

Dark matter in split supersymmetry: thermal wino dark matter and beyond

Ayuki Kamada (IBS-CTPU)



Based on

[AK, Toyokazu Sekiguchi, and Tomo Takahashi, arXiv:1901.09992](#)

Masahiro Ibe, [AK, Shin Kobayashi, and Wakutaka Nakano, JHEP, 2018](#)

Masahiro Ibe, [AK, Shin Kobayashi, Takumi Kuwahara, and Wakutaka Nakano, JHEP, 2019](#)

June 3, 2019 @ JHU workshop

Hai-bo cannot make it...

Composite asymmetric dark matter and galactic rotation curves

Ayuki Kamada (IBS-CTPU)



Based on

AK, Manoj Kaplinghat, Andrew B. Pace, and Hai-bo Yu, PRL, 2017

Masahiro Ibe, AK, Shin Kobayashi, and Wakutaka Nakano, JHEP, 2018

Masahiro Ibe, AK, Shin Kobayashi, Takumi Kuwahara, and Wakutaka Nakano, JHEP, 2019

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Dark matter

Accumulated evidences from observations of the Universe

Known properties

- long-lived over the age of the Universe
- accounting for about 30% of the present energy density of the Universe $\Omega_{\text{dm}} h^2 \simeq 5\Omega_{\text{baryon}} h^2 \simeq 0.12$
- feebly-interacting with photon and baryon
- not too hot to smear out primordial density contrast

No SM particle satisfies the properties

→ long-standing mystery in cosmology and particle physics

WIMP Miracle

Weakly interacting massive particle: WIMP

Stability: new \mathbb{Z}_2 symmetry e.g., matter parity: $U(1)_{B-L} \rightarrow (-1)^{3(B-L)}$

Abundance: annihilation $\chi\chi \rightarrow AA$ χ : WIMP A : SM

- thermal freeze-out: **electoweak-scale** interaction
- indirect detection (cosmic ray) experiments

Interaction with SM particles: (sub-) weak scale

- direct detection (nuclei recoil) experiments

Non-relativistic: cold dark matter

Related with **electoweak-scale** new physics that explains the origin of the weak scale against Planck scale (hierarchy problem)

- collider experiments

Supersymmetry

Theory is invariant under boson \leftrightarrow fermion

Theoretical properties

- non-trivially extend space-time (Poincaré) symmetry
- control quantum corrections through chiral symmetry

Phenomenological (MSSM) properties

- SUSY breaking \rightarrow Higgs potential
 - electroweak-scale SUSY \rightarrow hierarchy problem
- provide a dark matter candidate R -parity = $(-1)^{3(B-L)+2s}$
- precise grand unification of gauge couplings

No naturalness...

LHC discovery of 125 GeV Higgs and null-detection of top partners

- something wrong in the hierarchy problem and postulated solutions (including but not only electroweak-scale SUSY)

WIMP is no more as a miracle as we expected...

- new theoretical reasoning for WIMP?
 - Mini-split SUSY
 - sfermions > 100 TeV; gauginos \sim TeV
 - 125 GeV Higgs
 - dark matter
 - precise grand unification

- observational hints: small-scale issues in structure formation?

What I will discuss

What about others? What if WIMPs are subdominant?

Puzzles for WIMPs in structure formation

part 1

- diversity of rotation curves
- self-interacting dark matter $\sigma/m = \mathcal{O}(1) \text{ cm}^2/\text{g} = \mathcal{O}(1) \text{ barn/GeV}$

Composite asymmetric dark matter

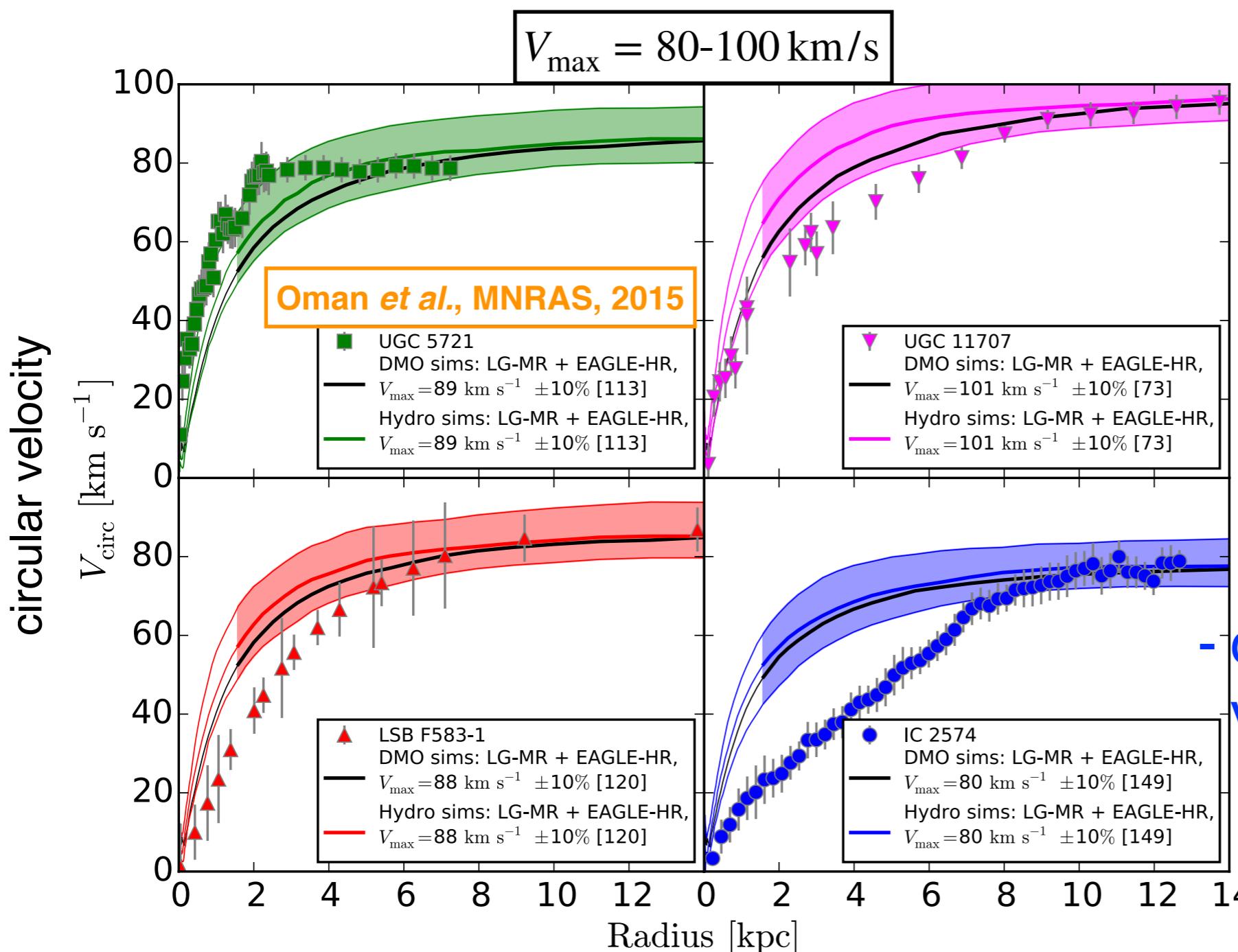
part 2

- naturally realize self-interacting dark matter
- simple model → ultraviolet completion

Part 1: Diversity of inner rotation curves

Collisionless dark matter prediction: inner circular velocity is almost uniquely determined by outer circular velocity

↔ observations show diversity



* unique prediction is related with the concentration-mass relation

- overpredict the circular velocity by a factor of ~ 2 (~ 4 in mass)

Possible solutions

The issues may be attributed to incomplete understanding of complex astrophysical processes (subgrid physics)

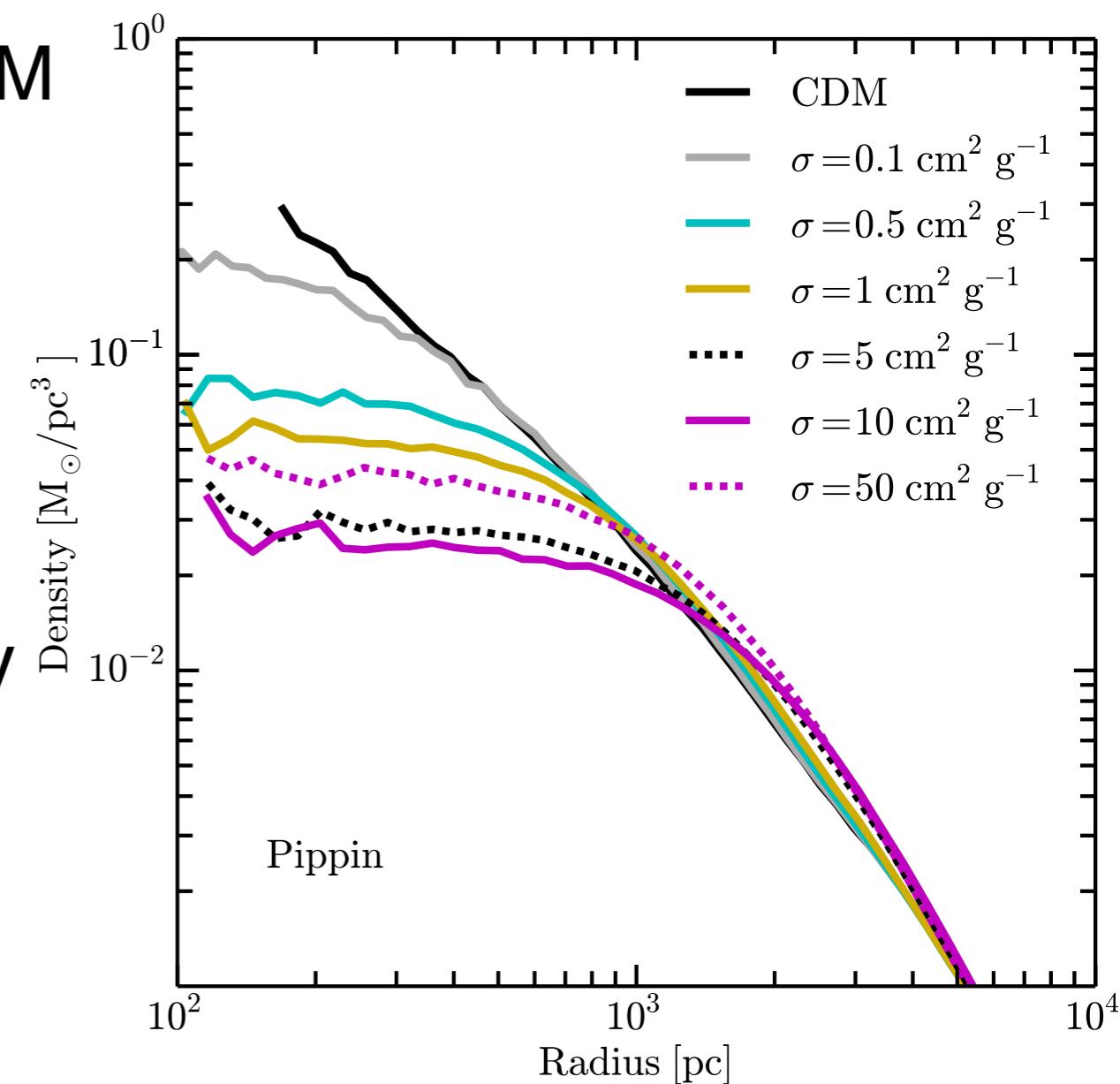
The issues may indicate alternatives to CDM (WIMPs)

- self-interacting dark matter: SIDM

$$\sigma/m = \mathcal{O}(1) \text{ cm}^2/\text{g}$$

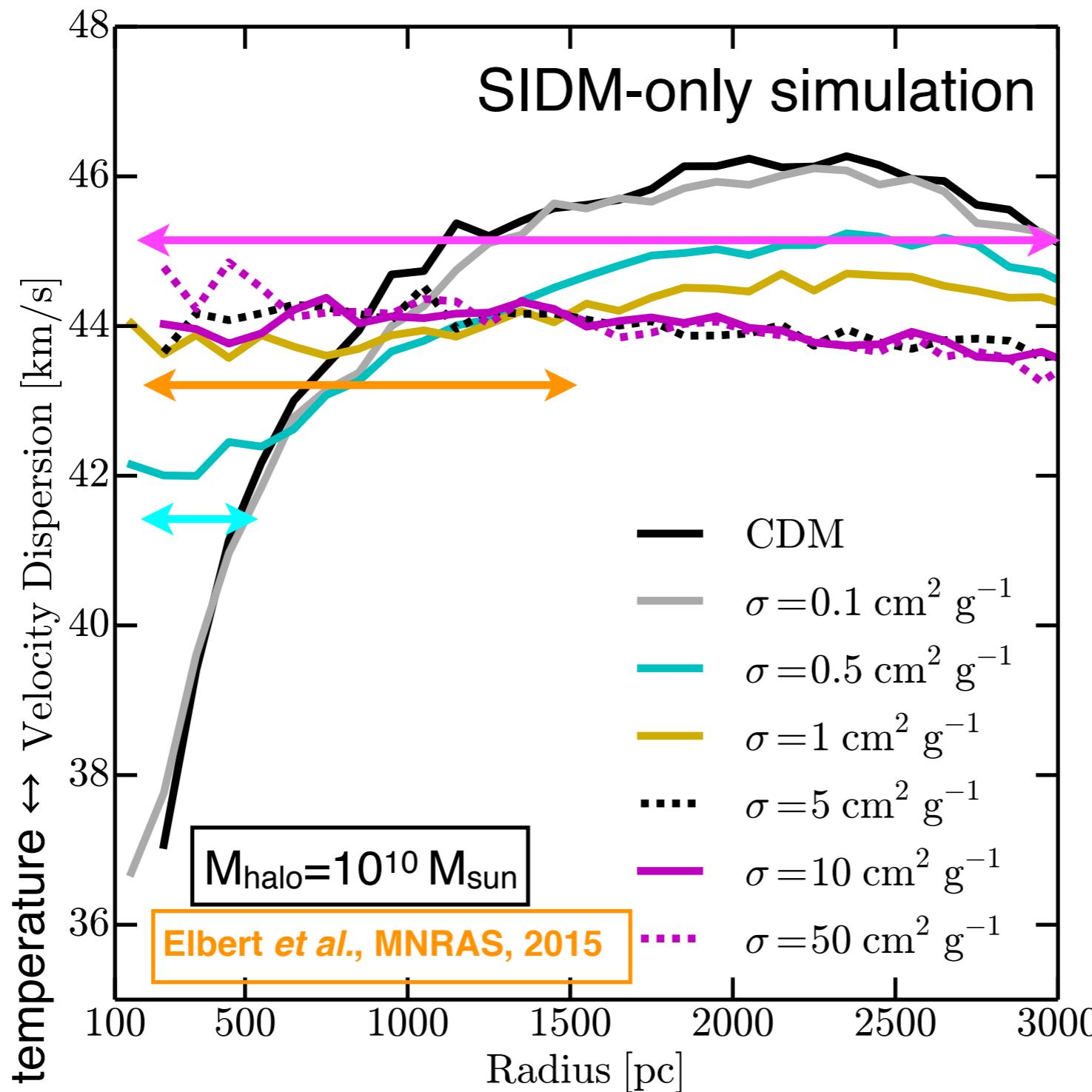
- reduce the central mass density

- ameliorate overprediction in some galaxies, but naively underpredict the circular velocity in other galaxies



Iso-thermal halo

Self-scattering leads to thermalization of DM halos at $r < r_1$
where self-scattering happens at least one time until now



$$\sigma/m \rho(r_1) v(r_1) t_{\text{age}} = 1$$

Key observation

Iso-thermal \rightarrow Boltzmann distribution

$$\rho_{\text{DM}}(\vec{x}) = \rho_{\text{DM}}^0 \exp(-\phi(\vec{x})/\sigma^2)$$

$$\Delta\phi = 4\pi G(\rho_{\text{DM}} + \rho_{\text{baryon}})$$

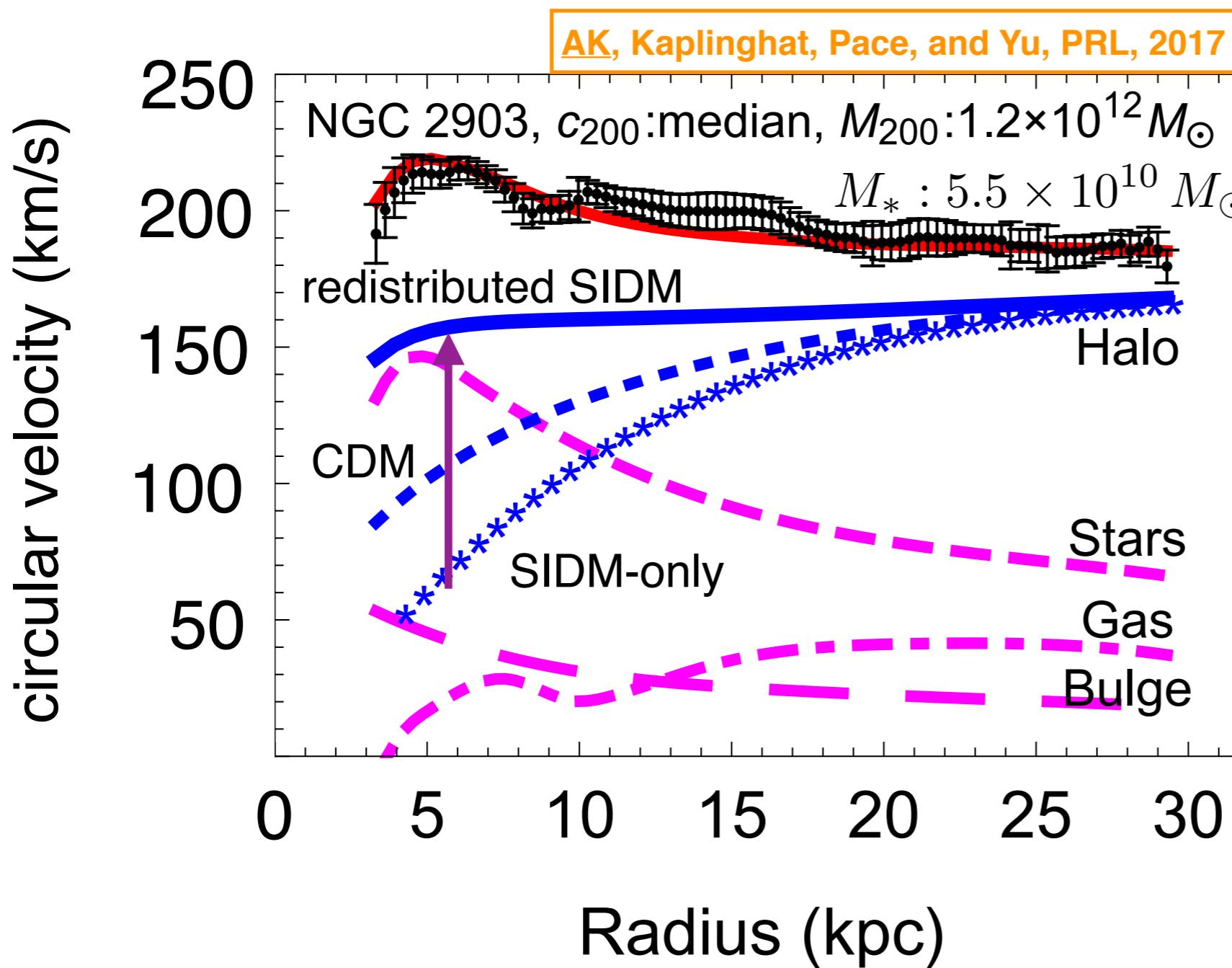
- inner profile is exponentially sensitive to baryon distribution

Baryons form complex objects, which show a large diversity

\rightarrow SIDM particles, redistributed according to formed baryonic objects, can show a diversity

- * do not rely on unconstrained subgrid astrophysical processes
take into account observed baryon distribution

Impacts in observed galaxies

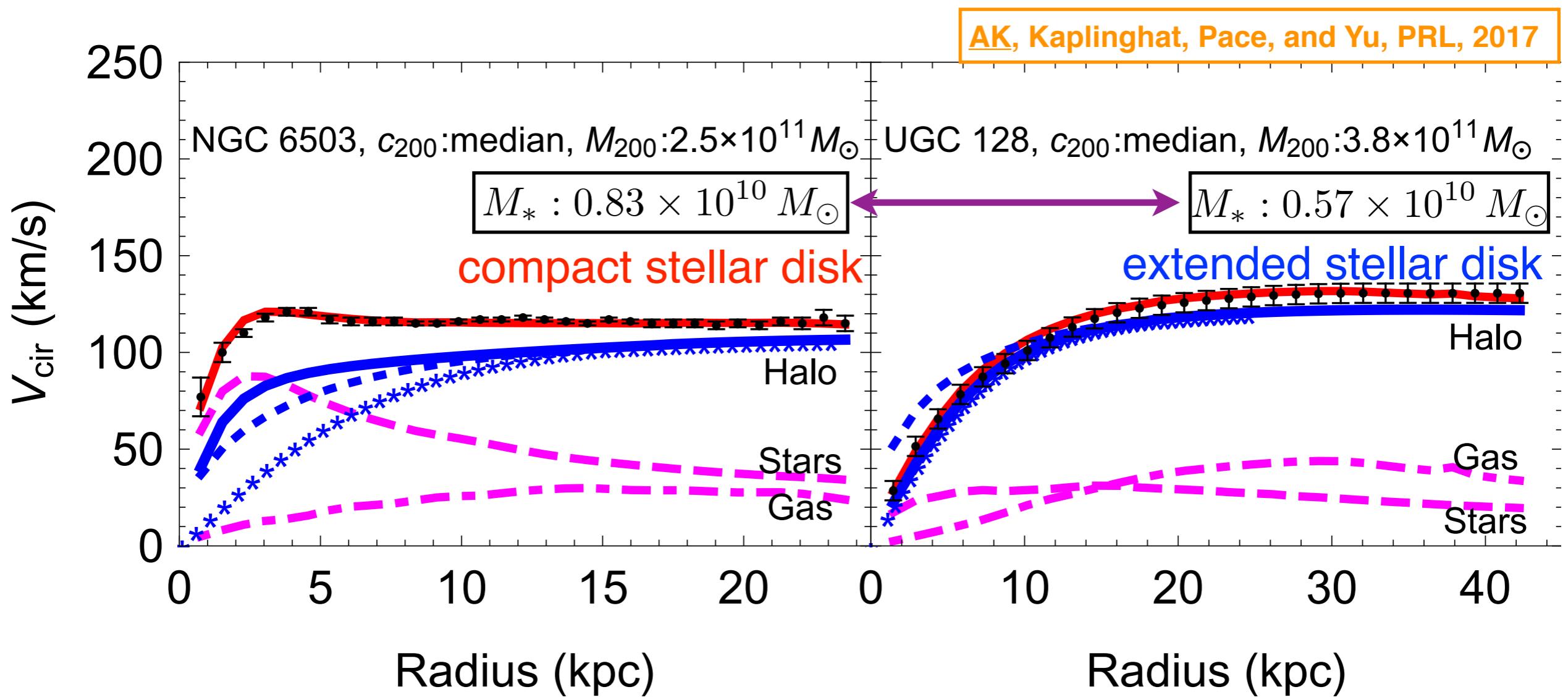


- Observed stellar disk makes SIDM inner circular velocity ~ 3 times higher
- reproducing flat circular velocity at 10-20 kpc

Diversity in stellar distribution

Similar outer circular velocity and stellar mass,
but different stellar distribution

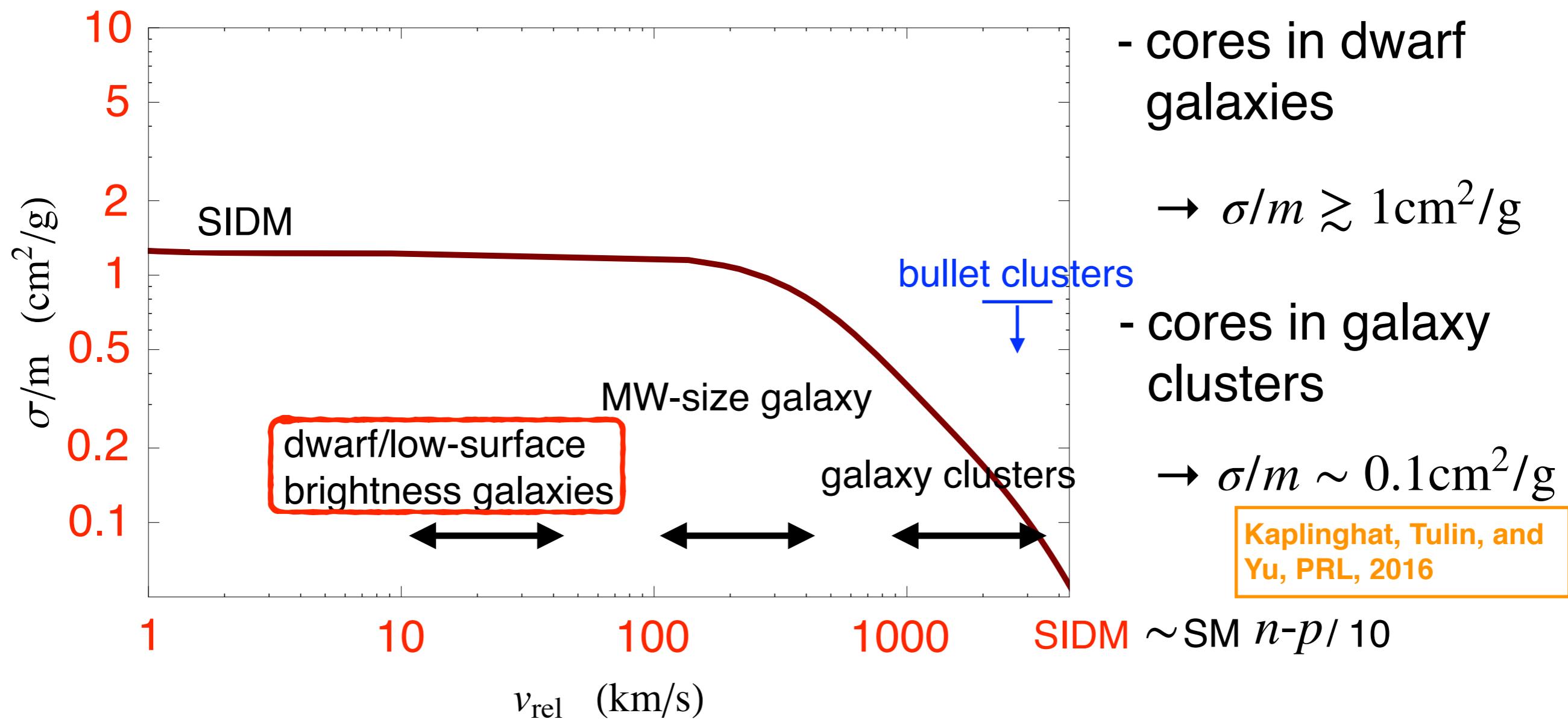
- compact → redistribute SIDM significantly
- extended → unchange SIDM distribution



Self-interacting dark matter

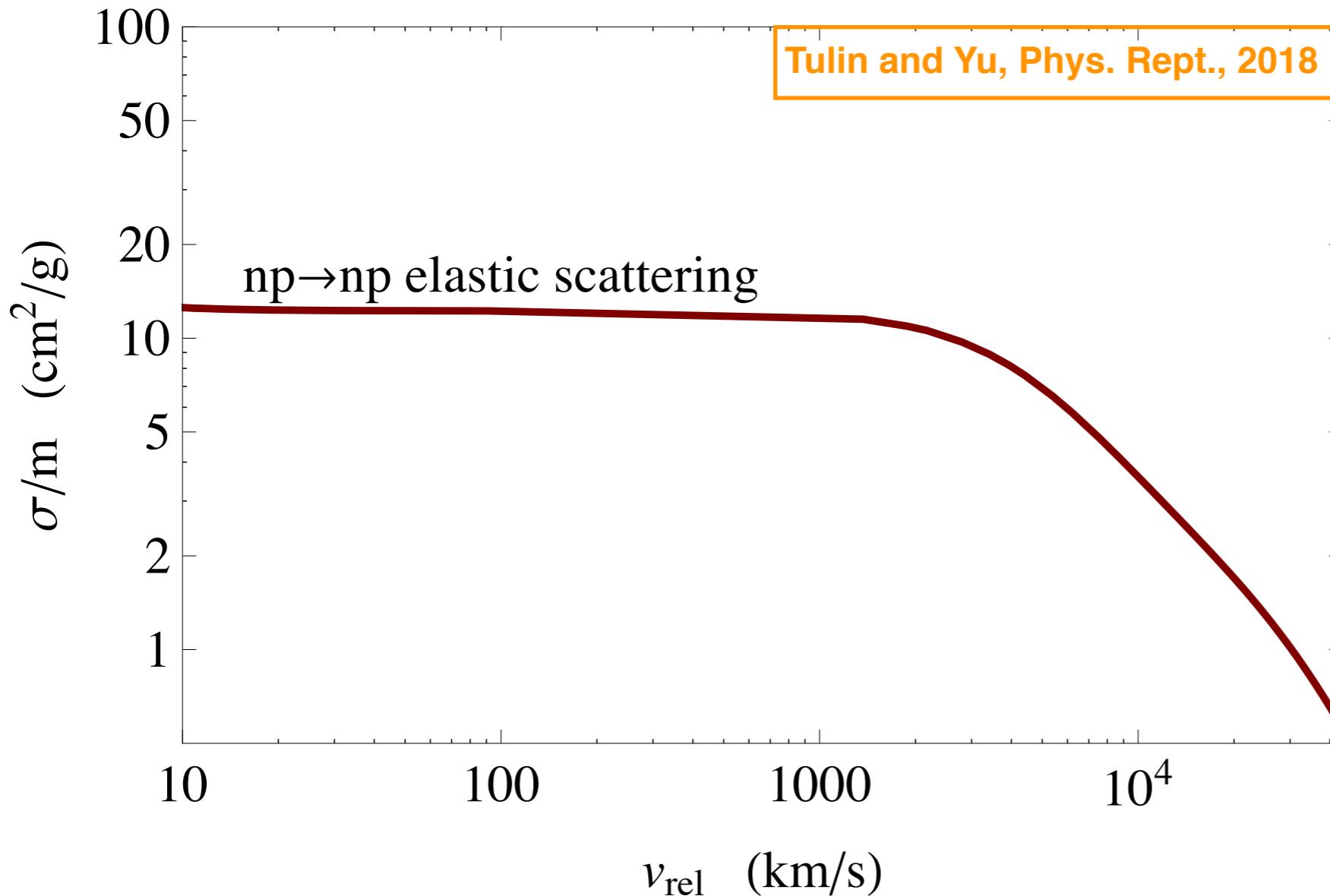
SIDM cross section indicated by small-scale puzzles

SIDM $\sim \text{SM } n-p/10$



Self-interacting dark matter

SM strong dynamics: nucleon elastic-scattering cross section
- diminishing w/ increasing velocity



Part 2: Composite asymmetric dark matter

Why is a dark matter particle long-lived?

