

# LHCb: $b \rightarrow sll$

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on behalf of the LHCb Collaboration

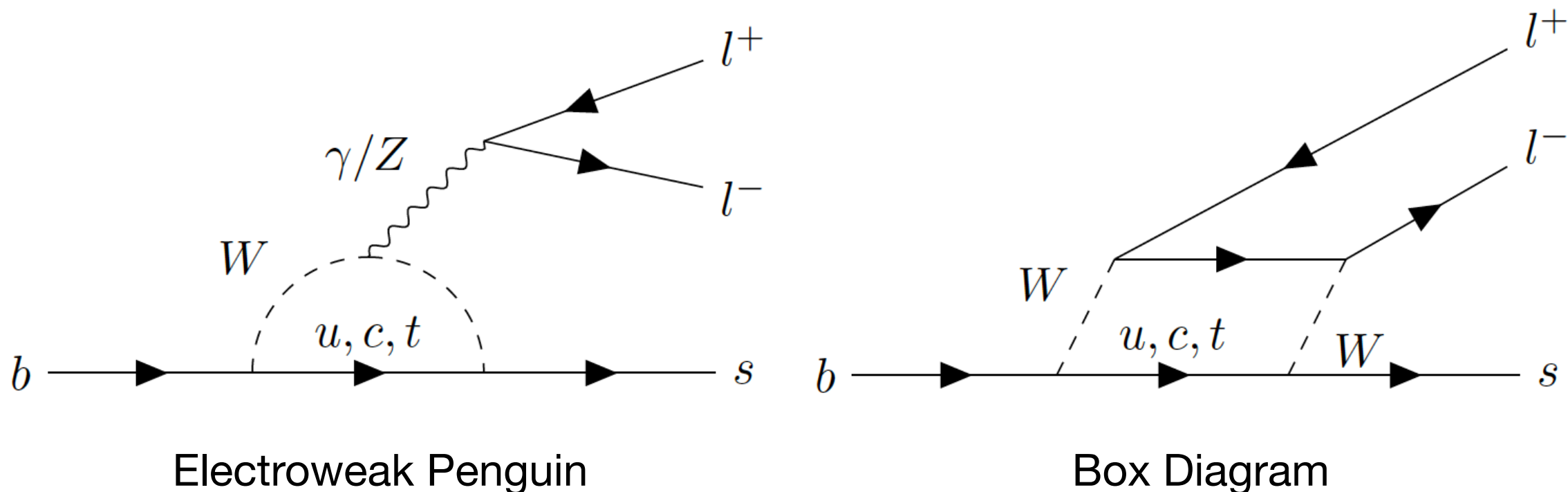


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# $b \rightarrow sll$ Decays

- SM forbids tree-level flavour changing neutral current transitions.
- Lowest-order Feynman diagrams are **electroweak penguin** or **box diagrams**.
  - Loops can **couple** to new physics and **access new physics scales** beyond direct searches.
  - Small branching fractions makes these decays **sensitive** to new physics effects.



# $b \rightarrow sll$ Effective Hamiltonian

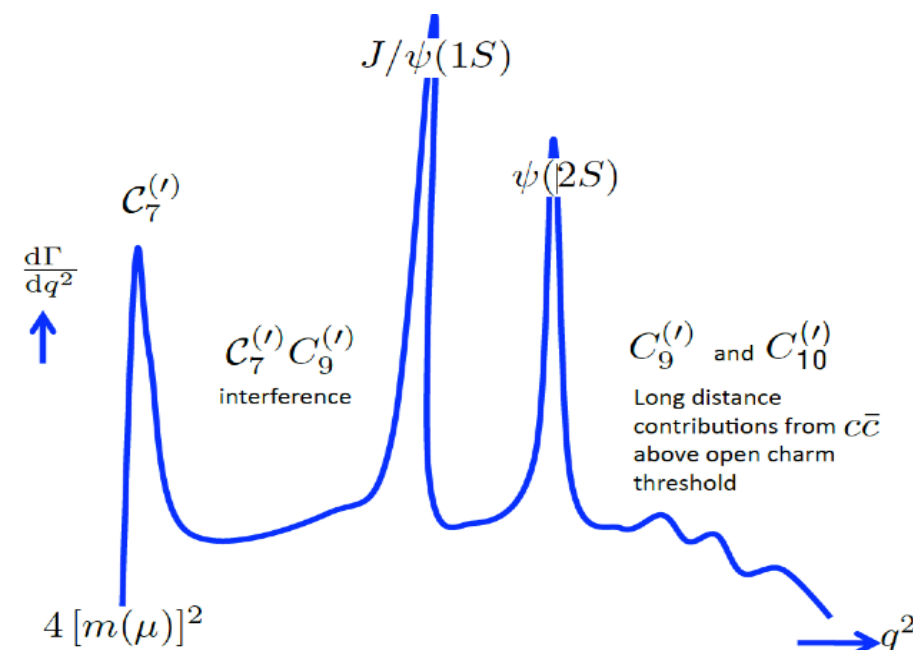
- $b \rightarrow sll$  decays can be modelled using a model-independent Effective Field theory approach

$$\mathcal{H}_{eff} = -\frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i C_i \mathcal{O}_i$$

Local Operators  
Long distance effects

Wilson Coefficients  
Short distance effects

- Different regions of  $q^2$  (dilepton invariant mass) probes different Wilson Coefficients



# Possible Measurements

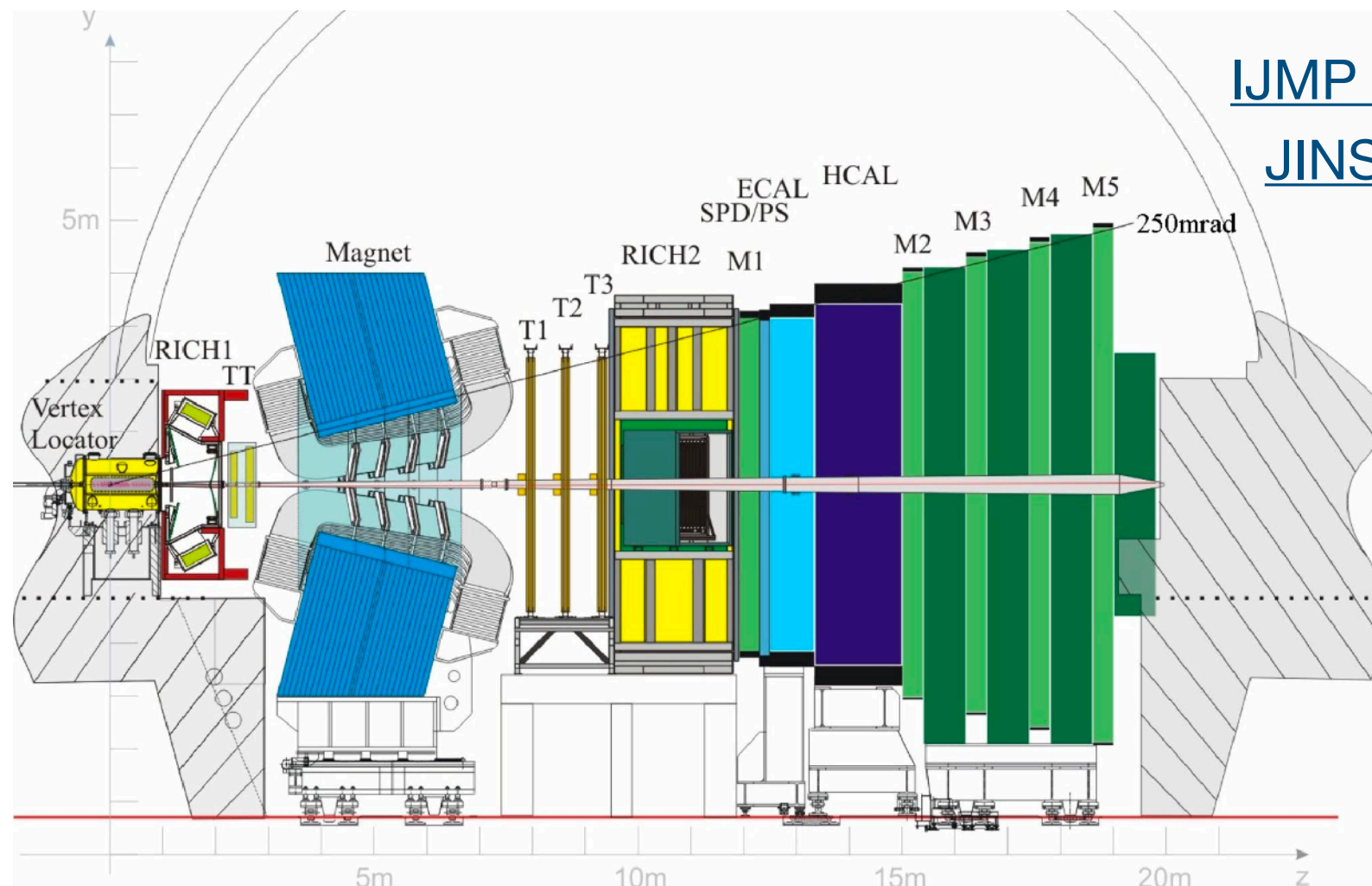
Decreasing hadronic  
form-factors  
uncertainty



- Differential branching fractions.
  - Uncertainties dominated by hadronic form-factor uncertainties.
- Angular observables.
  - Hadronic form-factors cancel to first-order.
- Lepton flavour universality ratios.
  - Hadronic form-factors cancel, theoretically clean.
  - SM is lepton flavour universal.



# The LHCb Detector

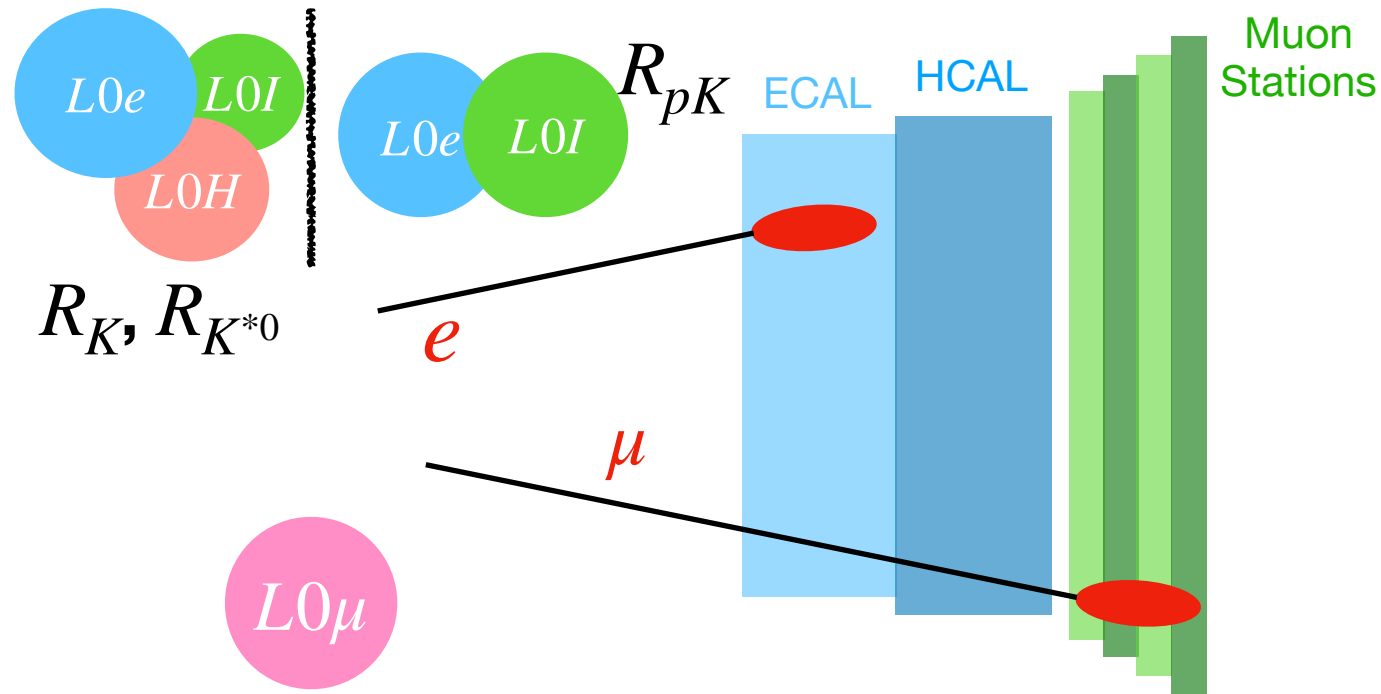


[IJMP A 30, 1530022 \(2015\)](#)

[JINST 14 \(2019\) P04013](#)

- LHCb is a forward spectrometer optimised in the  $2 < \eta < 5$  region for  $b$ -physics.
- 1 % momentum resolution,  $15 + \frac{29}{p_T(\text{GeV})} \mu\text{m}$  impact parameter resolution and good particle identification performance.

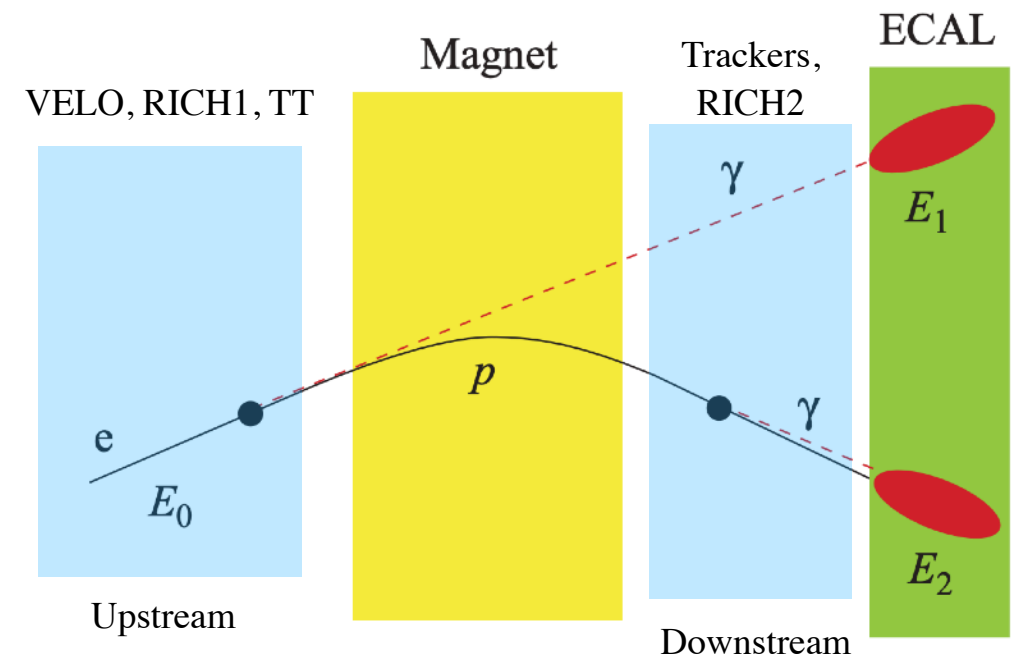
# Electrons vs Muons in LHCb



LHCb hardware trigger

$L0\mu$ : Triggered by muon  
 $L0e$ : Triggered by electron  
 $L0H$ : Triggered by hadron  
 $L0I$ : Triggered by other particle in event

- Electron triggers are **tighter and less efficient**.
- Electron modes use hadron and/or exclusive triggers to mitigate efficiency loss.

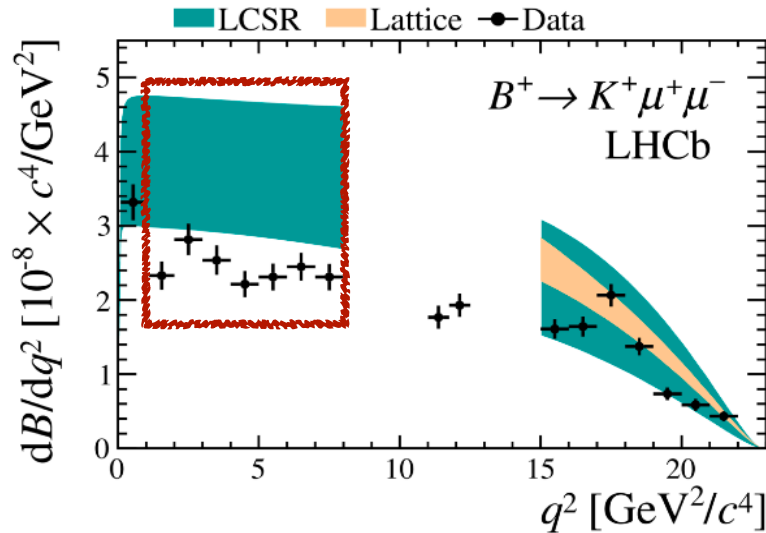


Bremsstrahlung in LHCb

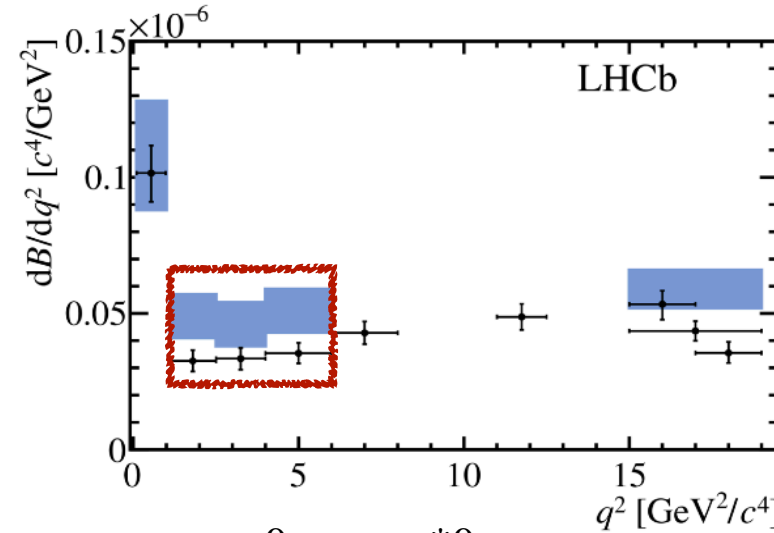
- Electrons emit bremsstrahlung due to material interactions.
- LHCb has recovery procedure but:
  - Photon recovery not 100% efficient.
  - ECAL has worse resolution than trackers.
- Electron modes have **worse momentum and mass resolution**.

