# Minimal gauged $U(1)_{L_{\mu}-L_{\tau}}$ model and leptogenesis

K. Asai, K. Hamaguchi, N. Nagata, S.-Y. Tseng, K. Tsumura, arXiv:1811.07571, PhysRevD.99.055029 K. Asai, K. Hamaguchi, N. Nagata, S.-Y. Tseng, in preparation



#### Shih-Yen Tseng

High Energy Physics Theory Group

Department of Physics, The Univ. of Tokyo

# Contents

- Introduction
- Minimal models
- Neutrino physics
- Leptogenesis
- Summary

G<sub>SM</sub>

Extending the gauge sector of SM

 $SU(3)_{C} \times SU(2)_{L} \times U(1)_{Y} \times U(1)_{L_{\alpha}-L_{\beta}}$ 

R. Foot, Mod.Phys.Lett. A6 (1991) 527-530 X.-G. He et al, Phys. Rev. D 43, R22

G<sub>SM</sub>

Extending the gauge sector of SM

 $SU(3)_{C} \times SU(2)_{L} \times U(1)_{Y} \times U(1)_{L_{\alpha}-L_{\beta}}$ 

 $U(1)_{L_e-L_{\mu}}$   $U(1)_{L_e-L_{\tau}}$   $U(1)_{L_{\mu}-L_{\tau}}$ 

X.-G. He et al, Phys. Rev. D 43, R22

R. Foot, Mod.Phys.Lett. A6 (1991) 527-530

• Transforming the lepton sector nontrivially compatible with the existing experimental data?

• Light neutrino mass  $\rightarrow$  adding RH neutrinos

 $M_{\nu} = -M_D M_R^{-1} M_D^T$ 

Seesaw mechanism P. Minkowski, Phys. Lett. B67 (1977) 421–428 T. Yanagida, Conf. Proc. C7902131 (1979) 95–99

! mass terms tightly restricted by the  $U(1)_{L_{\alpha}-L_{\beta}}$  symmetry

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! mass terms tightly restricted by the  $U(1)_{L_{\alpha}-L_{\beta}}$  symmetry

$$\begin{pmatrix} * & 0 & 0 \\ 0 & 0 & * \\ 0 & * & 0 \end{pmatrix} \simeq \begin{pmatrix} * & 0 & 0 \\ 0 & * & 0 \\ 0 & 0 & * \end{pmatrix} \begin{pmatrix} * & 0 & 0 \\ 0 & 0 & * \\ 0 & * & 0 \end{pmatrix} \begin{pmatrix} * & 0 & 0 \\ 0 & * & 0 \\ 0 & 0 & * \end{pmatrix} \begin{pmatrix} * & 0 & 0 \\ 0 & * & 0 \\ 0 & 0 & * \end{pmatrix}$$

block-diagonal

this simple structure fails to explain the sizable neutrino mixing...

• Spontaneous breaking of  $U(1)_{L_{\alpha}-L_{\beta}}$  symmetry

introduce only one additional scalar field



Two-zero structure leads into strong predictive power!

# Minimal models

K. Asai, K. Hamaguchi, N. Nagata, S.-Y. Tseng, K. Tsumura, arXiv:1811.07571, PhysRevD.99.055029

# A brief summary

The Standard Model  $\otimes$ 

$$\begin{cases} U(1)_{L_e - L_{\mu}} \\ U(1)_{L_e - L_{\tau}} \\ U(1)_{L_{\mu} - L_{\tau}} \end{cases}$$

 $\otimes$  3 RH neutrinos

 $\otimes \left( \begin{array}{c} \text{an extra scalar singlet} \\ \text{an extra scalar doublet} \end{array} \right)$ 

(normal mass ordering inverted mass ordering)  $\otimes$ 

# A brief summary



Phys.Rev. D99 (2019) no.5, 055029

#### $\otimes$ 3 RH neutrinos

an extra scalar singlet  $\otimes$ 

excluded by neutrino oscillation data, cosmological bound on  $\sum_i m_i$ , etc



Charge assignment

$L_{\mu} - L_{\tau}$	$L_{e,\mu, au}$	$e_R, \mu_R,  au_R$	$N_{e,\mu, au}$	$\sigma$	H
$U(1)_{Y}$	$-\frac{1}{2}$	-1	0	0	$+\frac{1}{2}$
$U(1)_{L_{\mu}-L_{\tau}}$	0,+1,-1	0,+1,-1	0,+1,-1	+1	0
SU(2)	2	1	1	1	2

Charge assignment

$L_{\mu} - L_{\tau}$	$L_{e,\mu, au}$	$e_R, \mu_R,  au_R$	$N_{e,\mu, au}$	$\sigma$	H
$U(1)_{Y}$	$-\frac{1}{2}$	-1	0	0	$+\frac{1}{2}$
$\mathrm{U}(1)_{\mathrm{L}_{\mu}-\mathrm{L}_{ au}}$	0,+1,-1	0,+1,-1	0,+1,-1	+1	0
SU(2)	2	1	1	1	2

$$\Delta \mathcal{L} = -y_e e_R^c L_e H^{\dagger} - y_{\mu} \mu_R^c L_{\mu} H^{\dagger} - y_{\tau} \tau_R^c L_{\tau} H^{\dagger} - \lambda_e N_e^c (L_e \cdot H) - \lambda_{\mu} N_{\mu}^c (L_{\mu} \cdot H) - \lambda_{\tau} N_{\tau}^c (L_{\tau} \cdot H) - \frac{1}{2} M_{ee} N_e^c N_e^c - M_{\mu\tau} N_{\mu}^c N_{\tau}^c - \lambda_{e\mu} \sigma N_e^c N_{\mu}^c - \lambda_{e\tau} \sigma^* N_e^c N_{\tau}^c + \text{h.c.}$$

# Neutrino physics

# After the SSB of $\sigma$

• Lepton mass matrices

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neutrino sector

$$M_D = \frac{v}{\sqrt{2}} \begin{pmatrix} \lambda_e & 0 & 0\\ 0 & \lambda_\mu & 0\\ 0 & 0 & \lambda_\tau \end{pmatrix} \qquad M_R = \begin{pmatrix} M_{ee} & \lambda_{e\mu} \langle \sigma \rangle & \lambda_{e\tau} \langle \sigma \rangle\\ \lambda_{e\mu} \langle \sigma \rangle & 0 & M_{\mu\tau}\\ \lambda_{e\tau} \langle \sigma \rangle & M_{\mu\tau} & 0 \end{pmatrix}$$

