

9 April 2019

Prospects of Neutrino Physics @IPMU

# Tomography by neutrino pair beam

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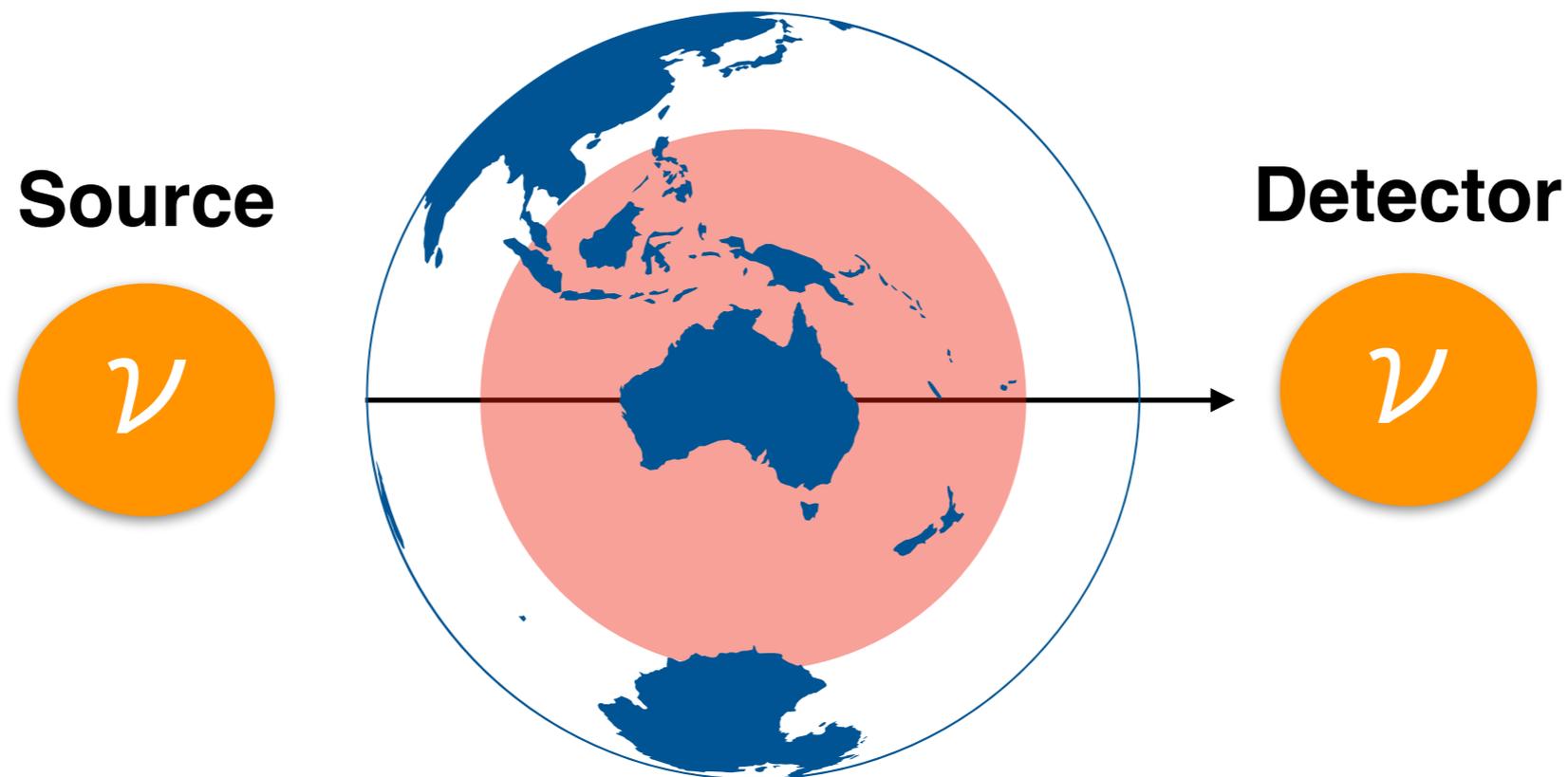
Okayama Univ.<sup>C</sup>, Motohiko Yoshimura<sup>C</sup>

[Phys.Lett.B785\(2018\) 536-542 \[arXiv:1805.10793\]](#)

**NIIGATA**  
UNIVERSITY

# Neutrino Tomography

- Thanks to the remarkable effort, our understanding of neutrino has improved greatly.
- **Neutrino Tomography** is one of the application of the Neutrino Physics.



Imaging of **the Earth's interior structure** by using neutrino

# Neutrino Tomography

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**Mainly we have two methods for neutrino tomography.**

- **Neutrino Absorption Tomography**

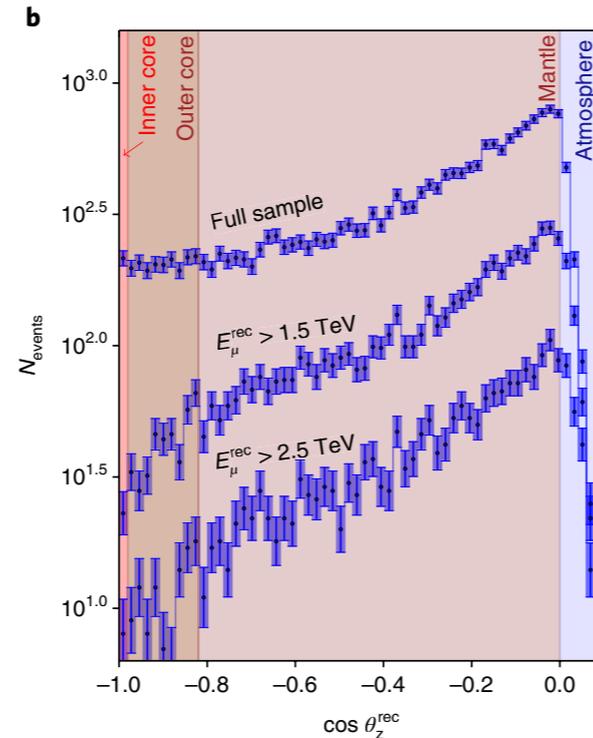
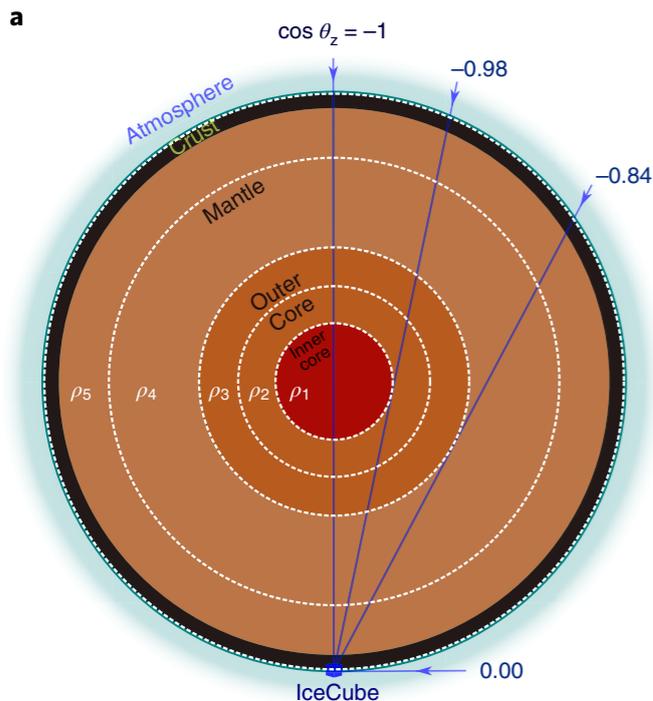
- **The image of the object can be reconstructed by measuring the absorption rates of high energy neutrino passing through the different angles.**
- **This is similar to X-ray computed tomography(X-ray CT).**

- **Neutrino Oscillation Tomography**

- **This aims to reconstruct the density profile by matter effect of the neutrino oscillation.**

# Neutrino Absorption Tomography

[A.Donini, S.Palomares-Ruiz, J.Salvado, Nature Phys. 15 \(2019\) no.1, 37-40](#)



They used the one-year of muon atmospheric neutrino data with energies extending above the TeV scale collected by the **IceCube** telescope.

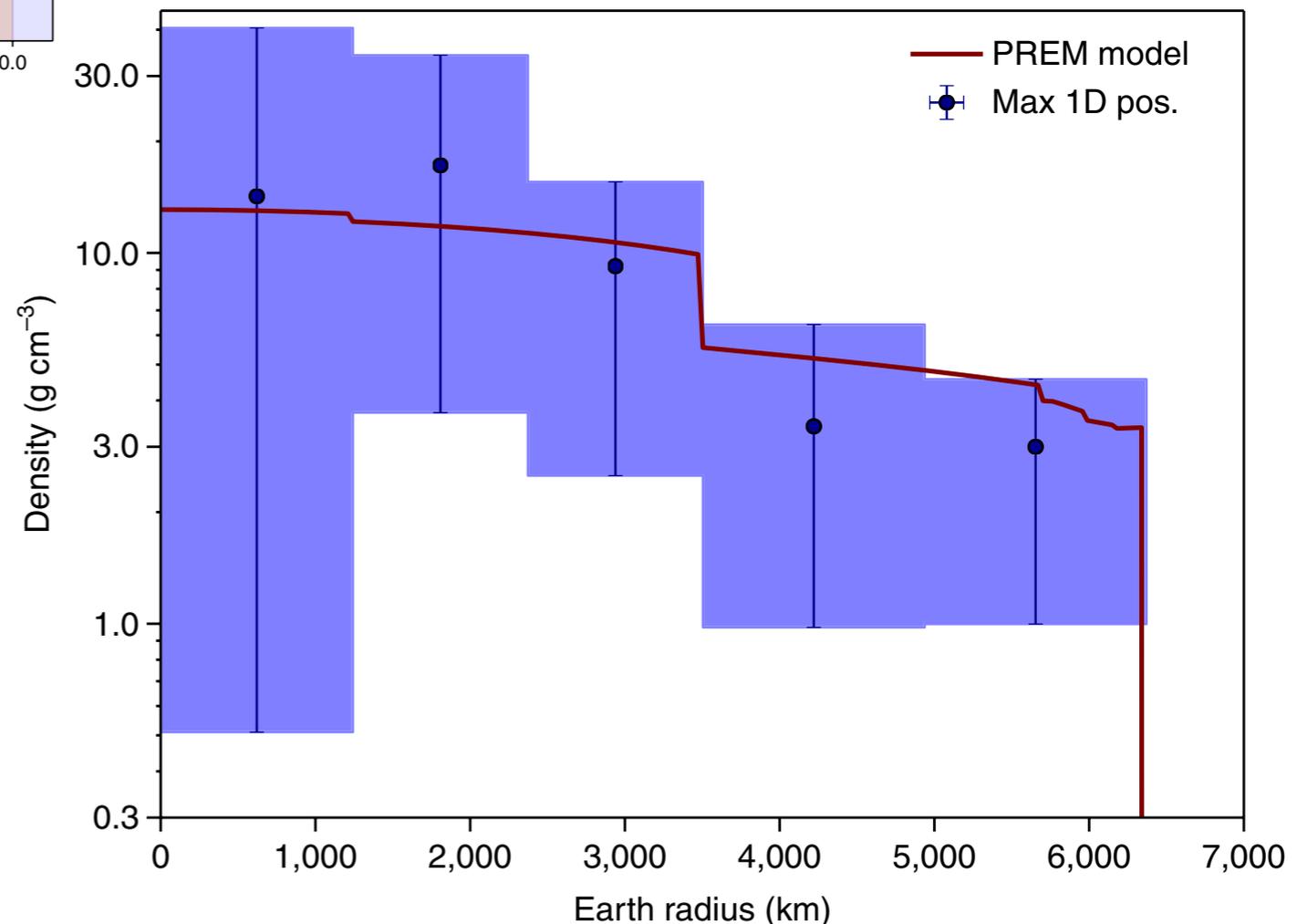
**20,145 muons was detected / 343.7 days**