- new accidental $U(1)_{B'}$ (like $U(1)_B$ for proton)
- decay operator: non-renormalizable $\Lambda_{\text{QCD}'} / M_* \ll 1$
- B' number asymmetry - cogenesis

Portal operator

$$\mathcal{L}_{\text{portal}} = \frac{1}{M_*^n} \mathcal{O}_{\text{SM}} \mathcal{O}_D : n+4 \text{ dim.} \quad * \text{ when no particle charged under both gauge groups}$$

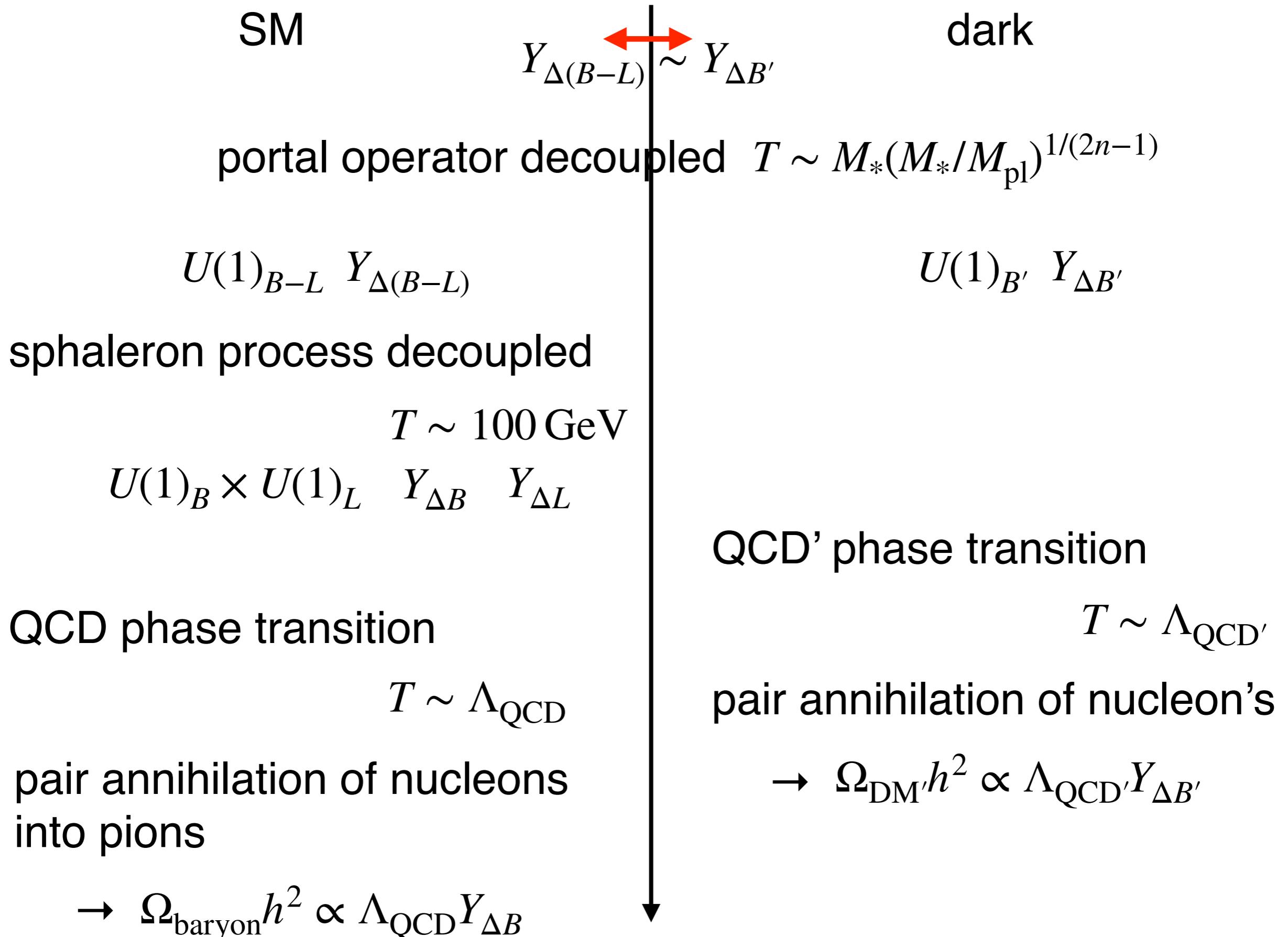
$\mathcal{O}_{\text{SM}(D)}$: SM (D) gauge neutral, but $U(1)_{B-L}$ ($U(1)_{B'}$) charged

→ at high energy (temperature) , $Y_{\Delta(B-L)} \leftrightarrow Y_{\Delta B'}$

$$Y_{\Delta B'} \sim Y_{\Delta B} \quad m_N \sim \Lambda_{\text{QCD}'} = \mathcal{O}(1) \text{ GeV} \rightarrow \Omega_{\text{dm}} h^2 \simeq 5 \Omega_{\text{baryon}} h^2 \simeq 0.12$$

- close to SM QCD dynamical scale

Thermal history



To be answered

Origin of the portal operator?

- high-energy

- if $\frac{1}{M_*^n} \mathcal{O}_{\text{SM}} \mathcal{O}_D$ and $\frac{1}{M_*^n} \mathcal{O}_{\text{SM}} \bar{\mathcal{O}}_D$ coexist, asymmetry is not left

Asymmetry generation?

Fukugita and Yanagida, PLB, 1986

- compatible with, e.g., thermal leptogenesis?

Where is dark sector entropy gone?

- low-energy

- ΔN_{eff} from the dark sector (e.g., dark pions)

Simple model

Ibe, AK, Kobayashi, and Nakano, JHEP 2018

Model setup: QCD×QED-like hidden sector $u' \bar{u}' d' \bar{d}'$
- dark nucleons as DM $p' \sim u' u' d' \bar{d}'$ $n' \sim u' d' d' \bar{d}'$

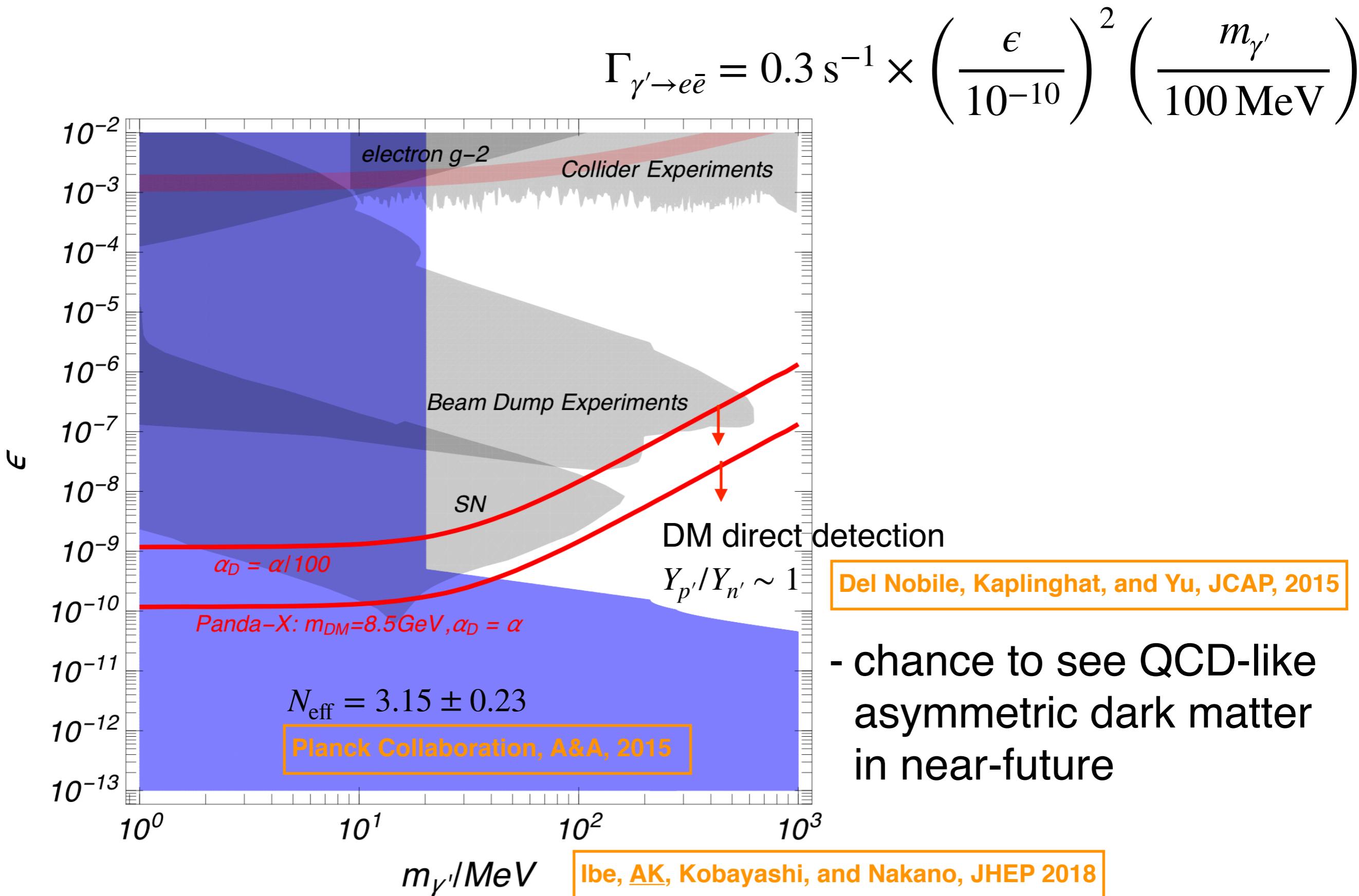
Right-handed neutrinos \bar{N} w/ soft breaking mass M_R
 and scalar down quark H'_C w/ mass $M_{H'_C}$ $U(1)_{B-L+B'} \rightarrow (-1)^{3(B-L+B')}$

- thermal leptogenesis $\rightarrow B - L$ asymmetry
 - see-saw mechanism \rightarrow active neutrino mass
 - only $\frac{y_N}{M_{H_C}^2 M_R} \bar{u}' \bar{d}' \bar{d}' LH$ and $\times \frac{y_N}{M_{H_C}^2 M_R} \bar{u} \bar{d} \bar{d} LH$

Kinetic mixing between SM and dark photons $\frac{\epsilon}{2} F_{\mu\nu} F'^{\mu\nu}$ and $U(1)'$ breaking scalar H^+

- dark photon decay releases dark sector entropy
 - direct detection: SM and dark protons scattering $Y_{p'}/Y_{n'}$?

Dark photon parameter plot



Origin of kinetic mixing

Ibe, AK, Kobayashi, Kuwahara and Nakano, JHEP, 2019

Grand unifications in both SM and dark sectors $SU(5) \times SU(4)'$

* mass splitting

$$m_{d'} < \Lambda_{\text{QCD}'} < m_{e'}$$

: dark nucleon decay

$$M_{H'_C} \gg m_{H^{+'}} : \text{portal operator}$$

- particles we introduce so far except for e' form $SU(4)'$ multiplets

$$\mathbf{6}' : (u', \bar{u}') \quad \mathbf{4}' : (d', \bar{e}') \quad \overline{\mathbf{4}}' : (\bar{d}', e')$$

$\mathbf{4}'_H : (H'_C, H^{+'})$ - $U(1)'$ breaking
- portal operator

Higher dimensional operator

$$\mathcal{L}_{\text{mix}} \sim \frac{1}{M_{\text{pl}}^2} \text{Tr} \left(F_{\text{GUT} \mu\nu} \Sigma_{\text{GUT}} \right) \text{Tr} \left(F_{\text{GUT}'}^{\mu\nu} \Sigma_{\text{GUT}'} \right) \quad \Sigma: \text{adjoint scalar}$$

$$\rightarrow 10^{-10} \left(\frac{\nu_{24}}{10^{16} \text{GeV}} \right) \left(\frac{\nu_{15}}{10^{10} \text{GeV}} \right) F_{\mu\nu} F'^{\mu\nu}$$

$$\sim M_{H_C} > M_R > 10^9 \text{GeV}$$

Mirror grand unification

Dream $SU(5) \times SU(4)' \rightarrow SU(5) \times SU(5)' / \mathbb{Z}_2$

10 : (Q, \bar{u}, \bar{e}) **5** : (\bar{d}, \hat{L})

5_H : (H_C, H_u) **5**_H : (\bar{H}_C, \hat{H}_d)

10' : $(\mathbf{6}'(u', \bar{u}') + \mathbf{4}'(d', \bar{e}'))$

5' : $(\bar{\mathbf{4}}'(\bar{d}', e'), -\nu')$

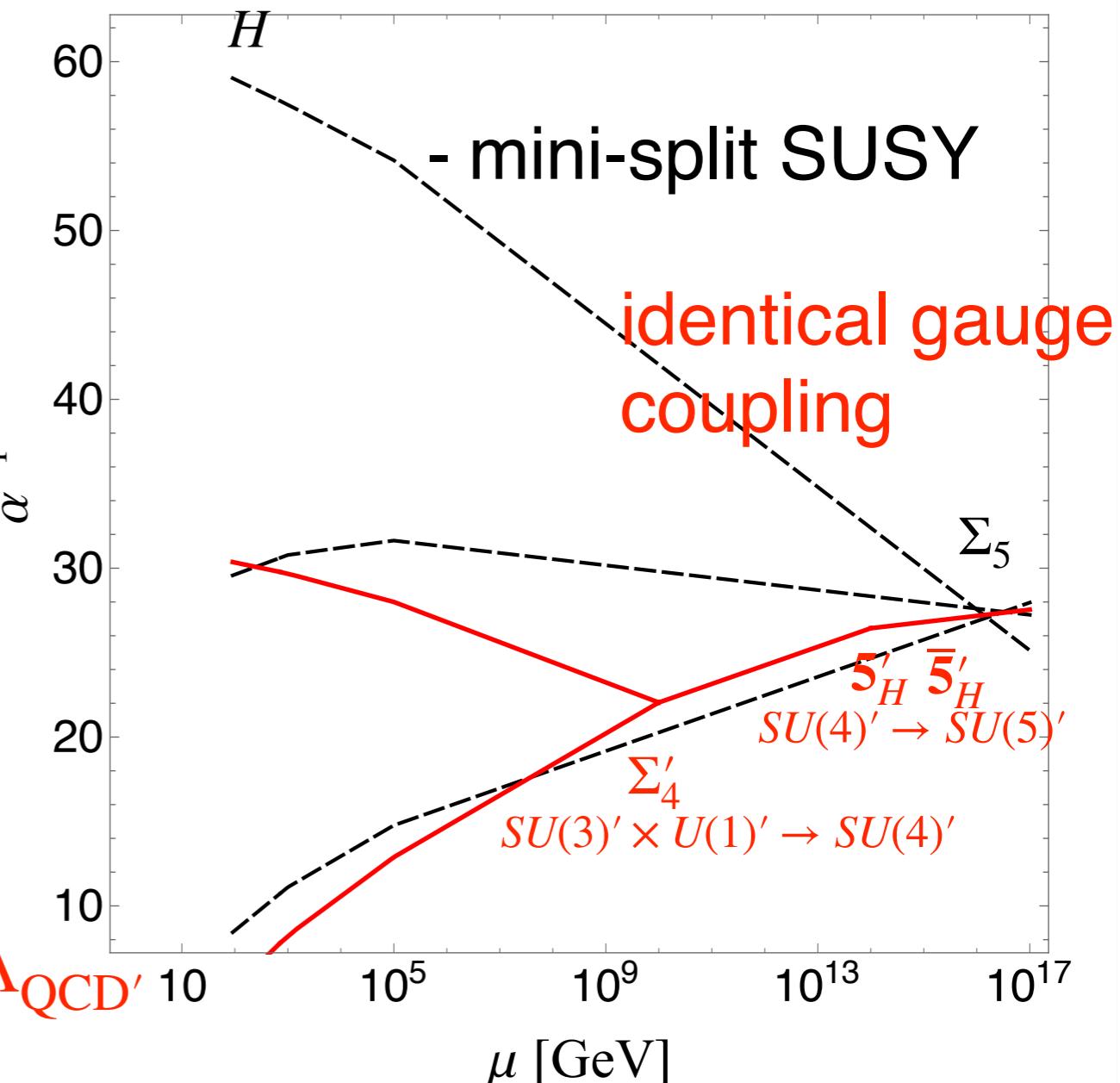
5'_H : $(\mathbf{4}'_H(H'_C, H^{+'}_u), H^{0'}_u)$

5'_H : $(\bar{\mathbf{4}}'_H(\bar{H}'_C, H^{-'}_d), -H^{0'}_d)$

large VEV
→ vector-like theory

Ibe, AK, Kobayashi, Kuwahara
and Nakano, work in progress

- softly broken

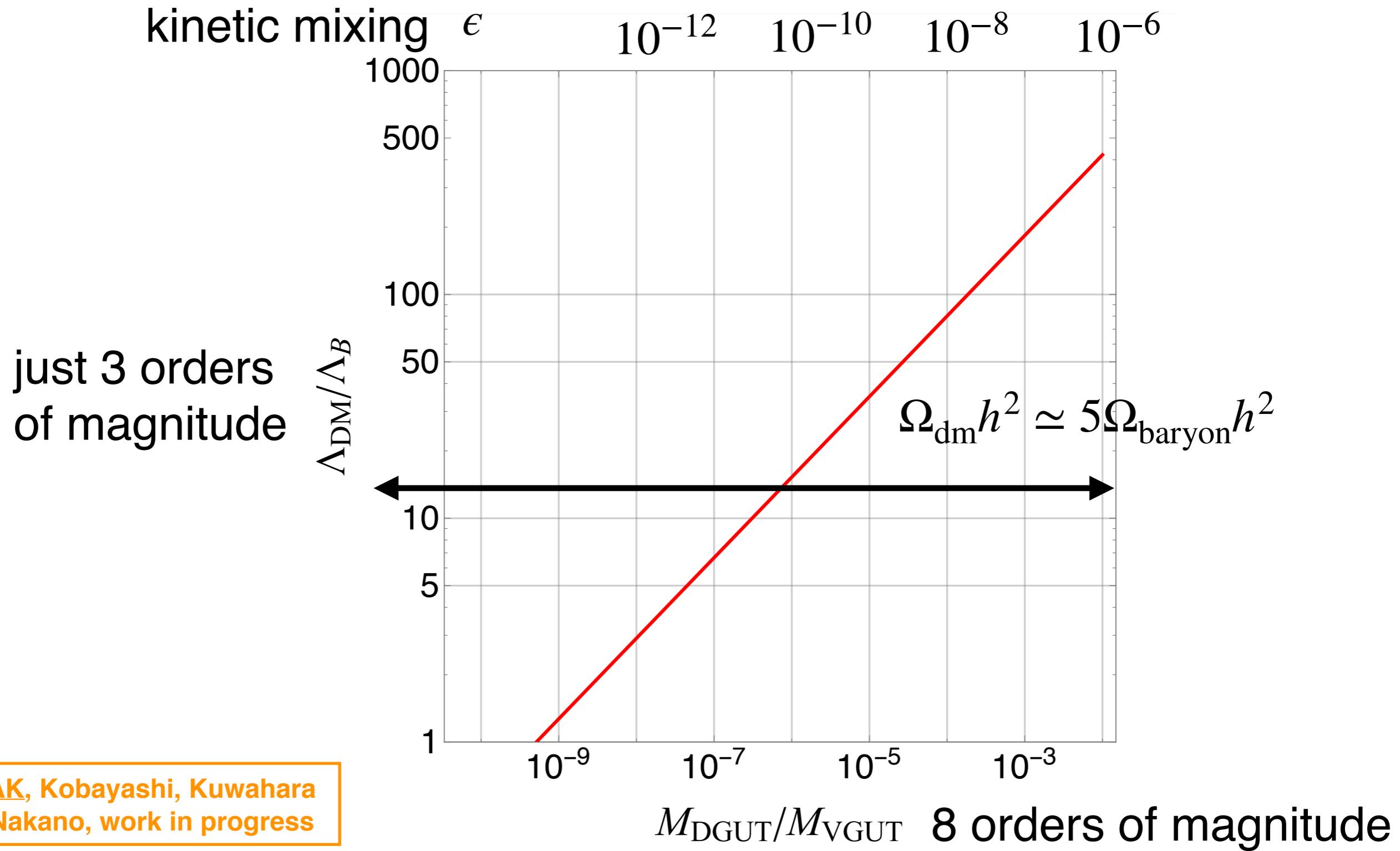


$\Lambda_{\text{QCD}} \sim$

$\Lambda_{\text{QCD}'} \sim$

Alleviating coincidence

Why $\Omega_{\text{dm}}h^2 \sim \Omega_{\text{baryon}}h^2$ or $\Lambda_{\text{QCD}} \sim \Lambda_{\text{QCD}'}?$



Summary

WIMP miracle may have been gone...

- another WIMP miracle related with GUT?
- mini-split SUSY: origin of electroweak symmetry breaking and precise gauge couplings

Small-scale puzzles: diversity of inner rotation curves

- SIDM can explain diversity by changing its distribution according to formed baryon structure (disks)

Velocity-dependent self-scattering cross section is indicated by small-scale puzzles

Asymmetric composite DM is a plausible framework

- DM stability: dark baryon number
- DM relic abundance: co-genesis

Summary

Simple QCD \times QED-like dark sector as a working example

- right-handed neutrino: see-saw mechanisms, thermal leptogenesis, and generating portal operator
- dark photon decay: releasing dark sector entropy
- kinetic mixing: DM direct detection

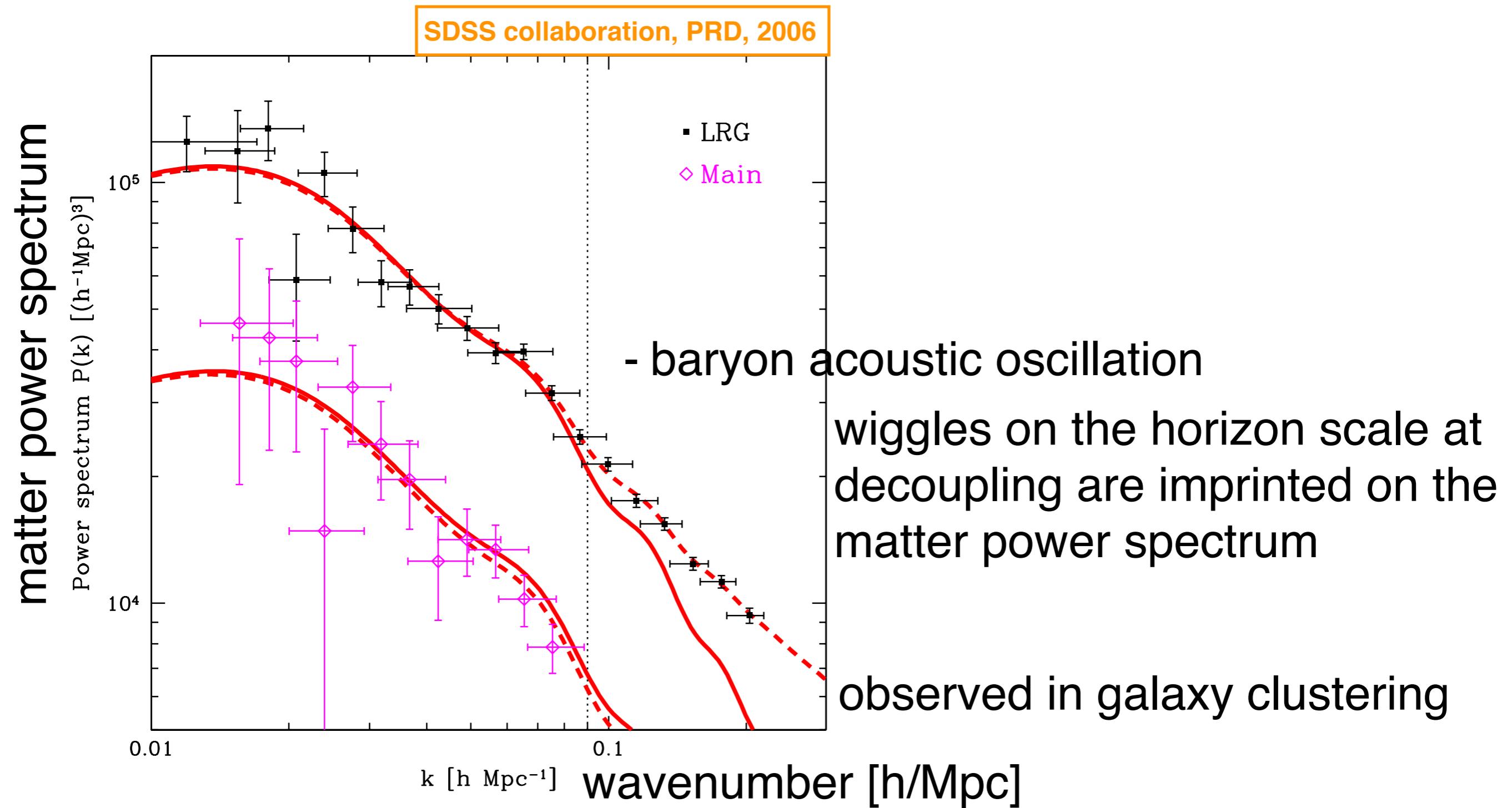
$SU(5) \times SU(4)'$ grand unification

- mini-split SUSY: precise $SU(5)$ grand unification and origins of electroweak and $U(1)'$ breaking
- DM decay into neutrino and dark pion (\rightarrow SM electrons)

$\rightarrow SU(5) \times SU(5)'/\mathbb{Z}_2$ grand unification?