# After the SSB of $\sigma$

Lepton mass matrices

neutrino sector

$$M_D = \frac{v}{\sqrt{2}} \begin{pmatrix} \lambda_e & 0 & 0\\ 0 & \lambda_\mu & 0\\ 0 & 0 & \lambda_\tau \end{pmatrix} \qquad M_R = \begin{pmatrix} M_{ee} & \lambda_{e\mu} \langle \sigma \rangle & \lambda_{e\tau} \langle \sigma \rangle\\ \lambda_{e\mu} \langle \sigma \rangle & 0 & M_{\mu\tau}\\ \lambda_{e\tau} \langle \sigma \rangle & M_{\mu\tau} & 0 \end{pmatrix}$$

charged lepton sector

$$M_{\ell} = \frac{v}{\sqrt{2}} \begin{pmatrix} y_e & 0 & 0\\ 0 & y_{\mu} & 0\\ 0 & 0 & y_{\tau} \end{pmatrix}$$

$$M_D = \frac{v}{\sqrt{2}} \begin{pmatrix} \lambda_e & 0 & 0\\ 0 & \lambda_\mu & 0\\ 0 & 0 & \lambda_\tau \end{pmatrix} \qquad M_R = \begin{pmatrix} M_{ee} & \lambda_{e\mu} \langle \sigma \rangle & \lambda_{e\tau} \langle \sigma \rangle\\ \lambda_{e\mu} \langle \sigma \rangle & 0 & M_{\mu\tau}\\ \lambda_{e\tau} \langle \sigma \rangle & M_{\mu\tau} & 0 \end{pmatrix}$$

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$$U_{\text{PMNS}} = U_{L}^{\dagger} U_{\nu}$$

$$M_{\nu}^{-1} = -(M_{D}^{-1})^{T} M_{R} M_{D}^{-1} = \begin{pmatrix} * & * \\ * & 0 \\ * & 0 \end{pmatrix} = U_{\nu} (M_{\nu}^{d})^{-1} U_{\nu}^{T}$$

$$M_{\nu} = -M_{D} M_{R}^{-1} M_{D}^{T}$$

$$M_{\nu} = U_{\nu}^{*} M_{\nu}^{d} U_{\nu}^{\dagger}$$



### Input parameters

#### global-fitting group

NuFIT 4.1 (2019)

		Normal Oro	lering (best fit)	Inverted Ordering ( $\Delta \chi^2 = 10.4$ )		
		bfp $\pm 1\sigma$	$3\sigma$ range	bfp $\pm 1\sigma$	$3\sigma$ range	
with SK atmospheric data	$\sin^2 heta_{12}$	$0.310\substack{+0.013\\-0.012}$	$0.275 \rightarrow 0.350$	$0.310\substack{+0.013\\-0.012}$	$0.275 \rightarrow 0.350$	
	$ heta_{12}/^{\circ}$	$33.82\substack{+0.78 \\ -0.76}$	$31.61 \rightarrow 36.27$	$33.82\substack{+0.78 \\ -0.75}$	$31.61 \rightarrow 36.27$	
	$\sin^2 heta_{23}$	$0.563\substack{+0.018\\-0.024}$	$0.433 \rightarrow 0.609$	$0.565\substack{+0.017\\-0.022}$	$0.436 \rightarrow 0.610$	
	$ heta_{23}/^{\circ}$	$48.6^{+1.0}_{-1.4}$	$41.1 \rightarrow 51.3$	$48.8^{+1.0}_{-1.2}$	$41.4 \rightarrow 51.3$	
	$\sin^2 heta_{13}$	$0.02237\substack{+0.00066\\-0.00065}$	$0.02044 \rightarrow 0.02435$	$0.02259\substack{+0.00065\\-0.00065}$	$0.02064 \rightarrow 0.02457$	
	$ heta_{13}/^\circ$	$8.60\substack{+0.13 \\ -0.13}$	$8.22 \rightarrow 8.98$	$8.64^{+0.12}_{-0.13}$	$8.26 \rightarrow 9.02$	
	$\delta_{ m CP}/^{\circ}$	$221^{+39}_{-28}$	$144 \rightarrow 357$	$282^{+23}_{-25}$	$205 \rightarrow 348$	
	$\frac{\Delta m_{21}^2}{10^{-5} \ {\rm eV}^2}$	$7.39\substack{+0.21 \\ -0.20}$	6.79  ightarrow 8.01	$7.39\substack{+0.21 \\ -0.20}$	6.79  ightarrow 8.01	
	$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.528^{+0.029}_{-0.031}$	$+2.436 \rightarrow +2.618$	$-2.510\substack{+0.030\\-0.031}$	-2.601  ightarrow -2.419	

## Results

Minimal gauged  $U(1)_{L_{\mu}-L_{\tau}}$  model, normal mass ordering





# Results

Minimal gauged  $U(1)_{L_{\mu}-L_{\tau}}$  model, normal mass ordering





# Leptogenesis in the minimal gauged $U(1)_{L_{\mu}-L_{\tau}}$ model

K. Asai, K. Hamaguchi, N. Nagata, S.-Y. Tseng, in preparation

M. Fukugita, T. Yanagida, Phys. Lett. B174, 45 (1986)

• Baryon asymmetry in the universe

$$Y_{\Delta B} \equiv \frac{n_B}{s} \simeq 8.7 \times 10^{-11}$$

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Decays of RH neutrinos generate lepton asymmetry



• Baryon asymmetry in the universe

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Decays of RH neutrinos generate lepton asymmetry

$$\frac{1}{(8\pi)} \frac{1}{[\lambda^{\dagger}\lambda]_{11}} \sum_{j} \operatorname{Im} \left\{ [(\lambda^{\dagger}\lambda)_{1j}]^2 \right\} g\left(x_j\right)$$

$$\lambda: \text{Yukawa coupling}$$

$$g(x) = \sqrt{x} \left[ \frac{1}{1-x} + 1 - (1+x) \ln\left(\frac{1+x}{x}\right) \right] \qquad x_j = \frac{M_j^2}{M_1^2}$$