## Non-gravitational measurement of Earth's mass

$$M_{\oplus}^{\nu} = (6.0_{-1.3}^{+1.6}) \times 10^{24} \text{ kg}$$

$$M_{\oplus}^{grav} = (5.9722 \pm 0.0006) \times 10^{24} \text{ kg}$$

**It requires more statistics for feasibility of the neutrino tomography.**



# Neutrino Oscillation Tomography

## Evolution equation in matter

$$i \frac{d}{dx} \begin{pmatrix} A_{\nu_e \rightarrow \nu_e} \\ A_{\nu_e \rightarrow \nu_\mu} \end{pmatrix} = \left[ U \begin{pmatrix} 0 & 0 \\ 0 & \frac{\Delta m^2}{2E} \end{pmatrix} U^\dagger + \begin{pmatrix} V_{CC}(x) & 0 \\ 0 & 0 \end{pmatrix} \right] \begin{pmatrix} A_{\nu_e \rightarrow \nu_e} \\ A_{\nu_e \rightarrow \nu_\mu} \end{pmatrix}$$

Effective potential is written as

$$V_{CC}(x) = \sqrt{2} G_F n_e(x)$$

The electron number density is translated into **the matter density**.

$$n_e(x) \simeq \frac{\rho(x)}{2m_p}$$

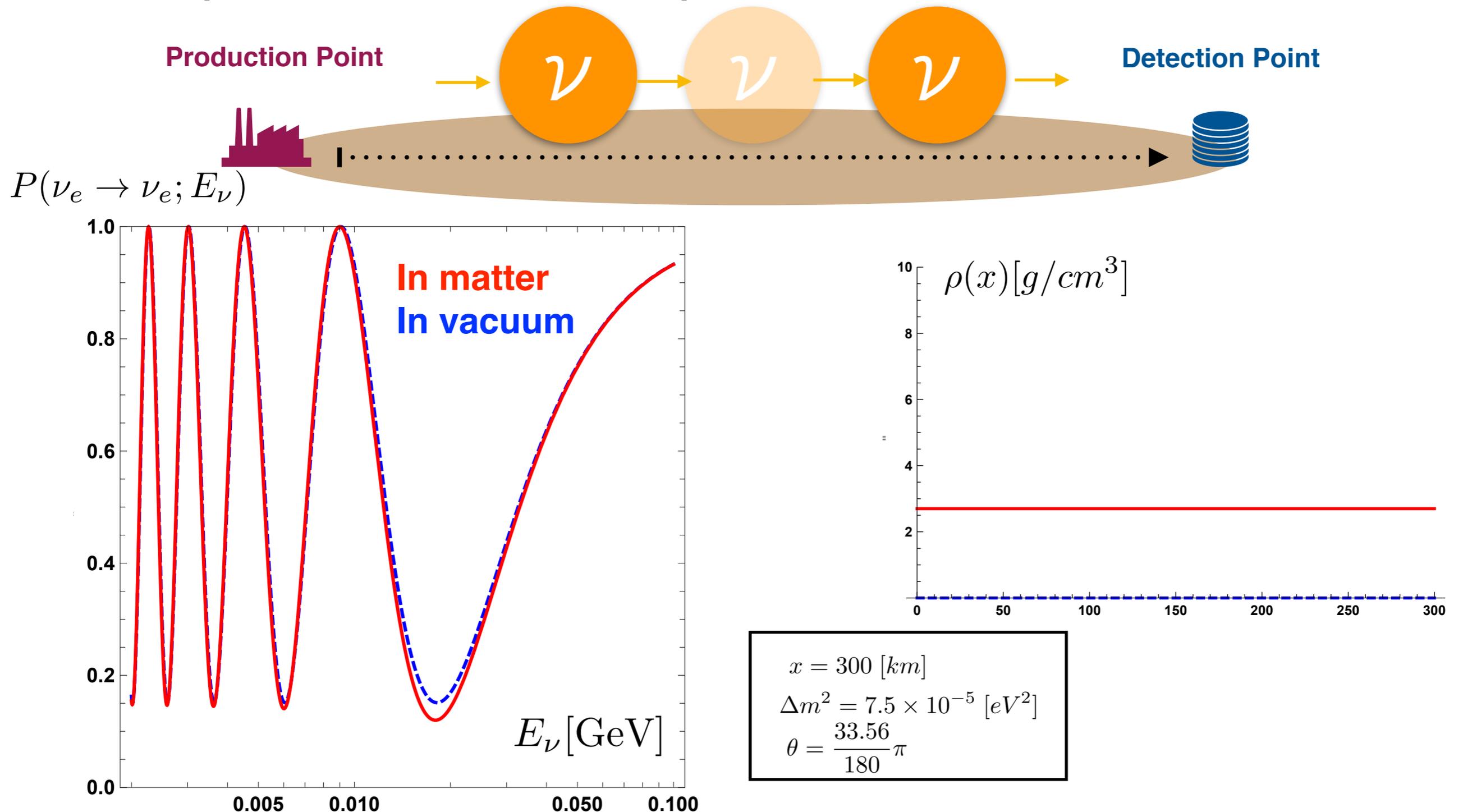
$$\begin{aligned} \rho &= m_p n_p + m_n n_n + m_e n_e \\ &\simeq m_N (n_p + n_n) && m_p \simeq m_n \gg m_e \\ &\simeq m_N 2n_e && n_e = n_p = n_n \\ \therefore n_e &\simeq \frac{\rho}{2m_N} \end{aligned}$$

Probability is calculated as follow

$$P_{\nu_\alpha \rightarrow \nu_\beta}(E_\nu, x) = |A_{\nu_\alpha \rightarrow \nu_\beta}(E_\nu, x)|^2$$

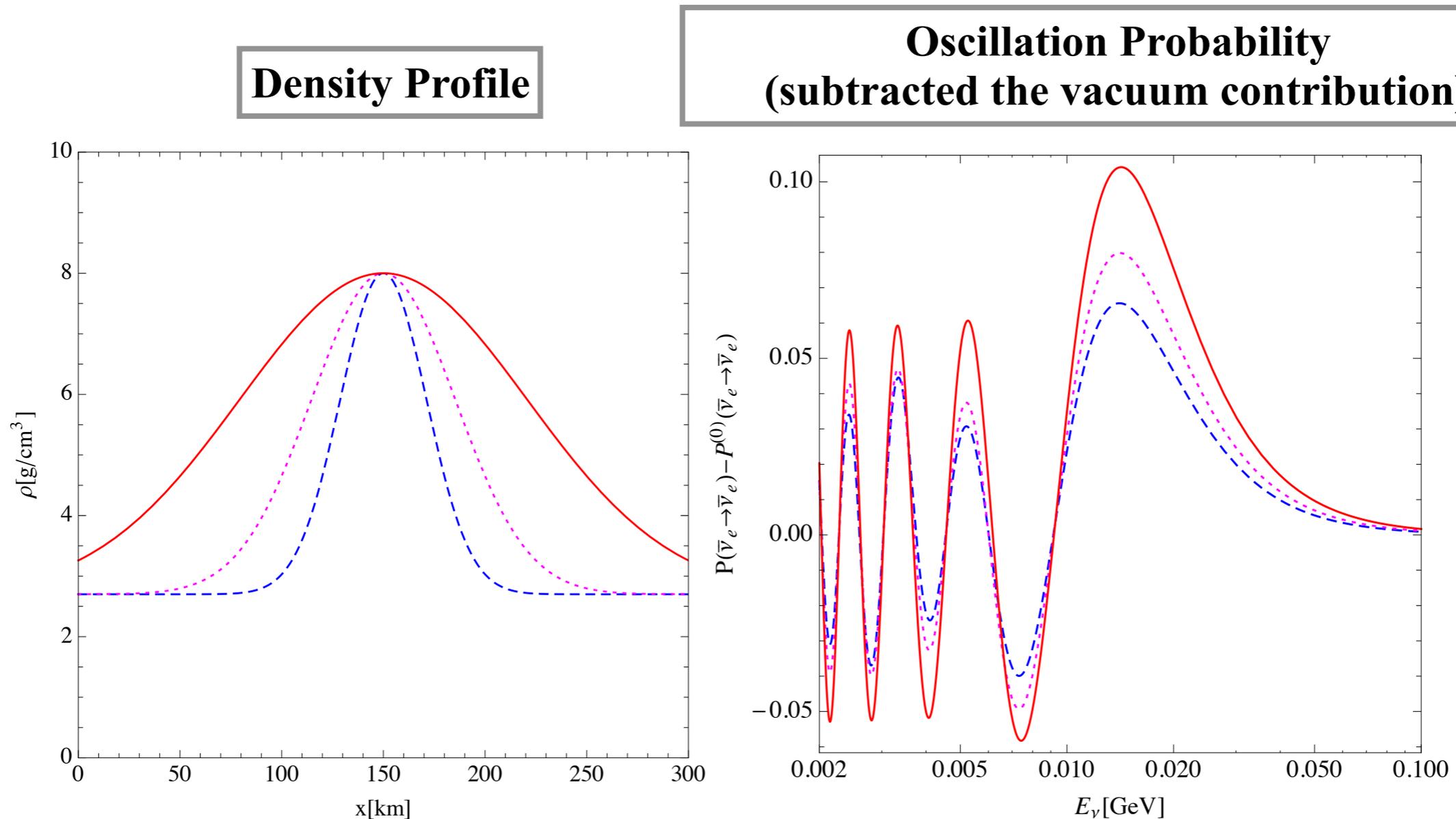
# Neutrino Oscillation Tomography

- The energy spectrum of the neutrino oscillation probability is **distorted**, compared to the vacuum one, by the **interaction with matter** through which neutrinos pass from the production to the detection point.



