

KAVLI  
IPMU



# Anatomy of tthh Physics

## Ying-Ying Li

### HKUST

[L. Li, YYL, T. Liu, [arXiv:1905.03772](https://arxiv.org/abs/1905.03772)]

[P. Asadi, N. Craig, YYL, [arXiv:1810.09467](https://arxiv.org/abs/1810.09467)]

June 05, 2019  
43rd Johns Hopkins Workshop



## Outline

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I will focus on  $t\bar{t}h$  channel, talk about its potential in

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Higgs Trilinear Coupling Measurement

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Contact Interaction Measurement

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Resonant Search

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heavy fermions, heavy scalars in turtling models/MSSM

BDT analysis and Results

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Conclusion and Outlook

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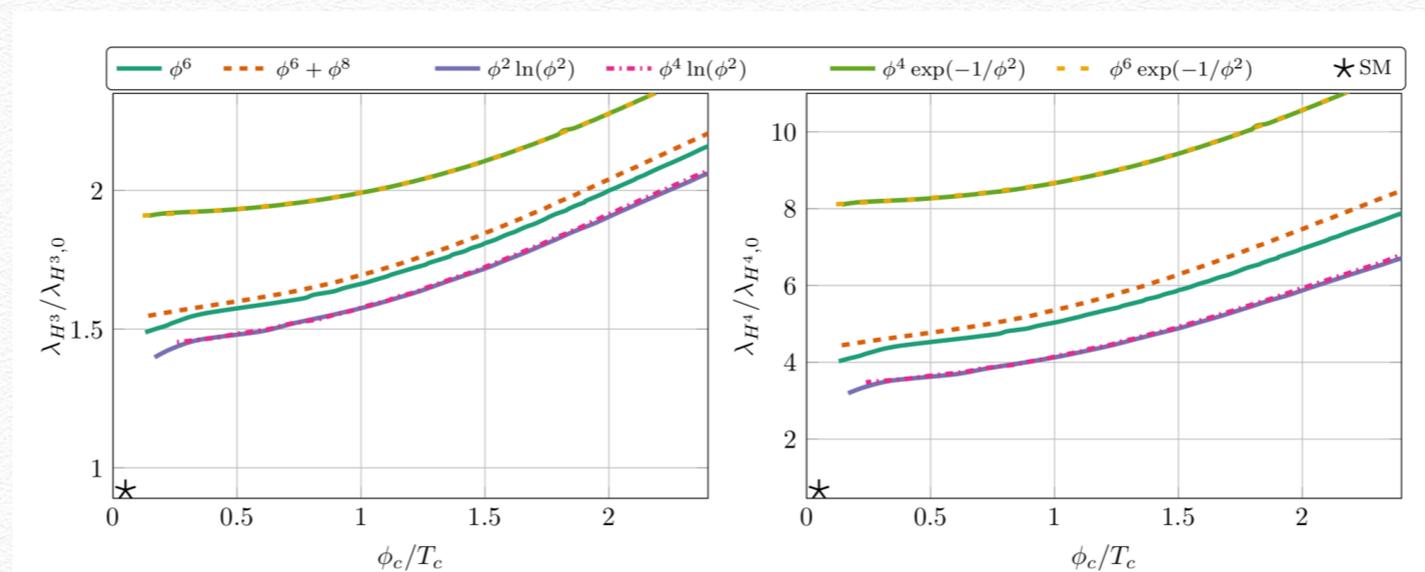
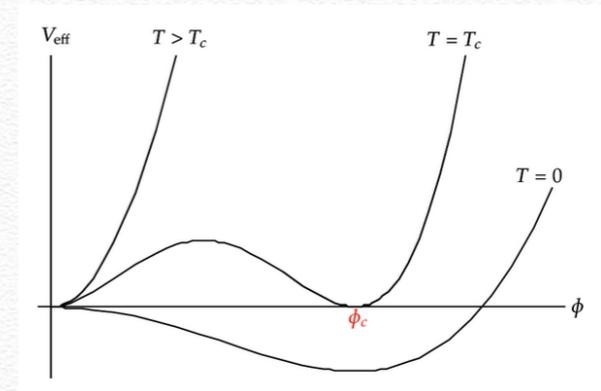
# Higgs trilinear Coupling

## 1, Electroweak baryogenesis: out of equilibrium

strong first order  
phase transition

$$\phi_c/T_c \gtrsim 1$$

baryon asymmetry preserved



[M. Reichert, et al. arXiv:1711.00019]

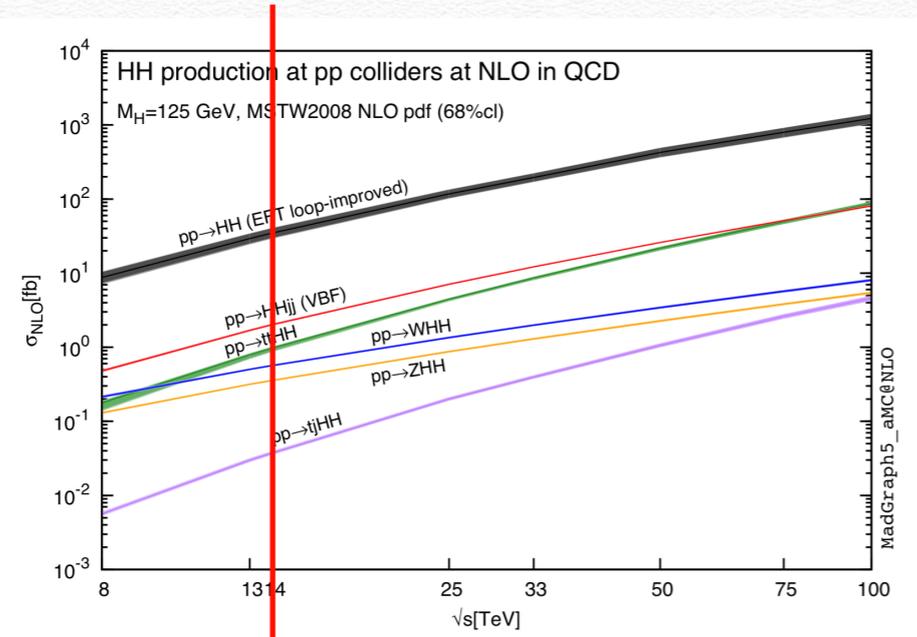
## 2, deviation of trilinear coupling -> unitarity bound of scale of new physics

[S. Chang, et al. arXiv:1902.05556]

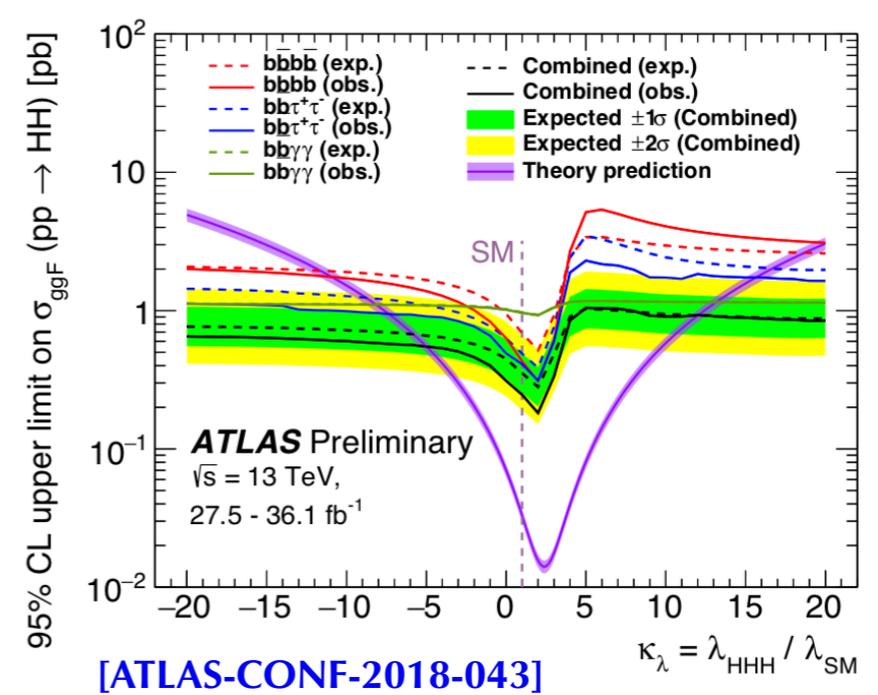
[A. Falkowski, et al. arXiv:1902.05936]

[see Spencer's talk tomorrow]

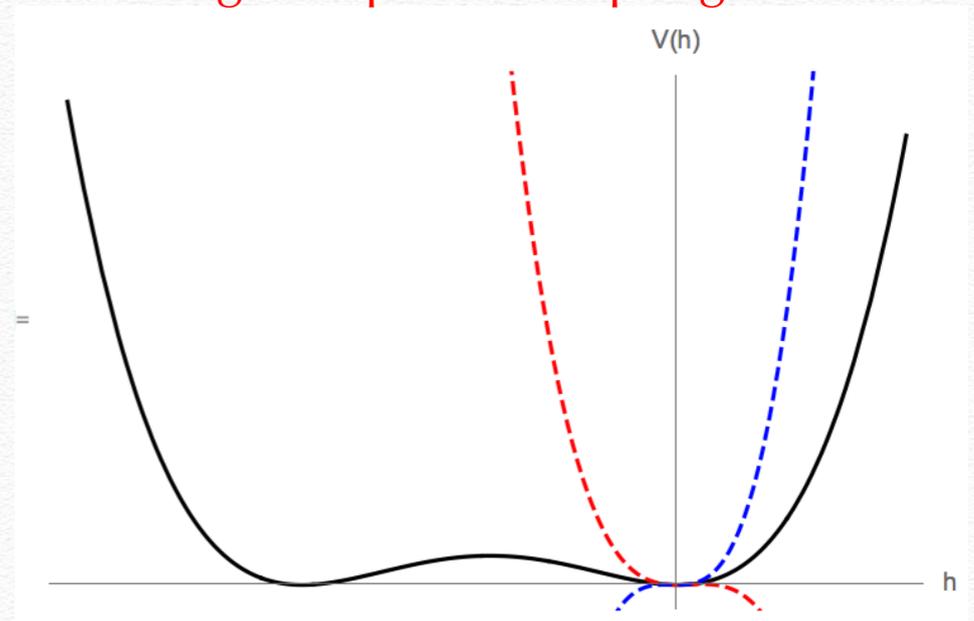
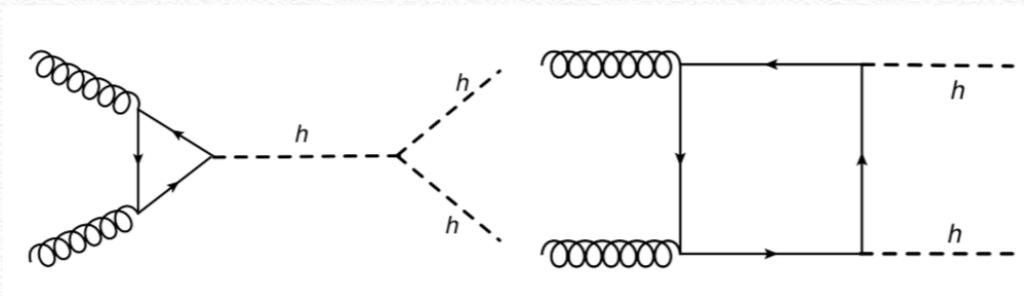
# Higgs trilinear Coupling



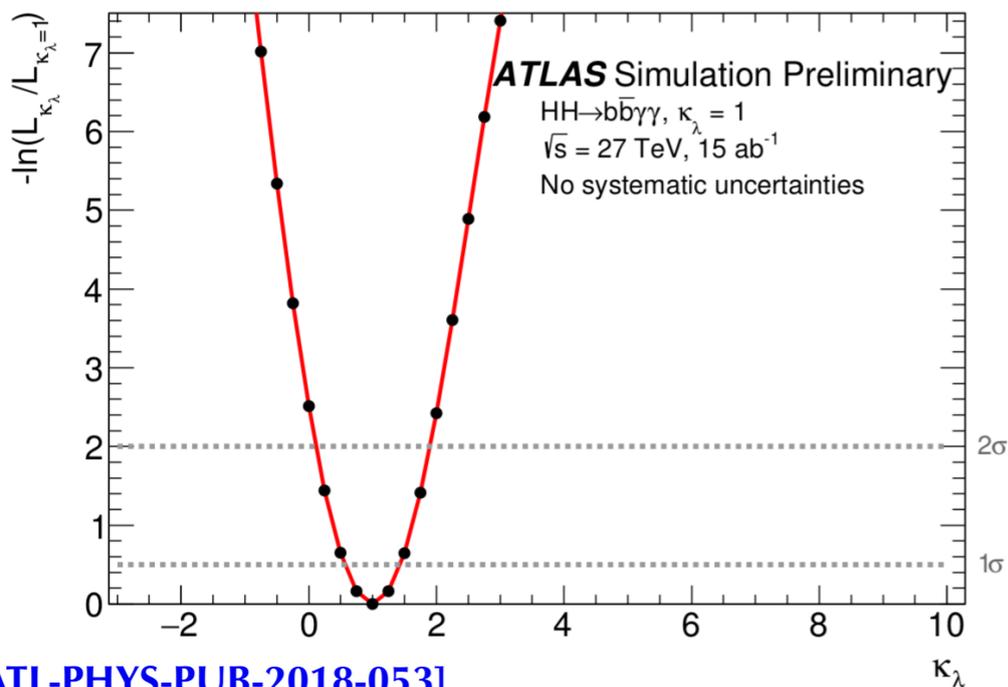
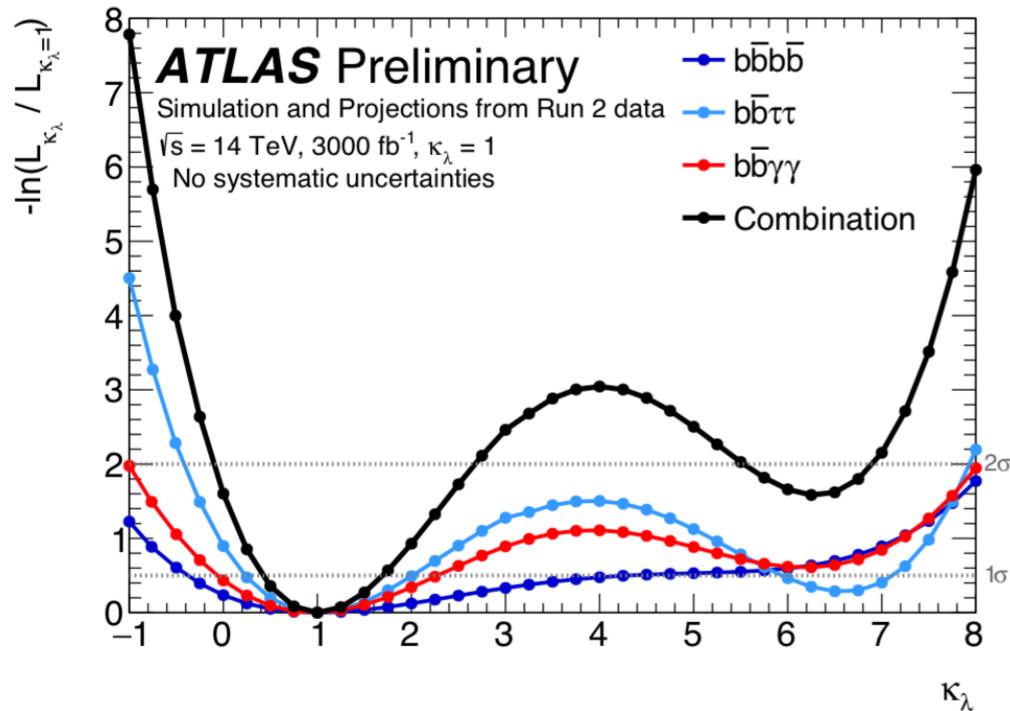
[R. Frederix, et al. arXiv:1401.7340]



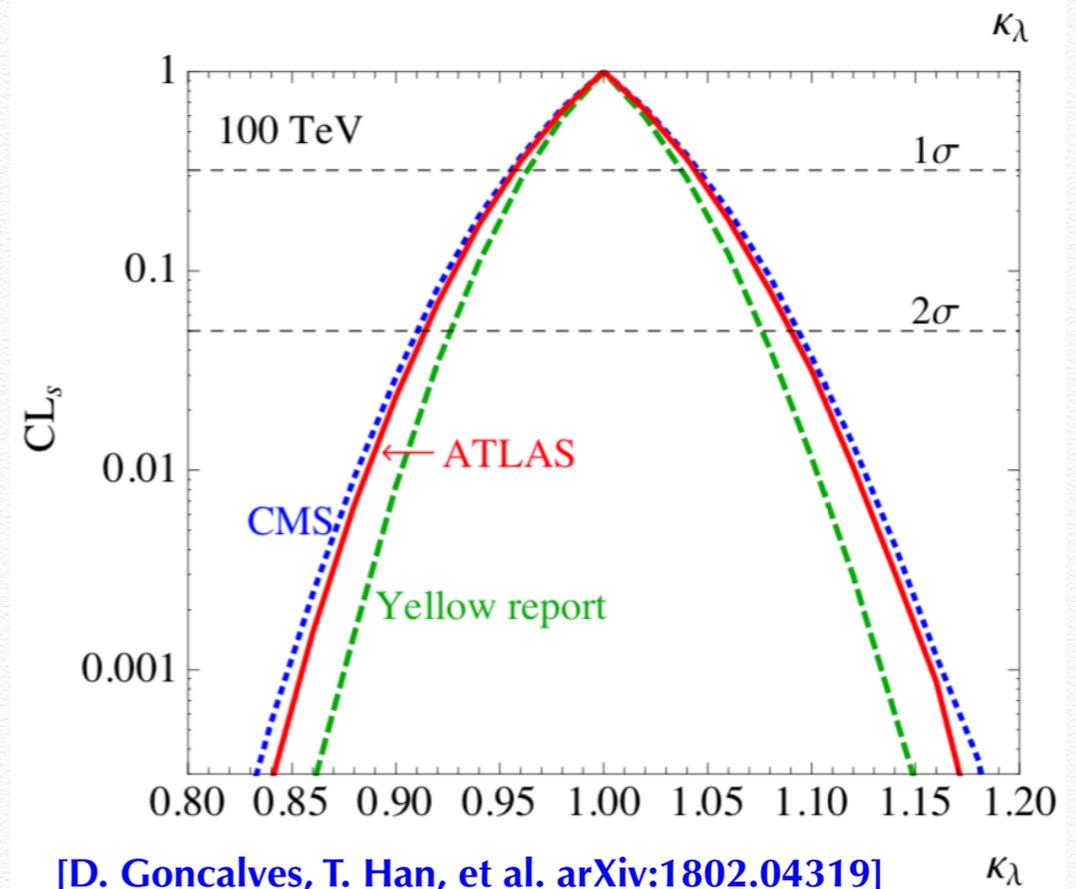
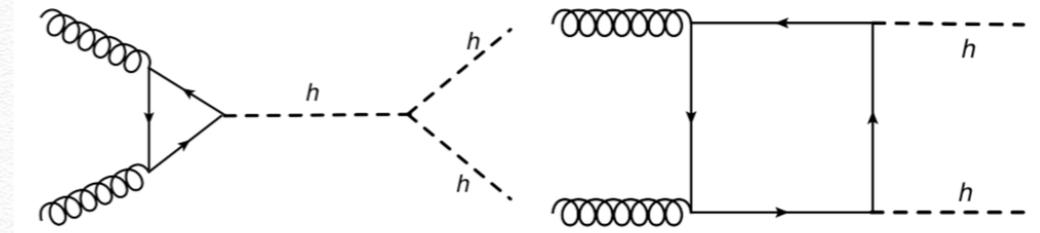
Assuming SM quartic coupling



# Higgs trilinear Coupling

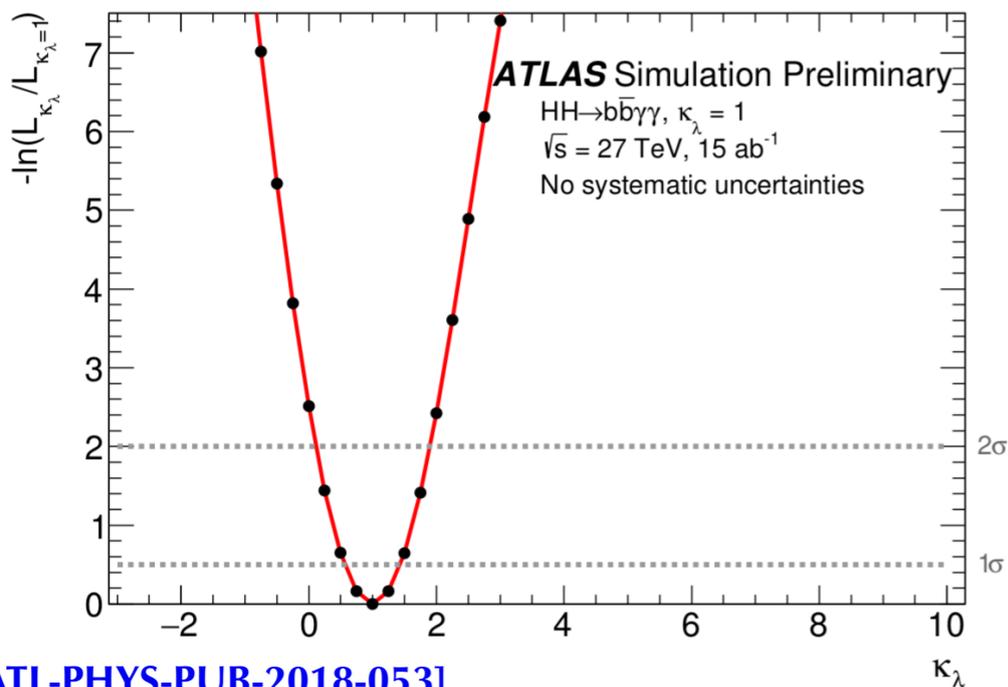
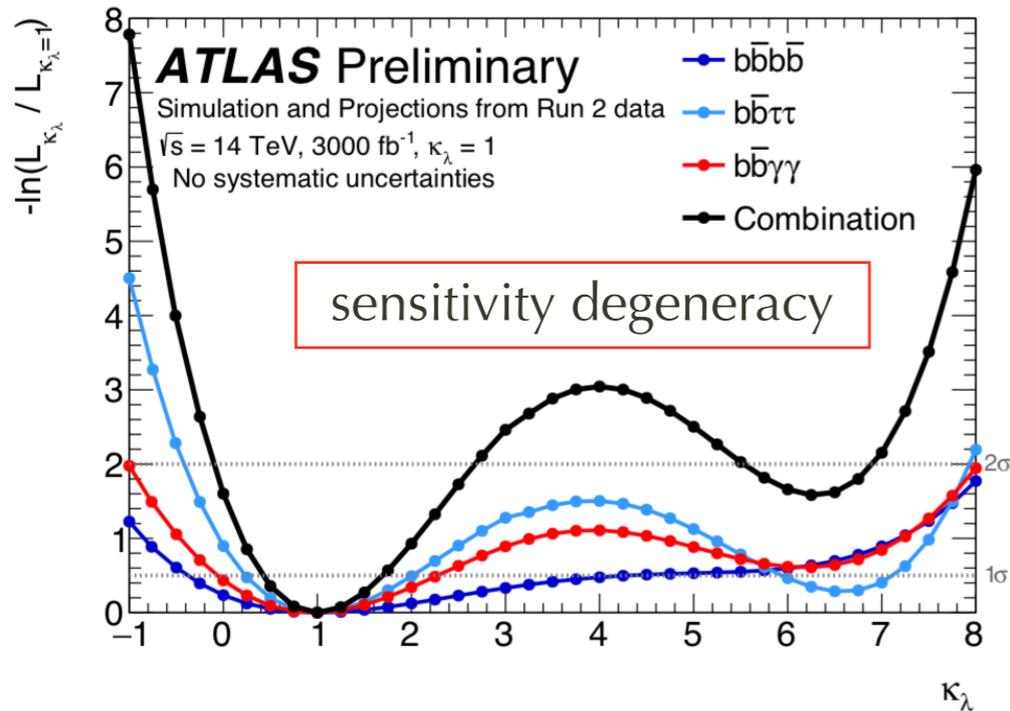


