# Migdal Effect in Dark Matter Direct Detection Experiments and Its Applications

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<u>Based on a collaboration</u> arXiv:1707.07258 [with W. Nakano, Y. Shoji, K. Suzuki @ ICRR]

# Dark Matter Direct Detection Experiment

- ✓ The Earth is immersed in a dark matter halo (*p<sub>DM</sub> ~ 0.3-0.6 GeV/cm<sup>3</sup>*)
- ✓ Dark Matter in such a halo has a velocity dispersion (<v<sub>DM</sub>>~220km/s)
- ✓ The Sun moves at a speed of **220 km/s** around the Galaxy.

(The Earth moves around the Sun with a speed of **30 km/s**)



 Dark matter scatters a nucleus of the detector material and deposits *recoil energy*.

The recoil energy is detected through *ionization*, *scintillation*, and the production of *heat* in the detectors.

# Why Nucleus Scattering ?

✓ Weakly Interacting Massive Particle (WIMP)

Thermal freeze out temperature >> O(1) MeV

 $\rightarrow M_{DM} >> O(10) MeV$ 

✓ Typical Momentum Transfer

 $q = 2 \mu v_{DM} \sin^2 \theta_{CM}/2$   $\mu = m_{target} M_{DM} / (m_{target} + M_{DM})$  $E_R (Lab) = q^2 / 2m_{target}$ 



✓ Nucleus Target ? *m*<sub>target</sub> = *O*(10-100)*GeV* 

 $q < O(100) MeV = E_{recoil} < O(100) keV$ 

✓ Free Electron Target at rest (unrealistic) (*m<sub>e</sub>* << *M<sub>DM</sub>*)

$$\mu \sim m_e \quad q \sim keV \quad E_{recoil} \sim O(1) eV$$

Too low to be detected... (scintillator threshold ~ keV)

Atomic Electron kinetic energy < O(1) keV</li>
 Still low energy deposit...

#### The nuclear recoil is more detectable !

# How is the Nucleus Scattering detected ?

e.g. Liquid Xenon (*LXe*) Detector







Recoiled **Xe** lose its energy via (in)elastic scattering with other **Xe**. Inelastic scattering leads to excitation/ionization of *Xe's*.

The *excited/ionized Xe*'s form excited molecular (excimer).



Excimer eventually decays by emitting a photon with a characteristic wave length (~ 175nm) = scintillation photon ! (Typical Time Scale ~ O(1)ns - O(10)ns)

# scintillation photon  $\propto$  Recoil Energy

Nuclear recoil is detected by looking for

Scintillation photons & emitted electrons @ ionizations

# What is missing in this analysis?

e.g. Liquid Xenon (*LXe*) Detector



In conventional analysis, the *recoiled nucleus* is treated as a *recoiled neutral atom*.

✓ In reality, it takes some "time" for the electrons to catch up...



✓ The process to catch up causes electron excitations/ionizations (of inner elecgtrons) !

→ Migdal Effect ! [1939, Migdal]

['05 Vergados&Ejiri, '07 Bernabei et al. Application to DM detection ]

# Migdal's approach



Just after the nuclear recoil, we assume only the nucleus is moving while the electron cloud is left behind.

(The electron clouds are no more in the energy eigenstates.)



Take the rest frame of the nucleus by the Galilei transformation.

In this frame, the wave function of the electron cloud looks like :

$$\Phi_{ec}^{\prime}\rangle = e^{-im_e\sum_i \mathbf{v}\cdot\hat{\mathbf{x}}_i} |\Phi_{ec}\rangle$$

Electron wave function in the initial state e.g. the ground state.

The probability of the excitation/ionization is given by

$$\mathcal{P} = |\langle \Phi_{ec}^F | \Phi_{ec}' \rangle|^2 = |\langle \Phi_{ec}^F | e^{-im_e \sum_i \mathbf{v} \cdot \hat{\mathbf{x}}_i} | \Phi_{ec}' \rangle|^2$$

# Disadvantage of the Migdal Approach

The nuclear scattering and the electron excitations/ionizations are treated separately.

Energy Momentum Conservation is not clear...

✓ Where does the electron get energy & momentum?

