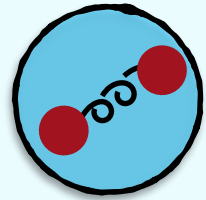
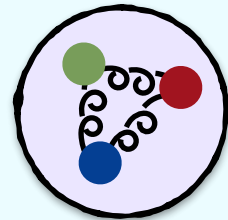


Theory Overview of Heavy Exotic Spectroscopy

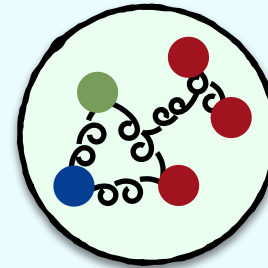
Ciaran Hughes (chughes@fnal.gov)



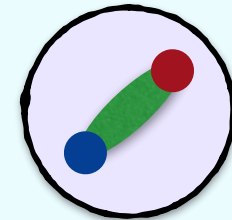
Mesons



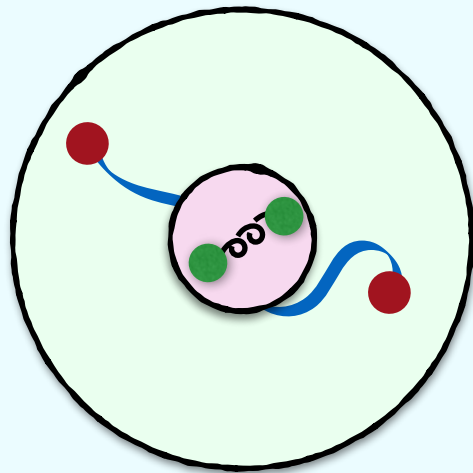
Baryons



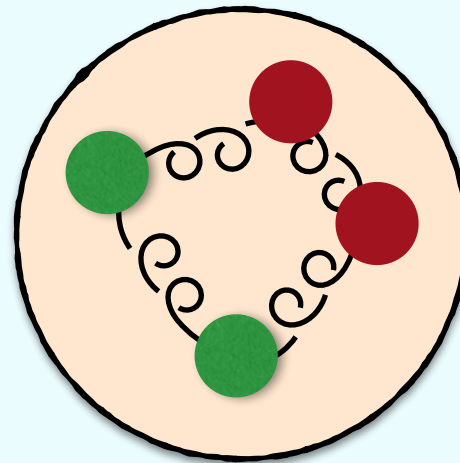
Pentaquarks



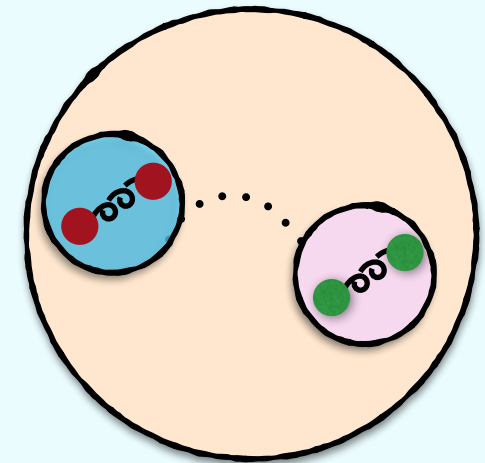
Hybrids



*Hadro-
Quarkonium*




*Compact
Tetraquarks*



Molecular


Pre 2003 Heavy Spectroscopy

 *Defⁿ*: “Conventional States” = Mesons (valence $\bar{q}q$) and Baryons (valence qqq) in line with quark potential model expectations

Post 2003 Heavy Spectroscopy

 *Defⁿ*: “Exotic States” = “States we **do not** understand yet (but not new physics)”

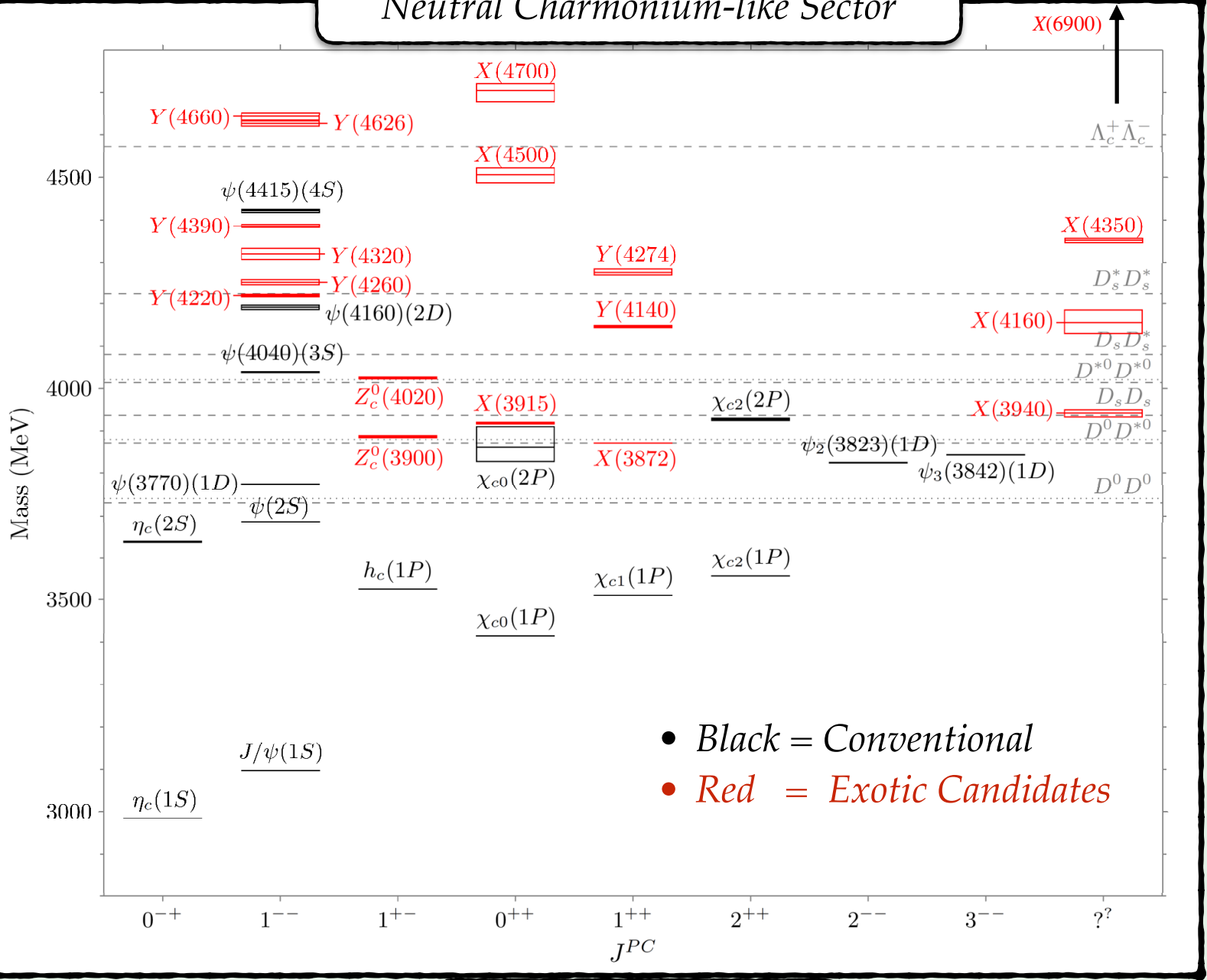
Post 2003 Heavy Spectroscopy

 Def^n : “Exotic States” = States which are not in line with quark potential model expectations, e.g., not mesons or baryons.

Post 2003 Heavy Spectroscopy

Def^n : "Exotic States" = States which are not in line with quark potential model expectations

Neutral Charmonium-like Sector



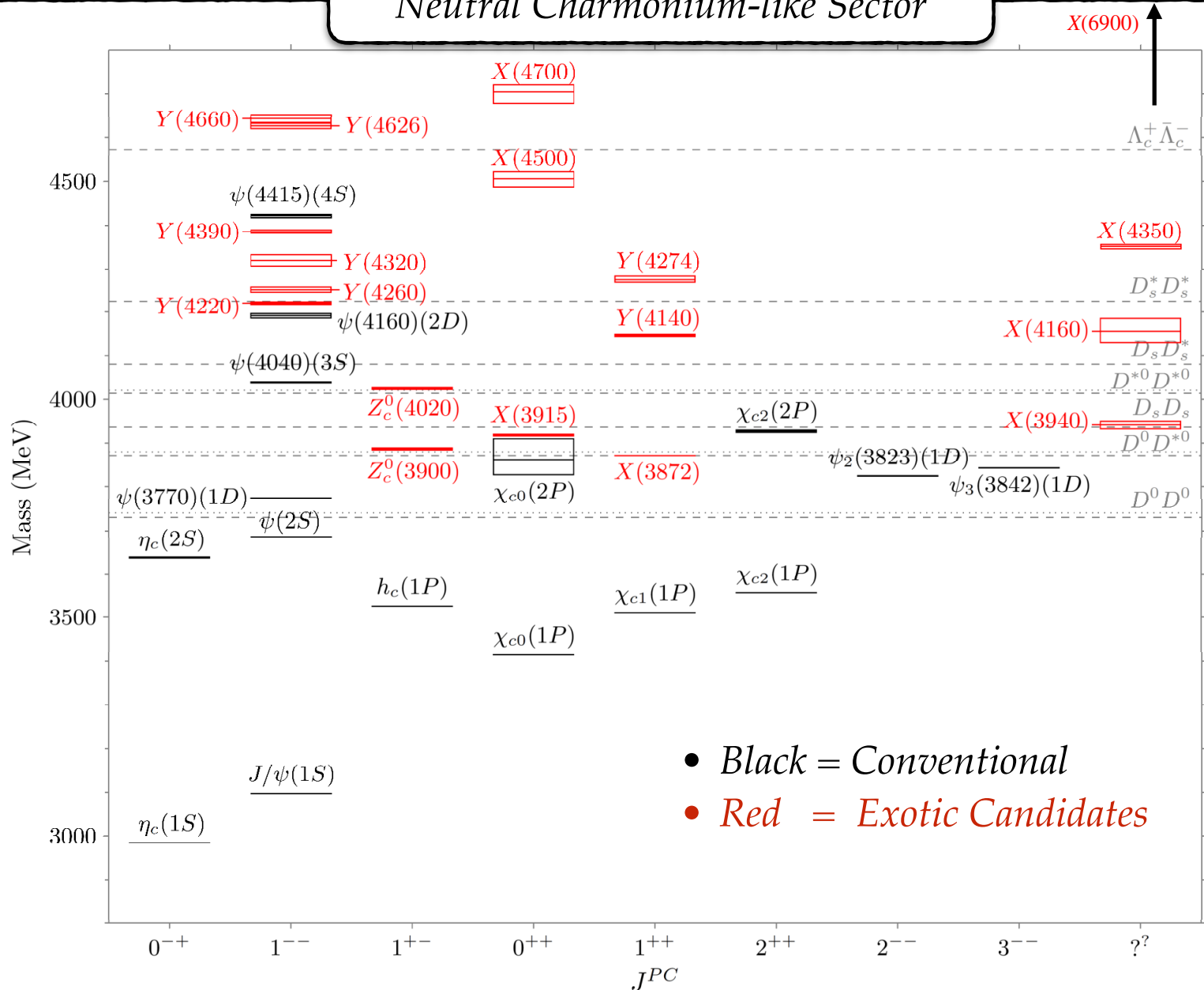
- Black = Conventional
- Red = Exotic Candidates

R. Lebed, 2020

Post 2003 Heavy Spectroscopy

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Neutral Charmonium-like Sector



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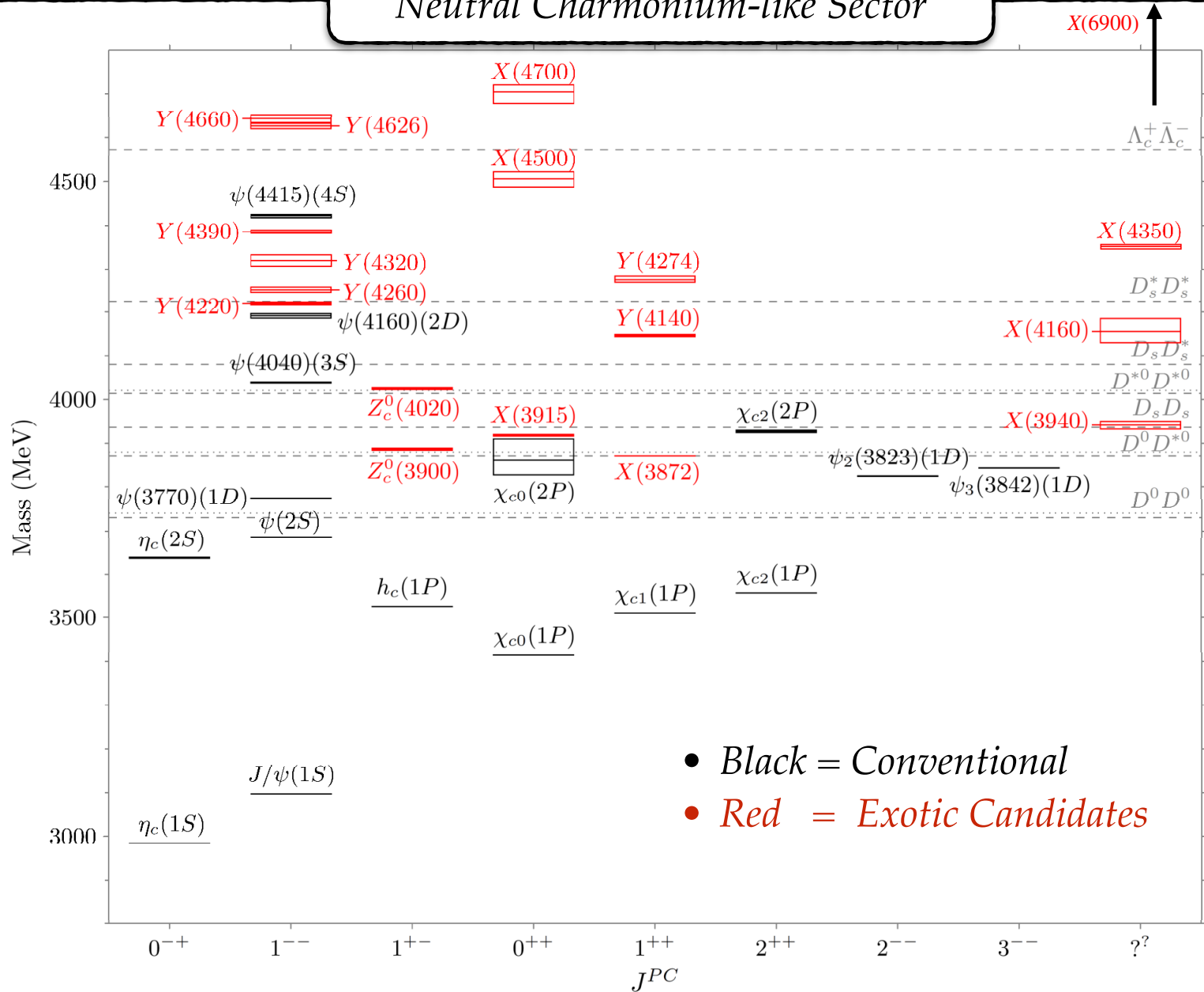
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\bullet Total of 15 Experimentally Established Exotics PDG

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R. Lebed, 2020

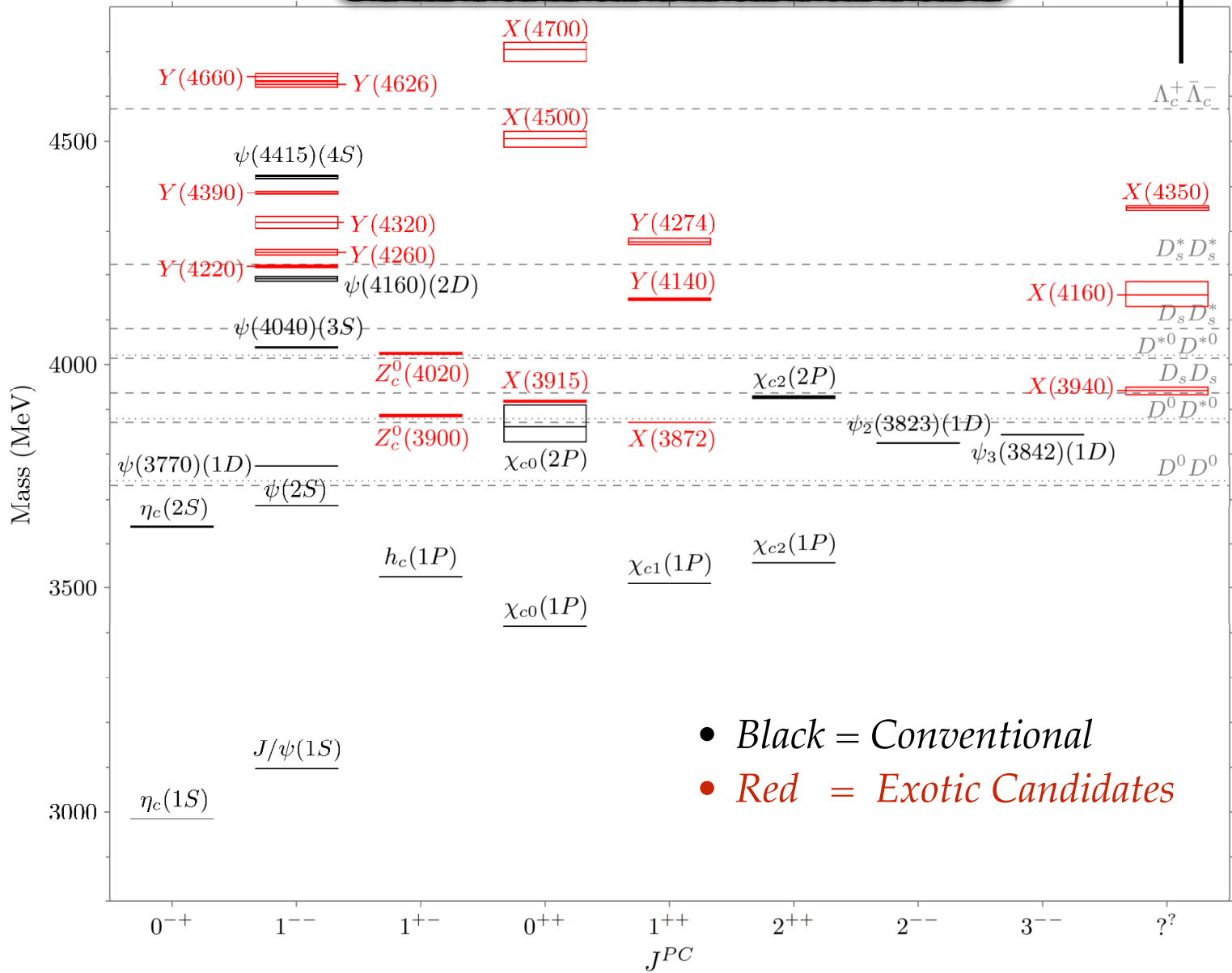
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Commonly called XYZ states (PDG has official naming convention)

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Neutral Charmonium-like Sector



R. Lebed, 2020

- \bullet Total of 15 Experimentally Established Exotics PDG
- \bullet Commonly called XYZ states (PDG has official naming convention)
- \bullet 44 Observed Exotic Candidates

Exotic States: What Can They Be?

 Gell-Mann (1964) : “Color Confinement allows $\bar{q}gq, \bar{q}\bar{q}qq, \bar{q}qqqq, \dots$ ”

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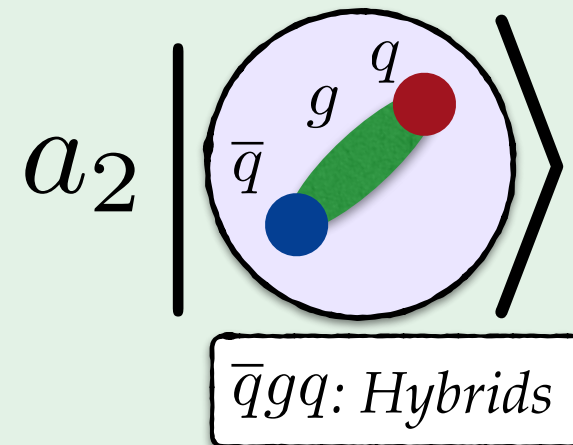
$$|\Psi\rangle = a_1 \left| \begin{array}{c} \bar{q} \\ \text{---} \\ q \\ \text{---} \\ \text{---} \\ \text{---} \end{array} \right\rangle$$

Mesons

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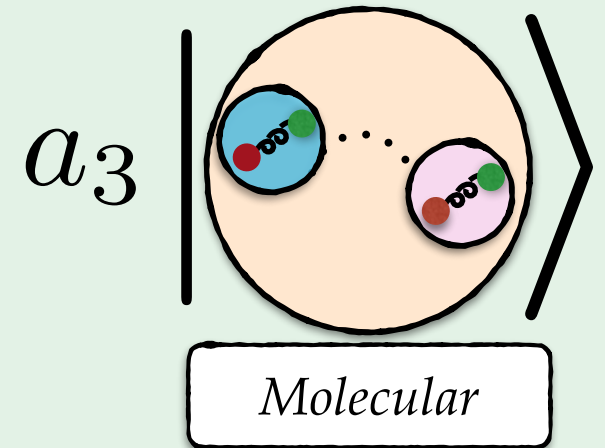
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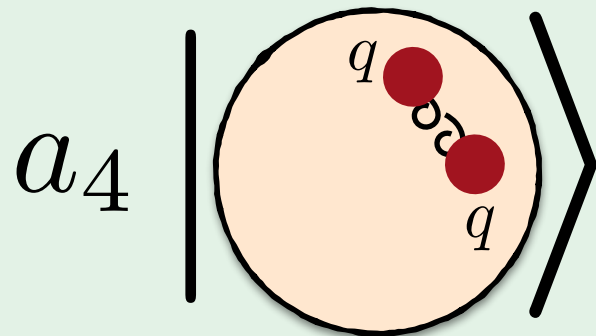
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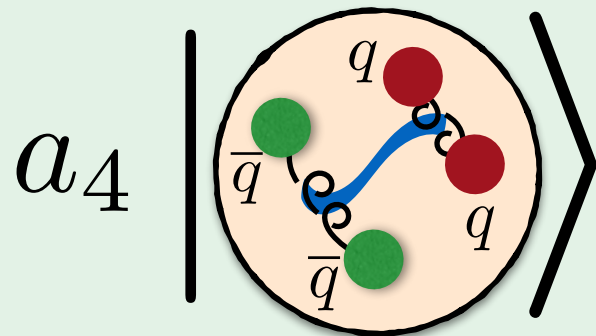


Diquark Tetraquarks

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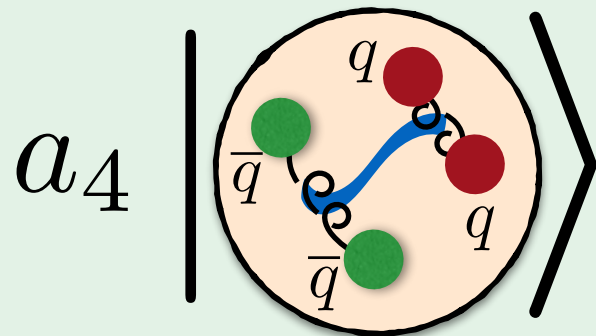


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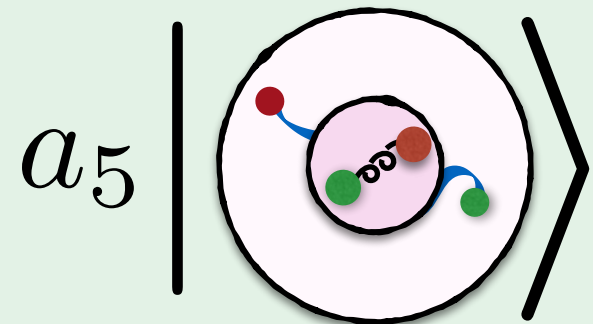


Compact Tetraquarks

Exotic States: What Can They Be?

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$$|\Psi\rangle =$$



Hadro-Quarkonium

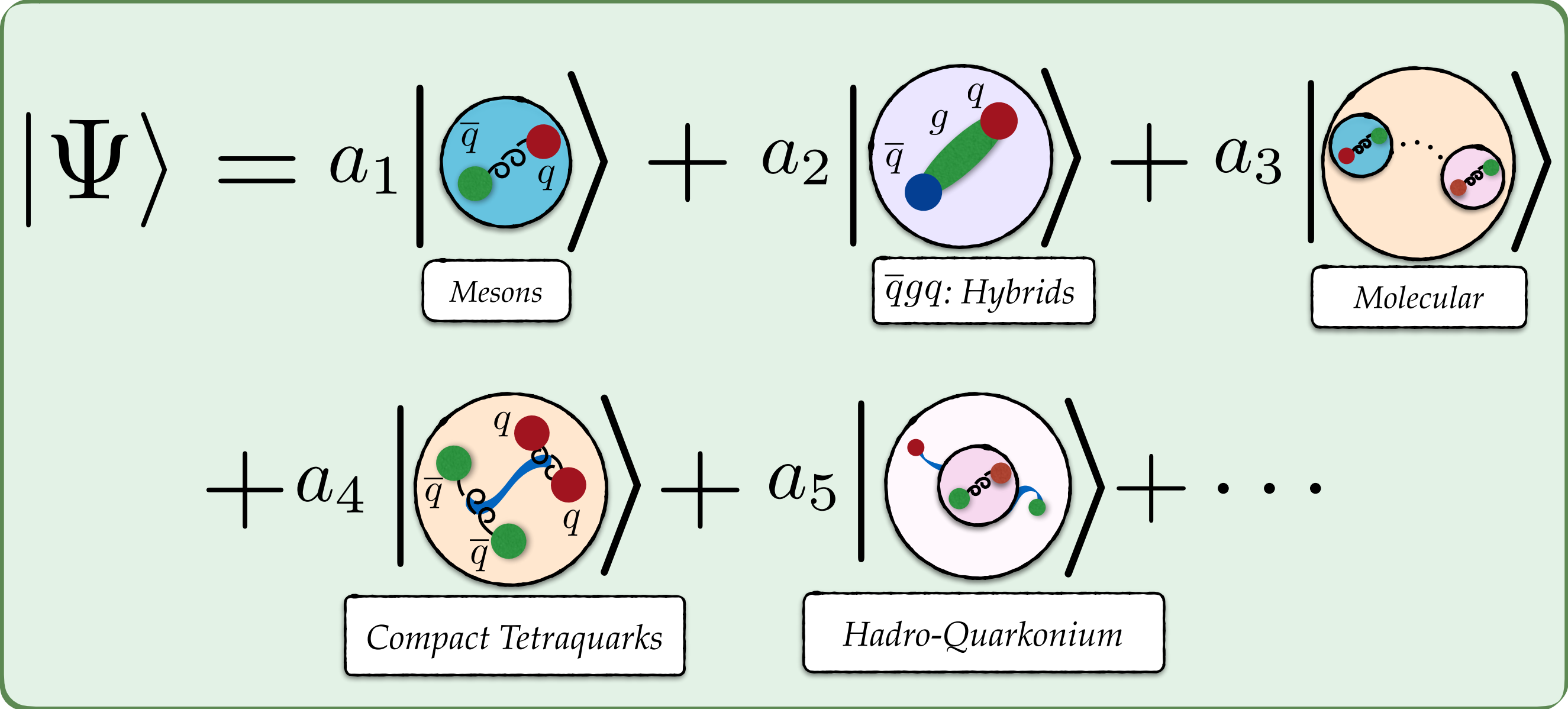
Exotic States: What Can They Be?

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$$\begin{aligned}
 |\Psi\rangle = & a_1 \left| \begin{array}{c} \bar{q} \quad q \\ \text{gluon} \end{array} \right\rangle + a_2 \left| \begin{array}{c} q \\ \bar{q} \quad g \end{array} \right\rangle + a_3 \left| \begin{array}{c} \dots \\ \text{meson} \dots \text{meson} \end{array} \right\rangle \\
 & + a_4 \left| \begin{array}{c} q \quad q \\ \bar{q} \quad \bar{q} \end{array} \right\rangle + a_5 \left| \begin{array}{c} \text{hadron} \\ \text{quarkonium} \end{array} \right\rangle + \dots
 \end{aligned}$$

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📌 Exotic Spectroscopy = Which of These Hopeful Exotic Configurations Can Explain The Experimentally Determined States?

Scattering Overview: What Is A State?

 *Defⁿ*: “State” = A Pole Singularity of the Scattering Matrix

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- $E = \sqrt{s} - 2m$

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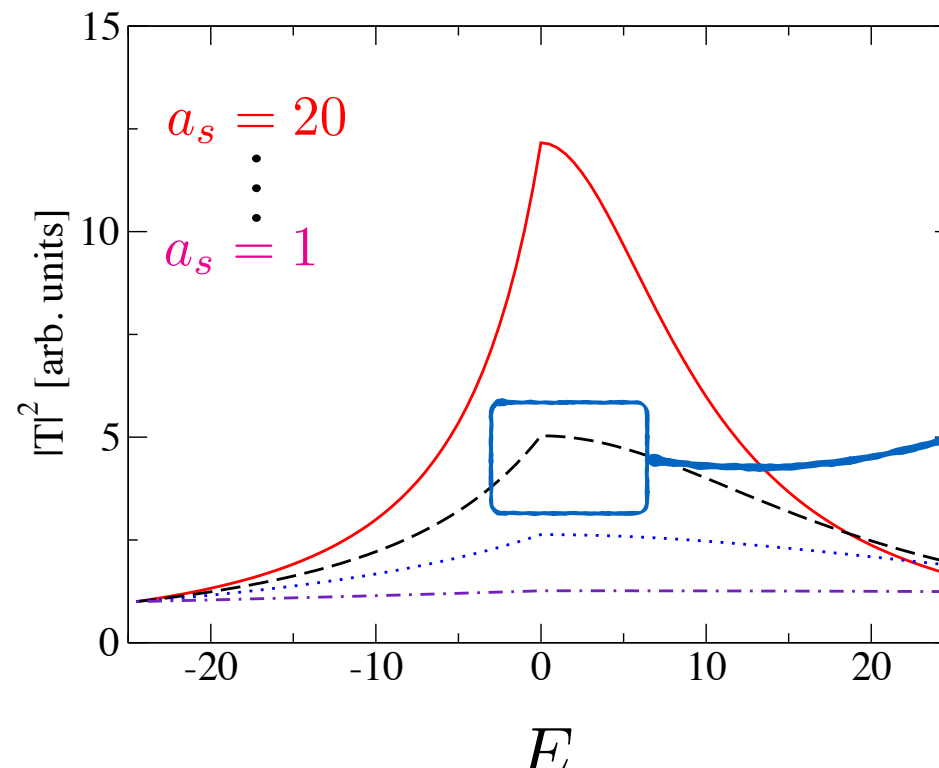
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Not A State

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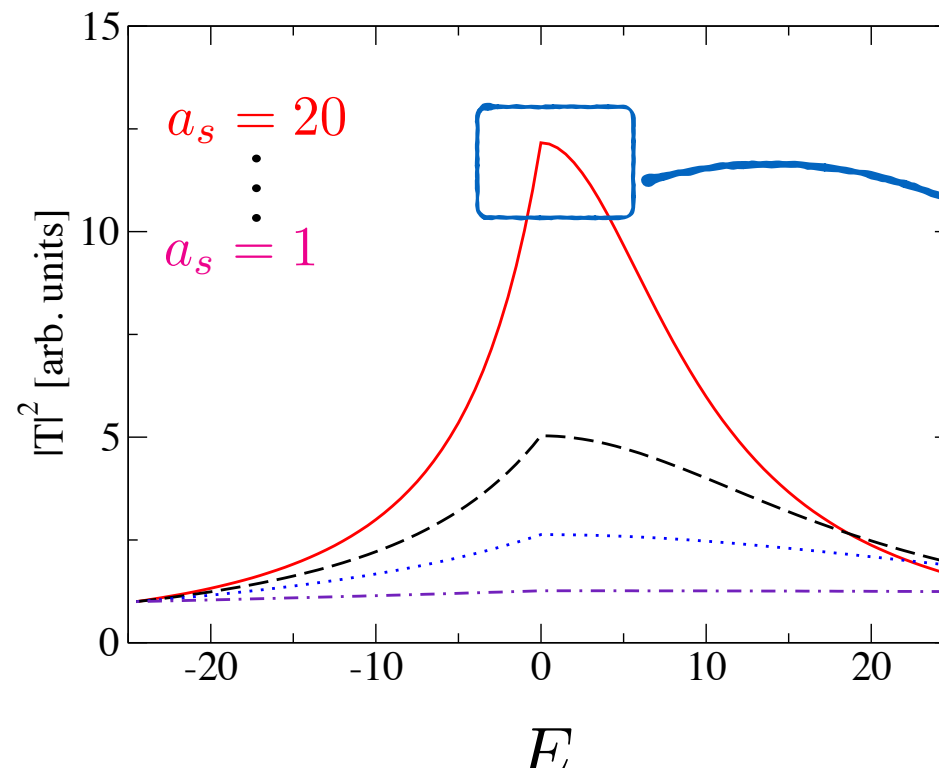
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Prominent Cusp
=> Virtual State

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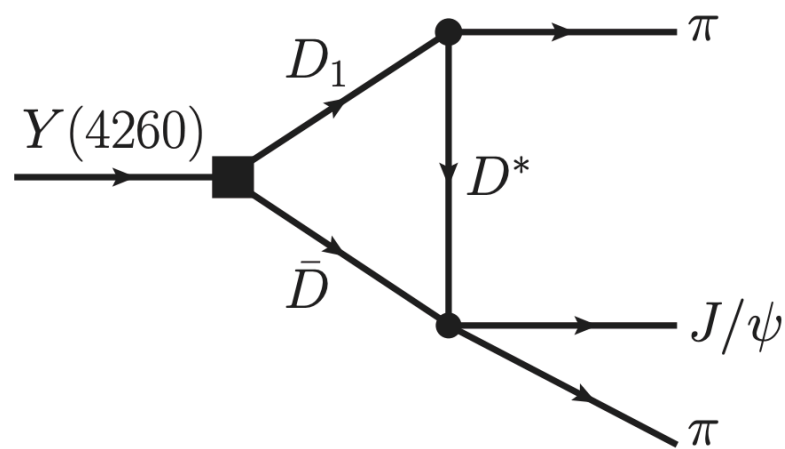
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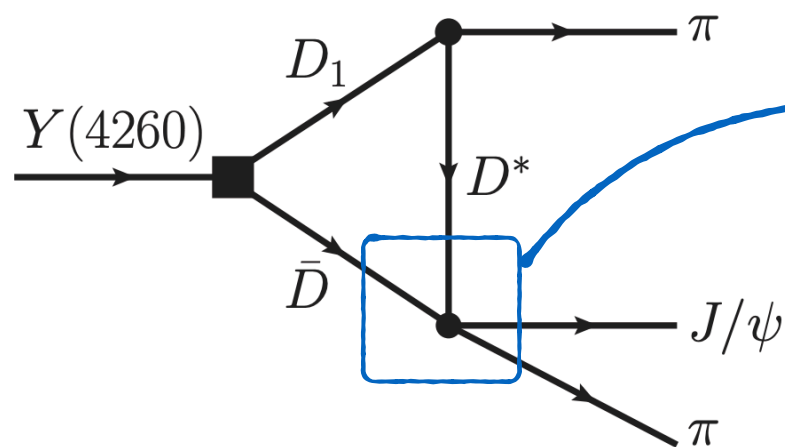


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📌 Rescattering Can Cause Logarithmic Singularity

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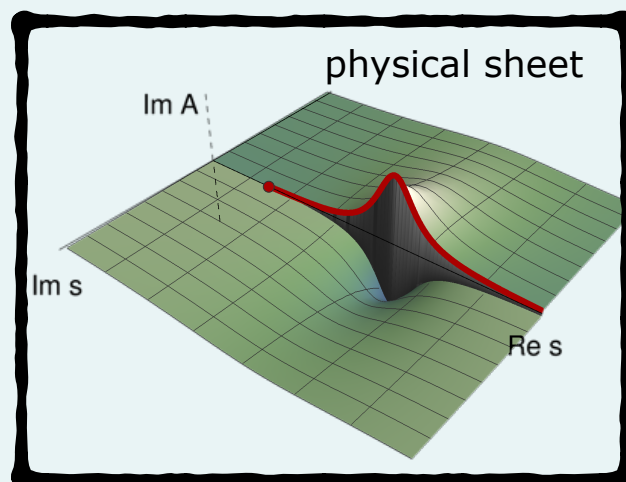
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 - Cusps (Opening of Nearby Multi-Particle Thresholds)
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- Cusp/Triangle Singularity and State (which is a Pole) may both be Present in Experimental Data

Scattering Overview: What Is A State?

