The Higgs Boson

Tilman Plehn

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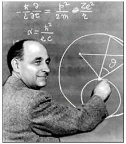
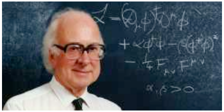
Weak interaction

Massive exchange bosons



– Fermi 1934: weak interactions [$n \to p e^- \bar{\nu}_e$]
  point-like ($2 \to 2$) amplitude $\mathcal{A} \propto G_F E^2$
  unitarity violation [$E < 600$ GeV]
  pre-80s effective theory

– Yukawa 1935: massive particles
  Fermi's theory for $E \ll M$
  modified amplitude $\mathcal{A} \propto g^2 E^2/(E^2 - M^2)$
  unitarity violation in $WW \to WW$ [$E < 1.2$ TeV]
  pre-LHC effective theory



– Higgs 1964: spontaneous symmetry breaking
  unitary through Higgs particle
  particle masses allowed
  fundamental weak-scale scalar

– 't Hooft & Veltman 1971: renormalizability
  no $1/M$ couplings allowed
  theory valid to high energy
  Standard Model with Higgs fundamental

Higgs boson

Two problems for spontaneous gauge symmetry breaking

– problem 1: Goldstone's theorem
  $SU(2)_L \times U(1)_Y \to U(1)_Q$ gives 3 massless scalars
– problem 2: massive gauge theories
  massive gauge bosons have 3 polarizations, and $3 \neq 2$

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Higgs-related papers [also Brout & Englert; Guralnik, Hagen, Kibble]

- 1964: combining two problems to one predictive solution

VOLUME 13, NUMBER 16 PHYSICAL REVIEW LETTERS 19 OCTOBER 1964

BROKEN SYMMETRIES AND THE MASSES OF GAUGE BOSONS

Peter W. Higgs
Tait Institute of Mathematical Physics, University of Edinburgh, Edinburgh, Scotland
(Received 31 August 1964)

In a recent note[1] it was shown that the Goldstone theorem,[2] that Lorentz-covariant field theories in which spontaneous breakdown of symmetry under an internal Lie group occurs contain zero-mass particles, fails if and only if

about the "vacuum" solution $\varphi_1(x) = 0$, $\varphi_2(x) = \varphi_0$:

$$\partial^\mu\{\partial_\mu(\Delta\varphi_1) - e\varphi_0 A_\mu\} = 0, \qquad (2a)$$

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A detailed discussion of these questions will be presented elsewhere.

It is worth noting that an essential feature of the type of theory which has been described in this note is the prediction of incomplete multiplets of scalar and vector bosons.[8] It is to be expected that this feature will appear also in theories in which the symmetry-breaking scalar fields are not elementary dynamic variables but bilinear combinations of Fermi fields.[9]

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$$\partial^\mu\{\partial_\mu(\Delta\varphi_1) - e\varphi_0 A_\mu\} = 0, \quad (2a)$$

[1]P. W. Higgs, to be published.
[2]J. Goldstone, Nuovo Cimento 19, 154 (1961); J. Goldstone, A. Salam, and S. Weinberg, Phys. Rev.

Higgs boson

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PHYSICAL REVIEW VOLUME 145, NUMBER 4 27 MAY 1966

Spontaneous Symmetry Breakdown without Massless Bosons*

PETER W. HIGGS†
Department of Physics, University of North Carolina, Chapel Hill, North Carolina
(Received 27 December 1965)

We examine a simple relativistic theory of two scalar fields, first discussed by Goldstone, in which as a result of spontaneous breakdown of $U(1)$ symmetry one of the scalar bosons is massless, in conformity with the Goldstone theorem. When the symmetry group of the Lagrangian is extended from global to local $U(1)$ transformations by the introduction of coupling with a vector gauge field, the Goldstone boson becomes the longitudinal state of a massive vector boson whose transverse states are the quanta of the transverse gauge field. A perturbative treatment of the model is developed in which the major features of these phenomena are present in zero order. Transition amplitudes for decay and scattering processes are evaluated in lowest order, and it is shown that they may be obtained more directly from an equivalent Lagrangian in which the original symmetry is no longer manifest. When the system is coupled to other systems in a $U(1)$ invariant Lagrangian, the other systems display an induced symmetry breakdown, associated with a partially conserved current which interacts with itself via the massive vector boson.

I. INTRODUCTION

THE idea that the apparently approximate nature of the internal symmetries of elementary-particle physics is the result of asymmetries in the stable solutions of exactly symmetric dynamical equations, rather than an indication of asymmetry in the dynamical

appear have been used by Coleman and Glashow[3] to account for the observed pattern of deviations from $SU(3)$ symmetry.

The study of field theoretical models which display spontaneous breakdown of symmetry under an internal Lie group was initiated by Nambu,[4] who had noticed[5]

Higgs boson

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II. THE MODEL

The Lagrangian density from which we shall work is given by[29]

$$\mathcal{L} = -\tfrac{1}{4} g^{\kappa\mu} g^{\lambda\nu} F_{\kappa\lambda} F_{\mu\nu} - \tfrac{1}{2} g^{\mu\nu} \nabla_\mu \Phi_a \nabla_\nu \Phi_a + \tfrac{1}{4} m_0^2 \Phi_a \Phi_a - \tfrac{1}{8} f^2 (\Phi_a \Phi_a)^2 . \quad (1)$$

In Eq. (1) the metric tensor $g^{\mu\nu} = -1$ ($\mu = \nu = 0$), $+1$ ($\mu = \nu \neq 0$) or 0 ($\mu \neq \nu$), Greek indices run from 0 to 3 and Latin indices from 1 to 2. The $U(1)$-covariant derivatives $F_{\mu\nu}$ and $\nabla_\mu \Phi_a$ are given by

