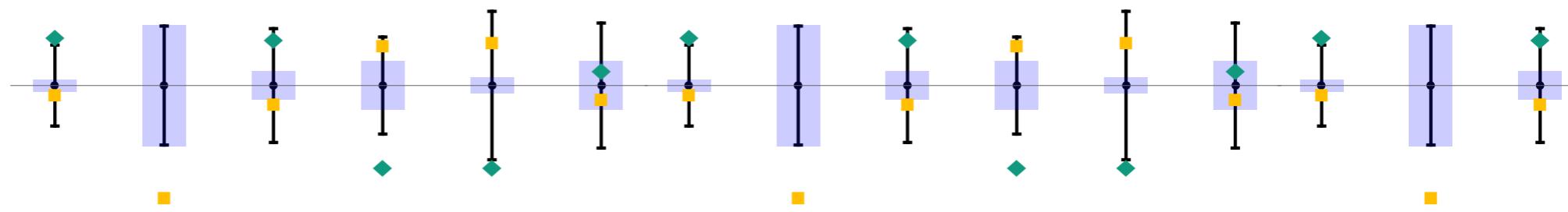


CRC-TRR-257



THEORY OF RD(*) AND TAU POLARIZATION



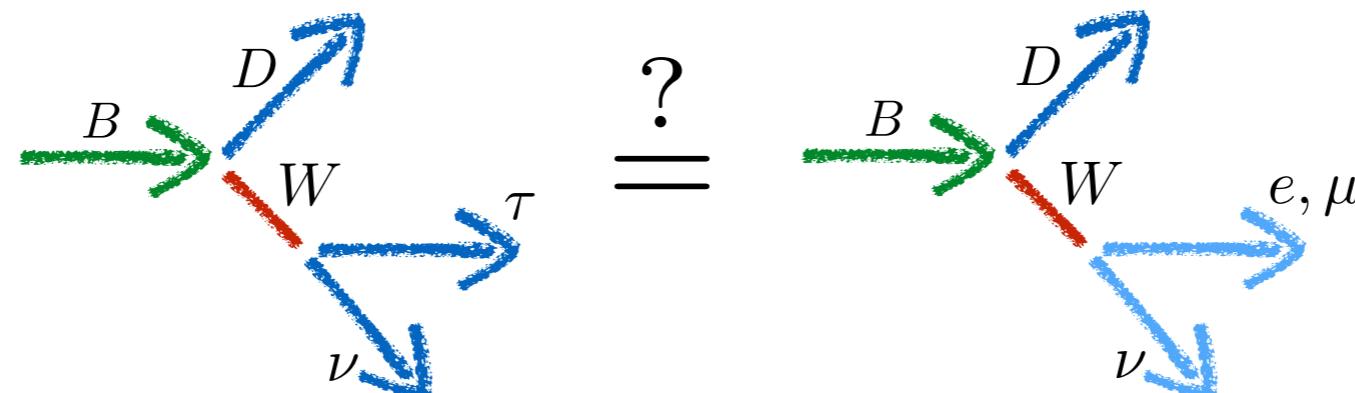
Susanne Westhoff
Heidelberg University



Why do we care?

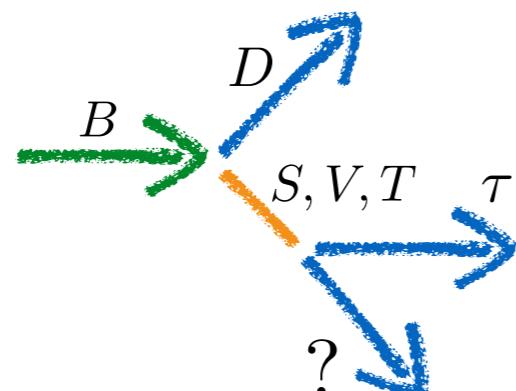
In the standard model:

- Are the weak interactions flavor-universal? CP violation?
- Are they mediated by a massive vector boson?



Beyond:

- Is there a new force mediating b - c - τ - ν interactions?
- Is the emitted missing energy a neutrino?