# $b \rightarrow s \mu^+ \mu^-$ BF Measurements

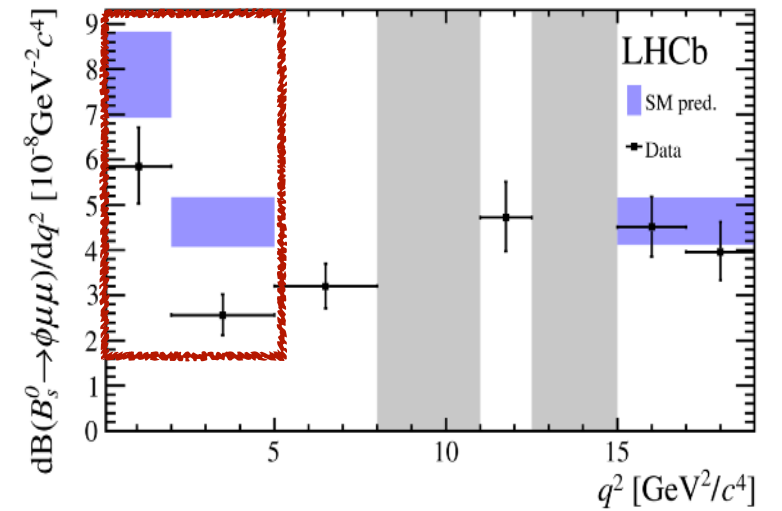
Low  $q^2$  measurements of different decay modes tend to lie consistently below SM predictions but no significant deviations are observed due to large theory uncertainties



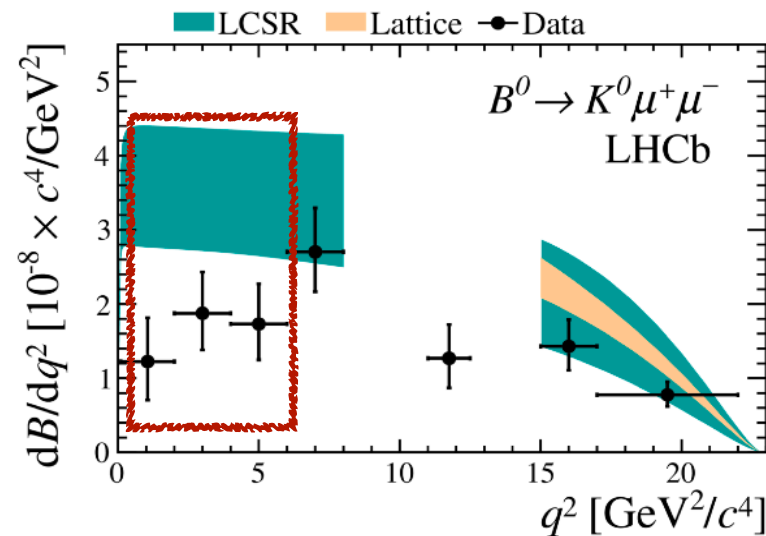
$B^+ \rightarrow K^+ \mu^+ \mu^-$   
[JHEP 06 \(2014\) 133](#)



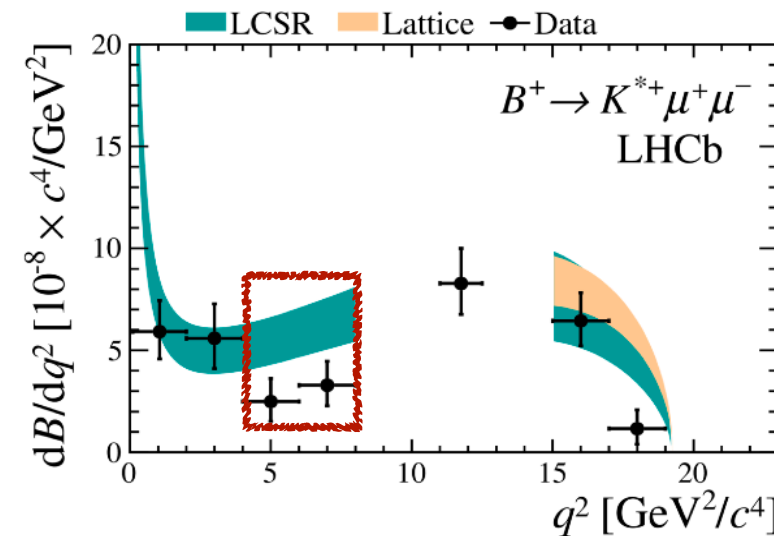
$B^0 \rightarrow K^{*0} \mu^+ \mu^-$   
[JHEP 11 \(2016\) 047](#)



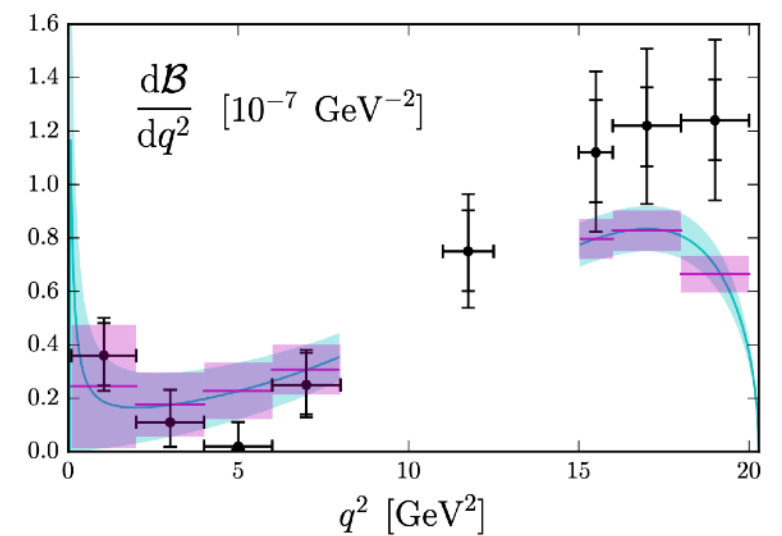
$B_s^0 \rightarrow \phi \mu^+ \mu^-$   
[JHEP 09 \(2015\) 179](#)



$B^0 \rightarrow K^0 \mu^+ \mu^-$   
[JHEP 06 \(2014\) 133](#)



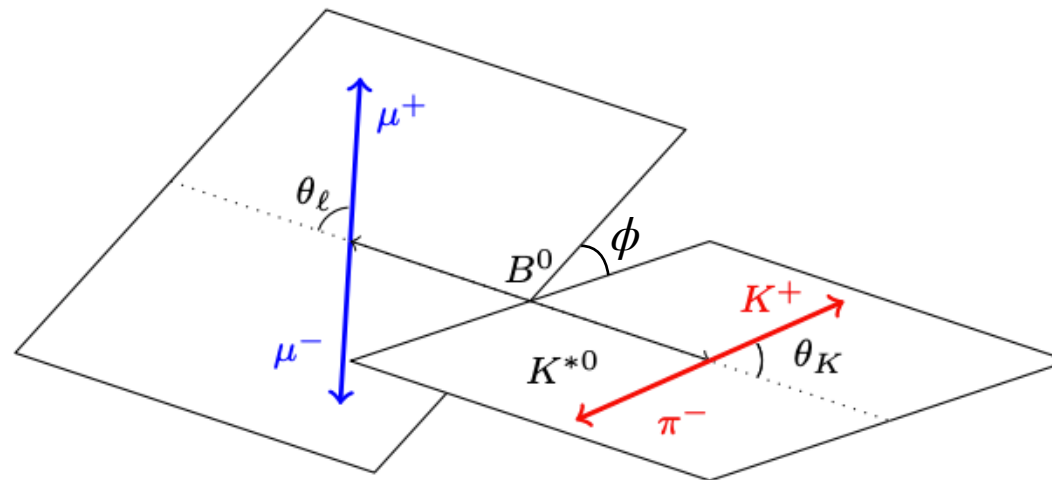
$B^+ \rightarrow K^{*+} \mu^+ \mu^-$   
[JHEP 06 \(2014\) 133](#)



$\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$   
[JHEP 06 \(2015\) 115](#)

# Angular Analysis of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

[PRL 125, 011802 \(2020\)](#)



$B^0 \rightarrow K^{*0} \mu^+ \mu^-$  Angle Definition

- Differential decay rate can be parameterised as a function of  $q^2$ , angles  $\vec{\Omega} = (\cos \theta_l, \cos \theta_K, \phi)$

$$\frac{d^4\Gamma[B^0 \rightarrow K^{*0} \mu^+ \mu^-]}{dq^2 d\vec{\Omega}} = \frac{9}{32\pi} \sum_i \boxed{I_i(q^2)} \boxed{f_i(\vec{\Omega})}$$

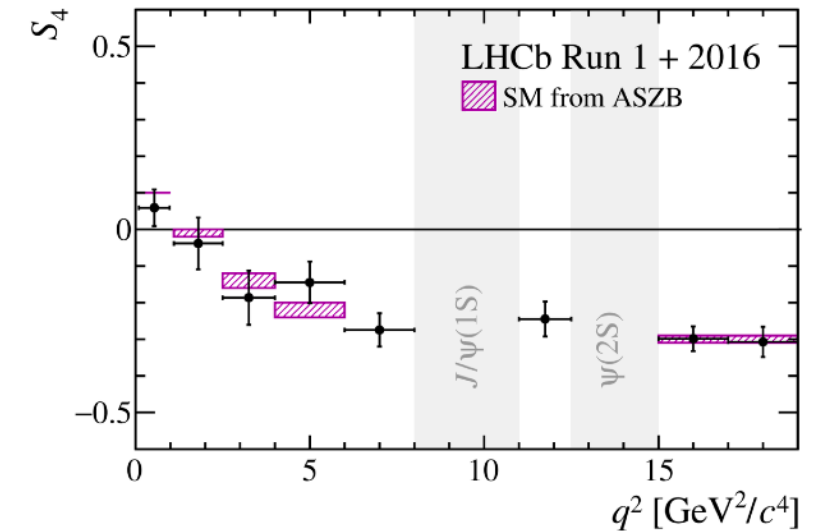
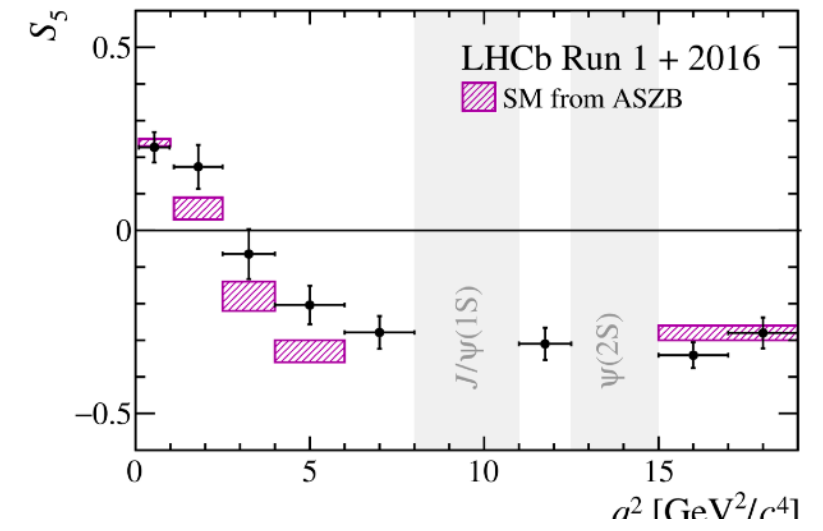
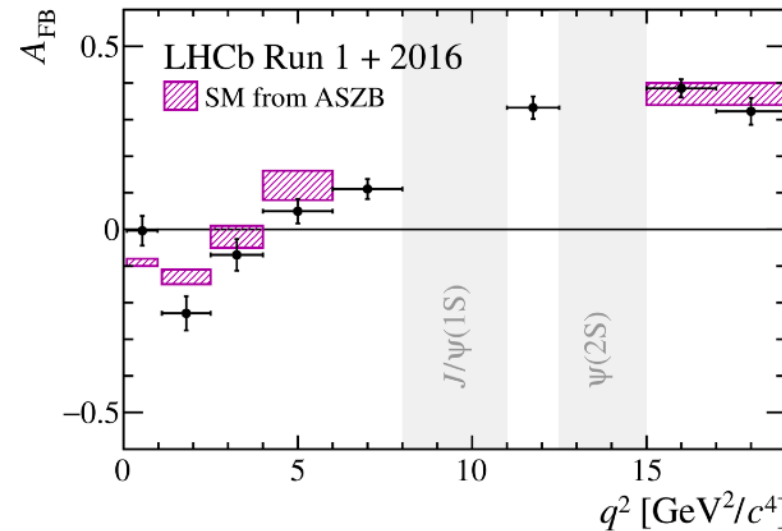
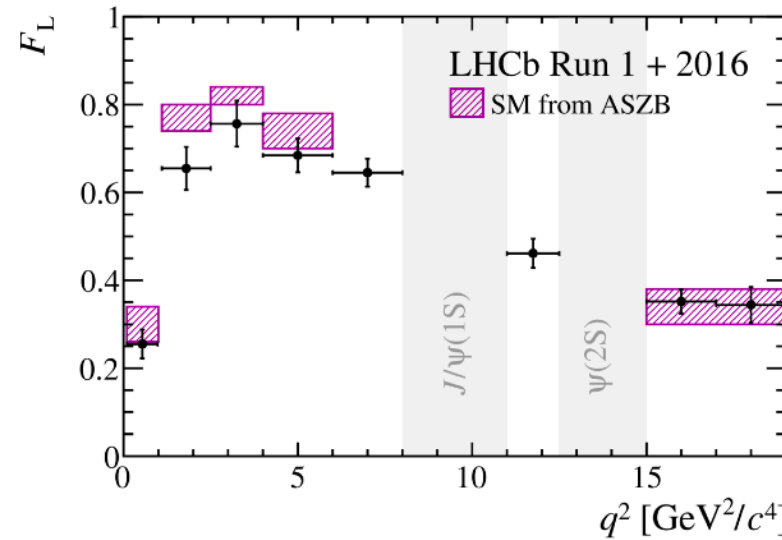
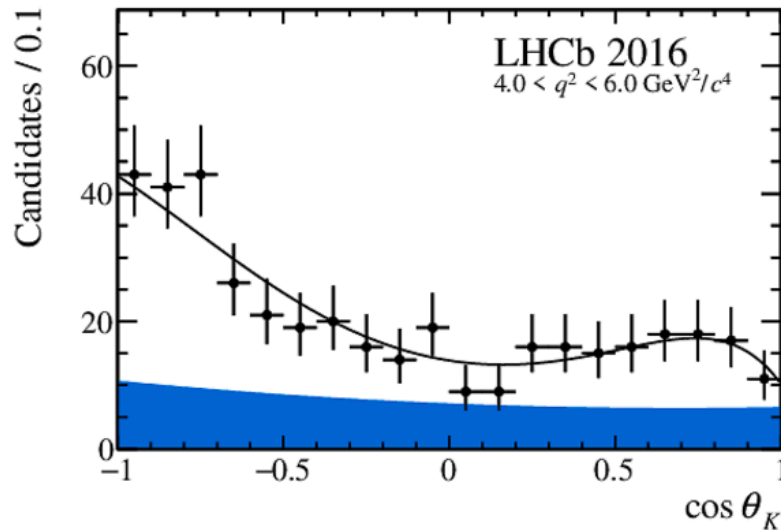
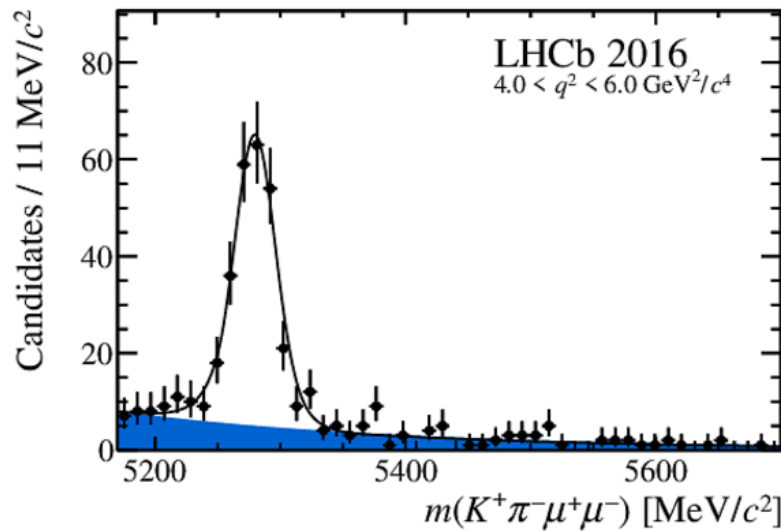
$q^2$  dependent  
angular observables

$\vec{\Omega}$  dependent  
angular functions

- Measure angular observables  $F_L, A_{FB}, S_i$  with  $4.7 \text{ fb}^{-1}$  of data.

# Fit Results

PRL 125, 011802 (2020)



- Efficiencies are evaluated as function of  $(q^2, \theta_l, \theta_K, \phi)$  and multiplied into  $\frac{d^4\Gamma}{dq^2 d\vec{q} d\vec{\Omega}}$

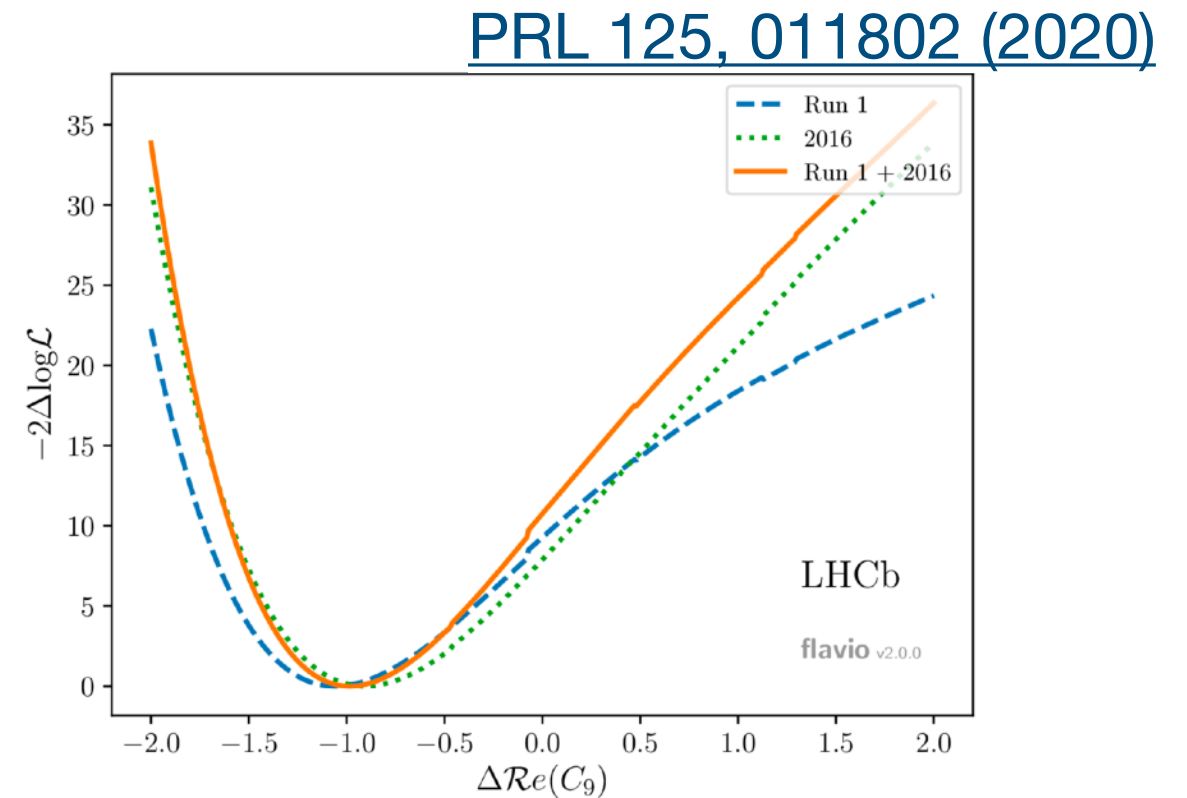
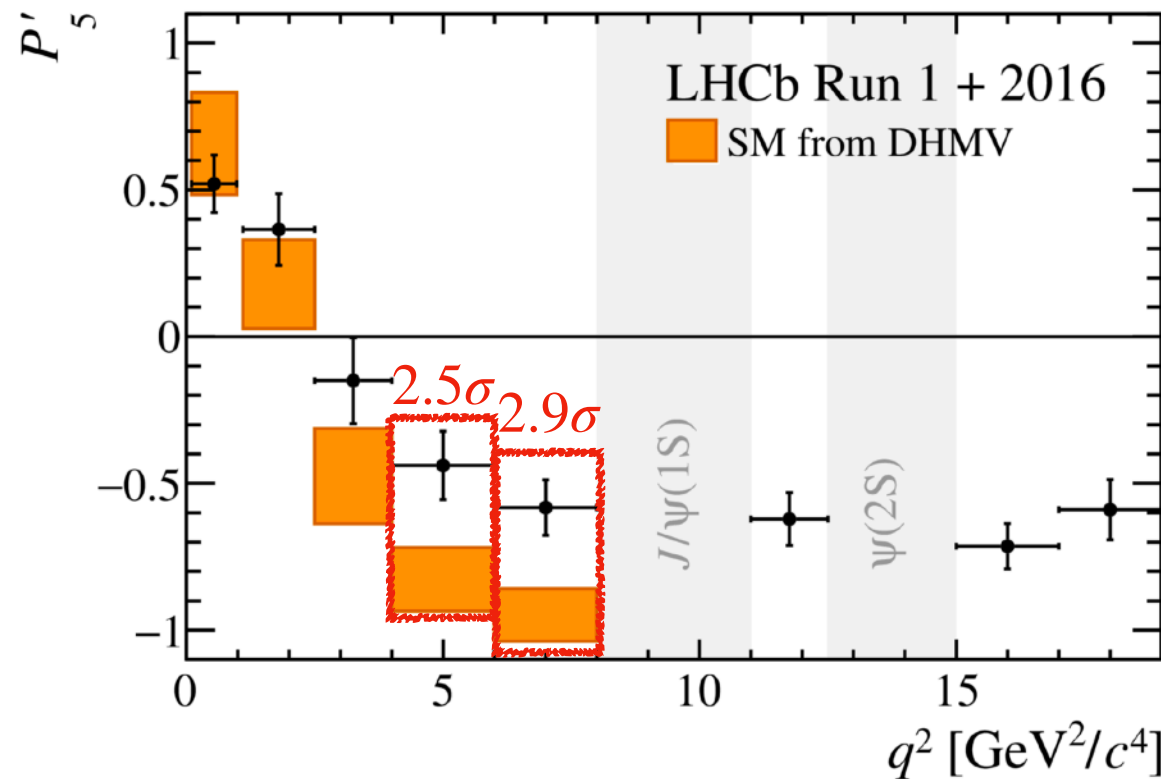
PDF.

Disentangle  $K^{*0}$  from  $S$ -Wave

- Fit  $(m_{K\pi\mu\mu}, m_{K\pi}, \vec{\Omega})$  distributions in 8  $q^2$  bins, excluding  $\phi(1020)$ ,  $J/\psi$ ,  $\psi(2S)$ .



# Optimised basis: $P'_5$



- Transform  $F_L, A_{FB}, S_i$  into  $P'_i$  basis which is independent, to first-order, of hadronic form-factors.