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu ,$$

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$$\mathcal{L} = -\tfrac14 g^{\kappa\mu} g^{\lambda\nu} F_{\kappa\lambda} F_{\mu\nu} - \tfrac12 g^{\mu\nu} \nabla_\mu \Phi_a \nabla_\nu \Phi_a + \tfrac14 m_0^2 \Phi_a \Phi_a - \tfrac18 f^2 (\Phi_a \Phi_a)^2 .$$

In Eq. (1) the metric tensor $g^{\mu\nu} = -1$ ($\mu = \nu$ +1 ($\mu = \nu \neq 0$) or 0 ($\mu \neq \nu$), Greek indices run fro to 3 and Latin indices from 1 to 2. The $U(1)$-covar derivatives $F_{\mu\nu}$ and $\nabla_\mu \Phi_a$ are given by

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu ,$$

i. Decay of a Scalar Boson into Two Vector Bosons

The process occurs in first order (four of the five cubic vertices contribute), provided that $m_0 > 2m_1$. Let p be the incoming and k_1, k_2 the outgoing momenta. Then

$$\begin{aligned} M = i\{ & e[a^{*\mu}(k_1)(-ik_{2\mu})\phi^*(k_2) + a^{*\mu}(k_2)(-ik_{1\mu})\phi^*(k_1)] \\ & - e(ip_\mu)[a^{*\mu}(k_1)\phi^*(k_2) + a^{*\mu}(k_2)\phi^*(k_1)] \\ & - 2em_1 a_\mu^*(k_1) a^{*\mu}(k_2) - f m_0 \phi^*(k_1)\phi^*(k_2)\} . \end{aligned}$$

By using Eq. (15), conservation of momentum, and the transversality $(k_\mu b^\mu(k) = 0)$ of the vector wave functions we reduce this to the form

Higgs boson

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- 1964: combining two problems to one predictive solution
- 1966: original Higgs phenomenology
- 1976 etc: collider phenomenology

A PHENOMENOLOGICAL PROFILE OF THE HIGGS BOSON

John ELLIS, Mary K. GAILLARD * and D.V. NANOPOULOS **
CERN, Geneva

Received 7 November 1975

A discussion is given of the production, decay and observability of the scalar Higgs boson H expected in gauge theories of the weak and electromagnetic interactions such as the Weinberg-Salam model. After reviewing previous experimental limits on the mass of the Higgs boson, we give a speculative cosmological argument for a small mass. If its mass is similar to that of the pion, the Higgs boson may be visible in the reactions $\pi^- p \to Hn$ or $\gamma p \to Hp$ near threshold. If its mass is $\lesssim$300 MeV, the Higgs boson may be present in the decays of kaons with a branching ratio $O(10^{-7})$, or in the decays of one of the new particles: $3.7 \to 3.1 + H$ with a branching ratio $O(10^{-4})$. If its mass is $\lesssim$4 GeV, the Higgs

Higgs boson

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We should perhaps finish with an apology and a caution. We apologize to experimentalists for having no idea what is the mass of the Higgs boson, unlike the case with charm [3,4] and for not being sure of its couplings to other particles, except that they are probably all very small. For these reasons we do not want to encourage big experimental searches for the Higgs boson, but we do feel that people performing experiments vulnerable to the Higgs boson should know how it may turn up.

Higgs
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$\Rightarrow$ Higgs boson predicted from mathematical field theory

Higgs boson

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In terms of Higgs potential

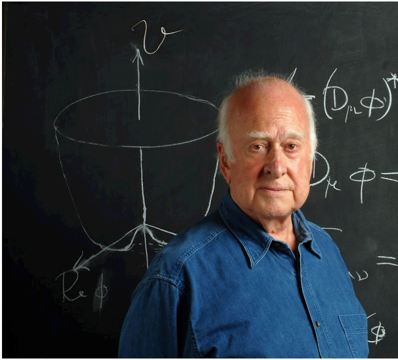
$$V = \mu^2 |\phi|^2 + \lambda |\phi|^4$$

minimum at $\phi = \frac{v}{\sqrt{2}}$

$$\frac{\partial V}{\partial |\phi|^2} = \mu^2 + 2\lambda|\phi|^2 \quad \Rightarrow \quad \frac{v^2}{2} = \frac{-\mu^2}{2\lambda}$$

excitation $\phi = \frac{v + H}{\sqrt{2}}$

$$m_H^2 = \frac{\partial^2 V}{\partial H^2}\bigg|_{\text{minimum}} = 2\lambda v^2$$



Exercise: D6-Higgs potential

Higgs sector including dimension-6 operators

$$\mathcal{L}_{D6} = \sum_{i=1}^{2} \frac{f_i}{\Lambda^2} \mathcal{O}_i \quad \text{with} \quad \mathcal{O}_1 = \frac{1}{2} \partial_\mu (\phi^\dagger \phi) \, \partial^\mu (\phi^\dagger \phi) \; , \quad \mathcal{O}_2 = -\frac{1}{3} (\phi^\dagger \phi)^3$$

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first operator, wave function renormalization

$$\begin{aligned}
\mathcal{O}_1 &= \frac{1}{2} \partial_\mu (\phi^\dagger \phi) \, \partial^\mu (\phi^\dagger \phi) \\
&= \frac{1}{2} \partial_\mu \left(\frac{(\tilde{H} + v)^2}{2} \right) \partial^\mu \left(\frac{(\tilde{H} + v)^2}{2} \right) \\
&= \frac{1}{2} \, (\tilde{H} + v)^2 \, \partial_\mu \tilde{H} \, \partial^\mu \tilde{H}
\end{aligned}$$

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proper normalization of combined kinetic term [LSZ]

$$\mathcal{L}_\text{kin} = \frac{1}{2} \partial_\mu \tilde{H} \partial^\mu \tilde{H} \left(1 + \frac{f_1 v^2}{\Lambda^2} \right) \stackrel{!}{=} \frac{1}{2} \partial_\mu H \, \partial^\mu H \quad \Leftrightarrow \quad H = \tilde{H} \sqrt{1 + \frac{f_1 v^2}{\Lambda^2}}$$