• Baryon asymmetry in the universe

$$Y_{\Delta B} \equiv \frac{n_B}{s} \simeq 8.7 \times 10^{-11}$$

- Decays of RH neutrinos generate lepton asymmetry
- Sphaleron processes

V. A. Kuzmin et al., Phys. Lett. 155B (1985) 36

$$n_B = \frac{28}{79} \times (n_B - n_L)$$



# **Right-handed neutrino sector**

• RH neutrino mass matrix  $M_R = -M_D^T M_v^{-1} M_D$ 

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- RH neutrino mass matrix  $M_R = -M_D^T M_v^{-1} M_D$
- Parameters  $(\lambda_e, \lambda_\mu, \lambda_\tau) \equiv \lambda(\cos\theta, \sin\theta\cos\phi, \sin\theta\sin\phi)$

### **Right-handed neutrino sector**

- RH neutrino mass matrix  $M_R = -M_D^T M_v^{-1} M_D$
- Parameters  $(\lambda_e, \lambda_\mu, \lambda_\tau) \equiv \lambda(\cos\theta, \sin\theta\cos\phi, \sin\theta\sin\phi)$

$$\Delta \mathcal{L} = -\sum_{\alpha=e,\mu,\tau} \sum_{i=1}^{3} \hat{\lambda}_{\alpha i} \left( L_{\alpha} \cdot H \right) \hat{N}_{i}^{c} - \frac{1}{2} \sum_{i=1}^{3} M_{Ri}^{\text{diag}} \hat{N}_{i}^{c} \hat{N}_{i}^{c} + \text{h.c.}$$

$$M_R = \Omega^* M_R^{\text{diag}} \Omega^{\dagger} , \ \hat{N}_i^c = \sum_{\alpha} \Omega_{i\alpha}^{\dagger} N_{\alpha}^c , \ \hat{\lambda}_{\alpha i} = \sum_{\beta} \lambda_{\alpha \beta} \Omega_{\beta i}$$

• RH neutrino non-thermal decay :  $T_R = \left(\frac{90}{-2\pi}\right)^2$ 

$$\left(\frac{90}{\pi^2 g_*}\right)^{\frac{1}{4}} \sqrt{\Gamma_\sigma M_P} < M_1$$

• RH neutrino non-thermal decay :  $T_R = \left(\frac{90}{\pi^2 g_*}\right)^{\frac{1}{4}} \sqrt{\Gamma_{\sigma} M_P} < M_1$ 

Pairs of RH neutrinos generated from inflaton decays

• Taking  $\sigma$  as inflaton

$$\Delta \mathcal{L} = -y_e e_R^c L_e H^{\dagger} - y_{\mu} \mu_R^c L_{\mu} H^{\dagger} - y_{\tau} \tau_R^c L_{\tau} H^{\dagger} - \lambda_e N_e^c (L_e \cdot H) - \lambda_{\mu} N_{\mu}^c (L_{\mu} \cdot H) - \lambda_{\tau} N_{\tau}^c (L_{\tau} \cdot H) - \frac{1}{2} M_{ee} N_e^c N_e^c - M_{\mu\tau} N_{\mu}^c N_{\tau}^c - \lambda_{e\mu} \sigma N_e^c N_{\mu}^c - \lambda_{e\tau} \sigma^* N_e^c N_{\tau}^c + \text{h.c.}$$

• RH neutrino non-thermal decay :  $T_R = \left(\frac{90}{\pi^2 g_*}\right)^{\frac{1}{4}} \sqrt{\Gamma_{\sigma} M_P} < M_1$ 

• Pairs of RH neutrinos generated from inflaton decays

• Taking  $\sigma$  as inflaton

$$\mathcal{L}_{\sigma} = \frac{|\partial_{\mu}\sigma|^2}{(1-|\sigma|^2/\Lambda^2)^2} - \kappa(|\sigma|^2 - \langle\sigma\rangle^2)^2$$

• RH neutrino non-thermal decay :  $T_R = \left(\frac{90}{\pi^2 g_*}\right)^{\frac{1}{4}} \sqrt{\Gamma_{\sigma} M_P} < M_1$ 

Pairs of RH neutrinos generated from inflaton decays

• Taking  $\sigma$  as inflaton  $\mathcal{L}_{\sigma} = \frac{1}{2} (\partial \widetilde{\varphi})^2 - \kappa \Lambda^4 \left[ \tanh^2 \left( \frac{\widetilde{\varphi}}{\sqrt{2}\Lambda} \right) - \left( \frac{\langle \sigma \rangle}{\Lambda} \right)^2 \right]^2 \quad \frac{\varphi}{\sqrt{2}\Lambda} \equiv \tanh \left( \frac{\widetilde{\varphi}}{\sqrt{2}\Lambda} \right)$
• RH neutrino non-thermal decay :  $T_R = \left(\frac{90}{\pi^2 g_*}\right)^{\frac{1}{4}} \sqrt{\Gamma_{\sigma} M_P} < M_1$ 

• Pairs of RH neutrinos generated from inflaton decays

• Taking  $\sigma$  as inflaton

$$m_{\sigma} \simeq 3.4 \times 10^{13} \times (\langle \sigma \rangle / \Lambda) \text{ GeV}$$

from CMB normalization

• Inflaton  $\sigma$ 

$$m_{\sigma} \simeq 3.4 \times 10^{13} \times (\langle \sigma \rangle / \Lambda) \text{ GeV}$$

- Pairs of RH neutrinos generated from inflaton decays
- RH neutrino non-thermal decay :  $T_R = \left(\frac{90}{\pi^2 g_*}\right)^{\frac{1}{4}} \sqrt{\Gamma_{\sigma} M_P} < M_1$
- Baryon asymmetry

$$Y_B = \frac{n_B}{s} = \frac{n_\phi}{s} \times \frac{n_N}{n_\phi} \times \frac{n_L}{n_N} \times \frac{n_B}{n_L}$$







