

CP violating mode of the stoponium decay into Zh

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> JHEP 1807 (2018) 025, arXiv: 1804.06089

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- In the MSSM (Minimal Supersymmetry SM), the lighter **Stop**, \tilde{t}_1 superpartner of top, can be lighter than other squarks.
- Because, i) top is heavy, large mixing angle between, $\widetilde{t}_{L,R}$. ii) if squarks have equal mass at high scale, the radiative correction will reduce the mass of $\widetilde{t}_{L,R}$. *M. Drees, Mihoko M. Nojiri, PRL 72, 2324(1994)*
- Stop cancel with the top quadratic divergence in the radiative correction to the Higgs mass. Hierarchy problem.

The LHC has put the Stop mass above 1 TeV:



ATLAS, 1711.11520, CMS,1711.00752.

*t*₁ is compress just above the lightest neutralino mass, there is not much missing momentum for tagging events at LHC.

- Lighter Stop is long-lived in comparison to the time scale QCD hadronization.
- Stoponium, $\tilde{\eta} \equiv {}^{1}S_{0}(\tilde{t}_{1}\tilde{t}^{*}_{1})$ stop-anti-stop bound state, can be formed. V.D. Bager, W.Y. Keung, PRL 211, 355(1988)
- It produced through gluon-gluon fusion and be identified by its distinctive decays: hh, WW, ZZ, γγ...

M. Drees, Mihoko M. Nojiri, PRL 72, 2324(1994)

 Studies the QCD corrections, lattice calculation, and dark matter co-annihilation.
 S.P. Martin, J.E. Younkin, PRD 80, 035026(2009), S. Kim, PRD 92, no.9 094505.

S. Kim, PRD 92, no.9 094505, F.Luo, J.Ellis et al, EPJ C78 (2018) no.5, 425.

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- The stoponium decay into channel hZ is forbidden by the assumption of CP conservation.
- There is no strong argument against *CP violation* in the stop sector.
- We will show $\tilde{\eta} \rightarrow hZ$ can have significant branching ratio withing the constraint from **eEDM** (electron electric dipole moment).

• The Z-boson couplings to the Stops $\widetilde{t}_{1,2}$, through the convection Feynman vertex amplitude:

$$\langle \tilde{t}_i(p_i) | J_{ij}^{\mu} | \tilde{t}_j(p_j) \rangle = (p_j + p_i)^{\mu}$$

• Where the convection current is $J_{ij}^{\mu} = i \tilde{t}_i^* \stackrel{\leftrightarrow}{\partial} \tilde{t}_j \quad \text{where} \quad \stackrel{\leftrightarrow}{\partial} \equiv \stackrel{\rightarrow}{\partial} - \stackrel{\leftarrow}{\partial}$ for incoming p_j and outgoing p_i .

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• The Z-boson couplings to the Stops $\widetilde{t}_{1,2}$, through the convection Feynman vertex amplitude:

$$\langle \widetilde{t}_i(p_i) | J_{ij}^{\mu} | \widetilde{t}_j(p_j) \rangle = (p_j + p_i)^{\mu}$$

Under the charge conjugation

$$C, \ \widetilde{t}_i \ \longleftrightarrow \ \widetilde{t}_i^*$$

$$J^{\mu}_{ij} \stackrel{C}{\longleftrightarrow} -J^{\mu}_{ji}$$

We need to make C-odd transformation for Z:

$$Z^{\mu} \stackrel{C}{\longleftrightarrow} -Z^{\mu}$$

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The Z-boson couplings to the Stops $\tilde{t}_{1,2}$, through the convection Feynman vertex amplitude:

$$\langle \widetilde{t}_i(p_i) | J_{ij}^{\mu} | \widetilde{t}_j(p_j) \rangle = (p_j + p_i)^{\mu}$$

- The hermiticity of the unitary interaction $\mathcal{L} \supset \sum_{ij} g_{ij}^Z J_{ij}^\mu Z_\mu$ requires $g_{ij}^Z = g_{ji}^{Z*}$.
- If Charge conjugation is good symmetry, $g_{ij}^Z = g_{ji}^Z$.

