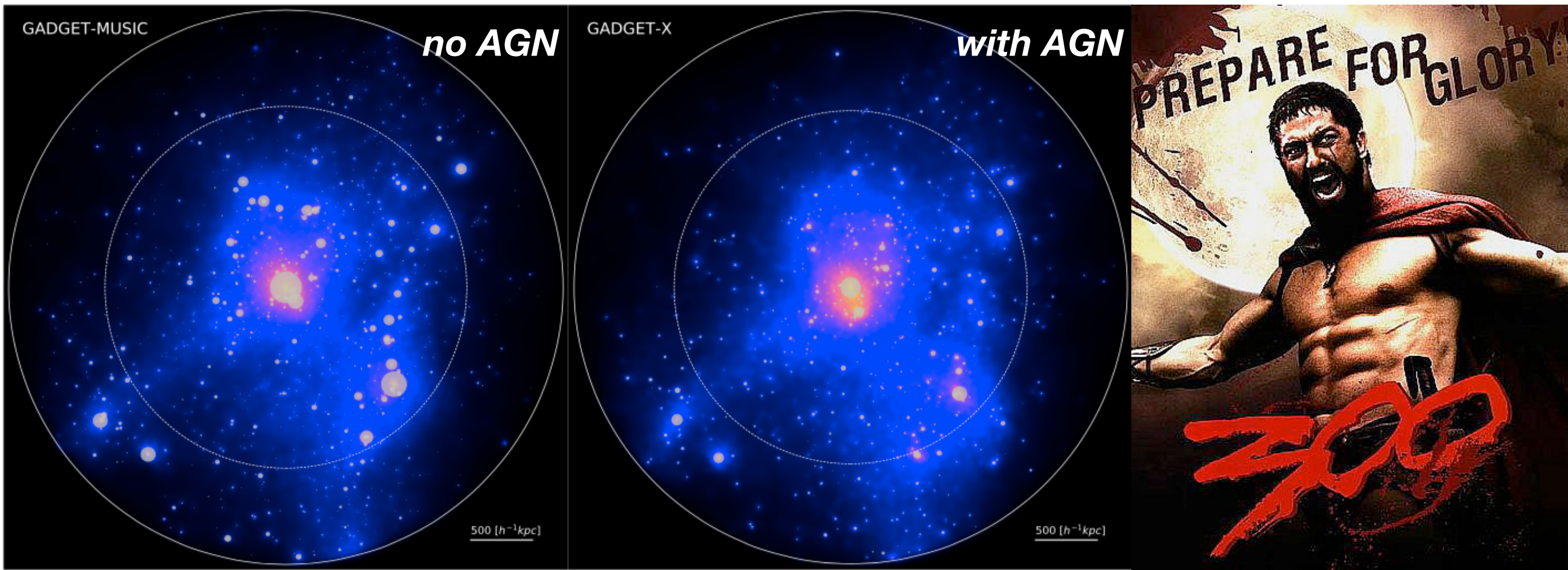


**SDSS redMaPPer:  
 $\sim 10,000$  clusters at  $z < 0.35$**



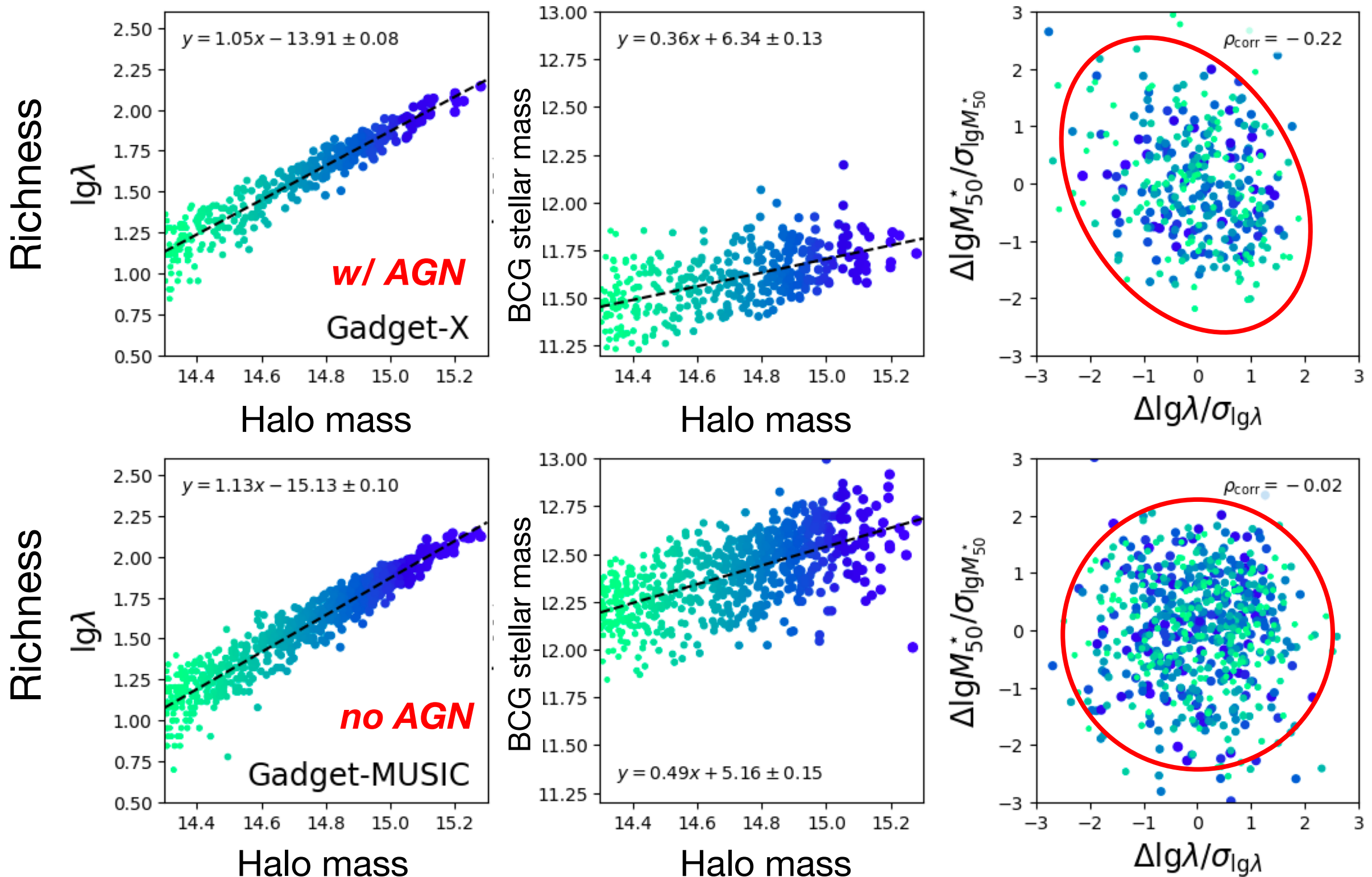


# The Three Hundred



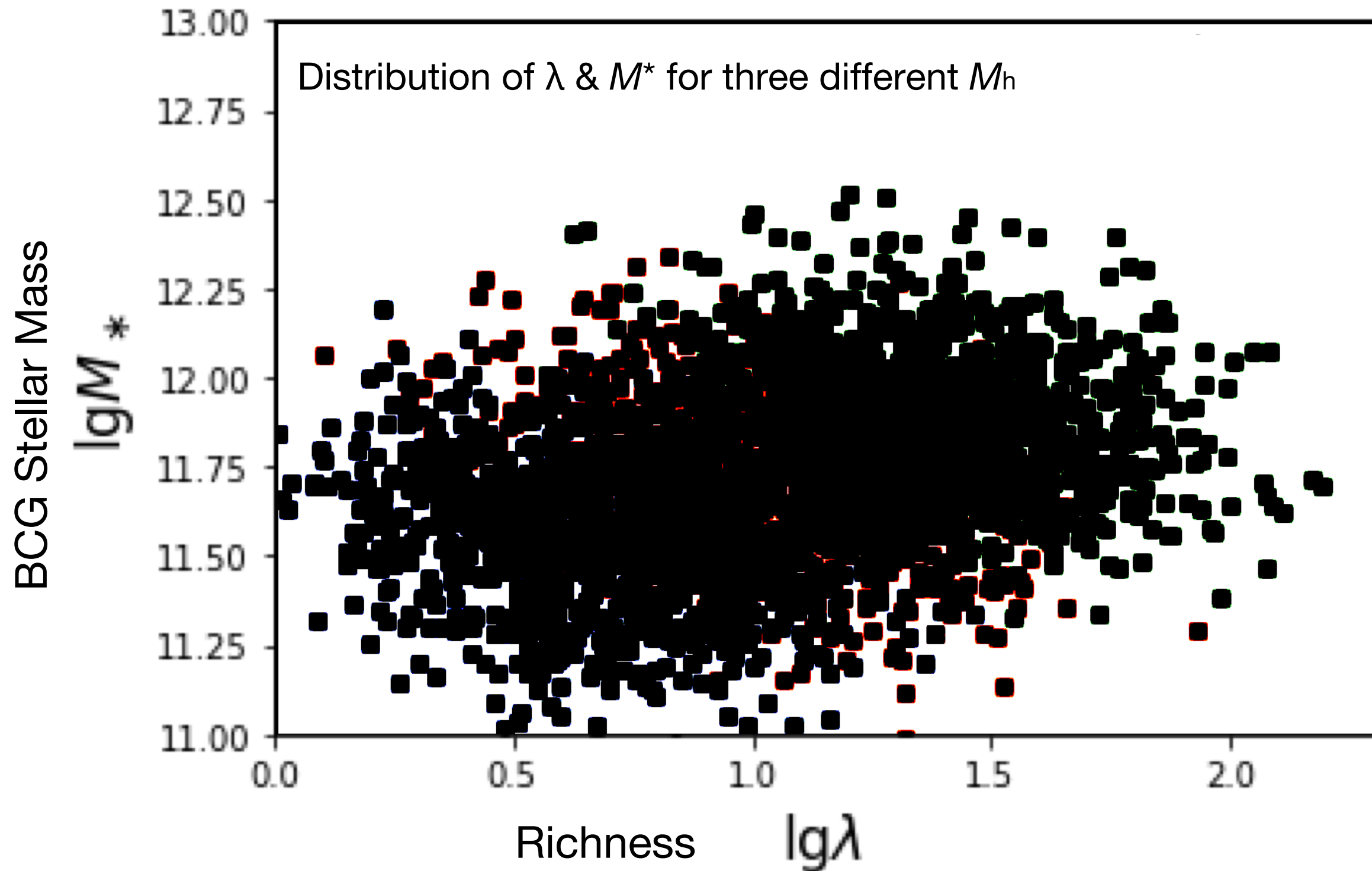
Zoom-in hydro-simulation of massive clusters selected from MPDL  
Same initial density field, with different galaxy formation recipes