#### Result



 $\log_{10}\langle\sigma\rangle$ 

#### Result



# Summary

## Summary

- Among minimal  $U(1)_{L_{\alpha}-L_{\beta}}$  models, only one survives constraints  $U(1)_{L_{\mu}-L_{\tau}}$  extension with an extra  $SU(2)_{L}$  scalar singlet
- Minimal gauged  $\text{U}(1)_{L_{\alpha}-L_{\beta}}$  models are driven into a corner

• Potential of successful leptogenesis

## Backup

#### Inflaton mass $\langle \zeta(\vec{k})\,\zeta(\vec{k}')\rangle = (2\pi)^3 \delta(\vec{k}+\vec{k}')\frac{2\pi^2}{\iota^3}\mathcal{P}_{\zeta}(k)$ $\zeta = -\frac{H_{\rm inf}}{\dot{\phi}}\delta\phi$ $\mathcal{P}_{\zeta}(k) = \frac{H_{\inf}^4}{4\pi^2(\dot{\phi})^2} = \frac{V^3}{12\pi^2(V')^2 M_C^6}$ $P_{\zeta} = \frac{V^3}{12\pi^2 M_D^6 V'^2}$ $= \frac{\kappa \Lambda^6}{96\pi^2 M_P^6} \left\{ 1 - \left[ \frac{\kappa}{\Lambda} \coth \left( \frac{\widetilde{\varphi}}{\sqrt{2}\Lambda} \right) \right]^2 \right\}^4 \sinh^4 \left( \frac{\widetilde{\varphi}}{\sqrt{2}\Lambda} \right) \tanh^2 \left( \frac{\widetilde{\varphi}}{\sqrt{2}\Lambda} \right)$ $\simeq \frac{\kappa}{6\pi^2} \left[ \frac{N_e \left( \Lambda^2 - \left\langle \sigma \right\rangle^2 \right)}{M_P \Lambda} \right]^2 \,.$ $m_{\sigma}^{2} = \frac{d^{2}V}{d\widetilde{\varphi}^{2}}\Big|_{\widetilde{\varphi} = \widetilde{\varphi}_{\min}} = 4\kappa \left\langle \sigma \right\rangle^{2} \left(1 - \frac{\left\langle \sigma \right\rangle^{2}}{\Lambda^{2}}\right)^{2}$

 $P_{\zeta} \simeq 2.1 \times 10^{-9}$   $m_{\sigma} \simeq 3.4 \times 10^{13} \times (\langle \sigma \rangle / \Lambda) \text{ GeV}$ 

$$\kappa \simeq 2.9 \times 10^{-2} \times \left(\frac{50}{N_e}\right)^2 \times \left(\frac{10^{14} \text{ GeV}}{\Lambda}\right)^2 \times \left(1 - \frac{\langle \sigma \rangle^2}{\Lambda^2}\right)^{-2}$$

• Taking  $\sigma$  as inflaton



#### Inflaton potential

![](_page_48_Figure_1.jpeg)

#### **Cosmic string**

$$\mathcal{L}=D_{\mu}\Phi D^{\mu}\Phi^{\dagger}-rac{1}{4}F_{\mu
u}F^{\mu
u}-\lambda(\Phi^{\dagger}\Phi-\sigma^{2}/2)^{2}$$

$$\mu \equiv \frac{dH}{dz} = \int r dr d\theta \mathcal{H} = -\int r dr d\theta \mathcal{L}$$
$$= \int_0^\infty \int_0^{2\pi} r dr d\theta \left[ \left| \frac{\partial \Phi}{\partial r} \right|^2 + \left| \frac{1}{r} \frac{\partial \Phi}{\partial \theta} - ieA_\theta \Phi \right|^2 + V(\Phi) + \frac{B^2}{2} \right]$$

$$\mu \simeq \pi \sigma^2$$

#### **Cosmic string**

 $\mu \simeq \pi \sigma^2$ 

#### $G\mu < 2.4 \times 10^{-7}$

![](_page_50_Picture_3.jpeg)

#### What are the contents?

#### • The SM

	$L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$	$e_R$	$Q = \begin{pmatrix} u_L \\ d_L \end{pmatrix}$	$u_R$	$d_R$	Н
$SU(3)_C$	1	1	3	3	3	1
$SU(2)_L$	2	1	2	1	1	2
$U(1)_{\rm Y}$	$-\frac{1}{2}$	-1	$\frac{1}{6}$	$\frac{2}{3}$	$-\frac{1}{3}$	$\frac{1}{2}$

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	$L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$	$e_R$	$Q = \begin{pmatrix} u_L \\ d_L \end{pmatrix}$	$u_R$	$d_R$	Н
${ m SU}(3)_{ m C}$	1	1	3	3	3	1
$SU(2)_L$	2	1	2	1	1	2
$U(1)_{Y}$	$-\frac{1}{2}$	-1	$\frac{1}{6}$	$\frac{2}{3}$	$-\frac{1}{3}$	$\frac{1}{2}$

• Three RH neutrinos

#### What are the contents?

• The SM

	$L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$	$e_R$	$Q = \begin{pmatrix} u_L \\ d_L \end{pmatrix}$	$u_R$	$d_R$	Н
${ m SU}(3)_{ m C}$	1	1	3	3	3	1
${ m SU}(2)_{ m L}$	2	1	2	1	1	2
$U(1)_{Y}$	$-\frac{1}{2}$	-1	$\frac{1}{6}$	$\frac{2}{3}$	$-\frac{1}{3}$	$\frac{1}{2}$

- Three RH neutrinos
- One extra scalar field

• Case (i)

one SU(2)<sub>L</sub> scalar singlet  $\sigma$  with Y = 0 and Q(U(1)<sub>L<sub> $\alpha$ </sub>-L<sub> $\beta$ </sub>) = +1</sub>

• Case (ii)

one SU(2)<sub>L</sub> scalar doublet  $\Phi_1$  with Y = +1/2 and Q(U(1)<sub>L<sub>\alpha</sub>-L<sub>β</sub></sub>) = +1

• Case (iii)

one SU(2)<sub>L</sub> scalar doublet  $\Phi_1$  with Y = +1/2 and Q(U(1)<sub>L<sub>\alpha</sub>-L<sub>β</sub>) = -1</sub>