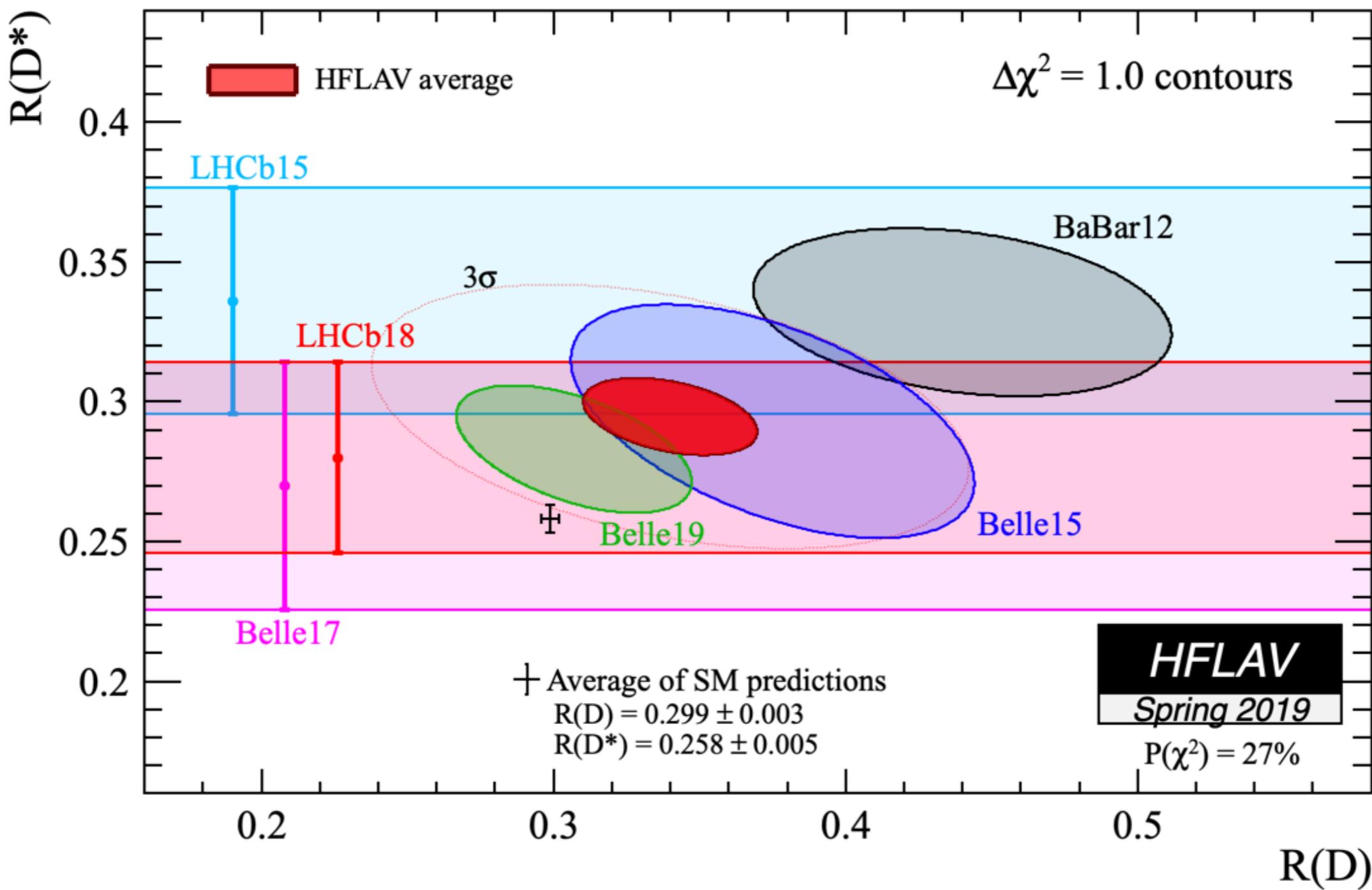


tau polarization



Ratios of branching ratios

$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu)}{\mathcal{B}(B \rightarrow D^{(*)}\ell\nu)}$$

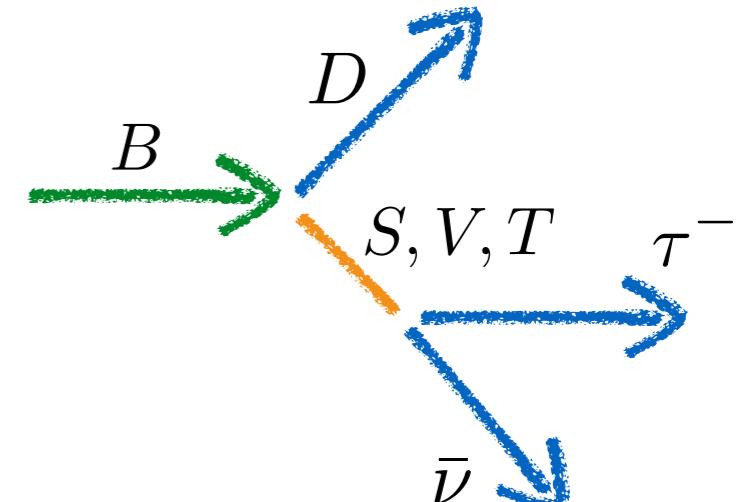
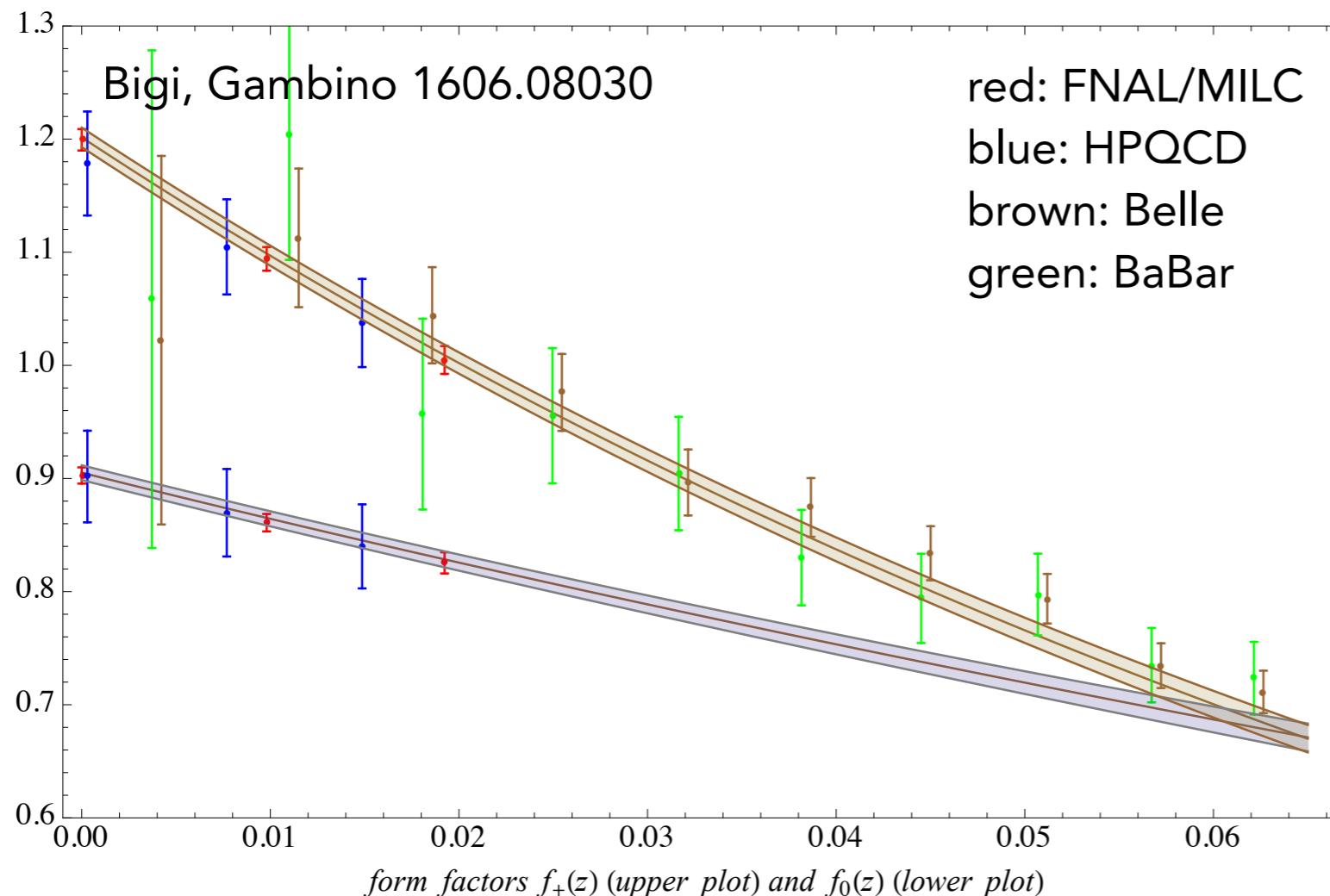


