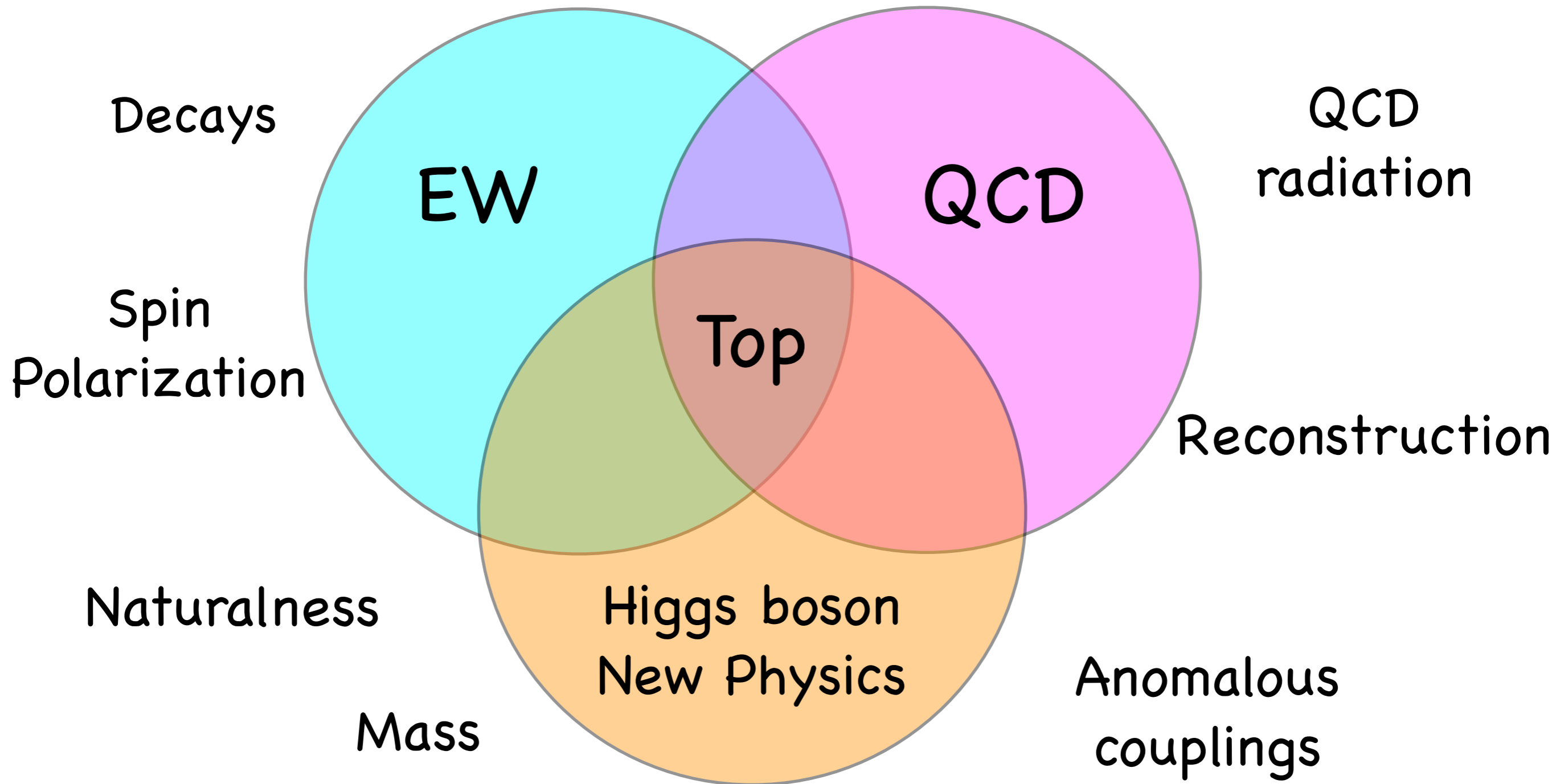


# Top physics after Higgs discovery



Michael Spannowsky  
University of Durham



Interacts over many time scales:

$$1/m_t <$$

Production time <

$$10^{-27} \text{ sec}$$

$$1/\Gamma_t <$$

Lifetime <

$$10^{-25} \text{ sec}$$

$$1/\Lambda <$$

Hadronization time <

$$10^{-24} \text{ sec}$$

$$m_t/\Lambda^2$$

Spin decorrelation time

# The top quark Lagrangian in the SM

Gauge interactions:

$$\mathcal{L} = i\bar{Q}_L \not{D} Q_L + i\bar{t}_R \not{D} t_R + i\bar{b}_R \not{D} b_R$$

with the SM covariant derivative

$$D_\mu = \partial^\mu + ig_s G_\mu^a T^a + ig W_\mu^i T^i + ig' B_\mu Y$$

in terms of the generators and gauge bosons of SU(3) ( $T^a, G_\mu^a, g_s$ )  
SU(2) ( $T^i, W_\mu^i, g$ ) and U(1) ( $Y, B_\mu, g'$ ) and

$$Z_\mu = \cos \theta_W W_\mu^3 - \sin \theta_W B_\mu \quad , \quad A_\mu = \sin \theta_W W_\mu^3 + \cos \theta_W B_\mu$$

with the Weinberg angle  $\theta_W$

Eventually, the coupling to the Higgs boson field is

$$\mathcal{L}_{\text{Yukawa}} = -y_t \bar{t} t H \quad \text{with} \quad y_t = m_t/v$$

After spontaneous symmetry breaking and rotating into the mass eigenstate basis, the charged current interactions introduce flavor mixing in the SM

$$\mathcal{L}_{W^\pm} = g W_\mu^\pm \sum_{i,j=\text{flavors}} V_{ij} \bar{q}_i \gamma^\mu q_j + \text{h.c.}$$

with the Cabibbo-Kobayashi-Maskawa matrix:

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

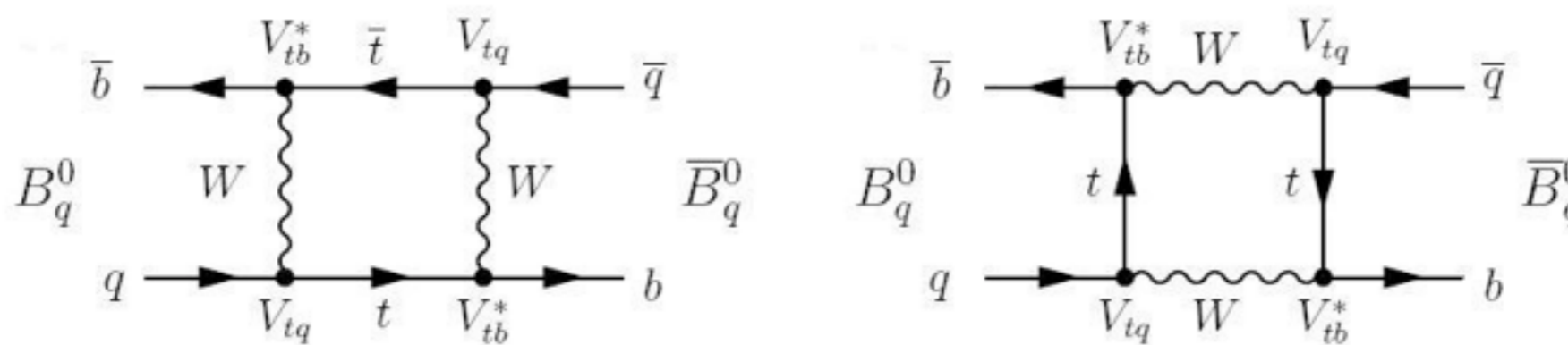
Need 3 generations for CP-violation in SM

→ top quark related to origin of CP  
and possibly baryogenesis

# Early indirect evidence for heavy top quark

- After discovering of b-quark existence of top expected
- Indirect evidence from B and K meson mixing - CP phase

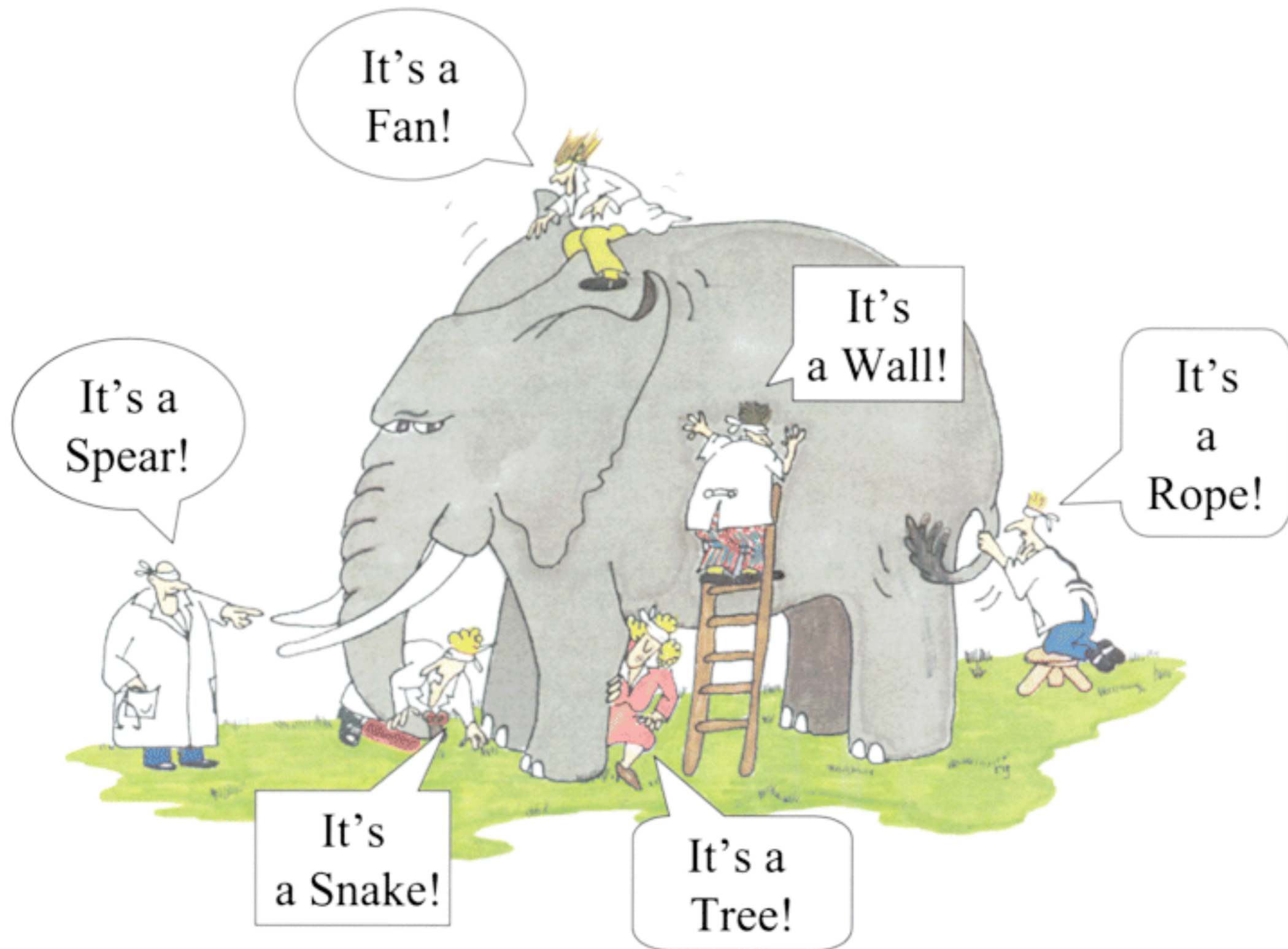
Kobayashi-Maskawa



Feynman box diagrams for B mixing.

- Vtb measurement: single top (Tevatron)  $V_{tb} = 0.88 \pm 0.07$   
 unitarity of CKM Mat.  $V_{tb} = 0.999135$
- EW precision tests at LEP give constraint of top mass

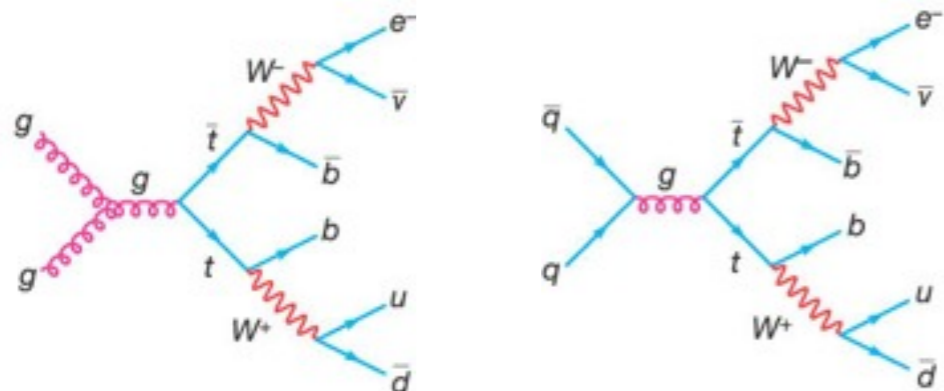
# Measurement of top quark properties



# $t\bar{t}$ production cross sections

- ▶  $t\bar{t}$  @ NLO [Nason, Dawson, Ellis ('88,'89); Beenakker, Kuijf, van Neerven, Smith]
- ▶  $t\bar{t}$  NNLO calculations [Czakon, Fiedler, Ferroglia, Pecjak, Yang; Mitov; Bonciani, Ferroglia, Gehrmann, Maitre, Studerus; Anastasiou, Aybat; Kniehl, Merebashvili, Korner, Rogal; Bonciani, Ferroglia, Gehrmann, Studerus; ... ]
- ▶  $t\bar{t}$  NNLL resummed [Czakon, Mitov; Kidonakis ('09,'10); Beneke, Falgari, Schwinn; Czakon, Mitov, Sterman; Beneke, Czakon, Falgari; ...]
- ▶  $t\bar{t}$  + (H, Z, photon) [Beenakker et al.; Dawson, Reina; Dawson, Reina, Wackerroth; Dawson Rein; Lazopoulos et al.; Peng-Fei et al.]
- ▶  $t\bar{t}$  + jet @ NLO [Dittmaier, Uwer, Weinzierl ('07,'09)]
- ▶  $t\bar{t}$  + 2jet @ NLO [Bevilacqua, Czakon, Papadopoulos, Worek]
- ▶  $t\bar{t}$  including decays @ NLO [Bevilacqua, Czakon, van Hameren, Papadopoulos, Worek]

# The dominant production mode: Top pair production



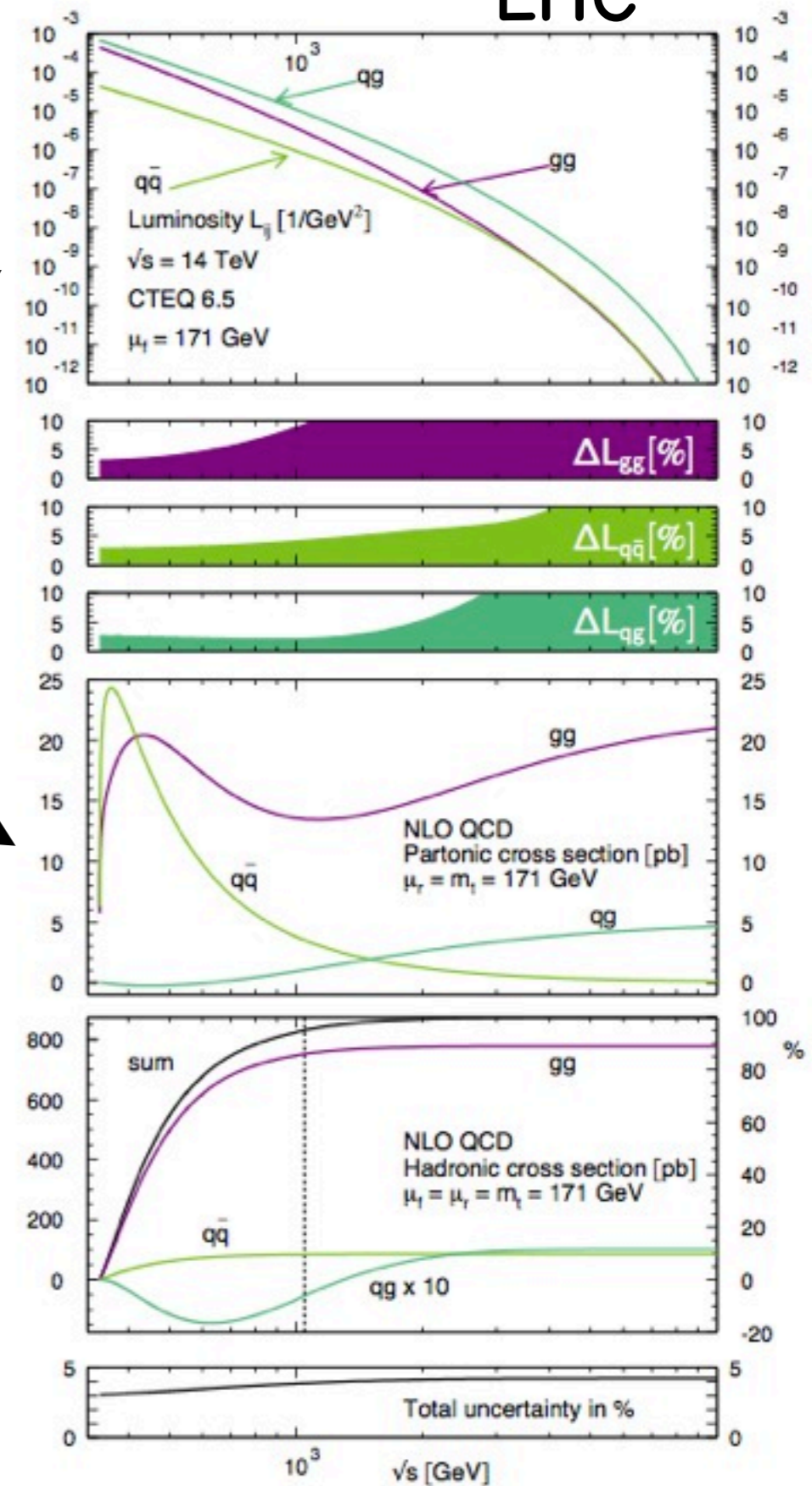
$$\sigma_{pp \rightarrow ttX}(s_{\text{had}}, m_t^2) = \sum_{i,j=q,q,g} \int_{4m_t^2}^{s_{\text{had}}} d\hat{s} L_{ij}(\hat{s}, s_{\text{had}}, \mu_f^2) \hat{\sigma}_{ij \rightarrow tt}(\hat{s}, m_t^2, \mu_f^2, \mu_r^2)$$

Collider	$\sigma_{\text{tot}}$ [pb]	scales [pb]	pdf [pb]
Tevatron	7.164	+0.110(1.5%) -0.200(2.8%)	+0.169(2.4%) -0.122(1.7%)
LHC 7 TeV	172.0	+4.4(2.6%) -5.8(3.4%)	+4.7(2.7%) -4.8(2.8%)
LHC 8 TeV	245.8	+6.2(2.5%) -8.4(3.4%)	+6.2(2.5%) -6.4(2.6%)
LHC 14 TeV	953.6	+22.7(2.4%) -33.9(3.6%)	+16.2(1.7%) -17.8(1.9%)

[@ NNLO+NNLL, Czakon, Fiedler, Mitov '13]

- Cross section roughly same for bbbar at B-factories as ttbar at LHC. LHC surpasses #Events after ~10 years (BABAR 530 fb).
- Measurements not statistics limited!

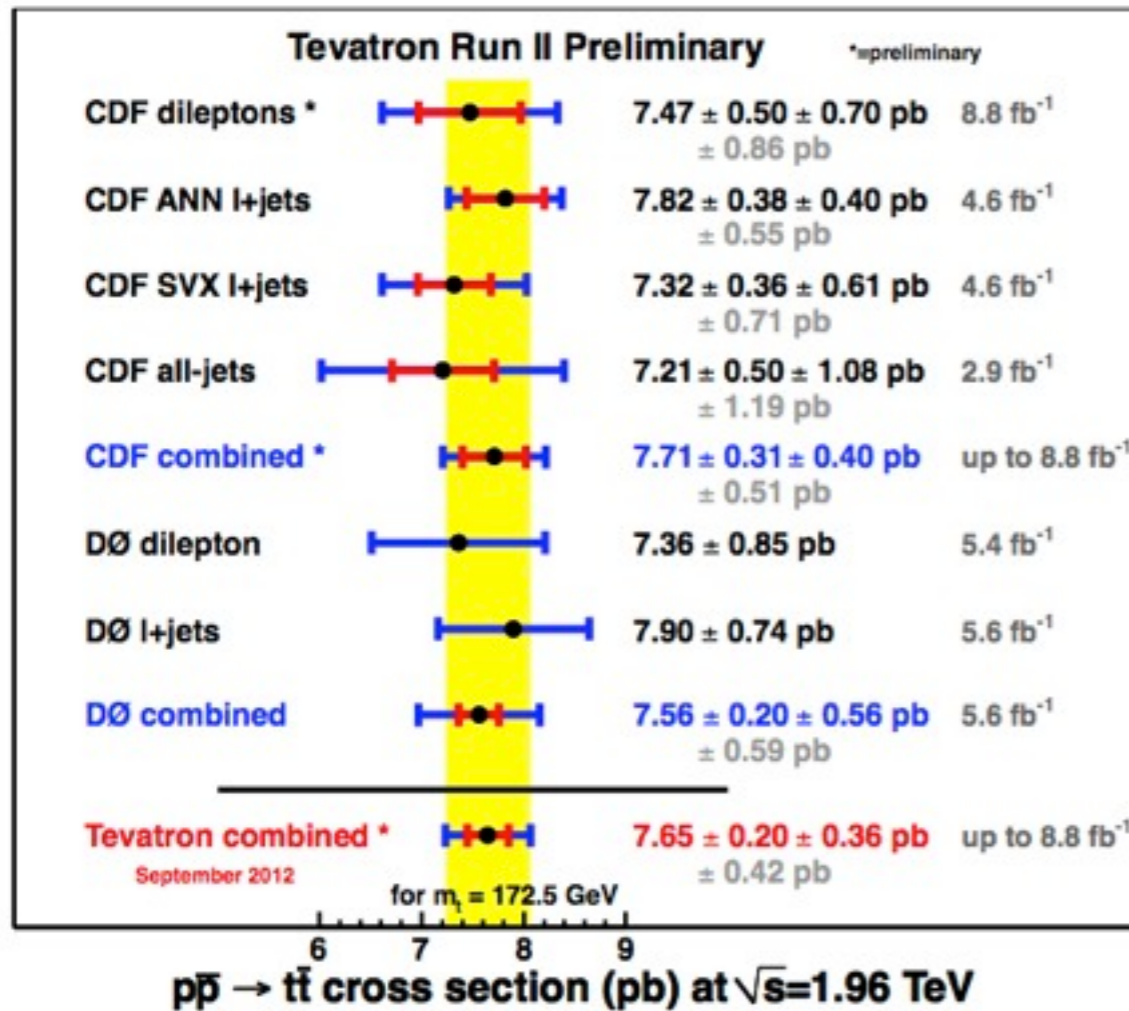
LHC



[Moch, Uwer 2008]

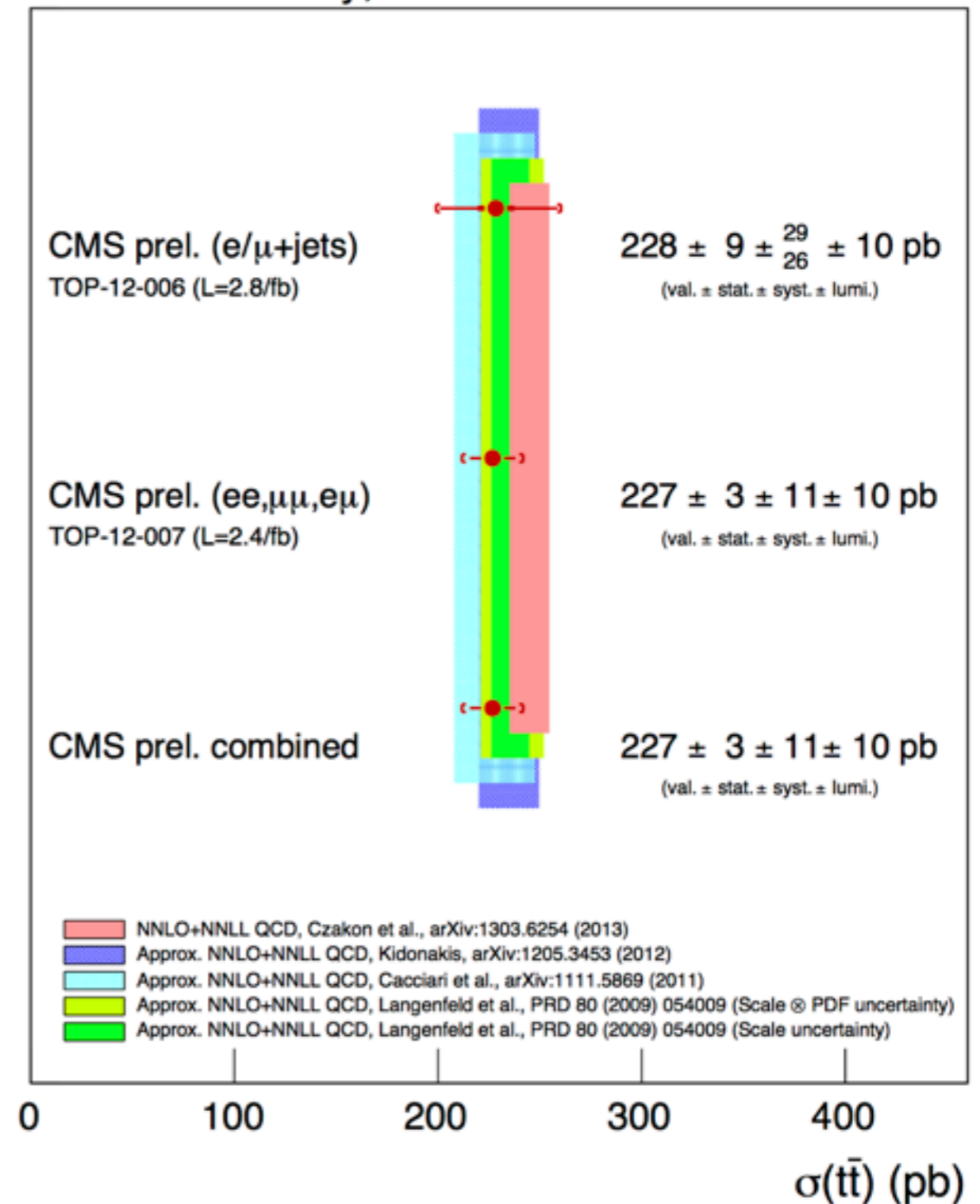


# $t\bar{t}$ production cross sections

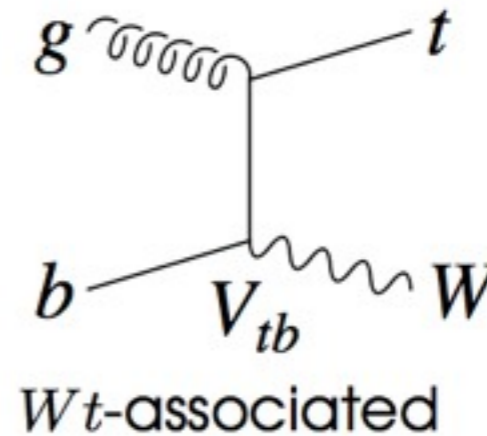
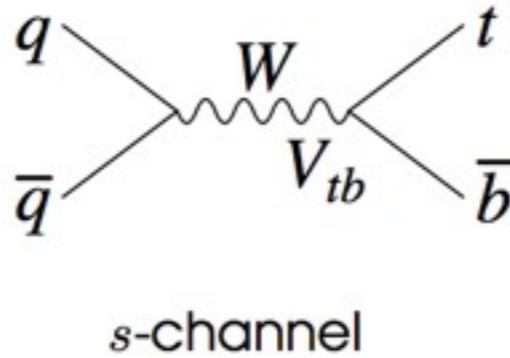
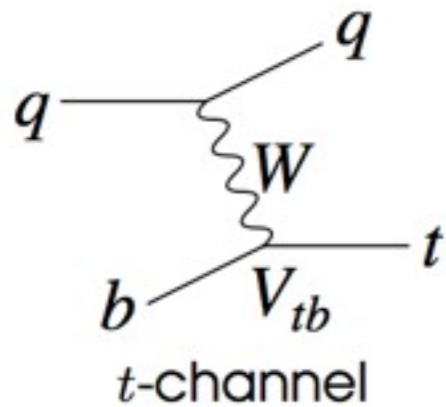


production cross section  
in very good agreement  
with theory prediction

CMS Preliminary,  $\sqrt{s} = 8 \text{ TeV}$



# Single top production



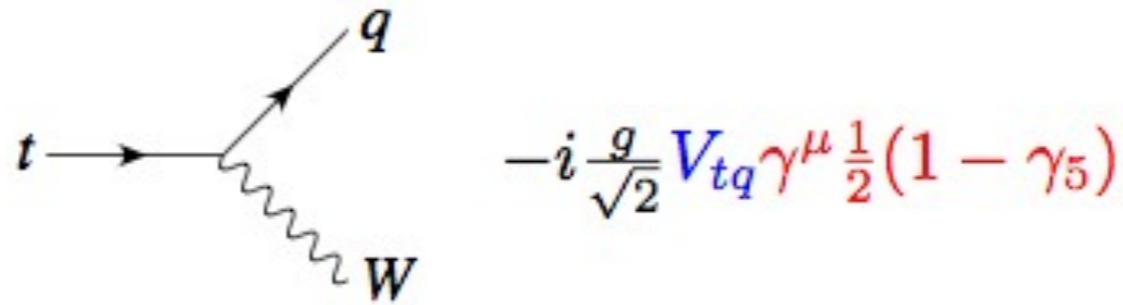
- production modes discriminated by # of tagged b-jets and their kinematics
- Cross sections for top / anti-top [pb]:

	t-channel	s-channel	Wt-channel
<b>LHC</b>	155.9 / 90.7	6.6 / 4.1	33 / 33
<b>Tevatron</b>	1.98	0.88	0.07

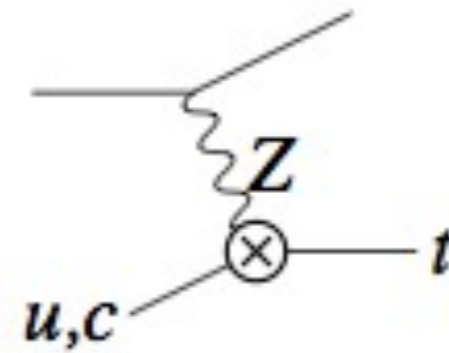
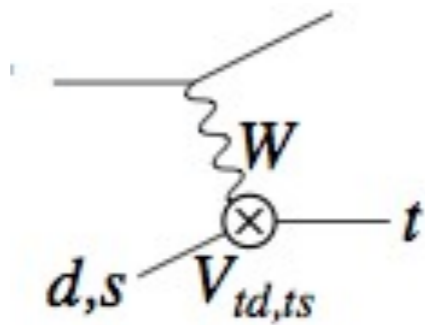
- At Tevatron with ~10 fb per experiment in total 60 000 single top events vs 150 000 pair top events

# Single top production subleading but useful for measurements

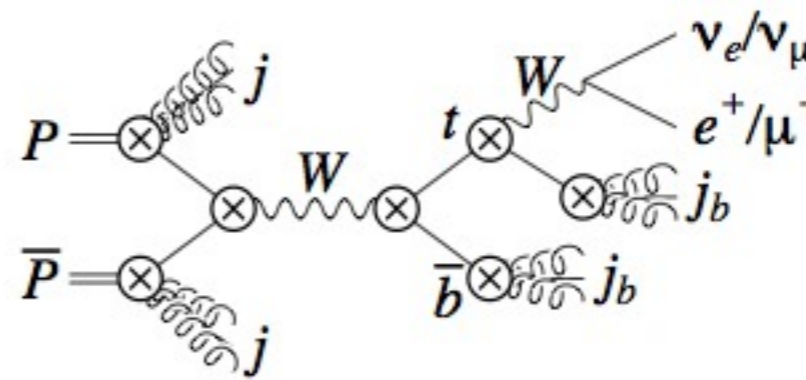
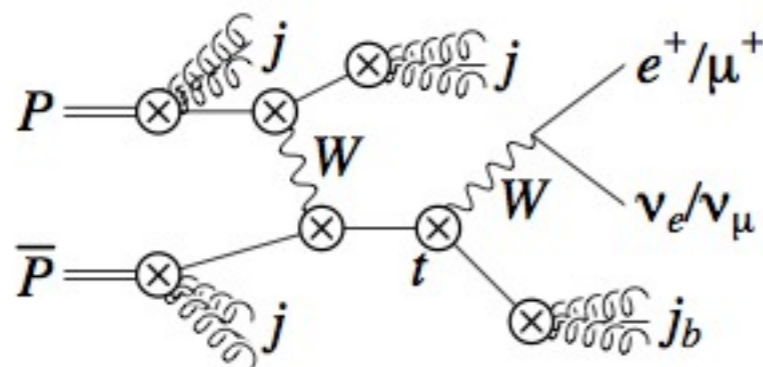
- $V_{tb}$