# Neutrino Oscillation Tomography

- Energy spectrum of the oscillation probability **changes according to the density profile.**



- **But this effect is small.**
- **So It requires the precise measurement of the energy spectrum.**

# Neutrino Oscillation Tomography

There are many approaches.

## Neutrino Source

Atmospheric

W.Winter;  
C.Rott, A.Taketa, D. Bose; ...

Solar

E.K.Akhmedov, M.Tortola, J.Valle;  
A.N.Ioannisiyam, A.Yu.Smirnov

Supernova

E.K.Akhmedov, M.Tortola, J.Valle;  
M.Lindner, T.Ohlsson, R.Tortola, W.Winter

man-made beam

V.Ermilova, V.Tsarev, V.Chechin;  
T.Ohlsson, W.Winter, ...

## Analysis

$\chi^2$  analysis

Likelihood analysis

Several papers

Fourier analysis

E.K.Akhmedov, M.Tortola, J.Valle;  
T.Ota, J.Sato; ....

Expansion analysis

A.N.Ioannisiyam, A.Yu.Smirnov;...

## Target

Density profile of entire Earth

Density fluctuation

Earth's core

Z/A ratio

Specific site

# Neutrino Oscillation Tomography

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## Open Questions

- **How do we realize accurate energy spectrum measurement ?**
- **How do we reconstruct the Earth's density distribution ?**

# Neutrino Oscillation Tomography

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## Open Questions

## Our Approach

- How do we realize accurate energy spectrum measurement ?  
→ **Powerful source (Neutrino pair beam)**
- How do we reconstruct the Earth's density distribution ?  
→ **Reconstruction method with 2nd order perturbation**

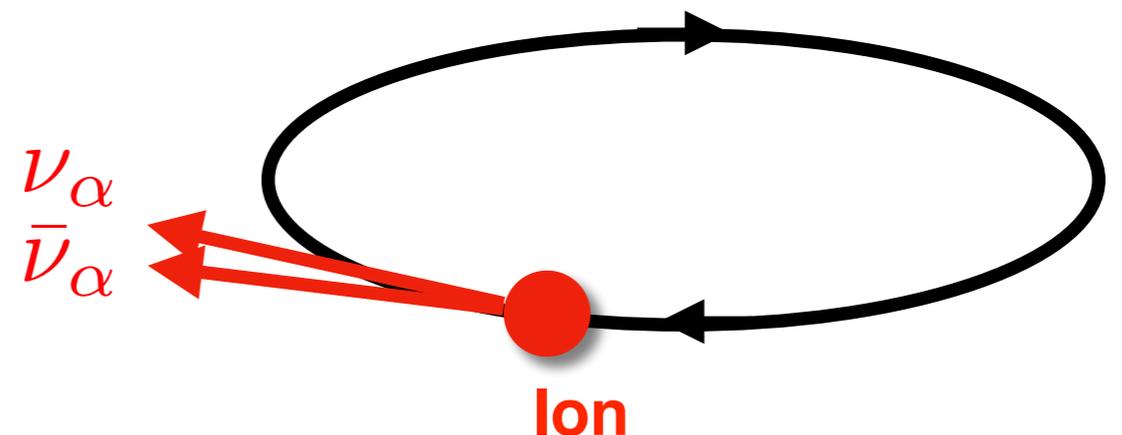
# Neutrino Pair Beam

- The **pair beam**, which has been proposed recently, can produce a large amount of neutrino pairs from the circulating partially stripped ions.

[Yoshimura, Sasao, Phys. Rev. D 92, 073015 (2015)]

## Characteristics of the Neutrino Pair Beam

- It generates the all flavor neutrino pairs  
 $(\nu_e, \bar{\nu}_e), (\nu_\mu, \bar{\nu}_\mu), (\nu_\tau, \bar{\nu}_\tau)$
- Very high intensity flux of neutrino beam
- High beam directivity
- Mainly electron neutrino pair being generated



- Neutrino tomography requires **the precise measurement** of the energy spectrum for the precise reconstruction of the density profile.
- **High event rate (high flux)** is essential.

# Neutrino Pair Beam

Source	Energy	Flux
Atmospheric : $\nu_\mu$ ( $\cos \theta_Z = 0$ )	3.2 GeV	$3.6 \times 10^2 [\text{m}^{-2}\text{s}^{-1}]$
Solar	10MeV	$10^4 [\text{m}^{-2}\text{s}^{-1}]$
T2K at SK : $\nu_\mu$	1GeV	$2 \times 10^4 [\text{m}^{-2}\text{s}^{-1}]$
Beta beam at 100 km : $\bar{\nu}_e$	581 MeV (average)	$2.1 \times 10^5 [\text{m}^{-2}\text{s}^{-1}]$
Neutrino Pair Beam at 100 km	100 MeV	$\sim 10^{10} [\text{m}^{-2}\text{s}^{-1}]$
Neutrino Pair Beam at 300 km	100 MeV	$\sim 10^9 [\text{m}^{-2}\text{s}^{-1}]$

**Atmospheric : M. Honda et.al., PhysRevD.92.023004**

**Solar : J. N. Bahcall et.al., New J. Phys. 6 (2004) 63**

**T2K : K. Abe et al. Phys. Rev. D 87 (2013) no.1, 012001**

**Beta beam : P. Zucchelli, Phys. Lett. B 532 (2002) 166**

**Neutrino Pair Beam : M.Yoshimura, N.Sasao, Phys.Rev.D92(2015) no.7, 073015**

**Production amount of neutrino (estimation)**

**nuMAX (Neutrino Factory) :  $\sim 10^{20}$  / yr**

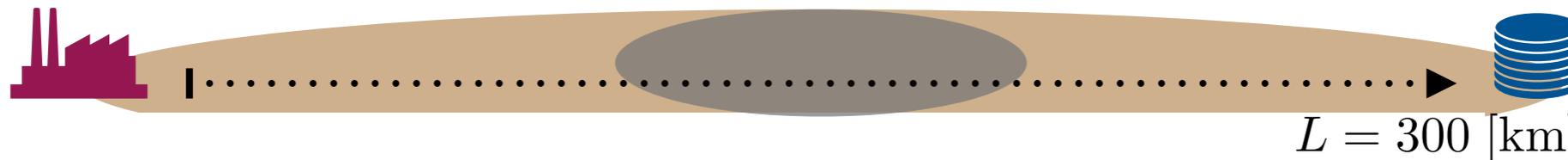
**NPB :  $\sim 10^{22}$  / yr**

# Toy Model

Source Point

?

Detection Point



- We consider the symmetric density profile.

e.g.

$$\rho(x) = \bar{\rho} + (\rho_l - \bar{\rho}) \exp\left[-\frac{\left(x - \frac{L}{2}\right)^2}{D_l^2}\right]$$

$L$  : length of the baseline  
 $D_l$  : width of the lump

- We consider the low energy  $\bar{\nu}_e \rightarrow \bar{\nu}_e$  oscillation.

$$E_\nu : 2 \sim 100 \text{ [MeV]}$$

The neutrino energy threshold  $\approx 1.806$  MeV.

- We assume the huge liquid Argon as the neutrino detector.

Fiducial volume  $10^5 \text{ m}^3$

e.g. HK's volume  $2.6 \times 10^5 \text{ m}^3$

<http://www.hyper-k.org/overview.html>

We don't discuss about systematic error.

# Statistical Analysis

We estimate how precisely the width ( $D_*$ ) and density ( $\rho_*$ ) of the lump can be reconstructed under this set-up.

$$\rho(x) = \bar{\rho} + (\rho_l - \bar{\rho}) \exp\left[-\frac{(x - \frac{L}{2})^2}{D_l^2}\right] \quad \bar{\rho} = 2.7[\text{g/cm}^3]$$

We perform the  $\chi^2$  analysis.

$$\Delta\chi^2 = \sum_{i=1}^{N_b} \frac{[N(E_i)|_{D_*,\rho_*} - N(E_i)|_{D_l,\rho_l}]^2}{\sigma^2(E_i)}$$

$N_b = 100$  : the number of energy bin

$N$  (Event number) = flux  $\times$  oscillation probability  $\times$  detection rate