Beyond rates

Tau mass probes scalar form factor:

$$\frac{d\Gamma(B \rightarrow D\tau\nu)}{dq^2} = \frac{d\Gamma_\ell}{dq^2} \left(1 - \frac{m_\tau^2}{q^2}\right)^2 \left[1 + \frac{m_\tau^2}{2q^2} + \frac{m_\tau^2}{q^2} f(q^2) \frac{f_0^2(q^2)}{f_+^2(q^2)}\right]$$

Form factors determined with input from lattice and data:

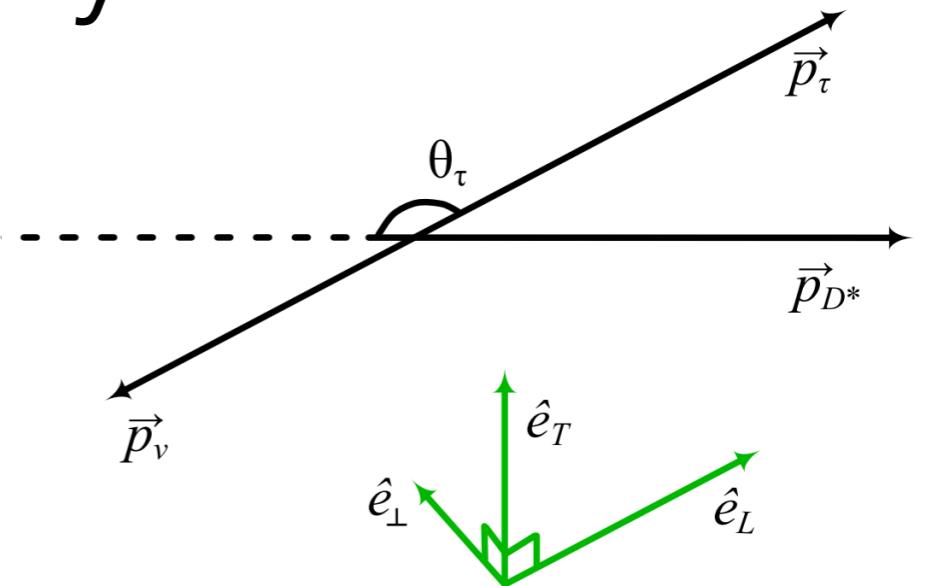


$$q^2 = (p_B - p_D)^2$$

Tau polarimetry

Tau helicity amplitudes in $B \rightarrow D^{(*)}\tau\nu$:

$\cos\theta_\tau, \lambda_\tau = \pm$ (q^2 frame)



Expand differential rates in spherical harmonics.

Koerner, Schuler 1990

$$\frac{d^2\Gamma_B^{\lambda_\tau}}{dq^2 d\cos\theta_\tau} = \frac{d\Gamma_B}{dq^2} \sum_{\ell=0}^2 B_\ell^{\lambda_\tau}(q^2) P_\ell^0(\cos\theta_\tau)$$

$$\frac{d^2\mathcal{P}_B^\perp}{dq^2 d\cos\theta_\tau} = \frac{d\Gamma_B}{dq^2} \sum_{\ell=1}^2 \text{Re}[C_\ell(q^2)] P_\ell^1(\cos\theta_\tau)$$

$$\frac{d^2\mathcal{P}_B^T}{dq^2 d\cos\theta_\tau} = \frac{d\Gamma_B}{dq^2} \sum_{\ell=1}^2 \text{Im}[C_\ell(q^2)] P_\ell^1(\cos\theta_\tau)$$

Rate:

$$d\Gamma_B = d\Gamma_B^{+,L} + d\Gamma_B^{-,L}$$

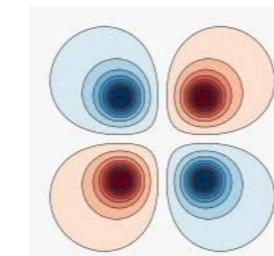
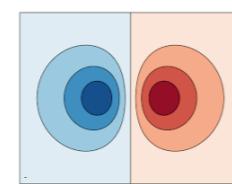
Spin asymmetries:

$$d\mathcal{P}_B^a = d\Gamma_B^{+,a} - d\Gamma_B^{-,a}$$

10 independent helicity amplitudes to fully describe tau production.

Tau asymmetries

		dipole	quadru pole
1	Γ	A_{FB}	A_Q
L	P_L	Z_L	Z_Q
\perp	P_\perp	Z_\perp	
T	P_T	Z_T	



Polarization:

$$P_a(q^2) \sim \int \frac{d\mathcal{P}_a}{dq^2 d\cos\theta_\tau} d\cos\theta_\tau$$

Angular asymmetry:

$$A_\ell(q^2) \sim \int \frac{d\Gamma}{dq^2 dc\theta_\tau} P_\ell^0(c\theta_\tau) dc\theta_\tau$$

Zweifach (double):

$$Z_{a,\ell}(q^2) \sim \int \frac{d\mathcal{P}_a}{dq^2 dc\theta_\tau} P_\ell^0(c\theta_\tau) dc\theta_\tau$$