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- Summarizing above discussion: Complex g_{ij}^Z (for $i \neq j$) if its phase is NOT removable implies *C-parity violation*.
- We can make g_{12}^Z real by redefining the relative phase between $\widetilde{t}_{1,2}$.
- To have *C-parity violation*, additional complex coupling coefficient \mathcal{Y} from Higgs vertex $yh(\tilde{t}_2^*\tilde{t}_1)$ is needed.

- The P-parity is conserved in the Z-vertex.
- Because for the renormalizable interaction of the pure bosonic sector, operators of dim 4 or less do not involve the P-odd Levi-Civita *∈*-symbol.
- C-parity violation is CP-violation.

• Our example is the decay of the ground state **stoponium** in ${}^{1}S_{0}(\tilde{t}_{1}\tilde{t}_{1}^{*}) \rightarrow Zh$.



FIG. 1. Feynman diagrams for the stoponium decaying into Zh via the t,u,s channels from the left to the right.

• The exchange \widetilde{t}_2 appear in t-channel and u-channel.

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FIG. 1. Feynman diagrams for the stoponium decaying into Zh via the t, u, s channels from the left to the right.

• The phase of g_{ij}^{Z} is tied with vertex $yh(\tilde{t}_{2}^{*}\tilde{t}_{1})$, and thus overall unremovable.

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FIG. 1. Feynman diagrams for the stoponium decaying into Zh via the t, u, s channels from the left to the right.

 The two amplitudes of t- and u-channels cancel if the coupling factor is real, but add up if imaginary.

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FIG. 1. Feynman diagrams for the stoponium decaying into Zh via the t, u, s channels from the left to the right.

 The production of Zh from stoponium decay is a sign of CP-violation.

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FIG. 1. Feynman diagrams for the stoponium decaying into Zh via the t,u,s channels from the left to the right.

• Direct coupling of pseudoscalar **A** to the **Stops** $A^0(\tilde{t}_1^*\tilde{t}_1 - \tilde{t}_2^*\tilde{t}_2)$, which is CP-violating.

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FIG. 1. Feynman diagrams for the stoponium decaying into Zh via the t, u, s channels from the left to the right.

• $m_{A^0} \simeq m_{\tilde{\eta}}$ will enhance the **Zh** decay mode, but restricted by the **eEDM**.

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- The process $\widetilde{t_1}\widetilde{t_1^*} \to hZ$.
- In the non-relativistic approximation, the amplitude is

$$\mathcal{M}(\tilde{t_1}\tilde{t_1}^* \to hZ) = -\left[\frac{4i\mathrm{Im}(g_{\tilde{t_1}\tilde{t_2}}^{Z*}y_{\tilde{t_1}\tilde{t_2}}^h)}{m_h^2 + m_Z^2 - 2(m_{\tilde{t_1}}^2 + m_{\tilde{t_2}}^2)} + \frac{2y_{\tilde{t_1}\tilde{t_1}}^A g_{Ah}^Z}{4m_{\tilde{t_1}}^2 - m_A^2}\right](P \cdot \varepsilon_Z)$$

$$u - \text{ and } t - \text{channel, exchange } \tilde{t_2}$$

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- The process $\widetilde{t_1}\widetilde{t_1}^* o hZ$.
- In the non-relativistic approximation, the amplitude is

$$\mathcal{M}(\tilde{t_1}\tilde{t_1^*} \to hZ) = -\left[\frac{4i\mathrm{Im}(g_{\tilde{t_1}\tilde{t_2}}^{2*}y_{\tilde{t_1}\tilde{t_2}}^h)}{m_h^2 + m_Z^2 - 2(m_{\tilde{t_1}}^2 + m_{\tilde{t_2}}^2)} + \frac{2y_{\tilde{t_1}\tilde{t_1}}^A g_{Ah}^Z}{4m_{\tilde{t_1}}^2 - m_A^2}\right](P \cdot \varepsilon_Z)$$
$$s-\text{channel, exchange } A^0$$

