PRIMORDIAL BLACK HOLES AS THE SOLUTION OF MANY COSMOLOGICAL CONUNDRA



Bernard Carr, Queen Mary University of London IPMU workshop (2/12/19)



PRIMORDIAL BLACK HOLES AFTER 50 YEARS: A HISTORICAL OVERVIEW

Bernard Carr Queen Mary University of London

PBH?

IPMU 13/11/17

PUBLICATION RATE OF PBH PAPERS



Impossible to keep up with literature!

Mon. Not. R. astr. Soc. (1974) 168, 399-415.

BLACK HOLES IN THE EARLY UNIVERSE

B. J. Carr and S. W. Hawking

(Received 1974 February 25)

SUMMARY

The existence of galaxies today implies that the early Universe must have been inhomogeneous. Some regions might have got so compressed that they underwent gravitational collapse to produce black holes. Once formed, black holes in the early Universe would grow by accreting nearby matter. A first estimate suggests that they might grow at the same rate as the Universe during the radiation era and be of the order of ro^{15} to ro^{17} solar masses now. The observational evidence however is against the existence of such giant black holes. This motivates a more detailed study of the rate of accretion which shows that black holes will not in fact substantially increase their original mass by accretion. There could thus be primordial black holes around now with masses from ro^{-5} g upwards.



THE PRIMORDIAL BLACK HOLE MASS SPECTRUM*

Bernard J. Carr

Department of Applied Mathematics and Theoretical Physics, Cambridge University, Cambridge, England;

California Institute of Technology, Pasadena Received 1975 January 31

ABSTRACT

We examine what mass spectrum of primordial black holes should result if the early universe consisted of small density fluctuations superposed on a Friedmann background. It is shown that only a certain type of fluctuation favors the formation of primordial black holes and that, consequently, their spectrum should always have a particular form. Since both the fluctuations which arise naturally and the fluctuations which are often invoked to explain galaxy formation are of the required type, primordial black holes could have had an important effect on the evolution of the universe. In particular, although primordial black holes are unlikely to have a critical density, big ones could have been sufficiently numerous to act as condensation nuclei for galaxies. Observational limits on the spectrum of primordial black holes glace strong constraints on the magnitude of density fluctuations in the early universe and support the assumption that the early universe was nearly Friedmann rather than chaotic. Any model in which the early universe has a soft equation of state for a prolonged period is shown to be suspect, since primordial black holes place, since primordial black holes placed, since pri-

PHYSICAL REVIEW D 81, 104019 (2010)

New cosmological constraints on primordial black holes

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We update the constraints on the fraction of the Universe going into primordial black holes in the mass range $10^{9}-10^{17}$ g associated with the effects of their evaporations on big bang nucleosynthesis and the extragalactic photon background. We include for the first time all the effects of quark and gluon emission by black holes on these constraints and account for the latest observational developments. We then discuss the other constraints in this mass range and show that these are weaker than the nucleosynthesis and photon background. We range and show that these are weaker than the mucleosynthesis and photon background limits, apart from a small range $10^{13}-10^{14}$ g, where the damping of cosmic microwave background anisotropies dominates. Finally we review the gravitational and astrophysical effects of nonewaporating primordial black holes, updating constraints over the broader mass range $1-10^{19}$ g.







Career all downhill

until RESCEU!

PLAN OF TALK

- Formation and evaporation of PBHs
- Constraints on PBHs
- PBHs as dark matter dark
- PBHs as source of LIGO/Virgo events
- PBHs as generators of cosmic structure
- PBHs from QCD epoch and fine-tuning problem

PRIMORDIAL BLACK HOLE FORMATION

 $R_S = 2GM/c^2 = 3(M/M_O) \text{ km} \implies \rho_S = 10^{18}(M/M_O)^{-2} \text{ g/cm}^3$

Small BHs can only form in early Universe

cf. cosmological density $\rho \sim 1/(Gt^2) \sim 10^6 (t/s)^{-2} g/cm^3$

⇒ primordial BHs with horizon mass at formation

 $M_{PBH} \sim c^{3}t/G = \begin{cases} 10^{-5}g \text{ at } 10^{-43}s & (\text{minimum?}) \\ 10^{15}g \text{ at } 10^{-23}s & (\text{evaporating now}) \\ 1M_{O} \text{ at } 10^{-5}s & (\text{QCD transition}) \\ 10^{5}M_{O} \text{ at } 1s & (\text{maximum?}) \end{cases}$