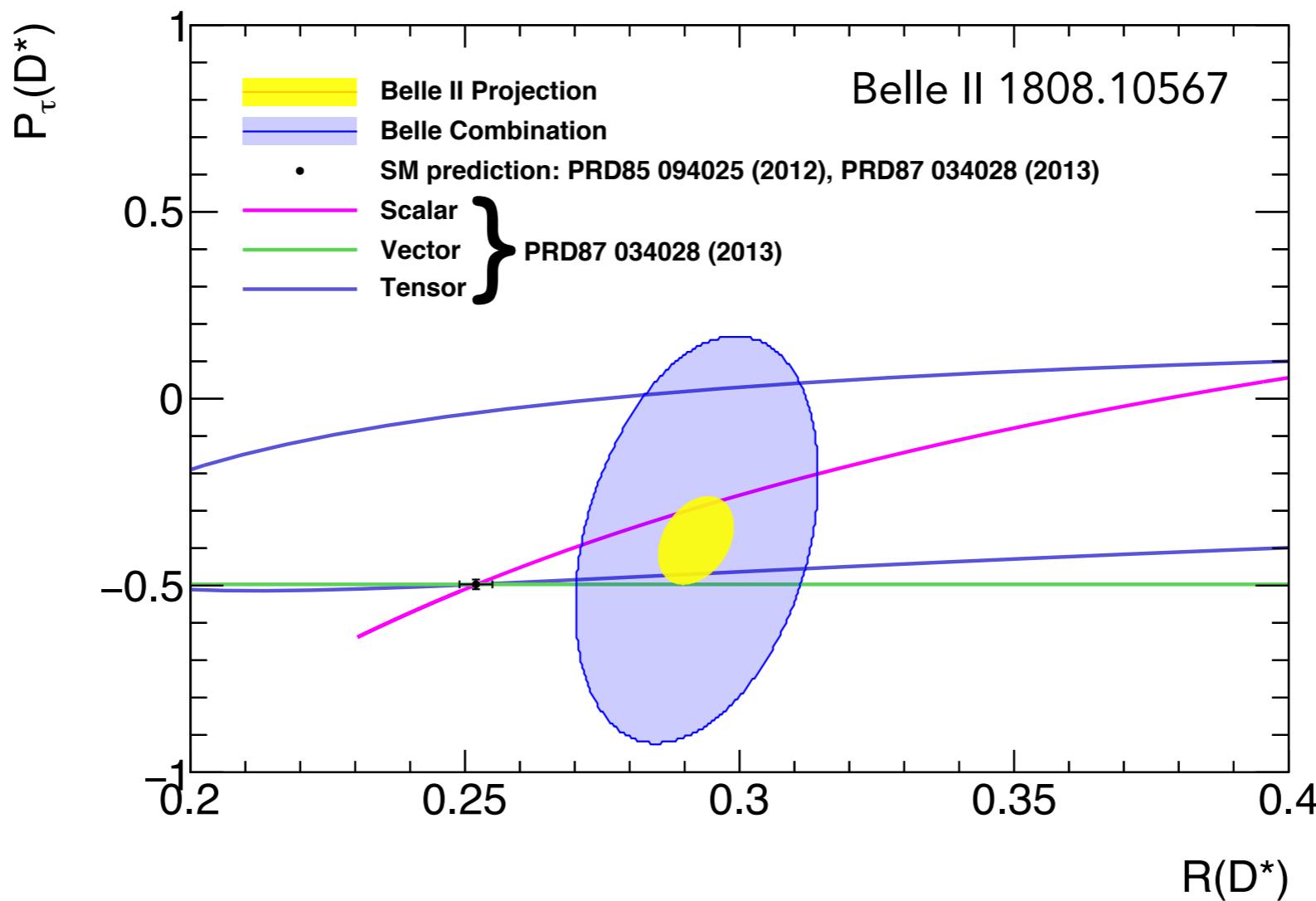
Total: 10 observables

Currently: tau polarization

Measured in hadronic tau decays $\tau \rightarrow \pi\nu, \tau \rightarrow \rho\nu$: Belle 1709.00129

$$P_\tau(D^*) = P_L(D^*) = -0.38 \pm 0.51 \text{ (stat)} {}^{+0.21}_{-0.16} \text{ (syst)}$$

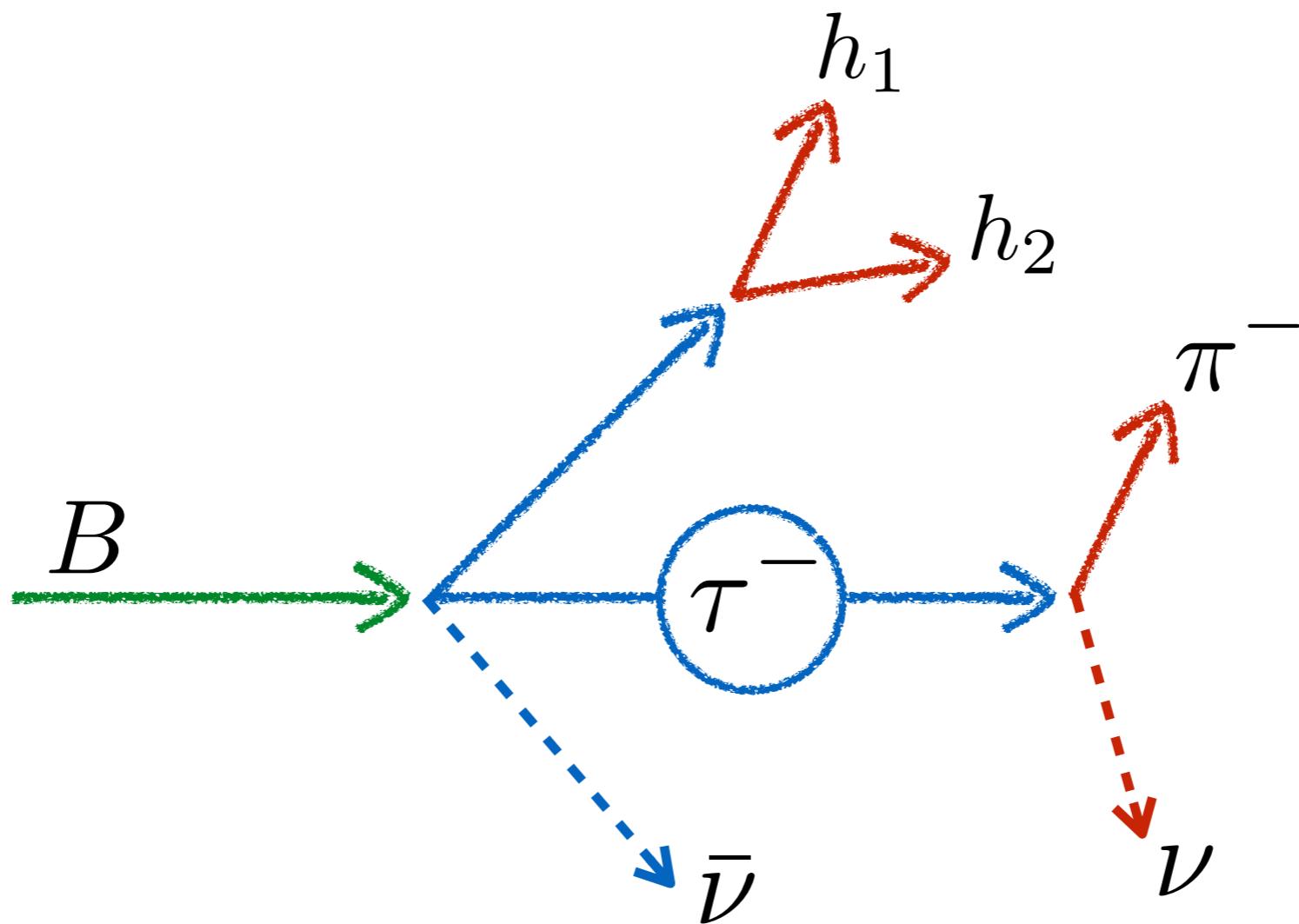
Prospects for Belle II:



What we observe

Idea: reconstruct tau production from **visible** final-state kinematics.