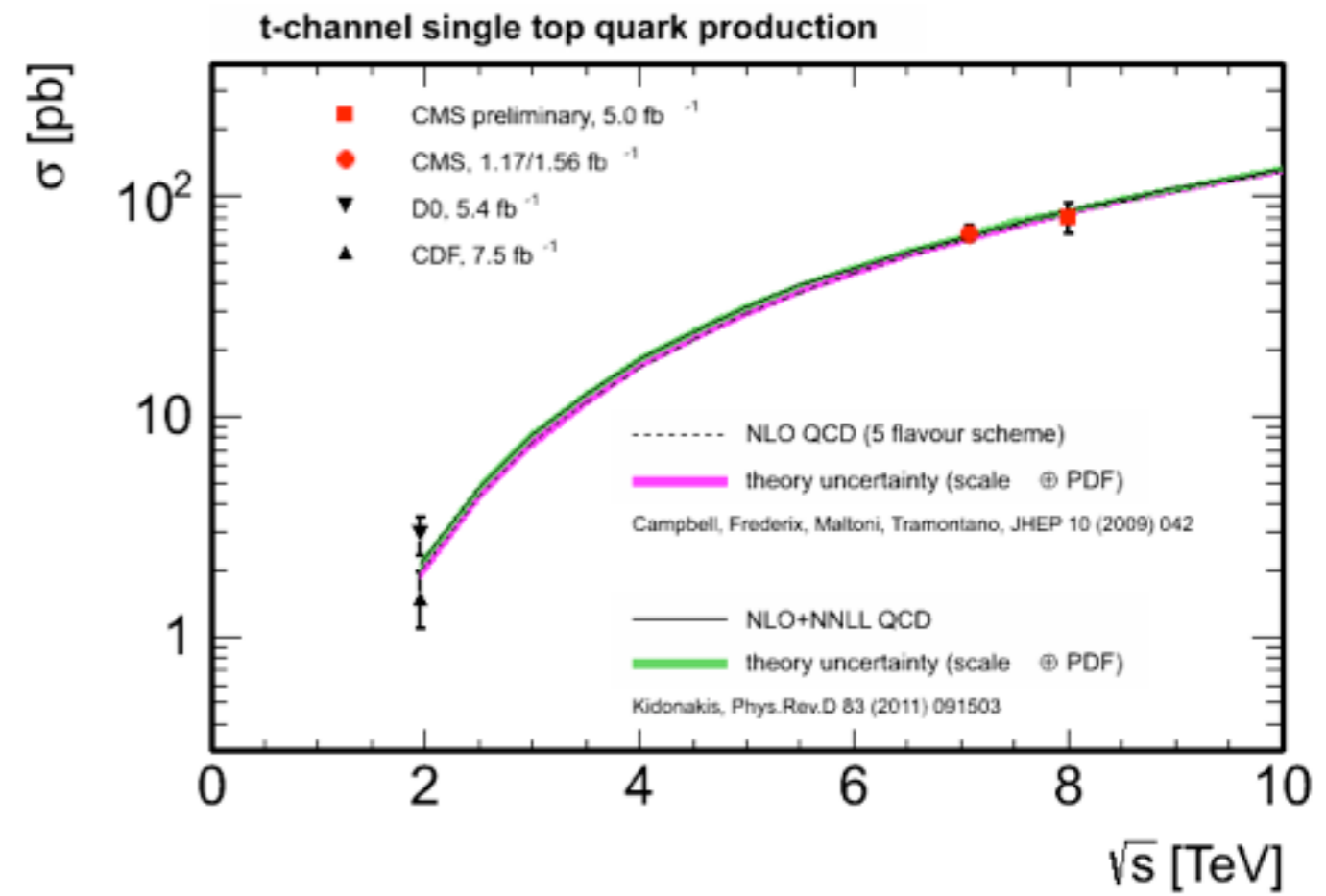
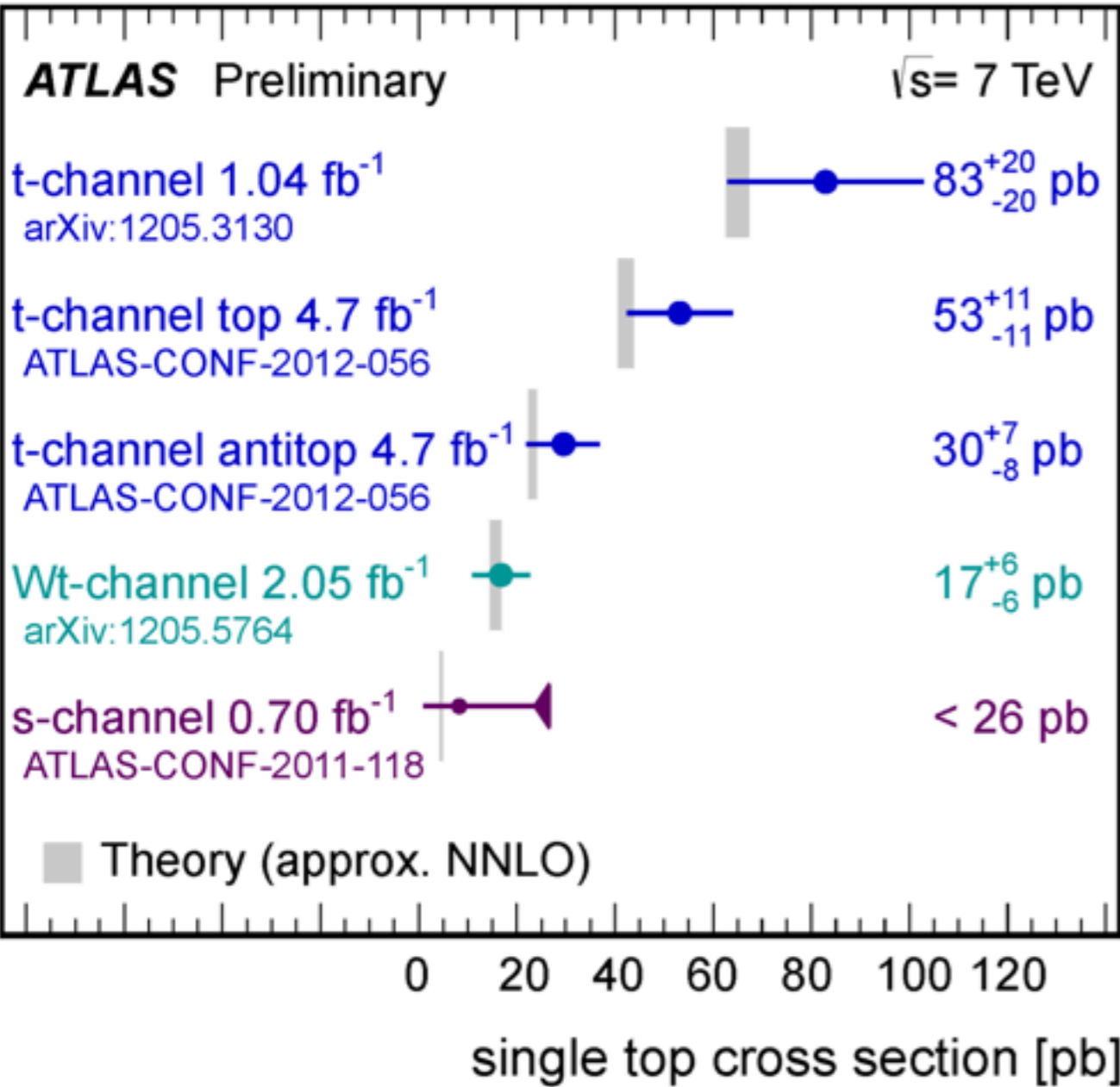
- Anomalous couplings in production



- Perfect factorization through NLO, like DIS and DY

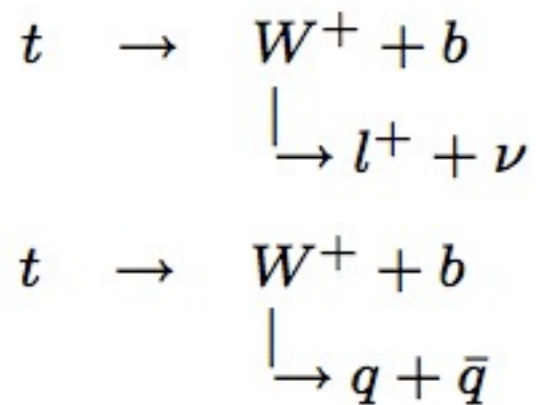


[Graphs Z. Sullivan]



# Top Quark decays

Decays before hadronizes via EW interaction. Since  $m_t > m_W + m_b$



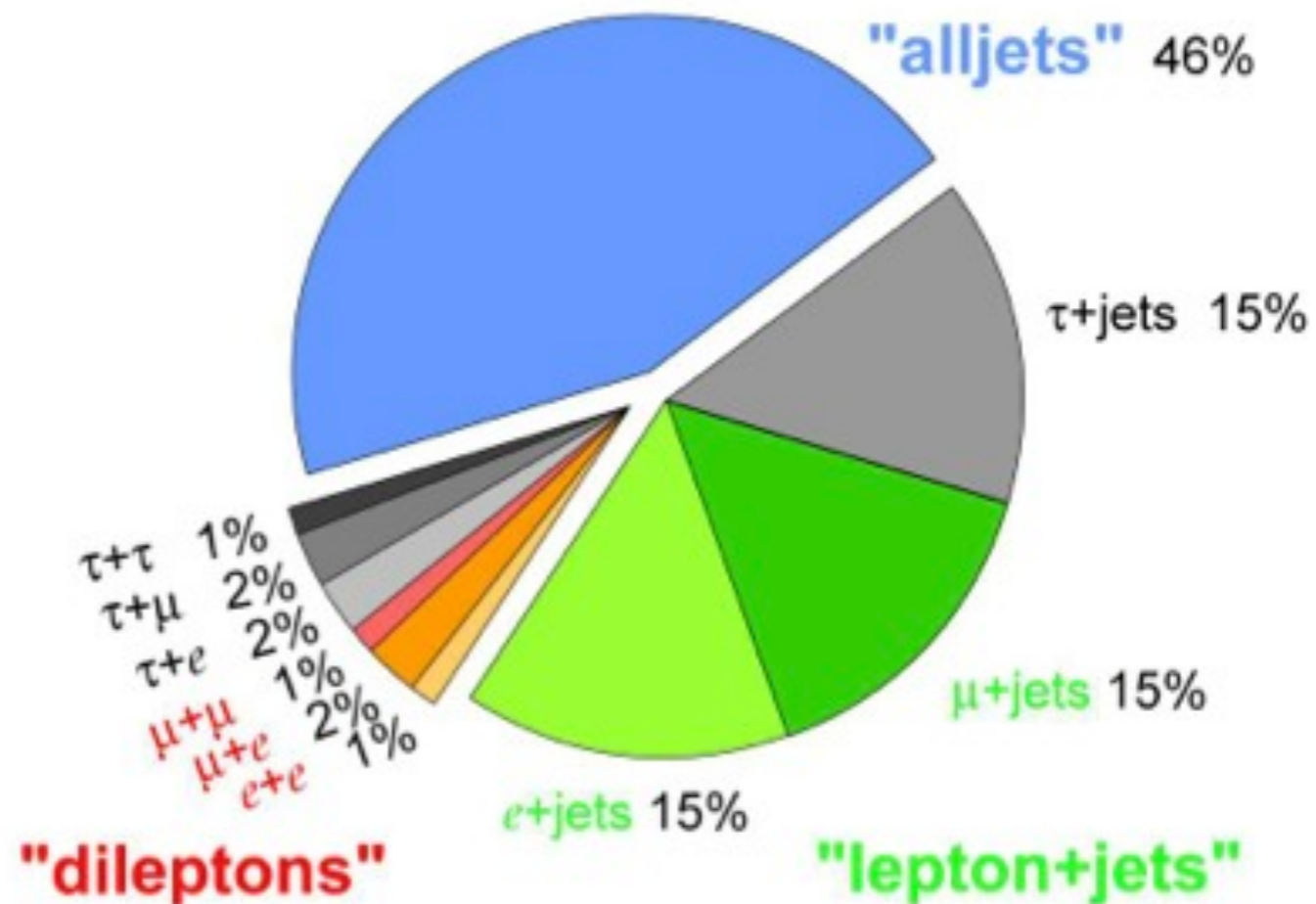
with  $\Gamma_t \simeq 1.4 \text{ GeV}$

Top decay modes determined by W decay, e.g.

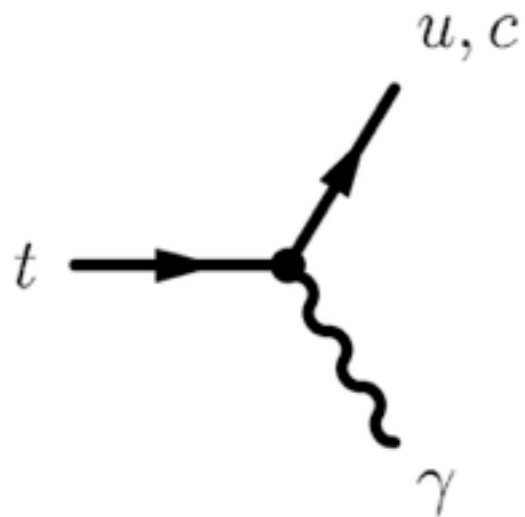
$$\text{BR}(W^+ \rightarrow e^+ \bar{\nu}) = \frac{1}{3 + 3 + 3} \approx 11\%.$$

$\swarrow$   $\uparrow$   $\nwarrow$   
 $l\nu$      $3 \times ud$      $3 \times cs$

Top Pair Branching Fractions



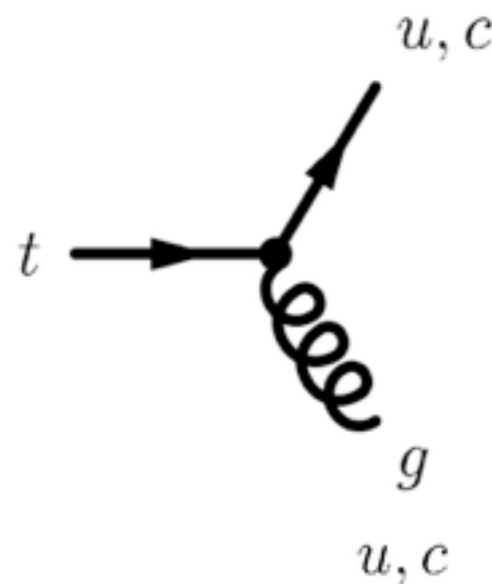
# Rare/Anomalous Top Quark decays



FCNC can be loop-induced in the SM and enhanced by New Physics

$$\mathcal{L}_{\text{eff}} = g_s \sum_{q=u,c} \frac{\kappa_{qgt}}{\Lambda} t \sigma^{\mu\nu} T^a (f_q^L P_L + f_q^R P_R) q G_{\mu\nu}^a + h.c.,$$

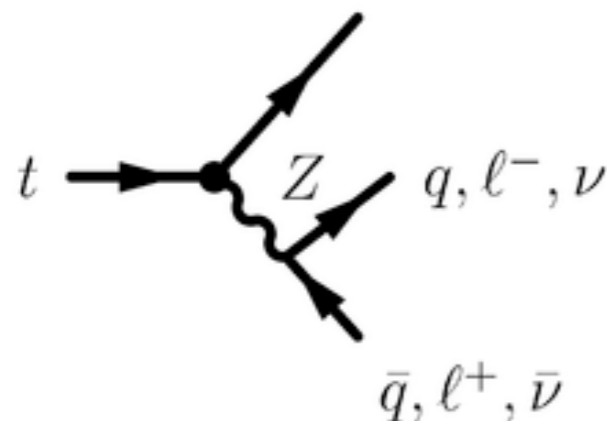
ATLAS study at 7 TeV with 2 fb



$$\kappa_{cgt}/\Lambda < 1.6 \cdot 10^{-2} \text{ TeV}^{-1} \quad \mathcal{B}(t \rightarrow cg) < 2.7 \cdot 10^{-4}$$

$$\kappa_{ugt}/\Lambda < 6.9 \cdot 10^{-3} \text{ TeV}^{-1} \quad \mathcal{B}(t \rightarrow ug) < 5.7 \cdot 10^{-5}$$

from single top prod converted



No evidence for  $t \rightarrow Zq$  decay found

$$\rightarrow \text{BR}(t \rightarrow Zq) < 0.73\%$$

# Top quark spin and polarization

The decay amplitude for  $t(p_t) \rightarrow b(p_b)W^+(p_W)$  is given by

$$\mathcal{M}(t \rightarrow bW^+) = -\frac{ig}{2\sqrt{s}} V_{tb} \bar{u}(p_b) \gamma^\mu (1 - \gamma_5) u(p_t) \epsilon_\mu^{\lambda*}(p_W)$$

and the decay rate for a given W-boson polarization is calculated as:

$$\Gamma = \frac{1}{2m_t} \int dLIPS \sum_{\lambda} |\mathcal{M}(t \rightarrow bW^+)|^2$$

Assuming the top quark is unpolarized, working in its rest frame, the momentum configuration can be parametrized as:

$$p_t = (m_t, 0, 0, 0) \quad p_W = (E_W, 0, p \sin \theta, p \cos \theta) \quad p_b = (E_b, 0, -p \sin \theta, -p \cos \theta)$$

with  $E_W = \frac{m_t^2 + M_W^2}{2m_t}$  and  $p = \frac{m_t^2 - M_W^2}{2m_t}$ , W polarization vectors are

$$\epsilon_0 = \frac{1}{M_W} (p, 0, E_W \sin \theta, E_W \cos \theta) \quad \epsilon_{\pm} = \frac{1}{\sqrt{2}} (0, 1, \pm i \cos \theta, \mp \sin \theta)$$

with  $m_b = 0$  we get

$$\overline{\sum} |\mathcal{M}(t \rightarrow bW^+)|^2 = \frac{g^2}{8} |V_{tb}|^2 \text{Tr} [(p'_t + m_t) \epsilon_{/\lambda}^* (1 - \gamma_5) p'_b \epsilon_{/\lambda}]$$

and substituting the explicit polarization vectors one derives

$$\overline{\sum} |\mathcal{M}_0|^2 = \frac{2G_F m_t^4}{\sqrt{2}} |V_{tb}|^2 (1 - x)$$

$$\overline{\sum} |\mathcal{M}_-|^2 = \frac{2G_F m_t^4}{\sqrt{2}} |V_{tb}|^2 2x^2 (1 - x^2)$$

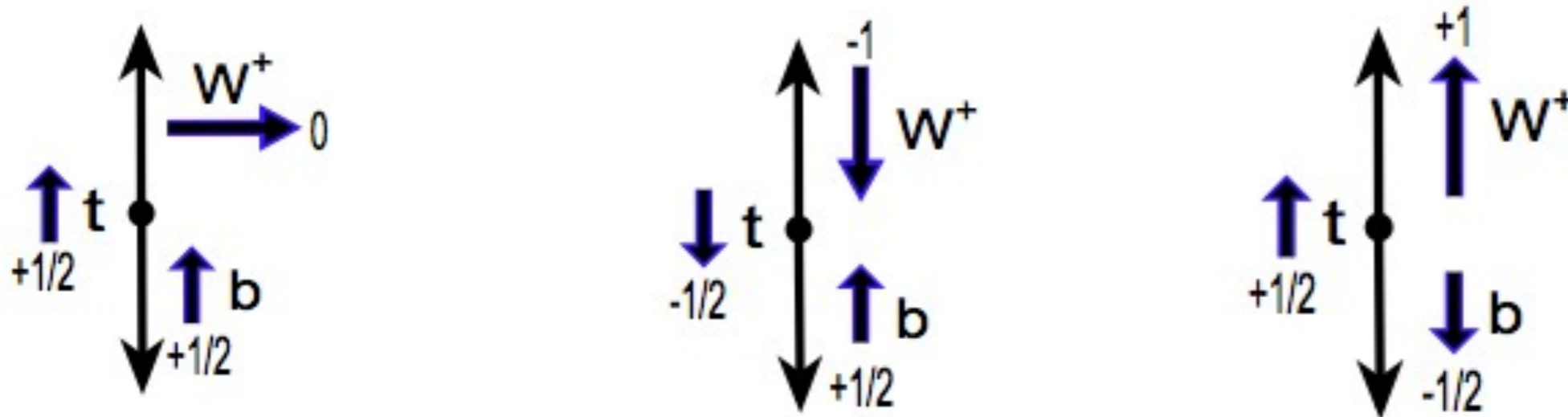
for  $x = \frac{M_W}{m_t}$ , such that the fraction of longitudinally polarized W is:

$$F_0 = \frac{\Gamma_0}{\Gamma_{\text{tot}}} = \frac{1}{1 + 2x^2} = \frac{m_t^2}{m_t^2 + 2M_W^2} \simeq 0.70$$



# Structure of elw. top interactions

For  $m_b = 0$  the  $W$  coming from  $t \rightarrow bW^+$  can either be left-handed or longitudinal, never right-handed, because of angular momentum conservation



$$F_0 = \frac{m_t^2}{m_t^2 + 2M_W^2} + \mathcal{O}\left(\frac{m_b^2}{m_t^2}\right) \quad F_- = 1 - F_0 + \mathcal{O}\left(\frac{m_b^2}{m_t^2}\right) \quad F_+ = \mathcal{O}\left(\frac{m_b^2}{m_t^2}\right)$$

- Probes Weak interactions near EW symmetry breaking scale
- Test of V-A interaction in Standard Model

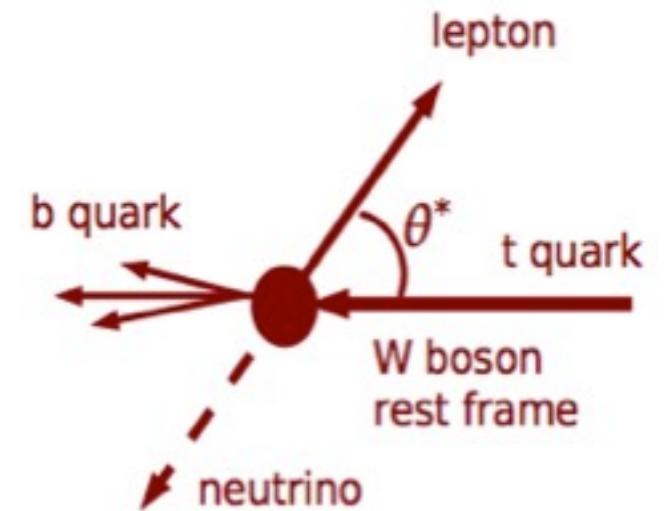
Including second stage decay  $W^+ \rightarrow l^+ \nu$

allows to use charged lepton to measure W helicity fractions

$$\begin{aligned} \frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta^*} &= F_0 \frac{3}{4} (1 - \cos^2\theta^*) \\ &+ F_- \frac{3}{8} (1 - \cos\theta^*)^2 \\ &+ F_+ \frac{3}{8} (1 + \cos\theta^*)^2 \end{aligned}$$

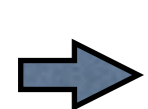


(Collins-Soper angle)



or to measure top quark polarization. After summing all W helicities the squared matrix element is

$$\sum |M|^2 \sim \frac{(m_b^2 p_t \cdot p_l - m_t^2 p_t \cdot p_l + 2p_t \cdot p_l)}{((p_l + p_\nu)^2 - m_W^2)^2}$$



lepton - top perfectly correlated  
to check for top polarization

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta_{l,n}} = \frac{1}{2} (1 + \mathcal{P}_n \cos\theta_{l,n})$$

[Mahlon, Parke 1996]

top completely polarized:  $\mathcal{P}_n = \pm 1$

# top polarization: Important for many applications

Example: Polarized tops from stop decays  $\tilde{t} \rightarrow \chi_1^0 t$

[Perelstein, Weiler JHEP]  
 [Han, Katz, Krohn, Reece JHEP]  
 [Bhattacharjee, Mandal, Nojiri JHEP]

stop mass terms in MSSM:

$$\mathcal{L} = (\tilde{t}_L^*, \tilde{t}_R^*) M^2 (\tilde{t}_L, \tilde{t}_R)^T$$

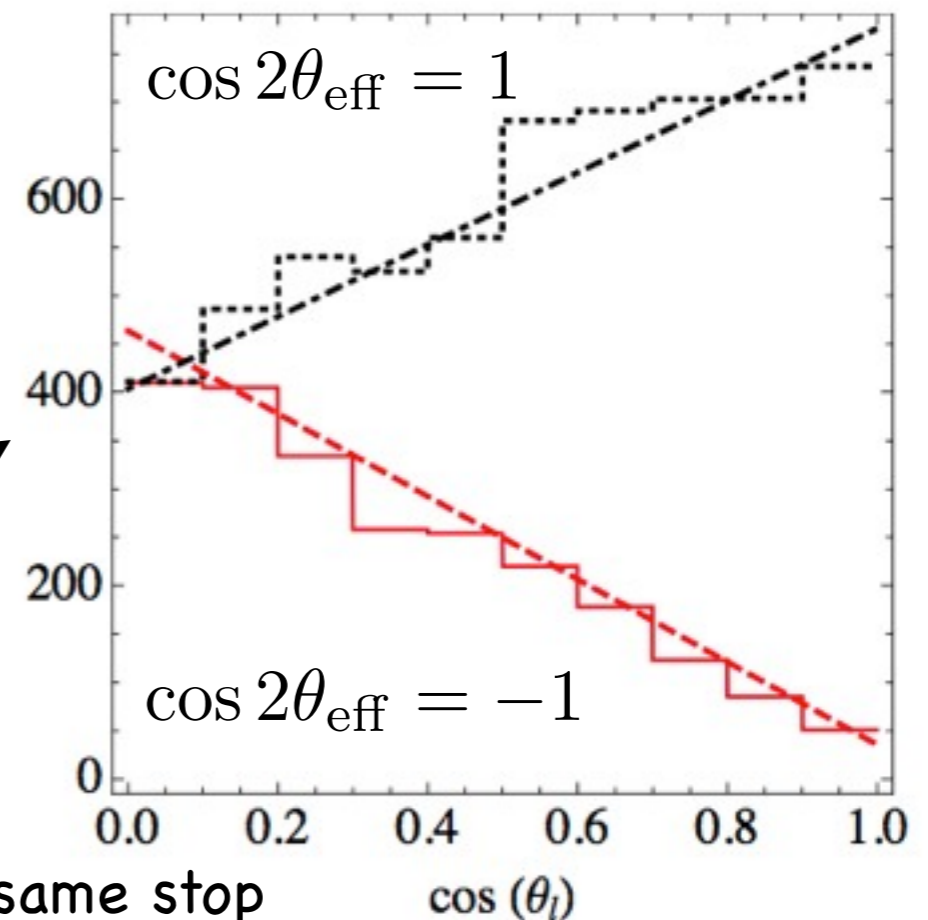
mass eigenstates

$$\begin{aligned} \tilde{t}_1 &= \cos \theta_t \tilde{t}_L + \sin \theta_t \tilde{t}_R, \\ \tilde{t}_2 &= -\sin \theta_t \tilde{t}_L + \cos \theta_t \tilde{t}_R, \end{aligned}$$

➔ resulting vertex:

$$g_{\text{eff}}^{ij} \tilde{t}_i \tilde{\chi}_j^0 (\cos \theta_{\text{eff}}^{ij} P_L + \sin \theta_{\text{eff}}^{ij} P_R) t$$

Maybe can be used to measure stop mixing angle, i.e. composition of mass eigenstates



angle between lepton and neutralino from same stop

# Top Quark mass

See talks by Brian and CP

The top quark mass is fundamental parameter of SM and input to electroweak precision measurements

**Problem:** the top quark mass is not an observable, unlike decay rates or cross sections, but is scheme and scale dependent quantity.

Measurement of mass of colored object by color neutral decay products inherently ambiguous  $\rightarrow$  Cannot be determined better than  $\mathcal{O}(\Lambda_{\text{QCD}})$

[Smith, Willenbrock PRL 79]

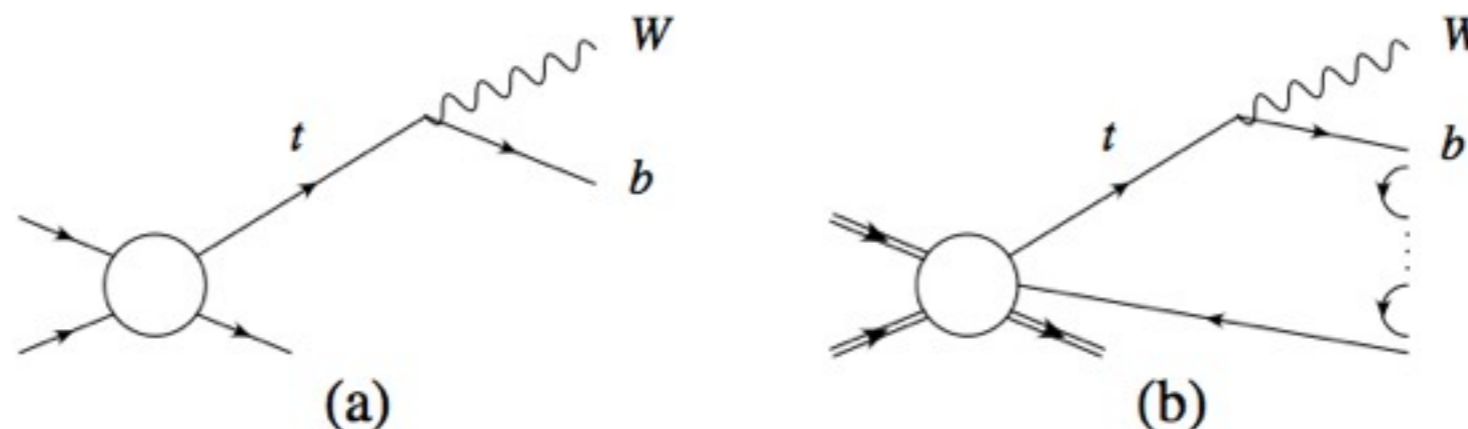
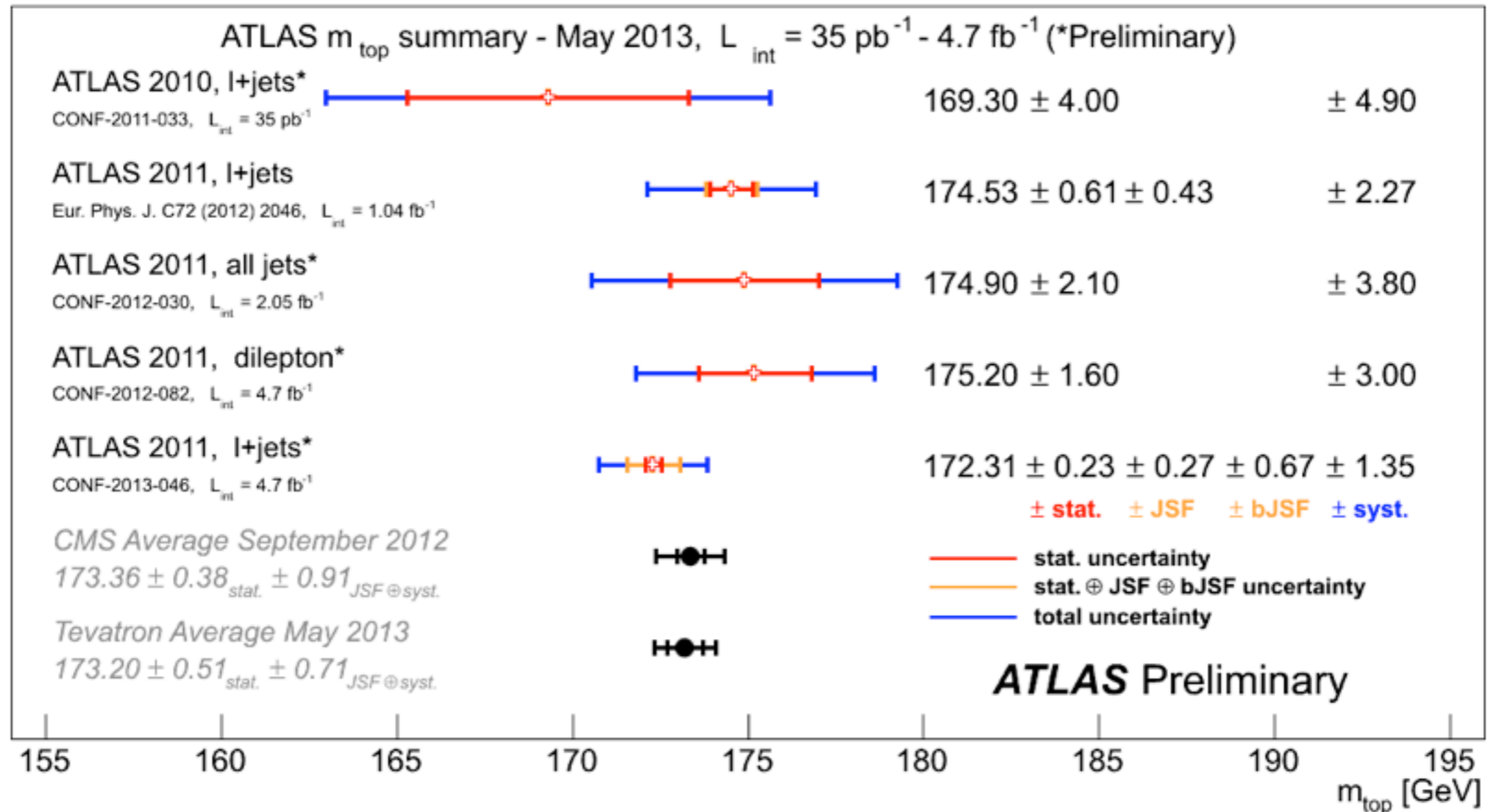


Figure 2: The production and decay of a top quark in (a) perturbation theory, and (b) nonperturbatively.

# top quark mass measurements



ATLAS and CMS combined top mass measurement:

$$m_{\text{top}} = 173.3 \pm 1.8 \text{ GeV} \quad [\text{CMS-PAS-TOP-12-001}]$$

Measured mass is the input parameter of the used Monte Carlo

# Top reconstruction/tagging

You cant measure what you cant detect

Top physics at LHC systematics limited, not statistics!



