

b anomalies at LHCb

status and prospect

A. Hicheur*

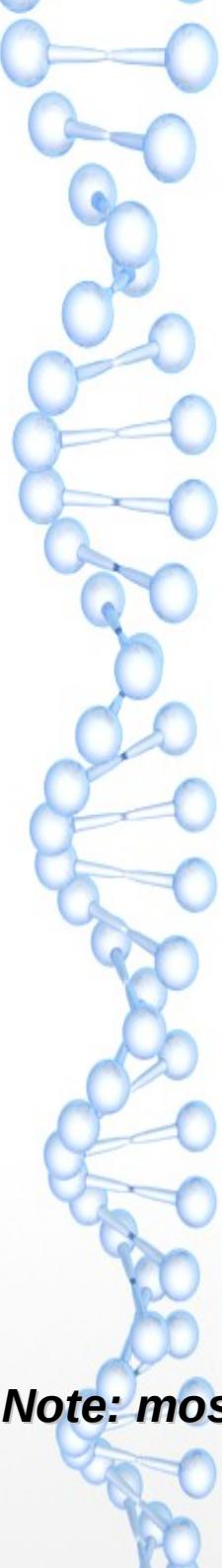
UFRJ

On behalf of the LHCb collaboration

Beauty, 21-24 September 2020, Japan (virtual)

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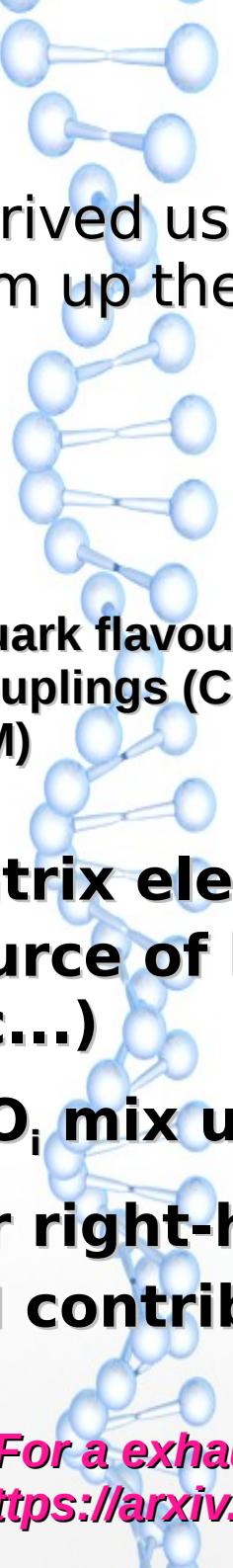




Outline

- Representation of anomalies in EFT
- Tree-level (semi-leptonic) decays
 - LFU ratios
- Loop $b \rightarrow s,d$ decays
 - Angular analyses, LFU ratios
- Leptonic: Branching fractions
- LFV searches
- Summary

Note: most results shown are based on full Run 1 (3fb^{-1}) + 2015+2016 (2 fb^{-1}) Run 2 data



Effective Hamiltonians

Derived using Operator Product Expansion + renormalization group to sum up the radiative corrections*

$$H_{\text{eff}} = \sum_i V_{\text{CKM}}^i C_i(\mu) O_i(\mu)$$

Quark flavour
couplings (CKM for the
SM)

Wilson coefficients,
integrate physics from
EW scale to μ (~ 1 GeV)

- $i = 1,2$: tree diagrams
- $i = 3-6$: gluonic penguin
- $i = 7-10$: electroweak penguin
($7\gamma, 8G$: magnetic-penguin)
- leptonic operators (S,P)
- Box operators : to describe oscillations

6-dim operators
(higher orders
negligible)

**Matrix elements of operators O_i : non perturbative calculations:
source of hadronic uncertainties (decay constants, form factors,
etc...)**

C_i/O_i mix under RG equations: in practice, use effective C_i^{eff}

**For right-handed current, use of primed coefficients, C'_i (beyond
SM contributions)**

* For a exhaustive review, see : G.Buchalla et al, Rev.Mod.Phys.68 (1996) 1125-1144
<https://arxiv.org/abs/hep-ph/9512380>

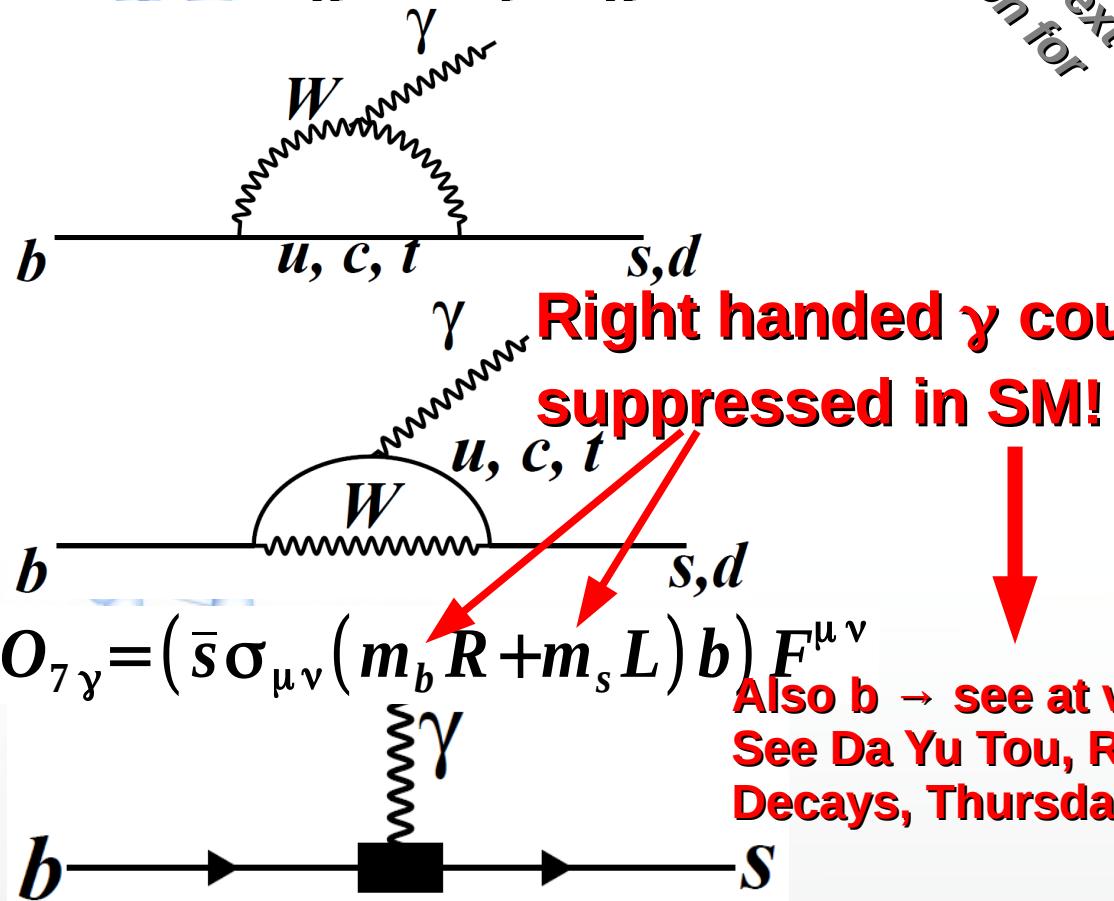
Loop operators and new physics

Loop operators → massive (electroweak) virtual particles : New Physics might intervene. Wilson coefficients affected by NP.

$$C_i(\prime) \rightarrow C_i(\prime) + C_i^{\text{NP}}$$

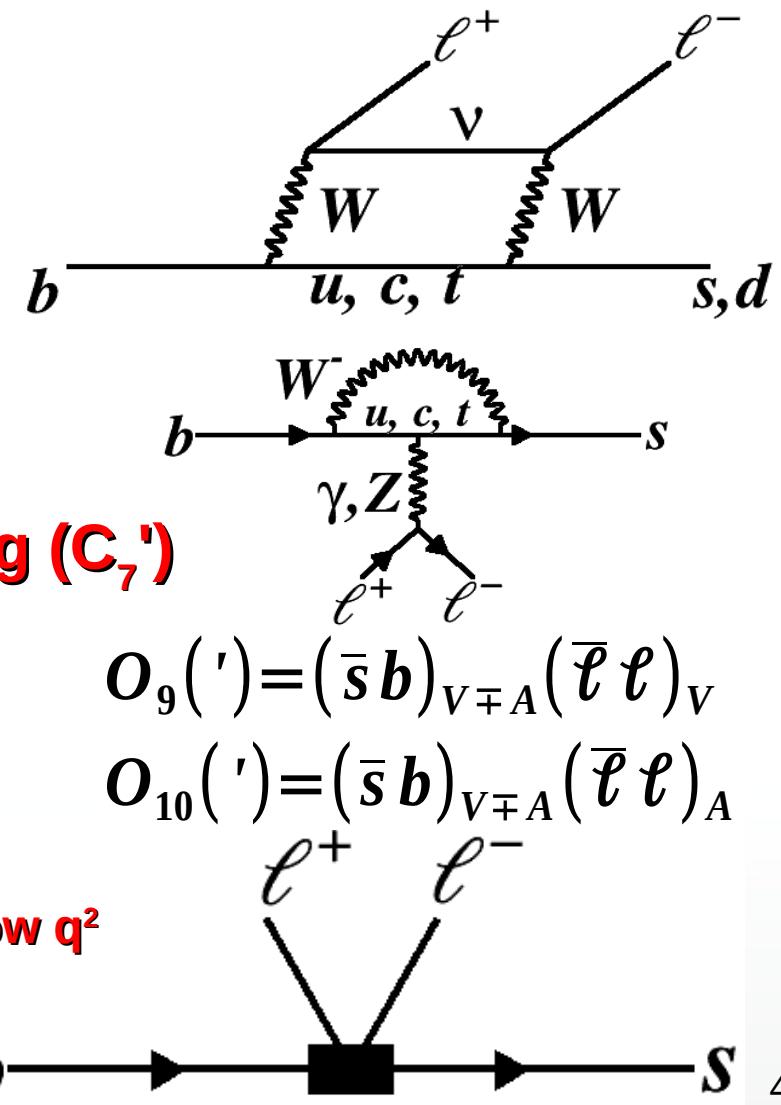
Electromagnetic penguin

See J.Virto, next presentation for details



Right handed γ coupling (C_7) suppressed in SM!

Also $b \rightarrow s$ see at very low q^2
See Da Yu Tou, Rare Decays, Thursday



A great variety of b hadrons: $B_{u,d}$, B_s , B_c , b baryons, etc...

LHCb detector

**Forward single-arm spectrometer with warm magnet
(possibility to inverse polarity)**

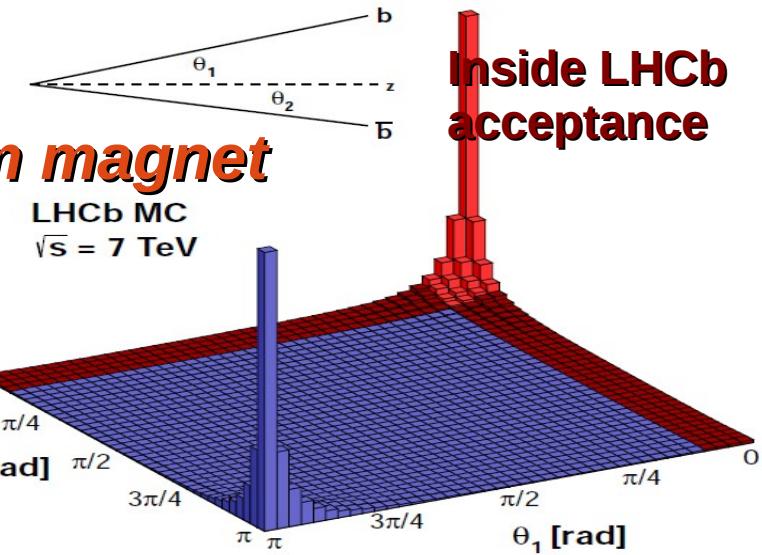
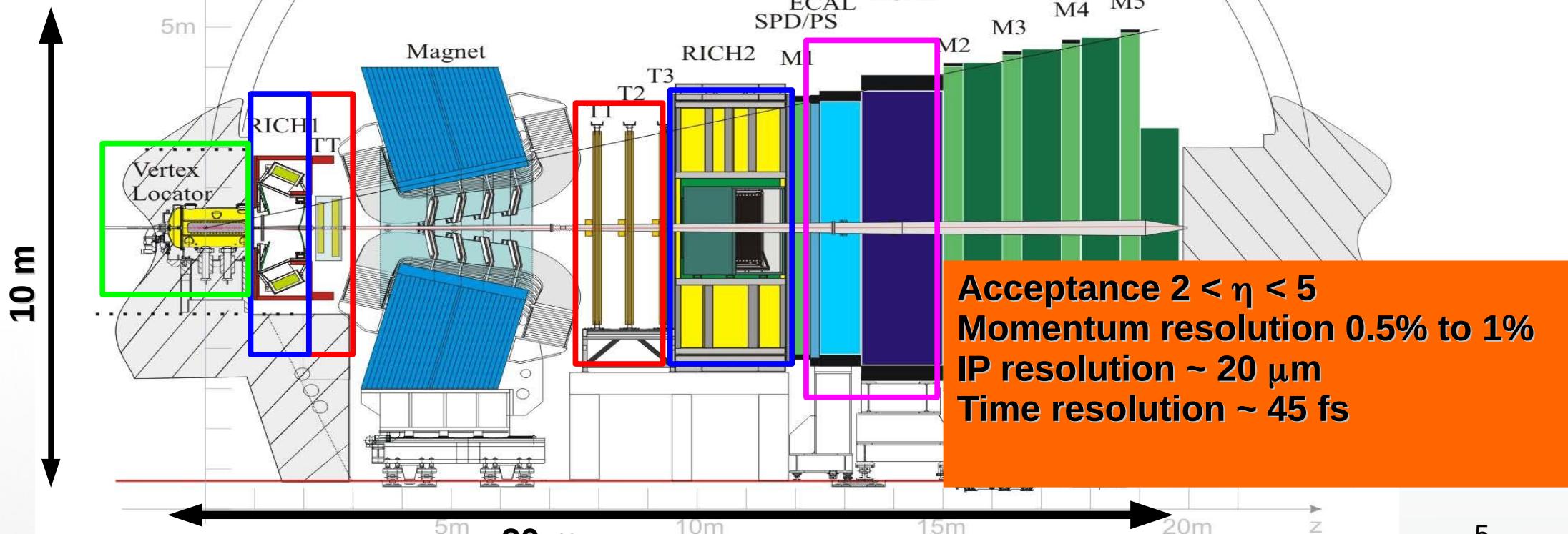
Optimized for b and c hadron studies

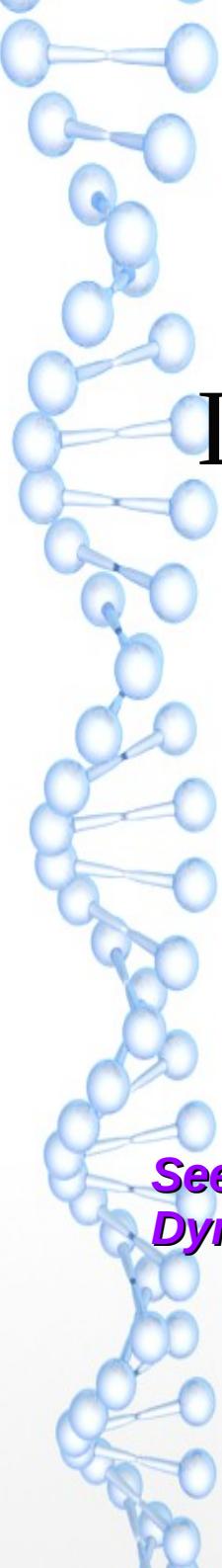
Vertexing

Tracking stations

Particle ID Ring Imaging Cherenkov

Calorimeters and Muon Chambers

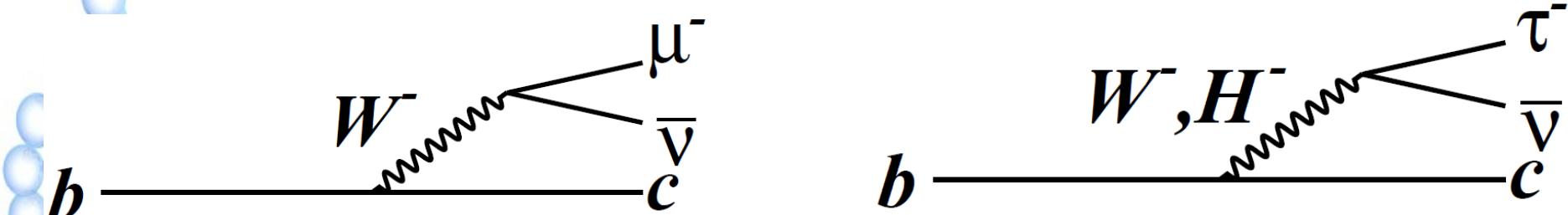




Lepton Flavour Universality with Semileptonic tree $b \rightarrow c \ell \nu$

See S.Braun, *semileptonic parallel session, Tuesday*
Dynamics of Bs semileptonic

$H_b \rightarrow H_c^{(*)} \tau^- \bar{\nu}$ vs $H_b \rightarrow H_c^{(*)} \mu^- \bar{\nu}$



Test of Lepton Flavour Universality in SM. NP might prefer heavy lepton (τ)

Measure:

$$R(H_c^{(*)}) = \frac{BR(H_b \rightarrow H_c^{(*)} \tau^- \bar{\nu})}{BR(H_b \rightarrow H_c^{(*)} \mu^- \bar{\nu})}$$