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📌 Type of States:

1. Bound states: Poles on the real axis of complex energy plane, below threshold of the Physical (first) Sheet.



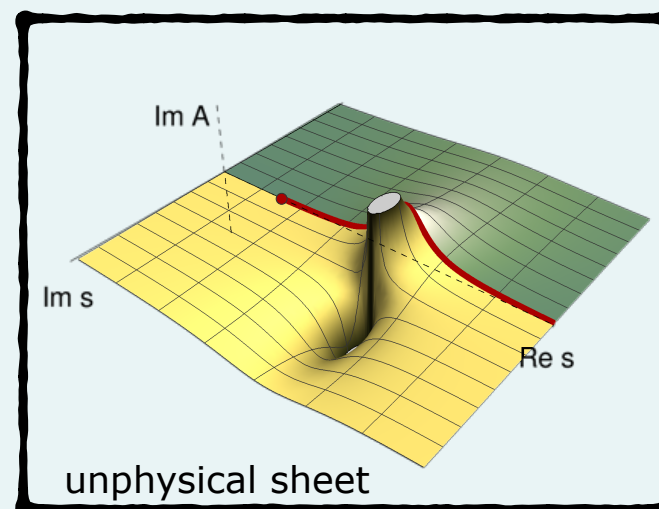
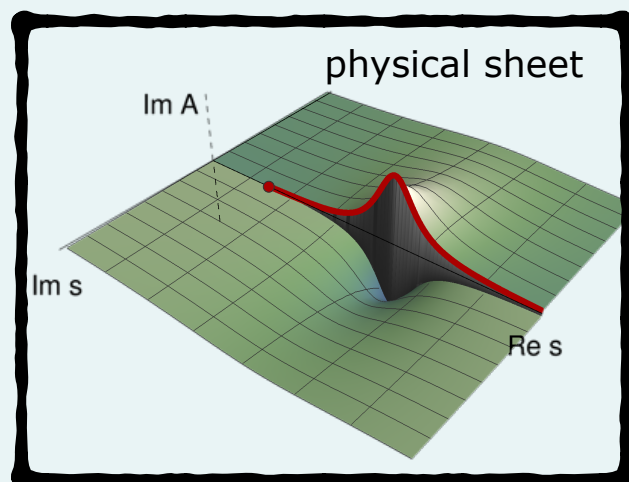
PDG, resonances review

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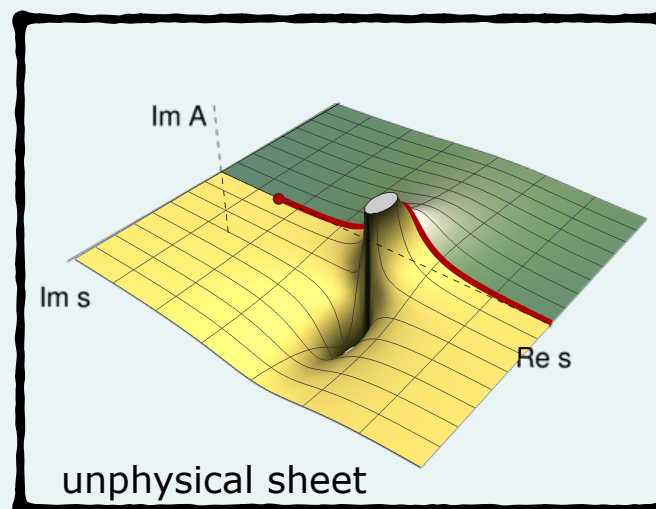
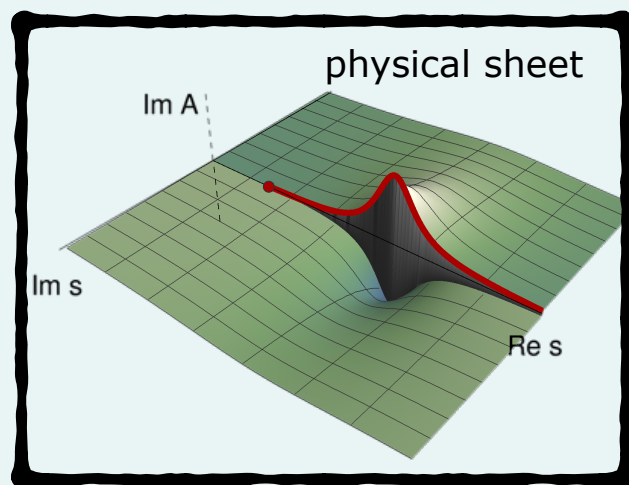
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E.g., $I = 1$, $S = 0$ nucleon-nucleon scattering ([arxiv:1705.00141](https://arxiv.org/abs/1705.00141))



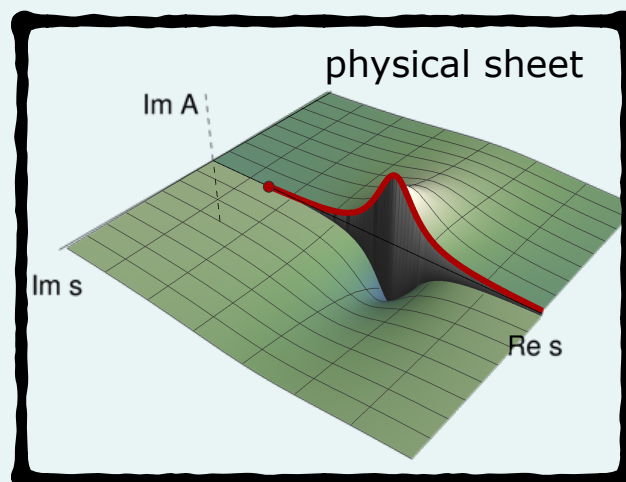
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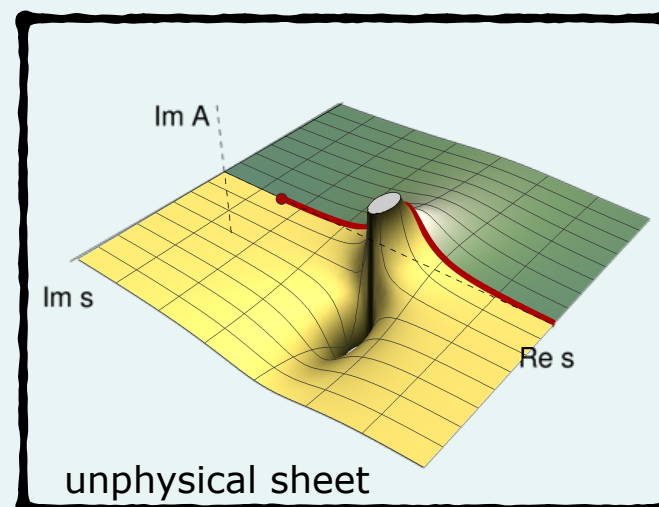
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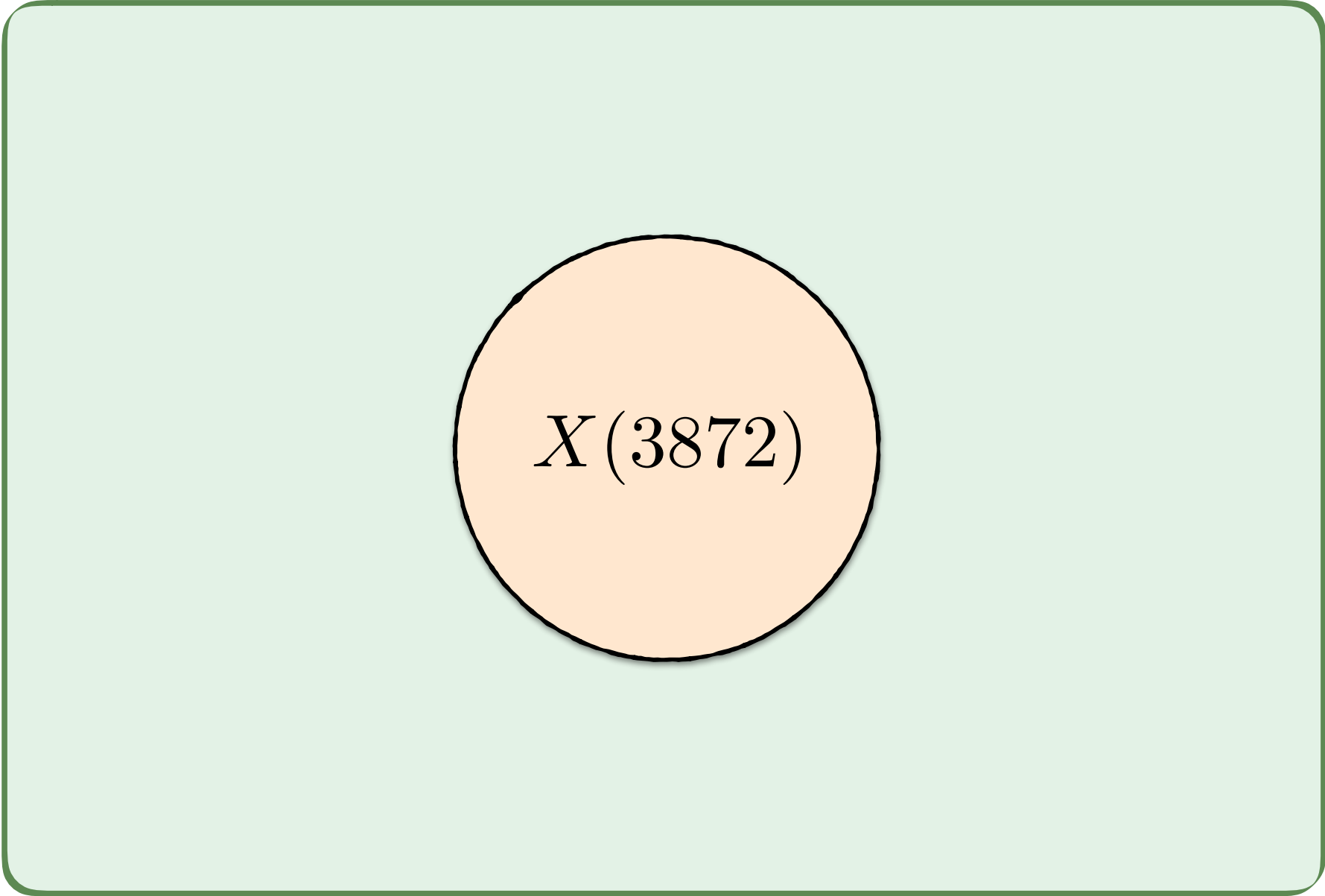


PDG, resonances review



[arxiv:2007.05329](https://arxiv.org/abs/2007.05329)
*Shallow Virtual States are
predominantly Molecular.*

$\chi_{c1}(3872)$ aka $X(3872)$



$X(3872)$

$\chi_{c1}(3872)$ aka $X(3872)$

📌 Notable Decays

$$\mathcal{B}(\pi^+ \pi^- J/\psi) > 3.2\%$$

$$\mathcal{B}(D^0 \bar{D}^*) > 30\%$$

$$\mathcal{B}(\rho^0 J/\psi) \sim \mathcal{B}(\omega J/\psi)$$

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*Annihilation Effects Suppressed =
 $\bar{c}c$ minimal valence components*

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$$M_{PDG} = 3871.69 \pm 0.17 \text{ MeV}$$

$$\Gamma_{PDG} < 1.2 \text{ MeV}$$

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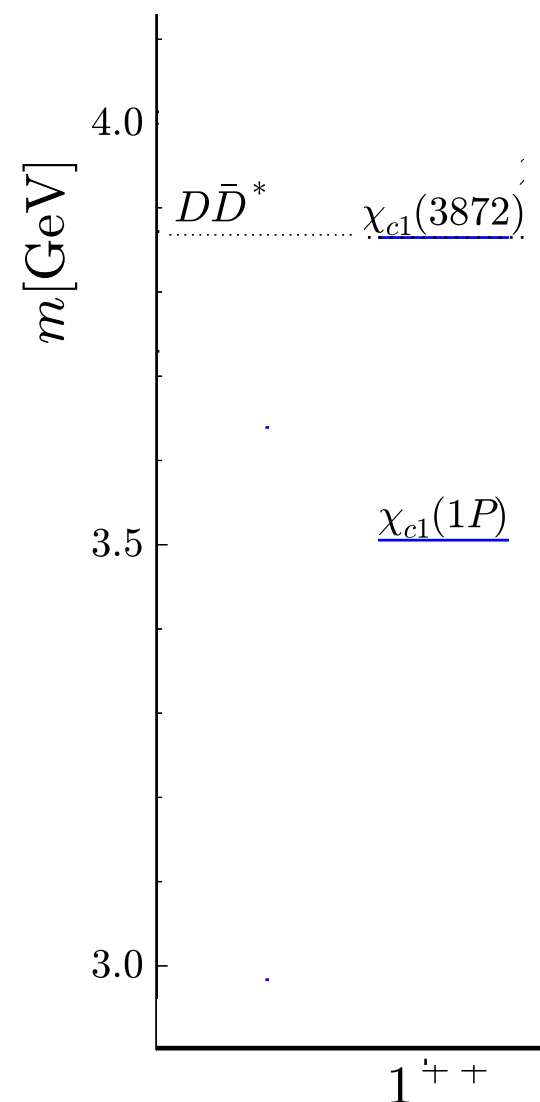
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*S-wave Threshold =
Kinematical
Singularities Possible*

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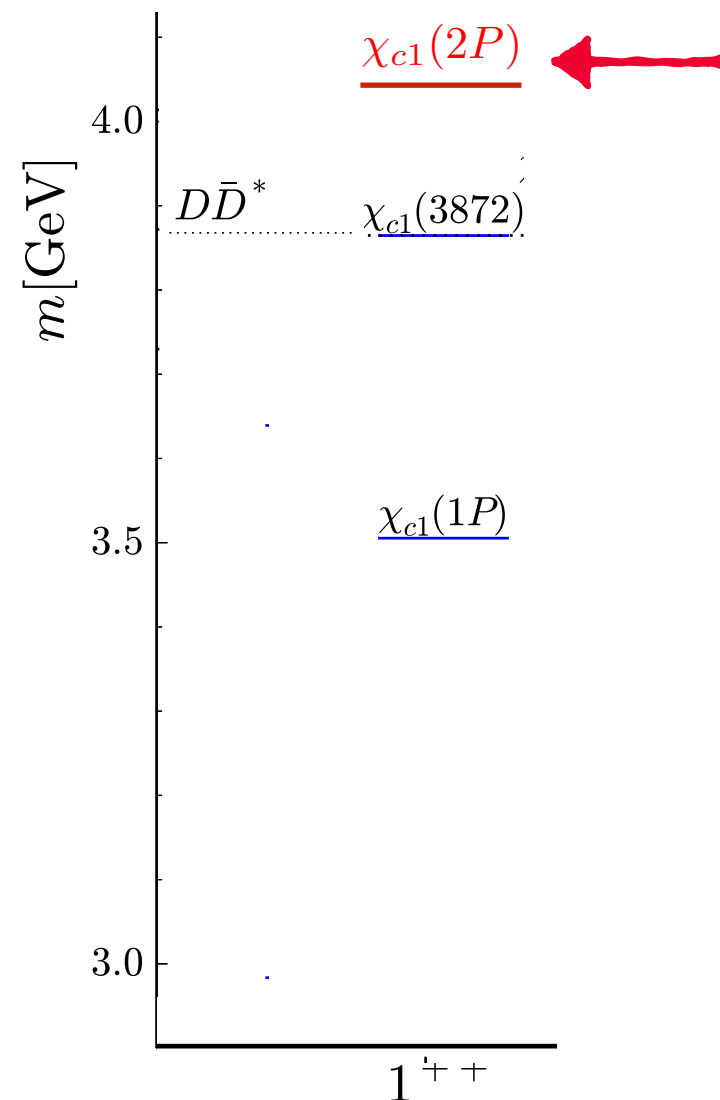
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Potential Model with $\bar{c}c$

[arxiv:1302.6857](https://arxiv.org/abs/1302.6857)

$\chi_{c1}(3872)$ aka $X(3872)$

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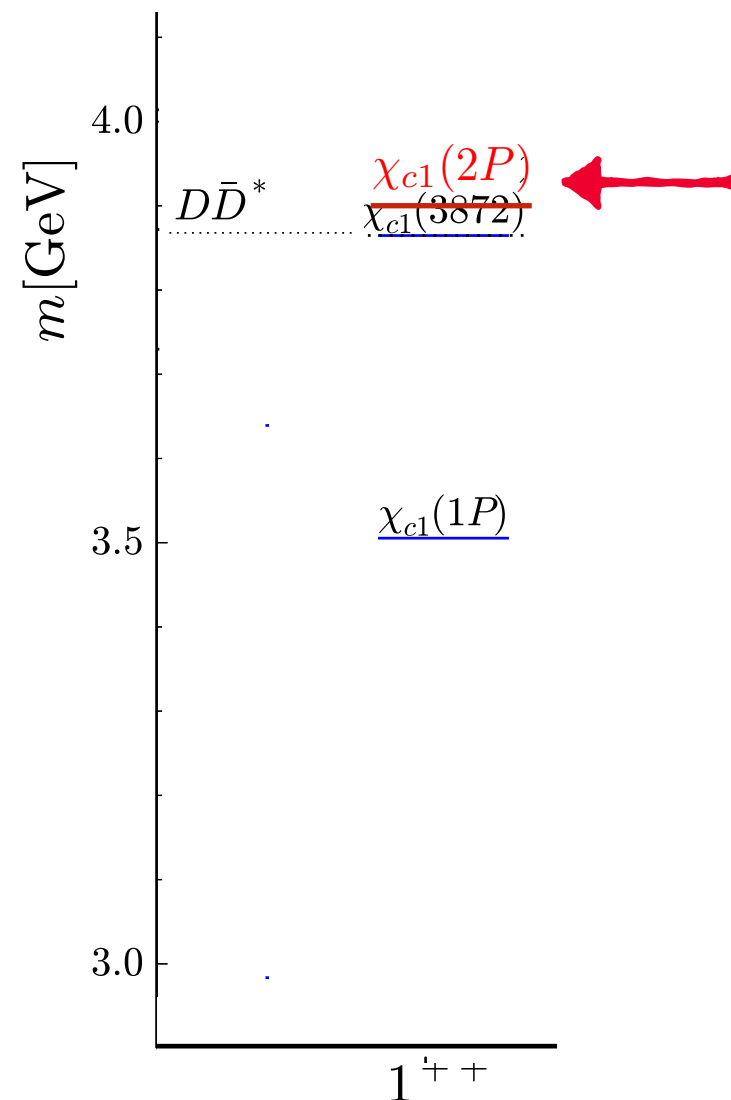
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*Potential Model with $\bar{c}c$
and meson-meson couplings*

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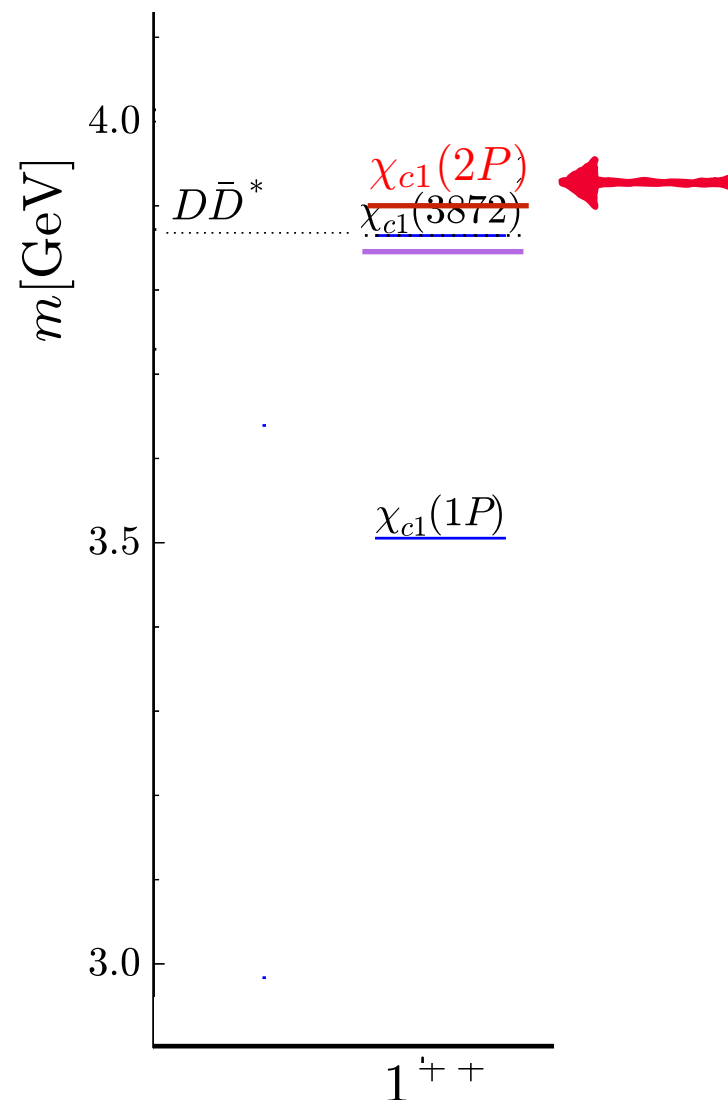
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$$\Gamma_{PDG} < 1.2 \text{ MeV}$$

[arxiv:1503.03257](https://arxiv.org/abs/1503.03257)

| $X(3872)$ | $m_X - m_{D_0} - m_{D_0^*}$ |
|-----------------|-----------------------------|
| Lat. | -8(15) |
| Lat. - O^{4q} | -9(8) |
| LQCD [17] | -11(7) |
| LQCD [18] | -13(6) |

Lattice QCD



Potential Model with $\bar{c}c$
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$$\delta = M_D + M_{D^*} - M_X = 0.0 \pm 180 \text{ keV}$$

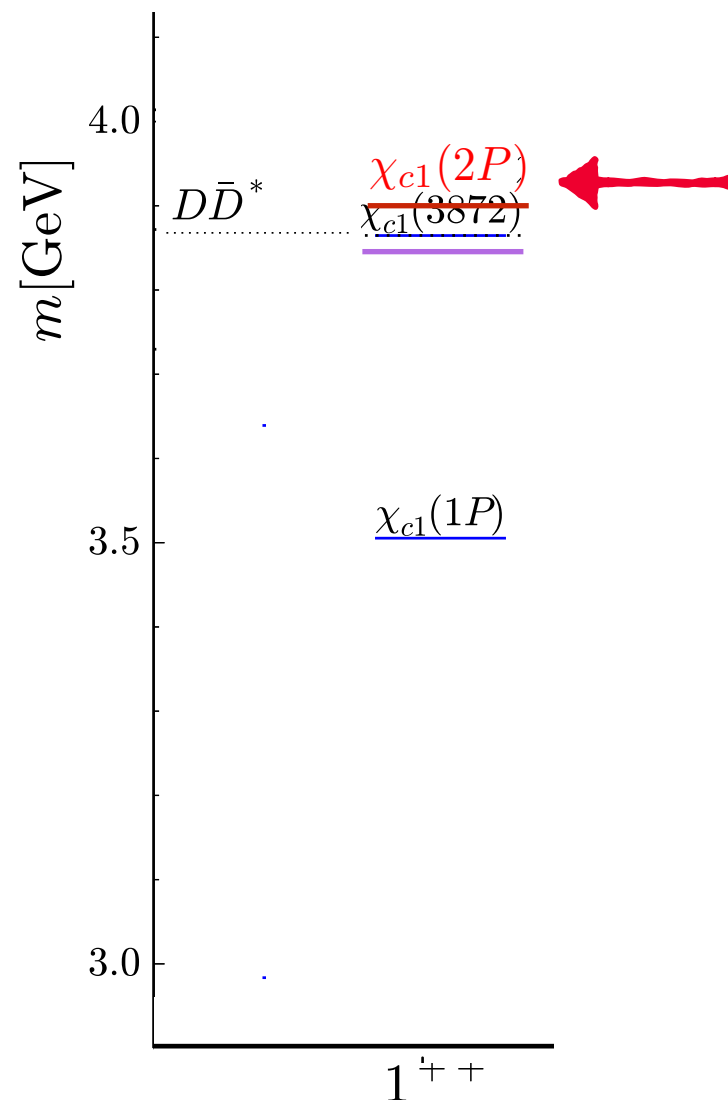
$$\Gamma_{PDG} < 1.2 \text{ MeV}$$

[arxiv:1503.03257](https://arxiv.org/abs/1503.03257)

| $X(3872)$ | $m_X - m_{D_0} - m_{D_0^*}$ |
|-----------------|-----------------------------|
| Lat. | -8(15) |
| Lat. - O^{4q} | -9(8) |
| LQCD [17] | -11(7) |
| LQCD [18] | -13(6) |

- 📌 $\bar{c}c$ and DD^* important
- 📌 Diquarks not important
- 📌 Find Bound State Pole

Lattice QCD



Potential Model with $\bar{c}c$ and meson-meson couplings

[arxiv:1302.6857](https://arxiv.org/abs/1302.6857)

$\chi_{c1}(3872)$ aka $X(3872)$

📌 Notable Decays

$$\mathcal{B}(\pi^+\pi^-J/\psi) > 3.2\%$$

$$\mathcal{B}(D^0\bar{D}^{0*}) > 30\%$$

$$\mathcal{B}(\rho^0 J/\psi) \sim \mathcal{B}(\omega J/\psi)$$

$$M_{PDG} = 3871.69 \pm 0.17 \text{ MeV}$$

$$\delta = M_D + M_{D^*} - M_X = 0.0 \pm 180 \text{ keV}$$

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📌 Quantum Numbers

$$J^{PC} = 1^{++}$$

$$Q = 0$$

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$$\begin{array}{cc} I = 1 & I = 0 \\ \mathcal{B}(\rho^0 J/\psi) \sim \mathcal{B}(\omega J/\psi) \end{array}$$

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Kinematically Allowed since $5 \text{ MeV} < M_X$ and $\Gamma(\rho) = 150 \text{ MeV}$

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Kinematically Suppressed as $7 \text{ MeV} > M_X$ and $\Gamma(\omega) = 8 \text{ MeV}$

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Kinematically Suppressed as $7 \text{ MeV} > M_X$ and $\Gamma(\omega) = 8 \text{ MeV}$

📌 $X(3872)$ is $I = 0$, if molecular then $\sim |D^0\bar{D}^{0*}\rangle + |D^+D^{*-}\rangle + \text{c.c.}$

📌 Isospin violations occurs in decays due to 8 MeV mass difference between $|D^0\bar{D}^{0*}\rangle$ and $|D^+\bar{D}^{*-}\rangle$ ([arxiv:1711.01930](https://arxiv.org/abs/1711.01930))

$\chi_{c1}(3872)$ aka $X(3872)$

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📌 Pole Structure: [arxiv:2005.13419](https://arxiv.org/abs/2005.13419)

- Pure Cusp ruled out.
- Virtual or Bound State Compatible With Data

$\chi_{c1}(3872)$ aka $X(3872)$

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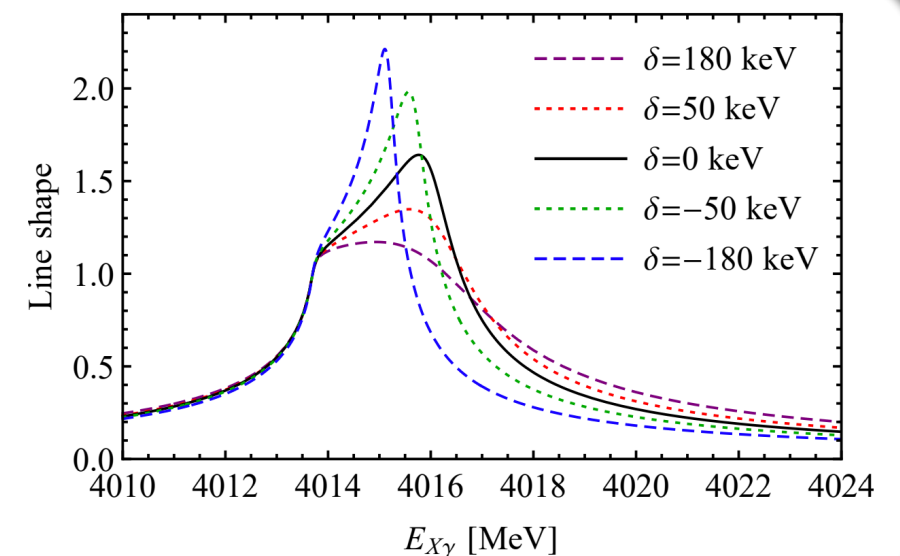
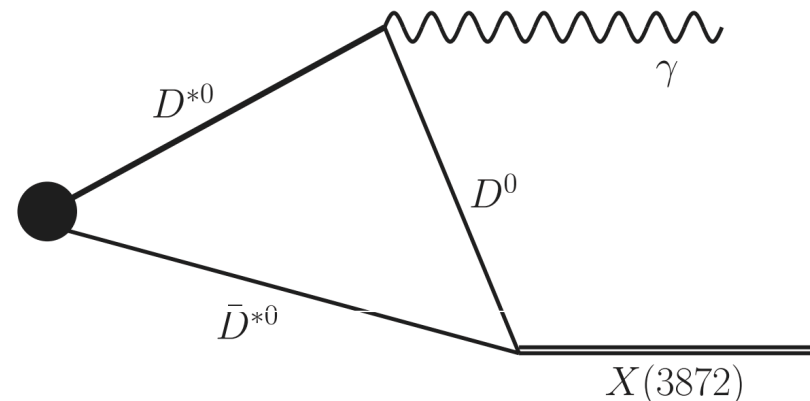
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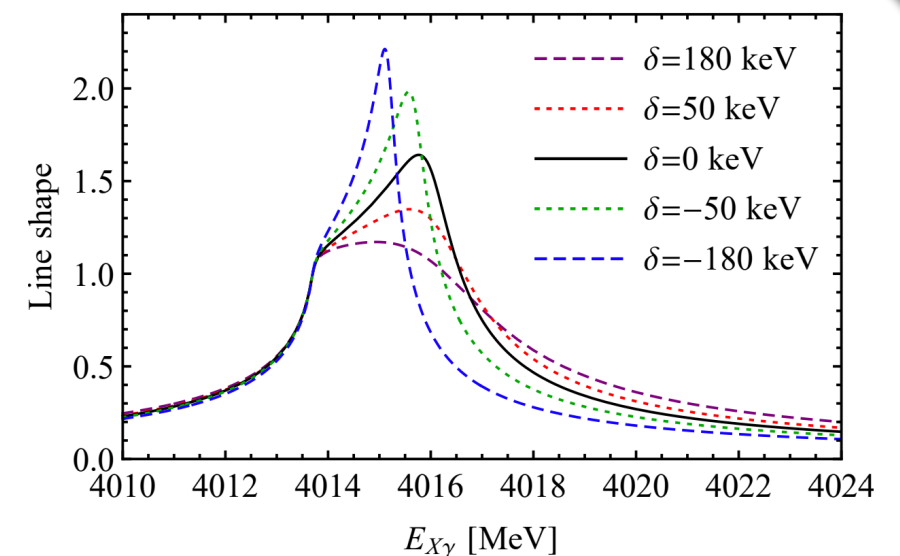
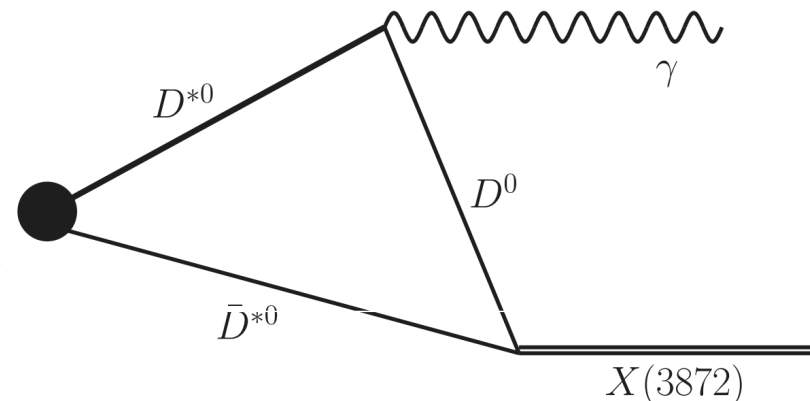
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📌 Needs large number of low energy $D^{0*}\bar{D}^{0*}$



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- Molecular $D^0\bar{D}^{0*} + \chi_{c1}(2P)$: Lattice / Pheno / (Sum Rules [arxiv:1812.08207](https://arxiv.org/abs/1812.08207))

$\chi_{c1}(3872)$ aka $X(3872)$

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- But Compact Tetraquarks Proposed: [arxiv:1611.07920](https://arxiv.org/abs/1611.07920)

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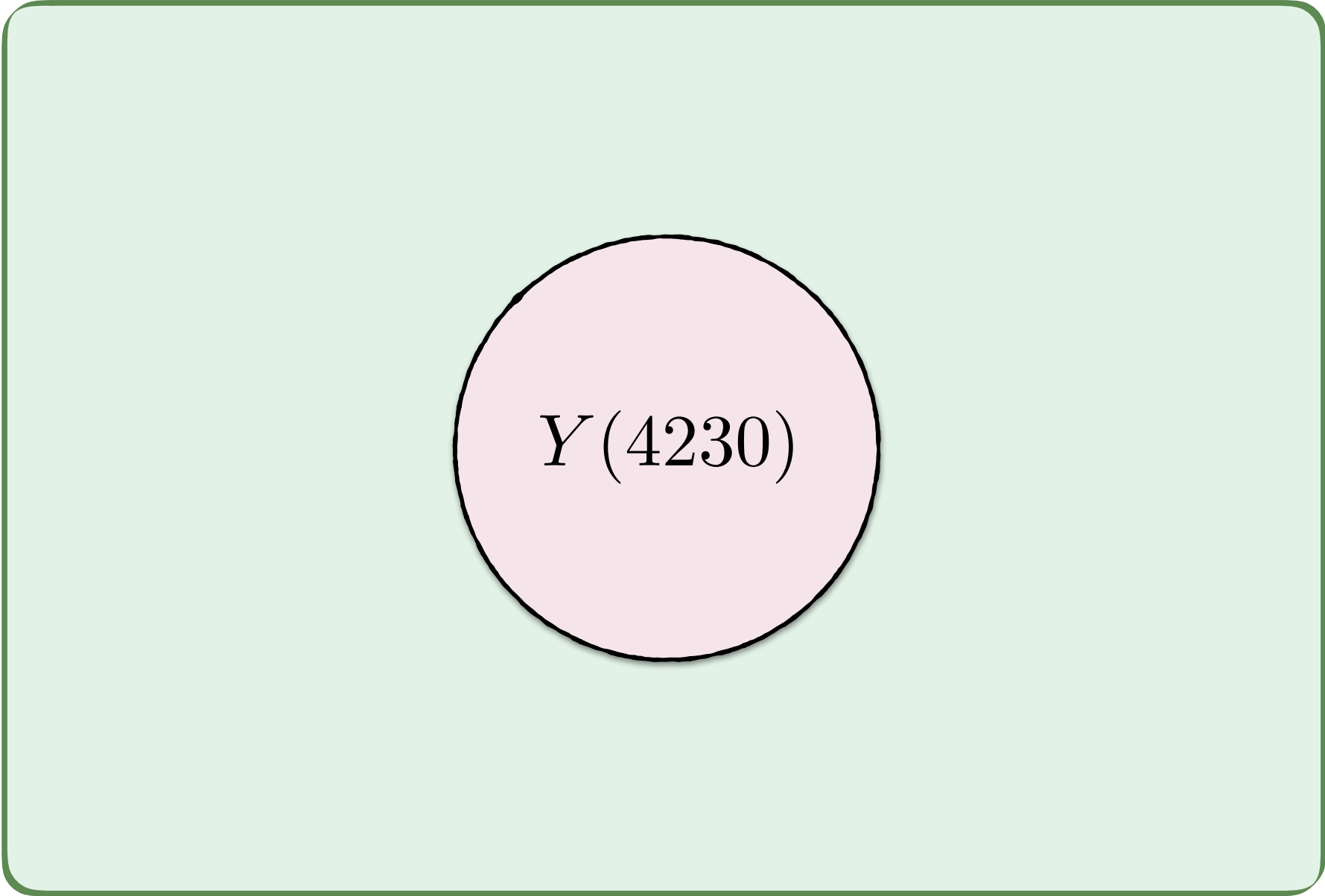
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📌 Debates: Prompt Production [arxiv:1709.09631](https://arxiv.org/abs/1709.09631), [arxiv:1709.09101](https://arxiv.org/abs/1709.09101)