# Top reconstruction/tagging

You cant measure what you cant detect

## Leptonic top reconstruction

Using  $m_W^2 = (p_l + p_\nu)^2 = m_l^2 + 2(E_l E_\nu - \vec{p}_l \vec{p}_\nu)$  and  $E_i = \sqrt{m_i^2 + \vec{p}_i^2}$

with  $\vec{p}_i = (p_{T,i}, p_{Z,i})$  and  $m_l = 0$  one obtains

$$p_{Z,\nu} = \frac{\kappa p_{Z,l} \pm \sqrt{\vec{p}_l^2 (\kappa^2 - p_{T,l}^2 p_{T,\nu}^2)}}{p_{T,l}^2} \quad \text{with} \quad \kappa = \frac{m_W^2}{2} + \vec{p}_{T,l} \cdot \vec{p}_{T,\nu}$$

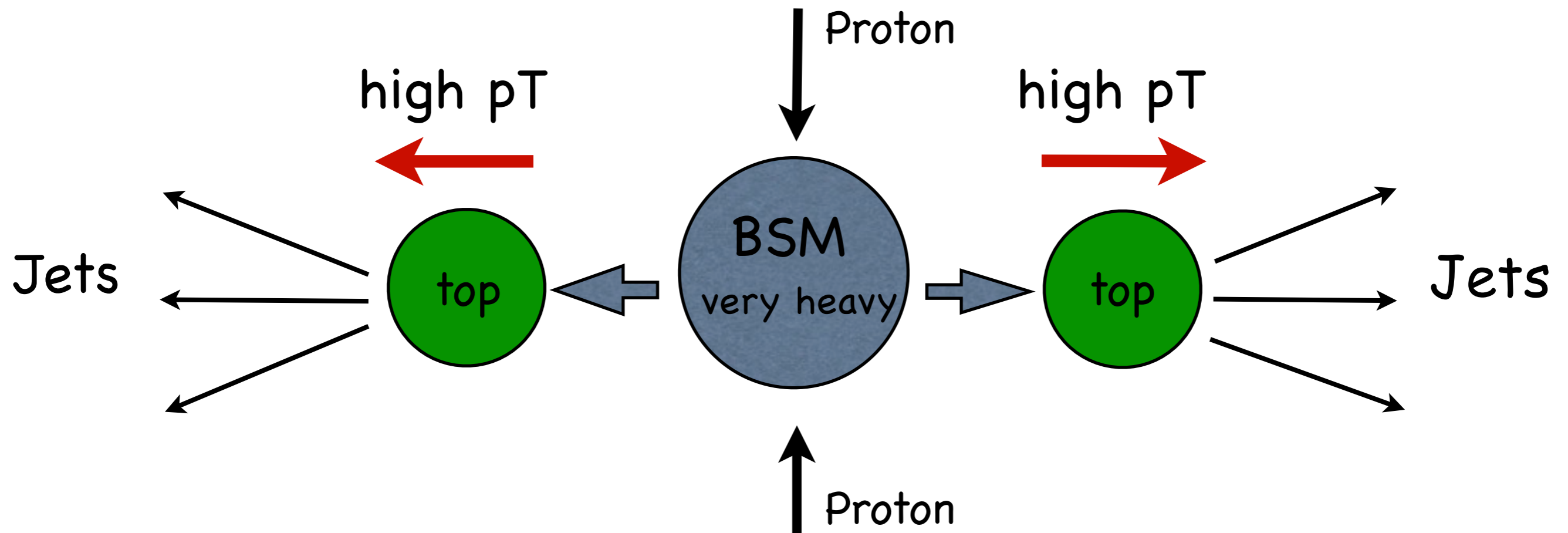
often the solution is chosen which yields the best  $m_t^2 = (p_b + p_l + p_\nu)^2$

## Hadronic top reconstruction

Often simple  $\chi^2$ -fit with  $m_W^2 = m_{j_1 j_2}^2$  and  $m_t^2 = m_{b, j_1, j_2}^2$

# Top reconstruction in boosted final states

In many scenarios where top quarks have to be measured they are produced with large transverse momentum



- Here jet substructure cannot be avoided
- Many reconstruction techniques have been proposed and compared

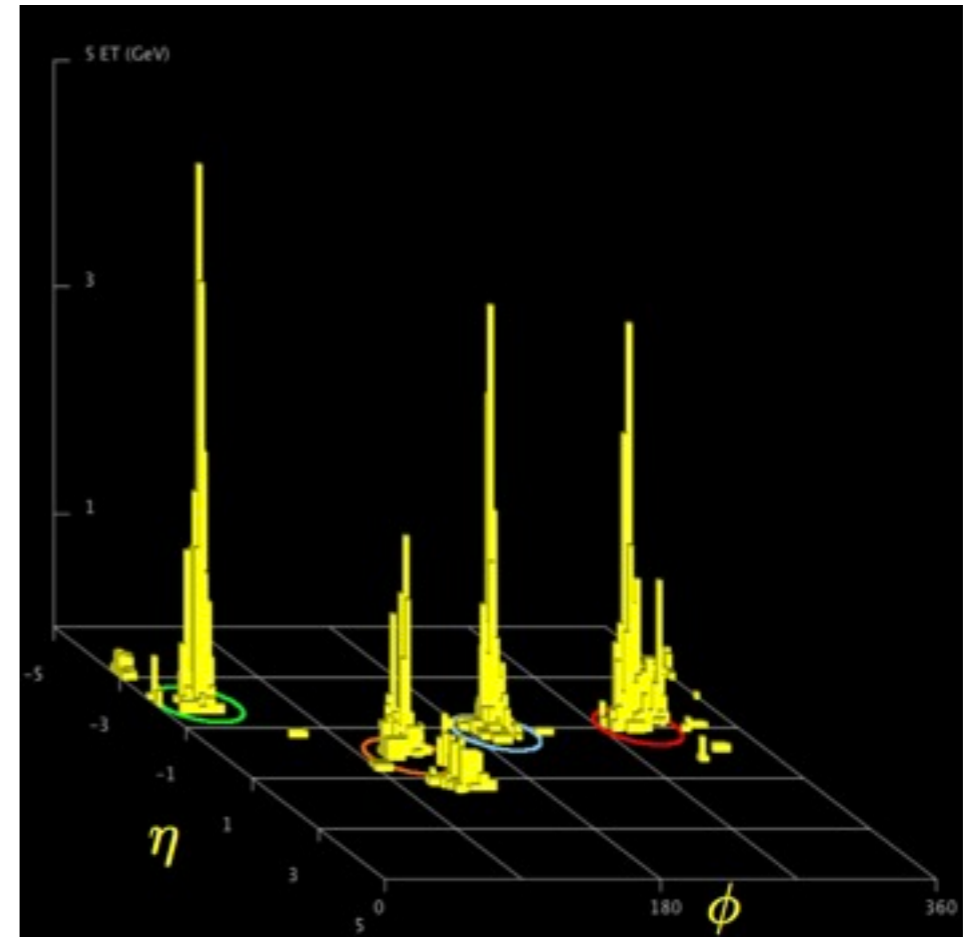
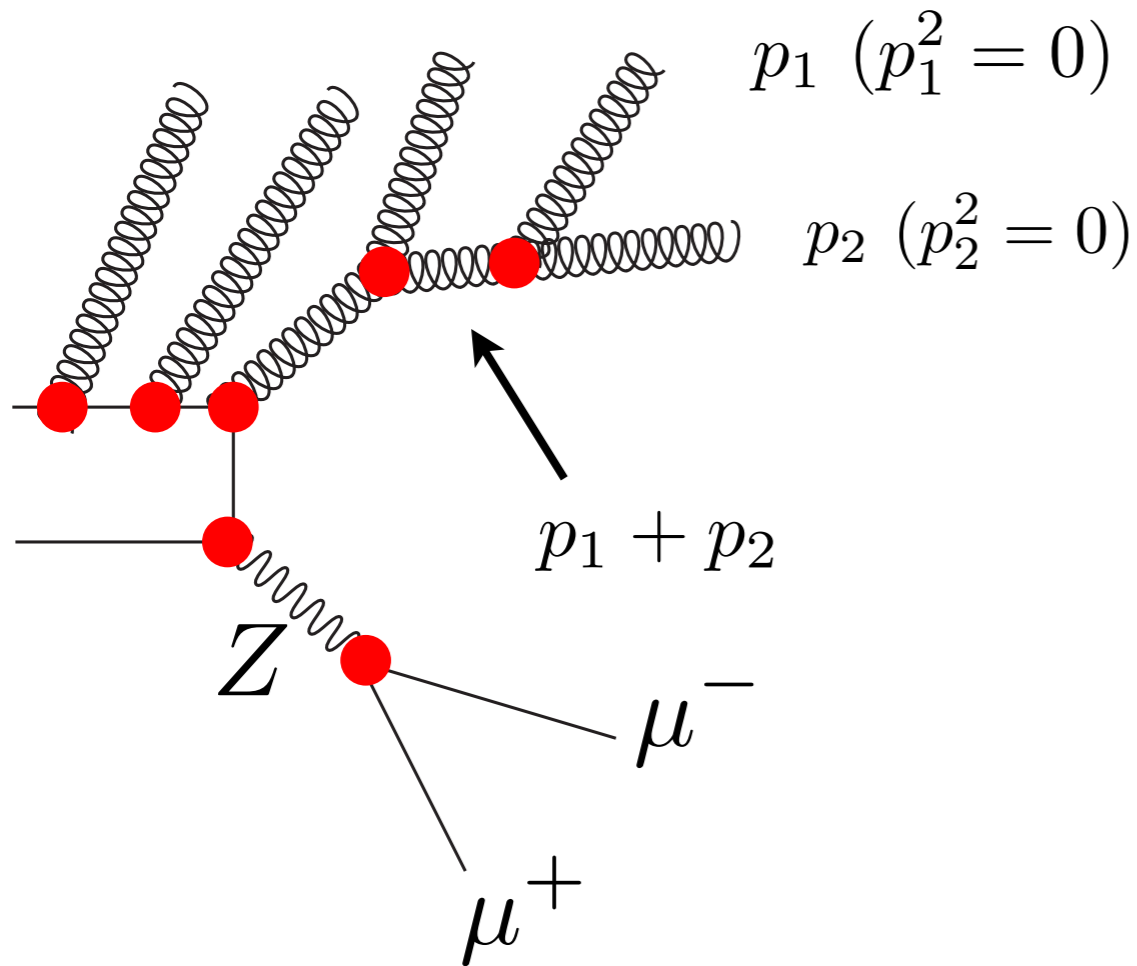


# A brief review of jet physics

## At the LHC many sources of radiation:

- Pileup  $\rightarrow$  Can add up to 100 GeV of soft radiation per unit rapidity  
[Cacciari, Salam, Sapeta JHEP 1004]
  - Underlying Event  $\rightarrow \langle \delta m_j^2 \rangle \simeq \Lambda_{\text{UE}} p_{T,j} \left( \frac{R^4}{4} + \frac{R^8}{4608} + \mathcal{O}(R^{12}) \right)$  with  $\Lambda_{\text{UE}} \sim \mathcal{O}(10)$  GeV  
[Dasgupta, Magnea, Salam JHEP 0802]
  - Initial state radiation (ISR)
  - Hard radiation from many resonances in event
- $\rightarrow$  Need methods to separate final state radiation (FSR) from rest of event

# Jets are collimated sprays of hadrons



Probability enhanced in soft and collinear region due to  $\sim 1/(p_1 + p_2)^2$

- If  $p_1 \rightarrow 0$ , then  $1/(p_1 + p_2)^2 \rightarrow \infty$
- If  $p_2 \rightarrow 0$ , then  $1/(p_1 + p_2)^2 \rightarrow \infty$
- If  $p_2 \rightarrow \lambda p_1$ , then  $1/(p_1 + p_2)^2 \rightarrow \infty$

For more detail see also talk by Brian, CP or Dave Soper at CTEQ summer school

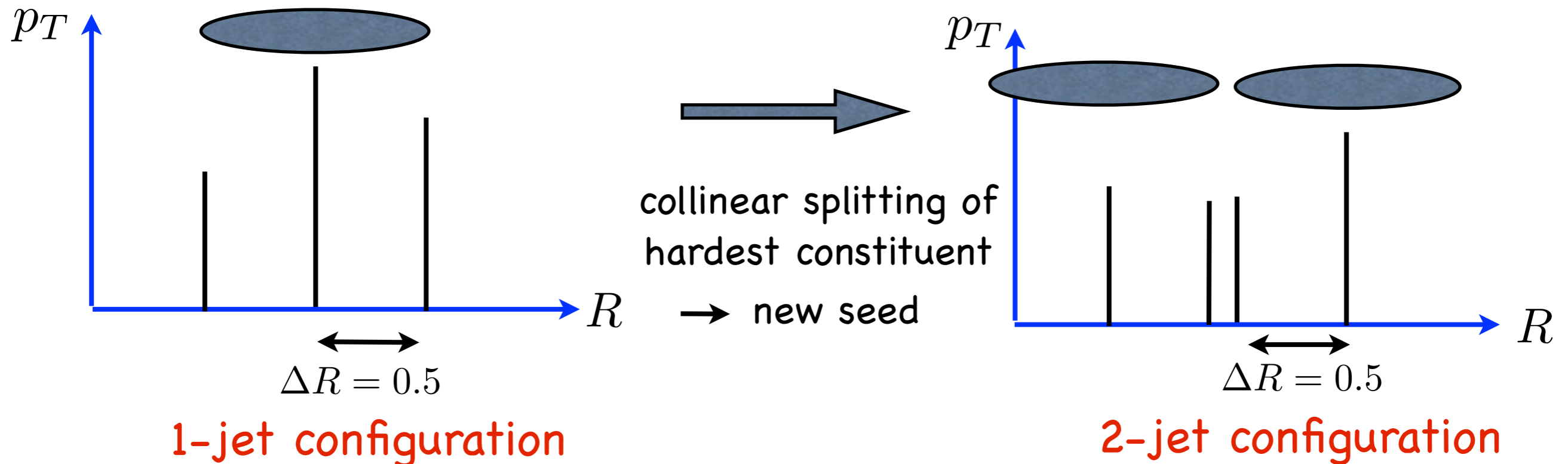
## IR safe definition of jets:

Observables must be insensitive to modification of final state with respect to soft and/or collinear splitting

Seeded cone algorithms are infrared unsafe!

Example: Take the hardest constituent of event as seed for jet cone

Assume 3 constituents in event with cone size  $R=0.5$



- Sequential recombination, e.g. inclusive kT algorithm

[S.D. Ellis & Soper, '93]  
 [Catani, Dokshitzer,  
 Seymour Webber '93]

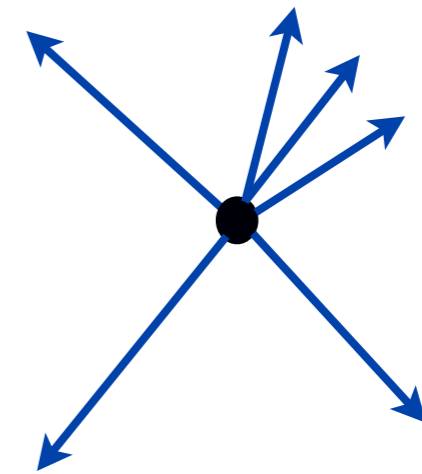
Distance measure

$$d_{ij} = \min(p_{Ti}^2, p_{Tj}^2) \frac{\Delta R_{ij}^2}{R^2}$$

$$d_{iB} = p_{Ti}^2$$

$$\Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

1. Find smallest of  $d_{ij}$   $d_{iB}$
2. if  $ij$  recombine them
3. if  $iB$  call  $i$  a jet and remove from list of particles
4. repeat from 1. until no particles left



Minimum distance between jets is R

Only number of jets above pt cut is IR safe

Cambridge/Aachen alg. - distance measure:  $d_{ij} = \frac{\Delta R_{ij}^2}{R^2}$   $d_{iB} = 1$

anti-kT alg. - distance measure:  $d_{ij} = \min(p_{Ti}^{-2}, p_{Tj}^{-2}) \frac{\Delta R_{ij}^2}{R^2}$   $d_{iB} = p_{Ti}^{-2}$

- Sequential recombination, e.g. inclusive kT algorithm

[S.D. Ellis & Soper, '93]  
[Catani, Dokshitzer, Seymour Webber '93]

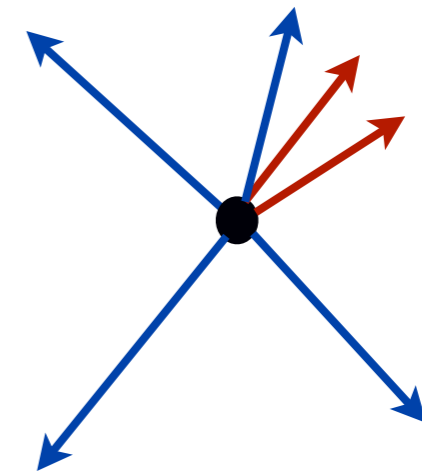
Distance  
measure

$$d_{ij} = \min(p_{Ti}^2, p_{Tj}^2) \frac{\Delta R_{ij}^2}{R^2}$$

$$d_{iB} = p_{Ti}^2$$

$$\Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

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- Sequential recombination, e.g. inclusive kT algorithm

[S.D. Ellis & Soper, '93]  
[Catani, Dokshitzer, Seymour Webber '93]

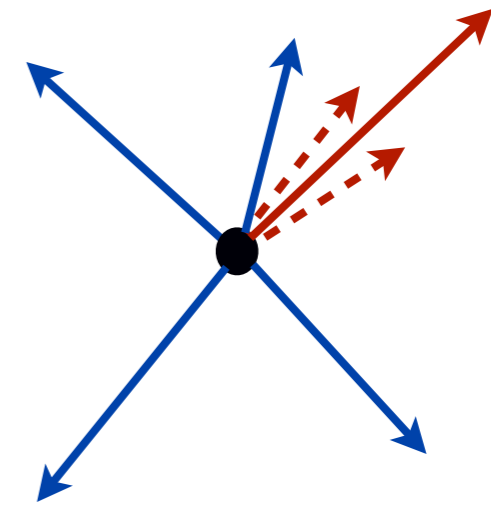
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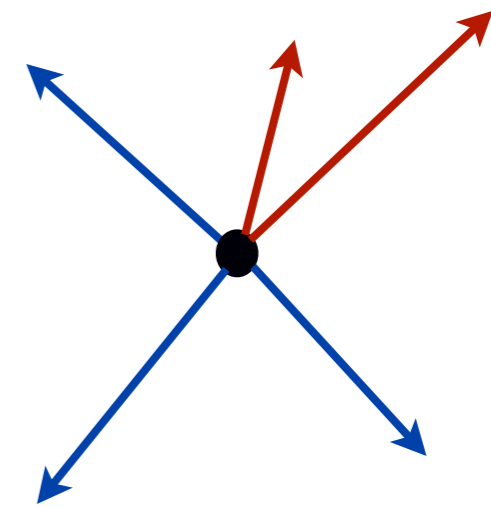
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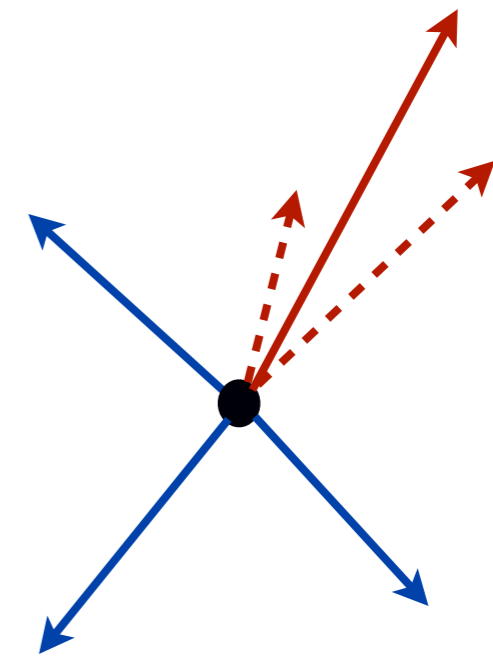
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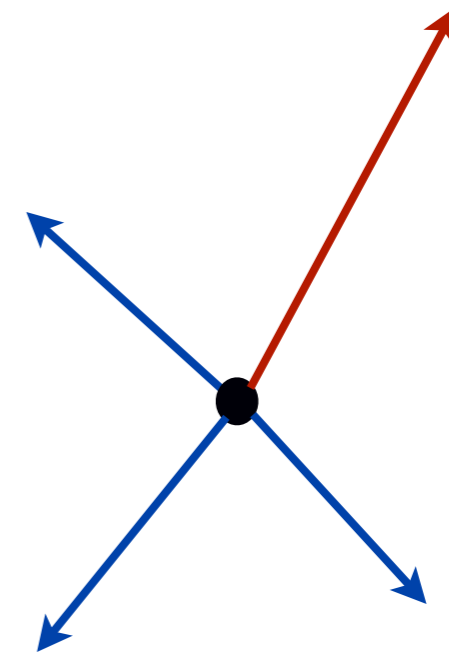
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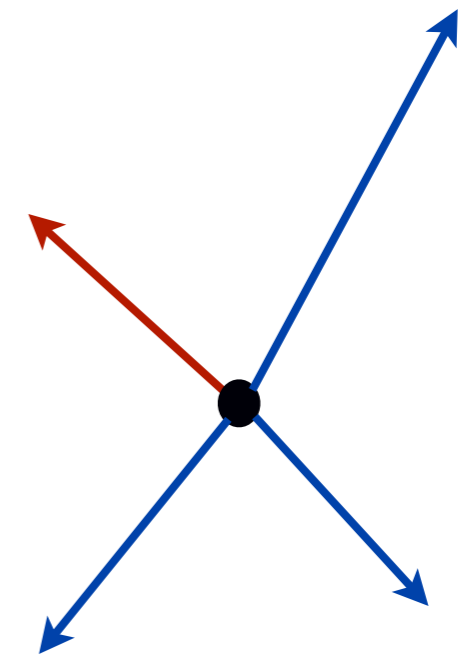
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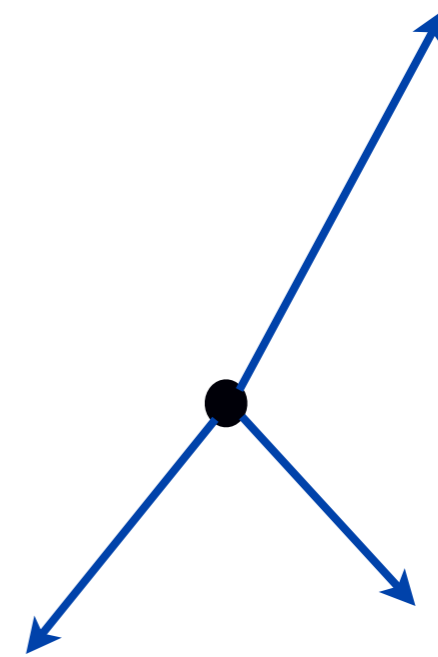
[S.D. Ellis & Soper, '93]  
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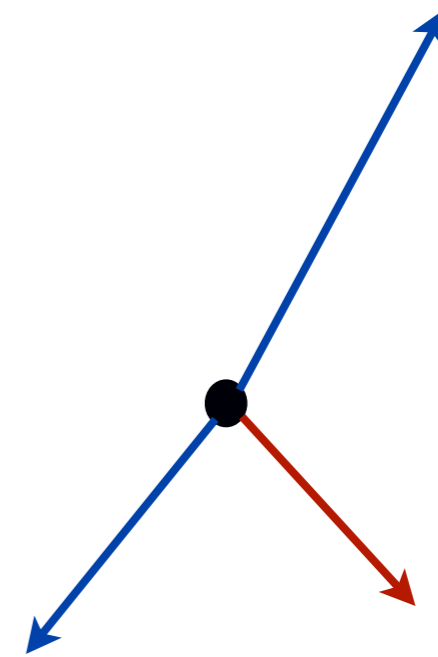
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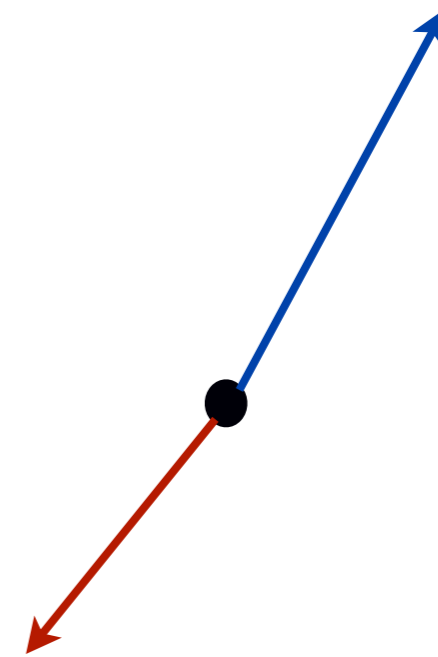
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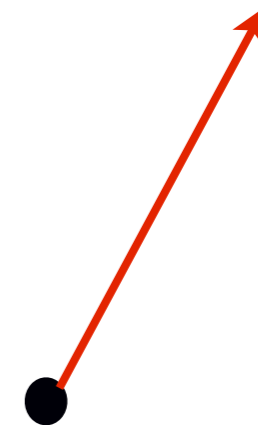
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Found 4 Jets

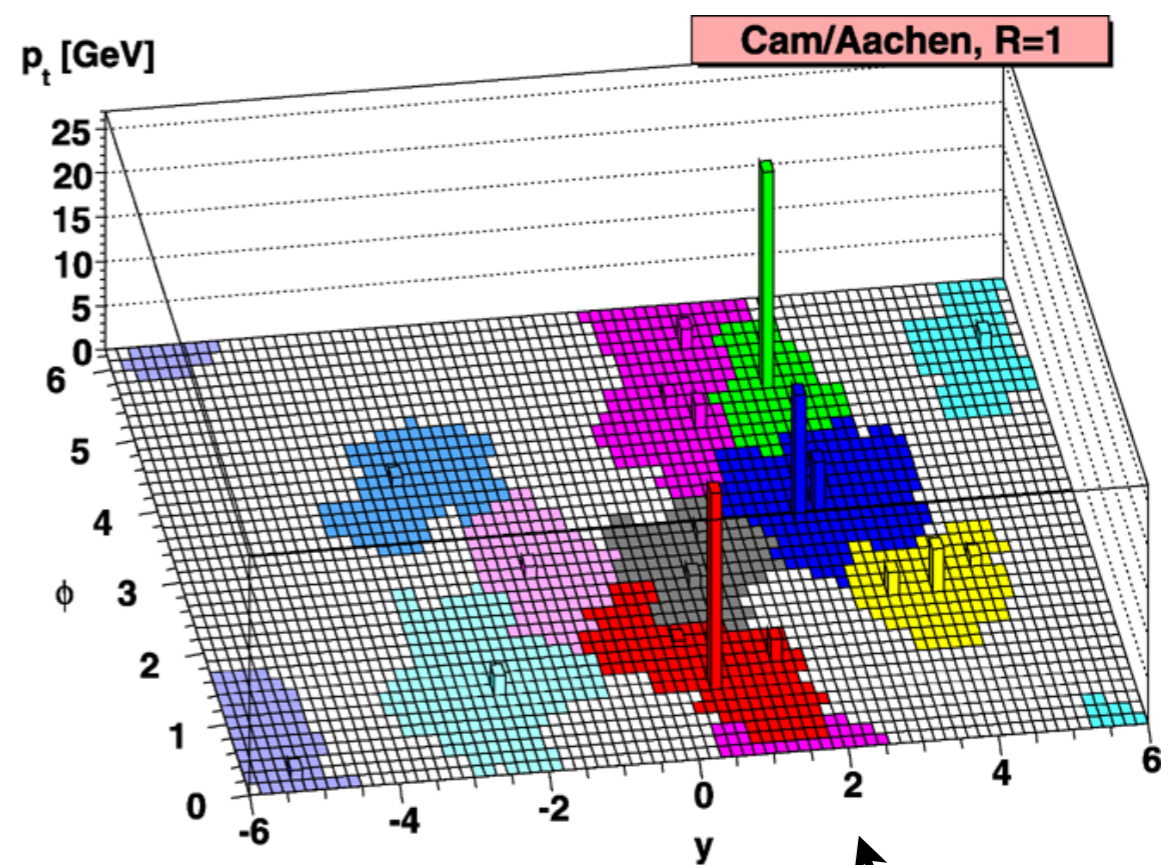
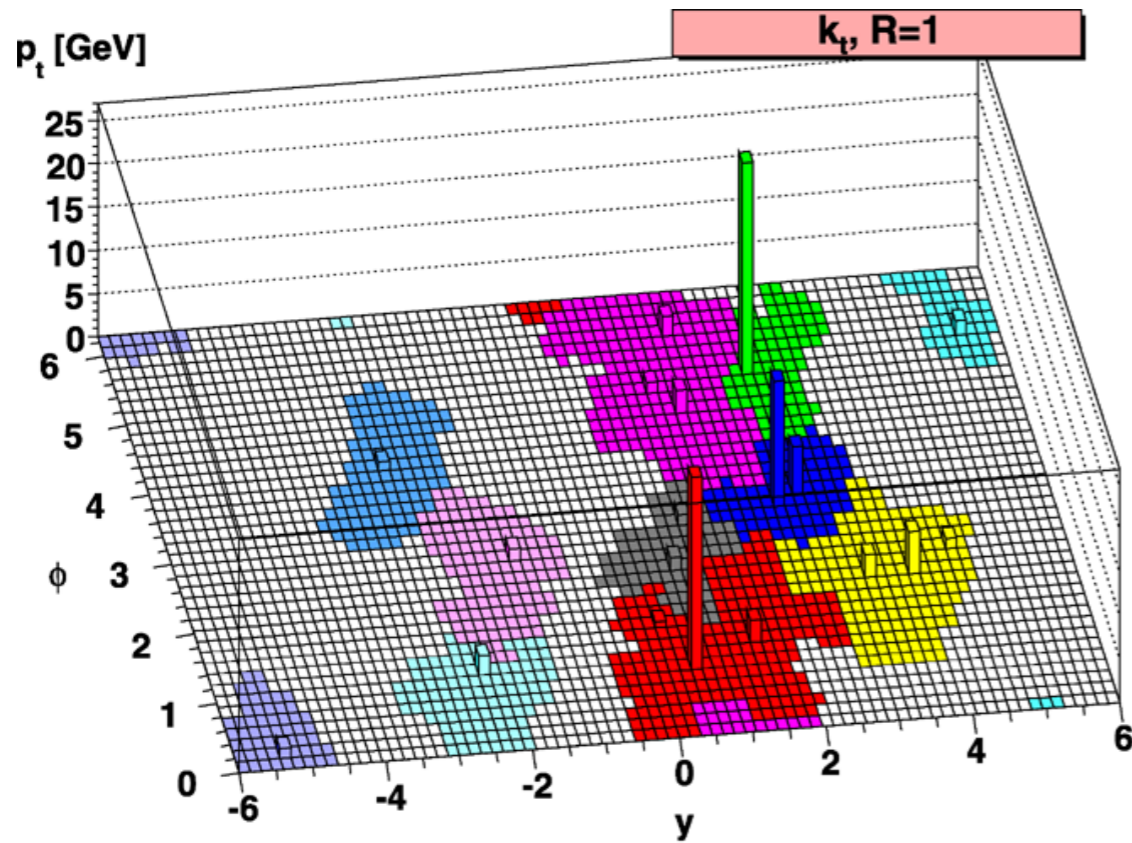
Minimum distance between  
 jets is  $R$

Only number of jets above  $p_t$   
 cut is IR safe

Cambridge/Aachen alg. - distance measure:  $d_{ij} = \frac{\Delta R_{ij}^2}{R^2}$   $d_{iB} = 1$

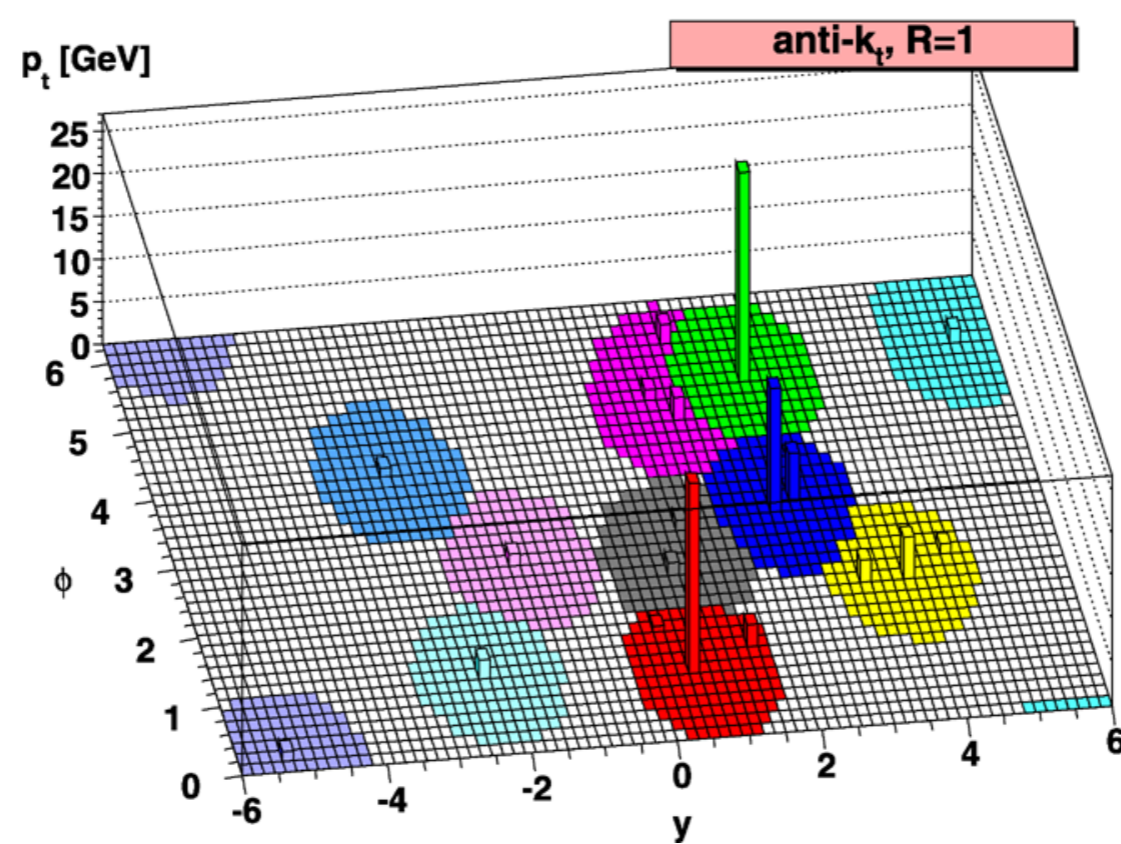
anti-kT alg. - distance measure:  $d_{ij} = \min(p_{Ti}^{-2}, p_{Tj}^{-2}) \frac{\Delta R_{ij}^2}{R^2}$   $d_{iB} = p_{Ti}^{-2}$

[G. Salam, Towards Jetography]



soft jet  
more  
circular

shape independent  
of jet pT



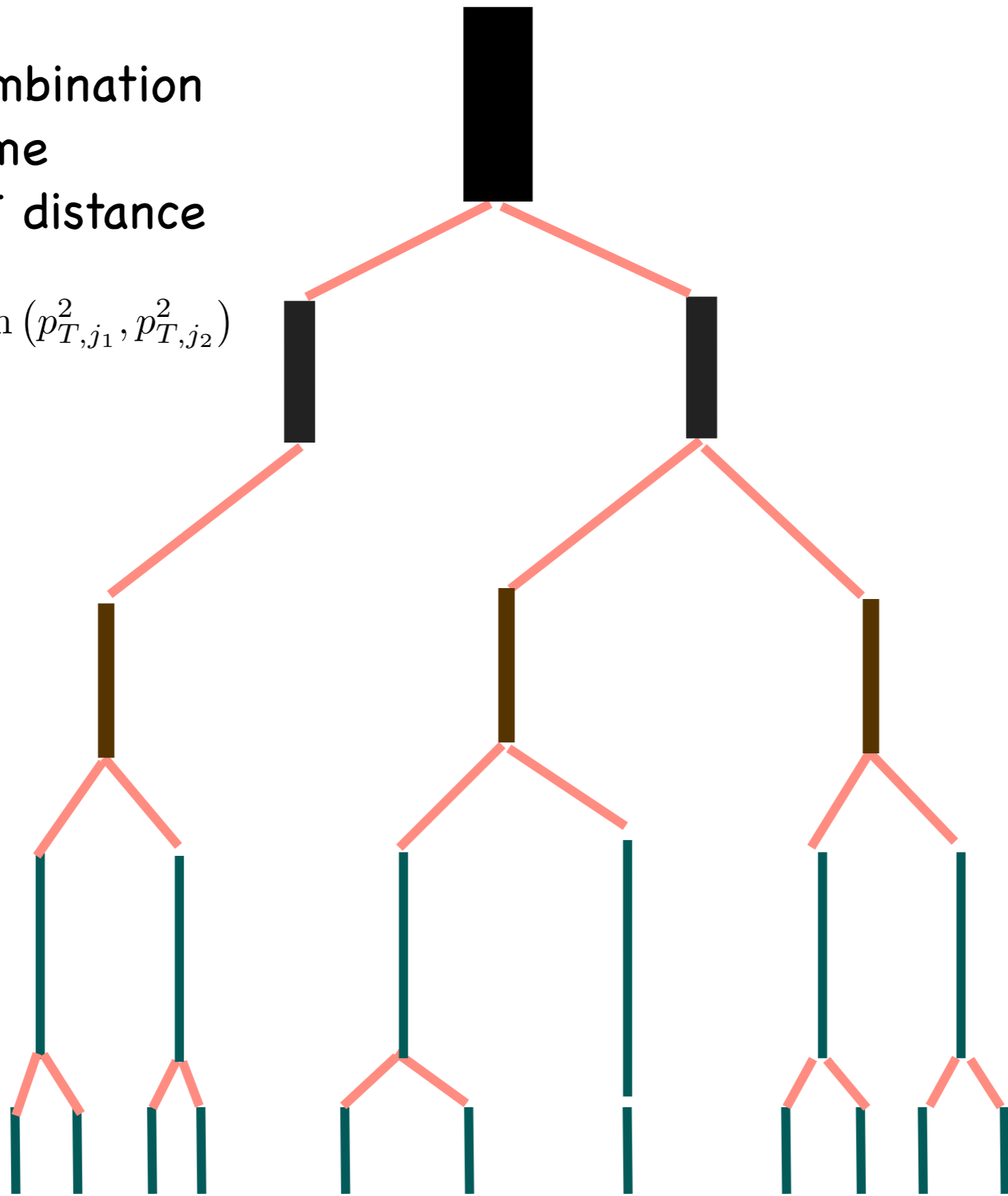
hard jet  
more  
circular



order of recombination  
defined by some  
metric, e.g. kT distance

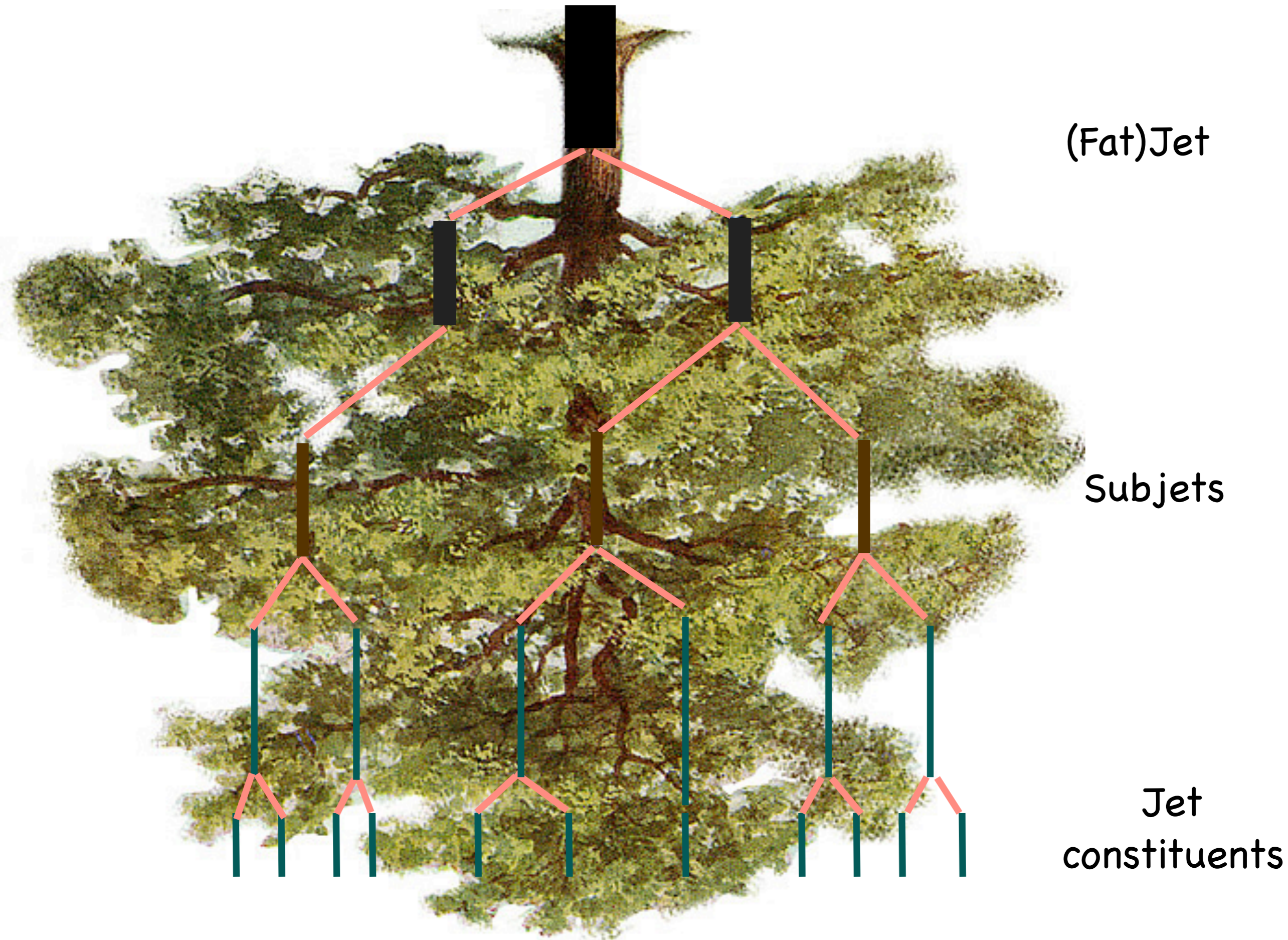
$$d_{j_1 j_2} = \frac{\Delta R_{j_1 j_2}^2}{D^2} \min(p_{T,j_1}^2, p_{T,j_2}^2)$$