[ATL-PHYS-PUB-2018-053]  
[...many other works]

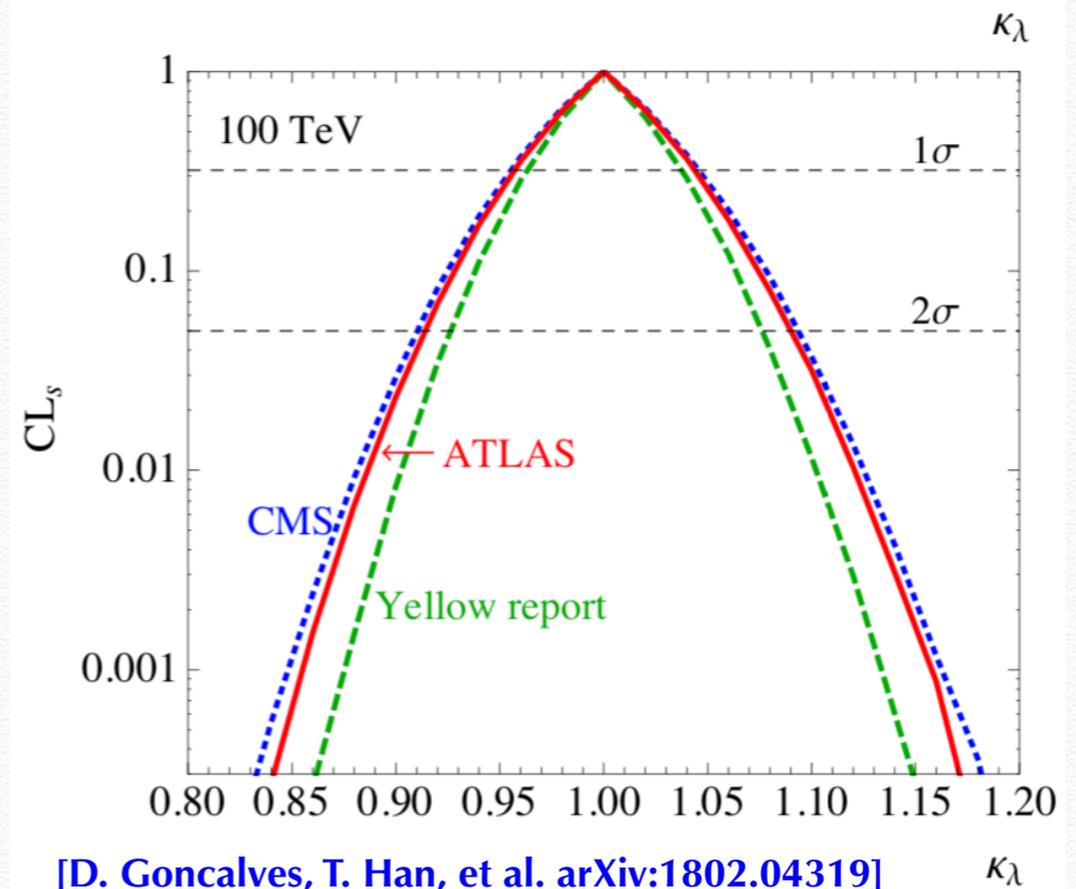
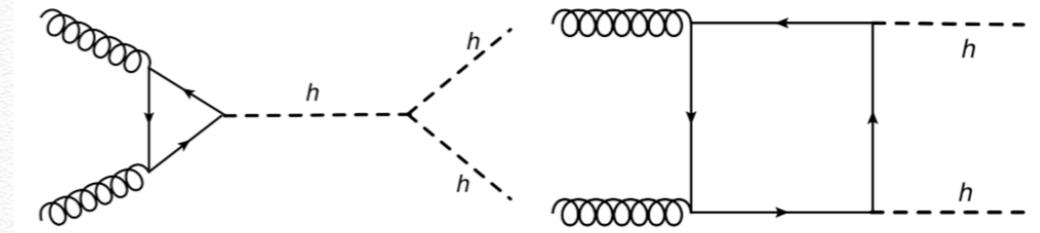


[D. Goncalves, T. Han, et al. arXiv:1802.04319]  
[...many other works]

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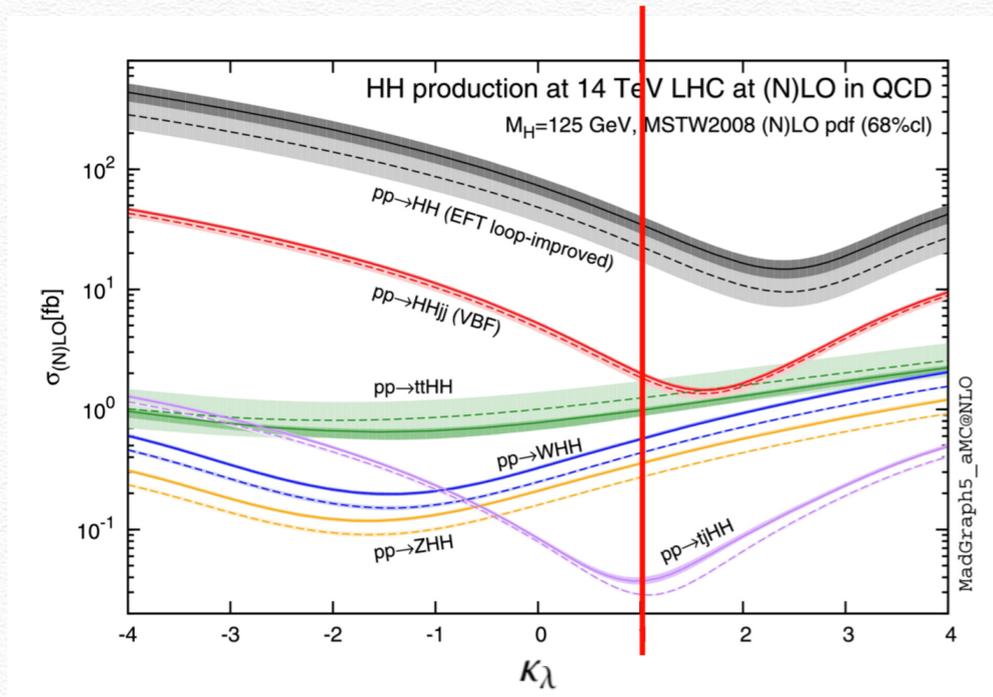
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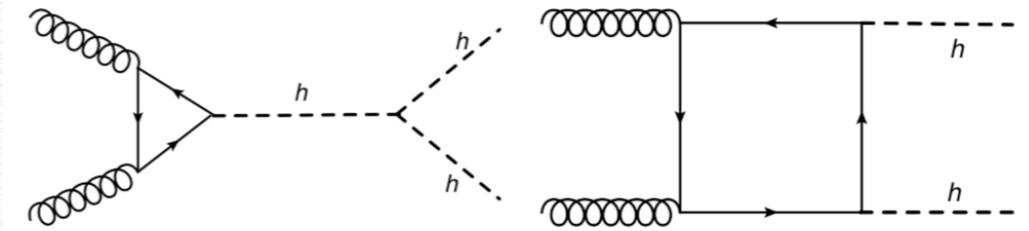
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# Higgs trilinear Coupling

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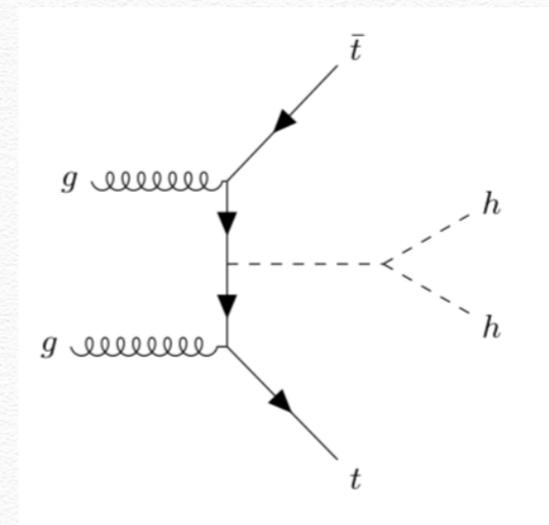


destructive interference



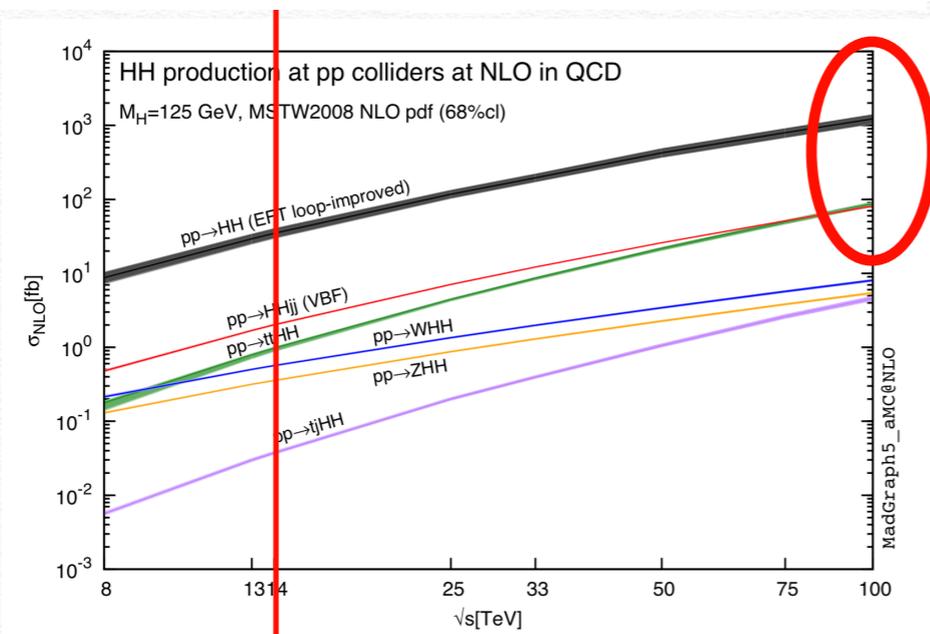
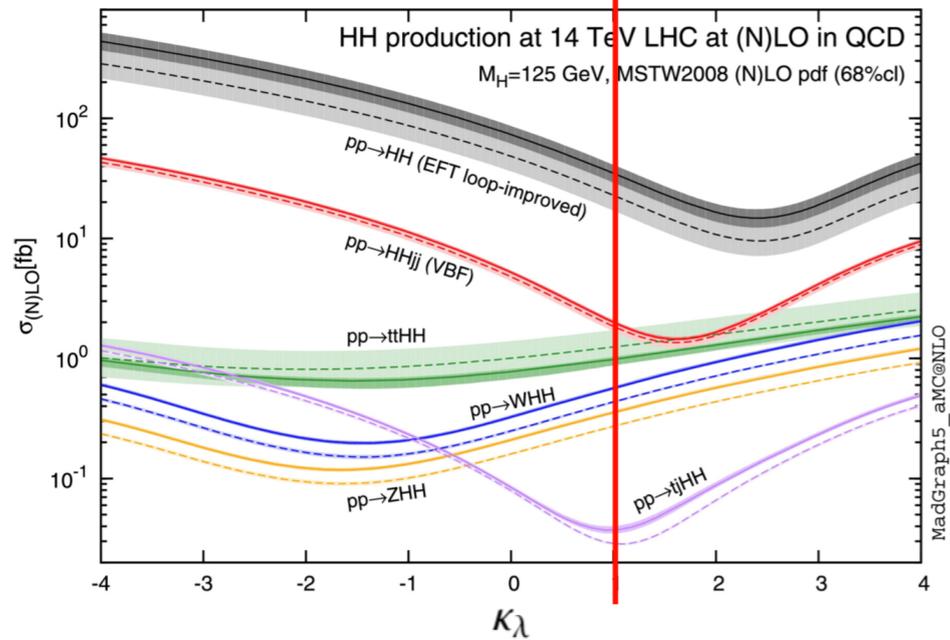
sensitivity degeneracy for gluon fusion di-Higgs production;

tthh channel: constructive interference for enhanced trilinear coupling;



# tthh—Higgs trilinear coupling

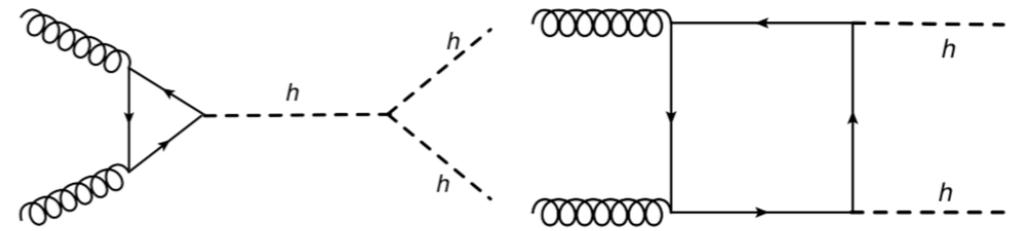
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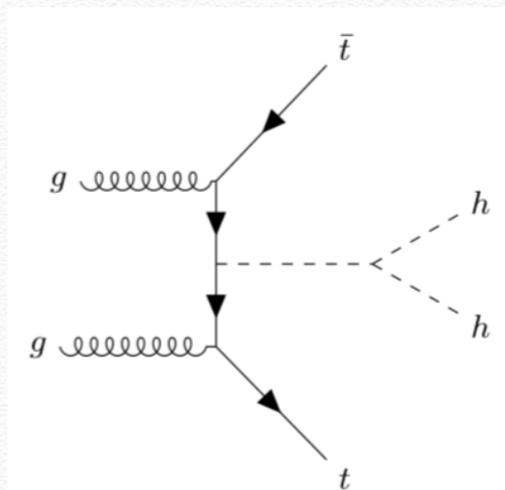
tthh could play a complementary role!

destructive interference



sensitivity degeneracy for gluon fusion di-Higgs production;

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## tthh—contact interactions

[L. Li, YYL, T. Liu, arXiv:1905.03772]

$$\mathcal{L} \supset -y \frac{m_t}{v} t\bar{t}h - \kappa \frac{1}{3!} \frac{3m_h^2}{v} h^3 - c_t \frac{1}{2!} \frac{m_t}{v^2} t\bar{t}hh$$

Assuming SM top Yukawa coupling

$$\frac{\sigma(gg \rightarrow hh \rightarrow bb\gamma\gamma)_{14}}{\sigma(gg \rightarrow hh \rightarrow bb\gamma\gamma)_{14}^{\text{SM}}} = 1.70 - 0.82\kappa + 0.12\kappa^2 - 3.79c_t + 0.98c_t\kappa + 2.68c_t^2$$

$$\frac{\sigma(tthh)_{14}}{\sigma(tthh)_{14}^{\text{SM}}} = 0.82 + 0.14\kappa + 0.04\kappa^2 + 0.28c_t + 0.21\kappa c_t + 0.44c_t^2$$

tthh could play a complementary role

tthh channel: constructive interference for enhanced trilinear coupling and enhanced contact interactions;



## tthh—Resonance Search—fermions

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direct search for new states, highly motivated by naturalness

Coloured vector-like top partners are predicted in natural models,  
e.g. Composite Higgs

[R. Contino, et al. [arXiv:hep-ph/0612190](https://arxiv.org/abs/hep-ph/0612190)]

Singlet, e.g. little higgs,  
decay via its mixing with SM top quark

$$BR(T \rightarrow th) \sim BR(T \rightarrow tZ) \sim \frac{1}{2}BR(T \rightarrow Wb) \sim 25\%$$

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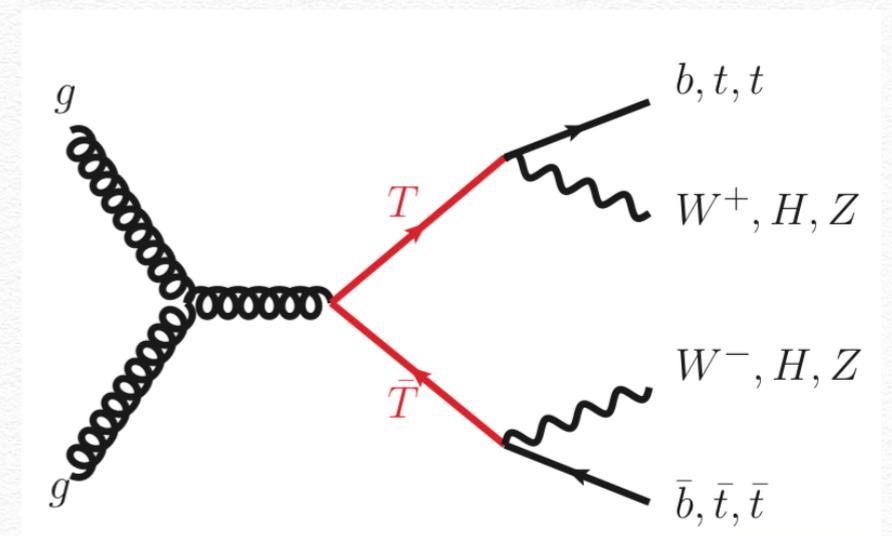
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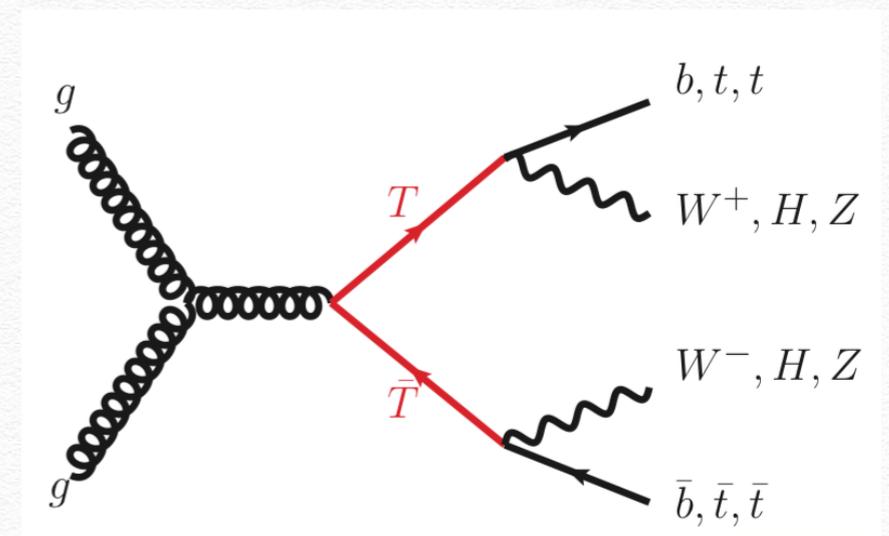
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**tthh could play an important role!**

Current bound: 1.3TeV [ATLAS, arXiv:1808.02343]



Re-introduce tuning:  
neutral naturalness model,  
e.g. twin Higgs model

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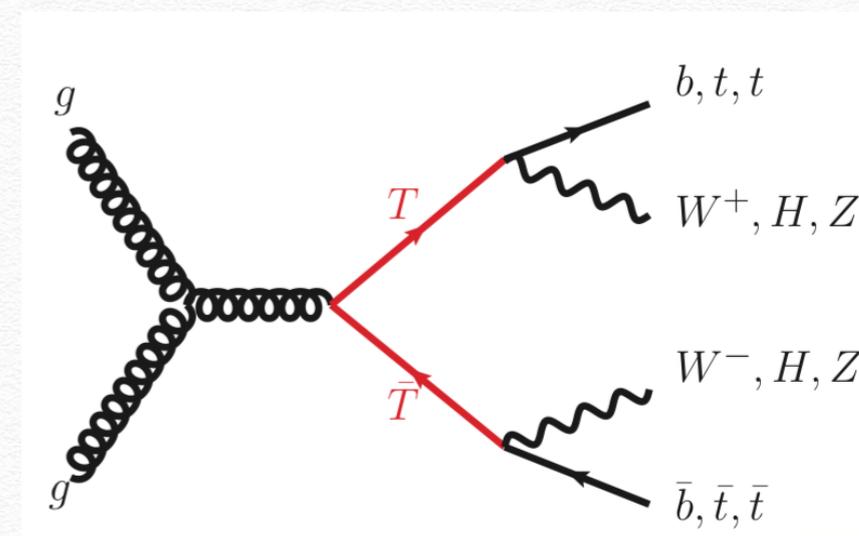
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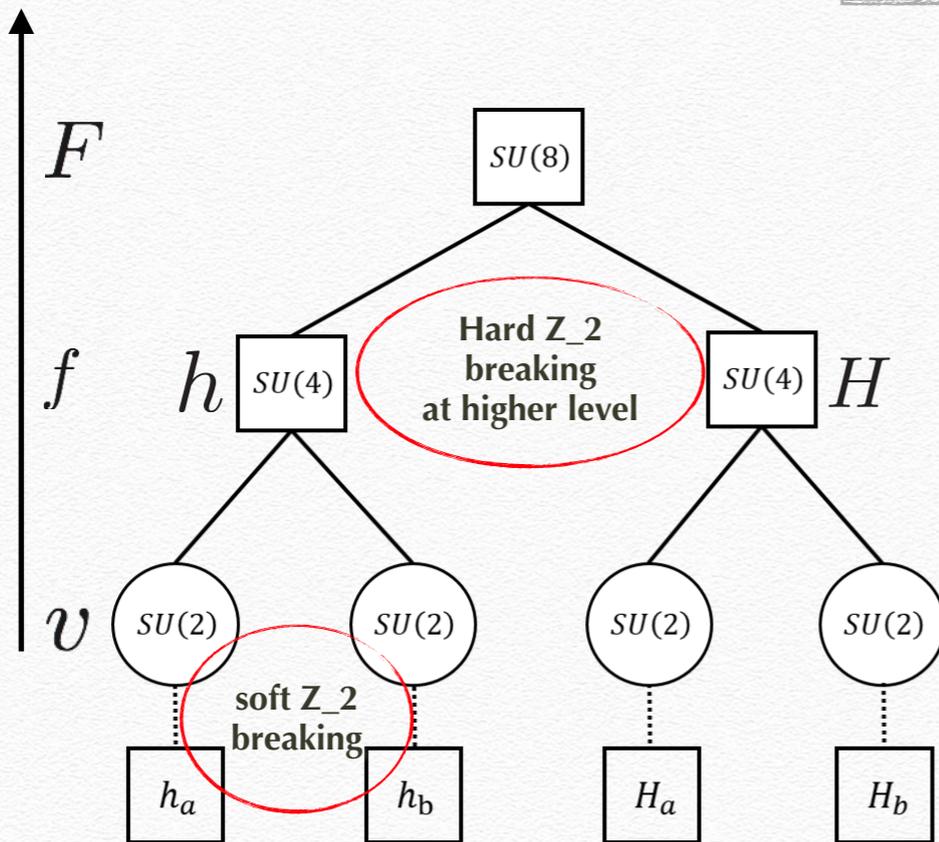
twin Higgs model need to be  
further extended to push the  
coloured top partner out of  
reach.