Precise SM-based predictions:

$$R(D) = 0.299 \pm 0.003$$

$$R(D^*) = 0.252 \pm 0.003$$

H. Na et al., PRD 92(2015) 054510

Fajfer, Kamenic, Nišandić, PRD85 (2012) 094025

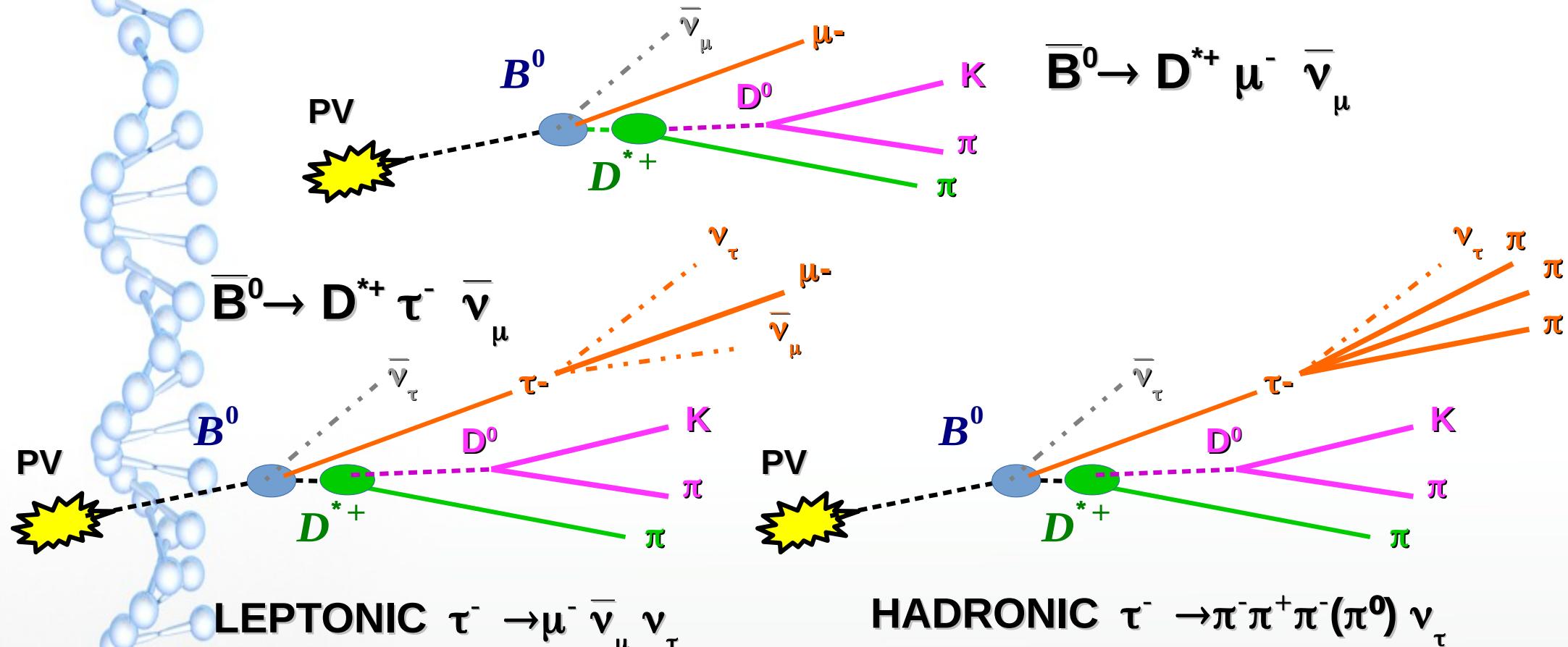
D.Bigi, Gambino, PRD 94 (2016) 094008

LHCb

$$\overline{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau \text{ vs } \overline{B}^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu$$

Very specific topologies for different τ decays (leptonic vs hadronic)

Use of missing mass, muon energy, momentum transfer q , and τ decay time (hadronic mode)

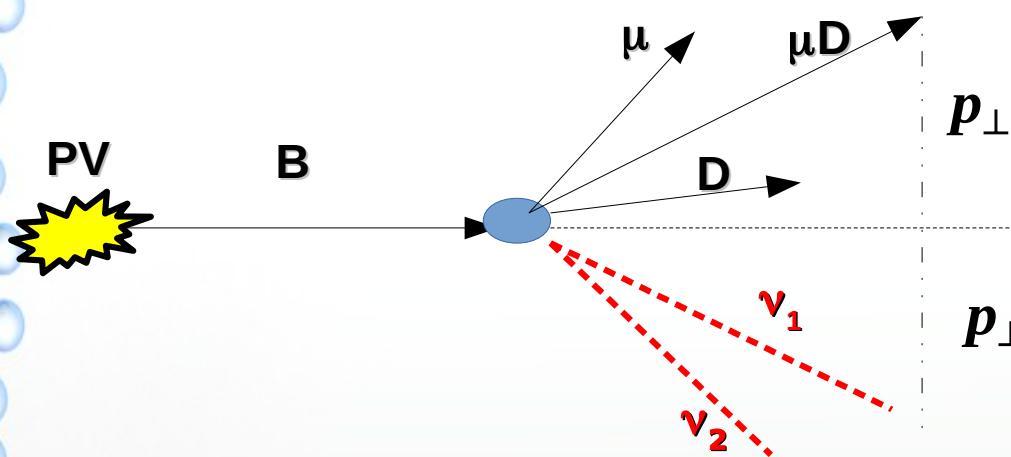


$\overline{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau$ vs $\overline{B}^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu$

Specific variables and neutrino reconstruction

$$m_{miss}^2 = (P_B - P_{D^*} - P_\mu)^2 \quad q^2 = (P_B - P_{D^*})^2$$

Use approximation of P_B , infer the neutrino 4-momentum from geometrical considerations



Two folds ambiguity for the determination of $p_{||}(\nu)$, resolved with a regression method.

p_{\perp} *J. High Energ. Phys. (2017) 2017: 21*

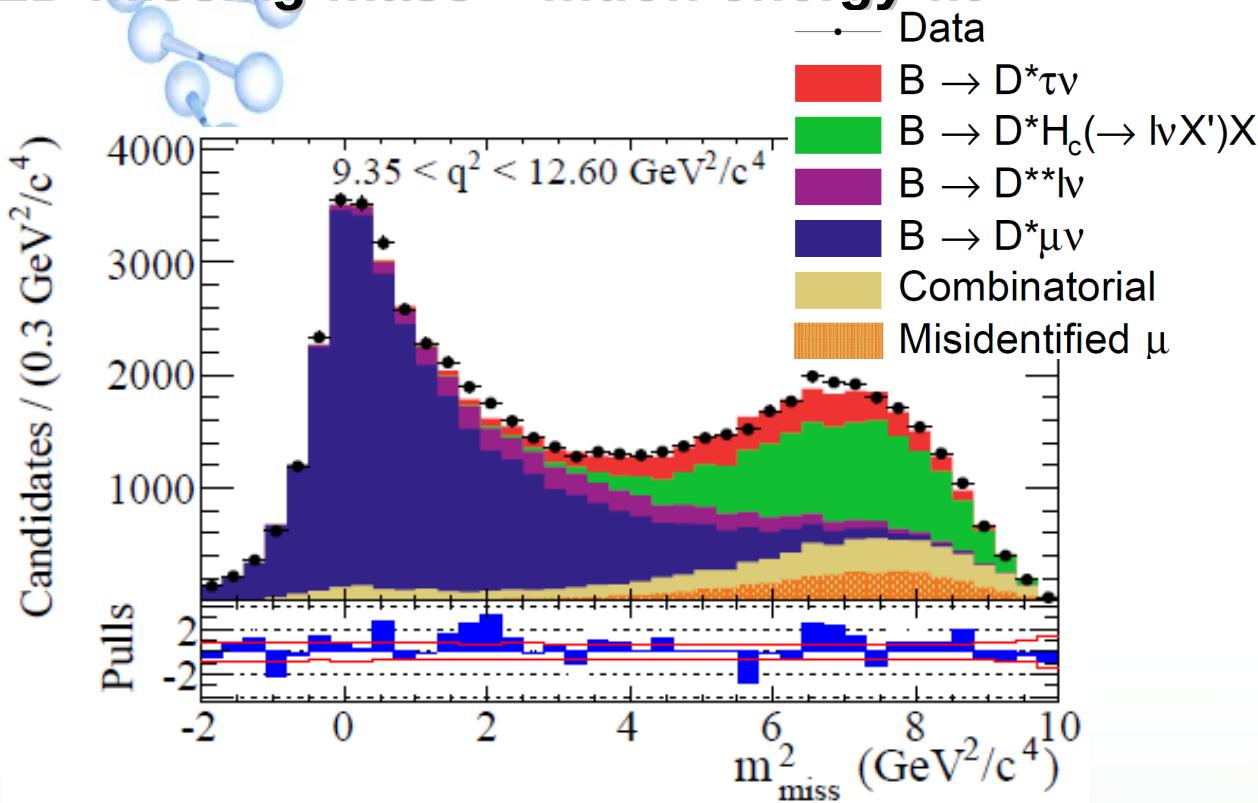
LHCb

$\overline{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau$ vs $\overline{B}^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu$

$$\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$$

PRL 115 (2015) 111803

2D missing mass – muon energy fit



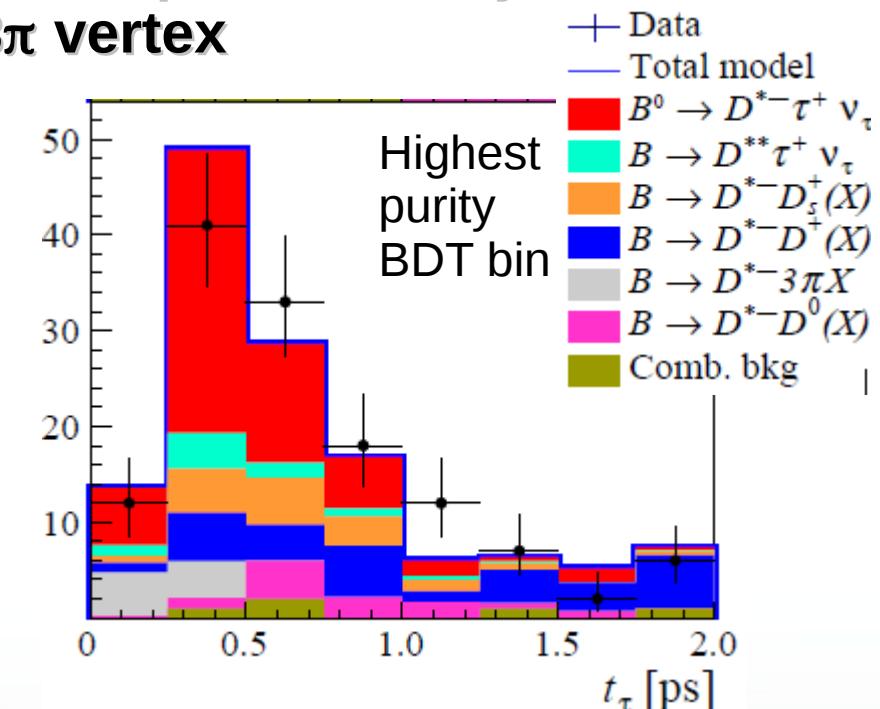
$$R(D^*) = 0.336 \pm 0.027(\text{stat}) \pm 0.030(\text{syst})$$

$$R(D^*) = 0.291 \pm 0.021(\text{stat}) \pm 0.026(\text{syst}) \pm 0.013(\text{BR})$$

$$\tau^- \rightarrow \pi^- \pi^+ \pi^- (\pi^0) \nu_\tau$$

PRL 120 (2018) 171802

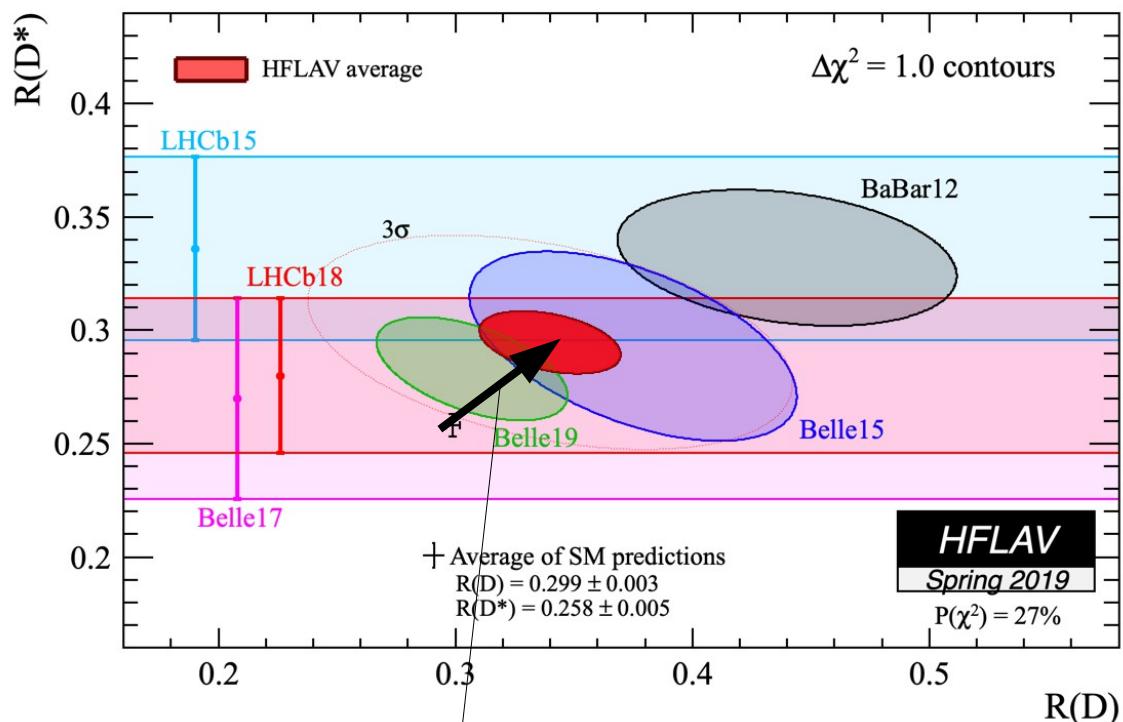
$\overline{B}^0 \rightarrow D^{*+} \pi^- \pi^+ \pi^-$ as normalization 2D fit q^2 – tau decay time from 3 π vertex



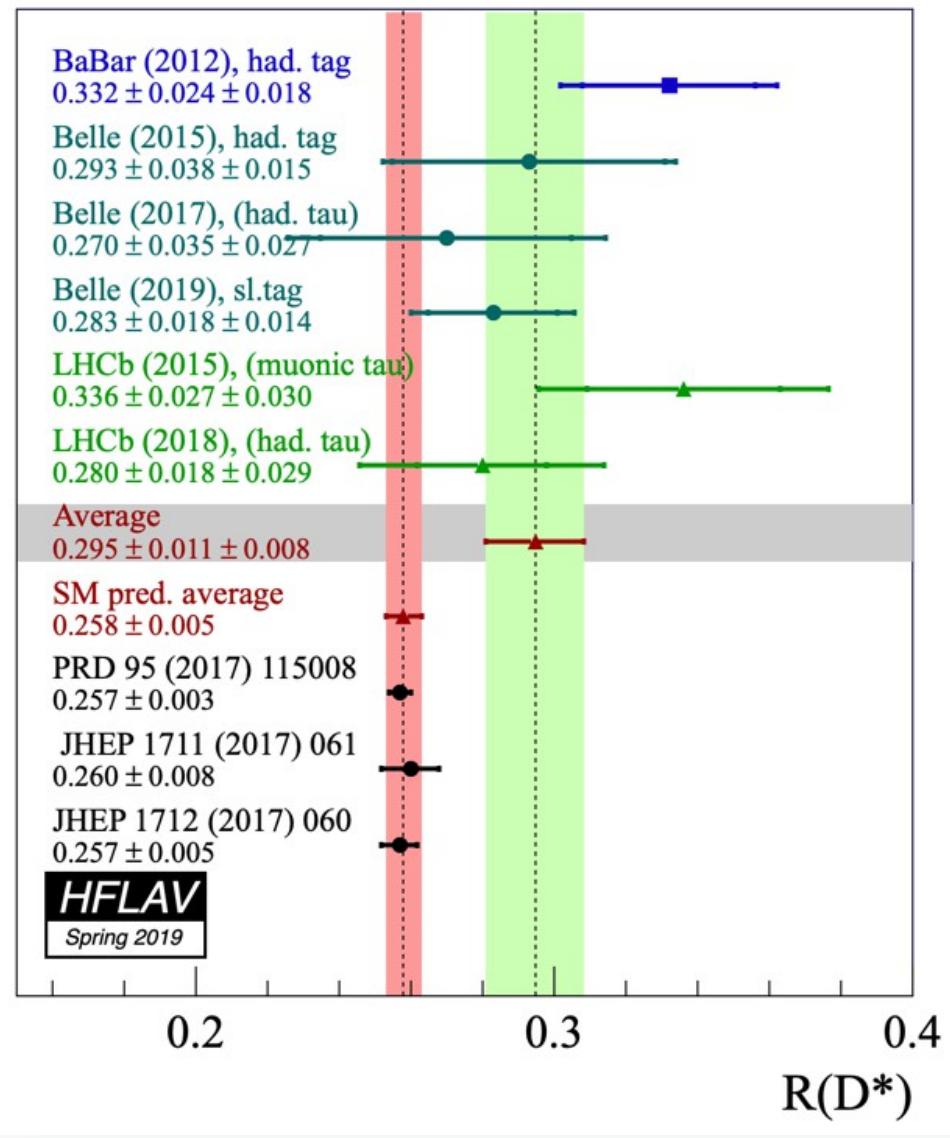
Complicated analyses with huge MC samples, and many background sources ¹⁰

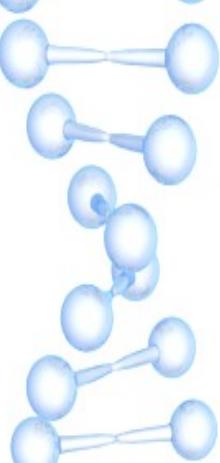
Global situation for $R(D^{(*)})$

LHCb 2D $R(D)$ & $R(D^*)$ analysis currently in internal review



After recent (Belle) result, discrepancy is 3.1σ wrt SM.