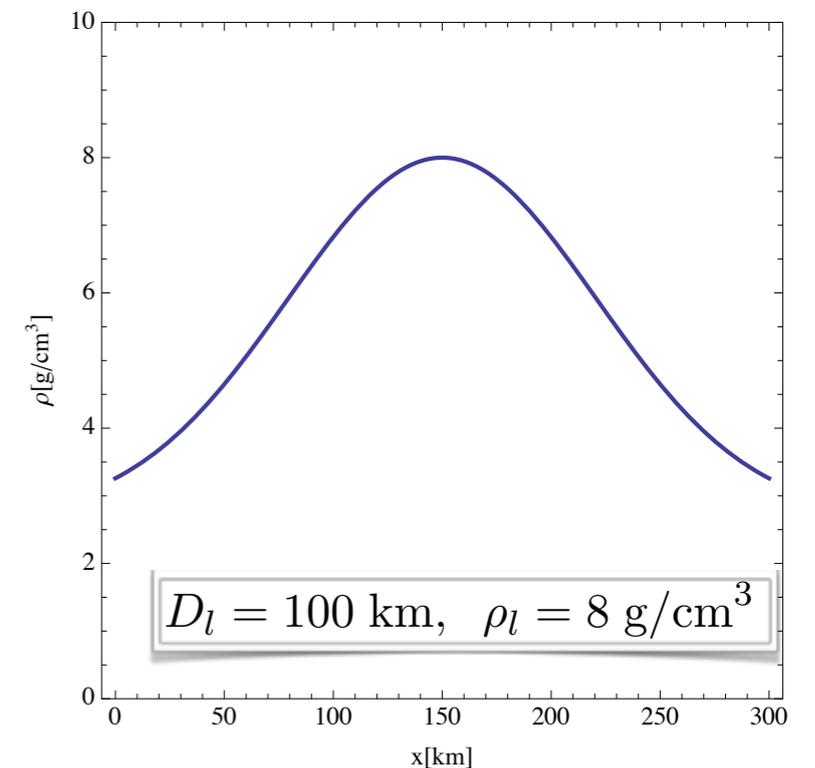
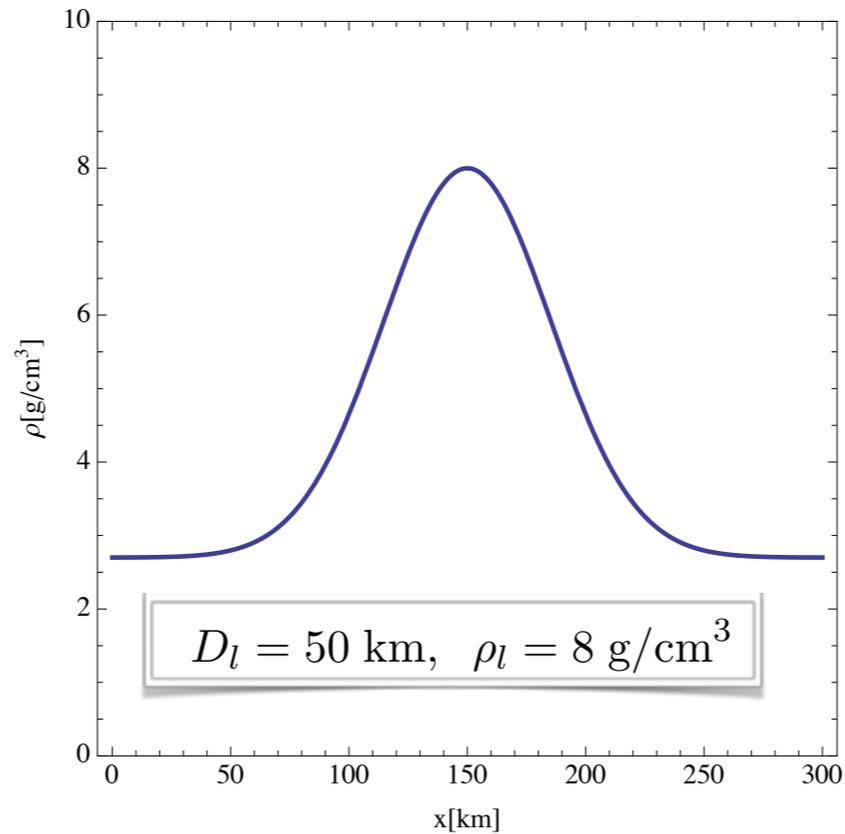
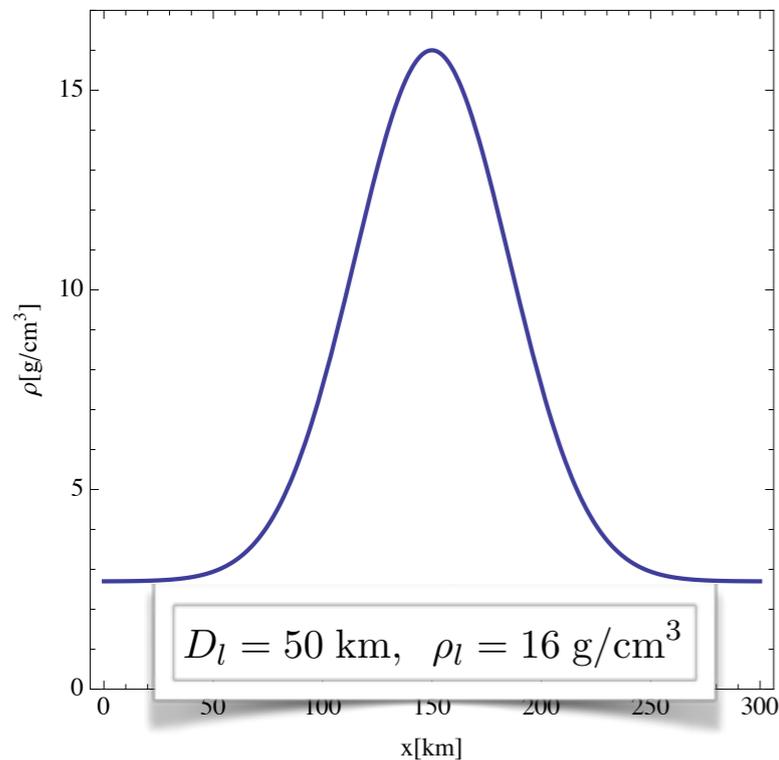
We assume 1 year as experimental running time.

- \* We only consider the statistical error in this calculation.
- \* (It is not included the systematic error)

# Statistical Analysis

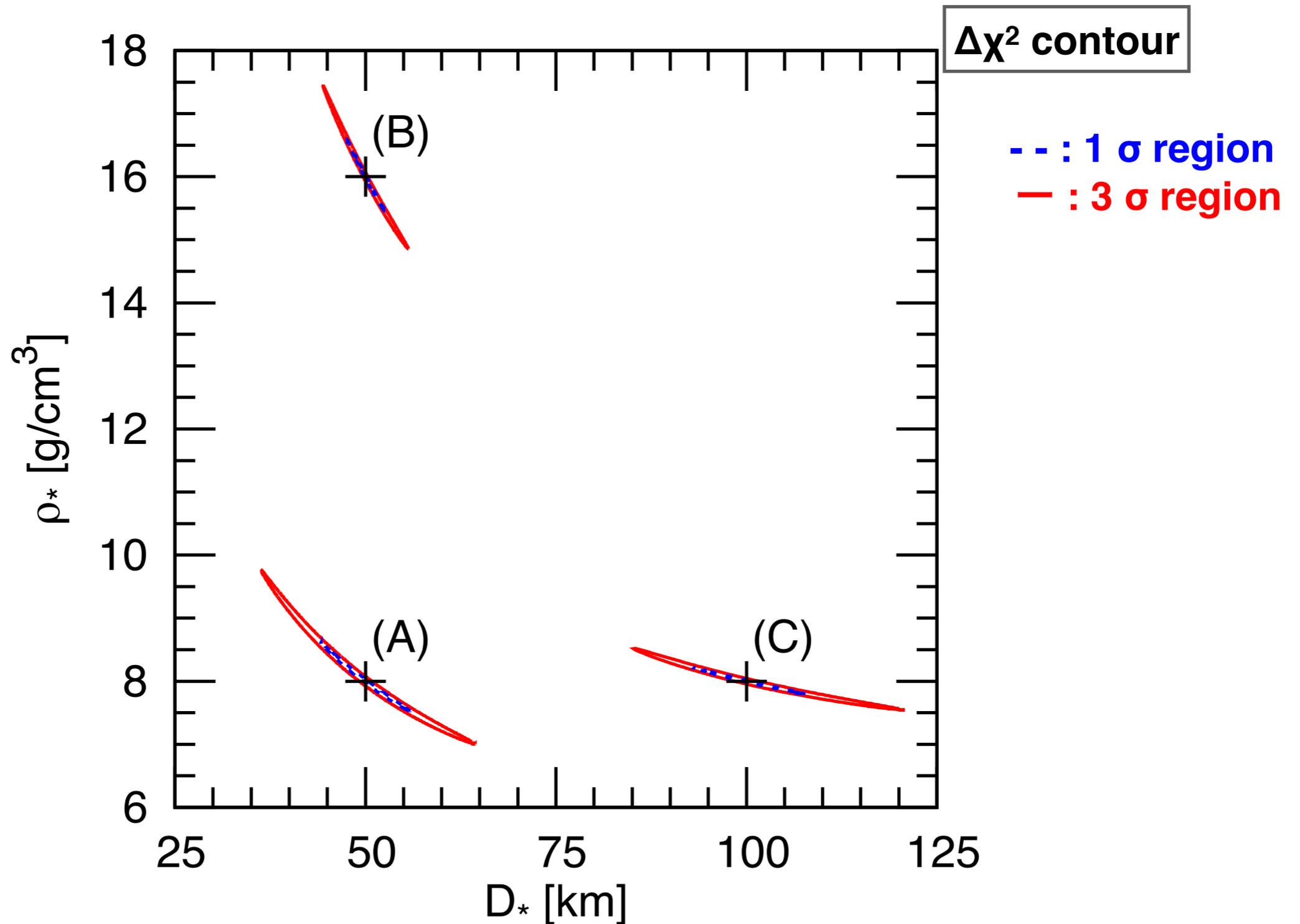
We assume the 3 density profiles.

$$\rho(x) = \bar{\rho} + (\rho_l - \bar{\rho}) \exp\left[-\frac{\left(x - \frac{L}{2}\right)^2}{D_l^2}\right]$$



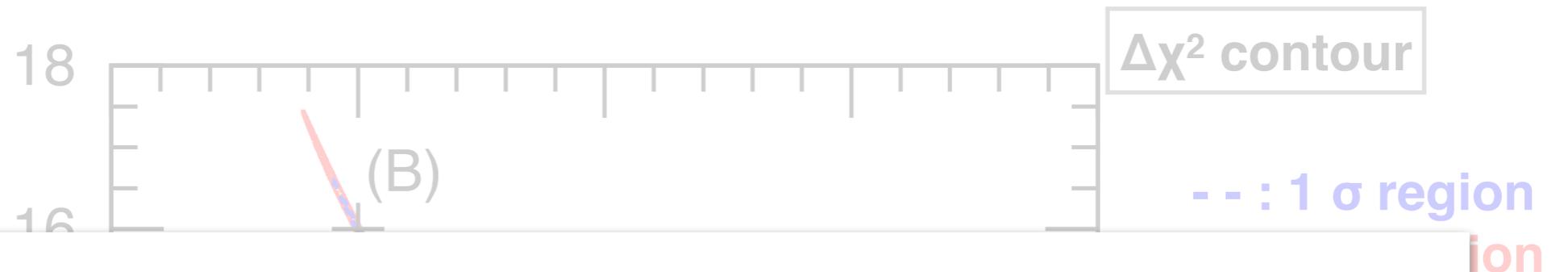
# Results

We assume the 3 density profiles.



