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東京大学 国際高等研究所 カブリ数物連携宇宙研究機構
KAVLI INSTITUTE FOR THE PHYSICS AND MATHEMATICS OF THE UNIVERSE

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NEUTRINO TRIDENT PRODUCTION

A SHORT REVIEW

Matheus Hostert

IPPP, Durham University, UK



Outline

Intro

Neutrino trident scattering cross section

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Neutrino trident scattering cross section

Measurement in neutrino experiments (past, present and future)

Outline

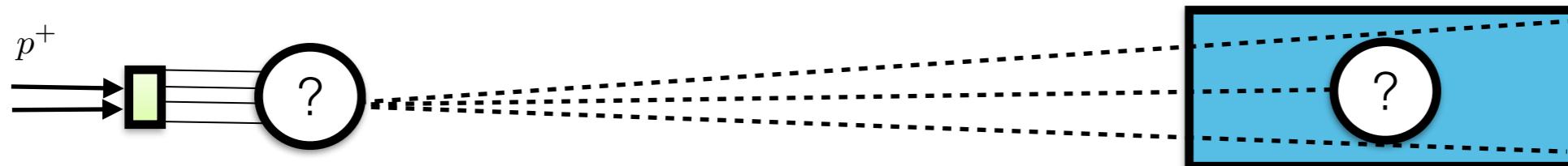
Intro

Neutrino trident scattering cross section

Measurement in neutrino experiments (past, present and future)

New physics
Z's and other sources of multi-lepton signatures

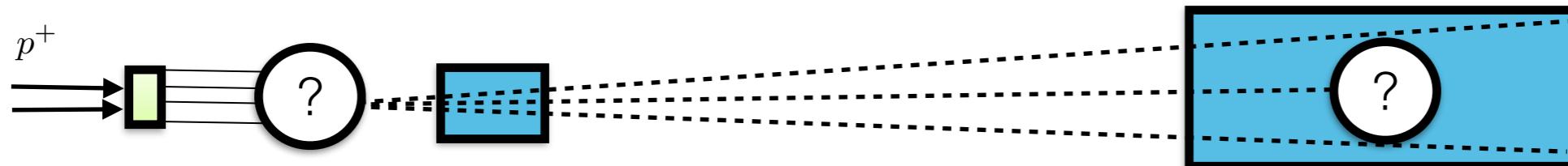
Oscillation experiments — precision era



Flux uncertainties are large
(hadro-production and focusing)
> 8% at the NuMI beam

Neutrino-nucleus cross sections:
nuclear physics + lack of data

Oscillation experiments — precision era



Flux uncertainties are large
(hadro-production and focusing)
> 8% at the NuMI beam

Neutrino-nucleus cross sections:
nuclear physics + lack of data

Beating systematics for
precision on oscillation



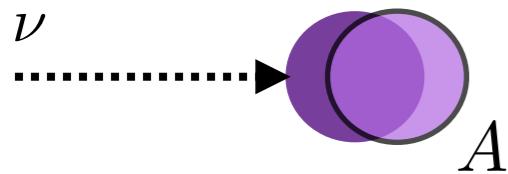
Near detectors
Typically > 10^5 interactions

Physics of the 70-90's... but harder.
(GeV neutrino energies/nuclear targets/precision)

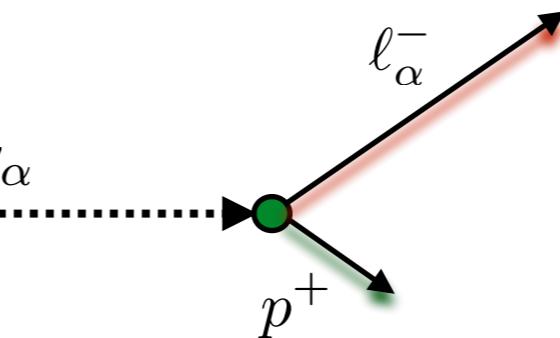
Neutrino interactions

CEvNS

- Large cross section
- NC only
- Low energy recoil



$$\sim 10^{-38} \text{ cm}^2$$



$$\sim 10^{-38} \text{ cm}^2$$

Neutrino-electron

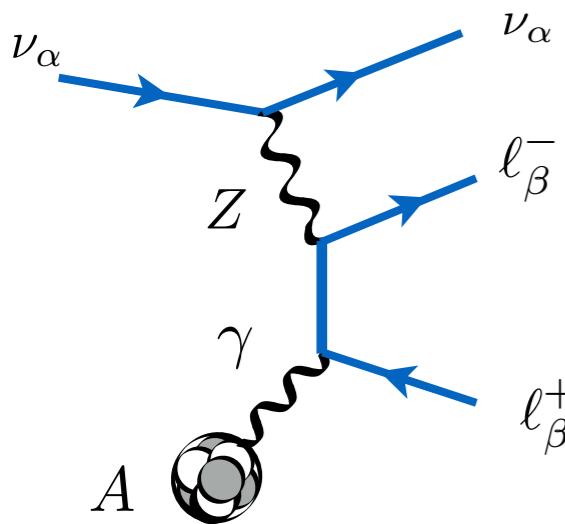
- Low statistics
- NC or NC+CC
- Fundamental couplings



$$\sim 10^{-41} \text{ cm}^2$$

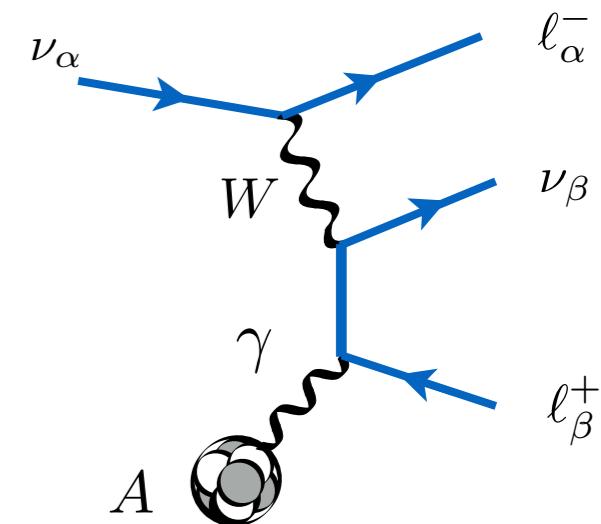
- Weak force in isolation
- Small G_F — sensitive to light new physics

Neutrino trident production



Neutrino trident production/scattering:
Neutrino charged lepton production in the
Coulomb field of a nucleus*.

$$\sim 10^{-44} \text{ cm}^2$$

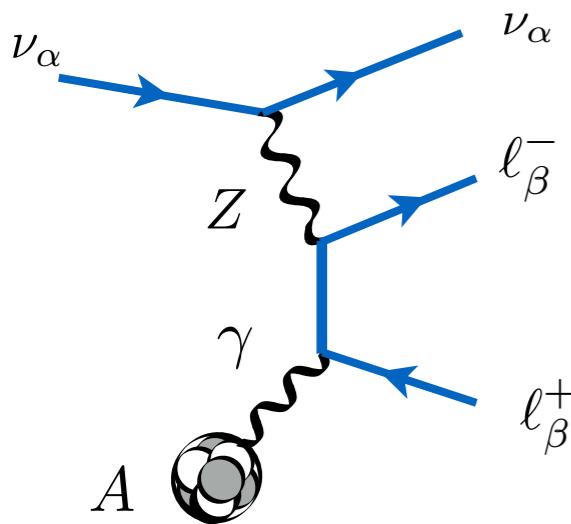


why?

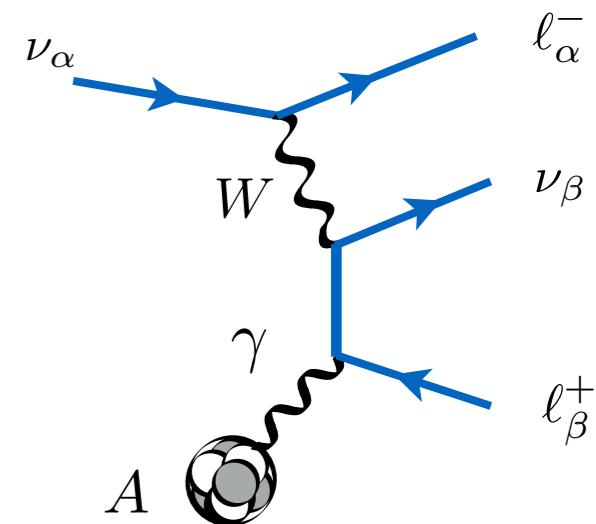
- 1) Sensitive to neutrino interactions with the charged-leptons.
- 2) Well understood cross section with distinct final state.

* Usually extended to include contributions from nucleons and quarks.

Neutrino trident production



Neutrino trident production/scattering:
Neutrino charged lepton production in the Coulomb field of a nucleus.



Very crude approximation for the total cross section:

$$\sigma_\Psi \approx (g_V^2 + g_A^2) \frac{Z^2 \alpha^2 G_F^2}{9\pi^3} \log \left(\frac{2E_\nu \Lambda_{\text{QCD}}}{4m_\ell^2 A^{1/3}} \right) \frac{2E_\nu \Lambda_{\text{QCD}}}{A^{1/3}}$$

Channel	SM Contributions	g_V	g_A
$\nu_\mu \rightarrow \nu_\mu \mu^+ \mu^-$	CC, NC	$1/2 + 2s_w^2$	$1/2$
$\nu_\mu \rightarrow \nu_\mu e^+ e^-$	NC	$-1/2 + 2s_w^2$	$-1/2$
$\nu_\mu \rightarrow \nu_e e^+ \mu^-$	CC	1	1

$$\frac{(g_V^2 + g_A^2)_{\text{CC+NC}}}{(g_V^2 + g_A^2)_{\text{CC}}} \approx 0.60 \longrightarrow \text{NC+CC destructive interference.}$$

Old history

V-A theory

Total cross section calculation within V-A theory

W. Czyz et al, 1964
(Nuovo Cim. 34 404-435)

Kinematical distributions

{ J. Lovseth et al, 1971
Phys. Rev. D3 2686-2706

K. Fujikawa, 1971
Annals Phys. 68 102-162

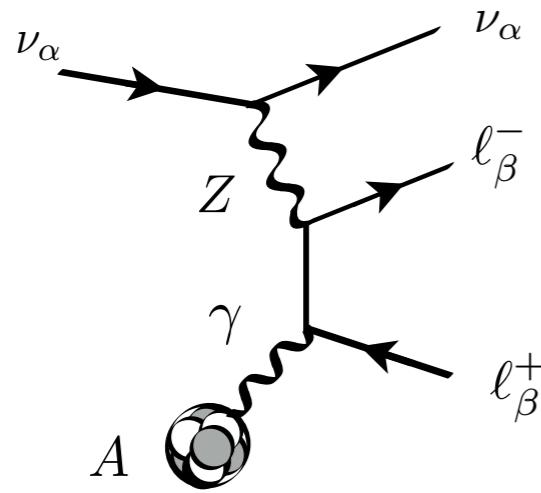
Sensitive to CC and NC interference in the SM

Complete calculation in the (early stages of) SM

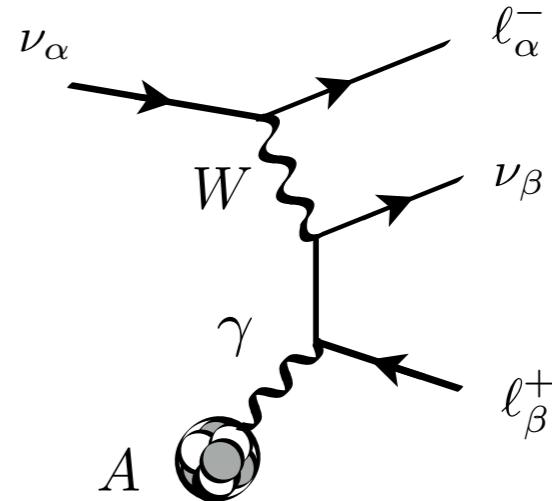
R.W. Brown et al, 1972
(Phys. Rev. D 6, 3273)

This was the goal of HE neutrino experiments in the 80's and 90's

Standard Model contributions

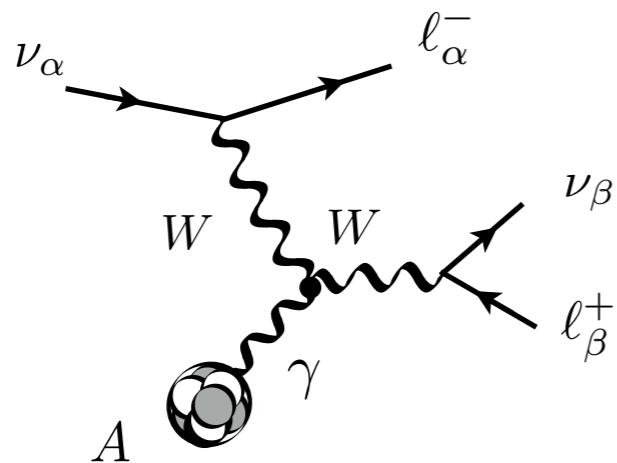


+ crossed boson
lines

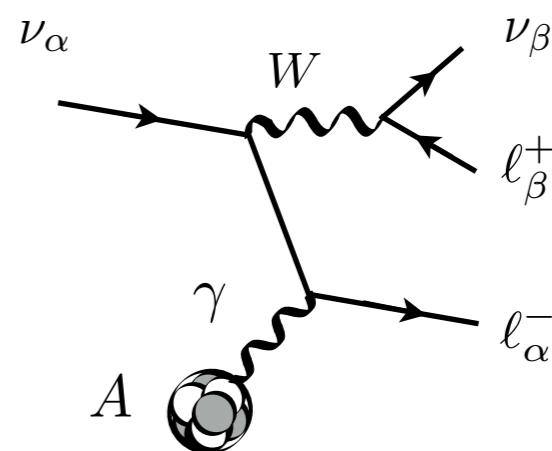


Z exchange boson lines
—Bethe-Heitler resembling photon pair production—

W exchange

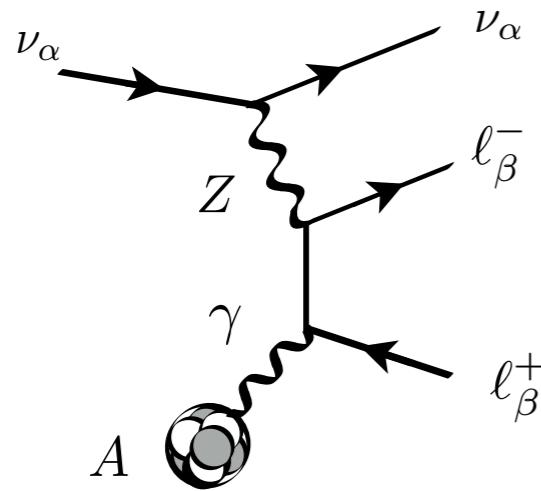


Triple gauge boson coupling
(order M_W^4)