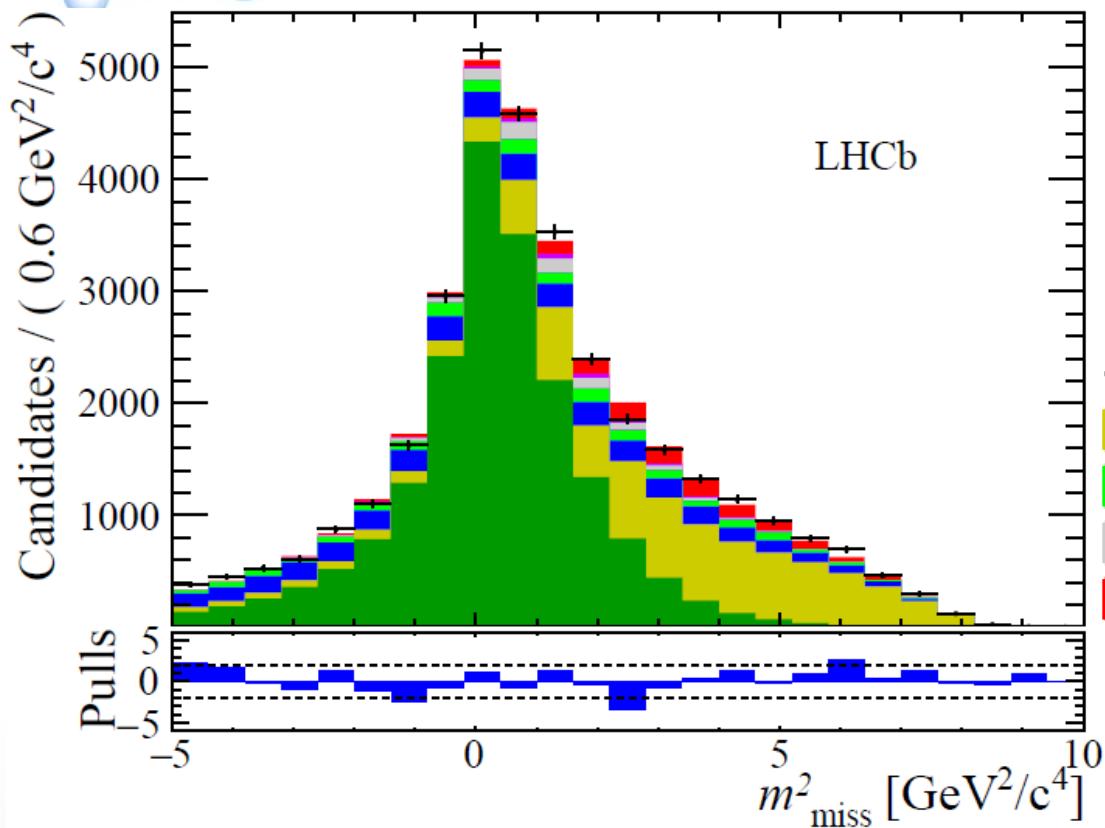




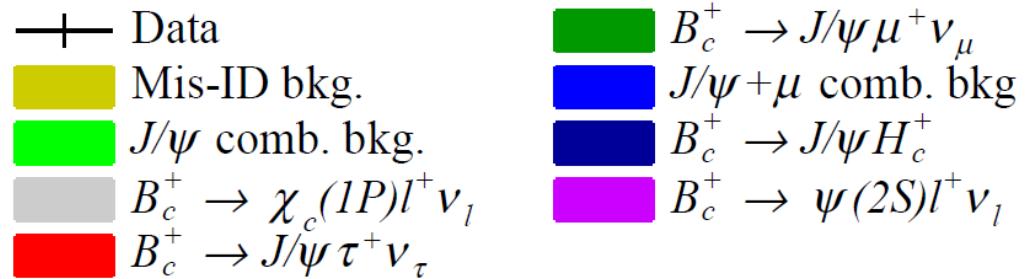
$B_c^+ \rightarrow J/\psi \tau^- \bar{\nu}_\tau$
 $\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$

vs $B_c^+ \rightarrow J/\psi \mu^- \bar{\nu}_\mu$

PRL 120 (2018) 121801
LHCb-PAPER-2017-035



2 variables (missing mass, B_c decay time)
+ 1 category fit.
Category variable Z = bins in q^2 and muon energy.

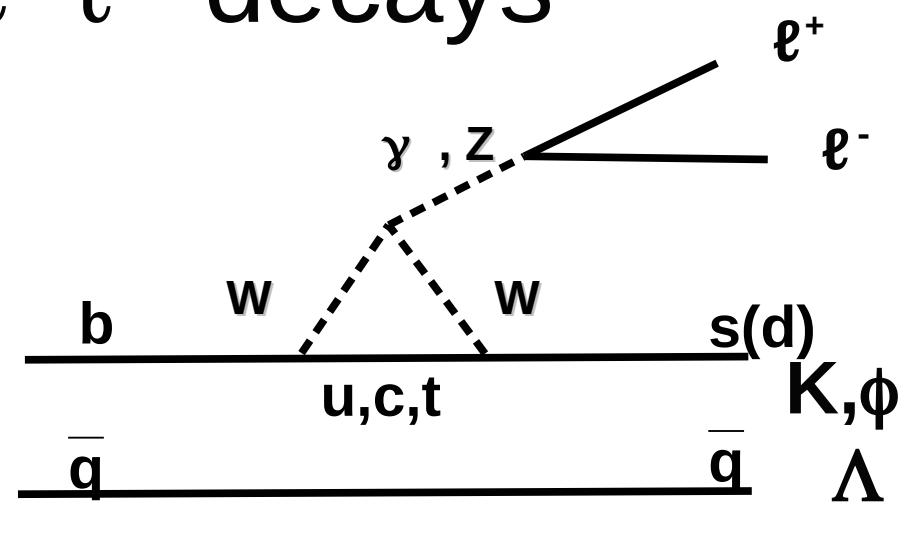
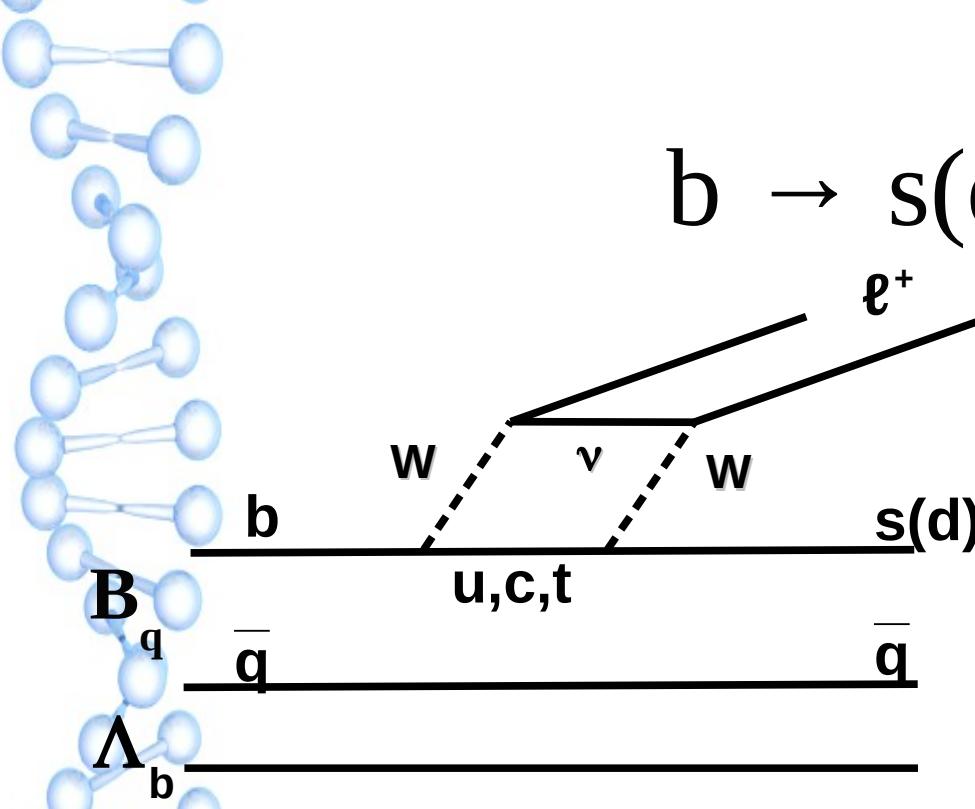


$R(J/\psi) = 0.71 \pm 0.17(\text{stat}) \pm 0.18(\text{syst})$

2 σ above the range of predictions

Available SM-based predictions in the range 0.25 - 0.28
e.g. PLB452 (1999) 129, PRD73 (2006) 054024, PRD74 (2006) 074008

$b \rightarrow s(d) \ell^+ \ell^-$ decays



New physics can intervene in the loops/boxes

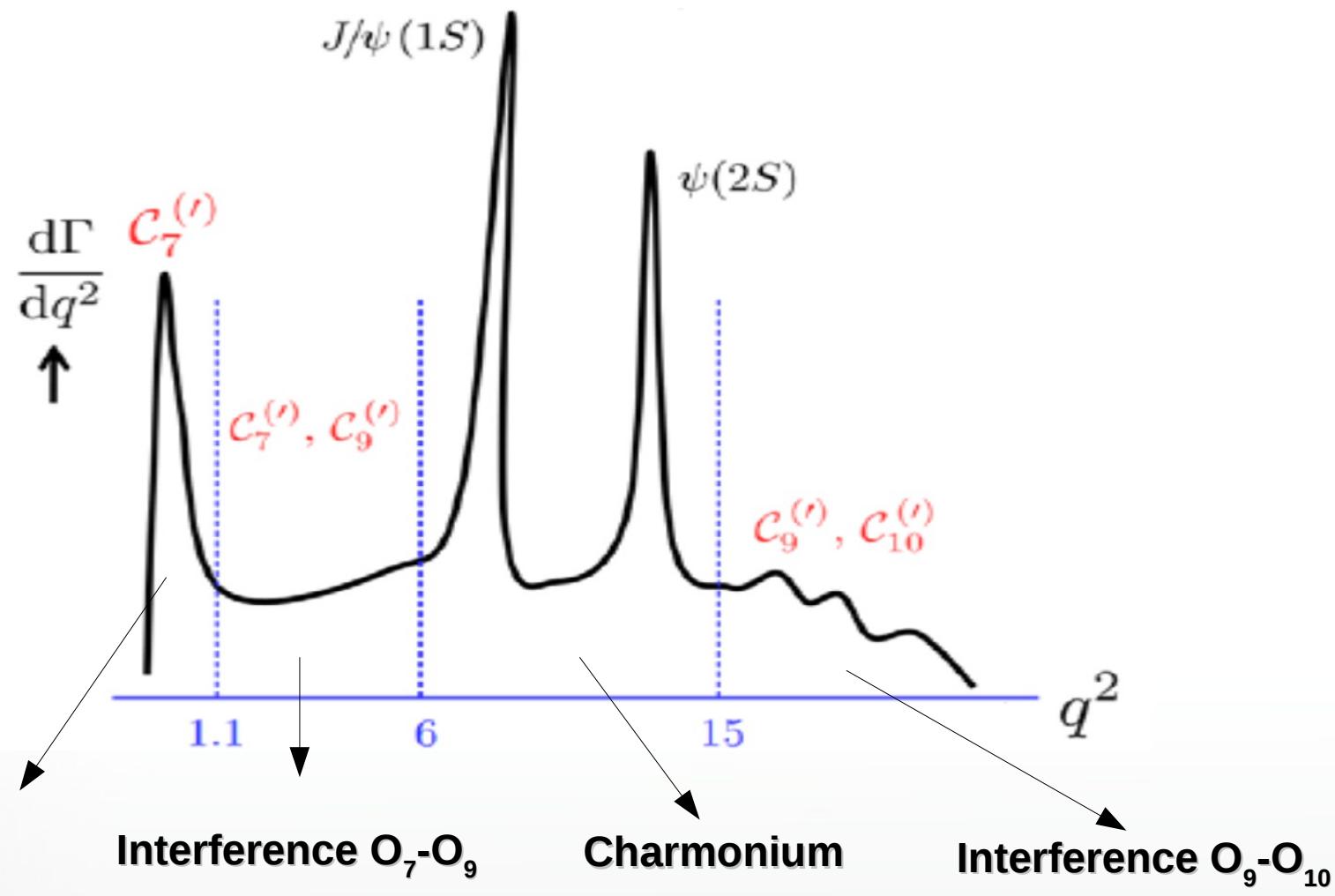
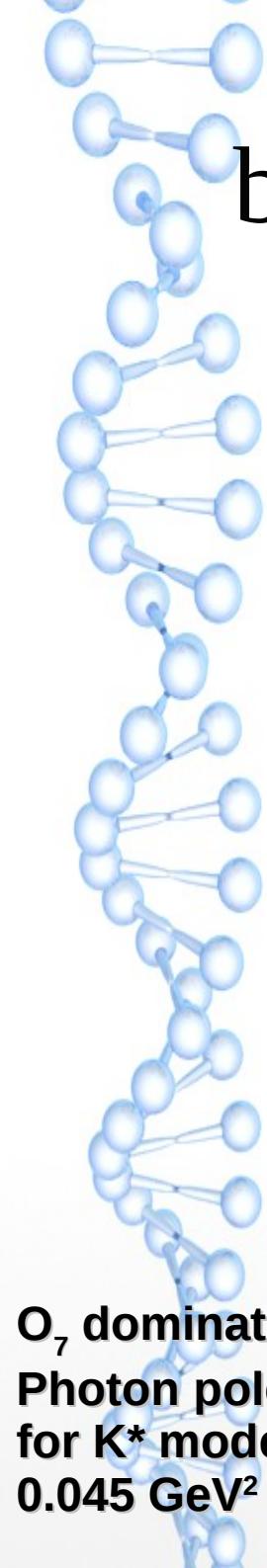
Can be probed through the analysis of the dynamics of the decays

Or testing, e.g., lepton universality $b \rightarrow s e^+ e^- / b \rightarrow s \mu^+ \mu^-$

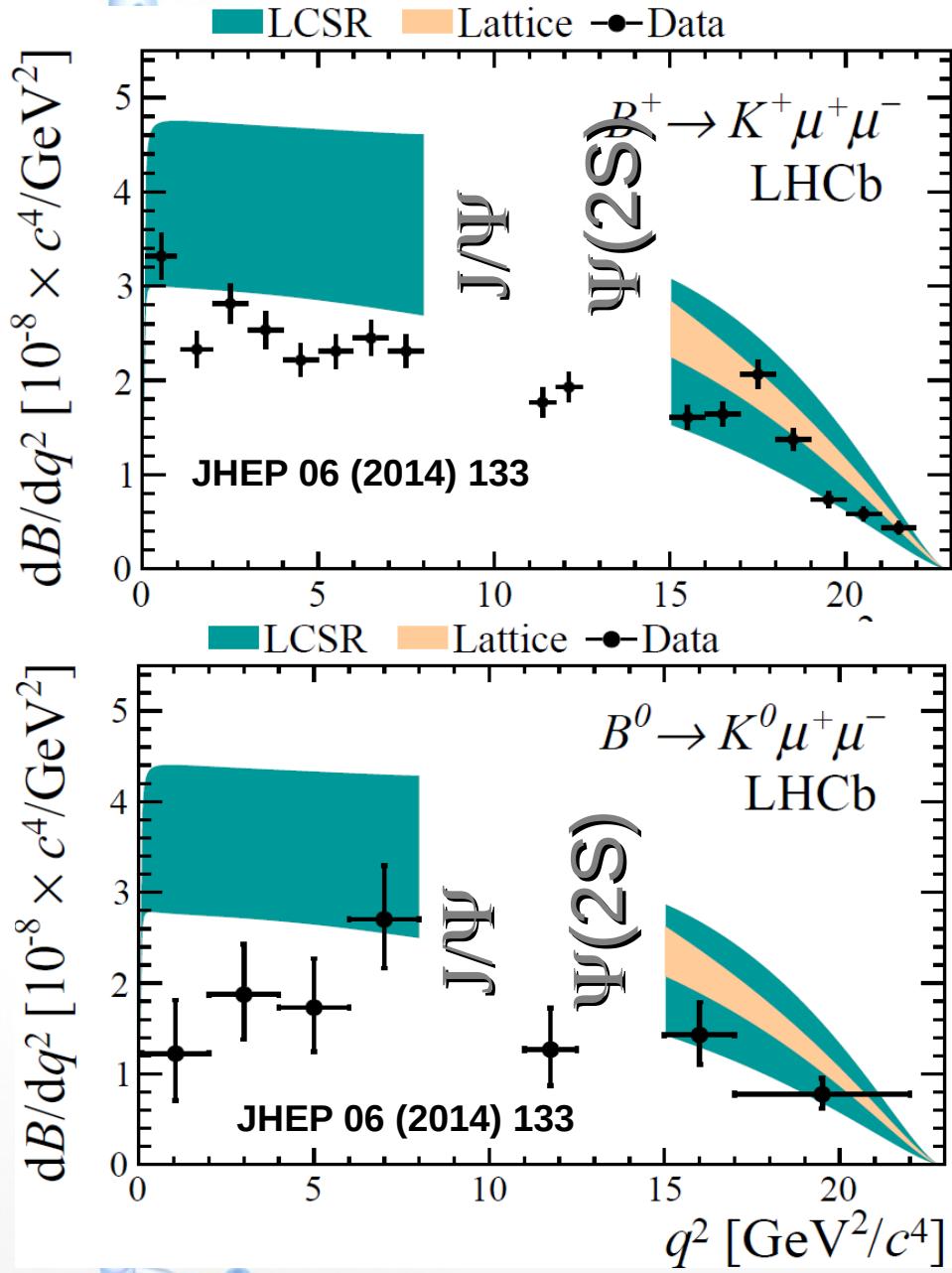
Dominated by O_7 , O_9 , O_{10} operators