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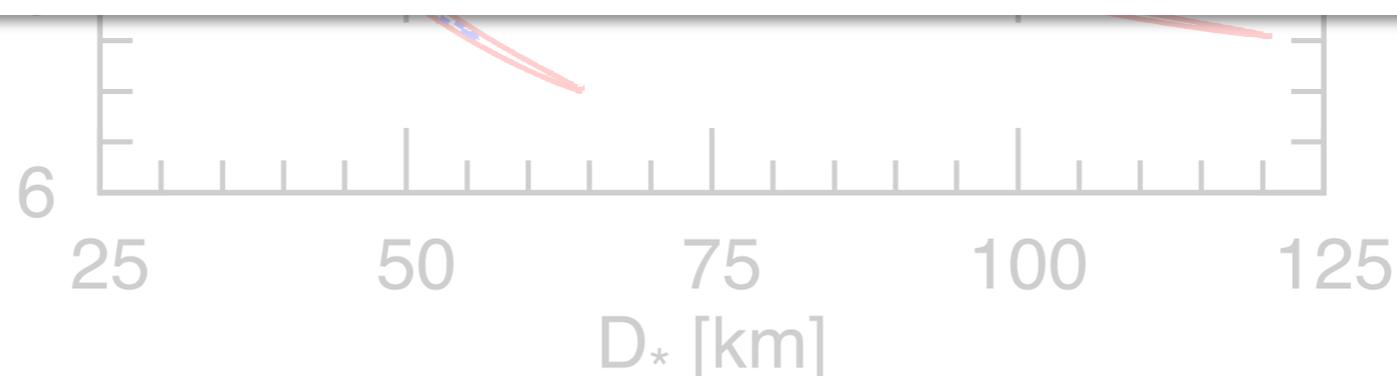
The pair beam can probe the lump at the 1  $\sigma$  level as

$$(A) \quad D_* = 50_{-5.9}^{+5.9} \text{ km} \quad \text{and} \quad \rho_* = 8.0_{-0.48}^{+0.62} \text{ g cm}^{-3},$$

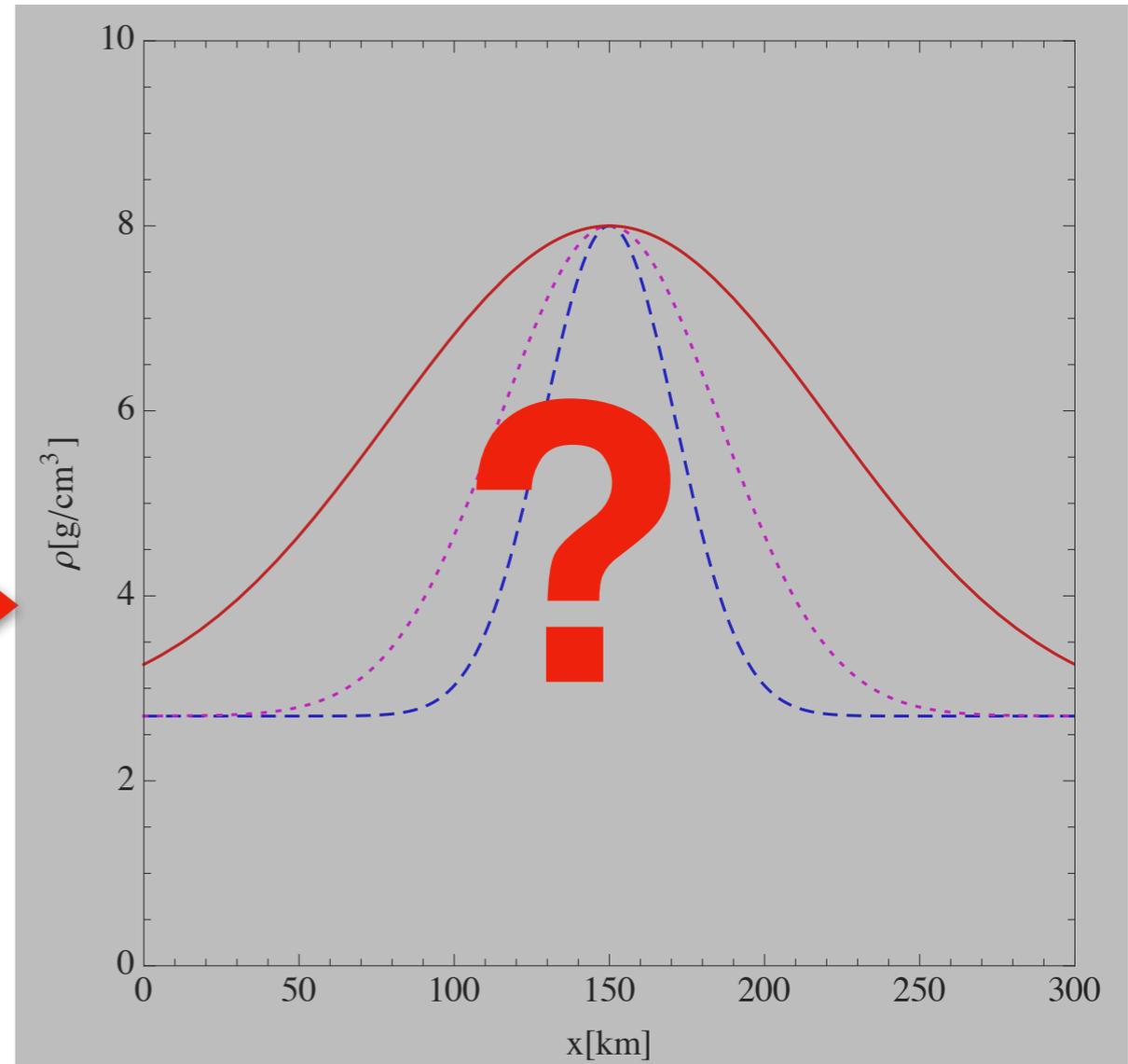
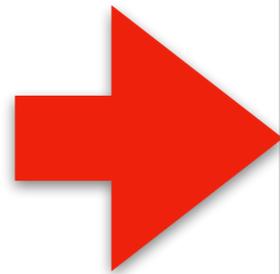
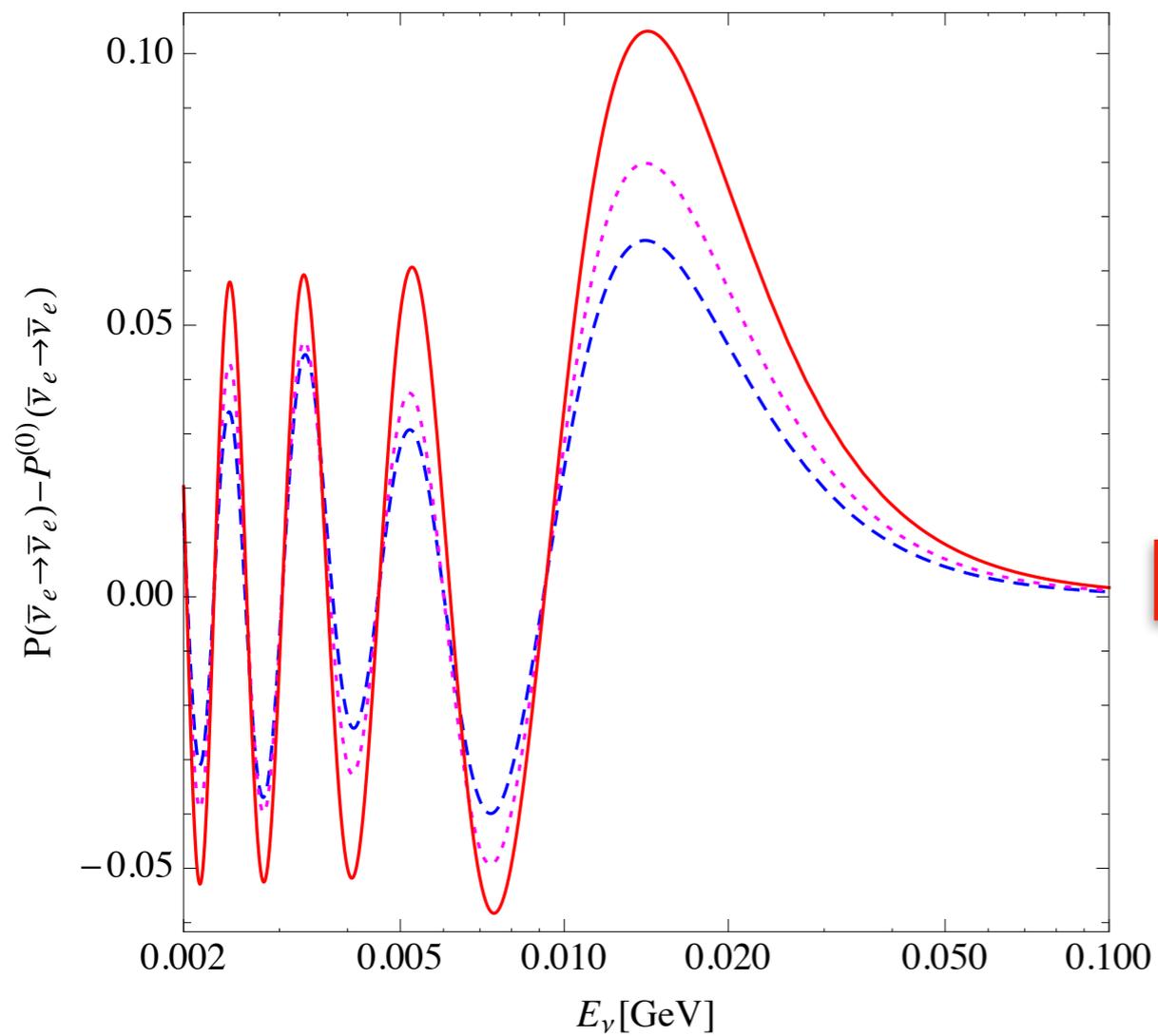
$$(B) \quad D_* = 50_{-2.4}^{+2.5} \text{ km} \quad \text{and} \quad \rho_* = 16_{-0.53}^{+0.58} \text{ g cm}^{-3},$$

$$(C) \quad D_* = 100_{-7.1}^{+8.2} \text{ km} \quad \text{and} \quad \rho_* = 8.0_{-0.21}^{+0.22} \text{ g cm}^{-3},$$