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second operator, potential

$$V = \mu^2 |\phi|^2 + \lambda |\phi|^4 + \frac{f_2}{3\Lambda^2} |\phi|^6$$

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second operator, potential

$$V = \mu^2 |\phi|^2 + \lambda |\phi|^4 + \frac{f_2}{3\Lambda^2} |\phi|^6$$

minimum condition to fix v

$$\frac{v^2}{2} = -\frac{\lambda\Lambda^2}{f_2} \pm \left[\left(\frac{\lambda\Lambda^2}{f_2} \right)^2 - \frac{\mu^2\Lambda^2}{f_2} \right]^{\frac{1}{2}} = \frac{\lambda\Lambda^2}{f_2} \left[-1 \pm \sqrt{1 - \frac{\mu^2 f_2}{\Lambda^2\lambda^2}} \right]$$

$$= \frac{\lambda\Lambda^2}{f_2} \left[-1 \pm \left(1 - \frac{f_2\mu^2}{2\lambda^2\Lambda^2} - \frac{f_2^2\mu^4}{8\lambda^4\Lambda^4} + \mathcal{O}(\Lambda^{-6}) \right) \right]$$

$$= \begin{cases} -\dfrac{\mu^2}{2\lambda} - \dfrac{f_2\mu^4}{8\lambda^3\Lambda^2} + \mathcal{O}(\Lambda^{-4}) = -\dfrac{\mu^2}{2\lambda} \left(1 + \dfrac{f_2\mu^2}{4\lambda^2\Lambda^2} \right) \\ -\dfrac{2\lambda\Lambda^2}{f_2^2} + \mathcal{O}(\Lambda^0) \end{cases}$$

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physical Higgs mass

$$\begin{aligned} \mathcal{O}_2 = -\frac{1}{3} (\phi^\dagger \phi)^3 &= -\frac{1}{3} \frac{(\tilde{H} + v)^6}{8} \\ &= -\frac{1}{24} \left(\tilde{H}^6 + 6 \tilde{H}^5 v + 15 \tilde{H}^4 v^2 + 20 \tilde{H}^3 v^3 + 15 \tilde{H}^2 v^4 + 6 \tilde{H} v^5 + v^6 \right) \end{aligned}$$

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$$\begin{aligned} \mathcal{L}_\text{mass} &= -\frac{\mu^2}{2} \tilde{H}^2 - \frac{3}{2} \lambda v^2 \tilde{H}^2 - \frac{f_2}{\Lambda^2} \frac{15}{24} v^4 \tilde{H}^2 \\ &= -\lambda v^2 \left(1 - \frac{f_1 v^2}{\Lambda^2} + \frac{f_2 v^2}{2\Lambda^2 \lambda} + \mathcal{O}(\Lambda^{-4}) \right) H^2 \stackrel{!}{=} -\frac{m_H^2}{2} H^2 \end{aligned}$$

$$\Leftrightarrow \qquad m_H^2 = 2\lambda v^2 \left(1 - \frac{f_1 v^2}{\Lambda^2} + \frac{f_2 v^2}{2\Lambda^2 \lambda} \right)$$

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Higgs self couplings momentum dependent

$$\begin{aligned} \mathcal{L}_{\text{self}} = & - \frac{m_H^2}{2v} \left[\left(1 - \frac{f_1 v^2}{2\Lambda^2} + \frac{2 f_2 v^4}{3\Lambda^2 m_H^2} \right) H^3 - \frac{2 f_1 v^2}{\Lambda^2 m_H^2} H \, \partial_\mu H \, \partial^\mu H \right] \\ & - \frac{m_H^2}{8v^2} \left[\left(1 - \frac{f_1 v^2}{\Lambda^2} + \frac{4 f_2 v^4}{\Lambda^2 m_H^2} \right) H^4 - \frac{4 f_1 v^2}{\Lambda^2 m_H^2} H^2 \, \partial_\mu H \partial^\mu H \right] \, . \end{aligned}$$

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absorb momentum dependence into field renormalization

$$H = \left(1 + \frac{a_0 \, v^2}{\Lambda^2} \right) \tilde{H} + \frac{a_1 \, v}{\Lambda^2} \tilde{H}^2 + \frac{a_2}{\Lambda^2} \tilde{H}^3$$

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general kinetic term

$$\begin{aligned}
\mathcal{L}_{\text{kin}} &= \frac{1}{2} \partial_\mu H \, \partial^\mu H \\
&= \left(1 + \frac{a_0 v^2}{\Lambda^2} + \frac{2 a_1 v}{\Lambda^2} \tilde{H} + \frac{3 a_2}{\Lambda^2} \tilde{H}^2 \right)^2 \frac{\partial_\mu \tilde{H} \partial^\mu \tilde{H}}{2} \\
&= \left[1 + \frac{2 a_0 v^2}{\Lambda^2} + \frac{4 a_1 v}{\Lambda^2} \tilde{H} + \frac{6 a_2}{\Lambda^2} \tilde{H}^2 + \mathcal{O}(\tilde{H}^3) + \mathcal{O}(\Lambda^{-4}) \right] \frac{\partial_\mu \tilde{H} \partial^\mu \tilde{H}}{2}
\end{aligned}$$