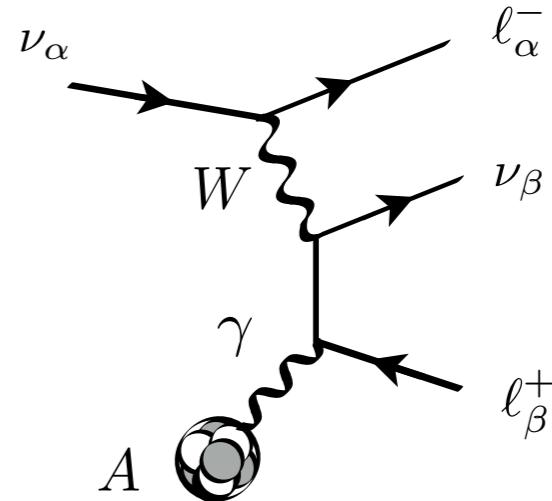


W radiation

Standard Model contributions



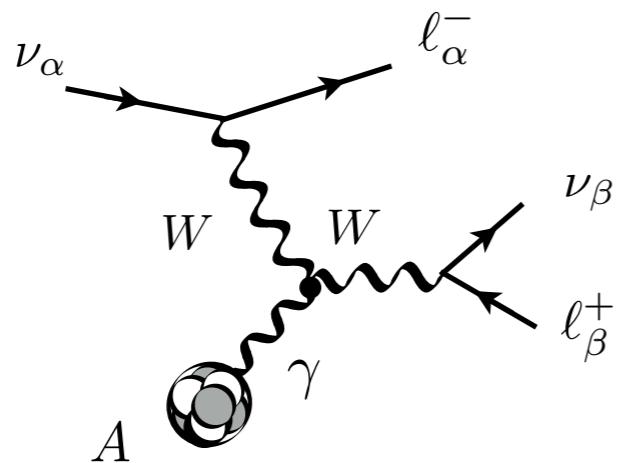
+ crossed boson
lines



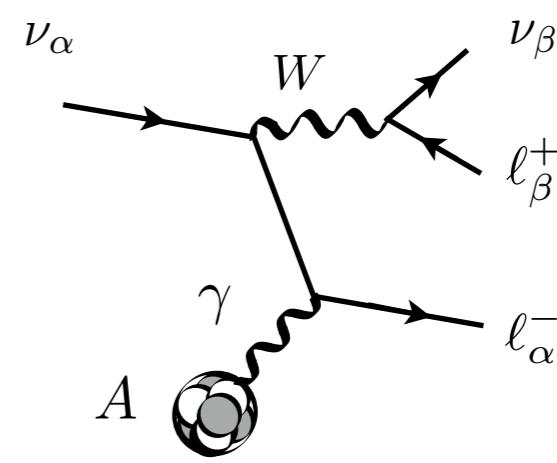
Z exchange boson lines

—Bethe-Heitler resembling photon pair production—

W exchange



Resonant at
high energies



Triple gauge boson coupling
(order M_W^4)

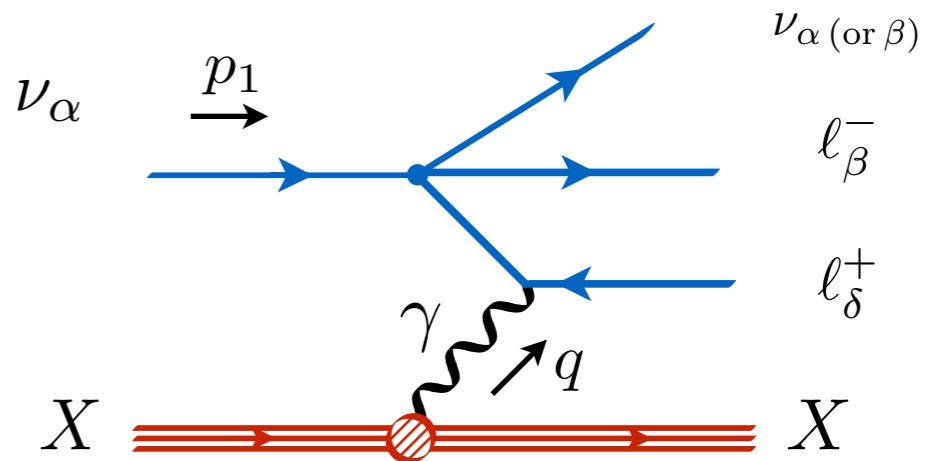
W radiation

Low energy cross sections

Process in coherent, diffractive or DIS limit:

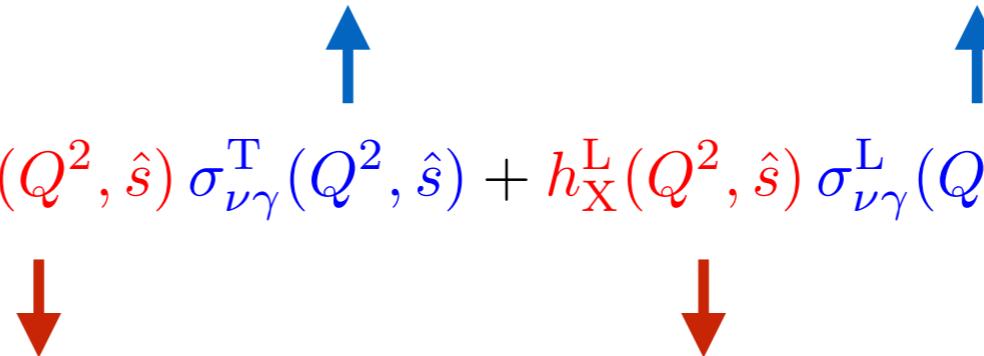
$$\frac{d^2\sigma_{\nu X}}{dQ^2 d\hat{s}} = \frac{1}{32\pi^2(s - M_X^2)^2} \frac{H_X^{\mu\nu} L_{\mu\nu}}{Q^4}$$

where $\hat{s} = 2(p_1 \cdot q)$ and $Q^2 = \sqrt{-q^2}$.



Universal leptonic T and L cross sections.

$$\frac{d^2\sigma_{\nu X}}{dQ^2 d\hat{s}} = \frac{1}{32\pi^2} \frac{1}{\hat{s} Q^2} [h_X^T(Q^2, \hat{s}) \sigma_{\nu\gamma}^T(Q^2, \hat{s}) + h_X^L(Q^2, \hat{s}) \sigma_{\nu\gamma}^L(Q^2, \hat{s})]$$



T and L photon flux function (**target** and **regime** dependent)

*On-shell photon (EPA or Weiszacker-Williams) is a bad approximation at LE
(factors of 2 or 3 difference — unsuitable for diffractive scattering)

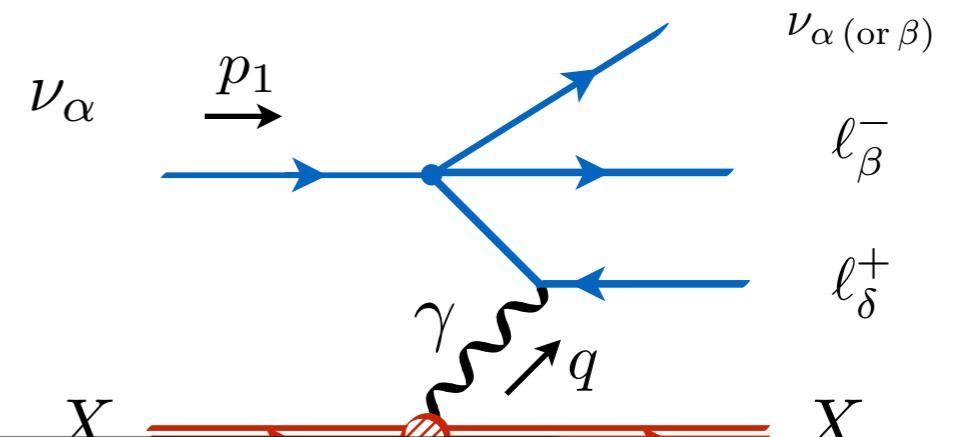
P. Ballett et al, JHEP 1901 (2019) 119.

Low energy cross sections

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$$\frac{d^2\sigma_{\nu X}}{dQ^2 d\hat{s}} = \frac{1}{32\pi^2(s - M_X^2)^2} \frac{H_X^{\mu\nu} L_{\mu\nu}}{Q^4}$$

where $\hat{s} = 2(p_1 \cdot q)$



Well understood process.

Electromagnetic nuclear form factors

+

fundamental neutrino-lepton scattering

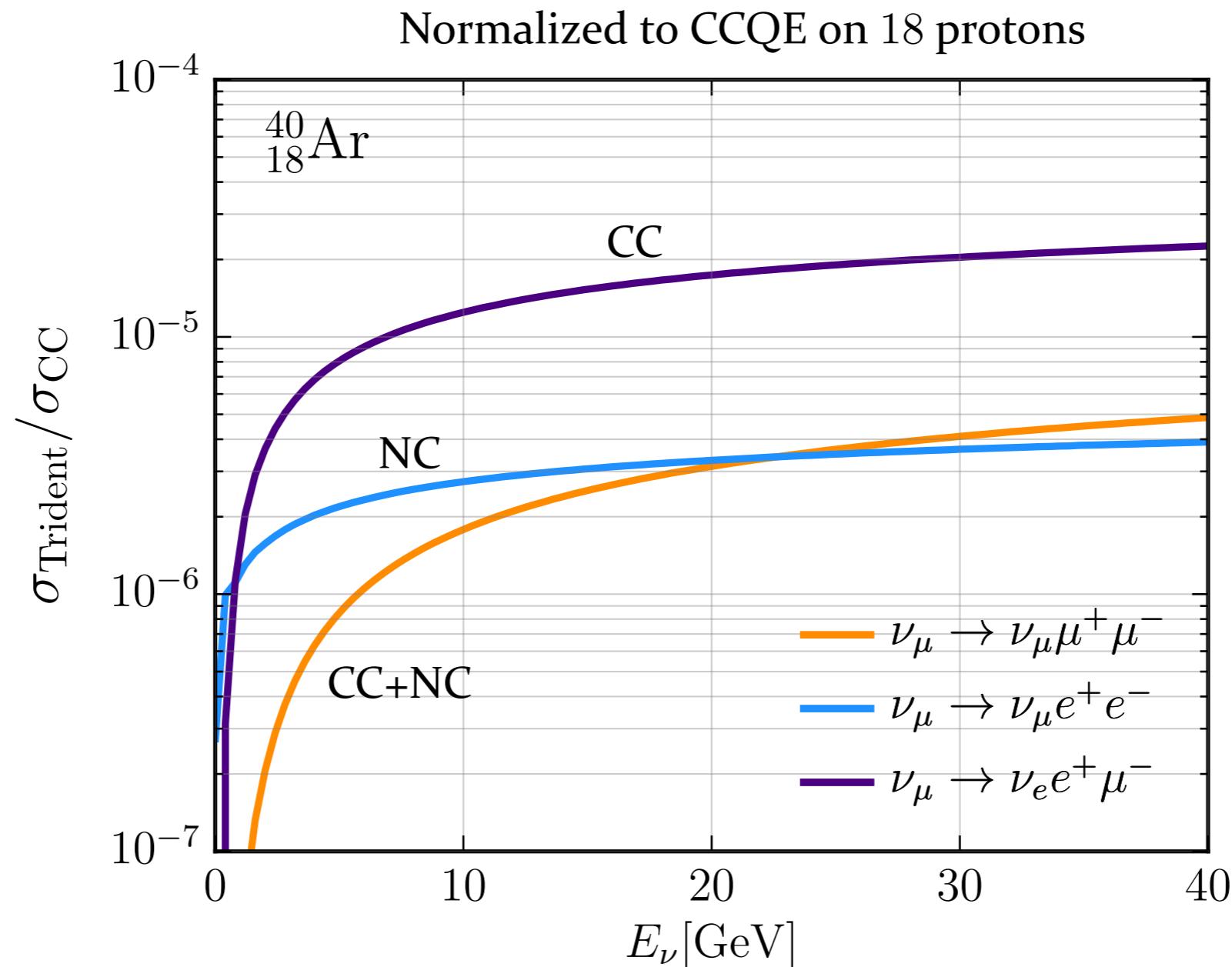
$$\frac{d^2\sigma_{\nu X}}{dQ^2 d\hat{s}} =$$

T and L photon flux function (**target** and **regime** dependent)

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P. Ballett et al, JHEP 1901 (2019) 119.

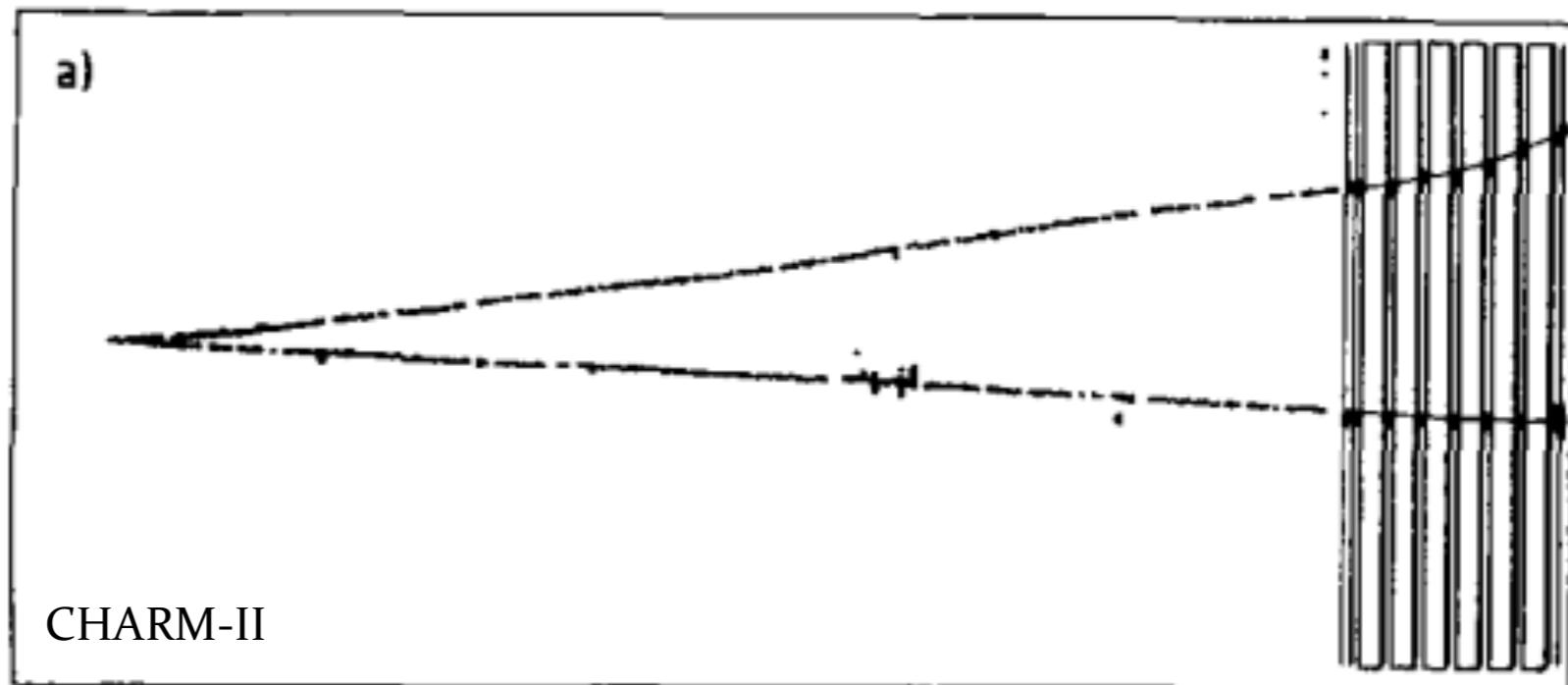
Cross sections



Need $> 10^6$ CCQE events to join the game at LE.