**It is seen that the neutrino pair beam can provide a powerful source for the measurement of the density profile.**

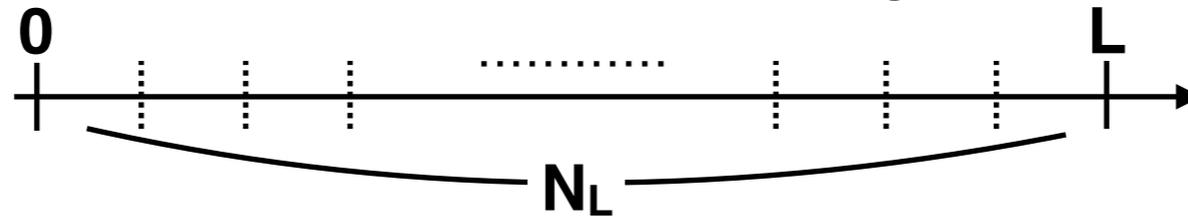


# How reconstruct the entire density profile from the energy spectrum of the neutrino oscillation?

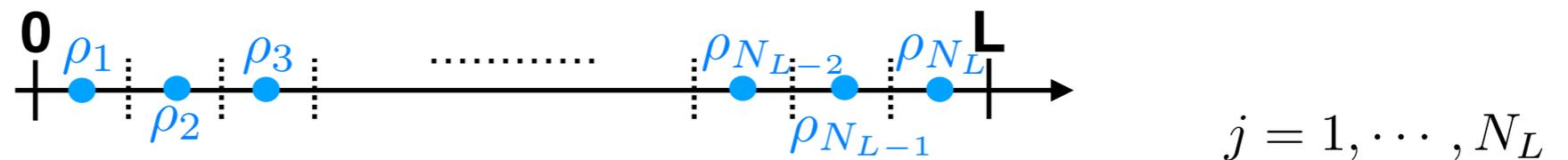


# Reconstruction Method

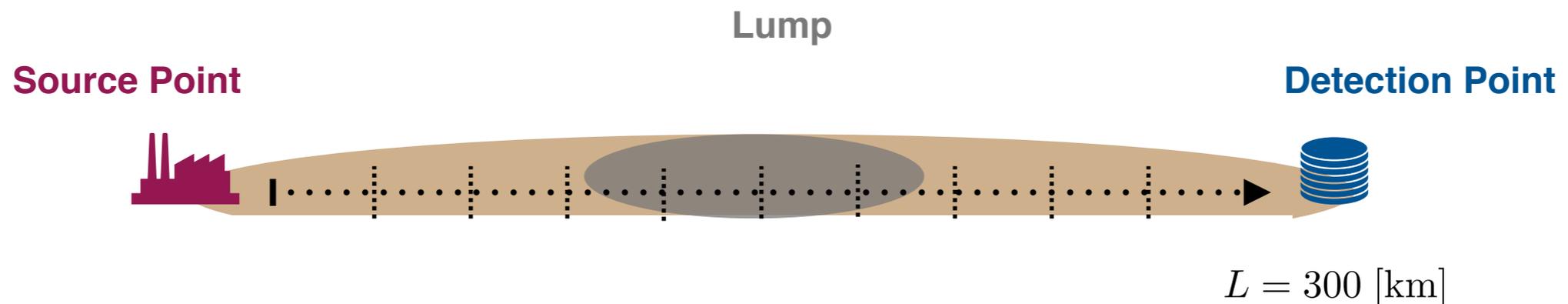
1. We discretize the neutrino baseline into the  $N_L$  segments.



2. We consider the matter densities for these segments as free parameters  $\rho_j$ .

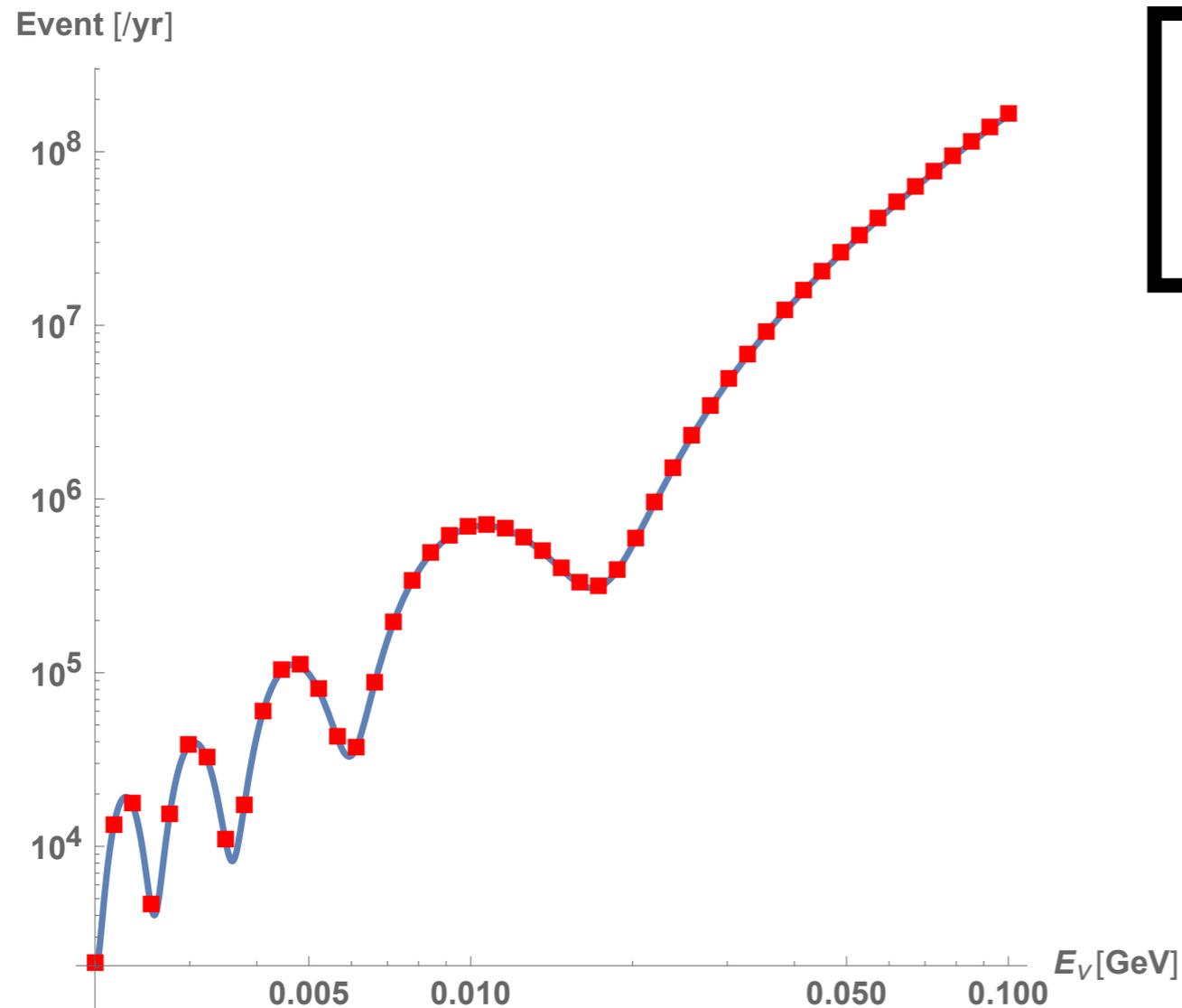


We assume that the each density is constant within each segment.



# Reconstruction Method

3. We also divide the energy range into the  $N_E$  parts, and define the  $\chi^2$  function



$$\chi^2 = \sum_{i=1, N_E} \frac{[N^{\text{obs}}(E_i) - N^{\text{th}}(E_i)]^2}{\sigma^2(E_i)}$$

$$\sigma(E_i) = \sqrt{N^{\text{obs}}(E_i)}.$$

$$\begin{aligned} N(E_\nu) &\simeq 4.73 \times 10^7 \times P(\bar{\nu}_e \rightarrow \bar{\nu}_e; E_\nu) \\ &\times \left( \frac{E_\nu}{100 \text{ MeV}} \right)^{\frac{5}{2}} \left( \frac{\Delta E_\nu}{1 \text{ MeV}} \right) \left( \frac{300 \text{ km}}{L} \right)^2 \\ &\times \left( \frac{V_d}{10^5 \text{ m}^3} \right) \left( \frac{T}{1 \text{ year}} \right). \end{aligned}$$

# Reconstruction Method

$$N^{\text{th}}(E_i) = \text{flux} \times P_{\bar{\nu}_e \rightarrow \bar{\nu}_e}(E, L) \times \text{detection rate}$$

Neutrino oscillation probability is calculated from the evolution equation.

$$i \frac{d}{dx} \vec{A}(x) = [H_0^F + V^F] \vec{A}(x)$$

Then we assume the relation  $H_0^F > V^F$

And calculate the oscillation probability by perturbation.

$$\begin{aligned} P_{\alpha\beta} &= |A_{\beta\alpha}^{(0)} + A_{\beta\alpha}^{(1)} + A_{\beta\alpha}^{(2)} + \dots|^2 \\ &= \underbrace{|A_{\beta\alpha}^{(0)}|^2}_{\text{0th}} + \underbrace{A_{\beta\alpha}^{(0)*} A_{\beta\alpha}^{(1)} + A_{\beta\alpha}^{(0)} A_{\beta\alpha}^{(1)*}}_{\text{1st}} + \underbrace{|A_{\beta\alpha}^{(1)}|^2 + A_{\beta\alpha}^{(0)*} A_{\beta\alpha}^{(2)} + A_{\beta\alpha}^{(0)} A_{\beta\alpha}^{(2)*}}_{\text{2nd}} + \dots \end{aligned}$$

Ex) perturbation formula at 1st order is written as

$$P^{(1)}(E_i) \propto \sum \rho(x_j) \left[ \sin \left\{ \frac{\Delta m^2}{2E_i} L \right\} - \sin \left\{ \frac{\Delta m^2}{2E_i} L \right\} x_j - \sin \left\{ \frac{\Delta m^2}{2E_i} (L - x_j) \right\} \right]$$

# Reconstruction Method

4. We determine density profile by minimizing the  $\chi^2$  function by comparing the observational data  $N^{\text{obs}}(E_i)$  with given original profile  $\rho(x)$  and the theoretical prediction  $N^{\text{th}}(E_i)$  with unknown parameters  $\rho_j$ .