# tthh—Resonance Search—scalars

direct search for new states, highly motivated by naturalness

[P. Asadi, N. Craig, YYL, arXiv:1810.09467]

Twin Turtles

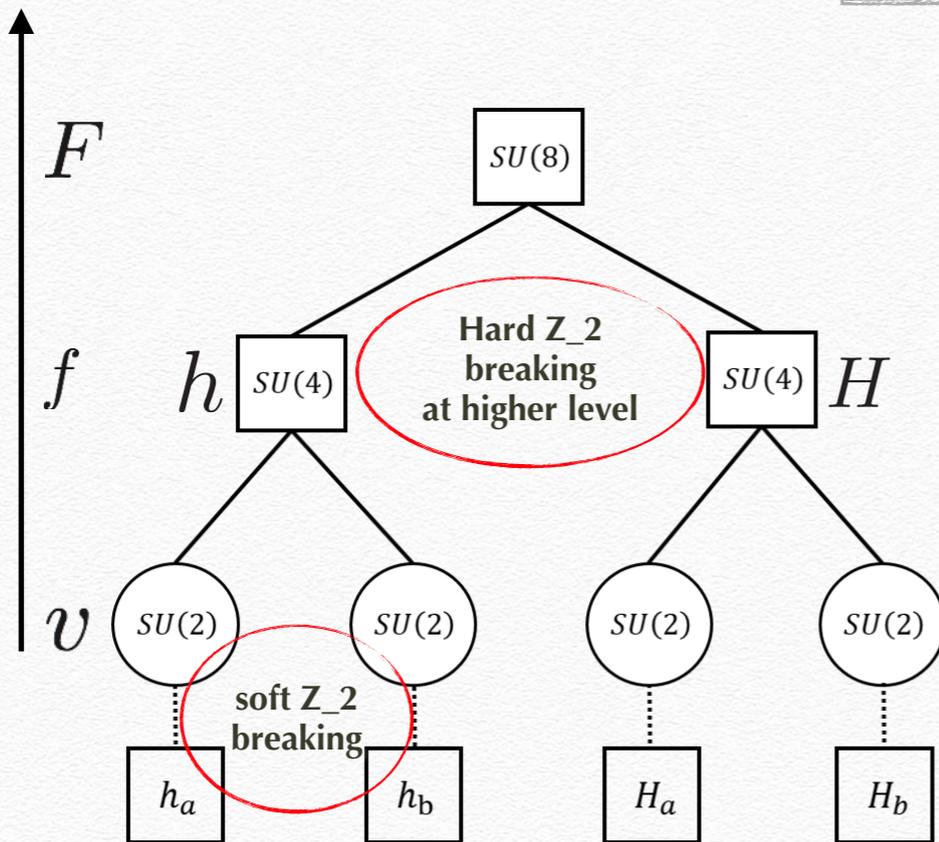


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## Twin Turtles



$$\Delta_{v/\Lambda}^{\text{TMNT}} \approx \frac{1}{64\pi^2} \frac{\bar{\kappa}}{2\bar{\kappa} + \bar{\rho}} \left( \frac{3y_t^2}{\bar{\lambda}} \frac{\Lambda_t^2}{v^2} - \left(9 + 5\epsilon_{\pm} \frac{\bar{\rho}}{\bar{\kappa}}\right) \frac{\Lambda_{\rho}^2}{v^2} \right)$$

$$\Delta_{v/\Lambda}^{\text{SM}} \approx \frac{1}{32\pi^2} \left( \frac{3y_t^2}{\lambda_{\text{SM}}} \frac{\Lambda_t^2}{v^2} - 3 \frac{\Lambda_{\rho}^2}{v^2} \right)$$

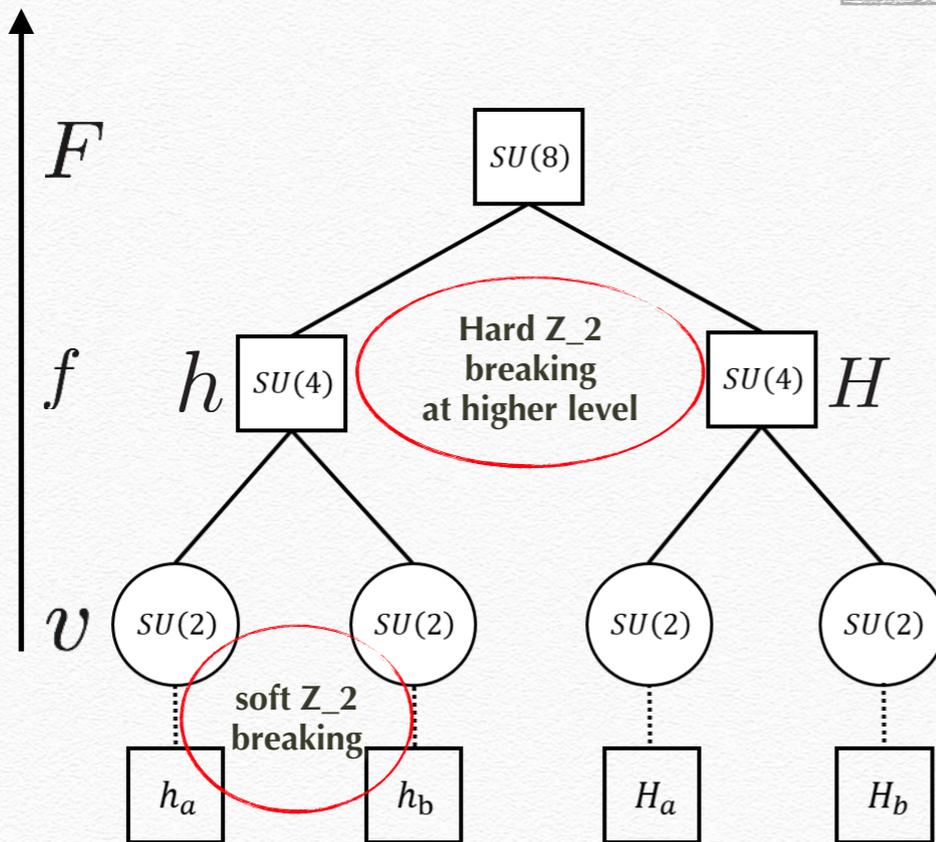
$$\begin{aligned} V \supset & \frac{\bar{\lambda}(|h|^2 + |H|^2)^2 + m^2(|h|^2 + |H|^2) + \bar{\kappa}(|h|^4 + |H|^4) + \bar{\rho}|h|^4 + m_h'^2|h|^2}{\phantom{V \supset}} \\ & + \rho''(|h_a|^2 + |H|^2)^2 + \kappa''(|h_a|^4 + |h_b|^4 + |H_a|^4 + |H_b|^4) \\ & + \kappa'(|h_a|^4 + |h_b|^4) + \rho'|h_a|^4 + \mu'^2|h_a|^2. \end{aligned}$$

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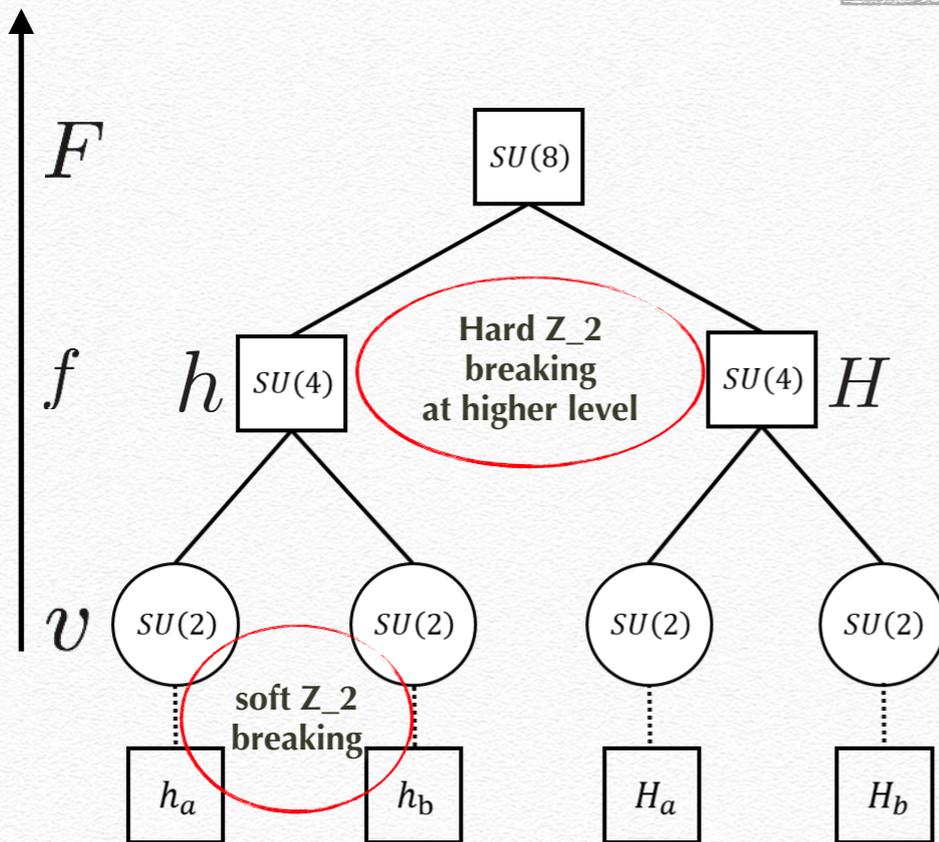
More scalars are introduced to push up the scale of coloured states!  
Higgs like scalars  $\rightarrow$  definite signature of naturalness

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Twin Turtles



More scalars are introduced to push up the scale of coloured states!  
Higgs like scalars -> definite signature of naturalness

Precision measurement?

$$g_{hii} \sim g_{h_{SM}ii} \left( 1 - \frac{1}{2} (\sin^2 \theta_{a1} + \sin^2 \theta_{a2}) \right) \sim g_{h_{SM}ii} \left( 1 - \frac{v^2}{2f^2} \right)$$

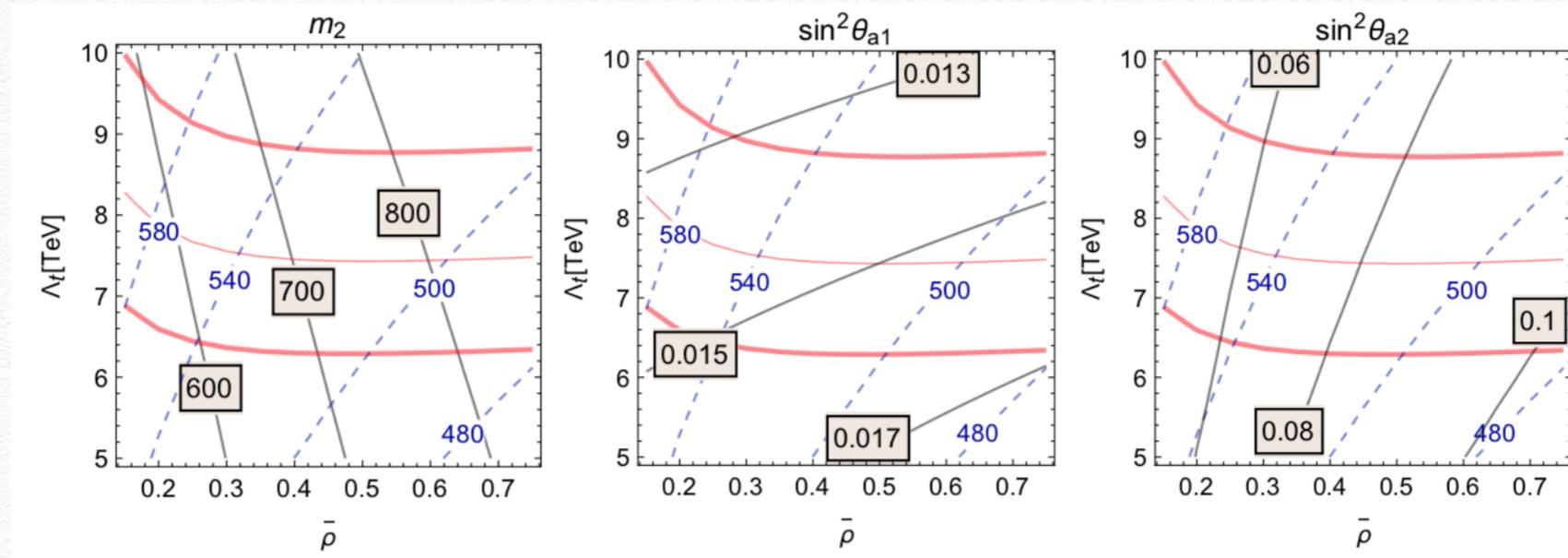
Precision could not distinguish twin from turtles.



# tthh—Resonance Search—scalars

[P. Asadi, N. Craig, YYL, arXiv:1810.09467]

More scalars mix with the SM-like Higgs states

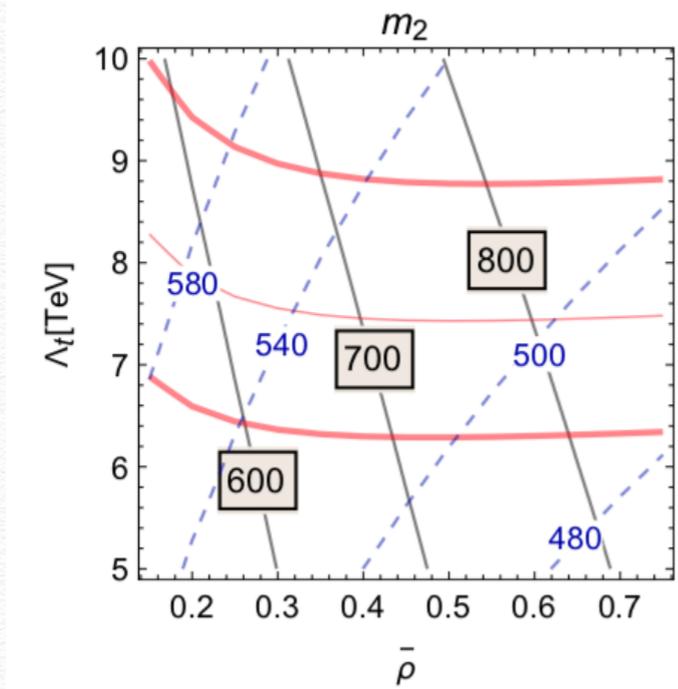


Direct production of heavy scalars ( $h_2$ ) becomes crucial!

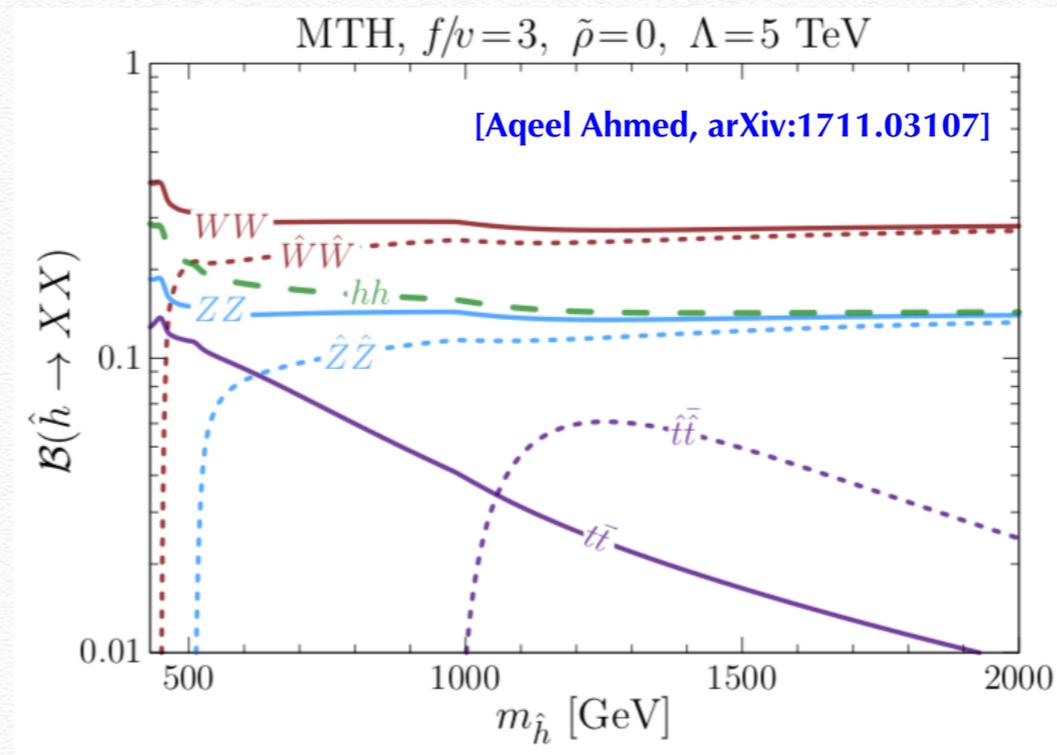
# tthh—Resonance Search—scalars

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[Aqeel Ahmed, arXiv:1711.03107]

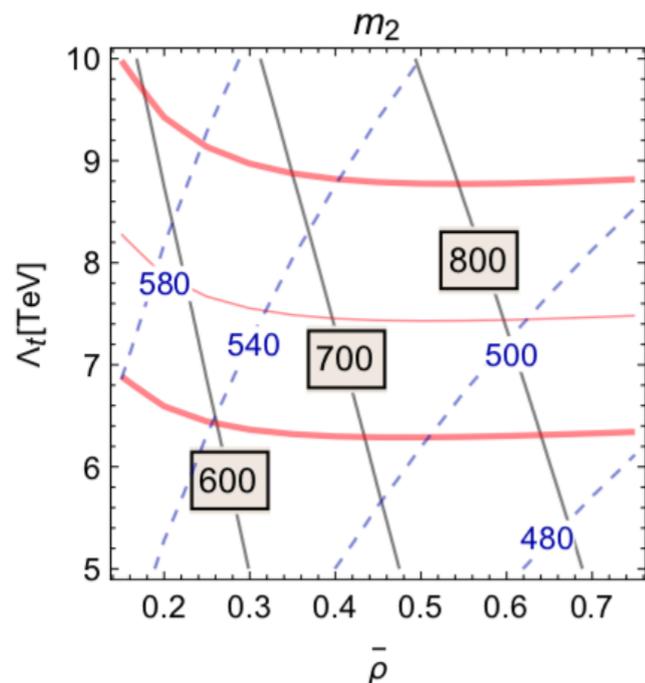


large  $Br(h_2 \rightarrow hh)$ ;  
rich signatures from di-Higgs decay.

# tthh—Resonance Search—scalars

Direct production of heavy scalars ( $h_2$ ) becomes crucial!

[P. Asadi, N. Craig, YYL, arXiv:1810.09467]



gluon fusion:

$500\text{GeV}(mh_2)@14/100\text{TeV} = 2.13/102.7\text{pb};$   
 $600\text{GeV}(mh_2)@14/100\text{TeV} = 0.968/55.2\text{pb};$

tth2:

$500\text{GeV}(mh_2)@14/100\text{TeV} = 0.013/2.17\text{pb};$   
 $600\text{GeV}(mh_2)@14/100\text{TeV} = 0.0083/1.63\text{pb};$

decay products from associated top  
could help to suppress background;

production cross section increases  
faster at 100TeV.

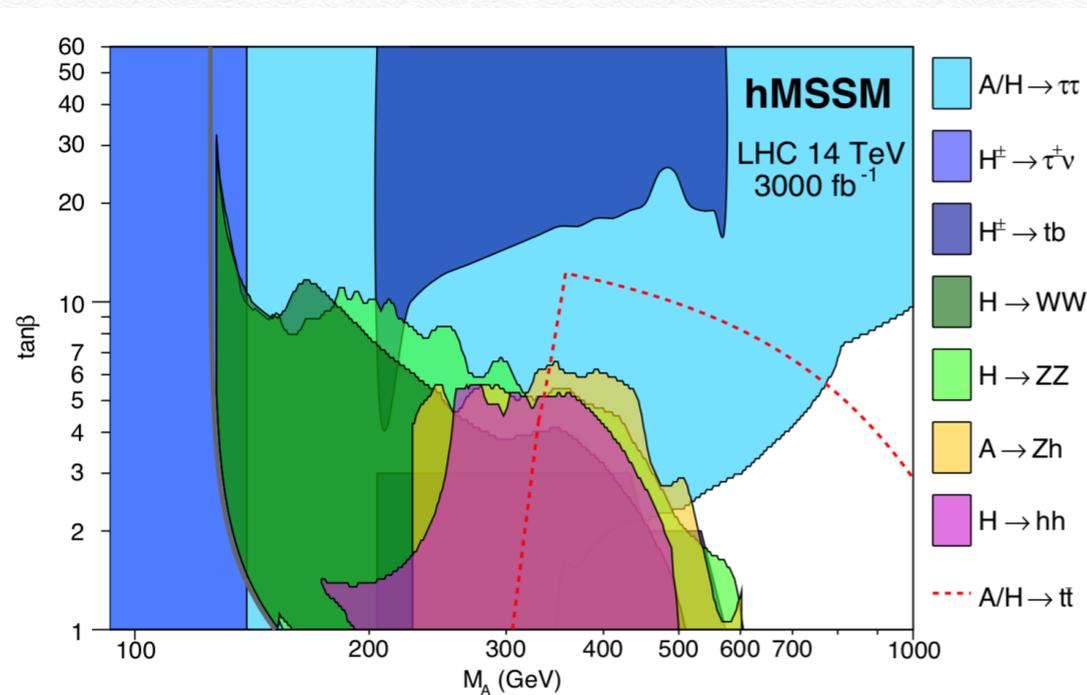
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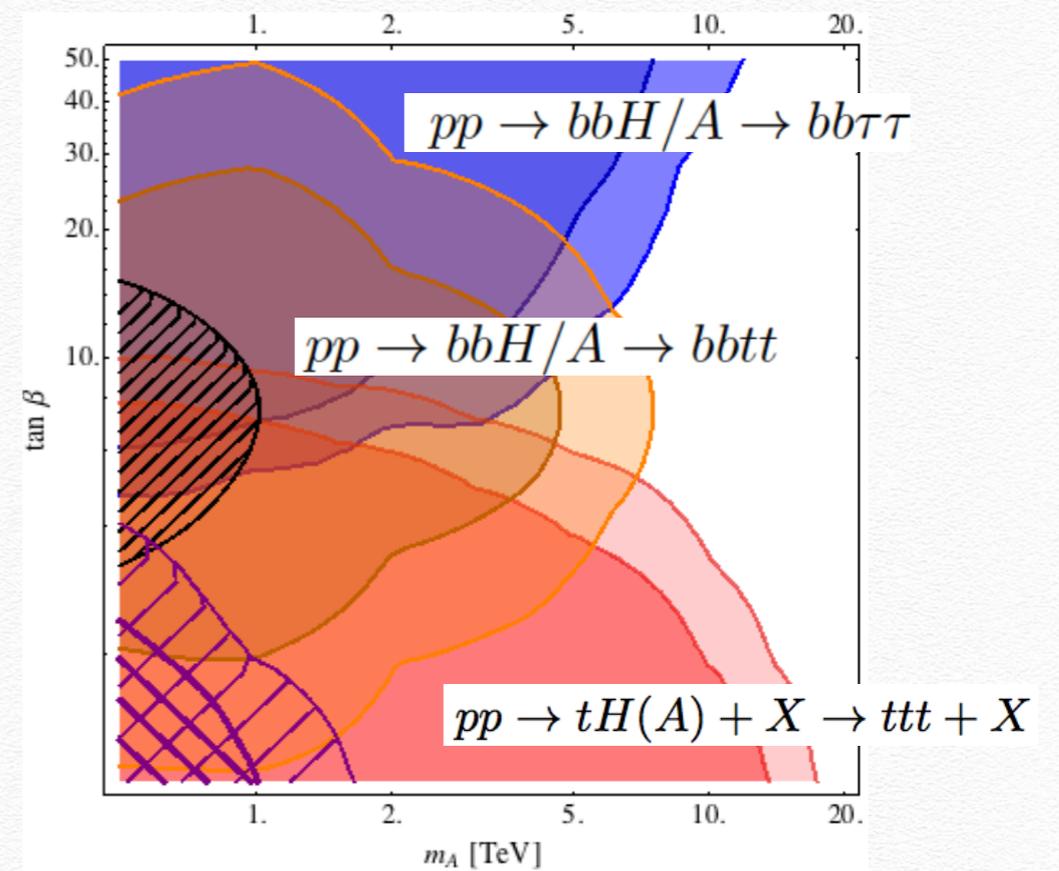
MSSM Higgs bosons(no CP-violation):H,A,Hc

Higgs mass spectrum and couplings only depend on two parameters (in addition to the SM ones) at tree-level:  $\tan_\beta$ ,  $m_A/m_{Hc}$ ;

[A. Djouadi, et al. arXiv:1502.05653]



[N. Craig, J. Hajer, YYL, T. Liu, H. Zhang, arXiv:1605.08744]