Production of taus is very small... not visible in the plot. If q is large, three propagator suppression.

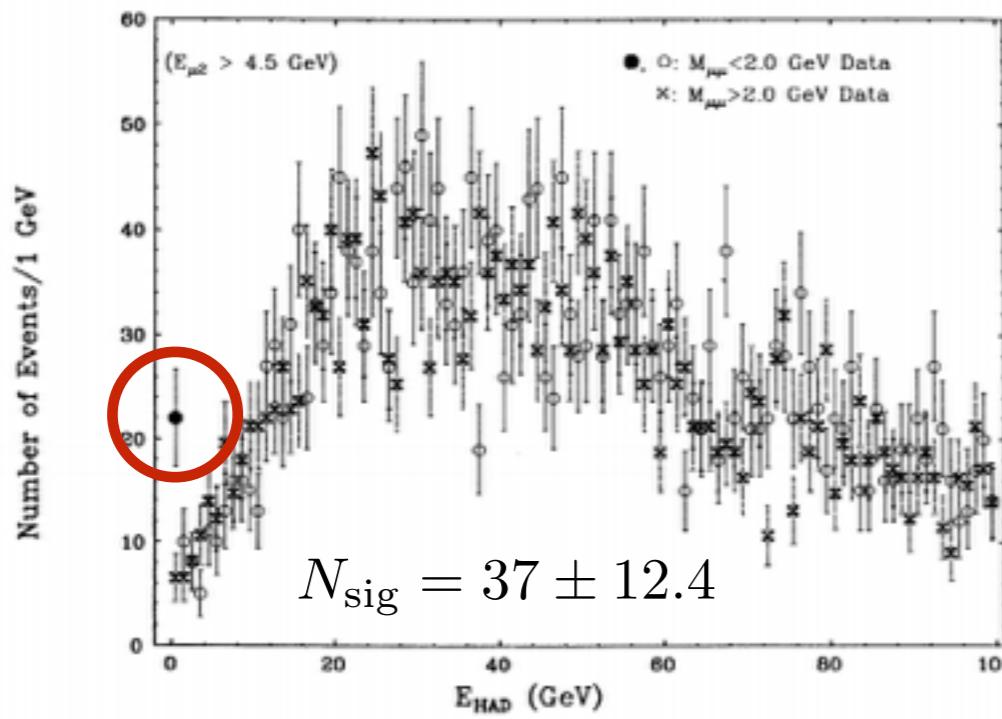
Measurements



Dimuon

CCFR

Lab E detector at FNAL



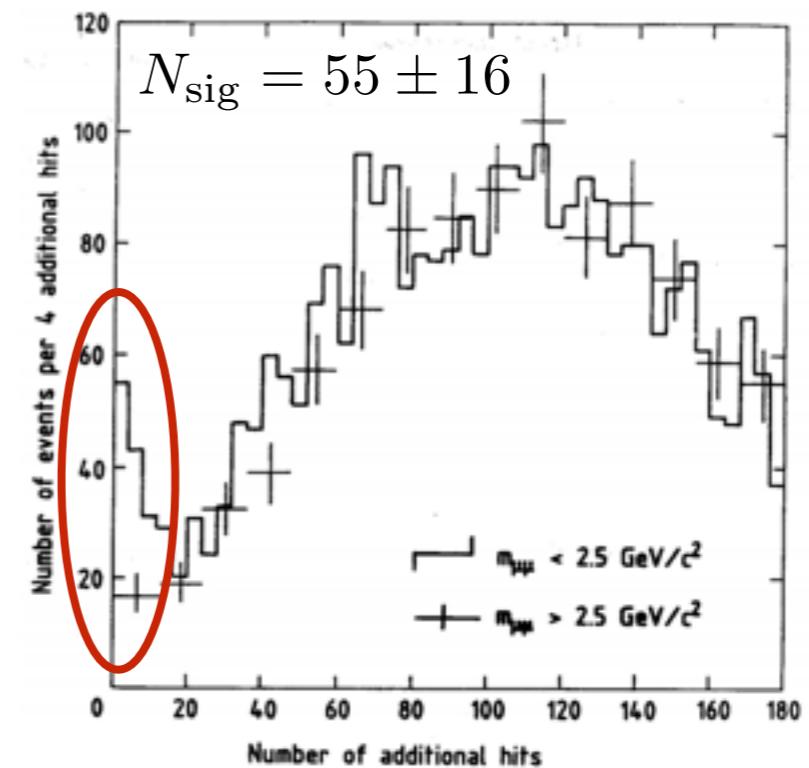
$$\langle E_\nu \rangle = 160 \text{ GeV}$$

$$\frac{\sigma_{\text{CCFR}}}{\sigma_{\text{SM}}} = 0.82 \pm 0.28$$

Phys. Rev. Lett. 66, 3117 (1991).

CHARM-II

WANF beam (CERN)



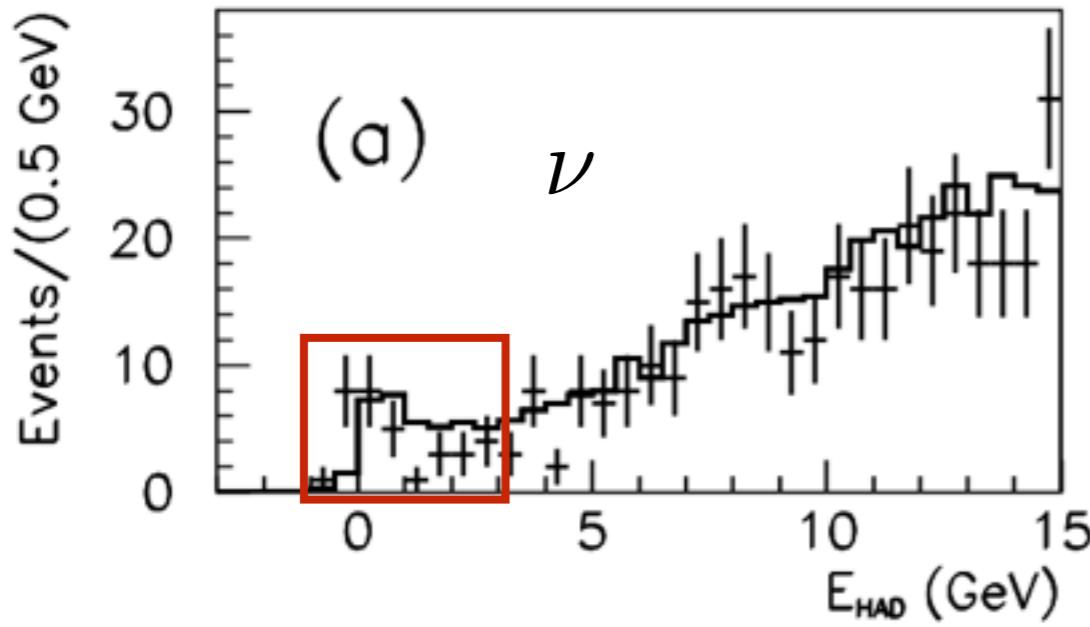
$$\langle E_\nu \rangle = 25 \text{ GeV}$$

$$\frac{\sigma_{\text{CHARM-II}}}{\sigma_{\text{SM}}} = 1.58 \pm 0.57$$

Phys. Lett. B 245, 271 (1990)

Dimuon

NuTeV
Lab E detector at FNAL

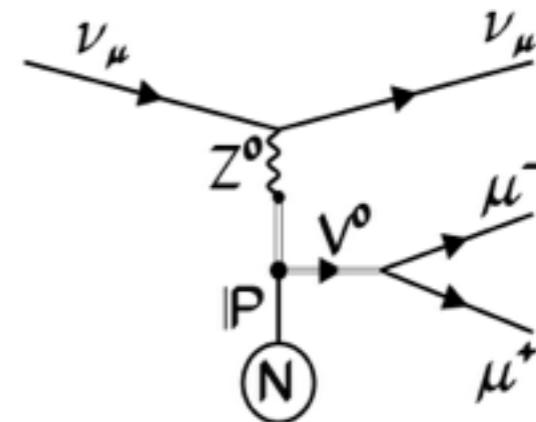


$$\langle E_\nu \rangle = 160 \text{ GeV}$$

$$\frac{\sigma_{\text{NuTeV}}}{\sigma_{\text{SM}}} = 0.72^{+1.73}_{-0.72}$$

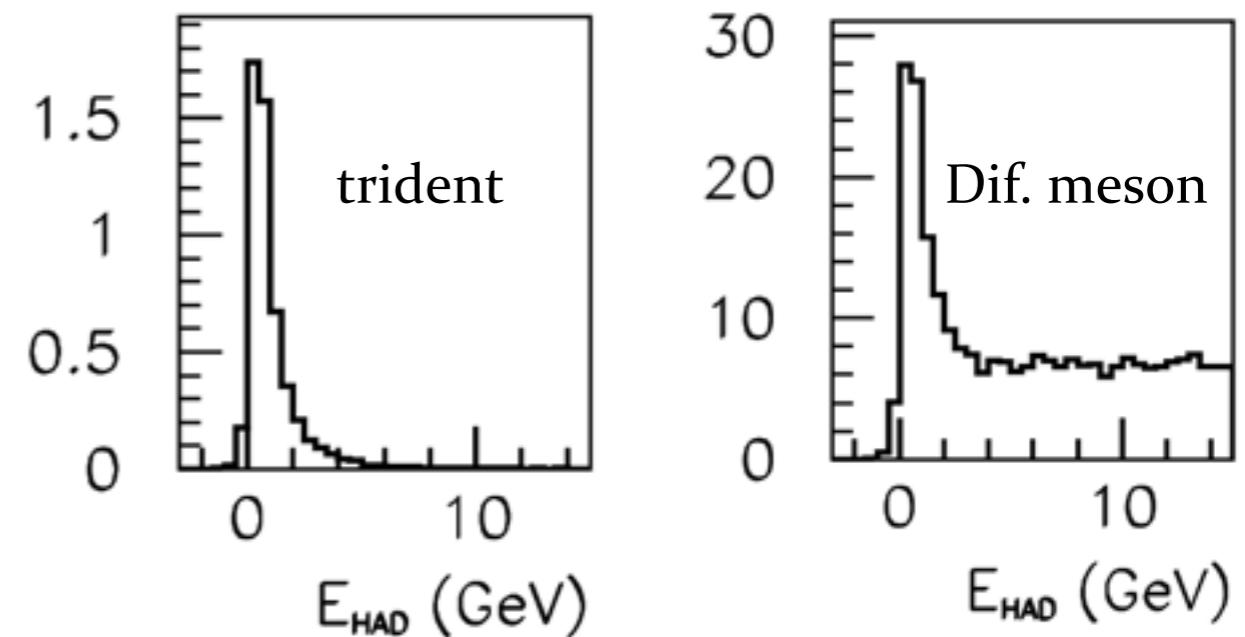
Inconclusive

Phys. Rev. D 61, 092001 (2000)



Diffractive vector meson contribution.

NuTeV MC



See discussion in
G. Krnjaic, arXiv:1902.07715

Other channels

Coherent-like production of

$$e^+ e^- \quad \mu^\pm e^\mp$$

Not yet observed or even searched for!

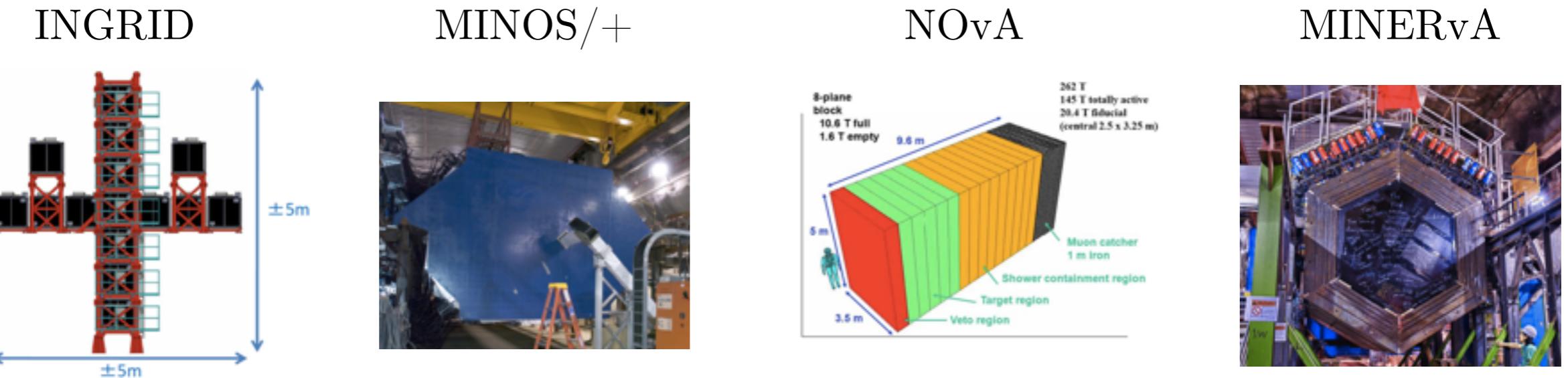
Challenging because of **PID** and **backgrounds**.

With new technology and large rates in current and future neutrino experiments
we should consider these again.

G. Magill et al, Phys. Rev. D 95

Dilepton production in neutrino experiments is old physics, but trident is unique.

Present



Channel	T2K-I	T2K-II	MINOS	MINOS+	NO ν A-I	NO ν A-II	MINER ν A
Total $e^\pm \mu^\mp$	563	1444	222 (56)	730	83 (72)	340 (374)	149 (102)
	96	246	46 (11)	151	25 (22)	102 (114)	56 (39)
Total $e^+ e^-$	277	711	61 (15)	62	29 (22)	119 (114)	39 (27)
	24	62	9 (2)	8	4 (4)	16 (21)	10 (7)
Total $\mu^+ \mu^-$	30	76	26 (6)	86	9 (9)	37 (47)	18 (13)
	21	54	15 (3)	49	8 (8)	34 (36)	18 (13)

100% efficiencies. Detector capability is the name of the game.

Future



Channel	SBND	μ BooNE	ICARUS	DUNE ND
Total $e^\pm\mu^\mp$	10	0.7	1	2993 (2307)
	2	0.1	0.2	692 (530)
Total e^+e^-	6	0.4	0.7	1007 (800)
	0.7	0.0	0.1	143 (111)
Total $\mu^+\mu^-$	0.4	0.0	0.0	286 (210)
	0.4	0.0	0.0	196 (147)

Hyper-K? ND

Why is it hard?