FORMATION MECHANISMS

Primordial inhomogeneities Inflation



Cosmic strings PBH constraints => $G \mu < 10^{-6}$



Bubble collisions Need fine-tuning of bubble formation rate Domain walls PBHs can be very large





 \bigcirc

PBH EVAPORATION

Black holes radiate thermally with temperature

$$T = \frac{hc^{3}}{8\pi G k M} \sim 10^{-7} \left[\frac{M}{M_{0}}\right]^{-1} K$$

=> evaporate completely in time $t_{evap} \sim 10^{64} \left[\frac{M}{M_{0}}\right]^{3} y$
 $M \sim 10^{15} g$ => final explosion phase today (10^{30} ergs)
This can only be important for PBHs
 γ -ray background at 100 MeV => $\Omega_{PBH}(10^{15} g) < 10^{-8}$
=> explosions undetectable in standard particle physics model
Are some short γ -ray bursts PBH explosions (Cline et al.)
 $T > T_{CMB}$ =3K for M < $10^{26} g$ => "quantum" black holes



PBHs are important even if they never formed!

BLACK HOLE INFORMATION PARADOX

PHYSICAL REVIEW D

VOLUME 14, NUMBER 10

15 NOVEMBER 1976

Breakdown of predictability in gravitational collapse*

S. W. Hawking[†]

Whereas Stephen Hawking and Kip Thorne firmly believe that information swallowed by a black hole is forever hidden from the outside universe, and can never be revealed even as the black hole evaporates and completely disappears,

And whereas John Preskill firmly believes that a mechanism for the information to be released by the evaporating black hole must and will be found in the correct theory of quantum gravity,

Therefore Preskill offers, and Hawking/Thorne accept, a wager that:

When an initial pure quantum state undergoes gravitational collapse to form a black hole, the final state at the end of black hole evaporation will always be a pure quantum state.

The loser(s) will reward the winner(s) with an encyclopedia of the winner's choice, from which information can be recovered at will.

me JAn P. Pres Kul John P. Preskill

Stephen W. Hawking & Kip S. Thorne

Pasadena, California, 6 February 1997

I concede, now I have Seen inside black holes -21 July 2004 Stephen W. Hawking



An ordinary mistake is one that leads to a dead end, while a profound mistake is one that leads to progress. Anyone can make an ordinary mistake, but it takes a genius to make a profound mistake.

— Frank Wilczek —

AZQUOTES

Hawking's bet

BLACK HOLES AS LINK BETWEEN MICRO AND MACRO PHYSICS



BLACK HOLES AS LINK LIGHT AND DARK



PBH FORMATION => LARGE INHOMOGENEITIES

To collapse against pressure, need (Carr 1975)

 $R > \sqrt{\alpha}$ ct when $\delta \sim 1 \implies \delta_{\rm H} > \alpha$ (p= $\alpha \rho c^2$)



p=0 => need spherical symmetry => $\beta(M) \sim 0.06 \epsilon(M)^6$

(Khlopov & Polnarev 1982)

Fraction of Universe collapsing

 $\beta(M)$ fraction of density in PBHs of mass M at formation

General limit

$$\frac{\rho_{PBH}}{\rho_{CBR}} \approx \frac{\Omega_{PBH}}{10^{-4}} \left[\frac{R}{R_0} \right] \Longrightarrow \beta \sim 10^{-6} \Omega_{PBH} \left[\frac{t}{\text{sec}} \right]^{1/2} \sim 10^{-18} \Omega_{PBH} \left[\frac{M}{10^{15} g} \right]^{1/2}$$

So both require and expect $\beta(M)$ to be tiny

Fraction of dark matter $f_{DM} \sim (\beta / 10^{-9}) (M/M_o)^{-1/2}$

Fine-tuning problem!

β too large => PBHs overdominate => no galaxies
β too small => insufficient DM => no galaxies

Limit on fraction of Universe collapsing

UnevaporatedM>10^{15}g $\Rightarrow \Omega_{PBH} < 0.25$ (CDM)Evaporating nowM~10^{15}g $\Rightarrow \Omega_{PBH} < 10^{-8}$ (GRB)Evaporated in pastM<10^{15}g</td>

=> constraints from entropy, γ-background, BBNS



PBHs are unique probe of ε on small scales.