$\psi(4230)$ aka $Y(4230)$ aka $Y(4260)$



$Y(4230)$

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- Seen $\mathcal{B}(\pi^+\pi^-J/\psi)$ $\mathcal{B}(\pi^+\pi^-h_c)$ $\mathcal{B}(\pi^+D^{*-}D^0)$ $\mathcal{B}(\gamma X(3872))$

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*Annihilation Effects Suppressed =
 $\bar{c}c$ minimal valence components*

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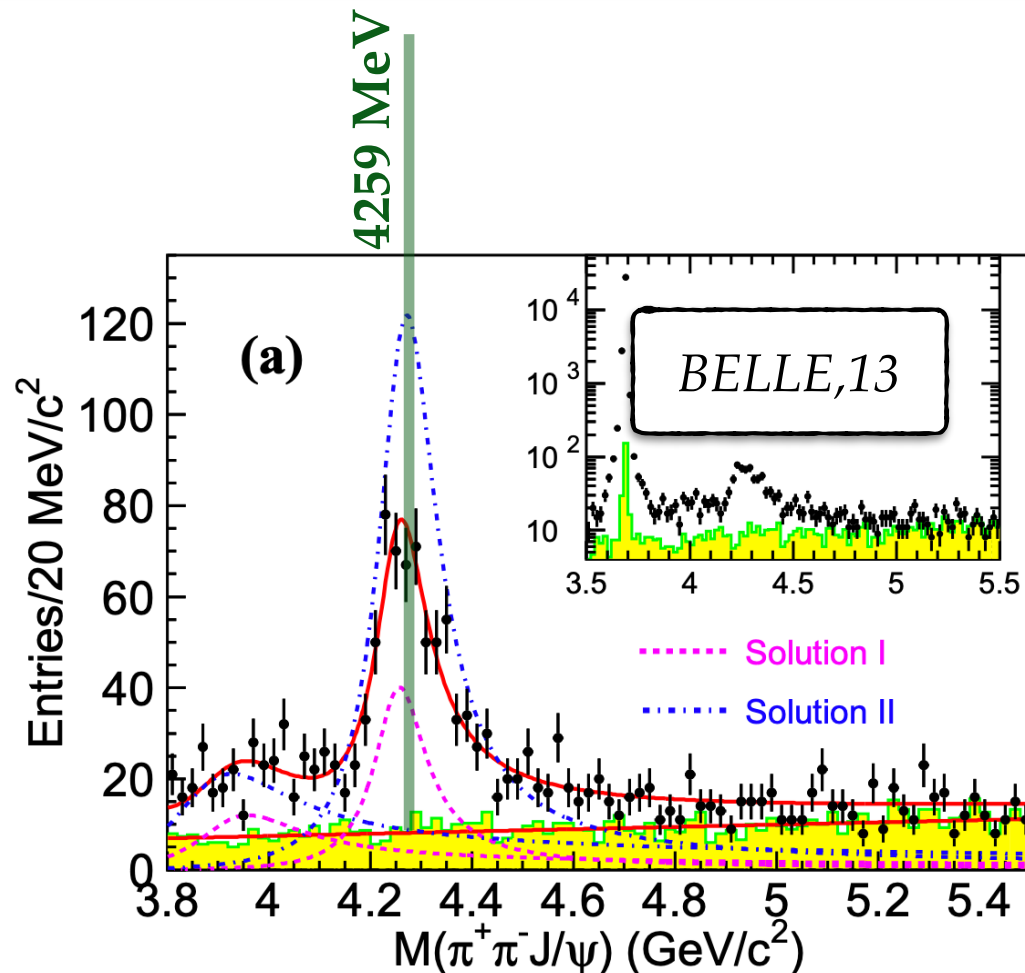
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$$\bullet M_{PDG} = 4220 \pm 15 \text{ MeV}$$

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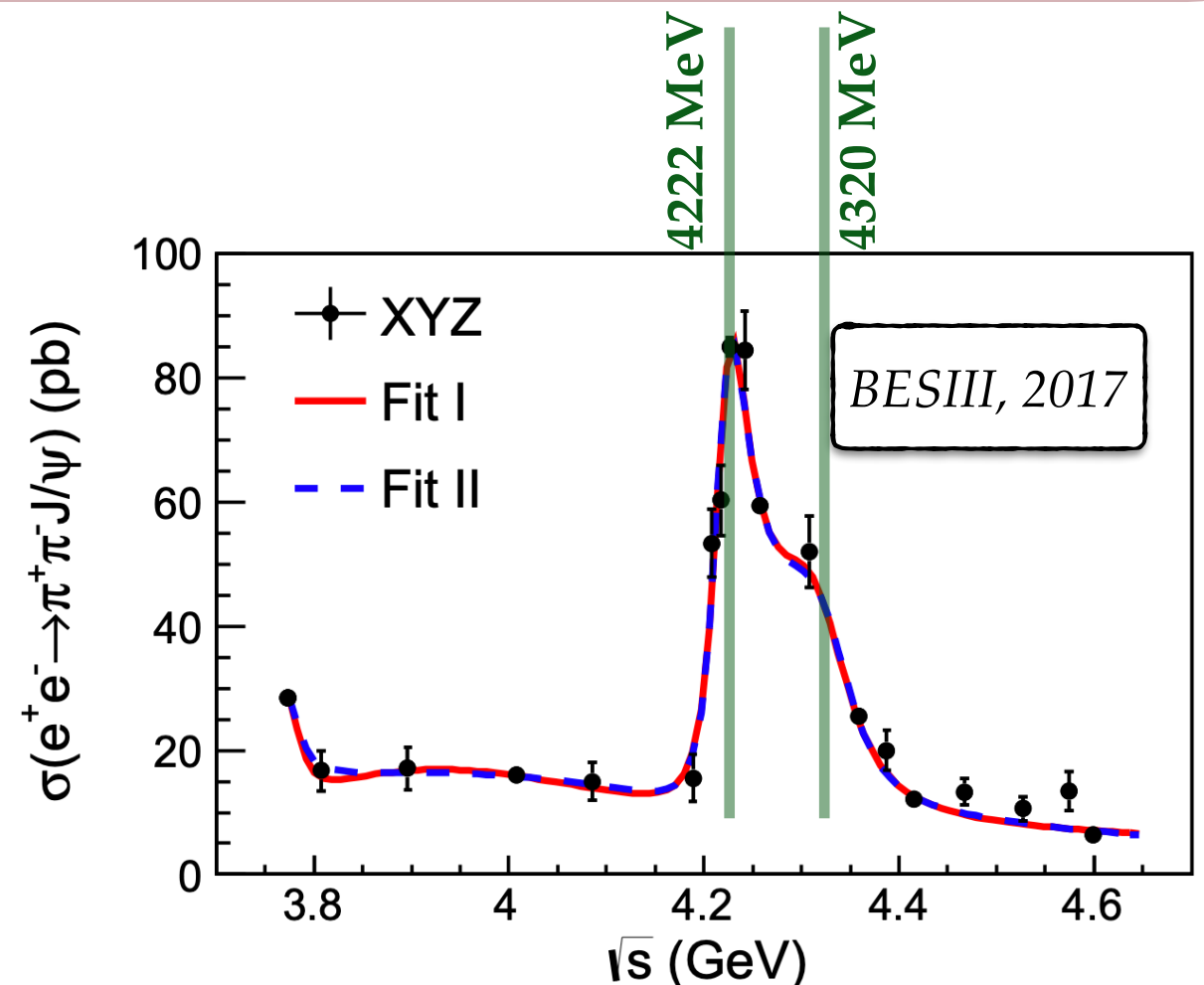
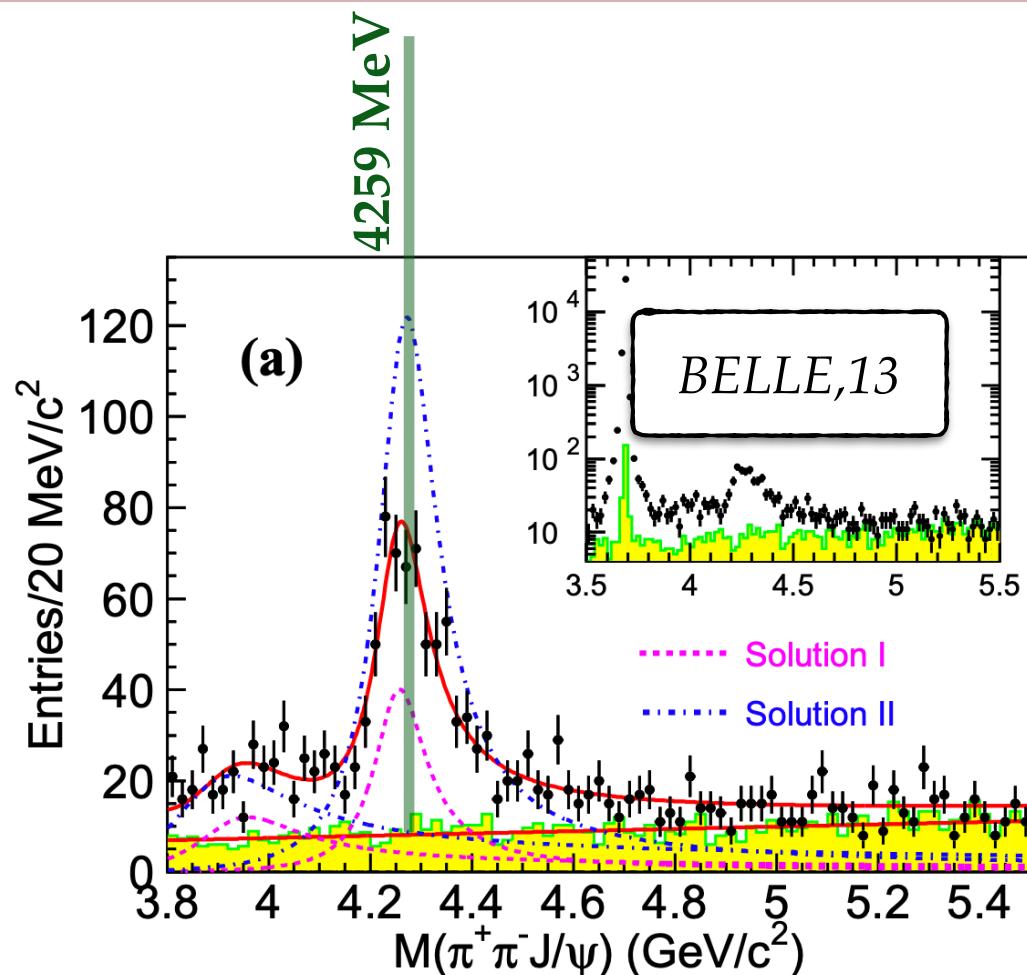
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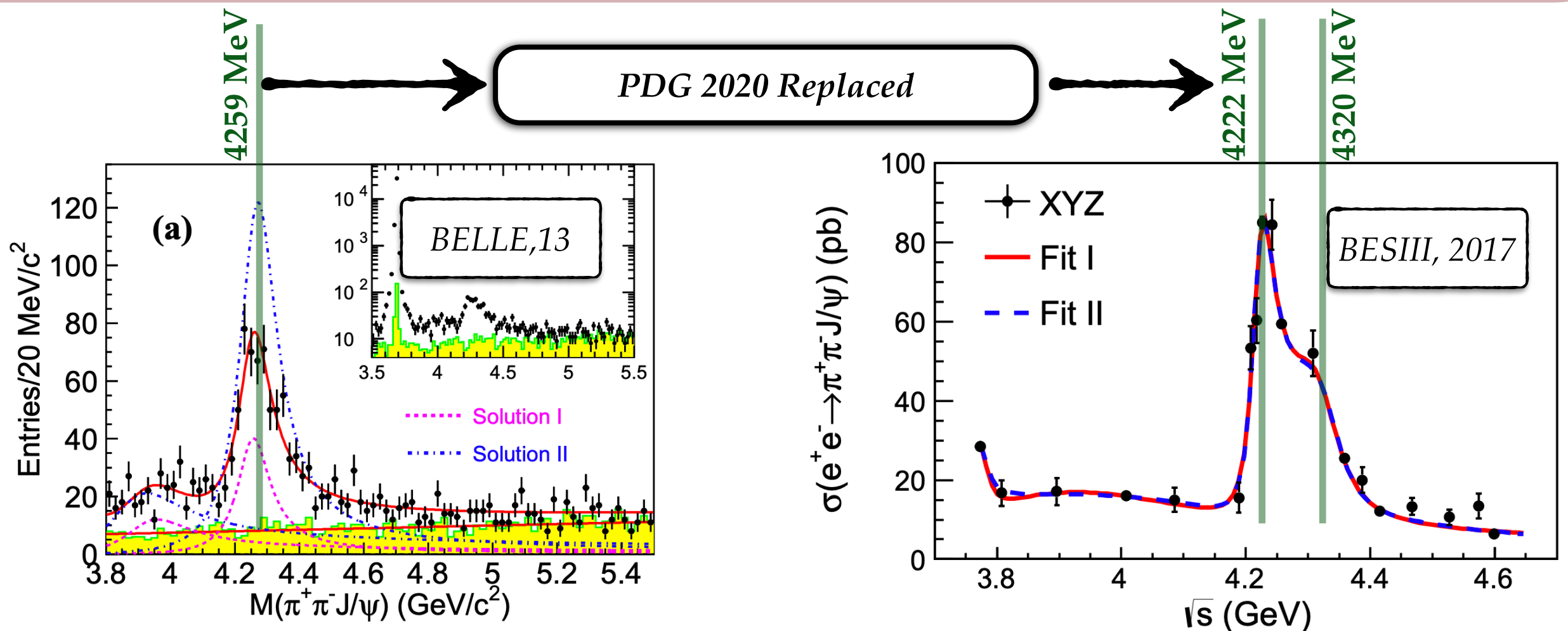
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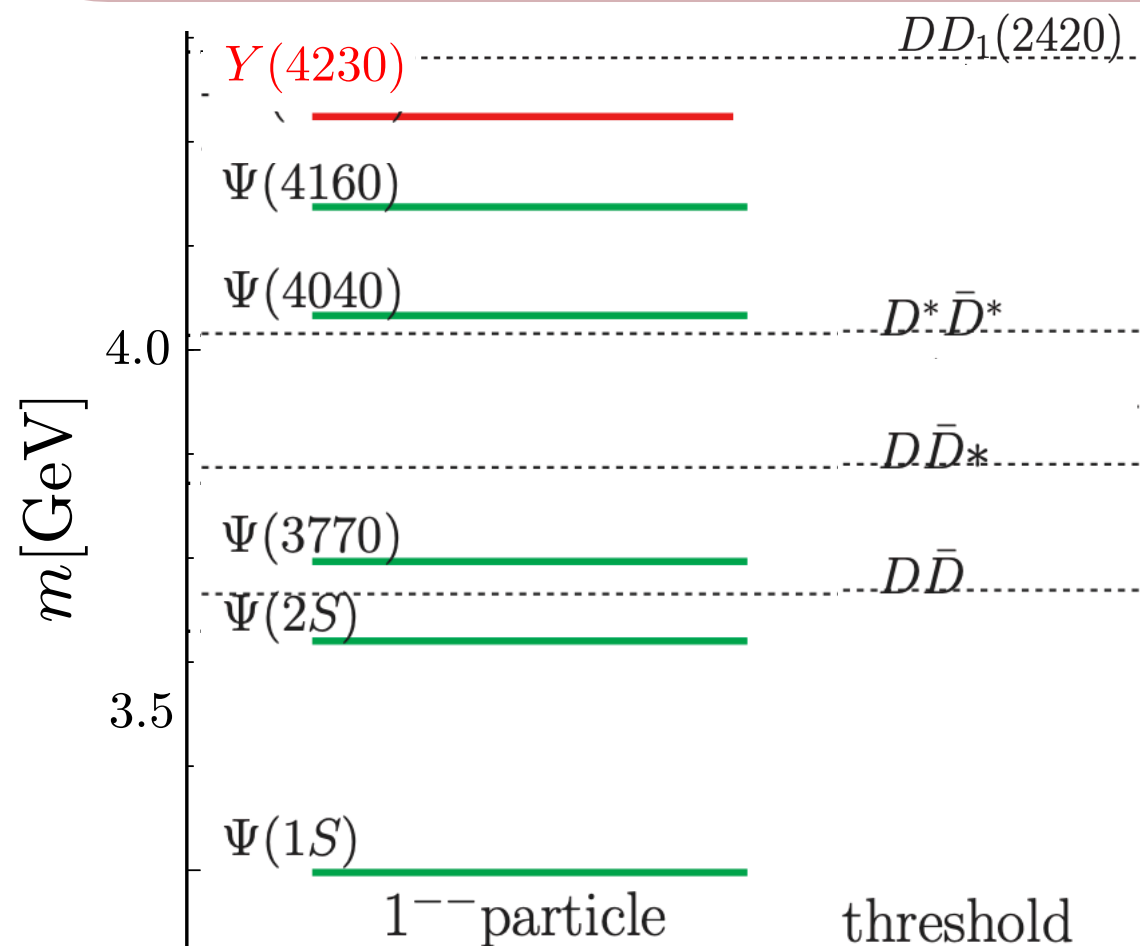
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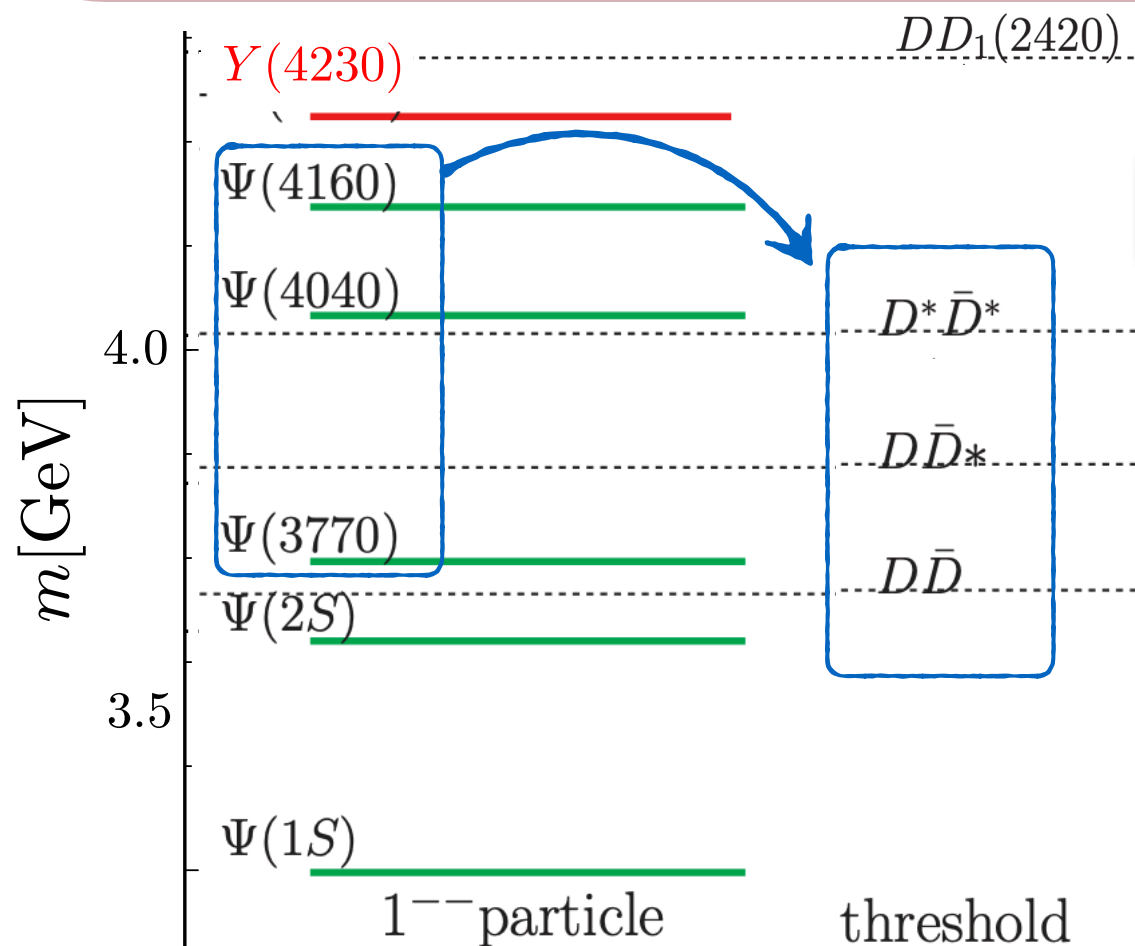
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Charmonium states decay to open flavour thresholds

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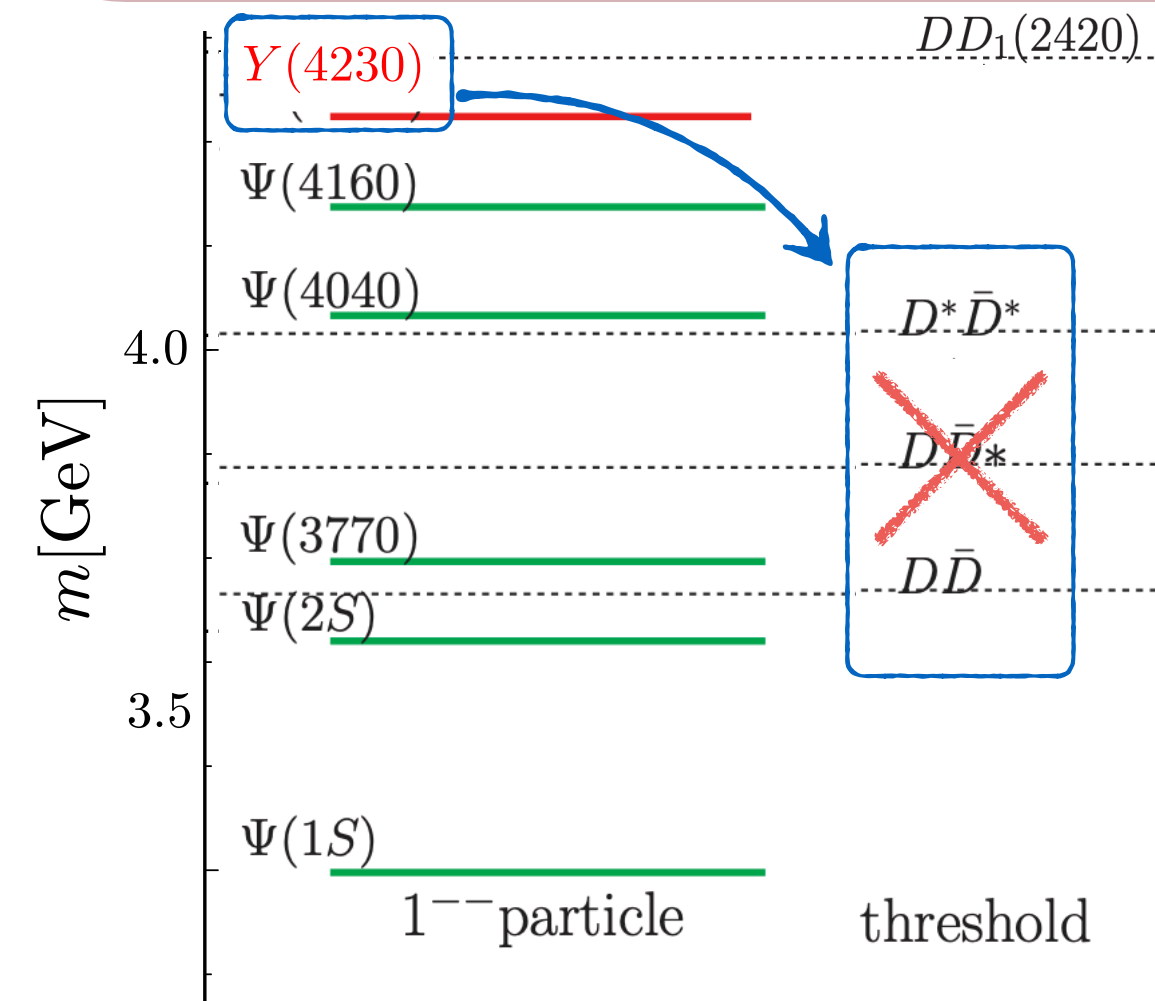
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- **Not Seen:** Any Open-Charm Decays, e.g, $\mathcal{B}(D\bar{D})$

$$\bullet M_{PDG} = 4220 \pm 15 \text{ MeV}$$

$$\bullet \Gamma_{PDG} = 20 - 100 \text{ MeV}$$



$Y(4230)$ cannot contain $\bar{c}c$ as it does not decay to open charm!

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Quantum Numbers

$$J^{PC} = 1^{--}$$

$$Q = 0$$

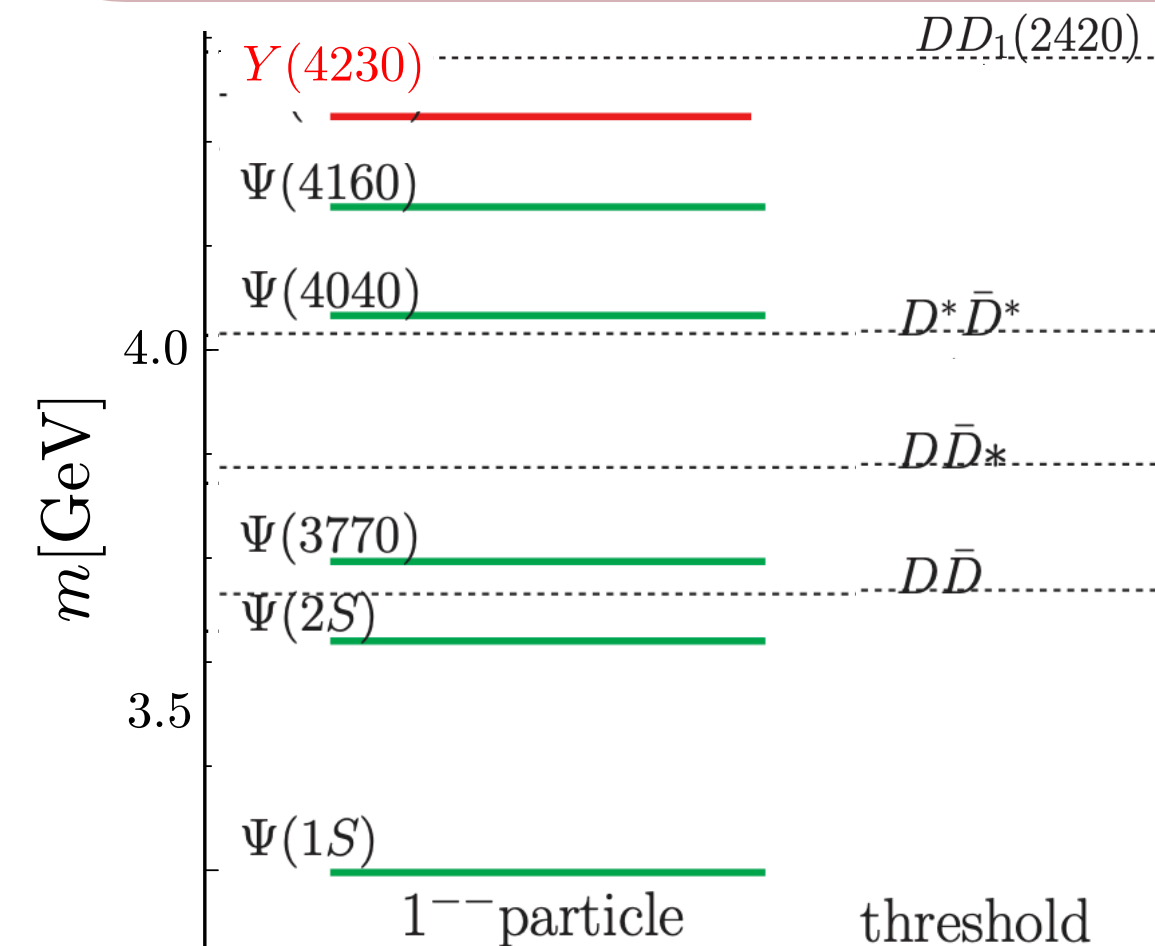
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Notable Decays

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- Not Seen: Any Open-Charmed Decays, e.g, $\mathcal{B}(D\bar{D})$

$$\bullet M_{PDG} = 4220 \pm 15 \text{ MeV}$$

$$\bullet \Gamma_{PDG} = 20 - 100 \text{ MeV}$$



Scenario 1: $D\bar{D}_1(2420)$ Molecular State

$\psi(4230)$ aka $Y(4230)$ aka $Y(4260)$

Quantum Numbers

$$J^{PC} = 1^{--}$$

$$Q = 0$$

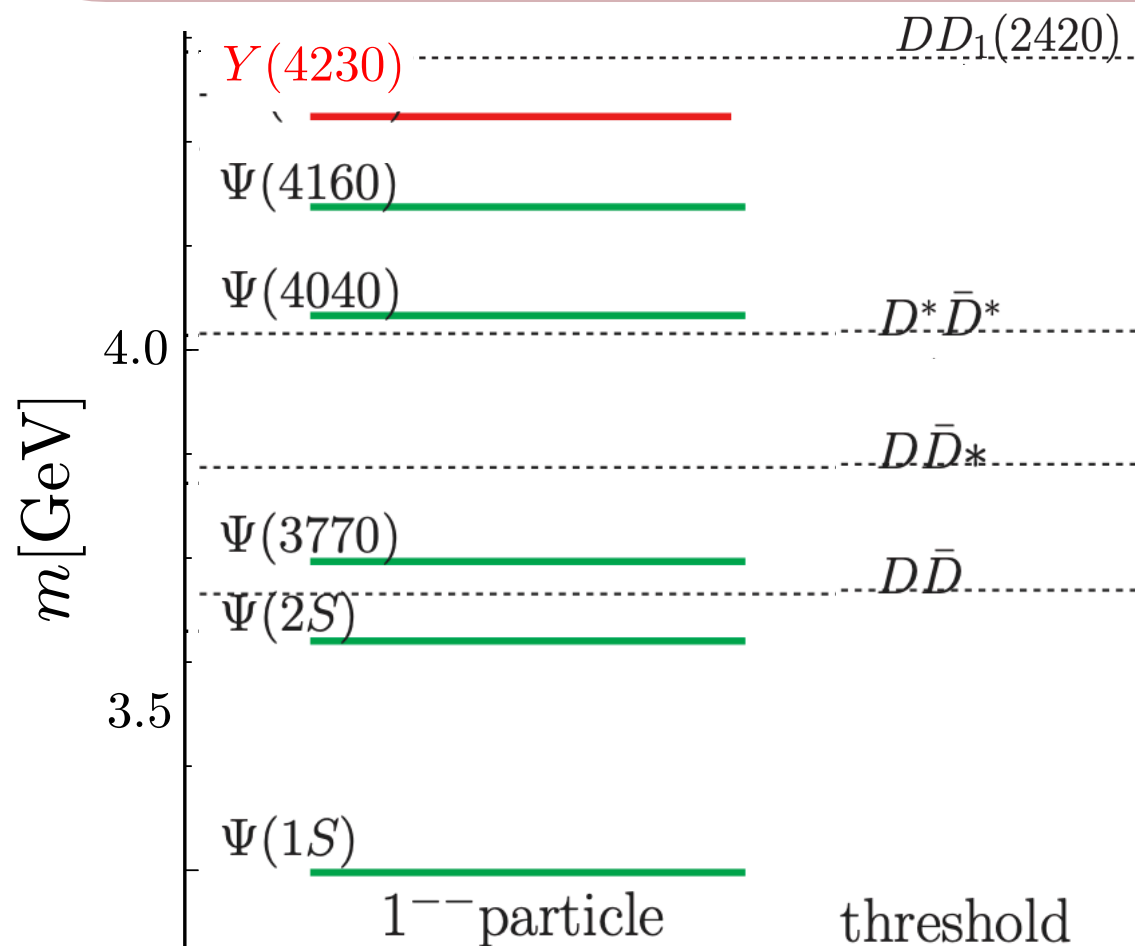
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Scenario 1: $D\bar{D}_1(2420)$ Molecular State

- $M_Y - M_{D\bar{D}_1} = -65 \text{ MeV}$ within reason for potential models ([arxiv:1910.14455](https://arxiv.org/abs/1910.14455))

$\psi(4230)$ aka $Y(4230)$ aka $Y(4260)$

Quantum Numbers

$$J^{PC} = 1^{--}$$

$$Q = 0$$

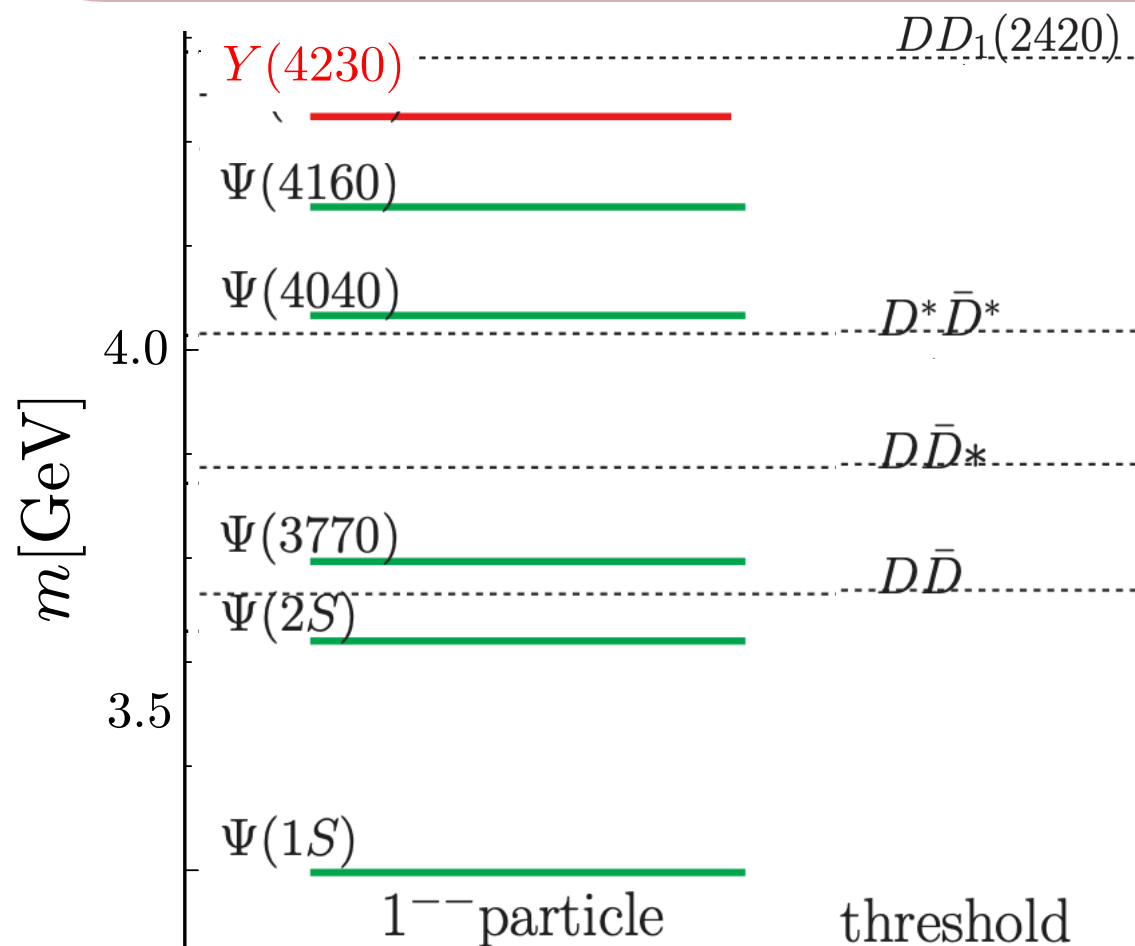
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- Not Seen: Any Open-Charm Decays, e.g, $\mathcal{B}(D\bar{D})$

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- Molecular States decay through constituents: explains decay patterns ([arxiv:1306.3096](https://arxiv.org/abs/1306.3096))