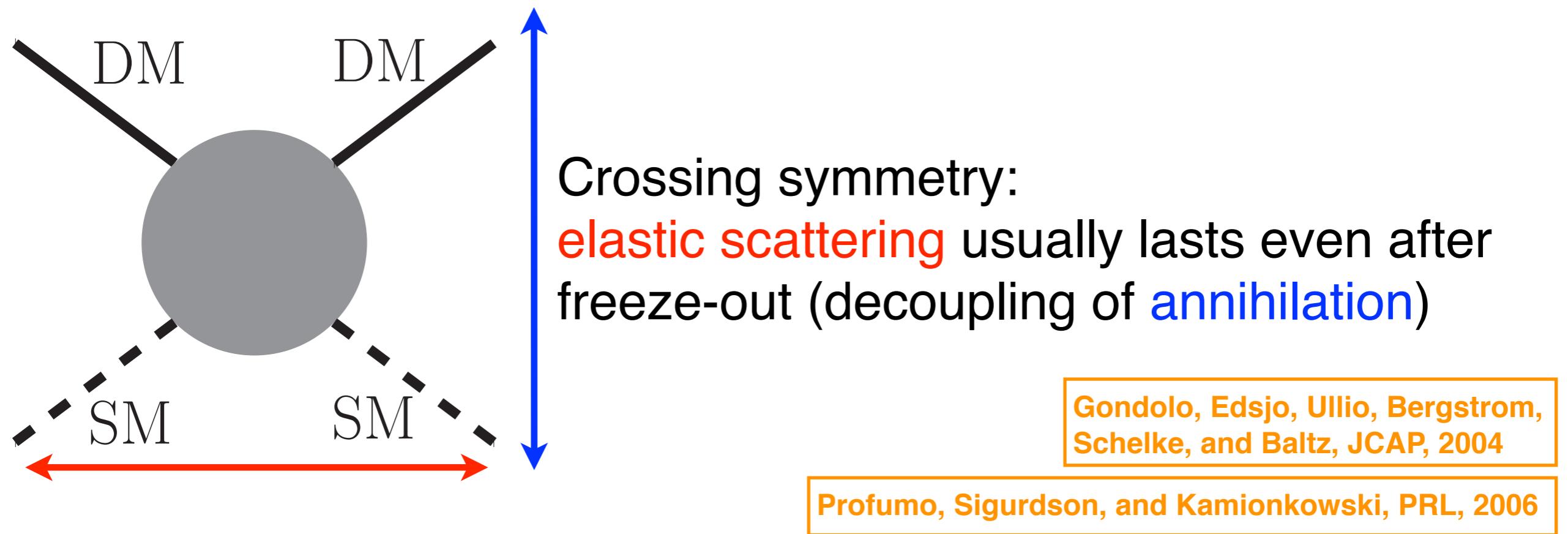
Part X: Baryon acoustic oscillation

Baryons are involved in plasma acoustic oscillation until decoupling (recombination)



Dark acoustic oscillation

WIMPs (weakly interacting massive particles) are in thermal equilibrium in the early Universe



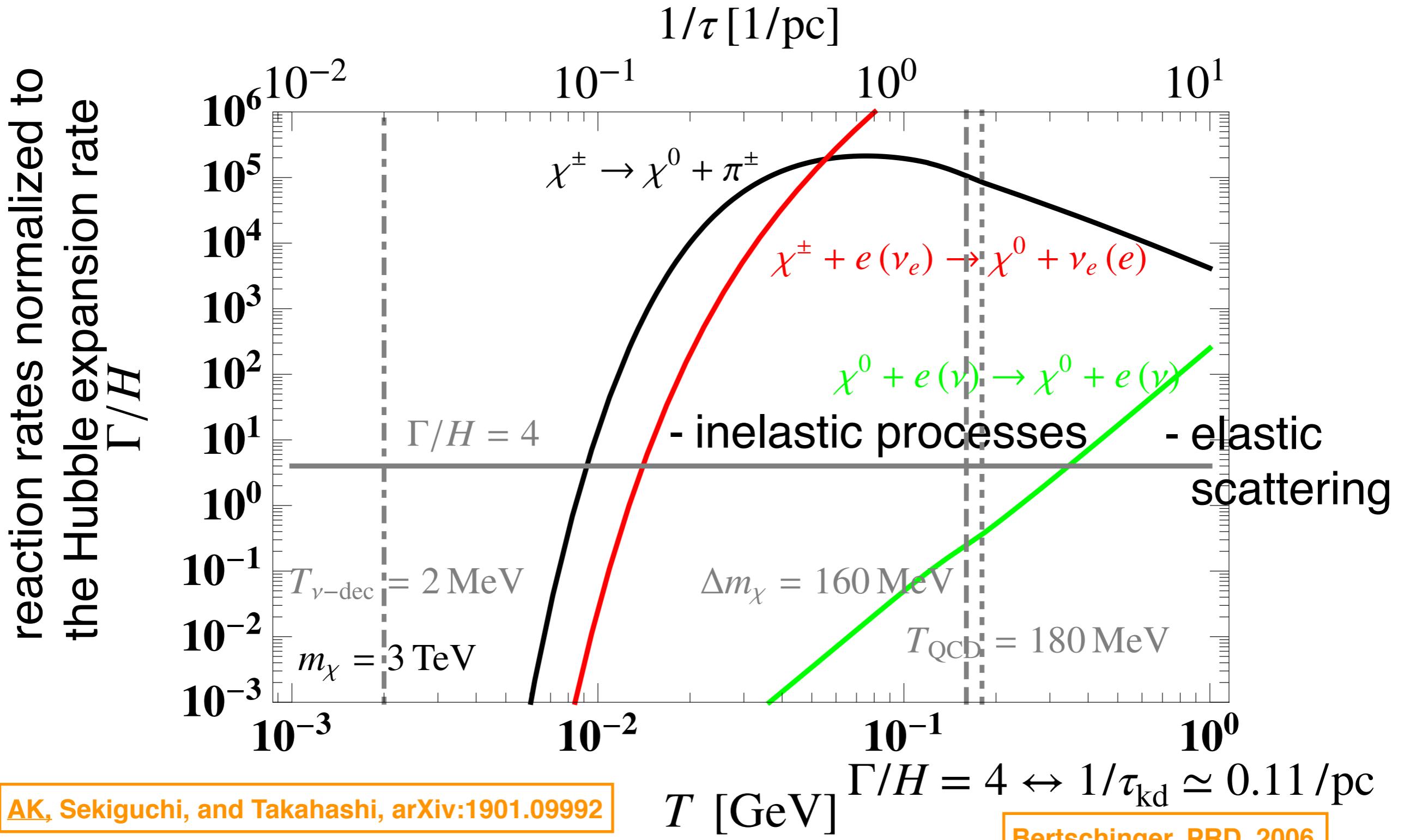
Dark matter is involved in plasma acoustic oscillation until kinetic decoupling - **dark acoustic oscillation**

horizon scale at decoupling \leftrightarrow smallest (proto) halos

Shin'ichiro's talk →

→ may impact indirect detection signals

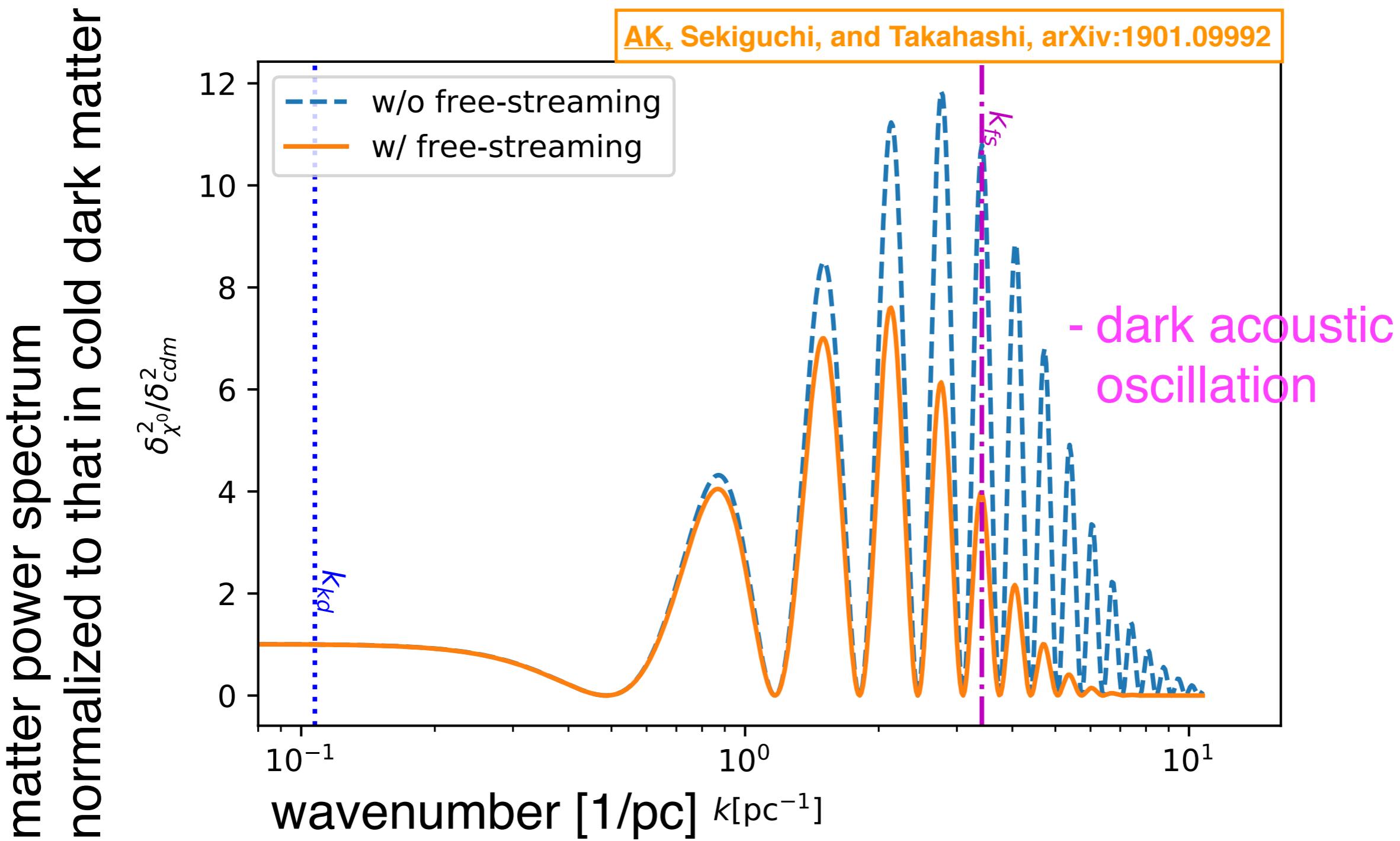
Kinetic decoupling



Inelastic processes with charginos involve neutralinos in dark acoustic oscillation

Power spectrum

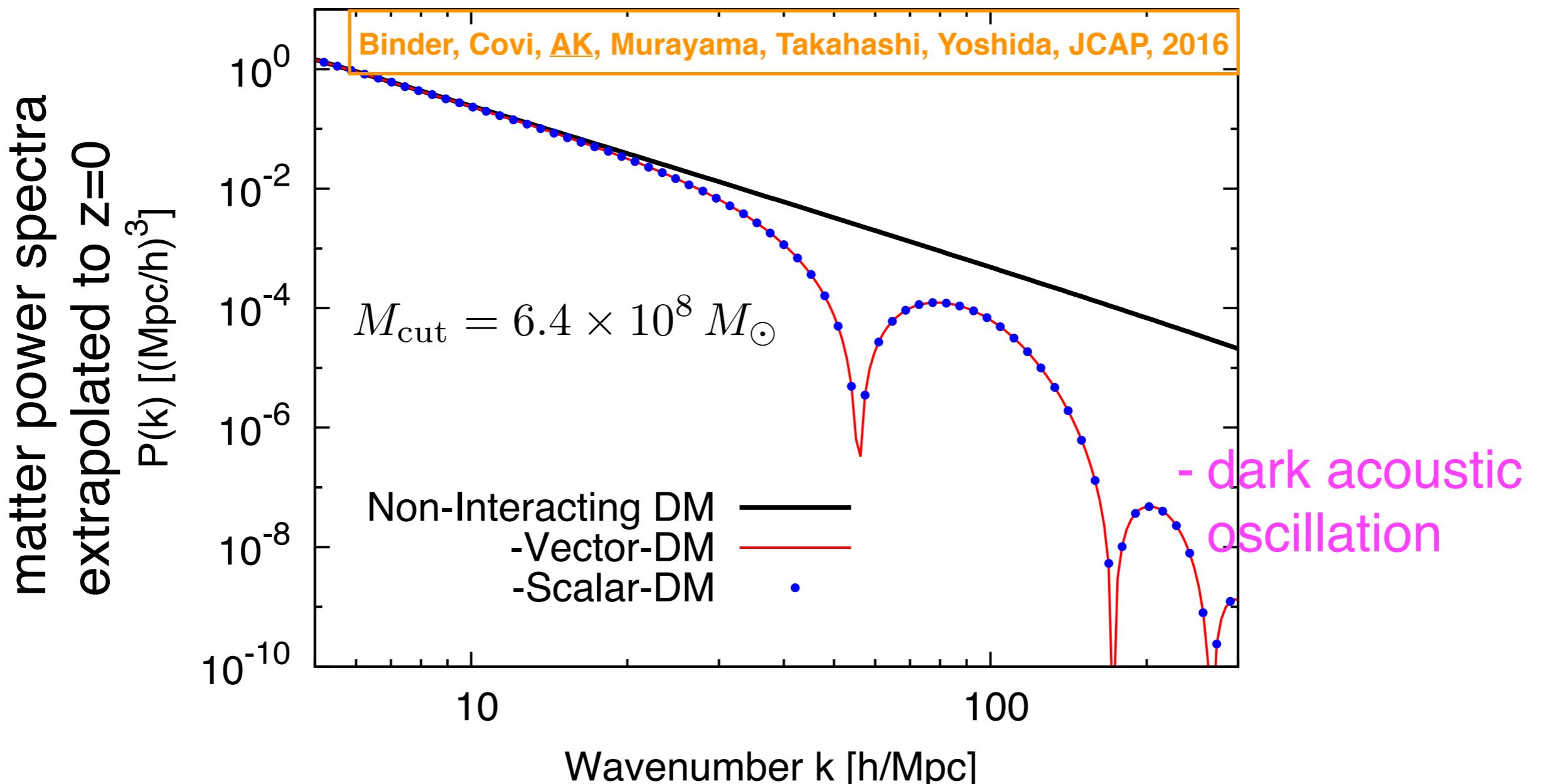
Wino dark matter - inelastic scattering



Peak amplitudes are enhanced!: overshooting phenomenon

Power spectrum

Typical WIMPs - elastic scattering

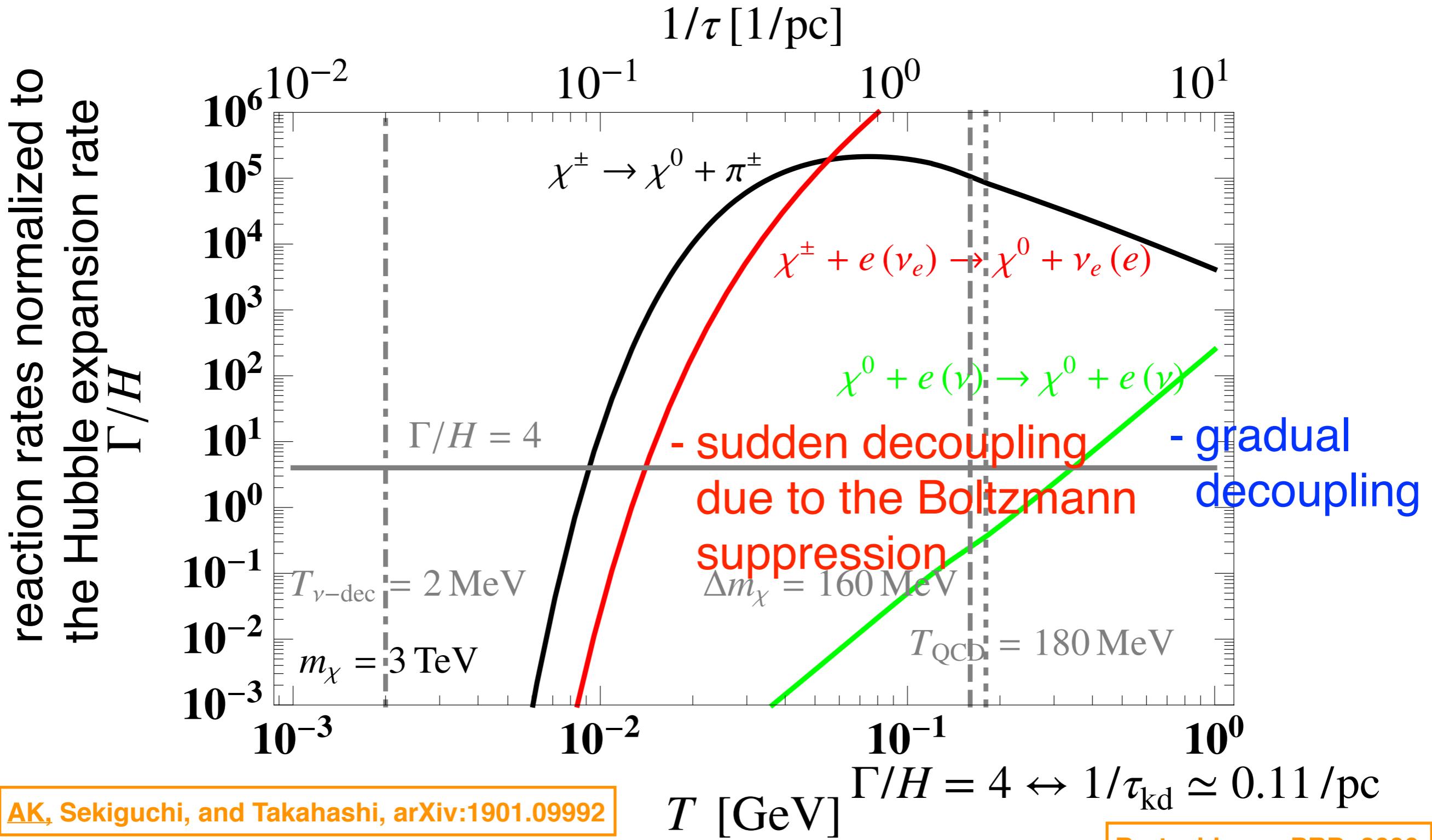


Peak amplitudes are damped

- Landau damping known for baryon acoustic oscillation

Oscillation phase is averaged over the finite duration of decoupling

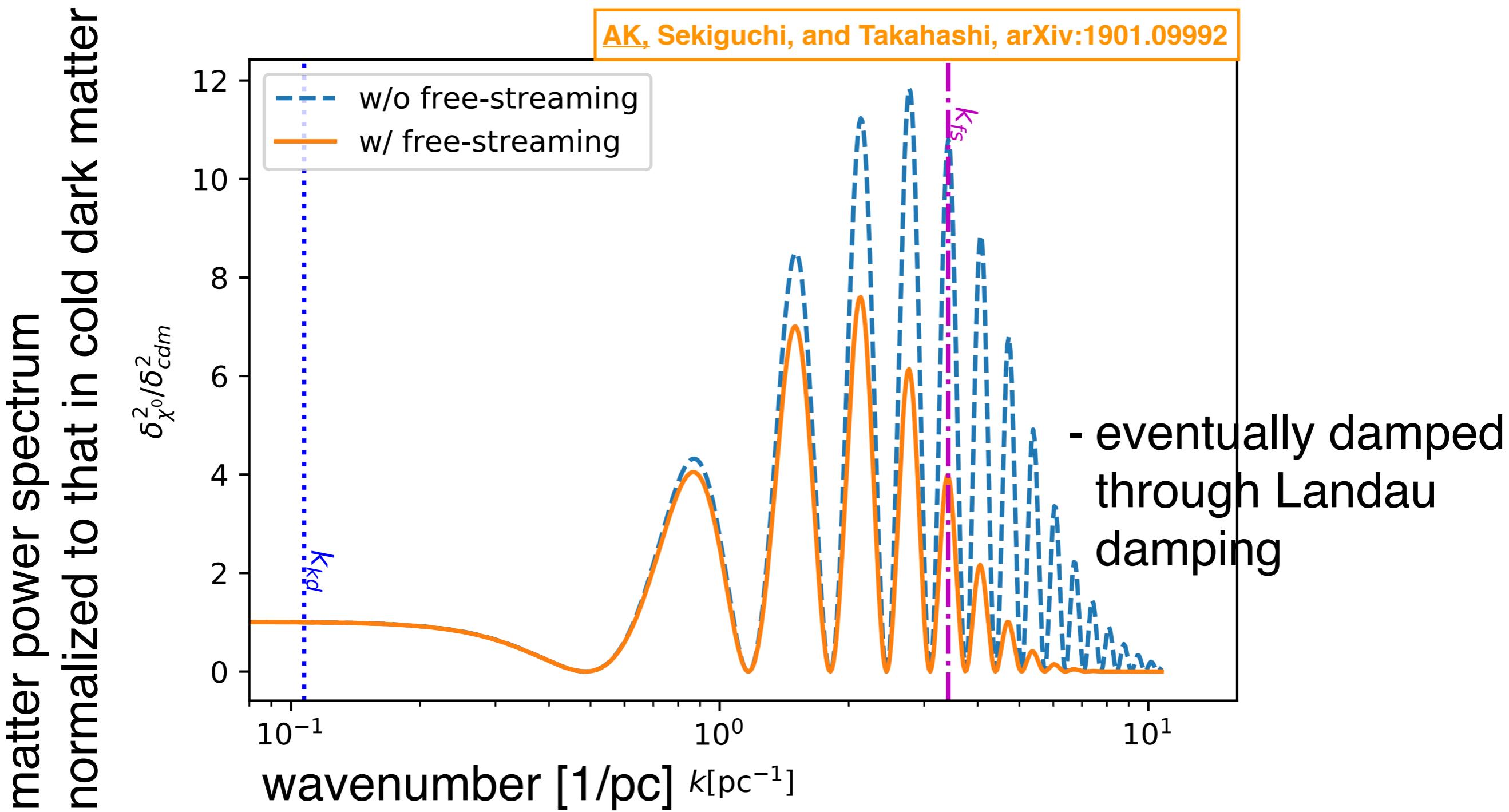
Kinetic decoupling



sudden (gradual) decoupling → horizon scale at decoupling << (~) damping scale → enhanced (damped) dark acoustic oscillation

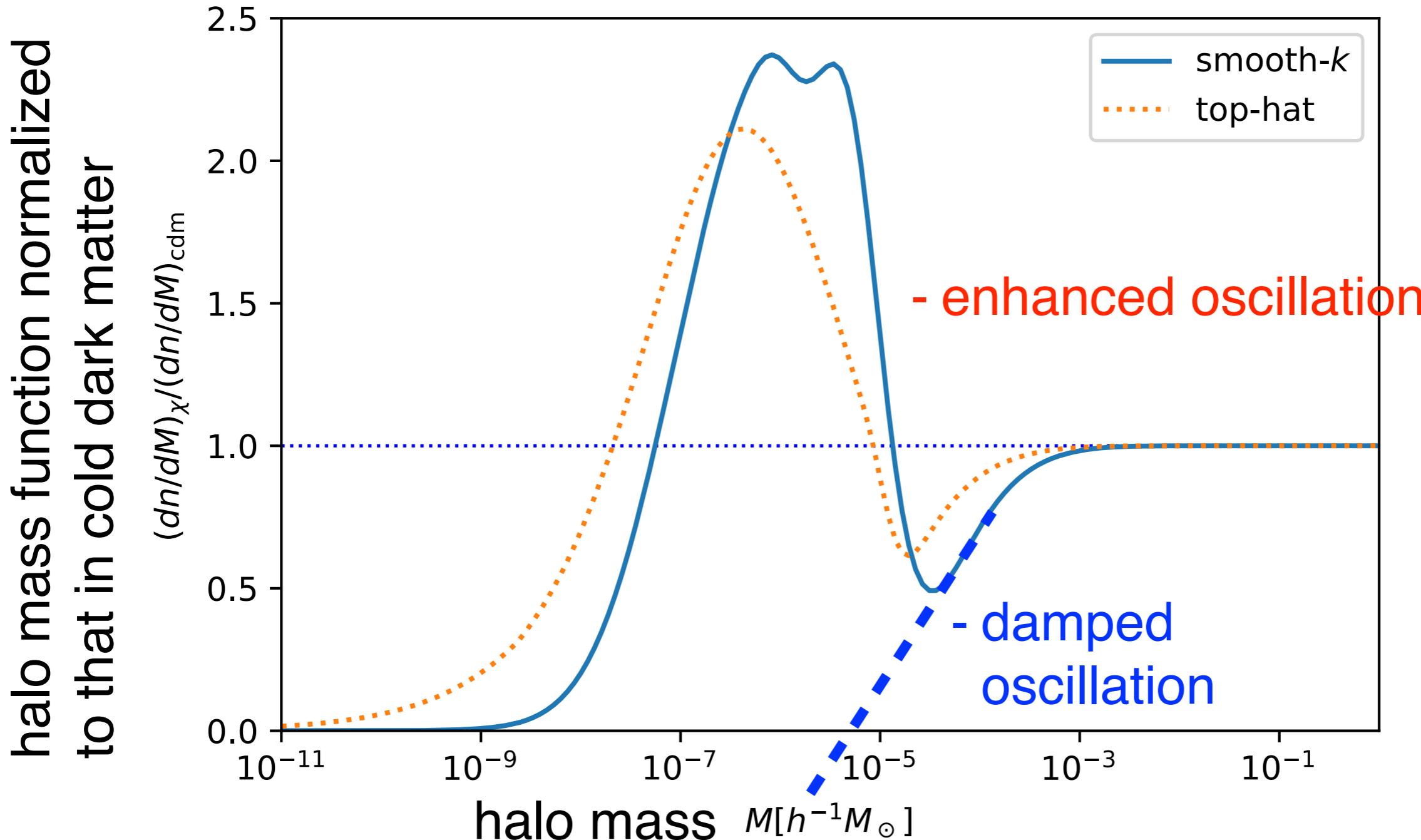
Power spectrum

Wino dark matter - inelastic scattering



Free-streaming after decoupling dominates damping

Estimated boost factor



$B(M)$ enhanced by a factor of 4.1 and 8.8 (1.5 and 2.9)
with $\alpha = 1.9$ and 2.0 in case 1 (2)
when compared to **damped oscillation**

→ Shin'ichiro's talk

Thank you for your attention

Mini-split supersymmetry

Arkani-Hamed and Dimopoulos, JHEP, 2005

Giudice and Romanino, NPB, 2004

Wells, PRD, 2005

...

Mini-split SUSY: pragmatic SUSY mass spectrum

- sfermions, heavy Higgses > 100 TeV; gravitino > 100 TeV
 - 125 GeV Higgs although the little hierarchy problem (electroweak scale v.s. SUSY breaking scale) unanswered
 - no experimental (e.g., flavor) or cosmological (e.g., gravitino) problem
- gauginos \sim TeV; higgsino \sim ???: experimental window
 - provide a dark matter candidate
 - another WIMP miracle?
 - precise grand unification of gauge couplings

Dark matter candidate

gravitino ~ 100 TeV, gauginos \sim TeV - anomaly mediation

\rightarrow (likely) **wino** (or higgsino) **dark matter**

Randall and Sundrum, NPB, 1999

Giudice, Luty, Murayama,
and Rattazzi, JHEP, 1998

Thermal pure wino dark matter

Ibe and Yanagida, PLB, 2012

Ibe, Matsumoto and Yanagida, PRD, 2012

higgsino > 100 TeV

neutralino (χ^0) and charginos (χ^\pm) $\Delta m_\chi \simeq 160$ MeV

perturbative annihilation $\chi^0 \chi^0 \rightarrow W^+ W^-$

Ibe, Matsumoto, and Sato PLB, 2013

+ co-annihilation

$\rightarrow \Omega_\chi h^2 = \Omega_{\text{dm}} h^2$ for $m_\chi \simeq 3$ TeV

+ Sommerfeld enhancement

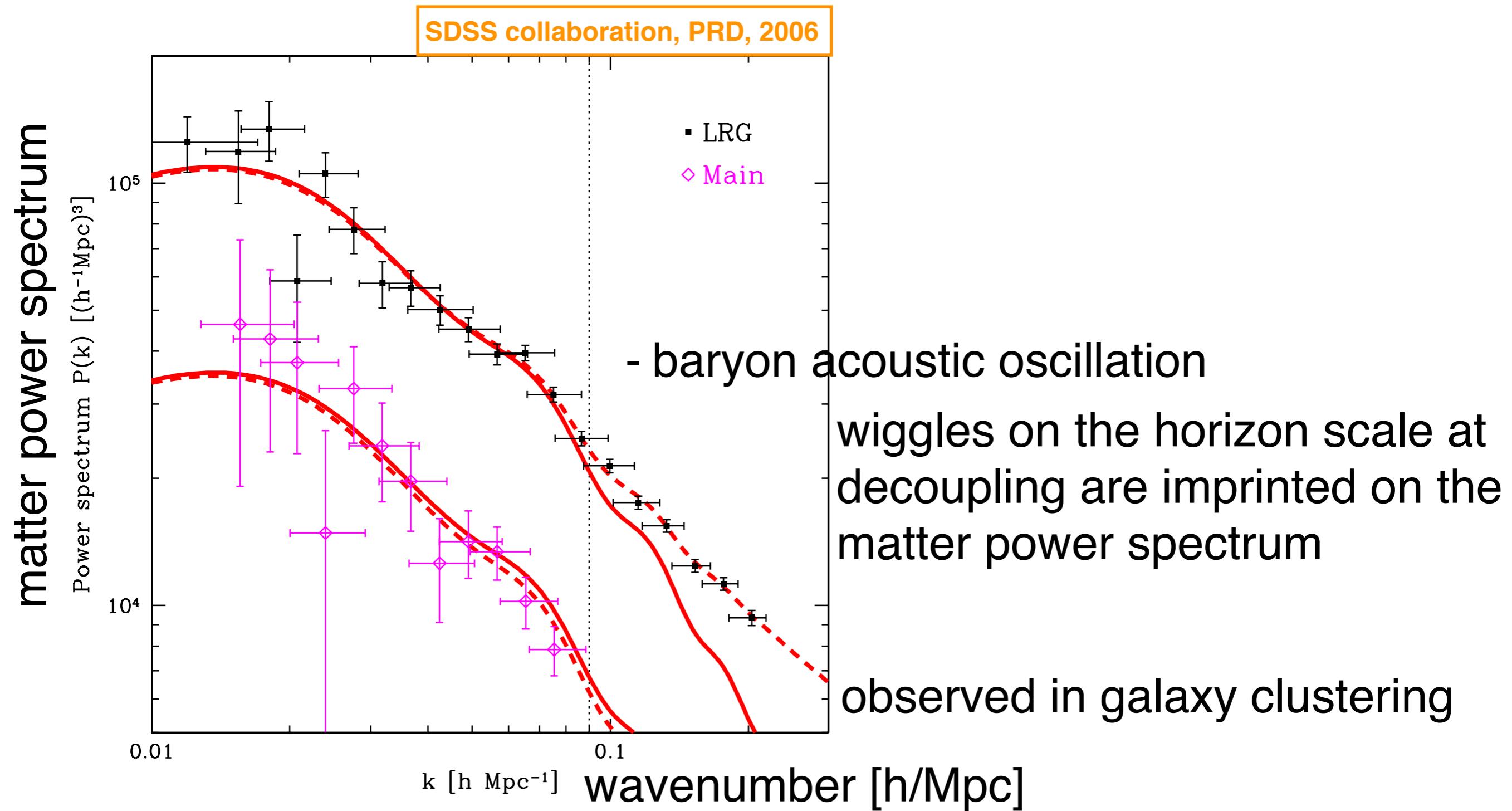
Hisano, Matsumoto, Nagai, Saito, and Senami, PLB, 2007

- no free parameter left

- accompanied by slightly heavier charged component
(EWIMP or electroweakino)