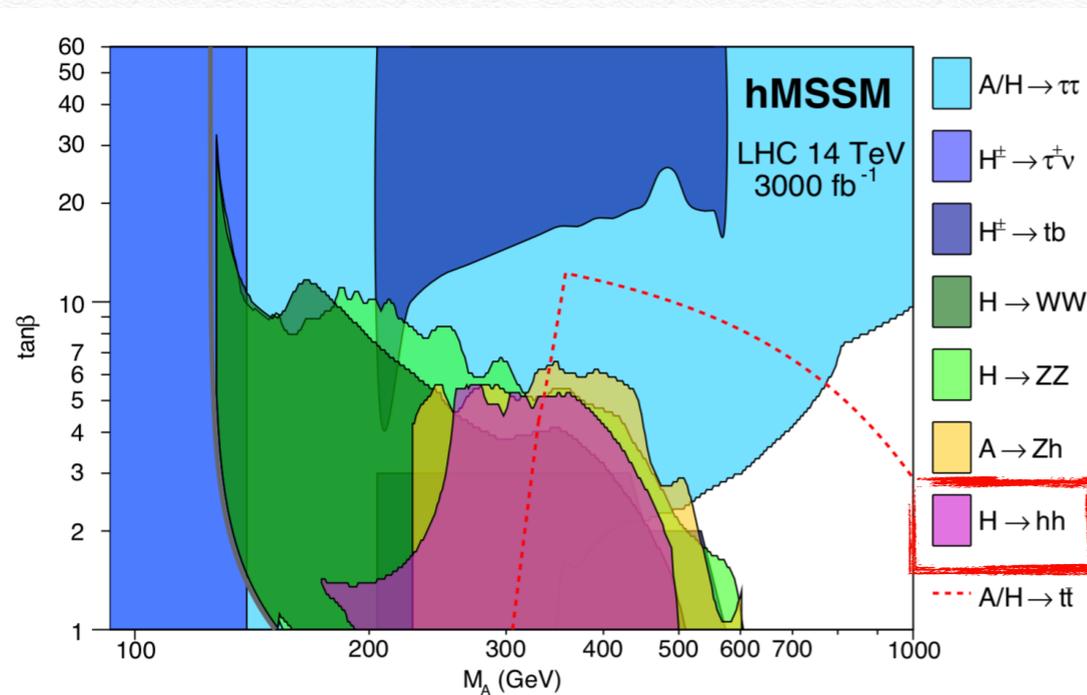
Neutral Higgs Exclusion limit

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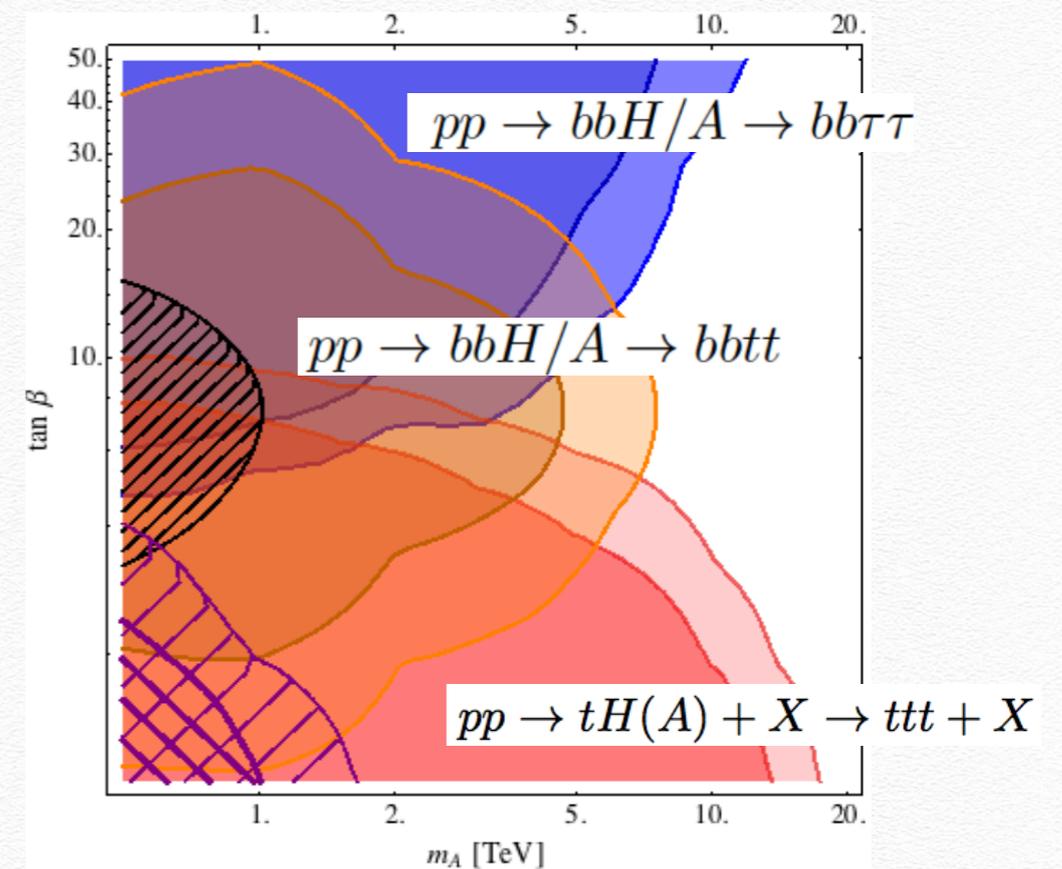
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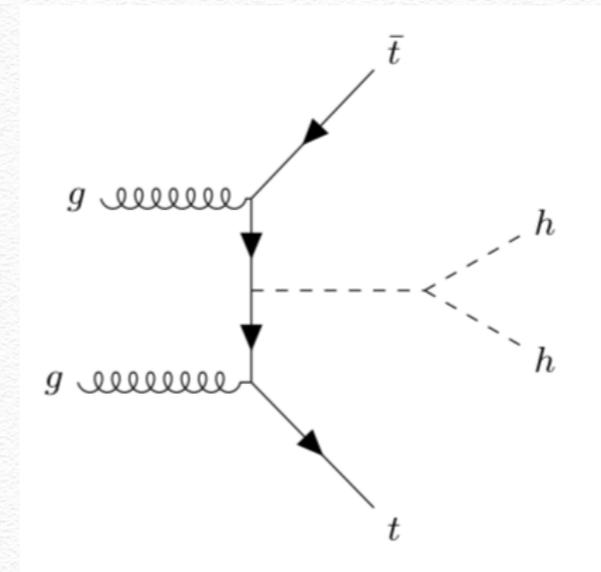
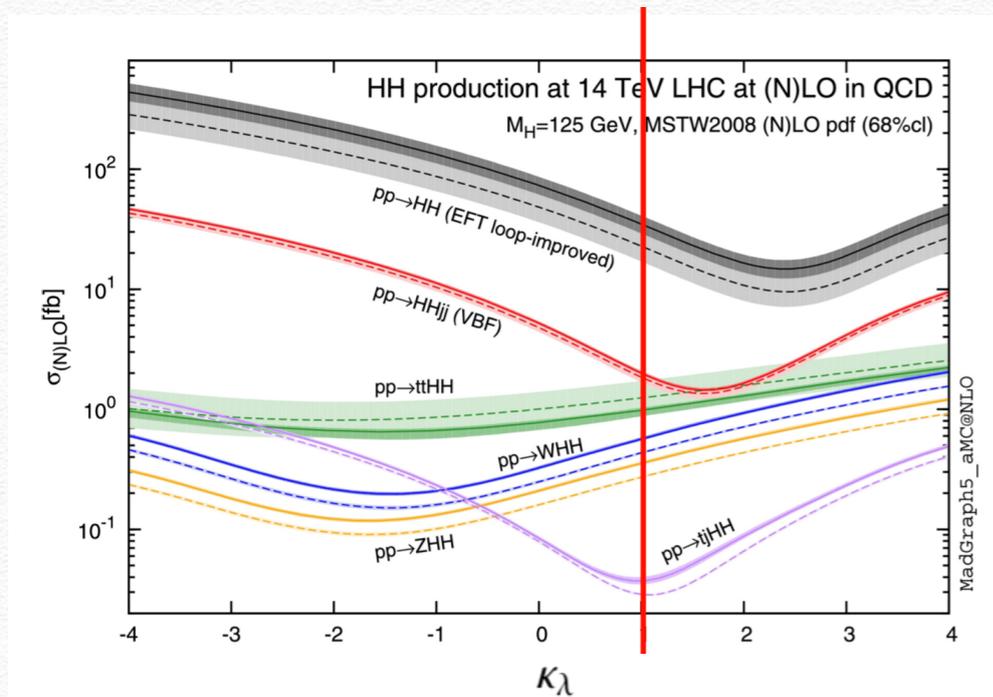
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Neutral Higgs Exclusion limit



# tthh channel analysis



tthh  $\rightarrow$  ttbbbb channel

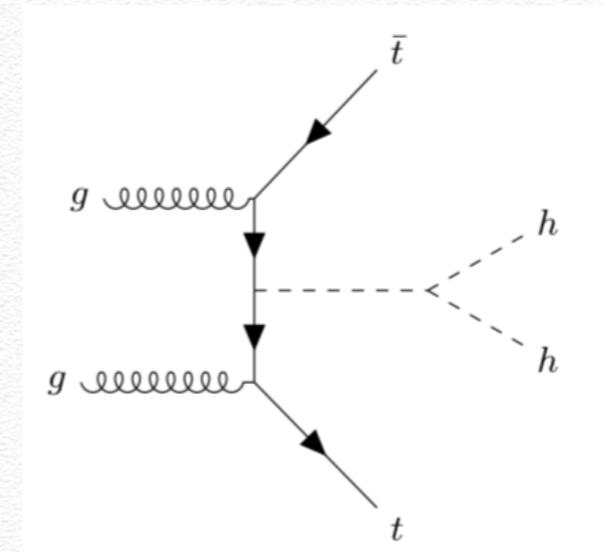
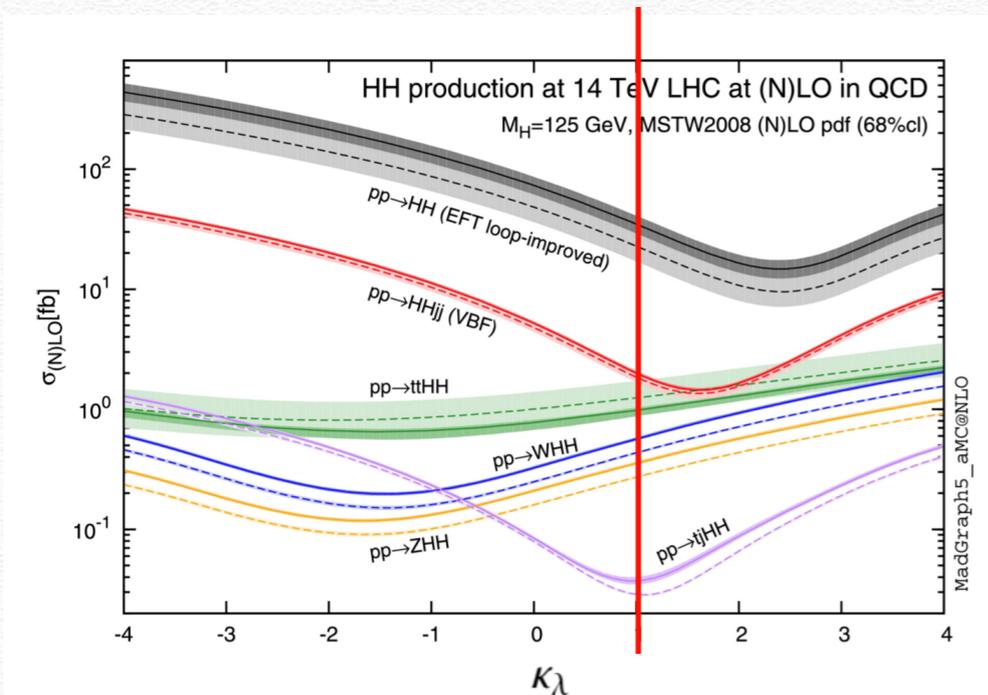
[T. Liu, H. Zhang, arXiv:1410.1855]

[C. Englert, et al. arXiv:1409.8074]

[ATL-PHYS-PUB-2016-023] with aggressive cut



# tthh channel analysis



tthh->ttbbbb channel

[T. Liu, H. Zhang, arXiv:1410.1855]

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[ATL-PHYS-PUB-2016-023] with aggressive cut

different decay channels with very rich kinematics, combining all channels?  
 complicated topologies, BDT method?



# tthh channel analysis

[L. Li, YYL, T. Liu, arXiv:1905.03772]

@HL-LHC

$5b1\ell$	$5b2\ell$	SS2 $\ell$	Multi- $\ell$	$\tau\tau$
-----------	-----------	------------	---------------	------------

5(or more)b+1 lepton

tt(semi-leptonic)bbbb

5(or more)b + OS dilepton

tt(leptonic)bbbb

SS dilepton (w/  $\geq 4$  b jets)

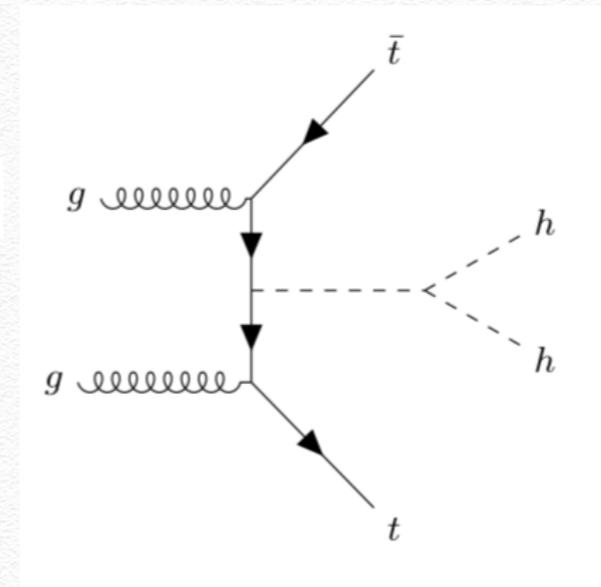
tt(semi)VV\*bb

Multi-lepton (w/  $\geq 4$  b jets)

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2 $\tau$  jets (w/  $\geq 4$  b jets & 1 lepton)

tt(semi)bb $\tau\tau$





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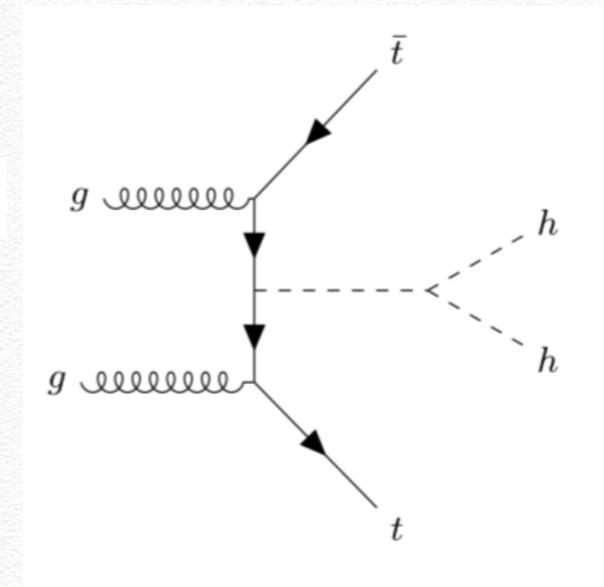
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Multi-lepton (w/  $\geq 4$  b jets)

tt(semi)VV\*bb

2 $\tau$  jets (w/  $\geq 4$ b jets & 1 lepton) tt(semi)bb $\tau\tau$



	No cut	Preselection	$5b1\ell$	$5b2\ell$	SS2 $\ell$	Multi- $\ell$	$\tau\tau$
$tthh$	2.9e3	7.37e2	50.9 (97.2)	6.1 (12.0)	14.6 (15.7)	8.6 (9.2)	3.6 (3.8)
$tt4b$	1.1e6	1.79e5	6.56e3 (1.31e4)	664 (1.30e3)	212 (223)	115 (121)	94.1 (95.1)
$tt2b2c$	3.1e5	4.28e4	621 (1.73e3)	59.4 (163)	38.0 (42.4)	24.1(26.8)	43.6 (48.6)
$ttVV$	4.4e4	3.64e3	20.7 (52.7)	3.5 (6.4)	51.8(60.9)	32.4 (36.5)	3.1 (3.9)
$4t$	3.54e4	1.30e4	350 (804)	68.3 (152)	592 (635)	307 (324)	59.8 (64.2)
$ttbbV$	8.29e4	1.54e4	353 (765)	47.8 (105)	114 (124)	203 (221)	22.2 (24.2)
$ttbbh$	4.68e4	1.04e4	608 (1.15e3)	69.0 (136)	91.0 (98.0)	53.4 (56.2)	24.2 (25.9)
$tthZ$	4.65e3	881	28.1 (58.5)	4.1 (9.1)	8.8 (9.5)	18.5 (19.9)	2.3 (2.5)
Total	1.6e6	2.65e5	8.53e3 (1.76e4)	918 (1.88e3)	1.11e3 (1.19e3)	753 (806)	249 (265)
$\sigma_{\text{cut}}$			0.46 (0.62)	0.17 (0.23)	0.39 (0.40)	0.28 (0.29)	0.20 (0.20)
$(S/B)_{\text{cut}}(\%)$			0.42 (0.40)	0.47 (0.55)	1.1 (1.1)	0.9 (0.9)	1.1 (1.1)

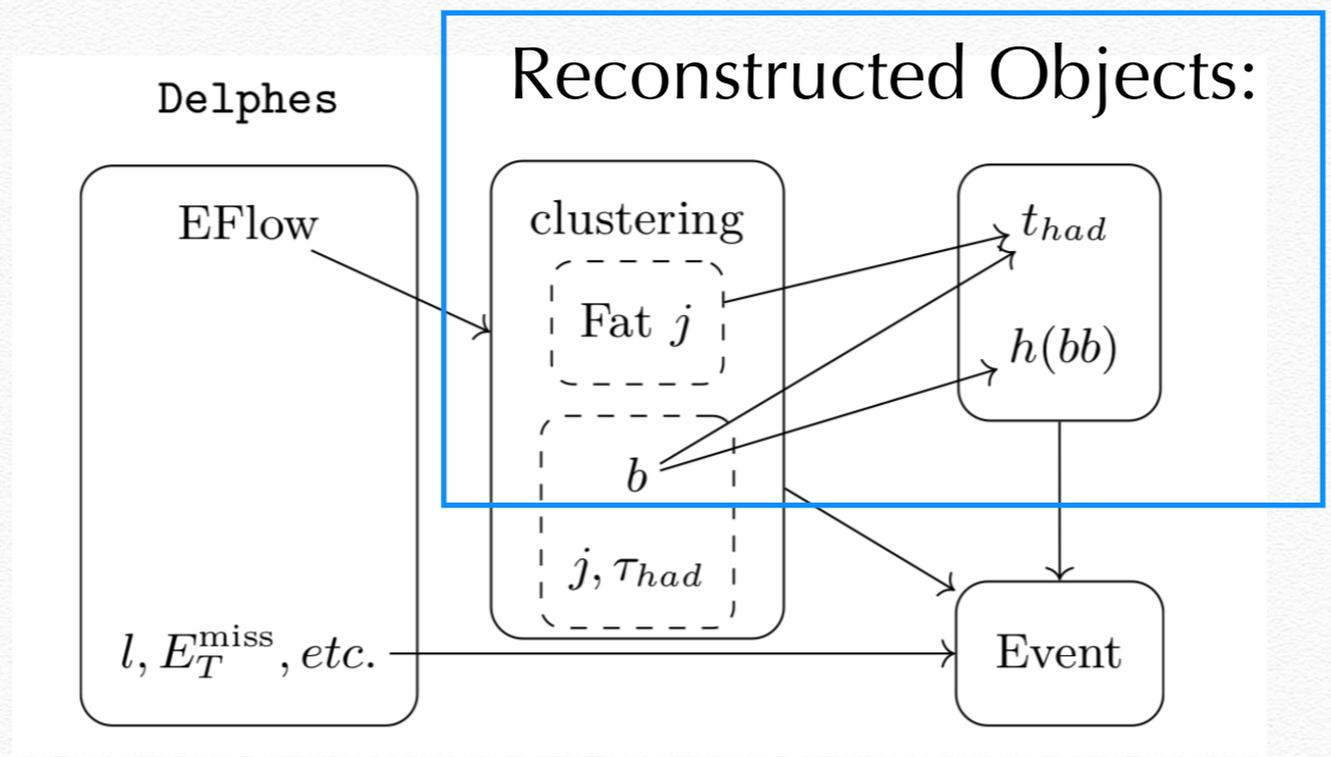
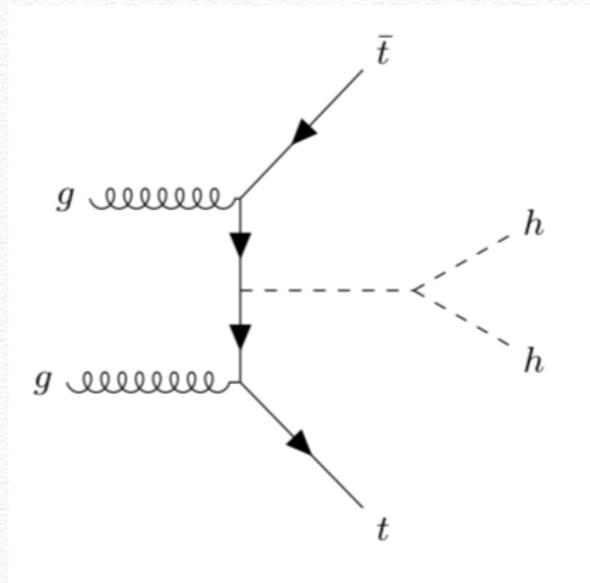


# tthh channel analysis

[L. Li, YYL, T. Liu, arXiv:1905.03772]