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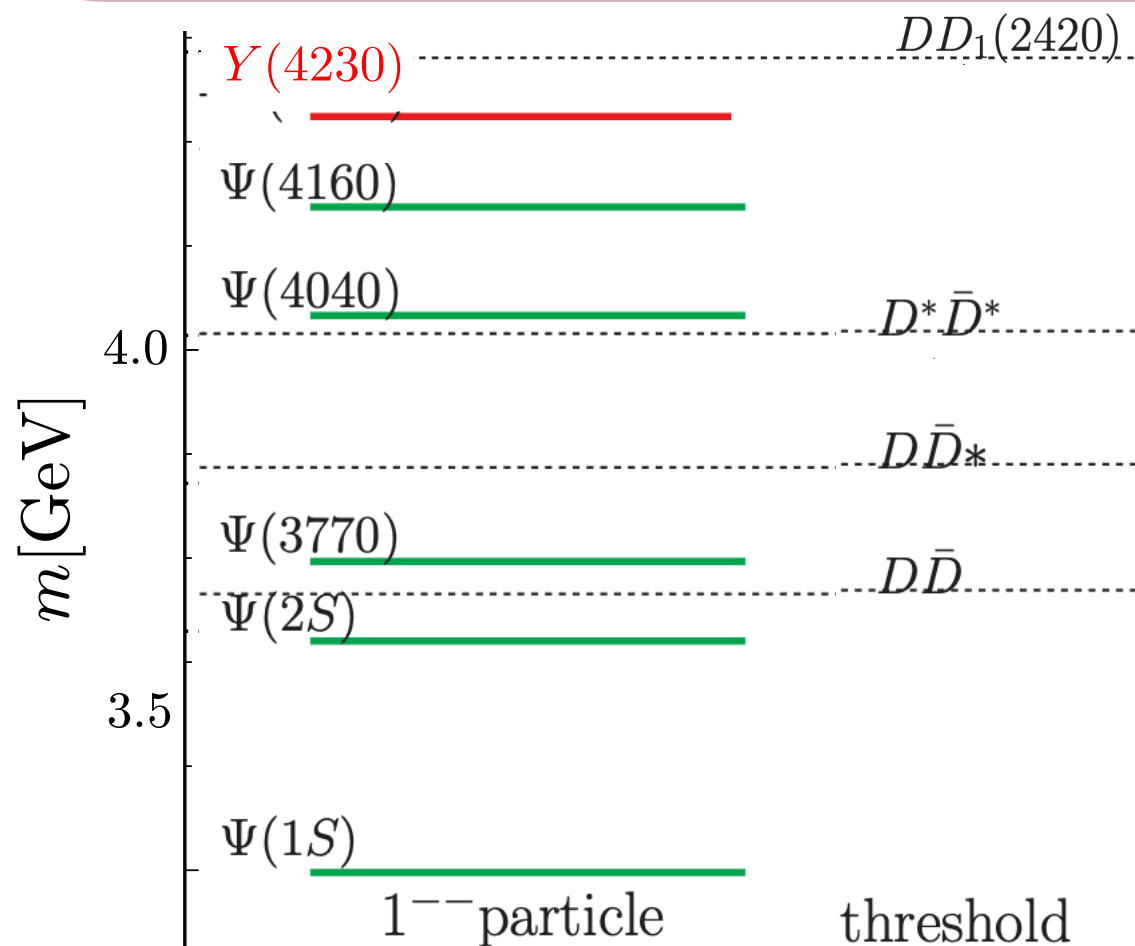
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- Not Seen: Any Open-Charm Decays, e.g, $\mathcal{B}(D\bar{D})$

● $M_{PDG} = 4220 \pm 15 \text{ MeV}$

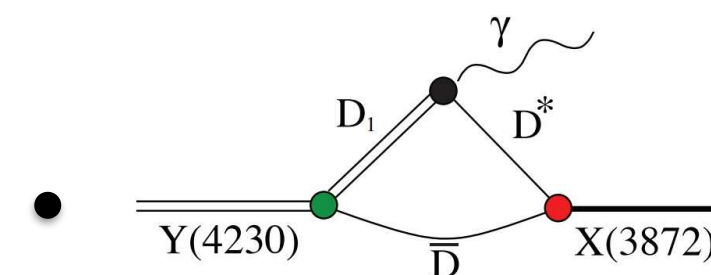
● $\Gamma_{PDG} = 20 - 100 \text{ MeV}$



Scenario 1: $D\bar{D}_1(2420)$ Molecular State

- $M_Y - M_{D\bar{D}_1} = -65 \text{ MeV}$ within reason for potential models ([arxiv:1910.14455](https://arxiv.org/abs/1910.14455))
- Molecular States decay through constituents: explains decay patterns ([arxiv:1306.3096](https://arxiv.org/abs/1306.3096))

● $Y(4230) = D^0\bar{D}_1 \rightarrow D^0\pi^+D^{*-}$



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Quantum Numbers

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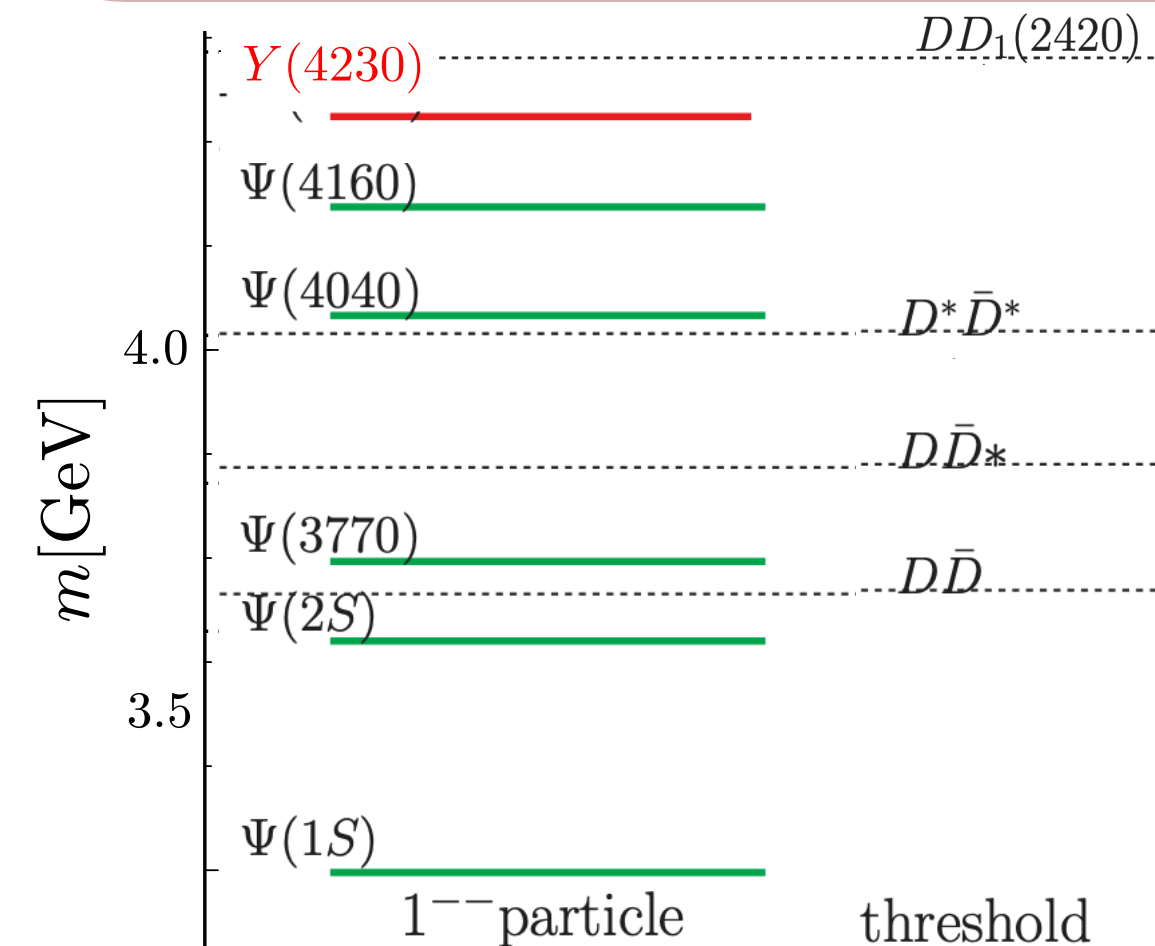
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$$\bullet \Gamma_{PDG} = 20 - 100 \text{ MeV}$$



Scenario 1: $D\bar{D}_1(2420)$ Molecular State

- ([arxiv:1902.10957](https://arxiv.org/abs/1902.10957)) By studying $\pi\pi, Y(4230)$

$\psi(4230)$ aka $Y(4230)$ aka $Y(4260)$

Quantum Numbers

$$J^{PC} = 1^{--}$$

$$Q = 0$$

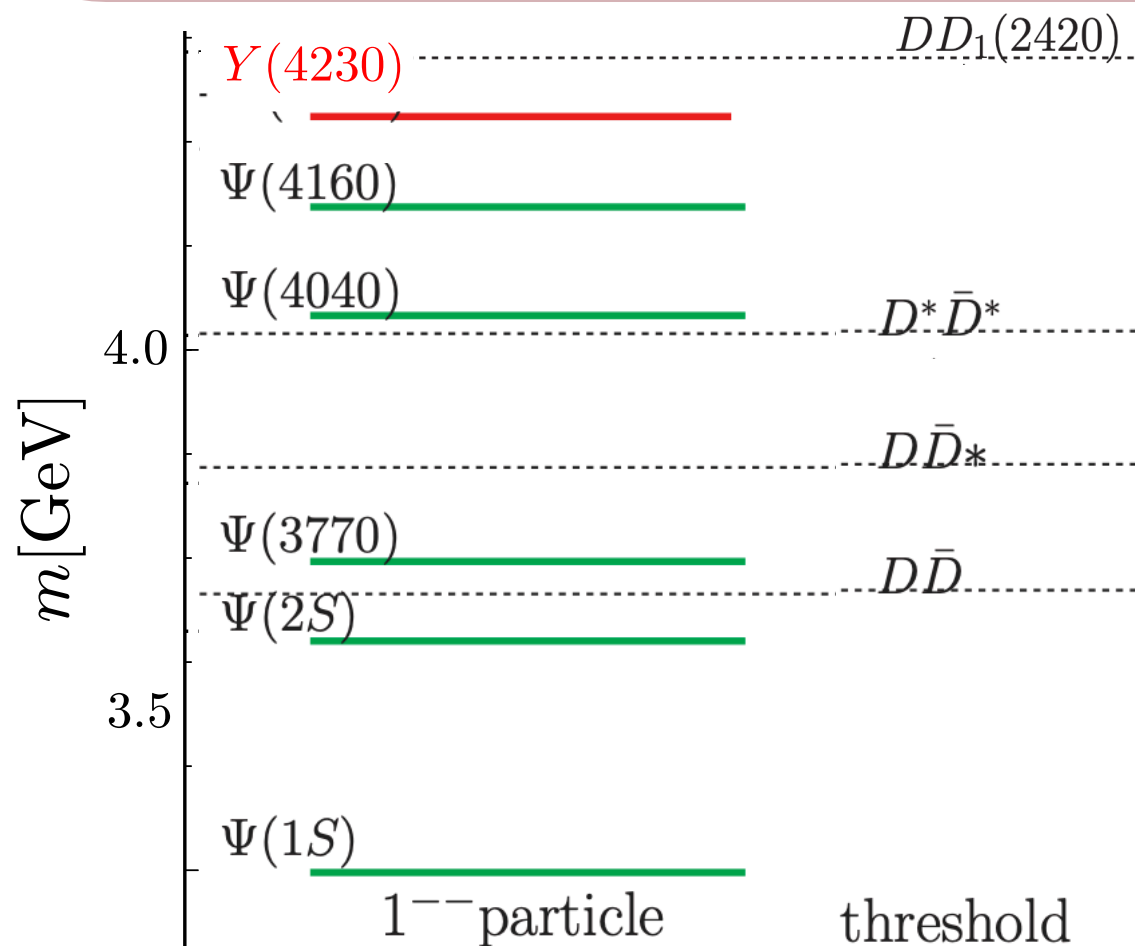
$$I^G = 0^-$$

Notable Decays

- Seen $\mathcal{B}(\pi^+\pi^- J/\psi)$ $\mathcal{B}(\pi^+\pi^- h_c)$ $\mathcal{B}(\pi^+ D^{*-} D^0)$ $\mathcal{B}(\gamma X(3872))$
- Not Seen: Any Open-Charm Decays, e.g, $\mathcal{B}(D\bar{D})$

- $M_{PDG} = 4220 \pm 15 \text{ MeV}$

- $\Gamma_{PDG} = 20 - 100 \text{ MeV}$



Scenario 1: $D\bar{D}_1(2420)$ Molecular State

- ([arxiv:1902.10957](https://arxiv.org/abs/1902.10957)) By studying $\pi\pi, Y(4230)$
 - cannot be fully molecular
 - has sizable SU(3) flavour octet component
=> Cannot be dominated by $\bar{c}c$ or hybrid.

$\psi(4230)$ aka $Y(4230)$ aka $Y(4260)$

Quantum Numbers

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$$Q = 0$$

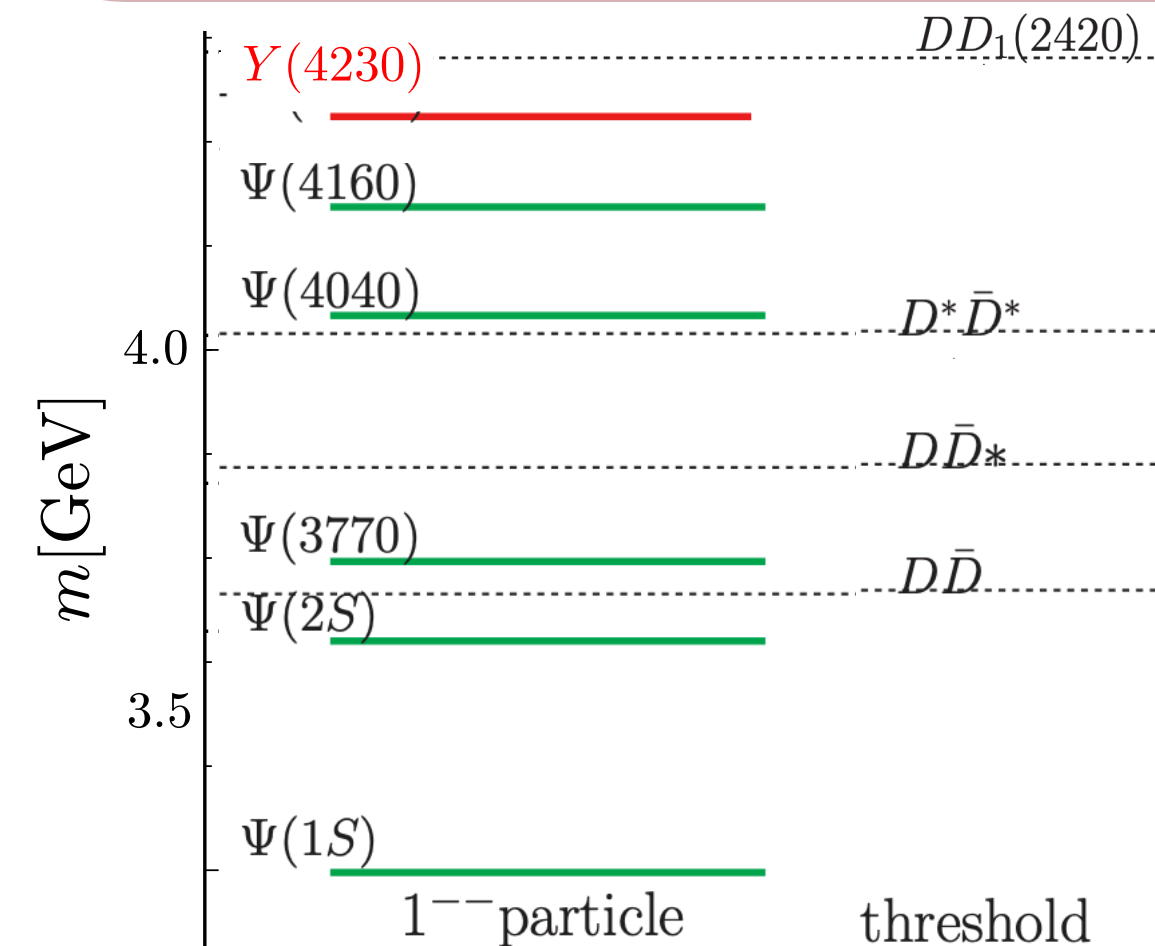
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$$\bullet M_{PDG} = 4220 \pm 15 \text{ MeV}$$

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Scenario 2: $\bar{c}gc$ hybrid

- Lattice hybrid energy 180 MeV high, but with systematics roughly correct ([arxiv:1610.01073](https://arxiv.org/abs/1610.01073))

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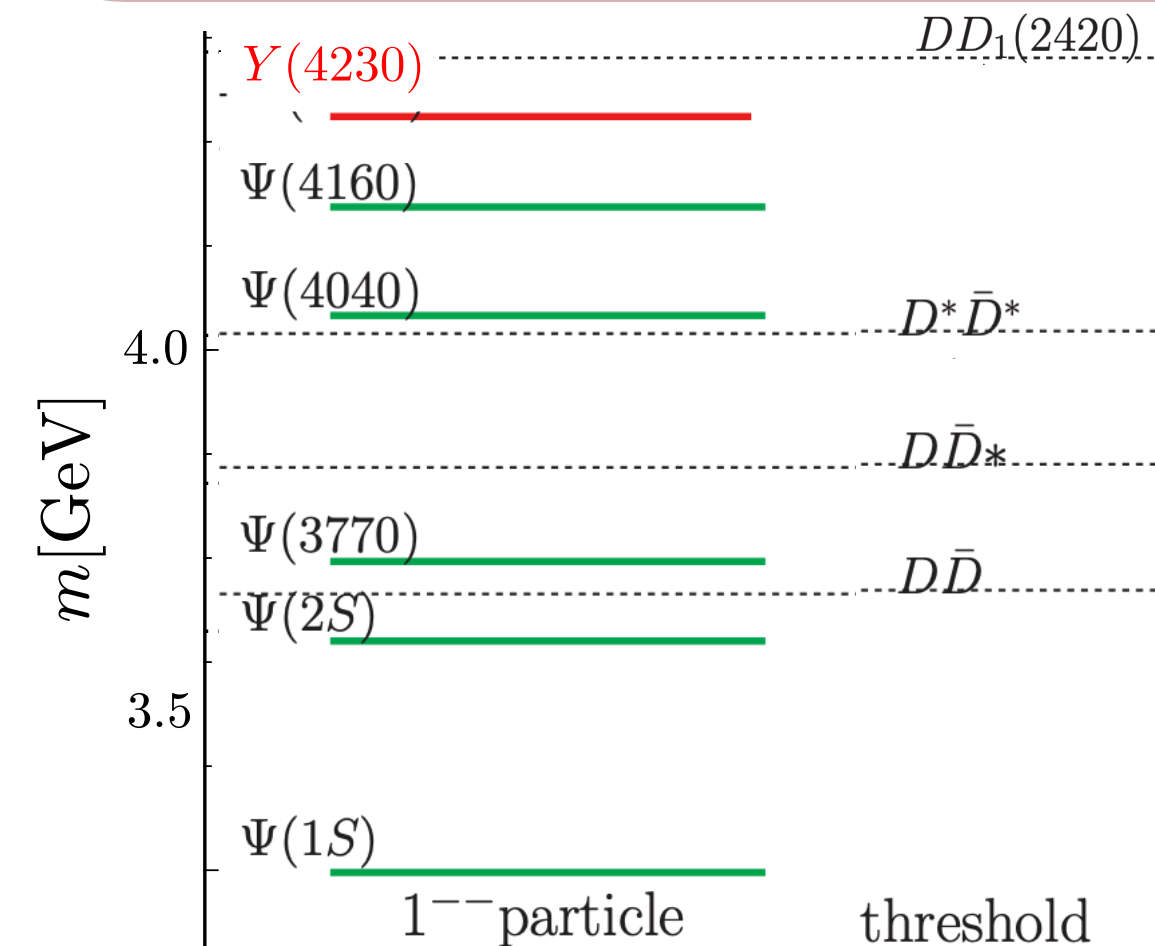
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Scenario 2: $\bar{c}gc$ hybrid

- Lattice hybrid energy 180 MeV high, but with systematics roughly correct ([arxiv:1610.01073](https://arxiv.org/abs/1610.01073))
- Lattice Potential + pNRQCD energy consistent ([arxiv:1510.04299](https://arxiv.org/abs/1510.04299))

$\psi(4230)$ aka $Y(4230)$ aka $Y(4260)$

Quantum Numbers

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$$Q = 0$$

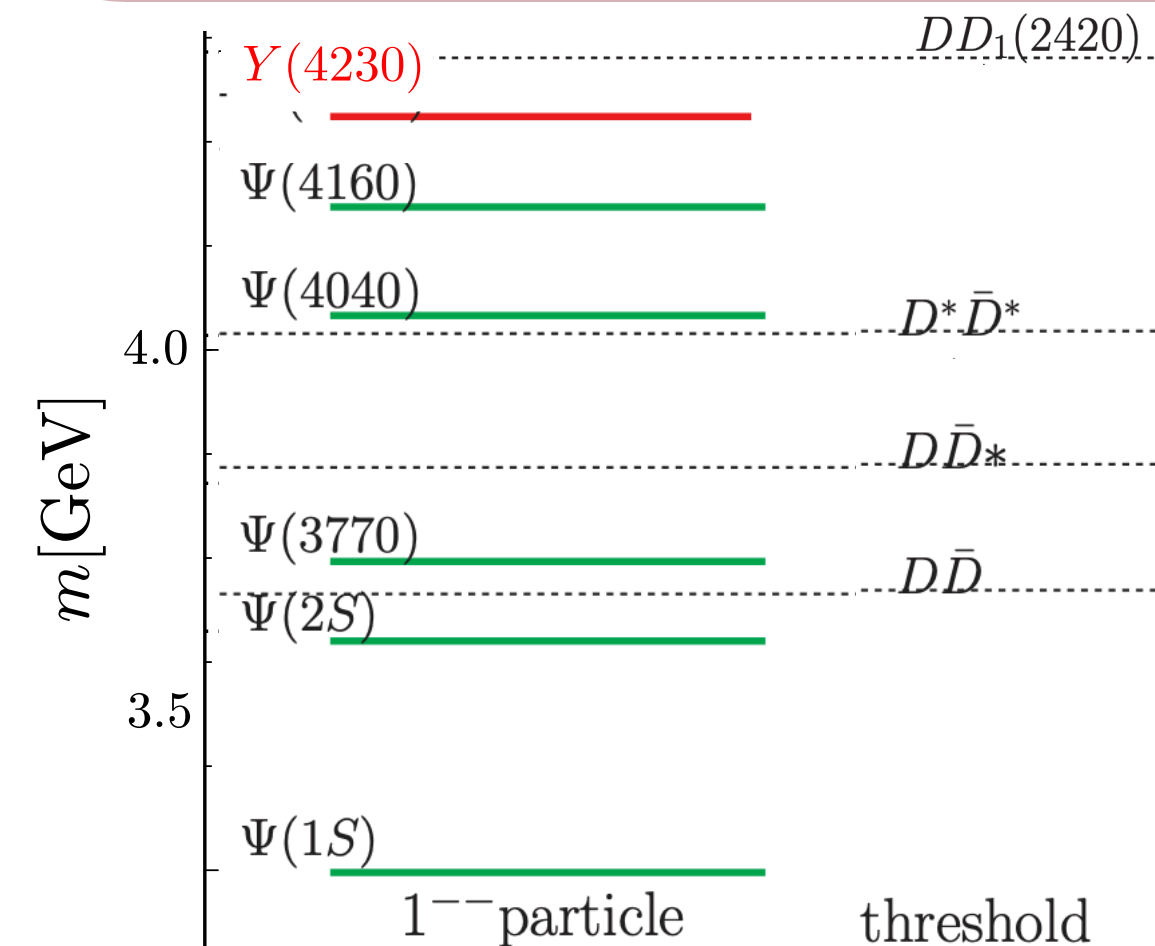
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- Decays to S-wave open charm forbidden ([arxiv:0507119](https://arxiv.org/abs/0507119)) \Rightarrow S-P mesons $D_1\bar{D}$ important

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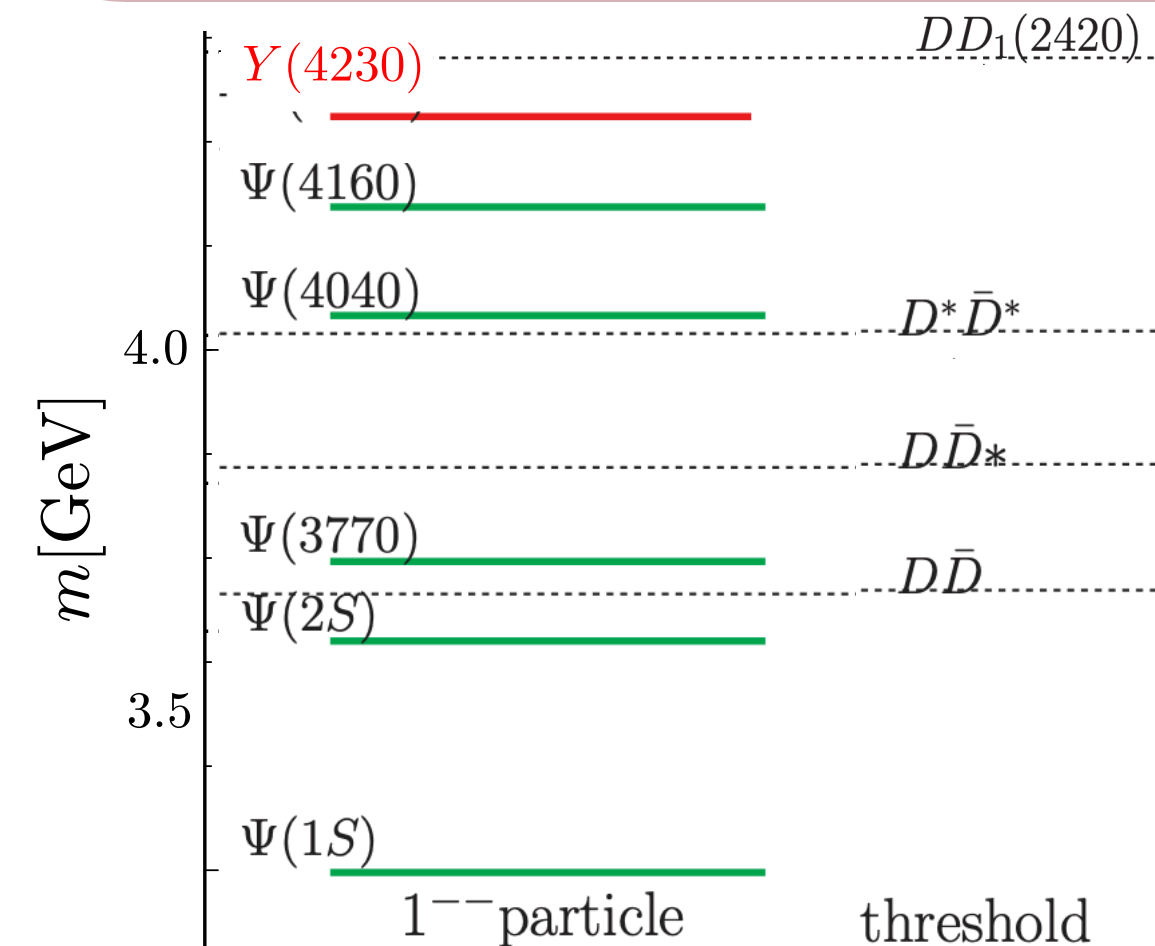
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- Decays to S-wave open charm forbidden ([arxiv:0507119](https://arxiv.org/abs/0507119)) \Rightarrow S-P mesons $D_1\bar{D}$ important
- Heavy quark spin symmetry less broken than in quarkonia: Λ_{QCD}/m_Q

$\psi(4230)$ aka $Y(4230)$ aka $Y(4260)$

📌 Quantum Numbers

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📌 Spatial Structure

- Molecular + Hybrid most probable

$\psi(4230)$ aka $Y(4230)$ aka $Y(4260)$

📌 Quantum Numbers

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- Molecular + Hybrid most probable
- Hydrocharmonium proposed ([arxiv:1309.1681](https://arxiv.org/abs/1309.1681))

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- Hydrocharmonium proposed ([arxiv:1309.1681](https://arxiv.org/abs/1309.1681))
- Compact Tetraquarks proposed ([arxiv:1405.1551](https://arxiv.org/abs/1405.1551))

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📌 Pole Structure: Bound State (if molecular)

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📌 Quantum Numbers

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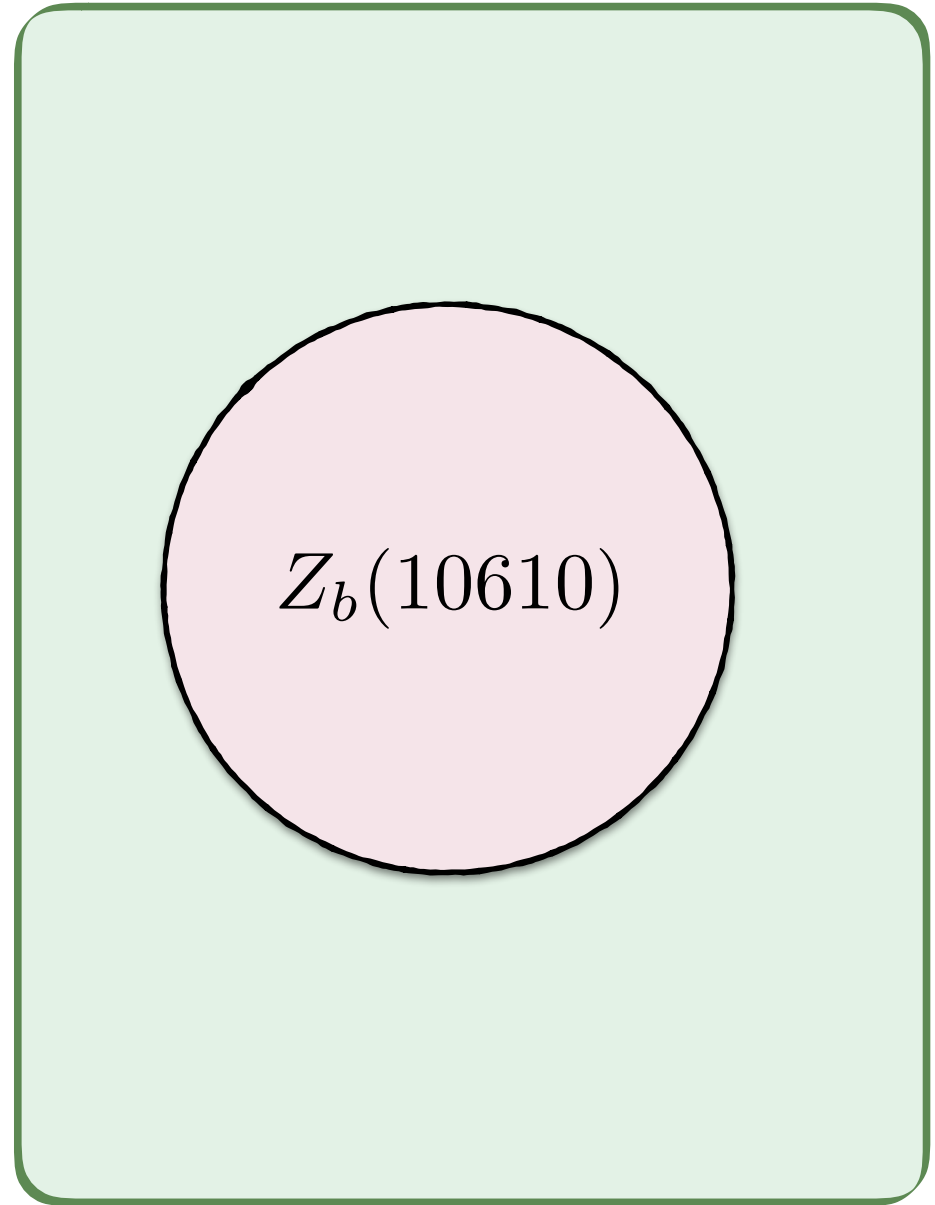
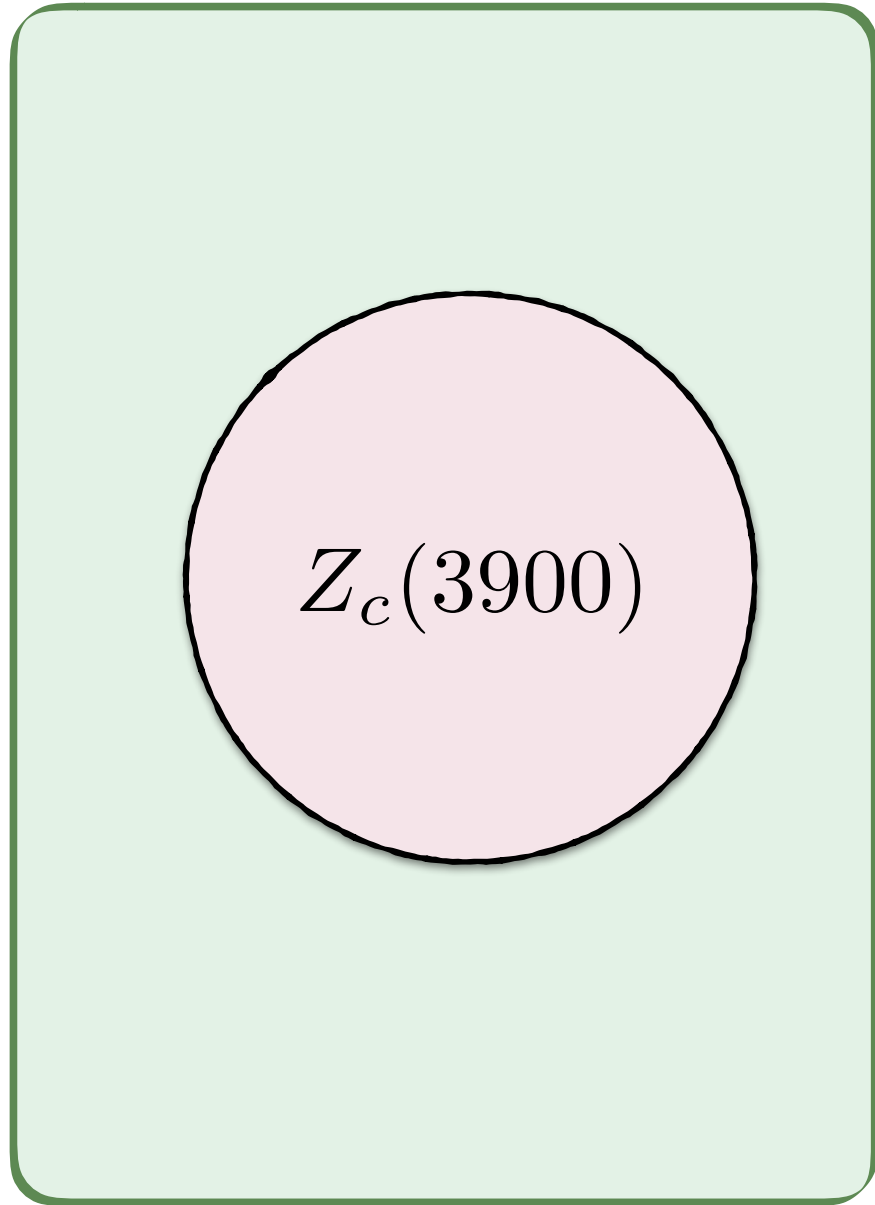
📌 Pole Structure: Bound State (if molecular)

📌 Leptonic Width to Distinguish Measurements $\Gamma_{e^+e^-}[Y(4230)] > 29.1 \pm 7.4 \text{ eV}$

- Molecular: $\sim 500 \text{ eV}$
- Hybrid: $\sim 40 \text{ eV}$

[arxiv:1907.07583](https://arxiv.org/abs/1907.07583)

$Z_c(3900)$ and $Z_b(10610)$



$Z_c(3900)$ and $Z_b(10610)$

Quantum Numbers

$$Q = \pm, 0$$

$$I^G = 1^+$$

$$J^{PC} = 1^{+-}$$

$Z_c(3900)$ and $Z_b(10610)$

Quantum Numbers

$$Q = \pm, 0$$

$$I^G = 1^+$$

$$J^{PC} = 1^{+-}$$

*Has Isospin charge
=> cannot be quarkonia*

$Z_c(3900)$ and $Z_b(10610)$

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$$Q = \pm, 0$$

$$I^G = 1^+$$

$$J^{PC} = 1^{+-}$$

📌 Notable Decays

- $Z_b(10610)$: $\mathcal{B}((B\bar{B}^*)^+) = 86\%$, $\mathcal{B}(\Upsilon(nS)\pi^+) \sim 3\%$

$Z_c(3900)$ and $Z_b(10610)$

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$Z_c(3900)$ and $Z_b(10610)$

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*Annihilation Effects Suppressed =
minimal valence components*
 $\bar{Q}Q\bar{q}q$

$Z_c(3900)$ and $Z_b(10610)$

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- $M_{Z_b} = 10607.2 \pm 2.0 \text{ MeV}$ $\Gamma_{Z_b} = 18.4 \pm 2.4 \text{ MeV}$