Bullock, Hagiwara, Martin 1993; Kiers, Soni 1997; Nierste, Trine, SW 2008



Hadronic decays $\tau \rightarrow \pi\nu$, $\tau \rightarrow \rho\nu$ preserve most information.

Tau production properties from the final state

Tau polarisations and FB asymmetry:

$$B \rightarrow D^{(*)} \nu [\tau \rightarrow (\ell \nu, \pi, \rho) \nu]$$

Tanaka, Watanabe 2010
Sakaki, Tanaka 2013
Alonso, Martin Camalich, SW 2017
Ivanov, Koerner, Tran 2017+
Asadi, Buckley, Shih 2018
Asadi, Hallin, Martin Camalich, Shih, SW 2020

CP violation:

$$B \rightarrow D \nu [\tau \rightarrow 3\pi \nu]$$

Hagiwara, Nojiri, Sakaki 2014

$$B \rightarrow [D^* \rightarrow D \pi] [\tau \rightarrow \pi \nu] \nu$$

Bhattacharya, Datta, Kamali, London 2020

Search for new physics:

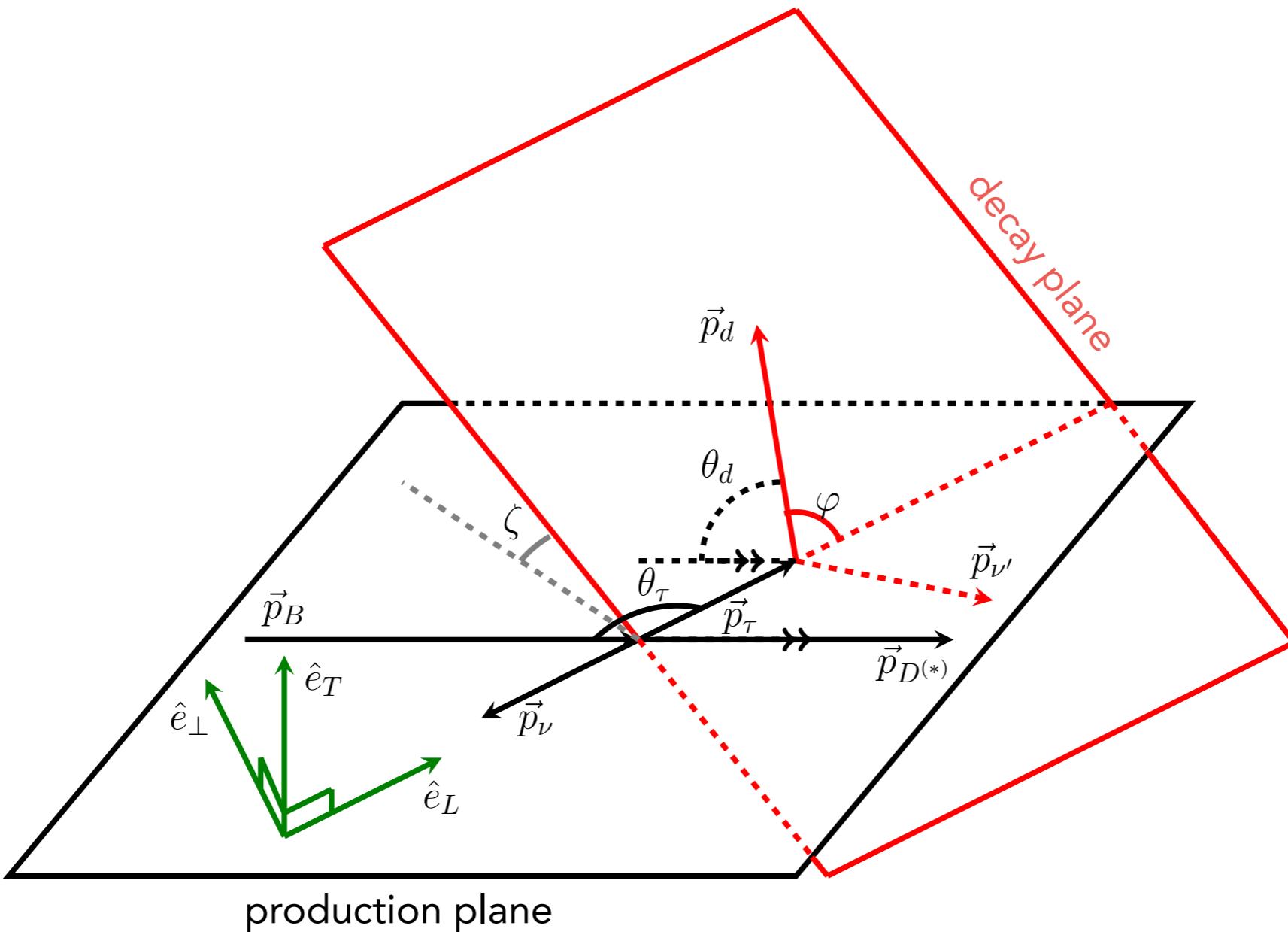
$$B \rightarrow [D^{(*)} \rightarrow D(\pi, \gamma)] \nu [\tau \rightarrow (\ell \nu, \pi) \nu]$$

Ligeti, Papucci, Robinson 2016+
Alonso, Kobach, Martin Camalich 2016
Bhattacharya et al. 2018
Colangelo, De Fazio 2018
Asadi, Buckley, Shih 2018

Reweighting simulations for NP:

HAMMER software: Bernlochner et al. 2020

Final-state kinematics



Measurable: q^2 , $\cos \theta_d$, $s_d = \frac{E_d}{\sqrt{q^2}}$ (meson fully reconstructed)

Here: $\tau \rightarrow \pi\nu$, $\tau \rightarrow \rho\nu$ (most information on tau production)

Tau asymmetries from final-state kinematics

Differential rate factorizes into tau **production** and **decay**

$$\frac{d^4\Gamma_d}{dq^2 d\cos\theta_\tau ds_d d\zeta} = \frac{E_\tau}{\Gamma_\tau m_\tau} \left(\frac{d^2\Gamma_B^{\lambda_\tau}}{dq^2 d\cos\theta_\tau} \frac{d^2\Gamma_\tau^{\lambda_\tau}}{ds_d d\zeta} + \frac{1}{2} \left[\frac{d^2\mathcal{P}_B^\perp}{dq^2 d\cos\theta_\tau} \frac{d^2\mathcal{P}_\tau^\perp}{ds_d d\zeta} - \frac{d^2\mathcal{P}_B^T}{dq^2 d\cos\theta_\tau} \frac{d^2\mathcal{P}_\tau^T}{ds_d d\zeta} \right] \right)$$