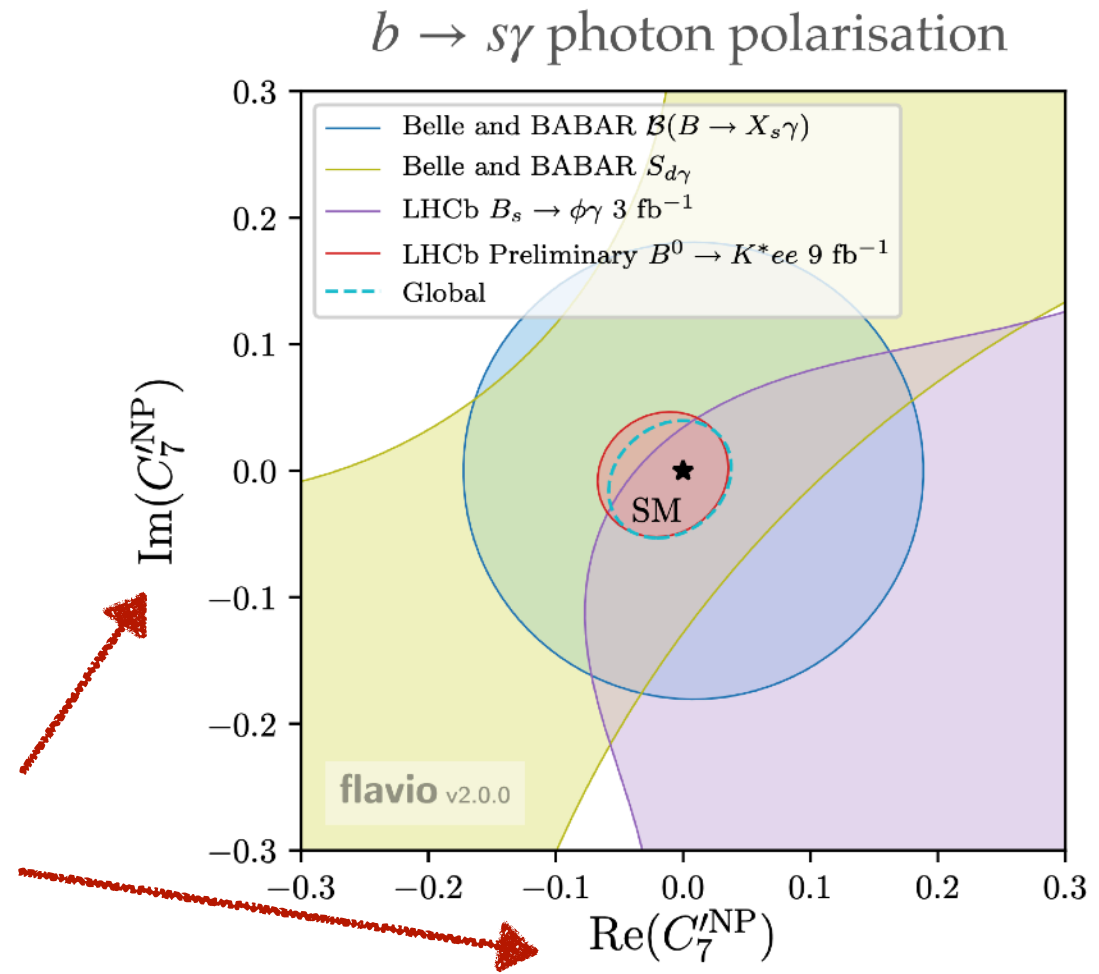
- Fit in  $P'_i$  basis.  $P'_5 = \frac{S_5}{\sqrt{F_L(1 - F_L)}}$ , tension with SM at  $2.5\sigma$  and  $2.9\sigma$ .

- Fit  $\Delta\text{Re}(C_9)$  using FLAVIO package and other parameters assuming their SM value:  $3.3\sigma$  tension with SM.

# Angular Analysis of $B^0 \rightarrow K^{*0} e^+ e^-$ [preliminary]

$$\begin{aligned}
 F_L &= 0.044 \pm 0.026 \pm 0.014 \\
 A_T^{\text{Re}} &= -0.064 \pm 0.077 \pm 0.015 \\
 A_T^{(2)} &= +0.106 \pm 0.103^{+0.016}_{-0.017} \\
 A_T^{\text{Im}} &= +0.015 \pm 0.102 \pm 0.012,
 \end{aligned}$$

$$\begin{aligned}
 A_T^{(2)}(q^2 \rightarrow 0) &= \frac{2 \operatorname{Re}(C_7 C_7'^*)}{|C_7|^2 + |C_7'|^2} \\
 A_T^{\text{Im}}(q^2 \rightarrow 0) &= \frac{2 \operatorname{Im}(C_7 C_7'^*)}{|C_7|^2 + |C_7'|^2}
 \end{aligned}$$



- Measured with  $9 \text{ fb}^{-1}$  of data, in the very low  $q^2$  range  $[0.0008, 0.256] \text{ GeV}^2/c^4$ .
- Similar to  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ , 4D fit to  $(m_{K\pi ee}, \cos \theta_l, \cos \theta_K, \tilde{\phi})$ ,  $\tilde{\phi} = \phi + \pi$ .
- Results agree with SM. Strong constraints on right-handed photon polarisation Wilson coefficient  $C_7'$ . (left plot).
- Presented at [ICHEP](#), paper LHCb-PAPER-2020-020 in preparation.

# Measurement of short-distance and long-distance interference

[Eur. Phys. J. C \(2017\) 77: 161](#)

- Experimental measurements of  $b \rightarrow sl^+l^-$  typically avoid the  $q^2$  region around  $J/\psi$  and  $\psi(2S)$  charmonium resonances
- However, these resonances (and  $\rho$ ,  $\omega$ ,  $\phi$ ) might interfere destructively with  $b \rightarrow sl^+l^-$  decays and mimic a new physics effect. Argued by:

[arXiv:1406.0566](#)

[arXiv:1503.06199](#)

[JHEP 06\(2016\)116](#)

- Analysis selects  $K^+\mu^+\mu^-$  final states and fits the  $m_{\mu^+\mu^-}$  spectrum using the effective Hamiltonian to study the interference effect, assuming

$$C_9^{eff} = C_9 + \sum_j \overset{\text{Magnitude}}{\eta_j} \overset{\text{Phase}}{e^{i\delta_j}} \overset{\text{Lineshape function, typically relativistic Breit-Wigner}}{A_j^{res}(q^2)}$$

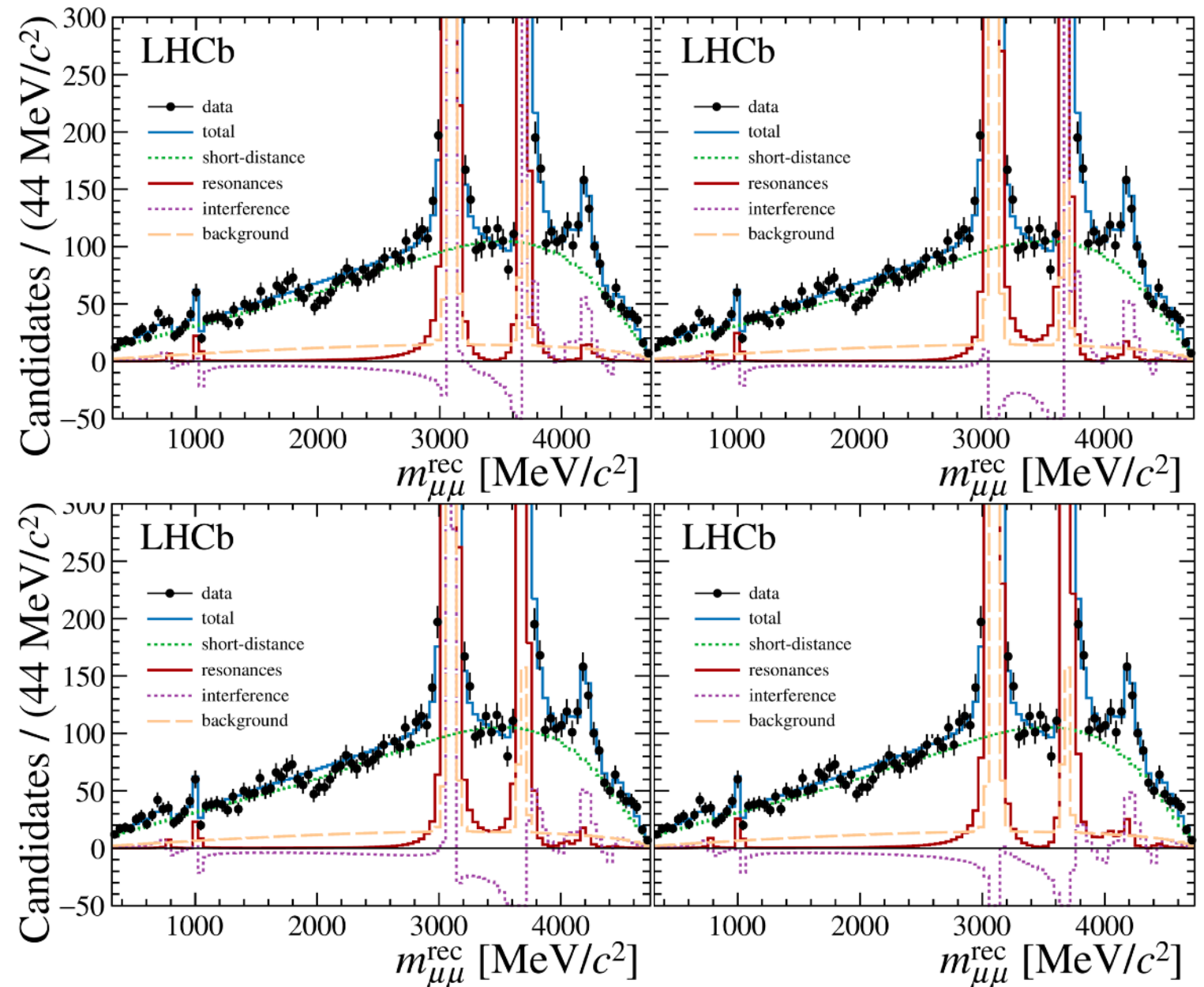


# Measurement of short-distance and long-distance interference

[Eur. Phys. J. C \(2017\) 77: 161](#)

- Model fits data well,  

$$\chi^2_{ndof} = \frac{110}{78}$$
- Four-fold ambiguities due to sign on  $J/\psi$  and  $\psi(2S)$  phases
- The contributions from charmonium resonances are small in the  $q^2$  region far away from the  $J/\psi$  mass



Four best-fit solutions to  $m_{\mu^+\mu^-}$

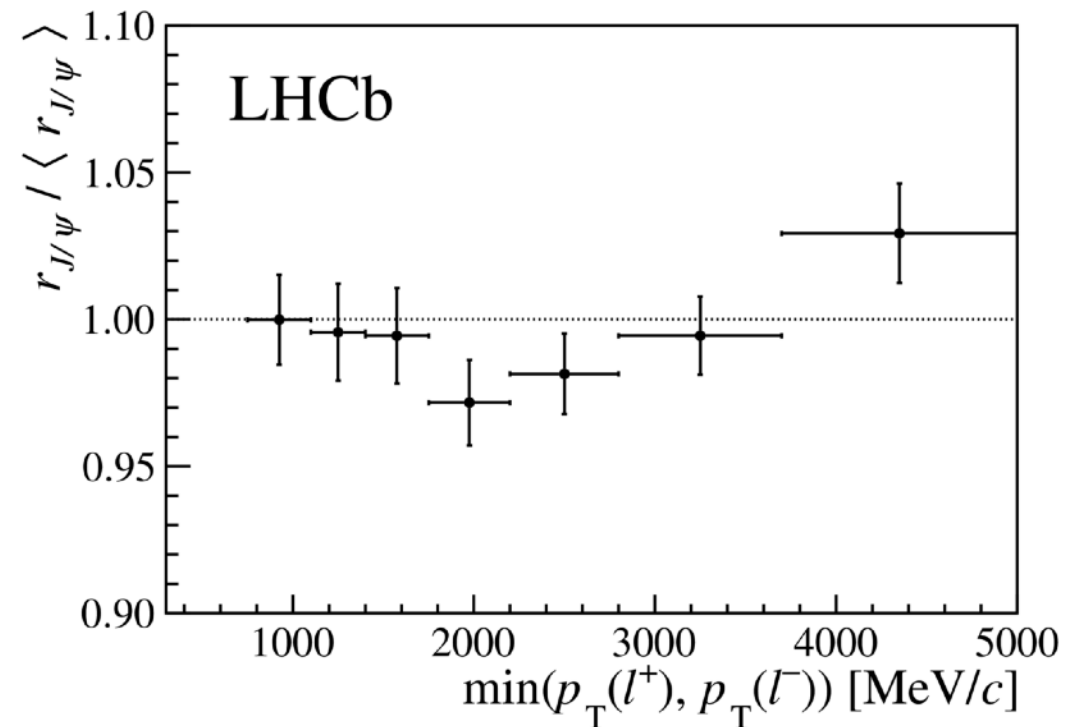
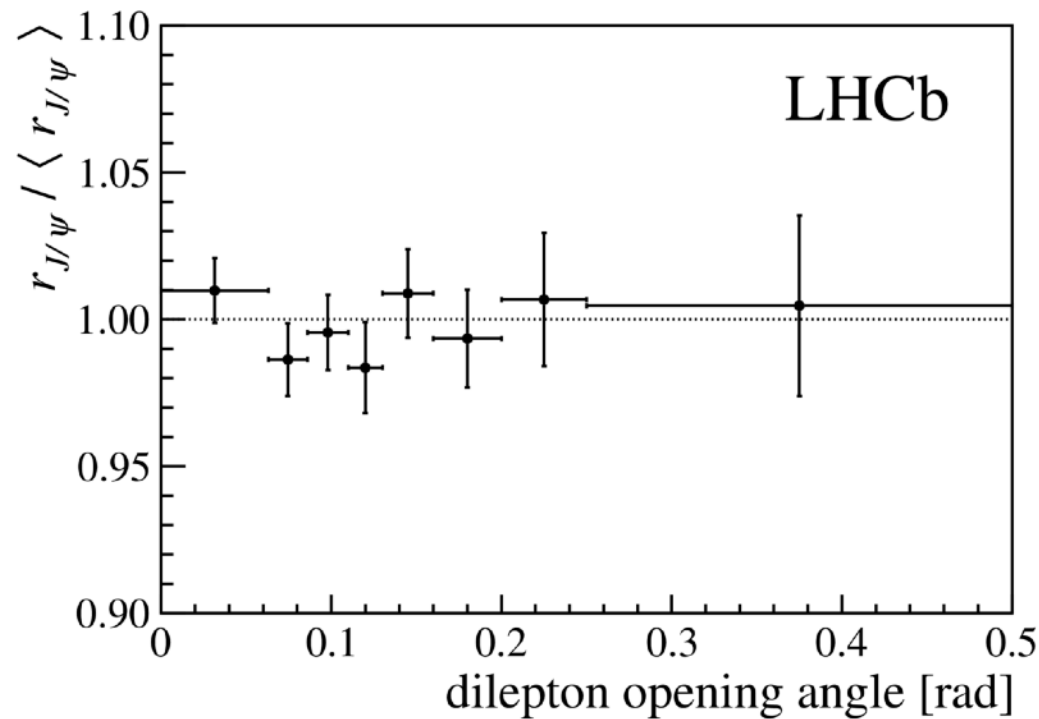
# Test of Lepton Flavour Universality

- Theoretical calculations predict  $R_H = \frac{\int_{q_{min}^2}^{q_{max}^2} \frac{d\mathcal{B}(B \rightarrow H\mu\mu)}{dq^2} dq^2}{\int_{q_{min}^2}^{q_{max}^2} \frac{d\mathcal{B}(B \rightarrow Hee)}{dq^2} dq^2}$ .
- LHCb analysis strategy: use tree-level  $B \rightarrow H J/\psi(\rightarrow l^+l^-)$  as a control mode. Measure lepton flavour universality as a double ratio.

$$\begin{aligned}
 R_H^{Double} &= \frac{R_H}{r_{J/\psi}} = \frac{\mathcal{B}(B \rightarrow H\mu\mu)}{\mathcal{B}(B \rightarrow HJ/\psi(\rightarrow \mu\mu))} \bigg/ \frac{\mathcal{B}(B \rightarrow Hee)}{\mathcal{B}(B \rightarrow HJ/\psi(\rightarrow ee))} \\
 &\quad \text{Expected to be unity} \\
 &= \frac{N(B \rightarrow H\mu\mu)}{N(B \rightarrow HJ/\psi(\rightarrow \mu\mu))} \times \frac{\epsilon(B \rightarrow HJ/\psi(\rightarrow \mu\mu))}{\epsilon(B \rightarrow H\mu\mu)} \quad \text{Estimate with simulation, corrected using data-driven methods} \\
 &\quad \text{Measure with mass fits to } m_{Hu} \\
 &\quad \times \frac{N(B \rightarrow HJ/\psi(\rightarrow ee))}{N(B \rightarrow Hee)} \times \frac{\epsilon(B \rightarrow Hee)}{\epsilon(B \rightarrow HJ/\psi(\rightarrow ee))}
 \end{aligned}$$

- Systematics cancel in the efficiency ratio.

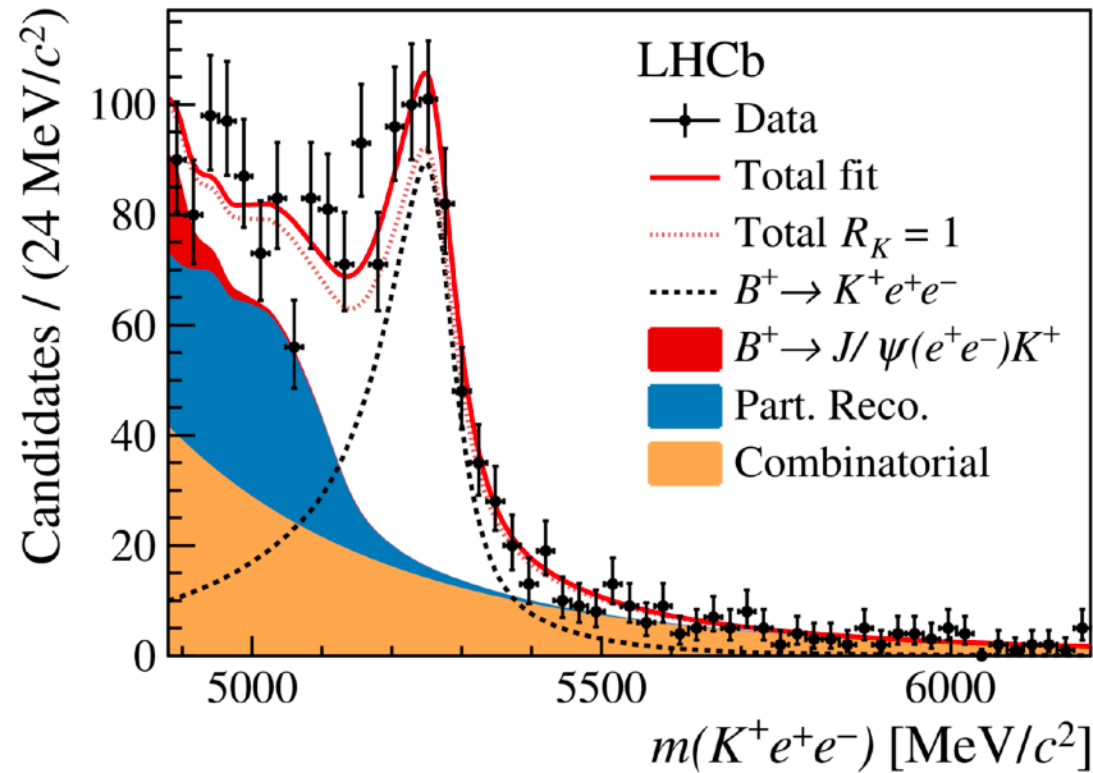
# $r_{J/\psi}$ and $R_{\psi(2S)}$ Cross-checks



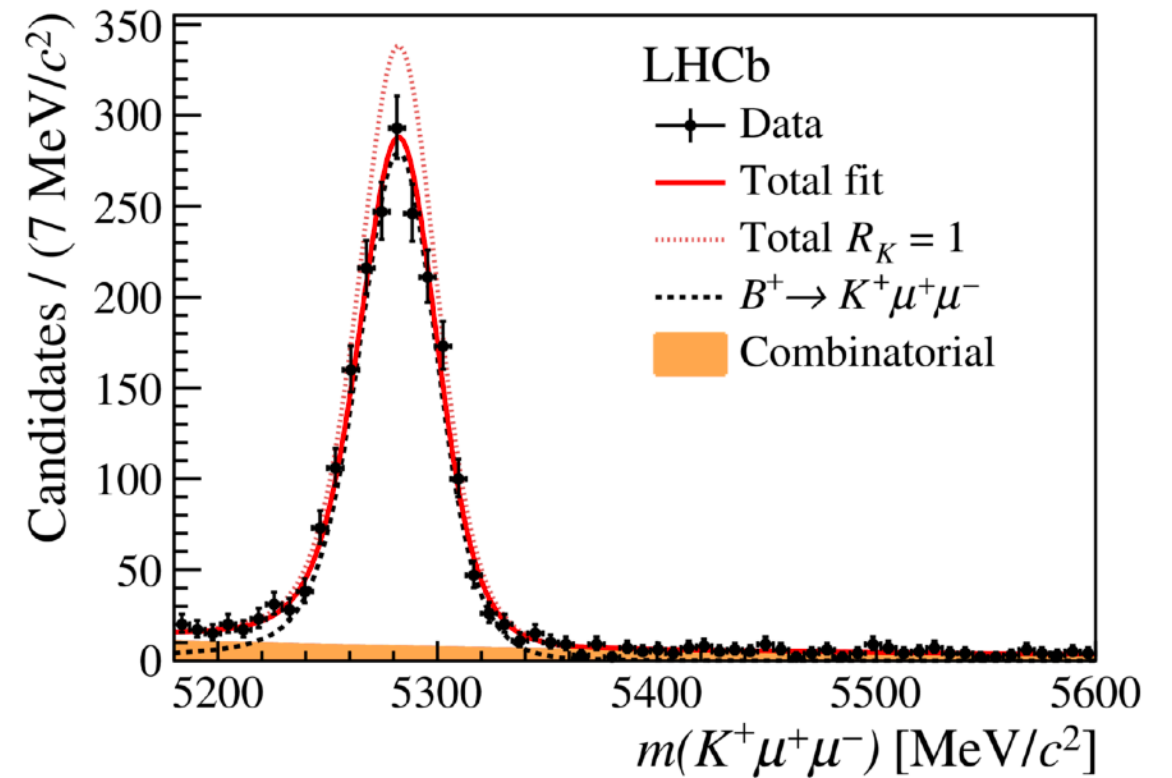
[PRL 122, 191801 \(2019\)](#)

- Measure  $r_{J/\psi} = \frac{\mathcal{B}(B \rightarrow HJ/\psi(\rightarrow \mu\mu))}{\mathcal{B}(B \rightarrow HJ/\psi(\rightarrow ee))}$  as an efficiency cross check. Systematics in  $\mu/e$  efficiency ratio do not cancel.
- Integrated  $r_{J/\psi}$  cross checks total efficiencies.
- Differential  $r_{J/\psi}$  flat, independent of kinematics (see plots).