$Z_c(3900)$ and $Z_b(10610)$

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Lattice QCD Studies

- $Z_b(10610)$ ([arxiv:1912.02656](https://arxiv.org/abs/1912.02656))
 - Extracted potential between B and B^* (assuming eigenstate exclusively BB^*)
 - Sizable attraction for small r
 - Virtual State found for certain parameterizations of extracted potential

$Z_c(3900)$ and $Z_b(10610)$

Quantum Numbers

$$Q = \pm, 0$$

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Notable Decays

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- $M_{Z_c} = 3888.4 \pm 2.5 \text{ MeV}$ $\Gamma_{Z_c} = 28.3 \pm 2.5 \text{ MeV}$ $\delta = M_{D\bar{D}^*} - M_{Z_c} = 13 \text{ MeV}$

$Z_c(3900)$ and $Z_b(10610)$

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Notable Decays

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Lattice QCD Studies

- $Z_c(3900)$: ([arxiv:1907.07583](https://arxiv.org/abs/1907.07583))
 - Lattice includes diquark and two meson operators but does not find a bound state or narrow resonance

$Z_c(3900)$ and $Z_b(10610)$

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Notable Decays

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Lattice QCD Studies

- $Z_c(3900)$: ([arxiv:1907.07583](https://arxiv.org/abs/1907.07583))
 - Lattice includes diquark and two meson operators but does not find a bound state or narrow resonance
 - [arxiv:1606.03008](https://arxiv.org/abs/1606.03008): consistent with both resonance and virtual states
=> Lattice studies done at multiple volumes can distinguish these cases

$Z_c(3900)$ and $Z_b(10610)$

📌 Quantum Numbers

$$Q = \pm, 0$$

$$I^G = 1^+$$

$$J^{PC} = 1^{+-}$$

📌 Pole Structure:

- $Z_b(10610)$ ([arxiv:1805.07453](https://arxiv.org/abs/1805.07453)): virtual state ~ 1 MeV below threshold

$Z_c(3900)$ and $Z_b(10610)$

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$$I^G = 1^+$$

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📌 Pole Structure:

- $Z_b(10610)$ ([arxiv:1805.07453](https://arxiv.org/abs/1805.07453)): virtual state ~ 1 MeV below threshold
- $Z_c(3900)$ ([arxiv:1512.03638](https://arxiv.org/abs/1512.03638)): virtual state or resonance

$Z_c(3900)$ and $Z_b(10610)$

Quantum Numbers

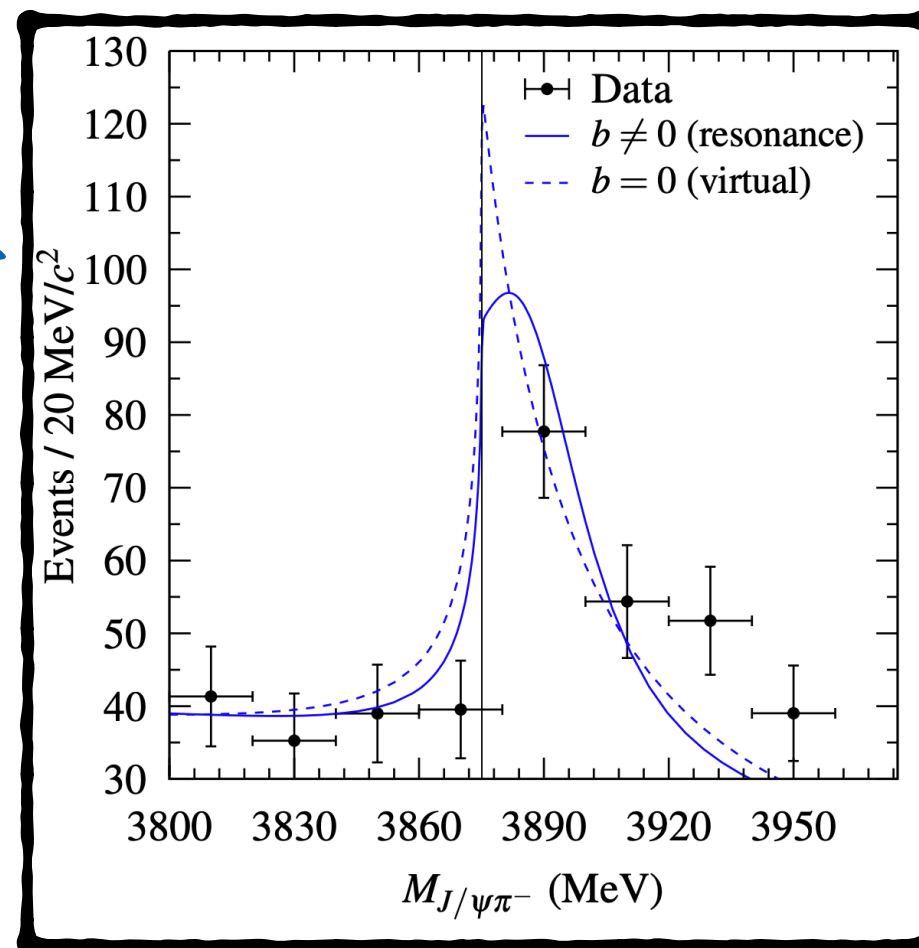
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Pole Structure:

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- $Z_c(3900)$ ([arxiv:1512.03638](https://arxiv.org/abs/1512.03638)): virtual state or resonance



Smaller bin sizes and good energy resolution needed to distinguish

$Z_c(3900)$ and $Z_b(10610)$

📌 Quantum Numbers

$$Q = \pm, 0$$

$$I^G = 1^+$$

$$J^{PC} = 1^{+-}$$

📌 Pole Structure:

- $Z_b(10610)$ ([arxiv:1805.07453](https://arxiv.org/abs/1805.07453)): virtual state ~1 MeV below threshold
- $Z_c(3900)$ ([arxiv:1512.03638](https://arxiv.org/abs/1512.03638)): virtual state or resonance

📌 Spatial Structure

- (Multi) Molecular
- ([arxiv:1808.00914](https://arxiv.org/abs/1808.00914)) $\pi J/\psi(\rho\eta_c) - D\bar{D}^*$ mixing just as important as diagonal parts of potential for $Z_c(3900)$

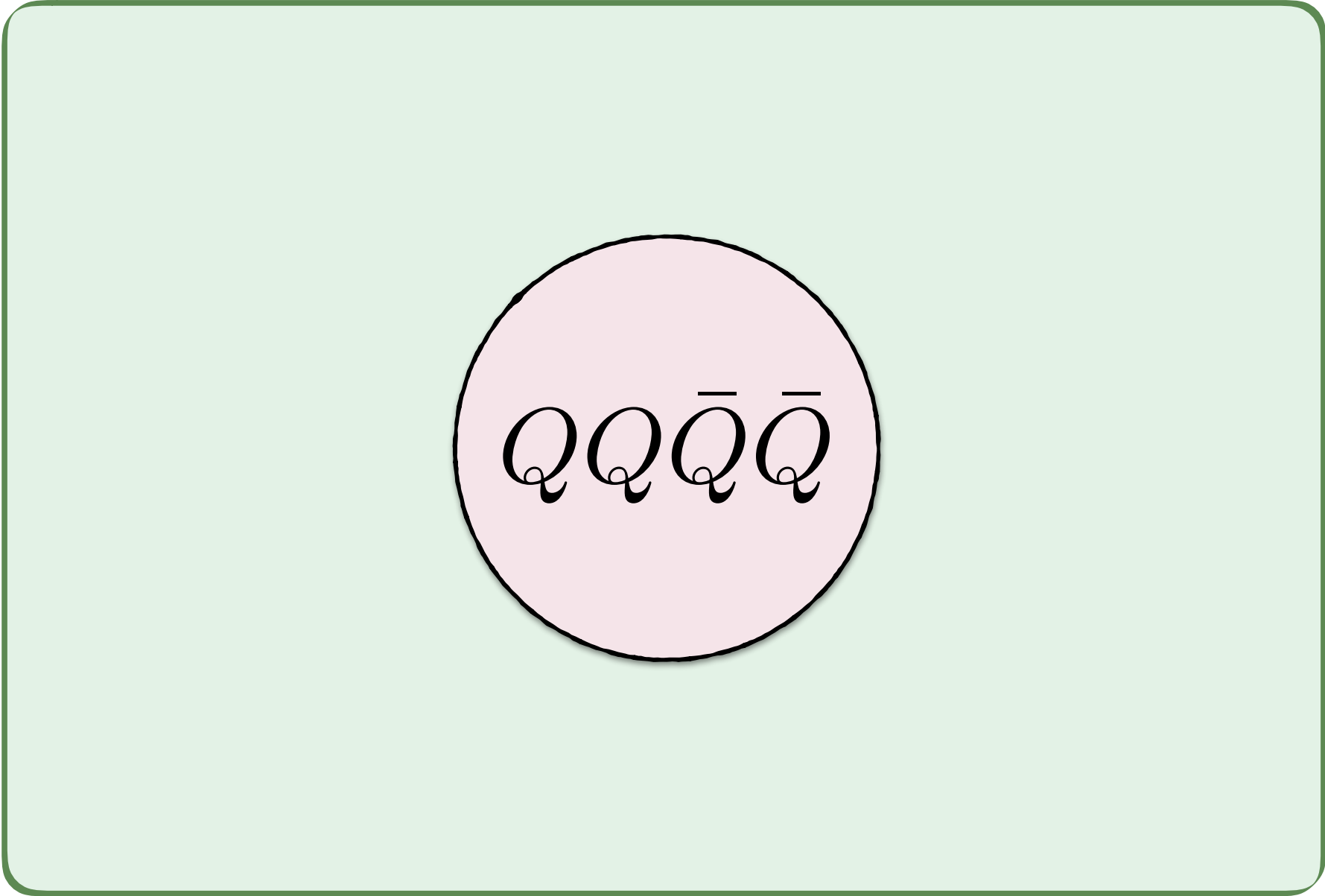
Other States I Won't Discuss

- $Z_b(10650)$ the B^*B^* partner to $Z_b(10610)$
- $Z_c(4020)$ the D^*D^* partner to $Z_c(3900)$
- X_b partner to $X(3872)$ not seen as $h_b(2P)$ below open threshold
- Pentaquarks P_c molecule of $\bar{c}c$ and p
- Exotic Flavour $cs\bar{u}\bar{d}$: HadSpec $D\bar{K}$, $I = 0$, $J^P = 0^+$ ([arxiv:2008.06432](https://arxiv.org/abs/2008.06432))
compared to $X(2900)$ LHCb prelim results
- $\bar{b}b+$ Spectrum from HadSpec ([arxiv:2008.02656](https://arxiv.org/abs/2008.02656))



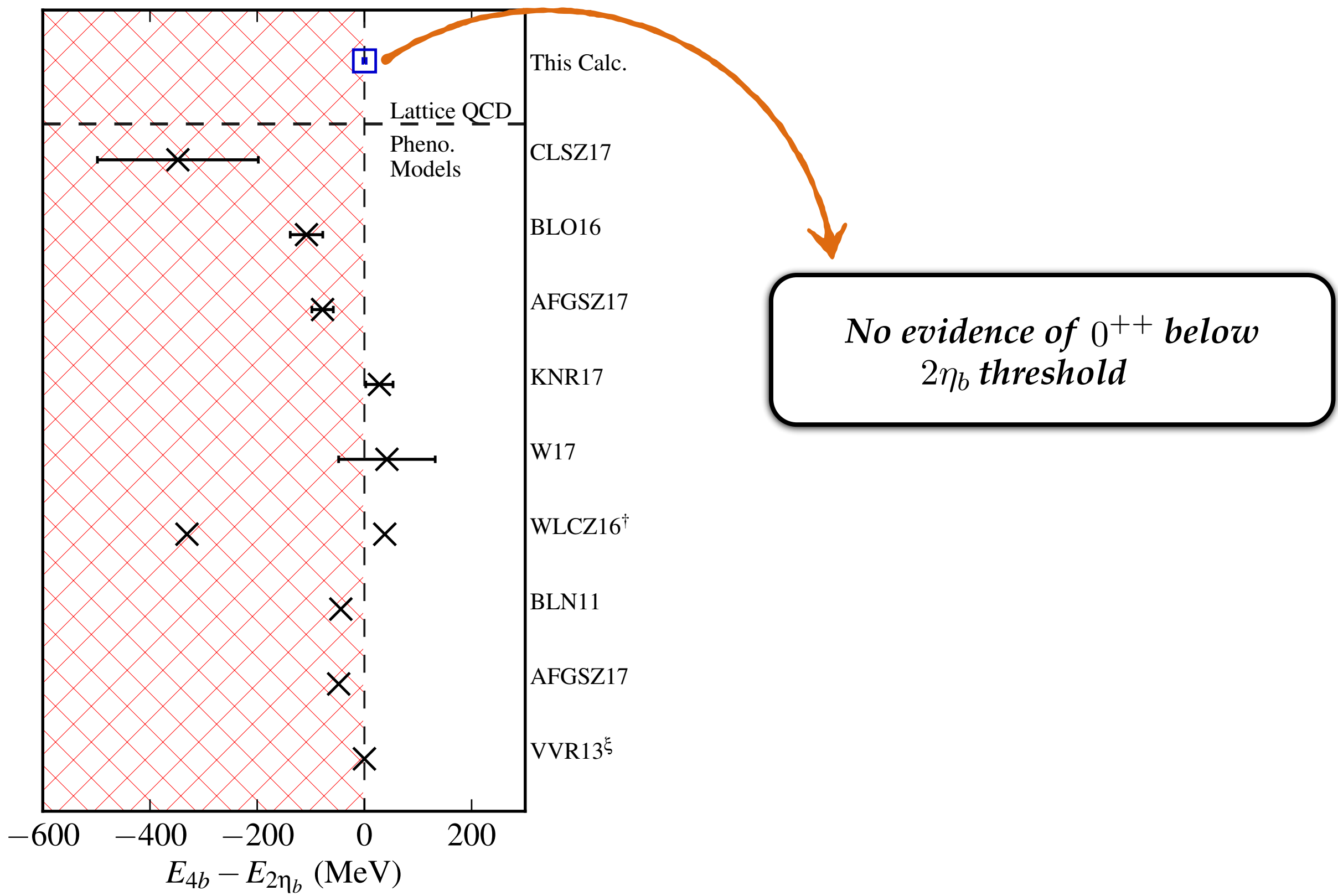
- More experimental data needed to nullify models for
 - $Y(4360)$ (D_1D^* partner of $Y(4230)$?)
 - $Y(4660)$ (D_sD_{s1} strange partner of $Y(4230)$)?
 - $Z(4430)$

$Q Q \bar{Q} \bar{Q}$

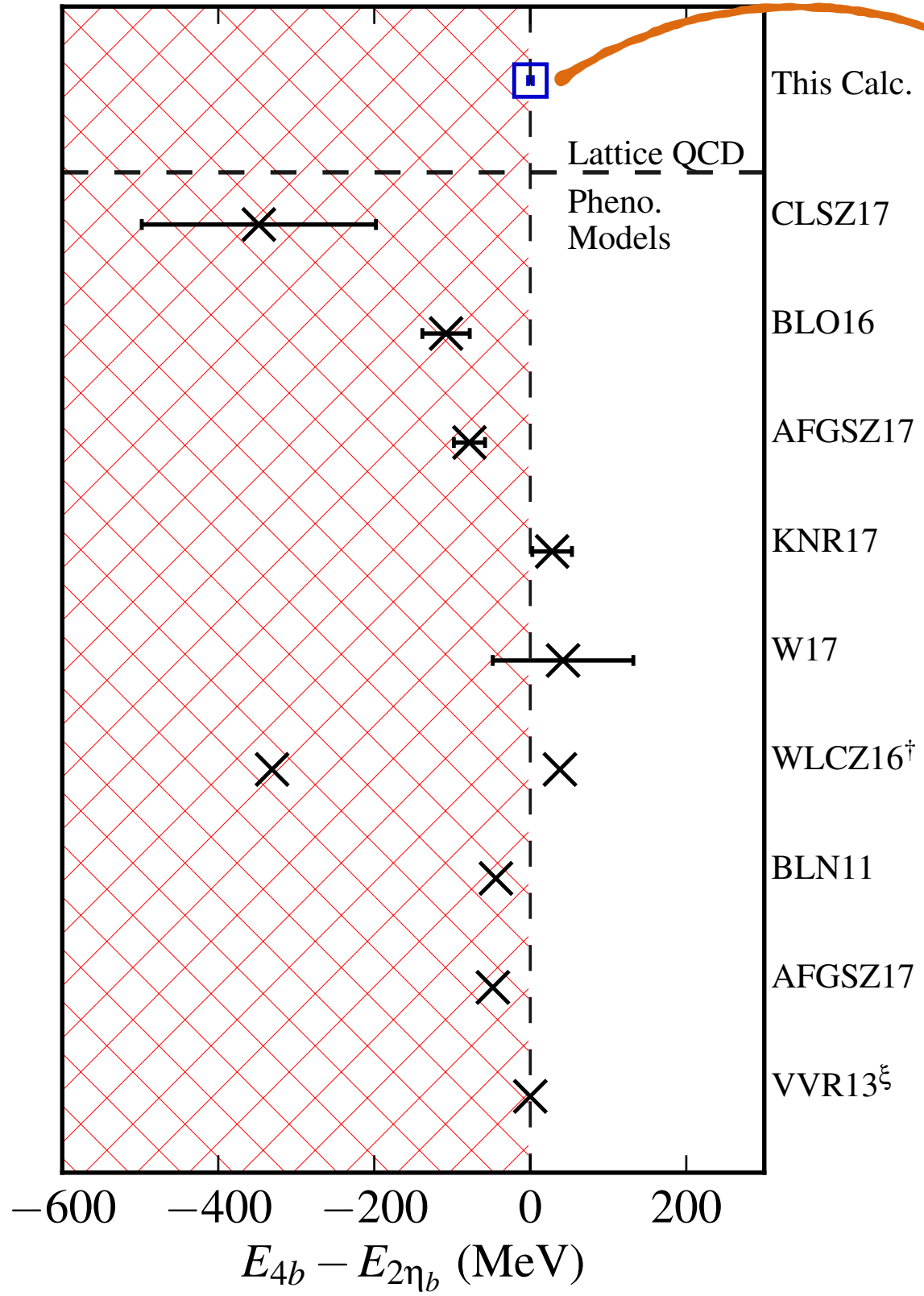


$Q Q \bar{Q} \bar{Q}$

$bb\bar{b}\bar{b}$ S-wave Bound State Doesn't exist [arxiv:1710.03236](https://arxiv.org/abs/1710.03236)



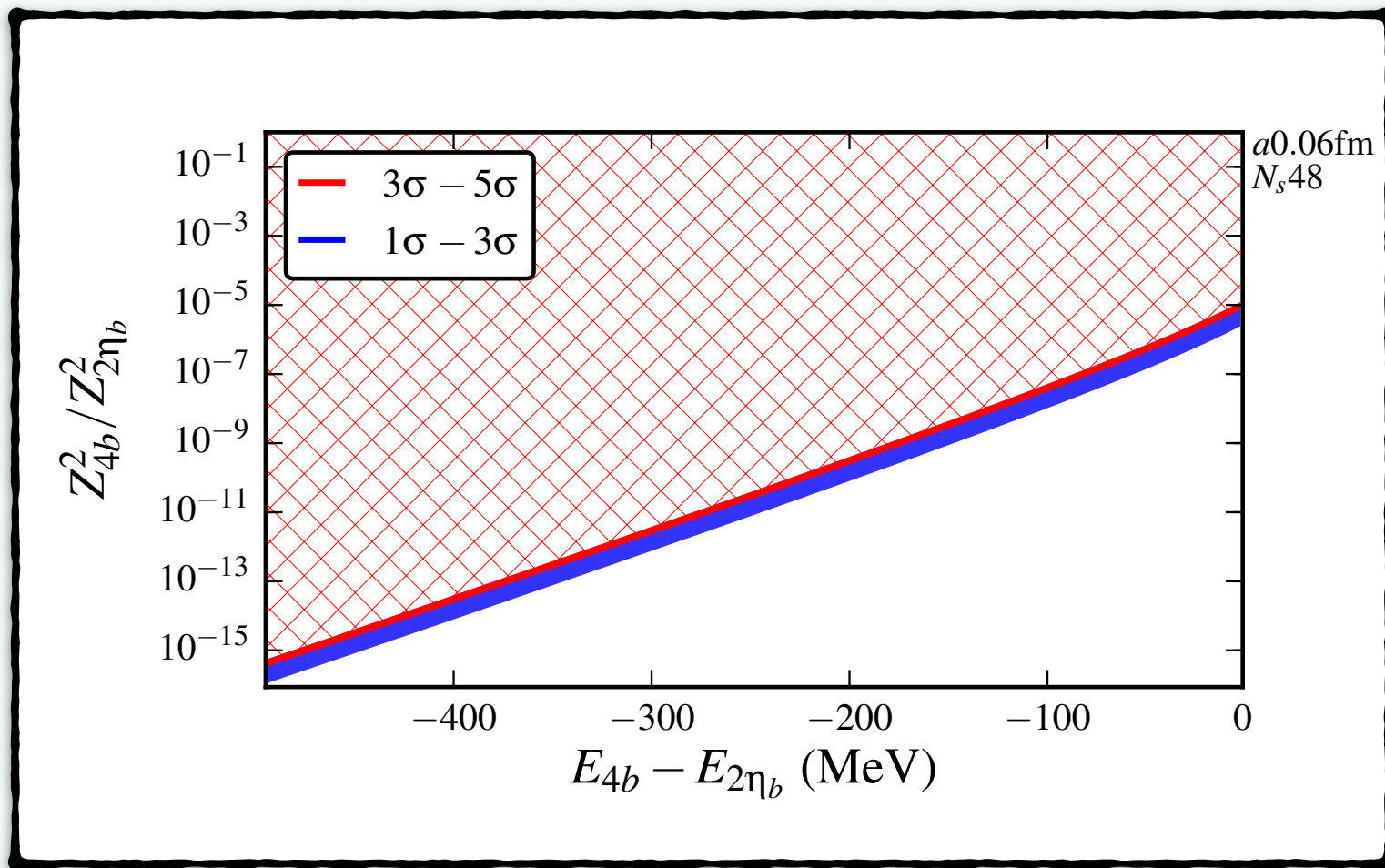
$bbbb$ S-wave Bound State Doesn't exist [arxiv:1710.03236](https://arxiv.org/abs/1710.03236)



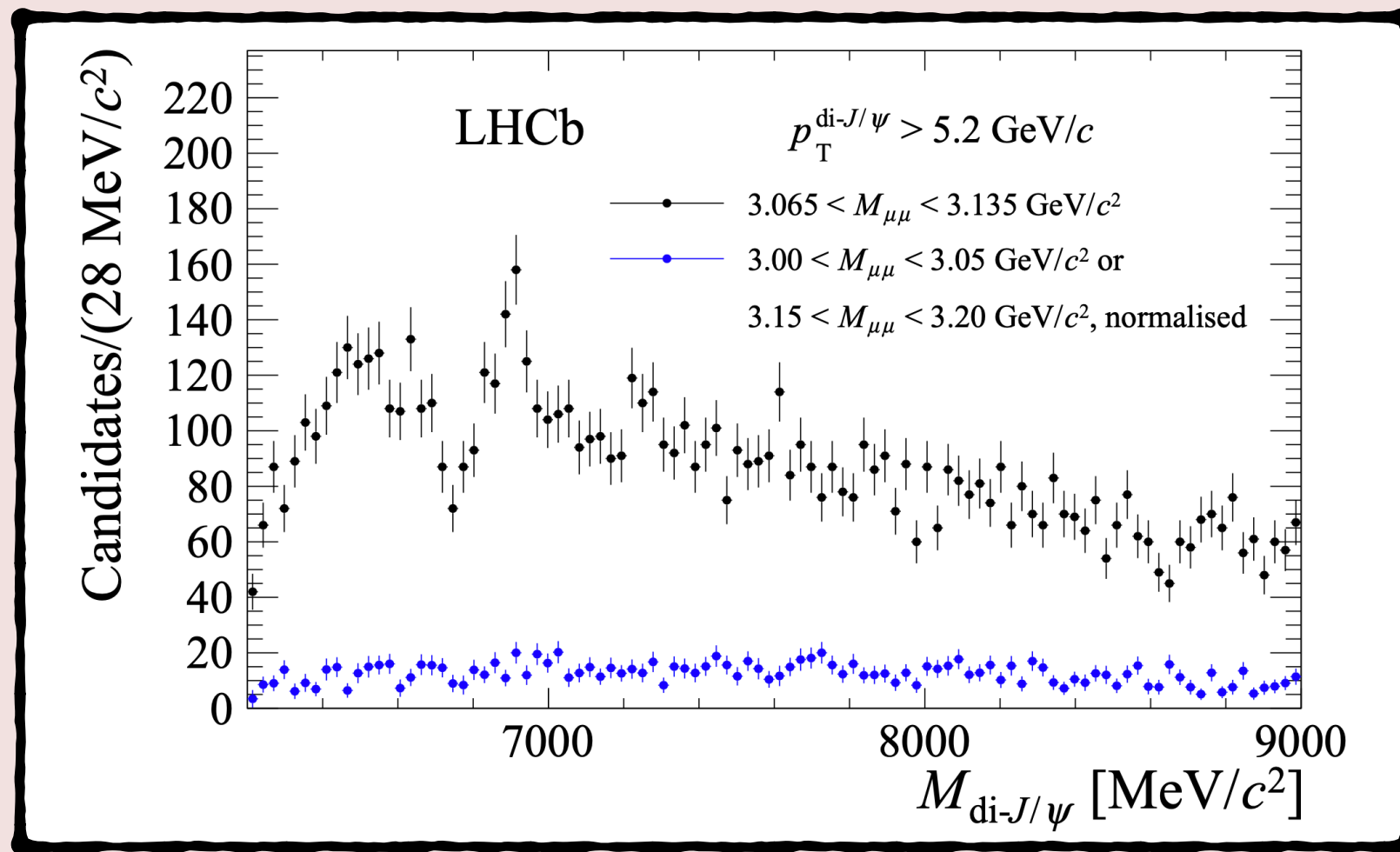
No evidence of 0^{++} below $2\eta_b$ threshold

If you don't observe a process, need to determine a bound, e.g, proton decay.

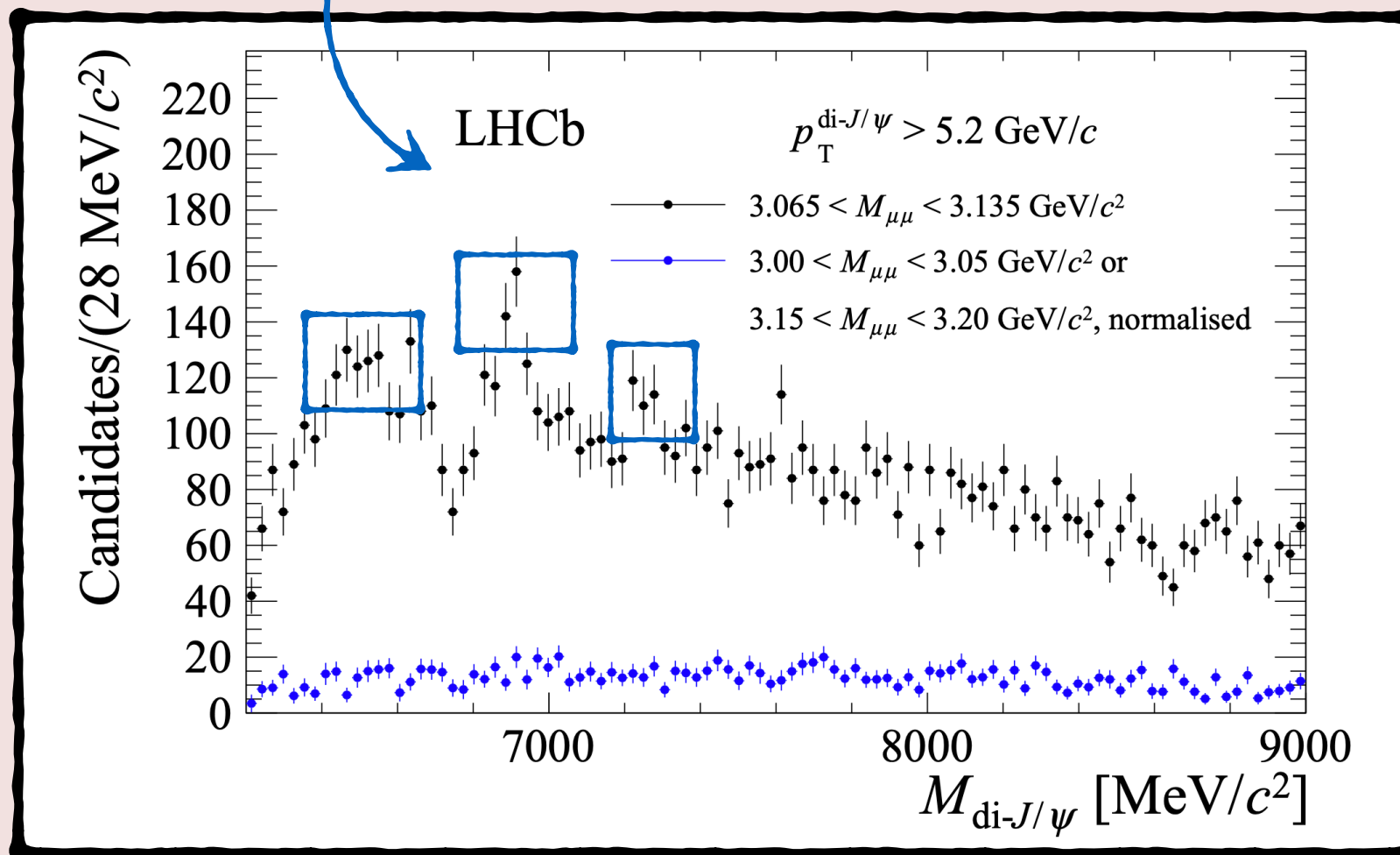
$bbbb$ S-wave Bound State Doesn't exist [arxiv:1710.03236](https://arxiv.org/abs/1710.03236)



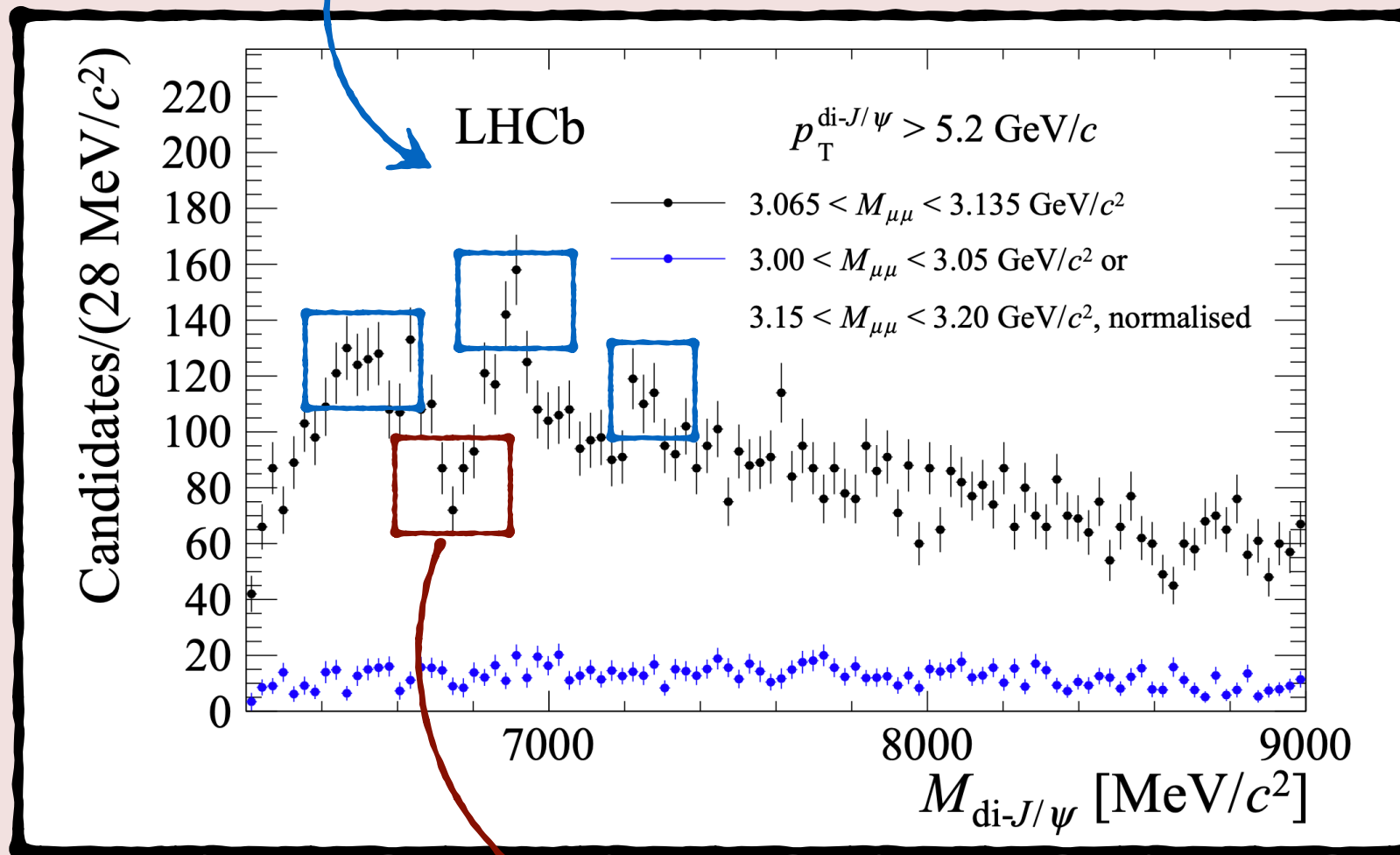
What is the probability we missed the bound state?