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- The process $\widetilde{t_1}\widetilde{t_1}^* o hZ$.
- In the non-relativistic approximation, the amplitude is

$$\mathcal{M}(\tilde{t}_1\tilde{t}_1^* \to hZ) = -\left[\frac{4i\mathrm{Im}(g_{\tilde{t}_1\tilde{t}_2}^{Z*}y_{\tilde{t}_1\tilde{t}_2}^h)}{m_h^2 + m_Z^2 - 2(m_{\tilde{t}_1}^2 + m_{\tilde{t}_2}^2)} + \frac{2y_{\tilde{t}_1\tilde{t}_1}^A g_{Ah}^Z}{4m_{\tilde{t}_1}^2 - m_A^2}\right](P \cdot \varepsilon_Z)$$
polarization sum
$$\sum_{\varepsilon_Z} (P \cdot \varepsilon_Z)^2 = P^{\mu} \left(-g_{\mu\nu} + \frac{p_{Z\mu}p_{Z\nu}}{m_Z^2}\right)P^{\nu} = \frac{\lambda(s, m_h^2, m_Z^2)}{4m_Z^2}$$

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- The process $\widetilde{t_1}\widetilde{t_1^*} \to hZ$.
- In the non-relativistic approximation, the amplitude is

$$\mathcal{M}(\tilde{t}_{1}\tilde{t}_{1}^{*} \to hZ) = -\left[\frac{4i\mathrm{Im}(g_{\tilde{t}_{1}\tilde{t}_{2}}^{Z*}y_{\tilde{t}_{1}\tilde{t}_{2}}^{h})}{m_{h}^{2} + m_{Z}^{2} - 2(m_{\tilde{t}}^{2} + m_{\tilde{t}_{2}}^{2})} + \frac{2y_{\tilde{t}_{1}h}^{A}(g_{Ah}^{Z})}{4m_{\tilde{t}_{1}}^{2} - m_{A}^{2}}\right](P \cdot \varepsilon_{Z})$$

The amplitude is suppressed by
non-alignment factor $\cos(\beta - \alpha)$

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- The process $\widetilde{t_1}\widetilde{t_1^*} \to hZ$.
- In the non-relativistic approximation, the amplitude is

$$\mathcal{M}(\widetilde{t_1}\widetilde{t_1^*} \to hZ) = -\left[\frac{4i\mathrm{Im}(g_{\widetilde{t_1}\widetilde{t_2}}^{Z*}y_{\widetilde{t_1}\widetilde{t_2}}^h)}{m_h^2 + m_Z^2 - 2(m_{\widetilde{t_1}}^2 + m_{\widetilde{t_2}}^2)} + \frac{2y_{\widetilde{t_1}\widetilde{t_1}}^A g_{Ah}^Z}{4m_{\widetilde{t_1}}^2 - m_A^2}\right](P \cdot \varepsilon_Z)$$

The partial decay width:

$$\begin{split} \Gamma(\widetilde{t_1}\widetilde{t_1^*} \to hZ) &= \frac{1}{(2m_{\widetilde{t_1}})^2} \sum_{\varepsilon_Z} |\mathcal{M}(\widetilde{t_1}\widetilde{t_1^*} \to hZ)|^2 |\psi(0)|^2 \frac{3}{8\pi} \lambda^{\frac{1}{2}}(1, m_h^2/s, m_Z^2/s) \\ \text{bound state wave function at the origin} \\ |\psi(0)|^2 &= \frac{1}{27\pi} (\alpha_s 2m_{\widetilde{t_1}})^3 \end{split}$$