It is not clear whether the electron excitation energy can be larger than the recoil energy or not.

 $\rightarrow$  It is important to reformulate the Migdal effects in a more coherent way !

# Reformulation of the Migdal Effect

Migdal's approach

Initial state of the DM scattering: (DM plane wave) x (Nucleus plane wave)
Final state of the DM scattering: (DM plane wave) x (Nucleus plane wave)
Migdal Effect = Final state effects

### The Migdal Effect is treated separately from the nuclear scattering

New approach

Initial state of the DM scattering : (DM plane wave) x (Atomic plane wave) Final state of the DM scattering : (DM plane wave) x (Atomic plane wave)

The Migdal Effect is automatically taken into account !

How do we construct the plane wave function of the atoms?

✓ Hamiltonian of an *isolated* atomic system (neutral atom)

$$\hat{H}_A \simeq \frac{\hat{\mathbf{p}}_N^2}{2m_N} + \hat{H}_{ec}(\hat{\mathbf{x}}_N) = \frac{\hat{\mathbf{p}}_N^2}{2m_N} + \sum_i^{N_e} \frac{\hat{\mathbf{p}}_i^2}{2m_e} + V(\hat{\mathbf{x}}_i - \hat{\mathbf{x}}_N)$$

✓ Energy eigenstate of the total atomic system (*E<sub>A</sub>* : non-relativistic energy)

$$\left(\frac{\hat{\mathbf{p}}_N^2}{2m_N} + \hat{H}_{ec}(\mathbf{x}_N)\right)\Psi_E(\mathbf{x}_N, \{\mathbf{x}\}) = E_A\Psi_E(\mathbf{x}_N, \{\mathbf{x}\})$$

### ✓ The Born-Oppenheimer approximation of the atom *at rest*.

Electron Cloud Energy Eigenstate for a "fixed"  $x_N$ .

$$\hat{H}_{ec}(\mathbf{x}_N)\Phi_{ec}(\{\mathbf{x}\}|\mathbf{x}_N) = E_{ec}(\mathbf{x}_N)\Phi_{ec}(\{\mathbf{x}\}|\mathbf{x}_N)$$

Electron could system does not depend on where the Nucleus is.

$$E_{ec}(\mathbf{x}_N) = E_{ec} , \qquad \Phi_{E_{ec}}(\{\mathbf{x}\}|\mathbf{x}_N) = \Phi_{E_{ec}}(\{\mathbf{x}-\mathbf{x}_N\})$$

Born-Oppenheimer approximation !

$$\Psi_{E_A}^{(\text{rest})}(\mathbf{x}_N, \{\mathbf{x}\}) \equiv \Phi_{E_{ec}}(\{\mathbf{x} - \mathbf{x}_N\})$$

 $E_A = E_{ec}$ 

✓ Is the Born-Oppenheimer approximation OK ?

$$\begin{pmatrix} \hat{\mathbf{p}}_N^2 \\ 2m_N \end{pmatrix} + \hat{H}_{ec}(\mathbf{x}_N) \Psi_E(\mathbf{x}_N, \{\mathbf{x}\}) = E_A \Psi_E(\mathbf{x}_N, \{\mathbf{x}\})$$

$$\begin{pmatrix} \hat{\mathbf{p}}_N^2 \\ 2m_N \end{pmatrix} \sim \frac{m_e}{m_N} \times E_{ec} \qquad \left( \hat{\mathbf{p}}_N \Phi_{E_c}(\{\mathbf{x} - \mathbf{x}_N\}) = -\sum_i \hat{\mathbf{p}}_i \Phi_{E_c}(\{\mathbf{x} - \mathbf{x}_N\}) \right)$$

Kinetic energy of the nucleus is negligible!

 Total Energy Eigenstate in the Born-Oppenheimer approximation of the total Atom at rest

$$\hat{H}_A \Psi_{E_A}^{(\text{rest})}(\mathbf{x}_N, \{\mathbf{x}\}) \simeq E_{ec} \Psi_{E_A}^{(\text{rest})}(\mathbf{x}_N, \{\mathbf{x}\}) .$$
$$\Psi_{E_A}^{(\text{rest})}(\mathbf{x}_N, \{\mathbf{x}\}) \equiv \Phi_{E_{ec}}(\{\mathbf{x} - \mathbf{x}_N\})$$

The EC wave function can be obtained by e.g. Hartree-Fock approximation !