(Fat)Jet



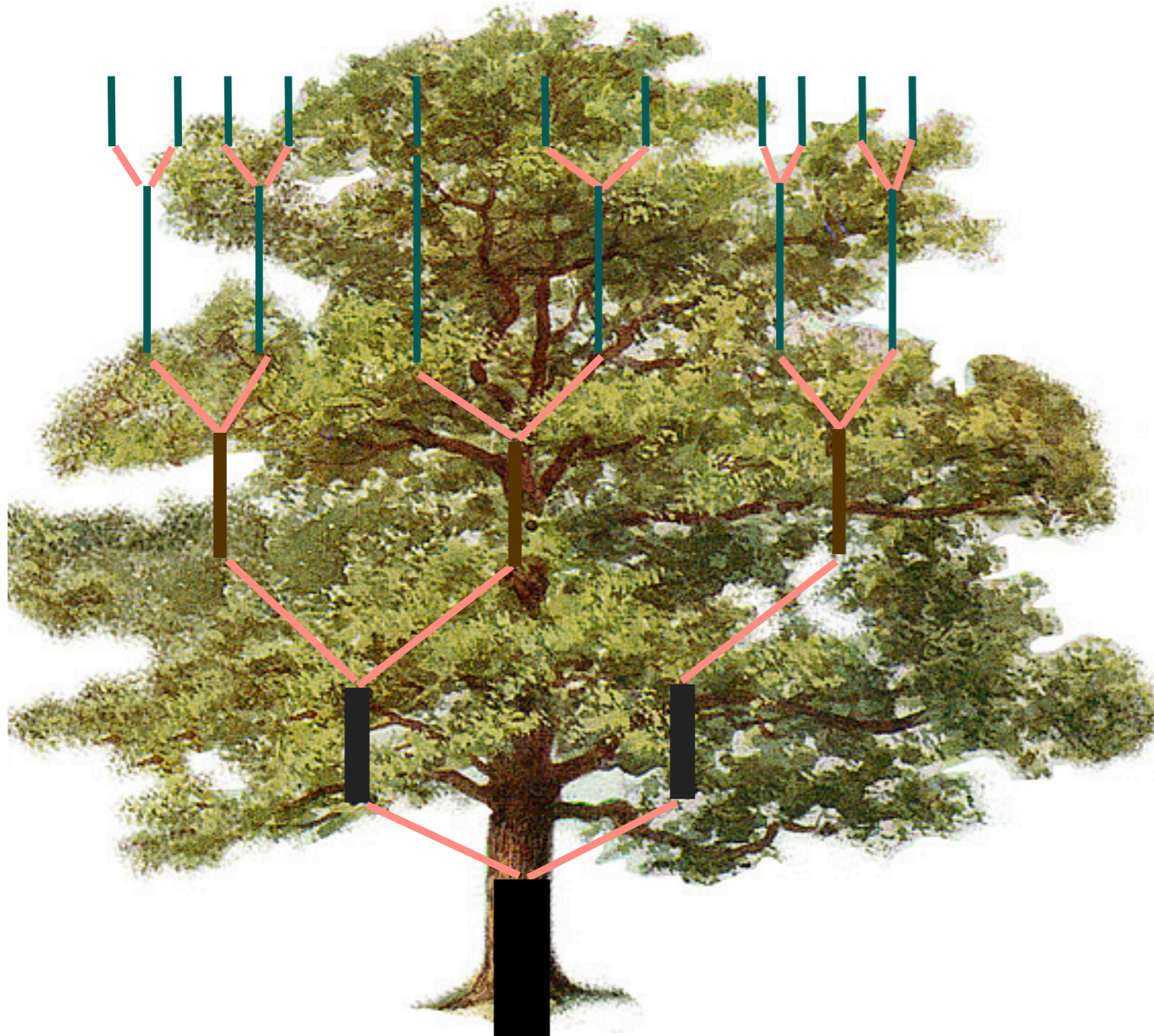
Subjets

Jet  
constituents



For jet substructure study reverse cluster history and analyze internal structure

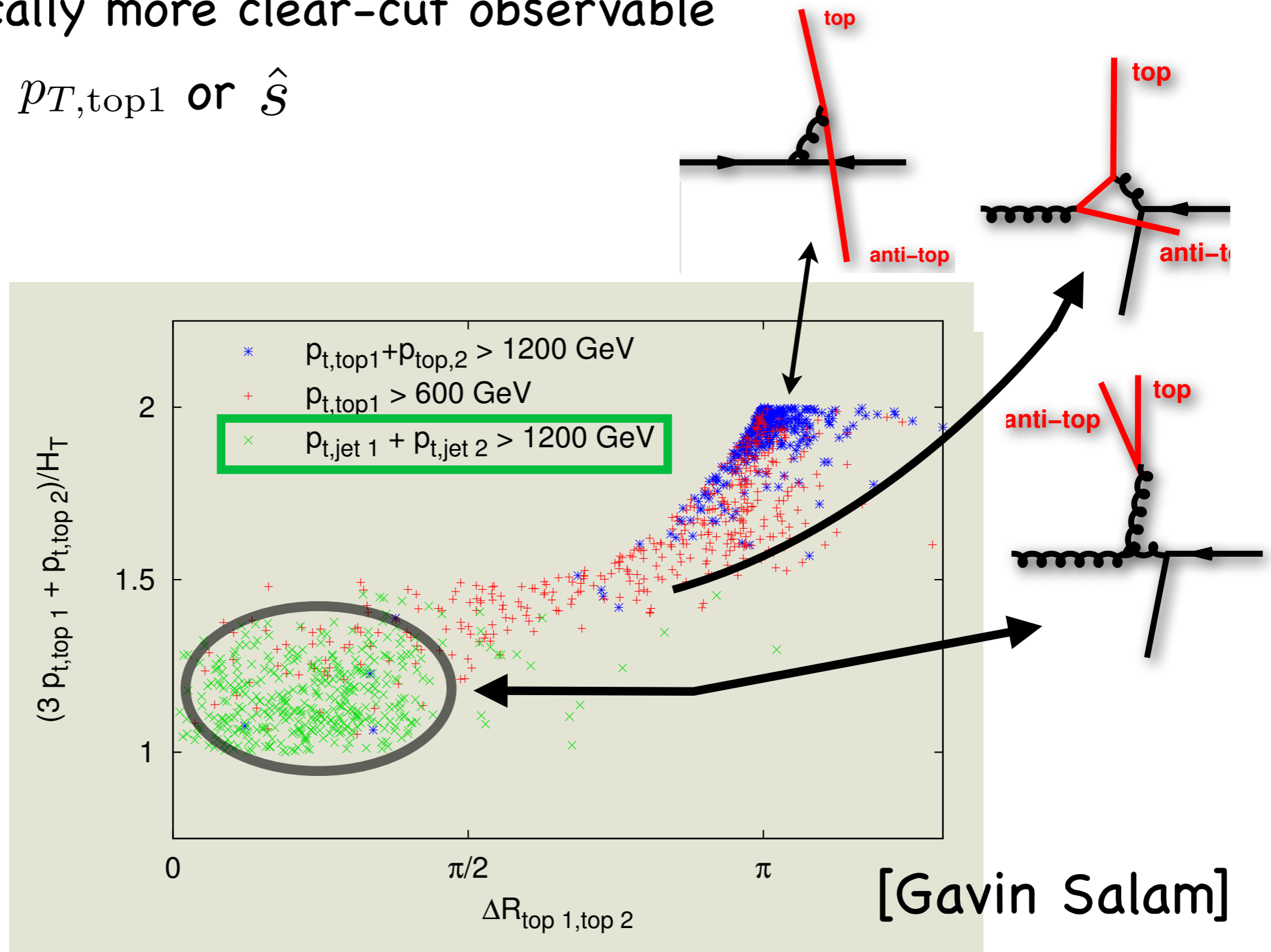
W-boson jet



QCD jet



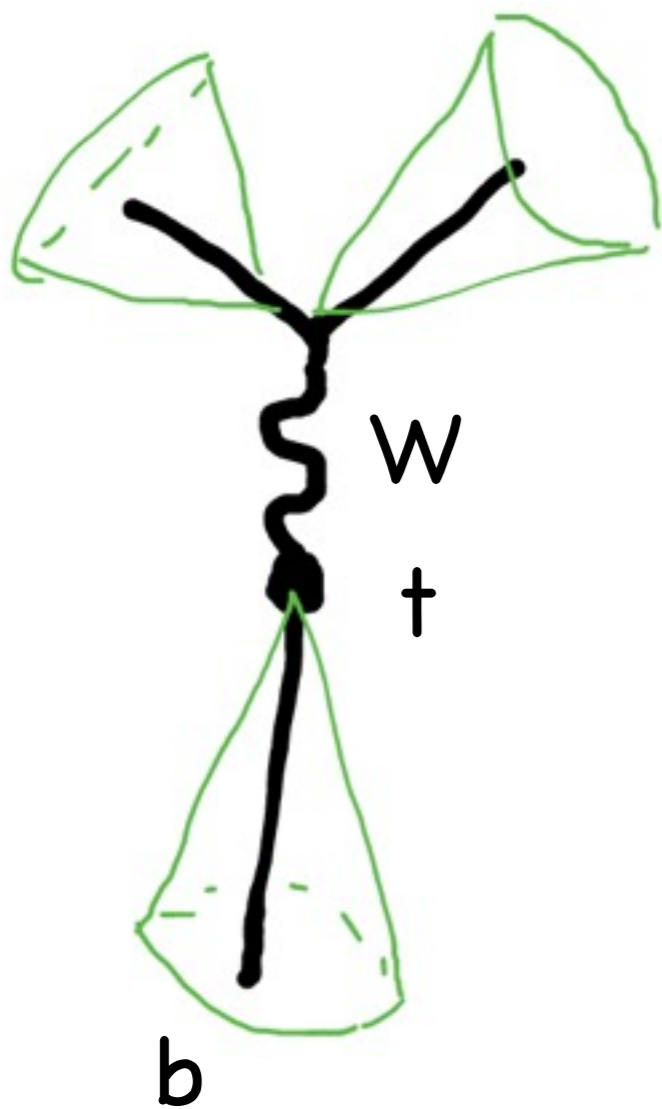
Will choose  $m_{t\bar{t}}$  in following for classification  
 kinematically more clear-cut observable  
 than say  $p_{T,\text{top}1}$  or  $\hat{s}$



# Different scenarios based on pT vs mass

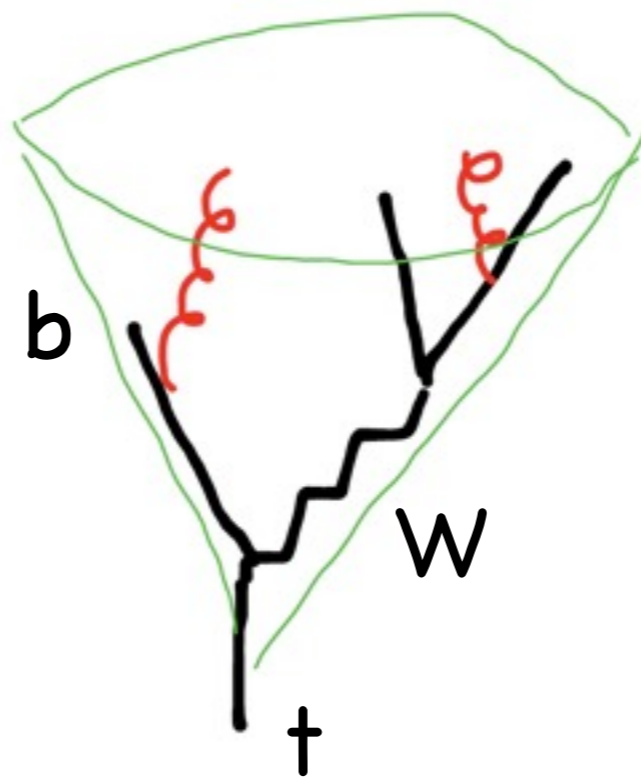
Scenario 1

$$m_{t\bar{t}} \simeq 2 m_t$$



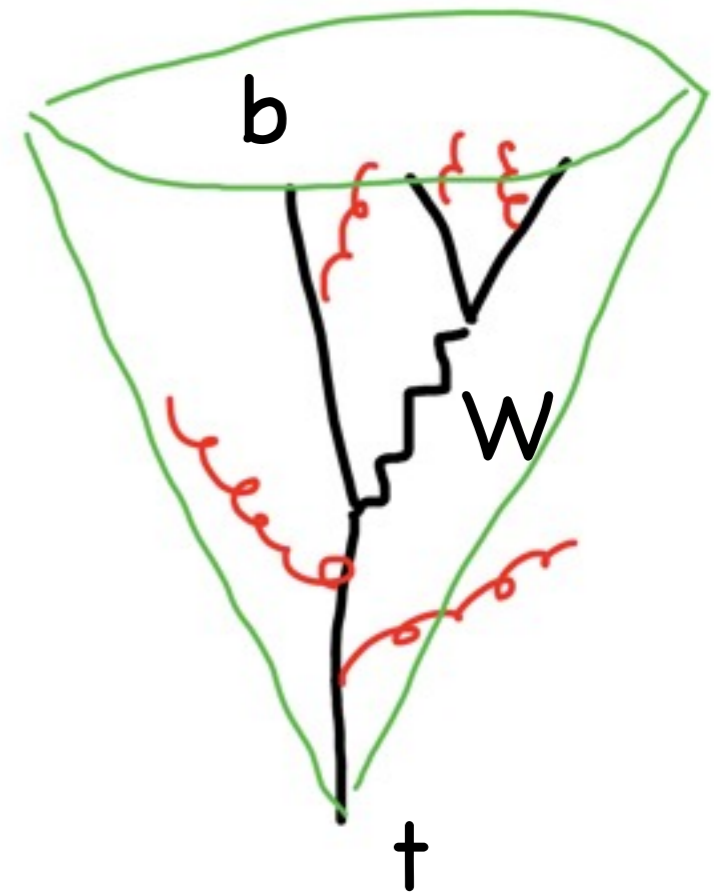
Scenario 2

$$m_{t\bar{t}} > 2 m_t$$



Scenario 3

$$m_{t\bar{t}} \gg 2 m_t$$



# Leptonic top reconstruction in boosted final states

Due to reconstruction of invariant masses in boosted and unboosted case very similar:

$$m_t^2 = (p_b + p_l + p_\nu)^2 \quad \text{and} \quad m_W^2 = (p_l + p_\nu)^2$$

However, for large boost lepton isolation a problem.

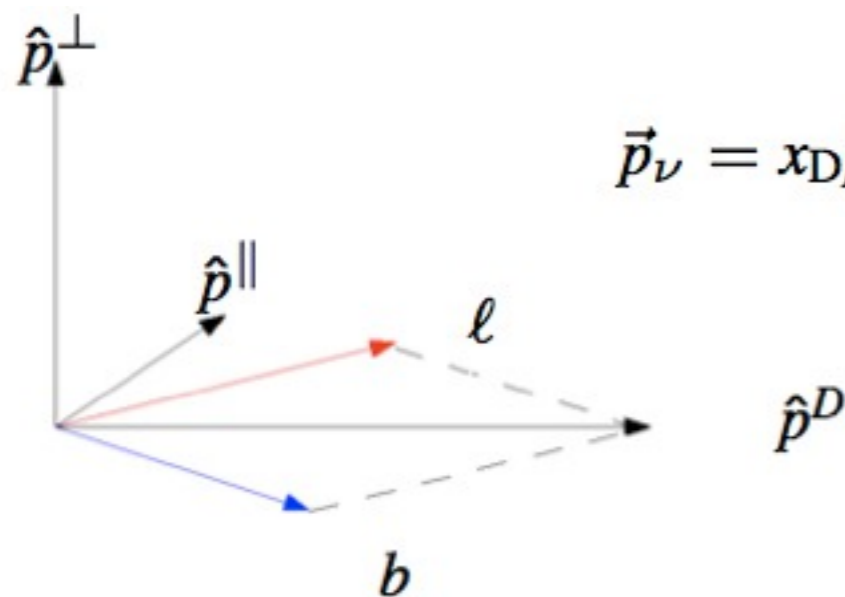
Define mini-isolation criterium

[Rehermann, Tweedie JHEP]

$$R_{iso} = \frac{15 \text{ GeV}}{p_{T\mu}} \simeq \frac{3m_B}{p_{T\mu}}$$

In boosted final states it is even possible to “guess” the full neutrino momentum

[Plehn, MS, Takeuchi JHEP]



$$\vec{p}_\nu = x_D \hat{p}^D + x_{\parallel} \hat{p}^{\parallel} + x_{\perp} \hat{p}^{\perp}$$

2 assumptions:

$$x_{\parallel} = 0 \quad \text{or} \quad x_{\perp} = 0$$

↕  
good top momentum reconstruction

# Hadronic top reconstruction: Many approaches

<u>top taggers:</u>		
	$\gamma$ -splitter Top Tagger	[Butterworth, Cox, Forshaw PRD 55 (2002)] [Broijmans ATL-COM-PHYS-2008-001]
	energy flow	[Thaler, Wang JHEP 0807]
	Johns Hopkins Tagger	[Kaplan, et al. PRL 101 (2008)]
	Pruning	[Ellis, Vermilion, Walsh PRD 80 (2009)]
	HEP Top Tagger	[Plehn, MS, Takeushi, Zerwas JHEP 1010]
	tree-less approach	[Jankowiak, Larkoski JHEP 1106]
	Template method	[Almeida et al. PRD 82 (2010)]
	N-subjettiness	[Kim PRD 83 (2011)] [Thaler, Van Tilburg JHEP 1103]
	Shower deconstruction	[Soper, MS PRD 84; PRD 87]
	Qjets	[Ellis, Hornig, Roy, Krohn, Schwartz PRL 108]

Tagger important to purify final state  
-> bridge gap between parton and hadron level

## Comparison of taggers in BOOST proceedings:

### Taggers compared:

- ▶ ATLAS
- ▶ CMS
- ▶ HEP
- ▶ JH
- ▶ NSubjettiness
- ▶ Pruning-Tagger
- ▶ Thaler/Wang Tagger
- ▶ Trimming-Tagger

### Samples used:

fully hadronic tt vs dijet events  
in pT slices of 100 GeV

- ▶ Herwig 6.5
- ▶ Herwig++
- ▶ Sherpa incl. matching

### Event selection cuts:

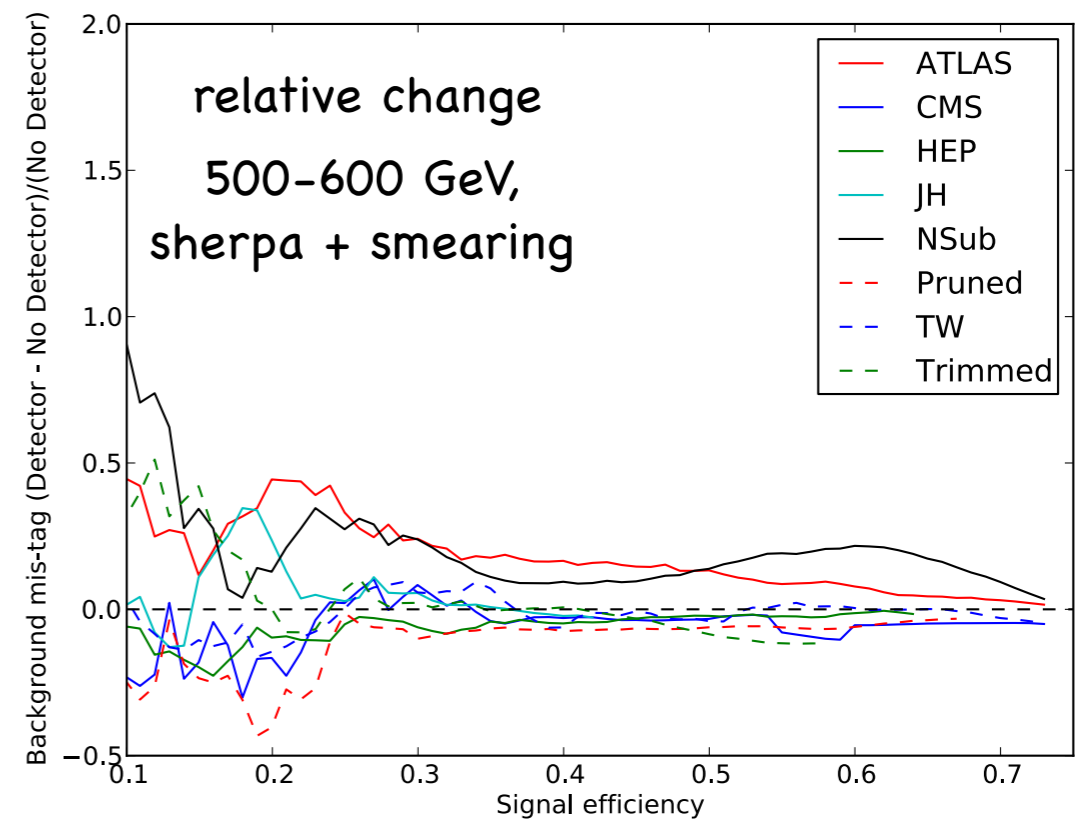
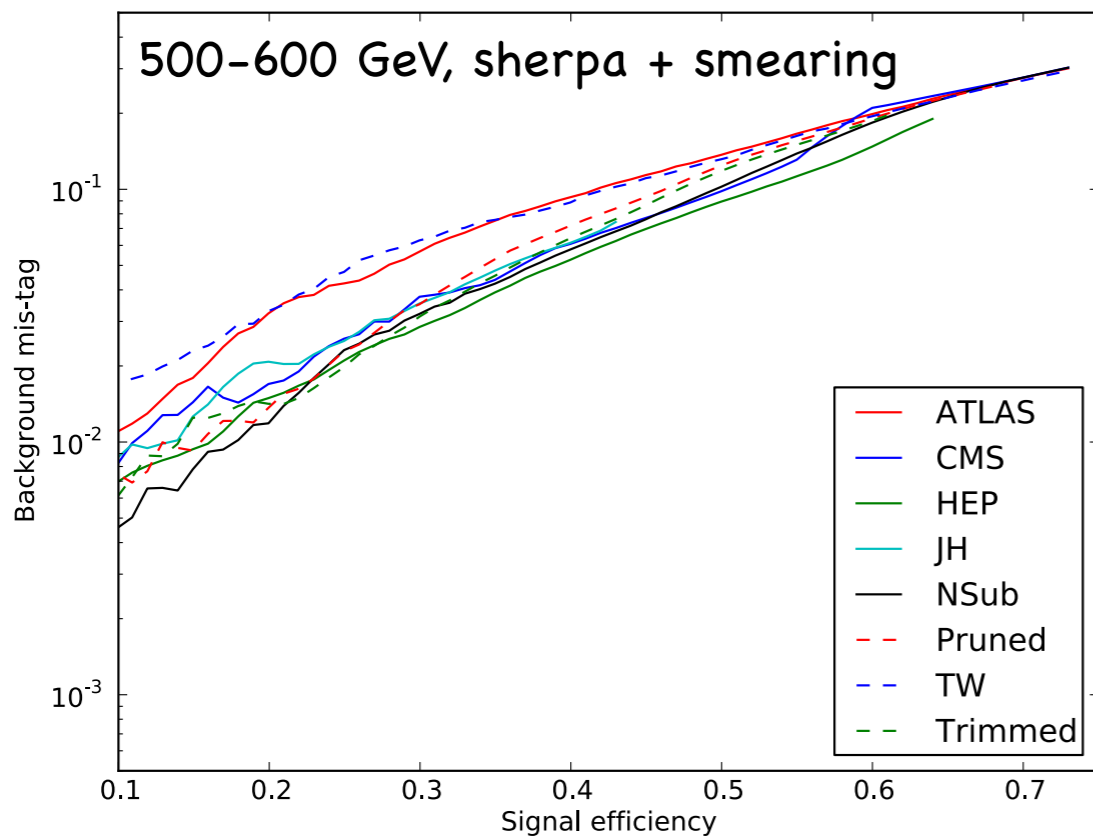
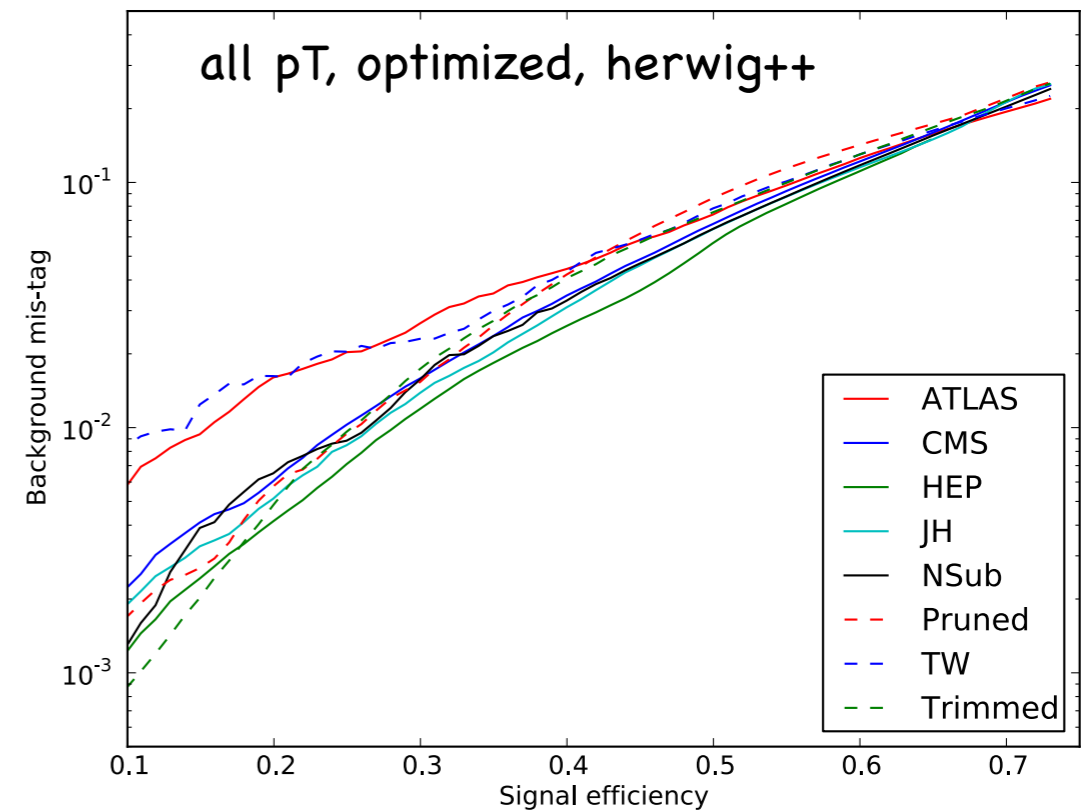
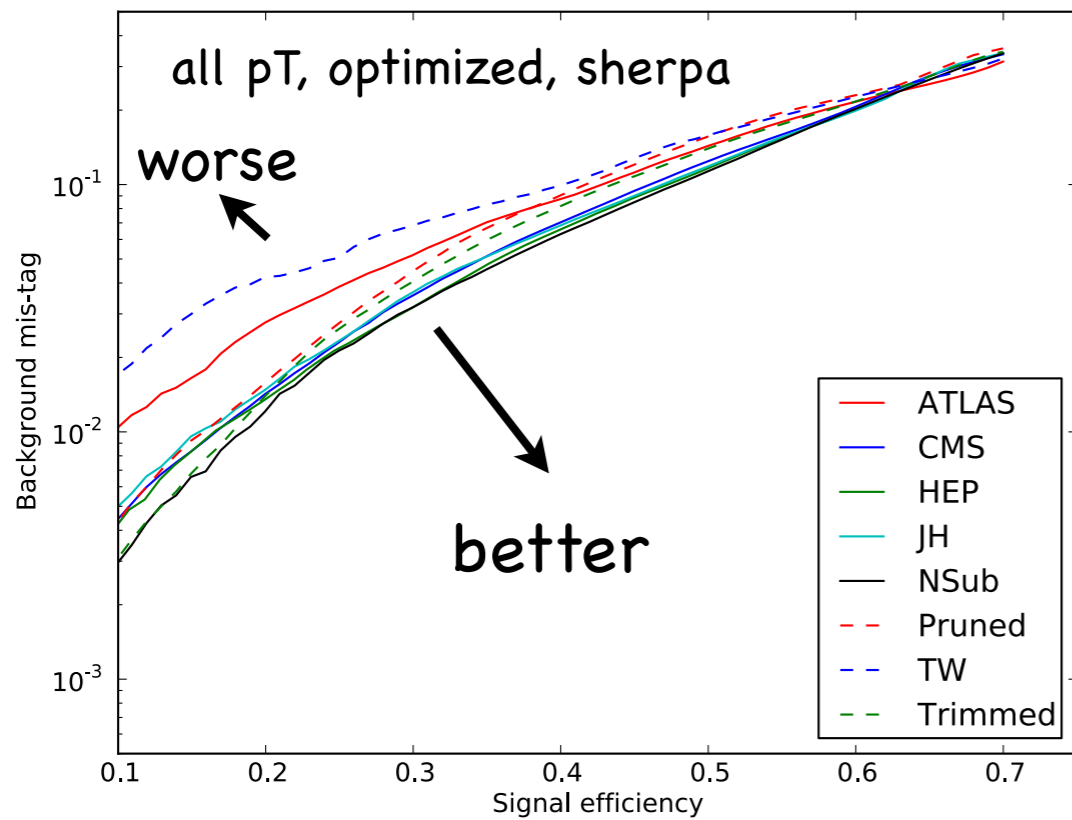
anti-kT jets with  $R=1.0$ ,  $p_T > 200$  GeV

### Efficiency:

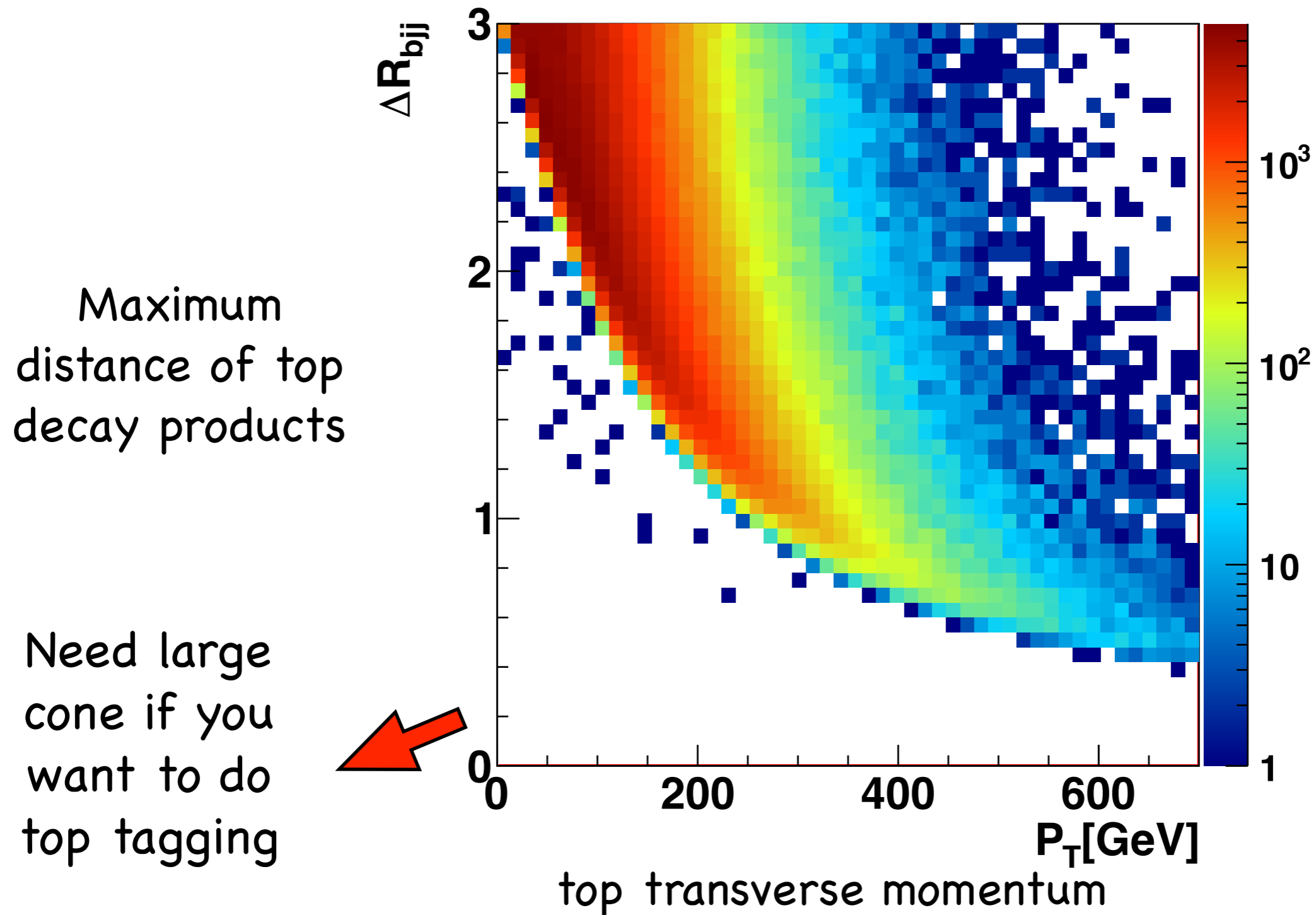
# tagged jets / # jets after selection cuts



# Comparison of top taggers (BOOST 2012 proceedings)



# Angular separation of boosted top's decay products in 14 TeV ttbar samples



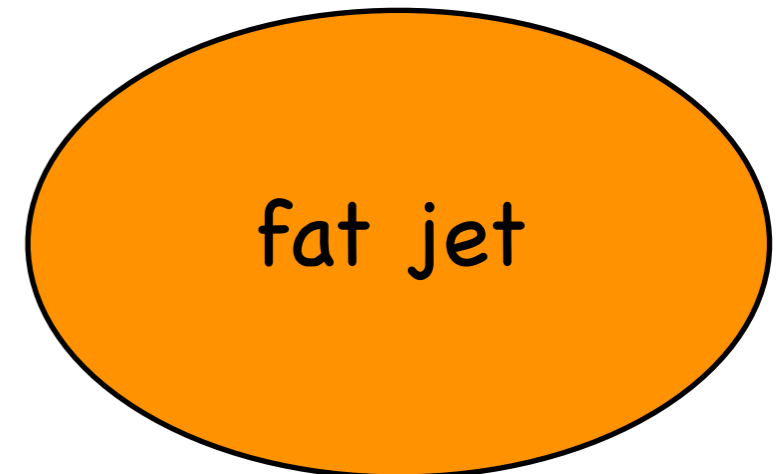
# How does the HEPTopTagger work?