What we (strive to) measure:

$$\frac{d^3\Gamma_d}{dq^2 d\cos\theta_d ds_d} = \text{BR}(\tau \rightarrow d\nu) \frac{d\Gamma_B}{dq^2} \sum_{\ell=0}^2 P_\ell(\cos\theta_d) I_\ell(q^2, s_d)$$

$$I_0 = \frac{1}{2} (f_0^d(q^2) + f_L^d(q^2, s_d) P_L(q^2))$$

$$I_1 = f_{A_{FB}}^d(q^2, s_d) A_{FB}(q^2) + f_\perp^d(q^2, s_d) P_\perp(q^2) + f_{Z_L}^d(q^2, s_d) Z_L(q^2)$$

$$I_2 = f_{Z_\perp}^d(q^2, s_d) Z_\perp(q^2) + f_{Z_Q}^d(q^2, s_d) Z_Q(q^2) + f_{A_Q}^d(q^2, s_d) A_Q(q^2).$$

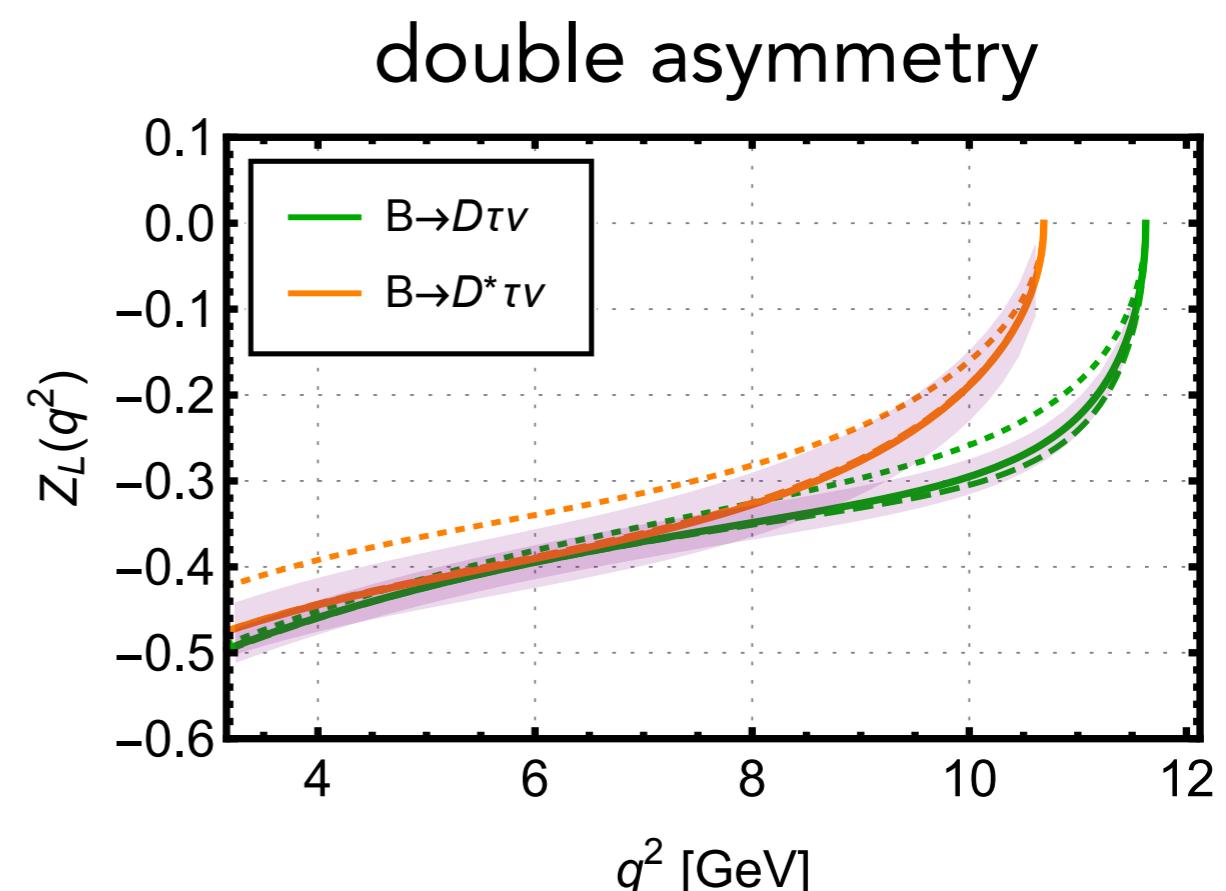
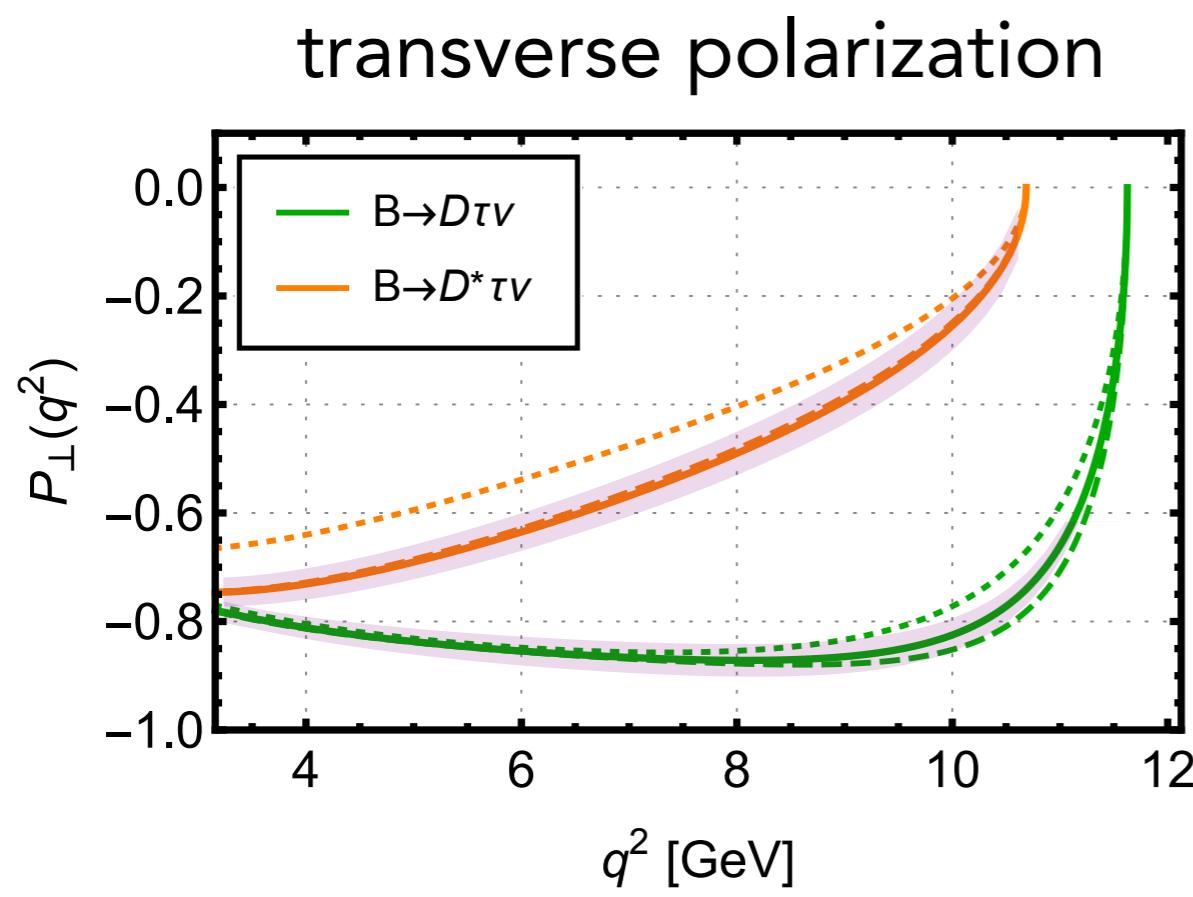
P_T, Z_T : need second plane (meson decay, 3-prong tau decay)

