UNITARITY VIOLATION FROM NONSTANDARD HIGGS COUPLINGS



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Discover New Physics (e.g. Supersymmetry, Composite Higgs, 2HDM, ...)

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Measure Standard Model Processes

PINNING DOWN HIGGS COUPLINGS



Fits for Higgs couplings Standard Model particles have 20-50% errors

One of the main motivation of HL-LHC and future colliders is measuring these better

PINNING DOWN HIGGS COUPLINGS



STANDARD MODEL PROCESSES



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UNITARITY VIOLATION



The Standard Model is a precise deck of cards, modifications (due to higher dimensional operators) lead to problems at high energies, in particular Unitarity violation

CLASSIC EXAMPLE SCATTERING $Z_L Z_L \Leftrightarrow W^+_L W^-_L$



 $M = c Energy^2 + ...$

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min

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mos YN $M = -c Energy^2 + ...$ $M = c Energy^2 + ...$

Higgs exchange cancels high energy growth if its couplings are SM-like, matrix element is Unitary if m_H ≤ ITeV (Lee, Quigg,Thacker)



HIGGS POTENTIAL UNITARITY (SC, LUTY, ALSO FALKOWSKI, RATTAZZI)

$$\lambda \left(|H|^2 - \frac{v^2}{2} \right)^2 = \lambda v^2 h^2 + \lambda v h^3 + \frac{\lambda}{4} h^4$$



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Higgs self-couplings probe its potential and test mechanism of electroweak symmetry breaking

$$m_h^2 = 2\lambda v^2$$

$$\delta_3 = \frac{\lambda_{hhh}}{m_h^2/(2v)} - 1$$

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$$\begin{split} m_h^2 &= 2\lambda v^2 \\ \delta_3 &= \underbrace{\frac{\lambda_{hhh}}{m_h^2/(2v)}}_{A_hhhh} - 1 & \text{also} \\ \taueferred to \\ as \ \mathbf{K}_{\lambda} \\ \delta_4 &= \frac{\lambda_{hhhh}}{m_h^2/(8v^2)} - 1 \end{split}$$

EXISTING INDIRECT TRILINEAR CONSTRAINTS



Precision Electroweak |κ_λ| ≤ 14 Kribs et.al. 1702.07678

EXISTING INDIRECT TRILINEAR CONSTRAINTS



 $\lambda_{\rm hhh} / \lambda_{\rm hhh}^{\rm SM} = 7$ $\lambda_{\rm hhhh} = \lambda_{\rm hhhh}^{\rm SM}$ 0.8 0.6 |Re a⁰h→hh t+u 0.4 s+t+u+4vrtx 0.2 4vrtx 0.0 300 400 500 600 700 800 √s [GeV]

Precision Electroweak |κ_λ| ≤ 14 Kribs et.al. 1702.07678 Low Energy Unitarity hh \rightarrow hh $|\kappa_{\lambda}| \leq 7$ Di Luzio et.al. 1704.02311

HIGGS TRILINEAR



Trilinear probed by search for Double Higgs production



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Trilinear probed by search for Double Higgs production





Currently only sensitive to O(10) variations, but projections estimate trilinear sensitivity to ~ [-0.2,3.6] at LHC w/ 3 ab⁻¹ and 20-30% at future colliders

TRIPLE HIGGS PROCESS

Papaefstathiou and Sakurai See also Chien et.al.



FIG. 6: The approximate expected 2σ (blue) and 5σ (red) exclusion regions on the $c_3 - d_4$ plane after 30 ab⁻¹ of integrated luminosity, derived assuming a constant signal efficiency, calculated along the $d_4 = 6c_3$ line in $c_3 \in [-3.0, 4.0]$.

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hh and hhh at one loop e.g. Bizon, et.al. (also Liu et.al.)



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Sensitivity to Higgs quartic is poor even in optimistic cases

GENERAL HIGGS POTENTIAL $V = \frac{1}{2}m_h^2 h^2 + \lambda_{hhh} h^3 + \lambda_{hhhh} h^4 + \lambda_{hhhhh} h^5 + \cdots$

Higgs Effective Field Theory (HEFT) parameterizes most general Higgs couplings

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Phenomenological and agnostic about origin of Higgs boson Not SU(2) \times U(1) invariant, but can be lifted to EW gauge invariant theory via

$$X \equiv \sqrt{2|H|^2} - v = \sqrt{(v+h)^2 + \vec{G}^2} - v$$
$$= h + \frac{1}{2v}\vec{G}^2 - \frac{1}{2v^2}h\vec{G}^2 + \cdots$$

TRILINEAR UNITARITY VIOLATION

Modifying trilinear from SM value automatically leads to Unitarity violation at high energies

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Cancellation to get M ~ I/Energy² requires SM trilinear value!