Need blue spectrum or spectral feature to produce them.

PBHS FROM NEAR-CRITICAL COLLAPSE

Critical phenomena \Rightarrow M = k M_H(δ - δ_c)^{γ} (Niemeyer & Jedamzik 1999) spectrum peaks at horizon mass with extended low mass tail

 $dN/dM \propto M^{1/\gamma-1} \exp[-(M/M_f)^{1/\gamma}]$ ($\gamma = 0.35$) (Yokoyama 1998)

Later calculations and peak analysis =>

 $\delta_{\rm C} \sim 0.45$ and applies to $\delta - \delta_{\rm C} \sim 10^{-10}$ (Musco & Miller 2013)



MORE PRECISE ESTIMATE OF δ_{C}

Threshold of primordial black hole formation

¹Tomohiro Harada,* ²Chul-Moon Yoo, and ^{3,4}Kazunori Kohri

PRD 88 084051 (2013)



$$\delta_{Hc}^{\rm UH} = \sin^2\left(\frac{\pi\sqrt{w}}{1+3w}\right)$$

0.62 for radiation

PBHS AND INFLATION

PBHs formed before reheat inflated away =>

 $M > M_{min} = M_{Pl} (T_{reheat} / T_{Pl})^{-2} > 1 \text{ gm}$

CMB quadrupole => T_{reheat} < 10¹⁶GeV

But inflation generates fluctuations

$$\frac{\delta\rho}{\rho} \sim \left[\frac{V^{3/2}}{M_{\rm Pl}^{3}V'}\right]_{H}$$



Can these generate PBHs?

[HUGE NUMBER OF PAPERS ON THIS]

QUANTUM DIFFUSION

★ Consider the possibility of a plateau in the inflaton potential:



QUANTUM DIFFUSION: CURRENT HOT TOPIC

Quantum diffusion during inflation and primordial black holes

arXiv:1705.04861

Chris Pattison,^a Vincent Vennin,^{b,a} Hooshyar Assadullahi,^{a,c} and David Wands^a

Quantum diffusion beyond slow-roll: implications for primordial black-hole production

arXiv:1805.06731

Jose María Ezquiaga^{*a,b*} and Juan García-Bellido^{*a,b*}

Single Field Double Inflation and Primordial Black Holes

arXiv:1705.06225 K. Kannike,^{*a*} L. Marzola,^{*a,b*} M. Raidal,^{*a*} and H. Veermäe^{*a*} Primordial black hole production in critical Higgs inflation arXiv:1705.04861 J Ezquiaga, J Garcia-Bellido, E Morales

Primordial black holes from an inflexion point arXiv:1706.042261

C Germani and T Prokopec

Primordial black holes from inflation and quantum diffusion

arXiv:1804.07124

M. Biagetti,^a G. Franciolini,^b A. Kehagias^c and A. Riotto^b



Dolgov & Silk (1993)



CONSTRAINTS FOR EVAPORATING PBHS

B. Carr, K. Kohri, Y. Sendouda & J. Yokoyama PRD 81(2010) 104019



CONSTRAINTS ON NON-EVAPORATED PBHS

Carr, Kuhnel & Sandstad, arXiv:1607.06077



But some of these limits are now thought to be wrong

SOME NEW RECENT CONSTRAINTS

VOYAGER-1 e^{\pm} further constrain Primordial Black Holes as Dark Matter

Mathieu Boudaud¹ and Marco Cirelli¹

arXiv:1807.03075



Constraining PBH abundance with the Galactic 511 keV line William DeRocco1 and Peter W. Graham arXiv:1906.07740



monochromatic

lognormal

PBHs as dark matter candidate are severely constrained by the Galactic Center 511 keV gamma-ray line

Laha arXiv:1906.09994



Constraining the Local Burst Rate Density of PBHs with HAWC

Albert et al. arXiv:1911.04356



X-ray and gamma-ray limits on the primordial black hole abundance from Hawking radiation Ballesteros, Coronado-Blazquez and Gaggero arXiv:1906.10113



Microlensing constraints on primordial black holes with the Subaru/HSC Andromeda observation

Hiroko Niikura^{1,2}, Masahiro Takada¹, Naoki Yasuda¹, Robert H. Lupton³, Takahiro Sumi⁴, Surhud More^{1,5}, Toshiki Kurita^{1,2}, Sunao Sugiyama^{1,2}, Anupreeta More¹, Masamune Oguri^{1,2,6}, Masashi Chiba⁷