Dilepton production is rare, usually alongside heavy resonances and had. E, but...

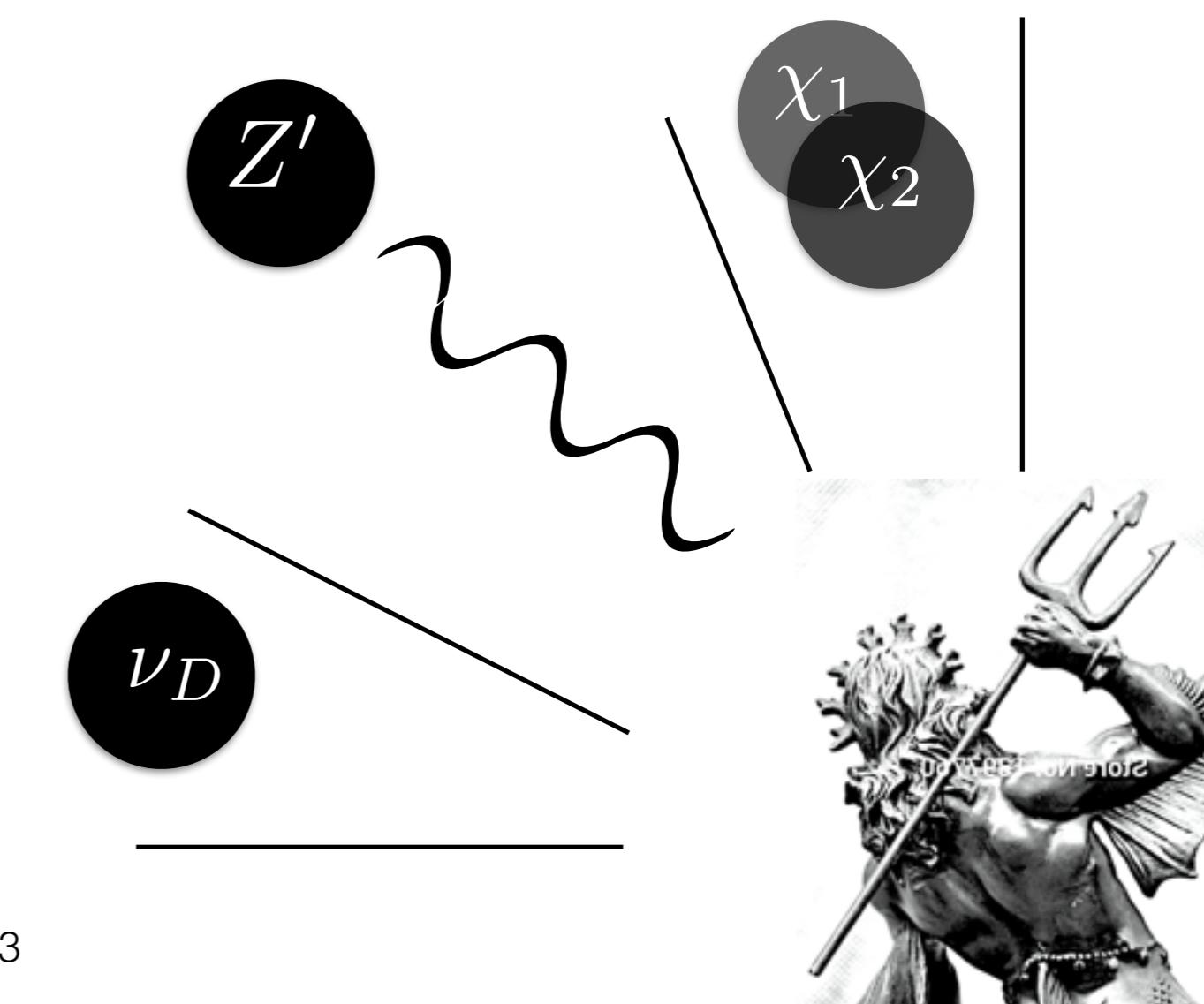
PID	$\mu^+ \mu^-$	CC1 π^\pm misID π^\pm .
$\left\{ \begin{array}{l} \mu^\pm/\pi^\pm \\ e^\pm/\gamma \end{array} \right.$	$e^+ e^-$	NC1 π^0 and ν_e CC π^0
	$e^+ \mu^-$	CC1 π^0 with misID γ .

Even if misID is few %, there are just too many, we have to rely on kinematics.

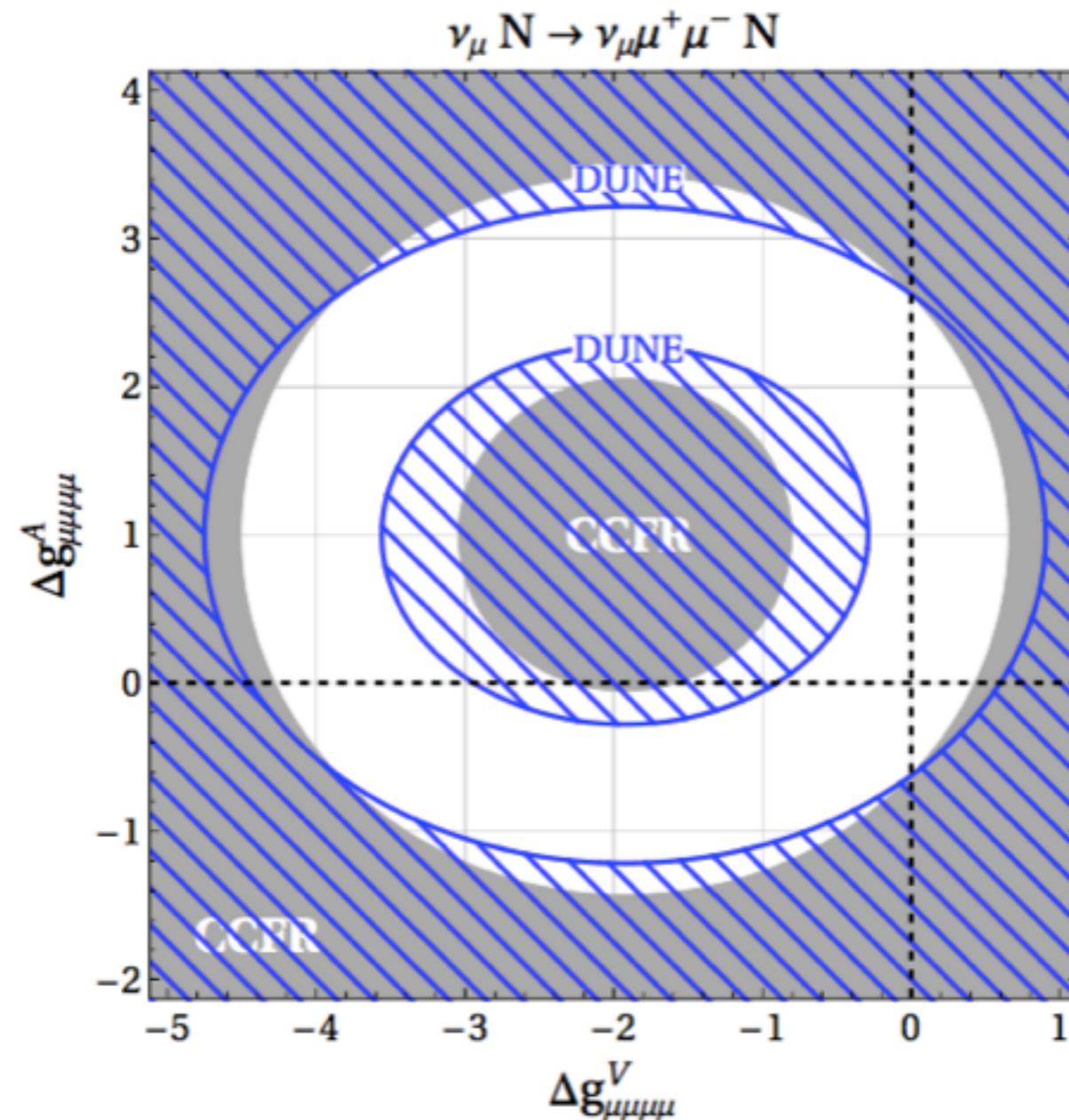
See P. Ballett et al, JHEP1901(2019)119 for preliminary analysis in LAr for all channels

W. Altmannshoffer et al, arXiv:1902.06765 for more sophisticated dimuon projection in DUNE.

Smiting New Physics



Precision physics?



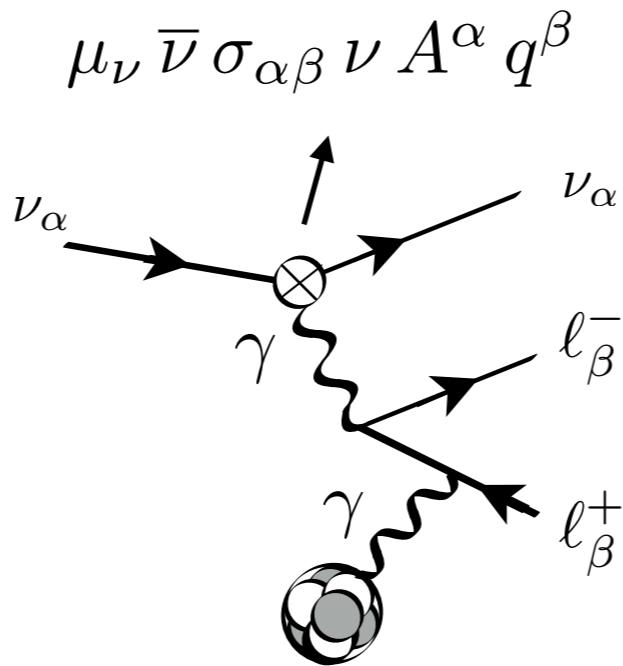
$$2g_V = 1 + 4 \sin^2 \theta_W + \Delta g_{\mu\mu\mu\mu}^V$$

$$-2g_A = -1 + \Delta g_{\mu\mu\mu\mu}^A$$

W. Altmannshoffer et al, arXiv:1902.06765

Neutrino magnetic moments

Large neutrino magnetic moments?



$\mu_{\nu_\mu} \lesssim 4.0 \times 10^{-8} \mu_B$ according
to the CCFR data,

M.I. Vysotsky et al., Phys. Atom. Nucl. 65 (2002) 1634

Bound from dimuon at large energies, but EPA used and **energy dependence** not studied.

As of now, unlikely to beat neutrino-electron scattering bounds.

$L_\mu - L_\tau$ model

$$\text{SM} \times U(1)_{L_\mu - L_\tau}$$

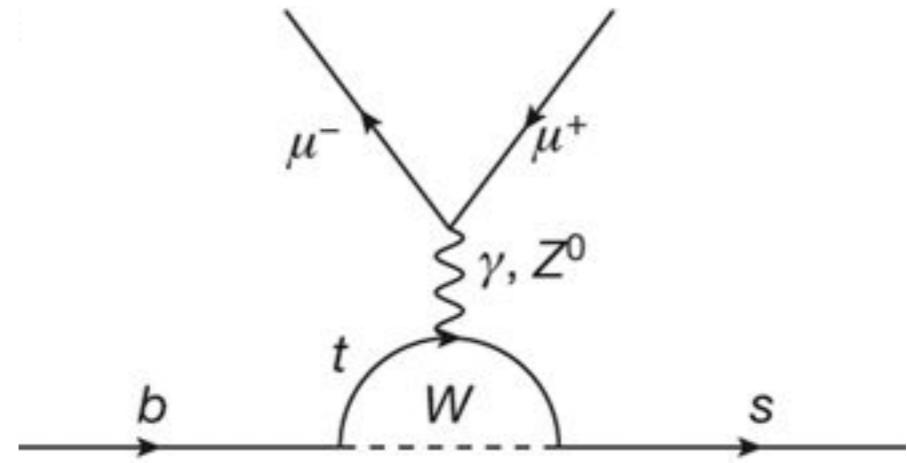
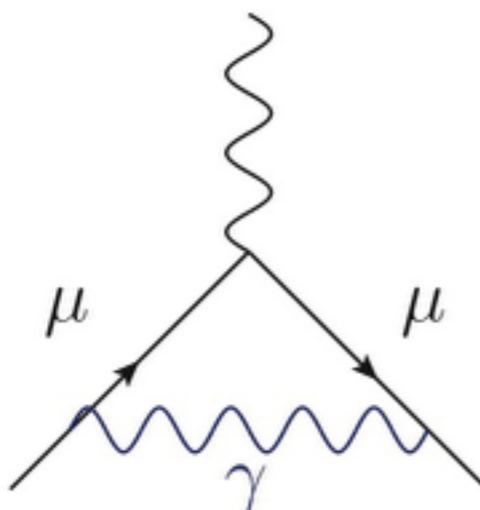
The model that revived the interest in dimuon tridents

[W. Altmannshoffer et al, PRL113\(2014\)091801](#)

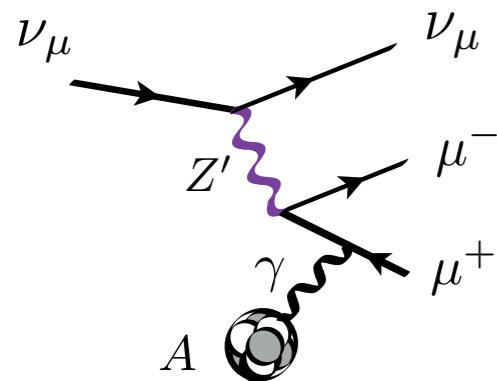
$$\mathcal{L}_{\text{int}} \supset g' Z'_\alpha (\bar{L}_\mu \gamma^\alpha L_\mu - \bar{L}_\tau \gamma^\alpha L_\tau + \bar{\mu}_R \gamma^\alpha \mu_R - \bar{\tau}_R \gamma^\alpha \tau_R)$$

Minimal **anomaly-free** extension that:

- can explain the muon ($g-2$) discrepancy.
- contains lepton non-universality (easily related to flavour anomalies in LHCb)
- allows to reproduce neutrino mixing data