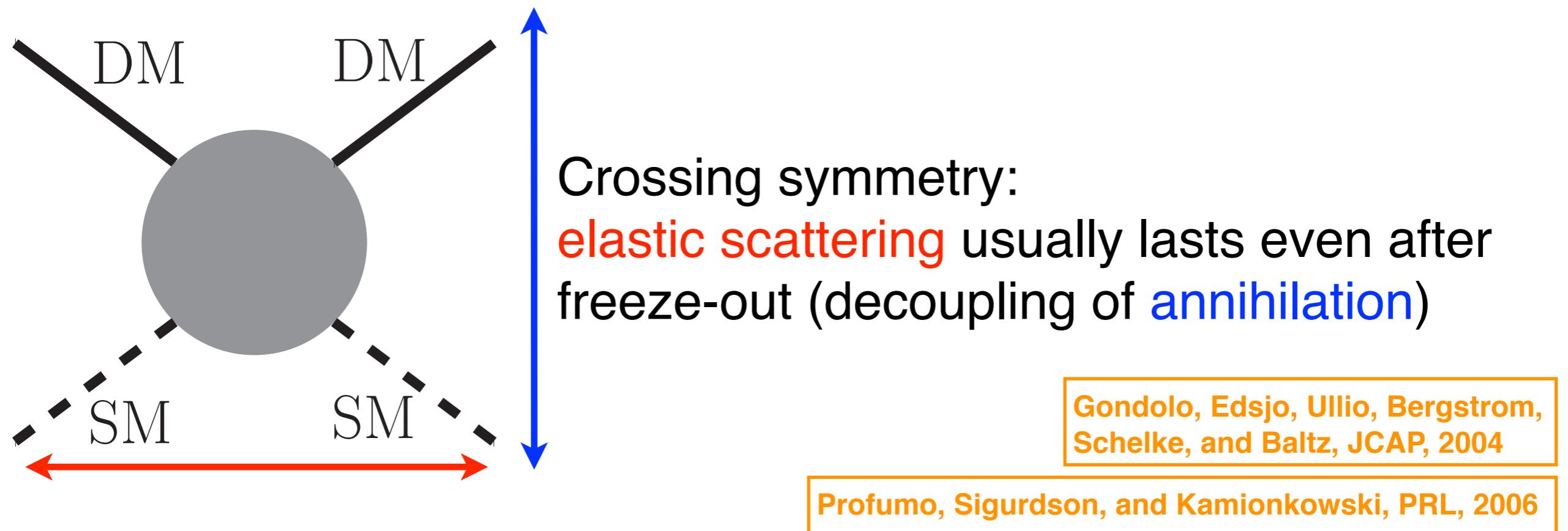
Part 1: Baryon acoustic oscillation

Baryons are involved in plasma acoustic oscillation until decoupling (recombination)



Dark acoustic oscillation

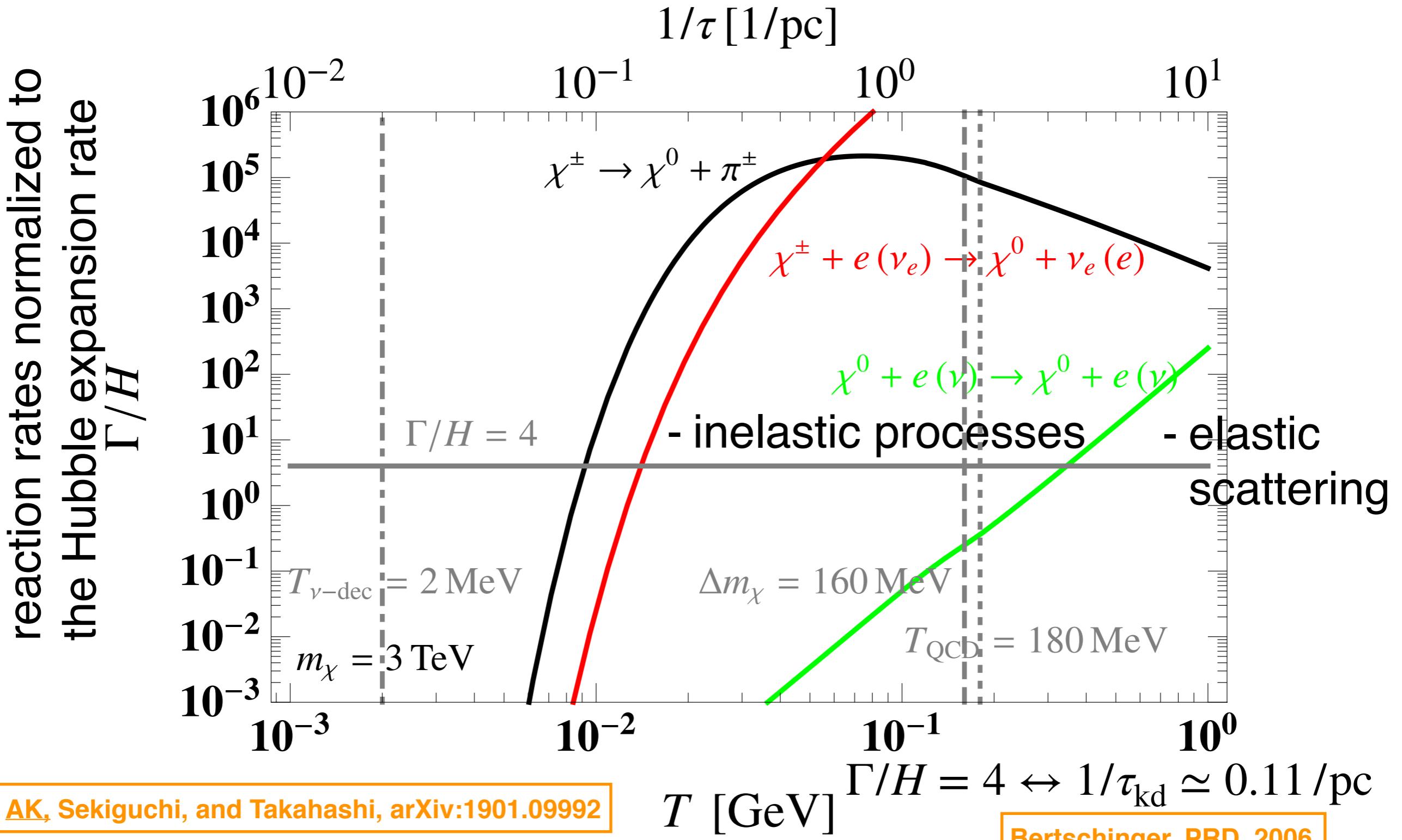
WIMPs (weakly interacting massive particles) are in thermal equilibrium in the early Universe



Dark matter is involved in plasma acoustic oscillation until kinetic decoupling - **dark acoustic oscillation**

horizon scale at decoupling \leftrightarrow smallest (proto) halos
 \rightarrow may impact indirect detection signals

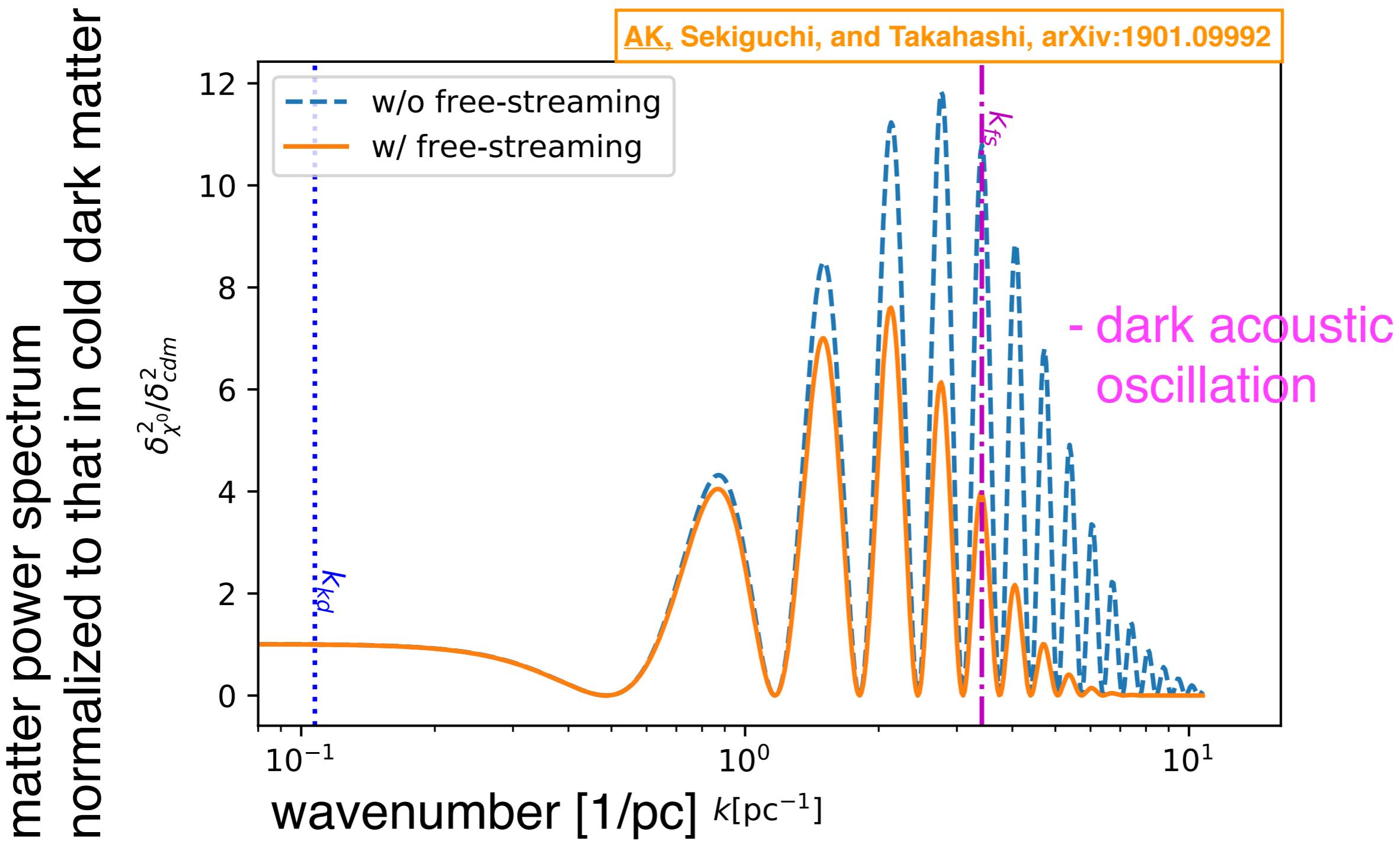
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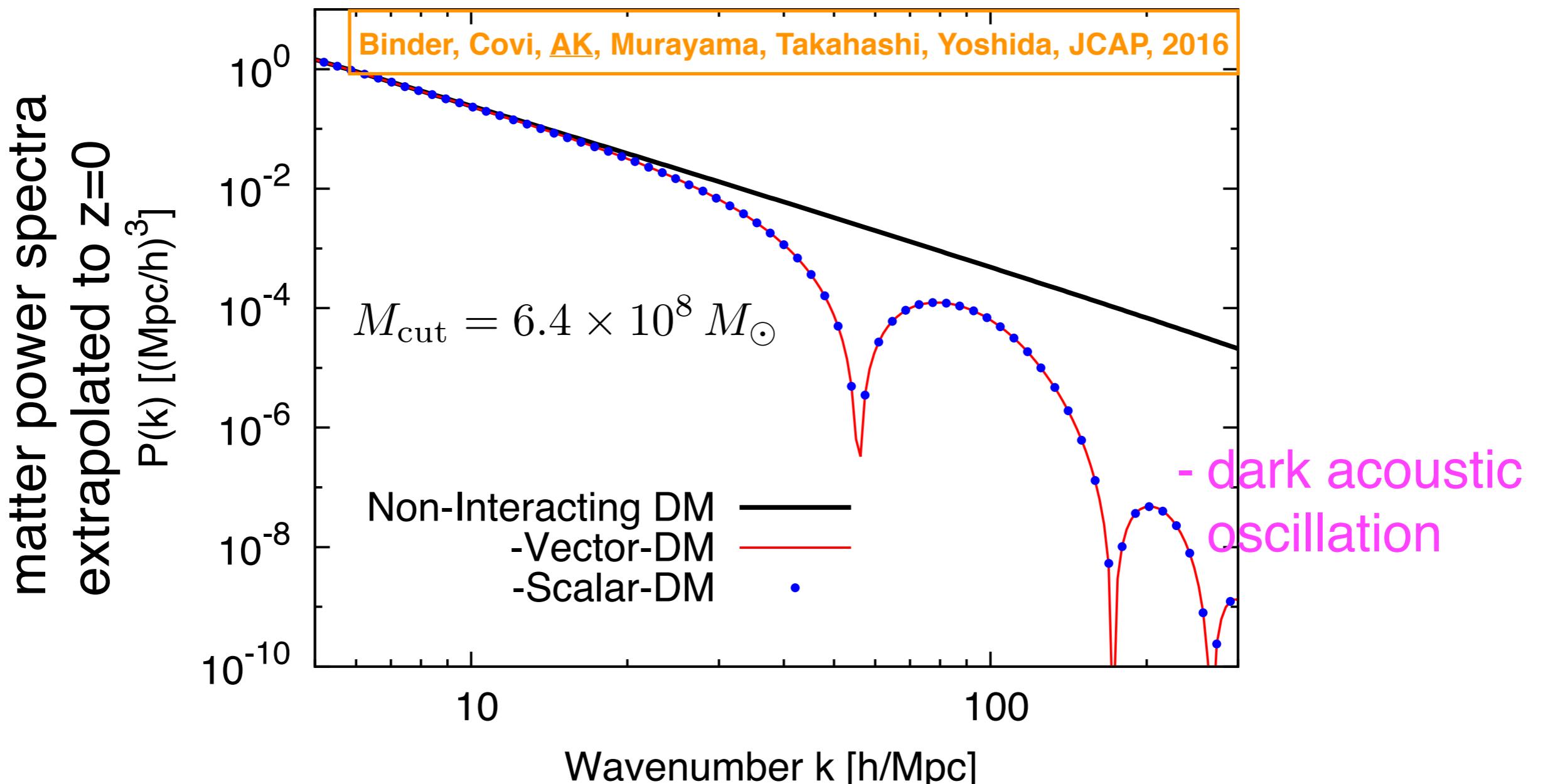
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Typical WIMPs - elastic scattering

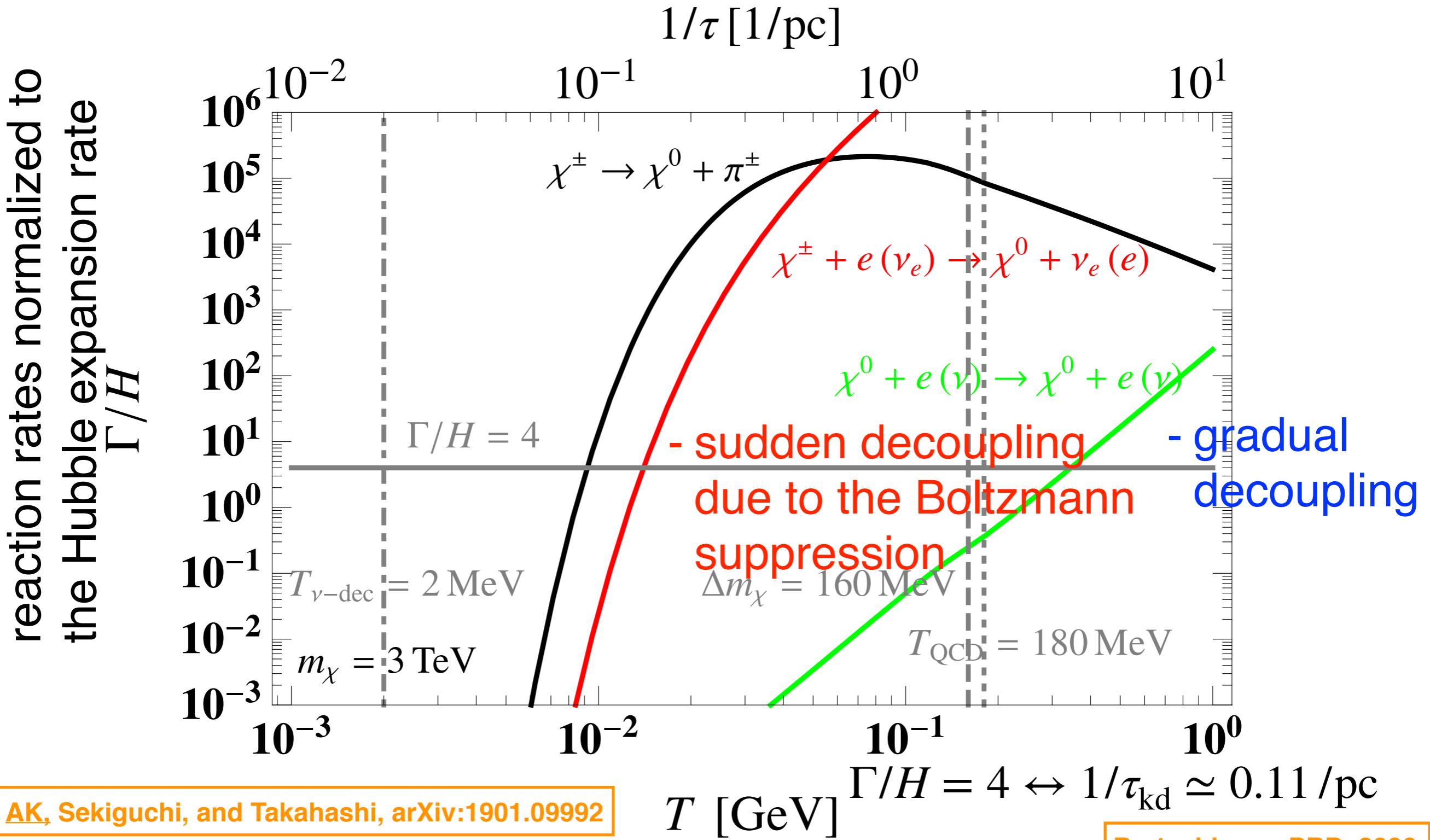


Peak amplitudes are damped

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Oscillation phase is averaged over the finite duration of decoupling

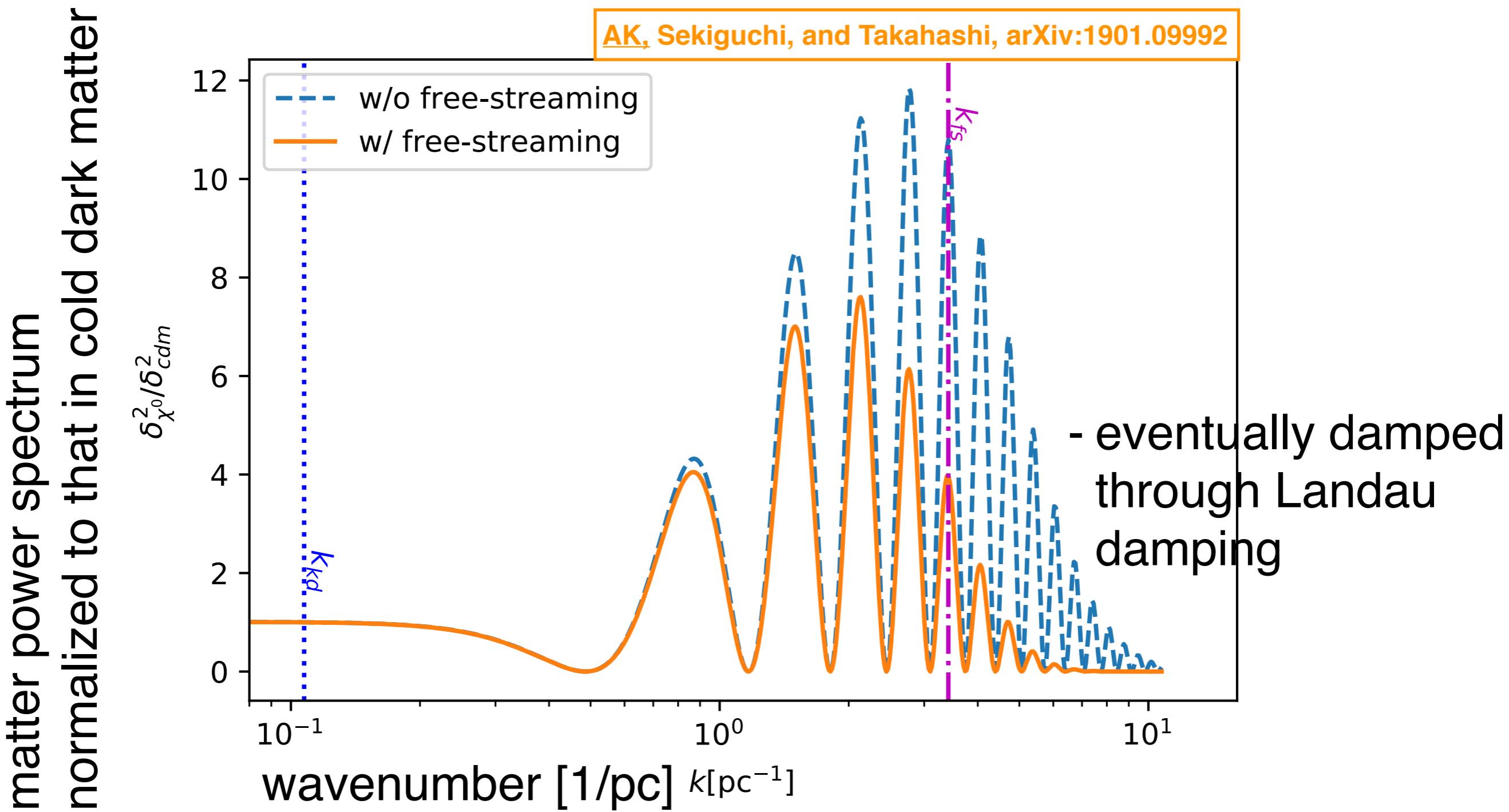
Kinetic decoupling



sudden (gradual) decoupling → horizon scale at decoupling << (\sim) damping scale → enhanced (damped) dark acoustic oscillation

Power spectrum

Wino dark matter - inelastic scattering



Free-streaming after decoupling dominates damping

Boost factor

Wino (or generically electroweakino) dark matter

- annihilation into gauge bosons are non-perturbatively enhanced toward lower velocity (Sommerfeld enhancement)

→ good target of indirect detection experiments

Hisano, Matsumoto,
and Nojiri, PRD, 2003

Hisano, Matsumoto,
and Nojiri, PRL, 2004

...

Boost factor: $L(M) = (1+B(M))\bar{L}(M)$ - total luminosity

$\bar{L}(M)$ - contribution from coarse-grained distribution squared $\langle \rho \rangle^2$

$\langle \rho^2 \rangle / \langle \rho \rangle^2 \geq 1$ $\langle \rho \rangle$ - e.g. Navarro-Frenk-White (NFW) profile

$B(M)$ - we estimate a subhalo contribution by using a halo model with extrapolations toward small scales

Strigari, Koushiappas, Bullock,
and Kaplinghat, PRD, 2007

Kuhlen, Diemand, and
Madau, ApJ, 2008

Boost factor

We adopt a halo model approach to estimate the boost factor with extrapolations

$$B(M) = \frac{1}{\bar{L}(M)} \int_{m_{\min}}^M dm \frac{dn_{\text{sub}}}{dm} (1 + B_{\text{sub}}(m)) \bar{L}_{\text{sub}}(m)$$

m_{\min} : minimal halo mass

Hierarchical structure: $B = B_{\text{sub}}$, $\bar{L} = \bar{L}_{\text{sub}}$

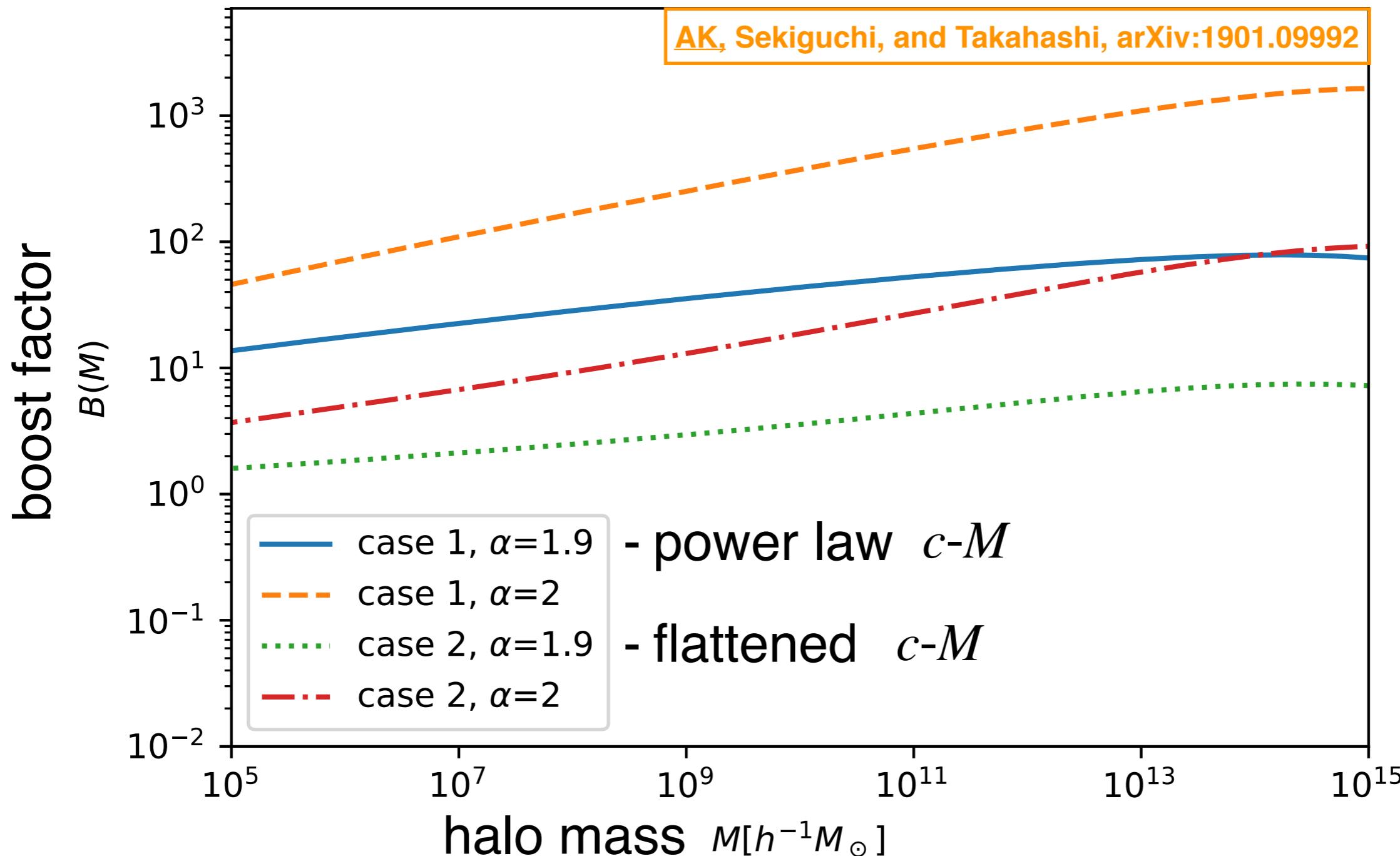
Coarse-grained luminosity \bar{L}

- Navarro-Frenk-White (NFW) profile c - M relation
power-law or flattened?