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- The eEDM constraint: $|d_e| < 8.7 \times 10^{-29} \ e \cdot [cm]$, at 90% C.L. ACME Collaboration, Science 343, 269(2014)
- In MSSM, *CP-violating* contribution in Stop sector via two-loop Barr-Zee diagram. D.Chang, W.Y.Keung, A.Pilaftsis,, PRL 82, 900 (1999)



$$\mathcal{L}_{CP} = -\xi_f v a (\tilde{f}_1^* \tilde{f}_1 - \tilde{f}_2^* \tilde{f}_2) + \frac{i g_w m_f}{2M_W} R_f a \bar{f} \gamma_5 f$$

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$$\left(\frac{d_e}{e}\right)_{2-\text{loop}}^{\tilde{t}} = 2Q_e Q_t^2 \frac{3\alpha_{\text{em}}}{64\pi^3} \frac{m_e}{m_A^2} \left(\frac{\sin 2\theta_{\tilde{t}} \ m_t \text{Im}[\mu^* e^{-i\delta_u}]}{v^2 \sin \beta \cos \beta}\right) \left[F\left(\frac{m_{\tilde{t}_1}^2}{m_A^2}\right) - F\left(\frac{m_{\tilde{t}_2}^2}{m_A^2}\right)\right]$$

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 We ignore one-loop contribution from neutralinoselectron, and chargino-sneutrino diagrams, involve different CP-violating parameters.

Analysis

Interplay between Zh channel and eEDM:

- 1. Near and below the pole, $m_{\tilde{\eta}} < m_A$ by setting $2m_{\tilde{t}_1} = 1200$ GeV and $m_A = 1.5$ TeV.
- 2. Well below the pole, $m_{\tilde{\eta}} \ll m_A$ by setting $2m_{\tilde{t}_1} = 1200$ GeV and $m_A = 2.5$ TeV.
- 3. Far from the pole for an extremely heavy m_A . We set $2m_{\tilde{t}_1} = 1200 \text{ GeV} \ll m_A$.

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Analysis

Interplay between Zh channel and eEDM:

$$\begin{split} & \overline{m}_{\widetilde{t}_1} \simeq \overline{m}_{\widetilde{t}_2} \\ & \mathrm{BR}(\widetilde{\eta} \to Zh) \simeq 10^{-1} \end{split}$$



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Observability at LHC

 The Stoponium LO production cross section at LHC through the gluon-gluon fusion:

$$\sigma(pp \to \widetilde{\eta}) = \frac{\pi^2}{8m_{\widetilde{\eta}}^3} \Gamma(\widetilde{t_1}\widetilde{t_1^*} \to gg) \int_{\tau}^1 dx \frac{\tau}{x} g(x,Q) g(\tau/x,Q)$$

Including NLO, at 13 TeV LHC, the cross section is

$$\sigma(pp \to \widetilde{\eta}) \simeq 1$$
 [fb] for $m_{\widetilde{\eta}} \simeq 1.2$ TeV

• At LHC, the signal would be $pp \to \tilde{\eta} \to hZ$, then $h \to b\bar{b}$ and $Z \to \ell\ell$ (or jj)

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Observability at LHC

At LHC, the signal would be

 $pp \to \widetilde{\eta} \to hZ$, then $h \to b\overline{b}$ and $Z \to \ell\ell$ (or jj)

- The Z and Higgs bosons are very boosted in contrast to the conventional QCD background.
- The current limit from ATLAS and CMS: $\sigma(pp \to X \to Zh) \times B(h \to b\bar{b} + c\bar{c}) < 10 \text{ fb.}$

◆ 300 fb^-1 luminosity at Run-II, 15 events for $BR(\tilde{\eta} \rightarrow Zh) = 10\%$

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- The Zh channel decay mode from the ground state of stoponium is clean signal of *CP-violation*.
- Under the **eEDM** constraint, $\tilde{\eta} \rightarrow Zh$ can have a significant branching ratio.
- If stoponium is around 1.2 TeV, highly boosted Z and Higgs bosons are distinguishable from the QCD background.