HIGGSTRILINEAR MODIFICATION

$$\frac{m_h^2}{2v}\delta_3 X^3 = \frac{m_h^2}{2v}\delta_3 \left(\sqrt{(v+h)^2 + \vec{G}^2} - v\right)^3$$

Goldstone Equivalence Theorem says Goldstone scattering gives high energy longitudinal W,Z scattering

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Unitarity violating scale for $Z_L h^{m/2} \iff Z_L h^{m/2}$ is ~5 TeV for m ~ 10-15



MODEL DEPENDENCE OF INTERACTIONS

$$\begin{split} X^3 &\sim h^3 + \vec{G}^2(h^2 + h^3 + \cdots) + \vec{G}^4(h + h^2 + \cdots) + \vec{G}^6(1 + h + \cdots) \\ &\quad + \vec{G}^8(1 + h + \cdots) + \vec{G}^{10}(1 + h + \cdots) + \cdots, \\ X^4 &\sim h^4 + \vec{G}^2(h^3 + h^4 + \cdots) + \vec{G}^4(h^2 + h^3 + \cdots) + \vec{G}^6(h + h^2 + \cdots) \\ &\quad + \vec{G}^8(1 + h + \cdots) + \vec{G}^{10}(1 + h + \cdots) + \cdots, \\ X^5 &\sim h^5 + \vec{G}^2(h^4 + h^5 + \cdots) + \vec{G}^4(h^3 + h^4 + \cdots) + \vec{G}^6(h^2 + h + \cdots) \\ &\quad + \vec{G}^8(h + h^2 + \cdots) + \vec{G}^{10}(1 + h + \cdots) + \cdots, \end{split}$$

(Schematic without coefficients)

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Terms circled can only come from trilinear!

HIGHER POINT CANCELLATIONS

SMEFT |H|⁶

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SMEFT
$$\delta_{3}\lambda v \left(\frac{2|H|^{2} - v^{2}}{2v}\right)^{3} = \delta_{3}\lambda v \left(h + \frac{h^{2} + \vec{G}^{2}}{2v}\right)^{3}$$
$$|\mathsf{H}|^{6} = \delta_{3}\lambda v \left(h^{3} + \frac{3}{2v}h^{4} + \frac{3}{4v^{2}}h^{5} + \frac{1}{8v^{3}}h^{6} + O(G^{6})\right)$$

HIGHER POINT CANCELLATIONS

SMEF

 $|H|^6$

$$\delta_3 \lambda v \left(\frac{2|H|^2 - v^2}{2v}\right)^3 = \delta_3 \lambda v \left(h + \frac{h^2 + \vec{G}^2}{2v}\right)^3$$
$$= \delta_3 \lambda v \left(h^3 + \frac{3}{2v}h^4 + \frac{3}{4v^2}h^5 + \frac{1}{8v^3}h^6 + O(G^6)\right)$$

Contact interactions with multiplicity greater than 7 particles are dependent on couplings that will never be directly measured

MODEL INDEPENDENT TRILINEAR UNITARITY VIOLATION

 $hG^2 \leftrightarrow G^2$

Weak Isospin = 0, 1, 2 channels singlet channel gives best bound of $57.4 \text{ TeV}/\delta_3$

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Identifies VBF production of hh, hVV and VVVV as interesting processes and motivates I 00 TeV pp collider can test new physics of trilinear

COLLIDER PROBES

SM behavior

ENERGY

COLLIDER PROBES

Probing high energy processes can test energy growth, complementary sensitivity to Higgs couplings

SM behavior

ENERGY

COLLIDER PROBES

17

Probing high energy processes can test energy growth, complementary sensitivity to Higgs couplings

New resonances possible, but not guaranteed. E.g. Higgs not discovered in VB scattering

SM behavior

VECTOR BOSON FUSION OF HH

(BISHARA ET.AL. 1611.03860)

LHC 14 TeV



More promising than vector boson scattering (sensitive to hVV, hhVV, hhh couplings)

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LHC 14TeV



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Search for jjbbbb is sensitive to hhVV coupling of 30% (1%) at HL-LHC (100 TeV)

"HIGGS W/O HIGGS"

Henning et.al. 1812.09299









 Higgs coupling measurements and searches for deviations in SM processes are correlated

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- Work in progress systematically investigating Unitarity violating channels

THANKS FOR YOUR TIME!