[Plehn, Salam, MS, Takeuchi]

I. Find fat jets (C/A,  $R=1.5$ ,  $p_T > 200$  GeV)

II. Find hard substructure using mass drop criterion

Undo clustering,  $m_{\text{daughter}_1} < 0.8 m_{\text{mother}}$  to keep both daughters

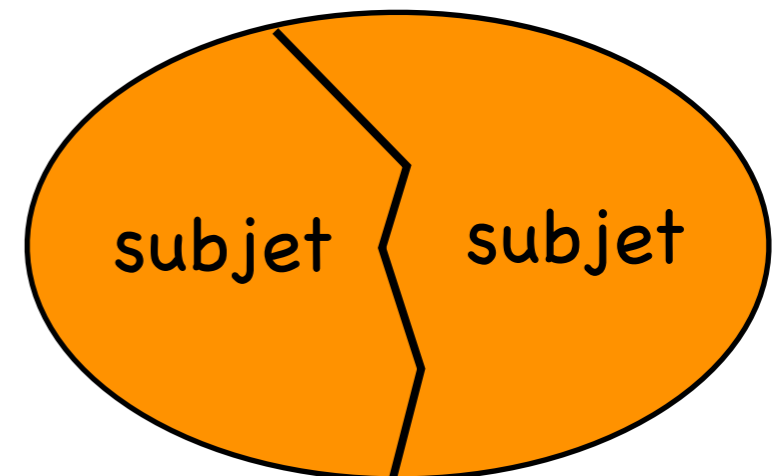


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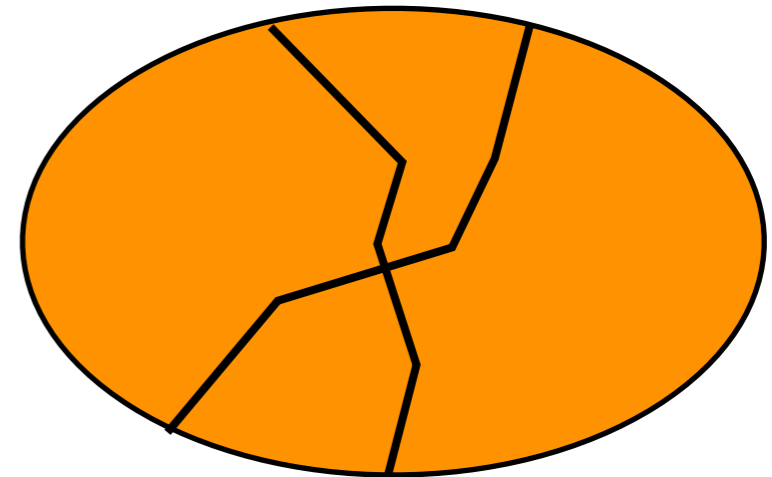


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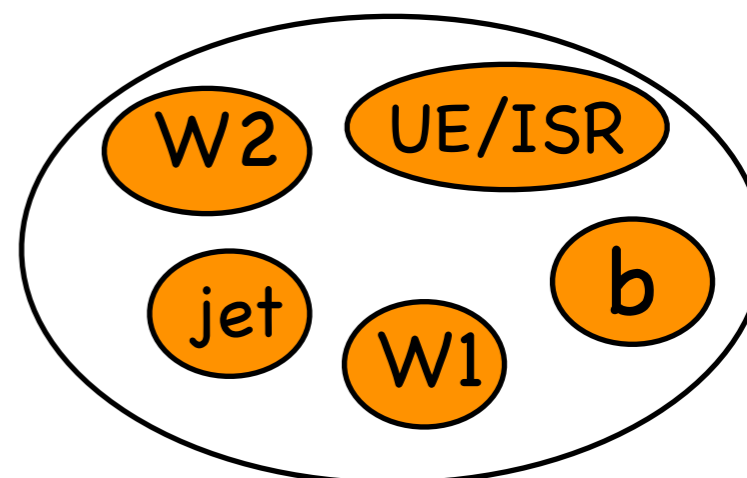
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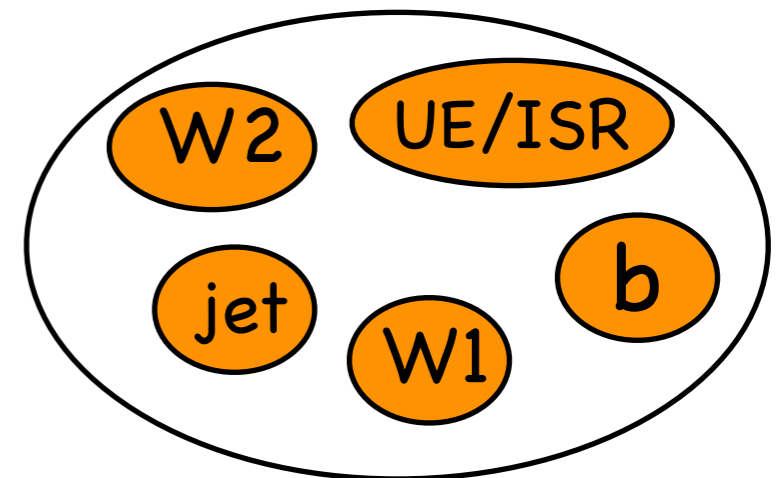
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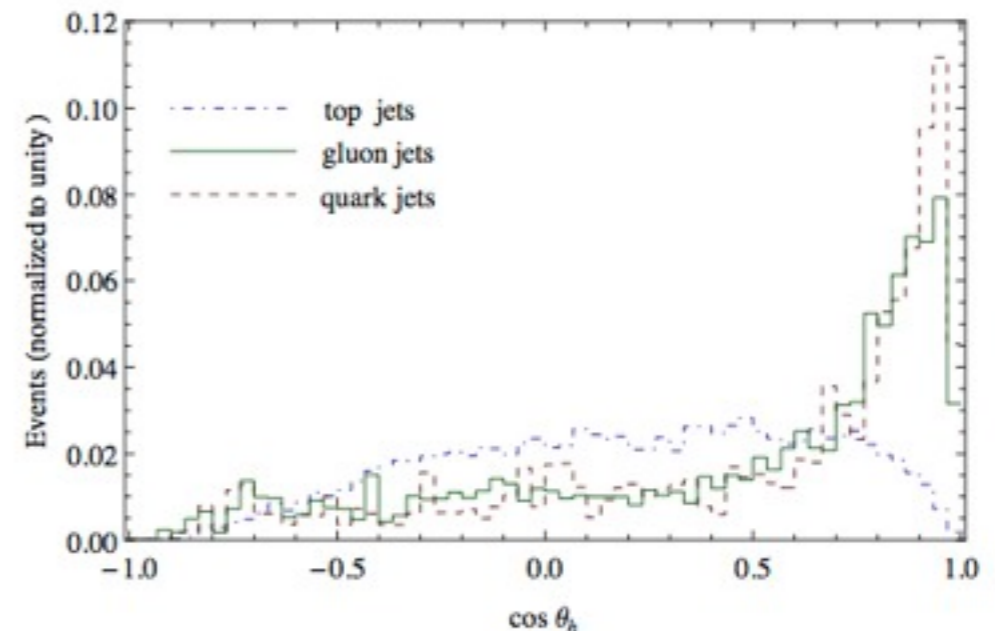
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IV.0 Like JH Tagger take,  $m_{\text{top}}$ ,  $m_W$  and  $W$  helicity angle

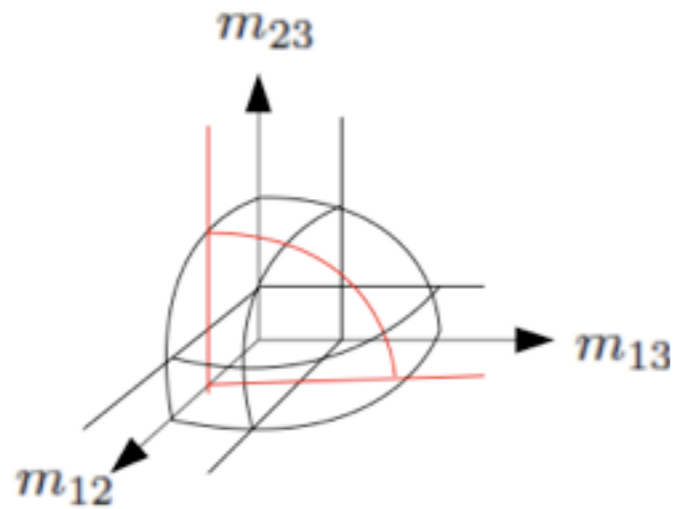
[Kaplan, et al. PRL 101 (2008)]



# IV.1 - better - check mass ratios

Cluster top candidate into 3 subjects  $j_1, j_2, j_3$

$$m_t^2 \equiv m_{123}^2 = (p_1 + p_2 + p_3)^2 = (p_1 + p_2)^2 + (p_1 + p_3)^2 + (p_2 + p_3)^2 = m_{12}^2 + m_{13}^2 + m_{23}^2$$



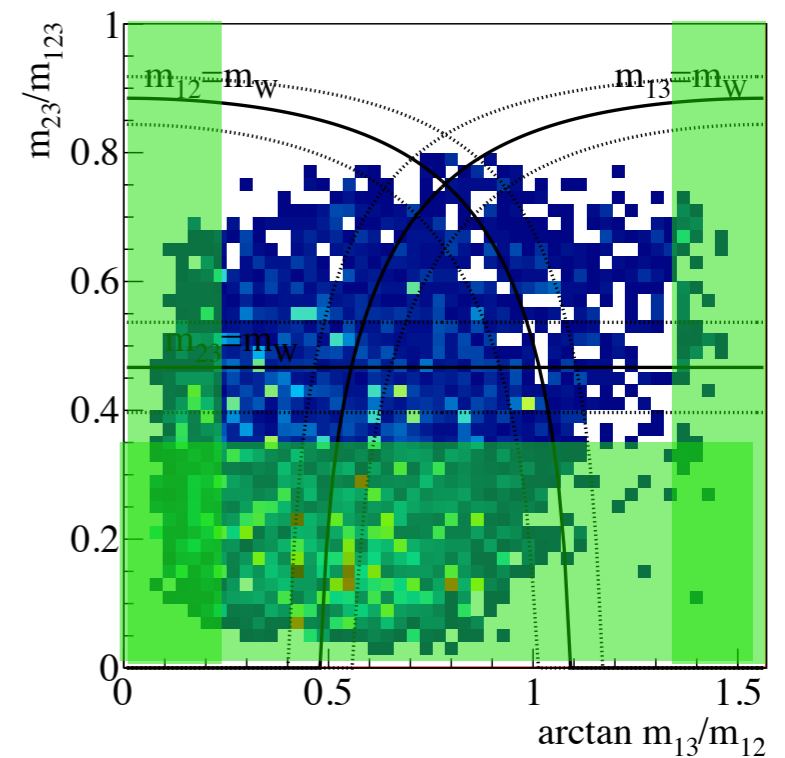
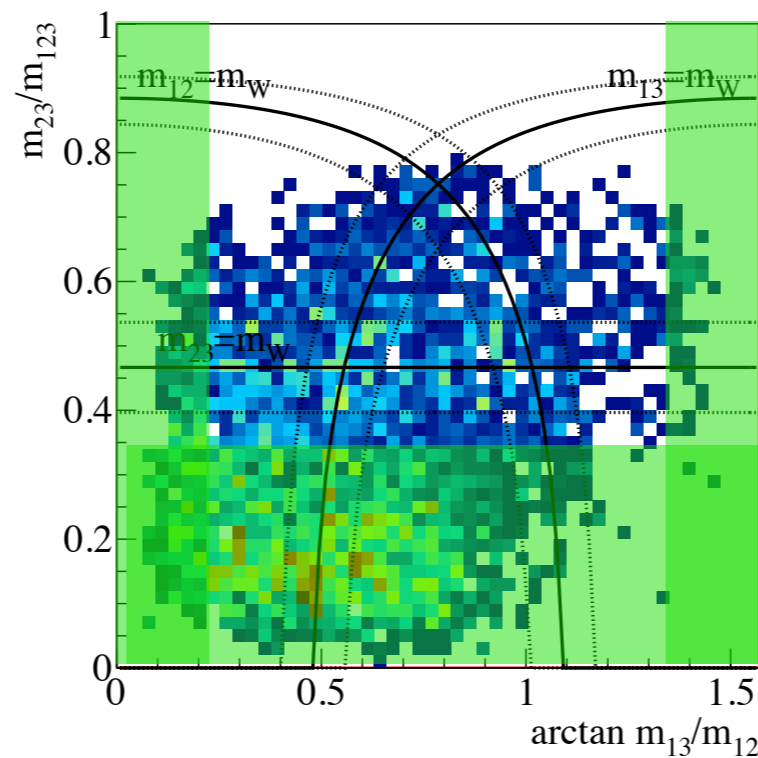
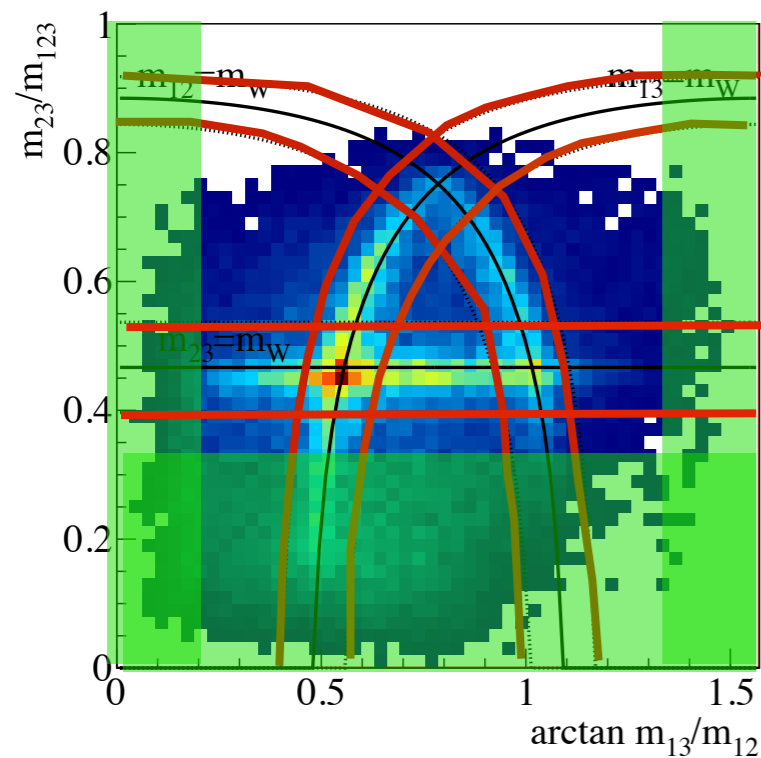
$$R_{\min} < \frac{m_{23}}{m_{123}} < R_{\max} \quad \text{and} \quad 0.2 < \arctan \frac{m_{13}}{m_{12}} < 1.3$$

$$R_{\min}^2 \left( 1 + \left( \frac{m_{13}}{m_{12}} \right)^2 \right) < 1 - \left( \frac{m_{23}}{m_{123}} \right)^2 < R_{\max}^2 \left( 1 + \left( \frac{m_{13}}{m_{12}} \right)^2 \right) \quad \text{and} \quad \frac{m_{23}}{m_{123}} > 0.3$$

$$R_{\min}^2 \left( 1 + \left( \frac{m_{12}}{m_{13}} \right)^2 \right) < 1 - \left( \frac{m_{23}}{m_{123}} \right)^2 < R_{\max}^2 \left( 1 + \left( \frac{m_{12}}{m_{13}} \right)^2 \right) \quad \text{and} \quad \frac{m_{23}}{m_{123}} > 0.3$$

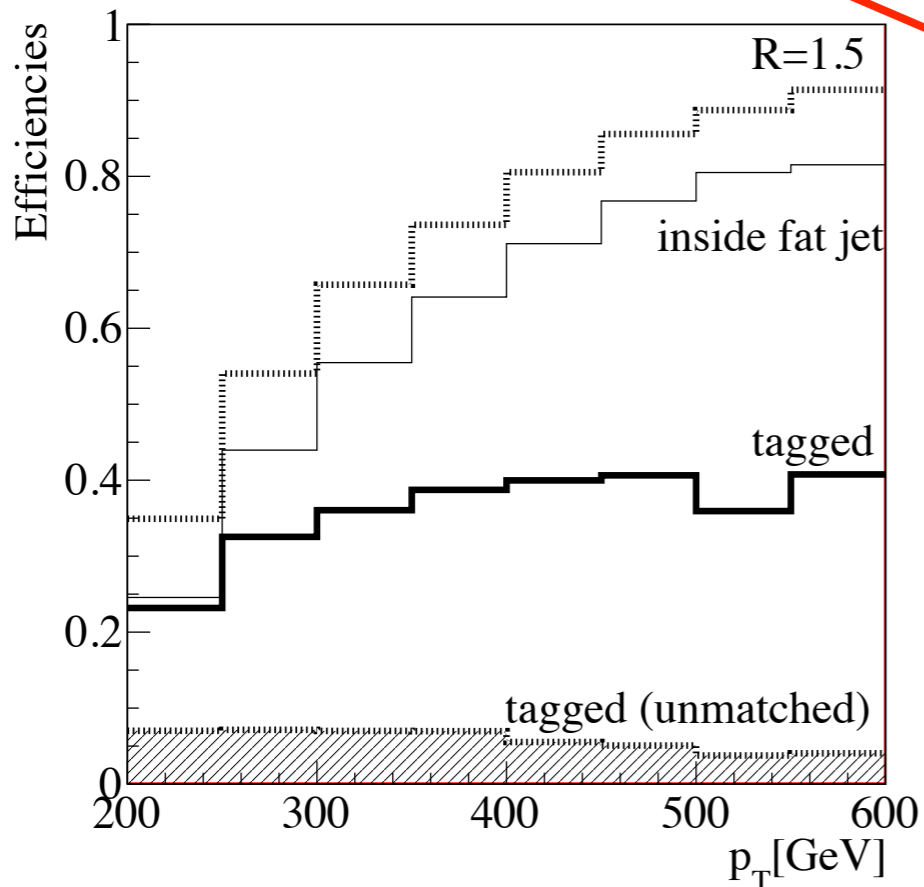
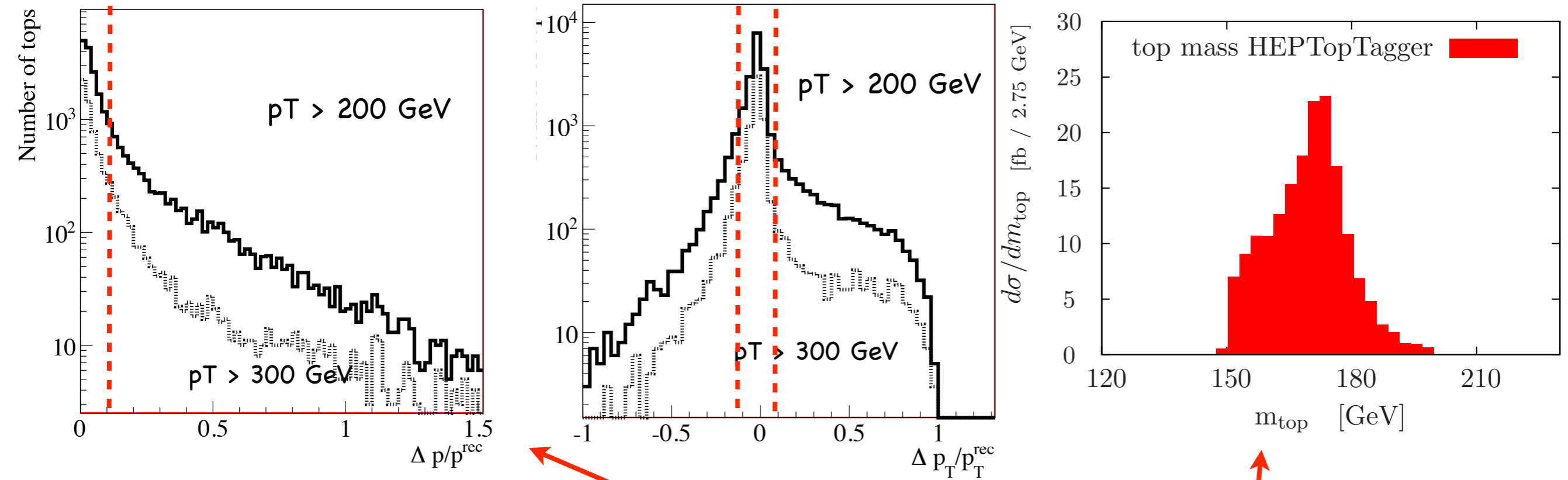
$$R_{\min} = 85\% \times m_W / m_t$$

$$R_{\max} = 115\% \times m_W / m_t$$





# Top quark momentum reconstruction

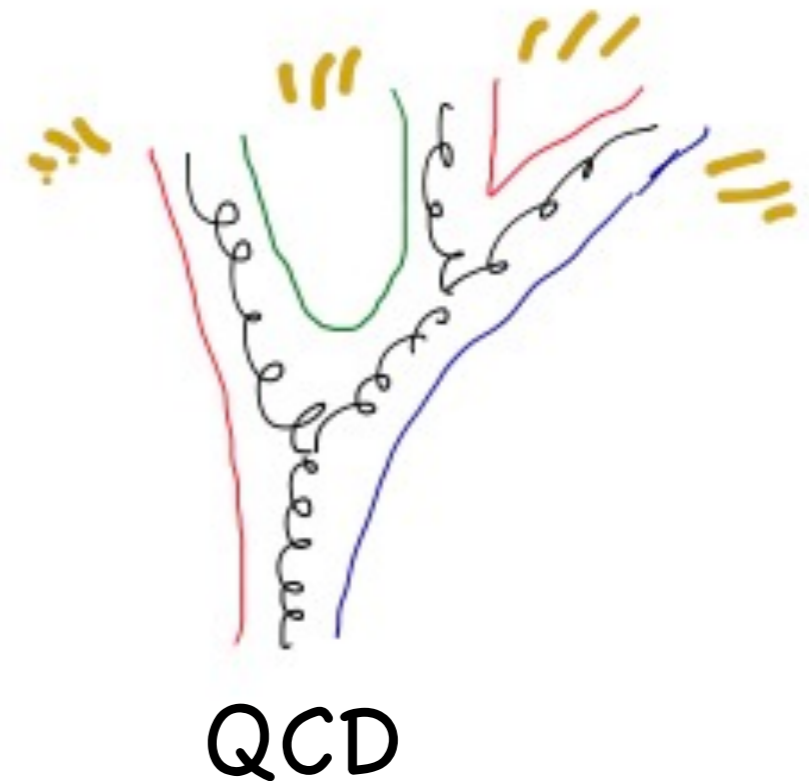
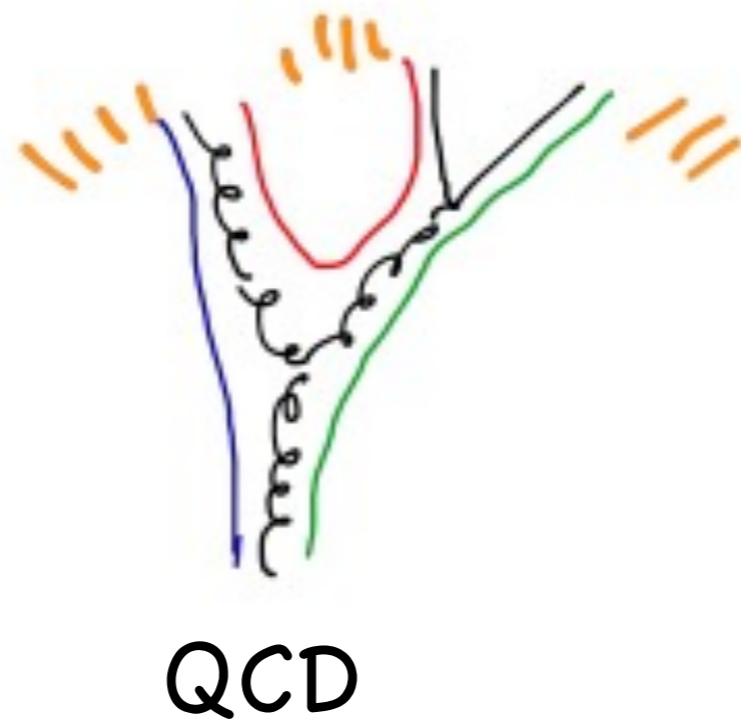
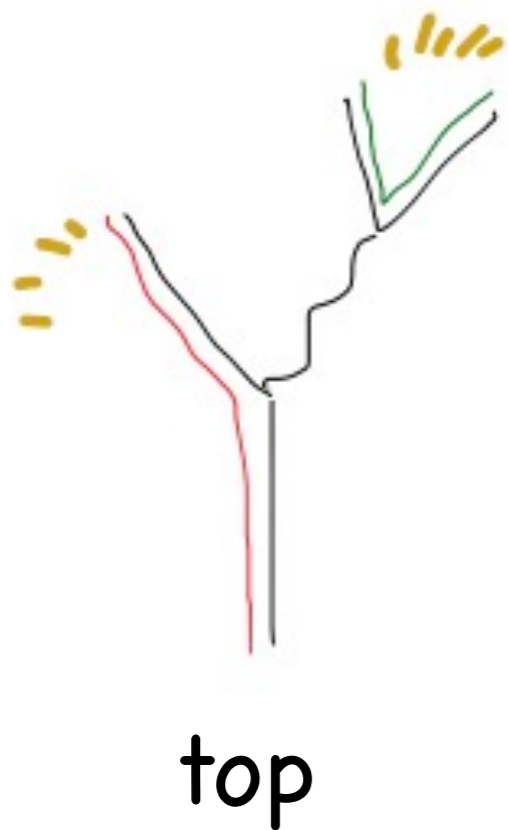


- ▶ Great reconstruction of top quark momentum
- ▶ 35% tagging efficiency  
2% W+jets fake rate

# First generation taggers, e.g. Hopkins, CMS, HEP

make use of many properties of the top for reconstruction  
(top mass, W mass, EW structure of decay)

However, QCD radiation pattern are left mostly aside.

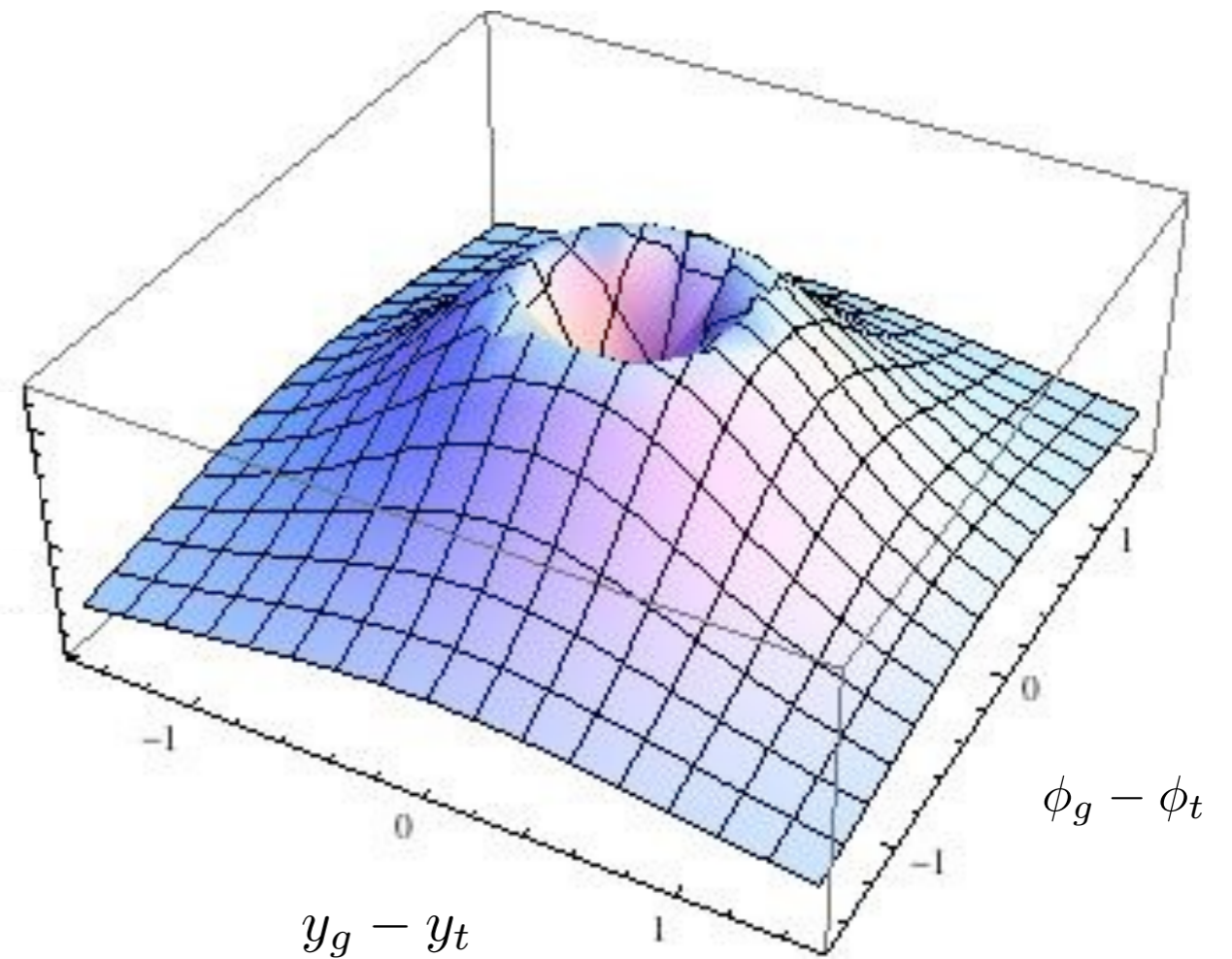
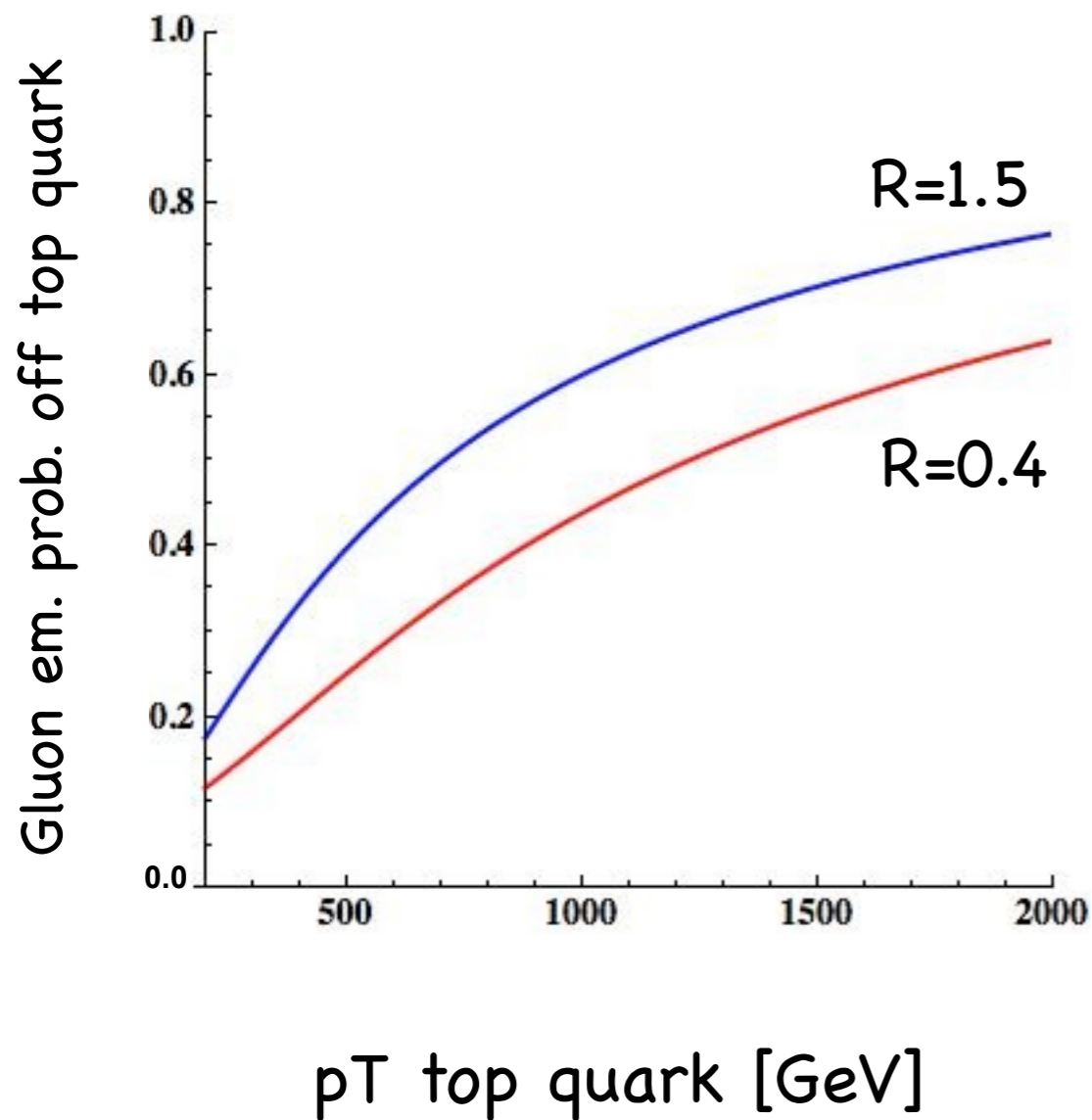