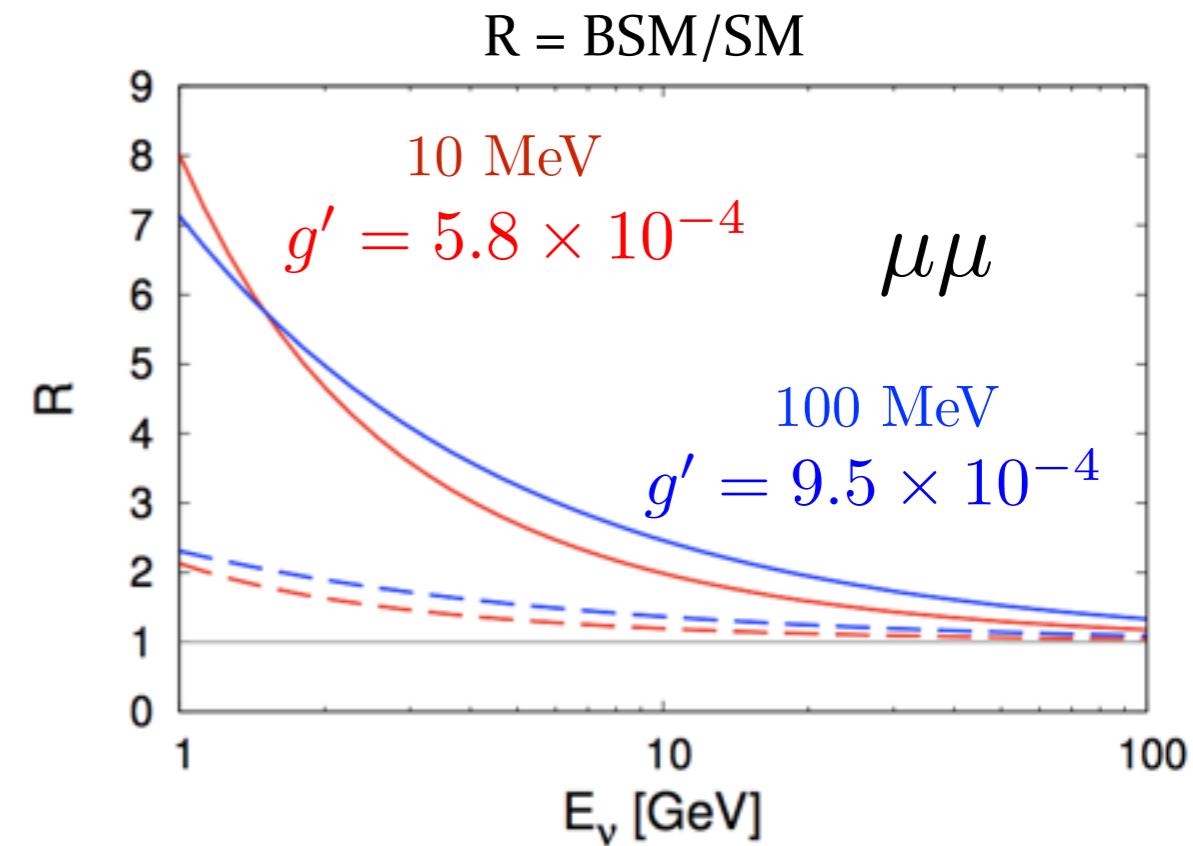
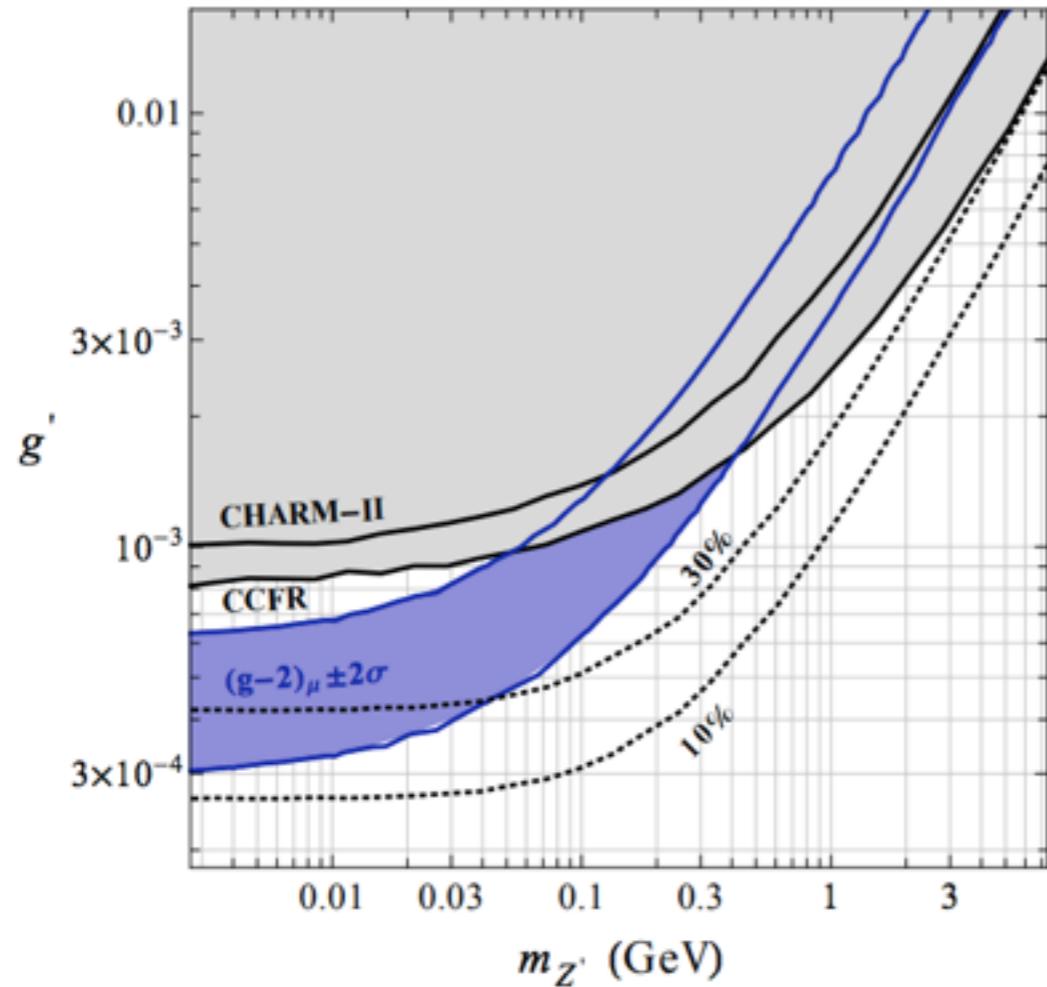
$L_\mu - L_\tau$ model



$\text{SM} \times U(1)_{L_\mu - L_\tau}$

The model that revived the interest in dimuon tridents

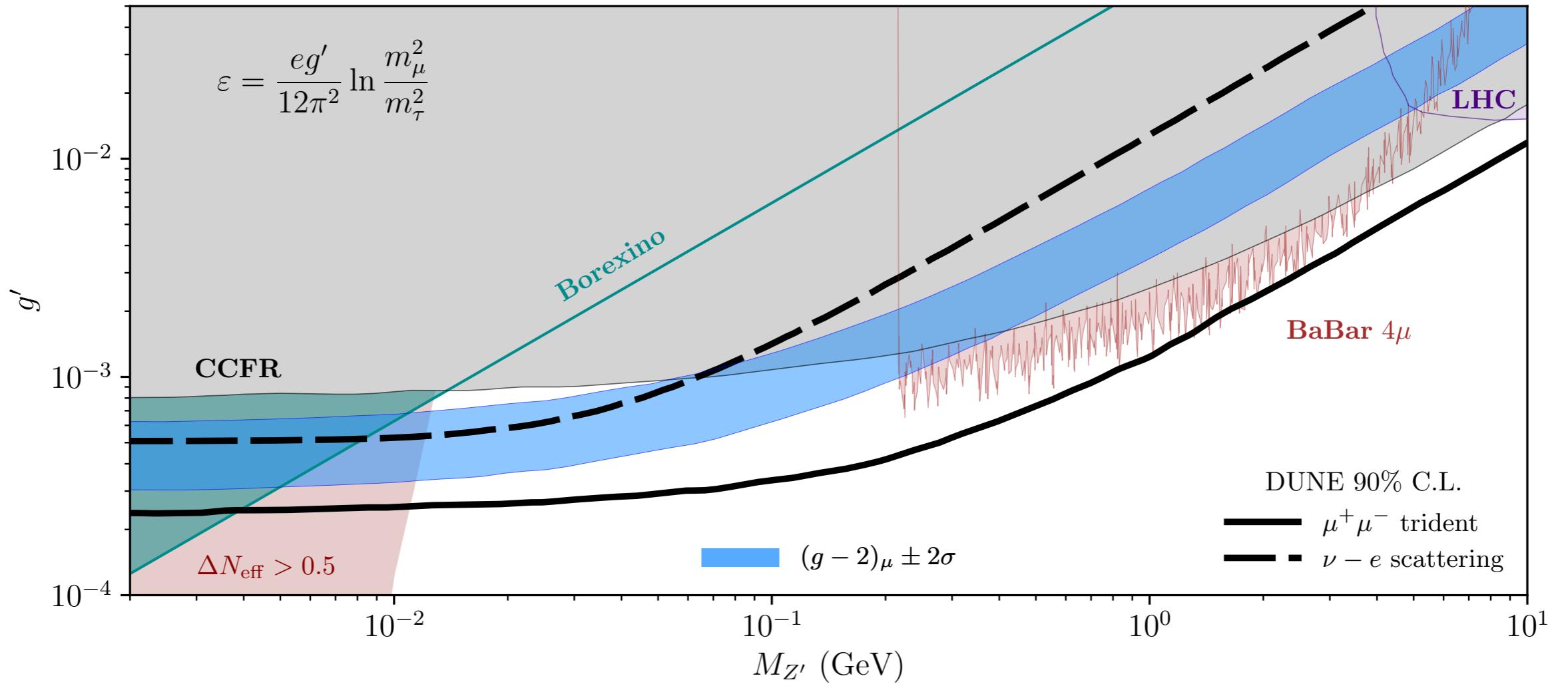
Measurement at low energies
more sensitive



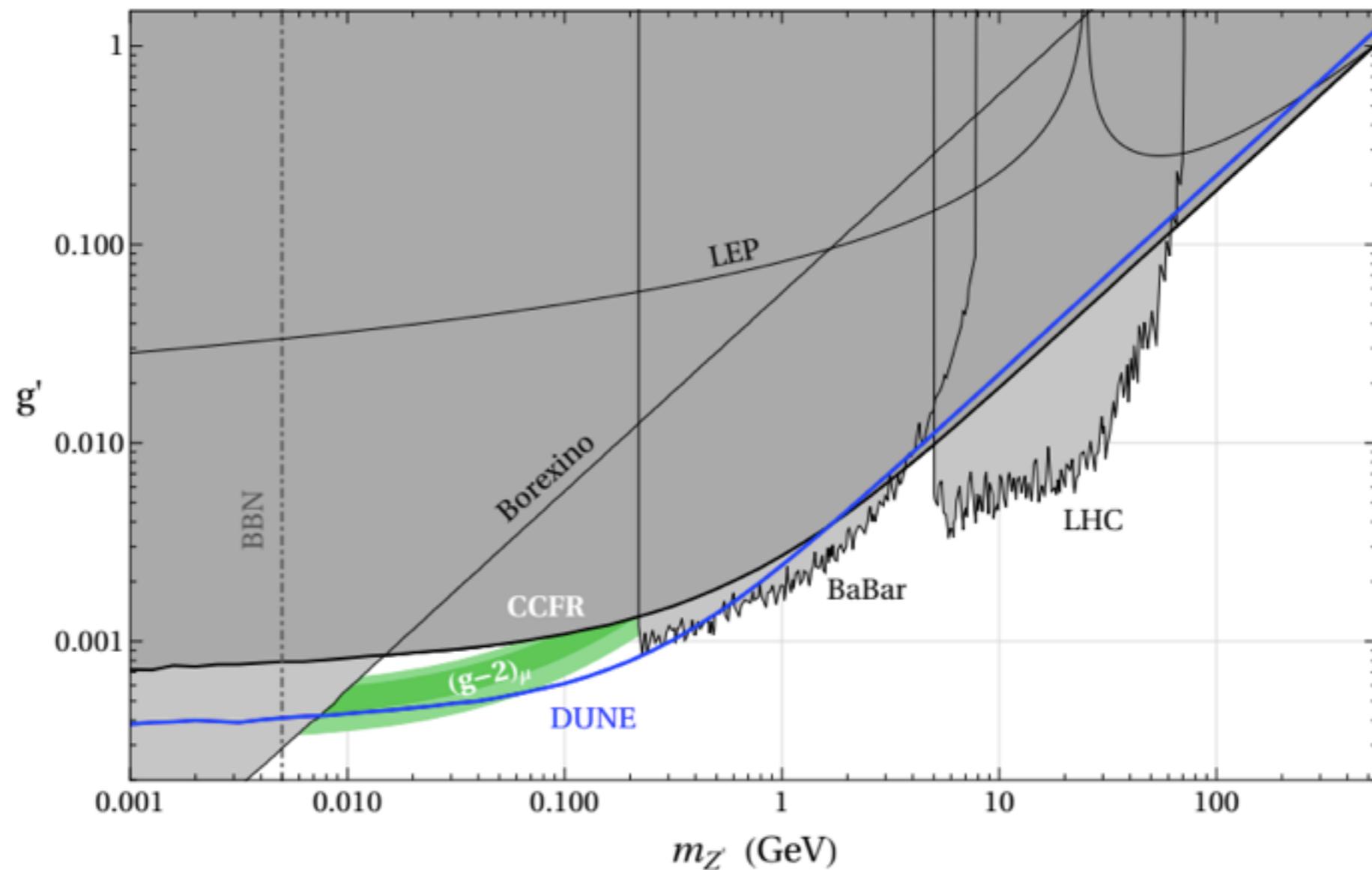
W. Altmannshoffer et al, PRL113(2014)091801

Y. Kaneta et al, PTEP 2017 (2017) no.5, 053B04

$L_\mu - L_\tau$, DUNE ND, 75 tonnes, 5 y ν -mode + 5 y $\bar{\nu}$ -mode, 120 GeV p^+ , $\sigma_{\text{norm}} = 5\%$



No backgrounds, but kin. cuts on signal, eg. $\theta_{\mu\mu} < 20^\circ$



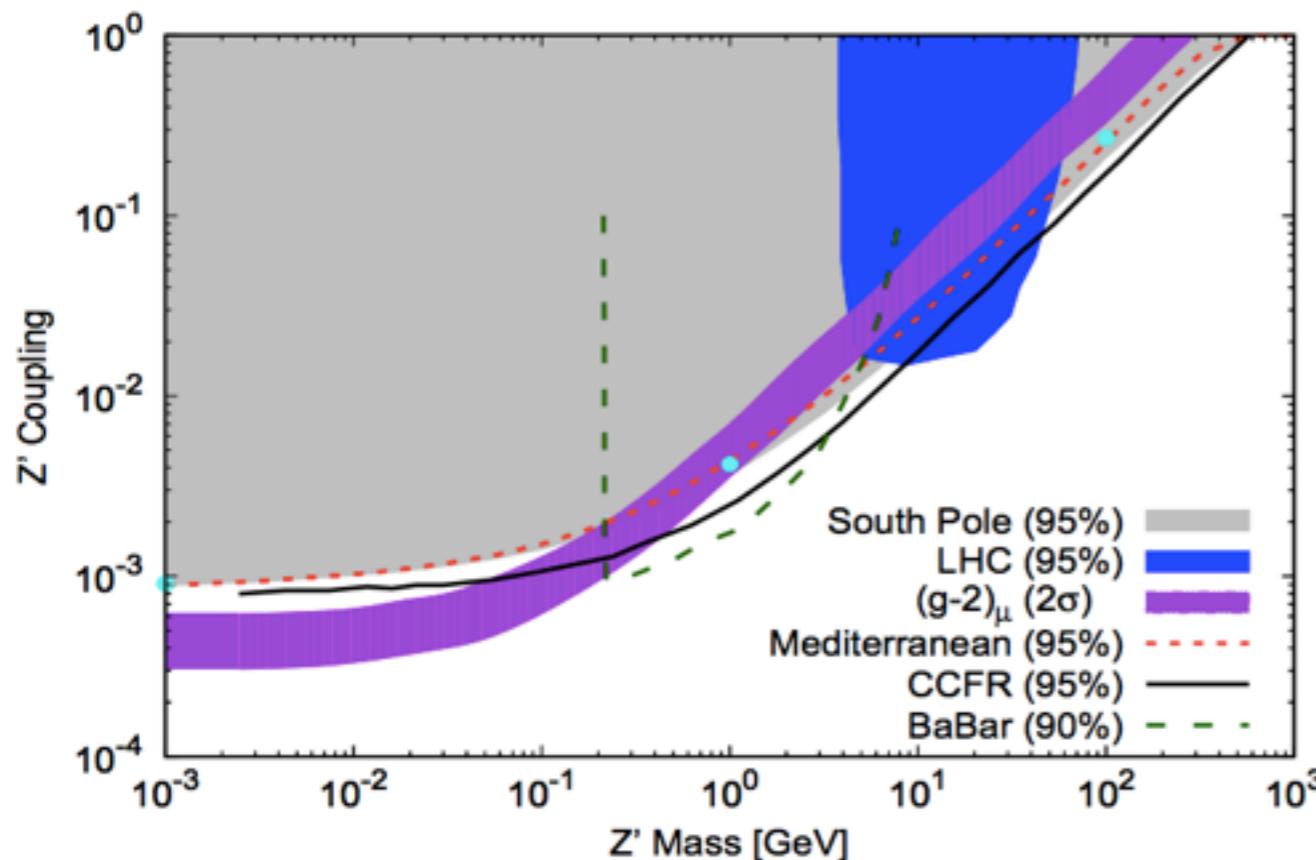
Backgrounds: $S/\sqrt{B} \sim 1.6$ per year, 25% measurement in ~ 6.5 years.