The electrons are not necessarily bounded by the nucleus coulomb force !

$$\Psi_{E_A}^{(\text{rest})}(\mathbf{x}_N, \{\mathbf{x}\}) \equiv \Phi_{E_{ec}}(\{\mathbf{x} - \mathbf{x}_N\})$$



All the electrons are bounded by the Coulomb force of the nucleus.



Not all the electrons are bounded by the Coulomb force of the nucleus = lonized atom

#### ONCE WE OBTAIN ELECTRON CLOUD WAVE FUNCTION OF THE NUCLEUS AT REST, WE OBTAIN ANY WAVE FUNCTIONS OF THE ATOMIC SYSTEM !

✓ The energy eigenstate of the moving atom with a velocity v.

$$\Psi_{E_A}(\mathbf{x}_N, \{\mathbf{x}\}) \simeq e^{i\mathbf{p}_N \cdot \mathbf{x}_N} e^{i\sum_{i=1}^{N_e} \mathbf{q}_e \cdot \mathbf{x}_i} \Psi_{E_A}^{(\text{rest})}(\mathbf{x}_N, \{\mathbf{x}\})$$

$$\underline{\mathbf{p}_N = m_N \mathbf{v}}_{E_A} \qquad \underline{\mathbf{q}_e = m_e \mathbf{v}}_{Atom wave function}$$

$$E_A \simeq E_{ec} + \frac{1}{2}\overline{m}_A v^2 \qquad \overline{m}_A = m_N + N_e m_e$$

$$Atom wave function at rest$$

(Galilei Transformation of the Rest Frame Solution)

 $\Psi_{EA}$  is the eigenstate of the energy and the total atomic momentum !

$$\left(\hat{\mathbf{p}}_N + \sum_i^{N_e} \hat{\mathbf{p}}_i\right) \Psi_{E_A}(\mathbf{x}_N, \{\mathbf{x}\}) = (\overline{m}_A \mathbf{v}) \times \Psi_{E_A}(\mathbf{x}_N, \{\mathbf{x}\})$$

 $\Psi_{EA}$  describes the place wave of the atom! ( $\partial_{xN}\psi_{EA}^{(rest)} = -\Sigma \partial_{xi}\psi_{EA}^{(rest)}$ )

( $\Psi_{EA}$  is not the eigenstates of the momentums of the nucleus and the electrons separately !)

✓ DM-Nuclear Scattering without scattering in a field theoretical treatment.

Contact interaction : 
$$\mathcal{L} = \frac{1}{M_*^2} \overline{\psi}_{p,n} \psi_{p,n} \overline{\psi}_{DM} \psi_{DM}$$
  
Invariant amplitude<sup>2</sup>: 
$$|\mathcal{M}|^2 = 16 \frac{m_N^2 m_{DM}^2}{M_*^4} A^2$$
  
Cross section: 
$$\bar{\sigma}_N \simeq \frac{1}{16\pi} \frac{|\mathcal{M}|^2}{(m_N + m_{DM})^2} \simeq \frac{1}{\pi} \frac{\mu_N^2}{M_*^4} A^2$$

✓ Nuclear Scattering is reproduced by the point-like interaction potential in QM.

$$\hat{H} = \hat{H}_0 + \hat{V}_{\text{int}} ,$$

$$\hat{H}_0 = \frac{\hat{\mathbf{p}}_N^2}{2m_N} + \frac{\hat{\mathbf{p}}_{DM}^2}{2m_{DM}} + \hat{V}_{\text{int}} ,$$

$$\hat{V}_{\text{int}} = \frac{-\mathcal{M}}{4m_N m_{DM}} \delta^3(\mathbf{x}_N - \mathbf{x}_{DM})$$