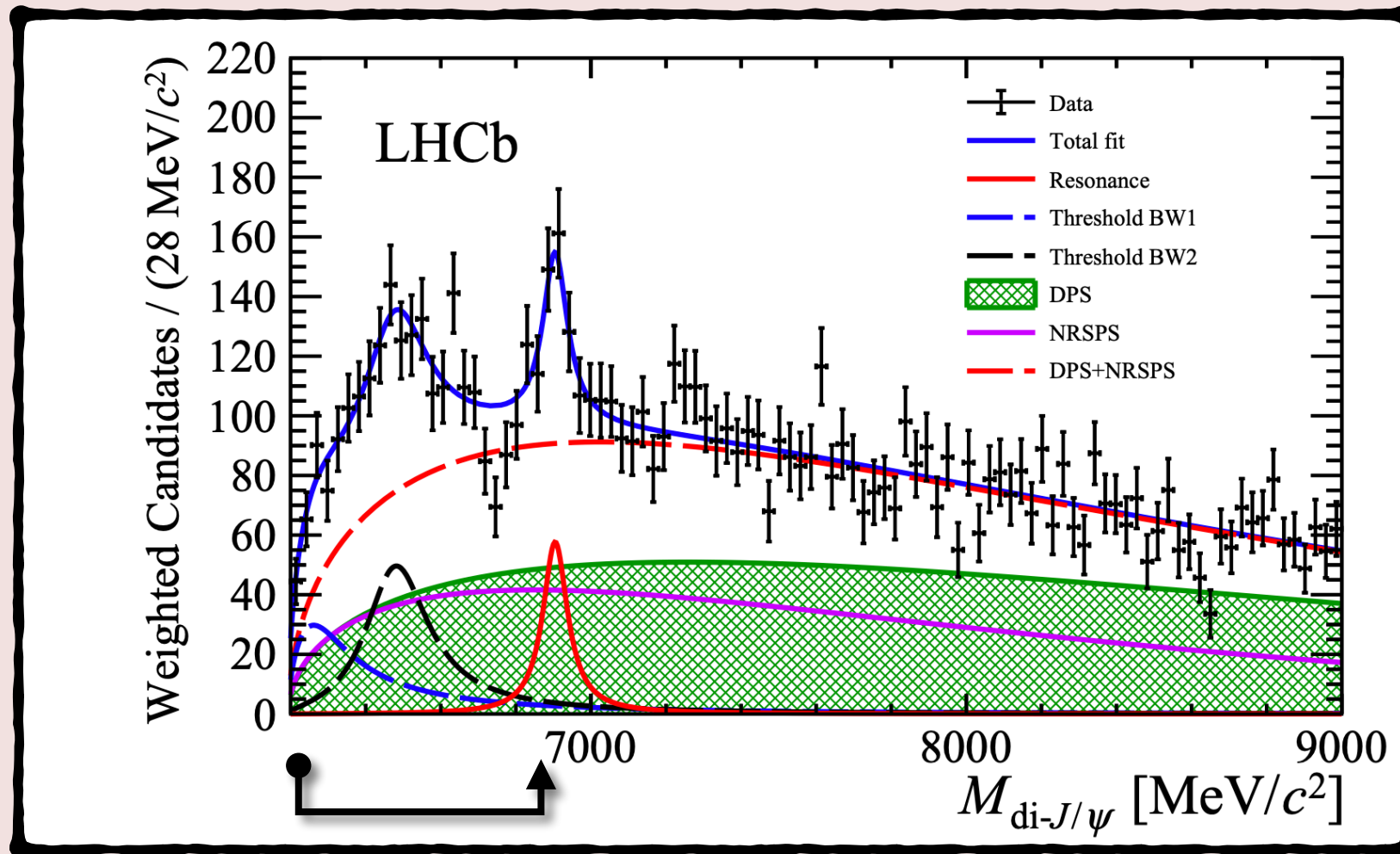
3 Possible Bumps



3 Possible Bumps

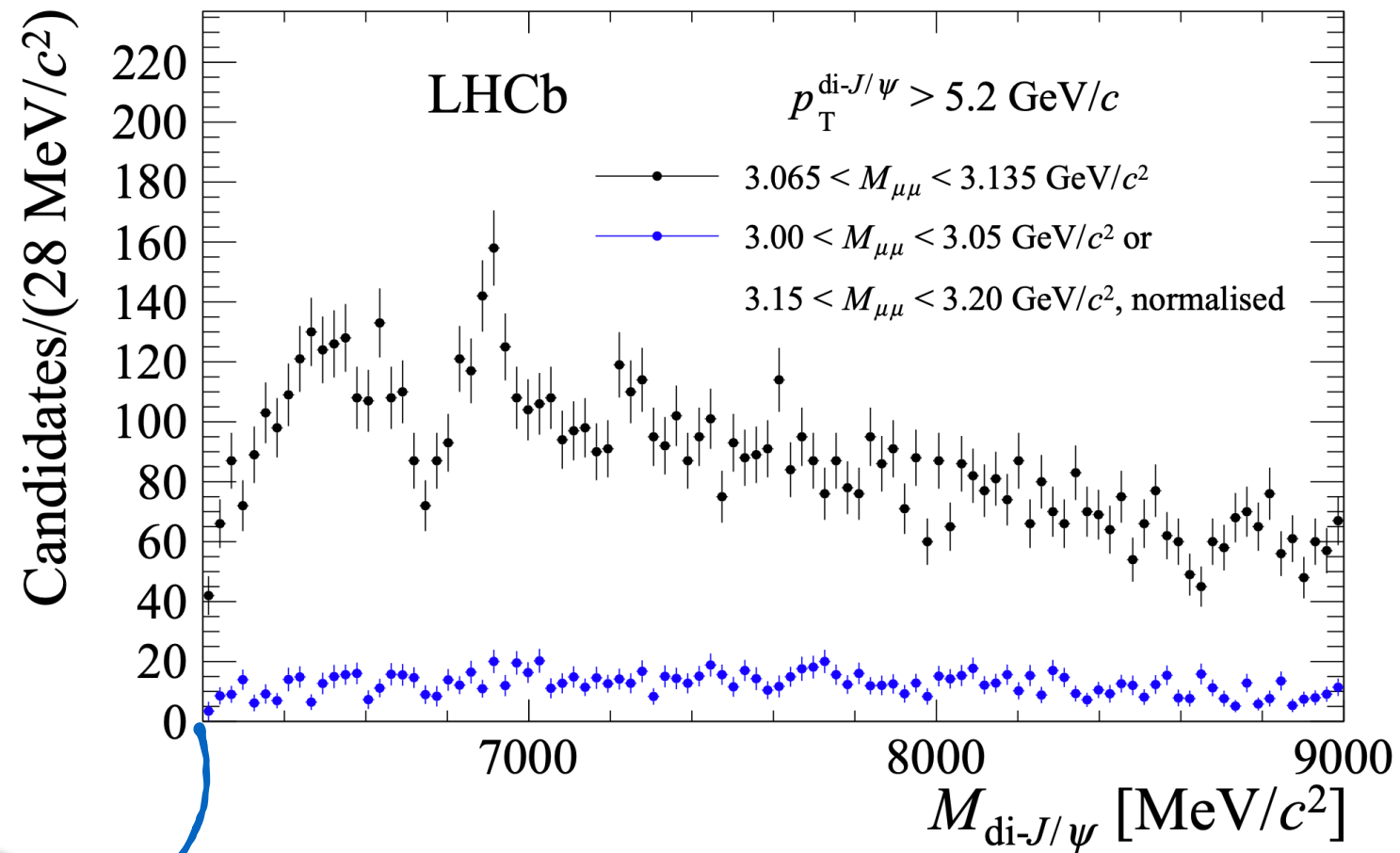


1 dip

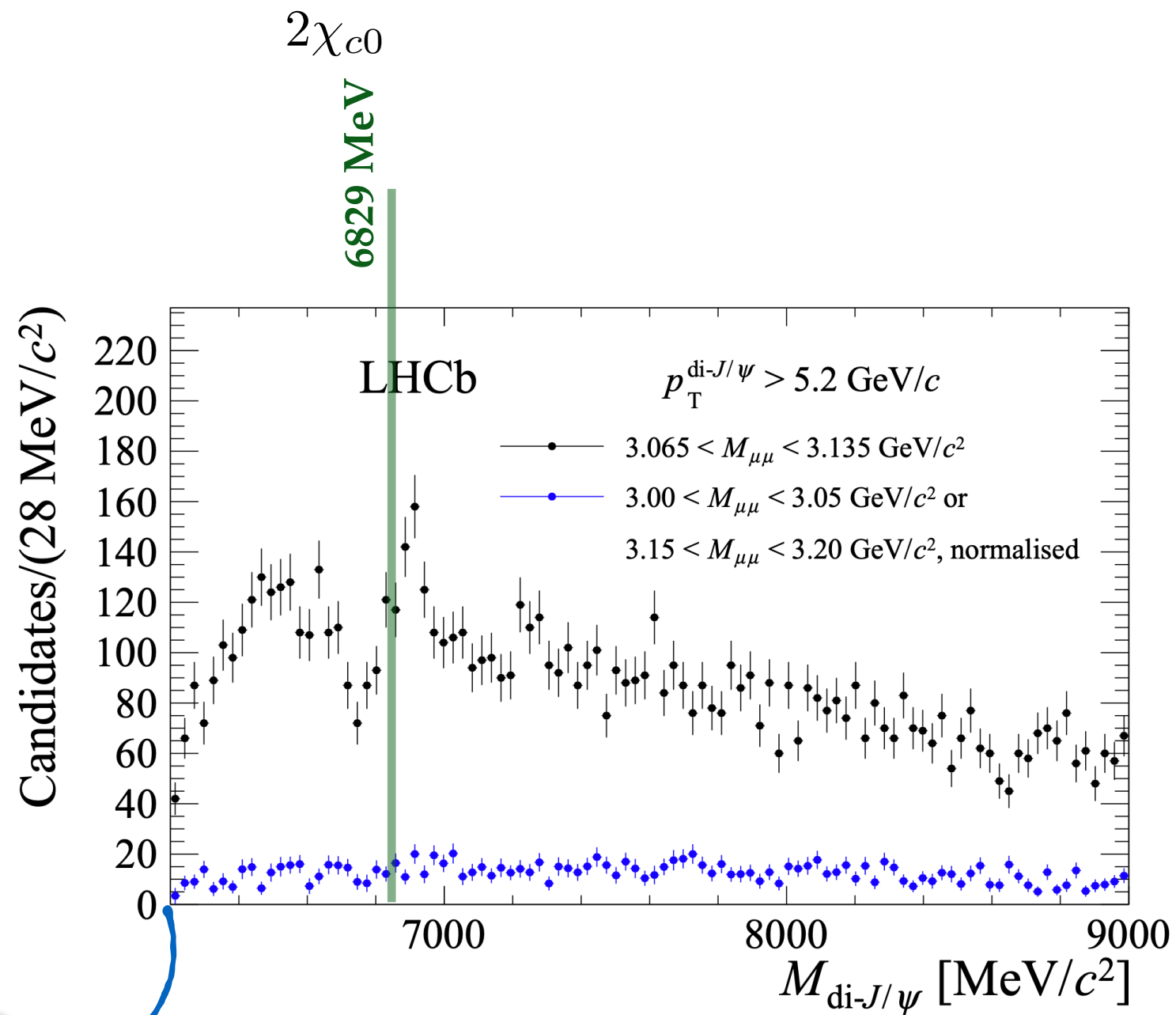


700 MeV above $2J/\psi$

Only Viable Model =
diquarks!!!!

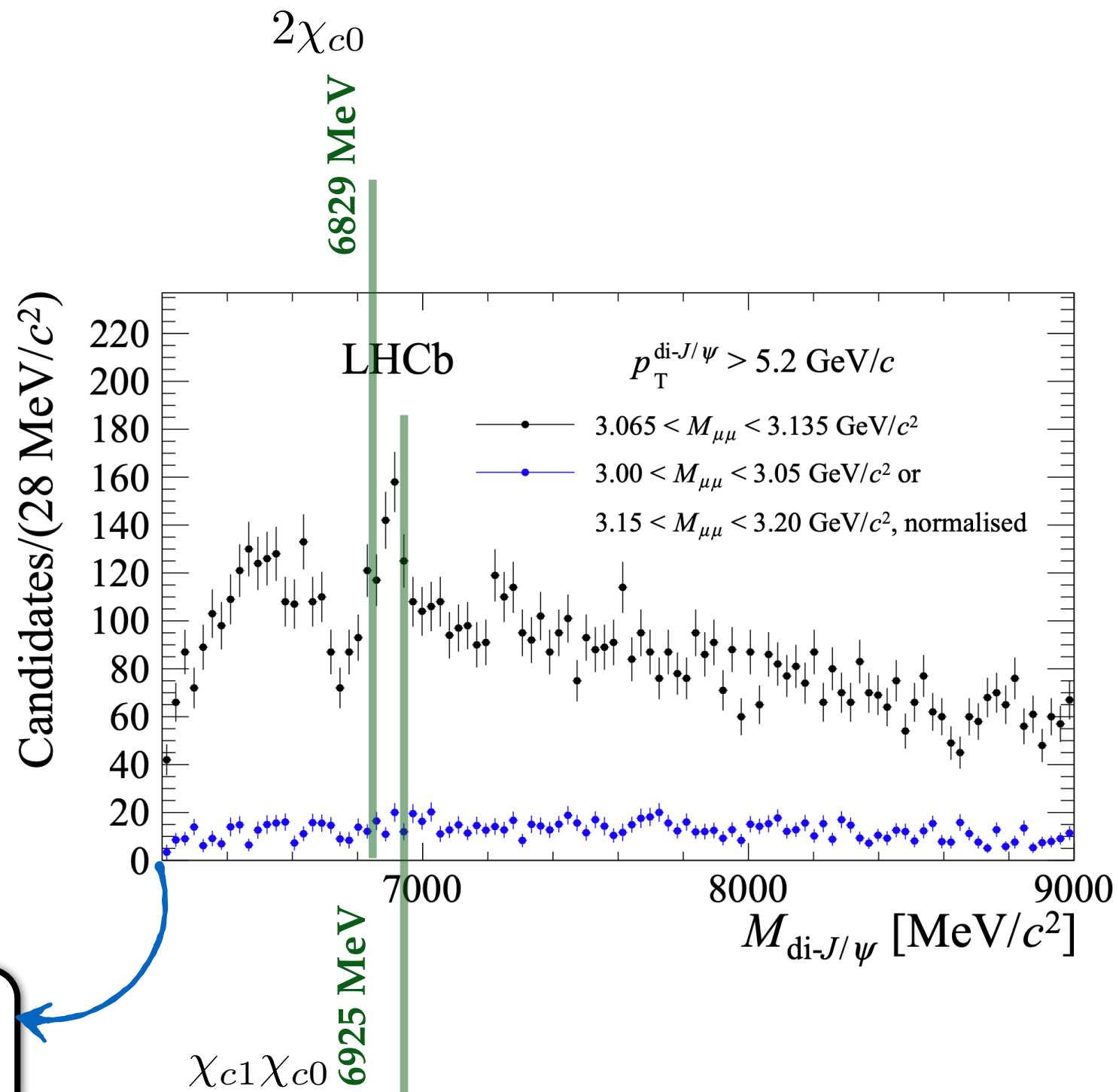


S-wave $2J/\psi$
threshold



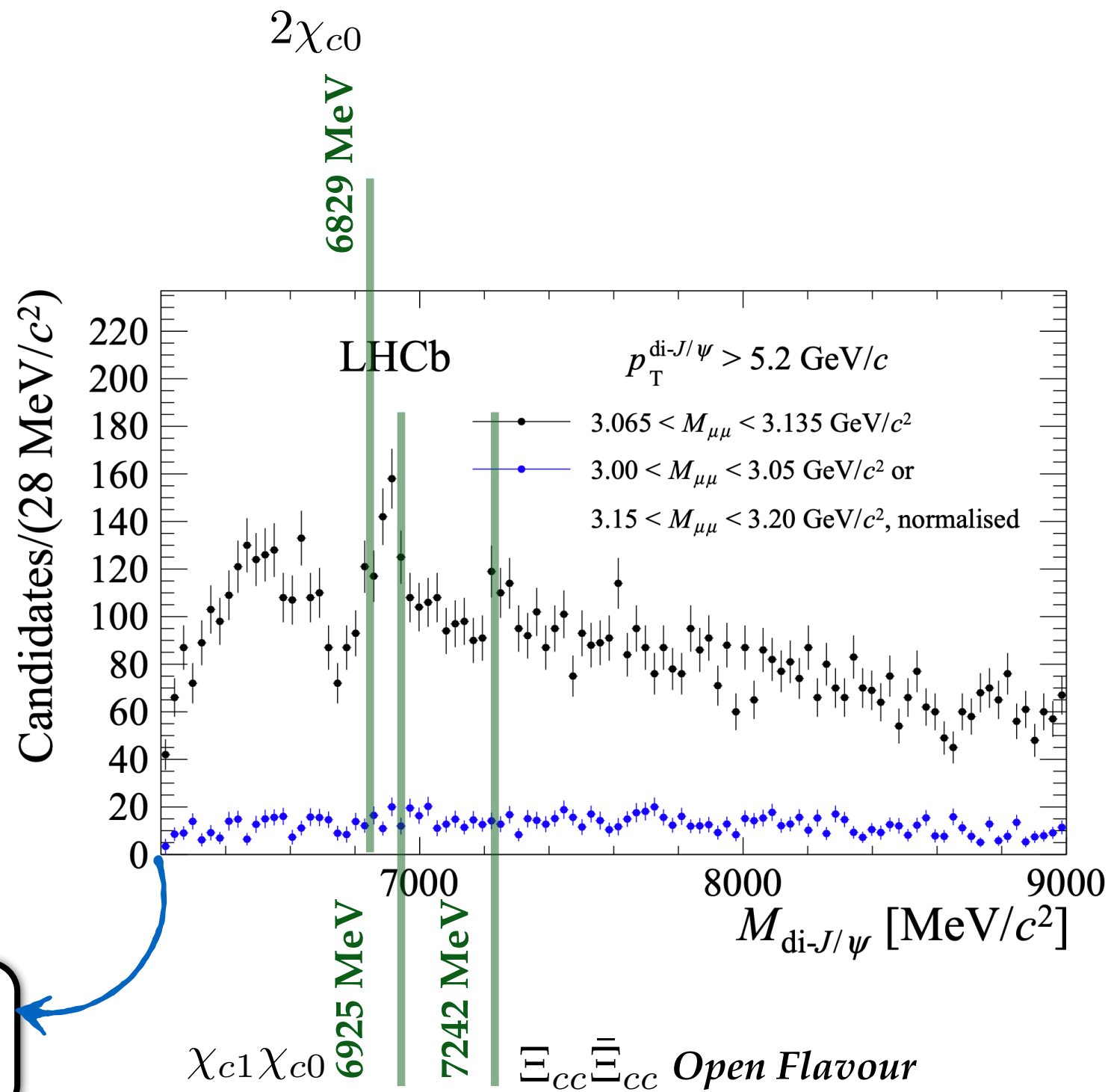
S-wave $2J/\psi$
threshold

$\bar{c}c\bar{c}c - X(6900)$ [arxiv: 2006.16957](https://arxiv.org/abs/2006.16957)



S-wave $2J/\psi$
threshold

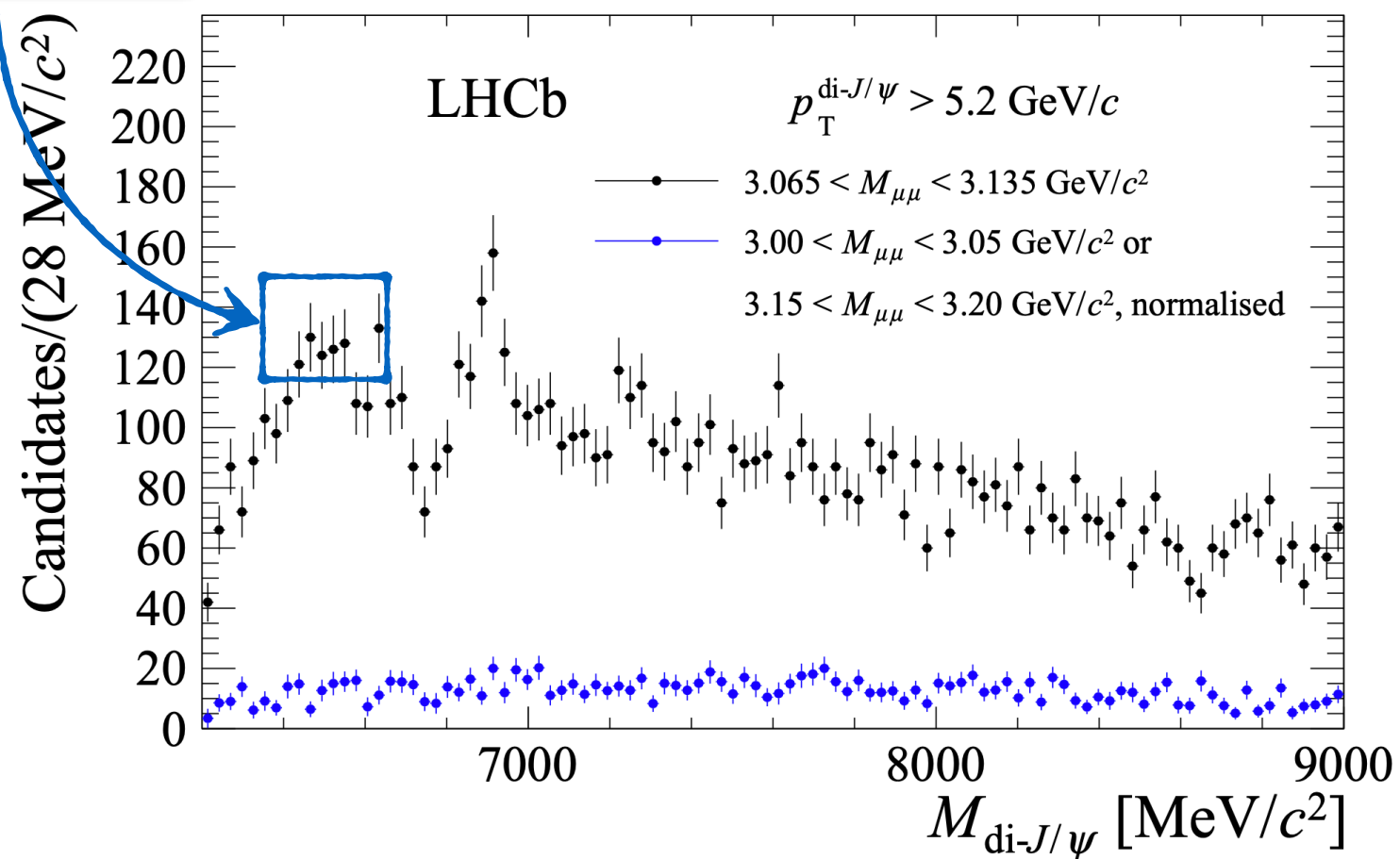
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S-wave $2J/\psi$
threshold

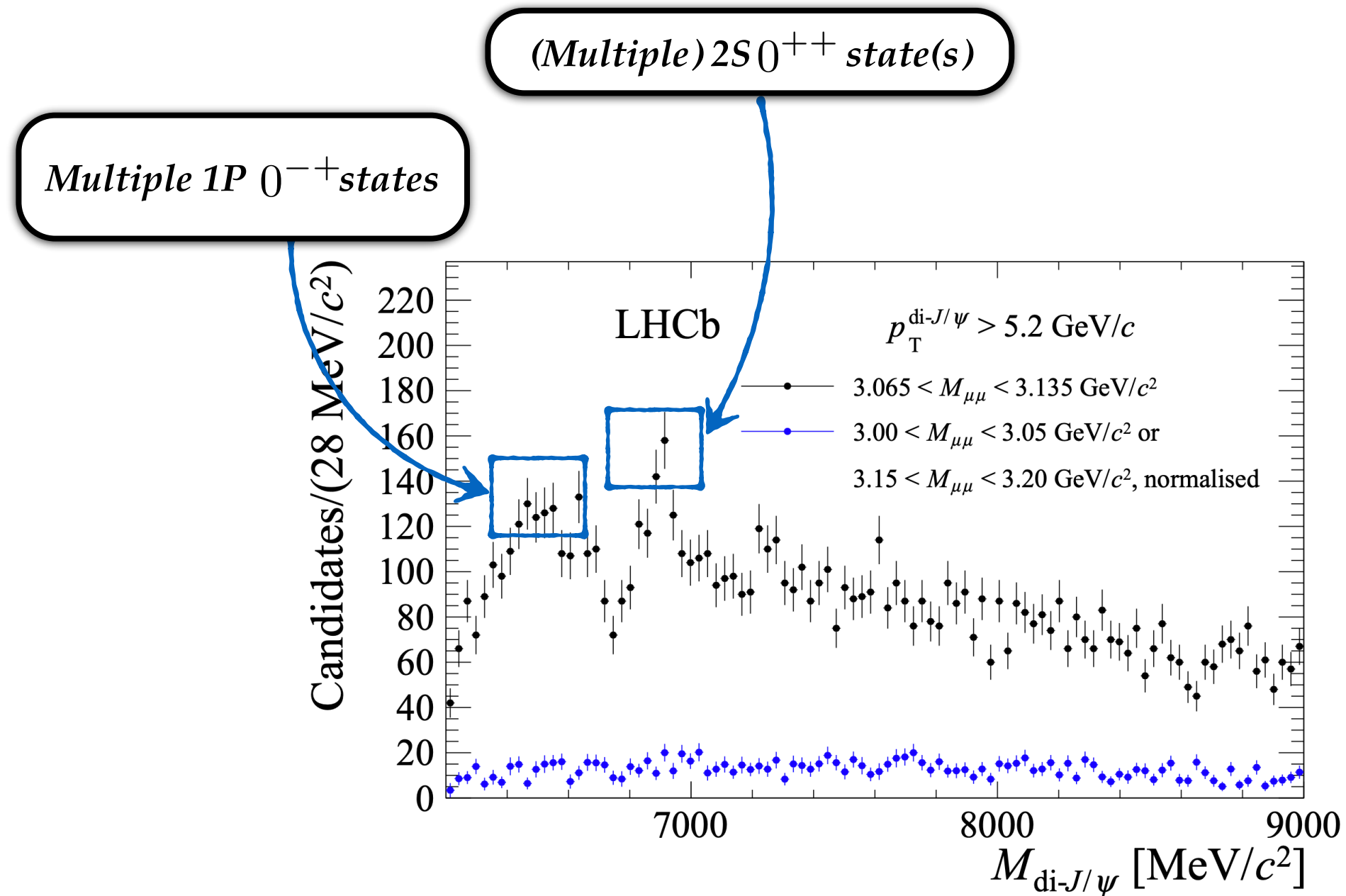
📌 Dynamical Diquark Model [arxiv:2008.01631](https://arxiv.org/abs/2008.01631)

Multiple $1P\ 0^{-+}$ states



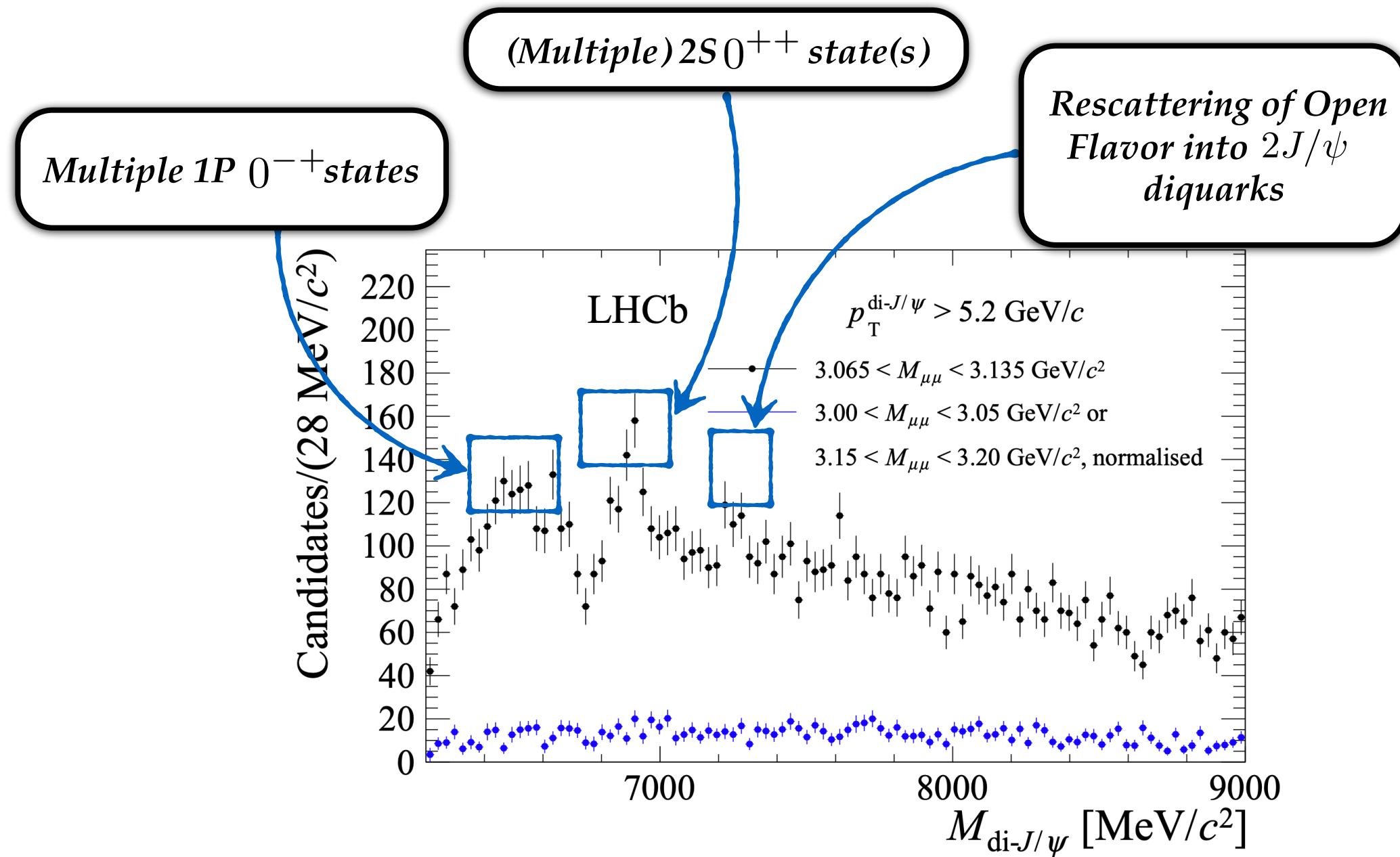
$\bar{c}c\bar{c}c - X(6900)$ [arxiv: 2006.16957](https://arxiv.org/abs/2006.16957)

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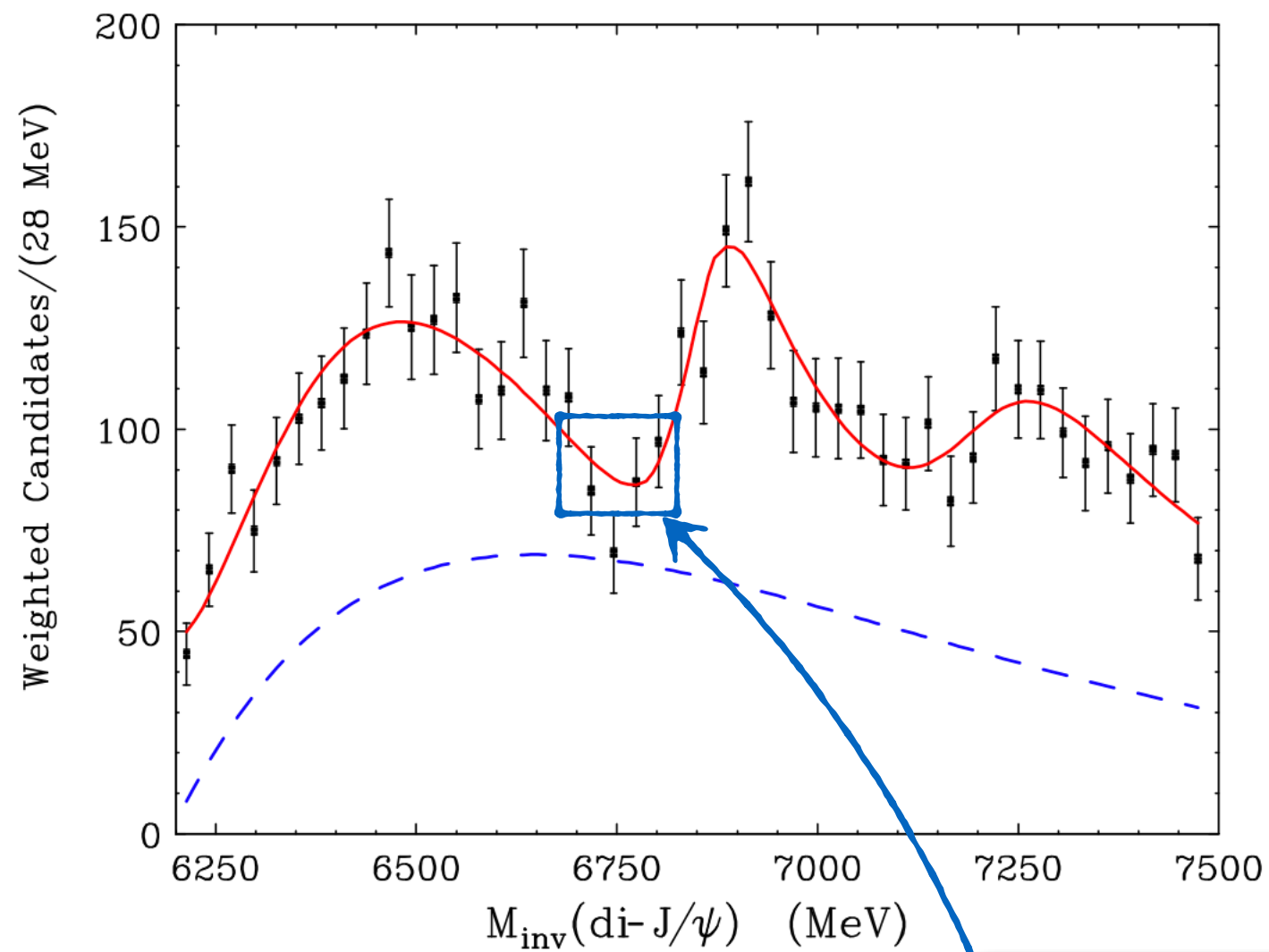
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$\bar{c}c\bar{c}c$ - $X(6900)$ [arxiv:2006.16957](https://arxiv.org/abs/2006.16957)

📌 Pheno model [arxiv:2009.4429](https://arxiv.org/abs/2009.4429)



*Dip due to Interference
from $2\chi_{c0}$ threshold
turning on*

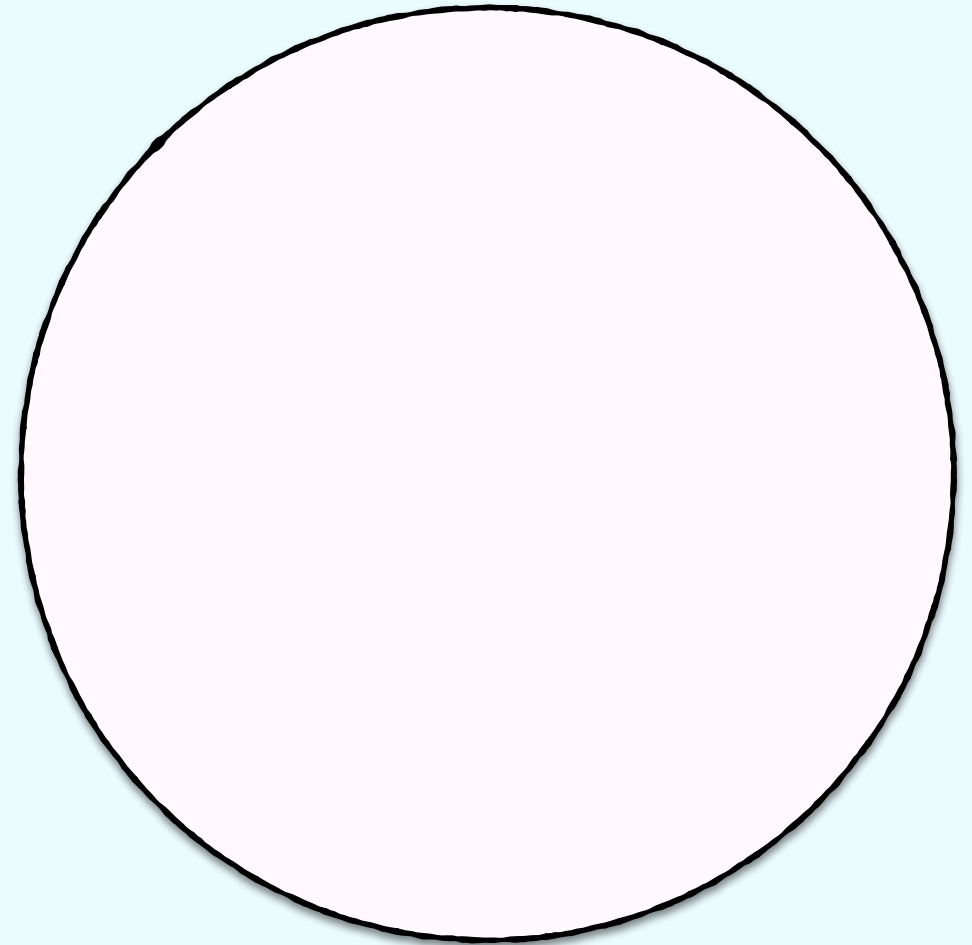
$bb\bar{u}\bar{d}$, $I = 0$, $J^P = 1^+$ is bound



$bb\bar{u}\bar{d}$

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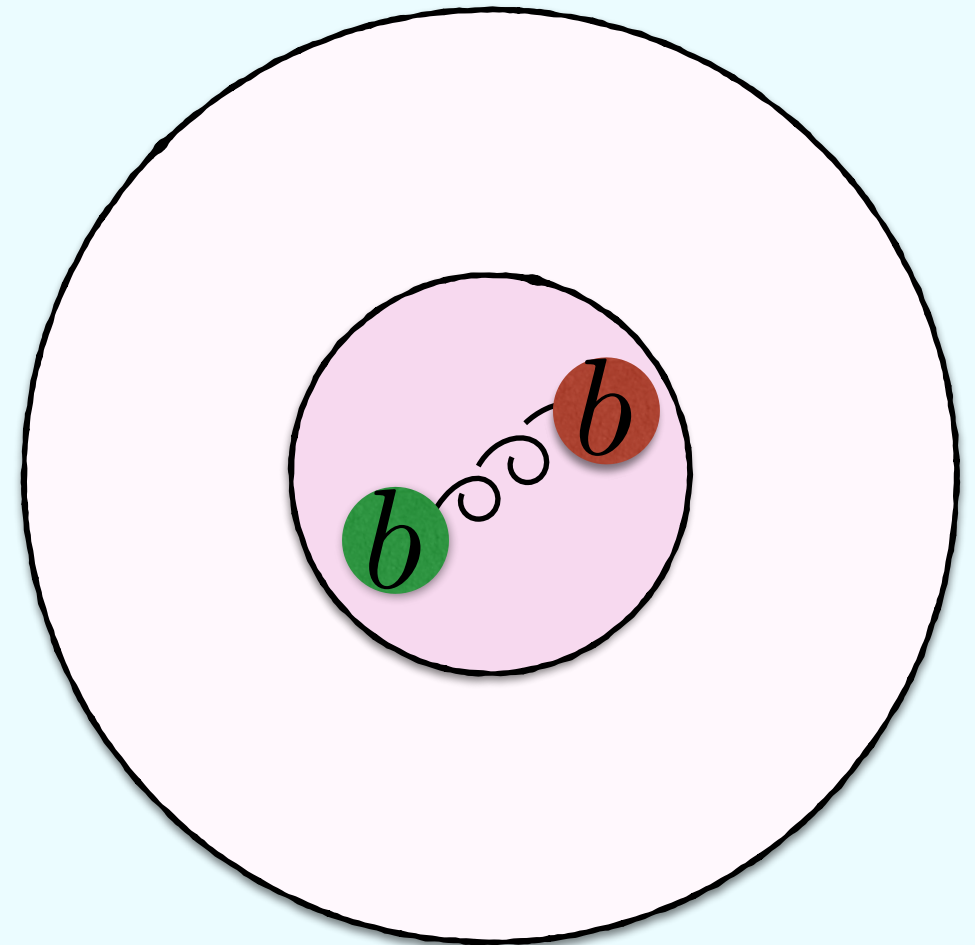
📌 Intuitive Understanding ([arxiv:1707.09575](https://arxiv.org/abs/1707.09575))