- Check double ratio  $R_{\psi(2S)} = \frac{\mathcal{B}(B \rightarrow H\psi(2S)(\rightarrow \mu\mu))}{\mathcal{B}(B \rightarrow H\psi(2S)(\rightarrow ee))} \times \frac{1}{r_{J/\psi}}$ .



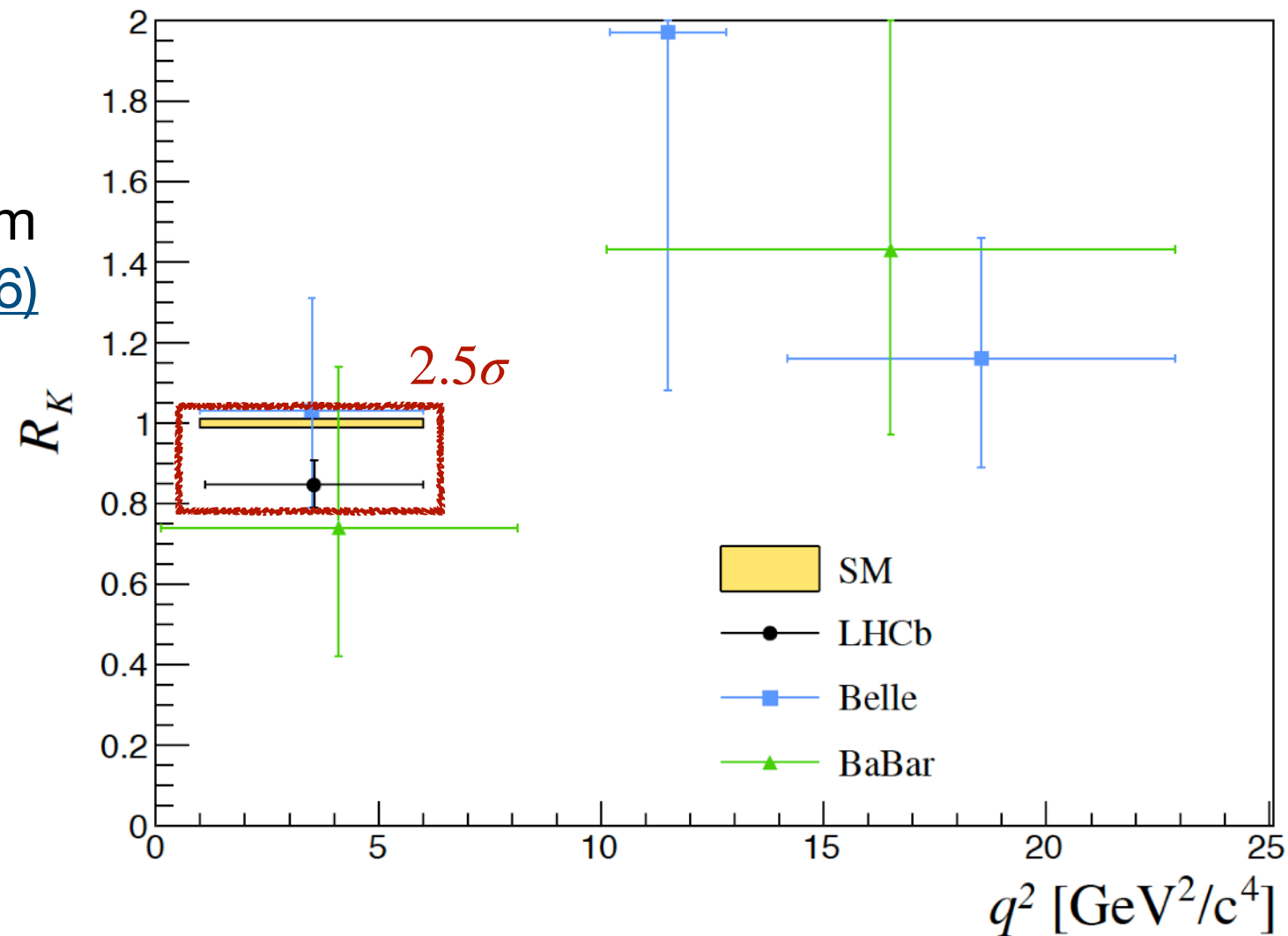
$$N(B^+ \rightarrow K^+ e^+ e^-) = 766 \pm 48$$



$$N(B^+ \rightarrow K^+ \mu^+ \mu^-) = 1943 \pm 49$$

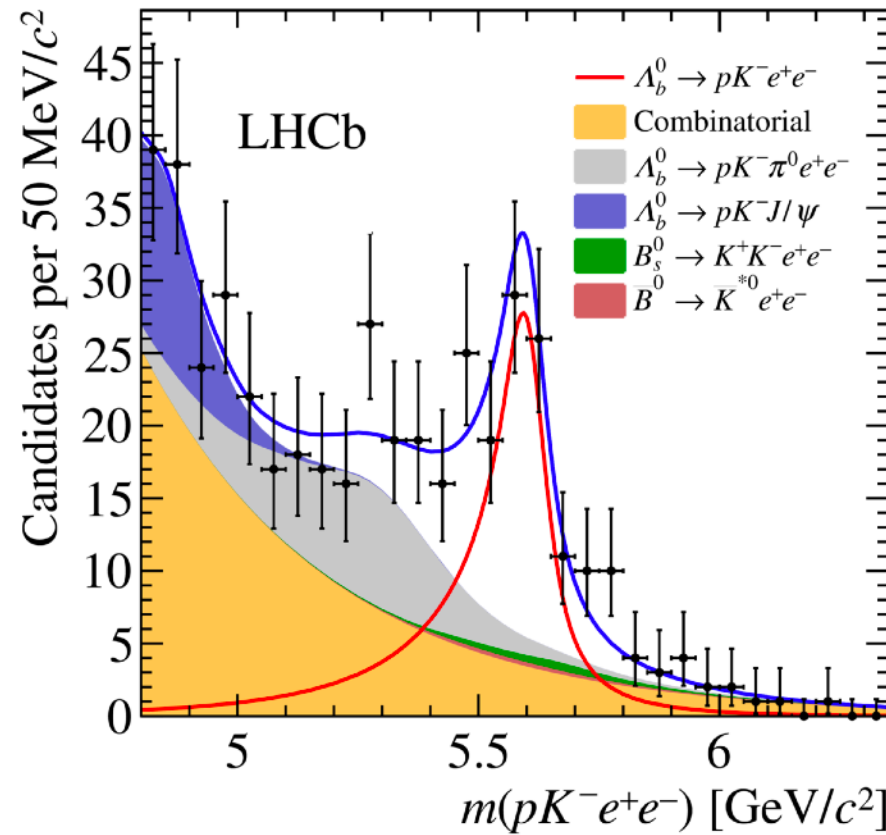
- Measure  $R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)}$  with  $5.0 \text{ fb}^{-1}$  of data.
- $1.1 < q^2 < 6.0 \text{ GeV}^2/c^4$  dilepton invariant mass.
- Cross-checked  $r_{J/\psi} = 0.986 \pm 0.013$ .

SM predictions from  
EPJC 76, 440 (2016)

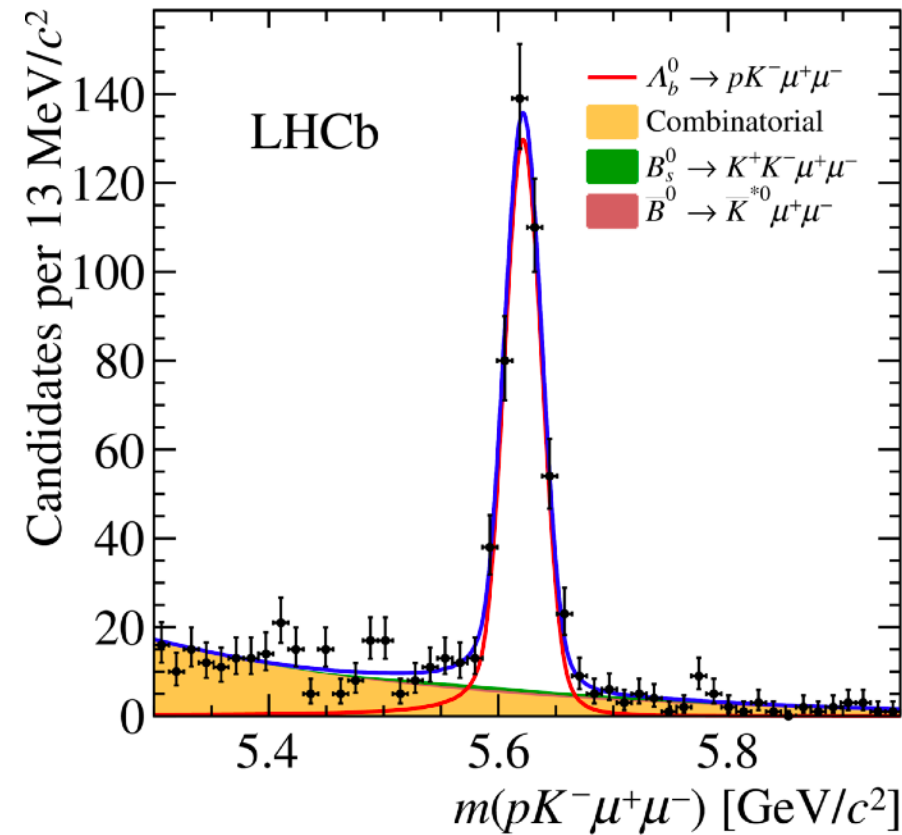


- $R_K = 0.846^{+0.060}_{-0.054} {}^{+0.016}_{-0.014}$  in  $1.1 < q^2 < 6.0 \text{ GeV}^2/c^4$ .
- $2.5\sigma$  tension with SM.

**Point out datapoint, highlight**



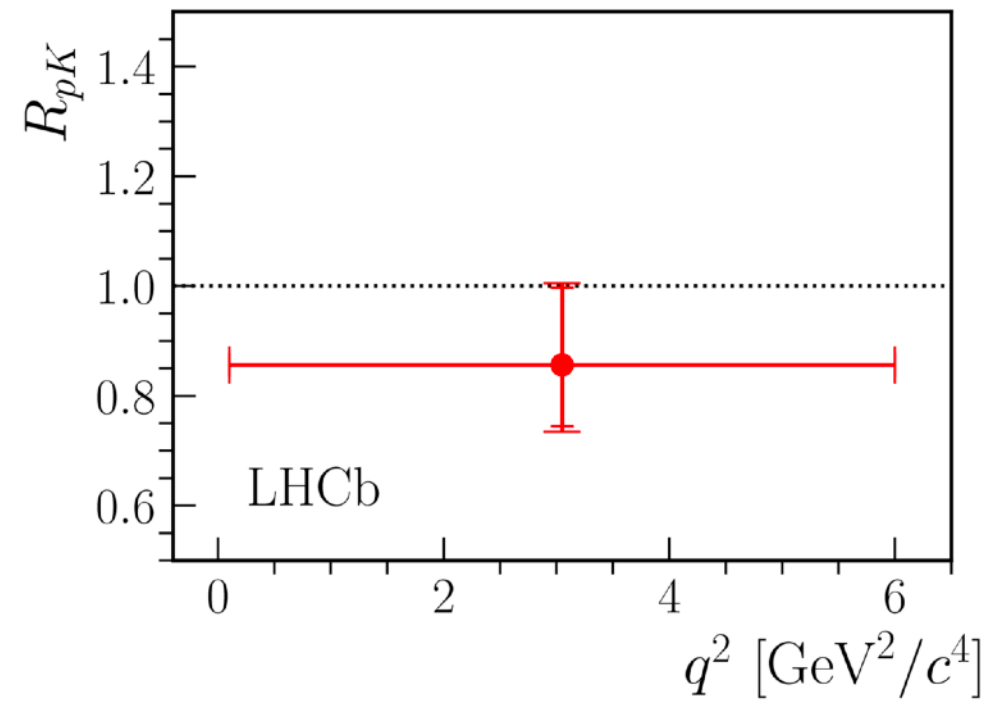
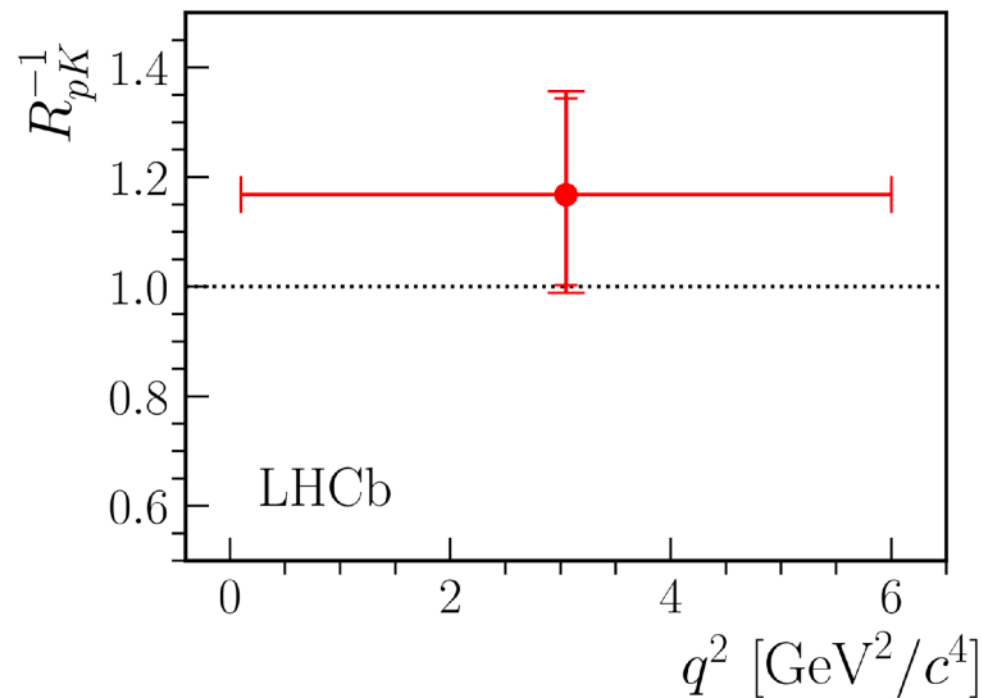
$$N(\Lambda_b \rightarrow pK^-e^+e^-) = 122 \pm 17$$



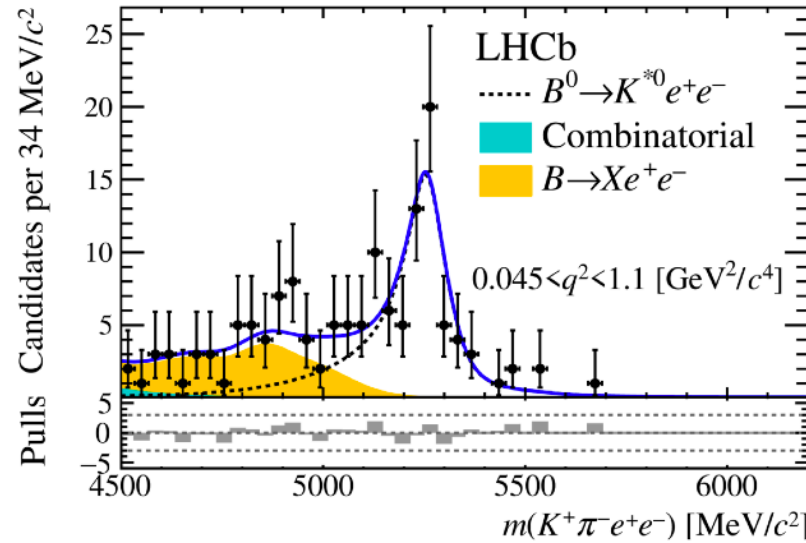
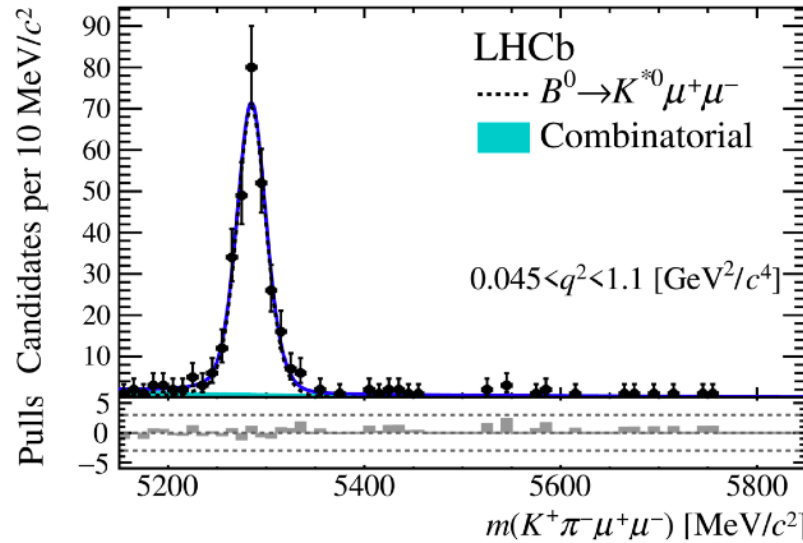
$$N(\Lambda_b \rightarrow pK^-mu^+mu^-) = 444 \pm 23$$

- Measure  $R_{pK}^{-1} = \frac{\mathcal{B}(\Lambda_b \rightarrow pK^-e^+e^-)}{\mathcal{B}(\Lambda_b \rightarrow pK^-mu^+mu^-)}$  inverted ratio with  $4.7 \text{ fb}^{-1}$  of data.
- $0.1 < q^2 < 6.0 \text{ GeV}^2/c^4$  dilepton invariant mass and  $m_{pK^-} < 2600 \text{ MeV}/c^2$ .
- First test of lepton universality in  $b$ -baryons.
- Cross-checked  $r_{J/\psi}^{-1} = 0.96 \pm 0.05$ .