See Da Yu Tou, Rare Decays parallel session, Tuesday

$b \rightarrow s(d) \ell^+ \ell^-$: contribution of operators vs q^2



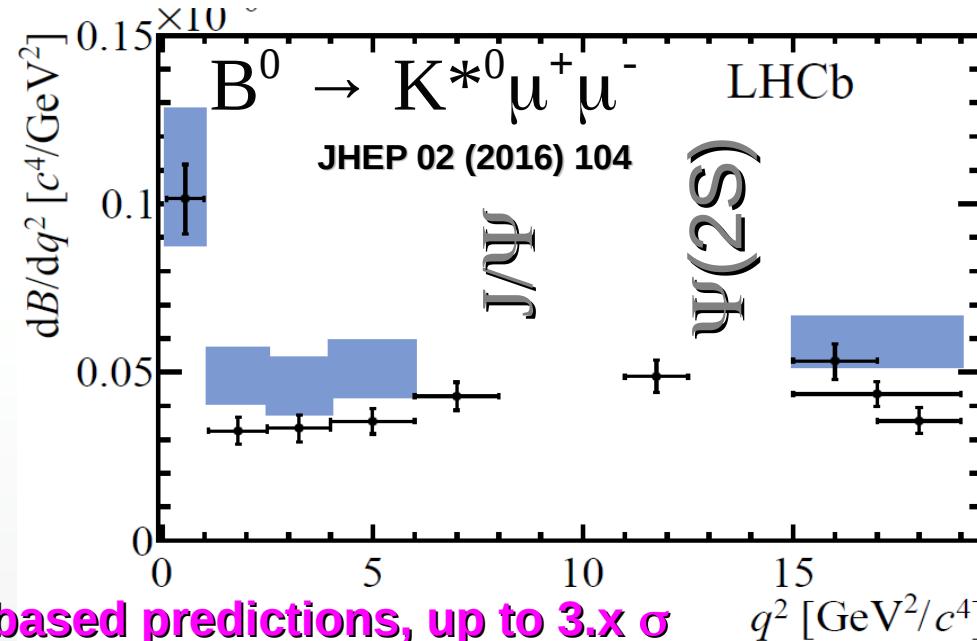
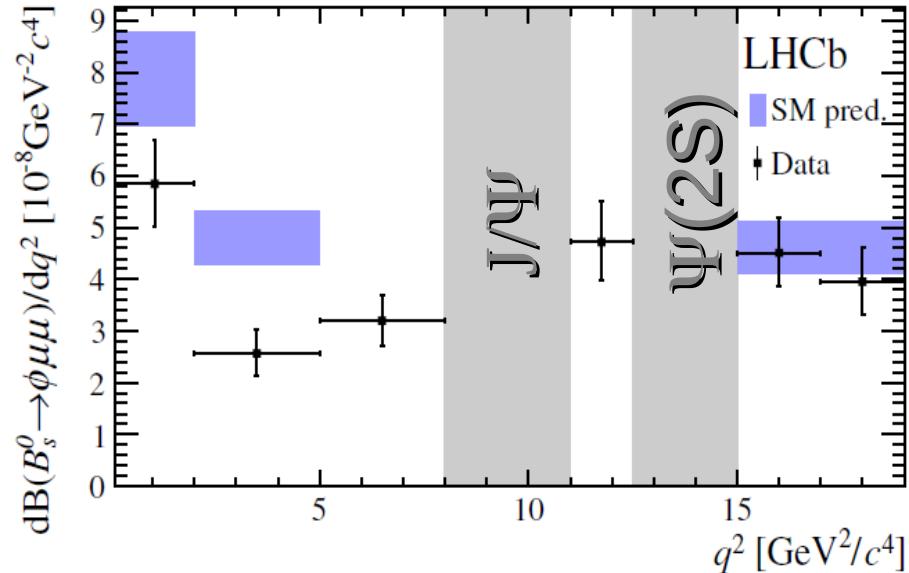
$B \rightarrow X \mu^+ \mu^-$ $d\Gamma/dq^2$ spectra



$$q^2 = (P_B - P_X)^2$$

$B \rightarrow \phi \mu^+ \mu^-$

JHEP 1509 (2015) 179



Data tends to be systematically below the SM-based predictions, up to $3 \times \sigma$

Dynamics for $B^0 \rightarrow K^{*0}\mu^+\mu^-$, $B_s \rightarrow \phi\mu^+\mu^-$

$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^4(\Gamma + \bar{\Gamma})}{dq^2 d\vec{\Omega}} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right.$$

$$+ \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_l$$

$$- F_L \cos^2 \theta_K \cos 2\theta_l + S_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi$$

$$+ S_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + S_5 \sin 2\theta_K \sin \theta_l \cos \phi$$

$$+ \frac{4}{3} A_{FB} \sin^2 \theta_K \cos \theta_l + S_7 \sin 2\theta_K \sin \theta_l \sin \phi$$

$$+ S_8 \sin 2\theta_K \sin 2\theta_l \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi \Big]$$

Formula slightly different between
K* (self-tagging) and ϕ

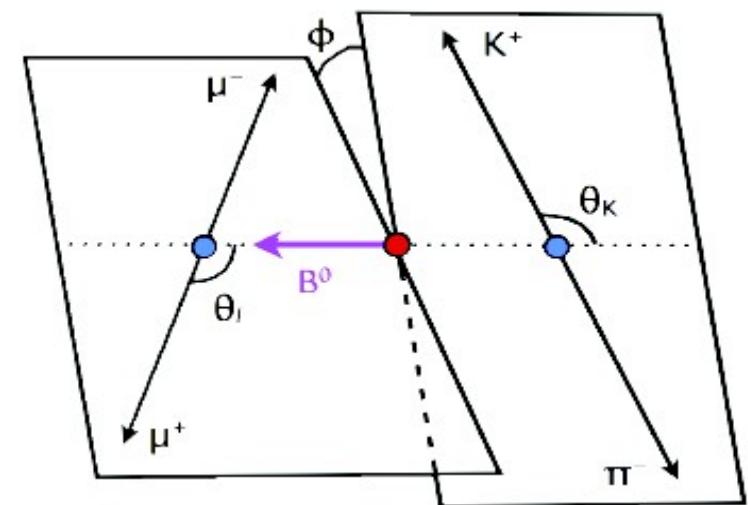
F_L : fraction of longitudinal polarization of K^*/ϕ

A_{FB} = forward-backward

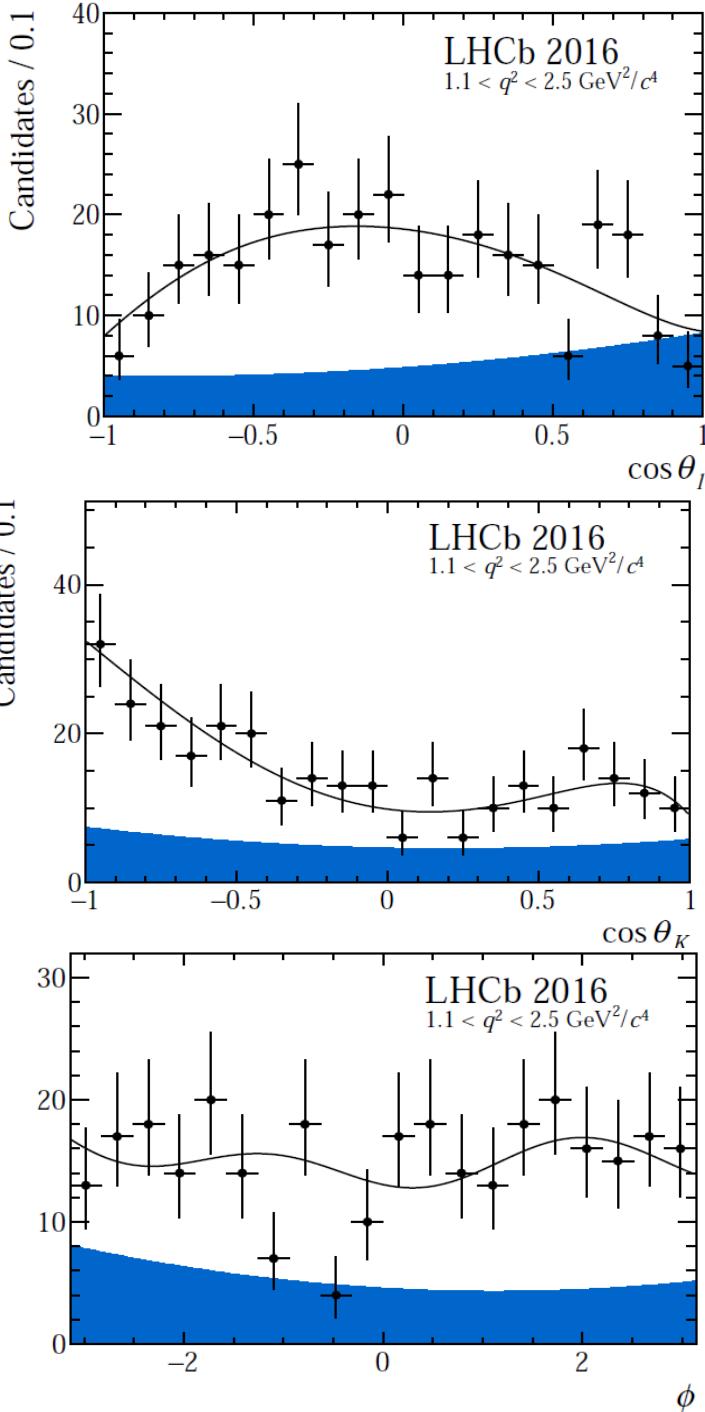
asymmetry of the dimuon system

$S_5 = A_5$ in the case of ϕ

They depend on $B \rightarrow K^*/\phi$ form factors and Wilson Coefficients of the OPE



$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ angular analysis (Run1+2016)

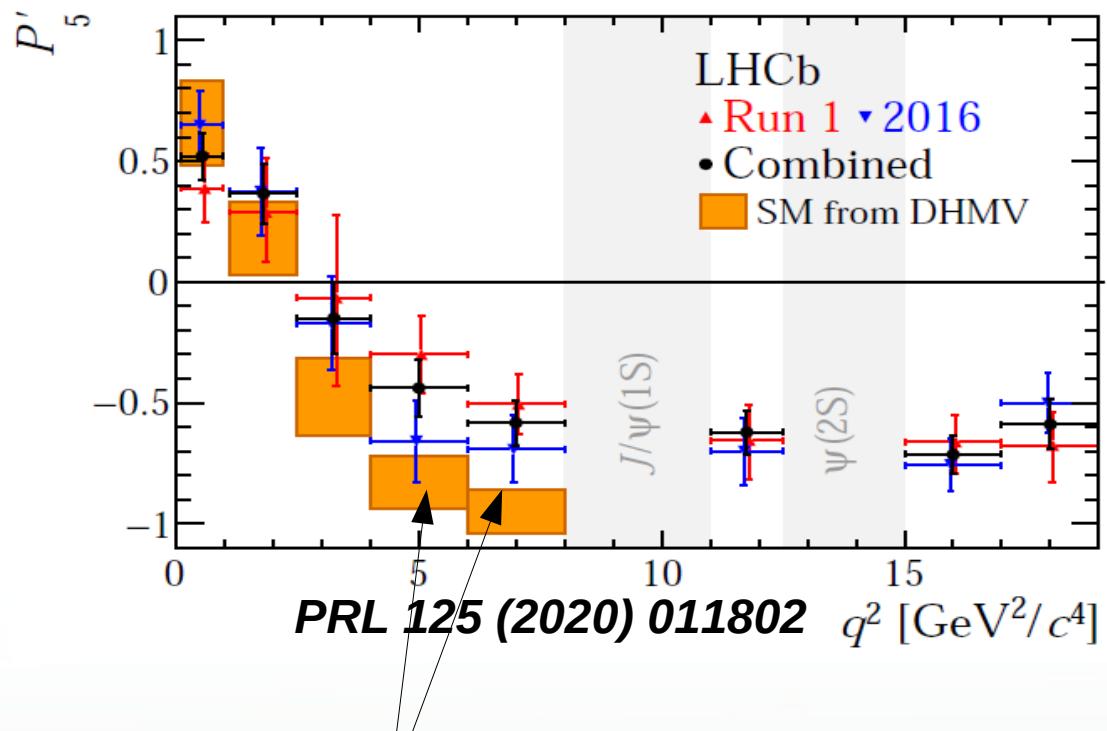


Form-factor independent (LO):

$$P'_{4,5,8} = \frac{S_{4,5,8}}{\sqrt{F_L(1 - F_L)}}$$

$$P'_6 = \frac{S_7}{\sqrt{F_L(1 - F_L)}}$$

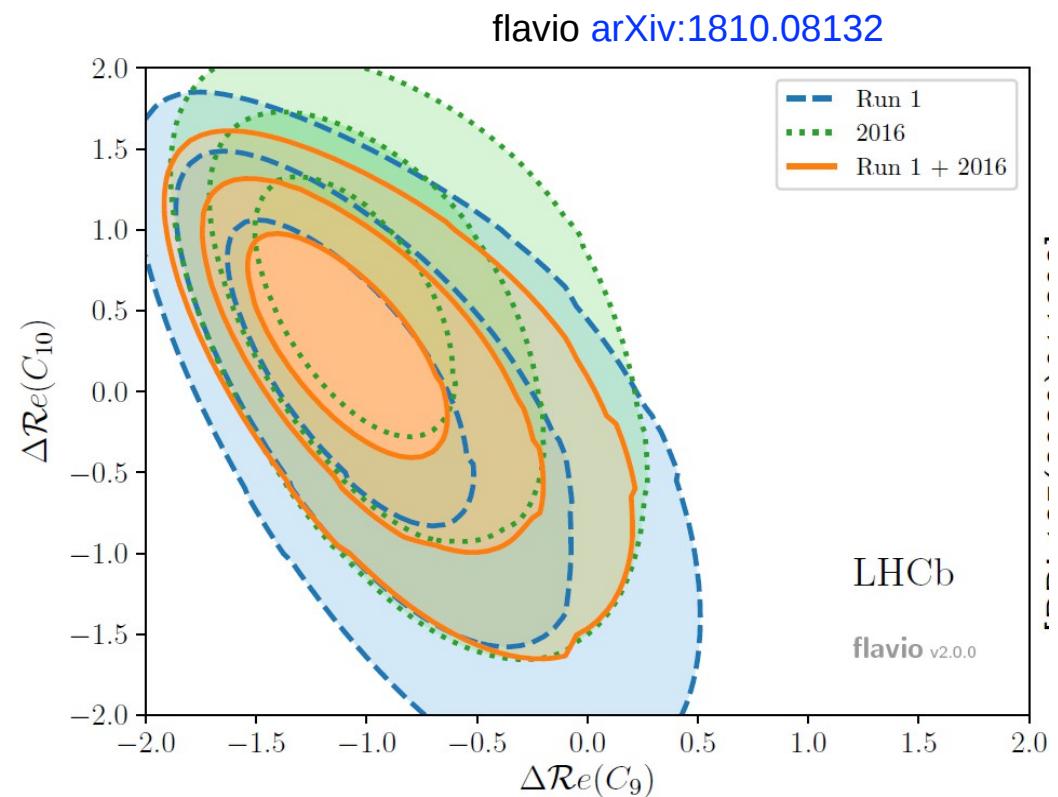
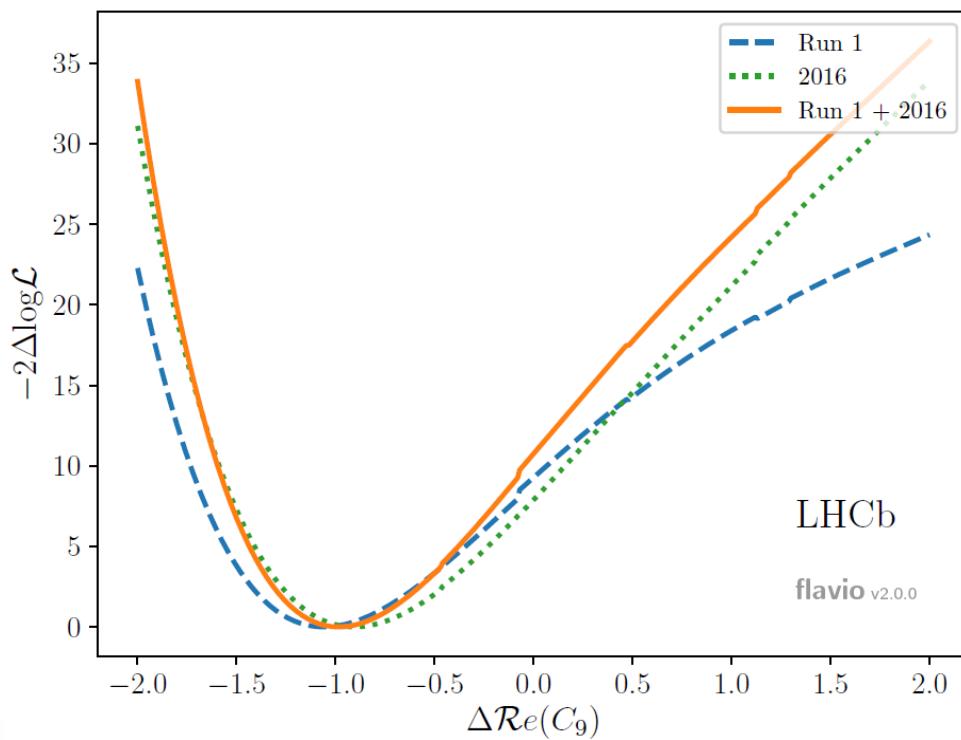
Descotes-Genon et al, JHEP 05 (2013) 137



2.5, 2.9 σ local
discrepancies

$B^0 \rightarrow K^{*0}\mu^+\mu^-$ fit to Wilson coefficients combining angular coefficients

$$\Delta C_i = C_i - C_i^{\text{SM}}$$



Fit favours $\Delta C_9 \sim -1$, discrepancy wrt SM: 3.3σ

R_X ratios

Test of Lepton Flavour Universality: R_K(SM)= 1 (+corrections order < 10⁻³)
 (excluding the γ pole for K* mode)

$$R_K = \frac{BR(B^+ \rightarrow K^+ \mu^+ \mu^-)}{BR(B^+ \rightarrow K^+ e^+ e^-)}$$