# One can be more quantitative...

use emission prob. from [Soper, MS PRD 87]

$$\mathcal{P} = 1 - e^{-S_{ttg}}$$

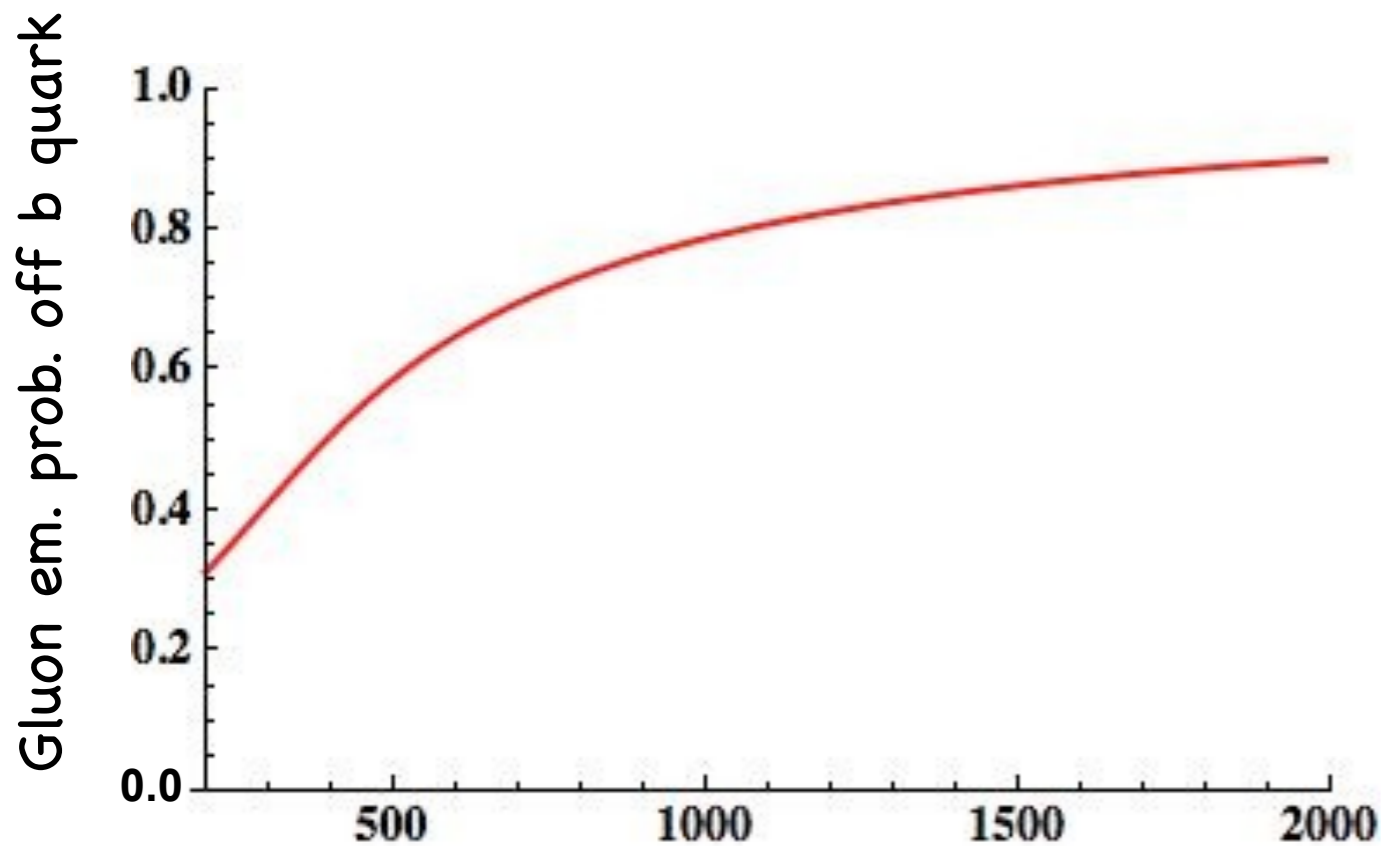
Dead region around top



pT top 500 GeV, pT gluon 20 GeV

Radiation off bottom quark down  
to hadronization scale

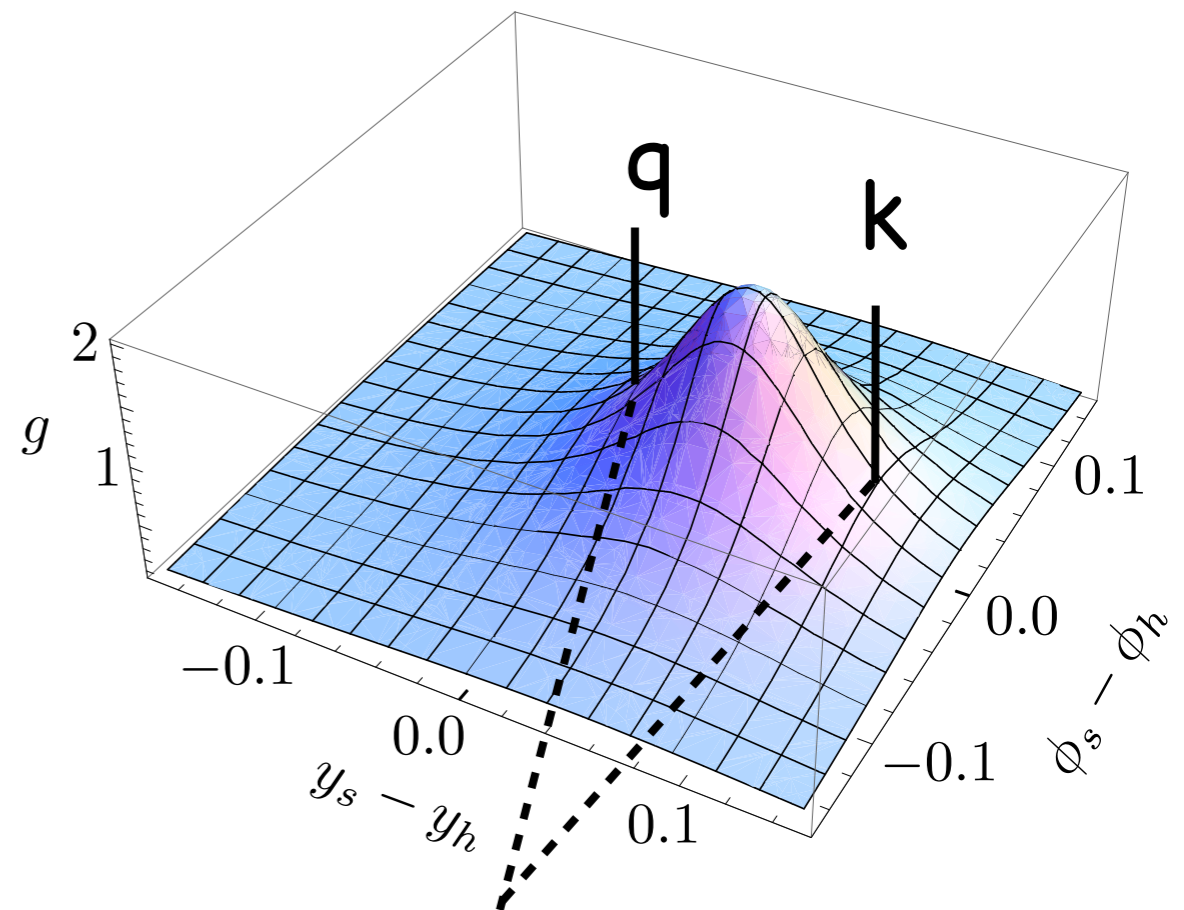
$$\mathcal{P} = 1 - e^{-S_{bbg}}$$



pT top quark [GeV]

pT bottom = pT top / 3

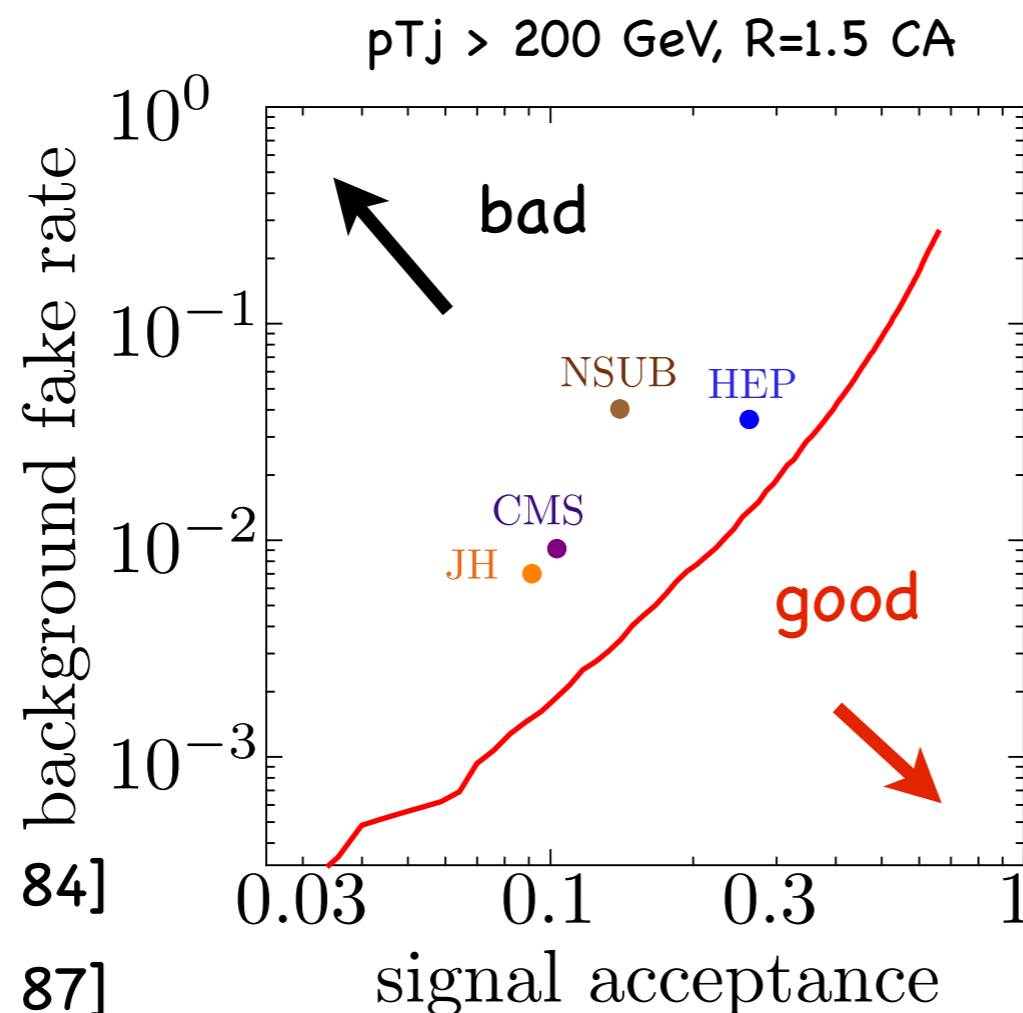
angular distribution for  
radiation off W decay products



W decay products

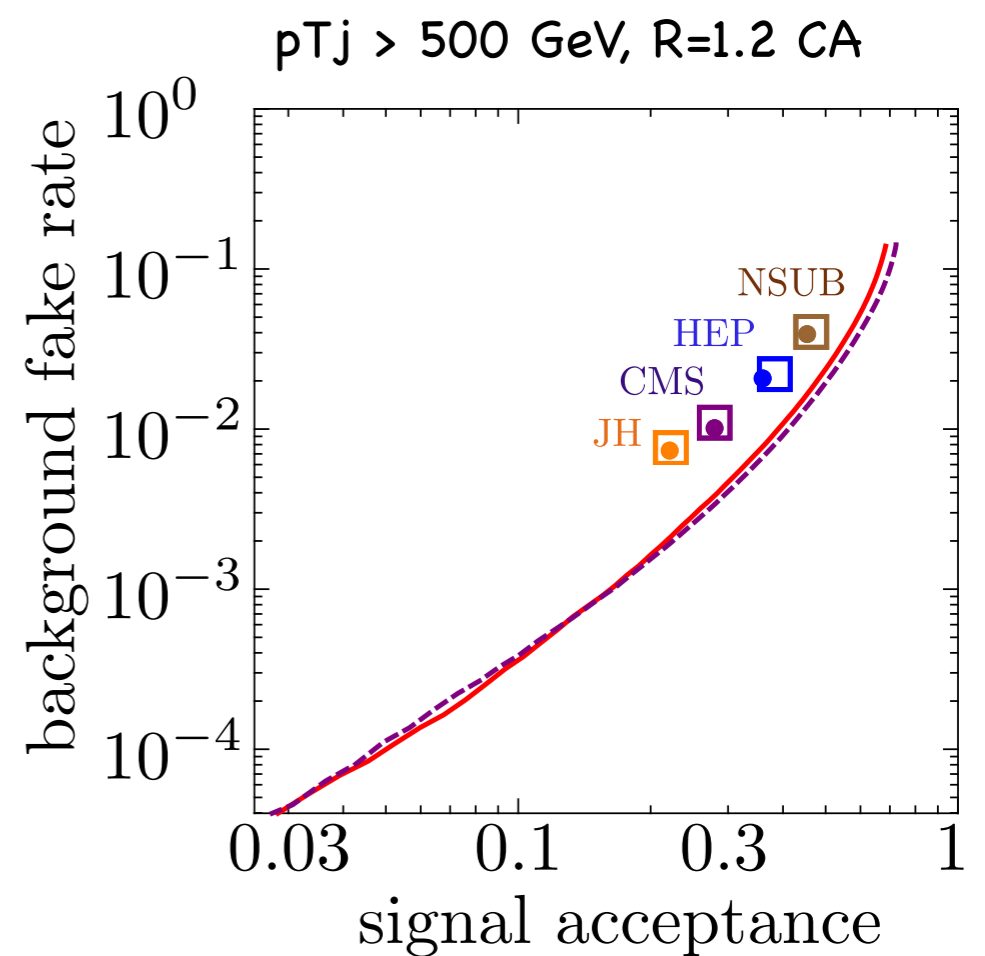
Newer taggers, e.g. based on the method shower deconstruction, make explicitly use of the fact that the top and its decay products have special QCD radiation profile:

Idea: Reverse engineer CKKW [Catani, Krauss, Kuhn, Webber JHEP]



[Soper, MS PRD 84]

[Soper, MS PRD 87]

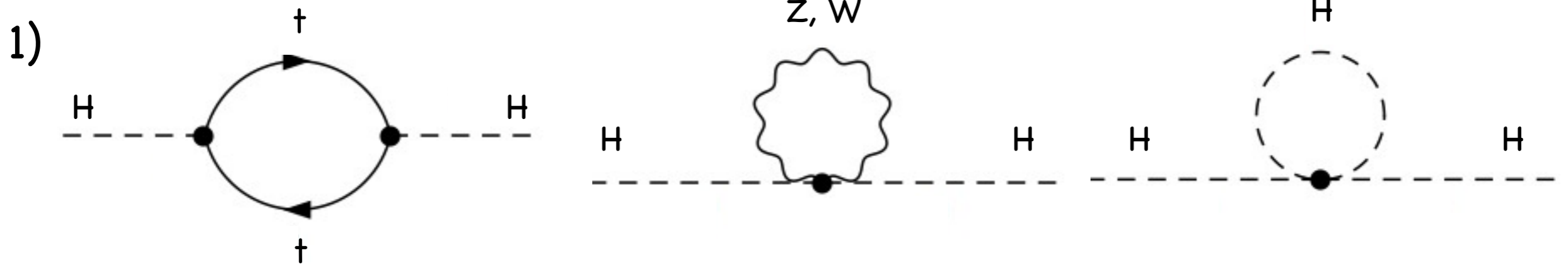


# Using the top quark to find new physics



# The Standard Model after the 4th of July

The discovery of a Standard-Model-like scalar resonance marked milestone in increasing understanding of nature. And raises questions:



$$m_{h,SM}^2 = \mu^2 + \frac{3\Lambda^2}{32\pi^2 v^2} (2m_W^2 + m_Z^2 + m_{h,SM}^2 - 4m_t^2), \quad \mu^2 = -2\lambda v^2$$

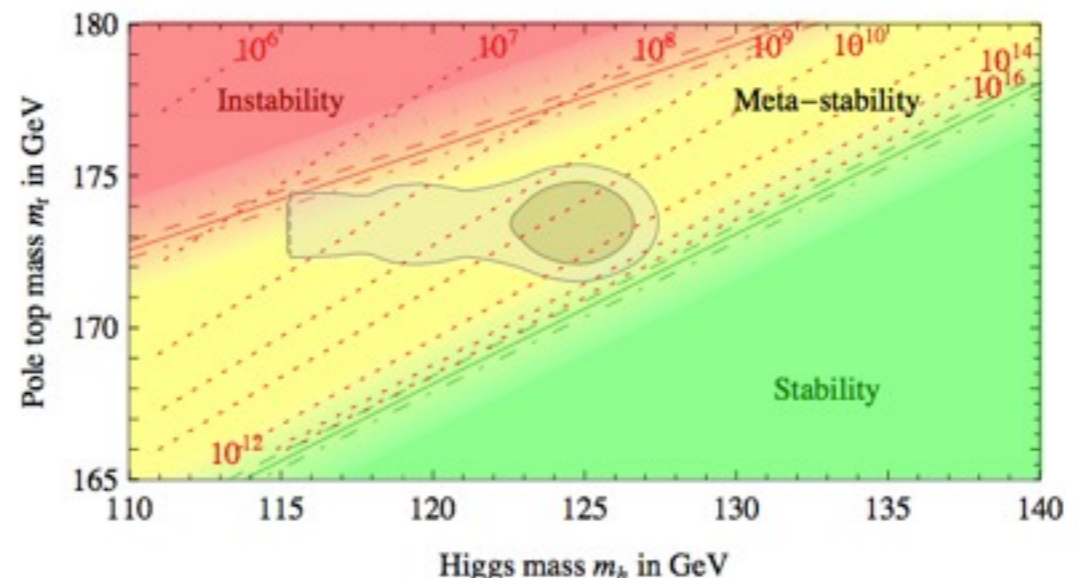
→ numerically top loop dominates:  $(2m_W^2 + m_Z^2 + m_{h,SM}^2 - 4m_t^2) \simeq -81700$

→ Up to which scale  $\Lambda$  is SM valid? How to avoid excessive fine-tuning?

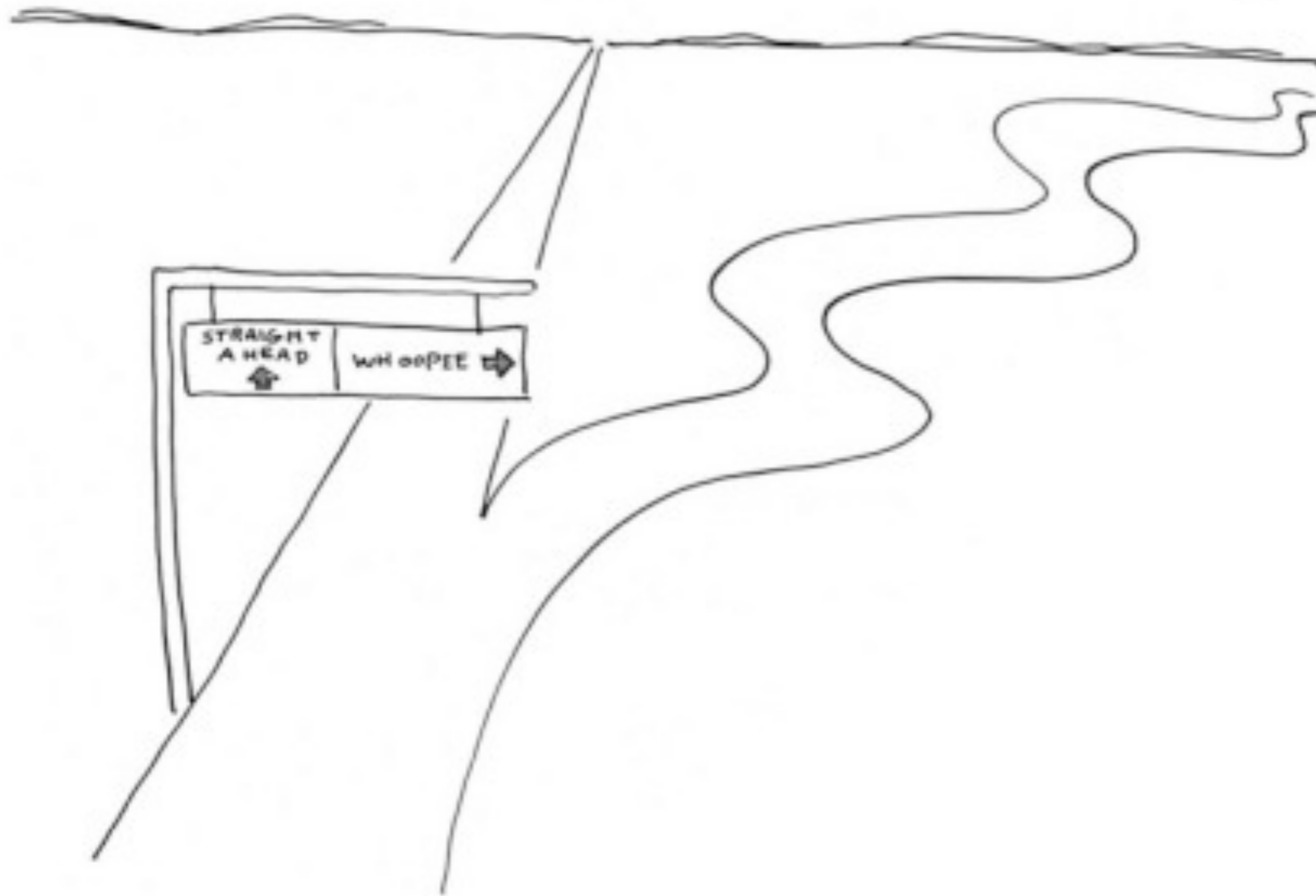
2) Is Higgs potential stable?

No definite answer due to large top mass uncertainty

[Elias-Miro et al, PLB 709]



Standard Model is valid  
to very high scale



Elementary scalar:

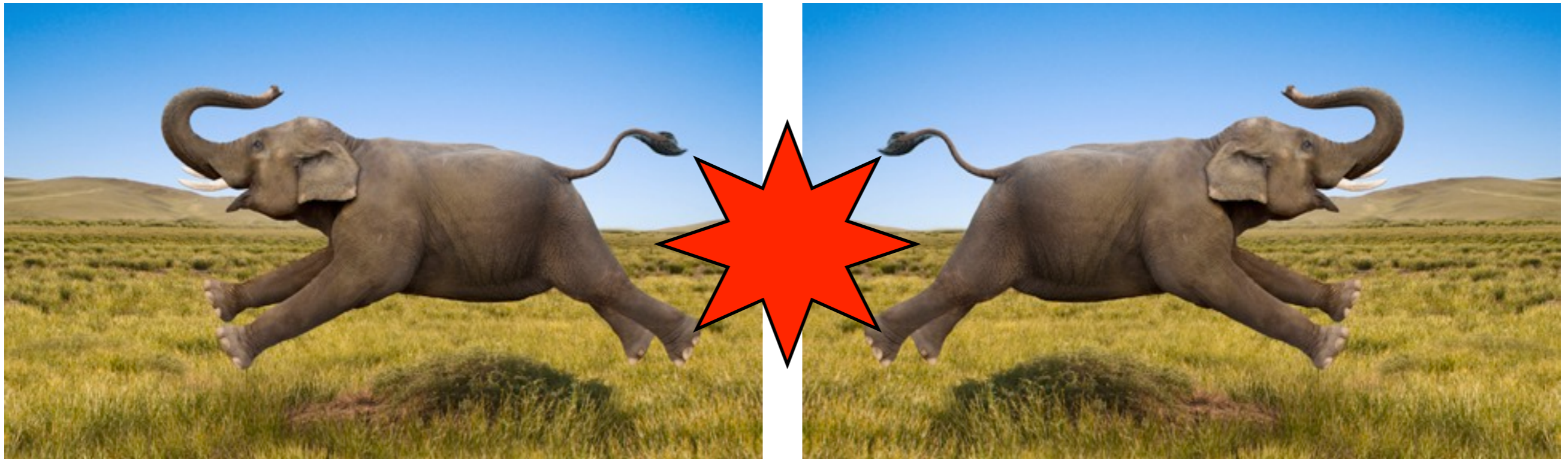
- SUSY restores naturalness
- Coleman-Weinberg potential
- ....

Composite scalar:

- Higgs as Pseudo-Nambu-Goldstone boson
- ....



# Energetic tops are often the key

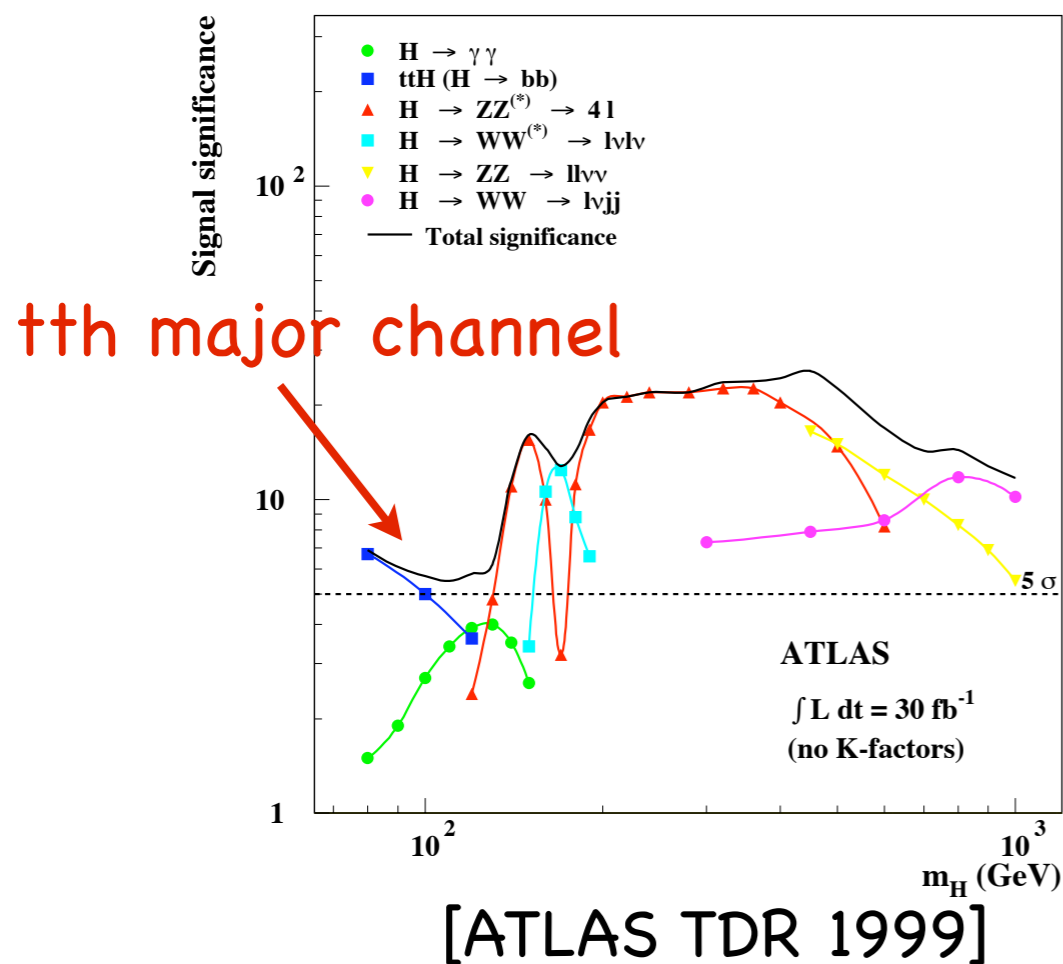


- Almost all signal events are boosted, e.g. heavy  $Z'$  or KK gluon...
- Background drops faster than signal, e.g.  $t\bar{t}h$ , top partner
- Couplings require large momentum ( $m_{tt}$ ), e.g.  $A_{fb}$ , top radius

# Applications: tth as busy as it gets in the SM

- Motivation:
- sizable cross-section
  - Higgs discovery contribution in low mass range
  - access to t- and b-Yukawa couplings

## High expectations:



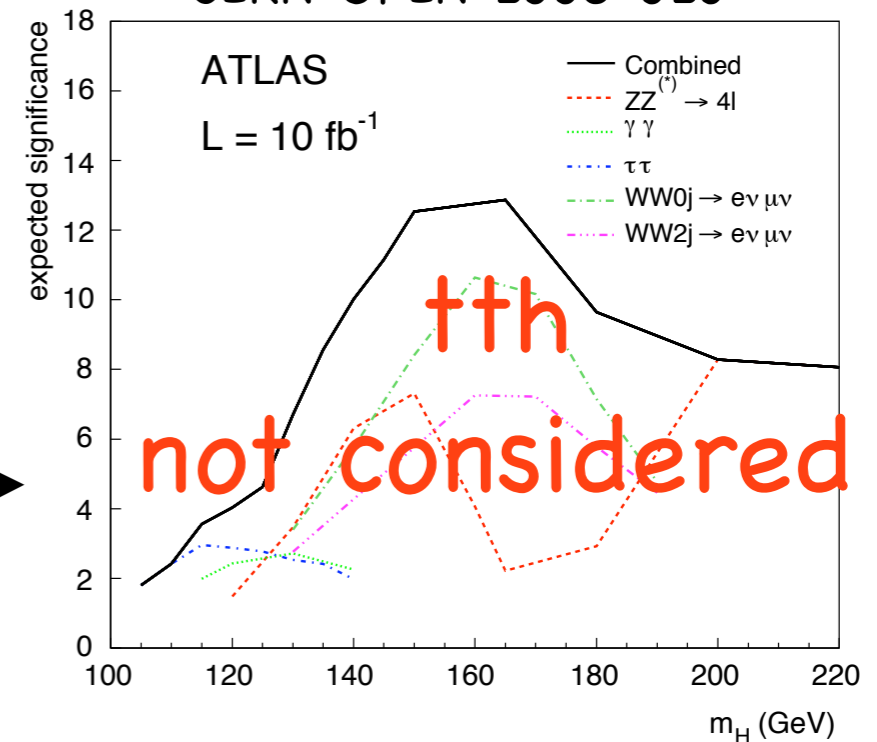
Cammin  
and  
Schumacher  
(ATLAS)

$S/B \simeq 1/9$

$S/\sqrt{B} \simeq 2.2$



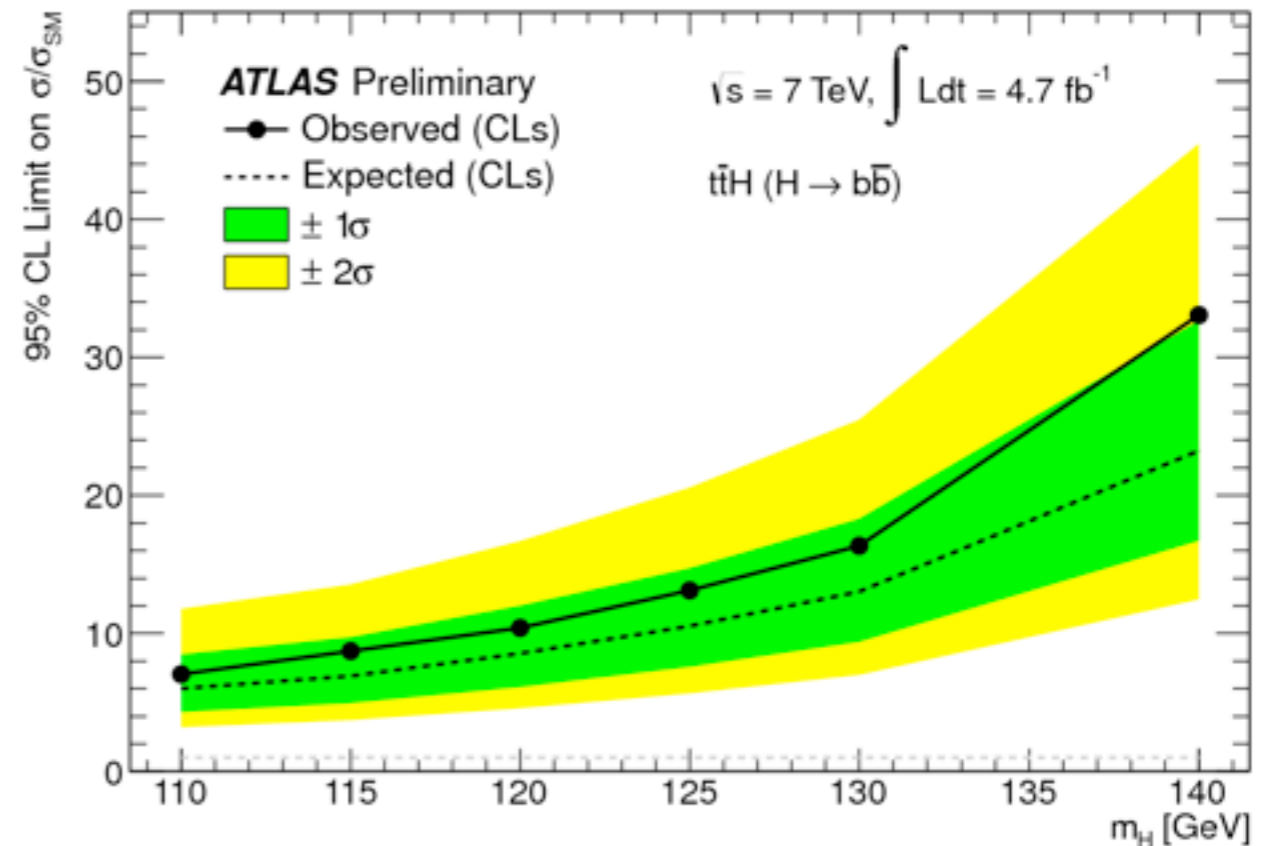
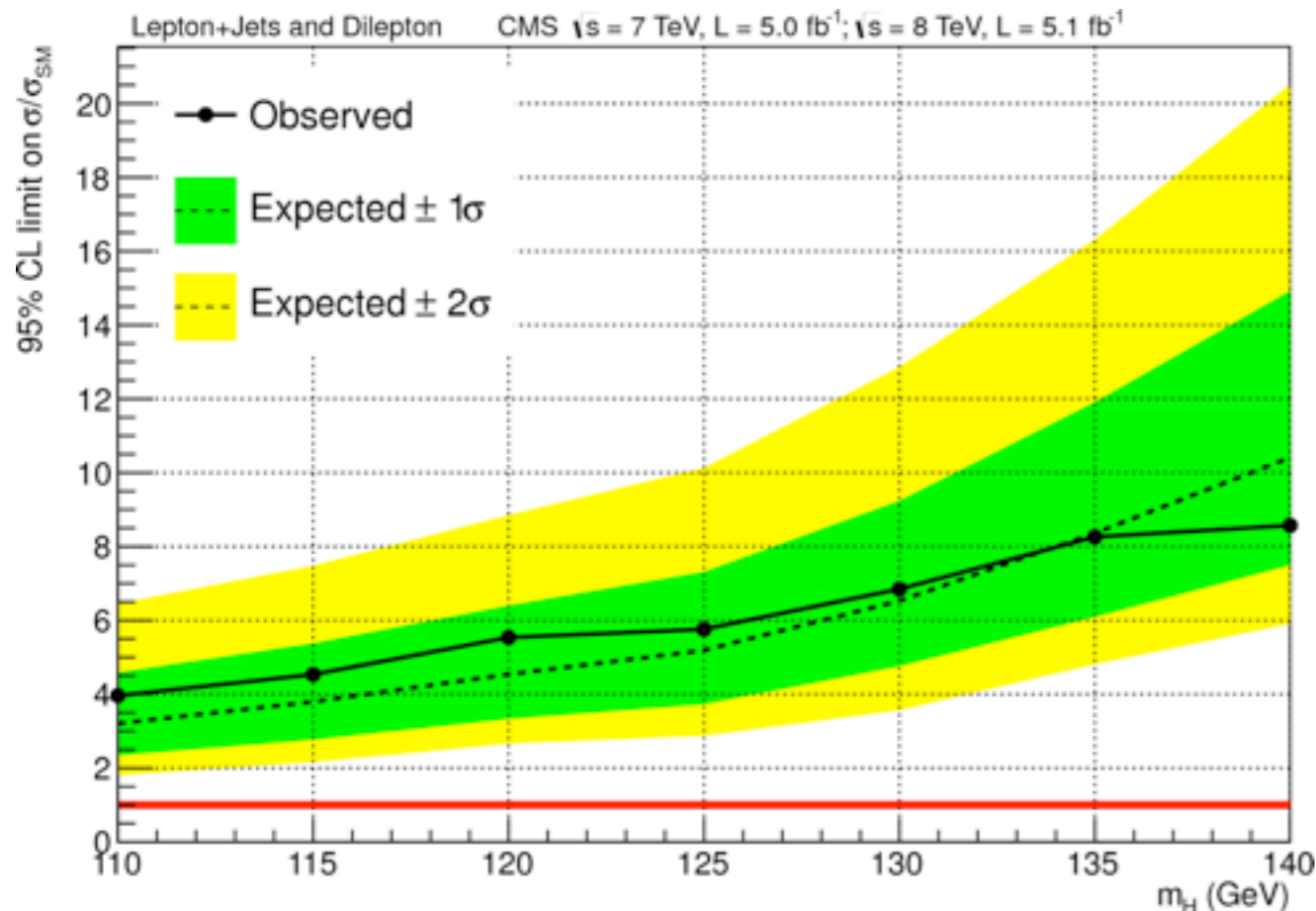
## Expected Performance of the ATLAS Experiment, CERN-OPEN-2008-020