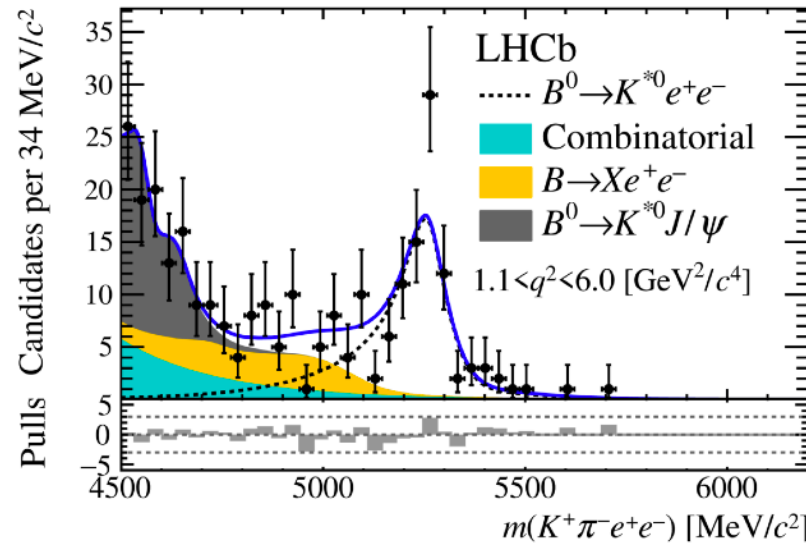
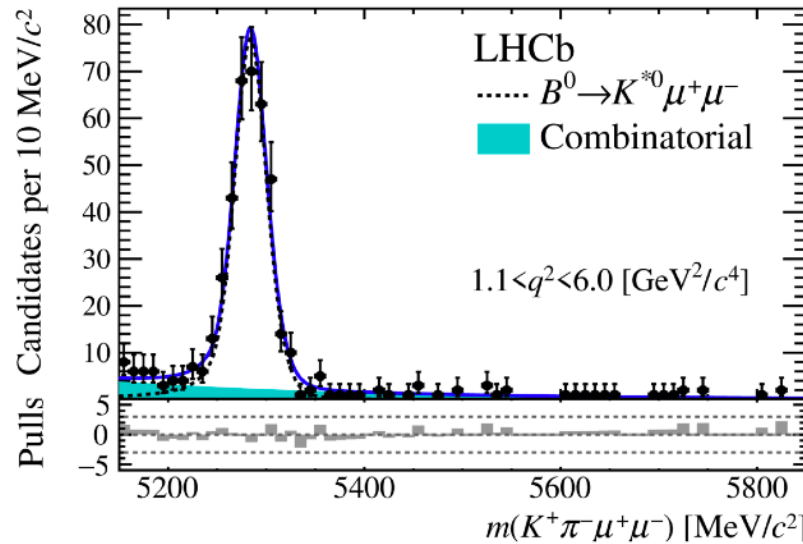
- $R_{pK}^{-1} = 1.17_{-0.16}^{+0.18} \pm 0.07$ , inverts into  $R_{pK} = 0.86_{-0.11}^{+0.14} \pm 0.05$ .
- **First measurement** of  $\mathcal{B}(\Lambda_b \rightarrow pK^- \mu^+ \mu^-)$ .  
Statistical Uncertainty on  $\mathcal{B}(\Lambda_b \rightarrow pK^- J/\psi)$
- $\mathcal{B}(\Lambda_b \rightarrow pK^- \mu^+ \mu^-) |_{0.1 < q^2 < 6.0 \text{ GeV}^2/c^4} = (2.65 \pm \boxed{0.14} \pm \boxed{0.12} \pm \boxed{0.29_{-0.23}^{+0.38}}) \times 10^{-7}$ .  
Systematic
- **First observation** of  $\Lambda_b \rightarrow pK^- e^+ e^-$ .



$$0.045 < q^2 < 1.1 \text{ GeV}^2/c^4$$

$$N(B^0 \rightarrow K^{*0} e^+ e^-) = 89^{+11}_{-10}$$

$$N(B^0 \rightarrow K^{*0} \mu^+ \mu^-) = 285^{+18}_{-18}$$



$$1.1 < q^2 < 6.0 \text{ GeV}^2/c^4$$

$$N(B^0 \rightarrow K^{*0} e^+ e^-) = 111^{+14}_{-13}$$

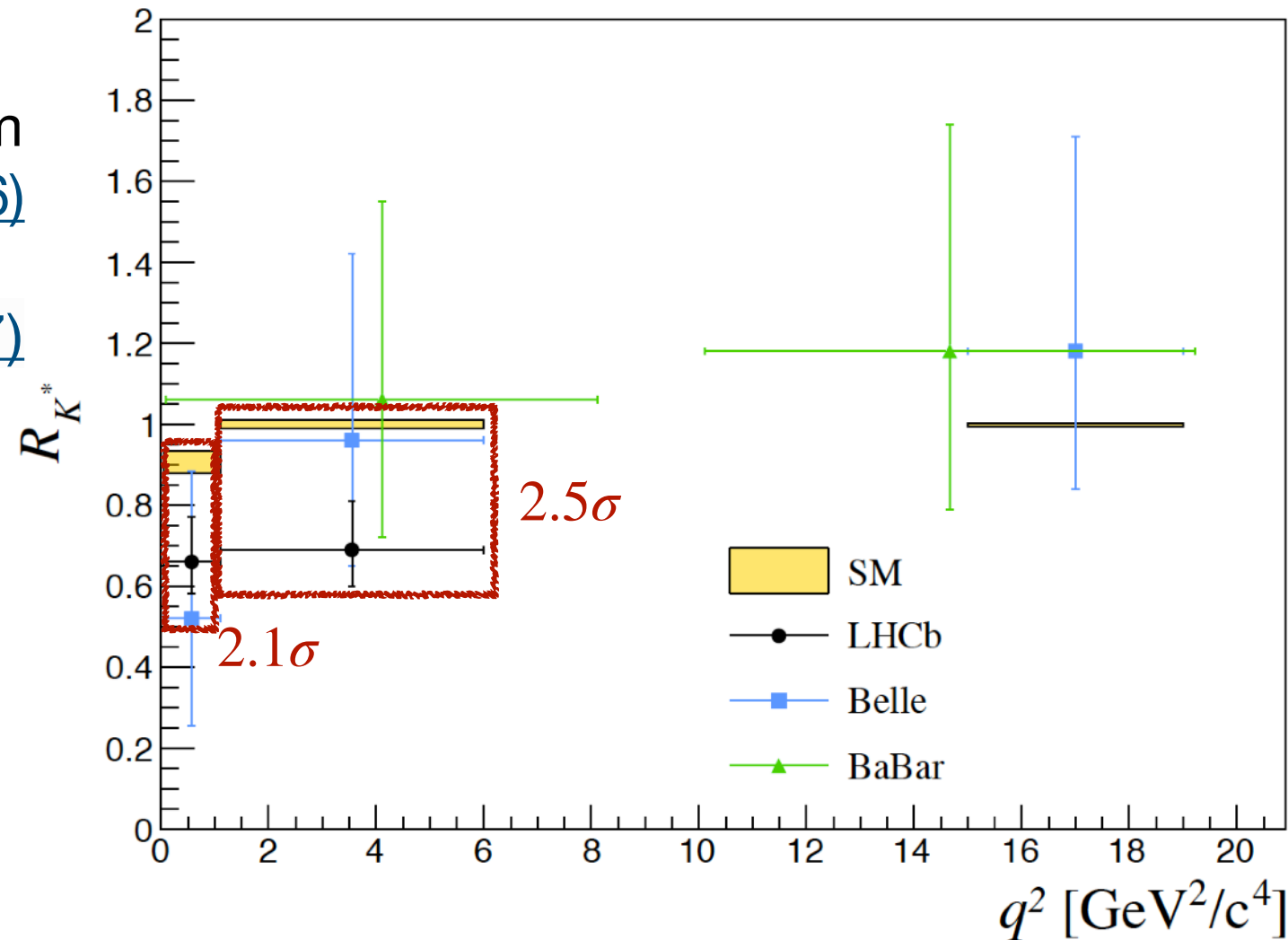
$$N(B^0 \rightarrow K^{*0} \mu^+ \mu^-) = 353^{+21}_{-21}$$

- Measure  $R_{K^{*0}} = \frac{\mathcal{B}(B^0 \rightarrow K^{*0} \mu^+ \mu^-)}{\mathcal{B}(B^0 \rightarrow K^{*0} e^+ e^-)}$  with  $3.0 \text{ fb}^{-1}$  of data.

- $0.045 < q^2 < 1.1 \text{ GeV}^2/c^4$  and  $1.1 < q^2 < 6.0 \text{ GeV}^2/c^4$  dilepton mass bins.

- $r_{J/\psi} = 1.043 \pm 0.006 \pm 0.045$ .

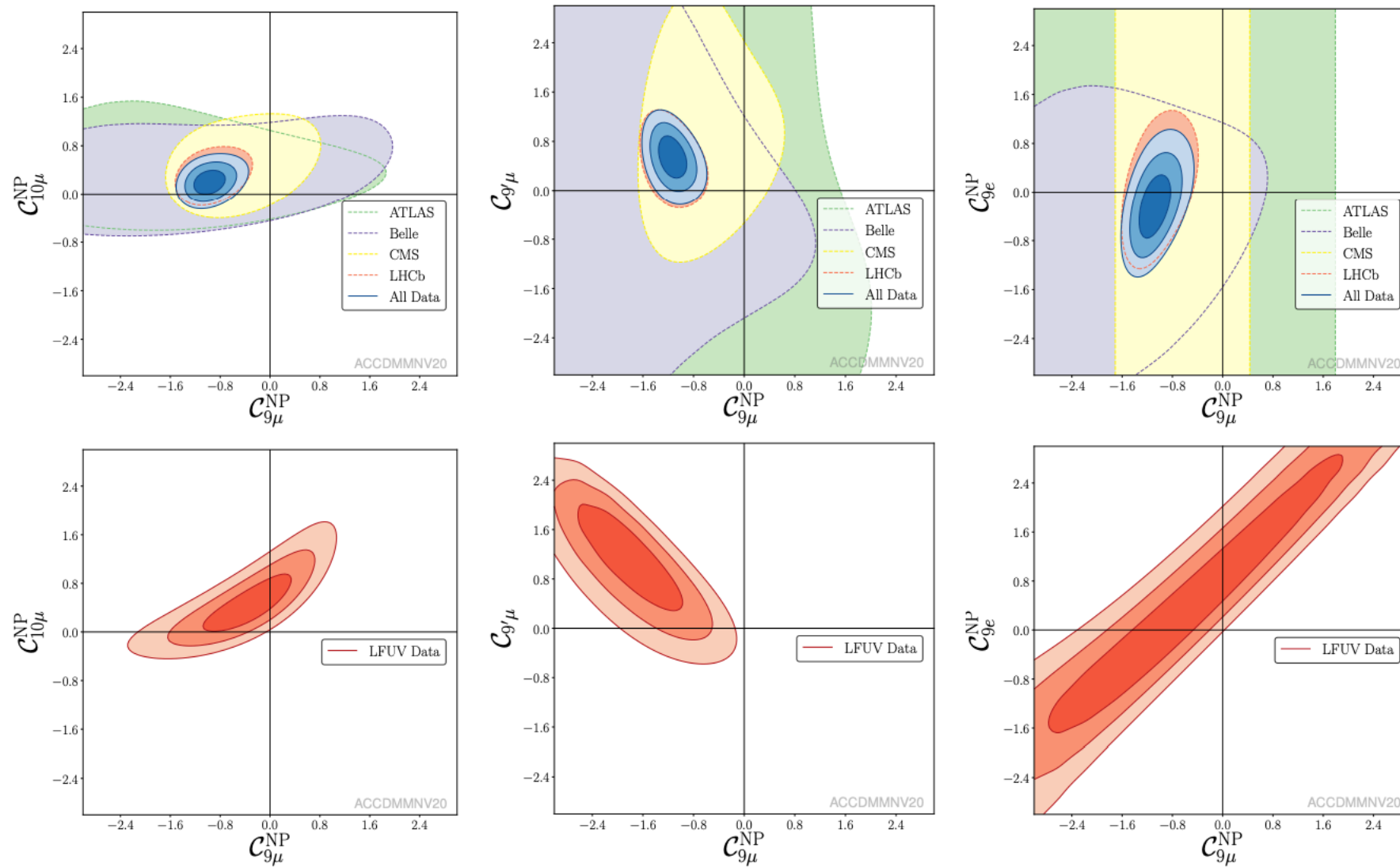
SM predictions from  
[EPJC 76, 440 \(2016\)](#)  
 and  
[EPJC 77, 377 \(2017\)](#)



- $R_{K^{*0}} = \begin{cases} 0.66 \pm_{-0.07}^{+0.11} \text{ (stat)} \pm 0.03 \text{ (syst)} & \text{for } 0.045 < q^2 < 1.1 \text{ GeV}^2 c^4, \\ 0.69 \pm_{-0.07}^{+0.11} \text{ (stat)} \pm 0.05 \text{ (syst)} & \text{for } 1.1 < q^2 < 6.0 \text{ GeV}^2 c^4. \end{cases}$
- Deviation from SM at  $2.1\sigma$  and  $2.5\sigma$  respectively.

# Global Fits

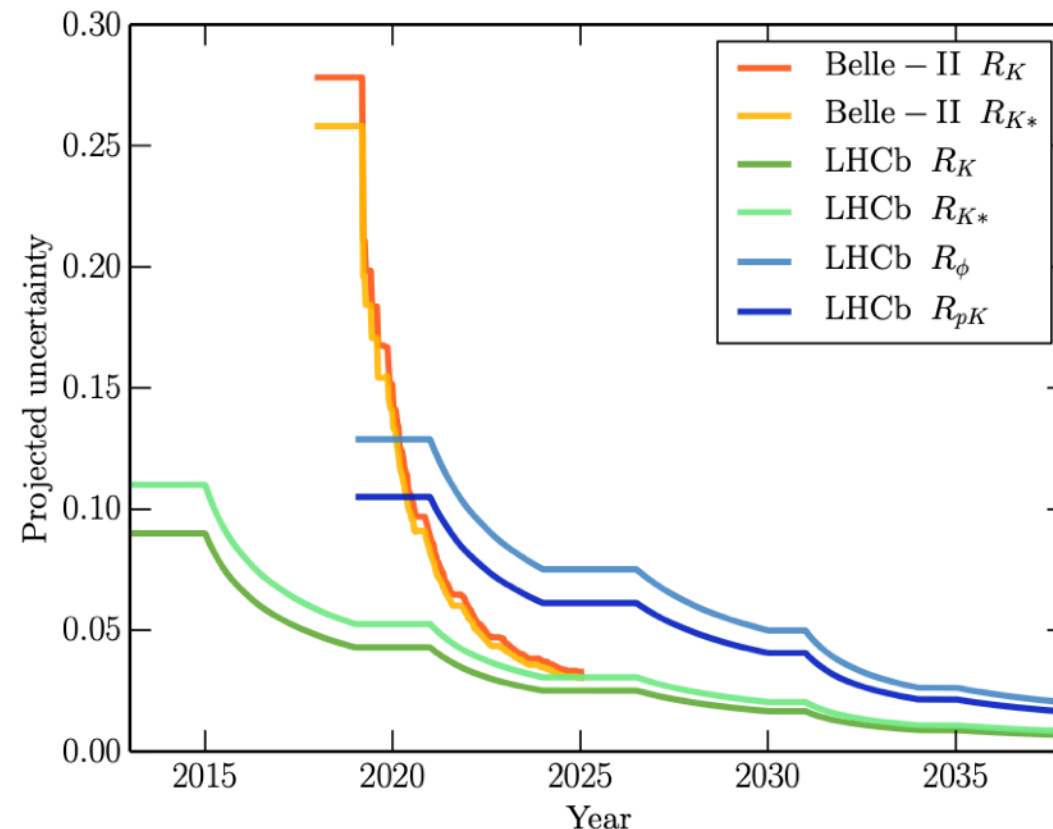
EPJC 79 (2019) 8, 714



- Most recent global fits of  $b \rightarrow sll$  observables to Wilson coefficients.
  - Top: global fits to 'All'  $b \rightarrow sll$  observables.
  - Bottom: global fits to lepton flavour universality measurements.
- 'All' deviates from SM at  $6.0 - 6.5\sigma$ , 'LFU' deviates from SM at  $2.9 - 3.5\sigma$ .
- Consistent patterns between 'All' and 'LFU' fits.

# Summary and Prospects

Projected uncertainty of Belle 2 and LHCb lepton flavour universality measurements.



[arXiv:1809.06229](https://arxiv.org/abs/1809.06229)

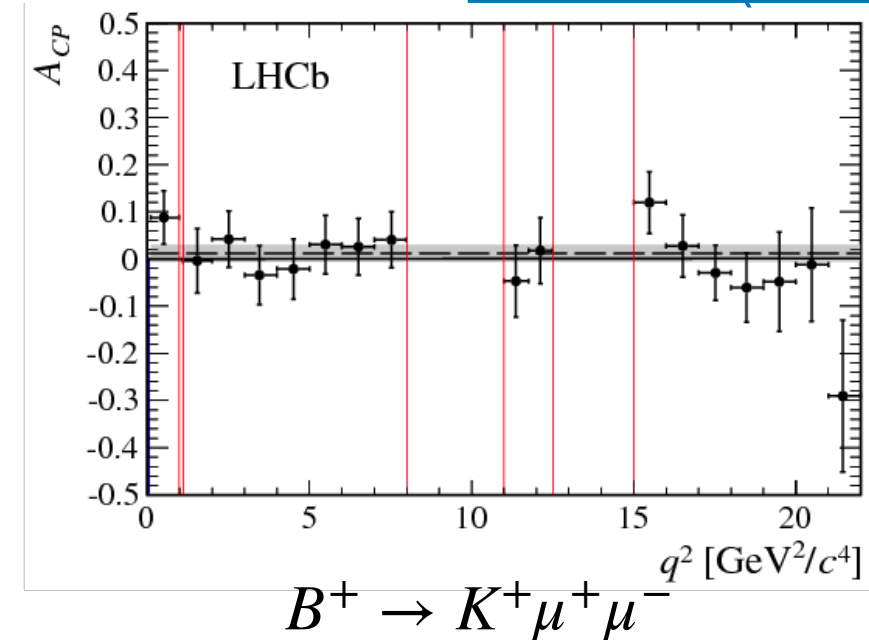
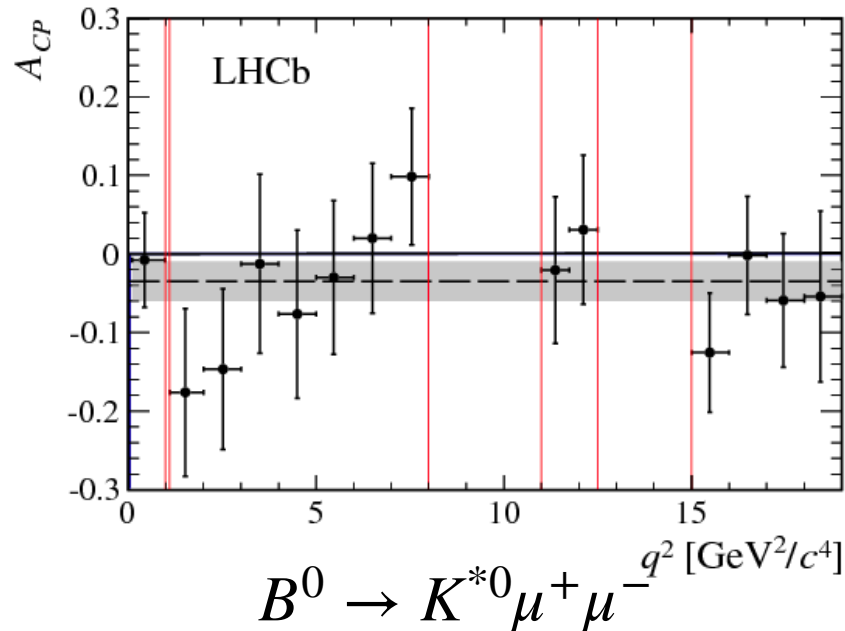
- Measurements:
  - ▶  $P'_5$  measured in  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  angular analysis in tension with SM.
  - ▶ Lepton flavour universality measurements deviate from SM in the same direction.
- Prospects:
  - ▶ Angular analysis of  $P'_5$  and  $R_K$  with another  $4 \text{ fb}^{-1}$  of data. ( $1.45 \times$  published)
  - ▶ Updated  $R_{K^{*0}}$  with full  $9 \text{ fb}^{-1}$  dataset. ( $3 \times$  published)
  - ▶  $R_\phi$  analysis in the works.

# Backup



# CP asymmetry in $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ and $B^+ \rightarrow K^+ \mu^+ \mu^-$

[JHEP 09 \(2014\) 177](#)



- Measure

$$\mathcal{A}_{CP} = \frac{\Gamma(\bar{B} \rightarrow \bar{K}^{(*)} \mu^+ \mu^-) - \Gamma(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\Gamma(\bar{B} \rightarrow \bar{K}^{(*)} \mu^+ \mu^-) + \Gamma(B \rightarrow K^{(*)} \mu^+ \mu^-)}$$

Hadronic form factors cancel

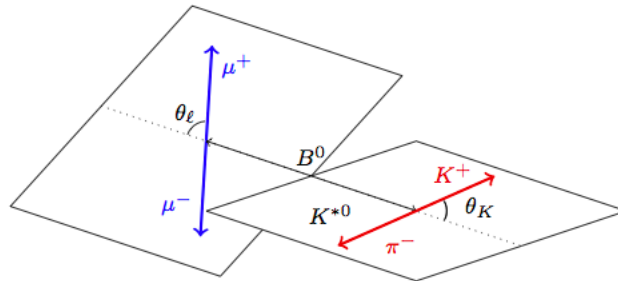
- Results agree with SM:

$$\mathcal{A}_{CP}(B^0 \rightarrow K^{*0} \mu^+ \mu^-) = -0.035 \pm 0.024 \pm 0.003$$

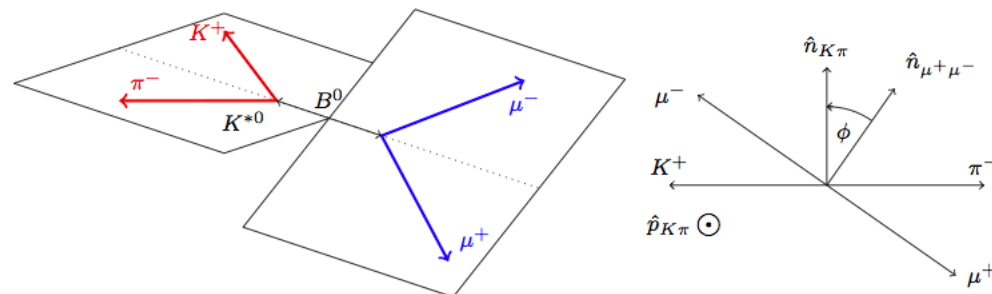
$$\mathcal{A}_{CP}(B^+ \rightarrow K^+ \mu^+ \mu^-) = 0.012 \pm 0.017 \pm 0.001$$

- NP contribution to  $b \rightarrow sl^+l^-$  has no CP violation or it is negligibly small.
- EFT assumes CP symmetry.