Nature Astronomy 3, 524 (2019),



Updated Constraints on Asteroid-Mass PBHs as Dark Matter Smyth et al arXiv:1910.01285



Earth-mass black holes? – Constraints on primordial black holes with 5-years OGLE microlensing events

Hiroko Niikura,^{1, 2, *} Masahiro Takada,^{2, †} Shuichiro Yokoyama,^{3, 2} Takahiro Sumi,⁴ and Shogo Masaki⁵

$\begin{array}{c} M_{\rm PBH} \, \left[M_\odot \right]_{10^{-6}} \, 10^{-2} \end{array}$ 10^{-10} 10^{2} Asteroid-mass window for PBH dark matter 10^{0} γ ray bkgnd HSC ROS/MACHO $f_{\text{PBH}} = \Omega_{\text{PBH}} / \Omega_{\text{DM}}$ 10^{-1} HSC 10⁻¹ limit on f_{PBH} 10^{-2} OGLE excl. region (95% CL) 10⁻² 10^{-3} 10⁻³ 10⁻¹⁷ 10⁻¹⁶ 10⁻¹⁵ 10^{-14} 10⁻¹³ 10⁻¹² 10⁻¹⁰ 10⁻¹¹ 10⁻⁹ 10^{-4} 10²⁰ M_{PBH} [solar masses] 10^{25} 10^{30} 10^{35} $M_{\rm PBH}$ [g]

arXiv:1901.07120

Revisiting constraints on asteroid-mass PBHs as DM candidates Paulo Montero-Camacho arXiv:1906.05950

Sunyaev-Zel'dovich anisotropy due to Primordial black holes

Katsuya T. Abe,* Hiroyuki Tashiro, and Toshiyuki Tanaka

arXiv:1901.06809



Pulsar Timing Array Constraints on PBHs with NANOGrav... Zu-Cheng Chen,1Chen Yuan and Qing-Guo Huang1 arXiv:1910.12239



Steepest growth of the power spectrum and PBHs Byrnes, Cole and Patil arXiv:1811.11158



Dissecting the growth of the power spectrum for PBHs Carrilho, Malik and Mulryne arXiv:1907.05237

CONSTRAINTS ON PRIMORDIAL BLACK HOLES

Bernard Carr,^{1, 2, *} Kazunori Kohri,^{3, †} Yuuiti Sendouda,^{4, ‡} and Jun'ichi Yokoyama^{2, 5, §}


LENSING, DYNAMICAL, ACCRETION AND COSMOLOGICIAL LIMITS



CONSTRAINTS ON POWER SPECTRUM



From PBH Abundance to Primordial Curvature Power Spectrum Kalaja et al arXiv: 1908.03596

Constraints on the primordial curvature power spectrum from PBHs Sato-Polito, Kovetz and Kamionkowski arXiv:1904.10971

These constraints are not just nails in a coffin!



All constraints have caveats and may change

Each constraint is a potential signature

PBHs are interesting even if f << 1

Alex Kusenko

CKS 2016

EXTENDED MASS FUNCTION

Most constraints assume monochromatic PBH mass function

Can we evade standard limits with extended mass spectrum?

But this is two-edged sword!

PBHs may be dark matter even if fraction is low at each scale

PBHs giving dark matter at one scale may violate limits at others

PBH CONSTRAINTS FOR EXTENDED MASS FUNCTIONS Carr, Raidal, Tenkanen, Vaskonen & Veermae (arXiv:1705.05567)

Possible PBH mass functions
$$\psi(M) \propto M \frac{\mathrm{d}n}{\mathrm{d}M} \Rightarrow \frac{\Omega_{\mathrm{PBH}}}{\Omega_{\mathrm{DM}}} = \int \mathrm{d}M \,\psi(M)$$
lognormal $\psi(M) = \frac{f_{\mathrm{PBH}}}{\sqrt{2\pi}\sigma M} \exp\left(-\frac{\log^2(M/M_c)}{2\sigma^2}\right)$ 2 parameters (M_c, σ)power-law $\psi(M) \propto M^{\gamma-1}$ ($M_{\min} < M < M_{\max}$)

critical collapse $\psi(M) \propto M^{2.85} \exp(-(M/M_f)^{2.85})$

f(M) limits themselves depend on PBH mass function

$$\int dM \frac{\psi(M)}{f_{\max}(M)} \le 1 \quad + \quad \psi(M; f_{\text{PBH}}, M_c, \sigma) \quad = > \quad f_{\text{PBH}}(\mathsf{M}_c, \sigma)$$



PRIMORDIAL BLACK HOLES AS DARK MATTER

PRO

* Black holes exist
* No new physics needed
* LIGO results

CON

* Requires fine-tuning

PBH can do it!