Tight kin. cuts (eg. $\theta_{\mu\mu} < 5^\circ$). Reducing pion misID can loosen it

[W. Altmannshoffer et al, arXiv:1902.06765](#)

Atmospheric neutrinos in the game

Trade off between # of events and BSM enhancement.

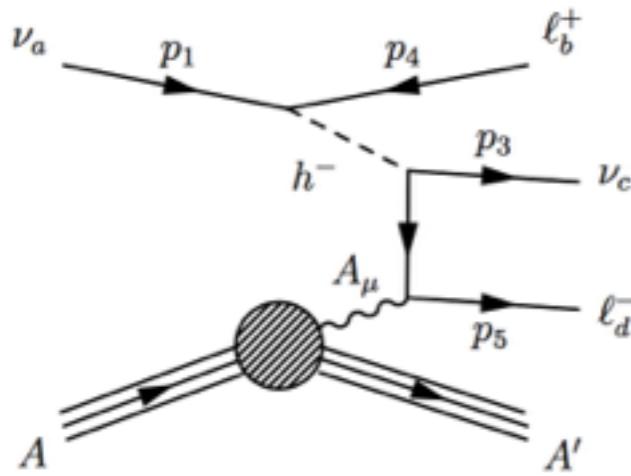


Total SM rate expected in 10 years:

7.4 (17, 63) at PINGU (DeepCore, IceCube)
16 (23) at ORCA (ARCA)

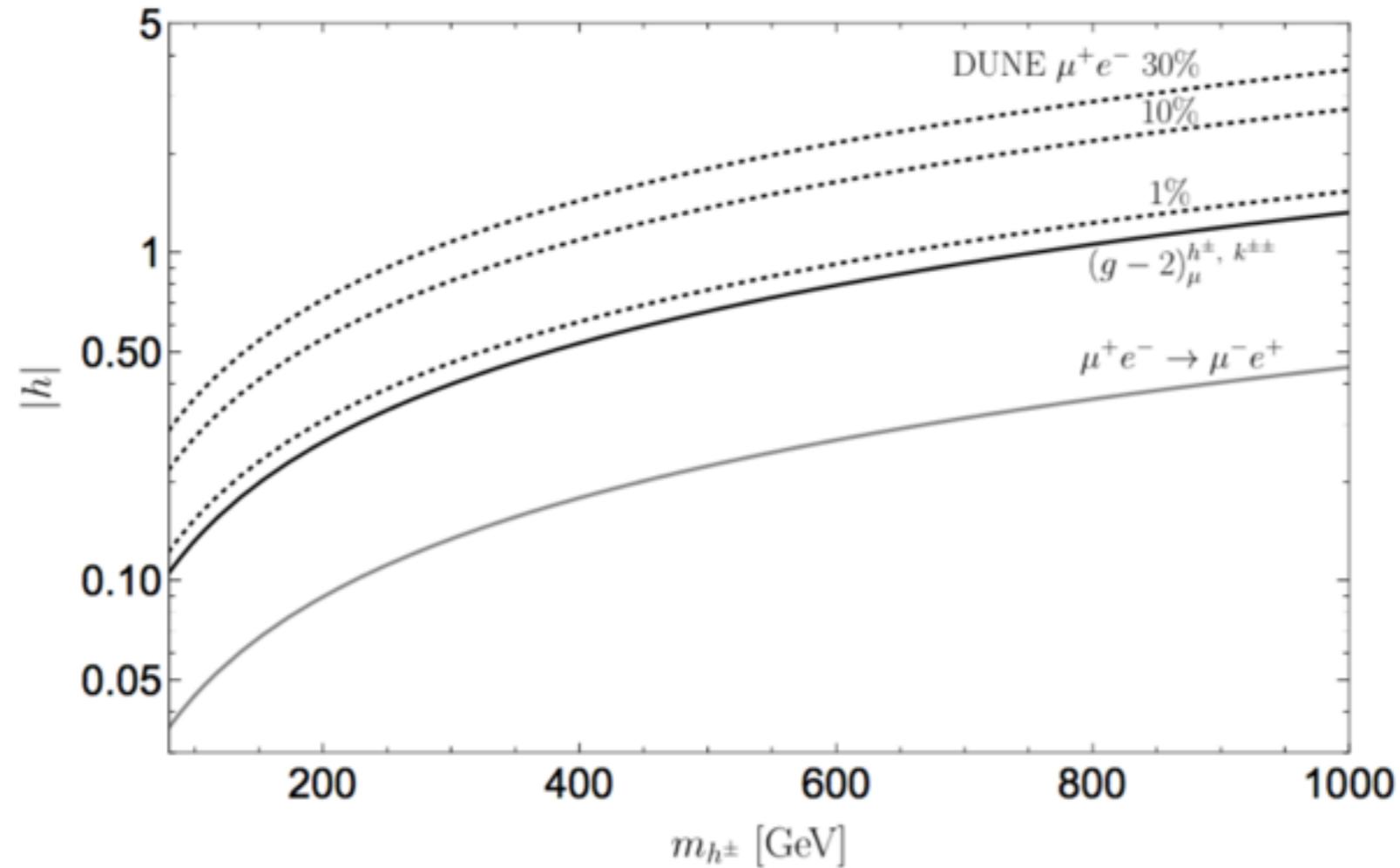
New physics in charge-current channels

G. Magill et al, PRD97 (2018) no.5, 055003



Much harder — new physics more easily constrained otherwise.

$$\mathcal{L} \supset |\partial_\mu h|^2 - m_h^2 |h|^2 + \sqrt{2} h_{ab} \nu^a \ell^b h + k_{ab} \ell^a \ell^b k + c.c.$$

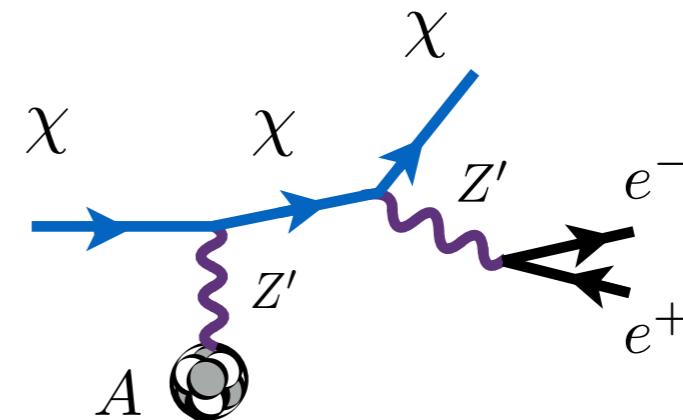
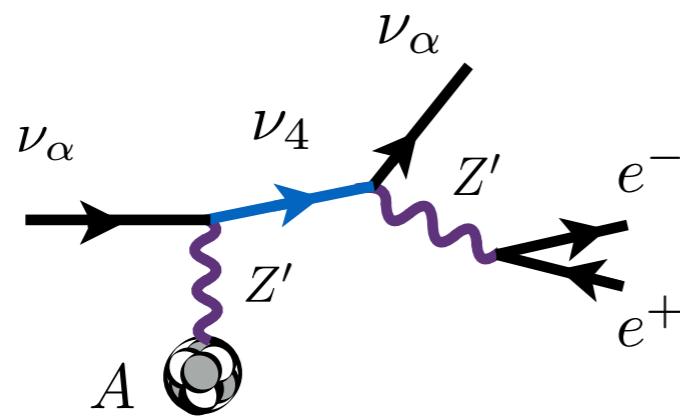


...but more data cannot harm!

Dielectron signatures

New forces that talk directly to electrons are can be bounded by neutrino-electron scattering data.

However, BSM e^+e^- signature still arise.



Dark neutrinos ($U'(1)$ charged heavy neutrinos)

- MiniBooNE explanation
- Neutrino mass generation at low scales

E. Bertuzzo et al, PRL121.241801

P. Ballett et al, arXiv:1808.02915

P. Ballett et al, arXiv:1903.07589

Light DM (+ Inelastic DM)

- produced in the beam
- scattering or decay signature

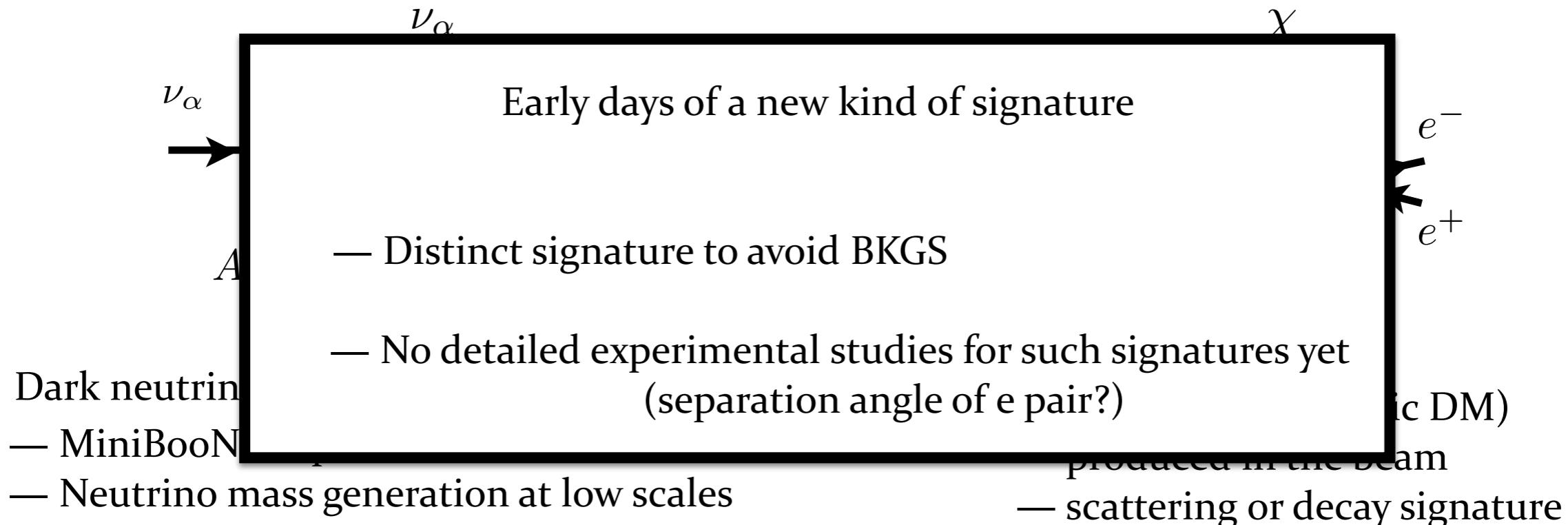
E. Izaguirre, PRD96(2017)no.5, 055007

A. de Gouvea et al, JHEP1901(2019)001

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E. Bertuzzo et al, PRL121.241801
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Conclusions

We have a chance to return to neutrino scattering physics

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Neutrino trident production is a unique signature with a lot of potential for SM and new physics.

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Neutrino trident production is a unique signature with a lot of potential for SM and new physics.

We can study it again at the DUNE ND, but no need to wait (see MINERvA, T2K).

Conclusions

We have a chance to return to neutrino scattering physics

Neutrino trident production is a unique signature with a lot of potential for SM and new physics.

We can study it again at the DUNE ND, but no need to wait (see MINERvA, T2K).

Beyond tridents, what else are neutrinos doing at the
per mille of a per mille level of CCQE?

THANK YOU



APPENDIX



Coherent cross sections

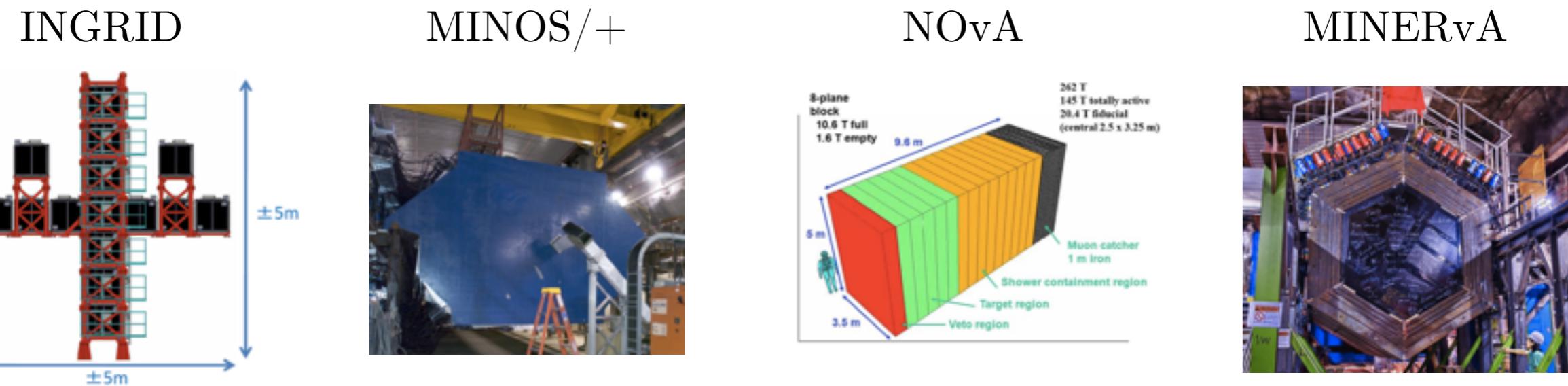


SBND	110 m, 112 t	6.6×10^{20} P.O.T.
μ BooNE	470 m, 89 t	13.2×10^{20} P.O.T.
ICARUS	600 m, 476 t	6.6×10^{20} P.O.T.