PRL 122 (2019) 191801

$$R_{K^{*0}} = \frac{BR(B^0 \rightarrow K^{*0} \mu^+ \mu^-)}{BR(B^0 \rightarrow K^{*0} e^+ e^-)}$$

JHEP 08 (2017) 055

Experimentally:

$$R_X = \frac{BR(B \rightarrow X \mu^+ \mu^-)}{BR(B \rightarrow X J/\psi(\mu^+ \mu^-))} / \frac{BR(B \rightarrow X e^+ e^-)}{BR(B \rightarrow X J/\psi(e^+ e^-))}$$

Minimize systematic uncertainties

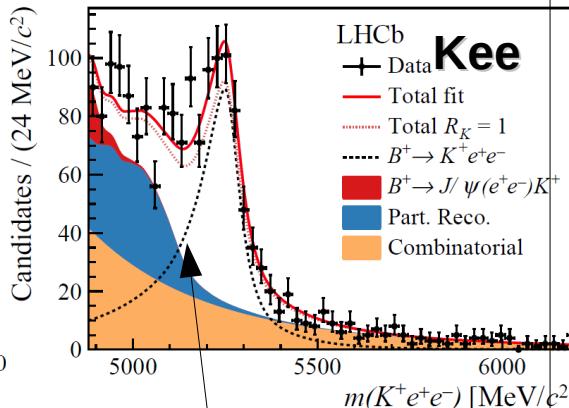
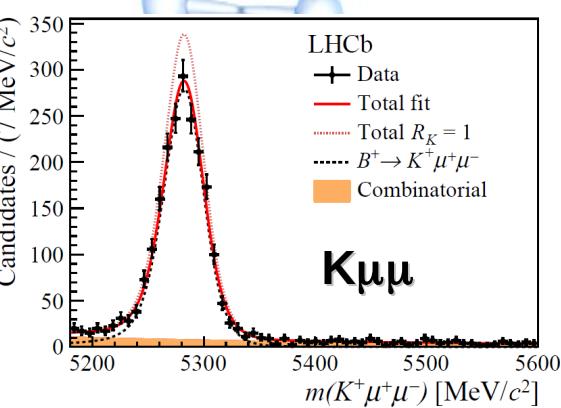
study of $r_{J/\psi} = \frac{BR(B \rightarrow X J/\psi(\mu^+ \mu^-))}{BR(B \rightarrow X J/\psi(e^+ e^-))}$ with high accuracy

q² range: above γ pole and background of type $B \rightarrow \phi(\rightarrow \ell\ell) K$
 and below J/ Ψ radiative tail

R_X ratios - fits

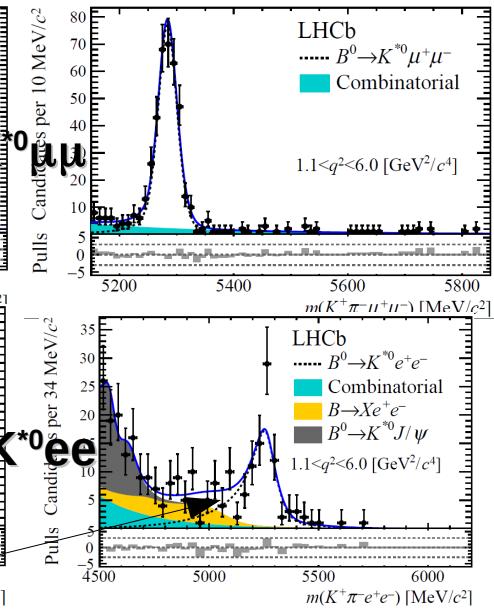
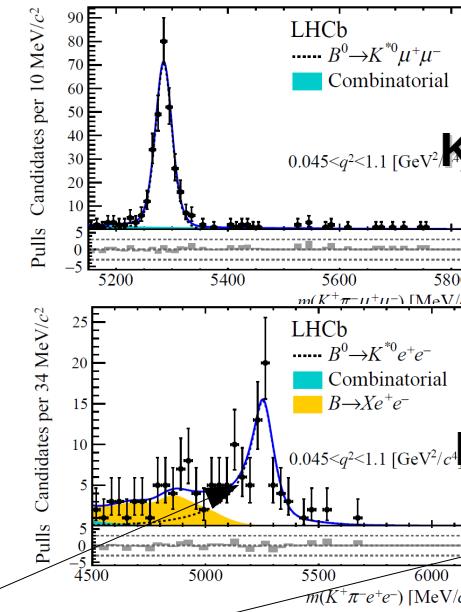
$$B^+ \rightarrow K^+ \ell^+ \ell^-$$

$1.1 \text{ GeV}^2 < q^2 < 6 \text{ GeV}^2$



$$B^0 \rightarrow K^{*0} \ell^+ \ell^-$$

$0.045 \text{ GeV}^2 < q^2 < 1.1 \text{ GeV}^2$ $1.1 \text{ GeV}^2 < q^2 < 6 \text{ GeV}^2$

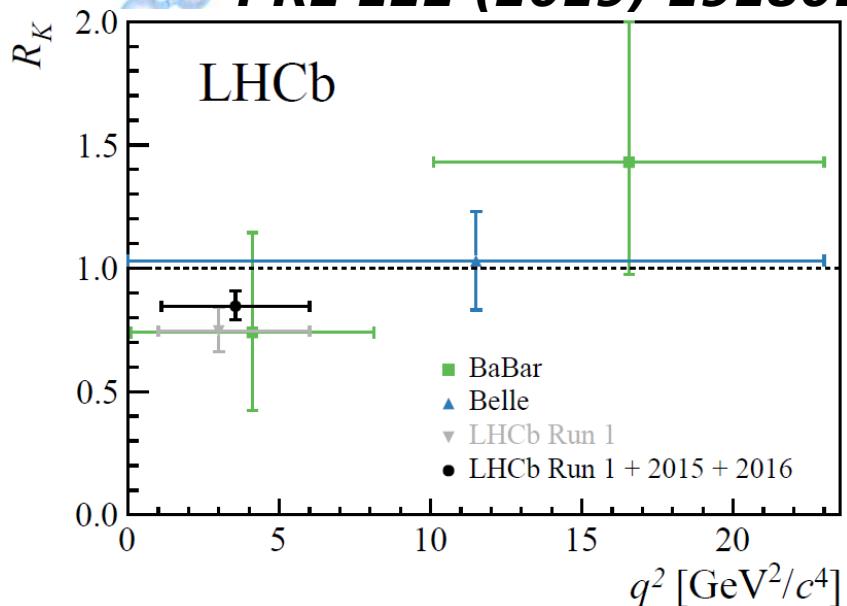


Radiative Bremsstrahlung tail for electron modes

R_X ratios, results

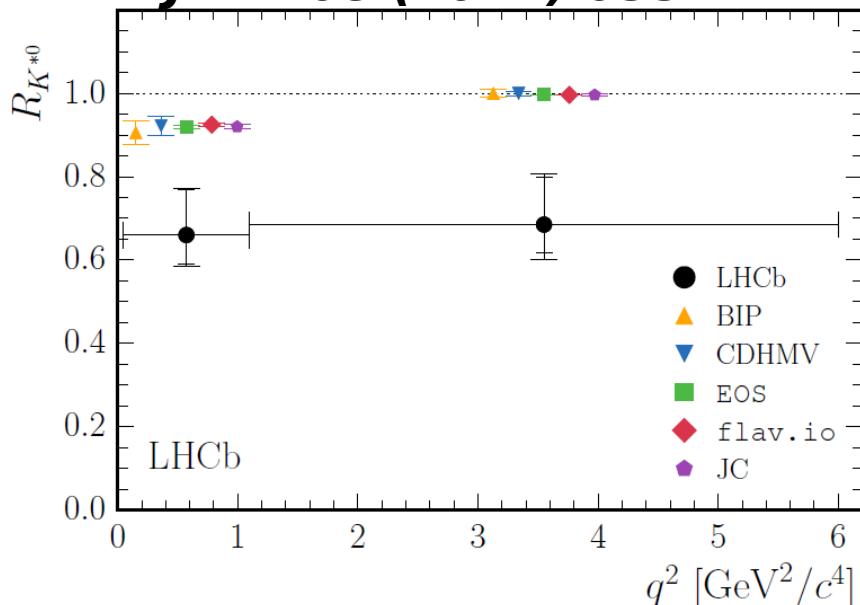
$B^+ \rightarrow K^+\ell^+\ell^-$

PRL 122 (2019) 191801



$B^0 \rightarrow K^{*0}\ell^+\ell^-$

JHEP 08 (2017) 055



$0.045 \text{ GeV}^2 < q^2 < 1.1 \text{ GeV}^2$

$$R_K = 0.846_{-0.054}^{+0.060} (\text{stat.})_{-0.014}^{+0.016} (\text{syst.})$$

2.5 σ below SM-based predictions

Update with full Run1+Run2 currently in internal review

$$R_{K^{*0}} = 0.66_{-0.07}^{+0.11} (\text{stat.}) \pm 0.03 (\text{syst.})$$

2.1-2.3 σ below SM

$1.1 \text{ GeV}^2 < q^2 < 6 \text{ GeV}^2$

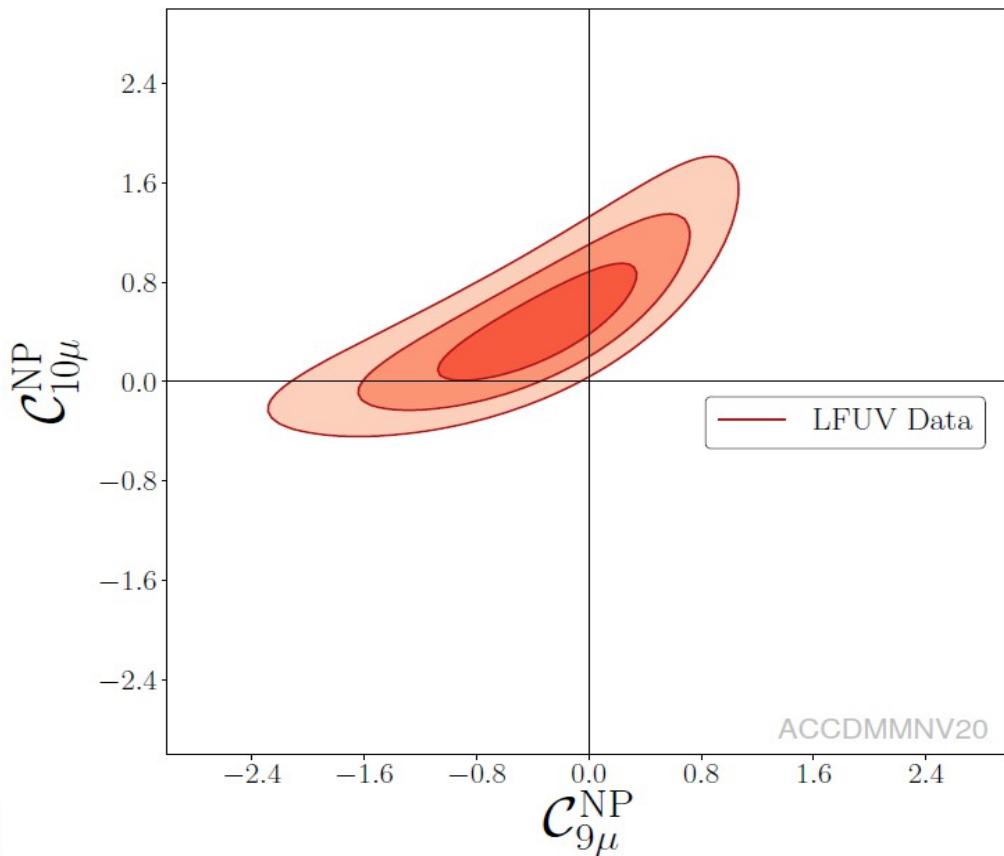
$$R_{K^{*0}} = 0.69_{-0.07}^{+0.11} (\text{stat.}) \pm 0.05 (\text{syst.})$$

2.4-2.5 σ below SM

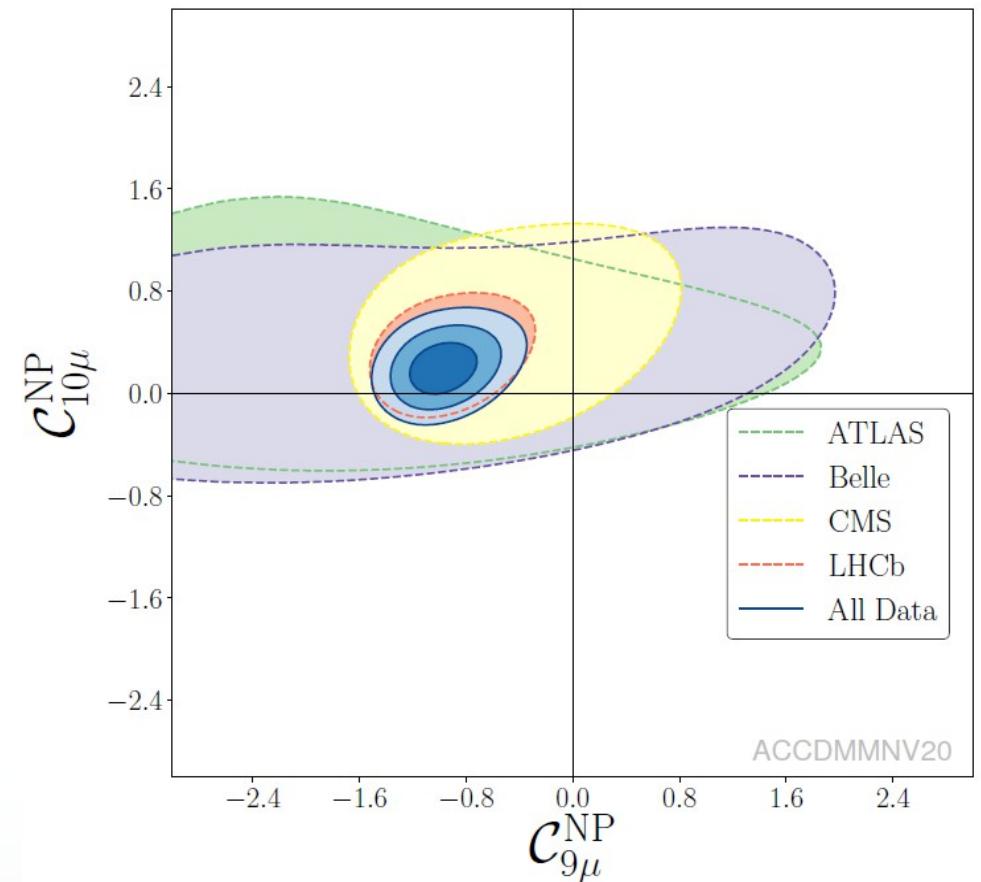
From R_K and R_{K^*} to fits to Wilson coefficients

LFUV only

Belle and LHCb data involved



LFUV + angular analyses



EPJC 79, 714 (2019)

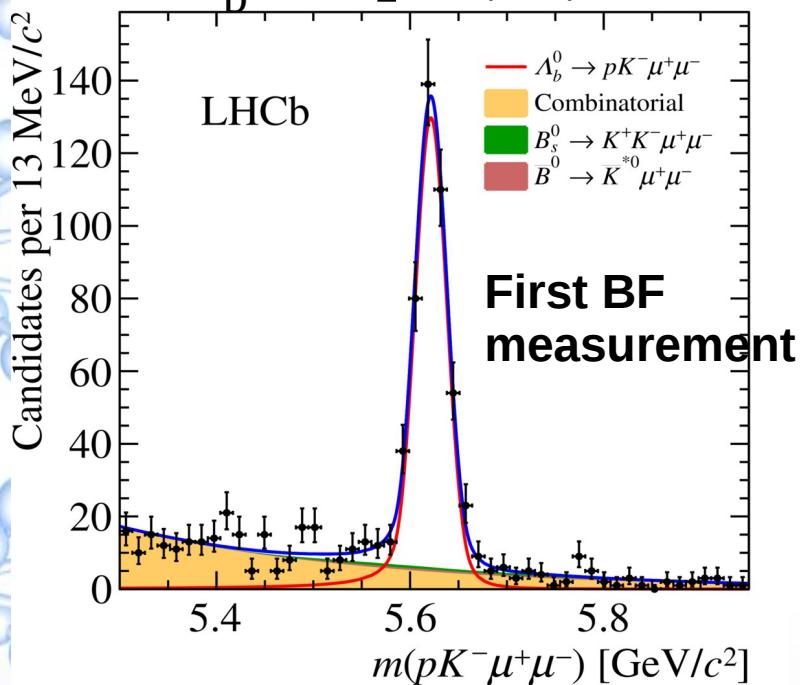
Updated June 2020 <https://arxiv.org/abs/1903.09578> v6