The 300 predicts ***negative*** correlation btw satellite richness and BCG stellar mass **at fixed halo mass**

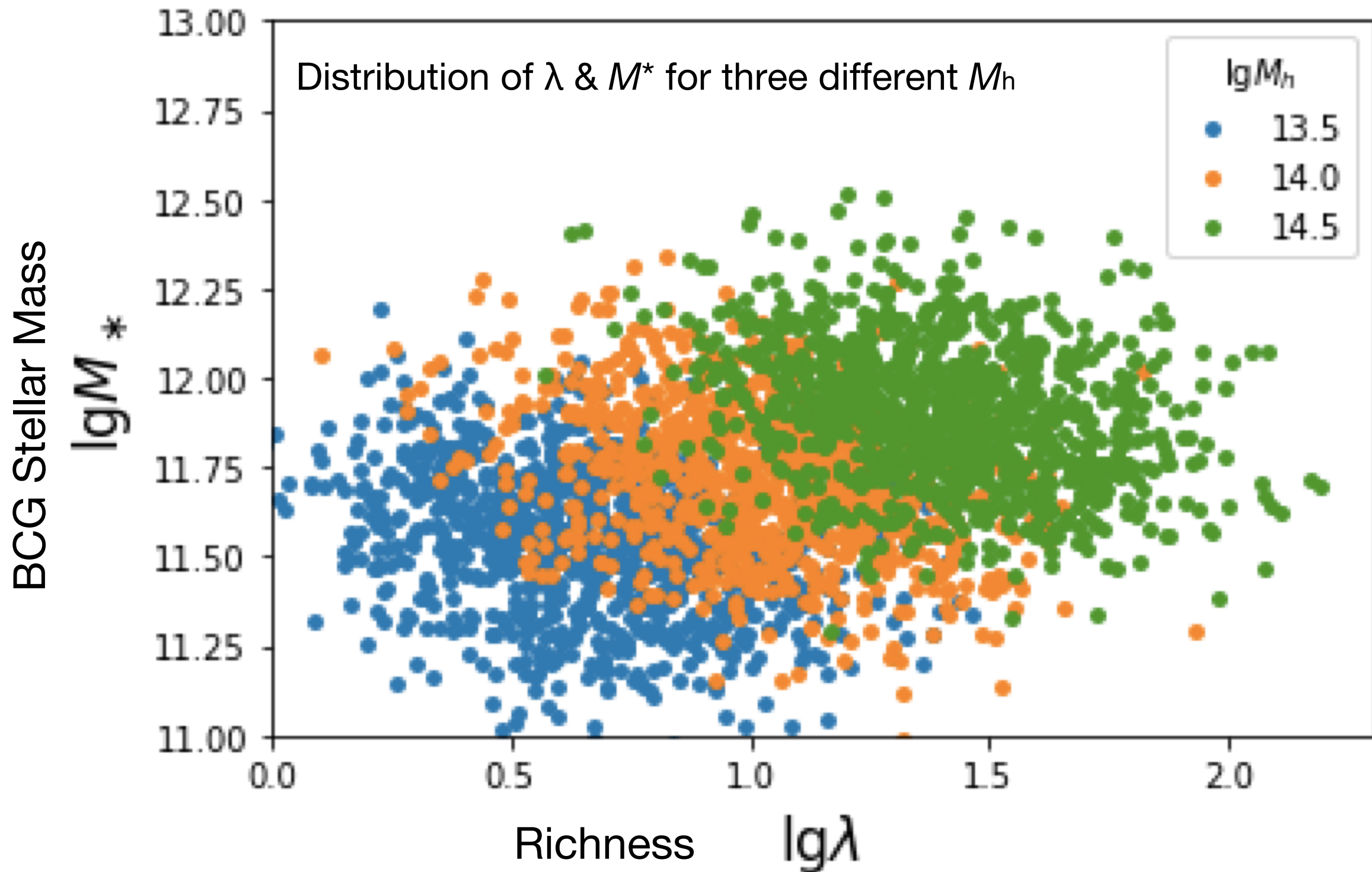




# Observed BCG mass – satellite richness correlation



# With negative correlation at fixed halo mass

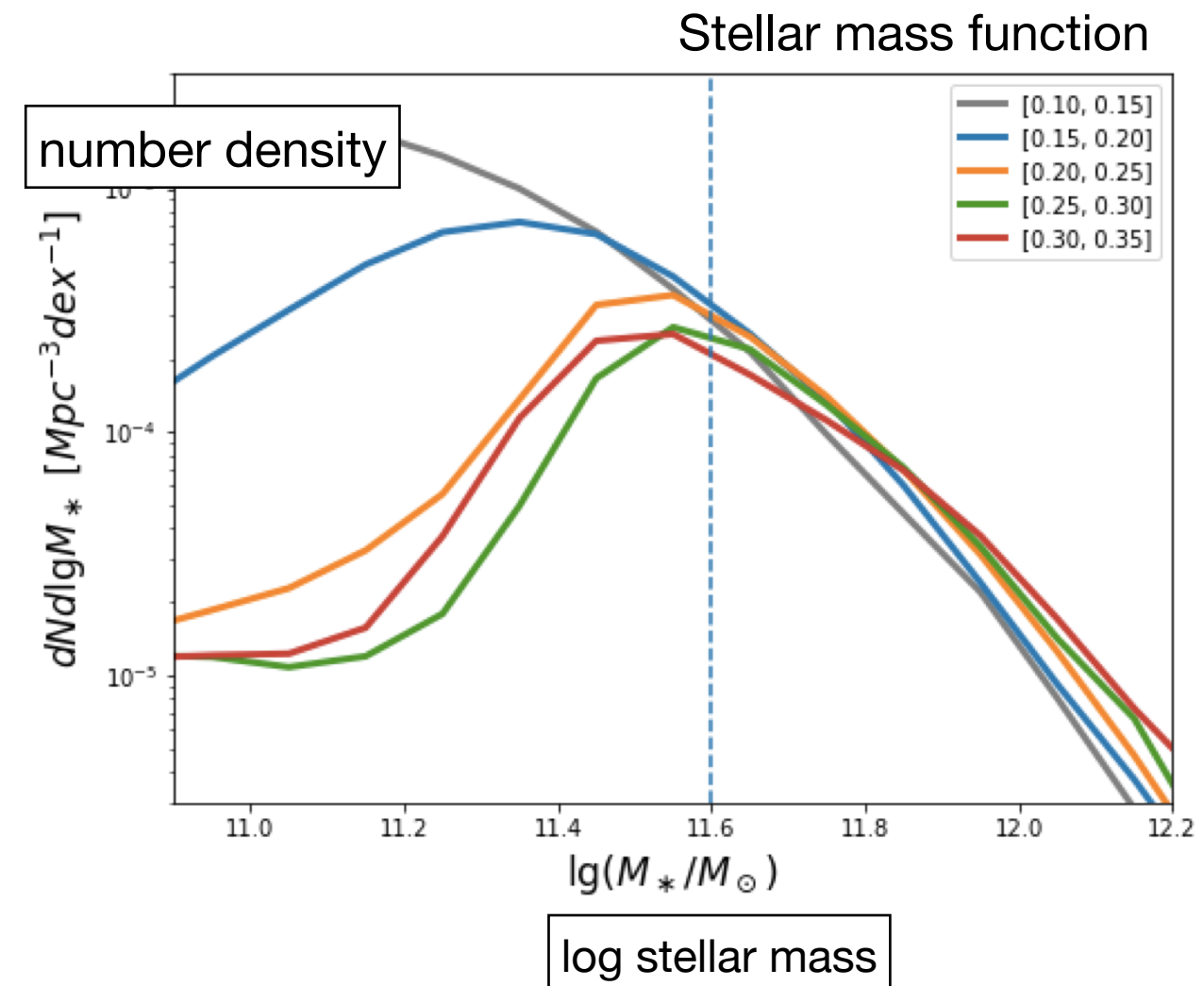
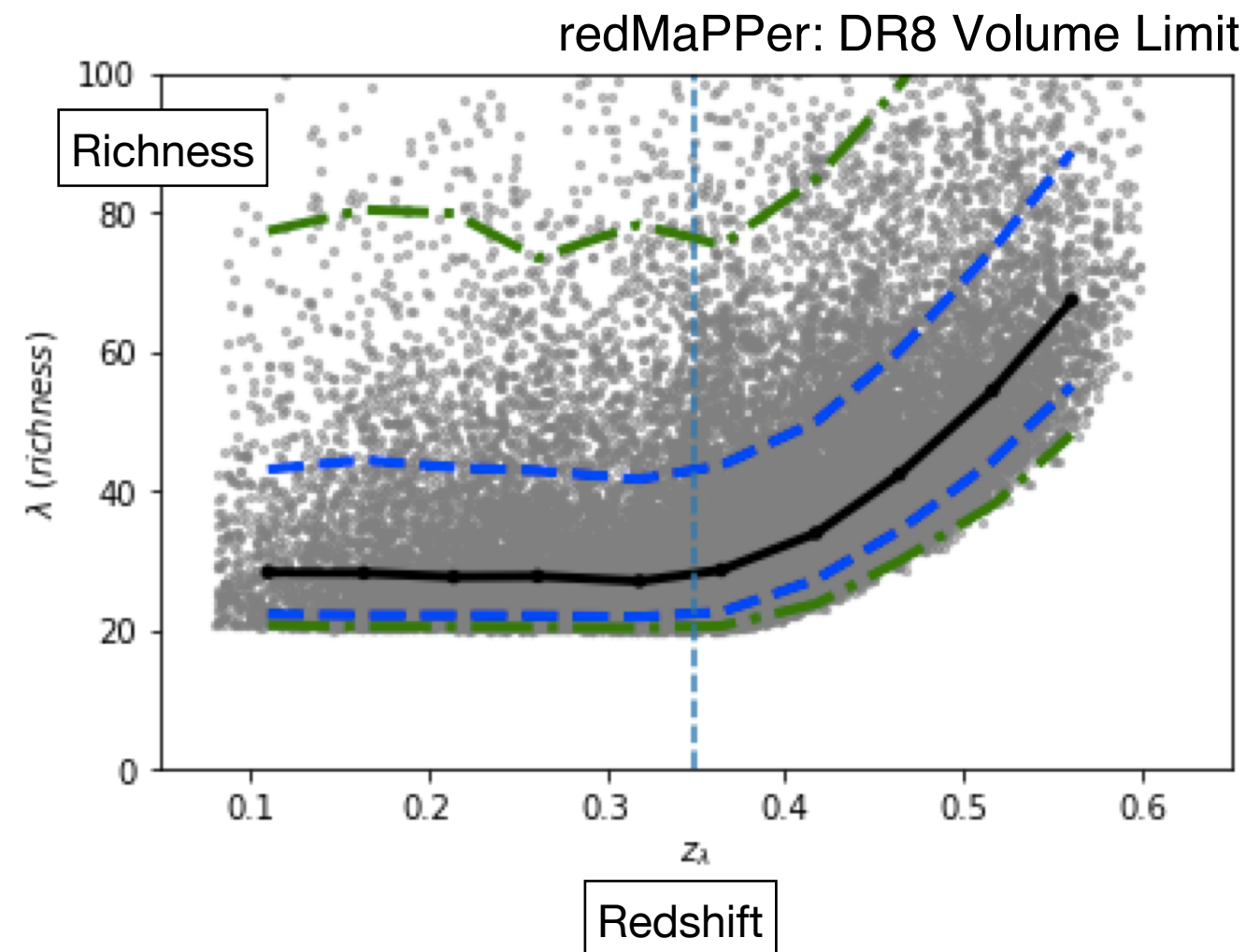
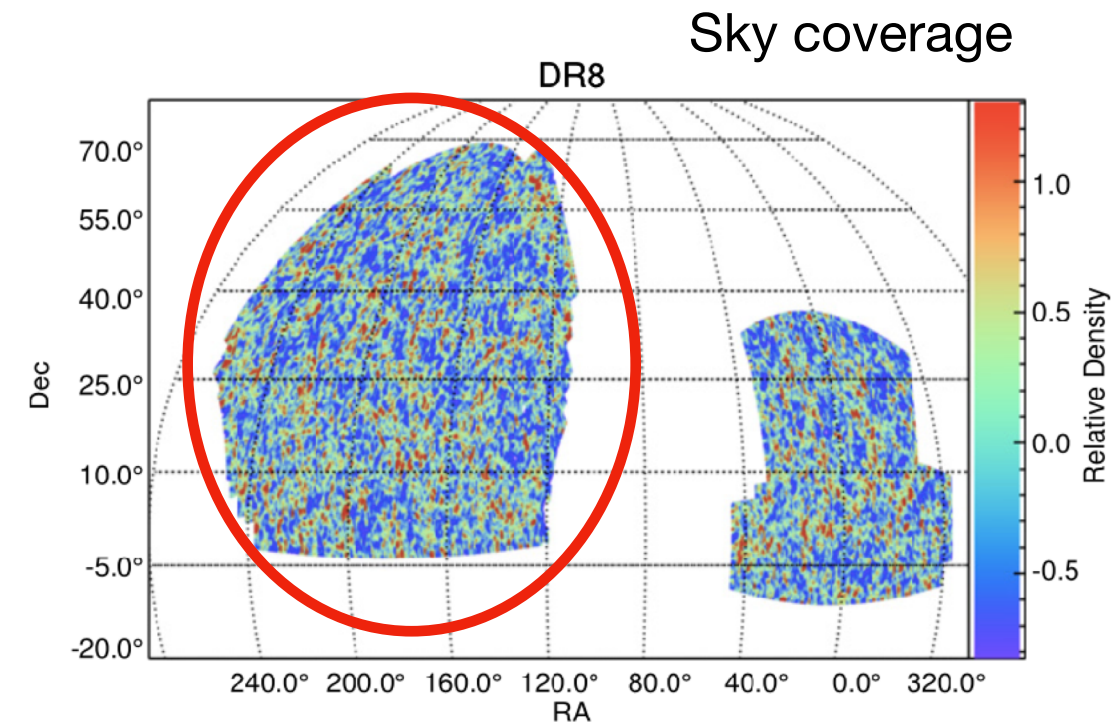