Subhalo mass function: dn_{sub}/dm power-law index $\alpha = 1.9-2.0$

$\times \frac{(dn/d \ln M)_\chi}{(dn/d \ln M)_{\text{cdm}}} \Big|_{\text{PS}}$ for wino dark matter

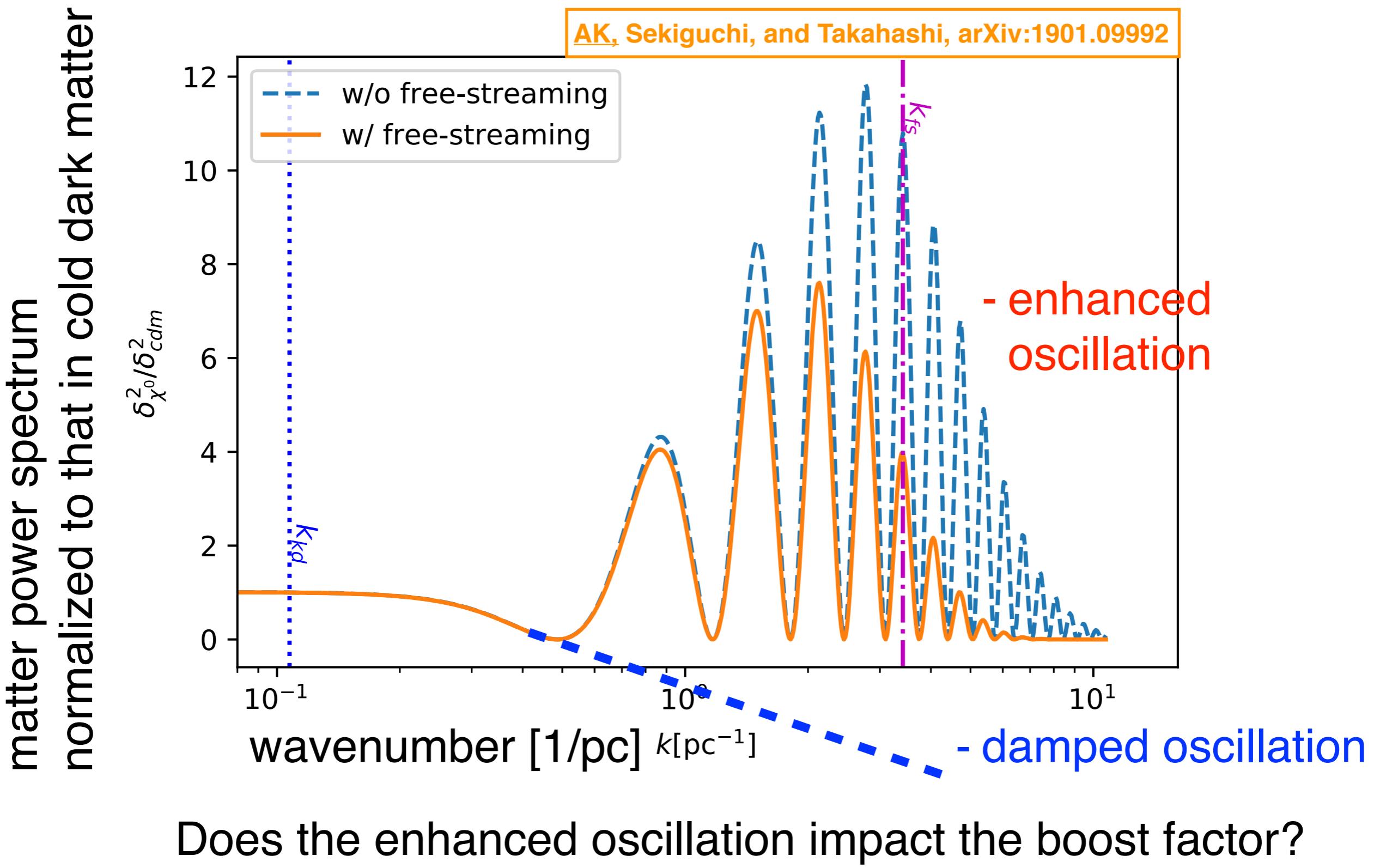
Estimated boost factor



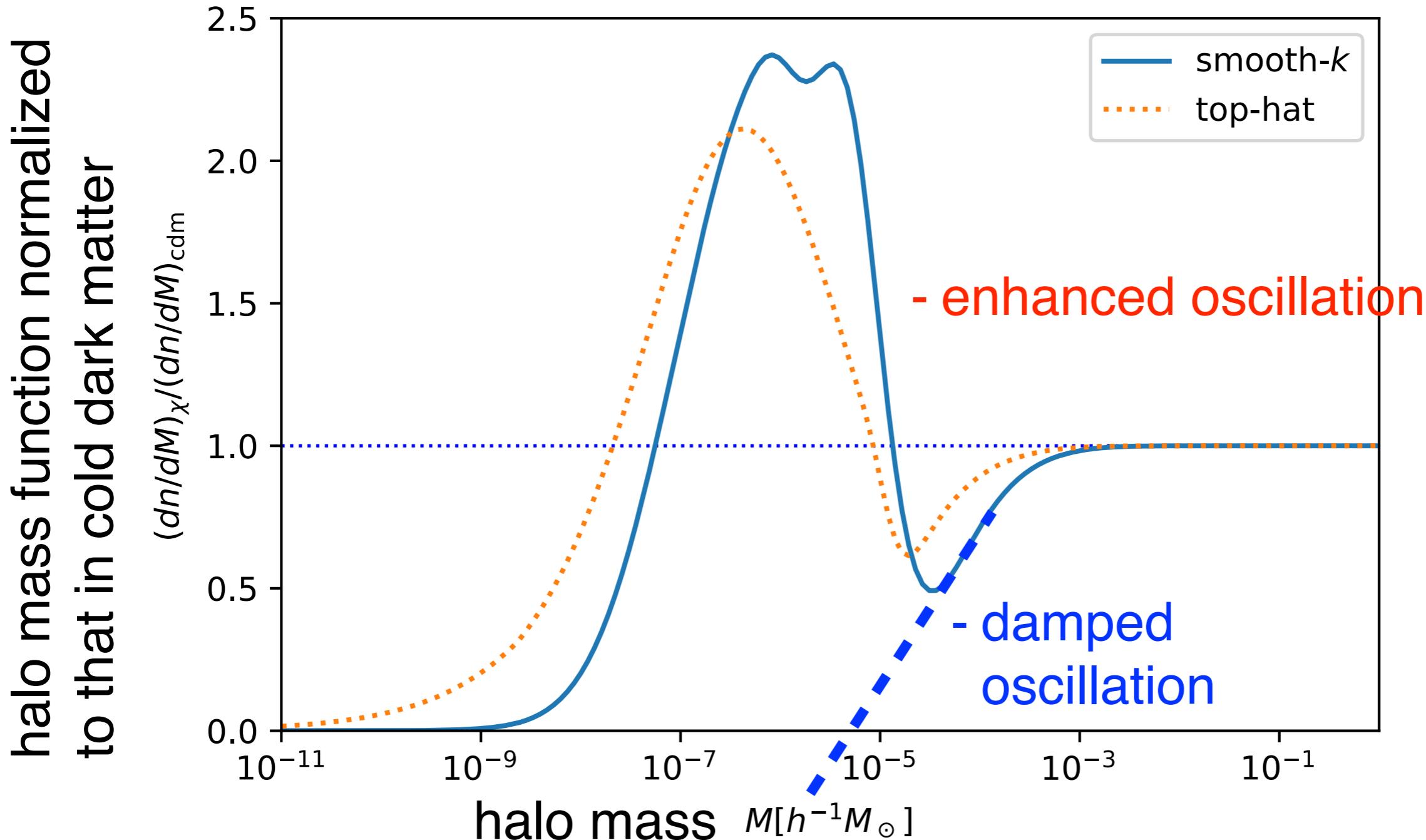
Boost factor depends on power-law index of the subhalo mass function α and the c - M relation

Power spectrum

Wino dark matter - inelastic scattering

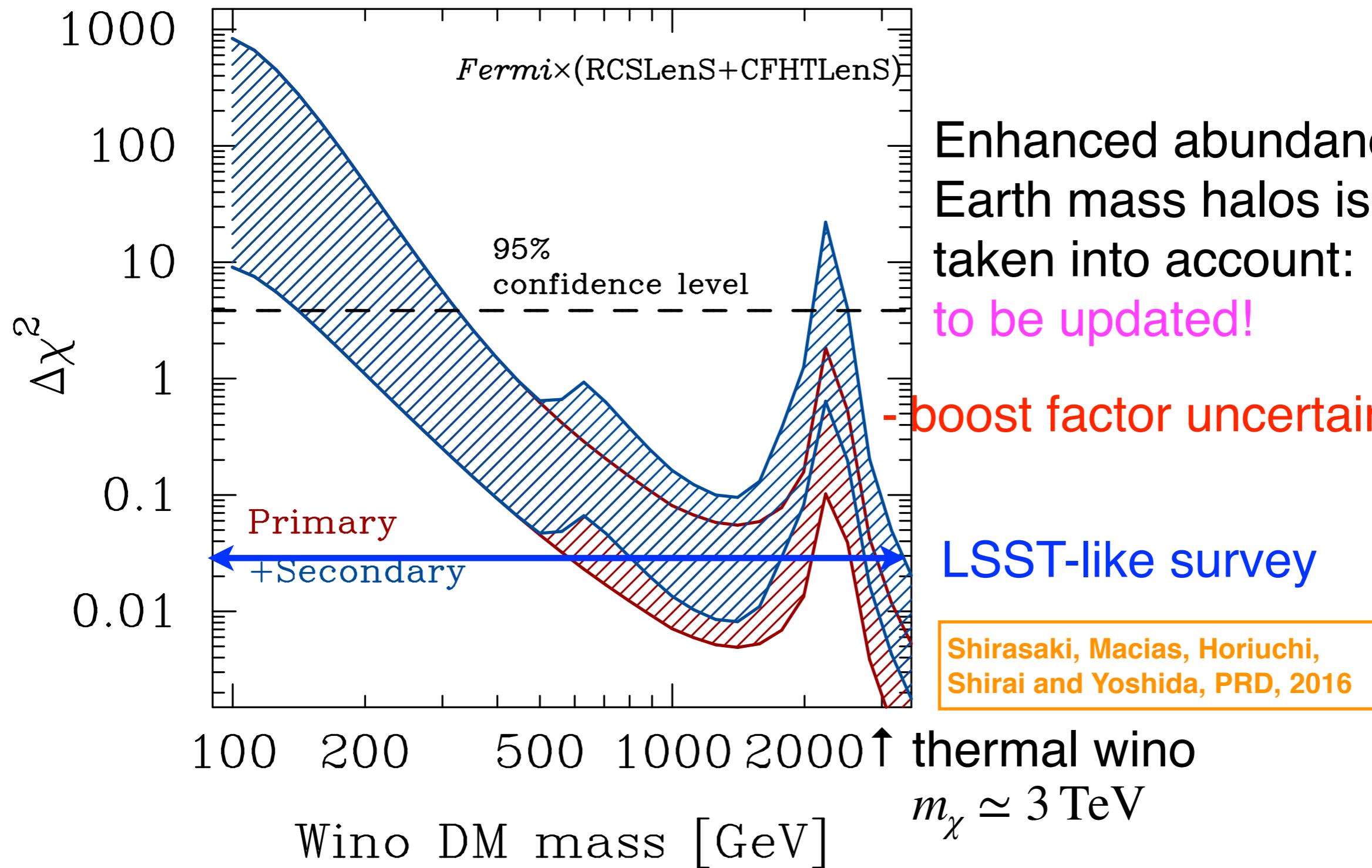


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Indirect detection



Cross-correlation of gamma-ray background w/ large-scale structure (e.g., weak lensing) will enjoy statistical improvement in near future!

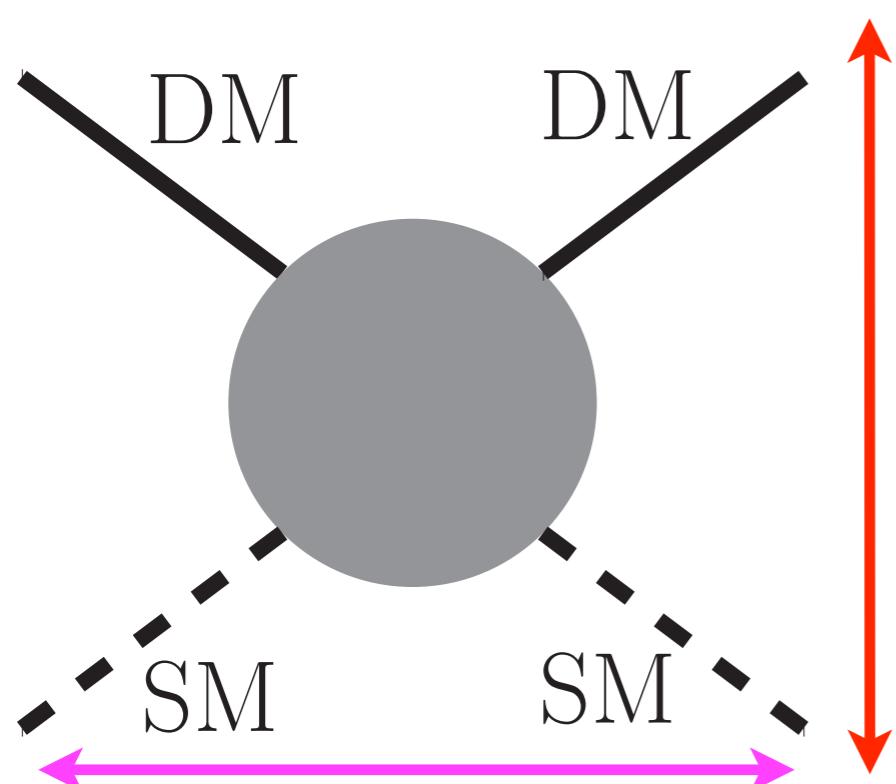
Enhanced abundance of Earth mass halos is not taken into account:
to be updated!

- boost factor uncertainty

Minimal halo mass

What determines the minimal halo mass?

- primordial density perturbation: $P(k) \propto k^{n_s}$?
- dark matter properties
 - free-streaming: smoothes the primordial density contrast
 - decoupling from primordial plasma: until then dark matter is involved in **plasma acoustic oscillation**



Gondolo, Edsjo, Ullio, Bergstrom, Schelke, and Baltz, JCAP, 2004

Profumo, Sigurdson, and Kamionkowski, PRL, 2006

...
Crossing symmetry:
elastic process usually lasts even after
freeze-out (decoupling of **inelastic process**)

Dark matter candidate

gravitino ~ 100 TeV, gauginos \sim TeV - anomaly mediation

\rightarrow (likely) **wino** (or higgsino) **dark matter**

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higgsino > 100 TeV

perturbative annihilation $\chi^0 \chi^0 \rightarrow W^+ W^-$

+ co-annihilation

+ Sommerfeld enhancement

$\rightarrow \Omega_\chi h^2 = \Omega_{\text{dm}} h^2$ for $m_\chi \simeq 3$ TeV

Hisano, Matsumoto, Nagai, Saito, and Senami, PLB, 2007

- no free parameter left

- annihilation into gauge bosons are non-perturbatively enhanced toward lower velocity (Sommerfeld enhancement)

\rightarrow good target of indirect detection experiments

Indirect detection experiments

High-energy cosmic rays: anti-particles; **gamma-ray**

- target approach: galactic center; dwarf galaxies

Cohen, Lisanti, Pierce, and Slatyer, JCAP, 2013

Fan and Reece, JHEP, 2013

Bhattacherjee, Ibe, Ichikawa, Matsumoto, and K. Nishiyama, JHEP, 2014

- statistical approach: diffuse background

- cross-correlations w/ large-scale structure data
will enjoy statistical improvement in near future

Uncertainty: dark matte distribution - J factor

Shirasaki, Macias, Horiuchi, Shirai, and Yoshida, PRD, 2016

- density profile of a dark matter halo $\langle \rho \rangle_{\text{coarse graining}}$
- flux multiplier/**boost factor**: $\langle \rho^2 \rangle / \langle \rho \rangle^2 \geq 1$
- (sub) halo mass function up to the **smallest halos**
- $\langle \rho \rangle$ up to the **smallest halos**: c - M relation

Elastic processes

Fokker-Planck approximation:
expanding the collision term w.r.t. $q/p \ll 1$

$$C[f_{\text{DM}}] = m_{\text{DM}} \frac{\partial}{\partial \mathbf{p}_{\text{DM}i}} \left[\gamma \left(m_{\text{DM}} T \frac{\partial f_{\text{DM}}}{\partial \mathbf{p}_{\text{DM}i}} + (\mathbf{p}_{\text{DM}i} - m_{\text{DM}} \mathbf{u}_i) f_{\text{DM}} \right) \right]$$

differential cross section

$$\gamma = \frac{1}{6m_{\text{DM}}T} \sum_{s_{\text{TP}}} \int \frac{d^3 \mathbf{p}_{\text{TP}}}{(2\pi)^3} f_{\text{TP}}^{\text{eq}} (1 \mp f_{\text{TP}}^{\text{eq}}) \int_{-4\mathbf{p}_{\text{TP}}^2}^0 dt (-t) \frac{d\sigma}{dt} v$$

thermal momentum squared $\propto p^2$ **momentum transfer squared $\propto q^2$**

Binder, Covi, AK, Murayama, Takahashi, and Yoshida, JCAP, 2016 ...

T : temperature
 $u^\mu(x)$: bulk velocity
of thermal bath plasma

Elastic processes for neutral wino

Elastic scattering is subdominant!

- $\chi^0 W^\pm \rightarrow \chi^0 W^\pm$: related with perturbative annihilation
inefficient after $T \sim m_W$

- $\chi^0 L \rightarrow \chi^0 L$ ($L = \nu, e$) : loop suppressed Ibe, AK, and Matsumoto, PRD, 2013

$$\gamma_{\text{ela}} = 8 \frac{100}{\pi^3} g_{\text{loop}}^2 G_F^4 m_W^4 \frac{T^6}{m_\chi}$$

$$g_{\text{loop}} = \frac{1}{3\pi^2} \left(2(8 - \omega - \omega^2) \sqrt{\frac{\omega}{4 - \omega}} \arctan \left(\sqrt{\frac{4 - \omega}{\omega}} \right) - \omega (2 - (3 + \omega) \ln \omega) \right)$$

$$\omega = m_W^2/m_\chi^2$$

inefficient after $T \sim 1 \text{ GeV}$

Relevant processes for charged wino

χ^\pm is in kinetic equilibrium with primordial plasma $\gamma, e, \nu, \pi, \dots$

$$f_{\chi^\pm}(\mathbf{p}) \approx \frac{n_{\chi^\pm}}{g_{\chi^\pm}} \left(\frac{2\pi}{m_\chi T} \right)^{3/2} \exp \left(-\frac{(\mathbf{p} - m_\chi \mathbf{u})^2}{2m_\chi T} \right) \quad \mathbf{u}: \text{bulk velocity}$$

χ^\pm and χ^0 are in chemical equilibrium through inelastic processes

Arcadi and Ullio, PRD, 2011

- $\chi^\pm \rightarrow \chi^0 + \pi^\pm$: decay

$$\Gamma_{\text{dec}} \approx \frac{f_\pi^2 G_F^2 |V_{ud}|^2}{\pi} \Delta m_\chi^3 \sqrt{1 - \frac{m_{\pi^\pm}^2}{\Delta m_\chi^2}}$$

- $\chi^\pm L' \rightarrow \chi^0 L$: inelastic scattering

$$\Gamma_{\text{inela}} = 2 \frac{8G_F^2}{\pi^3} T^3 \left(\Delta m_\chi^2 + 6\Delta m_\chi T + 12T^2 \right)$$

$$n_{\chi^\pm} \approx \frac{g_{\chi^\pm}}{g_{\chi^0}} n_{\chi^0} \exp \left(-\frac{\Delta m_\chi}{T} \right)$$

Relevant processes for neutral wino

Inelastic processes keep χ^0 in kinetic equilibrium and are dominant

- $\chi^0 + \pi^\pm \rightarrow \chi^\pm, \chi^0 L \rightarrow \chi^\pm L'$: conversion approximation

Arcadi and Ullio, PRD, 2011

$$\Delta m_\chi, T \ll \sqrt{m_\chi T}$$

$$\frac{1}{E} C_{\chi^0, \text{inela}} \approx g_{\chi^\pm} (\Gamma_{\text{dec}} + \Gamma_{\text{inela}}) \left(f_{\chi^\pm} - f_{\chi^0} \exp \left(-\frac{\Delta m_\chi}{T} \right) \right)$$

For χ^0 , interaction rates are suppressed by $\exp(-\Delta m_\chi/T)$
 - efficient until $T \sim \Delta m_\chi/20$

Cosmological background

- synchronous gauge

$$ds^2 = a^2 \left(-d\tau^2 + (\delta_{ij} + h_{ij}) dx^i dx^j \right), \quad h_{ij} = \hat{k}_i \hat{k}_j h + \left(\hat{k}_i \hat{k}_j - \frac{1}{3} \delta_{ij} \right) \eta$$

- evolution of number density $n_\chi = g_\chi \int \frac{d^3 \mathbf{p}}{(2\pi)^3} f_\chi$

$$\dot{n}_{\chi^0} + 3 \frac{\dot{a}}{a} n_{\chi^0} = - \left(\dot{n}_{\chi^\pm} - 3 \frac{\dot{a}}{a} n_{\chi^\pm} \right) (\approx 0),$$

- total wino number conservation - chemical equilibrium

- evolution of temperature $3m_\chi T_\chi n_\chi = g_\chi \int \frac{d^3 \mathbf{p}}{(2\pi)^3} \mathbf{p}^2 f_\chi$

$$\dot{T}_{\chi^0} + 2 \frac{\dot{a}}{a} T_{\chi^0} \approx a \left[g_{\chi^\pm} (\Gamma_{\text{dec}} + \Gamma_{\text{inel}}) \exp \left(-\frac{\Delta m_\chi}{T} \right) + 2g_{\chi^0} \gamma_{\text{ela}} \right] (T - T_{\chi^0})$$

- effective reaction rate

Cosmological perturbations

- evolution of density perturbation $n_\chi \delta_\chi = g_\chi \int \frac{d^3 p}{(2\pi)^3} \delta f_\chi$

$$\dot{\delta}_{\chi^0} + \theta_{\chi^0} + \frac{1}{2}\dot{h} = - \left(\frac{\dot{n}_{\chi^0}}{n_{\chi^0}} + 3\frac{\dot{a}}{a} \right) (\delta_{\chi^0} - \delta_{\chi^\pm}) - \frac{n_{\chi^\pm}}{n_{\chi^0}} \left(\dot{\delta}_{\chi^\pm} + \theta_T + \frac{1}{2}\dot{h} \right) (\approx 0)$$

- total wino number conservation

$$\delta_{\chi^\pm} \approx \delta_{\chi^0} + \frac{\Delta m_\chi}{T} \delta_T, \quad \delta_T = \frac{\delta T}{T}, \quad \theta_T = i\mathbf{k} \cdot \mathbf{u}$$

- chemical equilibrium

- evolution of velocity perturbation $m_\chi n_\chi \theta_\chi = g_\chi \int \frac{d^3 p}{(2\pi)^3} (i\mathbf{k} \cdot \mathbf{p}) \delta f_\chi$

$$\dot{\theta}_{\chi^0} + \frac{\dot{a}}{a} \theta_{\chi^0} \approx ag_{\chi^\pm}(\Gamma_{\text{dec}} + \Gamma_{\text{inela}}) \exp\left(-\frac{\Delta m_\chi}{T}\right) (\theta_T - \theta_{\chi^0})$$

- the same effective reaction rate as for temperature evolution

- sour term drives dark acoustic oscillation

Overshooting phenomenon

Seen when kinetic decoupling proceeds rapidly

$$\frac{1}{\Gamma/H} \frac{d(\Gamma/H)}{dt} \gg H \quad \text{around kinetic decoupling} \quad \Gamma/H \sim 1$$

Discovered for Coulomb scattering of charged massive particle (CHAMP) with electrons $\Gamma \propto \exp(-m_e/T)$ $T_{\text{kd}} \sim m_e/20$

[AK, Kohri, Takahashi, and Yoshida, PRD, 2017](#)

Analytic approximation can be derived for $\Gamma/H = (\tau/\tau_d)^n$

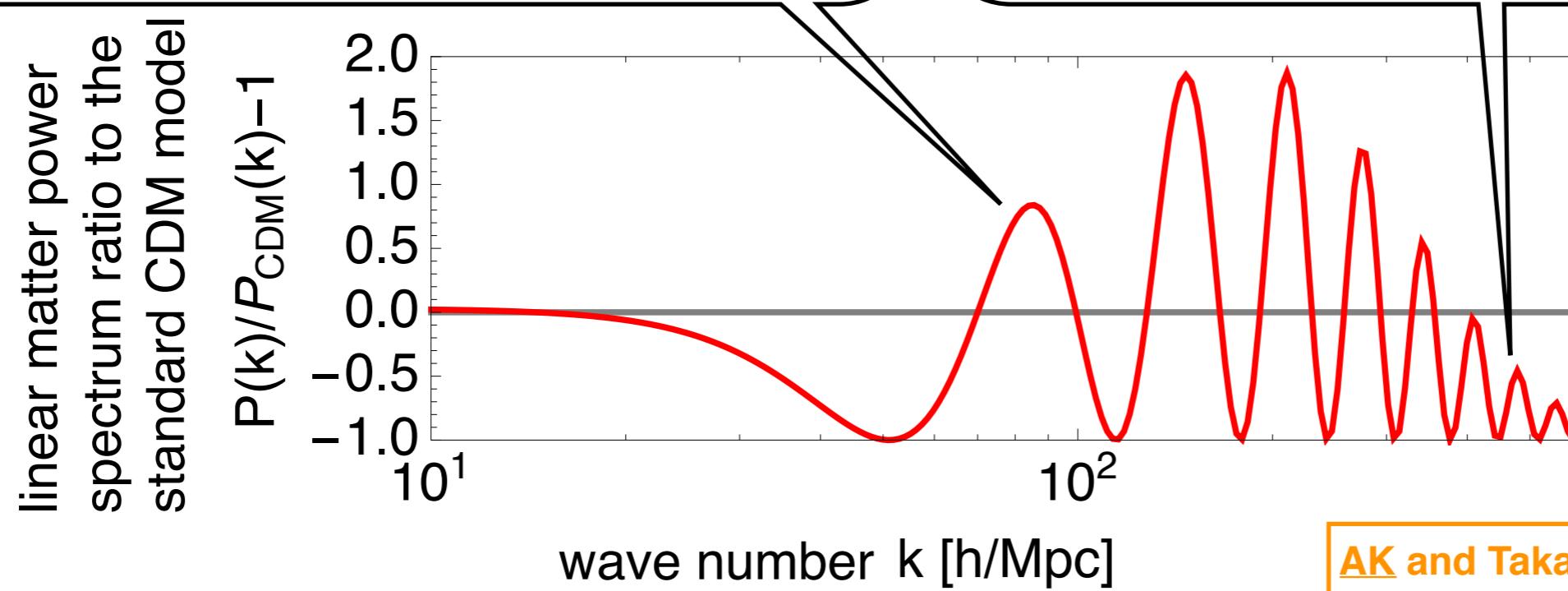
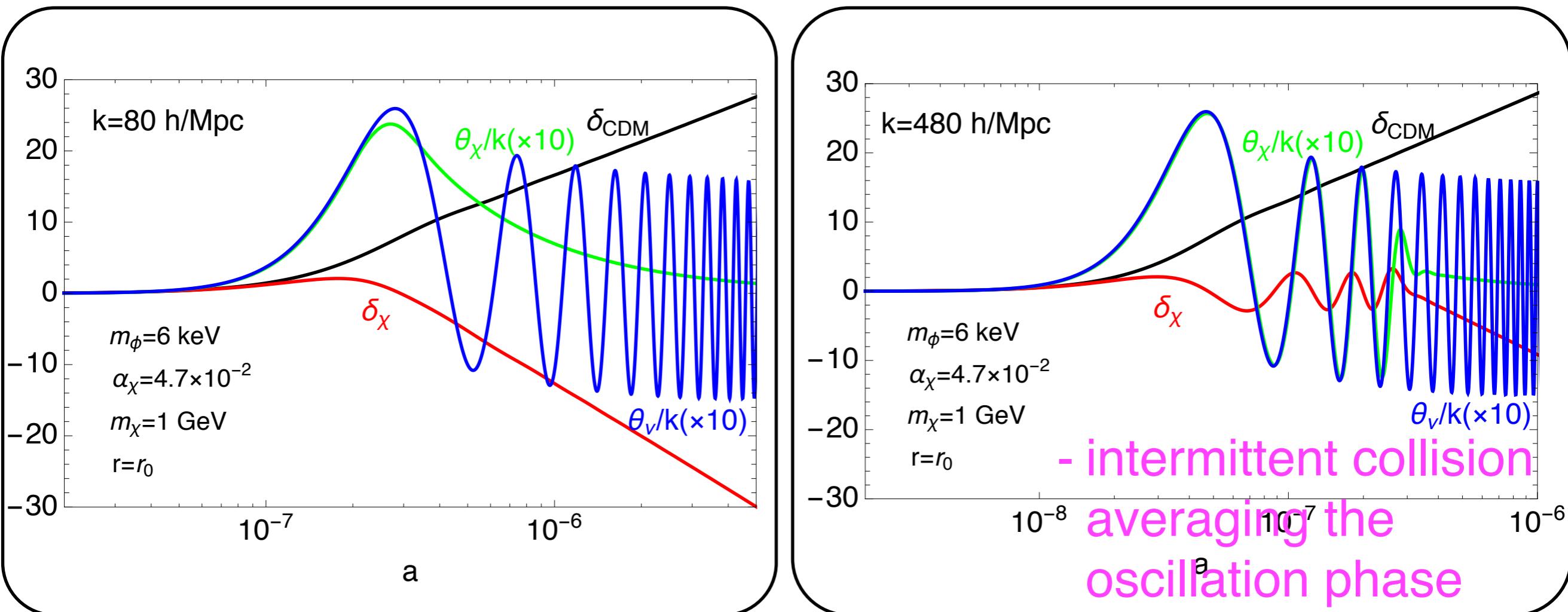
Extension with fudge factors for $k \gg k_{\text{kd}}$

[AK and Takahashi, JCAP, 2018](#)

$$\frac{\delta_{\chi^0}^2}{\delta_{\text{cdm}}^2} \approx c_{\mathcal{N}} \frac{4\pi}{n} \exp\left(-\frac{k}{k_{\text{damp}}}\right) \left(\frac{k}{2\sqrt{3}k_{\text{kd}}}\right)^3 \sin^2\left(\frac{k}{\sqrt{3}k_{\text{kd}}}\right)$$

$$k_{\text{damp}} = c_{\text{damp}} \frac{n}{\pi} \sqrt{3} k_{\text{kd}}, \quad \begin{array}{l} n \\ \text{- damping} \end{array} \quad \begin{array}{l} - \text{enhancement} \end{array} \quad k_{\text{kd}} = \frac{c_{\text{kd}}}{\tau_{\text{kd}}}$$

Evolution of adiabatic perturbation



Free-streaming

Dark matter thermal motion is neglected

- pressure, sound speed, ...

Higher multipoles in the Boltzmann hierarchy are truncated

- anisotropic inertia, entropy perturbation, ...