PRIMORDIAL BLACK HOLES AS DARK MATTER



 Ω_{vis} = 0.01, Ω_{dm} = 0.25 \Rightarrow need baryonic and non-baryonic DM MACHOs WIMPs

PBHs are non-baryonic with features of both WIMPs and MACHOs

PRIMORDIAL BLACK HOLES AS DARK MATTER

Bernard Carr,^{1,*} Florian Kühnel,^{2,†} and Marit Sandstad^{3,‡} PRD 94, 083504, arXiv:1607.06077



Three windows: (A) intermedate mass; (B) sublunar mass; (C) asteroid mass.

Also (D) Planck mass relics?

WHICH MASS WINDOW IS MOST PLAUSIBLE?

PBH dark matter @10²⁰g from double inflation Inomata et al arXiv:1701.02544 $\begin{array}{c} \text{PBH dark matter @10 } M_o \\ \text{from hybrid inflation} \end{array}$

Clesse & Garcia-Bellido arXiv:1501.07565



cf. light versus heavy dark matter particle



Early microlensing searches suggested MACHOs with 0.5 M_O => PBH formation at QCD transition? Pressure reduction => PBH mass function peak at 0.5 M_O

Later found that at most 20% of DM can be in these objects

PBHS AND LIGO/Virgo





Do we need Population III or primordial BHs?

Prescience of Japanese!

GRAVITATIONAL WAVES FROM COALESCING BLACK HOLE MACHO BINARIES Takashi Nakamura, Misao Sasaki, Takahiro Tanaka and Kip Thorne

THE ASTROPHYSICAL JOURNAL, 487:L139–L142, 1997



If MACHOs are black holes of mass ~0.5 M_{\odot} , they must have been formed in the early universe when the temperature was ~1 GeV. We estimate that in this case in our Galaxy's halo out to ~ 50 kpc there exist ~5 × 10⁸ black hole binaries the coalescence times of which are comparable to the age of the universe, so that the coalescence rate will be ~5 × 10⁻² events yr⁻¹ per galaxy. This suggests that we can expect a few events per year within 15 Mpc. The gravitational waves from such coalescing black hole MACHOs can be detected by the first generation of interferometers in the LIGO/VIRGO/TAMA/GEO network. Therefore, the existence of black hole MACHOs can be tested within the next 5 yr by gravitational waves.

POSSIBLE INDIRECT CONFIRMATION OF THE EXISTENCE OF POP III MASSIVE STARS BY GRAVITATIONAL WAVES

Tomaya Kinagawa, Kohei Inayoshi, Kenta Hotokezaka, Daisuka Nakauchi and Tahashi Nakamura



We perform population synthesis simulations for Population III (Pop III) coalescing compact binary which merges within the age of the Universe. We found that the typical mass of Pop III binary black holes (BH–BHs) is $\sim 30 \,\mathrm{M}_{\odot}$ so that the inspiral chirp signal of gravitational waves can be detected up to z = 0.28 by KAGRA, Adv. LIGO, Adv. Virgo and GEO

Did LIGO detect dark matter?

Simeon Bird,* Ilias Cholis, Julian B. Muñoz, Yacine Ali-Haïmoud, Marc Kamionkowski, Ely D. Kovetz, Alvise Raccanelli, and Adam G. Riess¹ arXiv:1603.00464

Dark matter in 20-100 M_O binaries may provide observed rate of 2-53 Gpc⁻¹yr⁻¹

Primordial Black Hole Scenario for the Gravitational-Wave Event GW150914

Misao Sasaki,¹ Teruaki Suyama,² Takahiro Tanaka,^{3,1} and Shuichiro Yokoyama⁴ arXiv:1603.08338

Only need small f and comparable to limits from CMB distortion

LIGO gravitational wave detection, primordial black holes and the near-IR cosmic infrared background anisotropies

A. Kashlinsky¹,

arXiv:1605.04023

PBHs may generate early structure and infrared background

Spin Distribution of Primordial Black Holes

Takeshi Chiba¹ and Shuichiro Yokoyama²

arXiv:1704.06573

Abstract

We estimate the spin distribution of primordial black holes based on the recent study of the critical phenomena in the gravitational collapse of a rotating radiation fluid. We find that primordial black holes are mostly slowly rotating.