@HL-LHC

5b1l	5b2l	SS2l	Multi-l	$\tau\tau$
------	------	------	---------	------------



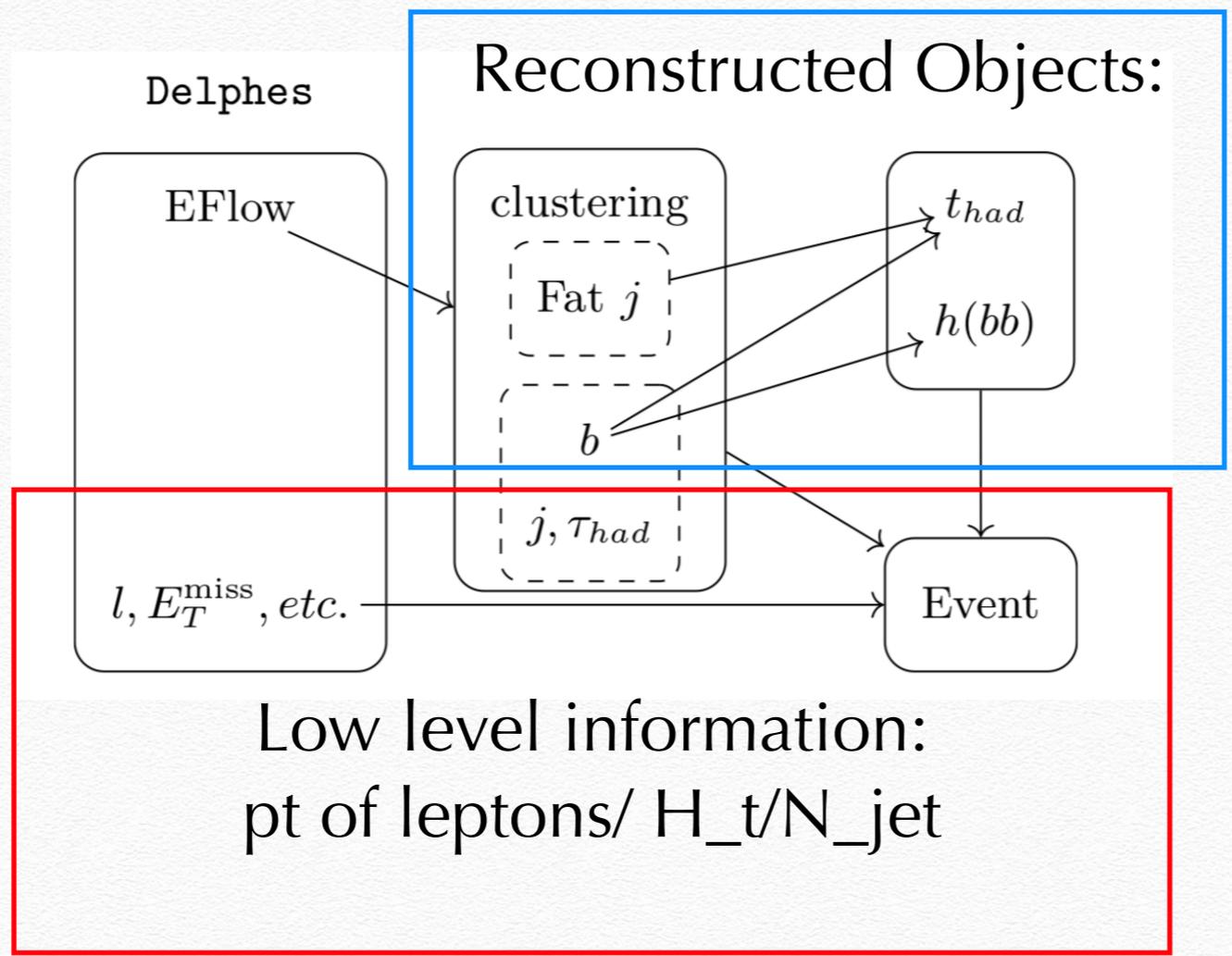
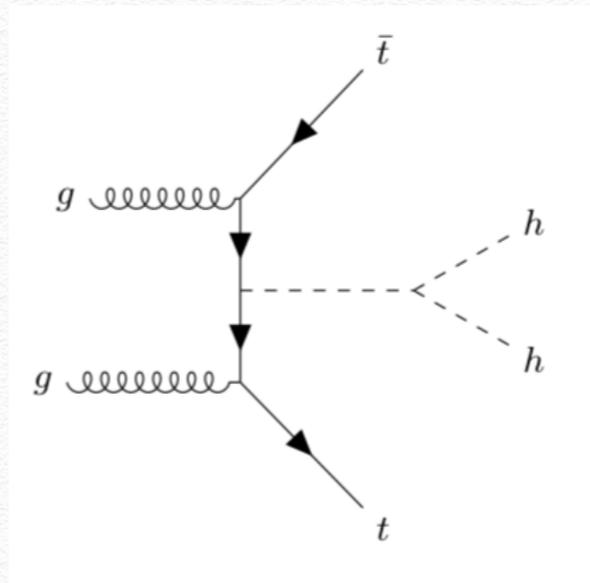


# tthh channel analysis

[L. Li, YYL, T. Liu, arXiv:1905.03772]

@HL-LHC

5b1l	5b2l	SS2l	Multi-l	$\tau\tau$
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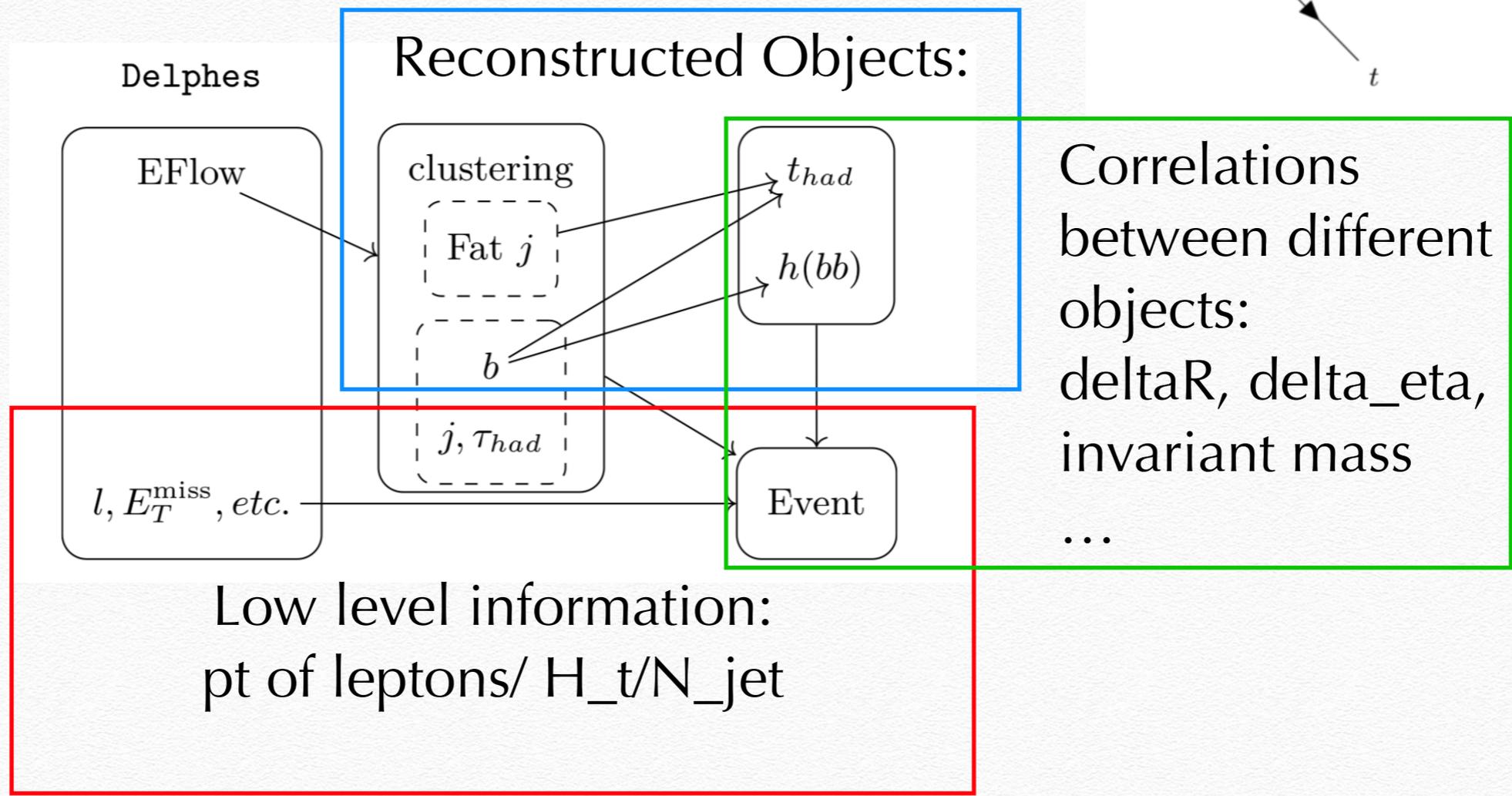
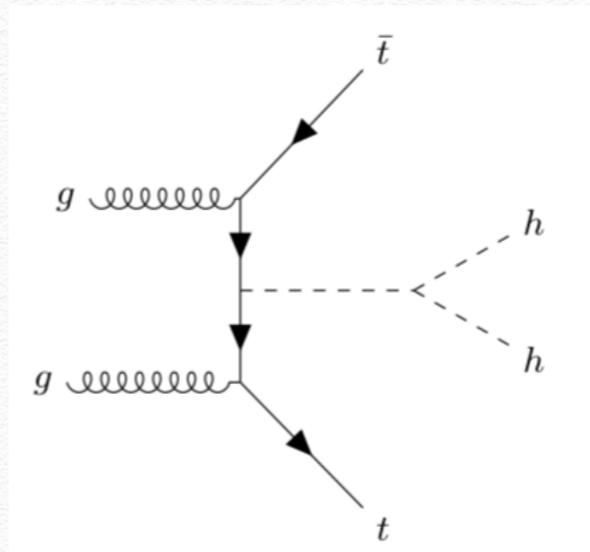


# tthh channel analysis

[L. Li, YYL, T. Liu, arXiv:1905.03772]

@HL-LHC

5b1l	5b2l	SS2l	Multi-l	$\tau\tau$
------	------	------	---------	------------



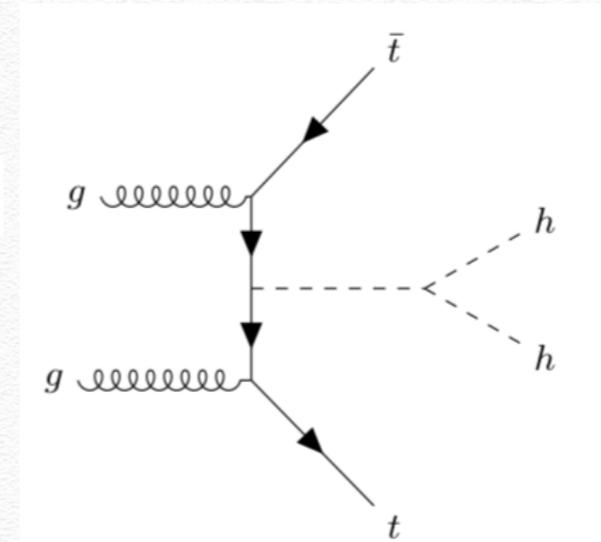


# tthh channel analysis

[L. Li, YYL, T. Liu, [arXiv:1905.03772](https://arxiv.org/abs/1905.03772)]

@HL-LHC

$5b1\ell$	$5b2\ell$	SS2 $\ell$	Multi- $\ell$	$\tau\tau$
-----------	-----------	------------	---------------	------------



$-10 < \kappa\lambda < 6.9@95\%C.L.$

	No cut	Preselection	$5b1\ell$	$5b2\ell$	SS2 $\ell$	Multi- $\ell$	$\tau\tau$
$tthh$	2.9e3	7.37e2	50.9 (97.2)	6.1 (12.0)	14.6 (15.7)	8.6 (9.2)	3.6 (3.8)
$tt4b$	1.1e6	1.79e5	6.56e3 (1.31e4)	664 (1.30e3)	212 (223)	115 (121)	94.1 (95.1)
$tt2b2c$	3.1e5	4.28e4	621 (1.73e3)	59.4 (163)	38.0 (42.4)	24.1(26.8)	43.6 (48.6)
$ttVV$	4.4e4	3.64e3	20.7 (52.7)	3.5 (6.4)	51.8(60.9)	32.4 (36.5)	3.1 (3.9)
$4t$	3.54e4	1.30e4	350 (804)	68.3 (152)	592 (635)	307 (324)	59.8 (64.2)
$ttbbV$	8.29e4	1.54e4	353 (765)	47.8 (105)	114 (124)	203 (221)	22.2 (24.2)
$ttbbh$	4.68e4	1.04e4	608 (1.15e3)	69.0 (136)	91.0 (98.0)	53.4 (56.2)	24.2 (25.9)
$tthZ$	4.65e3	881	28.1 (58.5)	4.1 (9.1)	8.8 (9.5)	18.5 (19.9)	2.3 (2.5)
Total	1.6e6	2.65e5	8.53e3 (1.76e4)	918 (1.88e3)	1.11e3 (1.19e3)	753 (806)	249 (265)
$\sigma_{\text{cut}}$			0.46 (0.62)	0.17 (0.23)	0.39 (0.40)	0.28 (0.29)	0.20 (0.20)
$(S/B)_{\text{cut}}(\%)$			0.42 (0.40)	0.47 (0.55)	1.1 (1.1)	0.9 (0.9)	1.1 (1.1)
$\sigma_{\text{BDT}}$			0.59 (0.79)	0.21 (0.30)	0.45 (0.46)	0.33 (0.35)	0.21 (0.21)
$(S/B)_{\text{BDT}}(\%)$			1.2 (1.0)	1.3 (1.6)	1.6 (1.6)	1.6 (1.9)	1.6 (1.6)
$\sigma_{\text{com}}$			0.86 (1.04)				

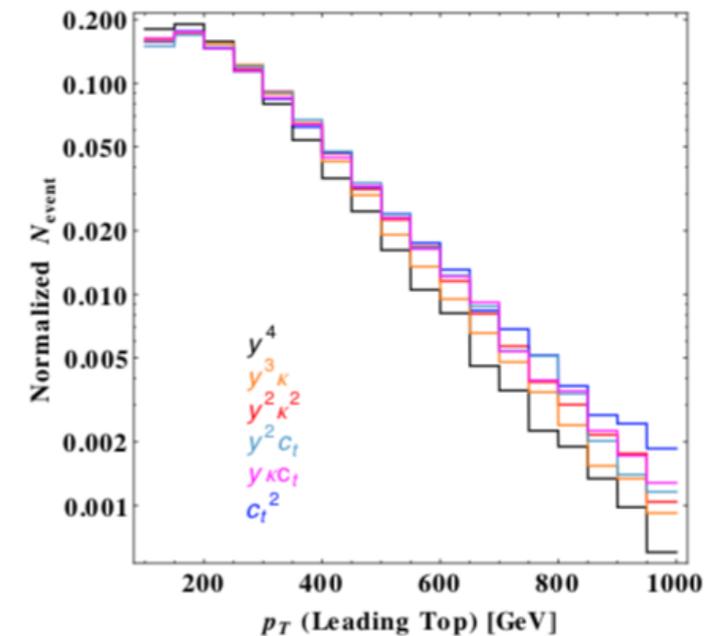
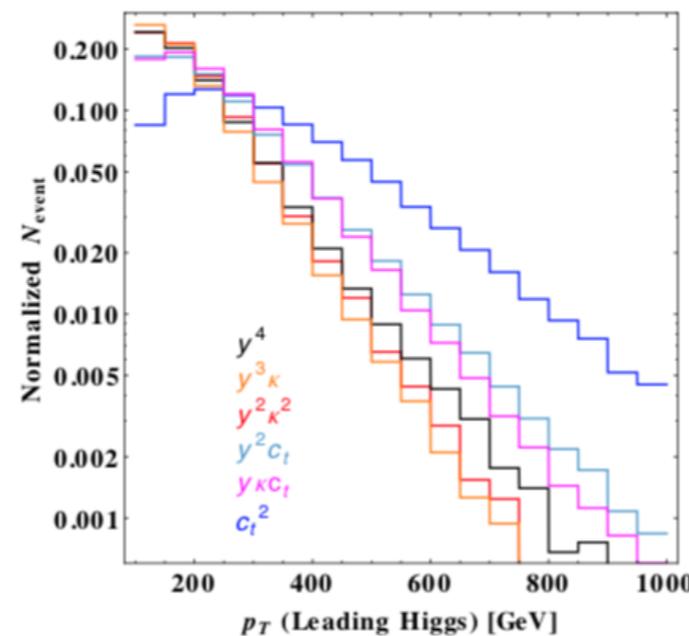
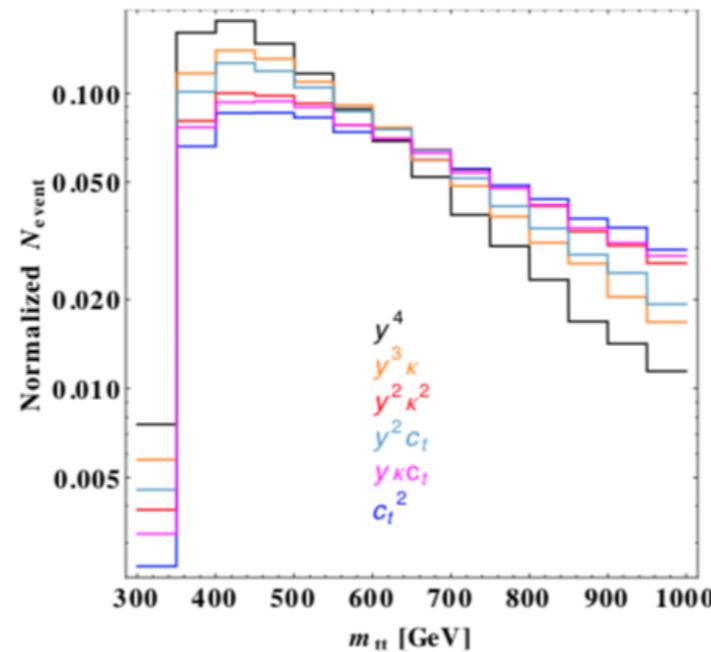
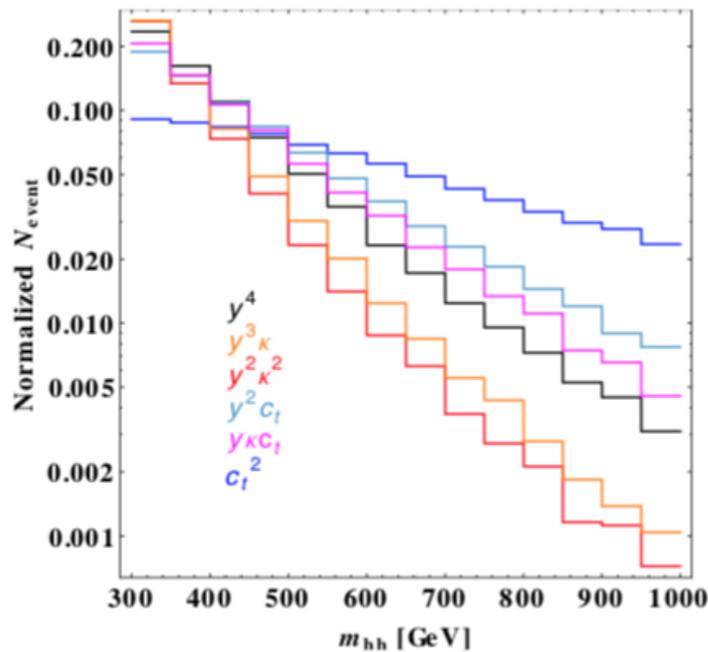
# tthh—contact interactions

$$\mathcal{L} \supset -y \frac{m_t}{v} t\bar{t}h - \kappa \frac{1}{3!} \frac{3m_h^2}{v} h^3 - c_t \frac{1}{2!} \frac{m_t}{v^2} t\bar{t}hh$$

Assuming SM top Yukawa coupling

@HL-LHC

[L. Li, YYL, T. Liu, arXiv:1905.03772]

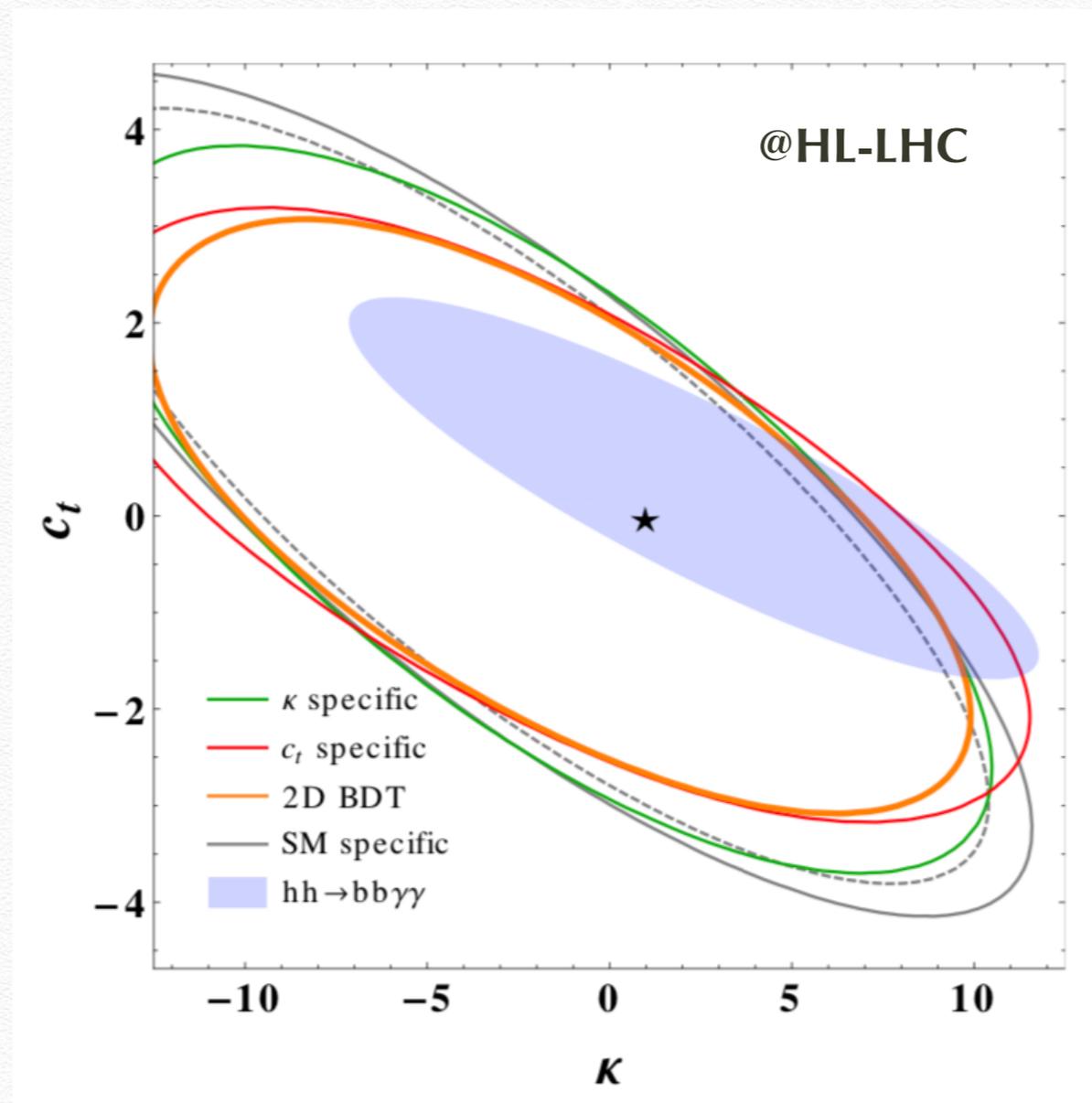


## tthh—contact interactions

$$\mathcal{L} \supset -y \frac{m_t}{v} t\bar{t}h - \kappa \frac{1}{3!} \frac{3m_h^2}{v} h^3 - c_t \frac{1}{2!} \frac{m_t}{v^2} t\bar{t}hh$$

Assuming SM top Yukawa coupling

[L. Li, YYL, T. Liu, arXiv:1905.03772]



Blue region is the exclusion limit based on gluon fusion channel projected from [ATL-PHYS-PUB-2018-053]

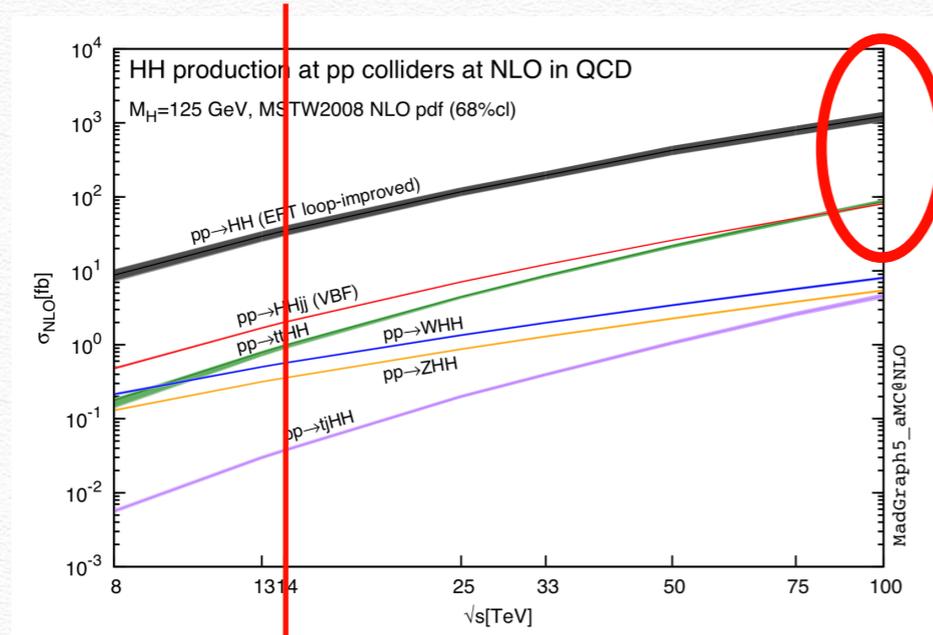
Partially breaks the degeneracy in the  $gg \rightarrow hh \rightarrow bb\gamma\gamma$

Kappa specific BDT help to improve the  $c_t$  direction.