# Present results by CMS and ATLAS

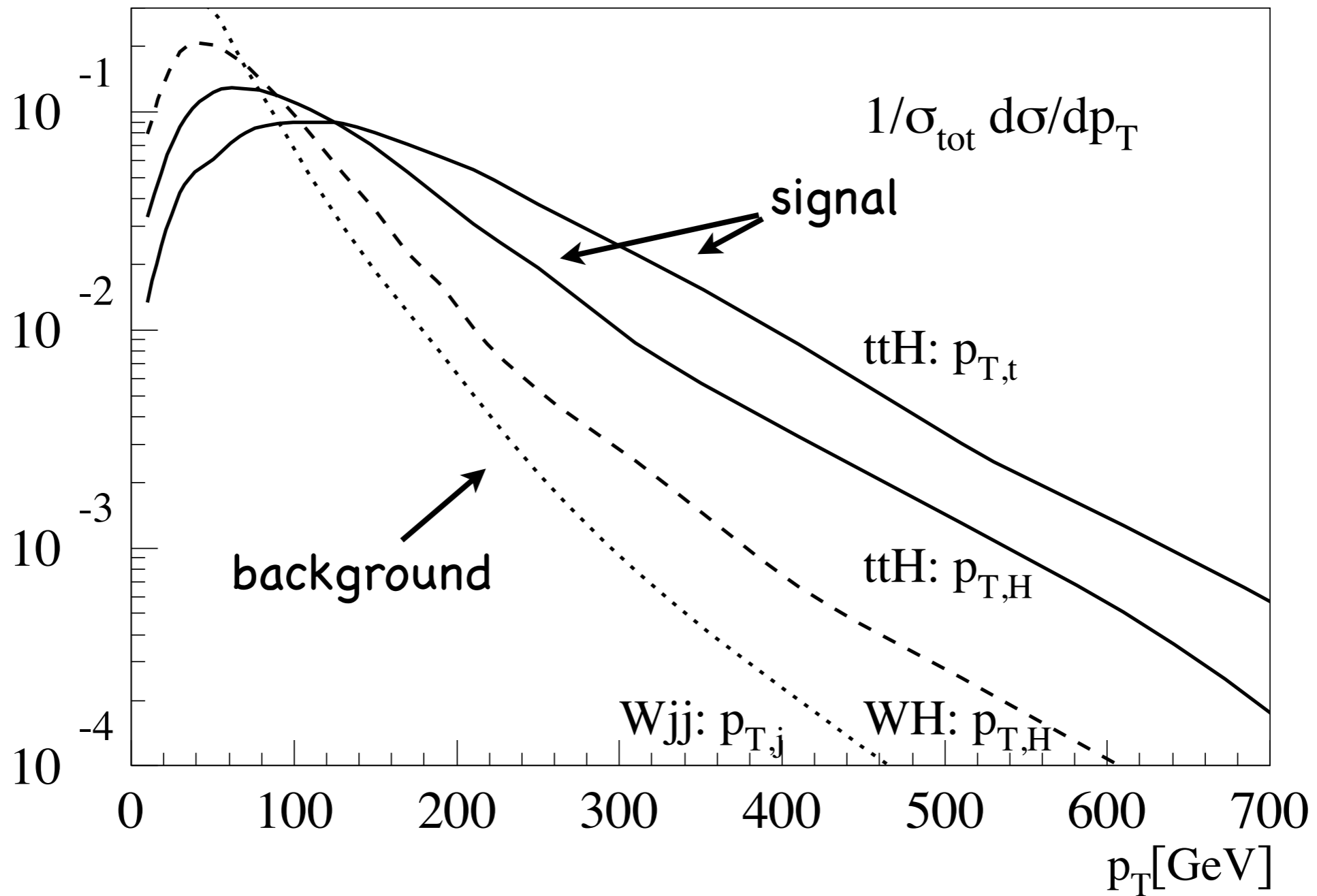
CMS, 7 and 8 TeV each 5 ifb comb.

ATLAS, 7 TeV at 4.7 ifb



Both experiments are sensitive at X-times the SM cross section  
 However,  $t\bar{t}h$  coupling measurement will be systematics limited.  
 Low S/B will render measurement notoriously difficult with  
 standard reconstruction techniques.

# pT distributions relevant for tth



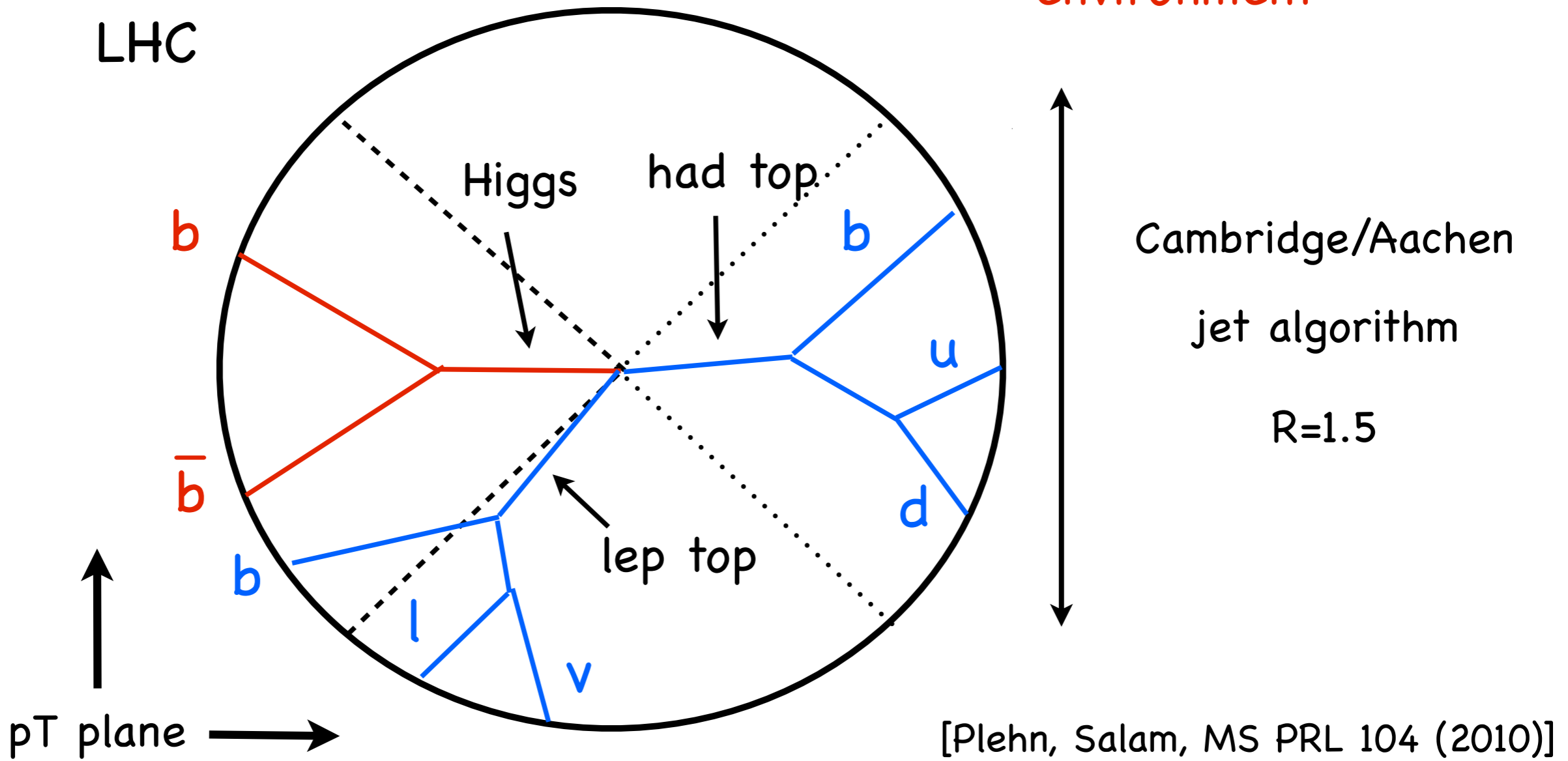
# Problems in event reconstruction:

- (b-)jet multiplicity
- reconstruction efficiency

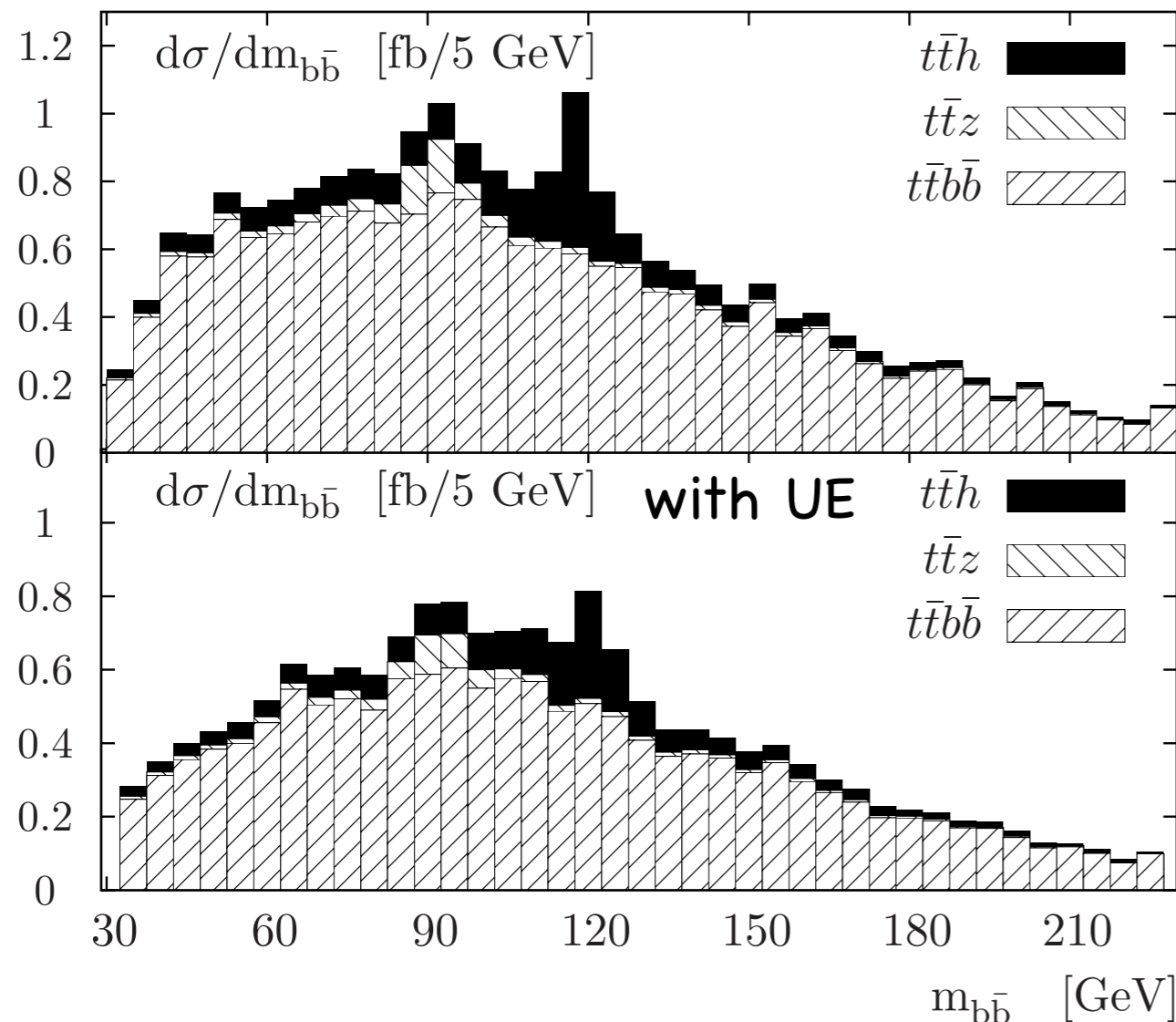


Boost should help  
but

need tagger for this  
environment



# Results for $t\bar{t}h$



- 5 sigma sign. with 100 1/fb

- Development of Higgs and top tagger for busy final state

- Improvement of S/B from 1/9 to 1/2

→ Can use Z peak to calibrate Higgs-top coupling

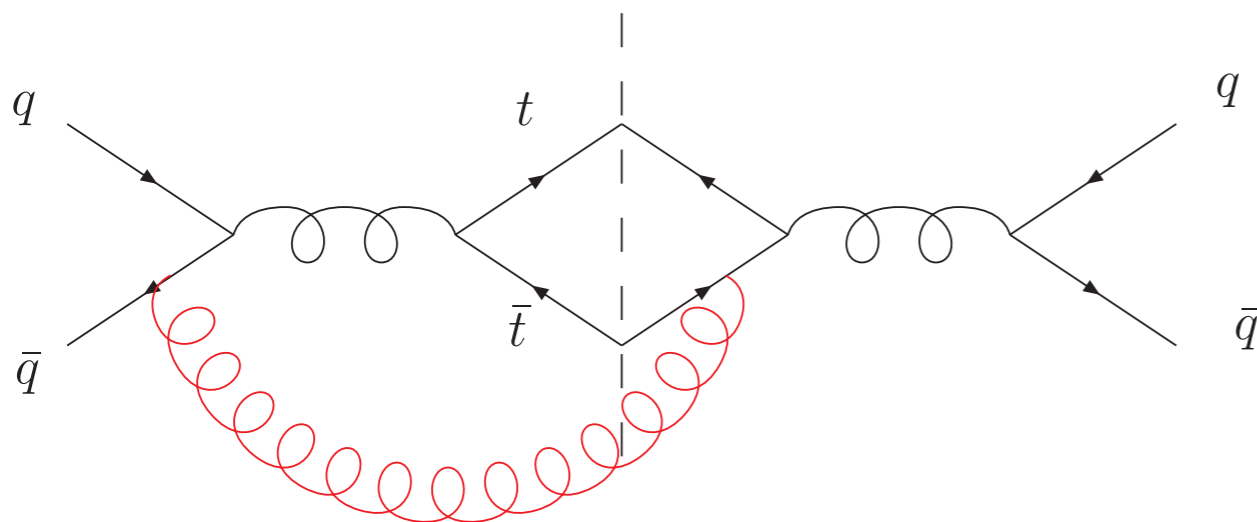
→  $t\bar{t}h$  might be a window to Higgs-top coupling

# Forward backward asymmetry

D0 and CDF observed anomalously large values of  $A_{fb}$

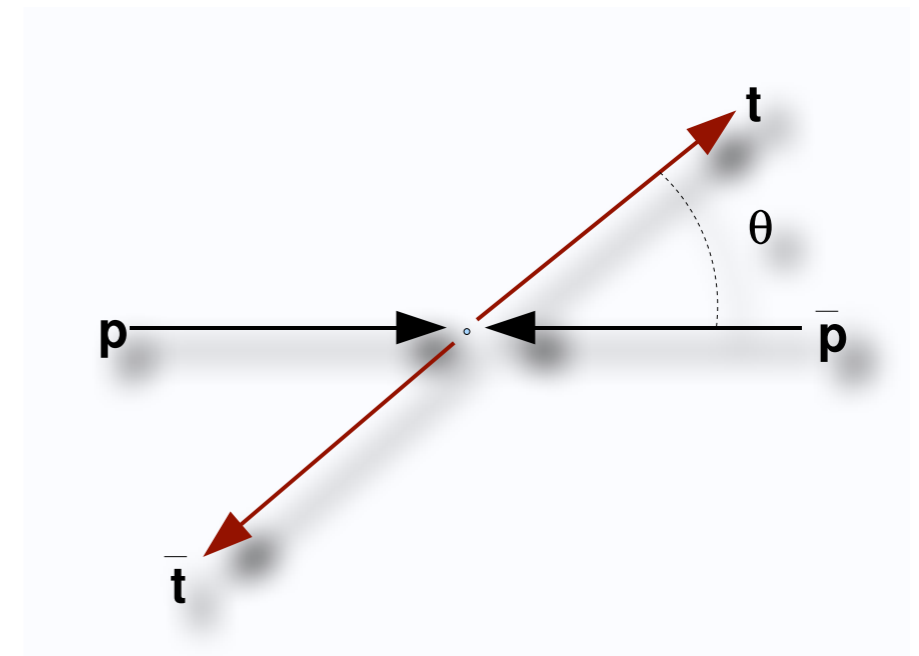
- ▶ Charge asymmetry small NLO effect ( $\sim 6\%$ ) [Kühn, Rodrigo]
- ▶ NLL threshold resummation reduces theory uncertainty

[Almeida, Sterman, Vogelsang]



$$A^{t\bar{t}} = \frac{N(\Delta y > 0) - N(\Delta y < 0)}{N(\Delta y > 0) + N(\Delta y < 0)}$$

$$\Delta y = y_t - y_{\bar{t}}$$

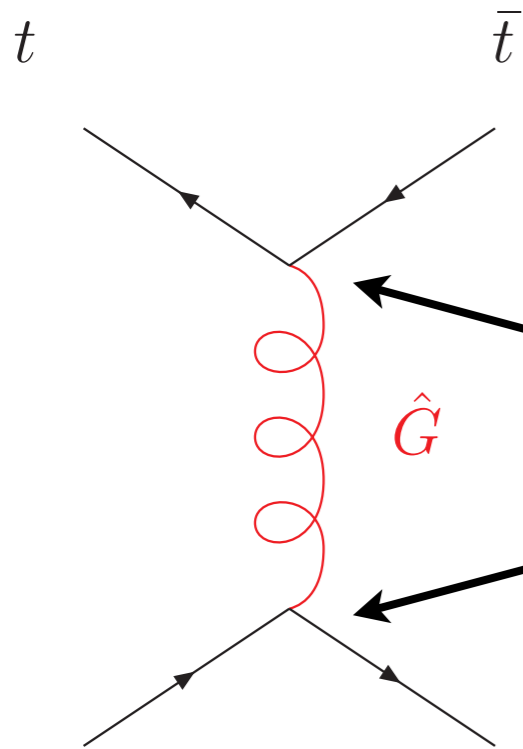


D0:  $A_{fb} = (8 \pm 4(\text{stat}) \pm 1(\text{syst}))\%$

CDF: (leptonic)  $A_{FB} = 0.21 \pm 0.07(\text{stat}) \pm 0.02(\text{bkg-shape})$   
 (semileptonic)  $A_{FB} = 0.150 \pm 0.050(\text{stat}) \pm 0.024(\text{syst})$

more pronounced at large invariant mass  
 ( $> 450 \text{ GeV}$ )

# Models to account for asymmetry

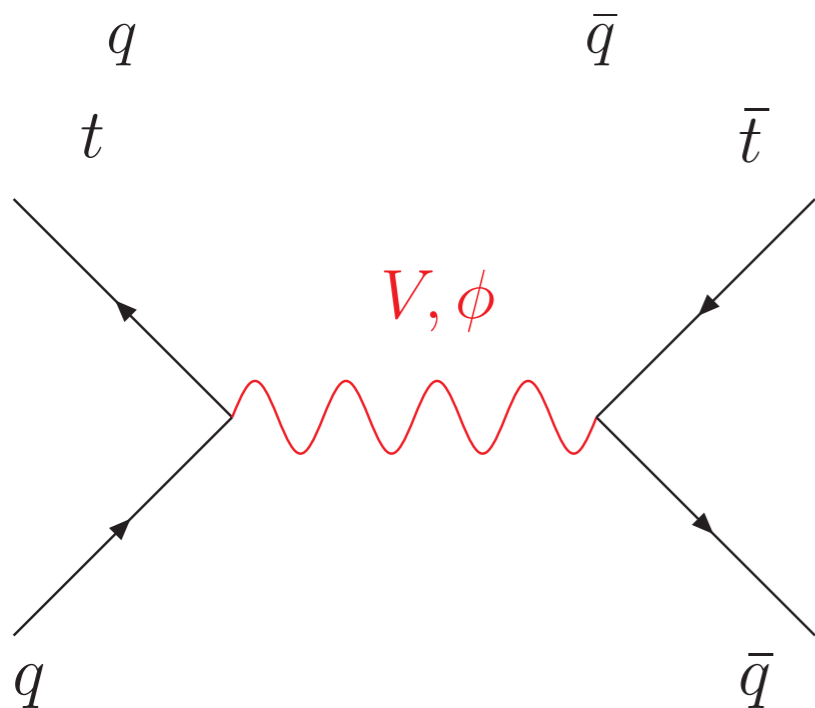


s-channel resonance:

[Frampton, Shu, Wang; Chivukula, Simmons, Yuan; Bai, Hewett, Kaplan, Rizzo]

-g<sub>u,d</sub> g<sub>t</sub> to get pos. asymmetry

requires flavor non-universal coupling



t-channel resonance:

[Jung, Murayama, Pierce et al.; Shu, Tait, Wang; Cheung, Keung, Yuan; Barger, Keung, Yu; Shelton, Zurek; Grinstein, Kagan, Trott, Zupan; Ligeti, Schmaltz, Tavares]

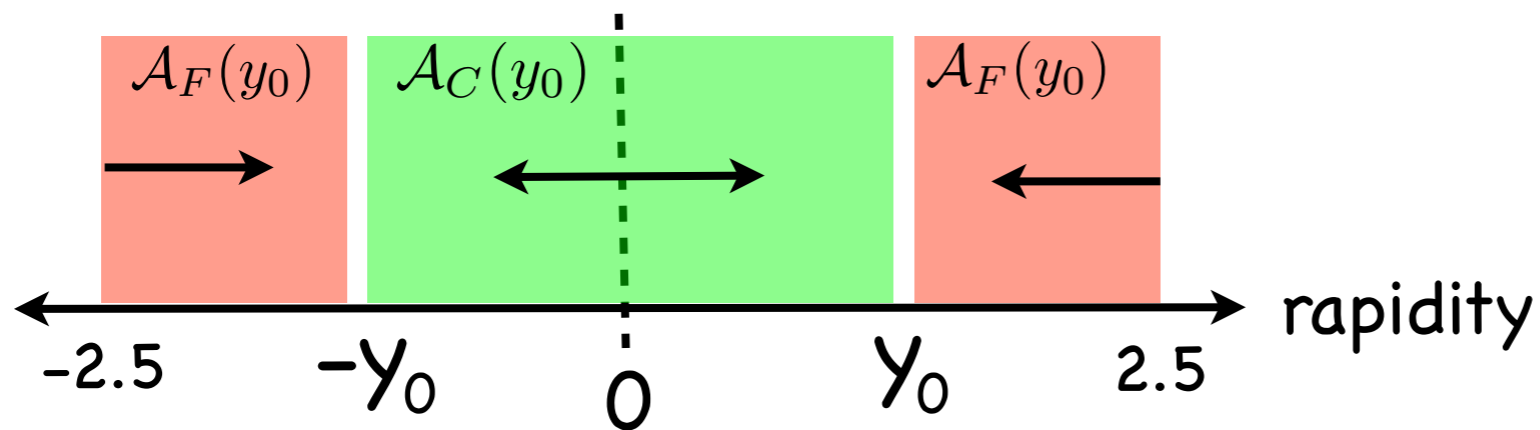
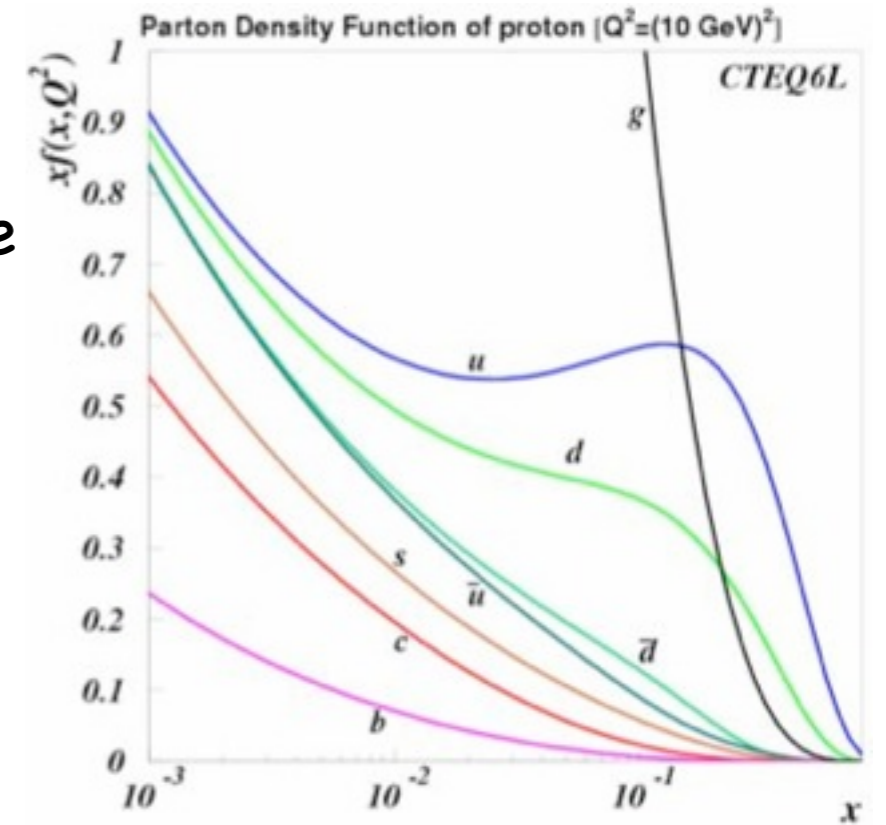
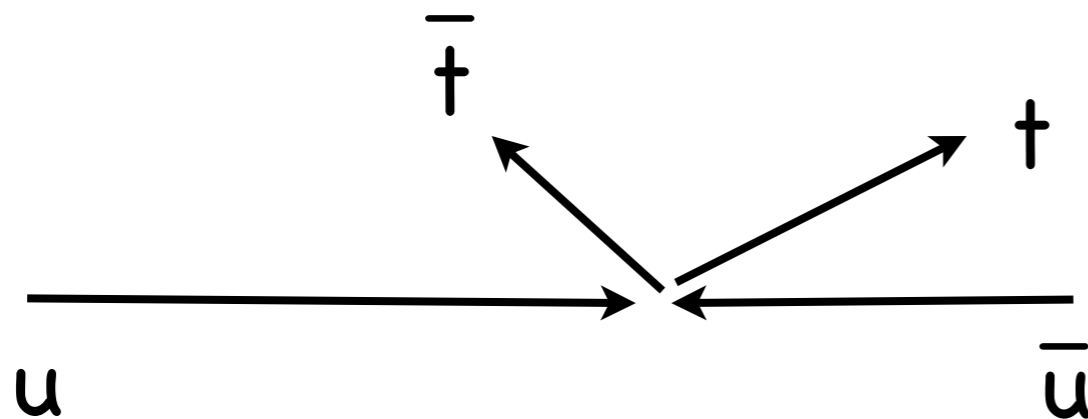
requires flavor off-diagonal coupling

Overview: [Gresham, Kim, Zurek]



# We will have to measure asymmetry at the LHC

- ▶ Symmetric proton beams
- ▶ If CP conserved → FB becomes Charge asymmetry



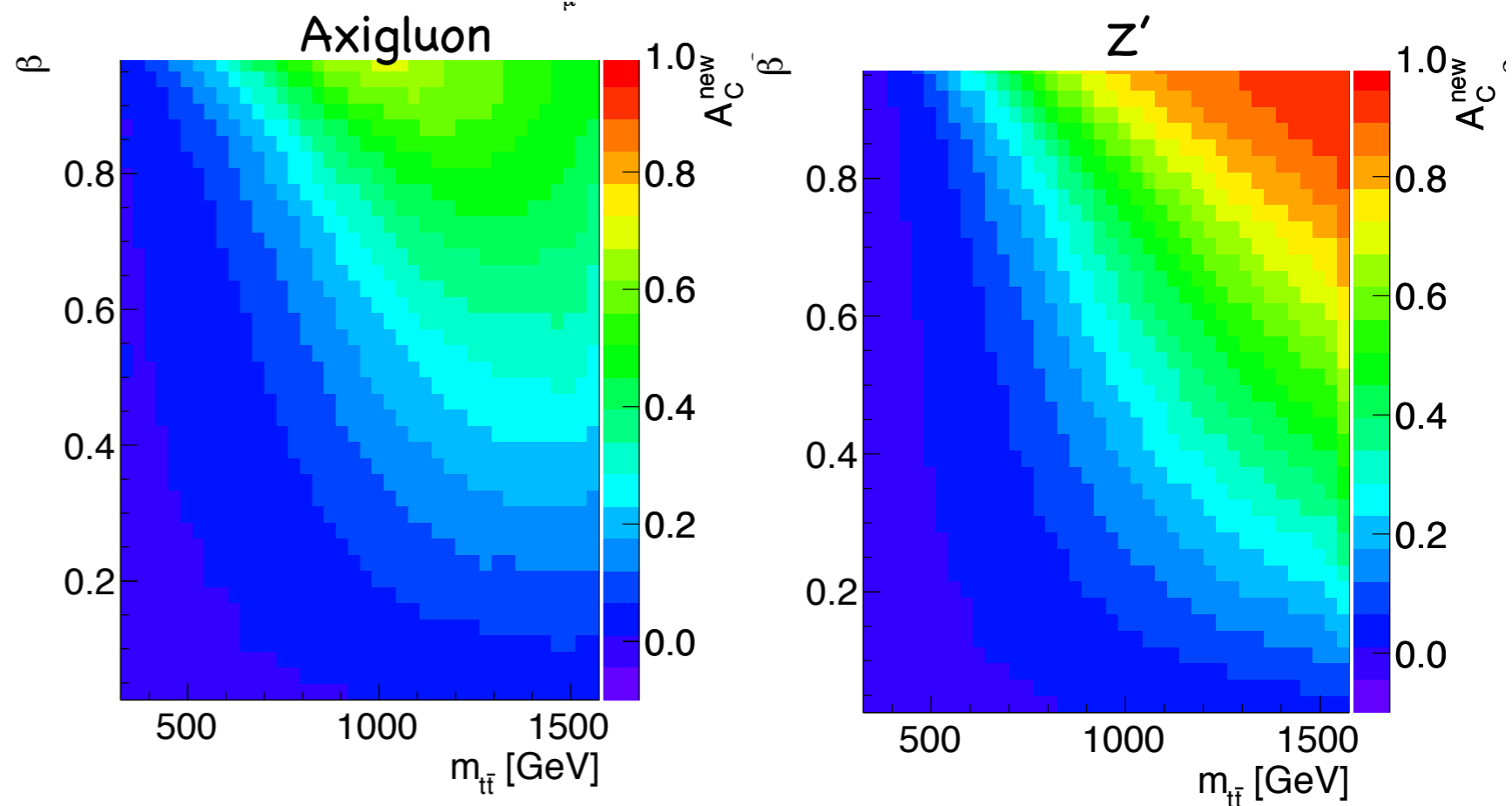
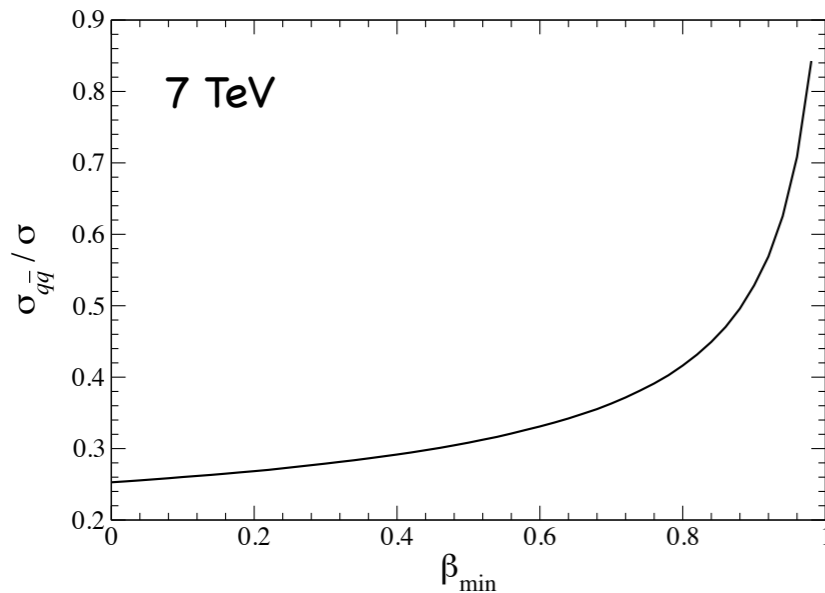
gg dominant prod.  
mode but symmetric

need qq and qg  
initial state

# Study for charge asymmetry @ LHC

[Aguilar-Saavedra, Juste, Rubbo]

$$\beta = \frac{|p_t^z + p_{\bar{t}}^z|}{E_t + E_{\bar{t}}}$$



Event reconstruction: Consider moderately boosted semileptonic tops

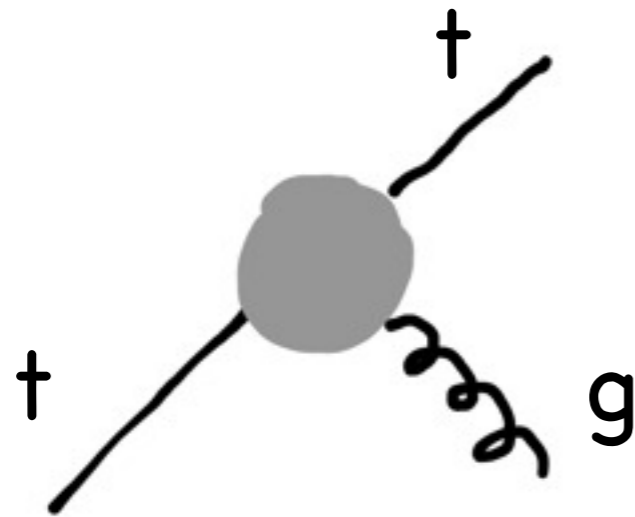
- ▶ require isolated lepton with  $p_T > 15$  GeV,  $\gamma_l = \gamma_{\text{lep. top}}$
- ▶ require jet with  $p_T > 200$  GeV, use HEPTopTagger
- ▶ demand b-tag in hadronic top