**Strong constraint on cluster formation physics!**

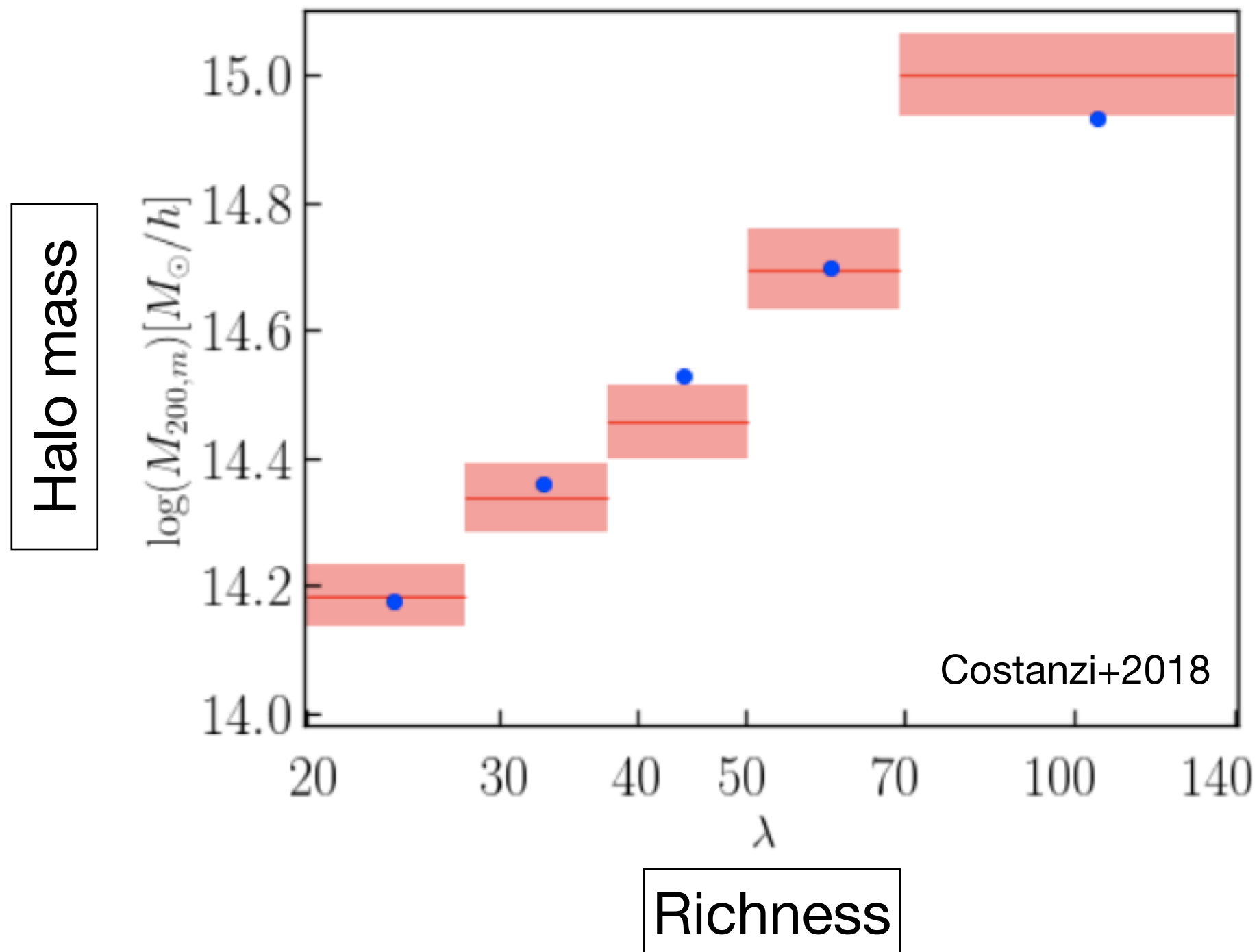


# redMaPPer cluster catalog

- redMaPPer (Rykoff+ 2014, SDSS *DR8*)  
red-sequence filter on photometric data
- BCG stellar mass (Chen+ 2012, SDSS/BOSS *DR12*)
- $0.17 < z < 0.35$ ,  $\lambda \geq 20$  ( $N=6412$ , North Cap)
- $\log_{10} M^*/M_{\odot} \geq 11.6$  ( $N=4590$ )



# Weak Lensing (WL) cluster masses



# Model

- Halo mass function (fixed for now, marginalize over cosmology in the future)
- **2D Gaussian** distribution for **(log λ, log M\*)** at fixed halo mass

halo mass-richness relation

$$\begin{aligned} \langle \lg \lambda \rangle &= \lg[\lambda_0 (M / M_0)^{\alpha_\lambda}] \\ \sigma(\lg \lambda) &= \begin{cases} \sigma_{\lg \lambda} & \text{for } M \leq M_0 \\ \sigma_{\lg \lambda} + \beta_\lambda \lg(M / M_0) & \text{for } M > M_0 \end{cases} \end{aligned}$$

power law

varying scatter

stellar-to-halo mass relation

$$\begin{aligned} \langle \lg m^* \rangle &= \lg[m_0^* (M / M_0)^{\alpha_*}] \\ \sigma(\lg m^*) &= \begin{cases} \sigma_{\lg m^*} & \text{for } M \leq M_0 \\ \sigma_{\lg m^*} + \beta_* \lg(M / M_0) & \text{for } M > M_0 \end{cases} \end{aligned}$$

$\rho_{corr}$  : correlation btw λ and M\*

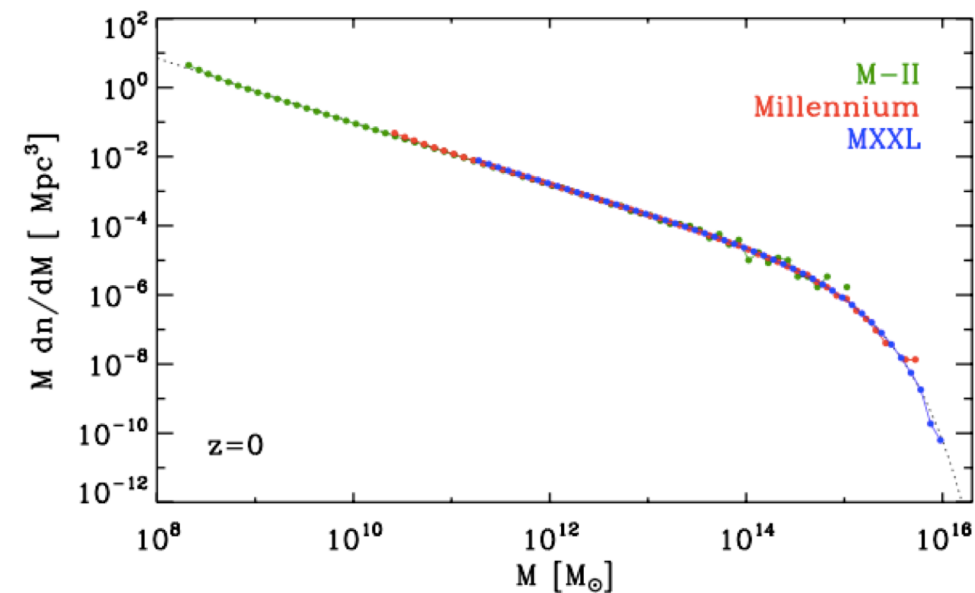
$$\begin{aligned} \langle \lg m^* \rangle|_{\lg \lambda} &= \langle \lg m^* \rangle + \rho_{corr} \frac{\sigma(\lg m^*)}{\sigma(\lg \lambda)} [\lg \lambda - \langle \lg \lambda \rangle] \\ \sigma(\lg m^*)|_{\lg \lambda} &= \sigma(\lg m^*) \times \sqrt{1 - \rho_{corr}^2} \end{aligned}$$