Extract tau asymmetries from a fully differential fit to data.

Belle II prospects: distributions

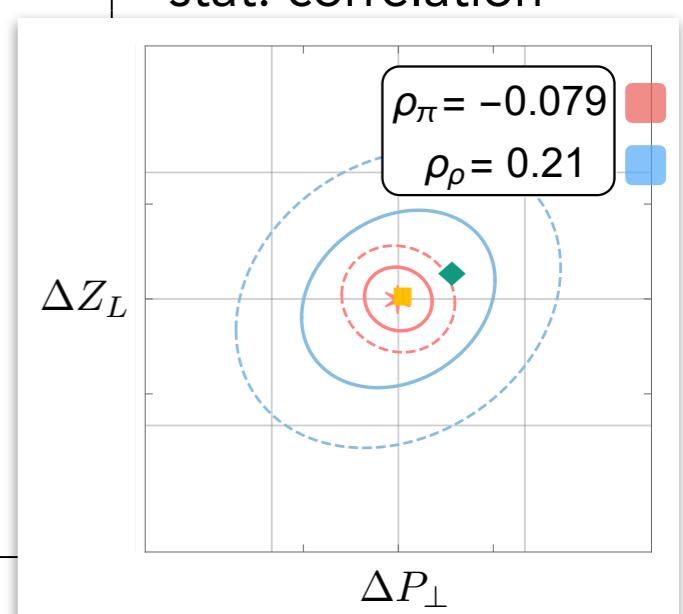
Expect 3000 events/channel (~in 50/ab).

Here: $\tau \rightarrow \pi\nu$. Unbinned maximum likelihood fit in $\cos\theta_d$, s_d .



Distributions can be measured with good statistical precision.

Belle II: integrated asymmetries

		SM	σ_{th}	σ_π	σ_ρ	measured
$B \rightarrow D\tau\nu$	A_{FB}	-0.359	0.003	0.020	0.024	$= Z_L$ –
	P_L	0.34	0.03	0.029	0.069	–
	P_\perp	-0.839	0.007	0.028	0.094	–
	Z_\perp	0.224	0.012	0.024	0.091	–
	Z_Q	0.243	0.012	0.037	0.118	–
	A_Q	-0.088	0.004	0.031	0.042	–
$B \rightarrow D^*\tau\nu$	A_{FB}	0.07	0.02	0.031	0.037	–
	P_L	-0.50	0.02	0.029	0.070	-0.38(54) [Belle]
	P_\perp	-0.49	0.02	0.039	0.113	–
	Z_L	-0.323	0.007	0.037	0.104	–
	Z_\perp	0.054	0.002	0.041	0.101	–
	Z_Q	0.058	0.002	0.055	0.046	–
	A_Q	-0.0189	0.0005	0.146	0.050	–
						stat. correlation
						