$L_{\mu} - L_{\tau}$	$L_{e,\mu, au}$	$e_R, \mu_R,  au_R$	$N_{e,\mu, au}$	$\sigma$	$\Phi_{1,2}$
$U(1)_{Y}$	$-\frac{1}{2}$	-1	0	0	$+\frac{1}{2}$
$ [ U(1)_{L_{\mu}-L_{\tau}} ] $	0,+1,-1	0,+1,-1	0,+1,-1	+1	$\pm 1,0$
SU(2)	2	1	1	1	2

• Case (i) 
$$\Delta \mathcal{L} = -y_e e_R^c L_e H^{\dagger} - y_{\mu} \mu_R^c L_{\mu} H^{\dagger} - y_{\tau} \tau_R^c L_{\tau} H^{\dagger} \\ -\lambda_e N_e^c (L_e \cdot H) - \lambda_{\mu} N_{\mu}^c (L_{\mu} \cdot H) - \lambda_{\tau} N_{\tau}^c (L_{\tau} \cdot H) \\ -\frac{1}{2} M_{ee} N_e^c N_e^c - M_{\mu\tau} N_{\mu}^c N_{\tau}^c - \lambda_{e\mu} \sigma N_e^c N_{\mu}^c - \lambda_{e\tau} \sigma^* N_e^c N_{\tau}^c + \text{h.c.}$$

• **Case (ii)**  

$$\Delta \mathcal{L} = -y_e e_R^c L_e \Phi_2^{\dagger} - y_{\mu} \mu_R^c L_{\mu} \Phi_2^{\dagger} - y_{\tau} \tau_R^c L_{\tau} \Phi_2^{\dagger} - y_{\mu e} e_R^c L_{\mu} \Phi_1^{\dagger} - y_{e\tau} \tau_R^c L_e \Phi_1^{\dagger} - \lambda_e N_e^c (L_e \cdot \Phi_2) - \lambda_{\mu} N_{\mu}^c (L_{\mu} \cdot \Phi_2) - \lambda_{\tau} N_{\tau}^c (L_{\tau} \cdot \Phi_2) - \lambda_{\tau e} N_e^c (L_{\tau} \cdot \Phi_1) - \lambda_{e\mu} N_{\mu}^c (L_e \cdot \Phi_1) - \frac{1}{2} M_{ee} N_e^c N_e^c - M_{\mu\tau} N_{\mu}^c N_{\tau}^c + \text{h.c.}$$

• **Case (iii)**  

$$\Delta \mathcal{L} = -y_e e_R^c L_e \Phi_2^{\dagger} - y_{\mu} \mu_R^c L_{\mu} \Phi_2^{\dagger} - y_{\tau} \tau_R^c L_{\tau} \Phi_2^{\dagger} - y_{\tau e} e_R^c L_{\tau} \Phi_1^{\dagger} - y_{e\mu} \mu_R^c L_e \Phi_1^{\dagger} - \lambda_e N_e^c (L_e \cdot \Phi_2) - \lambda_{\mu} N_{\mu}^c (L_{\mu} \cdot \Phi_2) - \lambda_{\tau} N_{\tau}^c (L_{\tau} \cdot \Phi_2) - \lambda_{\mu e} N_e^c (L_{\mu} \cdot \Phi_1) - \lambda_{e\tau} N_{\tau}^c (L_e \cdot \Phi_1) - \frac{1}{2} M_{ee} N_e^c N_e^c - M_{\mu\tau} N_{\mu}^c N_{\tau}^c + \text{h.c.}$$

#### After the SSB...

• **Case (i)**  

$$M_{D} = \frac{v}{\sqrt{2}} \begin{pmatrix} \lambda_{e} & 0 & 0 \\ 0 & \lambda_{\mu} & 0 \\ 0 & 0 & \lambda_{\tau} \end{pmatrix} \quad M_{R} = \begin{pmatrix} M_{ee} & \lambda_{e\mu} \langle \sigma \rangle & \lambda_{e\tau} \langle \sigma \rangle \\ \lambda_{e\mu} \langle \sigma \rangle & 0 & M_{\mu\tau} \\ \lambda_{e\tau} \langle \sigma \rangle & M_{\mu\tau} & 0 \end{pmatrix} \quad M_{\ell} = \frac{v}{\sqrt{2}} \begin{pmatrix} y_{e} & 0 & 0 \\ 0 & y_{\mu} & 0 \\ 0 & 0 & y_{\tau} \end{pmatrix}$$

• **Case (ii)**  

$$M_{D} = \frac{1}{\sqrt{2}} \begin{pmatrix} \lambda_{e}v_{2} & \lambda_{e\mu}v_{1} & 0 \\ 0 & \lambda_{\mu}v_{2} & 0 \\ \lambda_{\tau e}v_{1} & 0 & \lambda_{\tau}v_{2} \end{pmatrix} M_{R} = \begin{pmatrix} M_{ee} & 0 & 0 \\ 0 & 0 & M_{\mu\tau} \\ 0 & M_{\mu\tau} & 0 \end{pmatrix} M_{\ell} = \frac{1}{\sqrt{2}} \begin{pmatrix} y_{e}v_{2} & 0 & y_{e\tau}v_{1} \\ y_{\mu e}v_{1} & y_{\mu}v_{2} & 0 \\ 0 & 0 & y_{\tau}v_{2} \end{pmatrix}$$

• **Case (iii)**  

$$M_{D} = \frac{1}{\sqrt{2}} \begin{pmatrix} \lambda_{e}v_{2} & 0 & \lambda_{e\tau}v_{1} \\ \lambda_{\mu e}v_{1} & \lambda_{\mu}v_{2} & 0 \\ 0 & 0 & \lambda_{\tau}v_{2} \end{pmatrix} M_{R} = \begin{pmatrix} M_{ee} & 0 & 0 \\ 0 & 0 & M_{\mu\tau} \\ 0 & M_{\mu\tau} & 0 \end{pmatrix} M_{\ell} = \frac{1}{\sqrt{2}} \begin{pmatrix} y_{e}v_{2} & y_{e\mu}v_{1} & 0 \\ 0 & y_{\mu}v_{2} & 0 \\ y_{\tau e}v_{1} & 0 & y_{\tau}v_{2} \end{pmatrix}$$