$$\chi^2 = \sum_{i=1, N_E} \frac{[N^{\text{obs}}(E_i) - N^{\text{th}}(E_i)]^2}{\sigma^2(E_i)}$$

$$N^{\text{th}}(E_i) = \text{flux} \times P_{\bar{\nu}_e \rightarrow \bar{\nu}_e}(E, L) \times \text{detection rate}$$

Neutrino Oscillation Probability  
of the perturbation formulae

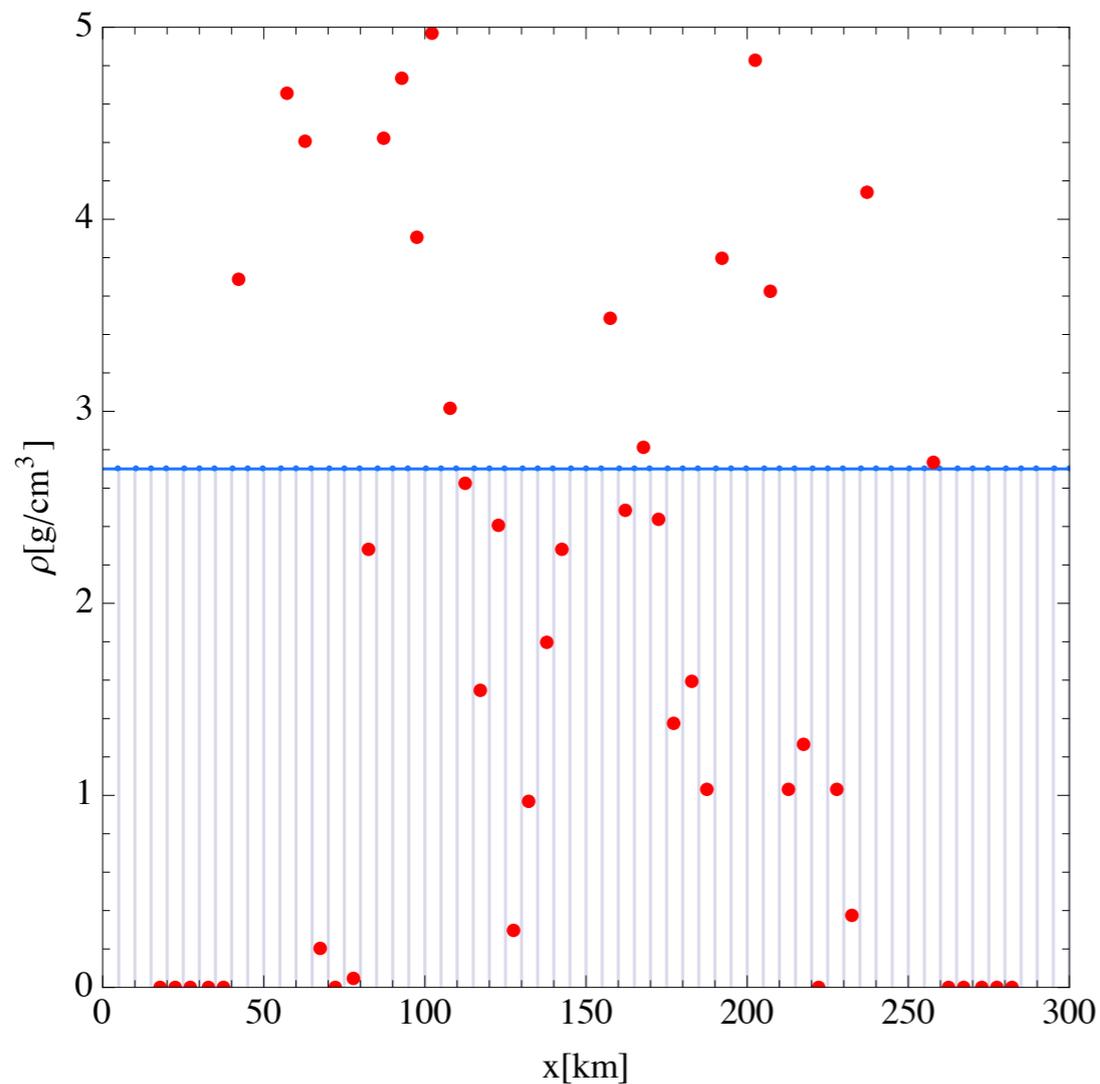
**We find the 2nd order perturbation is important for the successful reconstruction.**

# Results

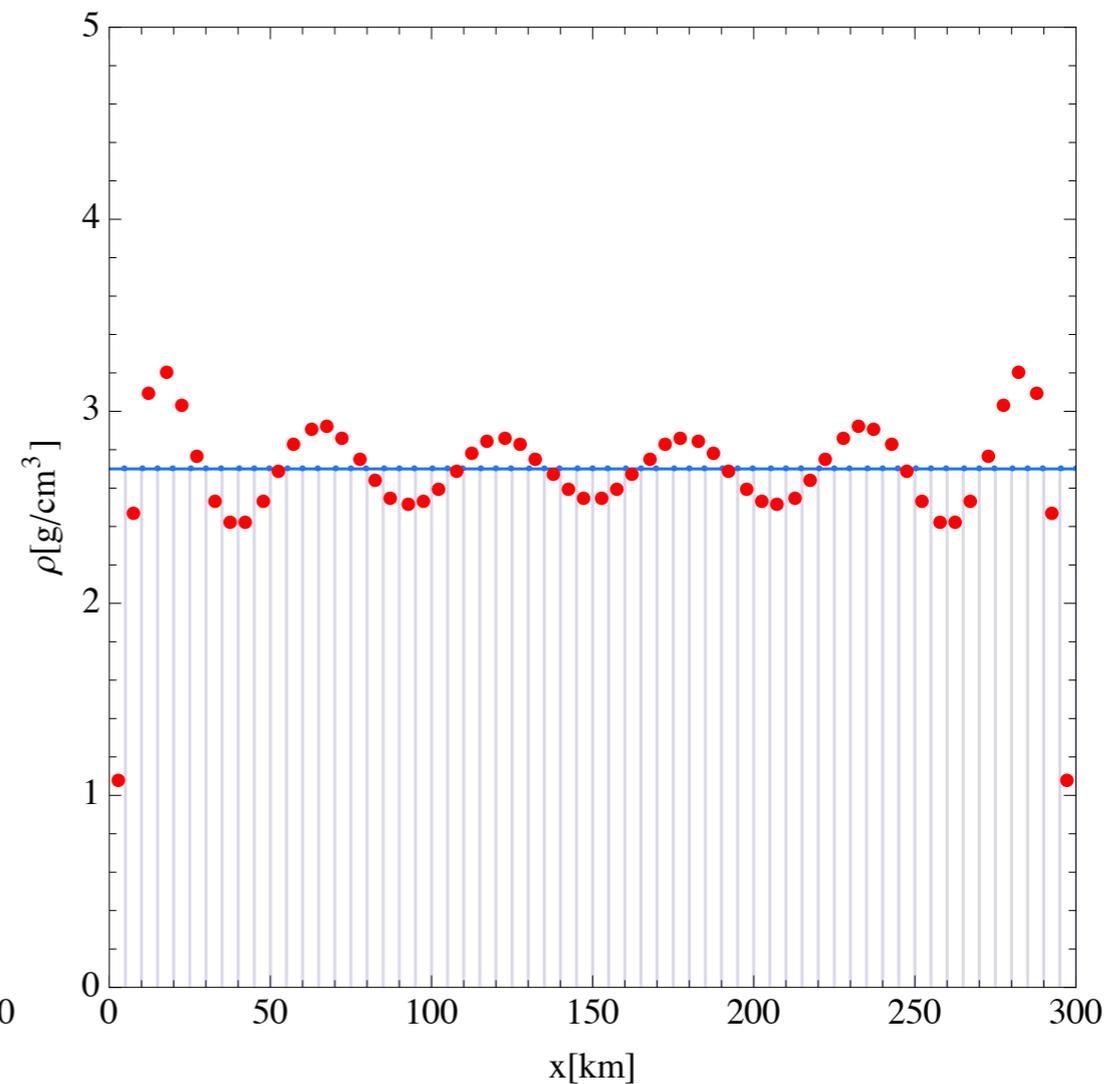
Reconstruction of 60 segment's densities  
with 100 energy bins