$R(pK), \Lambda_b \rightarrow pK \ell^+ \ell^-$

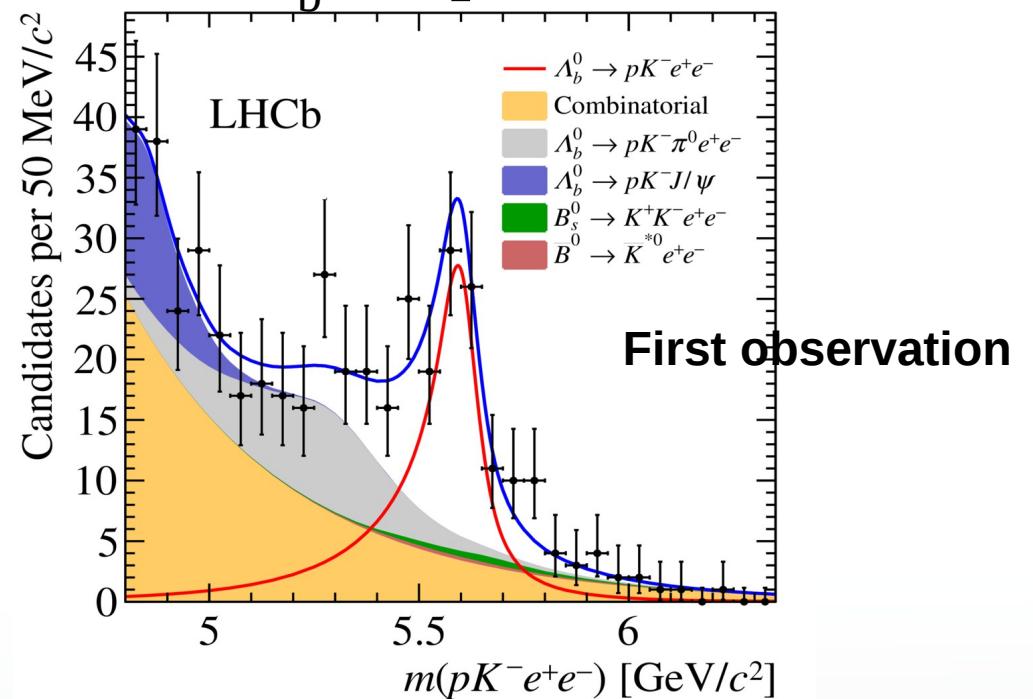
$0.1 < q^2 < 6.0 \text{ GeV}^2$
 $m(pK) < 2600 \text{ MeV}/c^2$

Same technique as for R_K , use of J/Ψ mode
as normalization to reduce systematics

$$\Lambda_b \rightarrow pK \mu^+ \mu^-$$



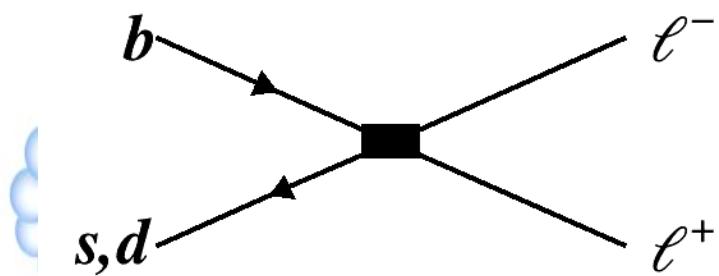
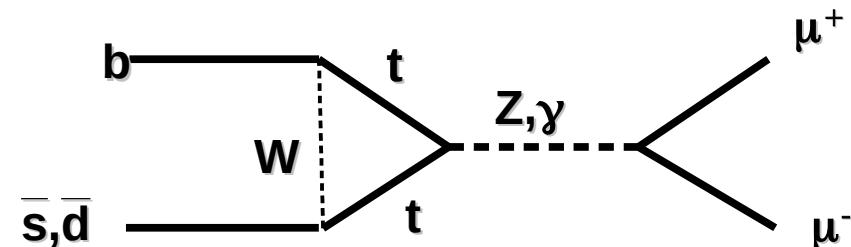
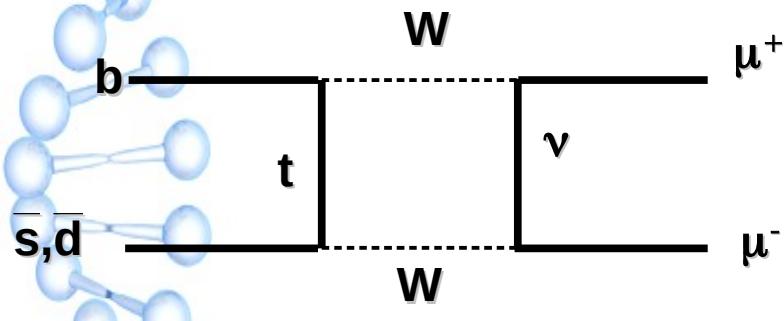
$$\Lambda_b \rightarrow pK e^+ e^-$$



$$R_{pK} = 0.86^{+0.14}_{-0.11} (\text{stat.}) \pm 0.05 (\text{syst.})$$

Compatible with unity
for now

B → ℓ⁺ℓ⁻ decays



Contribution from $O_{10}(\cdot)$
and

$$O_S(\cdot) = (\bar{s} b)_{V \pm A} (\bar{\ell} \ell)$$

$$O_P(\cdot) = (\bar{s} b)_{V \pm A} (\bar{\ell} \ell)_P$$

SM-based predictions:

$$BR(B^0 \rightarrow \mu^+ \mu^-) = (1.06 \pm 0.09) \times 10^{-10}$$

$$BR(B_s^0 \rightarrow \mu^+ \mu^-) = (3.66 \pm 0.23) \times 10^{-9}$$

See I. Williams, Rare Decays parallel session, Tuesday
For details on experimental status

C.Bobeth et al., PRL 112 (2014) 101801

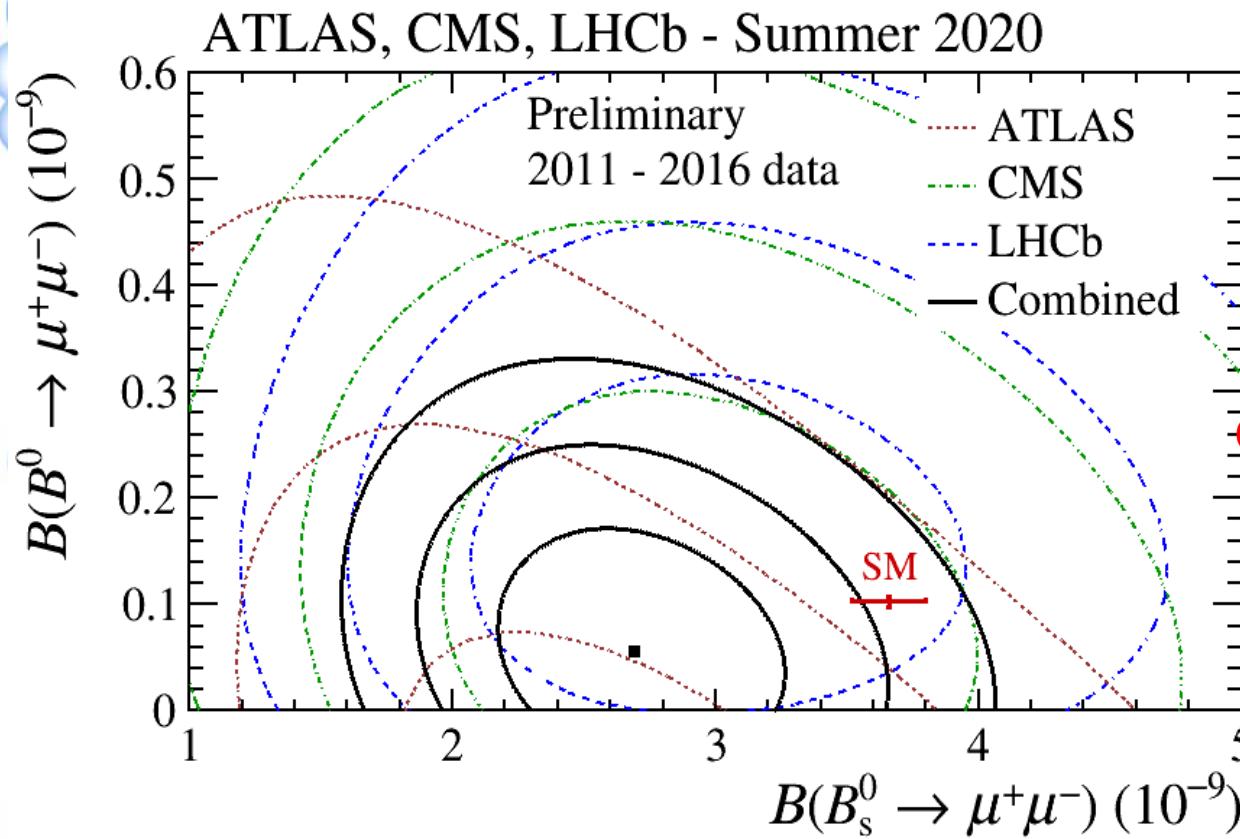
B → μ⁺μ⁻ status

Recent combination (08/2020)

LHCb-CONF-2020-002
CMS PAS BPH-20-003
ATLAS-CONF-2020-049

Based on

LHCb (PRL 118 (2017) 191801)
ATLAS (JHEP 04 (2019) 098)
CMS JHEP 04 (2020) 188



Combination within 2.1 σ of SM

$$BR(B_s^0 \rightarrow \mu^+\mu^-) = (2.69^{+0.37}_{-0.35}) \times 10^{-9}$$

$$BR(B^0 \rightarrow \mu^+\mu^-) < 1.9 \times 10^{-10} @ 95\% CL$$

On going:
LHCb full Run 1 + Run 2 results

LHCb

PRL 124 (2020) 211802

$B \rightarrow e^+ e^-$

SM-based predictions:

$$BR(B^0 \rightarrow e^+ e^-) = (2.41 \pm 0.13) \times 10^{-15}$$

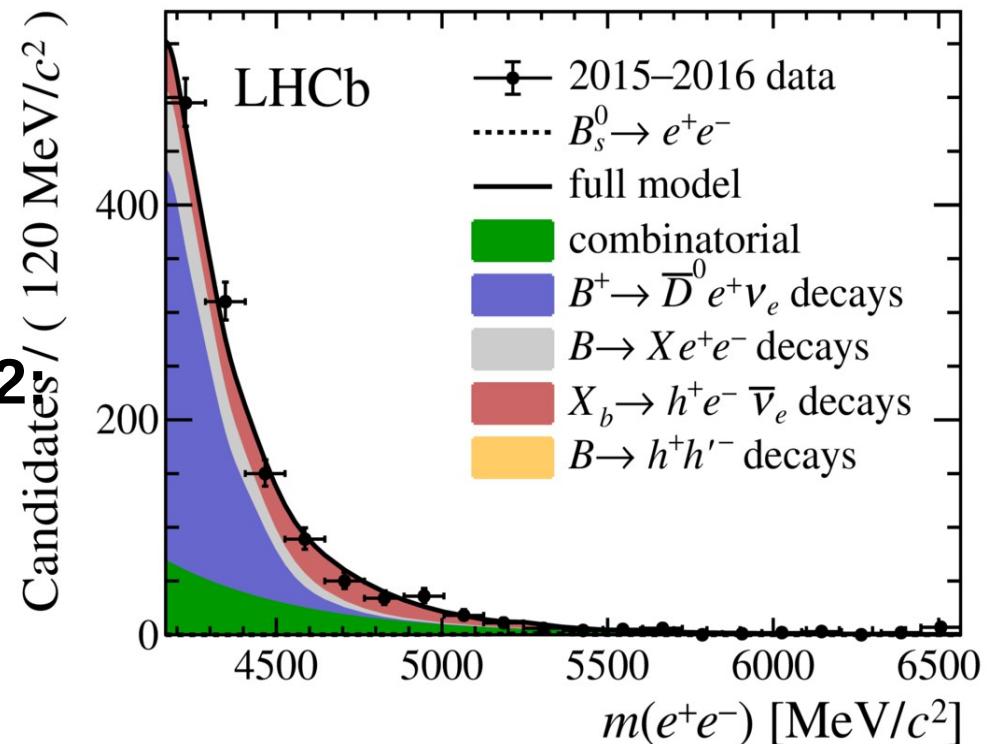
$$BR(B_s^0 \rightarrow e^+ e^-) = (8.60 \pm 0.36) \times 10^{-14}$$

M. Beneke et al., JHEP 10 (2019) 232

Fleischer et al., JHEP 05 (2017) 156

Analysis with Run 1 + part of Run 2

No excess of events/background



$$BR(B_s^0 \rightarrow e^+ e^-) < 9.4(11.2) \times 10^{-9} \text{ @ 90(95)% CL}$$

$$BR(B^0 \rightarrow e^+ e^-) < 2.5(3.0) \times 10^{-9} \text{ @ 90(95)% CL}$$

LFV searches

If LFUV confirmed, what about LFV?, e.g.:

$$B \rightarrow \ell\ell', b \rightarrow (s,d)\ell\ell'$$

Recent LHCb searches:

$$B_{(s)}^0 \rightarrow \tau^+ \mu^- \quad PRL 123 (2019) 211801$$

$$BR(B_s^0 \rightarrow \tau^+ \mu^-) < 1.4 \times 10^{-5} @ 95 \% CL$$

$$BR(B_s^0 \rightarrow \tau^+ \mu^-) < 4.2 \times 10^{-5} @ 95 \% CL$$

$$B^+ \rightarrow K^+ \mu^\pm e^\mp \quad PRL 123 (2019) 241802$$

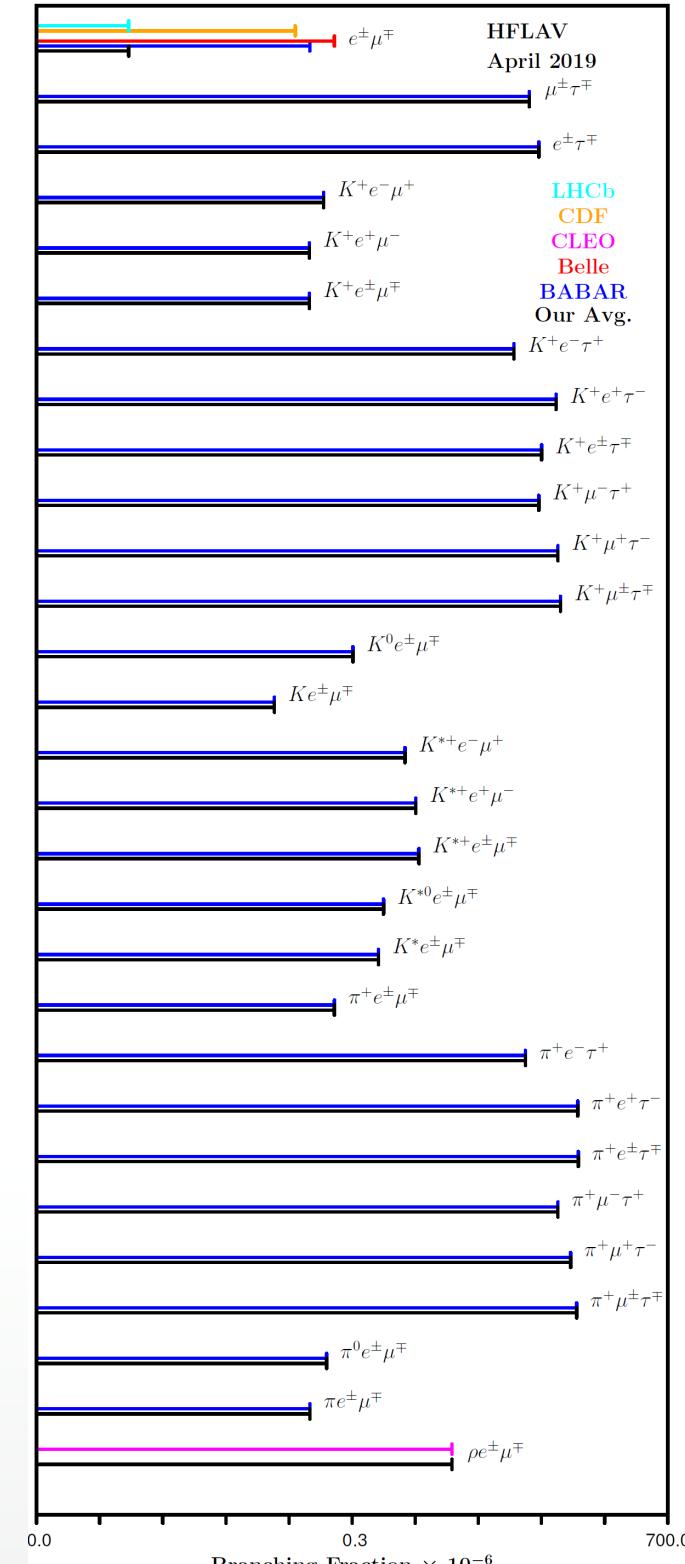
$$BR(B^+ \rightarrow K^+ \mu^- e^+) < 9.5 \times 10^{-9} @ 95 CL$$

$$BR(B^+ \rightarrow K^+ \mu^+ e^-) < 8.8 \times 10^{-9} @ 95 CL$$

$$B^+ \rightarrow K^+ \mu^- \tau^+ \quad JHEP 06 (2020) 129$$

$$BR(B^+ \rightarrow K^+ \mu^- \tau^+) < 4.5 \times 10^{-5} @ 95 CL$$

See I. Williams, Rare Decays parallel session, Tuesday



Prospects for LFU – finishing Run 2

Semileptonic LFU, ongoing effort:

$R(D^0)$: $B^+ \rightarrow D^0 \tau^- \nu_\tau$

$R(D^+)$: $B^0 \rightarrow D^+ \tau^- \nu_\tau$

$R(Ds^{(*)})$: $B_s \rightarrow D_s^{(*)} \tau^- \nu_\tau$

$R(\Lambda_c^{(*)})$: $\Lambda_b \rightarrow \Lambda_c^{(*)} \tau^- \nu_\tau$

$R(J/\Psi)$: $B_c \rightarrow J/\Psi \tau^- \nu_\tau$

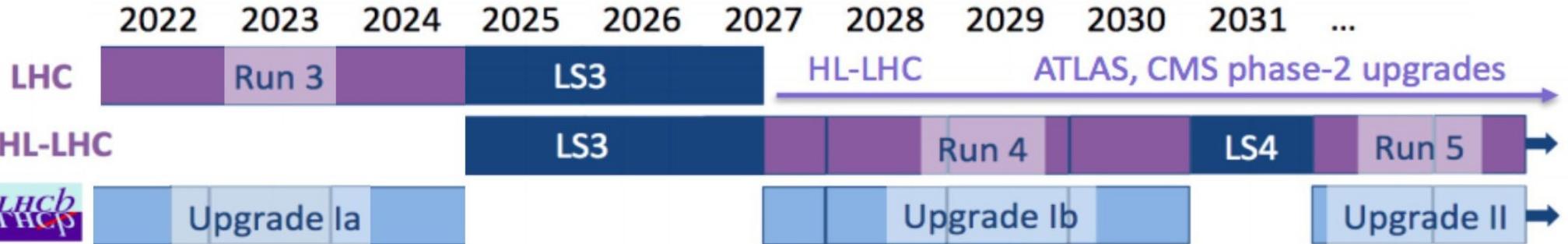
$R(p)$: $\Lambda_b \rightarrow p \tau^- \nu_\tau$