Free-streaming is taken into account as $\delta_\chi \rightarrow \delta_\chi \times \exp\left(-\frac{k^2}{2k_{\text{fs}}(\tau)^2}\right)$

$$k_{\text{fs}}^{-1} = \sqrt{\frac{6T_{\text{kd}}}{5m_{\chi^0}}} \int_{\tau_*}^{\tau} \frac{d\tau'}{a(\tau')/a_{\text{kd}}} \approx \sqrt{\frac{6T_{\text{kd}}}{5m_{\chi^0}}} \tau_{\text{kd}} \ln\left(\frac{\tau_{\text{eq}}}{\tau_*}\right), \quad \tau_* = 1.05\tau_{\text{kd}}$$

Bertschinger, PRD, 2006

- long after the matter radiation equality

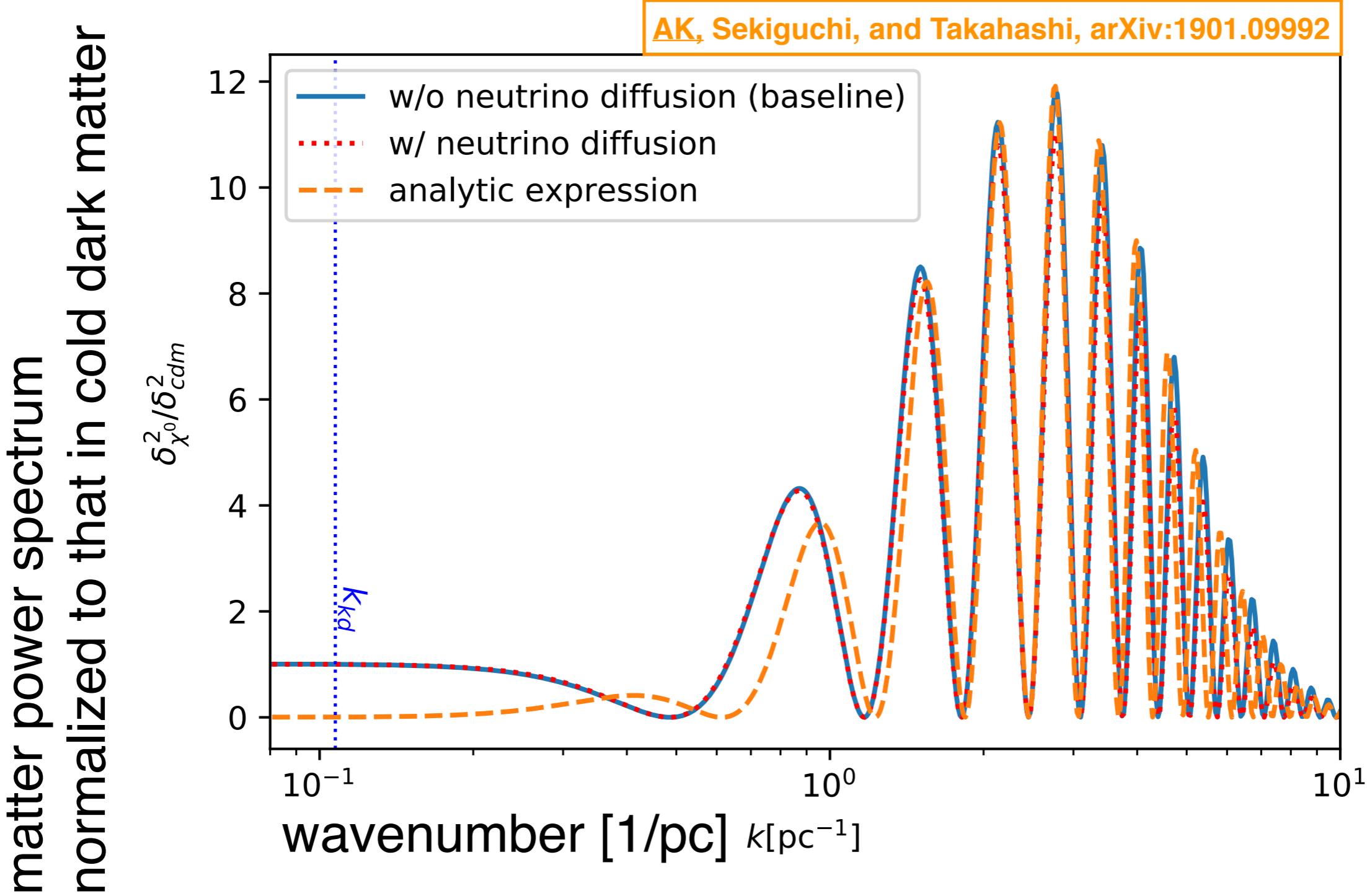
$$k_{\text{fs}} \simeq 3.5/\text{pc} > 1/\tau_{\text{kd}} \simeq 0.11/\text{pc}$$

$$M_{\text{kd}} = \frac{4\pi}{3} \rho_{\chi,0} \tau_{\text{kd}}^3$$

$$M_{\text{fs}} \simeq 1.0 \times 10^{-7} M_\odot < M_{\text{kd}} \simeq 1.1 \times 10^{-4} M_\odot$$

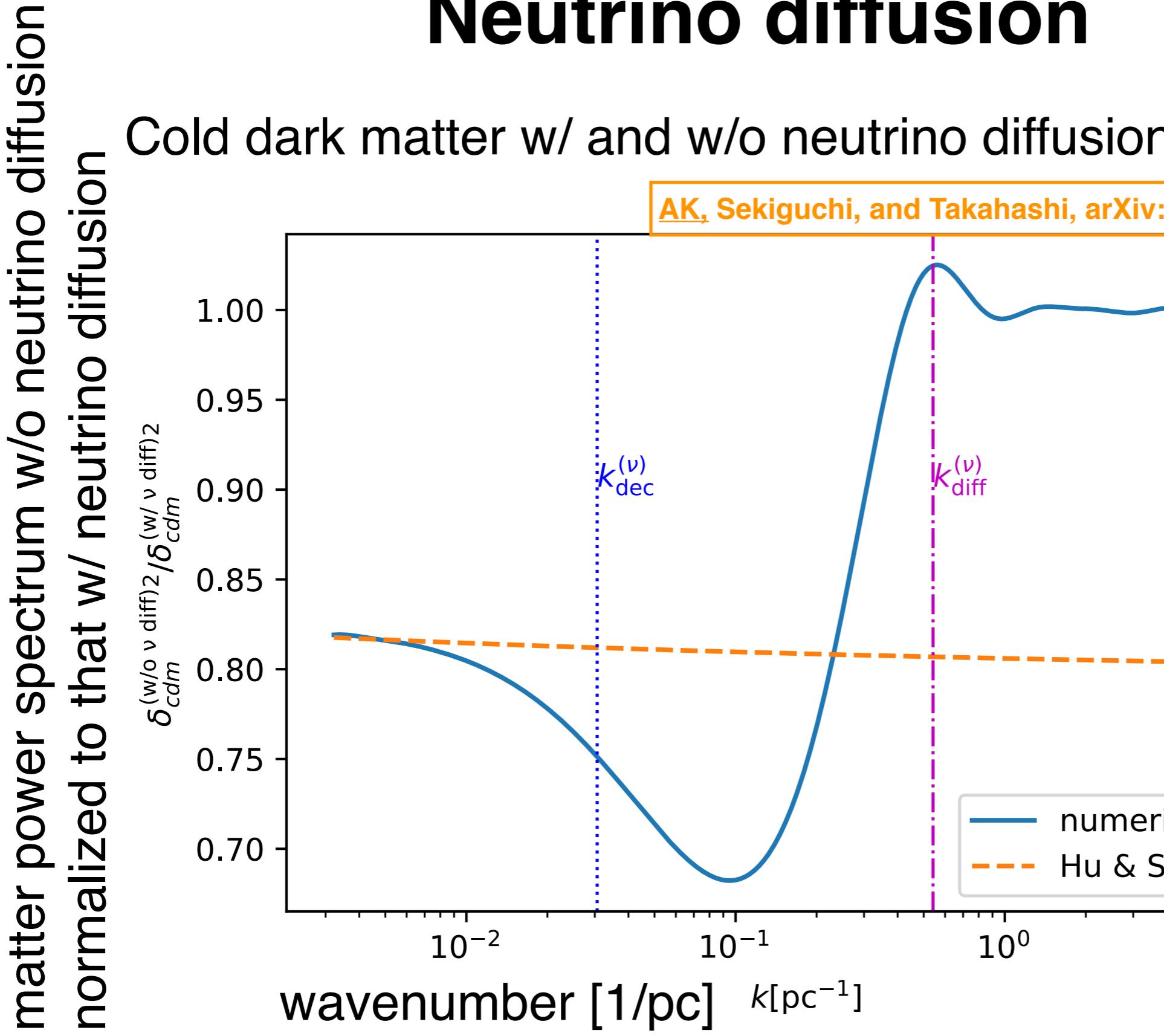
$$M_{\text{fs}} = \frac{4\pi}{3} \rho_{\chi,0} \left(\frac{\pi}{k_{\text{fs}}}\right)^3$$

Neutrino diffusion



Neutrino diffusion is not important for the ratio $\delta_{\chi^0}^2 / \delta_{\text{cdm}}^2$

Neutrino diffusion



Neutrino diffusion changes the power spectrum up to 30%

Halo profile

Navarro-Frenk-White (NFW) profile: $\rho = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2}$

$$(\rho_s, r_s) \leftrightarrow (c = r_{200}/r_s, M = M_{200}) \rightarrow \bar{L} = Mc^3/f(c)^2$$

Navarro, Frenk, and White, ApJ, 1996
Navarro, Frenk, and White, ApJ, 1997

$$f(c) = \ln(1 + c) - c/(1 + c)$$

- normalization does not matter

c - M relation

- case 1: power law - more sensitive to the smallest halos

$$c_{200} = 7.80 \left(\frac{M_{200}}{10^{12} M_\odot/h} \right)^{-0.08} \left[1 + 0.2 \left(\frac{M_{200}}{10^{15} M_\odot/h} \right)^{1/2} \right]$$

Gao, Frenk, Jenkins, Springel, and White, MNRAS, 2012

- case 2: flattening toward smaller halos

Diemand, Moore, and Stadel, Nature, 2005

$$c_{200} = \sum_{i=0}^5 c_i \left[\ln \left(\frac{M_{200}}{M_\odot/h} \right) \right]^i$$

...

Sanchez-Conde and Prada, MNRAS, 2012

$$c_i = \{37.5153, -1.5093, 1.636 \times 10^{-2}, \\ 3.66 \times 10^{-4}, -2.89237 \times 10^{-5}, 5.32 \times 10^{-7}\}$$

Subhalo mass function

Cold dark matter subhalo mass function:

$$\frac{dn_{\text{sub}}}{dm} = \frac{A}{M} \left(\frac{m}{M} \right)^{-\alpha}, \quad A : \int_{10^{-5}M}^{10^{-2}M} dm m \frac{dn_{\text{sub}}}{dm} = 0.1$$

$$(\alpha, A) = (1.9, 0.0318)$$

Diemand, Kuhlen, and Madau, ApJ, 2007

Madau, Diemand, and Kuhlen, ApJ, 2008

Springel, Wang, Vogelsberger, Ludlow, Jenkins, Helmi, Navarro, Frenk, and White, MNRAS, 2008

(2.0, 0.0145) - more sensitive to the smallest halos

Wino subhalo mass function:

$$\frac{dn_{\text{sub}}}{dm} \rightarrow \frac{dn_{\text{sub}}}{dm} \times \frac{(dn/d \ln M)_\chi}{(dn/d \ln M)_{\text{cdm}}} \Big|_{\text{PS}} \quad \text{and } m_{\min} = 0$$

(for comparison, $\frac{dn_{\text{sub}}}{dm}$ as it is and $m_{\min} = M_{\text{kd}} \simeq 1.1 \times 10^{-4} M_\odot$)

Subhalo mass function

Modified Press-Schechter: $\frac{dn}{d \ln M} = \frac{\rho_{\chi,0}}{M} f(\nu) \frac{d \ln \nu}{d \ln M}$

$$f(\nu) = A \sqrt{\frac{2q\nu^2}{\pi}} \left(1 + (q\nu^2)^{-p}\right) \exp\left(-\frac{q\nu^2}{2}\right), \quad \nu = \frac{\delta_c}{D(z)\sigma(M)}$$

- growth factor
 $D(0) = 1$

Ellipsoidal collapse: $A = 0.3222$, $p = 0.3$, $q = 1$

Sheth and Tormen, MNRAS, 1999

Leo, Baugh, Li, and Pascoli, JCAP, 2018

Smooth- k filter: $\sigma^2(M) = \int_0^\infty d \ln k \frac{k^3}{2\pi^2} P(k) W^2(k; M)$

$$W(k; M) = (1 + (kR)^{\hat{\beta}})^{-1}, \quad M = \frac{4\pi}{3} \rho_{m,0} (\hat{c}R)^3, \quad \hat{\beta} = 4.8, \quad \hat{c} = 3.30$$

- match to simulation results for matter power spectrum with dark acoustic oscillation

Subhalo mass function

Modified Press-Schechter: $\frac{dn}{d \ln M} = \frac{\rho_{\chi,0}}{M} f(\nu) \frac{d \ln \nu}{d \ln M}$

$$f(\nu) = A \sqrt{\frac{2q\nu^2}{\pi}} \left(1 + (q\nu^2)^{-p}\right) \exp\left(-\frac{q\nu^2}{2}\right), \quad \nu = \frac{\delta_c}{D(z)\sigma(M)}$$

Ellipsoidal collapse: $A = 0.3222$, $p = 0.3$, $q = 0.707$ - growth factor
 $D(0) = 1$

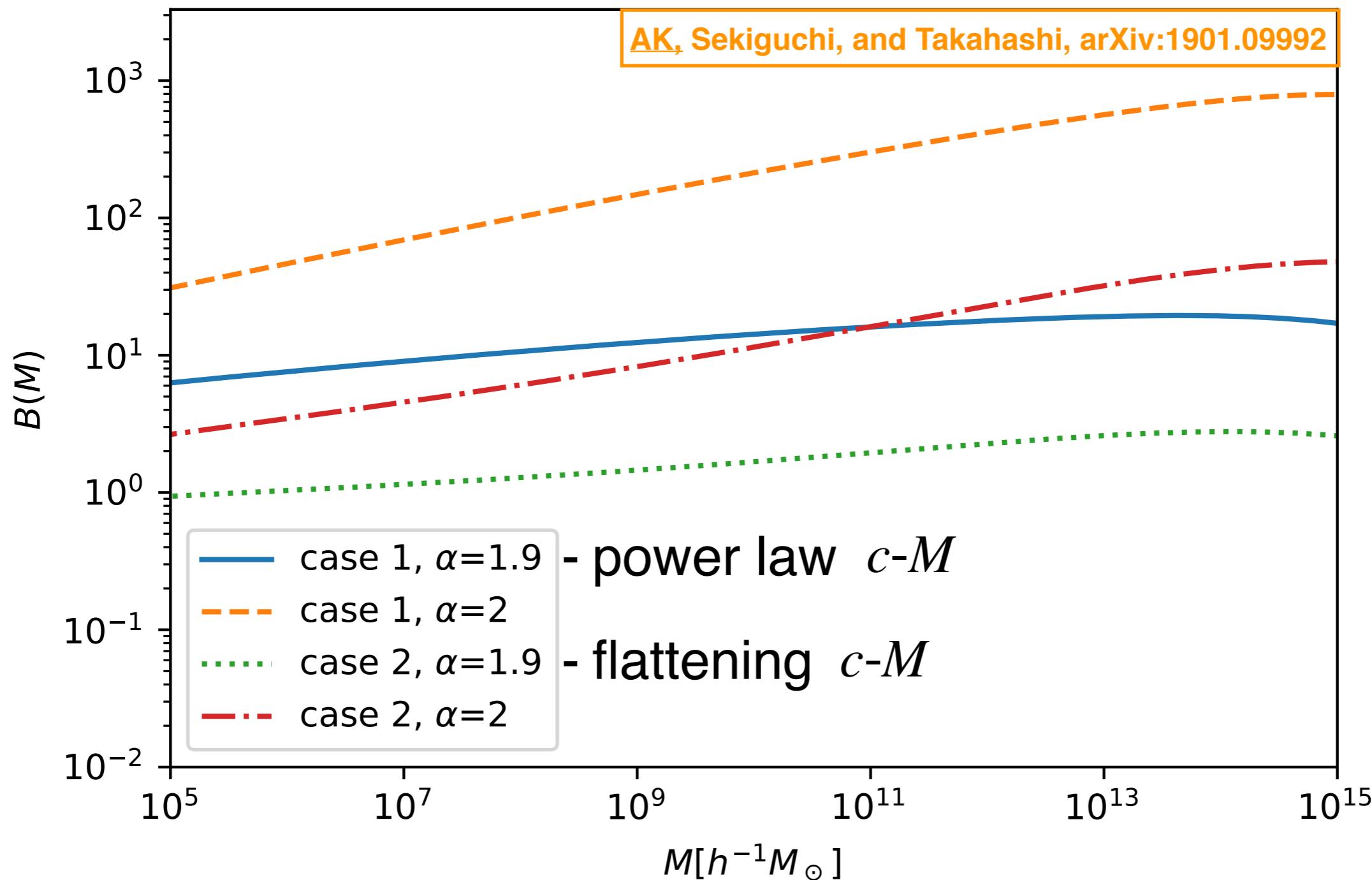
Sheth and Tormen, MNRAS, 1999

(Real-space) top-hat filter: $\sigma^2(M) = \int_0^\infty d \ln k \frac{k^3}{2\pi^2} P(k) W^2(k; M)$

$$W(k; M) = \frac{3(\sin(kR) - kR \cos(kR))}{(kR)^3}, \quad M = \frac{4\pi}{3} \rho_{m,0} R^3$$

Estimated boost factor

Without B_{sub}



Estimated boost factor

Smooth- k filter:

Enhanced by a factor of 4.1 and 8.8 (1.5 and 2.9)
with $\alpha = 1.9$ and 2.0 in case 1 (2) when compared to $m_{\min} = M_{\text{kd}}$

(Real-space) top-hat filter:

5.4 and 12.5 (1.7 and 3.5)

Without B_{sub}

Smooth- k filter:

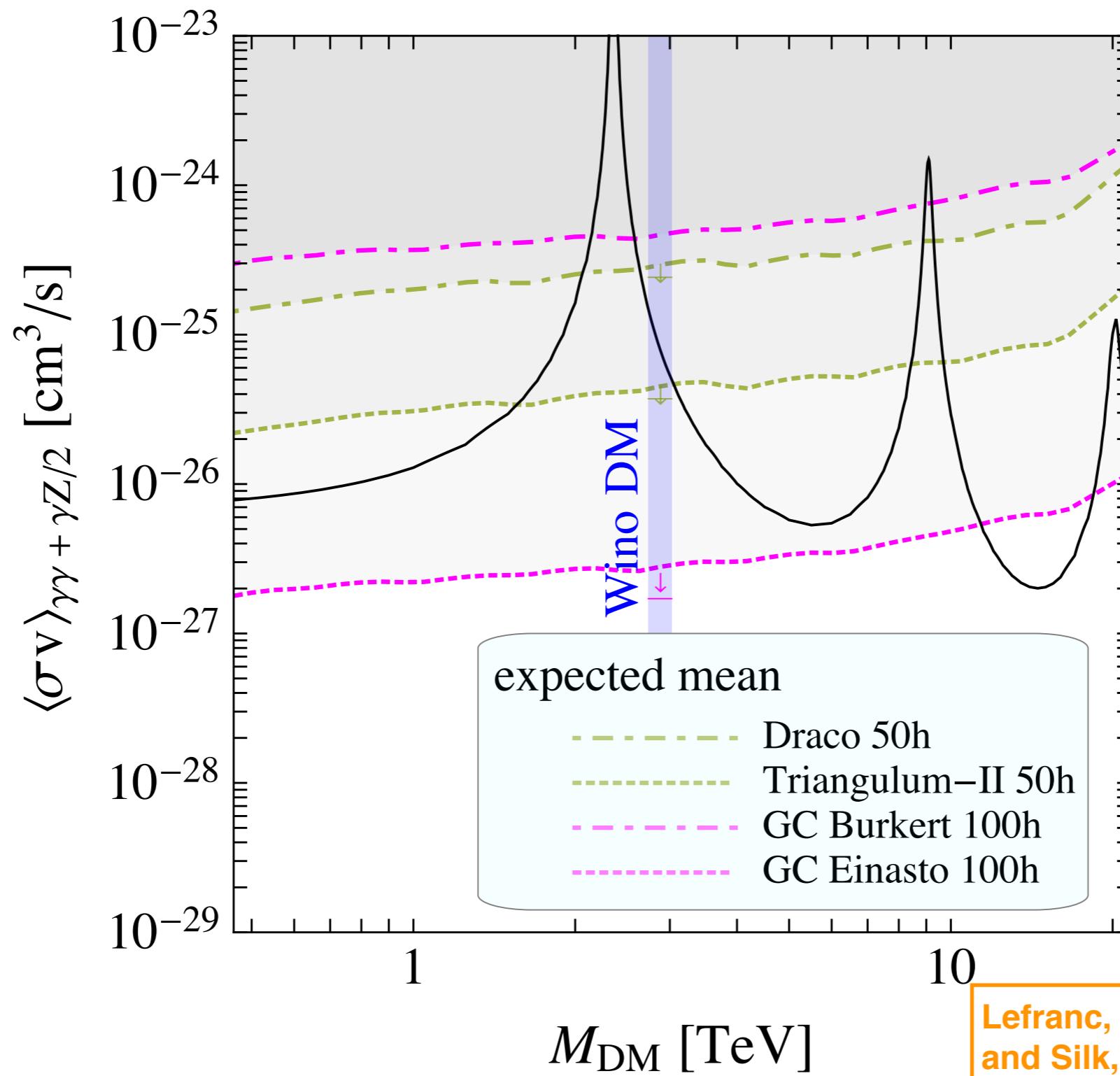
2.8 and 7.5 (1.2 and 2.5)

(Real-space) top-hat filter:

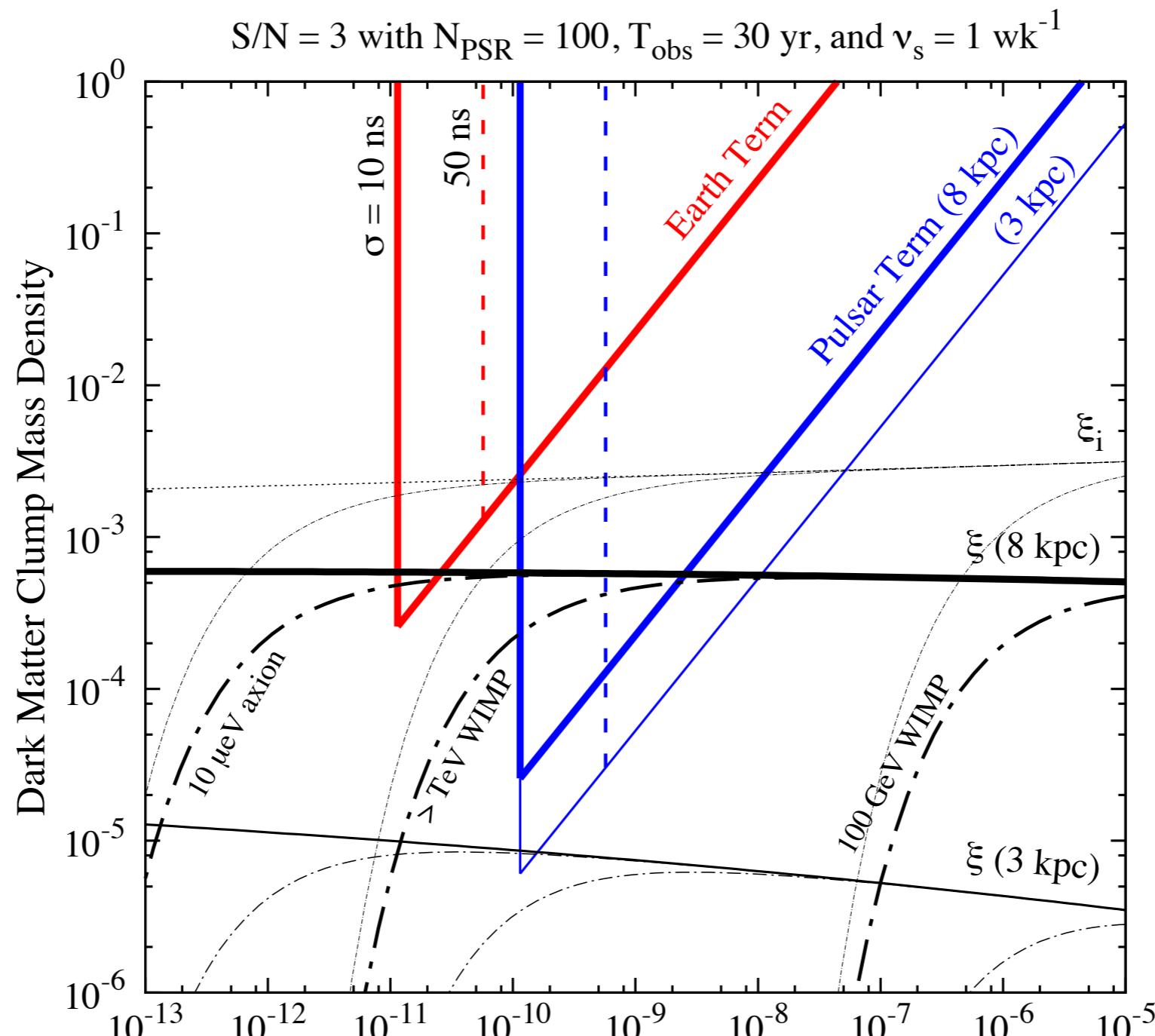
3.2 and 10.3 (1.2 and 2.7)

Indirect detection

CTA sensitivities



Detectability of small-size clump



Kashiyama and Oguri, 1801.07847

Dark Matter Clump Mass [M_\odot]

$M_{\text{fs}} \sim 10^{-7} M_\odot$

Detection of dark matter clump encounter with the Earth or a pulsar in pulsar timing array data

Constraints from galaxy clusters

$V_{\text{max}} \sim 1000 \text{ km/s}$
 $\leftrightarrow \text{galaxy: } V_{\text{max}} \sim 100 \text{ km/s}$

Halo shape - ellipticity

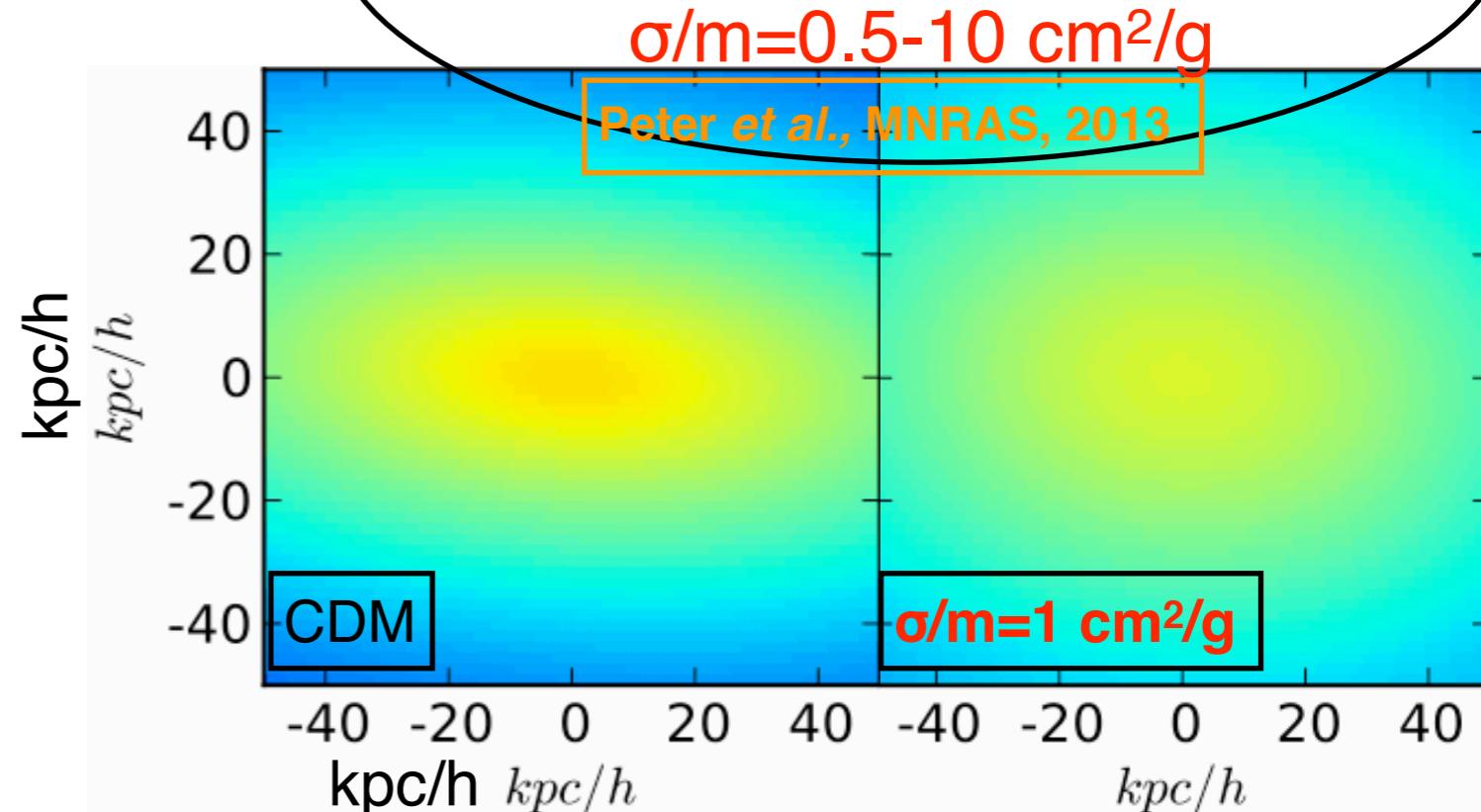
- galaxy cluster MS 2137-23
 $(e=0.18 @ r=70 \text{ kpc})$
(estimate) $\sigma/m < 0.02 \text{ cm}^2/\text{g}$

Miralda-Escudé *et al.*, ApJ, 2002

(simulation/l.o.s. effect)