#### After the SSB... ! cases (ii), (iii), $v = \sqrt{v_1^2 + v_2^2} \simeq 246 \text{ GeV}$

• **Case (i)**  $M_{D} = \frac{v}{\sqrt{2}} \begin{pmatrix} \lambda_{e} & 0 & 0 \\ 0 & \lambda_{\mu} & 0 \\ 0 & 0 & \lambda_{\tau} \end{pmatrix} \quad M_{R} = \begin{pmatrix} M_{ee} & \lambda_{e\mu} \langle \sigma \rangle & \lambda_{e\tau} \langle \sigma \rangle \\ \lambda_{e\mu} \langle \sigma \rangle & 0 & M_{\mu\tau} \\ \lambda_{e\tau} \langle \sigma \rangle & M_{\mu\tau} & 0 \end{pmatrix} \quad M_{\ell} = \frac{v}{\sqrt{2}} \begin{pmatrix} y_{e} & 0 & 0 \\ 0 & y_{\mu} & 0 \\ 0 & 0 & y_{\tau} \end{pmatrix}$ 

• **Case (ii)**  

$$M_{D} = \frac{1}{\sqrt{2}} \begin{pmatrix} \lambda_{e}v_{2} & \lambda_{e\mu}v_{1} & 0 \\ 0 & \lambda_{\mu}v_{2} & 0 \\ \lambda_{\tau e}v_{1} & 0 & \lambda_{\tau}v_{2} \end{pmatrix} M_{R} = \begin{pmatrix} M_{ee} & 0 & 0 \\ 0 & 0 & M_{\mu\tau} \\ 0 & M_{\mu\tau} & 0 \end{pmatrix} M_{\ell} = \frac{1}{\sqrt{2}} \begin{pmatrix} y_{e}v_{2} & 0 & y_{e\tau}v_{1} \\ y_{\mu e}v_{1} & y_{\mu}v_{2} & 0 \\ 0 & 0 & y_{\tau}v_{2} \end{pmatrix}$$

• **Case (iii)**  

$$M_{D} = \frac{1}{\sqrt{2}} \begin{pmatrix} \lambda_{e}v_{2} & 0 & \lambda_{e\tau}v_{1} \\ \lambda_{\mu e}v_{1} & \lambda_{\mu}v_{2} & 0 \\ 0 & 0 & \lambda_{\tau}v_{2} \end{pmatrix} M_{R} = \begin{pmatrix} M_{ee} & 0 & 0 \\ 0 & 0 & M_{\mu\tau} \\ 0 & M_{\mu\tau} & 0 \end{pmatrix} M_{\ell} = \frac{1}{\sqrt{2}} \begin{pmatrix} y_{e}v_{2} & y_{e\mu}v_{1} & 0 \\ 0 & y_{\mu}v_{2} & 0 \\ y_{\tau e}v_{1} & 0 & y_{\tau}v_{2} \end{pmatrix}$$

#### Introduction

Possible extension of SM

 $SU(3)_{\mathsf{C}} \times SU(2)_{\mathsf{L}} \times U(1)_{Y_{\mathsf{L}}} \times U(1)_{\mathsf{L}_{\alpha} - \mathsf{L}_{\beta} \quad \alpha, \beta \in e, \mu, \tau}$ Mod.Phys.Lett. A6 (1991) 527-530 G<sub>SM</sub> Phys. Rev. D 43, R22 Z'•  $U(1)_{L_{\mu}-L_{\tau}}$  models *g* – 2: PRD 64, 055006 (2001), PRD 84, 075007 (2011),

JHEP 03, 105 (2014)

#### Leptogenesis

 $(\lambda_e, \lambda_\mu, \lambda_\tau) \equiv \lambda(\cos\theta, \sin\theta\cos\phi, \sin\theta\sin\phi)$ 

![](_page_59_Figure_2.jpeg)

#### Leptogenesis

![](_page_60_Figure_1.jpeg)

![](_page_60_Figure_2.jpeg)

![](_page_61_Figure_0.jpeg)

#### LFV process in cases (ii) and (iii)

$$\Gamma(\tau \to eZ') = \frac{g_{Z'}^2 m_{\tau}}{128\pi} \sin^2 2\theta_L \left(2 + \frac{m_{\tau}^2}{m_{Z'}^2}\right) \left(1 - \frac{m_{Z'}^2}{m_{\tau}^2}\right)^2$$

$$|\sin 2\theta_L| < \begin{cases} 7 \times 10^{-5} & \text{for } m_{Z'} = 100 \text{ MeV and } g_{Z'} = 10^{-3} \\ 1 \times 10^{-5} & \text{for } m_{Z'} = 10 \text{ MeV and } g_{Z'} = 5 \times 10^{-4} \end{cases} \qquad \text{BR}(\tau \to eX) \lesssim 2.7 \times 10^{-3} \\ \text{Z.Phys. C68 (1995) 25-28} \qquad Z' \end{cases}$$

$$\theta_{L,R} \simeq 0 \text{ or } \frac{\pi/2}{\sqrt{2}} \qquad U_{L,R} \simeq \begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix} \implies Q_{\mu-\tau} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \rightarrow \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix} = Q_{\mu-e}$$

$$M_l = U_L \begin{pmatrix} m_e & 0 & 0 \\ 0 & m_\mu & 0 \\ 0 & 0 & m_\tau \end{pmatrix} U_R^T \implies \text{Symmetry group } \mathbf{S}_3 : D_3(g) \begin{pmatrix} m_e & 0 & 0 \\ 0 & m_\mu & 0 \\ 0 & 0 & m_\tau \end{pmatrix} D_3^T(g)$$

$$g = \underbrace{g_{e\mu\tau}}_{U(1)_{L_\mu-L_\tau}} \underbrace{g_{\mu\tau}}_{U(1)_{L_e-L_\tau}} \underbrace{g_{\tau\mu\tau}}_{U(1)_{L_e-L_\tau}} \underbrace{g_{\tau\mu}}_{U(1)_{L_e-L_\tau}} \underbrace{g_{\tau\mu}}_{U(1)_{L_e-L_\tau}} \underbrace{g_{\tau\mu}}_{U(1)_{L_e-L_\tau}} \underbrace{g_{\tau\mu}}_{HeT, 2BR} \\ \underbrace{g_{\mu}}_{R = 0} \underbrace{g$$