Unraveling origin of BHs from effective spin measurements with LIGO-Virgo Fernandez and Profumo arXiv:1905.13019

RECENT PAPERS

Merger rates in primordial black hole clusters without initial binaries Korol et al. arXiv:1911.033483

Search for sub-solar mass ultracompact binaries in Advanced LIGO... LIGO/Virgo collaboration arXiv:1904.08976

Constraining the abundance of PBHs with gravitational lensing of gravitational waves at LIGO frequencies Jose M. Diego arXiv:1911.05736

Merger rates in primordial black hole clusters without initial binaries Korol et al. arXiv:1911.033483

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LIGO/VIRGO PBH CONSTRAINTS

Raidal et al. arXiv:1812.01930

Kavanagh et al arXiv:1805.09034



PBHS AS GENERATORS OF COSMIC STRUCTURES B.J. Carr & J. Silk MNRAS 478 (2018) 3756; arXiv:1801.00672

What is maximum mass of PBH?

Could $10^6 - 10^{10} M_0$ black holes in galactic nuclei be primordial?

BBNS => t < 1 s => M < $10^{5}M_{\odot}$ but β < 10^{-6} (t/s)^{1/2}

Supermassive PBHs could also generate cosmic structures on larger scale through 'seed' or 'Poisson' effect

Upper limit on μ distortion of CMB excludes $10^4 < M/M_O < 10^{12}$ for Gaussian fluctuations but some models evades these limits. Otherwise need accretion factor of $(M/10^4M_o)^{-1}$

Dolgov talk

Limits on primordial black holes from μ distortions in cosmic microwave background

Tomohiro Nakama,¹ Bernard Carr,^{2,3} and Joseph Silk^{1,4,5}

PHYSICAL REVIEW D 97, 043525 (2018)

If primordial black holes (PBHs) form directly from inhomogeneities in the early Universe, then the number in the mass range $10^5 - 10^{12} M_{\odot}$ is severely constrained by upper limits to the μ distortion in the cosmic microwave background (CMB). This is because inhomogeneities on these scales will be dissipated by Silk damping in the redshift interval $5 \times 10^4 \leq z \leq 2 \times 10^6$. If the primordial fluctuations on a given mass scale have a Gaussian distribution and PBHs form on the high- σ tail, as in the simplest scenarios, then the μ constraints exclude PBHs in this mass range from playing any interesting cosmological role. Only if the fluctuations are highly non-Gaussian, or form through some mechanism unrelated to the primordial fluctuations, can this conclusion be obviated.



ADDRESSING FINE-TUNING PROBLEM

Primordial black holes, dark matter and hot-spot electroweak baryogenesis at the quark-hadron epoch

Bernard Carr^{a,b}, Sebastien Clesse^{c,d}, Juan García-Bellido^{e*}

arXiv:1904.02129

A common origin of baryons and dark matter via the gravitational collapse of black holes in the early universe

Juan García-Bellido^a, * Bernard Carr^{b,c}, † and Sébastien Clesse^{d,e‡}

arXiv:1904.11482

Cosmic Conundra Explained by Thermal History and Primordial Black Holes

Bernard Carr,^{1, 2, *} Sébastien Clesse,^{3, 4, †} Juan García-Bellido,^{5, ‡} and Florian Kühnel^{6, §}

arXiv:1906.08217

Primordial black holes with an accurate QCD equation of state

Christian T. Byrnes,^{1,*} Mark Hindmarsh,^{1,2,†} Sam Young,^{1,‡} and Michael R. S. Hawkins^{3,§}

arXiv:1801.06138



Jedamzik (1996), Cardal & Fuller (1998)

ADDRESSING FINE-TUNING PROBLEM AT QCD EPOCH

PBHs forming at time t have mass and collapse fraction $M \sim 10^{5}$ (t/s) M_{O} , β (M) ~ 10⁻⁹ f(M) (M/M_O)^{1/2}

So β appears fine-tuned and we must also explain why $\chi = \rho_{\text{PBH}} / \rho_{\text{B}} = f \rho_{\text{DM}} / \rho_{\text{B}} = 6 \text{ f is O(1)}.$