$\sigma/m < 1 \text{ cm}^2/\text{g}$

Peter *et al.*, MNRAS, 2013



Bullet cluster - transparency

- 1E0657-558

(offset) $\sigma/m < 1.25 \text{ cm}^2/\text{g}$

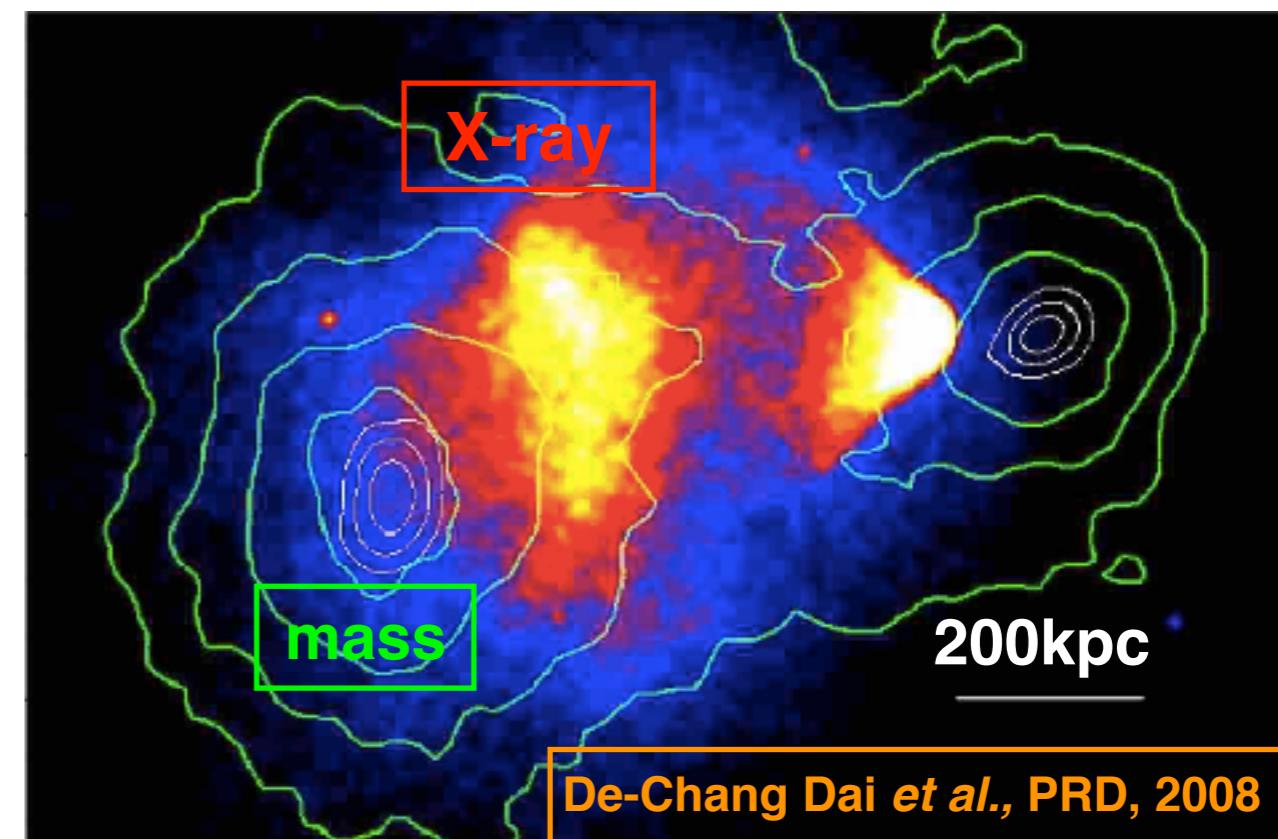
(massloss) $\sigma/m < 0.7 \text{ cm}^2/\text{g}$

Randall *et al.*, ApJ, 2008

- an ensemble (72)

(offset) $\sigma/m < 0.47 \text{ cm}^2/\text{g}$

Harvey *et al.*, Science, 2015



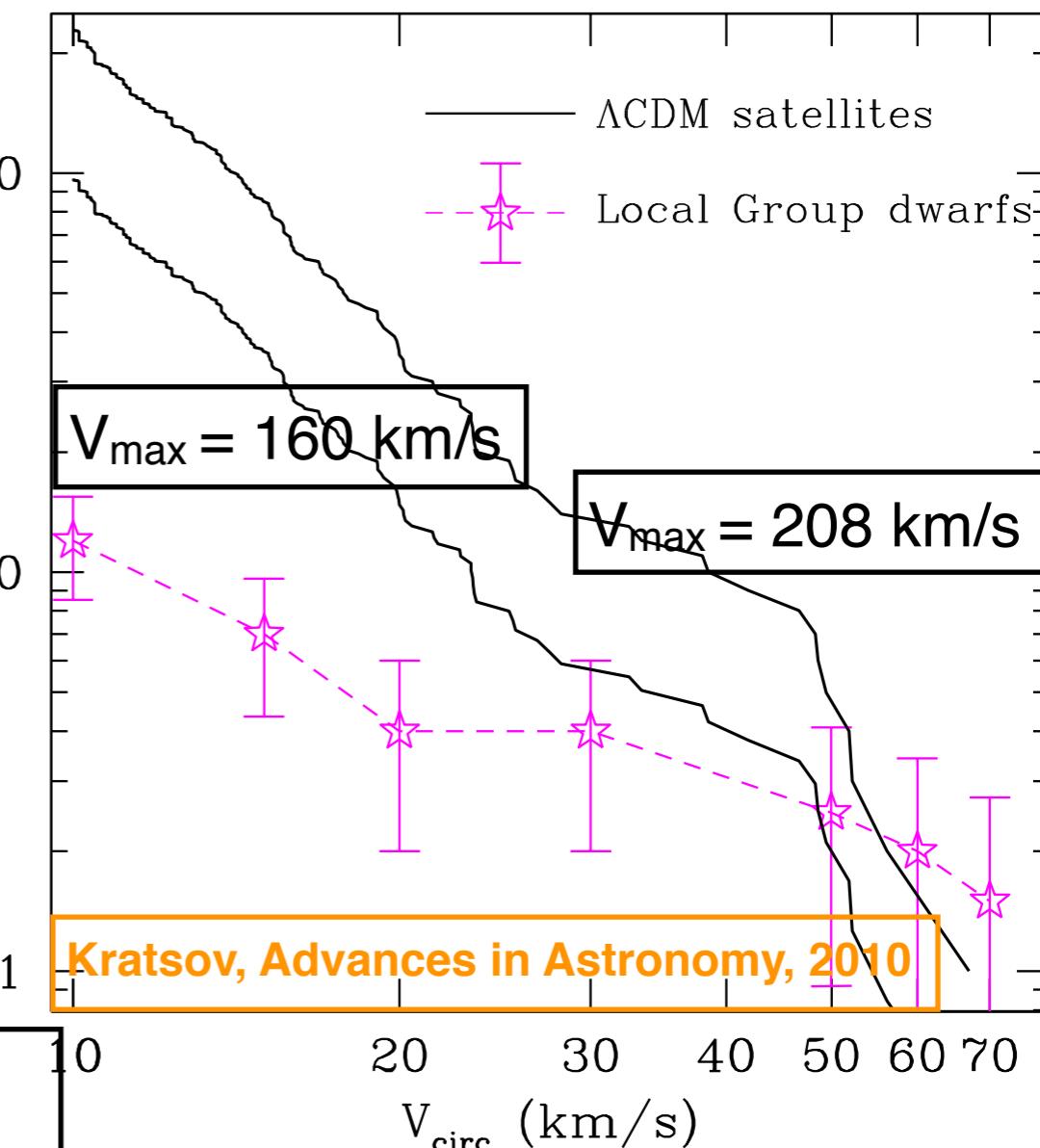
Small scale crisis I

When N -body simulations in the Λ CDM model and observations are compared, problems appear at (sub-)galactic scales: **small scale crisis**

missing satellite problem

N -body (DM-only) simulations in the Λ CDM model → Milky Way-size halos host $O(10)$ times larger number of subhalos than that of observed dwarf spheroidal galaxies

cumulative number of subhalos
 $N(>V_{\text{circ}})$



Kratsov, Advances in Astronomy, 2010

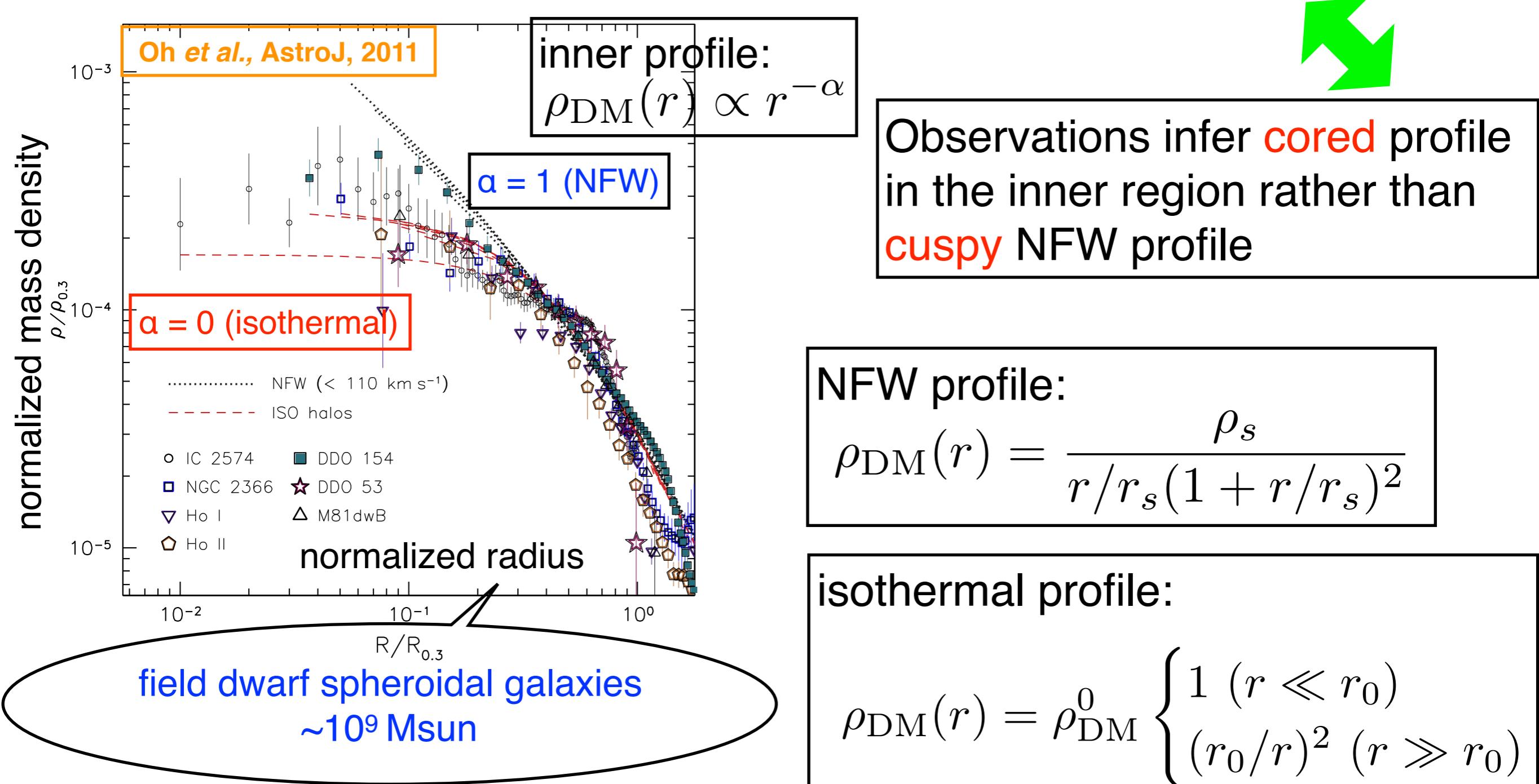
(maximum) circular velocity

$$V_{\text{circ}}^2(r) = \frac{GM(< r)}{r} \quad V_{\text{max}} = \max_r \{V_{\text{circ}}(r)\}$$

Small scale crisis II

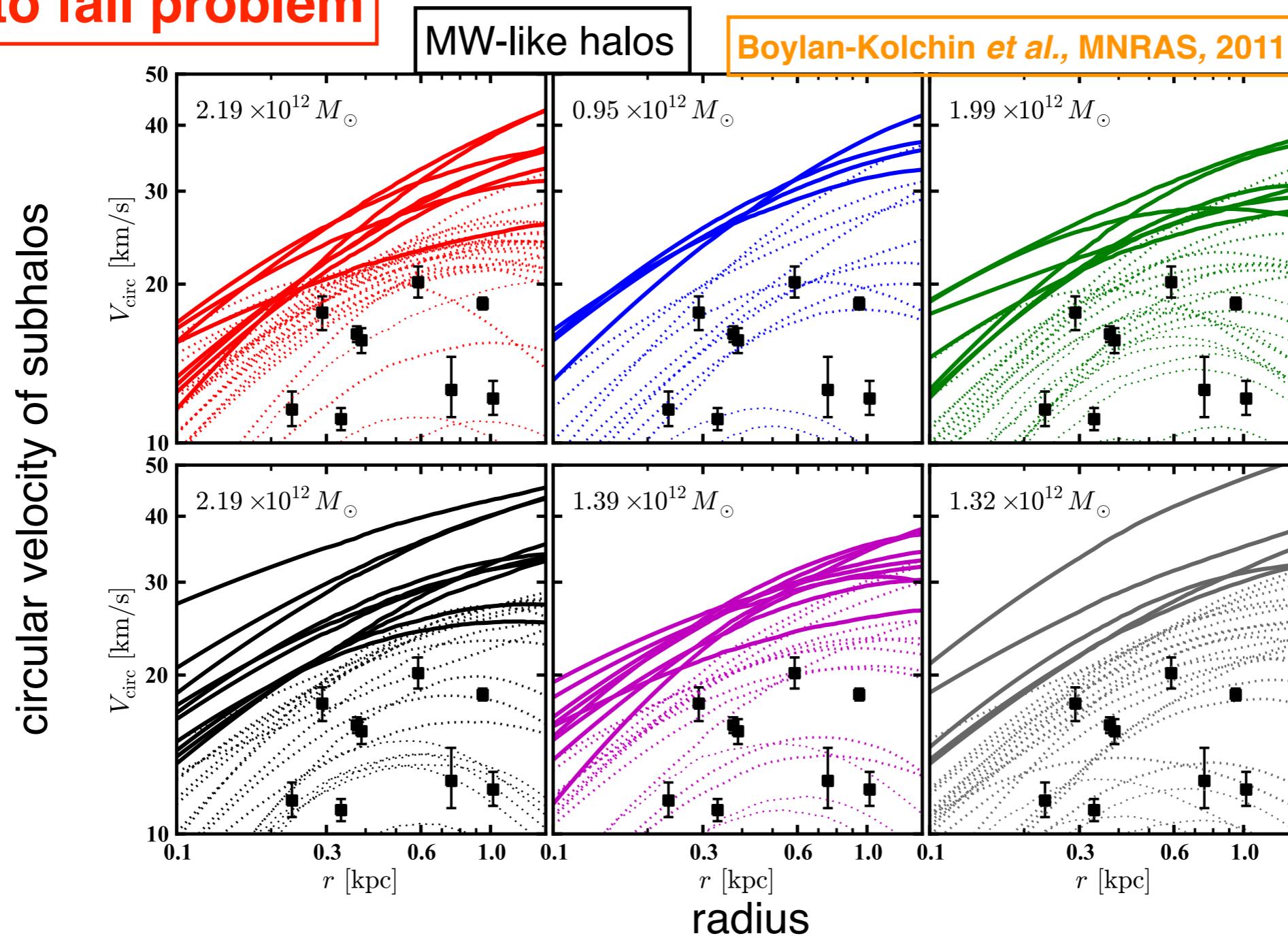
cusp vs core problem

N-body (DM-only) simulations in the Λ CDM model → common DM profile independent of halo size: **NFW profile**



Small scale crisis III

too big to fail problem



N -body (DM-only) simulations in Λ CDM model →
~10 subhalos with deepest potential wells in Milky Way-size halos
do not host observed counterparts (dwarf spheroidal galaxies)

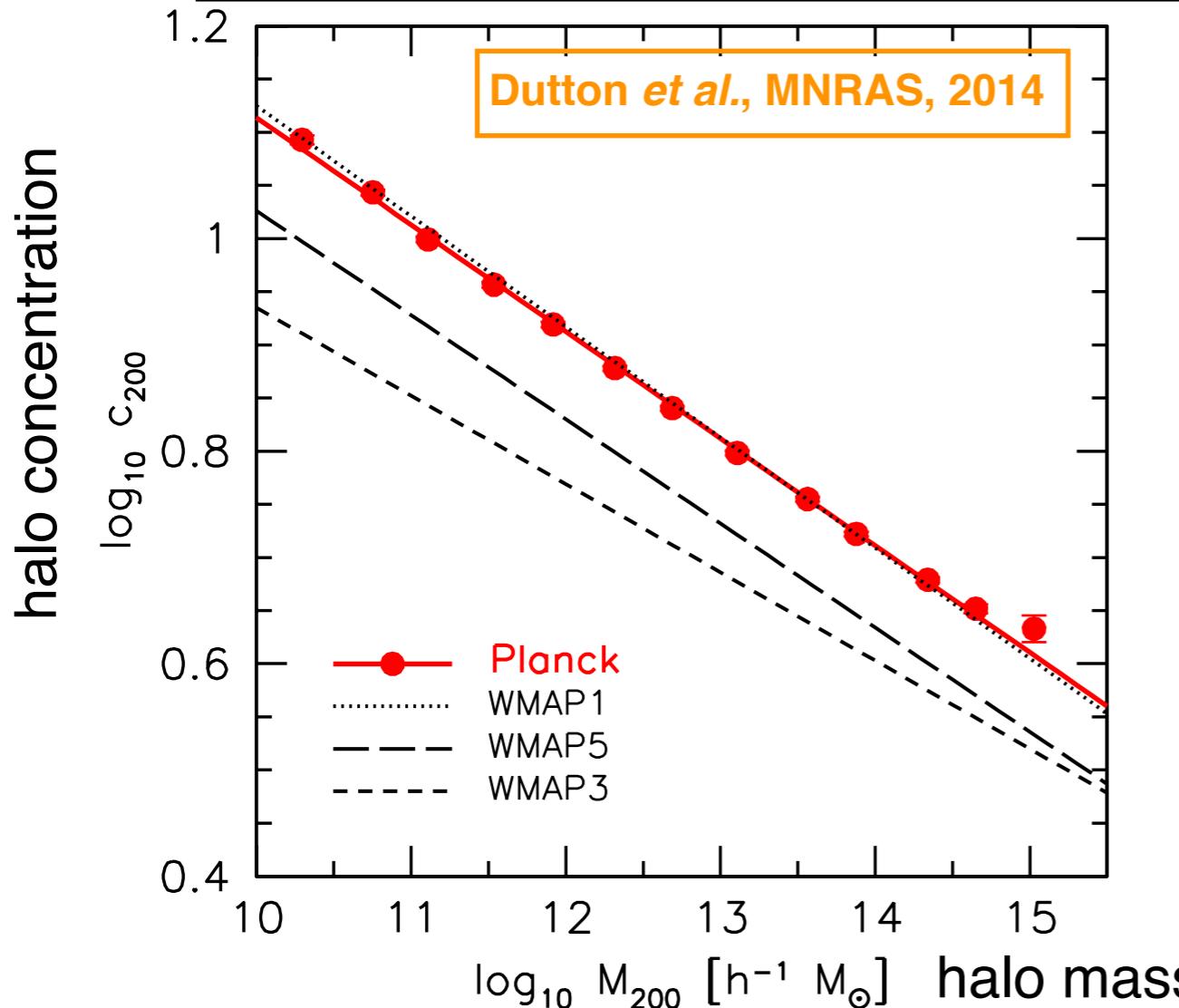
Concentration-mass relation

Why is a simulated rotation curve (almost) **DEFINITE** for a given V_{\max} ?
 Two parameters for the NFW profile

$$\rho_{\text{DM}}(r) = \frac{\rho_s}{r/r_s(1+r/r_s)^2}$$

A relation between two parameters usually given as
 the **CONCENTRATION-MASS RELATION**

$$c_{200} = 10^{0.905 \pm 0.11} (M_{200}/10^{12} h^{-1} M_{\odot})^{-0.101}$$



small
intrinsic scatter

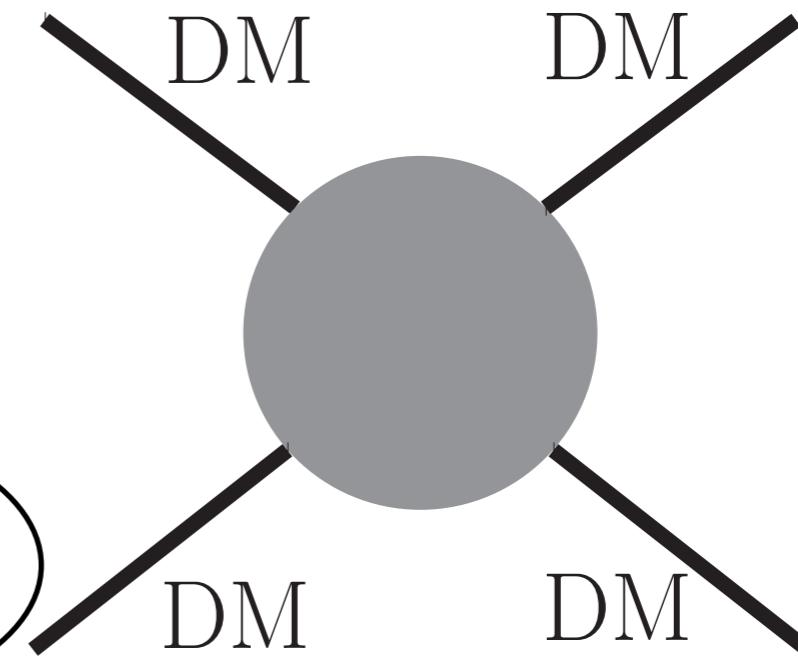
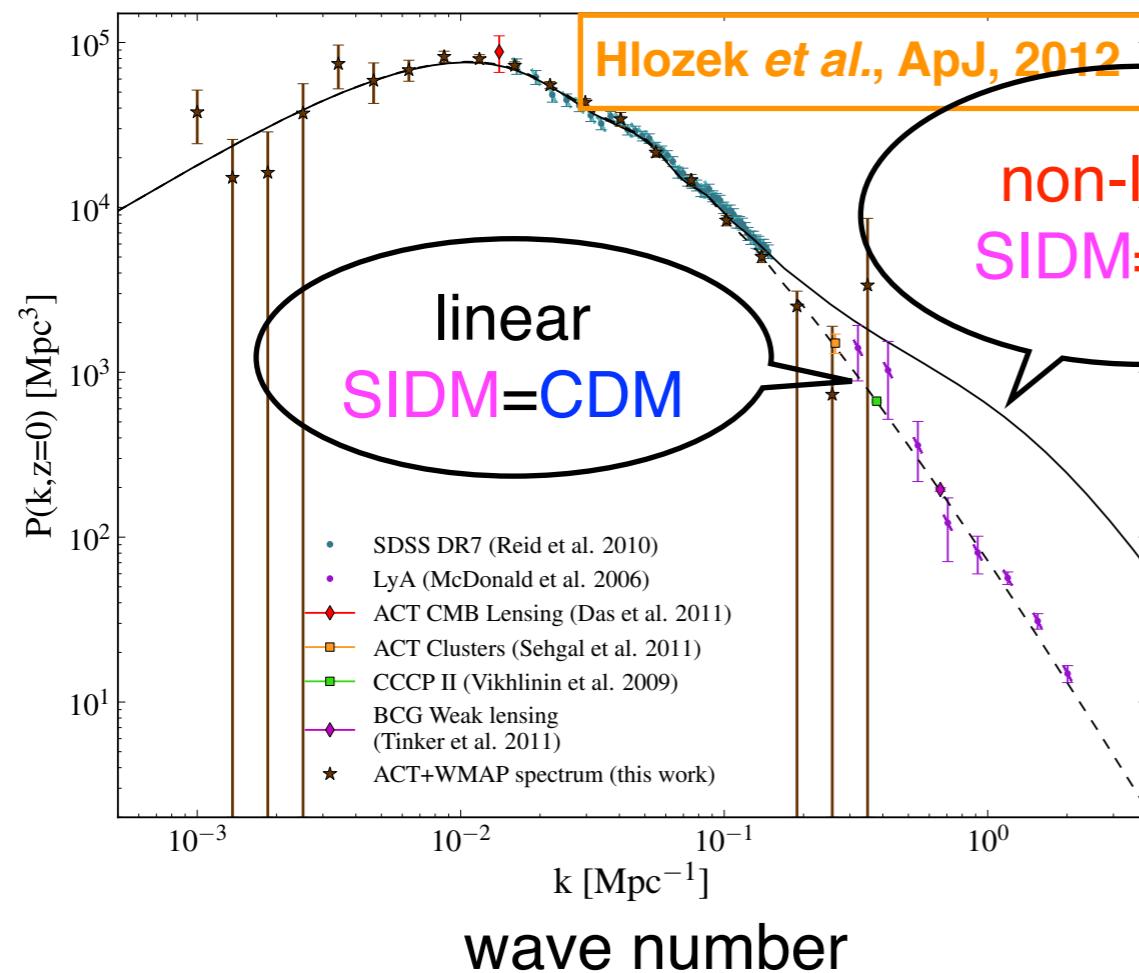
$$c_{200} = r_{200}/r_s$$

$$M_{200}(< r_{200}) = \frac{4\pi}{3} \bar{\rho}_{\text{M}} r_{200}^3$$

Dark matter self-interaction

Self-Interacting Dark Matter: SIDM

power spectrum of density perturbations



Reaction rate $\Gamma = \sigma v p / m$
 σ : cross section
 v : relative velocity
 p : dark matter mass density
 m : dark matter mass

SIDM structure formation starts with the same linear (initial) matter power spectra as CDM, but self-interactions become important as structure formation proceeds $\leftrightarrow p$ increases

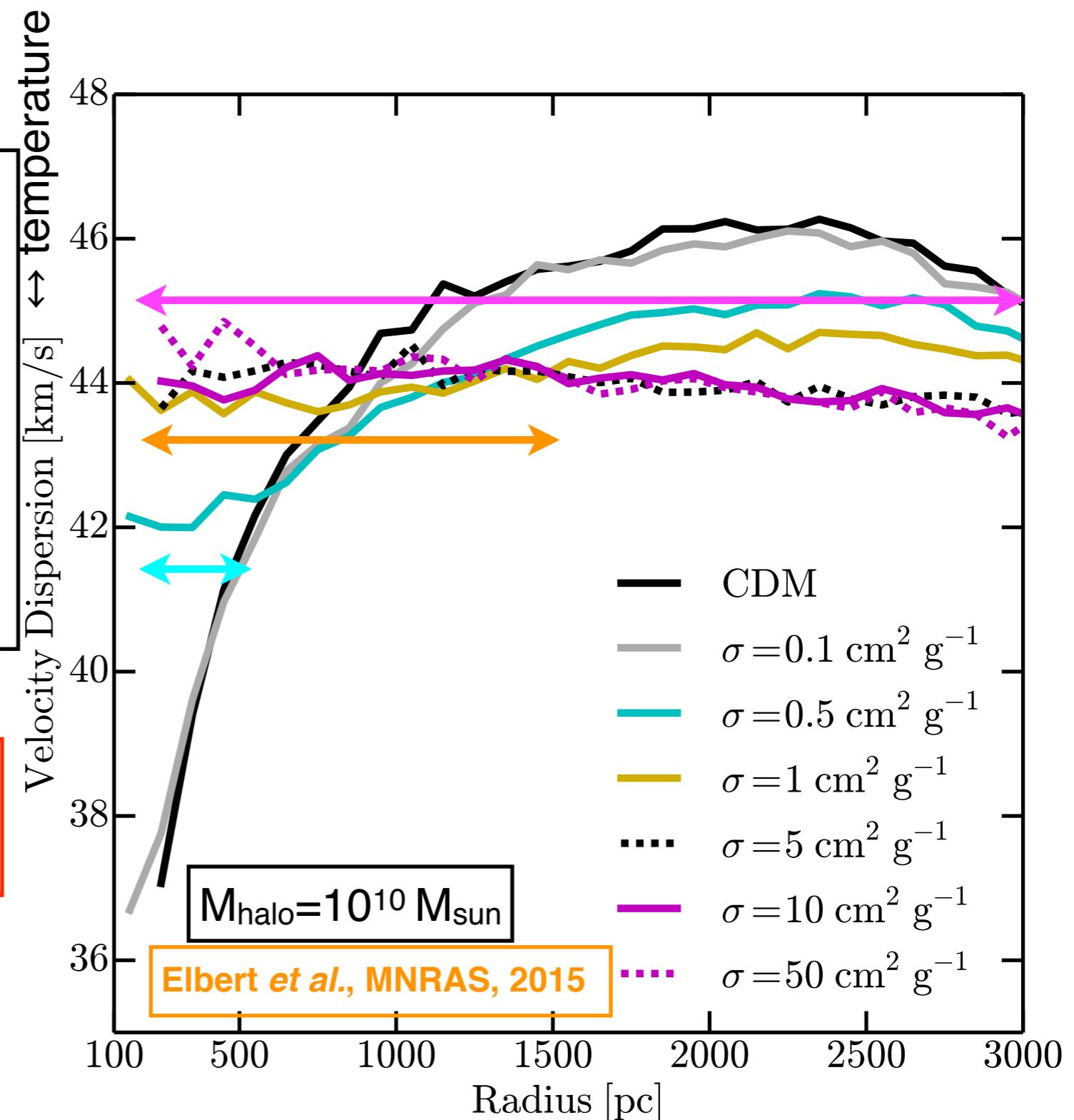
SIDM halo - velocity dispersion

SIDM-only simulation

SIDM halos are **THERMALIZED** (isothermal) in inner region $r < r_1$, where the self-scattering is efficient $\sigma v p(r_1) t_{\text{age}} / m = 1$
 $t_{\text{age}} = 5 \text{ Gyr} (\text{galaxy cluster})$
 $10 \text{ Gyr} (\text{galaxy})$