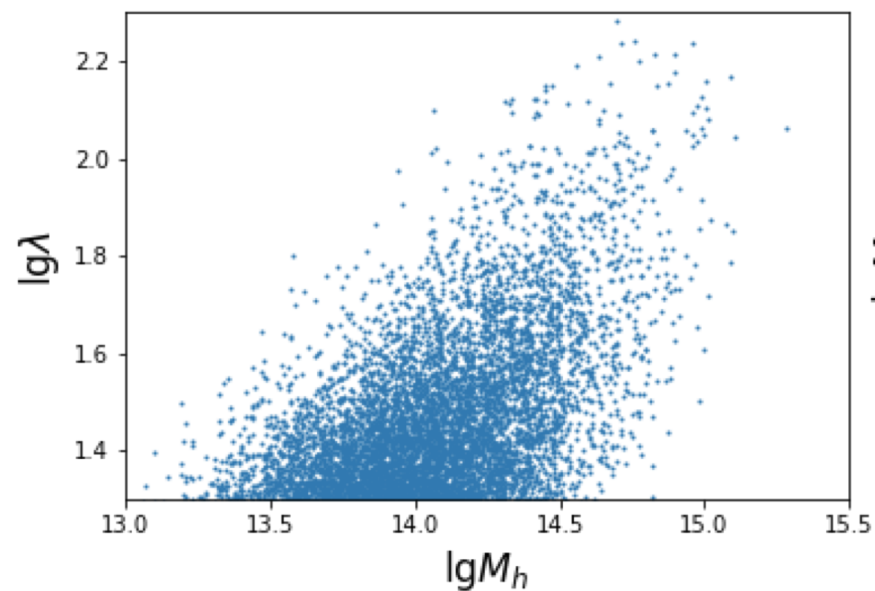
# Mock sample for method validation

- Generate  $M_h$  from halo mass function, assign  $\lambda$ ,  $M^*$  according to  $p(\lambda \mid M_h)$ ,  $p(M^* \mid M_h, \lambda)$
- Apply same sample selection

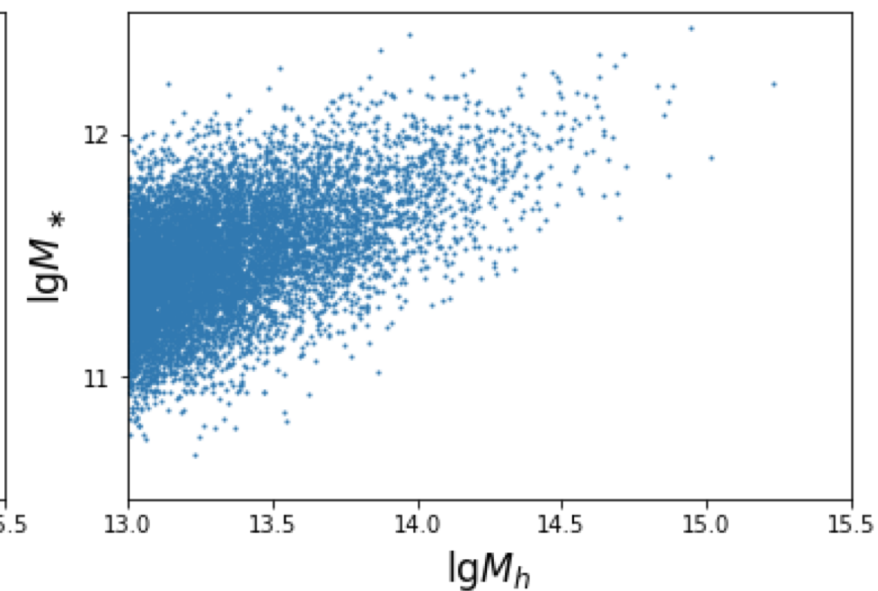
**Halo Mass Function**



**$\lambda \mid M_h$**



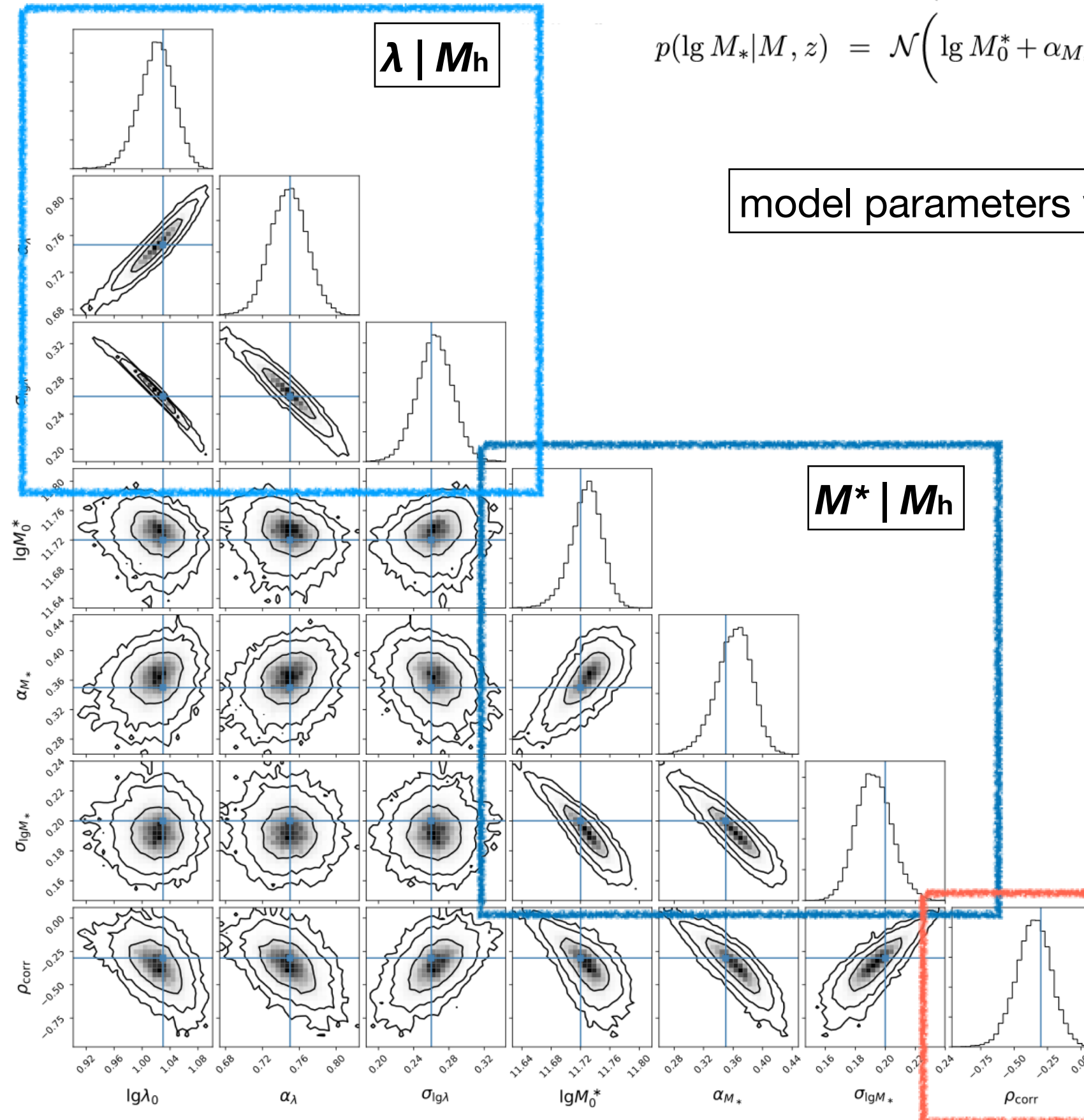
**$M^* \mid M_h$**



# Mock sample results

$$p(\lg \lambda | M, z) = \mathcal{N}\left(\lg \lambda_0 + \alpha_\lambda \lg \frac{M_h}{10^{14} h^{-1} M_\odot}, \sigma_{\lg \lambda}^2\right)$$

$$p(\lg M_* | M, z) = \mathcal{N}\left(\lg M_0^* + \alpha_{M_*} \lg \frac{M_h}{10^{14} h^{-1} M_\odot}, \sigma_{\lg M_*}^2\right)$$