$$\bar{\rho} = 2.7 \text{ [g/cm}^3\text{]}$$

Result with using the 1st order formula



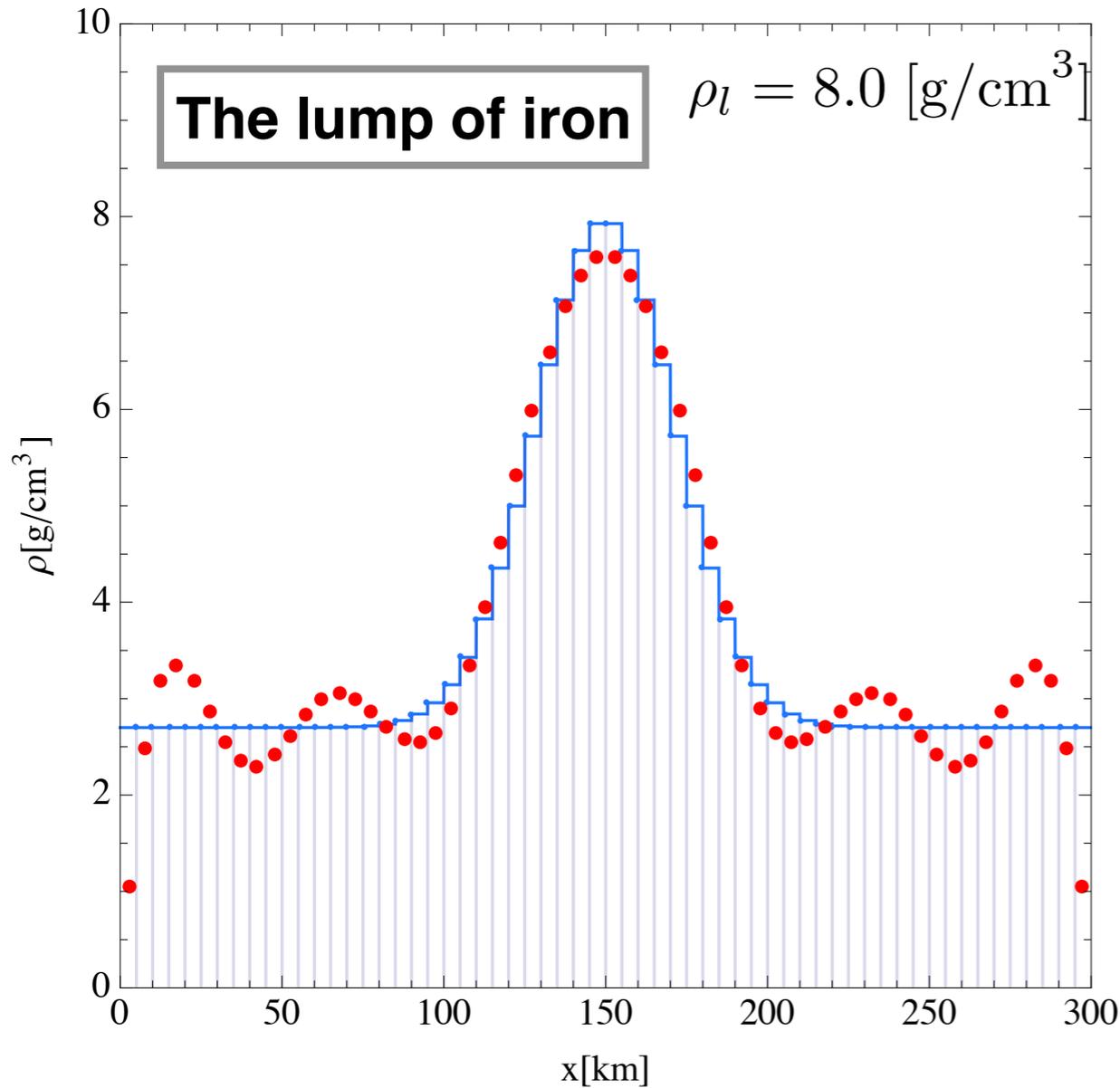
Result with using the 2nd order formula



- : Original density profile  
• : Reconstructed density profile

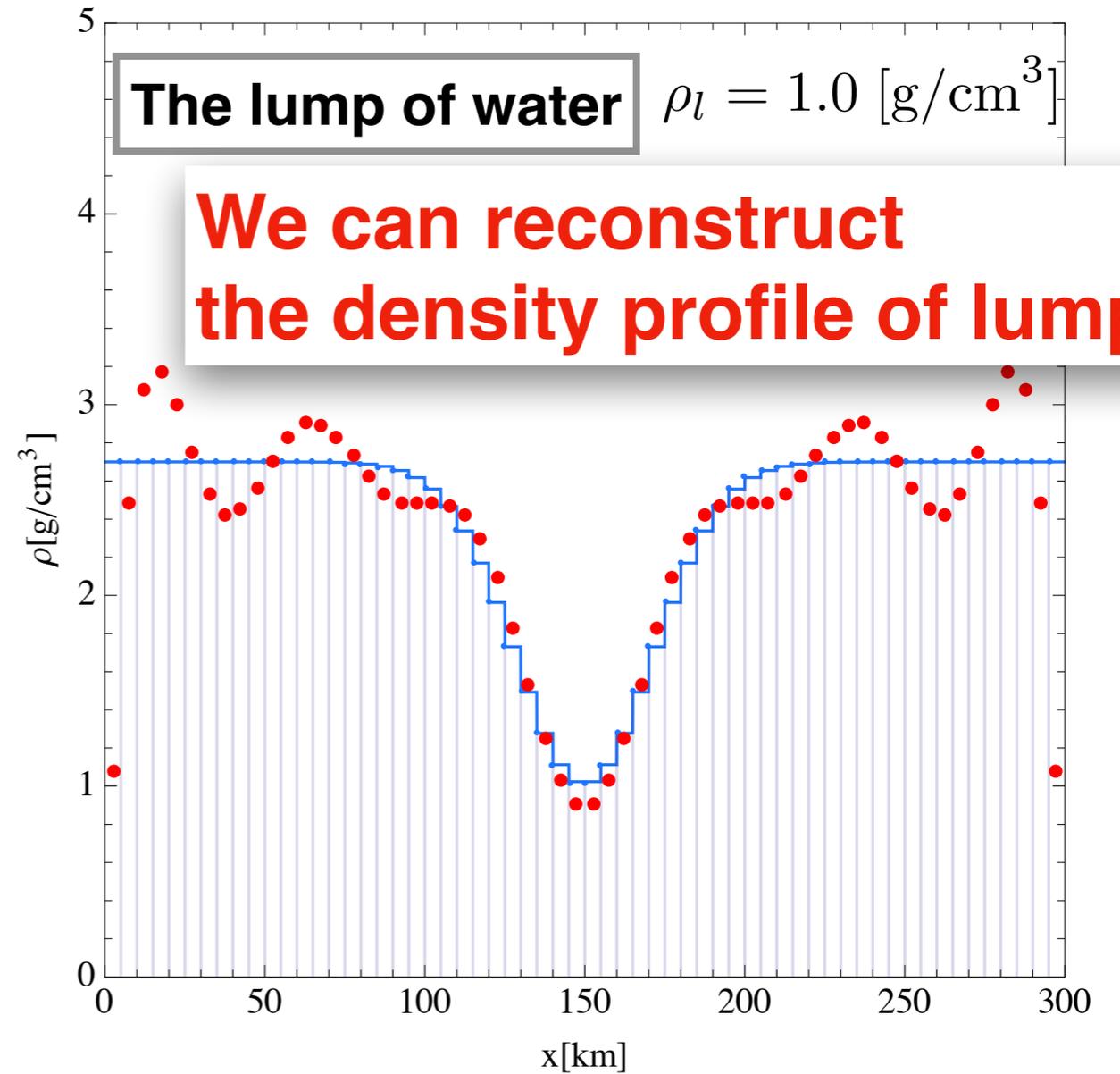
# Results

Reconstruction of 60 segment's densities  
with 100 energy bins



Original density profile  $\bar{\rho} = 2.7 \text{ [g/cm}^3\text{]}$   

$$\rho(x) = \bar{\rho} + (\rho_l - \bar{\rho}) \exp\left[-\frac{(x - \frac{L}{2})^2}{D_l^2}\right]$$



- : Original density profile  
 • : Reconstructed density profile

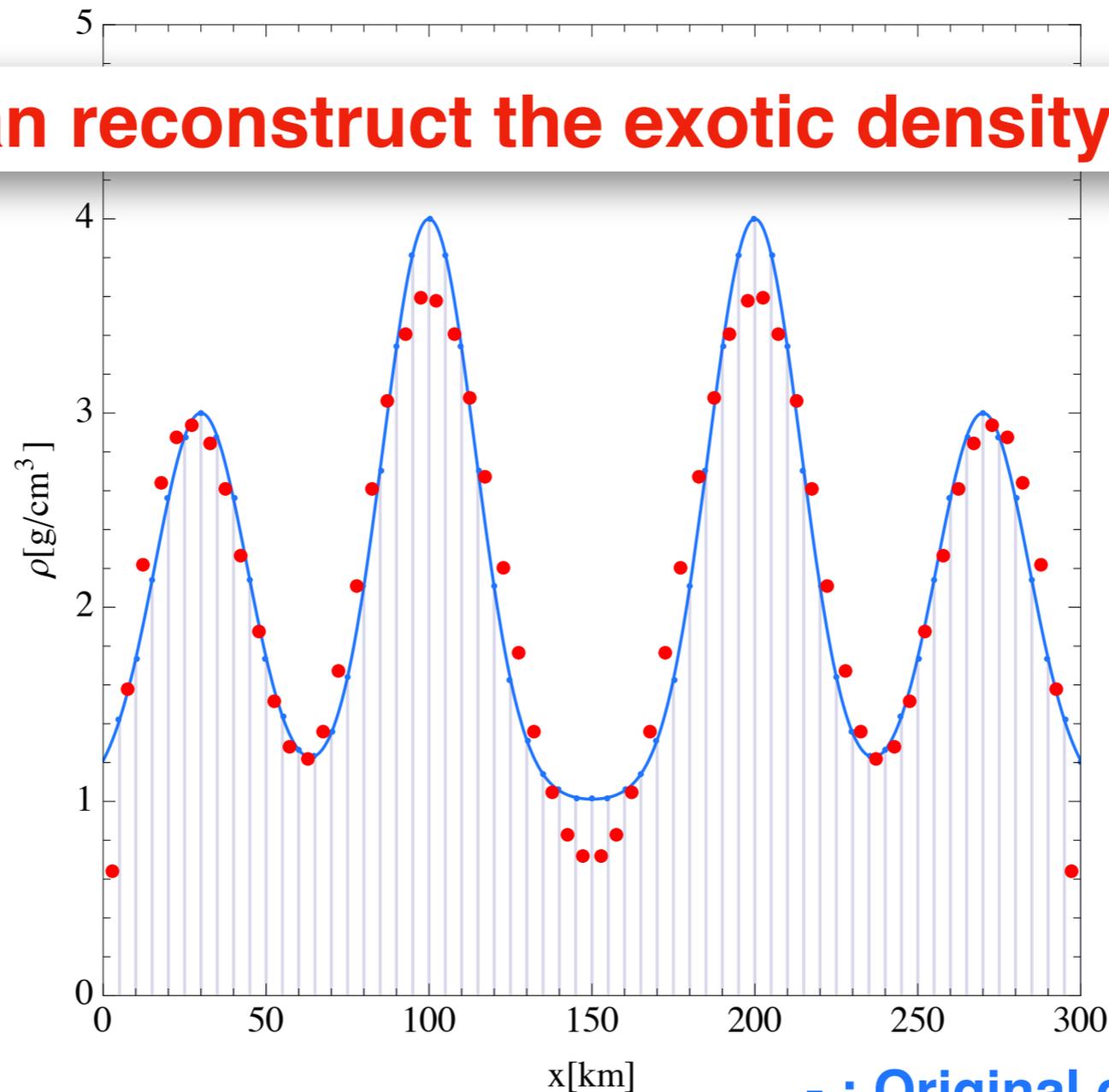
# Results

Reconstruction of 60 segment's densities  
by 100 energy bin data

using the 2nd order formula

4 lump

**We can reconstruct the exotic density profile.**



- : Original density profile

• : Reconstructed density profile

# Conclusions

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**We have investigated the neutrino oscillation tomography by the neutrino pair beam.**

## In this talk

- **The neutrino pair beam is a powerful source to the probe of the Earth's interior, especially the structures inside the crust.**
- **The reconstruction method with the 2nd order perturbation formula is successful tool.**
- **We believe that these two ingredients give considerable progress toward the realization of the neutrino tomography.**