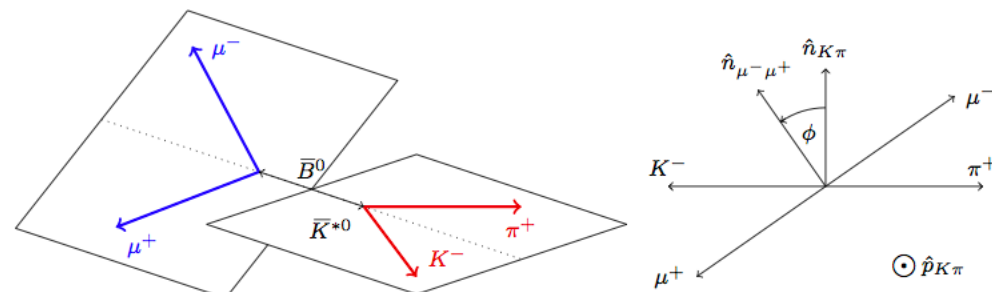
# $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ Angular Analysis PDF



(a)  $\theta_K$  and  $\theta_l$  definitions for the  $B^0$  decay



(b)  $\phi$  definition for the  $B^0$  decay

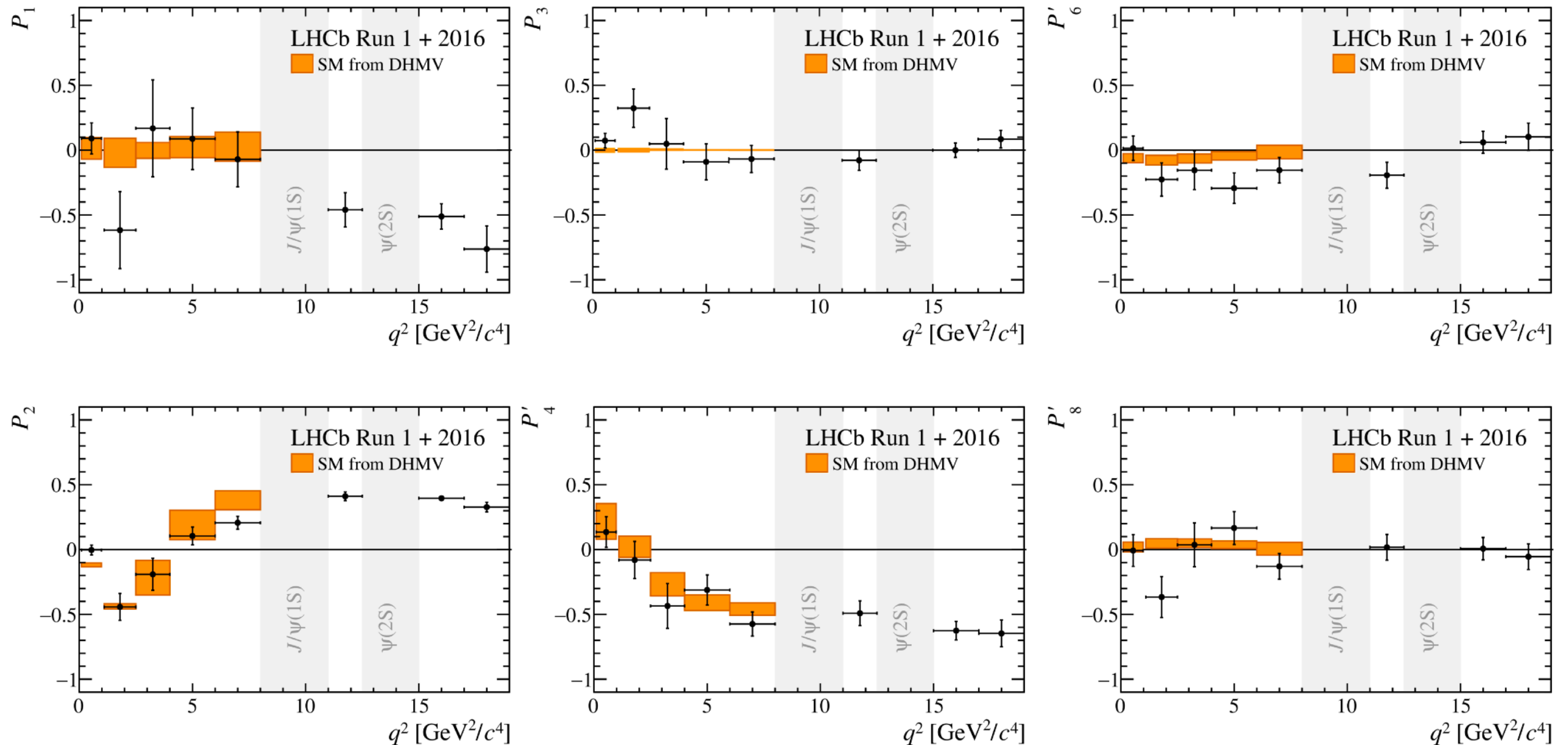


(c)  $\phi$  definition for the  $\bar{B}^0$  decay

$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^4(\Gamma + \bar{\Gamma})}{dq^2 d\vec{\Omega}}$$

$$= \frac{9}{32\pi} \left[ \begin{aligned} & \frac{3}{4}(1 - F_L)\sin^2 \theta_K + F_L \cos^2 \theta_K \\ & + \frac{1}{4}(1 - F_L)\sin^2 \theta_K \cos 2\theta_l - F_L \cos^2 \theta_K \cos 2\theta_l \\ & + S_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_l \cos \phi \\ & + S_5 \sin 2\theta_K \sin \theta_l \cos \phi + \frac{4}{3}A_{FB} \sin^2 \theta_K \cos \theta_l \\ & + S_7 \sin 2\theta_K \sin \theta_l \sin \phi + S_8 \sin 2\theta_K \sin 2\theta_l \sin \phi \\ & + S_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi \end{aligned} \right].$$

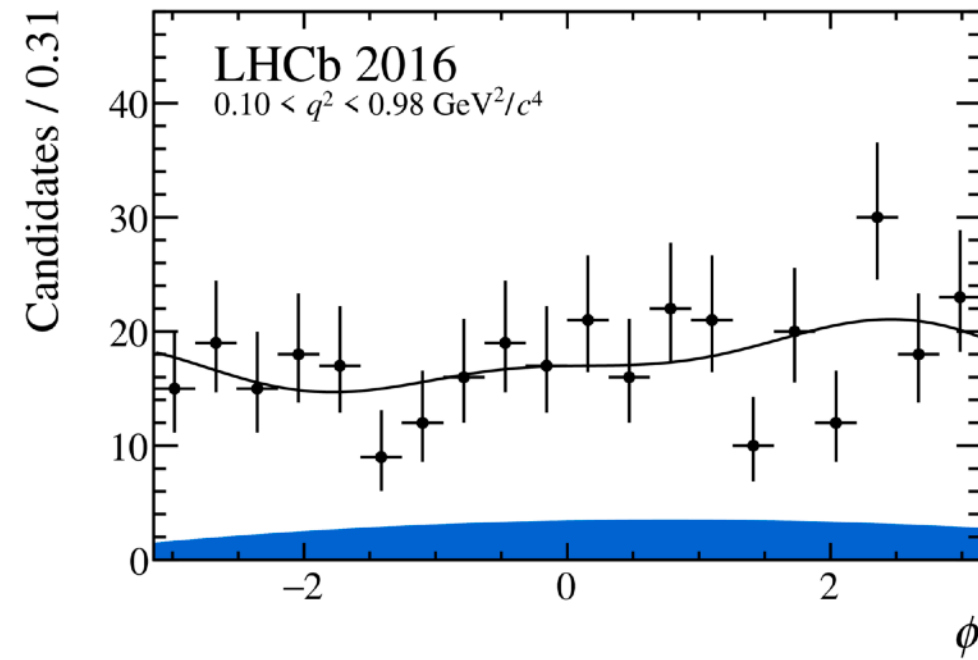
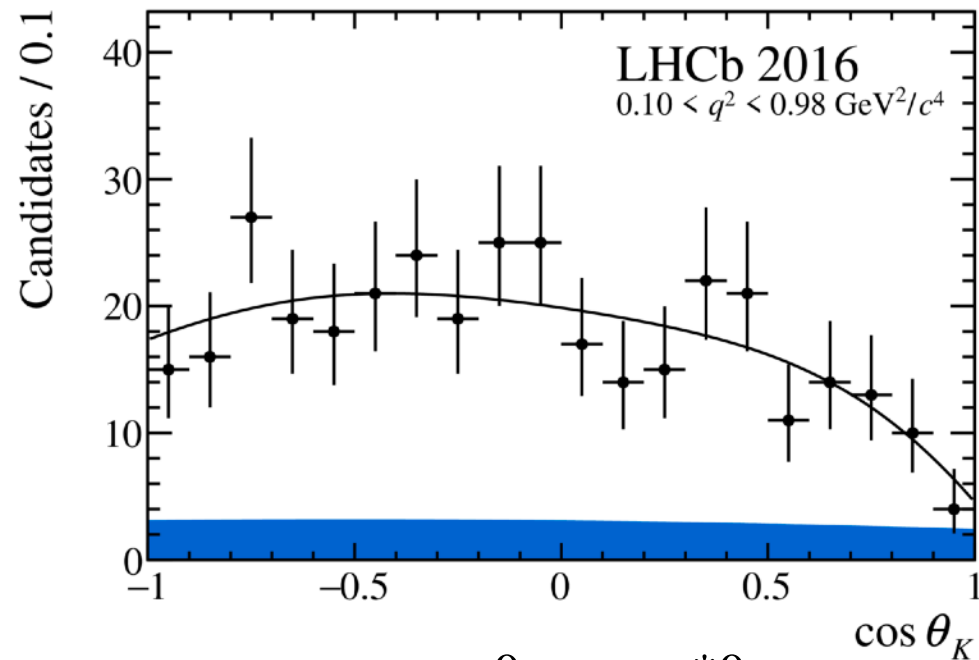
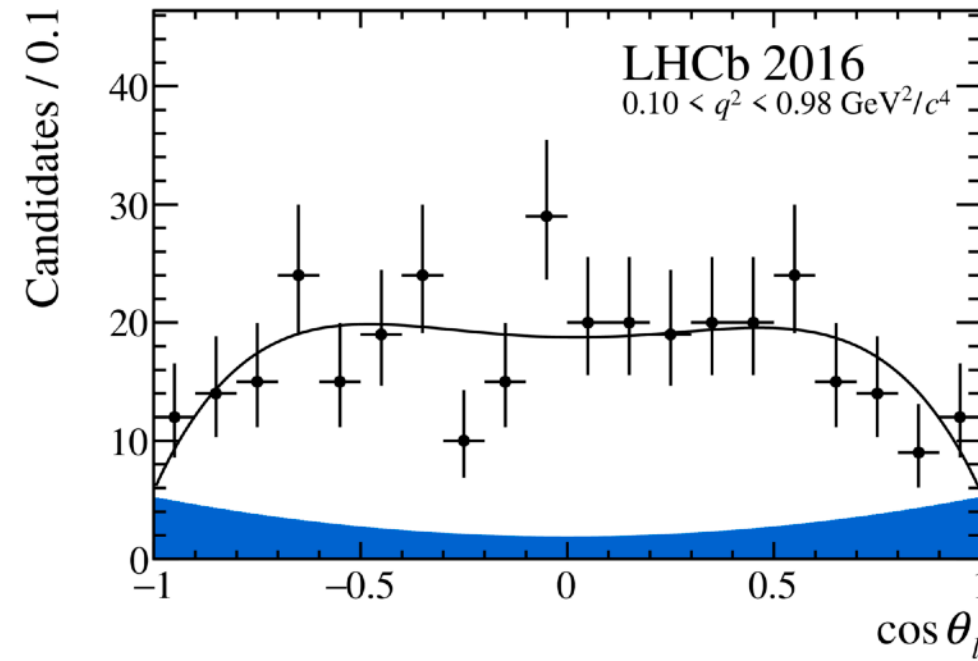
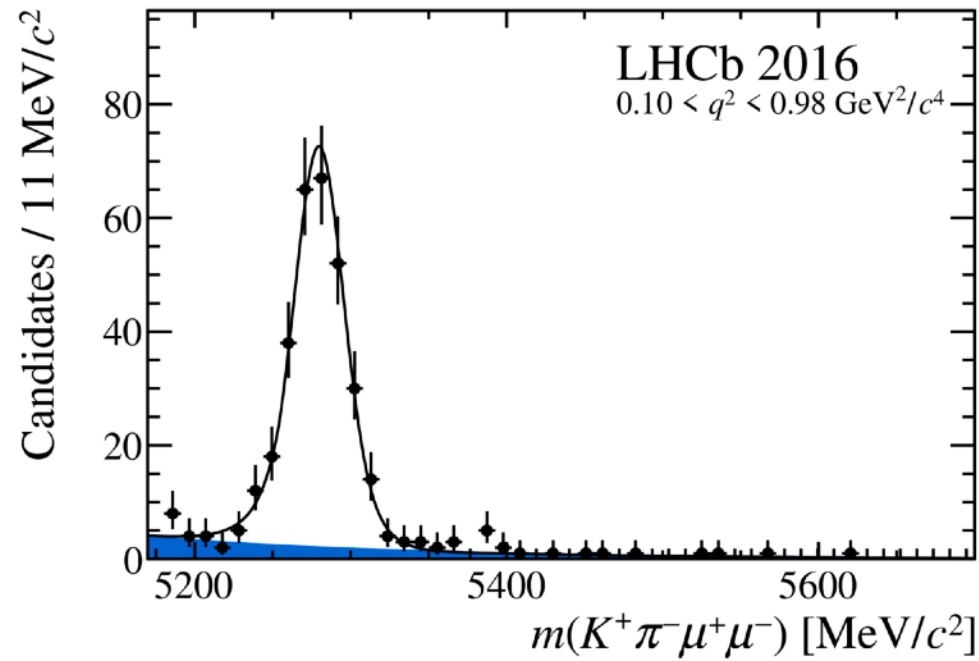
# Angular Analysis of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ : $P'_i$



Other observables in optimised basis agree with SM

# Angular Analysis of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

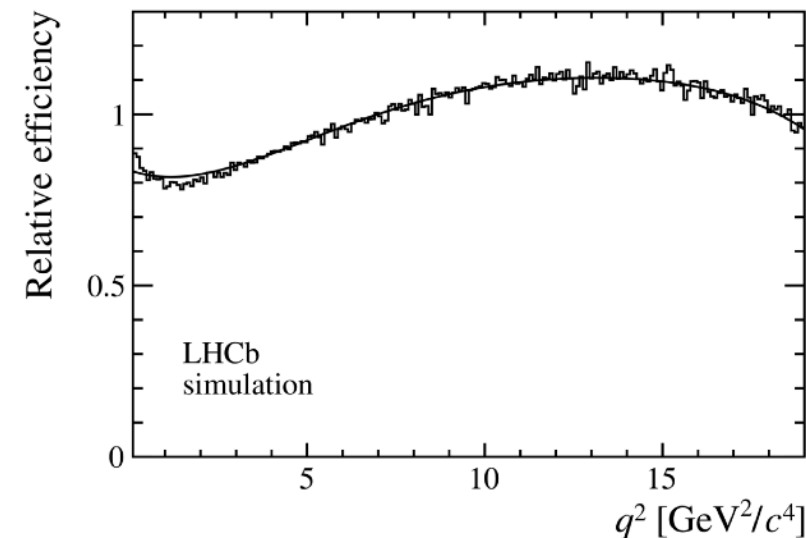
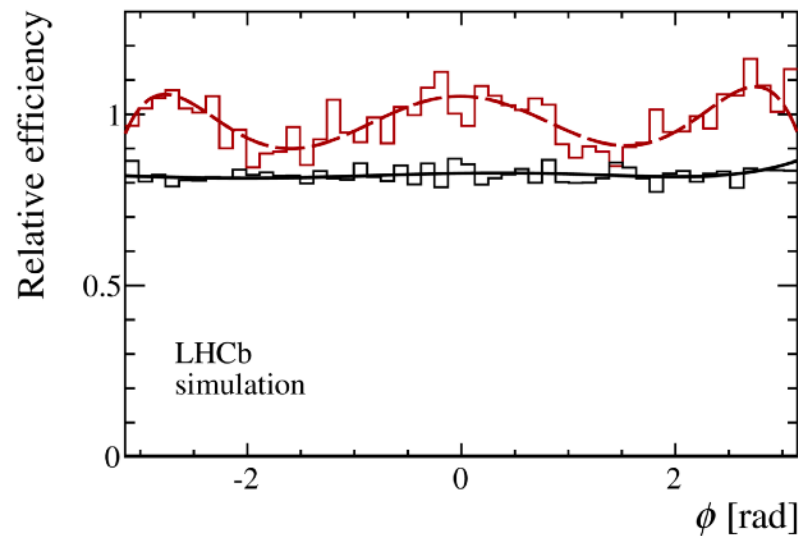
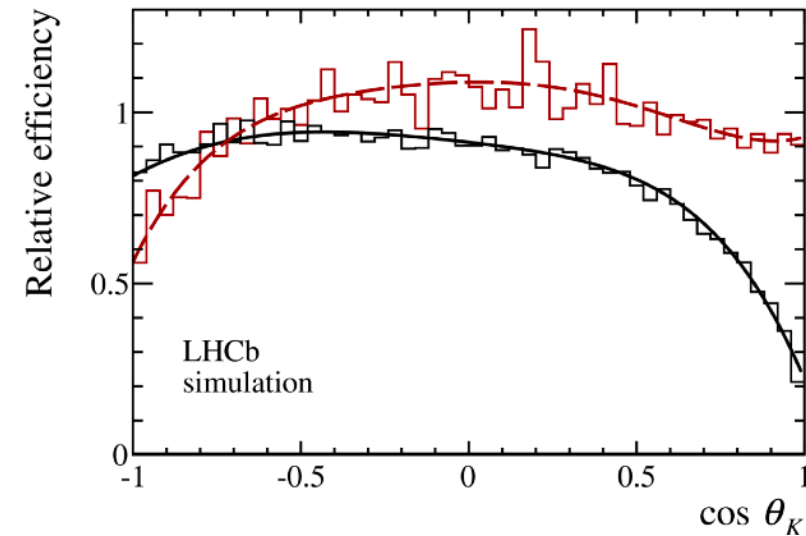
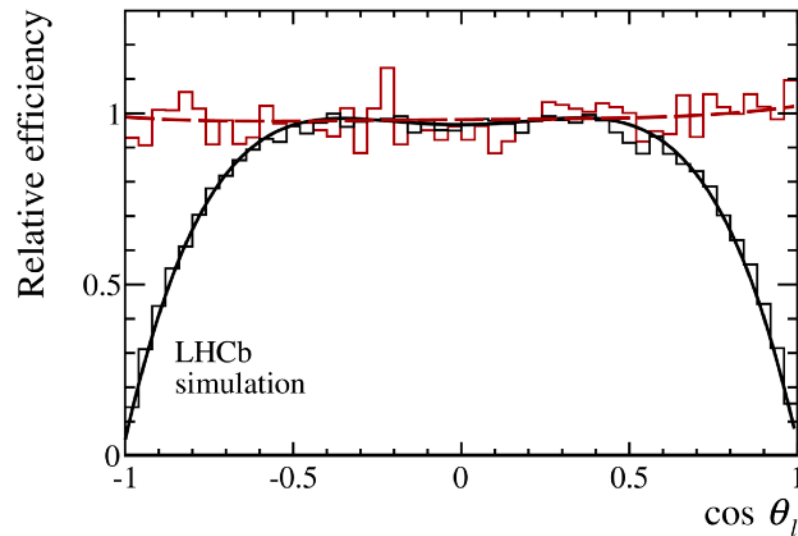
[PRL 125, 011802 \(2020\)](#)



Fitted  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  distribution in the angular analysis.