 $U(L)_{L_e-L_{\mu}}$ 

PRL 113, 091801

## LFV process

![](_page_63_Figure_1.jpeg)

$$\text{LFV decay} \qquad M_{\ell} = U_{L}^{*} \begin{pmatrix} m_{e} & 0 & 0 \\ 0 & m_{\mu} & 0 \\ 0 & 0 & m_{\tau} \end{pmatrix} U_{R}^{T} \qquad U_{L,R} = \begin{pmatrix} \cos \theta_{L,R} & 0 & e^{-i\phi} \sin \theta_{L,R} \\ 0 & 1 & 0 \\ -e^{i\phi} \sin \theta_{L,R} & 0 & \cos \theta_{L,R} \end{pmatrix}$$

$$\mathcal{L}_{Z'} = g_{Z'} \overline{\ell'} \gamma^{\mu} \left[ U_L^{\dagger} Q_{\mu-\tau} U_L P_L + U_R^{\dagger} Q_{\mu-\tau} U_R P_R \right] \ell' Z'_{\mu} \qquad \frac{\tan \theta_R}{\tan \theta_L} = \frac{m_e}{m_{\tau}}$$

$$Q_{\mu-\tau} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \qquad \qquad |y_{e\tau}v_1| = \frac{(m_{\tau}^2 - m_e^2)\sin 2\theta_L}{\sqrt{(m_{\tau}^2 + m_e^2) + (m_{\tau}^2 - m_e^2)\cos 2\theta_L}}$$

$$\Gamma(\tau \to eZ') = \frac{g_{Z'}^2 m_{\tau}}{32\pi} \left[ \left| \left( U_L^{\dagger} Q_{\mu-\tau} U_L \right)_{13} \right|^2 + \left| \left( U_R^{\dagger} Q_{\mu-\tau} U_R \right)_{13} \right|^2 \right] \left( 2 + \frac{m_{\tau}^2}{m_{Z'}^2} \right) \left( 1 - \frac{m_{Z'}^2}{m_{\tau}^2} \right)^2$$

 $\begin{array}{ll} {\rm BR}(\tau \to eX) \lesssim 2.7 \times 10^{-3} & {\rm BR}(\tau^- \to e^- \mu^+ \mu^-) < 2.7 \times 10^{-8} & {\rm BR}(\tau \to e\gamma) < 3.3 \times 10^{-8} \\ {\rm Z.Phys. \ C68\ (1995)\ 25-28} & {\rm PLB\ 687:139-143,2010} & {\rm PRL\ 104:021802,2010} \end{array}$ 

#### $\mu - e$ mixing

Massless  $m_{Z'}$ BR $(\mu \rightarrow eX) \leq 10^{-6}$ Phys. Rev. D 34, 1967 13 MeV  $\leq m_{Z'} \leq 80$  MeV BR $(\mu \rightarrow eX) \leq 10^{-5}$ Phys. Rev. D 91, 052020  $m_{Z'} \leq 100$  MeV BR $(\mu \rightarrow eX) \leq 10^{-4}$ Phys. Rev. Lett. 57, 2787 Z' contributes to

Z' contributes to  $\mu \rightarrow e\gamma$  loop corrections BR( $\mu \rightarrow e\gamma$ )  $\lesssim 10^{-13}$ 

Eur. Phys. J. C (2016) 76: 434

#### Analysis of $M_{\nu}$ : Model 1

$$M_{D} = \frac{v}{\sqrt{2}} \begin{pmatrix} \lambda_{e} & 0 & 0 \\ 0 & \lambda_{\mu} & 0 \\ 0 & 0 & \lambda_{\tau} \end{pmatrix} \qquad M_{R} = \begin{pmatrix} M_{ee} & \lambda_{e\mu} \langle \sigma \rangle & \lambda_{e\tau} \langle \sigma \rangle \\ \lambda_{e\mu} \langle \sigma \rangle & 0 & M_{\mu\tau} \\ \lambda_{e\tau} \langle \sigma \rangle & M_{\mu\tau} & 0 \end{pmatrix} \qquad M_{R} = \begin{pmatrix} M_{ee} & \lambda_{e\mu} \langle \sigma \rangle & \lambda_{e\tau} \langle \sigma \rangle \\ \lambda_{e\mu} \langle \sigma \rangle & 0 & M_{\mu\tau} \\ \lambda_{e\tau} \langle \sigma \rangle & M_{\mu\tau} & 0 \end{pmatrix} \qquad M_{R} = U_{V}^{*} M_{V}^{*} U_{V}^{\dagger} \qquad M_{V} = U_{V}^{*} (M_{V}^{*})^{-1} U_{V}^{*} = U_{L}^{*} (U_{V} = U_{L}^{*} U_{V} = U_{L}^{*} (U_{V} = U_{L}^{*} U_{V} = U_{L}^{*} (U_{V} = U_{L}^{*} U_{V} = U_{L}^{*} U_{V} = U_{L}^{*} (U_{V} = U_{L}^{*} U_{V} = U_{L}^{*} U_{V} = U_{L}^{*} (U_{V} = U_{L}^{*} U_{V} = U_{L}^{*} U_{L} = U_$$

#### Analysis of $M_{\nu}$ : Model 1

![](_page_67_Figure_1.jpeg)