Wave Function : [Nuclear Plane Wave] x [DM Plane Wave]

$$\psi_I(\mathbf{x}_N, \mathbf{x}_{DM}) = \sqrt{2m_N} e^{i\mathbf{p}_N^I \cdot \mathbf{x}_N} \times \sqrt{2m_{DM}} e^{i\mathbf{p}_{DM}^I \cdot \mathbf{x}_{DM}}$$
$$\psi_F(\mathbf{x}_N, \mathbf{x}_{DM}) = \sqrt{2m_N} e^{i\mathbf{p}_N^F \cdot \mathbf{x}_N} \times \sqrt{2m_{DM}} e^{i\mathbf{p}_{DM}^F \cdot \mathbf{x}_{DM}}$$

✓ DM-Nuclear Scattering without scattering in a field theoretical treatment.

Contact interaction : 
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Invariant amplitude<sup>2</sup>: 
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✓ Nuclear Scattering is reproduced by the point-like interaction potential.

$$\hat{H} = \hat{H}_0 + \hat{V}_{\text{int}} ,$$

$$\hat{H}_0 = \frac{\hat{\mathbf{p}}_N^2}{2m_N} + \frac{\hat{\mathbf{p}}_{DM}^2}{2m_{DM}} + \hat{V}_{\text{int}} ,$$

$$\hat{V}_{\text{int}} = \frac{-\mathcal{M}}{4m_N m_{DM}} \delta^3(\mathbf{x}_N - \mathbf{x}_{DM})$$

Born Approximation

$$\rightarrow \quad T_{FI} = \mathcal{M} \times i(2\pi)^4 \delta(E_N^F + E_{DM}^F - E_N^I - E_{DM}^I) \delta^3(\mathbf{p}_N^F + \mathbf{p}_{DM}^F - \mathbf{p}_N^I - \mathbf{p}_{DM}^I)$$

(with the asymptotic Nucleus plane waves)

✓ Atomic Scattering via the contact DM-nuclear interaction term :

$$\hat{H}_{\text{tot}} = \hat{H}_A + \frac{\hat{\mathbf{p}}_{DM}^2}{2m_{DM}} + \hat{V}_{\text{int}}$$
$$\hat{V}_{\text{int}} = \frac{-\mathcal{M}}{4m_N m_{DM}} \delta^3(\mathbf{x}_N - \mathbf{x}_{DM})$$

Initial: 
$$\Psi_{I}(\mathbf{x}_{N}, \{\mathbf{x}\}, \mathbf{x}_{DM}) = \sqrt{2m_{N}}\Psi_{E_{A}^{I}}(\mathbf{x}_{N}, \{\mathbf{x}\}) \times \sqrt{2m_{DM}}e^{i\mathbf{p}_{DM}^{I}\cdot\mathbf{x}_{DM}}$$
  
Final:  $\Psi_{F}(\mathbf{x}_{N}, \{\mathbf{x}\}, \mathbf{x}_{DM}) = \sqrt{2m_{N}}\Psi_{E_{A}^{F}}(\mathbf{x}_{N}, \{\mathbf{x}\}) \times \sqrt{2m_{DM}}e^{i\mathbf{p}_{DM}^{F}\cdot\mathbf{x}_{DM}}$   
(Atomic plane wave)

(The normalization is to conform with  $\langle p' | p \rangle = (2E)^{1/2} (2\pi)^{3/2} \delta^3(p'-p)$ )

✓ We assume that initial sate atom is at rest :  $p_A = 0$ .

Initial: 
$$E_{I} = E_{ec}^{I} + \frac{\mathbf{p}_{DM}^{I-2}}{2m_{DM}}$$
,  
Final:  $E_{F} = E_{ec}^{F} + \frac{\overline{m}_{A}}{2}v_{F}^{2} + \frac{\mathbf{p}_{DM}^{F-2}}{2m_{DM}}$ ,