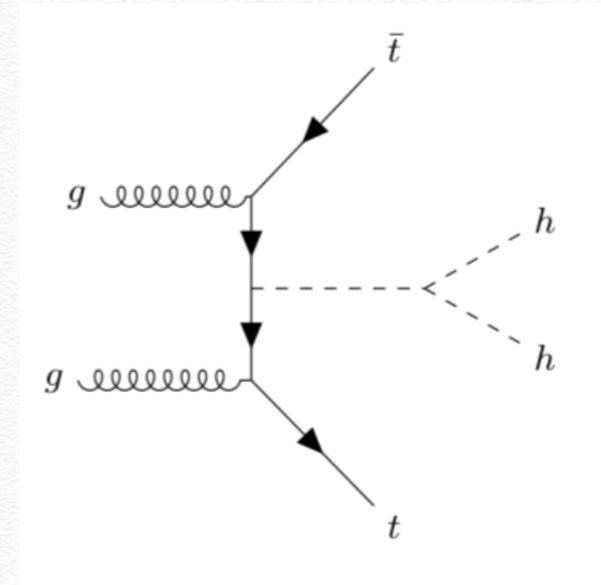
Kinematics help to further improve the sensitivity.



# tthh—Higgs self coupling measurement

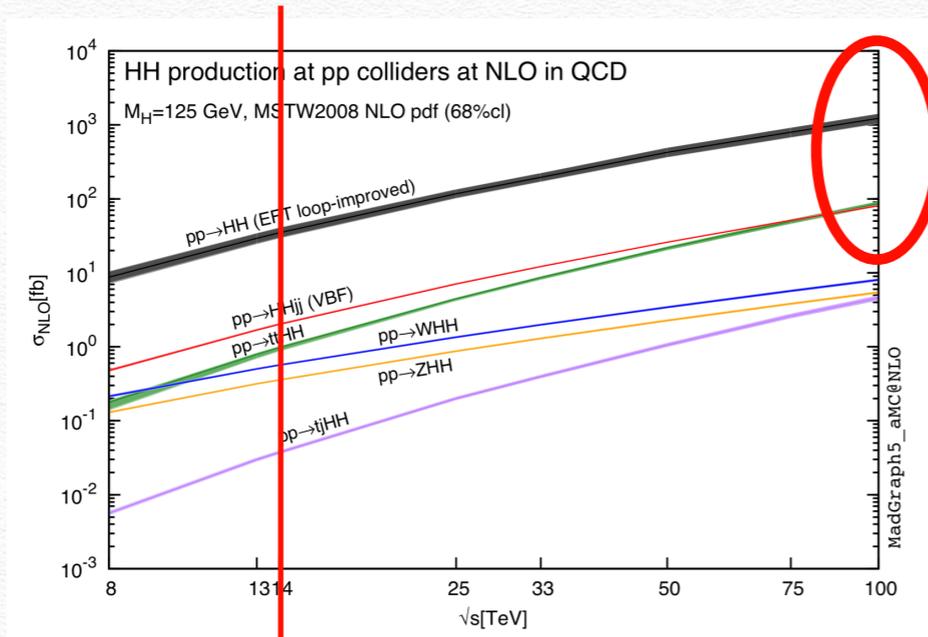


[R. Frederix, et al. arXiv:1401.7340]

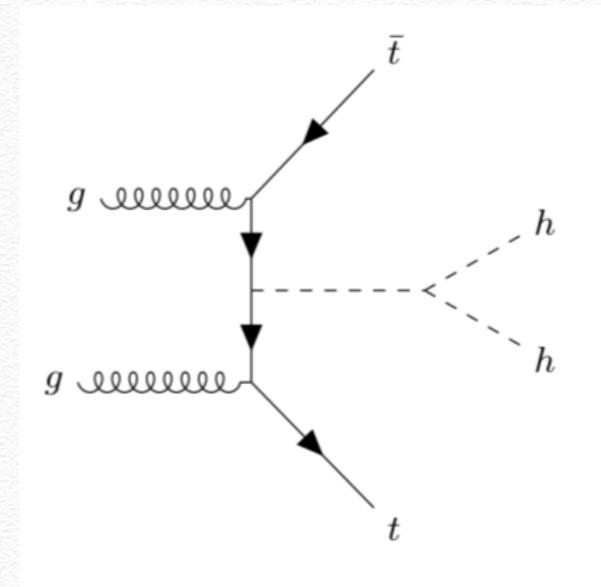




# tthh—Higgs self coupling measurement



[R. Frederix, et al. arXiv:1401.7340]



$$\frac{\sigma(gg \rightarrow hh \rightarrow bb\gamma\gamma)_{14}}{\sigma(gg \rightarrow hh \rightarrow bb\gamma\gamma)_{14}^{\text{SM}}} = 1.70 - 0.82\kappa + 0.12\kappa^2 - 3.79c_t + 0.98c_t\kappa + 2.68c_t^2$$

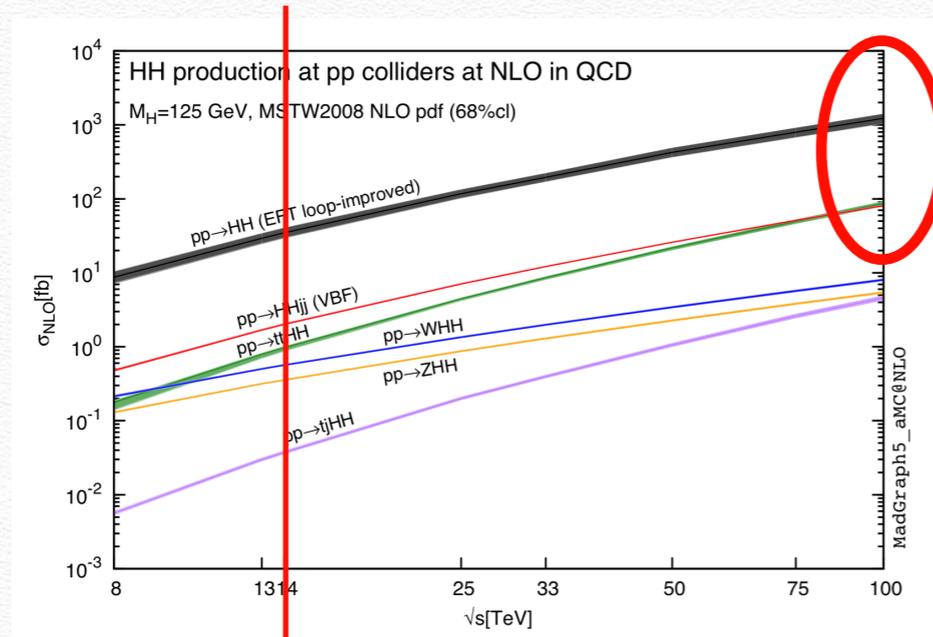
$$\frac{\sigma(gg \rightarrow hh \rightarrow bb\gamma\gamma)_{100}}{\sigma(gg \rightarrow hh \rightarrow bb\gamma\gamma)_{100}^{\text{SM}}} = 1.59 - 0.68\kappa + 0.09\kappa^2 - 3.83c_t + 0.92c_t\kappa + 3.20c_t^2$$

$$\frac{\sigma(tthh)_{14}}{\sigma(tthh)_{14}^{\text{SM}}} = 0.82 + 0.14\kappa + 0.04\kappa^2 + 0.28c_t + 0.21\kappa c_t + 0.44c_t^2$$

$$\frac{\sigma(tthh)_{100}}{\sigma(tthh)_{100}^{\text{SM}}} = 0.84 + 0.07\kappa + 0.09\kappa^2 + 0.15c_t + 0.41\kappa c_t + 1.73c_t^2$$



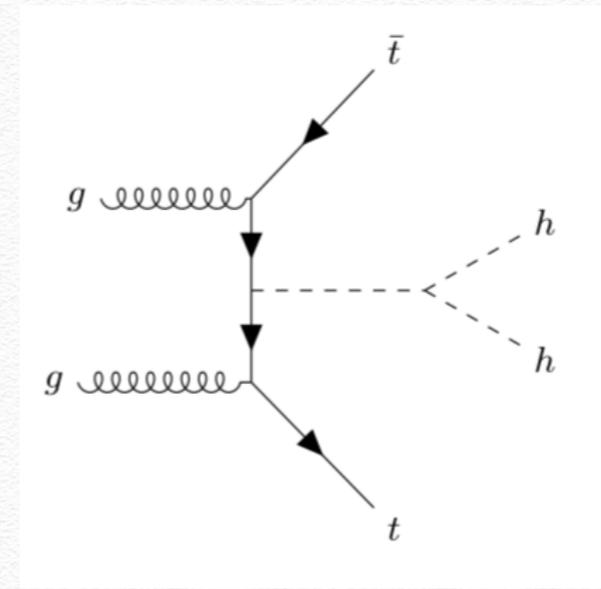
# tthh—Higgs self coupling measurement



[R. Frederix, et al. arXiv:1401.7340]

[S. Banerjee, et al. arXiv:1904.07886]

$\sim 5.9\sigma$  @100TeV 30/ab  
 $-3.01 < \kappa\lambda < 1.65$  @68% C.L.



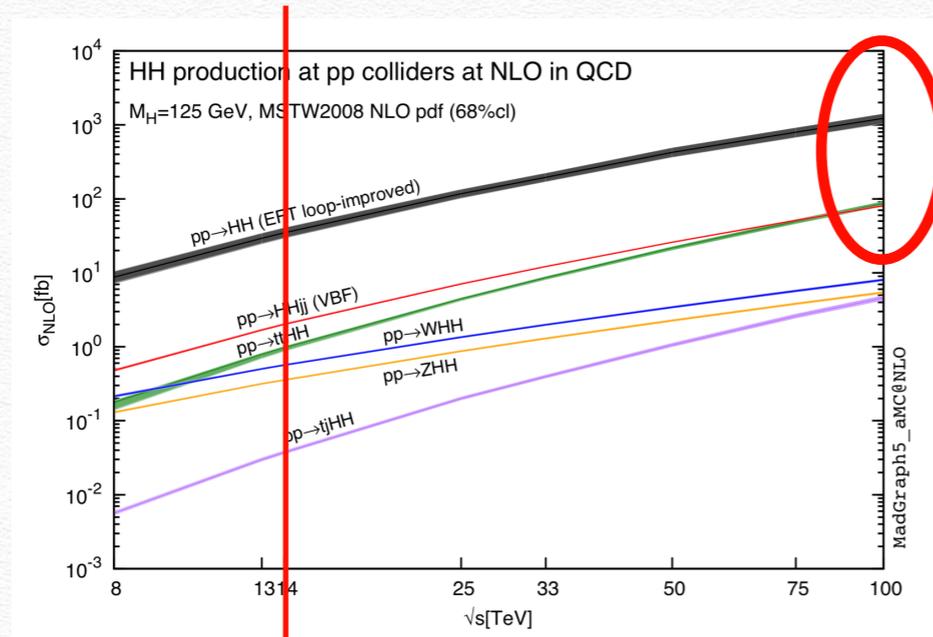
[L. Li, YYL, T. Liu, arXiv:1905.03772]

Projected @ 100TeV 30/ab  
 $\sim 14.3\sigma$

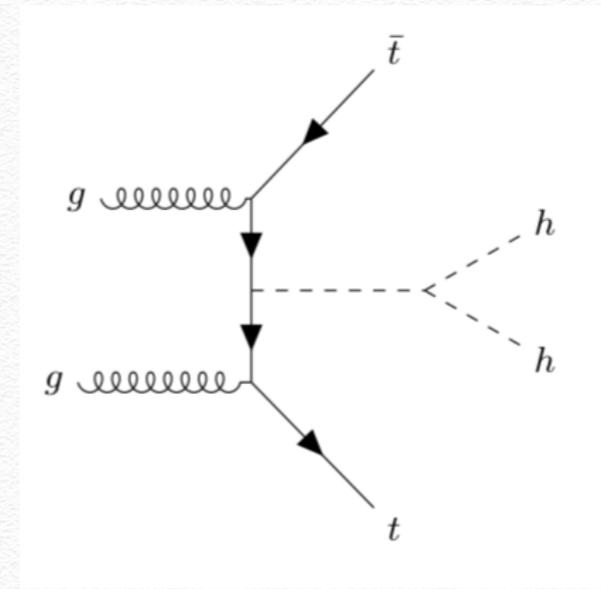
$-2.6 < \kappa\lambda < -1.6$  U  $0.2 < \kappa\lambda < 1.6$  @95% C.L.  
 gain mainly from combing all decay channels



# tthh—Higgs self coupling measurement



[R. Frederix, et al. arXiv:1401.7340]

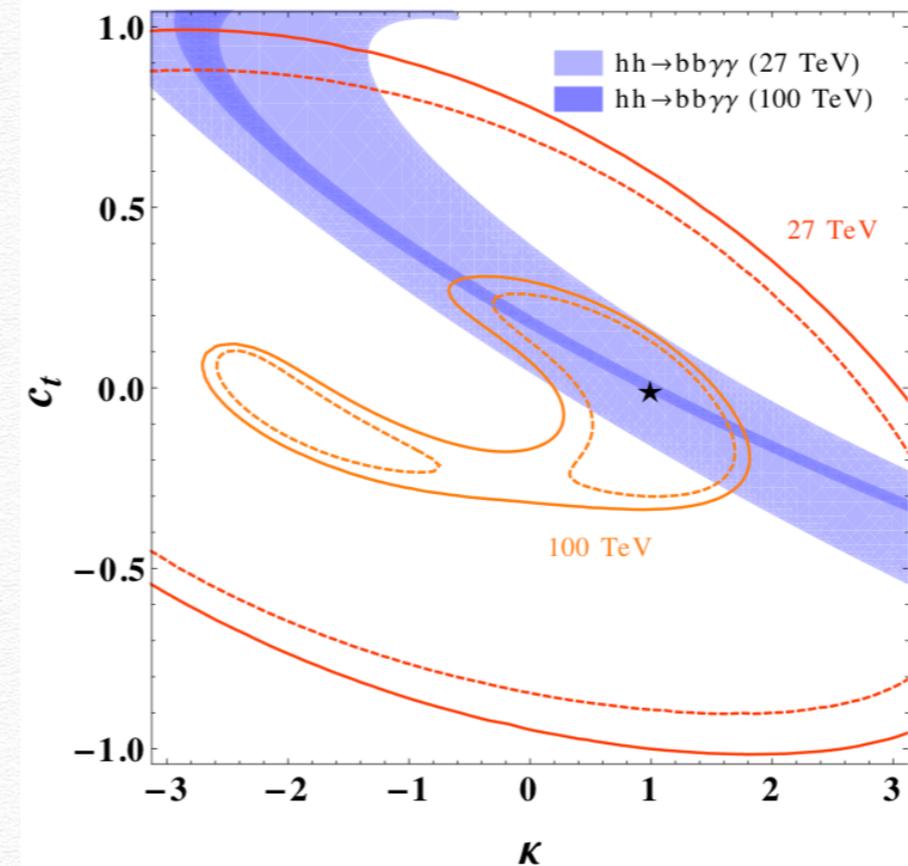


[L. Li, YYL, T. Liu, arXiv:1905.03772]

fitting to  $\{\kappa, c_t\} = \{1, 0\}$

cross section contour centre around  $\{\kappa, c_t\} = \{0, 0\}$

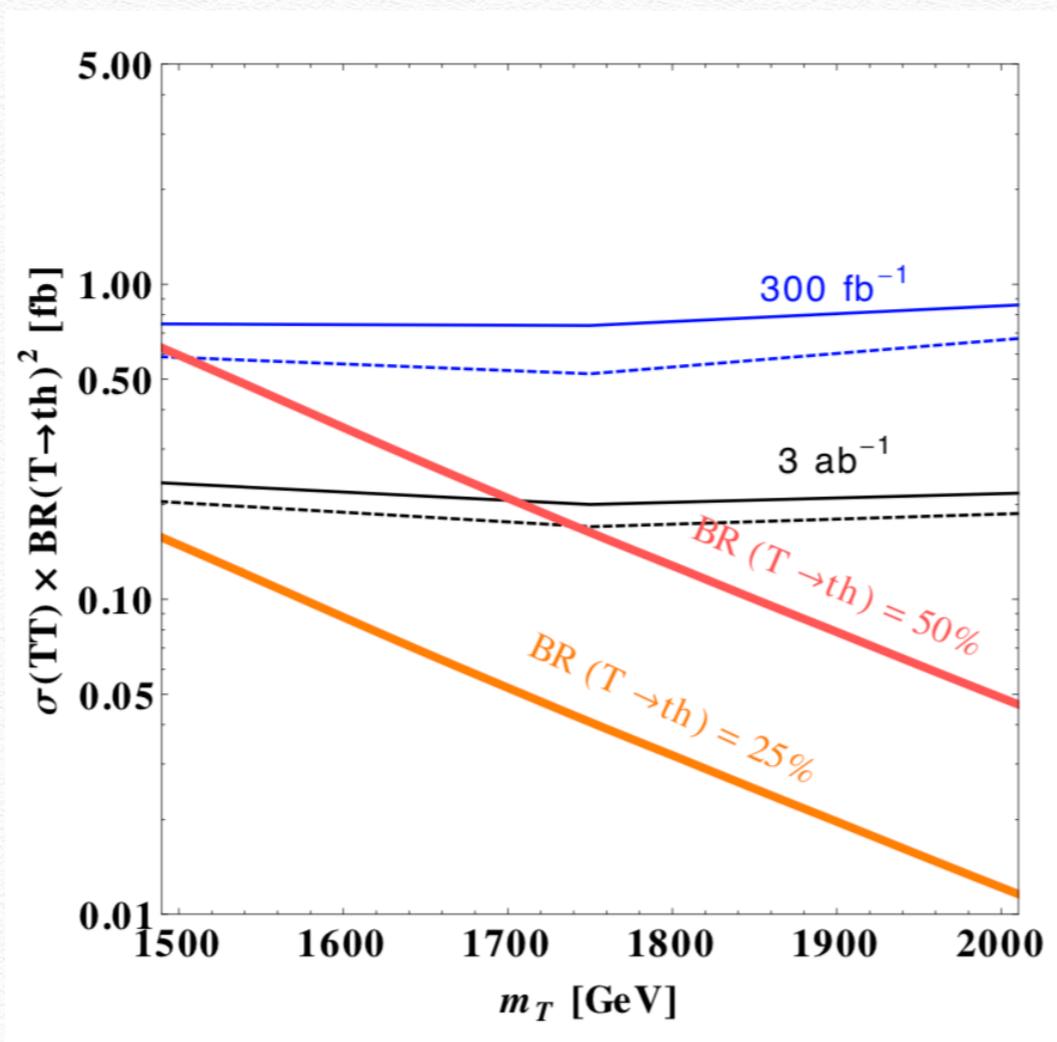
Encouraging from comparison with blue region, could be further improved by utilising kinematics.



# tthh—Resonance Search—fermions

## Coloured vector-like top partners

[L. Li, YYL, T. Liu, [arXiv:1905.03772](#)]



Limit is improved by combining all decay channels compared with that in [\[ATLAS, arXiv:1808.02343\]](#)

# tthh—Resonance Search—scalars

[L. Li, YYL, T. Liu, arXiv:1905.03772]

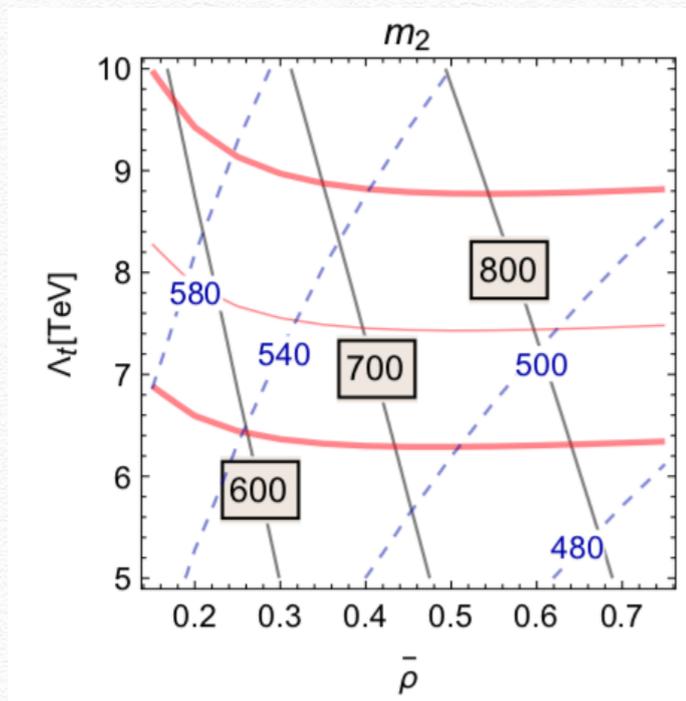
@HL-LHC

	5b1 $\ell$ (fb)	5b2 $\ell$ (fb)	SS2 $\ell$ (fb)	Multi- $\ell$ (fb)	$\tau\tau$ (fb)	Combined (fb)
$ttH, m_H = 300$ GeV	3.6 (2.4)	10 (7.4)	6.8 (6.5)	9.2 (8.9)	12 (11)	2.5 (2.2)
$ttH, m_H = 500$ GeV	2.6 (2.0)	7.6 (5.7)	5.3 (5.1)	7.4 (7.2)	8.0 (7.7)	2.0 (1.6)

$ttH, m_H=600\text{GeV}$

1.8

[P. Asadi, N. Craig, YYL, arXiv:1810.09467]



@HL-LHC with  $f/v \sim 3$ ,  $m_{h2} = 600\text{GeV}$ ,

$$\sigma(tt h_2 \rightarrow tthh) \sim 0.1 \text{ fb}$$



# tthh—Resonance Search—scalars

[L. Li, YYL, T. Liu, arXiv:1905.03772]

**@HL-LHC**

	5b1l (fb)	5b2l (fb)	SS2l (fb)	Multi-l (fb)	$\tau\tau$ (fb)	Combined (fb)
$ttH, m_H = 300 \text{ GeV}$	3.6 (2.4)	10 (7.4)	6.8 (6.5)	9.2 (8.9)	12 (11)	2.5 (2.2)
$ttH, m_H = 500 \text{ GeV}$	2.6 (2.0)	7.6 (5.7)	5.3 (5.1)	7.4 (7.2)	8.0 (7.7)	2.0 (1.6)

$ttH, m_H=600\text{GeV}$

1.8

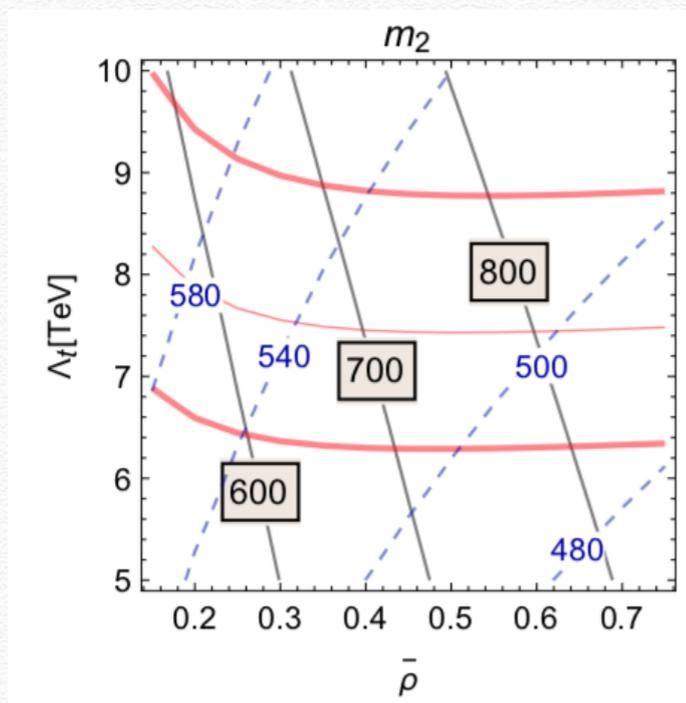
**@100TeV 30/ab**

	Combined (fb)
$ttH, m_H = 500 \text{ GeV}$	6.6(5.3)

$ttH, m_H=600\text{GeV}$  5.8

$ttH, m_H=800\text{GeV}$  3.2

[P. Asadi, N. Craig, YYL, arXiv:1810.09467]



**@HL-LHC with  $f/v \sim 3$ ,  $m_{H2} = 600\text{GeV}$ ,**

$$\sigma(ttH_2 \rightarrow tthh) \sim 0.1 \text{ fb}$$

**@100TeV with  $f/v \sim 3$ ,  $m_{H2} = 600\text{GeV}$ ,**

$$\sigma(ttH_2 \rightarrow tthh) \sim 21 \text{ fb}$$

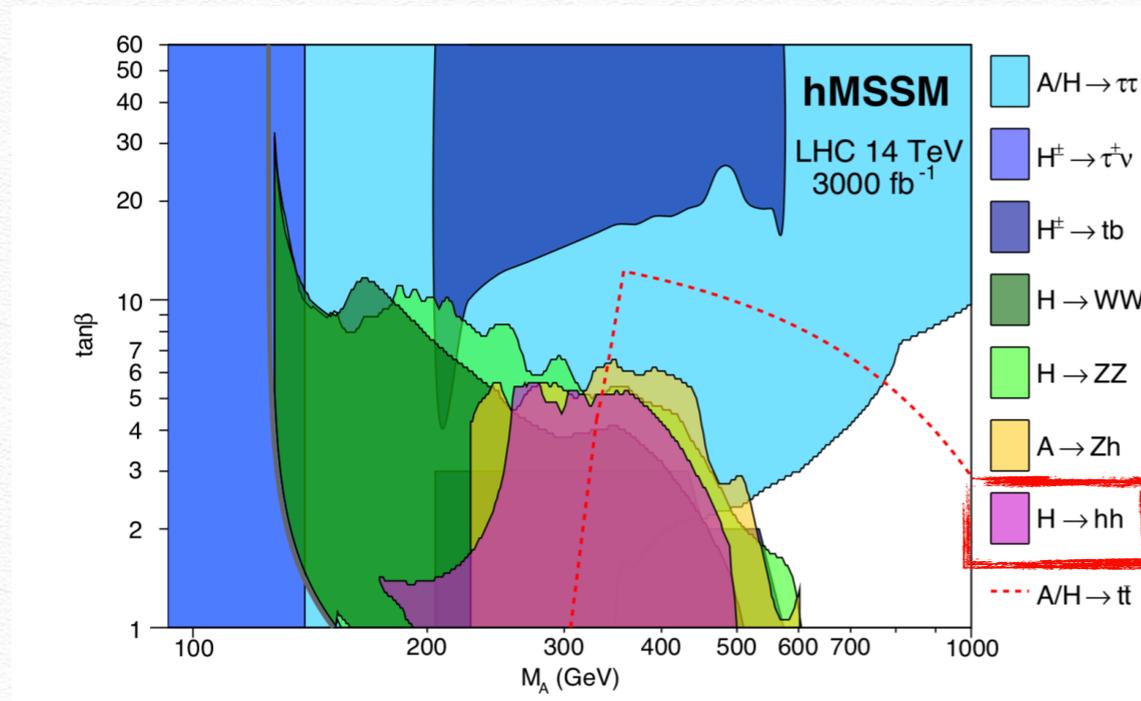
able to discover the turtling structure@100TeV!