### Analysis of $M_{\nu}$ : Model 2

	$Q_{L_{\mu}-L_{\tau}}(\Phi_1) = +1$				$Q_{L_{\mu}-L_{\tau}}(\Phi_1) = -1$			
		$\frac{v_2^2 y_{11}'^2}{M_{11}}$	0	$v_1 v_2 \left( \frac{y'_{11}g'_{31}}{M_{11}} + \frac{y'_{33}g'_{12}}{M_{23}} \right)$		$\left( \frac{v_2^2 y_{11}'^2}{M_{11}} \right)$	$v_1 v_2 \left( \frac{y_{11}' g_{21}'}{M_{11}} + \frac{y_{22}' g_{13}'}{M_{23}} \right)$	0
$M_{\nu}$	$-\frac{1}{2}$	0	0	$\frac{v_2^2 y_{22}' y_{33}'}{M_{23}}$	$-\frac{1}{2}$	$v_1 v_2 \left( \frac{y_{11}' g_{21}'}{M_{11}} + \frac{y_{22}' g_{13}'}{M_{23}} \right)$	$rac{v_1^2 g_{21}'^2}{M_{11}}$	$\frac{v_2^2 y_{22}' y_{33}'}{M_{23}}$
		$\left(v_1v_2\left(rac{y_{11}'g_{31}'}{M_{11}}+rac{y_{33}'g_{12}'}{M_{23}} ight) ight)$	$\frac{v_2^2 y_{22}' y_{33}'}{M_{23}}$	$rac{v_2^1 g_{31}'^2}{M_{11}}$		0	$rac{v_2^2y_{22}'y_{33}'}{M23}$	0

#### Basic Idea of the analysis

![](_page_69_Figure_1.jpeg)

## Analysis of $M_{\nu}$

#### Scalar-doublet case

![](_page_70_Figure_2.jpeg)

#### Analysis of $M_{\nu}$ : case(iii)

$$M_{\nu} = -\begin{pmatrix} \frac{\lambda_e^2 v_2^2}{2M_{ee}} & \frac{\lambda_{e\tau} \lambda_{\mu} v_1 v_2}{2M_{\mu\tau}} + \frac{\lambda_e \lambda_{\mu e} v_1 v_2}{2M_{ee}} & 0\\ \frac{\lambda_{e\tau} \lambda_{\mu} v_1 v_2}{2M_{\mu\tau}} + \frac{\lambda_e \lambda_{\mu e} v_1 v_2}{2M_{ee}} & \frac{\lambda_{\mu e}^2 v_1^2}{2M_{ee}} & \frac{\lambda_{\mu} \lambda_{\tau} v_2^2}{2M_{\mu\tau}} \\ 0 & \frac{\lambda_{\mu} \lambda_{\tau} v_2^2}{2M_{\mu\tau}} & 0 \end{pmatrix}$$

$$\begin{bmatrix} D_3(g)U_{\text{PMNS}}^* \text{diag}(m_1, m_2, m_3)U_{\text{PMNS}}^\dagger D_3^T(g) \end{bmatrix}_{e\tau} = 0$$
$$\begin{bmatrix} D_3(g)U_{\text{PMNS}}^* \text{diag}(m_1, m_2, m_3)U_{\text{PMNS}}^\dagger D_3^T(g) \end{bmatrix}_{\tau\tau} = 0$$

71
## Analysis of $M_{\nu}$ : case (ii)

$$M_{D} = \frac{1}{\sqrt{2}} \begin{pmatrix} \lambda_{e}v_{2} & \lambda_{e\mu}v_{1} & 0 \\ 0 & \lambda_{\mu}v_{2} & 0 \\ \lambda_{\tau e}v_{1} & 0 & \lambda_{\tau}v_{2} \end{pmatrix} M_{R} = \begin{pmatrix} M_{ee} & 0 & 0 \\ 0 & 0 & M_{\mu\tau} \\ 0 & M_{\mu\tau} & 0 \end{pmatrix}$$

$$Two-zero texture$$

$$M_{\nu} = -\begin{pmatrix} \frac{\lambda_{e}^{2}v_{2}^{2}}{2M_{ee}} & 0 & \frac{\lambda_{e\mu}\lambda_{\tau}v_{1}v_{2}}{2M_{\mu\tau}} + \frac{\lambda_{e}\lambda_{\tau e}v_{1}v_{2}}{2M_{\mu\tau}} \\ 0 & 0 & \frac{\lambda_{\mu}\lambda_{\tau}v_{2}^{2}}{2M_{\mu\tau}} \\ \frac{\lambda_{\mu}\lambda_{\tau}v_{2}^{2}}{2M_{\mu\tau}} + \frac{\lambda_{e}\lambda_{\tau}v_{2}^{2}}{2M_{\mu\tau}} & \frac{\lambda_{\mu}\lambda_{\tau}v_{2}^{2}}{2M_{\mu\tau}} \\ \end{bmatrix}$$

$$M_{\nu} = \begin{pmatrix} m_{\nu} & m_{\nu} & m_{\nu} \\ 0 & m_{\nu} & m_{\nu} \\ m_{\nu} & m_{\nu} \\ m_{\nu} & m_{\nu} & m_{\nu} \\ m_{\nu}$$

# Neutrino phenomenology : case (i)



## Neutrino phenomenology : case (i)

 $U(1)_{L_{\mu}-L_{\tau}}$  normal ordering :



### Neutrino phenomenology : cases (ii), (iii)

 $U(1)_{L_{u}-L_{\tau}}$  normal ordering with  $U(1)_{L_{u}-L_{\tau}}(\Phi_{1}) = +1$ : 0.25 The tight bound set by 0.2 Planck exp.  $\sum_{i} m_{i} < 0.12 \text{ eV}$ [\_\_\_\_\_0.15 [\_\_\_\_\_] Δ\_\_\_\_\_\_\_ 0.1 Planck, arXiv:1807.06209 PlanckTT+lowP+lensing+ 0.1  $U(1)_{L_{\alpha}-L_{\beta}}$  models with an extra 0.05 scalar doublet are excluded 42 52 44 46 48 50 *θ*<sub>23</sub> [°]

# Update of the results for case (i)

• The latest result of NuFIT

NuFIT 4.1 released in 2019

- Adopting different constraint on  $\sum_i m_i$ degenerate  $m_i$ s are assumed in the Planck results
- From a new analysis,
  - $\sum_{i} m_i < 0.121 \text{ eV}$  (degenerate)

 $\sum_i m_i < 0.146 \text{ eV}$  (normal)

We need this one.

 $\sum_{i} m_i < 0.172 \text{ eV} \text{ (inverted)}$ 

arXiv:1907.12598 [astro-ph.CO]

#### Mass ordering



Majorana phase