If $r_1 > r_{\max}$, the gravo-thermo instability is significant

$$V_{\text{circ}}(r_{\max}) = V_{\max}$$

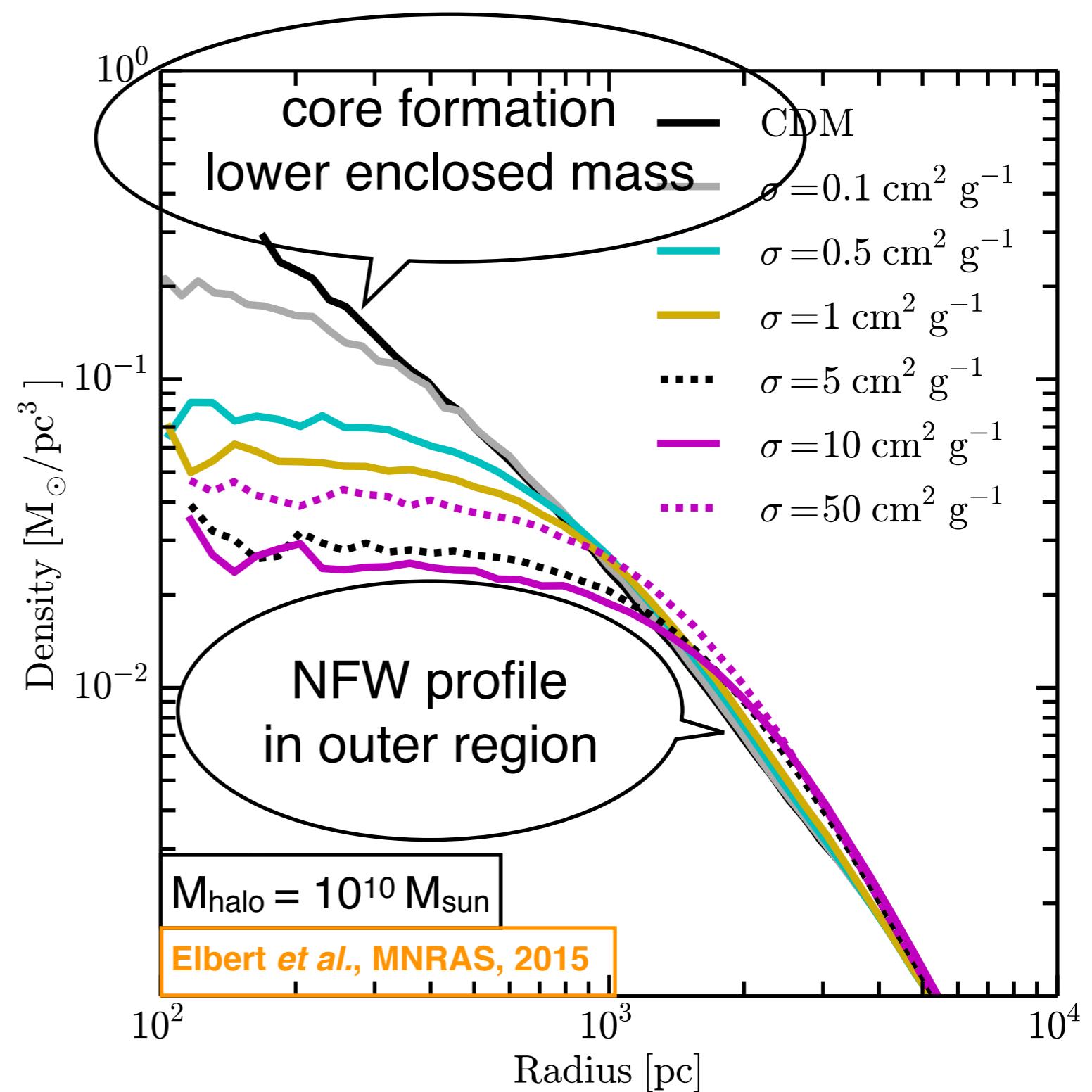
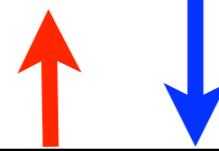


SIDM halo - mass density

SIDM-only simulation

As σ/m increases,
central density decreases

Inverted at some point
 ← gravo-thermo instability
 ↔ core-collapse

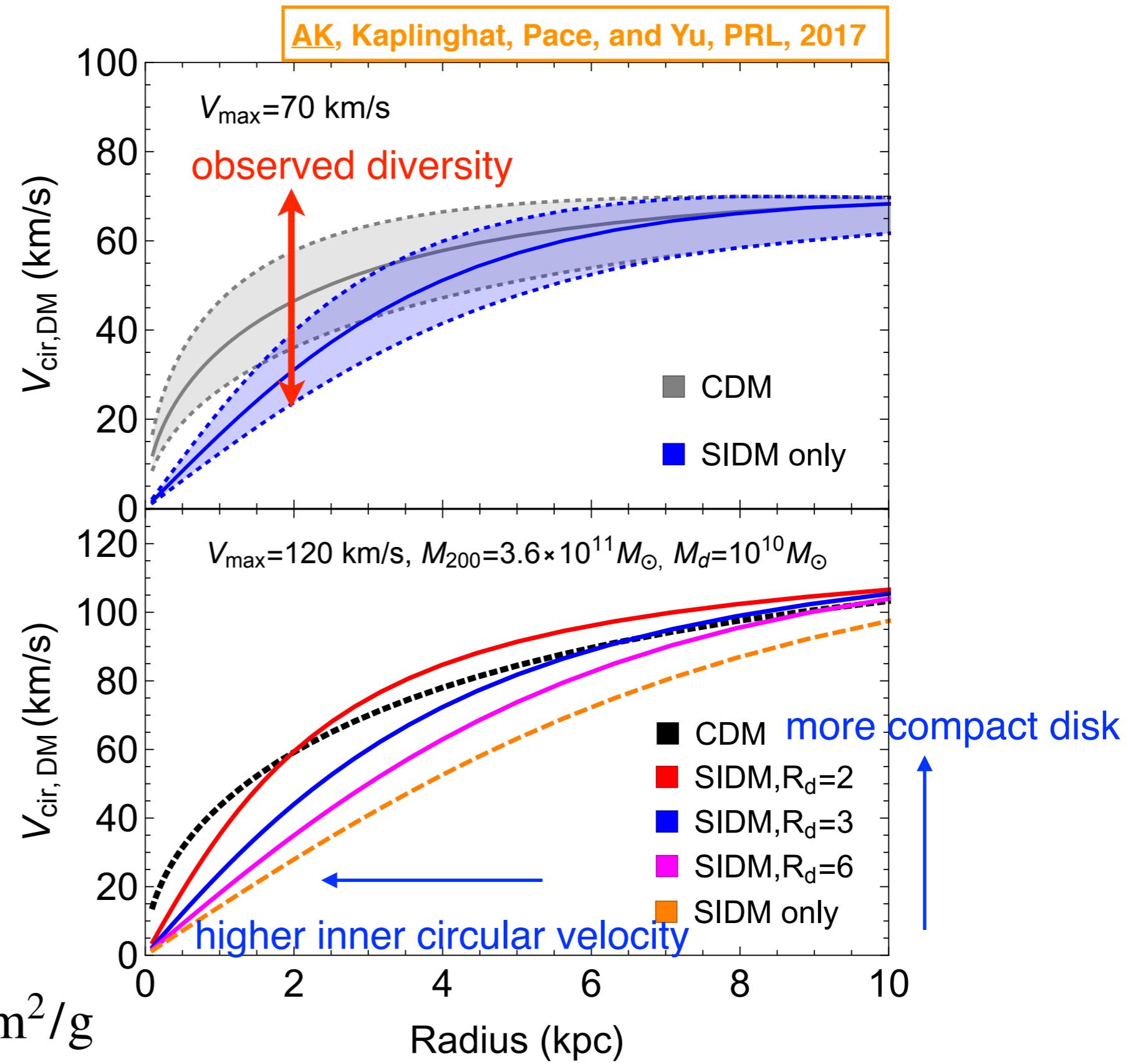


$\sigma/m = 0.5\text{-}5 \text{ cm}^2/\text{g}$ may solve the inner mass deficit problem

Demonstration with stellar disks

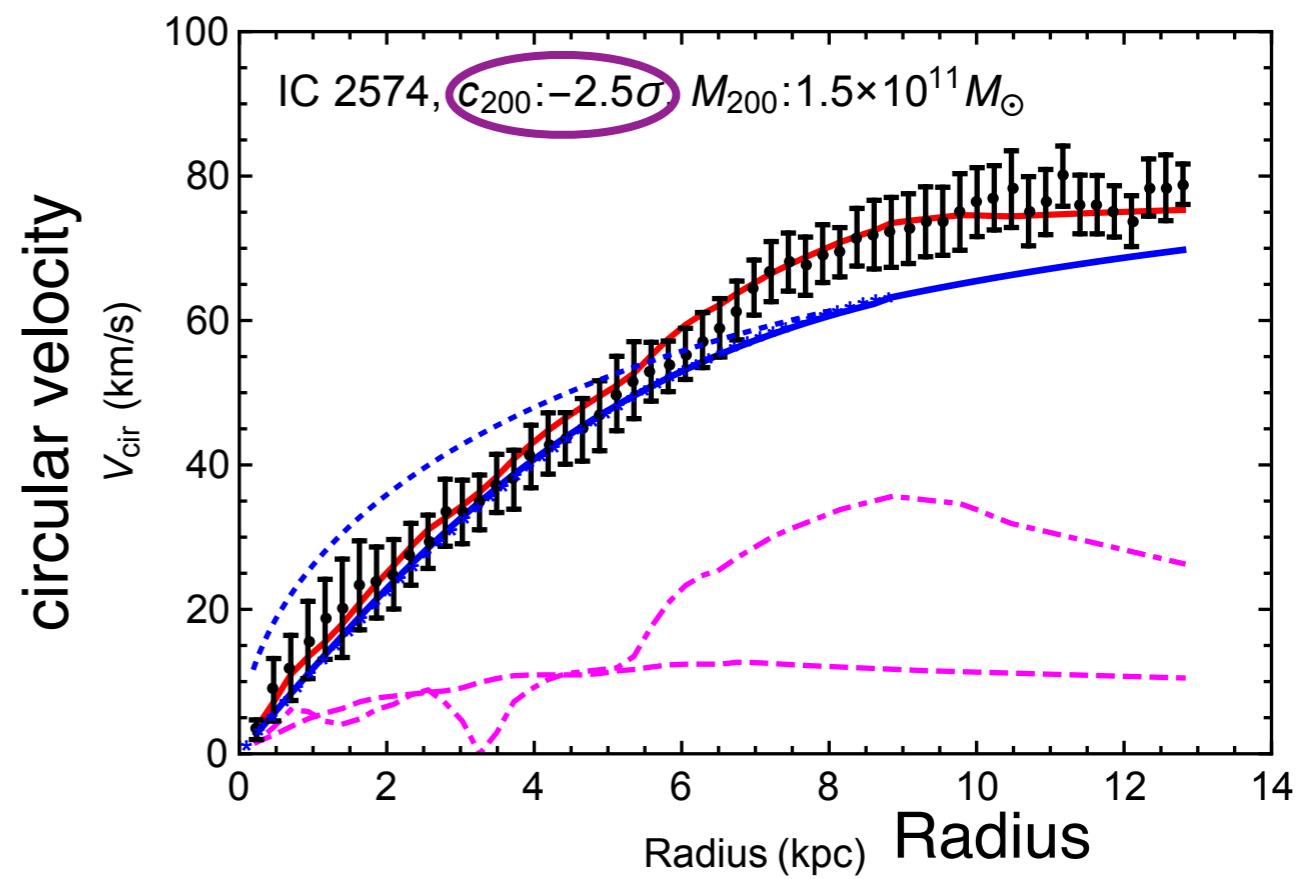
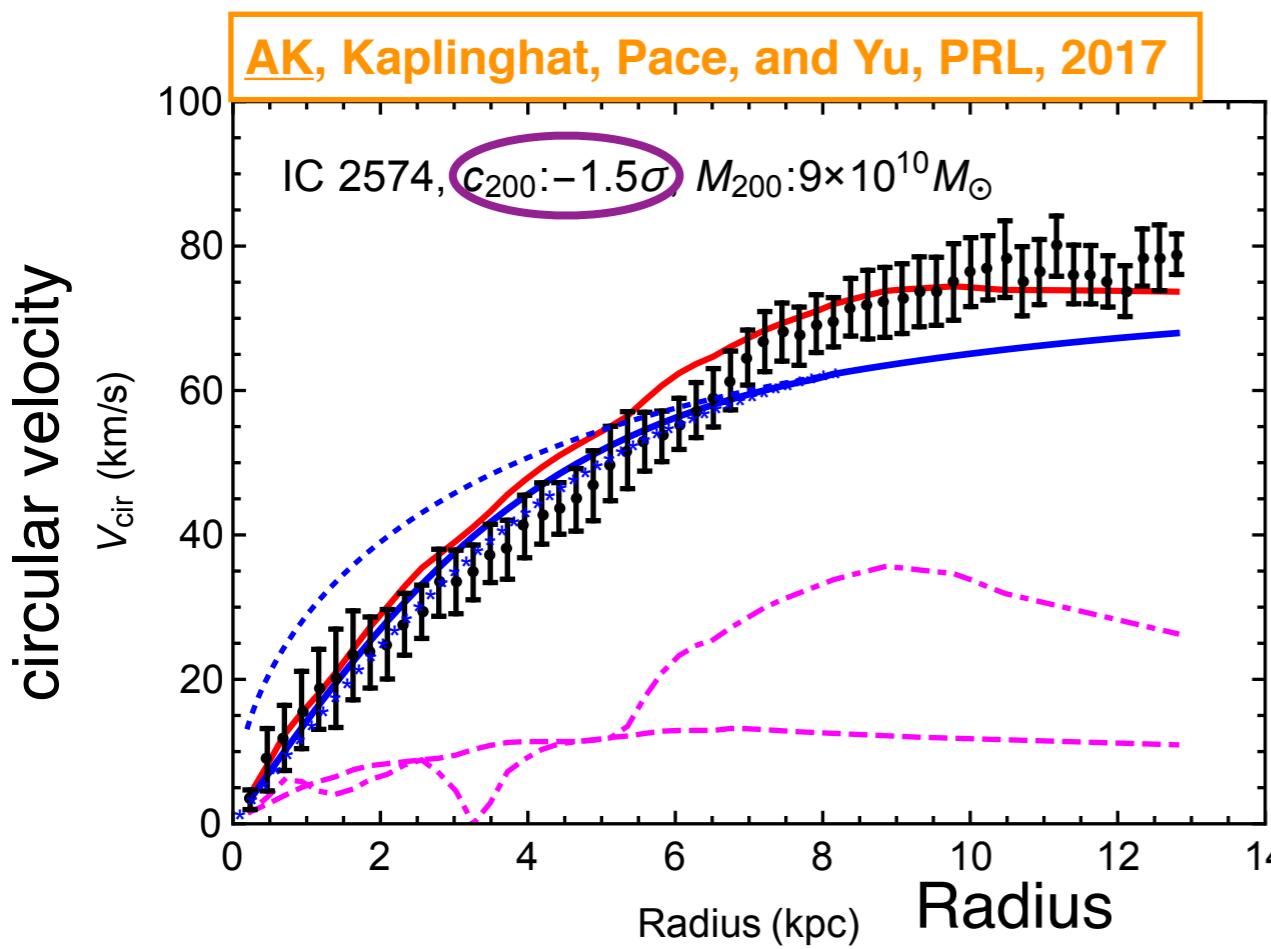
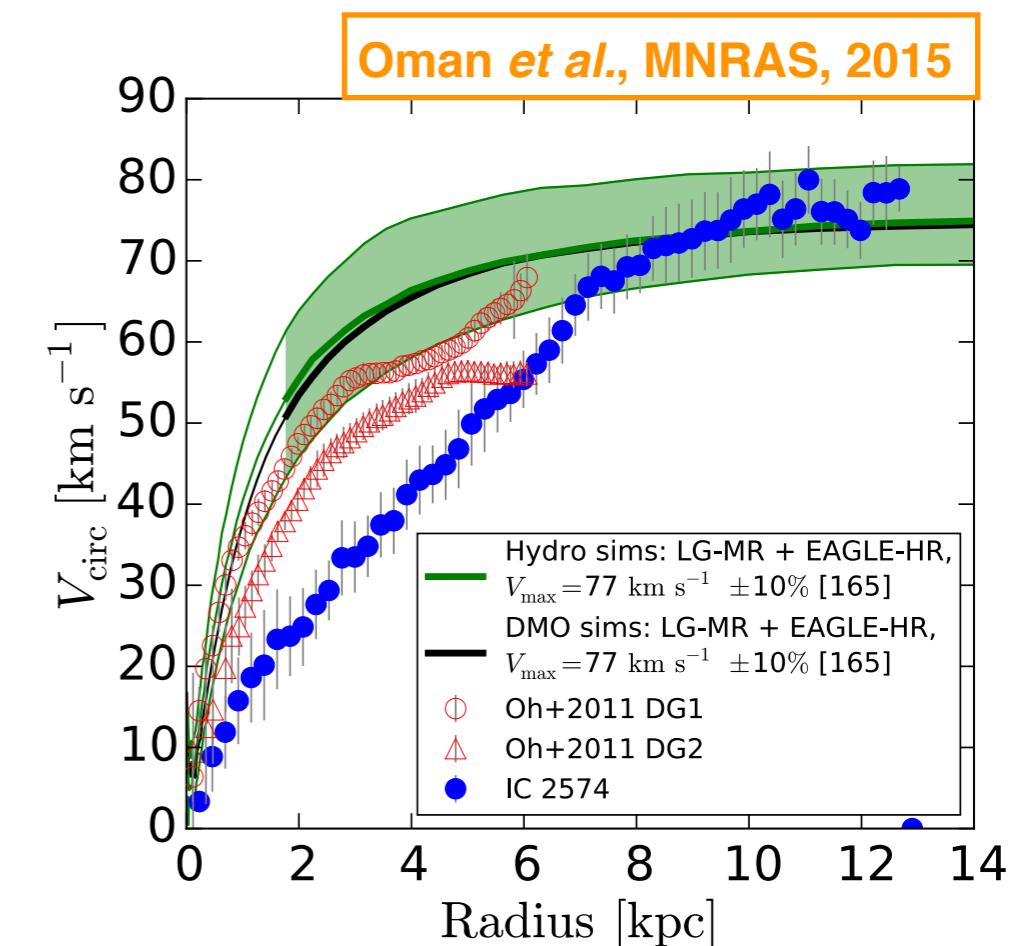
- observed diversity exceeds intrinsic diversity of DM halos
- compact disk can make SIDM inner circular velocity higher than the CDM prediction

* Hereafter $\sigma/m = 3 \text{ cm}^2/\text{g}$



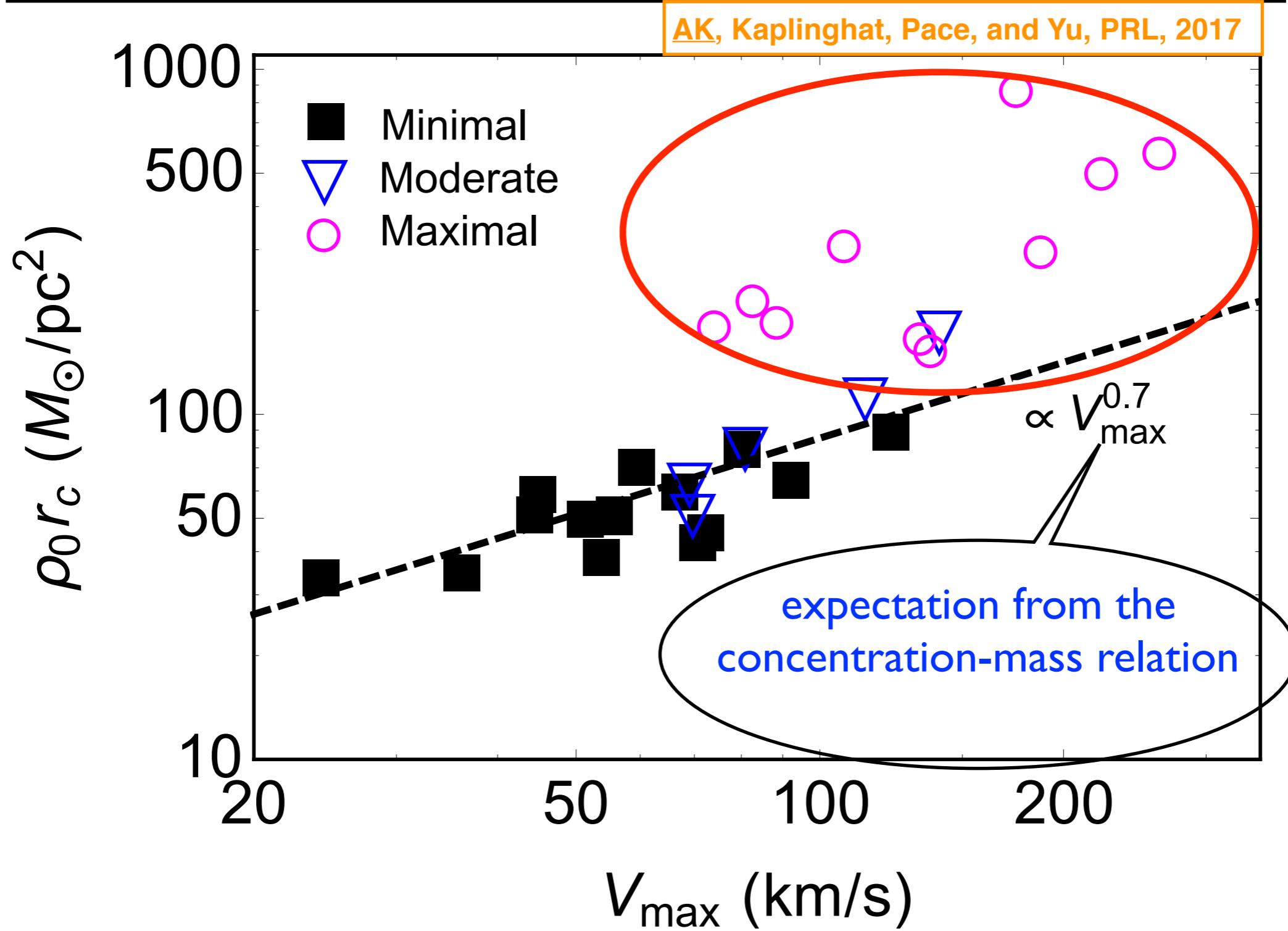
Intrinsic scatter

Intrinsic diversity of DM halos
should be taken into account to
explain the observed diversity



More samples

Massive spiral galaxies, **GENERALLY**, make SIDM halos **VIOLATE** the concentration-mass relation



Simple model

Model setup: QCD×QED-like hidden sector

- dark nucleons as DM

$$p' \sim u'u'd' \quad n' \sim u'd'd'$$

- * discussion applies to isospin quartet DM

- small quark mass term

$$\mathcal{L}_{\text{mass}} = m_u u' \bar{u}' + m_d d' \bar{d}'$$

- dark pions

$$\pi'^+ \sim u' \bar{d}' \quad \pi'^0 \sim u' \bar{u}' - d' \bar{d}'$$

$$\pi'^- \sim d' \bar{u}'$$

	$SU(3)_D$	$U(1)_D$	$U(1)_{B-L+B'}$
u'	3	2/3	1/3
\bar{u}'	$\bar{3}$	-2/3	-1/3
d'	3	-1/3	1/3
\bar{d}'	$\bar{3}$	1/3	-1/3

- * naturalness → chiral theory

- SM copy

- harmful neutrino's

Generation and transfer of asymmetry

$$U(1)_{B-L+B'} \rightarrow (-1)^{3(B-L+B')}$$

Right-handed neutrinos \bar{N} w/ soft breaking mass M_R

- thermal leptogenesis $\rightarrow B - L$ asymmetry $T \sim M_R > 10^9 \text{ GeV}$

Fukugita and Yanagida, PLB, 1986

- see-saw mechanism \rightarrow active neutrino mass $y_N LH \bar{N} \xrightarrow{\frac{y_N^2}{M_R}} LHLH$

- generation of the portal operator

$$y_N^2 \sim 10^{-5} \left(\frac{m_\nu}{0.1 \text{ eV}} \right) \left(\frac{M_R}{10^9 \text{ GeV}} \right)$$

Scalar down quark H'_C w/ mass $M_{H'_C}$

$$H'^\dagger_C \bar{u}' \bar{d}' \quad H'_C \bar{d}' \bar{N}$$

$$H'_C \frac{1}{M_{H'_C}^2} \bar{u}' \bar{d}' \bar{d}' \bar{N} \quad y_N LH \bar{N}$$

$$\bar{N} \rightarrow \frac{y_N}{M_{H'_C}^2 M_R} \bar{u}' \bar{d}' \bar{d}' LH$$

* decoupling after leptogenesis $M_{H'_C} \sim M_R$

	$SU(3)_D$	$U(1)_D$	$U(1)_{B-L+B'}$
H'_C	3	-1/3	-2/3
$U(1)_{B-L+B'}$			

✗ $H'_C u' d' \quad H'^\dagger_C d' \bar{N}$
 $\rightarrow \frac{1}{M_*^3} u' d' d' LH$

Entropy transfer

$U(1)'$ breaking scalar H^{+}'

$$\mathcal{L}_{A'} = \frac{\epsilon}{2} F_{\mu\nu} F'^{\mu\nu} + \frac{m_{\gamma'}}{2} A'_\mu A'^\mu$$

Dark pions annihilate/decay into dark photon $m_{\gamma'} < m_{\pi'}$

$$\rightarrow \Gamma_{\gamma' \rightarrow e\bar{e}} = 0.3 \text{ s}^{-1} \times \left(\frac{\epsilon}{10^{-10}} \right)^2 \left(\frac{m_{\gamma'}}{100 \text{ MeV}} \right)$$

- decay after neutrino decoupling $T \sim 1 \text{ MeV} \leftrightarrow t \sim 1 \text{ s}$

\rightarrow transferred entropy heating only e and γ

\rightarrow lower bound on $\Gamma_{\gamma' \rightarrow e\bar{e}}$

- decay before neutrino decoupling

\rightarrow thermalized dark photon heating only e and γ

\rightarrow lower bound on $m_{\gamma'}$

DM direct detection

$p' \sim x \sim p$ interaction
 ϵ

- DM direct detection \rightarrow upper bound on ϵ
- DM mass: $\frac{1}{M_{H'_C}^2 M_R} \bar{u}' \bar{d}' \bar{d}' L H \rightarrow m_{\text{DM}} \simeq 8.5 \text{ GeV}$ Weinberg, "Cosmology"
- $Y_{p'}/Y_{n'}$: freezes out at decoupling of conversion processes

$$Y_{p'}/Y_{n'} = e^{(m_{n'} - m_{p'})/T} \quad T \sim m_{\pi'}/20-30 \leftrightarrow \text{dark pion decoupling}$$

$$m_{n'} - m_{p'} = \mathcal{O}(m_{u'/d'}) \quad m_{\pi'}^2 = \mathcal{O}\left(m_{u'/d'} \Lambda_{\text{QCD}'}\right) \rightarrow Y_{p'}/Y_{n'} \sim 1$$

c.f. $m_n - m_p \simeq 1.2 \text{ MeV}$ $m_\pi \simeq 140 \text{ MeV}$ for reference

* if $m_{\gamma'} < B_{d'}$, dark nucleosynthesis proceeds

Krnjaic and Sigurdson,
PLB, 2015...

- impacting DM direct detection

Charge of breaking scalar

Ibe, AK, Kobayashi, Kuwahara
and Nakano, work in progress

$U(1)_D$ charge determines π' - \tilde{e} mixing

$SU(4)$	$SU(3)_D$	$U(1)_D$	$U(1)_{B-L+B'}$
\tilde{e}	1	-1	0

→ Yukawa interactions $\tilde{e}' u' \bar{d}'$ $\tilde{e}'^\dagger \bar{u}' d'$

- entropy transfer through π' - \tilde{e} mixing
+ Higgs portal $|\tilde{e}'|^2 |H|^2$

- DM direct detection through Higgs portal?

SUSY mass spectrum

Arkani-Hamed and Dimopoulos, JHEP, 2005

Giudice and Romanino, NPB, 2004

Wells, PRD, 2005

...

Mini-split SUSY mass spectrum:

sfermions, heavy Higgses > 100 TeV; gravitino > 100 TeV

- 125 GeV Higgs although naturalness unanswered

gauginos ~ TeV; higgsino ~TeV

- precise $SU(5)$ grand unification

- LSP and LSP' abundance: small enough

- LSP \rightarrow LSP' or vice versa long before big bang nucleosynthesis

$$\tau \sim 2 \times 10^{-3} \text{ s} \left(\frac{10^{-10}}{\epsilon} \right)^2 \left(\frac{10^3 \text{ GeV}}{M_{\text{light } S}} \right)^2$$

Supersymmetric realization

Precise $SU(5)$ grand unification and origins of electroweak and $U(1)'$ breaking \rightarrow SUSY

Ibe, AK, Kobayashi, Kuwahara
and Nakano, JHEP, 2019

Dark sector $SU(4)'$ $\mathbf{6}' : (u', \bar{u}')$ $\mathbf{4}' : (d', \bar{e}')$ $\bar{\mathbf{4}}' : (\bar{d}', e')$
 $\mathbf{4}'_H : (H'_C, H^+')$ $\bar{\mathbf{4}}'_H : (\bar{H}'_C, H^-')$

Portal superpotential $W \sim \frac{y_N}{M_{H_C} M_R} \bar{u}' \bar{d}' \bar{d}' L H_u$

$$\tilde{\bar{d}}' \rightarrow \mathcal{L} \sim \frac{\alpha'}{4\pi} \frac{y_N}{M_{H_C} M'_S M_R} \bar{u}' \bar{d}' \bar{d}' L H_u$$

dark nucleon decay into neutrino \rightarrow $n' \rightarrow \pi^{0'} + \nu$ $\tau \gtrsim 10^{23}$ sec $\lesssim \frac{1}{10^{26} \text{ GeV}^3}$

Covi, Grefe, Ibarra, and Tran, JCAP, 2010

Fukuda, Matsumoto, and Mukhopadhyay, PRD, 2015

hidden sparticle mass $M'_S \gtrsim 10^3 \text{ GeV} \left(\frac{M_R}{10^9 \text{ GeV}} \right)^{1/2}$ - split SUSY!