✓ Atomic Scattering via the contact DM-nuclear interaction term :

$$\hat{H}_{\text{tot}} = \hat{H}_A + \frac{\hat{\mathbf{p}}_{DM}^2}{2m_{DM}} + \hat{V}_{\text{int}}$$
$$\hat{V}_{\text{int}} = \frac{-\mathcal{M}}{4m_N m_{DM}} \delta^3(\mathbf{x}_N - \mathbf{x}_{DM})$$

$$T_{FI} = \mathcal{M} \times i(2\pi)\delta(E_F - E_I) \int d^3 \mathbf{x}_N d^3 \mathbf{x}_{DM} \prod_i d^3 \mathbf{x}_i \, \delta^3(\mathbf{x}_N - \mathbf{x}_{DM}) \\ \times \Phi^*_{E_{ec}^F}(\{\mathbf{x} - \mathbf{x}_N\}) e^{-i\sum_i \mathbf{q}_e \cdot \mathbf{x}_i} e^{-i\mathbf{p}_N^F \cdot \mathbf{x}_N} \Phi_{E_{ec}^I}(\{\mathbf{x} - \mathbf{x}_N\}) e^{-i(\mathbf{p}_{DM}^F - \mathbf{p}_{DM}^I) \cdot \mathbf{x}_{DM}} \\ = \mathcal{M} \times i(2\pi)^4 \delta(E_F - E_I) \delta^3(\overline{m}_A \mathbf{v}_F + \mathbf{p}_{DM}^F - \mathbf{p}_{DM}^I) \text{ (correct energy momentum conservation)} \\ \times \int \prod_i d^3 \mathbf{x}_i \, \Phi^*_{E_{ec}^F}(\{\mathbf{x}\}) e^{-i\sum_i \mathbf{q}_e \cdot \mathbf{x}_i} \Phi_{E_{ec}^I}(\{\mathbf{x}\}) \ .$$

#### Migdal factor !

By taking the asymptotic states consist of the atomic plane waves, the Migdal factor appears automatically. The total energy momentum conservation is manifest !

After phase space integration (center of mass frame):

$$\frac{d\sigma}{d\cos\theta_{CM}} \simeq \sum_{E_{ec}^{F}} \frac{1}{32\pi} \frac{|\mathbf{p}_{F}|}{(p_{A}^{I\,0} + p_{DM}^{I\,0})^{2}|\mathbf{p}_{I}|} |F_{A}(q_{A}^{2})|^{2} |\mathcal{M}(q_{A}^{2})|^{2} |Z_{FI}(q_{e})|^{2} .$$
$$Z_{FI}(\mathbf{q}_{e}) = \int \prod_{i} d^{3}\mathbf{x}_{i} \Phi_{E_{ec}^{F}}^{*}(\{\mathbf{x}\}) e^{-i\sum_{i}\mathbf{q}_{e}\cdot\mathbf{x}_{i}} \Phi_{E_{ec}^{I}}(\{\mathbf{x}\})$$
$$\mathbf{p}_{DM}^{I} = -\mathbf{p}_{A}^{I} = \mathbf{p}_{I} \simeq \mu_{N} \mathbf{v}_{DM}^{I} \qquad (\mathbf{p}_{A}^{I\,0} = \mathbf{m}_{A}, \mathbf{p}_{DM}^{I\,0} = \mathbf{m}_{DM})$$

In addition to the total momenta of the initial/final states, we need to specify the states of the electron clouds in the initial/finial states.

#### ✓ Initial state : DM = plane wave, atom = at rest, EC = Ground State

✓ Final state : DM = plane wave, atom = moving, EC = Ground/Excited/Ionized State

After phase space integration (center of mass frame):

$$\frac{d\sigma}{d\cos\theta_{CM}} \simeq \sum_{E_{ec}^F} \frac{1}{32\pi} \frac{|\mathbf{p}_F|}{(p_A^{I\,0} + p_{DM}^{I\,0})^2 |\mathbf{p}_I|} |F_A(q_A^2)|^2 |\mathcal{M}(q_A^2)|^2 |Z_{FI}(q_e)|^2 .$$
$$Z_{FI}(\mathbf{q}_e) = \int \prod_i d^3 \mathbf{x}_i \, \Phi_{E_{ec}^F}^*(\{\mathbf{x}\}) e^{-i\sum_i \mathbf{q}_e \cdot \mathbf{x}_i} \Phi_{E_{ec}^I}(\{\mathbf{x}\})$$
$$\mathbf{p}_{DM}^I = -\mathbf{p}_A^I = \mathbf{p}_I \simeq \mu_N \mathbf{v}_{DM}^I \quad (\mathbf{p}_A^{I\,0} = \mathbf{m}_{Ac}, \mathbf{p}_{DM}^{I,0} = \mathbf{m}_{DM})$$

The process is not elastic for  $E_{ec}^F \neq E_{ec}^I$ !