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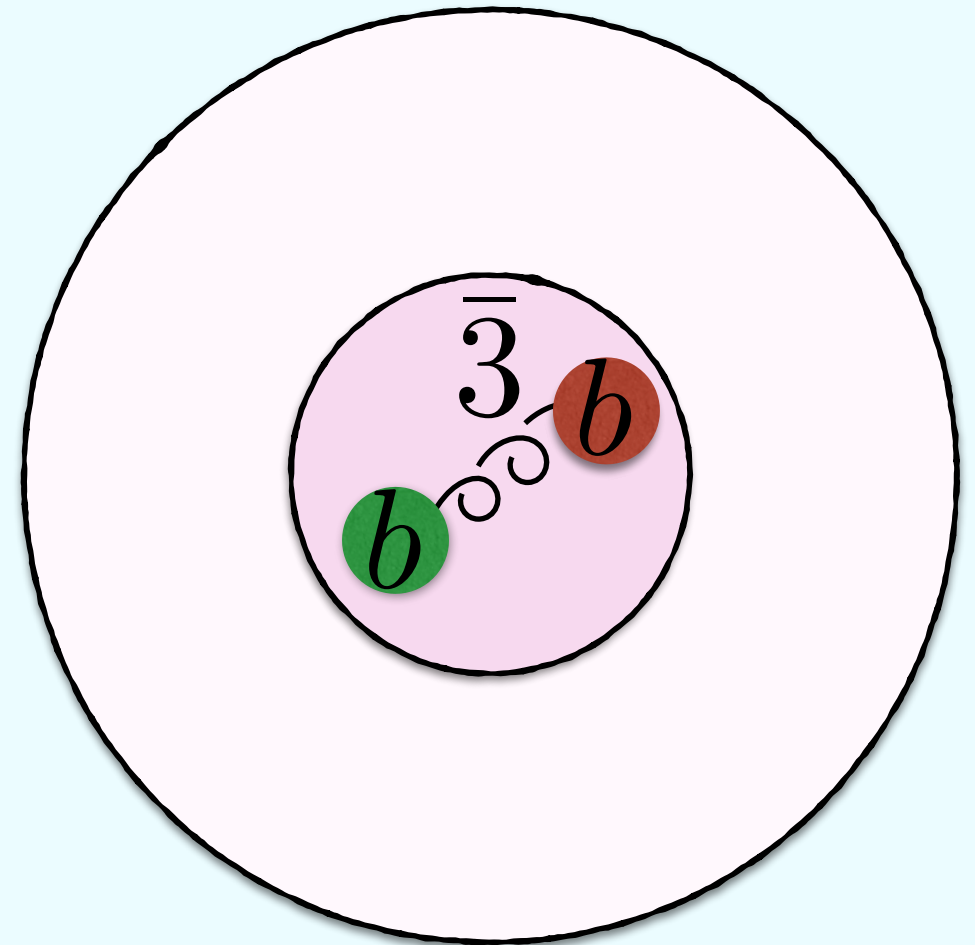
- bb diquark in heavy quark mass limit



$bb\bar{u}\bar{d}$, $I = 0$, $J^P = 1^+$ is bound

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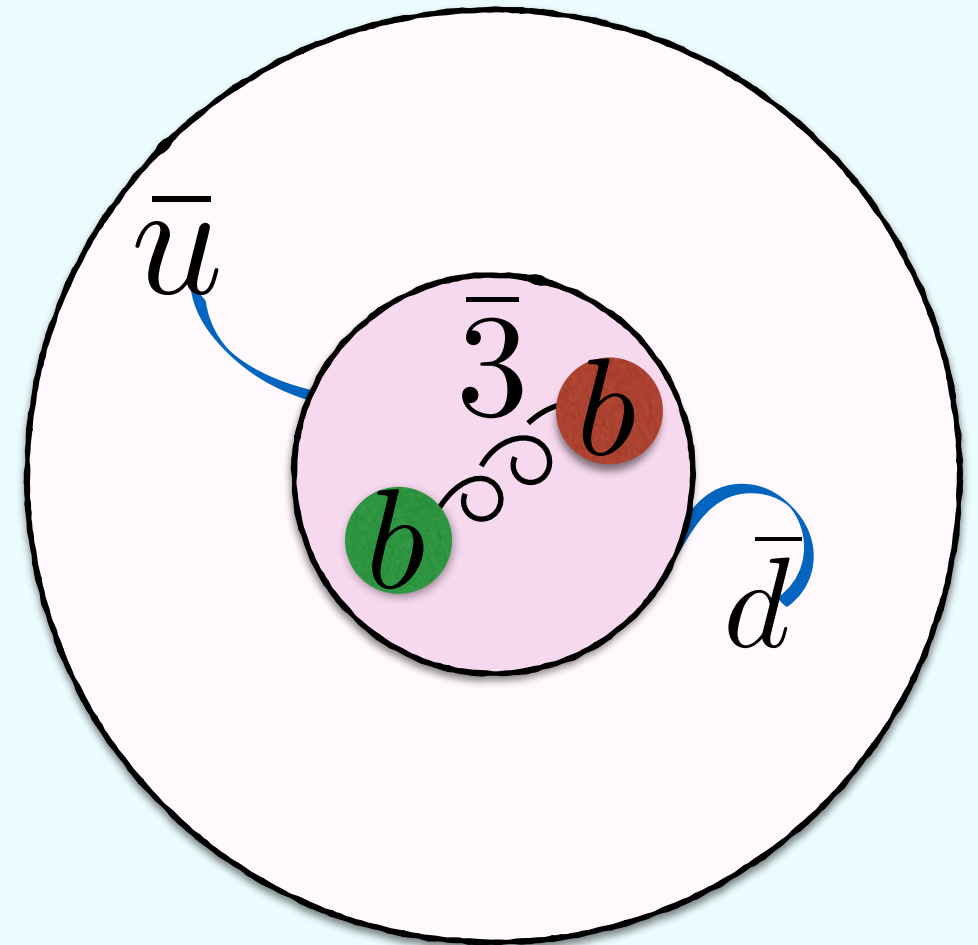
- bb diquark in heavy quark mass limit
- in attractive $\bar{3}$ channel



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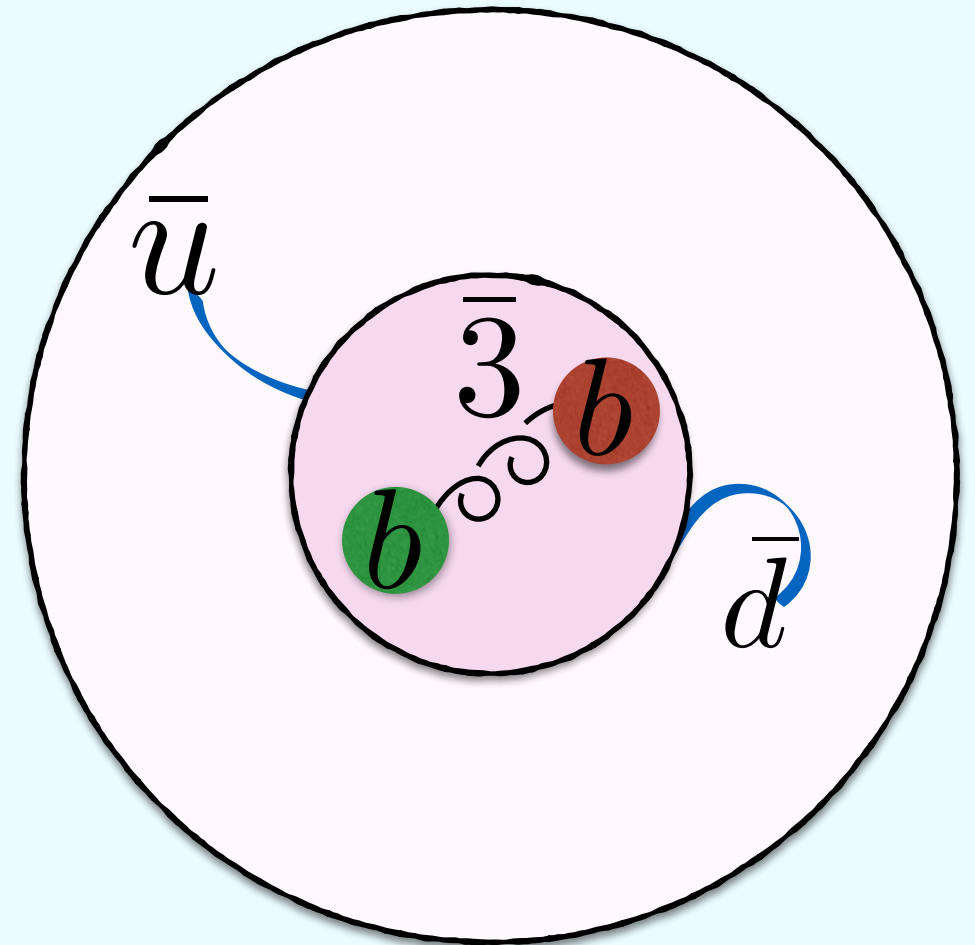
- bb diquark in heavy quark mass limit
- in attractive $\bar{3}$ channel
- light quarks in cloud screen bb interaction



$bb\bar{u}\bar{d}$, $I = 0$, $J^P = 1^+$ is bound

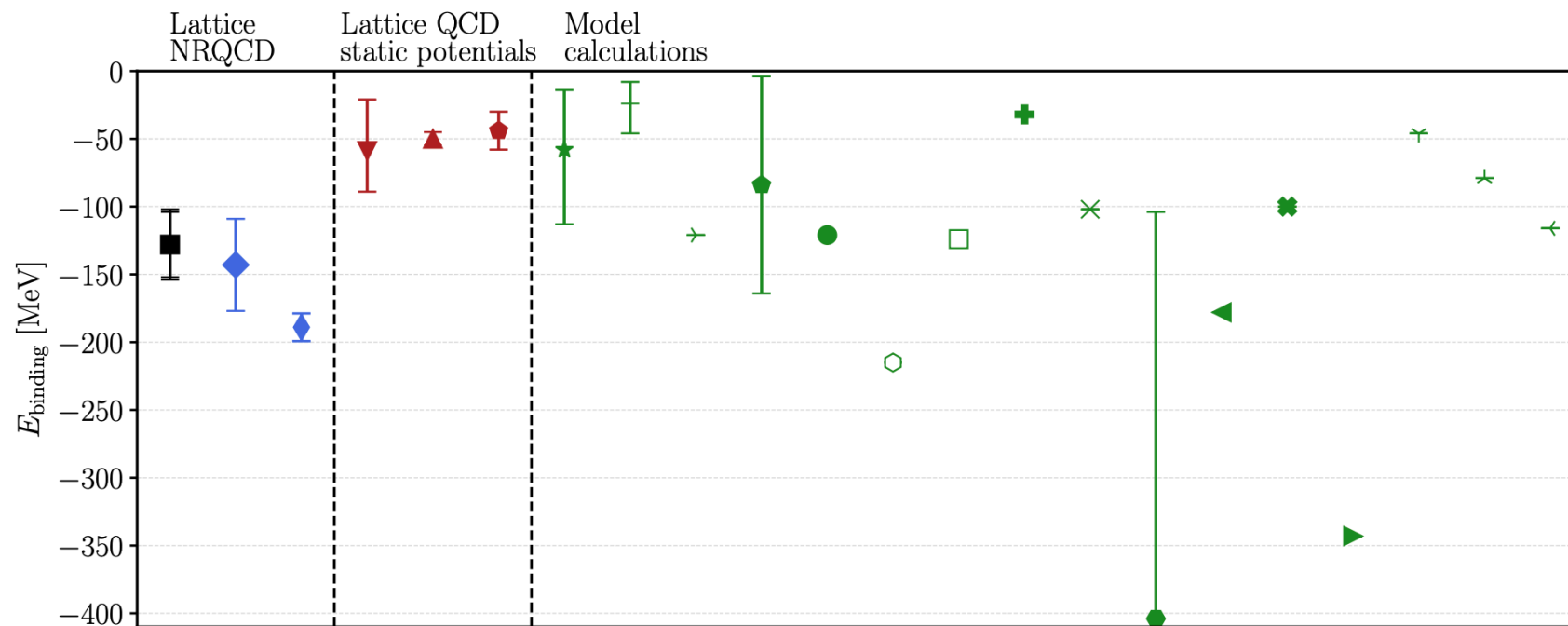
📌 Intuitive Understanding ([arxiv:1707.09575](https://arxiv.org/abs/1707.09575))

- bb diquark in heavy quark mass limit
- in attractive $\bar{3}$ channel
- light quarks in cloud screen bb interaction
- Finite b mass does not change picture



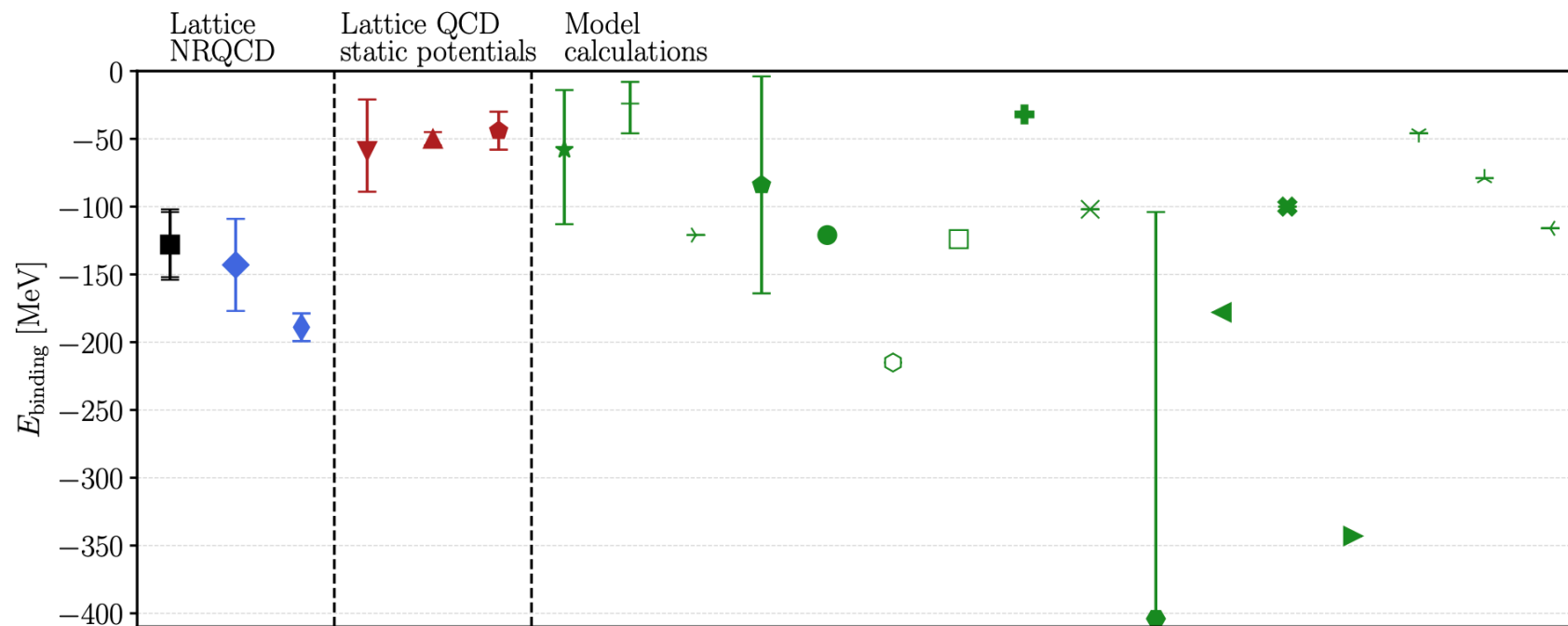
$bb\bar{u}\bar{d}$, $I = 0$, $J^P = 1^+$ is bound

📌 Broad theoretical consensus that this state is bound



[arxiv:1904.04197](https://arxiv.org/abs/1904.04197)

$bb\bar{u}\bar{d}$, $I = 0$, $J^P = 1^+$ is bound



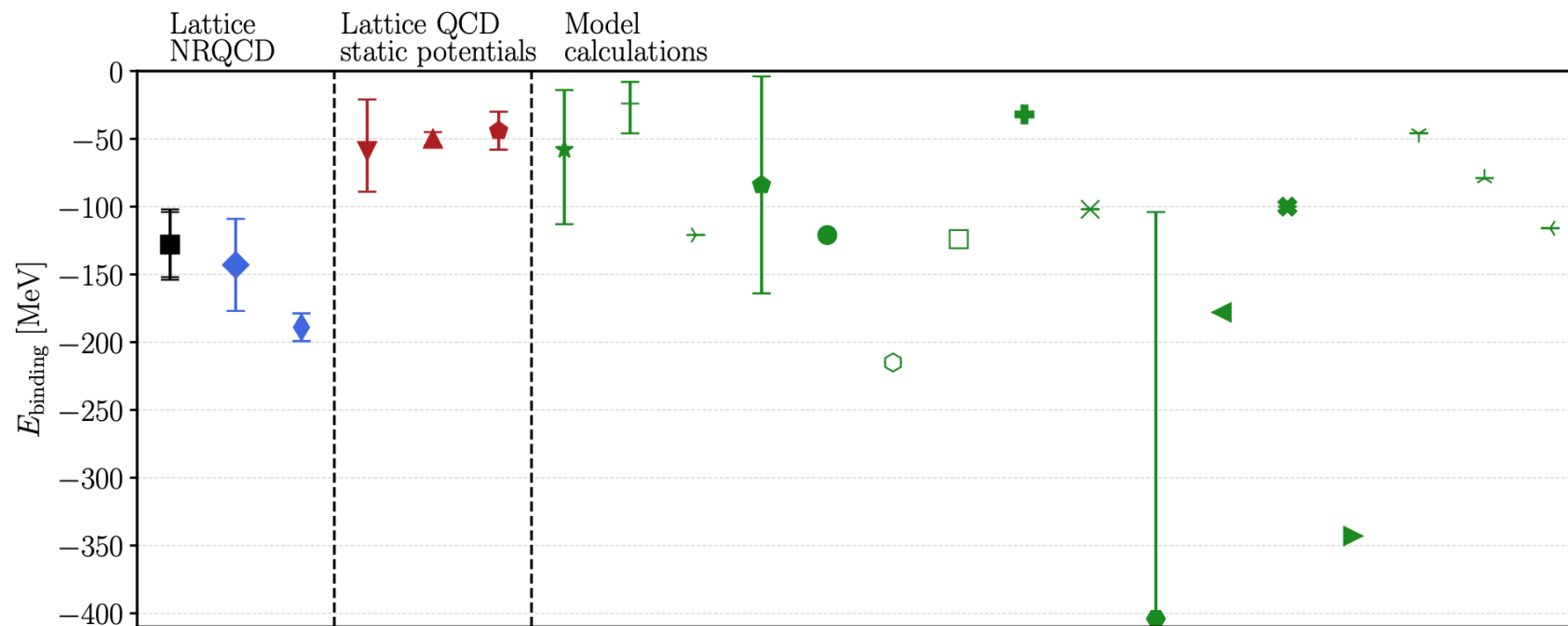
| | | |
|----------------------------|------------------------------|-----------------------------------|
| ■ This work | ⊥ Park et al. (2018) | ● Navarra et al. (2007) |
| ◆ Junnarkar et al. (2018) | ● Wang (2017) | ▲ Vijande et al. (2006) |
| ◇ Francis et al. (2016) | ● Eichten and Quigg (2017) | ✱ Janc and Rosina (2004) |
| ▽ Bicudo et al. (2016) | ◇ Karliner and Rosner (2017) | ▶ Vijande et al. (2003) |
| ▲ Brown and Orginos (2012) | □ Lee and Yasui (2009) | ⊥ Brink and Stancu (1998) |
| ● Bicudo and Wagner (2012) | ✱ Zhang et al. (2007) | ⊥ Silvestre-Brac and Semay (1993) |
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● Broad theoretical consensus that this state is bound

● Need experimental verification via perhaps

$$T_{\bar{u}\bar{d}}^{bb} \rightarrow \Xi_{bc}^0 \bar{p} \text{ or } B^- D^+ \pi^-$$

$bb\bar{u}\bar{d}$, $I = 0$, $J^P = 1^+$ is bound



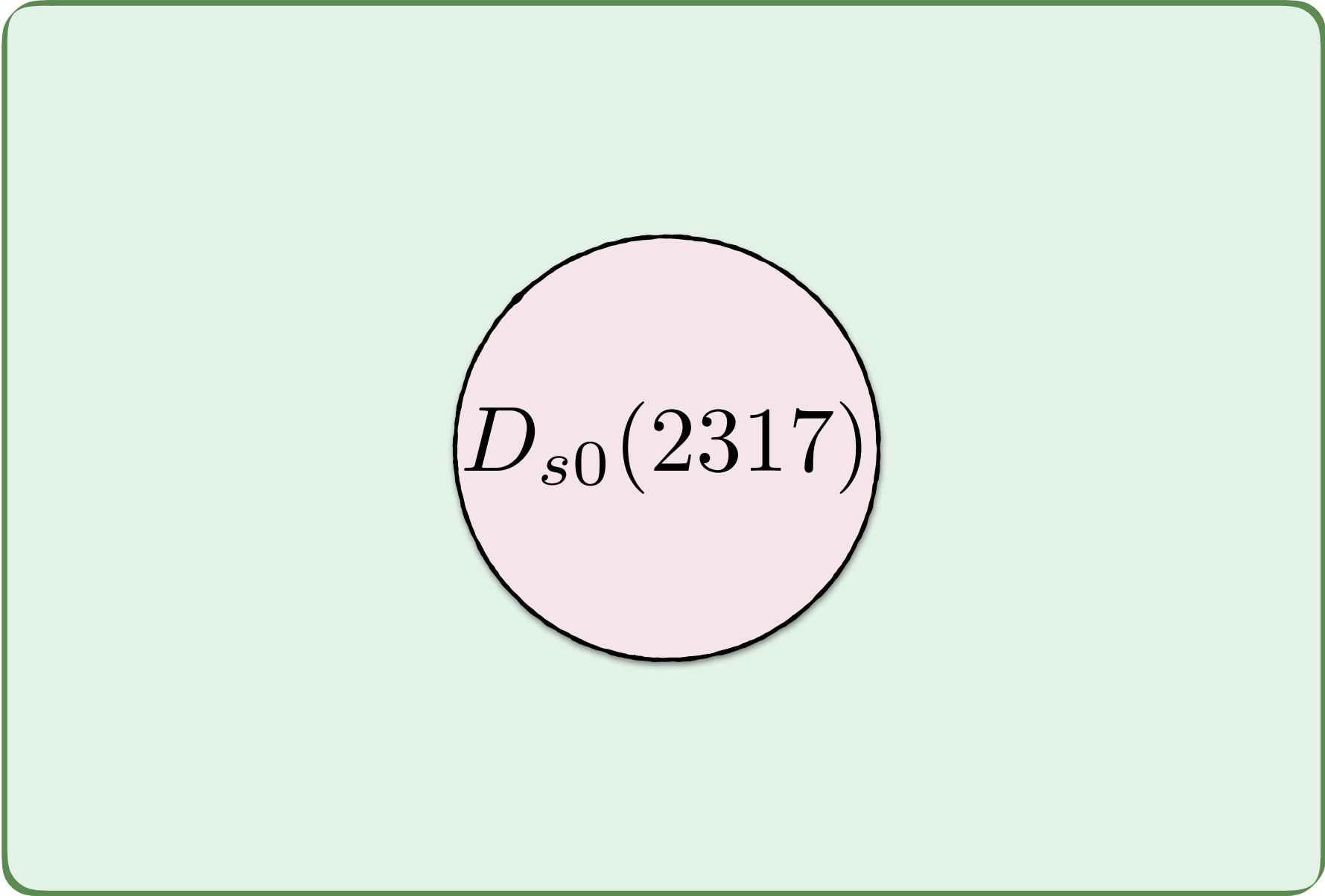
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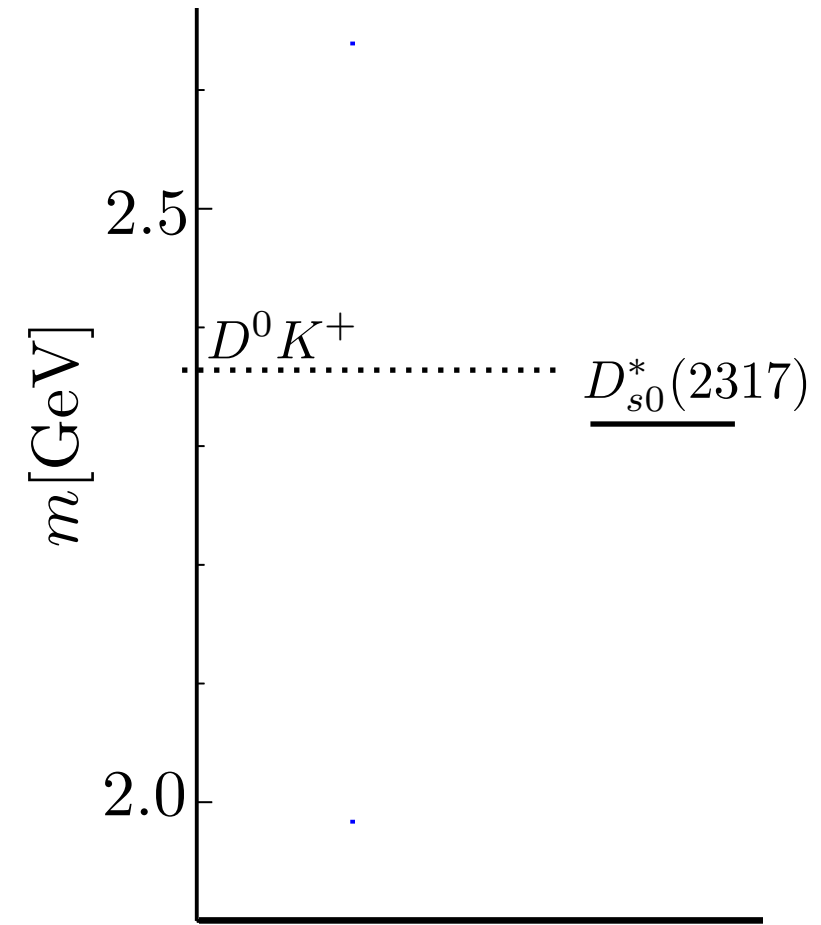
📌 For review talk of these types of tetraquarks see A. Francis talk [here](#)

$D_{s0}(2317)$

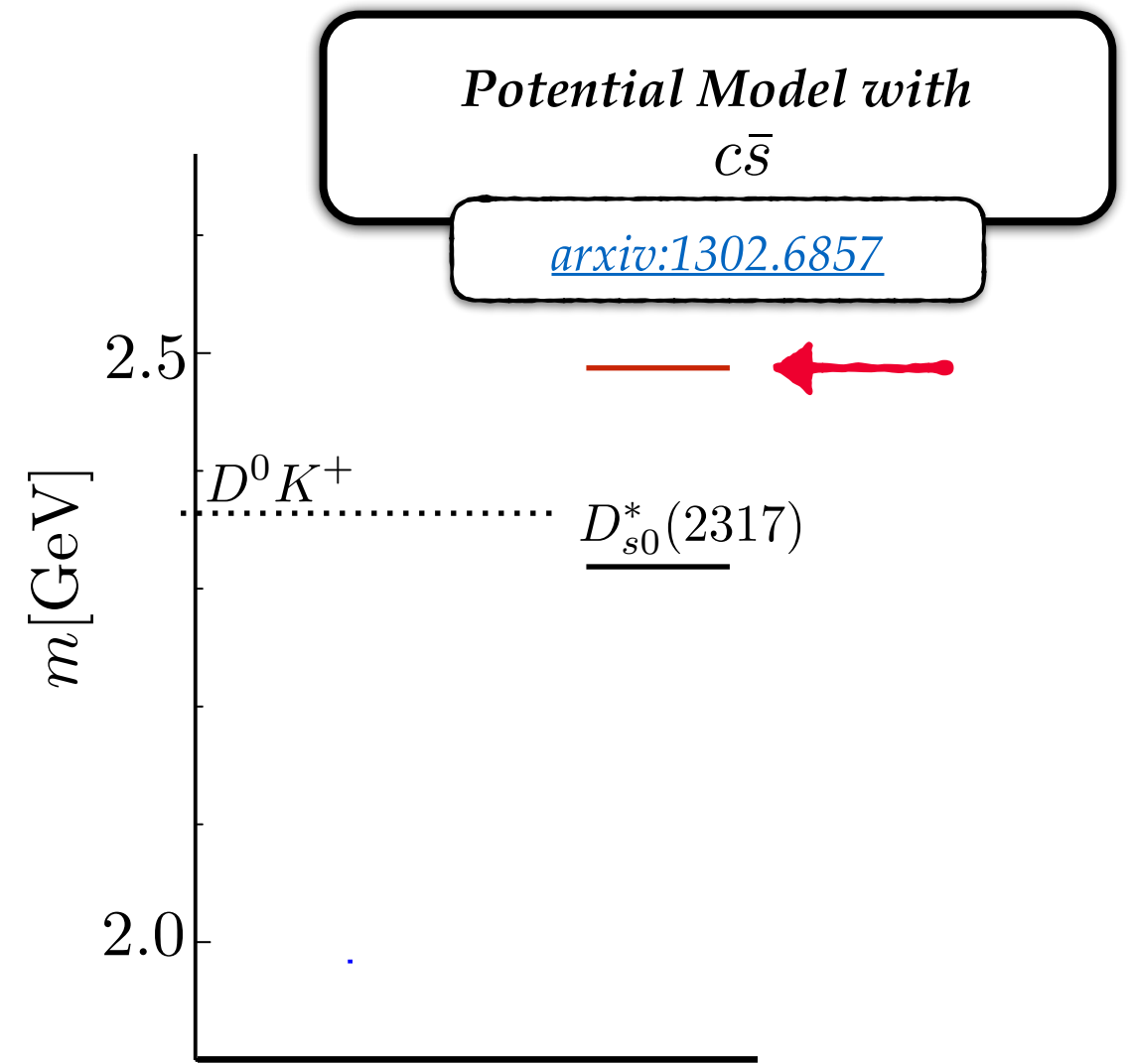


$D_{s0}(2317)$

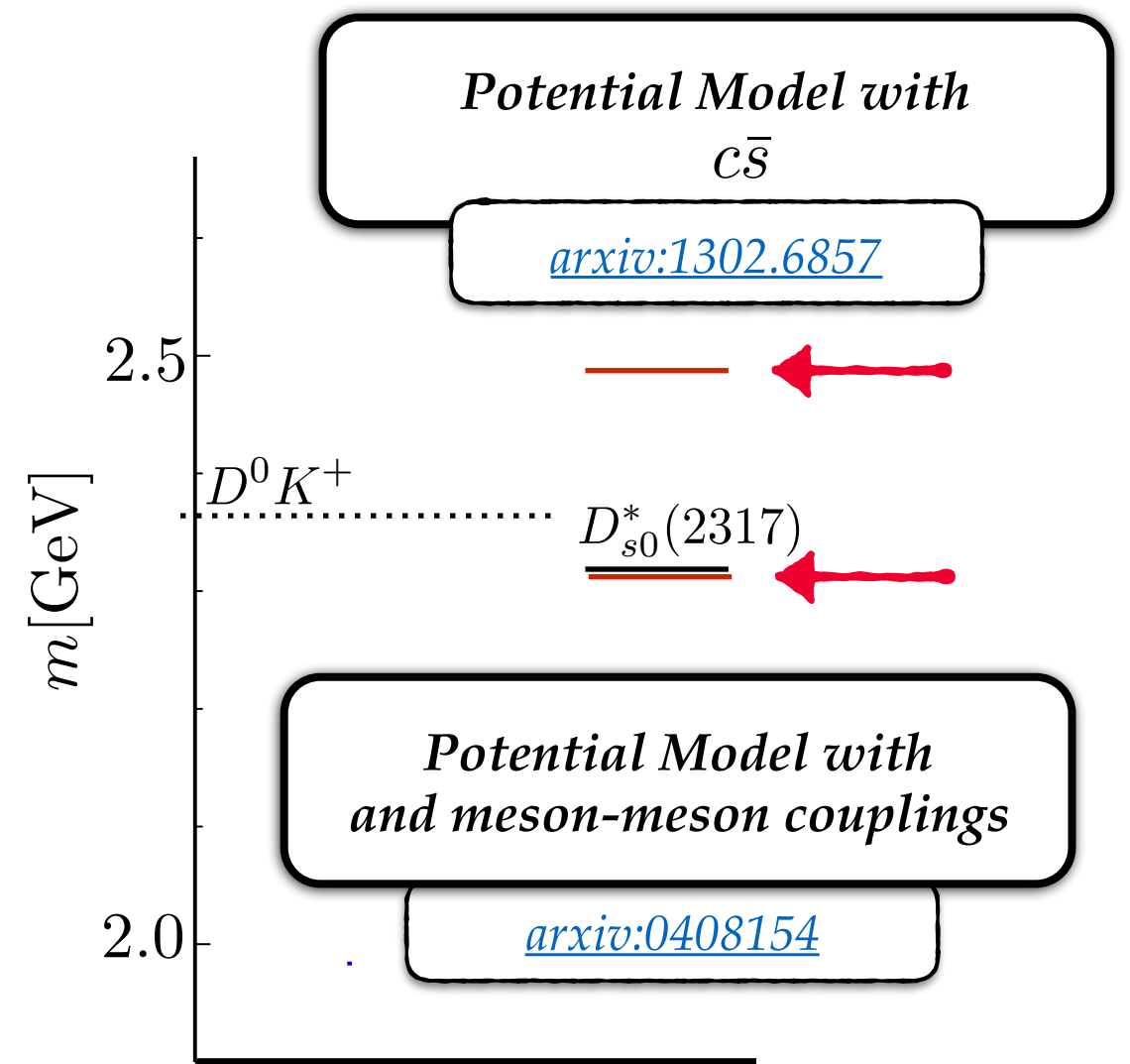
$D_{s0}(2317)$



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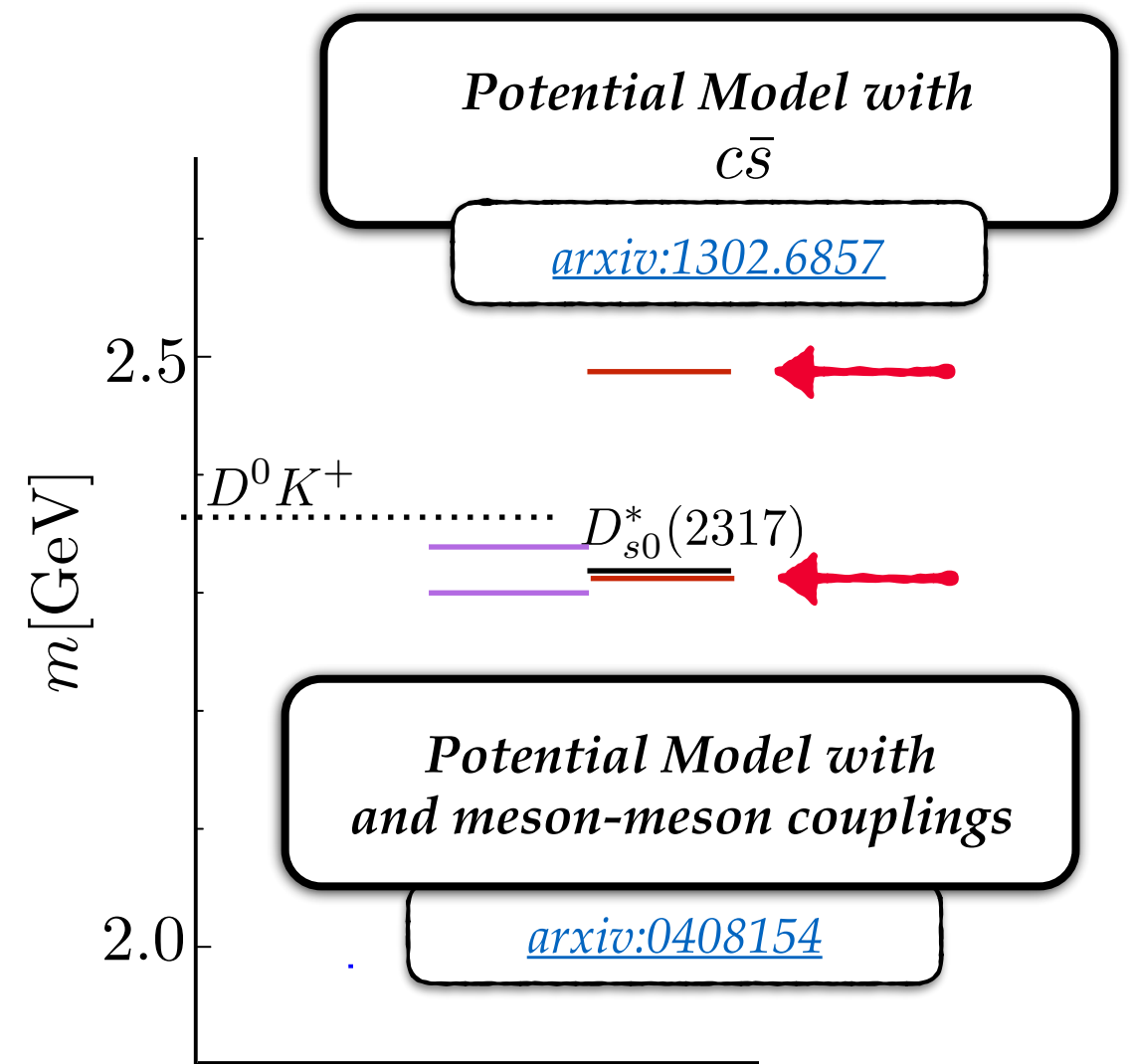
[arxiv:1308.3175](#), [arxiv:1706.01247](#),
[arxiv:2008.06432](#), [arxiv:1911.08435](#)