EW Penguin: Expected precisions with full Run1+Run2

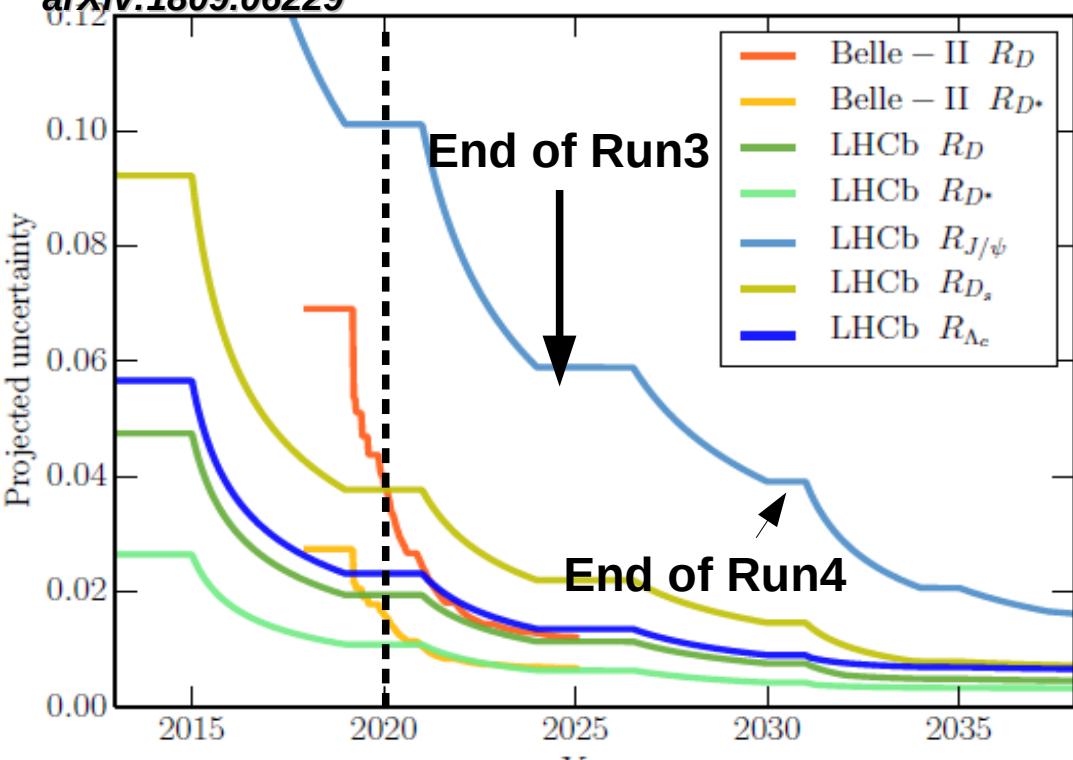
R_x precision	9 fb^{-1}
R_K	0.043
$R_{K^{*0}}$	0.052
R_ϕ	0.130
R_{pK}	0.105
R_π	0.302

CERN-LHCC-2018-027, LHCb-PUB-2018-009, arXiv:1808.08865

Prospects for LFU, upgrades



J. Phys. G: Nucl. Part. Phys. 46 (2019) 023001
arXiv:1809.06229



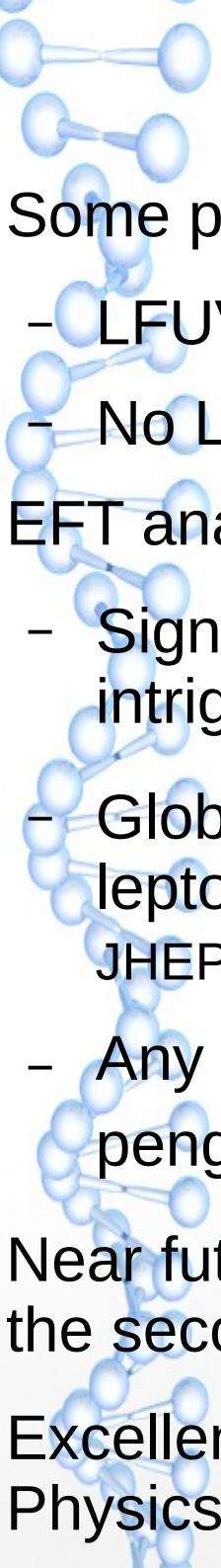
Tree $b \rightarrow c \ell \nu$

See L.Dufour, Thursday
HL-LHC upgrade & LHCb

	Run3	Run4	Run5
precision	23 fb^{-1}	50 fb^{-1}	300 fb^{-1}
R_K	0.025	0.017	0.007
$R_{K^{*0}}$	0.031	0.020	0.008
R_ϕ	0.076	0.050	0.020
R_{pK}	0.061	0.041	0.016
R_π	0.176	0.117	0.047

CERN-LHCC-2018-027, LHCb-PUB-2018-009, arXiv:1808.08865

Loop $b \rightarrow s(d)\ell^+\ell^-$



Conclusion

- Some persisting anomalies
 - LFUV tests 2-4 σ discrepancies
 - No LFV so far
- EFT analyses are becoming more and more accurate
 - Significance of NP contributions to Wilson coefficients becoming intriguing, e.g. for C_9
 - Global fit to WC are model-independent but models involving vector leptoquarks (JHEP 11 (2017) 044) or 4321 model (PRD 96, (2017) 115011, JHEP 11 (2018) 081) are regularly put forward
 - Any model is constrained by B_s mixing for $b \rightarrow s$ transitions (LFU EW penguins) and B_c lifetime for $b \rightarrow c$ (semileptonic LFU)
- Near future: more results and combinations are coming with analysis of the second half of Run 2
- Excellent prospects for Run 3 and after, fundamental role of Flavour Physics 30

Back up

LHCb data (2011+2012) – Run I

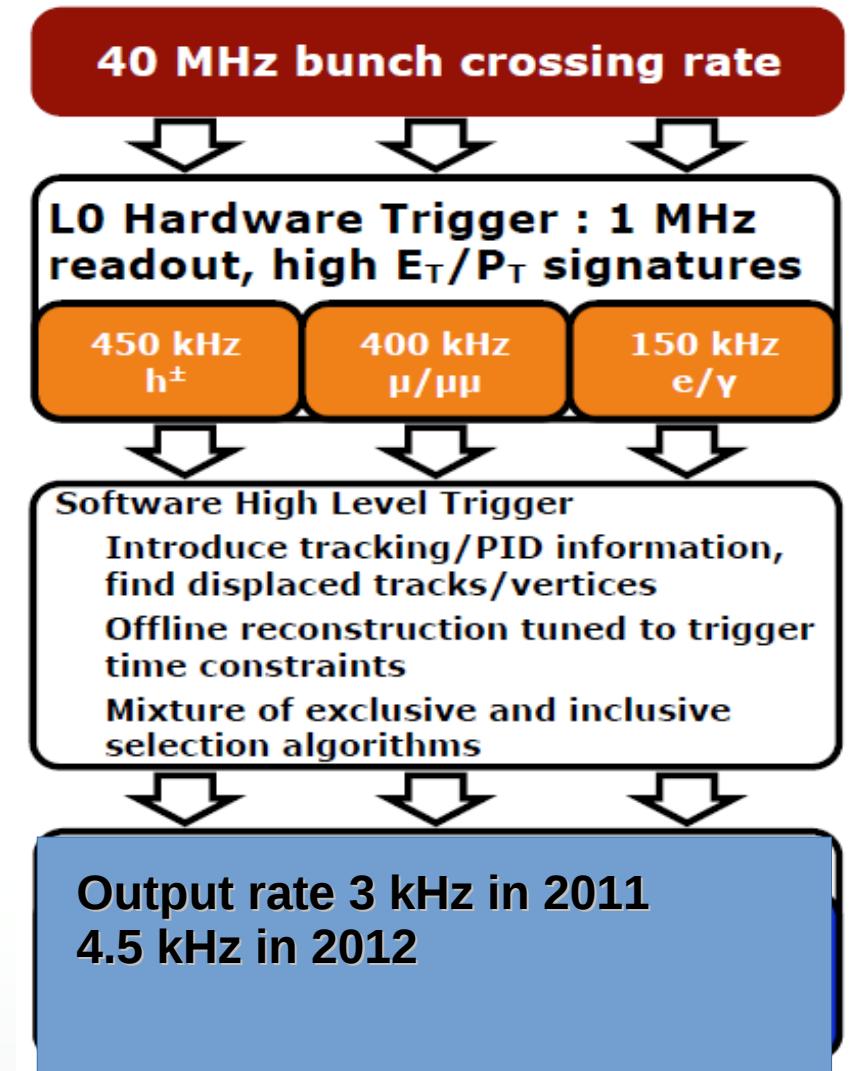
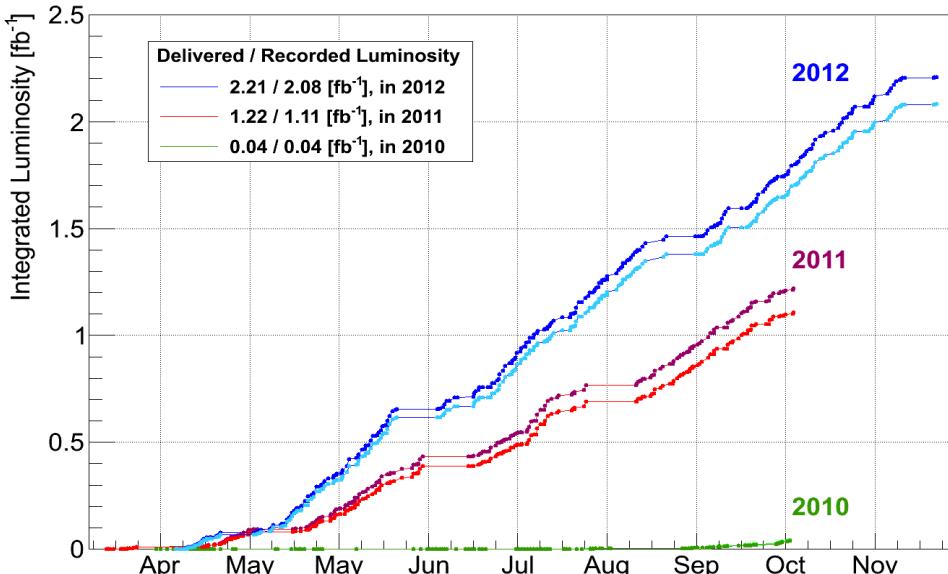
10^{11} protons per bunch colliding at 7 (2011) and 8 (2012) TeV

Luminosity at IP8 (LHCb): $2\text{--}4 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$

About 1500 charged particles produced at each pp collision

$\sigma(\text{bb}) \sim 75 \mu\text{b}$ @ 7 TeV* in LHCb acceptance
J. High Energy Phys. 08 (2013) 117

Dominated by B^+ (f_u) and B^0 (f_d) species but also B_s ,
 $f_s/(f_u + f_d) \sim 0.134$, b-baryons ($f(\Lambda_b)/(f_u + f_d) \sim 0.240$)
Traces of Bc, Eur. Phys. J. C77 (2017) 895



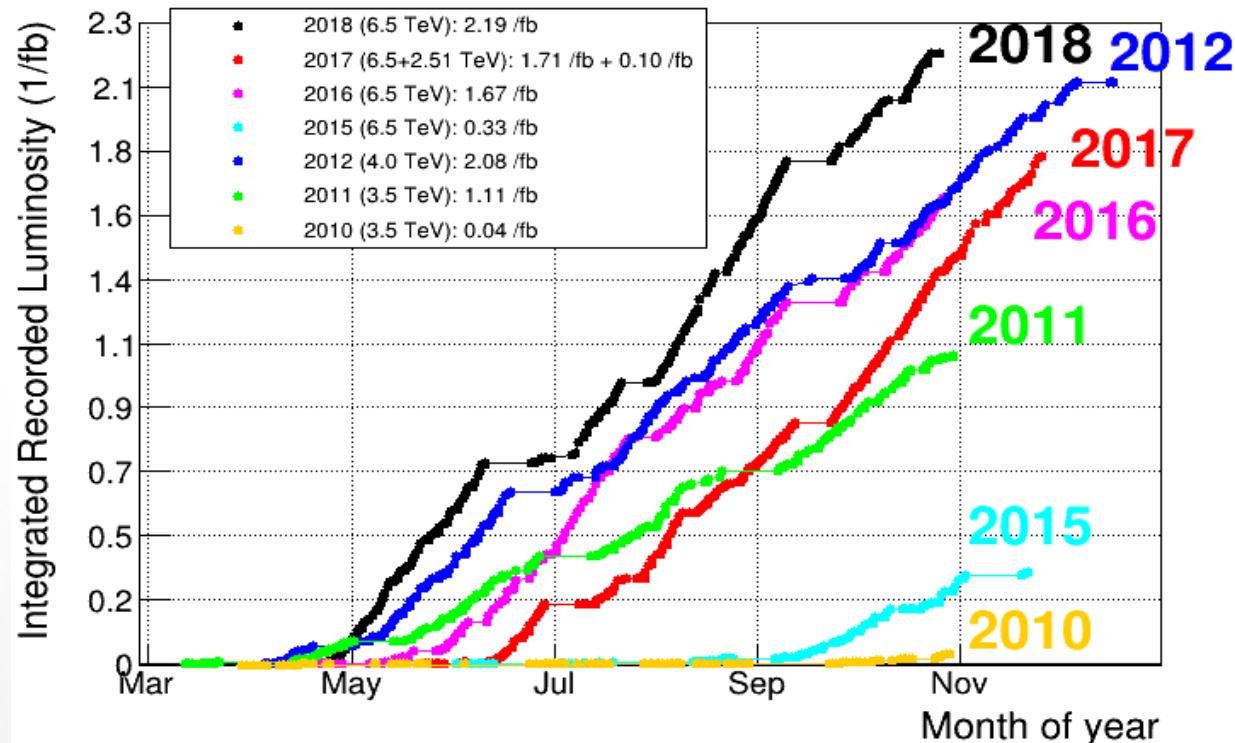
LHCb data (2015-2018) – Run II

Bunch colliding at 13 TeV

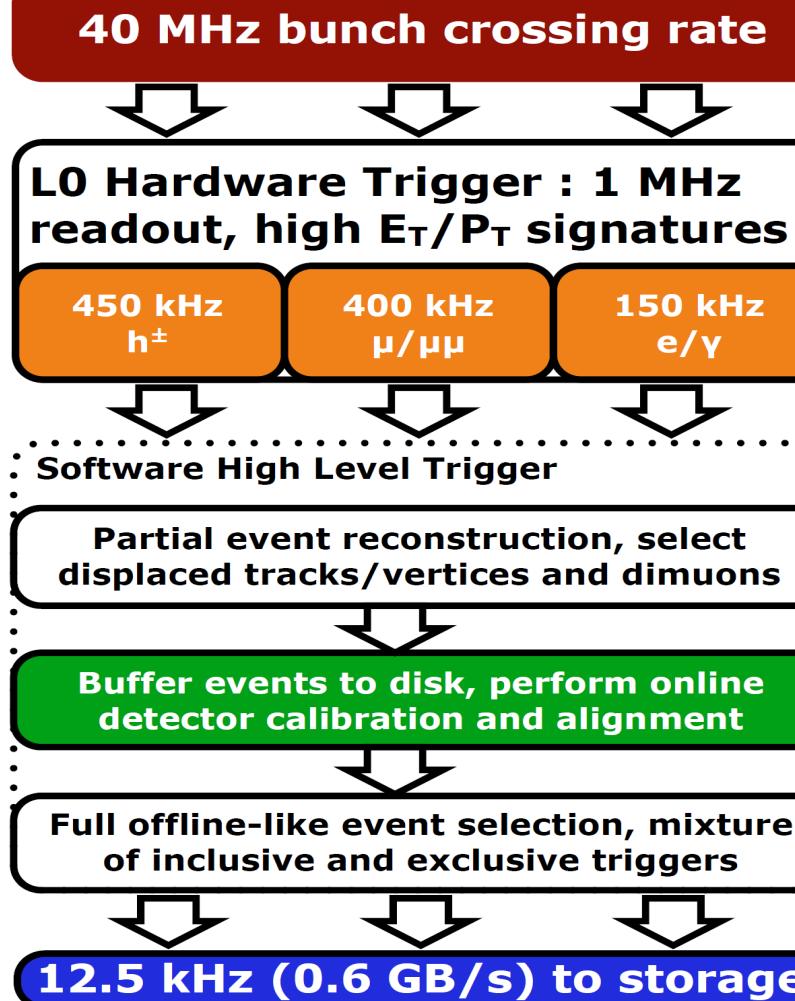
$\sigma(bb) \sim 165 \mu b$ @ 13 TeV* in LHCb acceptance
About 2.3 times the value @ 7-8 TeV

* *Phys. Rev. Lett.* 118, 052002 (2017)