50 t LAr, assuming
 $(2 + 2 \times 3) \times 1.83\text{e}21$ P.O.T.
in nu and nubar mode.



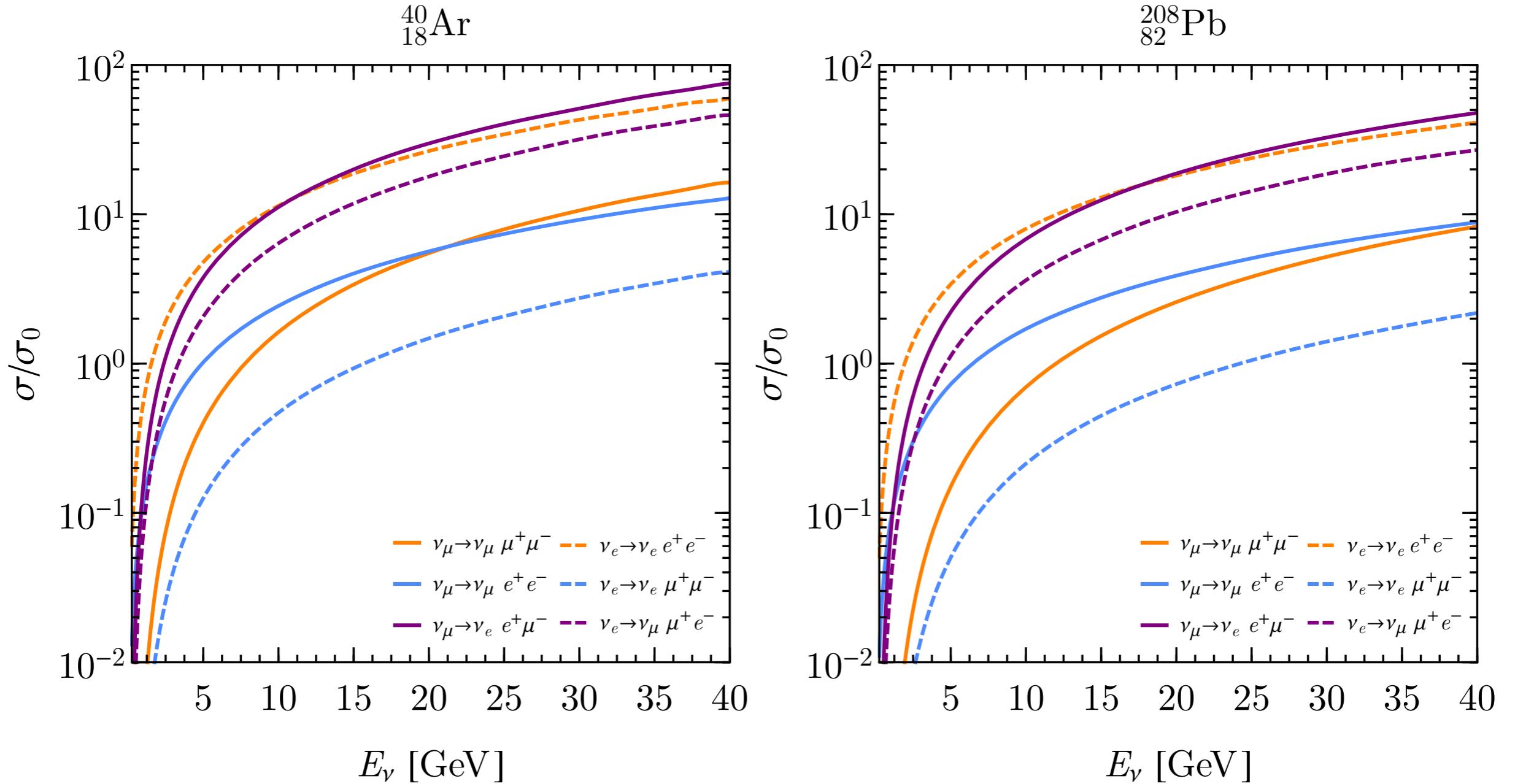
Coherent cross sections



Experiment	Material	Baseline (m)	Exposure (POT)	Fiducial Mass
INGRID	Fe	280	$3.9 \times 10^{21} [10^{22}]$ T2K-I [T2K-II]	99.4
MINOS[+]	Fe and C	1040	$10.56(3.36)[9.69] \times 10^{20}$	28.6
NO ν A	C ₂ H ₃ Cl and CH ₂	1000	$8.85(6.9) [36(36)] \times 10^{20}$ [NO ν A-II]	231
MINER ν A	CH, H ₂ O, Fe, Pb, C	1035	$12(12) \times 10^{20}$	7.98

POT in antineutrino mode in parentheses.

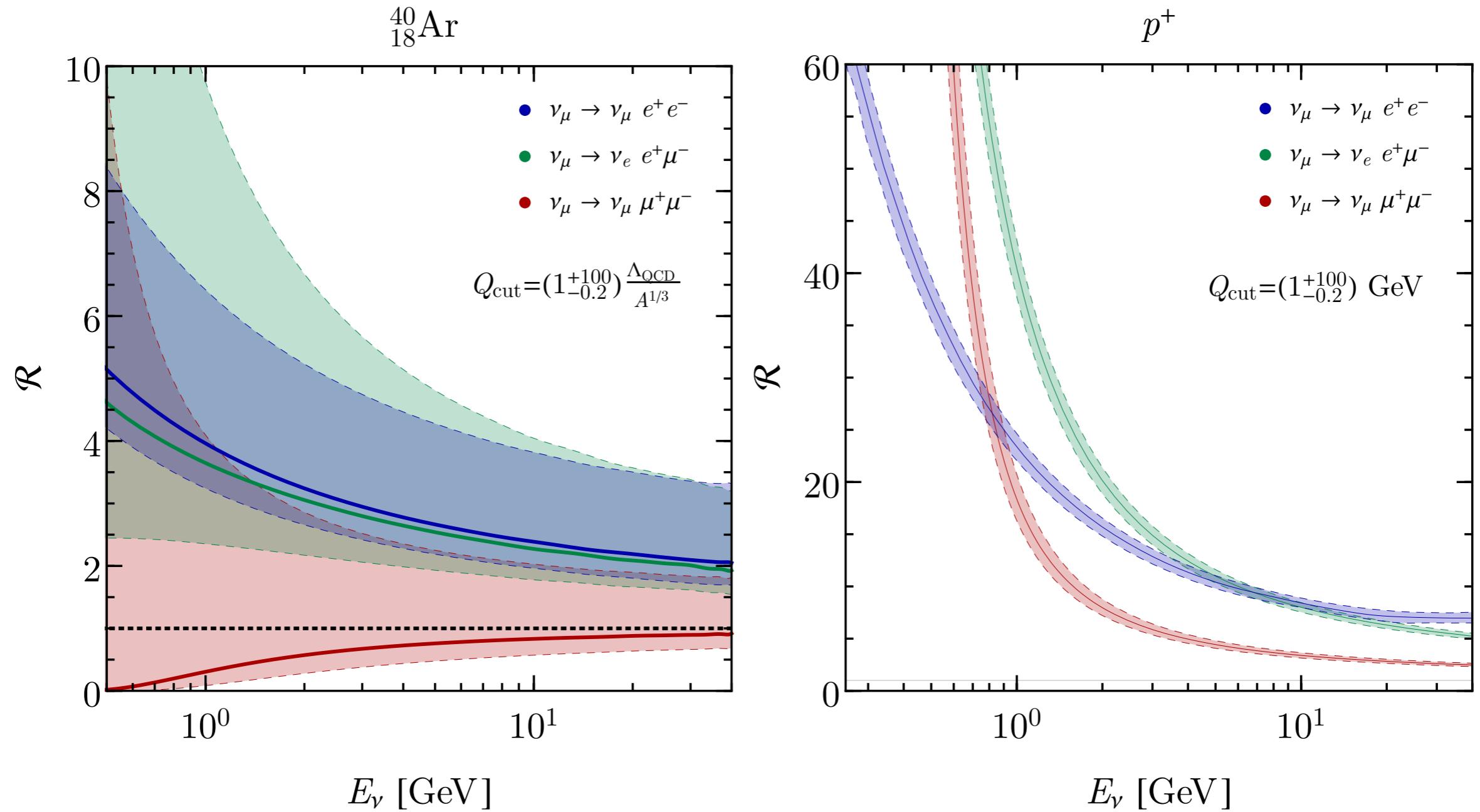
Coherent cross sections



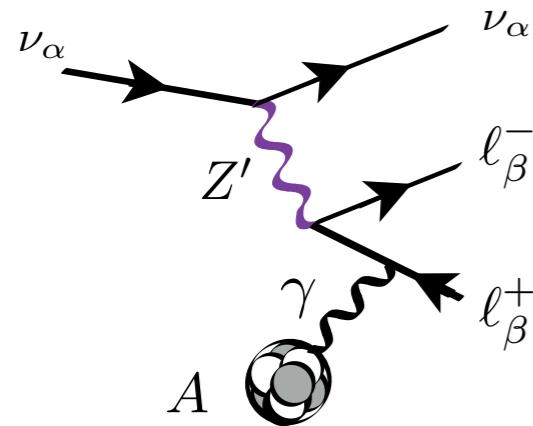
$$\sigma_0 = Z^2 10^{-44} \text{ cm}^2$$

Equivalent Photon Approximation

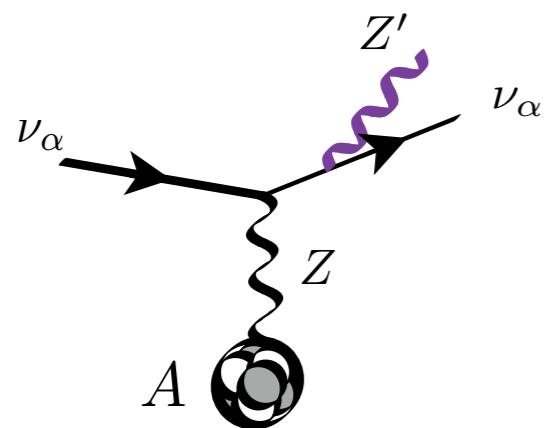
$$\mathcal{R} = \frac{\sigma_{\text{EPA}}(E_\nu)|_{Q_{\max}}}{\sigma_{\text{4PS}}(E_\nu)}$$



BSM tridents @ DUNE

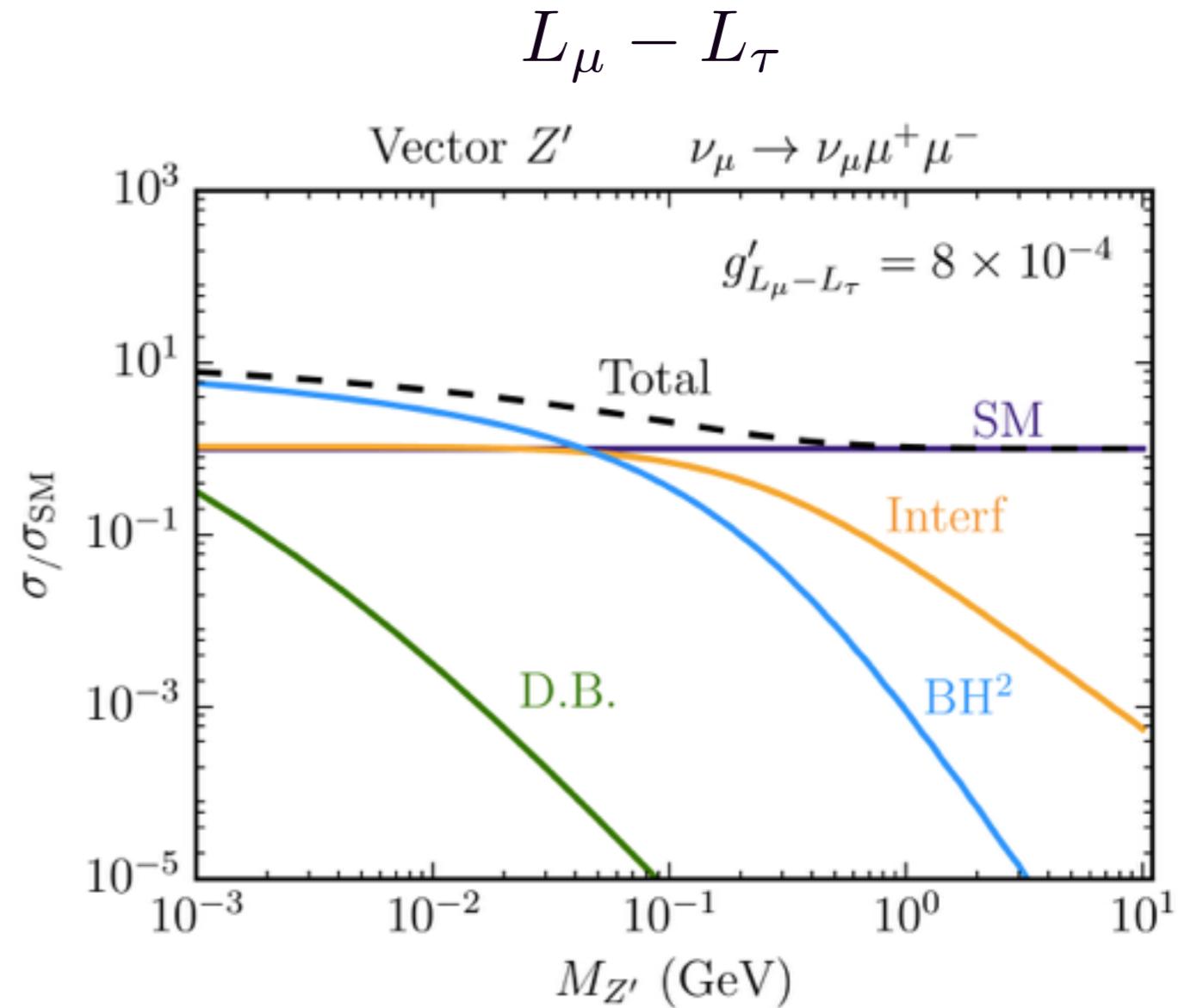


Bethe-Heitler (BH)