Thank You!

Back Up

The Stop mixing:

The stop mass matrix can be expressed as

$$(\widetilde{t}_L^*, \widetilde{t}_R^*) \begin{pmatrix} m_t^2 + M_{\widetilde{Q}}^2 + m_Z^2(\frac{1}{2} - \frac{2}{3}x_W)\cos(2\beta) & m_t(A_t^* - \mu\cot\beta) \\ m_t(A_t - \mu^*\cot\beta) & m_t^2 + M_{\widetilde{U}}^2 + m_Z^2(\frac{2}{3}x_W)\cos(2\beta) \end{pmatrix} \begin{pmatrix} \widetilde{t_L} \\ \widetilde{t_R} \end{pmatrix}$$

We can define a phase δ_u by

$$A_t - \mu^* \cot \beta = |A_t - \mu^* \cot \beta| e^{i\delta_u}$$

$$\begin{pmatrix} \widetilde{t_L} \\ \widetilde{t_R} \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & e^{i\delta_u} \end{pmatrix} \begin{pmatrix} \cos\theta_{\widetilde{t}} & -\sin\theta_{\widetilde{t}} \\ \sin\theta_{\widetilde{t}} & \cos\theta_{\widetilde{t}} \end{pmatrix} \begin{pmatrix} \widetilde{t_1} \\ \widetilde{t_2} \end{pmatrix}$$

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The Higgs-Stop-Stop couplings:

The interaction between
$$h$$
 and $\tilde{t}_{L,R}$ is

$$\mathcal{L} \subset h(\tilde{t}_{L}^{*}, \tilde{t}_{R}^{*}) \begin{pmatrix} V_{LL} & V_{LR}^{*} \\ V_{LR} & V_{RR} \end{pmatrix} \begin{pmatrix} \tilde{t}_{L} \\ \tilde{t}_{R} \end{pmatrix}$$

$$= h(\tilde{t}_{L}^{*}, \tilde{t}_{R}^{*}) \begin{pmatrix} -\frac{gm_{t}^{2}c_{\alpha}}{m_{W}s_{\beta}} + \frac{gm_{Z}}{\sqrt{1-x_{W}}} (\frac{1}{2} - \frac{2}{3}x_{W})s_{\alpha+\beta} & -\frac{1}{2}\frac{gm_{t}}{m_{W}s_{\beta}} (A_{t}^{*}c_{\alpha} + \mu s_{\alpha}) \\ -\frac{1}{2}\frac{gm_{t}}{m_{W}s_{\beta}} (A_{t}c_{\alpha} + \mu^{*}s_{\alpha}) & -\frac{gm_{t}^{2}c_{\alpha}}{m_{W}s_{\beta}} + \frac{gm_{Z}}{\sqrt{1-x_{W}}} (\frac{2}{3}x_{W})s_{\alpha+\beta} \end{pmatrix} \begin{pmatrix} \tilde{t}_{L} \\ \tilde{t}_{R} \end{pmatrix}$$

$$\equiv h(\tilde{t}_{1}^{*}, \tilde{t}_{2}^{*}) \begin{pmatrix} y_{t_{1}\tilde{t}_{1}}^{h} & y_{t_{1}\tilde{t}_{2}}^{h} \\ y_{t_{1}\tilde{t}_{2}}^{h} & y_{t_{2}\tilde{t}_{2}}^{h} \end{pmatrix} \begin{pmatrix} \tilde{t}_{1} \\ \tilde{t}_{2} \end{pmatrix}, \qquad (5)$$

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The Z-Stop-Stop couplings:

The interaction between Z boson and $\tilde{t}_{L,R}$ is

$$\begin{split} \mathcal{L} \supset \frac{g}{\sqrt{1 - x_W}} Z^{\mu}(\tilde{t_L^*}, \tilde{t_R^*}) i \stackrel{\leftrightarrow}{\partial}_{\mu} \begin{pmatrix} -\frac{1}{2} + Q_t x_W & 0\\ 0 & Q_t x_W \end{pmatrix} \begin{pmatrix} \tilde{t_L}\\ \tilde{t_R} \end{pmatrix} \\ &= \frac{g}{\sqrt{1 - x_W}} Z^{\mu} \left(\tilde{t_1^*}, \tilde{t_2^*}\right) i \stackrel{\leftrightarrow}{\partial}_{\mu} \begin{pmatrix} -\frac{1}{2} c_{\theta_{\tilde{t}}} + Q_t x_W & \frac{1}{2} s_{\theta_{\tilde{t}}} c_{\theta_{\tilde{t}}}\\ \frac{1}{2} s_{\theta_{\tilde{t}}} c_{\theta_{\tilde{t}}} & -\frac{1}{2} s_{\theta_{\tilde{t}}}^2 + Q_t x_W \end{pmatrix} \begin{pmatrix} \tilde{t_1}\\ \tilde{t_2} \end{pmatrix} \\ &\equiv Z^{\mu}(\tilde{t_1^*}, \tilde{t_2^*}) i \stackrel{\leftrightarrow}{\partial}_{\mu} \begin{pmatrix} g_{\tilde{t_1}\tilde{t_1}}^Z & g_{\tilde{t_1}\tilde{t_2}}^Z\\ g_{\tilde{t_1}\tilde{t_2}}^Z & g_{\tilde{t_2}\tilde{t_2}}^Z \end{pmatrix} \begin{pmatrix} \tilde{t_1}\\ \tilde{t_2} \end{pmatrix}, \end{split}$$

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The A-Stop-Stop couplings:

$$\begin{aligned} \mathcal{L} \supset &-\frac{im_t}{v\sin\beta} A^0(\tilde{t}_L^*, \tilde{t}_R^*) \begin{pmatrix} 0 & -(A_t^*c_\beta + \mu s_\beta) \\ A_tc_\beta + \mu^*s_\beta & 0 \end{pmatrix} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix} \\ &= \frac{m_t}{v\sin\beta} A^0(\tilde{t}_1^*, \tilde{t}_2^*) \begin{pmatrix} 2s_{\theta_{\tilde{t}}}c_{\theta_{\tilde{t}}}\mathrm{Im}[\hat{A}_t] & i(c_{\theta_{\tilde{t}}}^2\hat{A}_t^* + s_{\theta_{\tilde{t}}}^2\hat{A}_t) \\ -i(c_{\theta_{\tilde{t}}}^2\hat{A}_t + s_{\theta_{\tilde{t}}}^2\hat{A}_t^*) & -2s_{\theta_{\tilde{t}}}c_{\theta_{\tilde{t}}}\mathrm{Im}[\hat{A}_t] \end{pmatrix} \begin{pmatrix} \tilde{t}_1 \\ \tilde{t}_2 \end{pmatrix} \\ &\equiv A^0(\tilde{t}_1^*, \tilde{t}_2^*) \begin{pmatrix} y_{\tilde{t}_1\tilde{t}_1}^A & y_{\tilde{t}_1\tilde{t}_2}^A \\ y_{\tilde{t}_1\tilde{t}_2}^A & y_{\tilde{t}_2\tilde{t}_2}^A \end{pmatrix} \begin{pmatrix} \tilde{t}_1 \\ \tilde{t}_2 \end{pmatrix} \end{aligned}$$

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Analysis

Interplay between Zh channel and eEDM:

$$\begin{split} m_{A^0} &\simeq m_{\widetilde{\eta}} \\ \text{BR}(\widetilde{\eta} \to Zh) &\simeq 10^{-3} \end{split}$$



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Analysis

Interplay between Zh channel and eEDM:

 $m_{A^0} \to \infty$ and $m_{\widetilde{t}_1} \simeq m_{\widetilde{t}_2}$

 $BR(\tilde{\eta} \to Zh)$ can be dominating



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