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$$H = \left(1 + \frac{a_0 v^2}{\Lambda^2} \right) \tilde{H} + \frac{a_1 v}{\Lambda^2} \tilde{H}^2 + \frac{a_2}{\Lambda^2} \tilde{H}^3$$

general kinetic term

$$\begin{aligned} \mathcal{L}_{\text{kin}} &= \frac{1}{2} \partial_\mu H \, \partial^\mu H \\ &= \left(1 + \frac{a_0 v^2}{\Lambda^2} + \frac{2 a_1 v}{\Lambda^2} \tilde{H} + \frac{3 a_2}{\Lambda^2} \tilde{H}^2 \right)^2 \frac{\partial_\mu \tilde{H} \partial^\mu \tilde{H}}{2} \\ &= \left[1 + \frac{2 a_0 v^2}{\Lambda^2} + \frac{4 a_1 v}{\Lambda^2} \tilde{H} + \frac{6 a_2}{\Lambda^2} \tilde{H}^2 + \mathcal{O}(\tilde{H}^3) + \mathcal{O}(\Lambda^{-4}) \right] \frac{\partial_\mu \tilde{H} \partial^\mu \tilde{H}}{2} \end{aligned}$$

canonically normalized Higgs field

$$H = \left(1 + \frac{f_1 v^2}{2\Lambda^2} \right) \tilde{H} + \frac{f_1 v}{2\Lambda^2} \tilde{H}^2 + \frac{f_1}{6\Lambda^2} \tilde{H}^3 + \mathcal{O}(\tilde{H}^4)$$

Higgs signatures

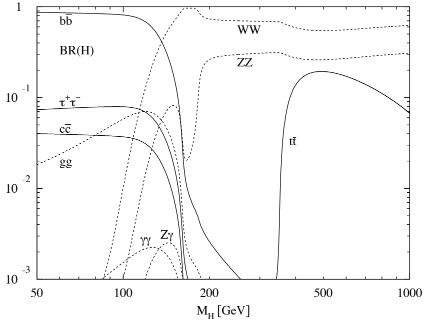
Higgs decays easy [Hdecay]

– weak-scale scalar coupling proportional to mass

– off-shell decays below threshold

– decay to $\gamma\gamma$ via W and top loop [destructive interference]

$\Rightarrow$ $m_H = 126$ GeV perfect



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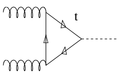
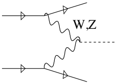
Higgs production hard [7-8 TeV, 5-15/fb]

– quantum effects needed

gluon fusion production loop induced [$\sigma \sim 15000$ fb]
weak boson fusion production with jets [$\sigma \sim 1200$ fb]





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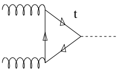

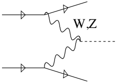

- easy channels for 2011-2012

  $pp \to H \to ZZ \to 4\ell$ fully reconstructed
  $pp \to H \to \gamma\gamma$ fully reconstructed
  $pp \to H \to WW \to (\ell^-\bar{\nu})(\ell^+\nu)$ large BR

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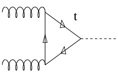

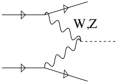

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$\Rightarrow$ fun still waiting

$pp \to H \to \tau\tau$ plus jets
$pp \to ZH \to (\ell^+ \ell^-)(b\bar{b})$ boosted
$pp \to t\bar{t}H$ waiting for a good idea...

Higgs discovery

4th of July fireworks [no theory input needed beyond basic Pythia/Herwig]

- ‘silver channel’ $H \to \gamma\gamma$
  local significance 4.5σ (ATLAS), 4.1σ (CMS)
- ‘golden channel’ $H \to ZZ \to 4\ell$
  local significance 3.4σ (ATLAS), 3.2σ (CMS)
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- combined 5.0σ (ATLAS), 4.9σ (CMS) [LEE 4.3σ]

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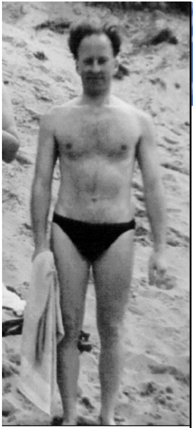

A sure sighting of a higgs... Peter Higgs on the shores of the Firth of Fourth by Prof J D Jackson, July 1960

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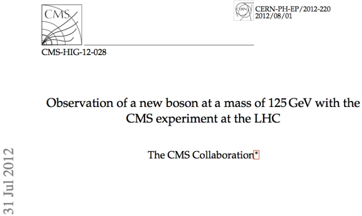


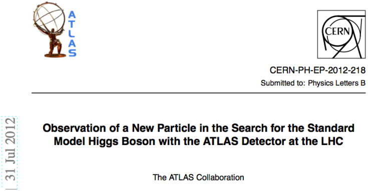
CMS-HIG-12-028

CERN-PH-EP/2012-220
2012/08/01

Observation of a new boson at a mass of 125 GeV with the CMS experiment at the LHC

The CMS Collaboration*

31 Jul 2012



CERN-PH-EP-2012-218
Submitted to: Physics Letters B

Observation of a New Particle in the Search for the Standard Model Higgs Boson with the ATLAS Detector at the LHC

The ATLAS Collaboration

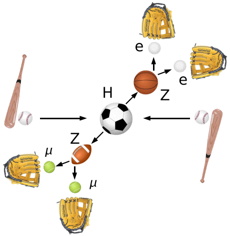
31 Jul 2012

Questions

1. What is the 'Higgs' Lagrangian?

   – psychologically: looked for Higgs, so found a Higgs

   – CP-even spin-0 scalar expected
   spin-1 vector unlikely
   spin-2 graviton unexpected



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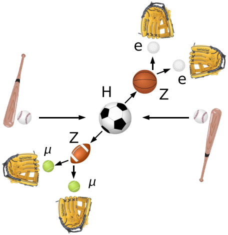

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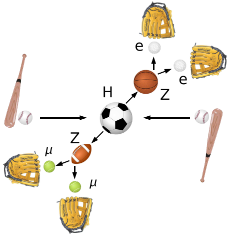

2. What are the coupling values?

   – 'coupling' after fixing operator basis

   – Standard Model Higgs vs anomalous couplings

3. What does all this tell us?

   – models predicting weak-scale new physics?