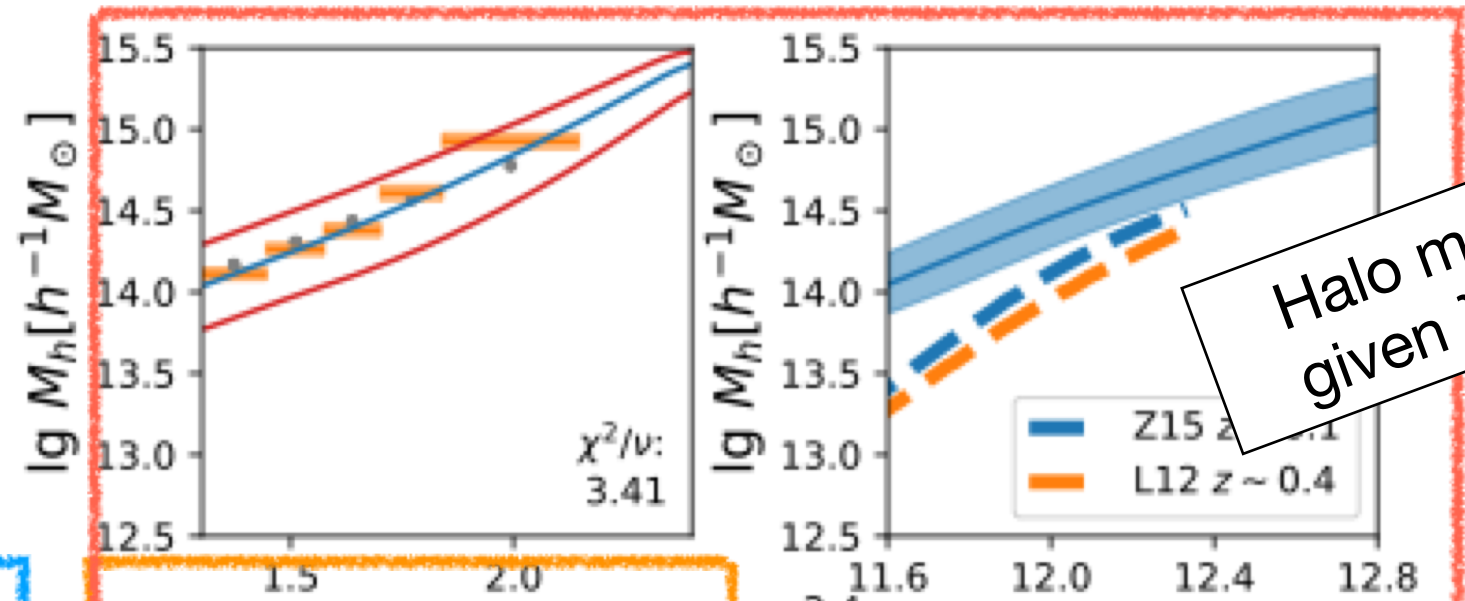
model parameters well recovered

Correlation  
Between  $\lambda$ ,  $M^*$

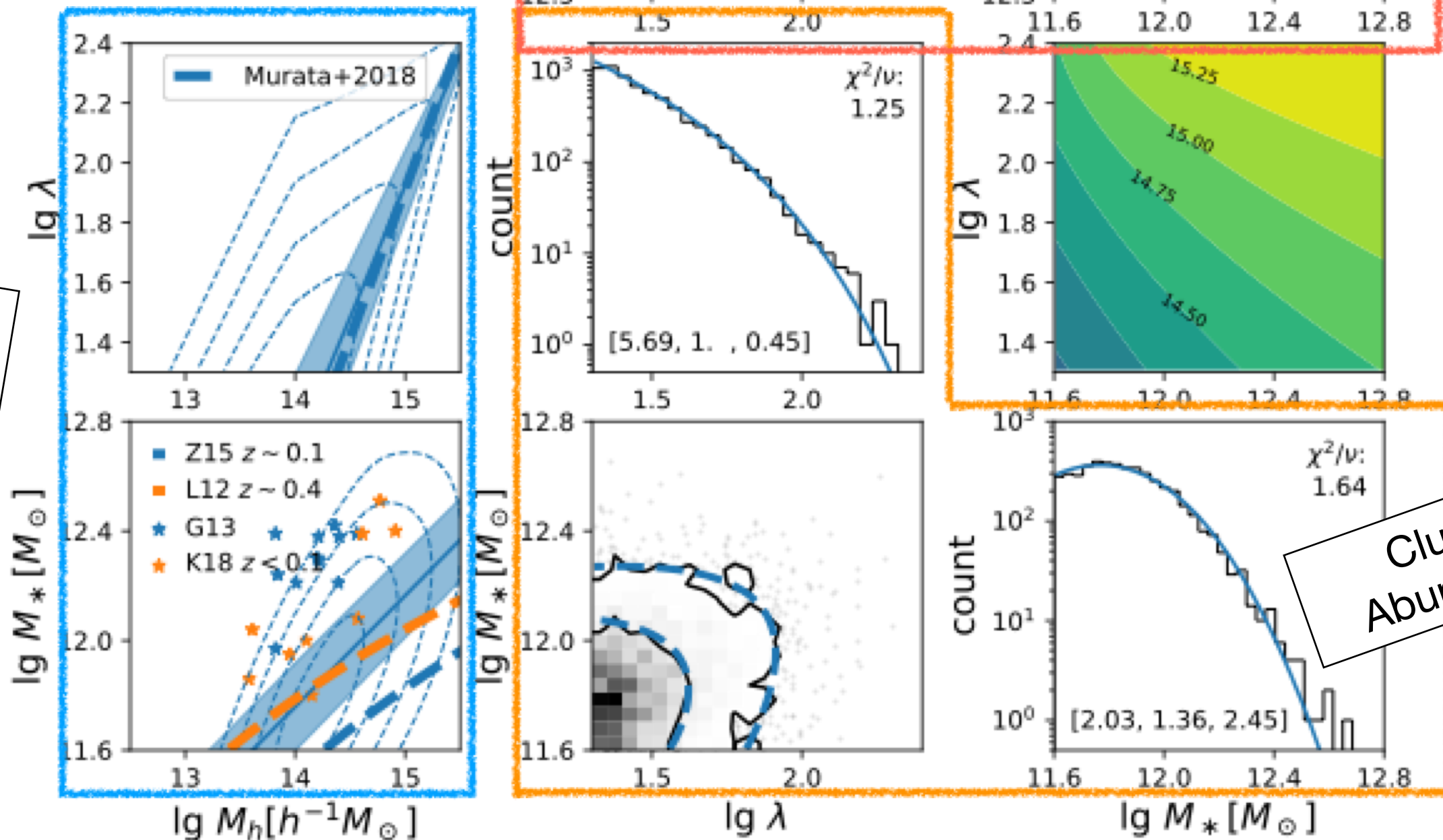


# data vs. best-fit model prediction at fixed $\rho_{corr}$

$\lg \lambda_0$ : 1.05  
 $\alpha_\lambda$ : 0.88  
 $\sigma_{\lg \lambda}$ : 0.25  
 $\beta_{\lg \lambda}$ : -0.13  
 $\lg M_0^*$ : 11.76  
 $\alpha_{M_*}$ : 0.41  
 $\sigma_{\lg M_*}$ : 0.16  
 $\beta_{\lg M_*}$ : -0.01  
 $\ln L$ : 8119417.98