						ΔZ_L
						ΔP_\perp

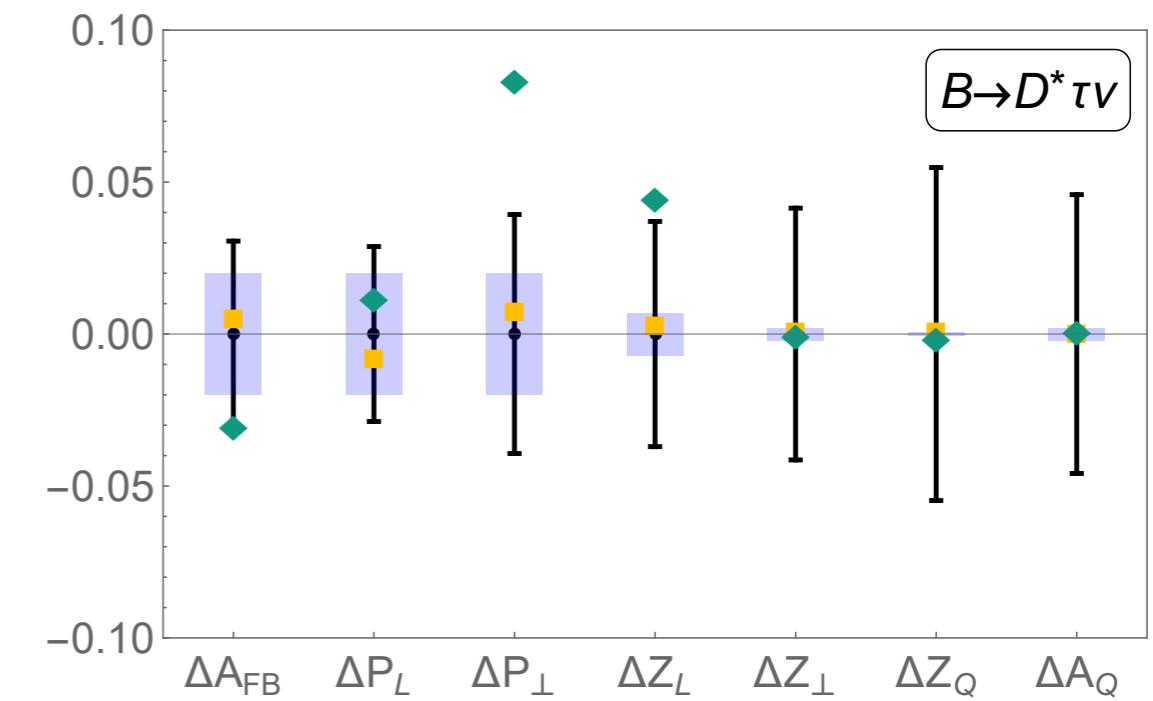
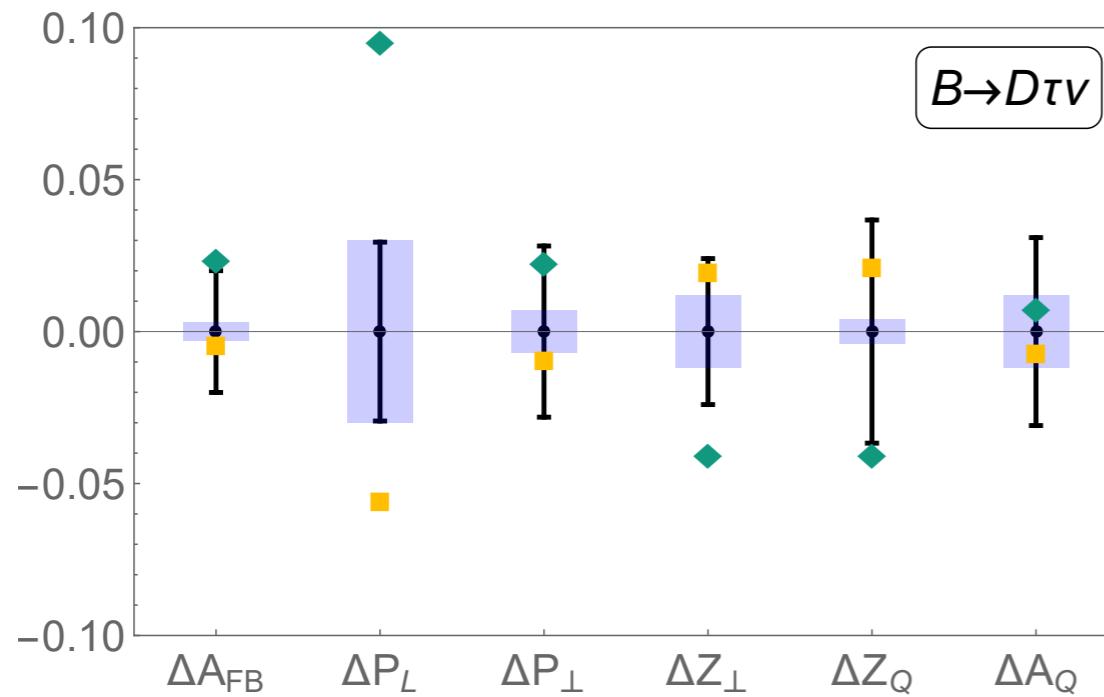
New physics in tau production

Effective four-fermion interactions change tau kinematics:

$$\mathcal{H}_{\text{eff}} = \frac{4G_F V_{cb}}{\sqrt{2}} \left(O_{LL}^V + \sum_{X,Y=L,R} (C_{XY}^S O_{XY}^S + C_{XY}^V O_{XY}^V) + \sum_{X=L,R} C_{XX}^T O_{XX}^T \right)$$

Motivated by b-c-tau-nu data: Shi et al. 1905.08498, see also Blanke et al. 1811.09603

- “ U_1 vector leptoquark” : $C_{LL}^V = 0.08$, $C_{RL}^S = -0.05$
- ◆ “ $S_1 - R_2$ scalar leptoquarks” : $C_{LL}^S = 0.07$, $C_{LL}^T = -0.03$



Tau asymmetries are sensitive to new scalar/tensor currents.

Summary: tau polarimetry in B to D(*) tau nu

- **new** full analytic description by 9 tau asymmetries
- ◆ **measure** them in differential distributions at Belle II
- ◆ **probe CP violation** with meson decays and 3-prong tau decays
- **probe new physics** with new asymmetry observables

Questions? westhoff@thphys.uni-heidelberg.de

Thank you!

Backup

TAU DECAYS

Tau decay branching ratios:

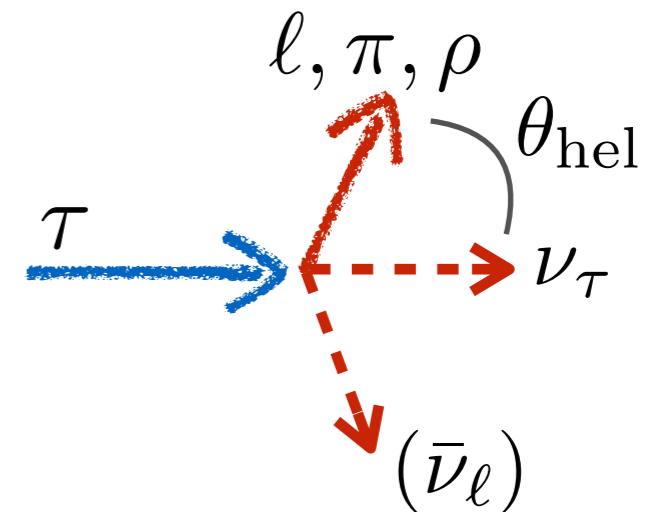
Channel	$\tau \rightarrow \mu \nu \nu$	$\tau \rightarrow e \nu \nu$	$\tau \rightarrow \pi \nu$	$\tau \rightarrow \rho \nu$	$\tau \rightarrow 3\pi \nu$	TOTAL
\mathcal{B}	17.4%	17.8%	10.82%	25%	9%	$\sim 80\%$

Hadronic tau decays have highest analyzing power:

$$\frac{1}{\Gamma_\tau} \frac{d\Gamma_\tau}{d \cos \theta_{\text{hel}}} = \frac{1}{2} (1 + \alpha P_L \cos \theta_{\text{hel}})$$

Scalar pion: $\alpha = 1$

Vector meson rho: $\alpha = \frac{m_\tau^2 - 2m_\rho^2}{m_\tau^2 + 2m_\rho^2} \approx 0.45$



Strong experimental bounds on new physics in tau decays.