# tthh—Resonance Search—scalars

MSSM Higgs bosons(no CP-violation):H,A,Hc

Higgs mass spectrum and couplings only depend on two parameters (in addition to the SM ones) at tree-level:  $\tan_\beta$ ,  $m_A/m_{Hc}$ ;

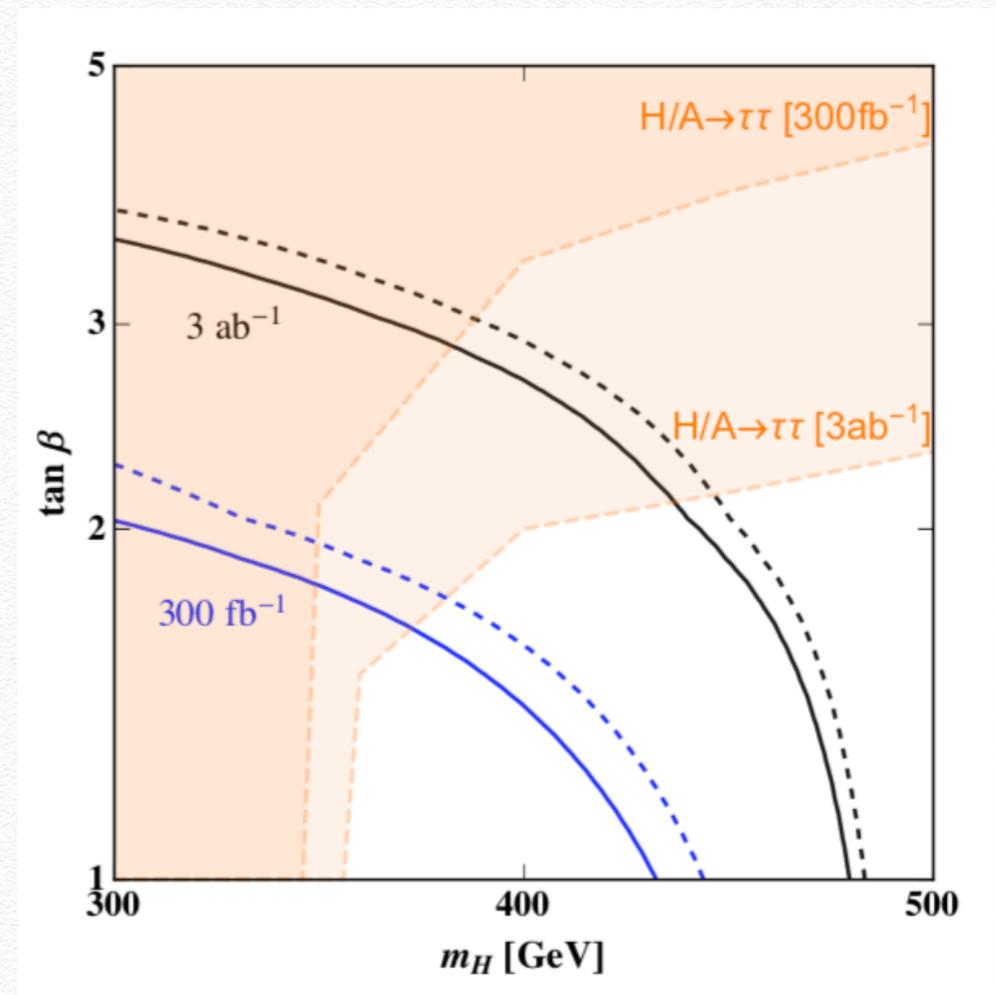
[A. Djouadi, et al. arXiv:1502.05653]



not bad compared with  $gg \rightarrow H \rightarrow hh$  channel

**Decay products from associated top help!**

[L. Li, YYL, T. Liu, arXiv:1905.03772]





## tthh—Conclusion and Outlook

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I have talked about tthh potential in

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Higgs Self Coupling Measurement

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Contact Interaction Measurement

---

Complementary to gluon fusion channel because of constructive interference;  
combining all decay channels to further improve the sensitivity;  
gain at 100TeV collider from kinematics potential ;

Resonant Search

---

heavy fermions, heavy scalars in turtling models/MSSM;  
able to probe the turnling structure at 100TeV colliders.

Outlook

---

including kinematics at 100TeV?? way to simulate the bg  
tthh potential with  $hh \rightarrow b\bar{b}aa$  at 100TeV??



We are heading forward to the truth of our nature  
gradually and passionately

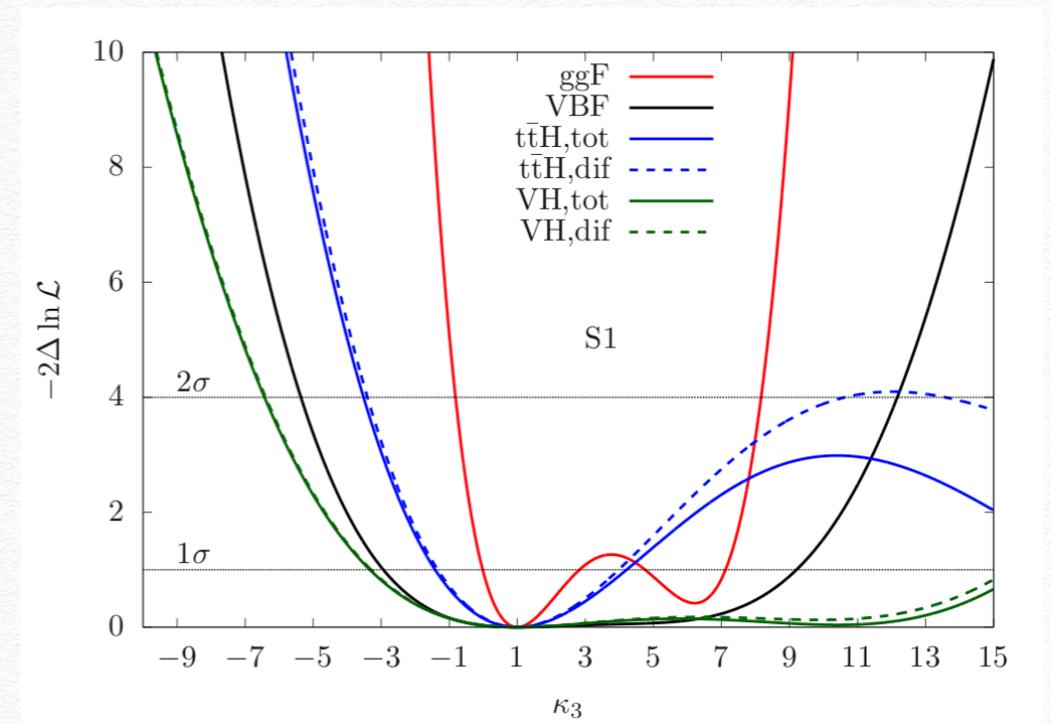
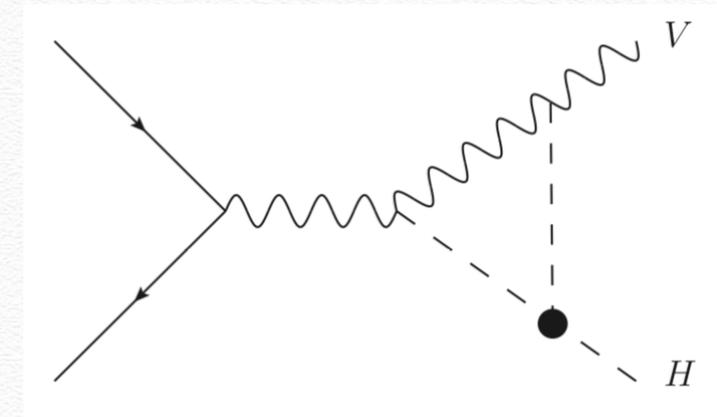
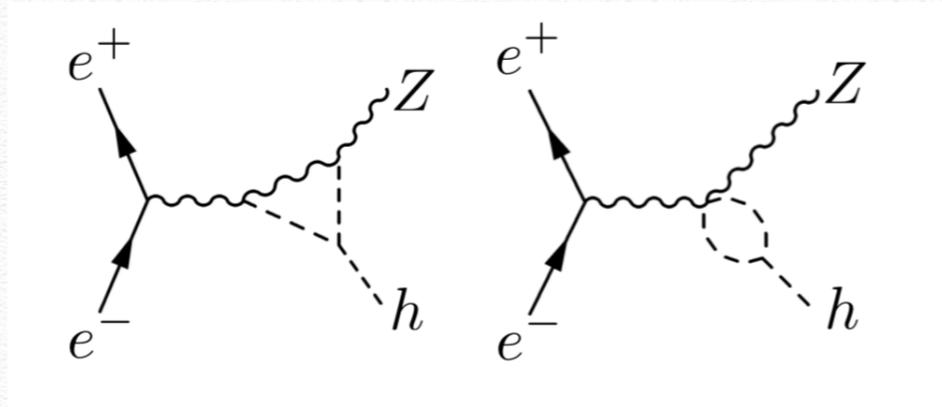
*Thank YOU!*

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# Higgs Self Coupling — indirect measurement

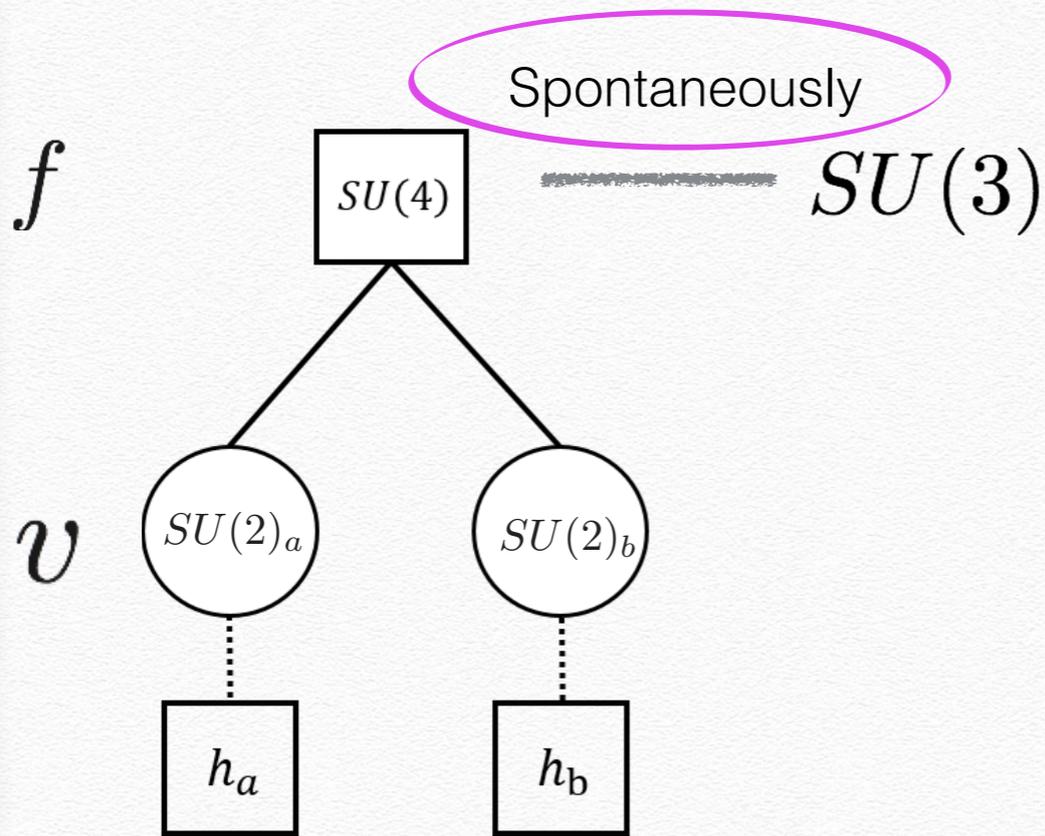
[Matthew McCullough arXiv:1312.3322]



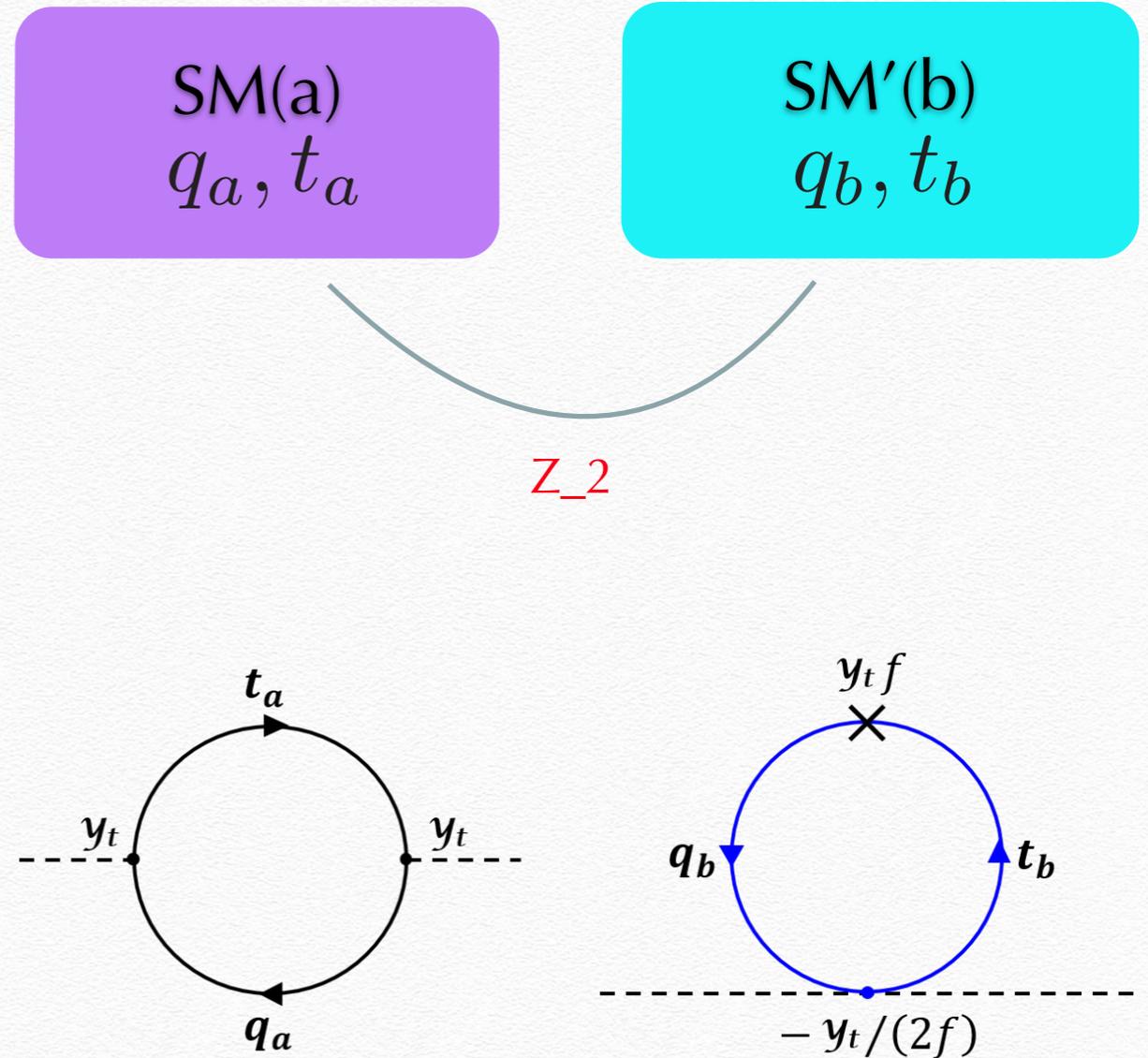
[F. Maltoni, et al. arXiv:1709.08649]

# tthh—Resonance Search—scalars

[Z.Chacko, Hock-Seng Goh and Roni Harnik] (2005)



$$[SU(3) \times SU(2) \times U(1)]_{a,b}$$



# tthh—Resonance Search—scalars

[Z.Chacko, Hock-Seng Goh and Roni Harnik] (2005)

$$v = \langle \mathbf{h} \rangle \ll f$$

$$V = \lambda(|h_a|^2 + |h_b|^2)^2 + m_h^2(|h_a|^2 + |h_b|^2) + \kappa(|h_a|^4 + |h_b|^4) + \rho|h_a|^4 + \mu^2|h_a|^2$$

●  $\rho|_{tree} = 0$

$$\Delta_{v/\Lambda}^{TH} \equiv \frac{d \log v^2}{d \log \Lambda^2} = \frac{\partial \log v^2}{\partial \log f^2} \frac{d \log f^2}{d \log \Lambda^2} + \frac{\partial \log v^2}{\partial \log \Lambda^2}$$

[Barbieri-Giudice measure](1988)

$$\Delta_{v/\Lambda}^{TH,soft} \approx \frac{1}{64\pi^2} \left( \frac{3y_t^2}{\lambda} \frac{\Lambda_t^2}{v^2} - 5 \frac{\Lambda_\rho^2}{v^2} \right)$$

$$\Delta_{v/\Lambda}^{SM} \approx \frac{1}{32\pi^2} \left( \frac{3y_t^2}{\lambda_{SM}} \frac{\Lambda_t^2}{v^2} - 3 \frac{\Lambda_\rho^2}{v^2} \right)$$

Tuning improvement:  $\frac{\lambda_{SM}}{2\lambda}$ , UV-extension is needed

# tthh—Resonance Search—scalars

[P. Asadi, N. Craig, YYL, arXiv:1810.09467]

## Turtling structure for twin Higgs

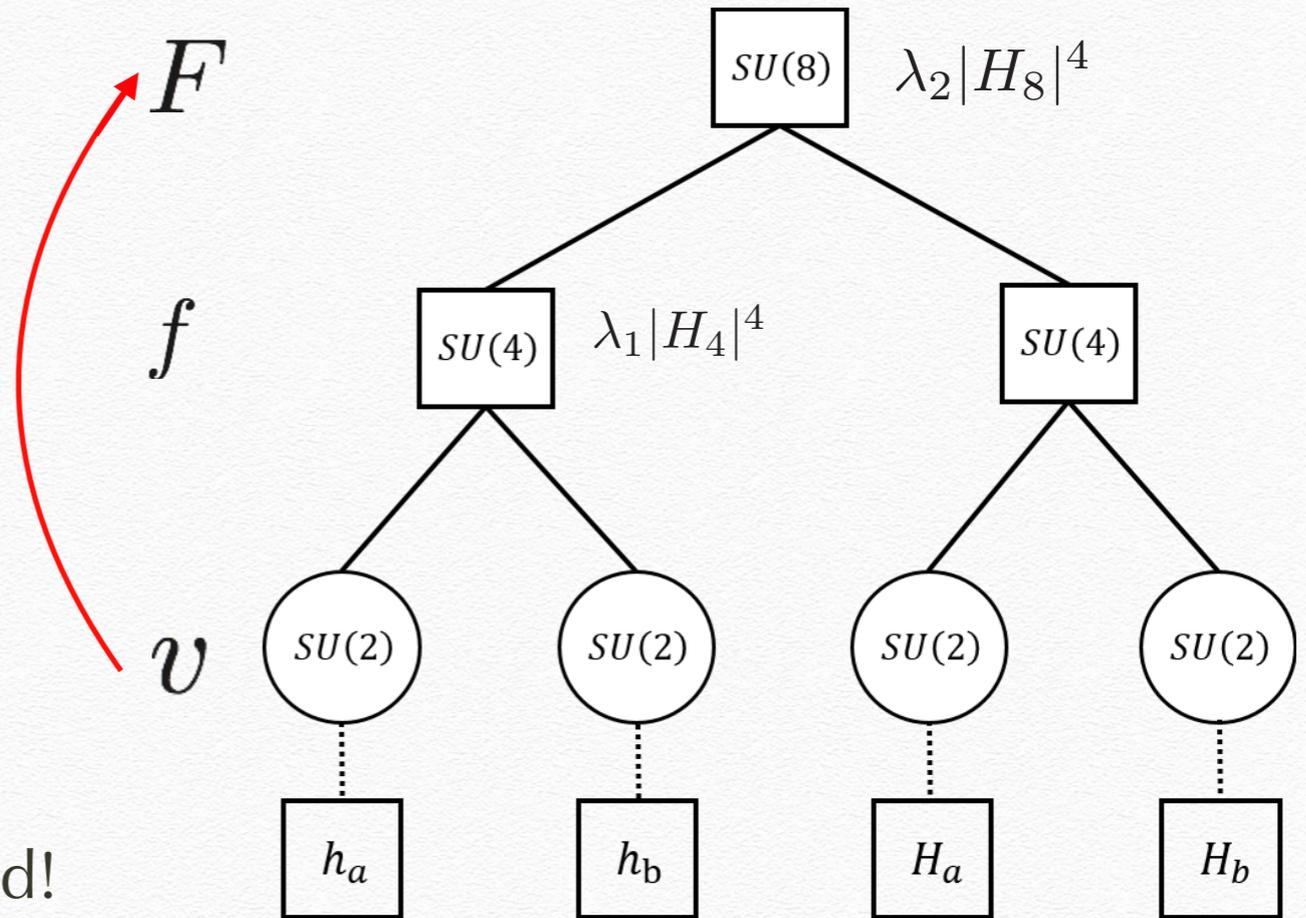
Symmetry breaking scale protected by another breaking of global symmetry

$$\frac{\lambda_{SM}}{2\lambda} \rightarrow \frac{\lambda_{SM}}{2\lambda_1} \times \frac{\lambda_1}{2\lambda_2} \times \dots \times \frac{\lambda_{n-1}}{2\lambda_n}$$

Landau pole scale not too low=>

$$\text{NEED } \lambda_i < \lambda_{i-1}$$

the tuning is not really improved!