Halo mass at given  $\lambda$  or  $M^*$

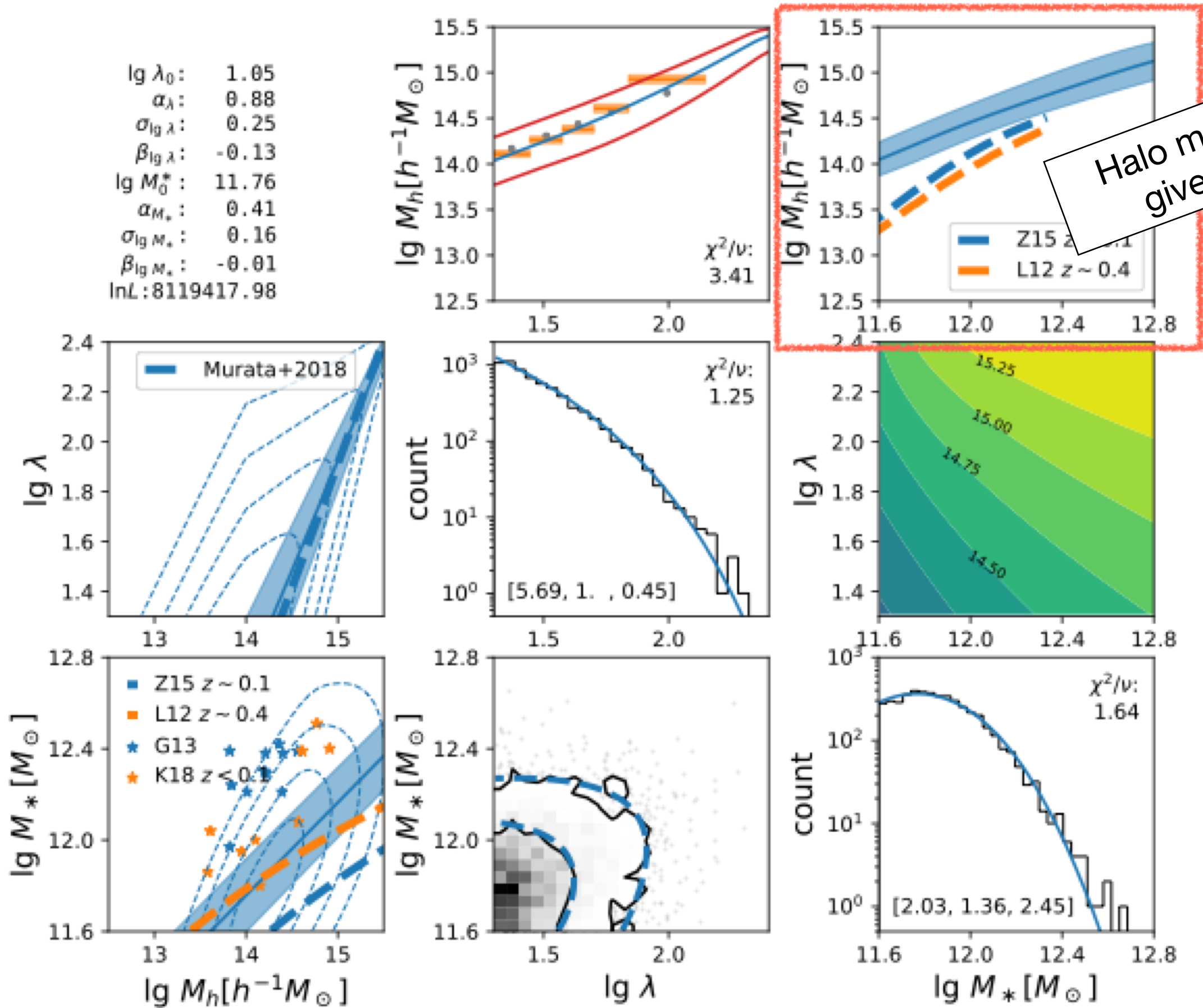


Mass-richness relation

Stellar-to-halo mass relation

Cluster Abundance

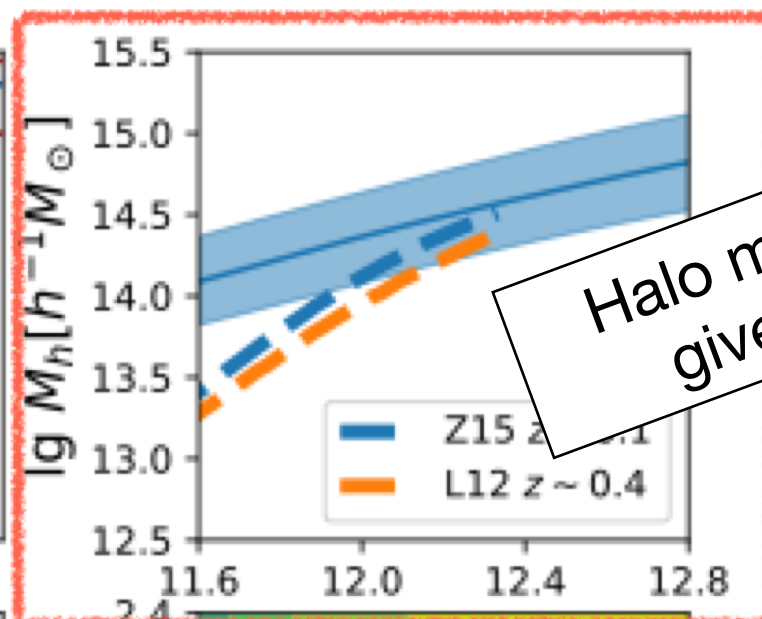
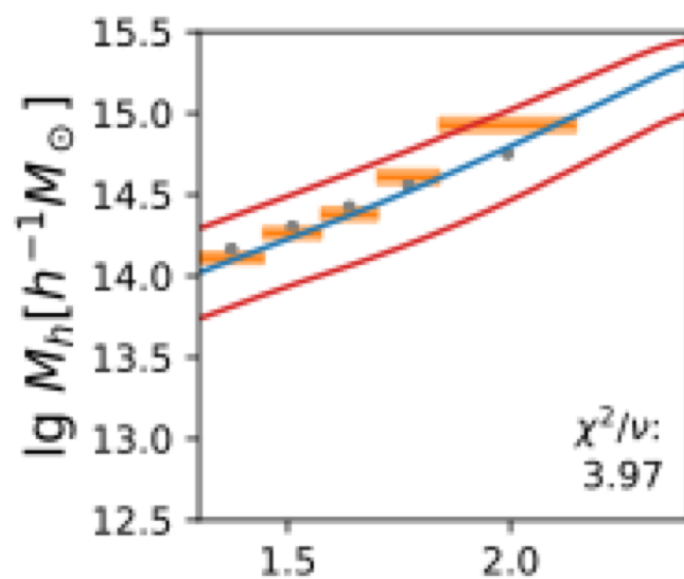
$$\rho_{corr} = -0.5$$



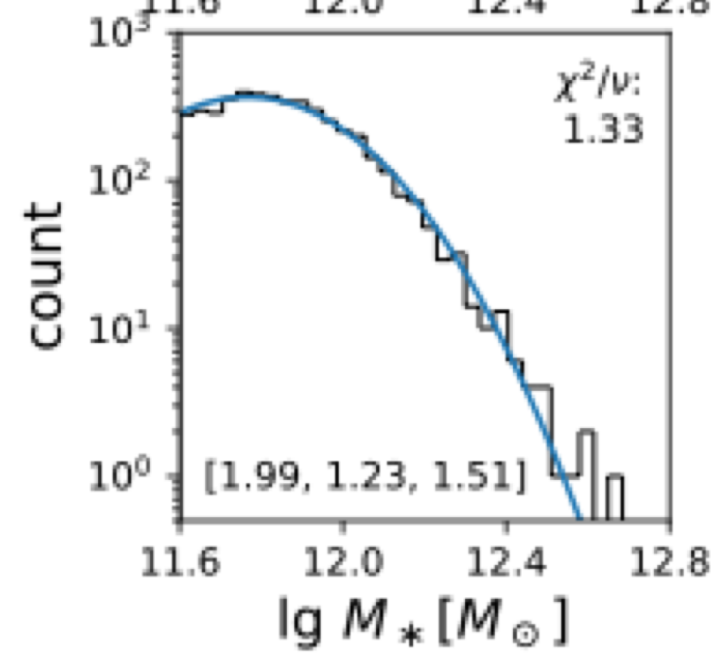
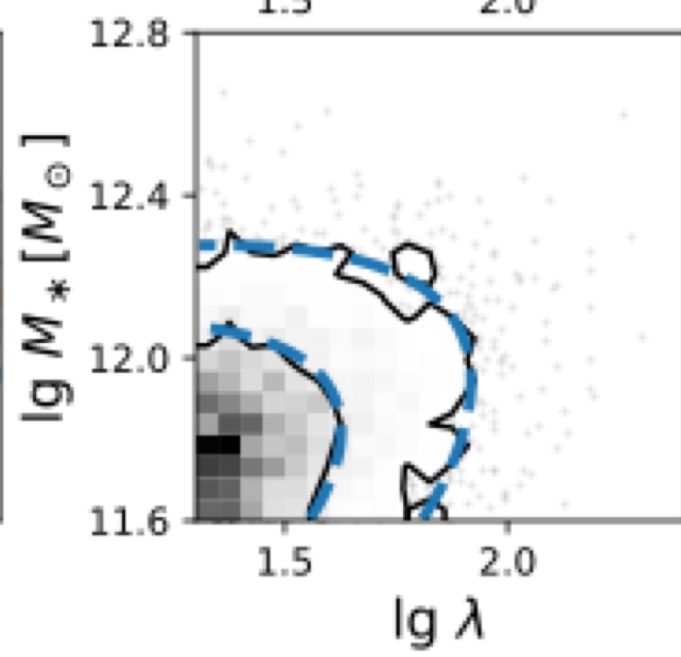
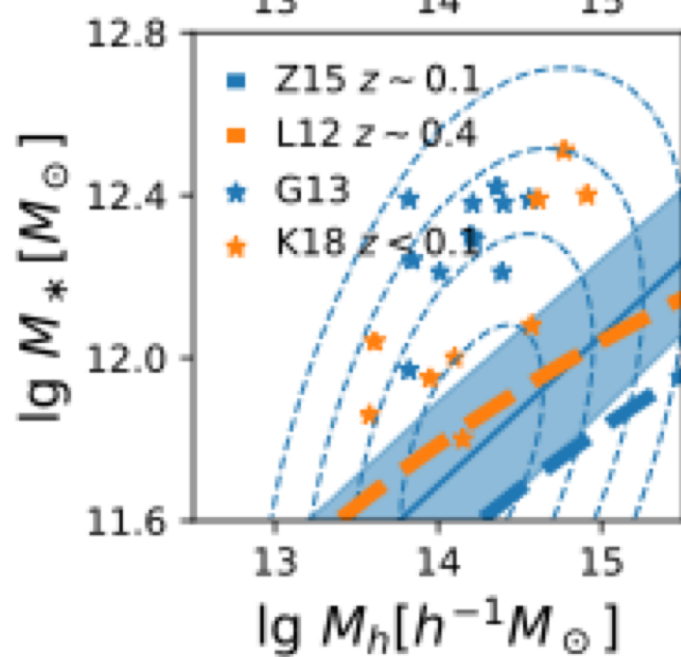
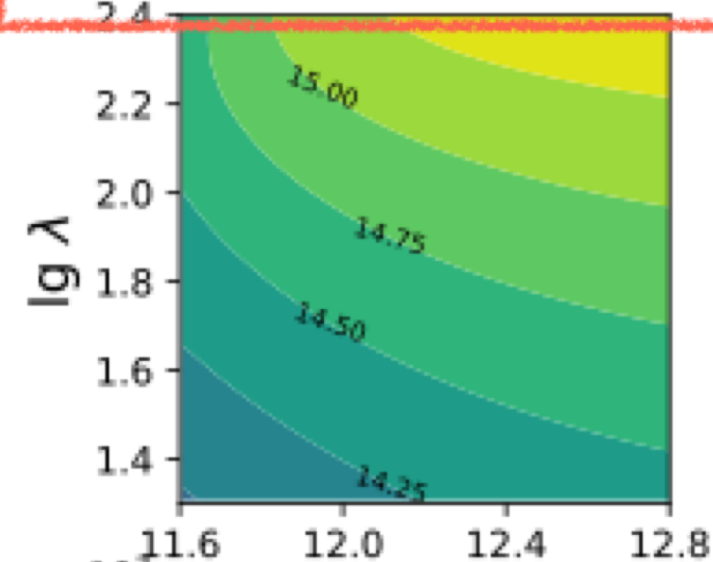
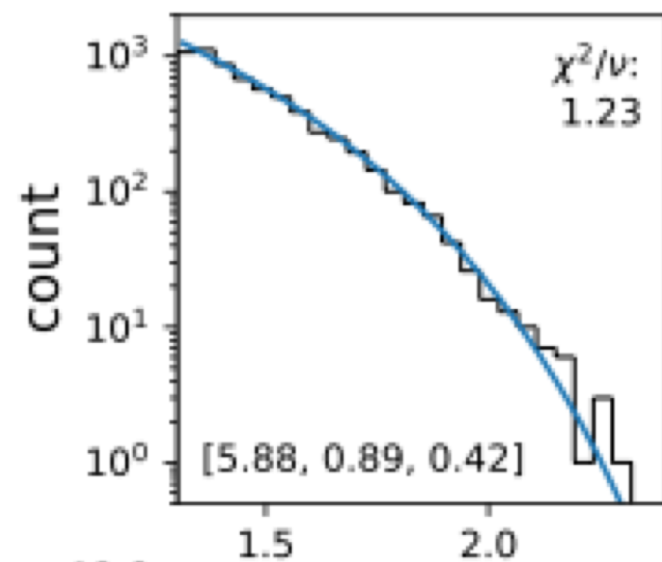
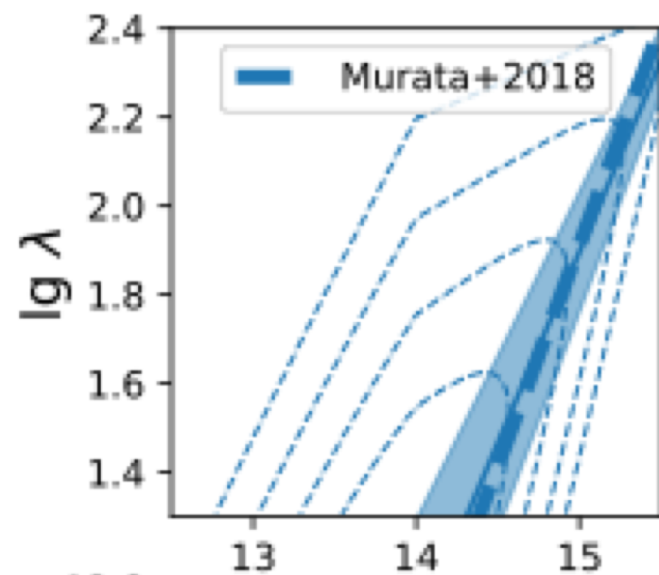


$$\rho_{corr} = 0$$

$\lg \lambda_0$ : 1.04  
 $\alpha_\lambda$ : 0.86  
 $\sigma_{\lg \lambda}$ : 0.26  
 $\beta_{\lg \lambda}$ : -0.12  
 $\lg M_0^*$ : 11.69  
 $\alpha_{M_*}$ : 0.37  
 $\sigma_{\lg M_*}$ : 0.21  
 $\beta_{\lg M_*}$ : -0.02  
 $\ln L$ : 8119420.66