   – renormalization group based Hail-Mary passes?

Higher-dimensional vs renormalizable

Light Higgs as a Goldstone boson [Giudice, Grojean, Pomarol, Rattazzi]

– strongly interacting models predicting heavy broad resonance(s)
– light state if protected by Goldstone's theorem [Georgi & Kaplan]
– interesting if $v \ll f < 4\pi f \sim m_\rho$ [little Higgs $v \sim g^2 f/(2\pi)$]
– adding D6 weak operators with relative strengths

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$$\begin{aligned}
\mathcal{L}_{\rm SILH} = & \frac{c_H}{2f^2}\partial^\mu \left(H^\dagger H\right)\partial_\mu \left(H^\dagger H\right) + \frac{c_T}{2f^2}\left(H^\dagger \overleftrightarrow{D^\mu} H\right)\left(H^\dagger \overleftrightarrow{D}_\mu H\right) \\
& - \frac{c_6 \lambda}{f^2}\left(H^\dagger H\right)^3 + \left(\frac{c_y y_f}{f^2} H^\dagger H \bar{f}_L H f_R + \text{h.c.}\right) \\
& + \frac{i c_W g}{2 m_\rho^2}\left(H^\dagger \sigma^i \overleftrightarrow{D^\mu} H\right)\left(D^\nu W_{\mu\nu}\right)^i + \frac{i c_B g'}{2 m_\rho^2}\left(H^\dagger \overleftrightarrow{D^\mu} H\right)\left(\partial^\nu B_{\mu\nu}\right) \\
& + \frac{i c_{HW} g}{16\pi^2 f^2}(D^\mu H)^\dagger \sigma^i (D^\nu H) W^i_{\mu\nu} + \frac{i c_{HB} g'}{16\pi^2 f^2}(D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\
& + \frac{c_\gamma g'^2}{16\pi^2 f^2}\frac{g^2}{g_\rho^2} H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{c_g g_S^2}{16\pi^2 f^2}\frac{y_t^2}{g_\rho^2} H^\dagger H G^a_{\mu\nu} G^{a\mu\nu} .
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& - \frac{c_6}{(3f)^2} \left(H^\dagger H \right)^3 + \left(\frac{c_y y_f}{f^2} H^\dagger H \bar{f}_L H f_R + \text{h.c.} \right) \\
& + \frac{i c_W}{(16f)^2} \left(H^\dagger \sigma^i \overleftrightarrow{D^\mu} H \right) (D^\nu W_{\mu\nu})^i + \frac{i c_B}{(16f)^2} \left(H^\dagger \overleftrightarrow{D^\mu} H \right) (\partial^\nu B_{\mu\nu}) \\
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& + \frac{c_\gamma}{(256f)^2} H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{c_g}{(256f)^2} H^\dagger H G^a_{\mu\nu} G^{a\mu\nu} .
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Anomalous Higgs couplings [Hagiwara etal; Corbett, Eboli, Gonzales-Fraile, Gonzales-Garcia]

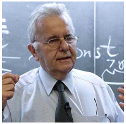
– assume Higgs is largely Standard Model
– additional higher-dimensional couplings

$$\begin{aligned}\mathcal{L}_{\text{eff}} = &- \frac{\alpha_s v}{8\pi}\frac{f_g}{\Lambda^2}(\Phi^\dagger\Phi)G_{\mu\nu}G^{\mu\nu} + \frac{f_{WW}}{\Lambda^2}\Phi^\dagger W_{\mu\nu}W^{\mu\nu}\Phi \\ &+ \frac{f_W}{\Lambda^2}(D_\mu\Phi)^\dagger W^{\mu\nu}(D_\nu\Phi) + \frac{f_B}{\Lambda^2}(D_\mu\Phi)^\dagger B^{\mu\nu}(D_\nu\Phi) + \frac{f_{WWW}}{\Lambda^2}\text{Tr}(W_{\mu\nu}W^{\nu\rho}W_\rho^\mu) \\ &+ \frac{f_b}{\Lambda^2}(\Phi^\dagger\Phi)(\overline{Q}_3\Phi d_{R,3}) + \frac{f_\tau}{\Lambda^2}(\Phi^\dagger\Phi)(\overline{L}_3\Phi e_{R,3})\end{aligned}$$

– plus e-w precision data and triple gauge couplings

$\Rightarrow$ remember what your operators are!

Lagrangian



Angular correlations

– Cabibbo–Maksymowicz–Dell'Aquila–Nelson angles for $H \to ZZ$

[Melnikov etal; Lykken etal; v d Bij etal; Choi etal; Englert, Spannowsky, Takeuchi]

$$\cos\theta_e = \hat{p}_{e^-} \cdot \hat{p}_{Z_\mu}\Big|_{Z_e} \qquad \cos\theta_\mu = \hat{p}_{\mu^-} \cdot \hat{p}_{Z_e}\Big|_{Z_\mu} \qquad \cos\theta^* = \hat{p}_{Z_e} \cdot \hat{p}_{\text{beam}}\Big|_X$$

$$\cos\phi_e = (\hat{p}_{\text{beam}} \times \hat{p}_{Z_\mu}) \cdot (\hat{p}_{Z_\mu} \times \hat{p}_{e^-})\Big|_{Z_e}$$

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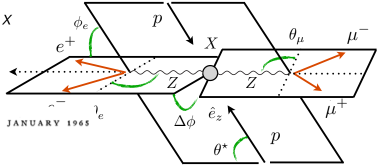


PHYSICAL REVIEW VOLUME 137, NUMBER 2B 25 JANUARY 1965

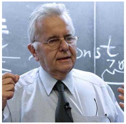
Angular Correlations in K_{e4} Decays and Determination of Low-Energy π-π Phase Shifts*