## tthh—Resonance Search—scalars

$$V = \lambda(|h_a|^2 + |h_b|^2)^2 + m_h^2(|h_a|^2 + |h_b|^2) + \kappa(|h_a|^4 + |h_b|^4) + \rho|h_a|^4 + \mu^2|h_a|^2$$

●  $\rho|_{tree} \neq 0$  [A.Katz, et al. arXiv:1611.08615]

$$\Delta_{v/\Lambda}^{\text{TH,hard}} = \frac{1}{64\pi^2} \frac{2\kappa}{2\kappa + \rho} \left( \frac{3y_t^2}{\lambda} \frac{\Lambda_t^2}{v^2} - \left( 5 + 3\epsilon_{\pm} \frac{\rho}{\kappa} \right) \frac{\Lambda_{\rho}^2}{v^2} \right)$$

$$m_{SM}^2 = 4v^2(2\kappa + \rho)\left(1 - \frac{v^2}{f^2}\right) \quad 2\kappa + \rho \sim \lambda_{SM}$$

## tthh—Resonance Search—scalars

$$V = \lambda(|h_a|^2 + |h_b|^2)^2 + m_h^2(|h_a|^2 + |h_b|^2) + \kappa(|h_a|^4 + |h_b|^4) + \rho|h_a|^4 + \mu^2|h_a|^2$$

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$$\Delta_{v/\Lambda}^{\text{TH,hard}} = \frac{1}{64\pi^2} \frac{2\kappa}{2\kappa + \rho} \left( \frac{3y_t^2}{\lambda} \frac{\Lambda_t^2}{v^2} - \left( 5 + 3\epsilon_{\pm} \frac{\rho}{\kappa} \right) \frac{\Lambda_{\rho}^2}{v^2} \right)$$

$$m_{SM}^2 = 4v^2(2\kappa + \rho)\left(1 - \frac{v^2}{f^2}\right)$$

$$2\kappa + \rho \sim \lambda_{SM}$$

## tthh—Resonance Search—scalars

$$V = \lambda(|h_a|^2 + |h_b|^2)^2 + m_h^2(|h_a|^2 + |h_b|^2) + \kappa(|h_a|^4 + |h_b|^4) + \rho|h_a|^4 + \mu^2|h_a|^2$$

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$$\Delta_{v/\Lambda}^{\text{TH,hard}} = \frac{1}{64\pi^2} \frac{2\kappa}{2\kappa + \rho} \left( \frac{3y_t^2}{\lambda} \frac{\Lambda_t^2}{v^2} - \left( 5 + 3\epsilon_{\pm} \frac{\rho}{\kappa} \right) \frac{\Lambda_{\rho}^2}{v^2} \right)$$

$$m_{SM}^2 = 4v^2(2\kappa + \rho)\left(1 - \frac{v^2}{f^2}\right) \quad 2\kappa + \rho \sim \lambda_{SM}$$

$$\Lambda_t \sim 5\text{TeV} \Rightarrow 2\kappa|_{loop} \sim \lambda_{SM}$$

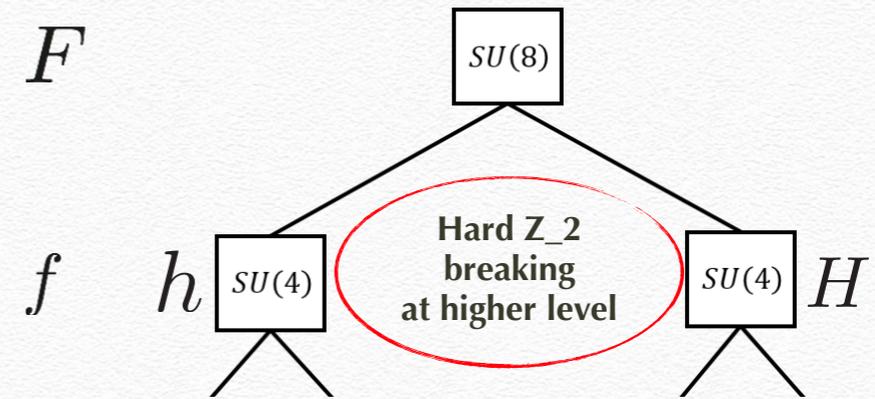
Tuning cannot be improved by much!

# tthh—Resonance Search—scalars

[P. Asadi, N. Craig, YYL, arXiv:1810.09467]

## Turtling structure for twin Higgs

Symmetry breaking scale protected by another breaking of global symmetry  
With hard breaking in the higher level  
To reduce tuning and push the cutoff to a higher scale



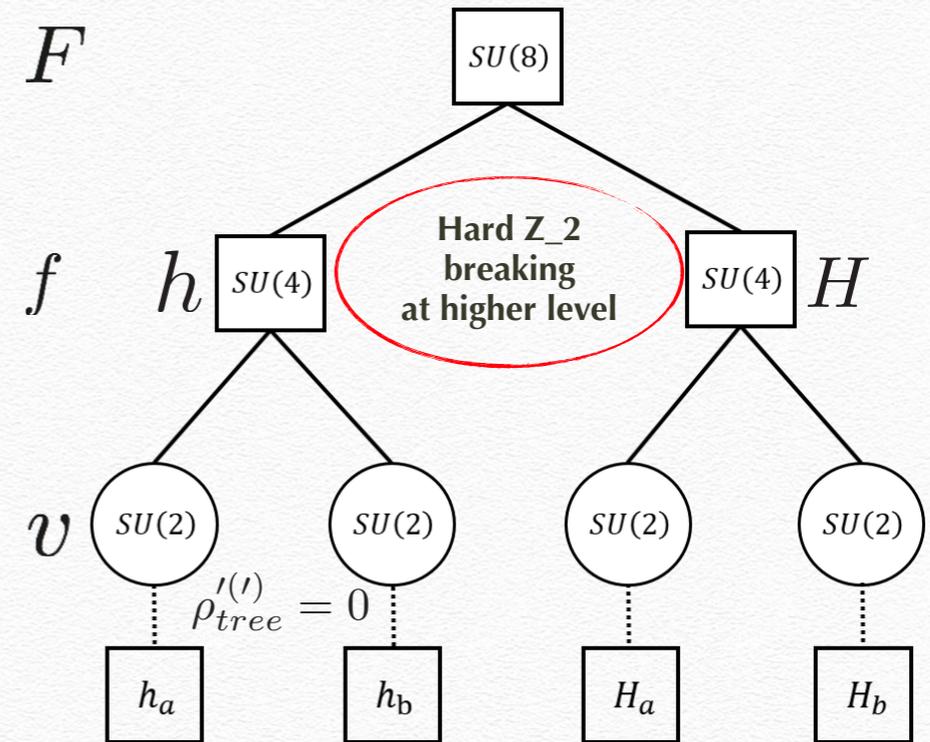
$$V \supset \underline{\bar{\lambda}(|h|^2 + |H|^2)^2 + m^2(|h|^2 + |H|^2) + \bar{\kappa}(|h|^4 + |H|^4) + \bar{\rho}|h|^4 + m_h'^2|h|^2}$$

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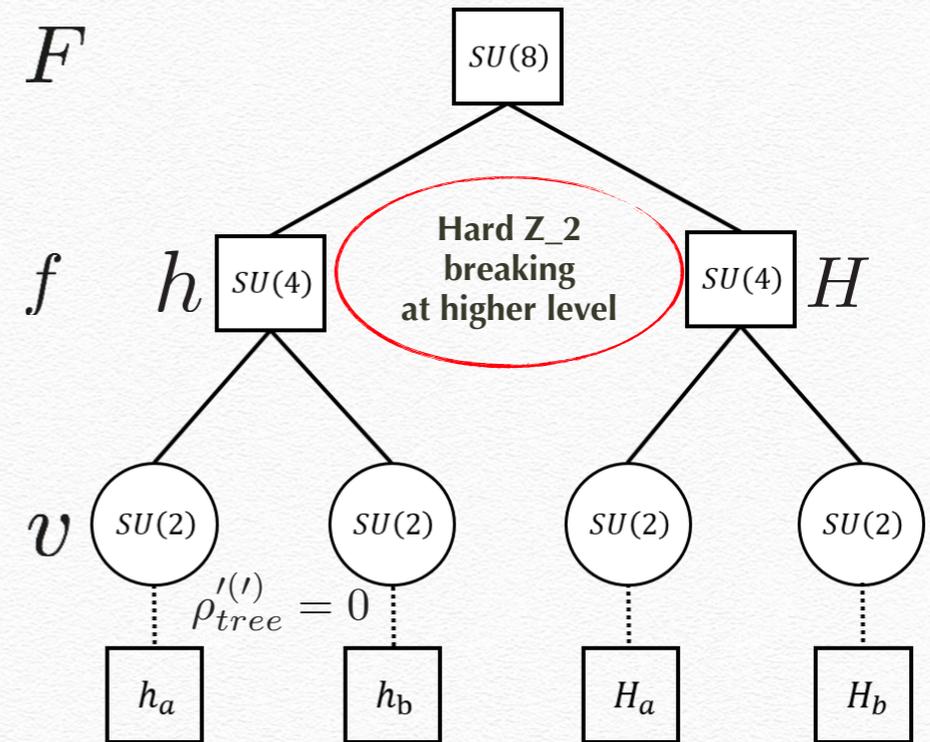
$$\begin{aligned}
 V \supset & \bar{\lambda}(|h|^2 + |H|^2)^2 + m^2(|h|^2 + |H|^2) + \bar{\kappa}(|h|^4 + |H|^4) + \bar{\rho}|h|^4 + m_h'^2|h|^2 \\
 & + \rho''(|h_a|^2 + |H|^2)^2 + \kappa''(|h_a|^4 + |h_b|^4 + |H_a|^4 + |H_b|^4) \\
 & + \kappa'(|h_a|^4 + |h_b|^4) + \rho'|h_a|^4 + \mu'^2|h_a|^2.
 \end{aligned}$$

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 \end{aligned}$$

$$m_{SM}^2 \sim 4v^2(2\kappa_1)\left(1 - \frac{v^2}{f^2}\right)$$

$$\kappa_1 = \kappa'' + \kappa'$$

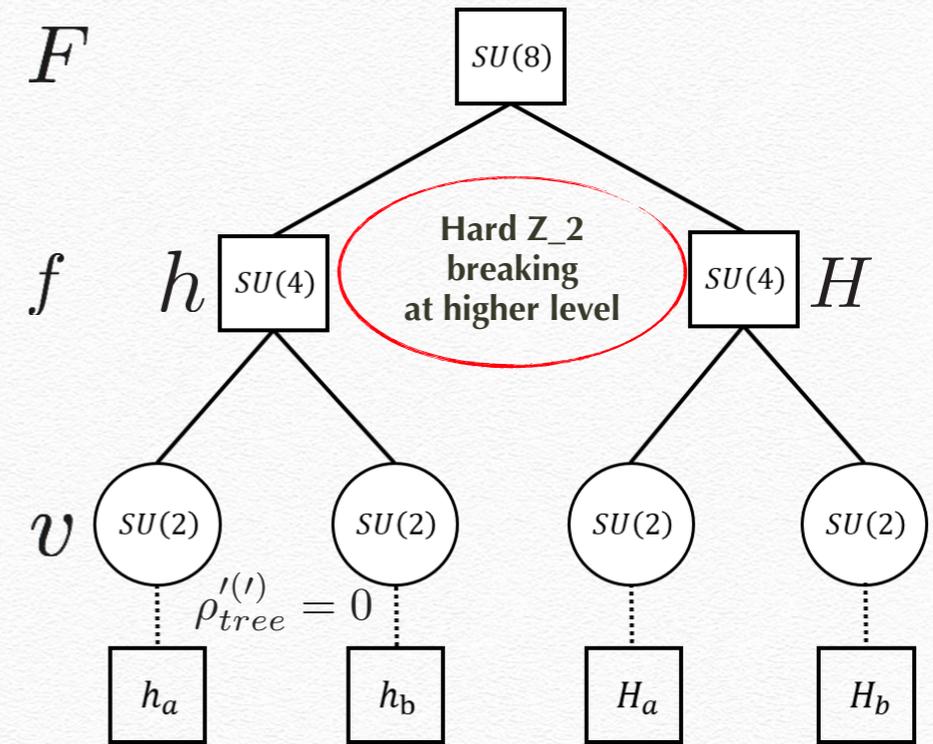
$$\Delta_{v/\Lambda}^{\text{TMNT}} \approx \frac{1}{64\pi^2} \frac{\bar{\kappa}}{2\bar{\kappa} + \bar{\rho}} \left( \frac{3y_t^2}{\bar{\lambda}} \frac{\Lambda_t^2}{v^2} - \left(9 + 5\epsilon_{\pm} \frac{\bar{\rho}}{\bar{\kappa}}\right) \frac{\Lambda_{\rho}^2}{v^2} \right)$$

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 \end{aligned}$$

$$m_{SM}^2 \sim 4v^2(2\kappa_1)\left(1 - \frac{v^2}{f^2}\right)$$

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$$\Delta_{v/\Lambda}^{\text{TMNT}} \approx \frac{1}{64\pi^2} \frac{\bar{\kappa}}{2\bar{\kappa} + \bar{\rho}} \left( \frac{3y_t^2}{\lambda} \frac{\Lambda_t^2}{v^2} - \left(9 + 5\epsilon_{\pm} \frac{\bar{\rho}}{\bar{\kappa}}\right) \frac{\Lambda_{\rho}^2}{v^2} \right)$$

$$\Delta_{v/\Lambda}^{\text{TH,soft}} \approx \frac{1}{64\pi^2} \left( \frac{3y_t^2}{\lambda} \frac{\Lambda_t^2}{v^2} - 5 \frac{\Lambda_{\rho}^2}{v^2} \right)$$

$$\Delta_{v/\Lambda}^{\text{SM}} \approx \frac{1}{32\pi^2} \left( \frac{3y_t^2}{\lambda_{\text{SM}}} \frac{\Lambda_t^2}{v^2} - 3 \frac{\Lambda_{\rho}^2}{v^2} \right)$$

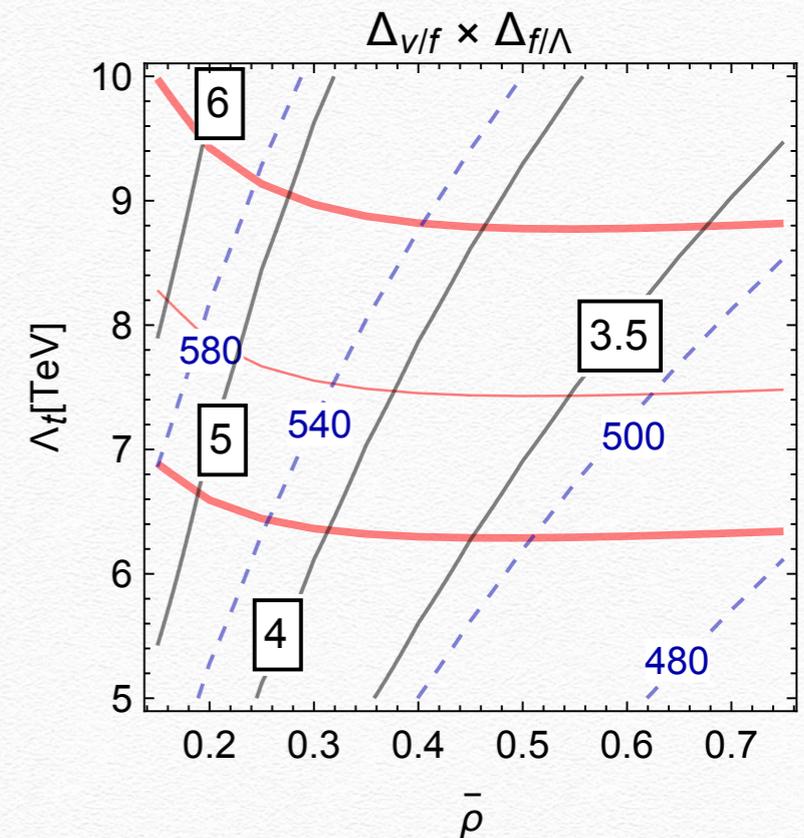
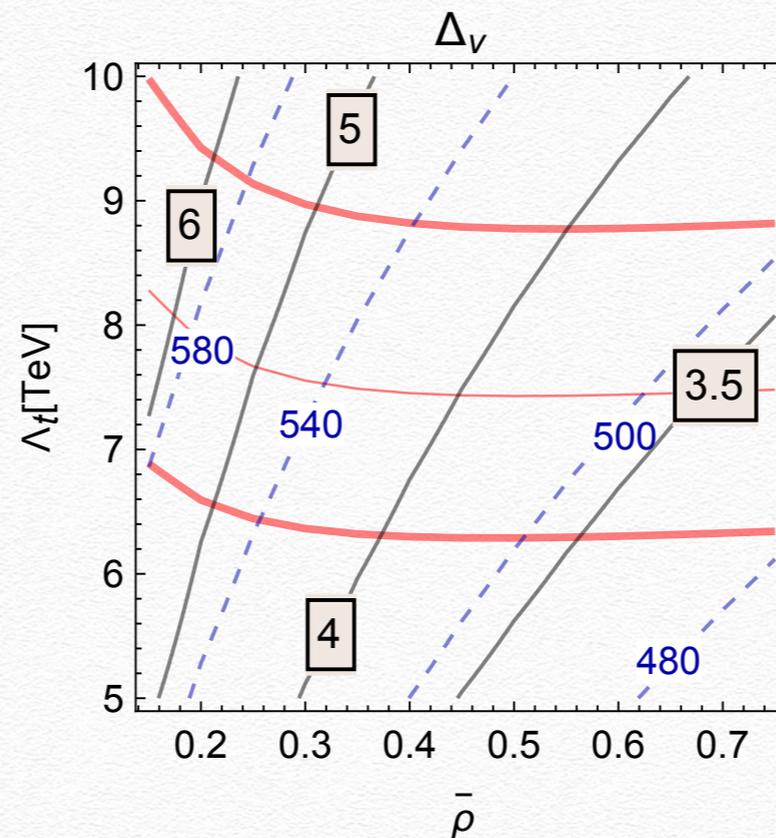


# tthh—Resonance Search

[P. Asadi, N. Craig, YYL, arXiv:1810.09467]

$m$ [TeV]	$\Lambda_\rho$ [TeV]	$\bar{\lambda}$	$\bar{\kappa}$	$\kappa''$	$\kappa'$	$\rho'$	$m_h^2$	$\rho''$
1.8	3.0	0.8	0.0(0.15)	0.0	0.005	0.0	0.0	0.0

$$\begin{aligned} \delta m^2 &= -\frac{3y_t^2}{16\pi^2}\Lambda_t^2 + \frac{9\bar{\lambda}}{16\pi^2}\Lambda_\rho^2, \\ \delta \bar{\kappa} &= \frac{5\bar{\rho}\bar{\lambda}}{32\pi^2}\log\frac{\Lambda_\rho^2}{m_2^2}, \\ \delta \kappa'' &= \frac{3y_t^4}{16\pi^2}\log\frac{\Lambda_t^2}{m_{T_a}^2}, \\ \delta \kappa' &= \frac{3y_t^4}{16\pi^2}\log\frac{m_{T_a}^2}{m_{t_b}^2}, \\ \delta \rho' &= \frac{3y_t^4}{16\pi^2}\log\frac{m_{t_b}^2}{m_{t_a}^2}, \\ \delta m_h'^2 &= \epsilon_\pm \frac{5\bar{\rho}}{16\pi^2}\Lambda_\rho^2, \end{aligned}$$



a factor of 8-15 improvement on tuning!

# tthh—Resonance Search—scalars

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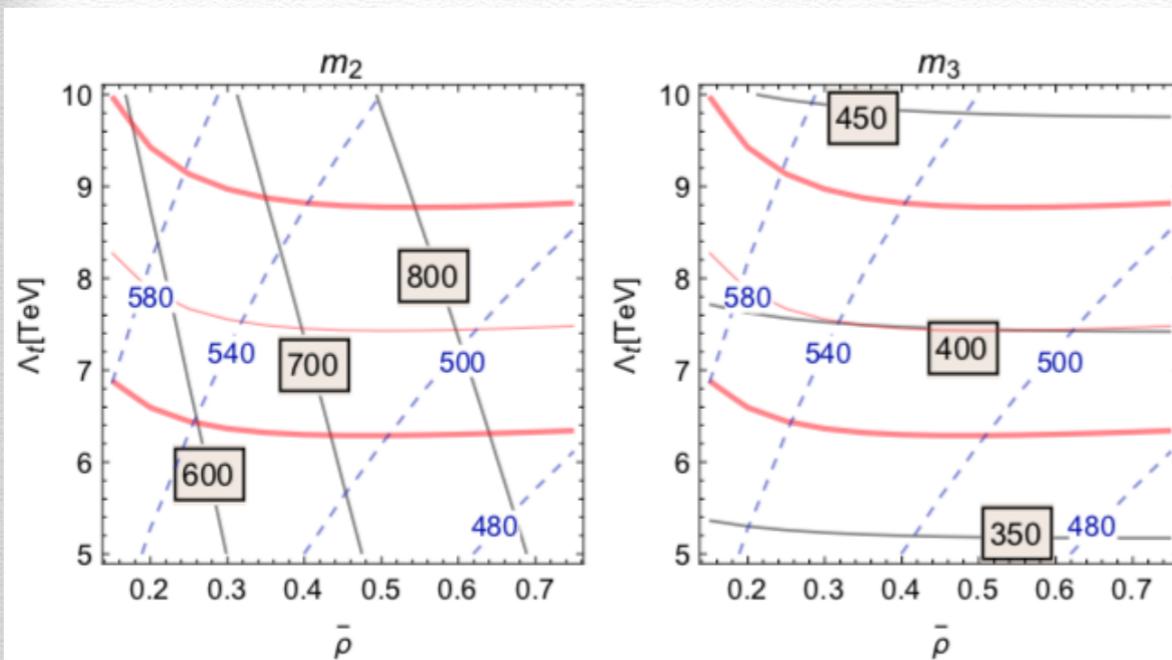
$$\delta m_{SM}^2 \sim -\frac{3y_t^2 \Lambda^2}{16\pi^2} + \frac{g^2 \Lambda^2}{32\pi^2} + \frac{\lambda_{SM} \Lambda^2}{32\pi^2}$$

$$\delta m_{SM}^2 = \frac{\kappa_1}{\lambda} \frac{\bar{\kappa}}{2\bar{\kappa} + \bar{\rho}} \left( m^2 - \frac{3y_t^2}{16\pi^2} \Lambda_t^2 + \frac{9\bar{\lambda}}{16\pi^2} \Lambda_\rho^2 \right) + \frac{\epsilon_\pm \bar{\rho}}{2\bar{\kappa} + \bar{\rho}} \frac{5\kappa_1 \Lambda_\rho^2}{16\pi^2} + \mu'^2$$

direct quadratic sensitivity to scalar cutoff

$\Lambda_\rho \sim 2\text{TeV}$  roughly the same cutoff scale as SM,  
at which new electroweak scalars appear

But stops us from turtling up



more light scalars (radial mode) are below TeV scale,  
almost not couples to our EW sector, safe from data

More scalars  $\rightarrow$  Higher colored states scale  
scalars are definite signature of naturalness!