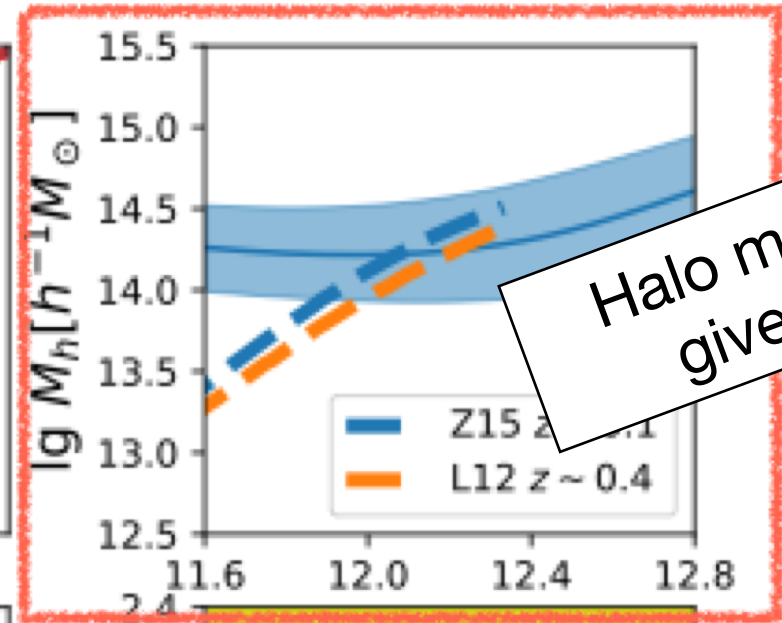
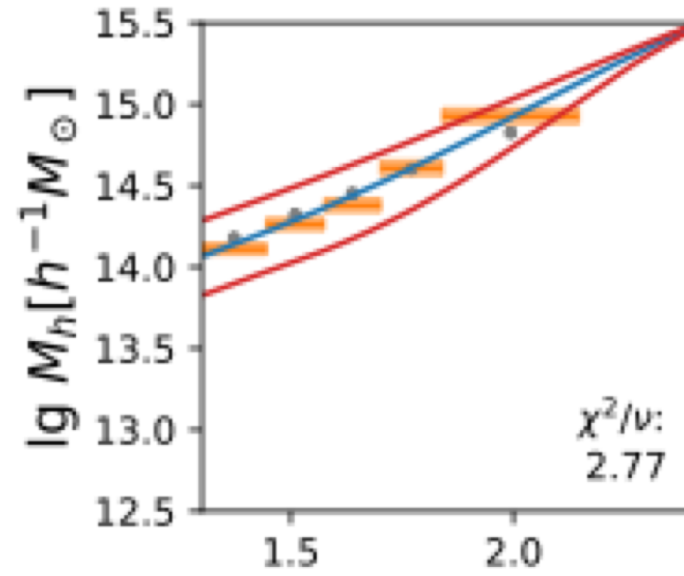


Halo mass at given  $M^*$

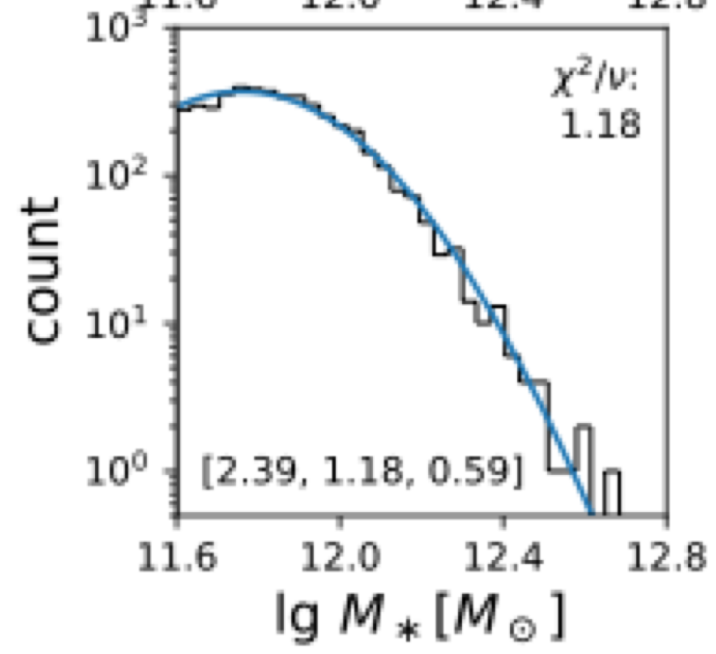
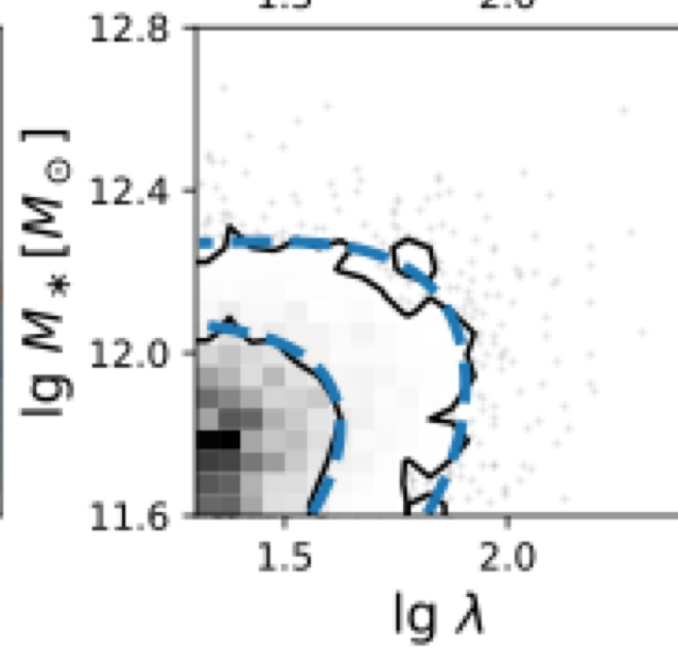
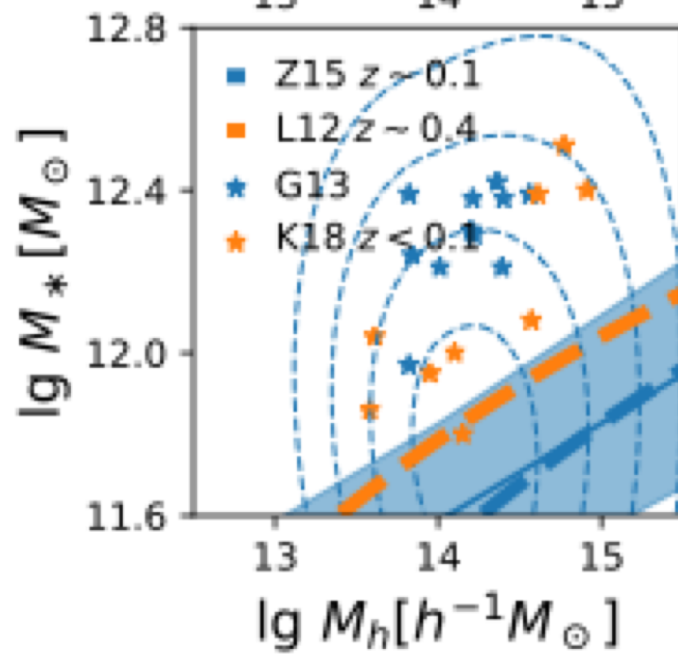
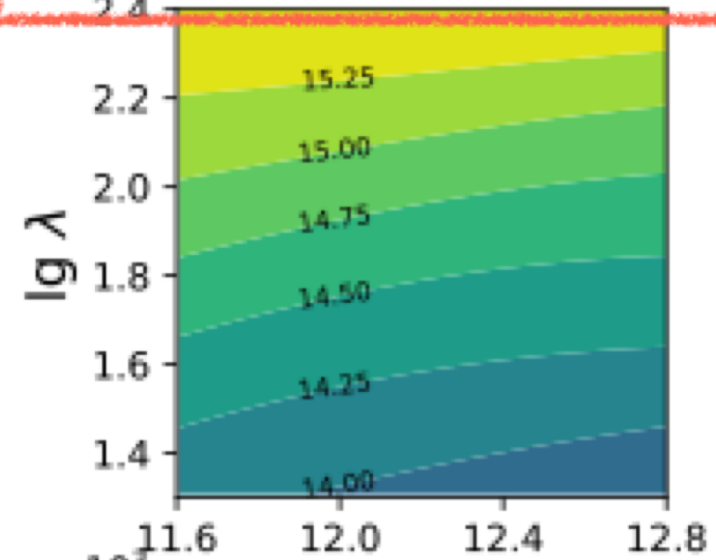
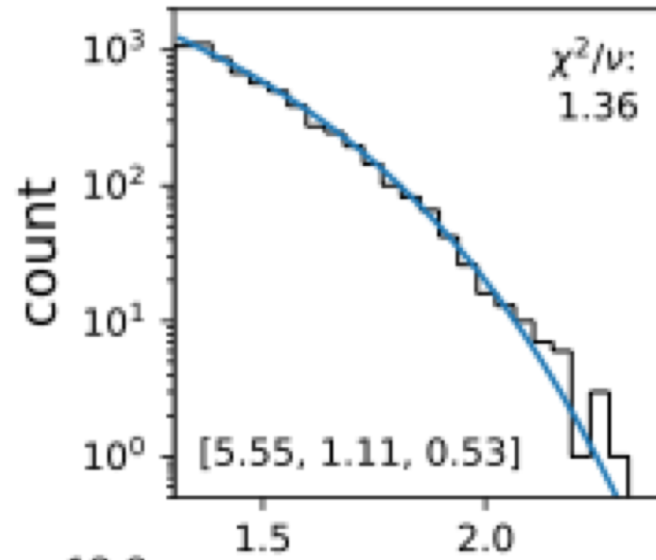
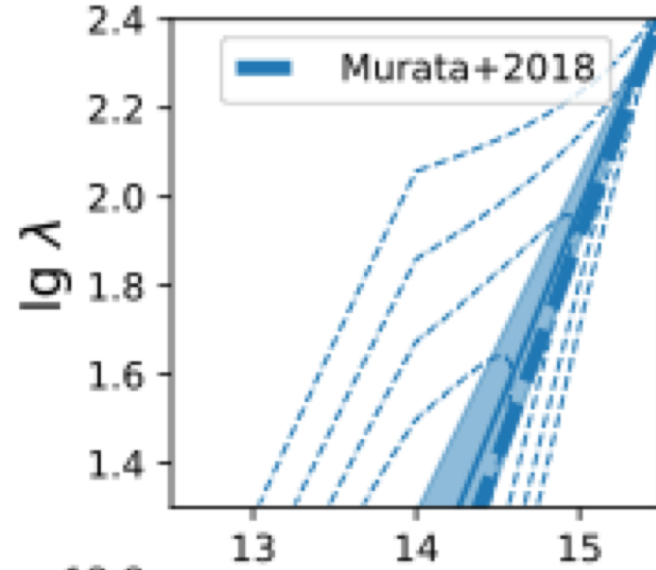