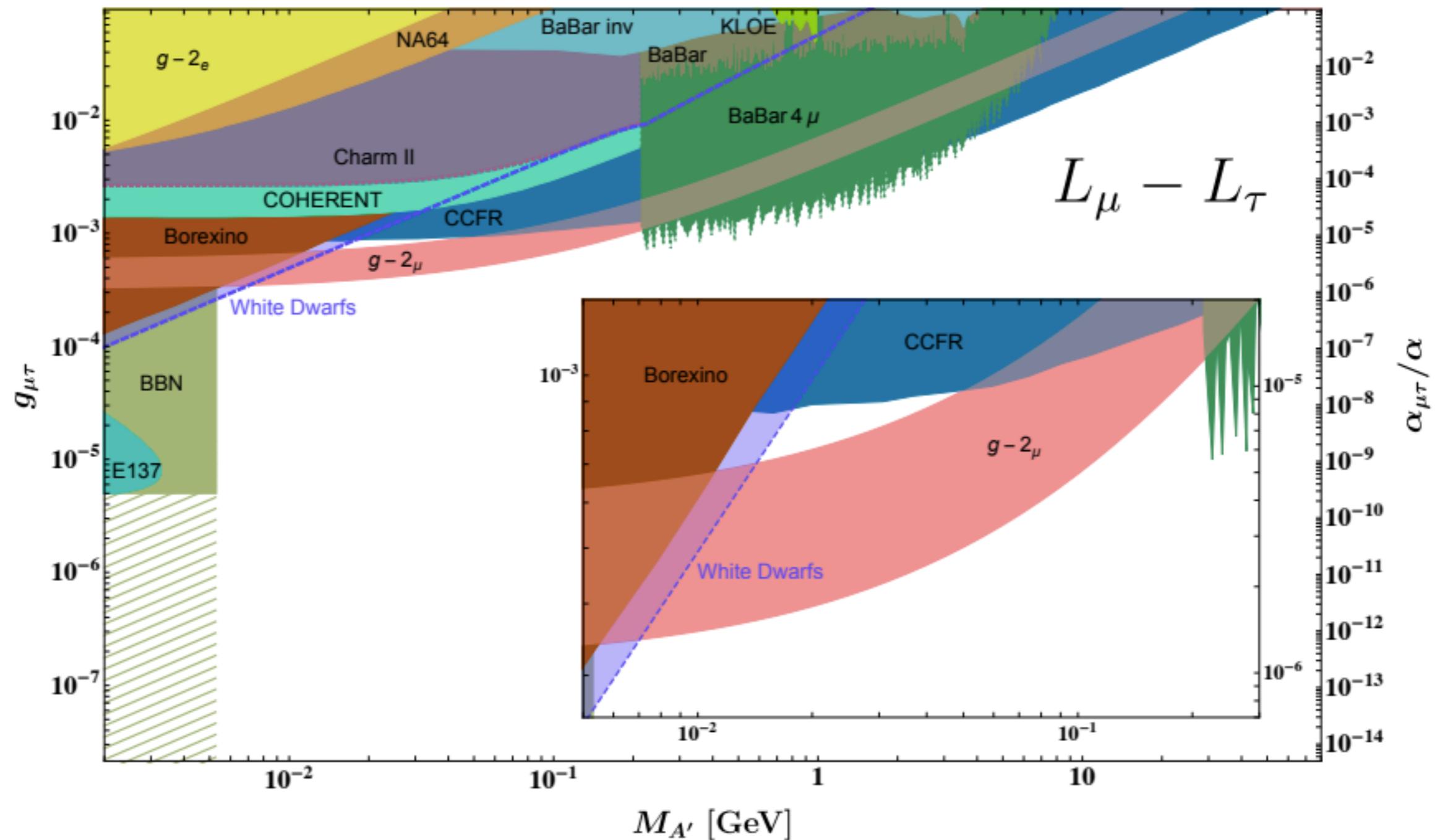
Dark-Bremsstrahlung (DB)

Calculation using NWA (negligible!)

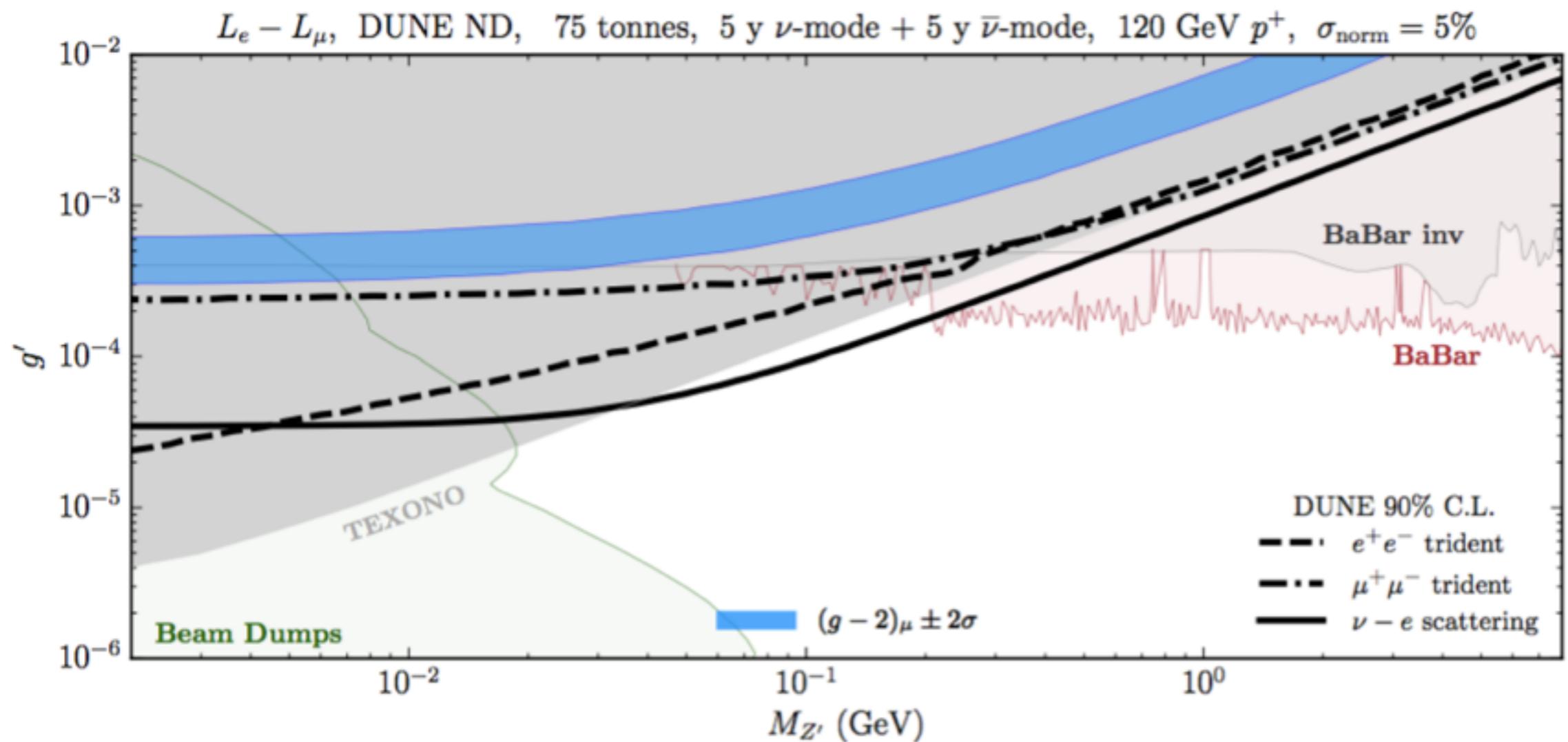


Other constraints

M. Bauer et al, 2018

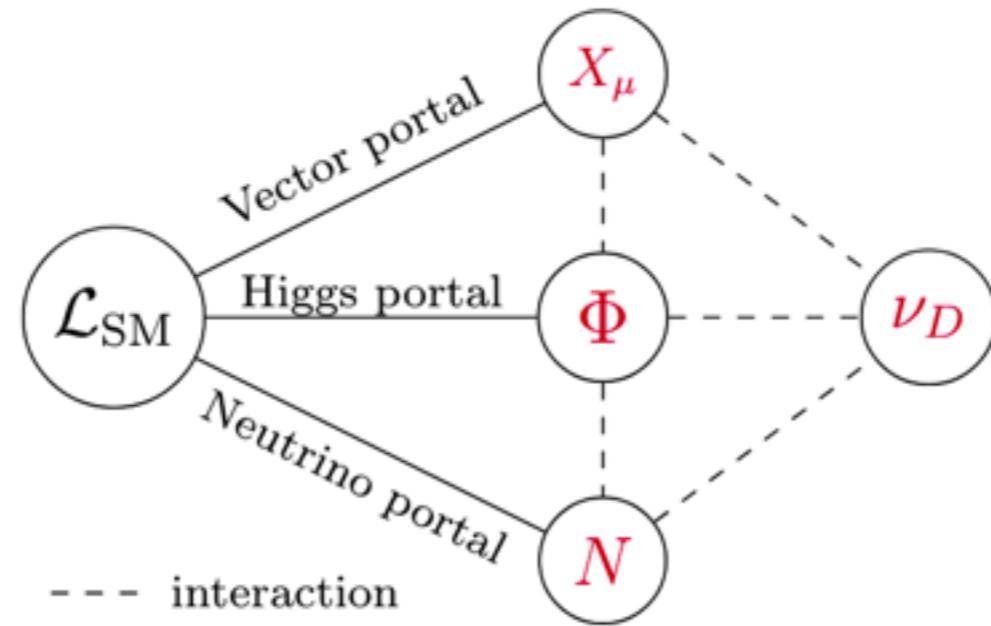


$L_e - L_\mu$ model



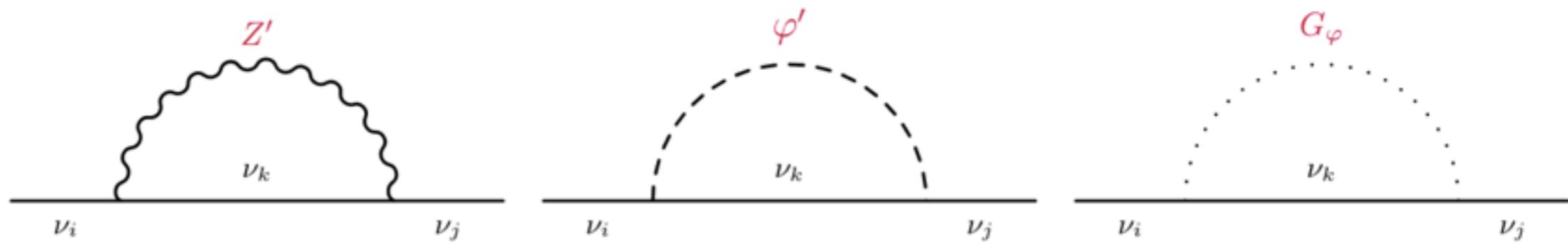
Dark Neutrinos

P. Ballett et al, arXiv:1903.07589



P. Ballett et al, arXiv:1903.07590

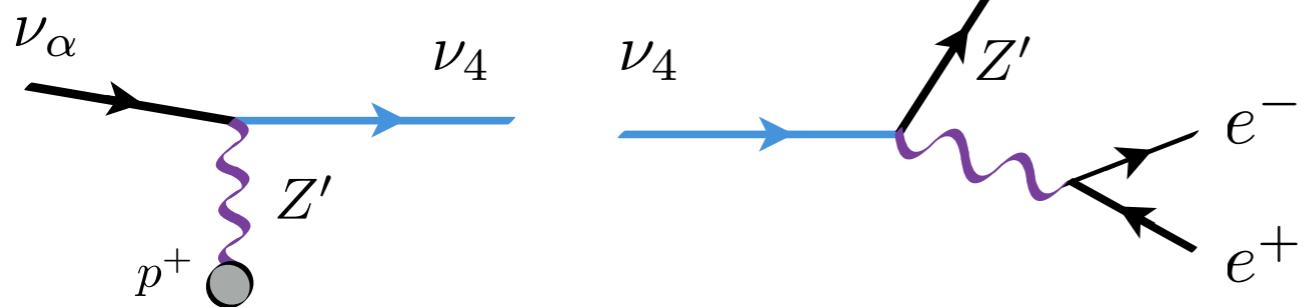
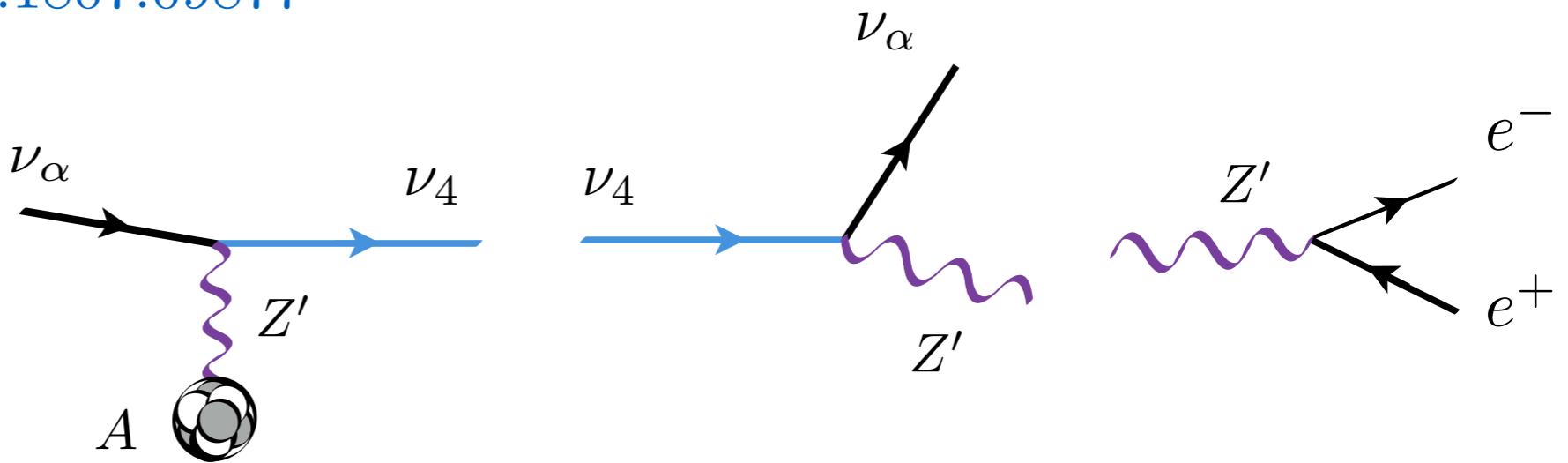
$$\mathcal{L}_{\text{mass}} \supset \frac{1}{2} \begin{pmatrix} \bar{\nu}_\alpha & \bar{N} & \bar{\nu}_D \end{pmatrix} \begin{pmatrix} 0 & m_D & 0 \\ m_D & \mu' & \Lambda \\ 0 & \Lambda & 0 \end{pmatrix} \begin{pmatrix} \nu_\alpha^c \\ N^c \\ \nu_D^c \end{pmatrix}$$



Dark Neutrinos

E. Bertuzzo et al. arXiv:1807.09877

$$m_{Z'} < m_4$$



P. Ballett et al. arXiv:1808.02915

$$m_{Z'} > m_4$$