EXTRA SLIDES

UNITARITY CONSTRAINTS ON NON-DERIVATIVE COUPLINGS

 $\frac{\lambda}{n_1!\cdots n_r!}\phi_1^{n_1}\cdots \phi_r^{n_r}$

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Consider s-wave scattering

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Unitarity constraints from this amplitude requires

$$E \le 4\pi \left[\frac{64\pi^2}{\lambda^2} \left(k_1! \cdots k_r! \left(k - 1 \right)! \left(k - 2 \right)! \right) \left(\left(n_1 - k_1 \right)! \cdots \left(n_r - k_r \right)! \left(n - k - 1 \right)! \left(n - k - 2 \right)! \right) \right]^{\frac{1}{2n - 8}}$$

where $n \equiv n_1 + \cdots + n_r, k \equiv k_1 + \cdots + k_r$

ONE PARTICLE EXAMPLE

 $\frac{\lambda}{n!}\phi^n$

Optimal bound is when k = n/2

ONE PARTICLE EXAMPLE



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$$\frac{E_{k=n/2}}{E_{k=2}} = \left[\frac{\{(n/2)!(n/2-1)!(n/2-2)!\}^2}{2!1!0!(n-2)!(n-3)!(n-4)!}\right]^{1/(2n-8)}$$



n/2 \Leftrightarrow n/2 channel improves Unitarity bound by up to factor of two compared to standard 2 \Leftrightarrow n-2





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Process	Unitarity Violating Scale
$h^2 Z_L \leftrightarrow h Z_L$	$66.7 \text{ TeV}/ \delta_3 - \frac{1}{3}\delta_4 $
$hZ_L^2 \leftrightarrow Z_L^2$	94.2 TeV/ $ \delta_3 $
$hW_L Z_L \leftrightarrow W_L Z_L$	$141 \text{ TeV}/ \delta_3 $
$hZ_L^2 \leftrightarrow hZ_L^2$	9.1 TeV/ $\sqrt{\left \delta_3 - \frac{1}{5}\delta_4\right }$
$hW_L Z_L \leftrightarrow hW_L Z_L$	11.1 TeV/ $\sqrt{\left \delta_3 - \frac{1}{5}\delta_4\right }$
$Z_L^3 \leftrightarrow Z_L^3$	$15.7 \text{ TeV}/\sqrt{ \delta_3 }$
$Z_L^2 W_L \leftrightarrow Z_L^2 W_L$	$20.4 \text{ TeV}/\sqrt{ \delta_3 }$
$hZ_L^3 \leftrightarrow Z_L^3$	$6.8 \text{ TeV}/ \delta_3 - \frac{1}{6}\delta_4 ^{\frac{1}{3}}$
$hZ_L^2 W_L \leftrightarrow Z_L^2 W_L$	$8.0 \text{ TeV}/ \delta_3 - \frac{1}{6}\delta_4 ^{\frac{1}{3}}$
$Z_L^4 \leftrightarrow Z_L^4$	$6.1 \text{ TeV}/ \delta_3 - \frac{1}{6}\delta_4 ^{\frac{1}{4}}$

FALKOWSKI & RATTAZZI



Figure 1: Parameter space for the cubic Higgs self-coupling deformation Δ_3 relative to the SM value. The allowed region depends on the value $c_4 = \xi a_4/a_2$, which encodes effects of dimension-8 SMEFT operators in the Higgs potential. The gray area is excluded by stability considerations, as the potential contains a deeper minimum that the EW vacuum at $\langle H^{\dagger}H\rangle = v^2/2$. Left: the purple areas are excluded for $a_4 = 1$ and $a_2 = 0.01$ under different hypotheses about the parameter $\xi = v^2/f^2$, which characterizes the size of the corrections to the single Higgs boson couplings to matter. Right: the blue areas are excluded for $a_4 = 1$ and $\xi = 0.1$ under different hypotheses about the coupling strength g_* of the BSM theory underlying the SM.