$$\rho_{corr} = +0.5$$

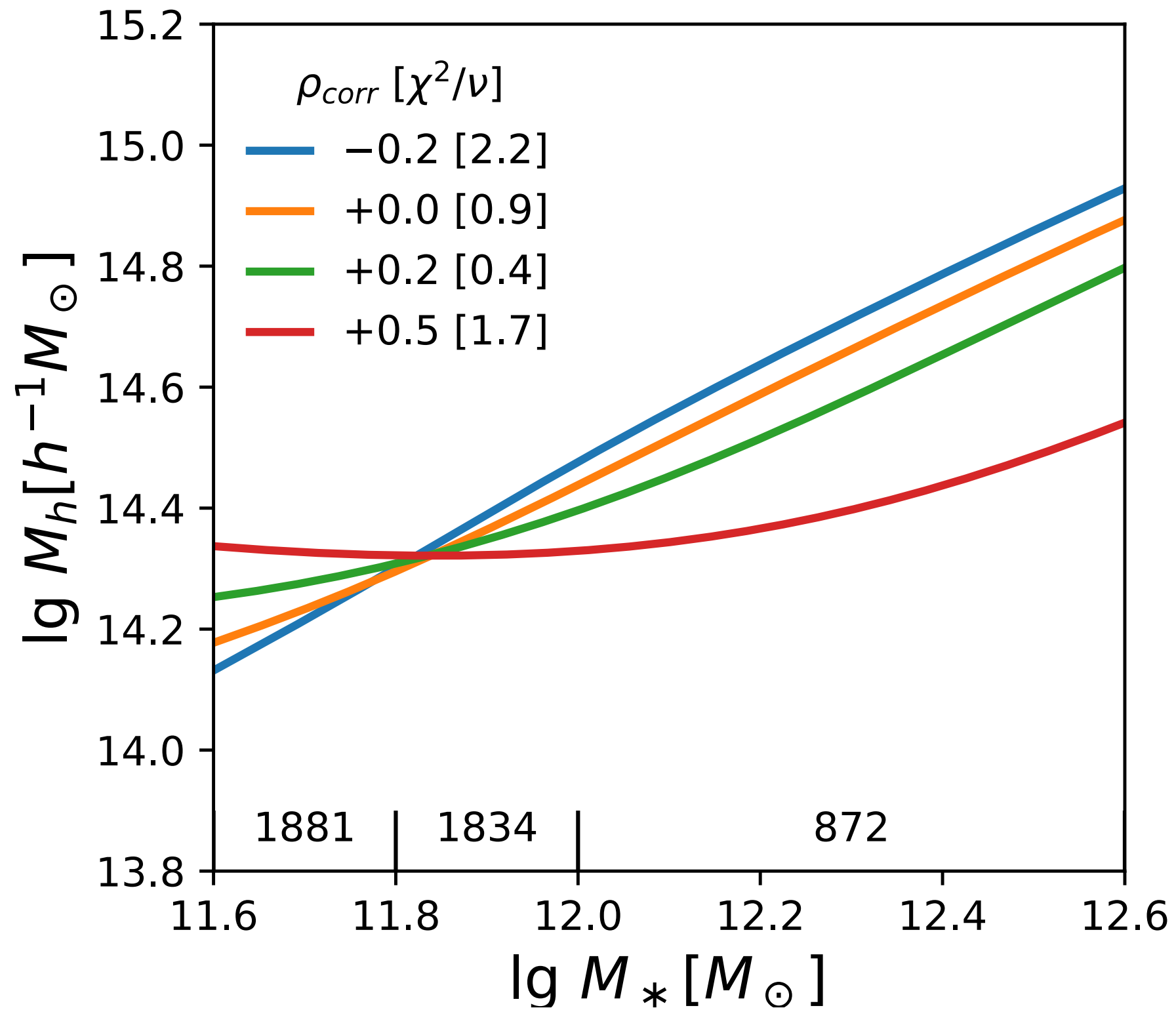
$\lg \lambda_0$ : 1.07  
 $\alpha_\lambda$ : 0.91  
 $\sigma_{\lg \lambda}$ : 0.22  
 $\beta_{\lg \lambda}$ : -0.15  
 $\lg M_0^*$ : 11.59  
 $\alpha_{M_*}$ : 0.24  
 $\sigma_{\lg M_*}$ : 0.24  
 $\beta_{\lg M_*}$ : 0.03  
 $\ln L$ : 8119428.27



Halo mass at given  $M^*$

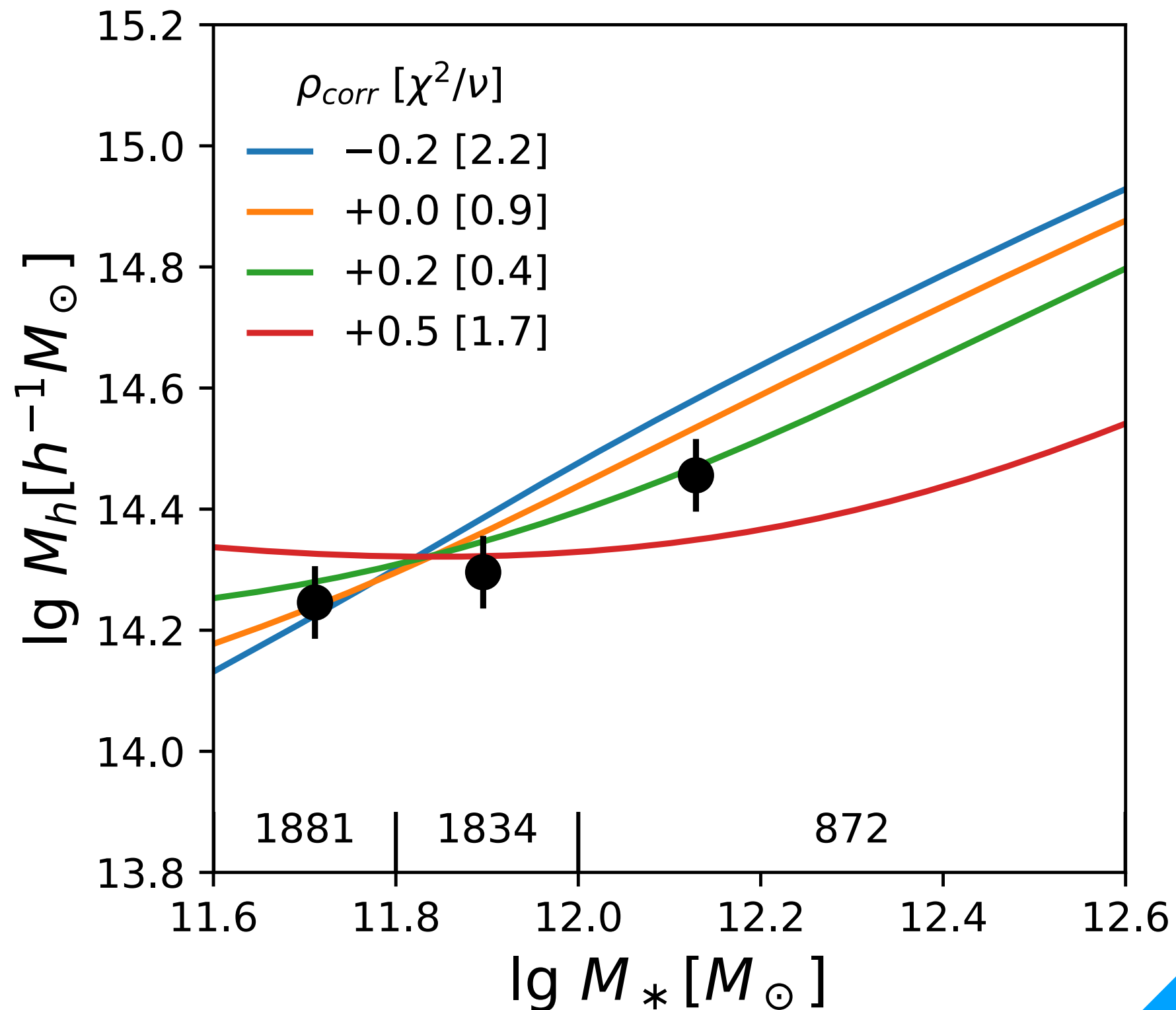


# WL halo mass at fixed BCG stellar mass can pin down $\rho_{\text{corr}}$





Well, WL tells us  $\rho_{\text{corr}}$  is close to +0.2



Preliminary!

# Possible boring explanations

- **We probably need to marginalize over cosmology**
- AGN feedback inhibits BCG growth, no doubt
- AGN feedback quenches star formation in satellites, making satellites (a) redder and (b) lighter
  - ✓ If (a)  $\rightarrow$  BCG mass and richness are negatively correlated.
  - ✓ If (b)  $\rightarrow$  BCG mass and richness are positively correlated.
- We probably need to run cluster finding algorithm on simulations.

# More exciting explanation

- At fixed halo mass, halos in dense environments have more substructure, i.e., higher (subhalo) richness (*halo assembly bias*)
- BCG *in-situ* growth is suppressed by AGN feedback, but *ex-situ* growth is due to accretion from the intra-cluster medium and hierarchical mergers.
- Next step: looking into the intra-cluster light!

**Stay tuned!**