# Angular Analysis Efficiency

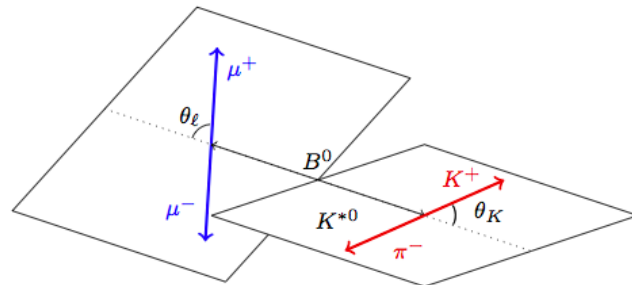
JHEP 02 (2016) 104



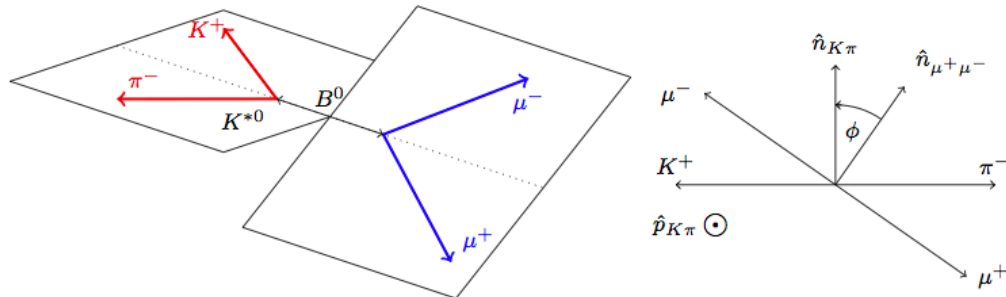
- Efficiencies of  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  in
  - $0.1 < q^2 < 0.98 \text{ GeV}^2/c^4$  (black line)
  - $18 < q^2 < 19 \text{ GeV}^2/c^4$  (red dashed)
- The efficiency as a function of  $q^2$  is integrated over the angles.

# $B^0 \rightarrow K^{*0} e^+ e^-$ Angular Analysis PDF

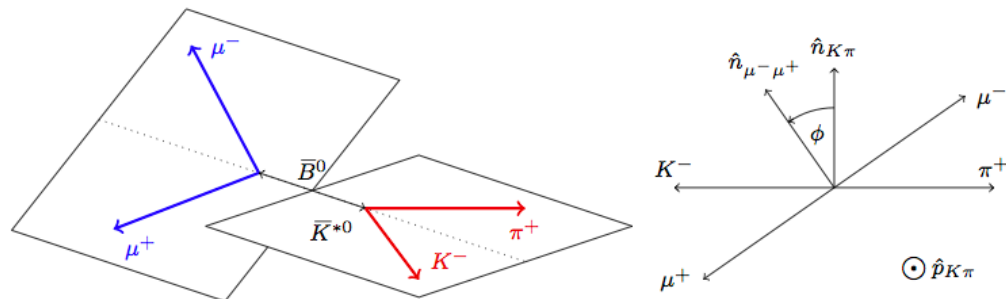
Same angle definition as  
 $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  but  $\tilde{\phi} \mapsto \phi + \pi$



(a)  $\theta_K$  and  $\theta_l$  definitions for the  $B^0$  decay



(b)  $\phi$  definition for the  $B^0$  decay



(c)  $\phi$  definition for the  $\bar{B}^0$  decay

$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^4(\Gamma + \bar{\Gamma})}{dq^2 d\vec{\Omega}}$$

$$= \frac{9}{16\pi} \left[ \begin{aligned} & \frac{3}{4}(1 - F_L)\sin^2 \theta_K + F_L \cos^2 \theta_K \\ & + \frac{1}{4}(1 - F_L)\sin^2 \theta_K \cos 2\theta_l - F_L \cos^2 \theta_K \cos 2\theta_l \\ & + (1 - F_L)A_T^{Re} \sin^2 \theta_K \cos \theta_l \\ & + (1 - F_L)A_T^{(2)} \sin^2 \theta_K \sin^2 \theta_l \cos 2\tilde{\phi} \\ & + (1 - F_L)A_T^{Im} \sin^2 \theta_K \sin^2 \theta_l \cos 2\tilde{\phi} \end{aligned} \right].$$



# $B^0 \rightarrow K^{*0} e^+ e^-$ angular observables

- SM predictions

$$F_L(\text{SM}) = 0.051 \pm 0.013, \quad A_T^{\text{Re}}(\text{SM}) = -0.0001 \pm 0.0004, \\ A_T^{(2)}(\text{SM}) = 0.033 \pm 0.020, \quad A_T^{\text{Im}}(\text{SM}) = -0.00012 \pm 0.00034.$$

- Relation to photon polarisation:

- $A_{R(L)} = |A_{R(L)}| e^{i\phi_{R(L)}}, \tan \chi = |A_R/A_L|$
- $A_T^{(2)} \simeq \sin(2\chi) \cos(\phi_L - \phi_R)$
- $A_T^{\text{Im}} \simeq \sin(2\chi) \sin(\phi_L - \phi_R)$

# Relation to Wilson Coefficients

$$F_L = \frac{|A_0|^2}{|A_0|^2 + |A_{\parallel}|^2 + |A_{\perp}|^2}$$

$$A_T^{(2)} = \frac{|A_{\perp}|^2 - |A_{\parallel}|^2}{|A_{\perp}|^2 + |A_{\parallel}|^2}$$

$$A_T^{Re} = \frac{2\mathcal{R}e \left( A_{\parallel}^L A_{\perp}^{*L} + A_{\parallel}^R A_{\perp}^{*R} \right)}{|A_{\parallel}|^2 + |A_{\perp}|^2}$$

$$A_T^{Im} = \frac{2\mathcal{I}m \left( A_{\parallel}^L A_{\perp}^{*L} + A_{\parallel}^R A_{\perp}^{*R} \right)}{|A_{\parallel}|^2 + |A_{\perp}|^2}$$

# Relation to Wilson Coefficients

$$A_{\perp L,R} = \sqrt{2} N m_B (1 - \hat{s}) \left[ (C_9^{\text{eff}} \mp C_{10}) + \frac{2\hat{m}_b}{\hat{s}} (C_7^{\text{eff}} + C_7^{\text{eff}'}) \right] \xi_{\perp}(E_{K^*}),$$

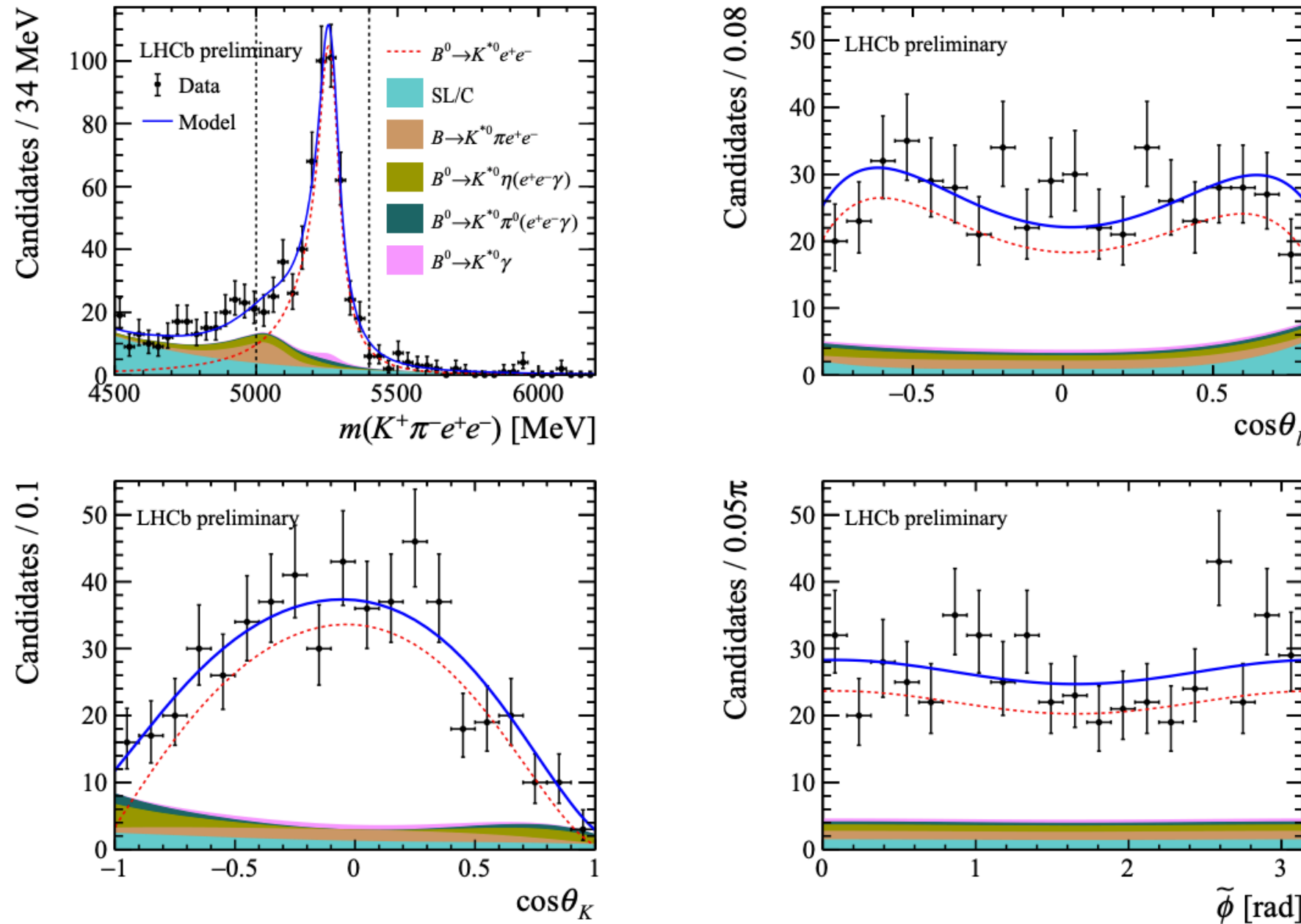
$$A_{\parallel L,R} = -\sqrt{2} N m_B (1 - \hat{s}) \left[ (C_9^{\text{eff}} \mp C_{10}) + \frac{2\hat{m}_b}{\hat{s}} (C_7^{\text{eff}} - C_7^{\text{eff}'}) \right] \xi_{\perp}(E_{K^*}),$$

$$A_{0L,R} = -\frac{N m_B}{2\hat{m}_{K^*} \sqrt{\hat{s}}} (1 - \hat{s})^2 \left[ (C_9^{\text{eff}} \mp C_{10}) + 2\hat{m}_b (C_7^{\text{eff}} - C_7^{\text{eff}'}) \right] \xi_{\parallel}(E_{K^*}),$$

$$A_t = \frac{N m_B}{\hat{m}_{K^*} \sqrt{\hat{s}}} (1 - \hat{s})^2 C_{10} \xi_{\parallel}(E_{K^*}),$$

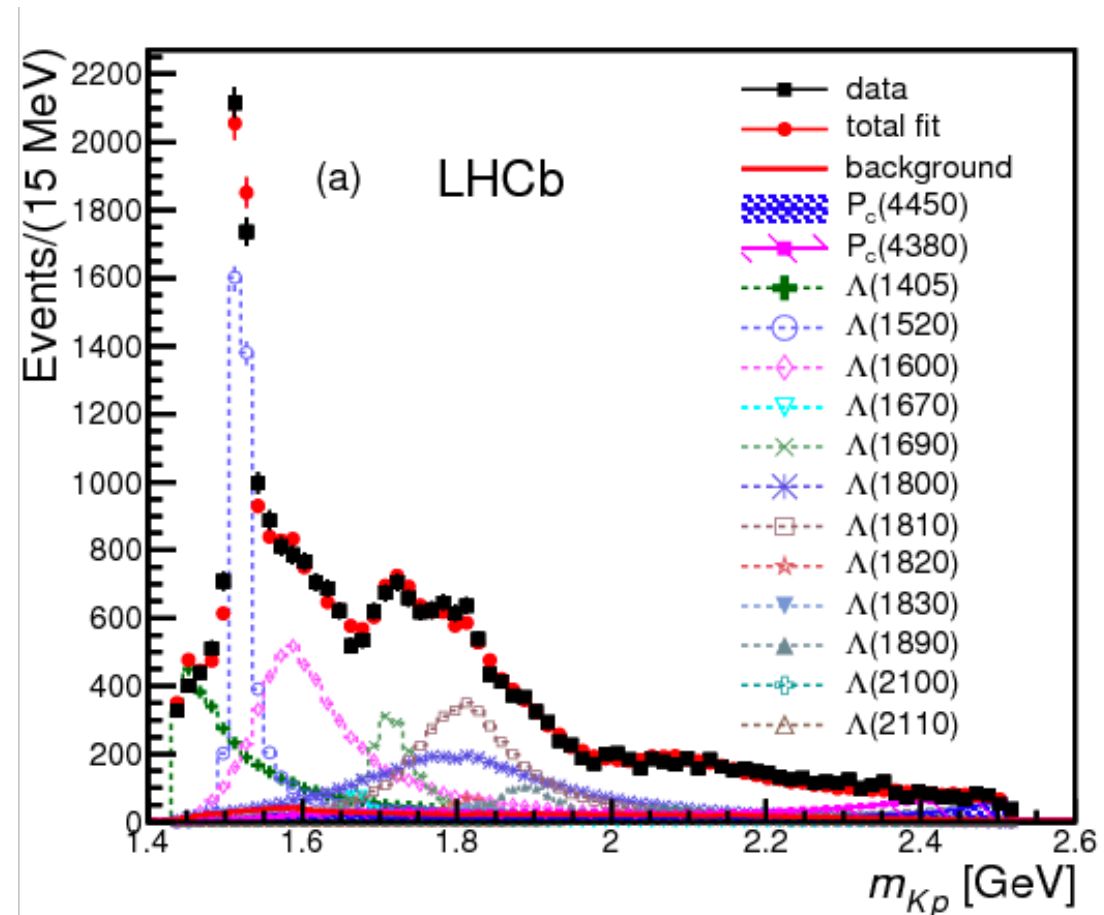
In the low  $q^2$  regime,  $\xi$  hadronic form factor. [PRD 71.094009](#)

# Angular Analysis of $B^0 \rightarrow K^{*0} e^+ e^-$



- Compared to  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  analysis,  $B^0 \rightarrow K^{*0} e^+ e^-$  invariant mass spectrum is significantly smeared and the background contamination is higher.
- Some of these background,  $B^0 \rightarrow K^{*0} \gamma$  for instance, are due to the  $q^2$  bin range.

# $m_{pK}$ Spectrum Re-weighting



[PRL 115, 072001 \(2015\)](#)

- Hadronic  $pK$  rich in structures.
- Weight  $m_{pK}$  according to measurements by  $\Lambda_b \rightarrow pKJ/\psi$  amplitude analysis

# Hardware Trigger Threshold

|                               | $p_T$ or $E_T$           |                          | SPD           |
|-------------------------------|--------------------------|--------------------------|---------------|
|                               | 2011                     | 2012                     | 2011 and 2012 |
| single muon                   | 1.48 GeV/ $c$            | 1.76 GeV/ $c$            | 600           |
| dimuon $p_{T1} \times p_{T2}$ | $(1.30 \text{ GeV}/c)^2$ | $(1.60 \text{ GeV}/c)^2$ | 900           |
| hadron                        | 3.50 GeV                 | 3.70 GeV                 | 600           |
| electron                      | 2.50 GeV                 | 3.00 GeV                 | 600           |
| photon                        | 2.50 GeV                 | 3.00 GeV                 | 600           |

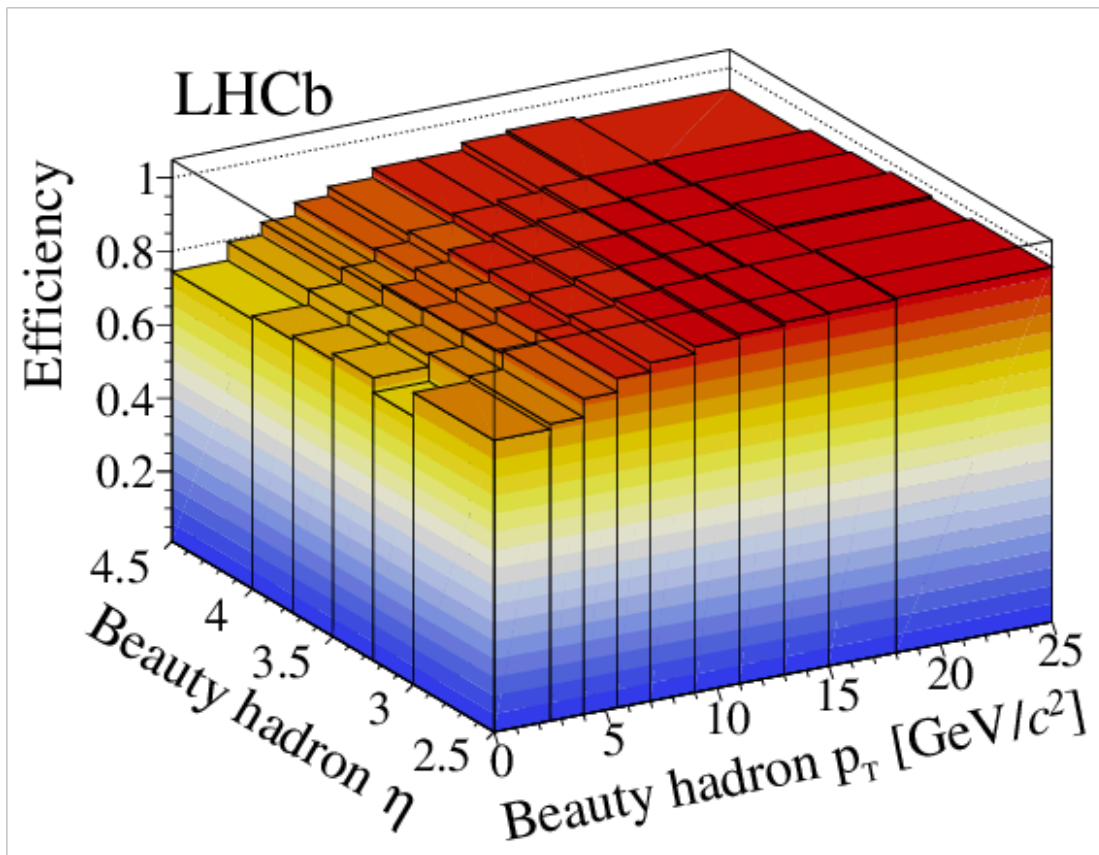
[Int. J. Mod. Phys. A 30, 1530022 \(2015\)](#)

| L0 trigger      | $E_T/p_T$ threshold    |                        |                        | SPD threshold |
|-----------------|------------------------|------------------------|------------------------|---------------|
|                 | 2015                   | 2016                   | 2017                   |               |
| Hadron          | $> 3.6 \text{ GeV}$    | $> 3.7 \text{ GeV}$    | $> 3.46 \text{ GeV}$   | $< 450$       |
| Photon          | $> 2.7 \text{ GeV}$    | $> 2.78 \text{ GeV}$   | $> 2.47 \text{ GeV}$   | $< 450$       |
| Electron        | $> 2.7 \text{ GeV}$    | $> 2.4 \text{ GeV}$    | $> 2.11 \text{ GeV}$   | $< 450$       |
| Muon            | $> 2.8 \text{ GeV}$    | $> 1.8 \text{ GeV}$    | $> 1.35 \text{ GeV}$   | $< 450$       |
| Muon high $p_T$ | $> 6.0 \text{ GeV}$    | $> 6.0 \text{ GeV}$    | $> 6.0 \text{ GeV}$    | none          |
| Dimuon          | $> 1.69 \text{ GeV}^2$ | $> 2.25 \text{ GeV}^2$ | $> 1.69 \text{ GeV}^2$ | $< 900$       |

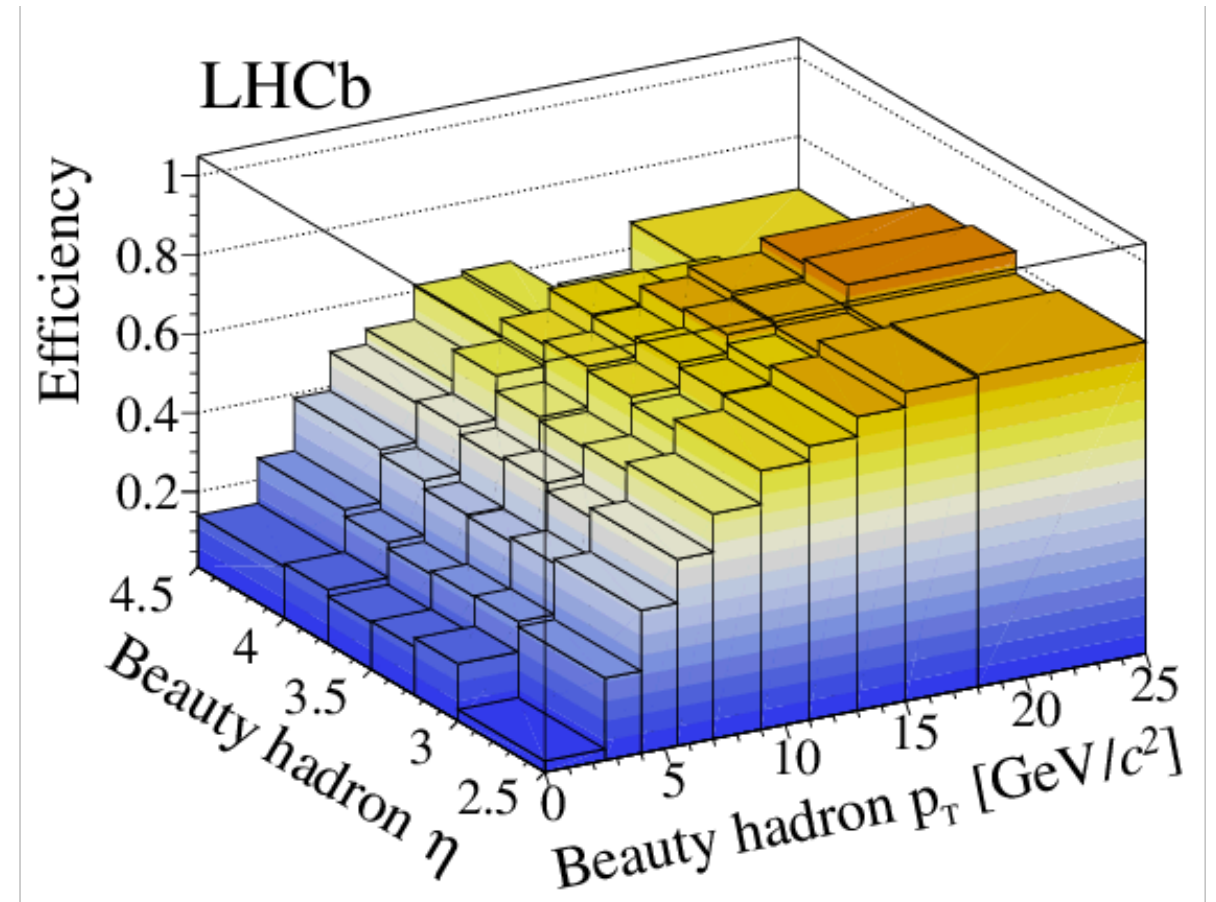
[JINST 14 \(2019\) P04013](#)