 $M_C \sim \alpha_G^{-3/2} m_P \sim 1 M_O$ is Chandra' mass ($\alpha_G \sim 10^{-38}$) and all stars have mass in range (0.1–10) M_C

ANTHROPIC CONSTRAINTS ON χ AND η

$$t_{\rm dec} \sim 10 \, (1+\chi)^{-1/2} \eta^{-1/2} \alpha_{\rm G}^{-1/2} \alpha^{-6} t_{\rm p} \sim 10^{13} \, (1+\chi)^{-1/2} {\rm s}$$
$$t_{\rm eq} \sim (1+\chi)^{-2} \eta^{-2} \alpha_{\rm G}^{-1/2} t_{\rm p} \sim 10^{12} \, (1+\chi)^{-2} {\rm s} \, .$$

where

$$\alpha \equiv e^2/(\hbar c) \sim 10^{-2}$$
 $\alpha_{\rm G} \equiv G m_{\rm p}^2/(\hbar c) = m_{\rm p}^2/M_{\rm P}^2 \approx 6 \times 10^{-39}$

$$\chi$$
 = 6 $\eta \equiv n_{\rm b}/n_{\gamma} = 2.8 \times 10^{-8} \Omega_{\rm b} h^2 = 6.1 \times 10^{-10}$

Formation of galaxies requires

$$t_{\rm eq} \sim t_{\rm dec} = \eta \sim 0.1 \, (1+\chi)^{-1} \alpha^4 \sim 10^{-9} (1+\chi)^{-1}$$

Lifetime of star exceeds t_{eq} for

 $\eta > (1+\chi)^{-1} \alpha_G^{1/4} \sim 10^{-10}$



• Out of thermal equilibrium (PBH collapse)

$$\Delta K \simeq \left(\frac{1}{\gamma} - 1\right) M_{\rm H} \qquad E_0 = \frac{\Delta K}{n_{\rm p} \Delta V} \qquad k_{\rm B} T_{\rm eff} = \frac{2}{3} E_0 \simeq 5 \,\text{TeV}$$
$$\delta_{\rm CP}(T) = 3 \times 10^{-5} \left(20.4 \,\text{GeV}/T\right)^{12} \quad \text{above sphaleron barrier}$$
$$\chi \approx \gamma/(1 - \gamma) \approx 5 \text{ if } \gamma \approx 0.8$$

Baryogenesis scenario

EW baryogenesis at QCD epoch

Baryon violation via sphaleron transitions and B+L chiral anomaly

CP violation via CKM matrix

Equilibrium violation via supercooling near QCD scale

PBH form'n => large curvature perturb'n => huge entropy prod'n => out-of-equilibrium condition => baryogenesis with $\eta_{loc} \sim 1$

Diffusion of baryon asymmetry => $\eta \sim \beta$ and $\chi \sim 1$

Curvature perturbation scenario

Natural peak in PBH mass function but need to fine-tune pert' amp'

Stochastic fluct'ns in spectator field during inflation (QCD axion) \Rightarrow different values in different patches

- \Rightarrow frozen until pot' energy dominates density long after inflation
- \Rightarrow 2nd inflation phase within region (few e-folds)
- \Rightarrow non-linear perturbations => PBHs.

Primordial Black Holes

without parameter fine-tuning



- Light **stochastic spectator** field during inflation (e.g. QCD axion)
- Plateau or small-field potential
- Domination before QCD epoch
- No parameter tuning

In the stochastic spectator scenario: no parameter tuning, but unavoidable **anthropic selection** due to the field **stochasticity**



PBH mass function

- 'Standard' PBH formation scenario: $\beta = \operatorname{erfc}(\zeta_{\mathrm{tr}}/\sqrt{2\sigma^2})$
- Light Stochastic Spectator: $m_{\psi} \ll H_{\text{inf}}$ and $\Delta \psi^{\text{stoch}} \sim H/2\pi$ $\langle \delta \psi^2 \rangle \simeq \int_0^N \frac{H(N')^2}{4\pi^2} dN' \simeq \frac{H_{\text{CMB}}^2}{8\pi^2\epsilon_*} \left(1 - e^{-2\epsilon_1 N}\right) \qquad P(\psi, N) = \frac{1}{\sqrt{2\pi \langle \delta \psi^2 \rangle}} \exp\left[-\frac{(\psi - \langle \psi \rangle)^2}{2\langle \delta \psi^2 \rangle}\right]$