[Hewett, Sheldon, MS, Takeuchi, Tait]

→ W+jets negligible

- 14 TeV:
- ▶  $5\sigma$  for SM after 60 fb
  - ▶  $5\sigma$  for BSM after 2 fb

# Anomalous top gluon couplings



Top-compositeness can induce magnetic moment and radius

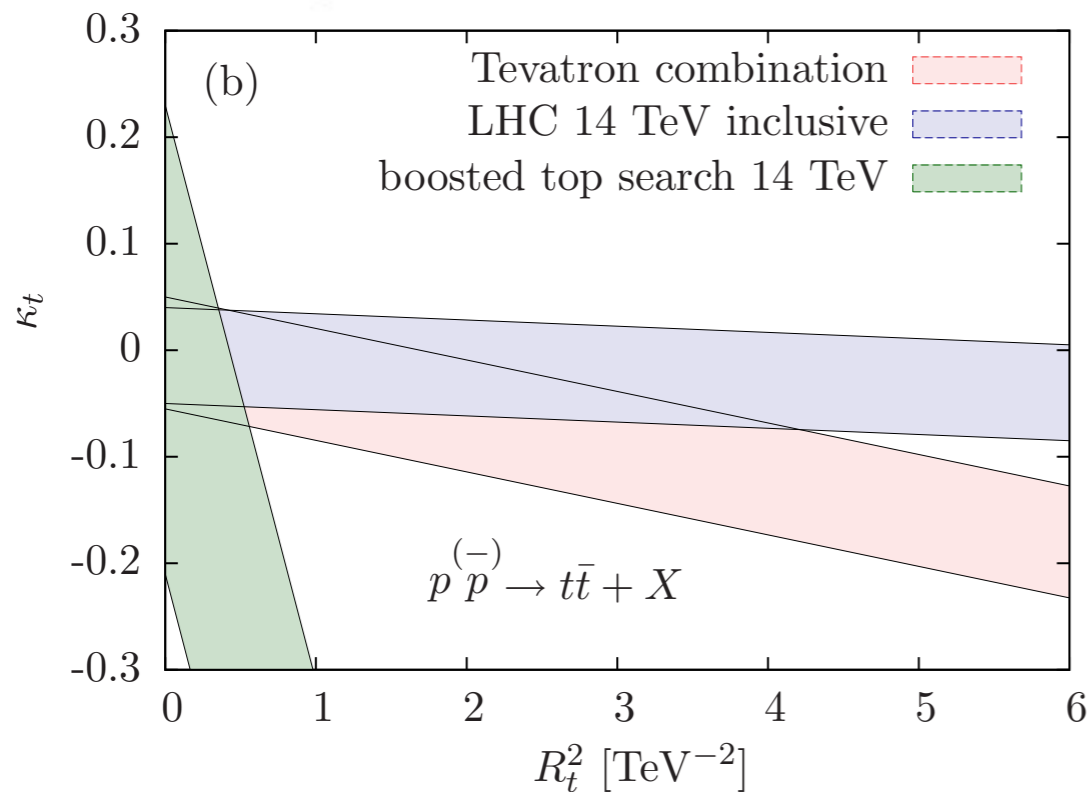
Effect of non-pointlike top structure via

$$\mathcal{L}_R = -g_s \frac{R_t^2}{6} \bar{t} \gamma^\mu \mathcal{G}_{\mu\nu} D^\nu t + \text{h.c.},$$

$$\mathcal{L}_\kappa = g_s \frac{\kappa_t}{4m_t} \bar{t} \sigma^{\mu\nu} \mathcal{G}_{\mu\nu} t,$$

gluon-fusion induced top production does not depend on  $R_t$  at leading order

Use large  $m_{t\bar{t}}$  to increase quark contribution in production



Combination of Tevatron, incl. LHC and boosted LHC gives good measurement

[Englert, Freytas, Spira, Zerwas]

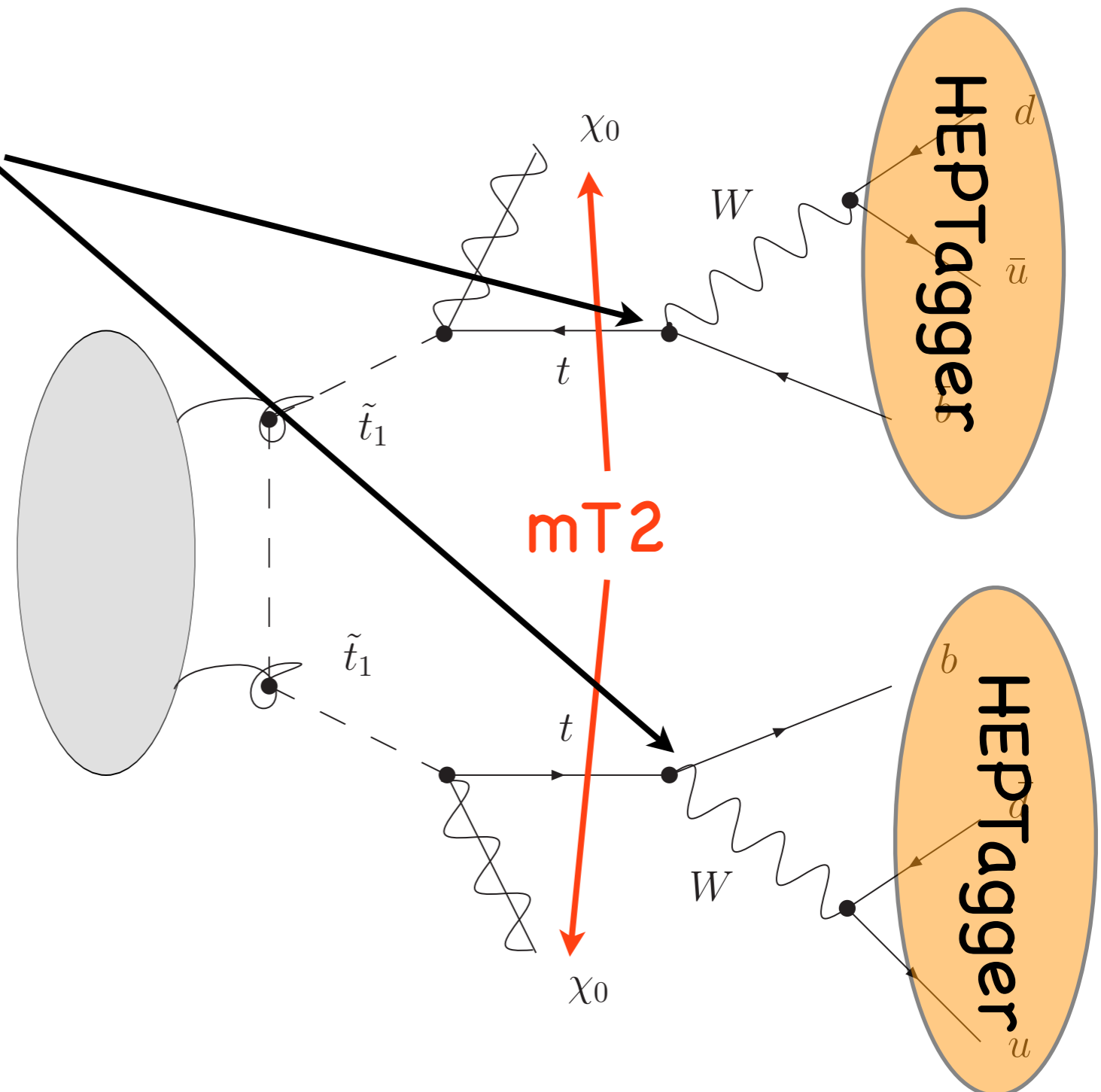
	$R_t$	$ \kappa_t $
Tevatron $\oplus$ LHC[7 TeV]	2.9 TeV <sup>-1</sup> $\sim$ 0.57 $\times$ 10 <sup>-16</sup> cm	0.17
Tevatron $\oplus$ LHC[14 TeV]	2.1 TeV <sup>-1</sup> $\sim$ 0.41 $\times$ 10 <sup>-16</sup> cm	0.07
LHC[14 TeV]: inclusive $\oplus$ boosted top	0.7 TeV <sup>-1</sup> $\sim$ 0.14 $\times$ 10 <sup>-16</sup> cm	0.05

# stop reconstruction using all hadronic top quarks

[ Plehn, MS, Takeuchi, Zerwas JHEP 1010 ]

## Strategy:

- ▶ Use purely **hadronic top decay** mode
- ▶ Use HEPTagger in hadronic final state  $\rightarrow$  2 tagged tops
- ▶ Separation of ISR and hard process improves  $mT2$
- ▶ stop reconstructable over wide range



## mT2 as an observable to look for stops

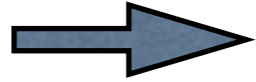
Consider the decay:  $\tilde{t} \rightarrow \chi_1^0 t$

One can express the invariant stop mass squared by:

$$m_{\tilde{t}}^2 = m_t^2 + m_{\chi_1^0}^2 + 2 \left[ E_T^t E_T^{\chi_1^0} \cosh(\Delta y) - \mathbf{p}_T^t \cdot \mathbf{p}_T^{\chi_1^0} \right]$$

Of the invisible LSP only the transverse component could be inferred. Thus use transverse mass:

$$m_T^2(\mathbf{p}_T^t, \mathbf{p}_T^{\chi_1^0}; m_{\chi_1^0}) = m_t^2 + m_{\chi_1^0}^2 + 2 \left( E_T^t E_T^{\chi_1^0} - \mathbf{p}_T^t \cdot \mathbf{p}_T^{\chi_1^0} \right)$$

where  $m_T^2 \leq m_{\tilde{t}}^2$   If  $p^{\chi_1^0}$  known  $m_T$  lower bound for stop mass (see also W mass measurement)

However, in R-parity conserved SUSY mostly squark-pair production, thus two stops decay.

Since only sum of two LSP momenta known, the best one can do is to evaluate

$$\min_{\mathbf{q}_T^{(1)} + \mathbf{q}_T^{(2)} = \mathbf{p}_T^t} \left[ \max \left\{ m_T^2(\mathbf{p}_T^t, \mathbf{q}_T^{(1)}; m_{\chi_1^0}), m_T^2(\mathbf{p}_T^t, \mathbf{q}_T^{(2)}; m_{\chi_1^0}) \right\} \right] \leq m_T$$

with the dummy vectors  $\mathbf{q}_T^{(1)}$  and  $\mathbf{q}_T^{(2)}$

$$m_{T2}^2(\chi) \equiv \min_{\mathbf{q}_T^{(1)} + \mathbf{q}_T^{(2)} = \mathbf{p}_T^t} \left[ \max \left\{ m_T^2(\mathbf{p}_T^t, \mathbf{q}_T^{(1)}; \chi), m_T^2(\mathbf{p}_T^t, \mathbf{q}_T^{(2)}; \chi) \right\} \right]$$

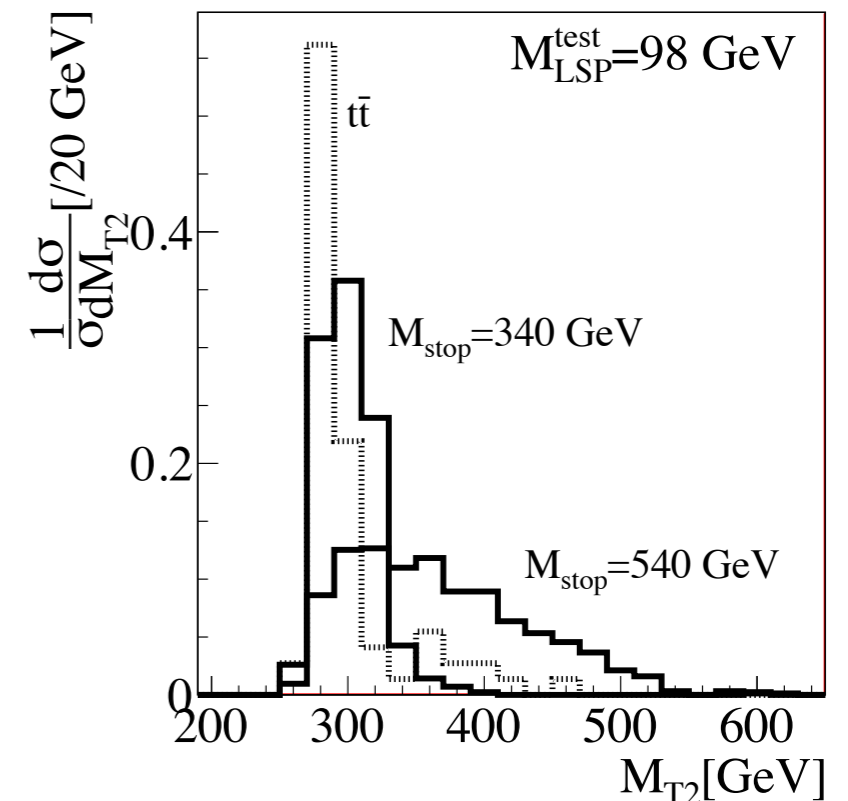
Final definition of  $m_{T2}$ . If neutralino mass not known replace by  $\chi$

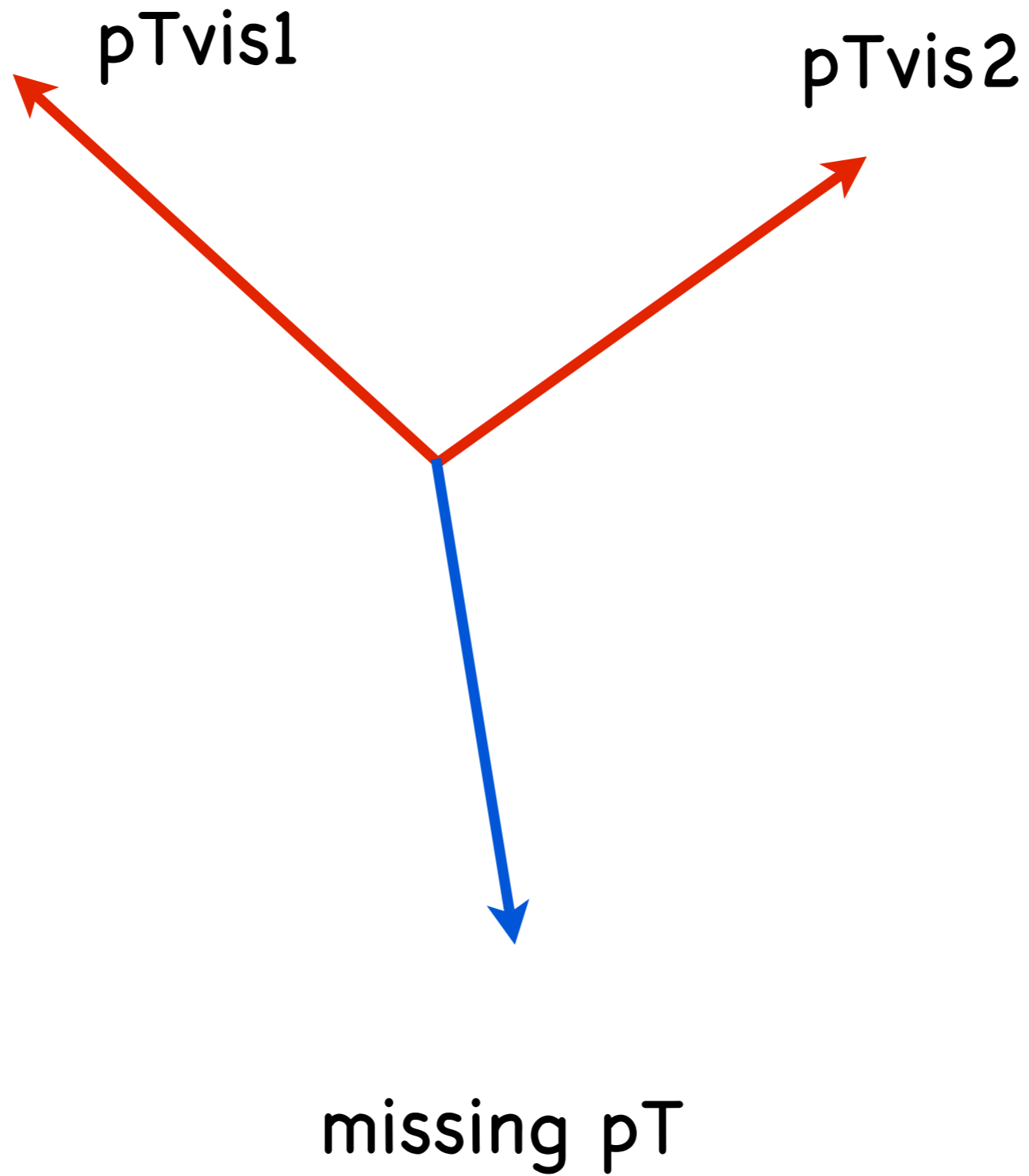
$m_{T2}$  is kinematic endpoint variable:

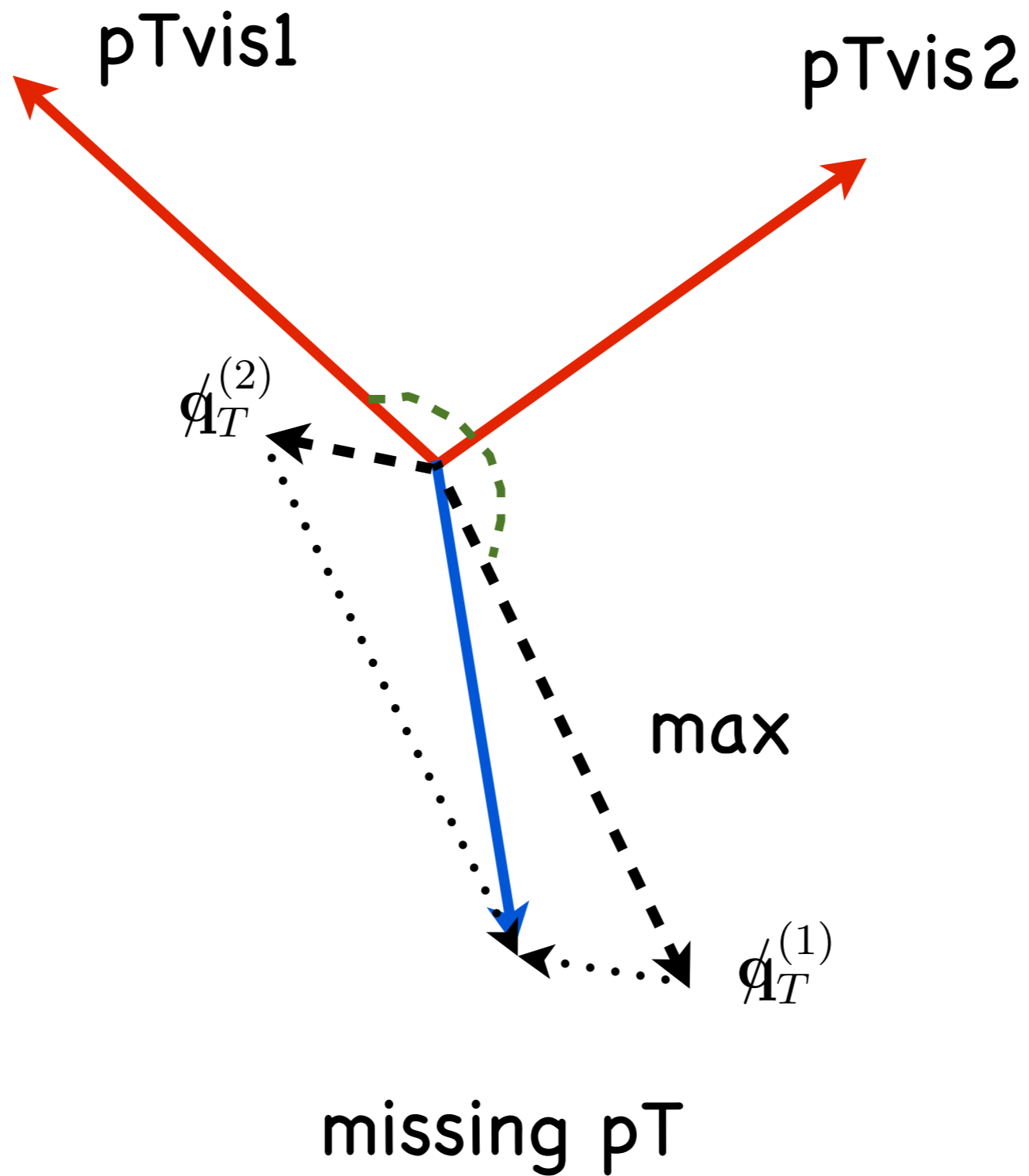
$$m_t + m_{\chi_1^0} \leq m_{T2}(m_{\chi_1^0}) \leq m_{\tilde{t}}$$

$$m_t + \chi \leq m_{T2}(\chi)$$

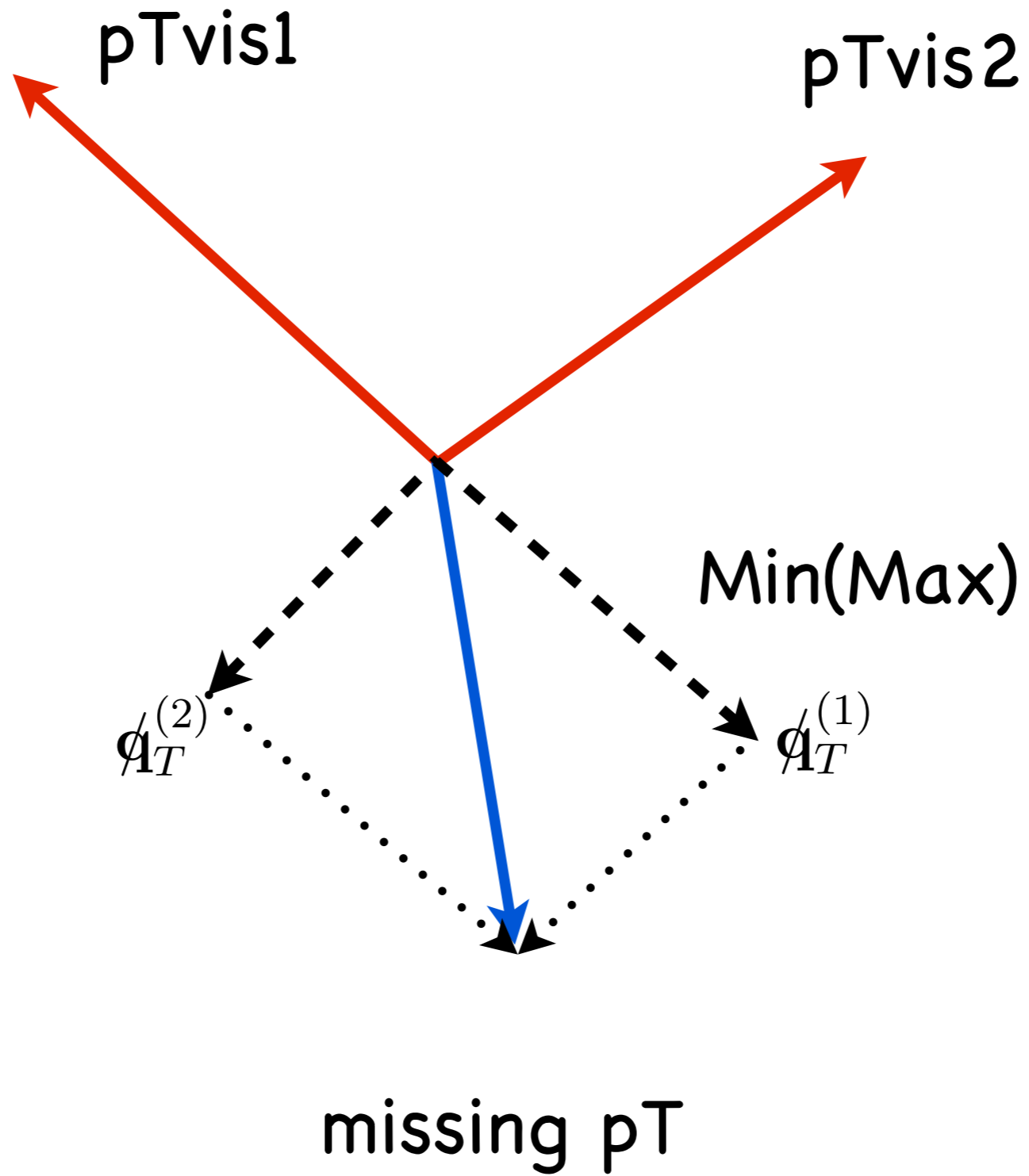
$$\max_{\text{many events}} [m_{T2}(\chi)] = m_t$$











**cuts:** [ Plehn, MS, Takeuchi, Zerwas JHEP 1010]

2 fat jets:  $p_{T,j} > 200/200$  GeV

lepton veto

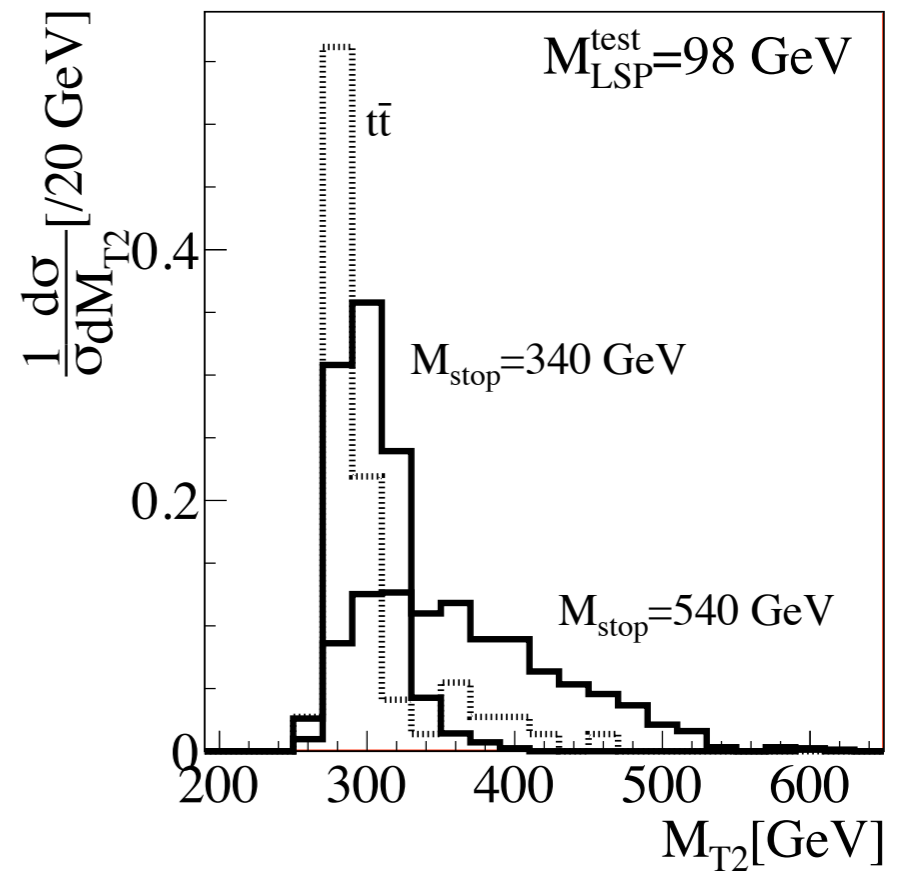
$\cancel{p}_T > 150$  GeV

2 tagged tops:  $p_T^{\text{rec}} > 200/200$  GeV

$b$  tag for 1st tagged top

$m_{T2} > 250$  GeV

$$m_{T2}^2(\chi) \equiv \min_{\cancel{q}_T^{(1)} + \cancel{q}_T^{(2)} = \cancel{p}_T} \left[ \max \left\{ m_T^2(\mathbf{p}_T^{\mathbf{t}^{(1)}}, \cancel{q}_T^{(1)}; \chi), m_T^2(\mathbf{p}_T^{\mathbf{t}^{(2)}}, \cancel{q}_T^{(2)}; \chi) \right\} \right]$$



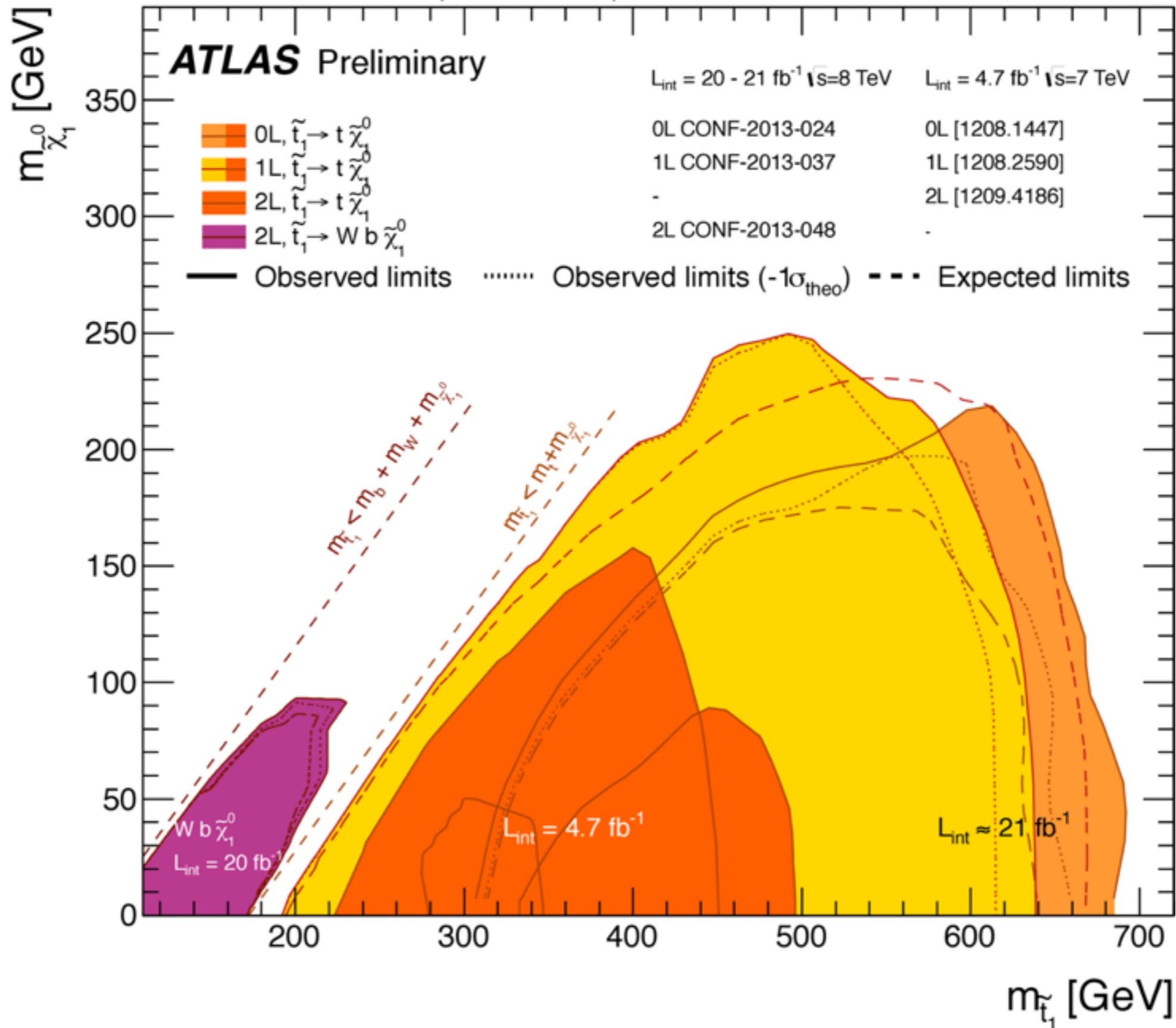
	$\tilde{t}_1 \tilde{t}_1^*$						$t\bar{t}$	QCD	$W$ +jets	$Z$ +jets	$S/B$	$S/\sqrt{B}_{10 \text{ fb}^{-1}}$
$m_{\tilde{t}}[\text{GeV}]$	340	390	440	490	540	640						340
$p_{T,j} > 200$ GeV, $\ell$ veto	728	447	292	187	124	46	87850	$2.4 \cdot 10^7$	$1.6 \cdot 10^5$	n/a	$3.0 \cdot 10^{-5}$	
$\cancel{p}_T > 150$ GeV	283	234	184	133	93	35	2245	$2.4 \cdot 10^5$	1710	2240	$1.2 \cdot 10^{-3}$	
first top tag	100	91	75	57	42	15	743	7590	90	114	$1.2 \cdot 10^{-2}$	
second top tag	15	12.4	11	8.4	6.3	2.3	32	129	5.7	1.4	$8.3 \cdot 10^{-2}$	
$b$ tag	8.7	7.4	6.3	5.0	3.8	1.4	19	2.6	$\lesssim 0.2$	$\lesssim 0.05$	0.40	5.9
$m_{T2} > 250$ GeV	4.3	5.0	4.9	4.2	3.2	1.2	4.2	$\lesssim 0.6$	$\lesssim 0.1$	$\lesssim 0.03$	0.88	6.1

**Tagger +  $m_{T2}$  go well together**

**340 - 540 GeV stop:  $S/B \sim 1$   $S/\sqrt{B}_{10 \text{ fb}^{-1}} \simeq 6$**

$\tilde{t}_1\tilde{t}_1$  production,  $\tilde{t}_1 \rightarrow t \tilde{\chi}_1^0 / \tilde{t}_1 \rightarrow W b \tilde{\chi}_1^0$

Status: LHCP 2013



# Prospects in top physics for the ILC

- Better precision – less noise!
- Likely not to be systematics limited
- Potentially off-shell contributions in  $e^+e^- \rightarrow \bar{t}t$  from heavy resonances
- Improved measurement of all kinds of couplings: anomalous couplings,  $t\bar{t}h$ ,  $hh$ ,  $hbb$ , ... (need at least 500 GeV)
- Improved direct measurement of mass and width
- Polarized beams can enrich tops of specific polarization
- Study QCD radiation, event shapes, jet substructure

# Summary

- The top quark is the new elephant in the room
- In pre-Higgs times we had the EW scale as target range for new physics (top mass, W and Z, Unitarization).  
If not  $\sim 200$  GeV say 3 TeV for composite models
  - Now we don't really!
  - Last guiding principle: Naturalness
  - Top partner search!



(much weaker, prepared to give up, .e.g Split SUSY...)

- Top affects Higgs most and is participating in all interactions
- If Higgs looks SM-like in 3 years from now, it's the top to be looked into