# Electron vs Muon L0 Efficiency



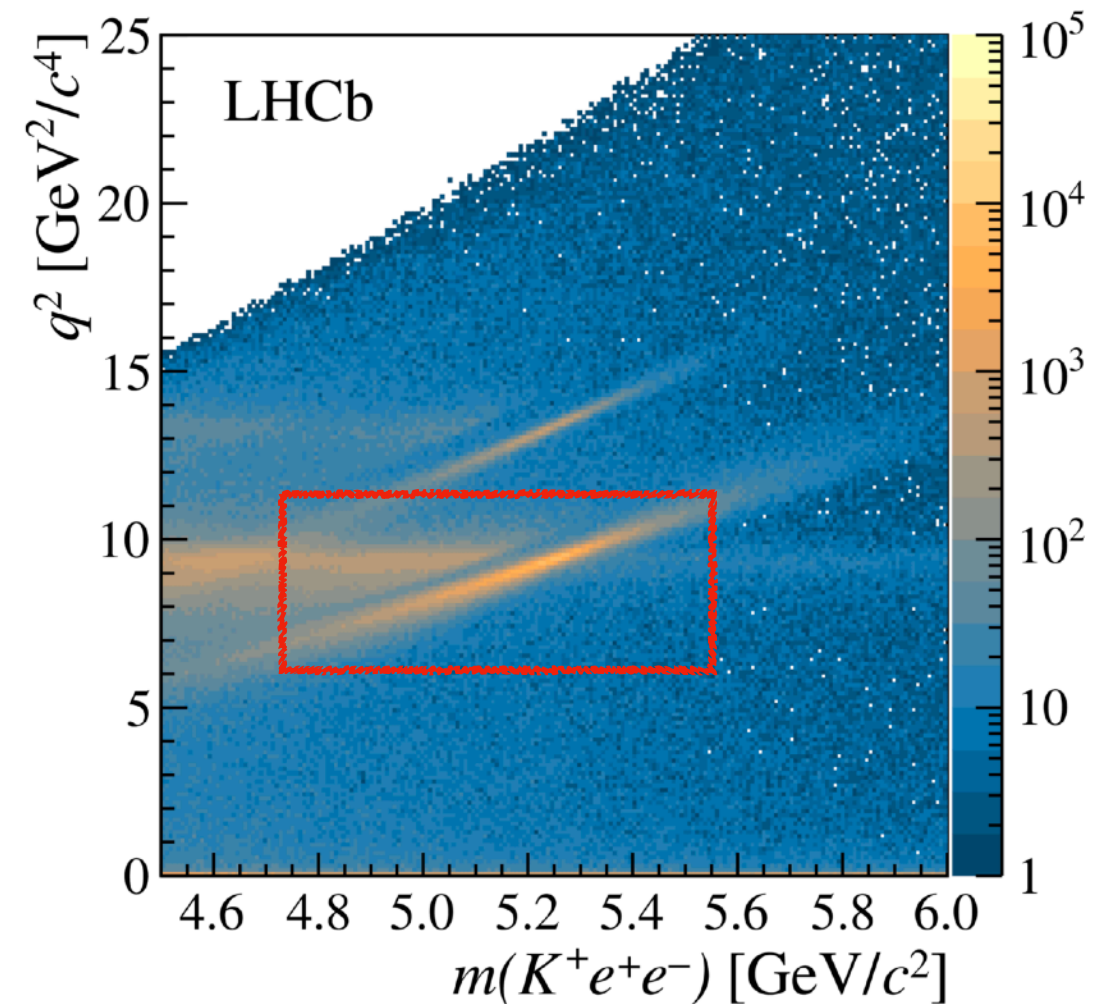
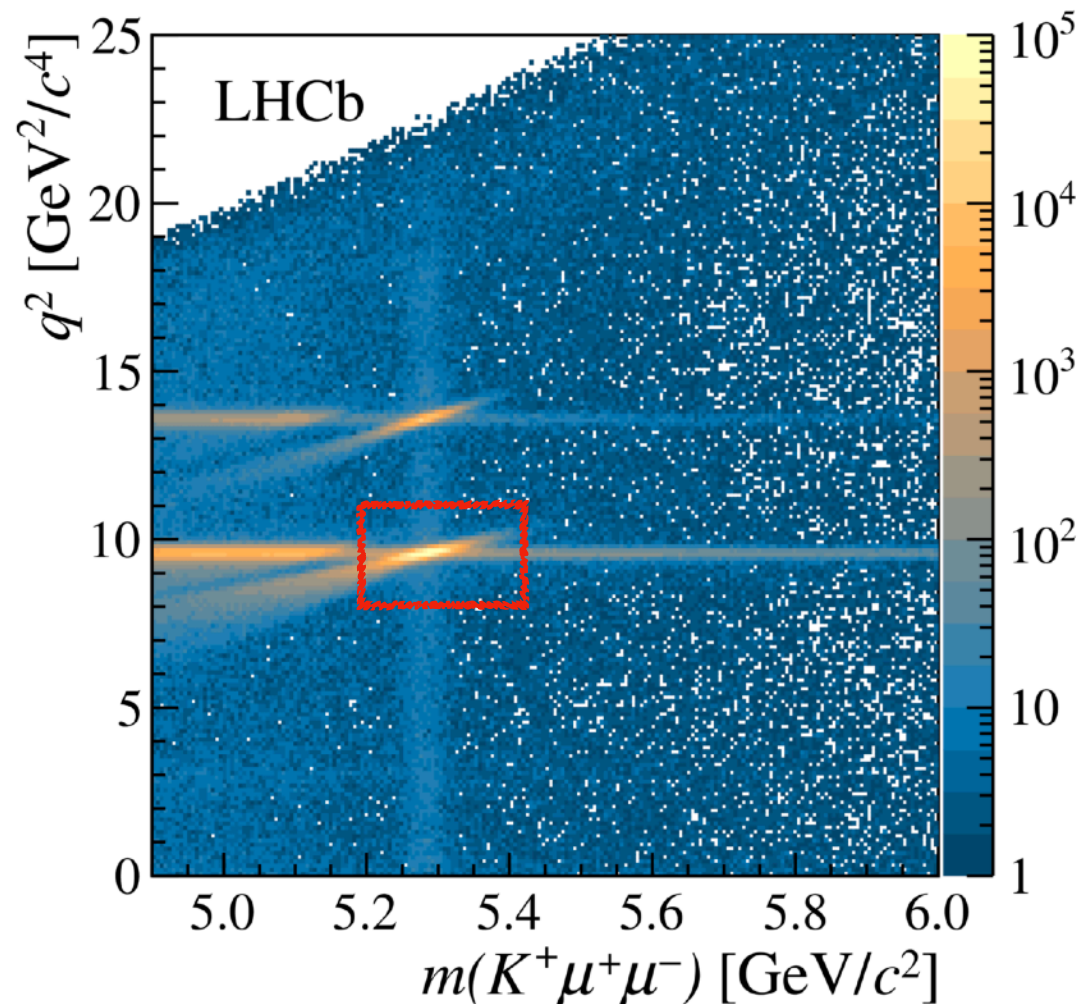
$L0\mu$  efficiency as a function of  $\eta$  and  $p_T$ .



$L0e$  efficiency as a function of  $\eta$  and  $p_T$ .

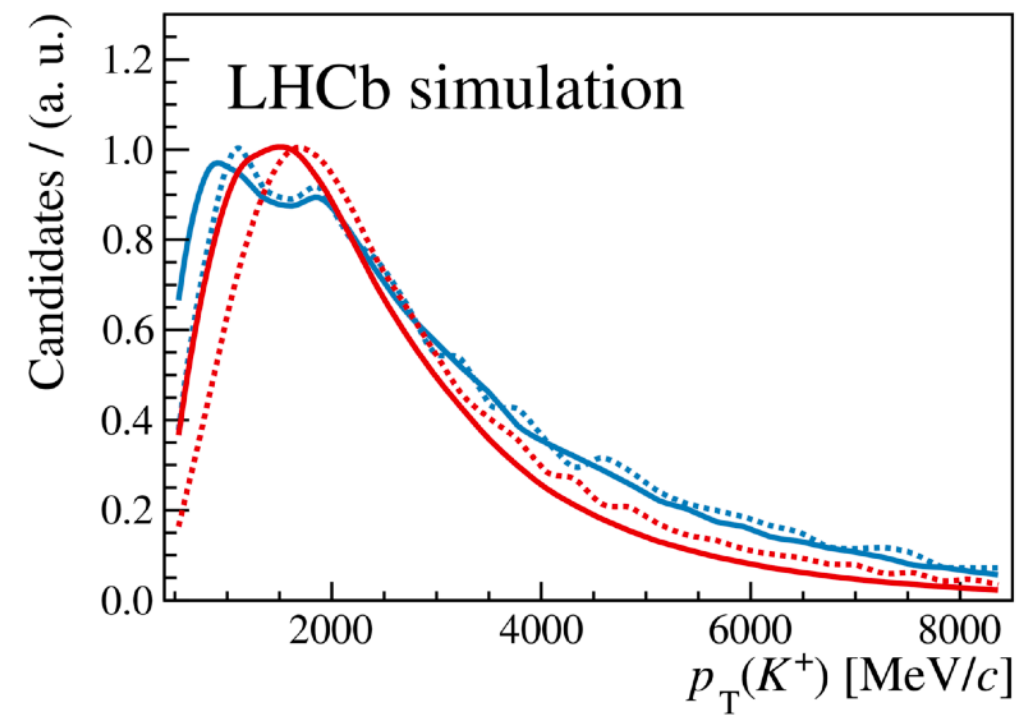
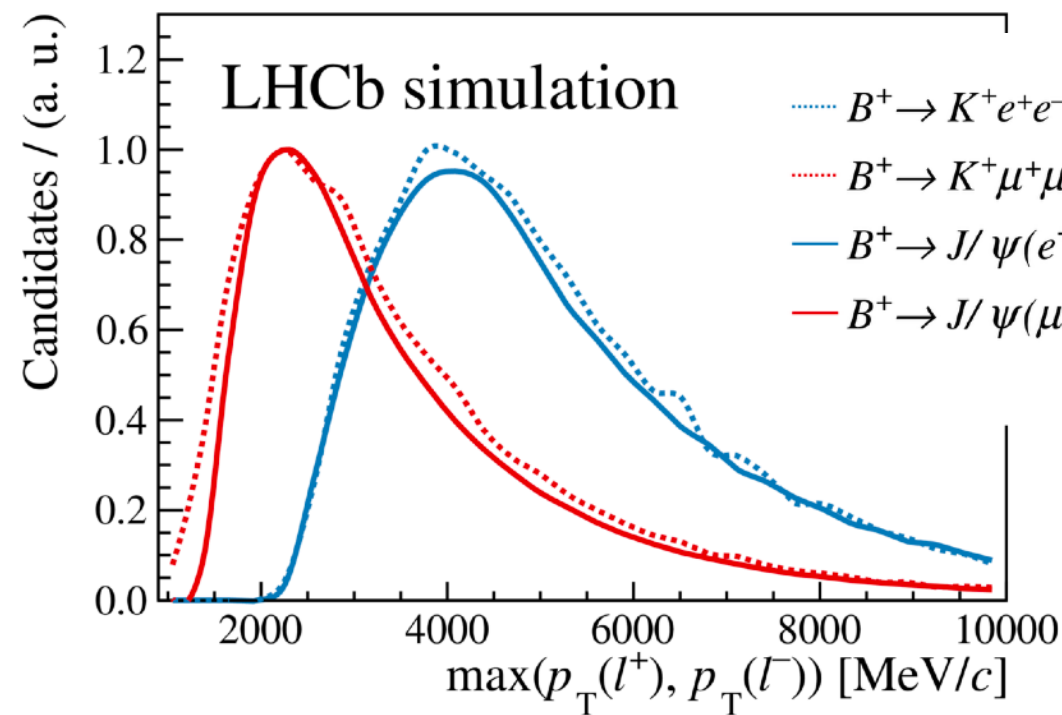
# Electron vs Muon Resolution

[PRL 122, 191801 \(2019\)](#)



- The diagonal lines highlighted in the red boxes are  $B^+ \rightarrow K^+ J/\psi(\rightarrow l^+ l^-)$  events.
- Due to Bremsstrahlung radiation, the electron resolution are significantly smeared.

# Lepton Flavour Universality Efficiencies



[PRL 122, 191801 \(2019\)](#)

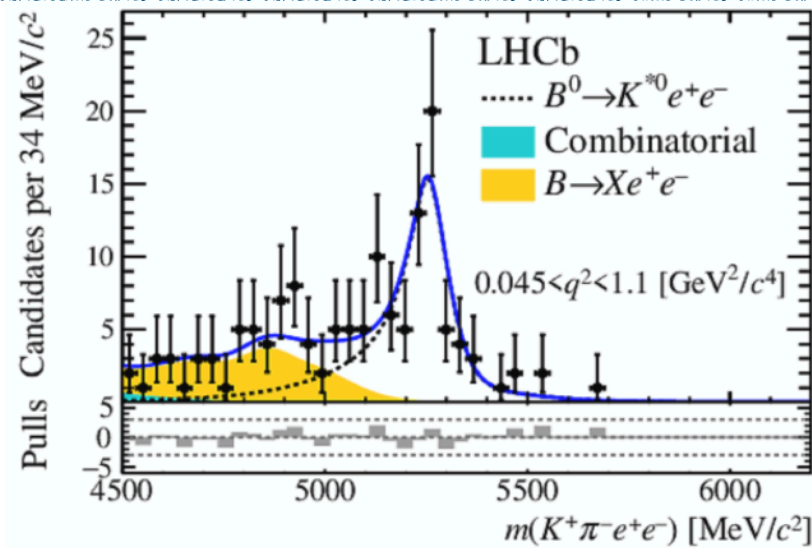
- Data-driven efficiency correction with high statistics sample.
  - $J/\psi$  control mode corrects  $B$  kinematics, reconstruction, trigger and multiplicity.
  - Collaboration-wide calibration samples to correct particle identification.
- Since the  $B$  daughters have high boost, control and signal modes are kinematically similar (see plots).
- Systematics cancel in efficiency ratio.



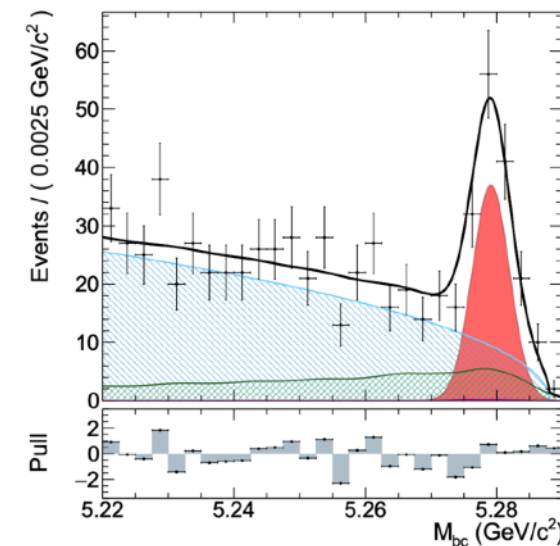
# Electrons: LHCb vs Belle

$e$

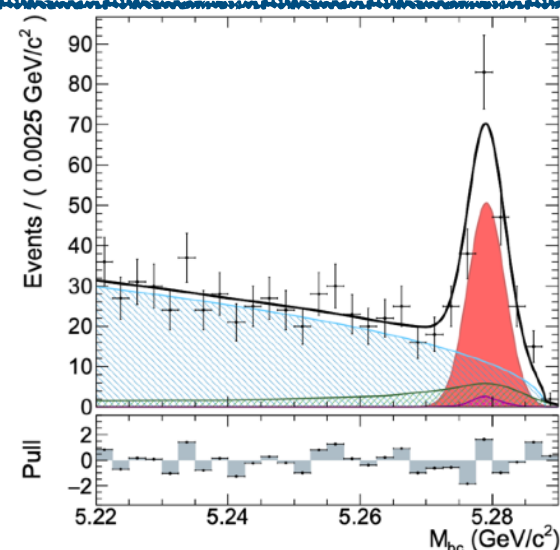
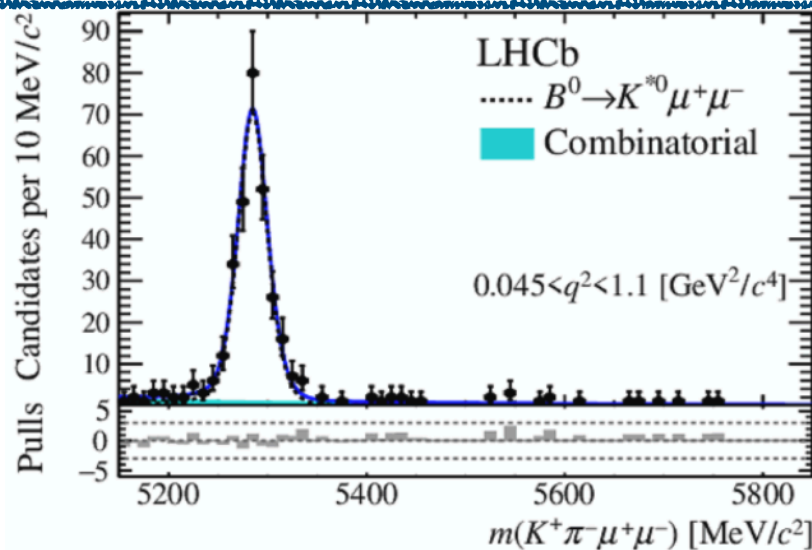
LHCb



Belle



$\mu$



- Reconstructed  $B^0 \rightarrow K^{*0} e^+ e^-$
- LHCb has worse electron mass resolution.

# Theory Predictions of $R_X$

| Decay                                  | $q^2$ range  | Ref. [38]       | Ref. [39]                    | Ref. [40]           | Ref. [41]         |
|----------------------------------------|--------------|-----------------|------------------------------|---------------------|-------------------|
| $B^+ \rightarrow K^+ \ell^+ \ell^-$    | [1, 6]       | $1.0 \pm 0.01$  | $1.0004^{+0.0008}_{-0.0007}$ | -                   | $1.00 \pm 0.01$   |
| $B^0 \rightarrow K^{*0} \ell^+ \ell^-$ | [0.045, 1.1] | $0.92 \pm 0.02$ | $0.920^{+0.007}_{-0.006}$    | $0.9259 \pm 0.0041$ | $0.906 \pm 0.028$ |
|                                        | [0.1, 1.1]   | —               | —                            | —                   | $0.983 \pm 0.014$ |
|                                        | [1.1, 6]     | $1.00 \pm 0.01$ | $0.996^{+0.002}_{-0.002}$    | $0.9965 \pm 0.0006$ | $1.00 \pm 0.01$   |
|                                        | [15, 19]     | —               | $0.998^{+0.001}_{-0.001}$    | $0.9981 \pm 0.0001$ | —                 |
| $B_s^0 \rightarrow \phi \ell^+ \ell^-$ | [0.045, 1.1] | —               | —                            | $0.9299 \pm 0.0028$ | —                 |
|                                        | [1.1, 6.0]   | —               | —                            | $0.9970 \pm 0.0002$ | —                 |
|                                        | [15, 19]     | —               | —                            | $0.9981 \pm 0.0001$ | —                 |

- 38: [JHEP 1801 \(2018\) 093](#)
- 39: [PRD 96, 093006 \(2017\)](#)
- 40: [EPJC 77, 377 \(2017\)](#)
- 41: [EPJC 76, 440 \(2016\)](#)