Probability of a local field fluctuation: $P(\Delta\psi, N) = \frac{1}{\sqrt{2\pi(H(N)^2/4\pi^2)}} \exp\left[-\frac{\Delta\psi^2}{2(H(N)^2/4\pi^2)}\right] \ .$



In both cases, the PBH mass function 'mimics' the standard scenario. With anthropic selection of $\langle \psi \rangle$ one gets PBH-DM with $A_s = 2.1 \times 10^{-9} \simeq \frac{H_*^2}{8\pi\epsilon_{1*}\bar{M}_2^2}$

PBH MASS FUNCTION

Axion field fluct' => $\Delta N \sim O(1) => O(1)$ curv' fluct' if f_a ~ 0.2 M_{Pl} => PQ breaking at GUT epoch => axions dominate at QCD epoch



1st peak at 1M_O for DM plus 2nd peak at 10-20 M_O for LIGO events

Cosmic Conundra Explained by Thermal History and Primordial Black Holes

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Extend this to include other stages in thermal history







$$\delta_{\rm rms}(M) = A \left(\frac{M}{M_{\odot}}\right)^{(1-n_{\rm s})/4}$$

Overproduce light PBHs for $n_S > 0.975$

Overproduce heavy PBHs for $n_S < 0.965$

IS PREDICTED MASS FUNCTION ALLOWED BY PBH LIMITS?

(monochromatic case)



Pre 2016





Ali-Hamoud & Kamionkowski arXiv:1612.05644

Poulin, Serpico, Clesse & Kohri arXiv:1707.04206







Green arXiv:1705.10818,1707.04206

ARE PBHS CLUSTERED?

- Lognormal wide-mass distribution JGB & Clesse (2017)
 - Clusters of PBH: $N_{cl} \sim 100-1000$, comoving size ~ 1 mpc





uniform single-mass is already ruled out



clustered wide-mass is still viable

Towards closing the window of PBHs as DM: the case of large clustering Bringmann et al. arXiv:1808.05910

Initial clustering and the PBH merger rate Young and Byrnes arXiv:1910.06077



Inflation =>

Planetary-mass microlenses

OGLE detected microlenses on 0.1-0.3 day timescale of unknown origin – free-floating planets of PBHs?



What if Planet 9 is a Primordial Black Hole? Scholtz and Unwin arXiv:1909.11090

Quasar microlensing

Evidence for dark matter in the form of compact bodies

Michael Hawkins University of Edinburgh

Evidence for Microlensing

- Lack of time dilation.
- Symmetry of variation.
- Achromatic variation.
- Microlensing in multiply lensed quasars
- Caustic features in light curves
- Slope of structure function

The timescale of variation implies that the mass of the microlensing bodies is around 0.1 M_{\odot}





Fig. 3. Light curves for two quasars showing all the characteristics expected of caustic crossing events. Symbols as for Fig. 1.

OGLE/GAIA excess of lenses in Galactic bulge





Cosmic infrared/X-ray backgrounds

PBHs generate early structure and infrared background



Kashlinsky arXiv:1605.04023


Ultra-faint dwarf galaxies



5 Minimum radius of (ultra-faint) dwarf galaxies and cored DM profiles

Improved constraints from ultra-faint dwarf galaxies on PBHs as DMStegmann et alarXiv:1910.04793

PBHs as dark matter: cusp-to-core transition in low-mass dwarf galaxies Boldrini et al. arXiv:1909.07395

LIGO/Virgo black holes









Intermediate and supermassive black holes



 $n_{\rm S}$ = 0.97 => observed relation between BH and halo mass only if $f_{\rm PBH} \sim 1$. We predict one $10^8 M_{\rm O}$ PBHs per halo with smaller ones seeding dwarf galaxies.

CONCLUSIONS

PBH studies have already led to profound insights into cosmology and fundamental physics, even if they never formed.

Until recently most work focused on PBH constraints but now they have been invoked to explain numerous cosmological conundra:

Cosmic rays

Dark matter

LIGO/Virgo

Cosmic structure

These are distinct roles but PBHs with extended mass function could play all of them and fine-tuning of collapse fraction.

PBHs naturally form at QCD epoch and could thereby explain both dark matter and baryon asymmetry.