NICOLA CABIBBO† AND ALEXANDER MAKSYMOWICZ
Lawrence Radiation Laboratory, University of California, Berkeley, California
(Received 1 September 1964)

The study of correlations in K_{e4} decays can give unique information on low-energy π-π scattering. To this end we introduce a particularly simple set of correlations. We show that the measurement of these correlations at any fixed π-π c.m. energy allows one to make a model-independent determination of the difference δ_0-δ_1 between the S- and P-wave π-π phase shifts at that energy. Information about the average value of δ_0-δ_1 can be obtained from a measurement of the same correlations averaged over the energy spectrum. Measurement of the average correlations is particularly suited to the testing of any model of low-energy π-π scattering. We discuss in particular two such models: (a) the Chew-Mandelstam effective-range description of S-wave scattering and (b) the Brown-Faier σ-resonance model for the S wave. If the Chew-Mandelstam description is adequate, the suggested measurements should yield a value for the S-wave scattering length in the $I=0$ state. If the σ-resonance model is correct, these measurements should yield a value for the mass of the resonance.

Lagrangian

Angular correlations



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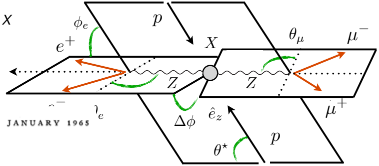

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* This work was done under the auspices of the U. S. Atomic Energy Commission.

† On leave from the Frascati National Laboratory, Frascati, Italy; present address: CERN, Geneva, Switzerland.

[1] L. B. Okun' and E. P. Shabalin, Zh. Eksperim. i Teor. Fiz. **37**, 1775 (1959) [English transl.: Soviet Phys.—JETP **10**, 1252 (1960)].

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[4] E. P. Shabalin, Zh. Eksperim. i Teor. Fiz. **39**, 345 (1960) [English transl.: Soviet Phys.—JETP **12**, 245 (1961)].

[5] R. W. Birge, R. P. Ely, G. Gidal, G. E. Kalmus, A. Kernan, W. M. Powell, U. Camerini, W. F. Fry, J. Gaidos, R. H. March, and S. Natali, Phys. Rev. Letters **11**, 35 (1963). Members of this group have kindly communicated to us that the total of 11 events reported in this paper has now increased to at least 80.

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[7] L. M. Brown and H. Faier, Phys. Rev. Letters **12**, 514 (1964).

[8] B. A. Arbuzov, Nguyen Van Hieu, and R. N. Faustov, Zh. Eksperim. i Teor. Fiz. **44**, 329 (1963) [English transl.: Soviet Phys.—JETP **17**, 225 (1963)].

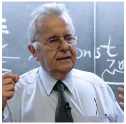
dominated by the postulated σ resonance. Measurement of average correlations could then be used to determine the mass of this resonance.

II. KINEMATICS AND CORRELATIONS

Our approach to the kinematics of the reaction $K^+ \to \pi^+\pi^- e^+\nu$ is the same as that used in analyzing resonances. We visualize this reaction as a two-body decay into a dipion of mass $M_{\pi\pi}$ and a dilepton of mass $M_{e\nu}$. We then consider the subsequent decay of each of these two "resonances" in its own center-of-mass system.

[9] The usefulness of angular correlations in the determination of $\delta_0-\delta_1$ was first recognized by E. P. Shabalin, Zh. Eksperim. i Teor. Fiz. 44, 765 (1963) [English transl.: Soviet Phys.—JETP **17**, 517 (1963)]. See also erratum, Zh. Eksperim. i Teor. Fiz. **45**, 2085 (1963).

Lagrangian



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– Breit frame or hadron collider (η, ϕ) in WBF [Breit: boost into space-like]

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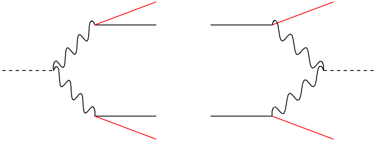

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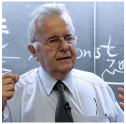

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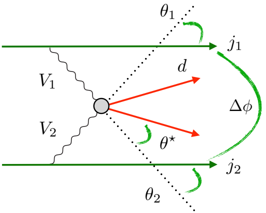
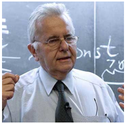
$$\cos\phi_1 = (\hat{p}_{V_2} \times \hat{p}_d) \cdot (\hat{p}_{V_2} \times \hat{p}_{j_1}) \Big|_{V_1 \text{Breit}}$$

$$\cos\Delta\phi = (\hat{p}_{q_1} \times \hat{p}_{j_1}) \cdot (\hat{p}_{q_2} \times \hat{p}_{j_2}) \Big|_X \, .$$



Lagrangian



Angular correlations

– Cabibbo–Maksymowicz–Dell'Aquila–Nelson angles for $H \to ZZ$

[Melnikov etal; Lykken etal; v d Bij etal; Choi etal; Englert, Spannowsky, Takeuchi]

– Breit frame or hadron collider (η, ϕ) in WBF [Breit: boost into space-like]

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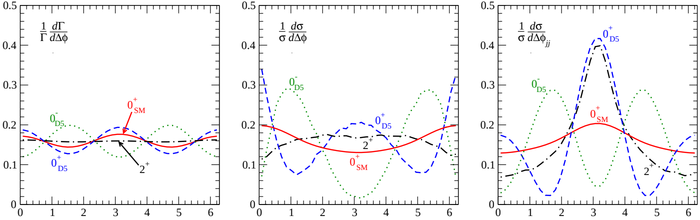
– possible scalar couplings

$$\mathcal{L} \supset (\phi^\dagger \phi) W^\mu W_\mu \qquad \frac{1}{\Lambda^2} (\phi^\dagger \phi) W^{\mu\nu} W_{\mu\nu} \qquad \frac{1}{\Lambda^2} (\phi^\dagger \phi) \epsilon_{\mu\nu\rho\sigma} W^{\mu\nu} W^{\rho\sigma}$$