In CM: 
$$|\mathbf{p}_F|^2 \simeq |\mathbf{p}_I|^2 - 2\mu_N (E_{ec}^F - E_{ec}^I) \qquad v_{DM}^{(th)} = \sqrt{\frac{2(E_{ec}^F - E_{ec}^I)}{\mu_N}}$$



$$q_{e} = m_{e}\mathbf{v} = m_{e}/m_{A}\mathbf{q} \sim \mu_{A}m_{e}/m_{A}v_{DM}$$

$$Z_{FI}(\mathbf{q}_{e}) = \int \prod_{i} d^{3}\mathbf{x}_{i} \Phi_{E_{e}^{F}}^{*}({\mathbf{x}})e^{-i\sum_{i}\mathbf{q}_{e}\cdot\mathbf{x}_{i}}\Phi_{E_{e}^{I}}({\mathbf{x}})$$

$$\sum_{F} |Z_{FI}|^{2} = |Z_{II}|^{2} + \sum_{n,\ell,n',\ell'} p_{q_{e}}^{d}(n\ell \rightarrow n'\ell') + \sum_{n,\ell} \int \frac{dE_{e}}{2\pi} \frac{d}{dE_{e}} p_{q_{e}}^{c}(n\ell \rightarrow E_{e})$$
elastic excitation ionization
$$DM \quad DM \quad DM \quad DM \quad DM$$
elastic (excitation ionization)
$$M \quad DM \quad DM \quad DM \quad DM \quad DM \quad M$$

$$\mathbf{xe} \quad \mathbf{xe} \quad \mathbf{xe} \quad \mathbf{xe} + electron$$

# Numerical Transition Rate (by using Flexible Atomic Code)

Hartree-Fock Approximation. Leading  $O(q_e^2)$  approximation.



(transition is possible only for  $|\Delta \ell| = 1$ )

- The ionization rate from n = 3 state can be of  $O(10^{-(3-2)})$ .
  - $\rightarrow$  leading to **O(1)keV** electronic energy deposition !

The rates for the excitation to the higher shells are smaller.

# Numerical Transition Rate (by using Flexible Atomic Code)

Hartree-Fock Approximation. Leading  $O(q_e^2)$  approximation.



(transition is possible only for  $|\Delta \ell| = 1$ )

 $E_e$  spectrum is purely determined by the structure of the electron cloud !  $E_e$  spectrum is independent of the dark matter velocity  $v_{DM}$  and  $m_{DM}$ .

# Differential Event Rate for an Isolated Atom

$$\frac{dR}{dE_R dE_e dv_{DM}} \simeq \frac{dR_0}{dE_R dv_{DM}} \times \frac{1}{2\pi} \sum_{n,\ell} \frac{d}{dE_e} p_{q_e}^c (n\ell \to E_e) ,$$
$$\frac{dR_0}{dE_R dv_{DM}} \simeq \frac{1}{2} \frac{\rho_{DM}}{m_{DM}} \frac{1}{\mu_N^2} |F_A(q_A^2)|^2 \bar{\sigma}_N \times \frac{\tilde{f}(v_{DM})}{v_{DM}} ,$$

(*E<sub>e</sub>* : free electron kinetic energy)

#### *Ionization = free electron + ion with a core hole*

✓ When the core-hole (the vacancy in the inner shell) is created by ionization, the states are de-excited immediately *O(10)fs*.



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The electron energy and the de-excitation energy are measured simultaneously.

$$E_{EM} = E_e + E_{\text{dex}}$$
$$\simeq \Delta E$$

#### Differential Event Rate with respect to the measurable electric energy

$$\frac{dR}{dE_R \, dE_{EM} \, dv_{DM}} \simeq \frac{dR_0}{dE_R \, dv_{DM}} \times \frac{1}{2\pi} \sum_{n,\ell} \frac{d}{dE_e} p_{q_e}^c (n\ell \to (E_{EM} - E_{dex}))$$

# Differential Event Rate for an Isolated Atom

#### $m_{DM} = 1 TeV, \sigma_N = 10^{-45} cm^2$



#### $dR/dE_R d\Delta E [ 1/kg/day/keV/keV ] \Delta E > E_{ion}$

Ionization rate from an outer orbit is higher !