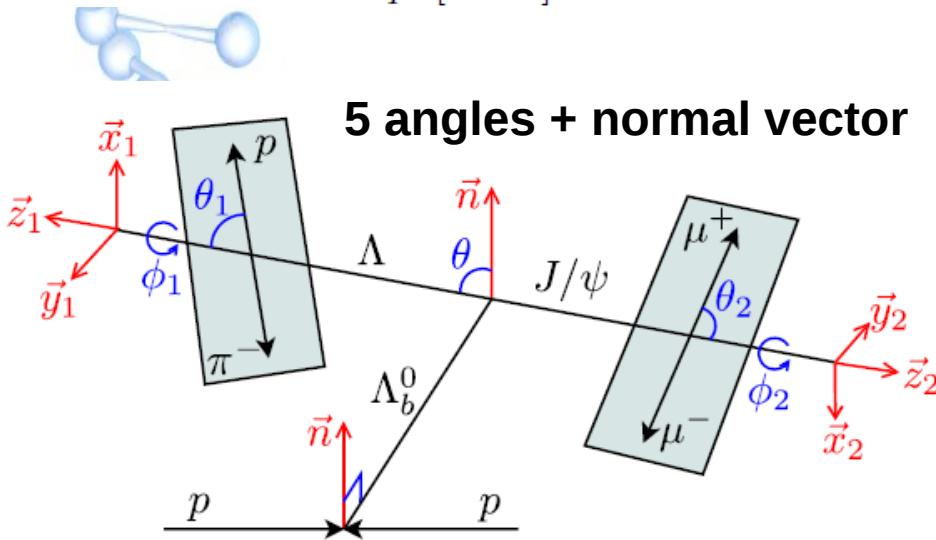
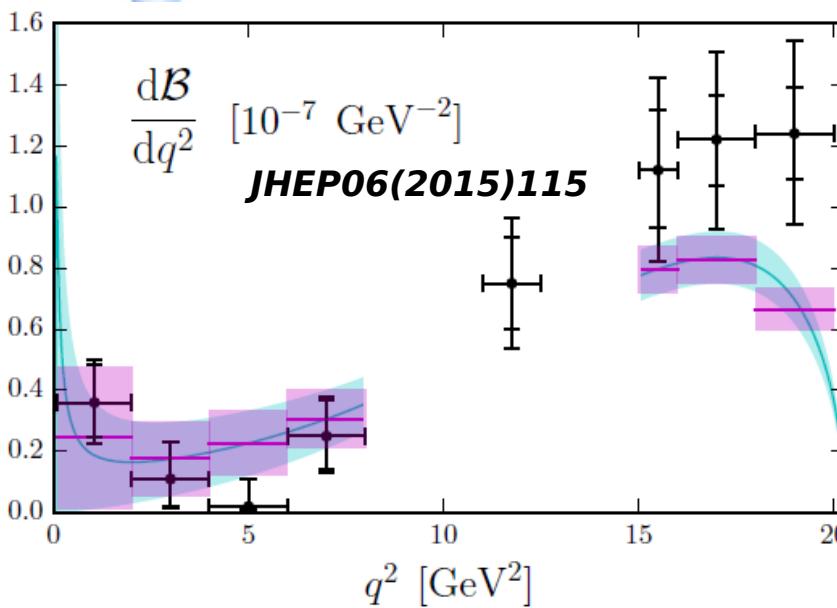
LHCb recorded luminosity in pp collisions / year



LHCb 2015 Trigger Diagram



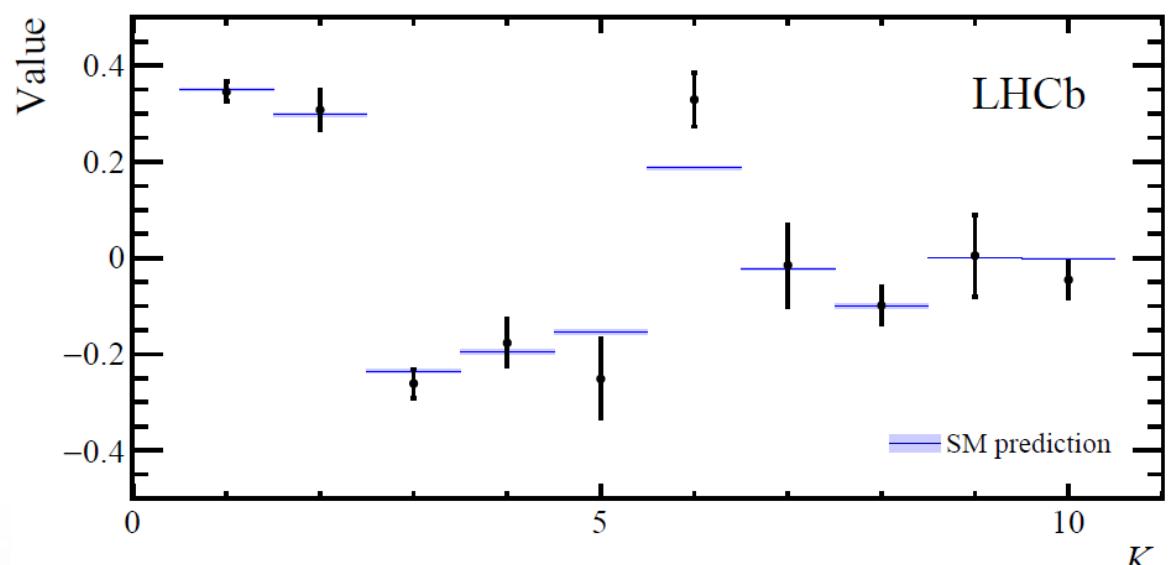
$\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$: q^2 and angular spectra



JHEP 09 (2018) 146

$$\frac{d^5\Gamma}{d\vec{\Omega}} = \frac{3}{32\pi^2} \sum_i^{34} K_i(q^2) f_i(\vec{\Omega})$$

Performed with Run 1 + Run 2 data



Compatibility with SM-based predictions
 Bo  r et al, JHEP01 (2015) 155
 Detmold et al., PRD93 (2016) 074501

Radiative $b \rightarrow s \gamma$

Let handed γ favoured, right handed suppressed by m_s/m_b
Mixing induced CP asymmetry suppressed similarly
Any substantial value of the parameters of time-dependent
CP asymmetry would be an indication of NP

$$\Gamma_B(t)/\Gamma_{\bar{B}}(t) \propto [\cosh(\Delta\Gamma t/2) - A^{\Delta\Gamma} \sinh(\Delta\Gamma t/2) \pm C \cos(\Delta m t/2) \mp S \sin(\Delta m t/2)]$$

Photon helicity and weak phases

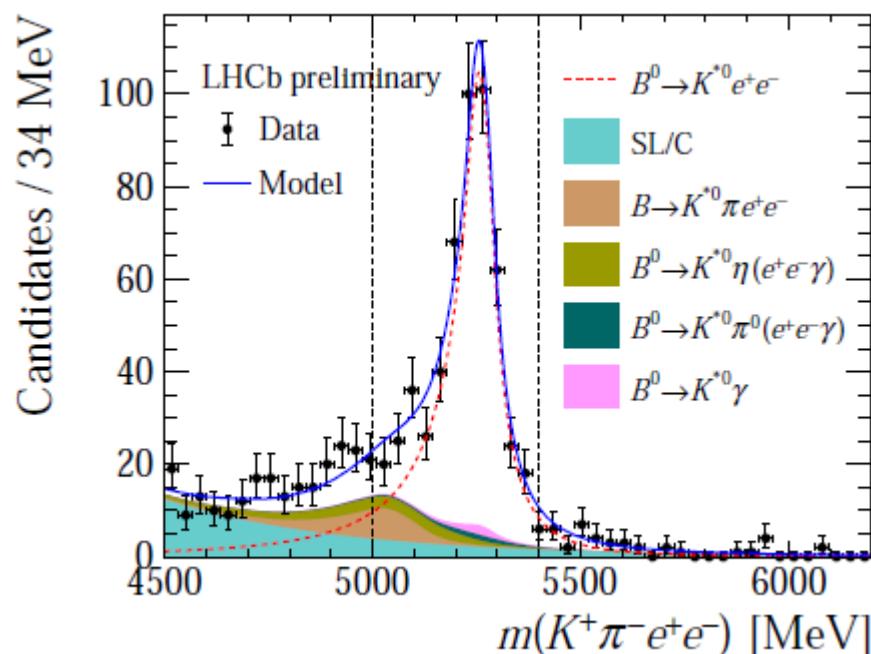
CP violation in the decay

Expected to be close to zero within SM (e.g., PLB664 (2008) 174)

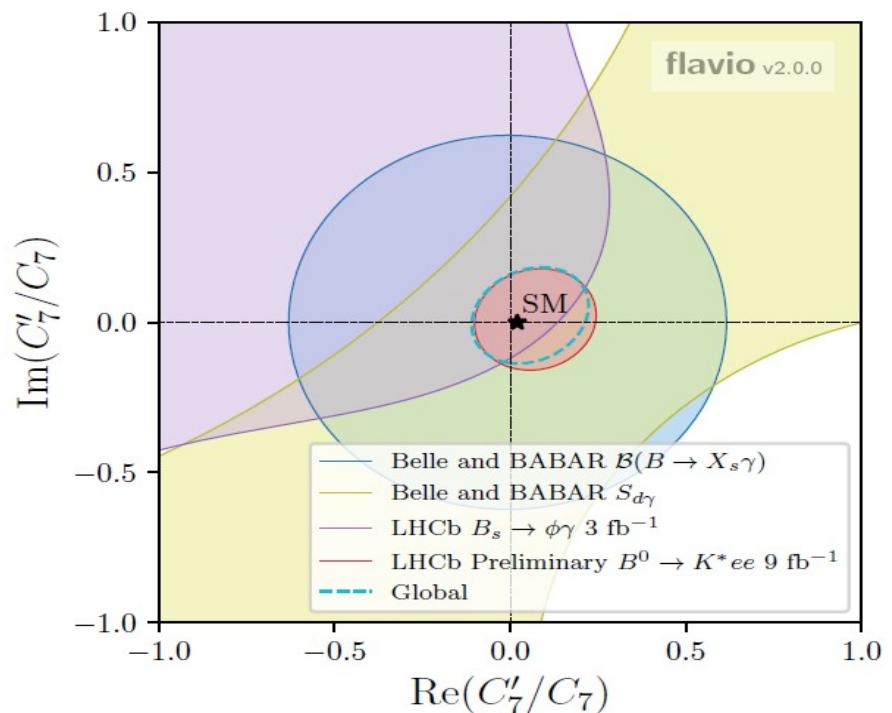
$B^0 \rightarrow K^{*0} e^+ e^-$ at very low q^2

**Sensitivity to γ polarization (operator O_7):
enhancement of RH current? (NP...)**

$0.0008 < q^2 < 0.257 \text{ GeV}^2$



Fit to $b \rightarrow s\gamma$ decays + low q^2 ee



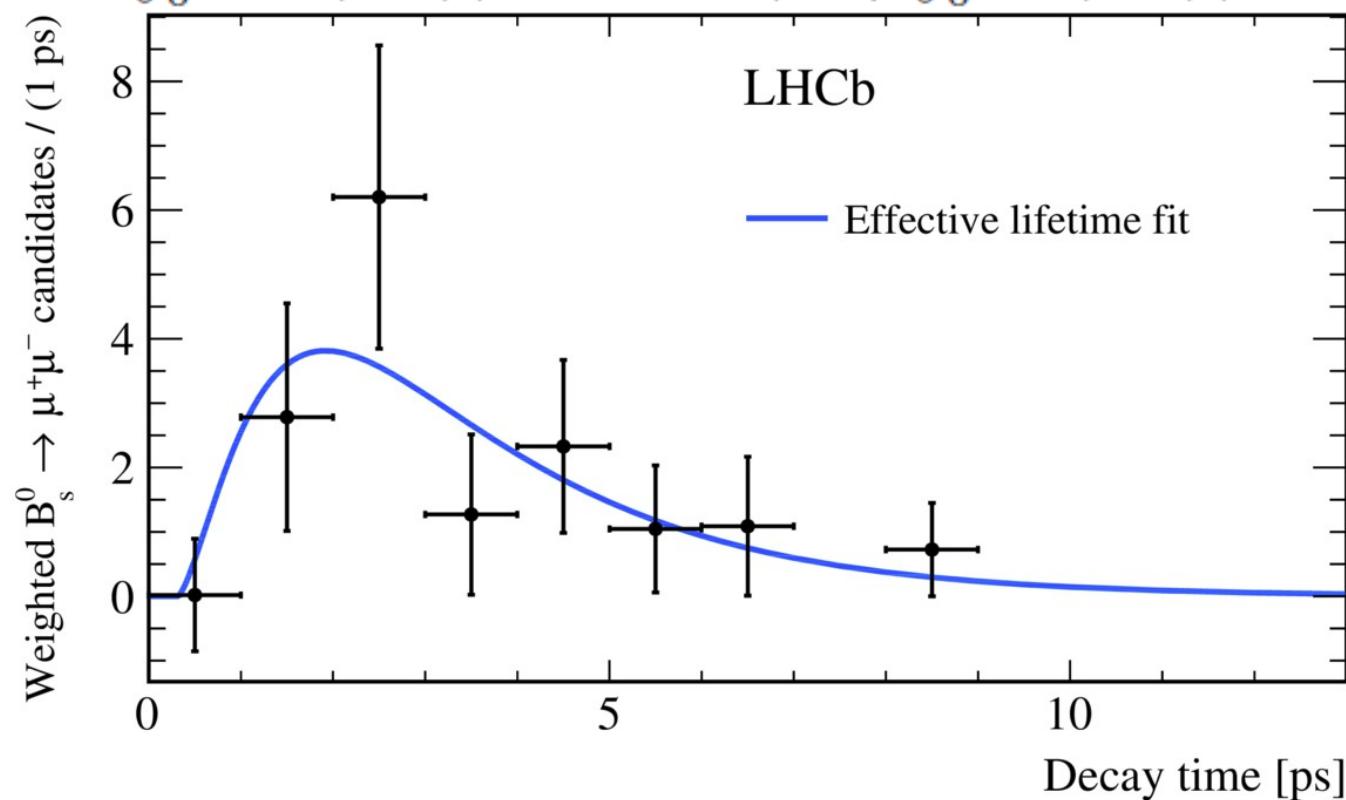
flavio arXiv:1810.08132

Folder angular analysis, coefficients compatible with SM.

$B_s \rightarrow \mu^+ \mu^-$ effective lifetime

LHCb (PRL 118 (2017) 191801)

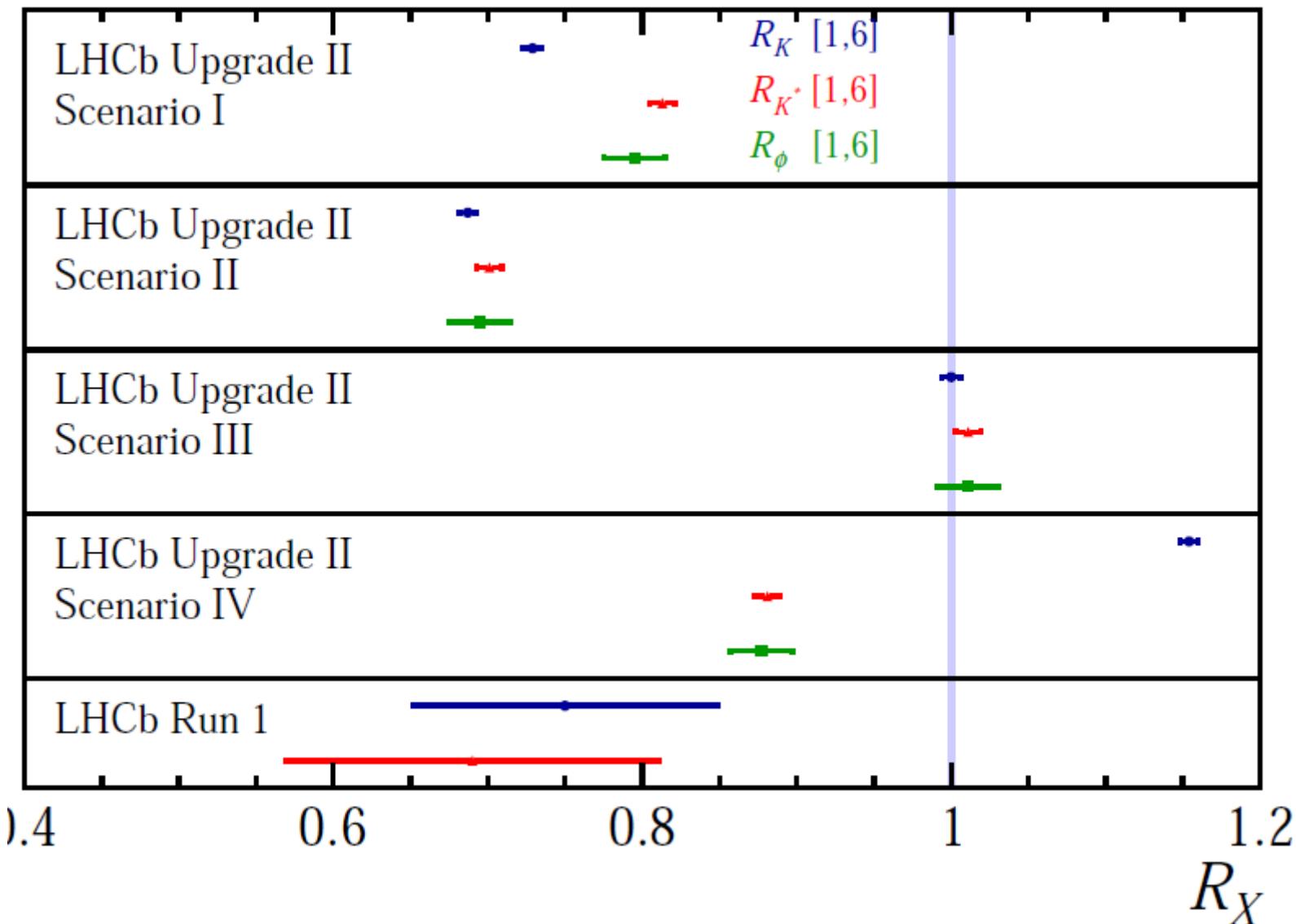
$$\tau_{\mu^+ \mu^-} \equiv \int_0^\infty t \Gamma(B_s(t) \rightarrow \mu^+ \mu^-) dt / \int_0^\infty \Gamma(B_s(t) \rightarrow \mu^+ \mu^-) dt$$



$$\tau(B_s \rightarrow \mu^+ \mu^-) = 2.04 \pm 0.44 \pm 0.05 \text{ ps}$$

R_X scenarios for Upgrade II

CERN-LHCC-2018-027, LHCb-PUB-2018-009, arXiv:1808.08865



Upgrade DAQ scheme