$\Rightarrow$ different channels, same physics



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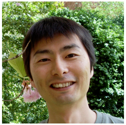

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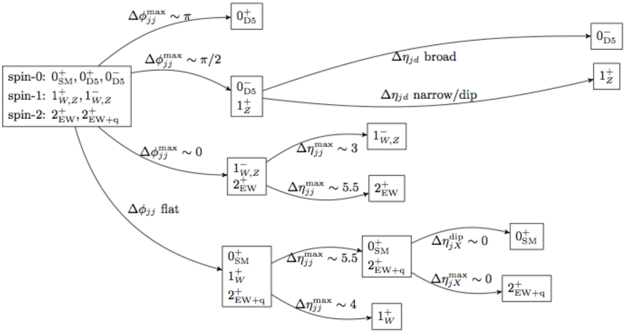
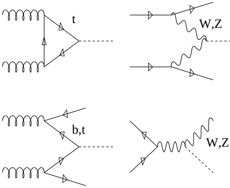


Couplings



Standard-Model-inspired model

- assume: narrow CP-even scalar
  Standard Model operators
  couplings proportional to masses?
- couplings from production & decay rates

$$\begin{array}{|l|}\hline gg \to H \\ qq \to qqH \\ gg \to t\bar{t}H \\ qq' \to VH \\ \hline\end{array} \quad \longleftrightarrow \quad \boxed{g_{HXX} = g_{HXX}^{\text{SM}} \; (1 + \Delta_X)} \quad \longleftrightarrow \quad \begin{array}{|l|}\hline H \to ZZ \\ H \to WW \\ H \to b\bar{b} \\ H \to \tau^+\tau^- \\ H \to \gamma\gamma \\ \hline\end{array}$$

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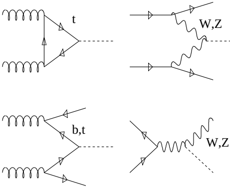

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Total width

- myths about scaling

$$N = \sigma\, BR \propto \frac{g_p^2}{\sqrt{\Gamma_{\text{tot}}}} \; \frac{g_d^2}{\sqrt{\Gamma_{\text{tot}}}} \sim \frac{g^4}{g^2 \dfrac{\sum \Gamma_i(g^2)}{g^2} + \Gamma_{\text{unobs}}} \stackrel{g^2 \to 0}{\longrightarrow} = 0$$

  gives constraint from $\sum \Gamma_i(g^2) < \Gamma_{\text{tot}} \to \Gamma_H|_{\text{min}}$
- $WW \to WW$ unitarity: $g_{WWH} \lesssim g_{WWH}^{\text{SM}} \to \Gamma_H|_{\text{max}}$
- SFitter assumption $\Gamma_{\text{tot}} = \sum_{\text{obs}} \Gamma_j$ [plus generation universality]

Error analysis

Sources of uncertainty

- statistical error: Poisson
  systematic error: Gaussian, if measured
  theory error: not Gaussian
- simple argument
  LHC rate 10% off: no problem
  LHC rate 30% off: no problem
  LHC rate 300% off: Standard Model wrong
- theory likelihood flat centrally and zero far away
- profile likelihood construction: RFit [CKMFitter]

$$-2 \log \mathcal{L} = \chi^2 = \vec{\chi}_d^T \; C^{-1} \; \vec{\chi}_d$$

$$\chi_{d,i} = \begin{cases} 0 & |d_i - \bar{d}_i| < \sigma_i^{\text{(theo)}} \\ \dfrac{|d_i - \bar{d}_i| - \sigma_i^{\text{(theo)}}}{\sigma_i^{\text{(exp)}}} & |d_i - \bar{d}_i| > \sigma_i^{\text{(theo)}} \end{cases}$$

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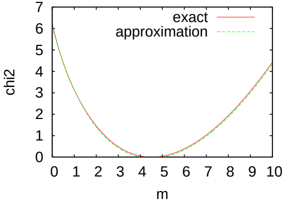
Efficient combination of errors [different from Michael's ATLAS analysis]

- Gaussian ⊗ Gaussian: half width added in quadrature
  Gaussian/Poisson ⊗ flat: RFit scheme
  Gaussian ⊗ Poisson: ??
- approximate formula

$$\frac{1}{\log\mathcal{L}_{\text{comb}}} = \frac{1}{\log\mathcal{L}_{\text{Gauss}}} + \frac{1}{\log\mathcal{L}_{\text{Poisson}}}$$

⇒ error bars from toy measurements



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Systematic uncertainties

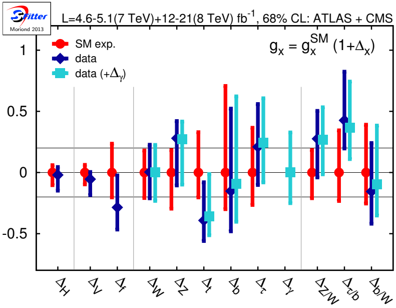
luminosity measurement	5 %
detector efficiency	2 %
lepton reconstruction efficiency	2 %
photon reconstruction efficiency	2 %
WBF tag-jets / jet-veto efficiency	5 %
b-tagging efficiency	3 %
τ-tagging efficiency (hadronic decay)	3 %
lepton isolation efficiency ($H \to 4\ell$)	3 %

	$\Delta B^{\text{(syst)}}$
$H \to ZZ$	1%
$H \to WW$	5%
$H \to \gamma\gamma$	0.1%
$H \to \tau\tau$	5%
$H \to b\bar{b}$	10%

Couplings now and in the future

Now [Aspen/Moriond 2013]