### Differential Event Rate for an Isolated Atom

 $m_{DM} = 2GeV, \sigma_N = 10^{-40}cm^2$ 



 $dR/dE_R d\Delta E [ 1/kg/day/keV/keV ] \Delta E > E_{ion}$ 

**Typical**  $\Delta E$  is independent of the DM mass  $E_{R, MAX}$  is suppressed for a smaller DM

In the detector, the atoms are not isolated .

e.g.) Typical separation in the liquid Xe ground state ~ 2 x 10-8 cm

The wave function of the valence (the outermost) electrons are affected by the electrons of the neighboring atoms.



2x10<sup>-8</sup> cm ~ 4 x Bohr radius

#### van der Waals force

#### = deformation of the electron cloud

→ the transition rate from the valence electrons for the isolated atom is not reliable

✓ Ionization energies are slightly reduced by about O(1)eV

→ the transition rates from the valence electrons for the isolated atom are not reliable



potential of the valence quark

### **Electron Orbits**

The number of electrons in a shell for the ground state configurations.



We cannot use our results based on the isolated atoms for the valence electrons.

For the inner electrons, the effects from the environments are not significant.

#### Migdal Effect single-phase Liquid Xe detectors



A few events with  $E_{det} = O(1)$ keV are expected for  $10^5$  kg days !

The atom recoil energy is lower than threshold  $E_R < M_{DM^2} / M_A \propto v_{DM^2} < O(1) keV$ 

#### Migdal Effect single-phase Liquid Xe detectors



A few hundred events with  $E_{det} = O(1) keV$  are expected for  $10^5 kg$  days !

The atom recoil energy is much lower than threshold  $E_R < M_{DM^2} / M_A \times v_{DM^2} = O(1)eV$ 



#### Migdal Effect single-phase Liquid Xe detectors

For heavier dark matter, the atom recoil energy is much lower than threshold  $E_R < M_{A^2} \times v_{DM^2} = O(10-100) \text{keV}$ 

The Migdal effect is submerged below the conventional nuclear recoil spectrum.

# LUX result (1811.11241 LUX collaboration)



#### Double Phase Experiment (detect scintillation photon and ionized electrons)

LUX collaboration analyzed data by taking into account of the Migdal effects.

The result shows that the LXe can test the low mass dark matter region !

10-1

 $10^{-2}$ 

 $10^{-3}$ 

 $10^{-4}$ 

# EDELWEISS result (1901.03588 EDELWEISS Collaboration)

#### EDELWEISS = Ge bolometer experiment : signal = deposited energy & ionization



Color solid line : raw prediction Color points : prediction after cut

The electron signal in the Migdal effects leads to a higher energy signal for a given size of the momentum transfer !

Again, the Migdal effects allow a search for a lighter WIMP !

### EDELWEISS result (1901.03588 EDELWEISS Collaboration)





The EDELWEISS extended their reach to the *sub-GeV* dark matter !



- In the conventional analysis of dark matter direct detection experiments through the nuclear scattering, the whole atom is assumed to be recoiled.
- ✓ In reality, the electrons take some time to catch up with the recoiled nucleus leading to electronic energy injection in addition to the atomic recoil → Migdal Effect
- ✓ We reformulated the Migdal effect, where we can manifestly see the energymomentum conservation and the probability conservation.
- ✓ The emitted electronic energy can be in the *keV* range even for a rather light dark matter (*M<sub>DM</sub>* < 10GeV) where the atomic recoil energy is lower than energy threshold, i.e. *O*(1)*keV*.
- ✓ Migdal Effects has advantageous to look for small "q" with a large cross section dark matter → Lower Mass dark matter such as SIDM/Asymmeteric Dark matter
- Can we use emulsion experiment to test the Migdal effects themselves ???