- focus SM-like [secondary solutions possible]
- six couplings and ratios from data
  g_b from width
  g_g vs g_t not yet possible
  [similar: Ellis etal, Djouadi etal, Strumia etal, Grojean etal]
- poor man's analyses: $\Delta_H, \Delta_V, \Delta_f$
- Tevatron $H \to b\bar{b}$ with little impact



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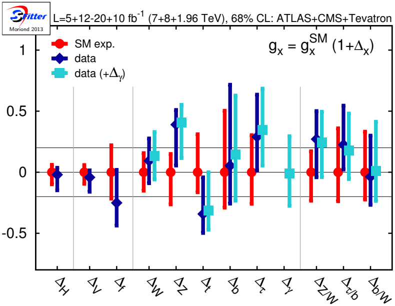

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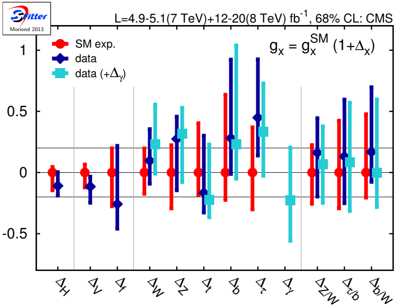

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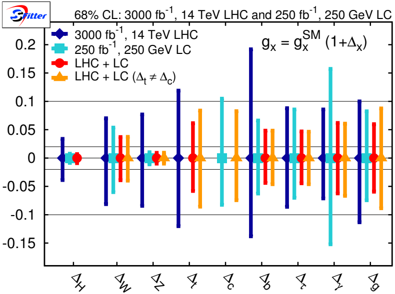
Future

- LHC extrapolations unclear
- theory extrapolations tricky
- ILC case obvious [500 GeV for now]
- interplay in loop-induced couplings



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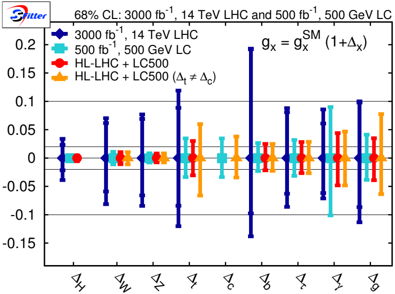

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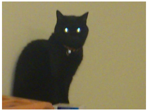
– fundamental advantages in $e^+e^- \to ZH$:

unobserved decays avoided
width measured from rates including σ_{ZH}
$H \to c\bar{c}$ accessible
invisible decays hugely improved

Meaning



TeV-scale scenarios

- fourth chiral generation excluded
- strongly interacting models retreating [Goldstone protection]
- extended Higgs sectors wide open
- no final verdict on the MSSM
- hierarchy problem worse than ever [light fundemental scalar discovered]

$\Rightarrow$ do not know

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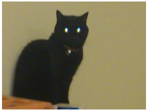

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High scales

– Planck-scale extrapolation [Holthausen, Lim, Lindner]

$$\frac{d\lambda}{d\log Q^2} = \frac{1}{16\pi^2}\left[12\lambda^2 + 6\lambda\lambda_t^2 - 3\lambda_t^4 - \frac{3}{2}\lambda\left(3g_2^2 + g_1^2\right) + \frac{3}{16}\left(2g_2^4 + (g_2^2 + g_1^2)^2\right)\right]$$

– vacuum stability right at edge
– IR fixed point for λ/λ_t^2 fixing m_H^2/m_t^2 [with gravity: Shaposhnikov, Wetterich]

$$m_H = 126.3 + \frac{m_t - 171.2}{2.1}\times 4.1 - \frac{\alpha_s - 0.1176}{0.002}\times 1.5$$

– IR fixed points experimental nightmare

$\Rightarrow$ do not know

Exercise: top–Higgs renormalization group

Running of coupling/mass ratios

RGE for Higgs self coupling and top Yukawa

$$\frac{d\,\lambda}{d\,\log Q^2} = \frac{1}{16\pi^2}\left(12\lambda^2 + 6\lambda y_t^2 - 3y_t^4\right) \qquad \frac{d\,y_t^2}{d\,\log Q^2} = \frac{9}{32\pi^2}\,y_t^4$$

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running of ratio $R = \lambda/y_t^2$

$$\begin{aligned}
\frac{dR}{d\log Q^2} &= \frac{d\lambda}{d\log Q^2}\,\frac{1}{y_t^2} + \lambda\frac{(-1)}{y_t^4}\,\frac{dy_t^2}{d\log Q^2} \\
&= \frac{1}{16\pi^2 y_t^2}\left(12\lambda^2 + 6\lambda y_t^2 - 3y_t^4\right) - \frac{1}{16\pi^2}\frac{9\lambda}{2} \\
&= \frac{3\lambda}{32\pi^2 R}\,\left(8R^2 + R - 2\right) \stackrel{!}{=} 0 \qquad \Leftrightarrow \qquad R_* = \frac{\sqrt{65}-1}{16} \simeq 0.44
\end{aligned}$$

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numbers in the far infrared, better for $Q \sim m_t$

$$\frac{\lambda}{y_t^2} = \frac{m_H^2}{2v^2}\,\frac{v^2}{2m_t^2}\bigg|_{\text{IR}} = \frac{m_H^2}{4m_t^2}\bigg|_{\text{IR}} = 0.44 \qquad \Leftrightarrow \qquad \frac{m_H}{m_t}\bigg|_{\text{IR}} = 1.33$$

Big and small questions for the LHC and ILC

Big

– is it really the Standard Model Higgs?

– is there space for new physics outside the Higgs sector?

Small

– what are good alternative test hypotheses?

– how can we improve the couplings fit precision?

– how can we measure the bottom Yukawa?

– how can we measure the top Yukawa?

– how can we measure the Higgs self coupling?

– which backgrounds do we need to know better?

– ...

Lectures on LHC Physics, Springer, arXiv:0910.4182 updated under `www.thphys.uni-heidelberg.de/~plehn/`