$c\bar{s}$ and DK important

Diquark not important

Bound State Pole

Lattice QCD



$D_{s0}(2317)$

📌 Practical Proposal: Supplement
Experimental Data with Lattice
QCD

[arxiv:1911.02024](https://arxiv.org/abs/1911.02024)

$D_{s0}(2317)$

- 📌 Practical Proposal: Supplement Experimental Data with Lattice QCD
- 📌 Use HQET and χ -PT to study

$$D_{s0} \rightarrow D \quad K$$


as a function of m_s

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as a function of m_s


$$\begin{aligned} \text{HQET: } & M_D = m_c + m_l + C \\ \chi\text{-PT: } & M_K^2 \propto m_l + m_s \end{aligned}$$


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as a function of m_s

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 - M_D changes as $-\epsilon$
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 \Rightarrow Can make D_{s0} sit at threshold


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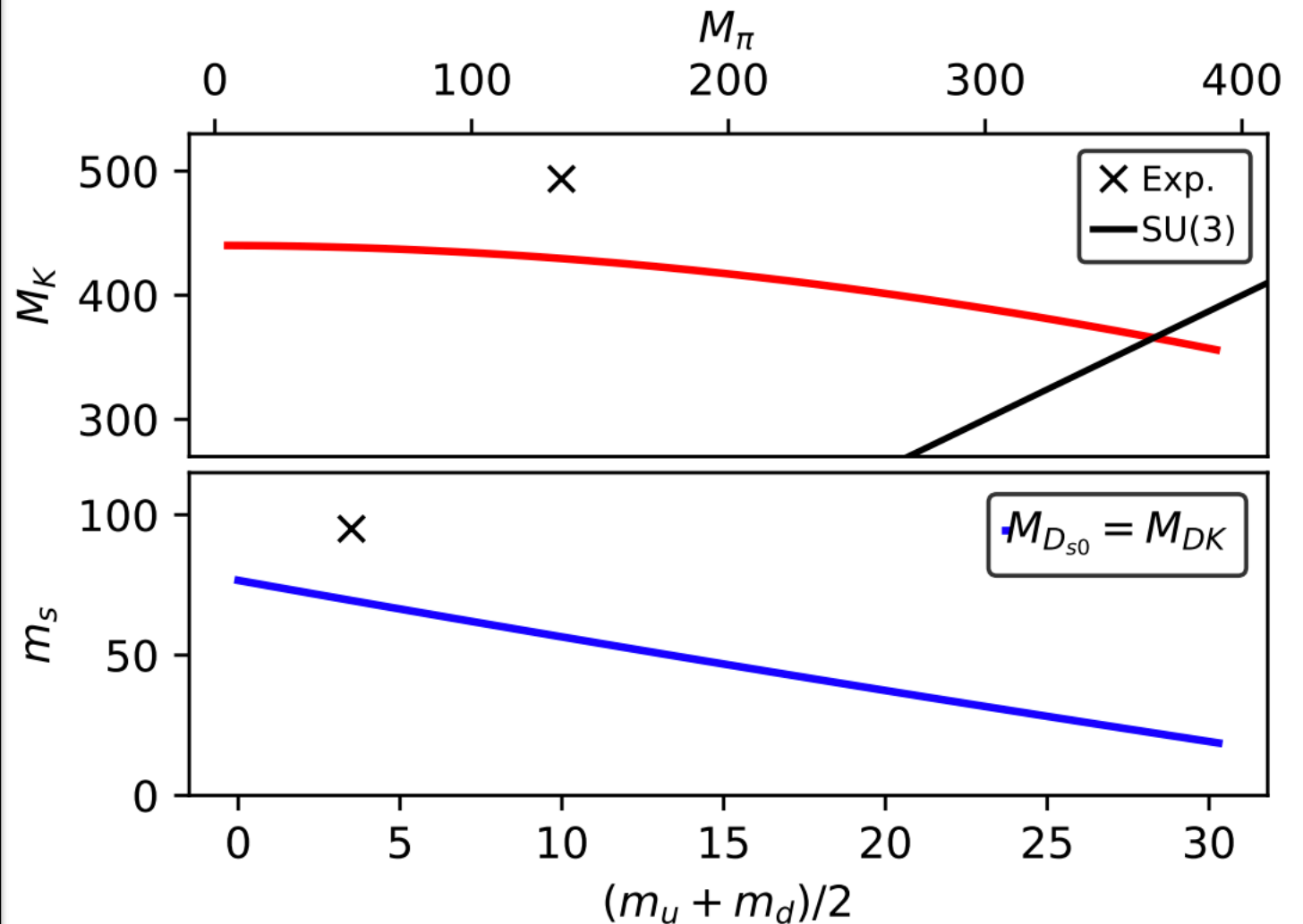
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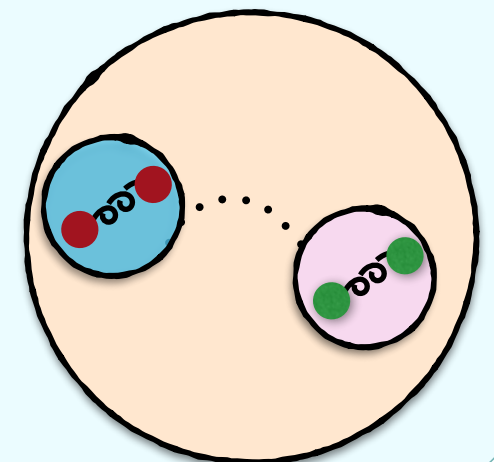
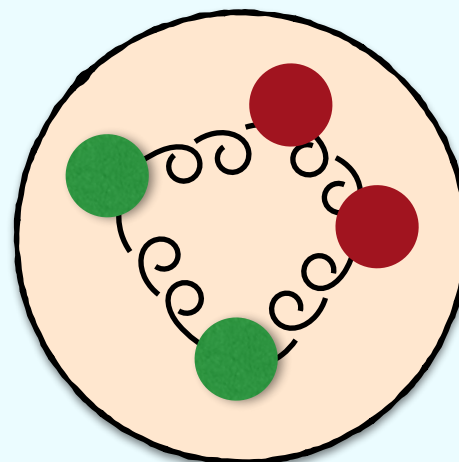
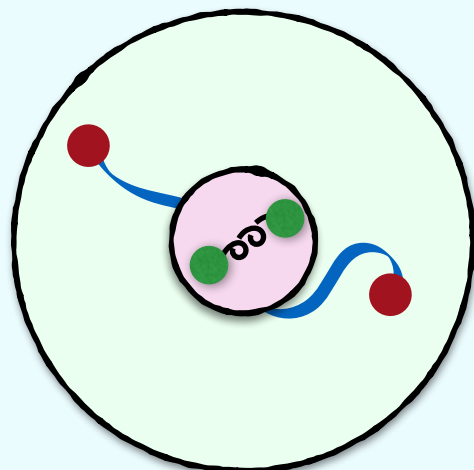


Theory Overview of Heavy Exotic Spectroscopy

Ciaran Hughes: chughes@fnal.gov



*Future Looking Bright With Lots
of New Experimental Data
combined with Exciting Theory
Understanding!*



Back-Up Slides

Scattering Overview: What Is A State?

📌 *Defⁿ*: “State” = A Pole Singularity of the Scattering Matrix

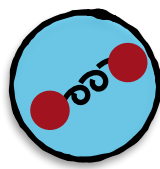
📌 What A State is *Not* : A Bump In Experimental Data


- Non-Pole Singularities of S-Matrix Due To Kinematical Effects (which are not a state) can cause Data to go bump, e.g., [arxiv:1912.07030](https://arxiv.org/abs/1912.07030)
 - Cusps (Opening of Nearby Multi-Particle Thresholds)
 - Triangle Singularity
- Cusp/Triangle Singularity and State (which is a Pole) may both be Present in Experimental Data

📌 Breit-Wigner theoretically motivated if only one resonance in one channel
(*pdg mini-review on resonances*)

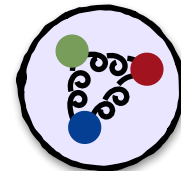
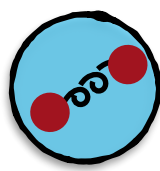
📌 N.B.: Unitarity and Analyticity give rise to non-trivial line shapes. Cannot use sum of Breit-Wigners, use eg., K-matrix, see [inspire:1519654](https://inspirehep.net/literature/1519654)

Conventional States



 Def^n : “Conventional States” = “States we understand well enough”

Conventional States



📌 *Defⁿ*: “Conventional States” = “States we understand well enough”

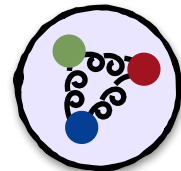
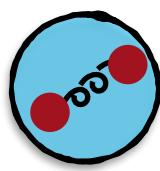
📌 For $\Lambda_{\text{QCD}} \ll m_q$, potentials between valence quarks justified

$$V(r) = -\frac{\kappa}{r} + \sigma r + C + \dots$$

Pheno: (1978) Phys. Rev. D 17 3090

Lattice: arxiv:0001312
arxiv:0903.3598

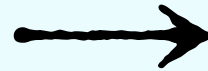
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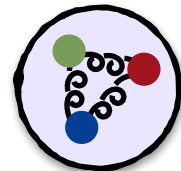
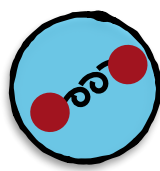



$$(T + V(r))\psi(r) = E\psi(r)$$

Pheno: (1978) Phys. Rev. D 17 3090

*Lattice: arxiv-0001312
arxiv:0903.3598*

Conventional States



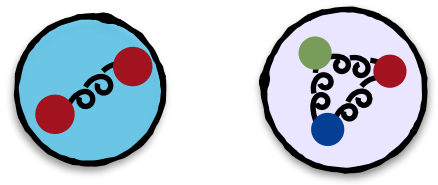
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Conventional States

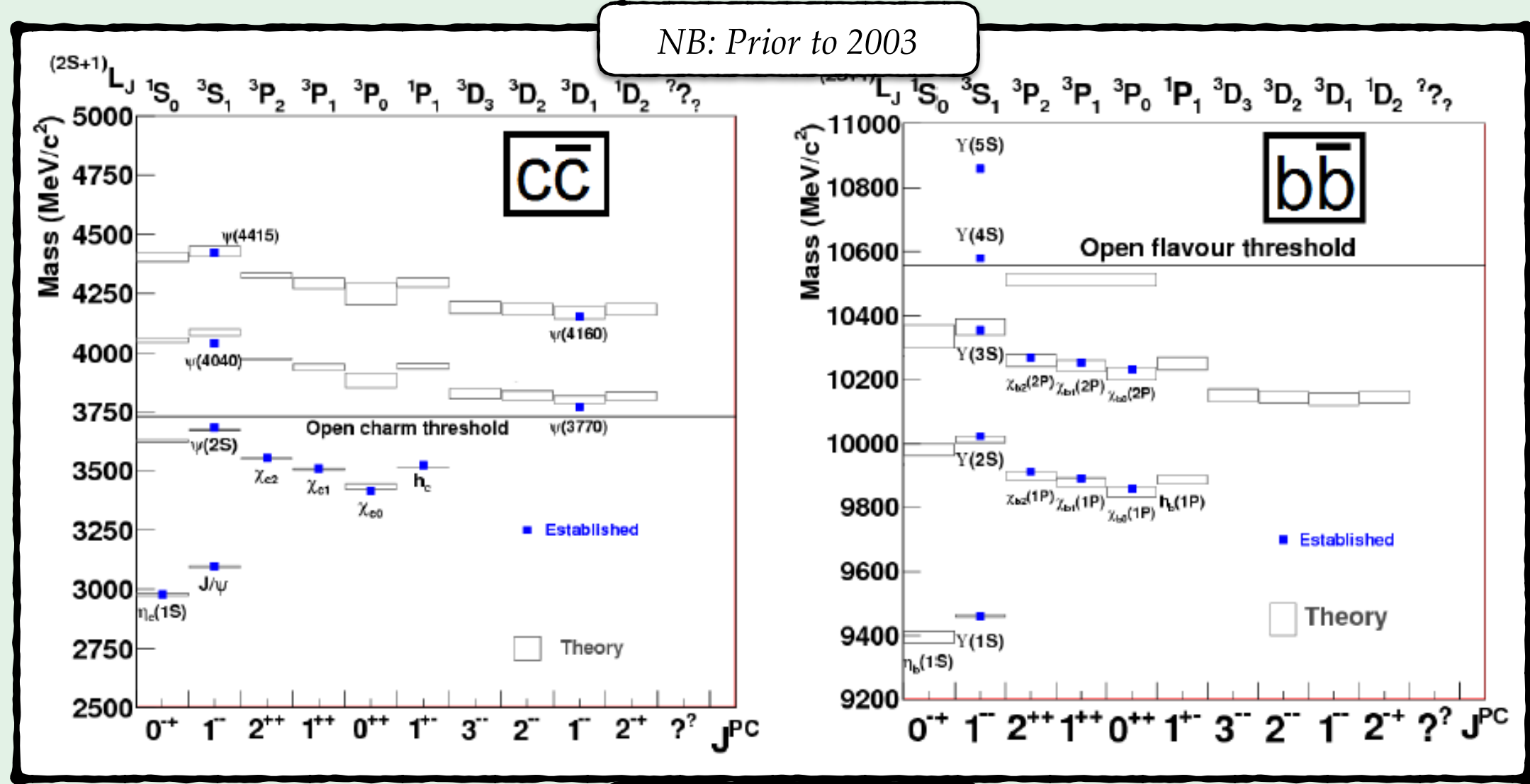


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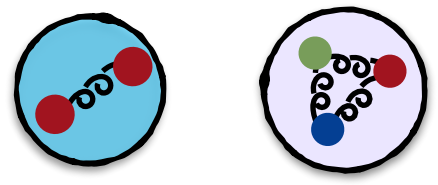
\uparrow

$$(T + V(r))\psi(r) = E\psi(r)$$



E. Prencipe, 2019

Conventional States

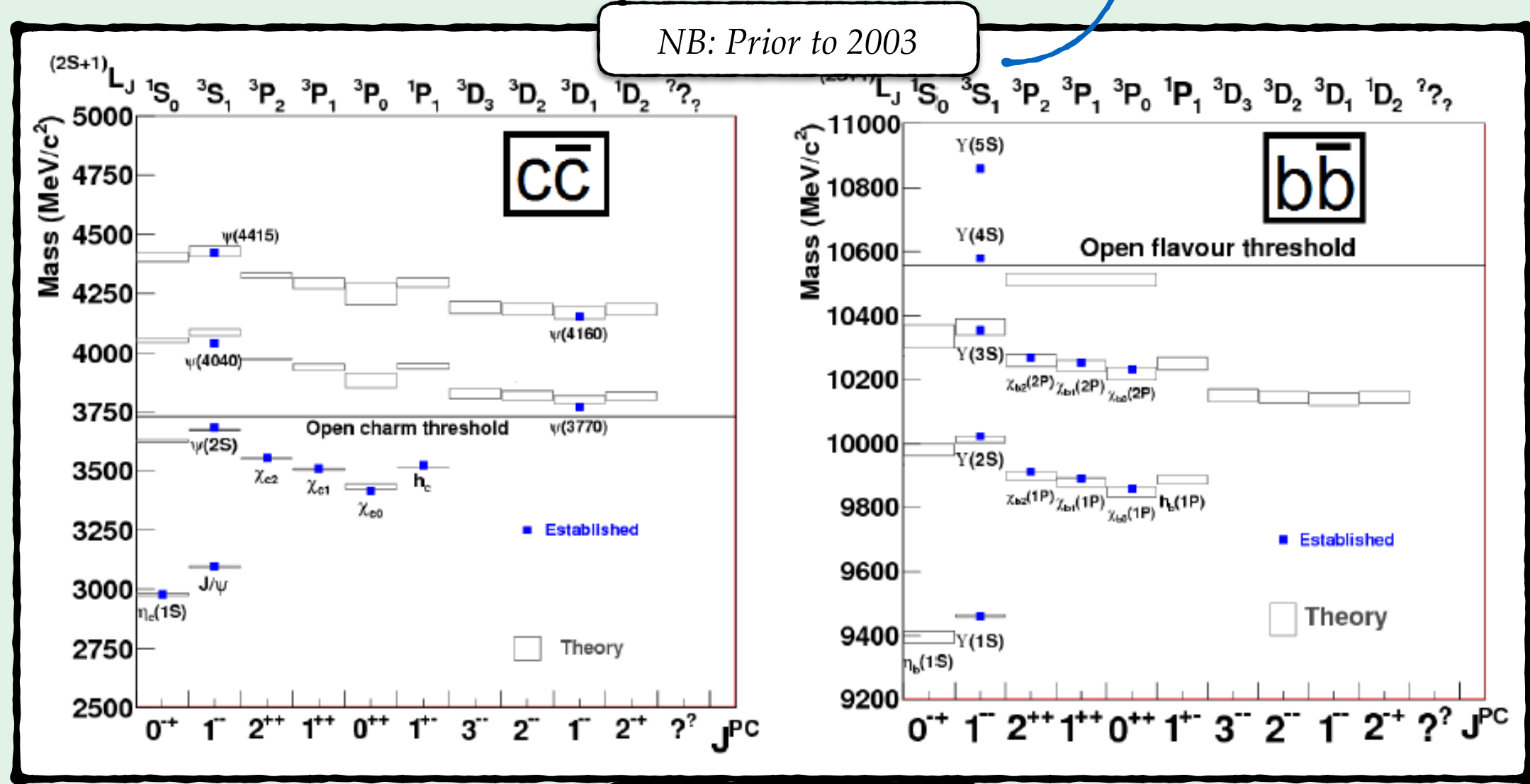


Defⁿ: “Conventional States” = Mesons (valence $\bar{q}q$) and Baryons (valence qqq) in line with quark potential model expectations

$$V(r) = -\frac{\kappa}{r} + \sigma r + C + \dots$$

↑

$$(T + V(r))\psi(r) = E\psi(r)$$



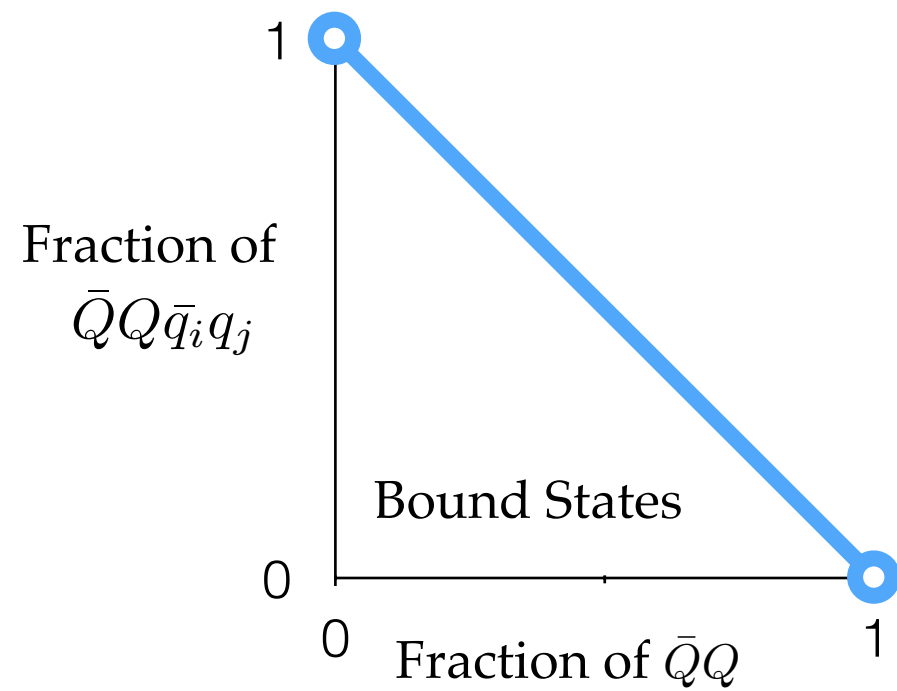
E. Prencipe, 2019

Classification

📌 Need a classification system like “Periodic Table of Exotics”

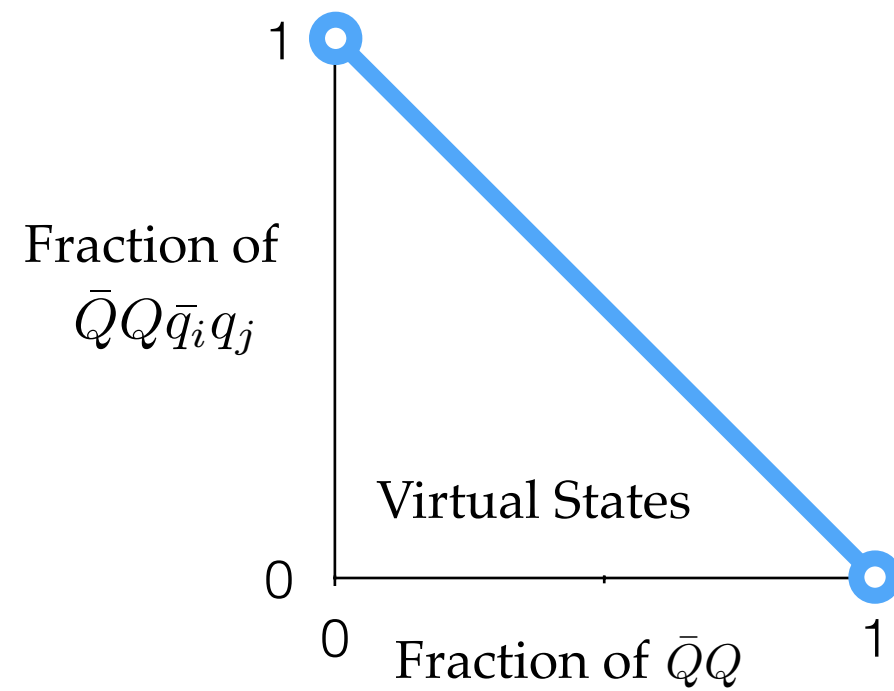
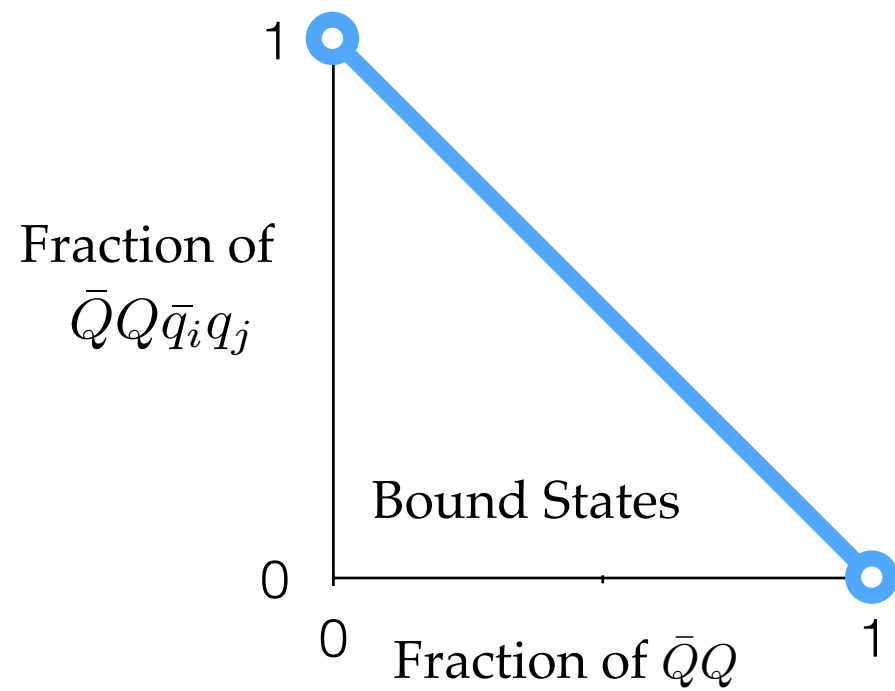
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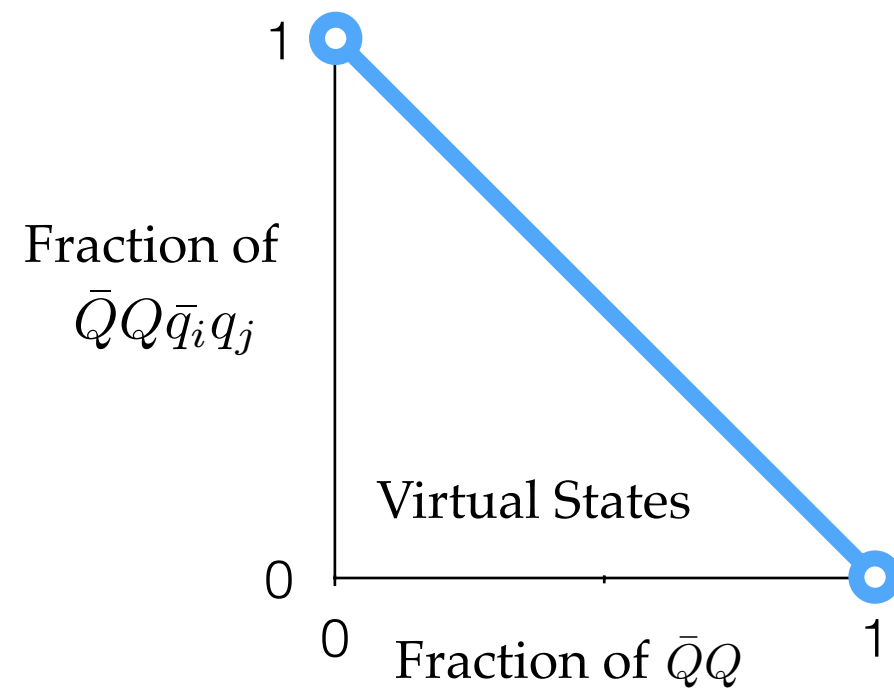
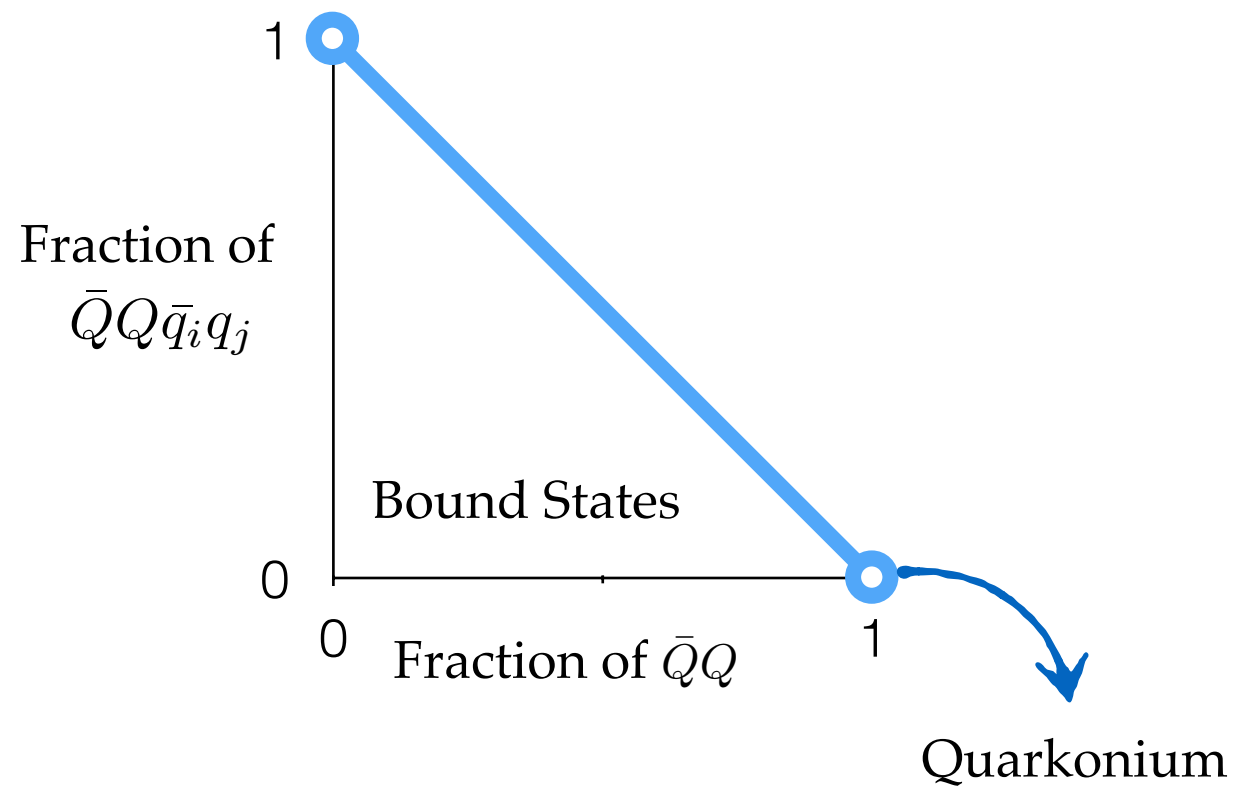
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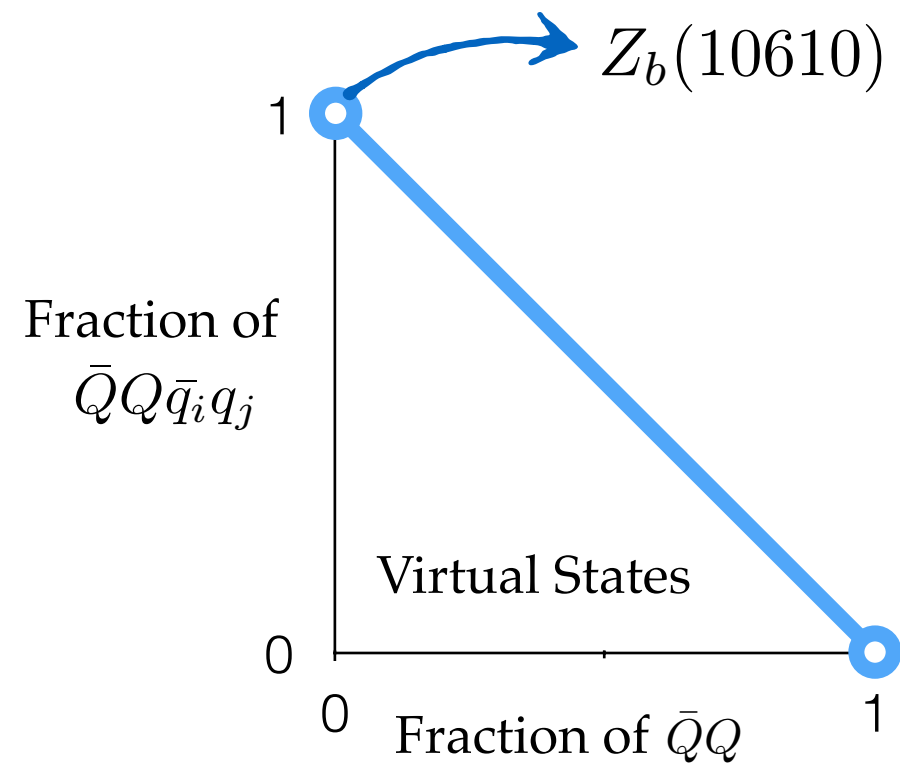
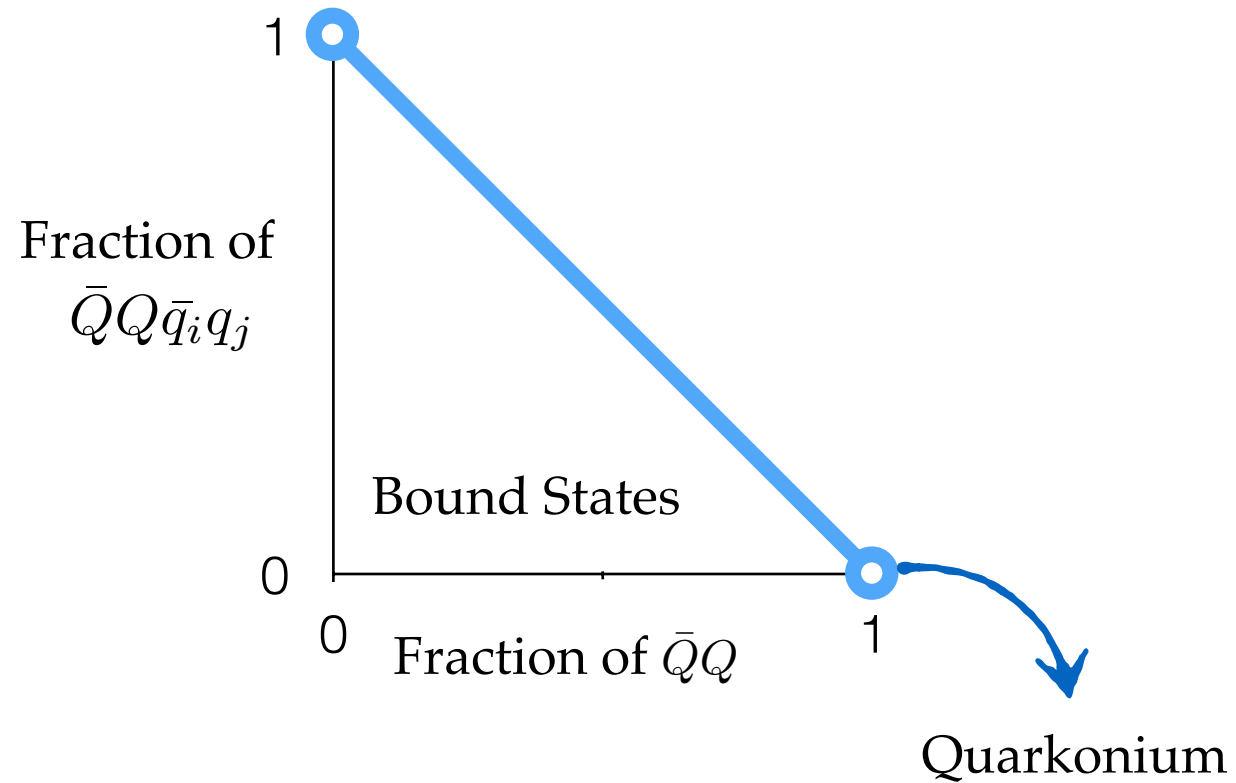
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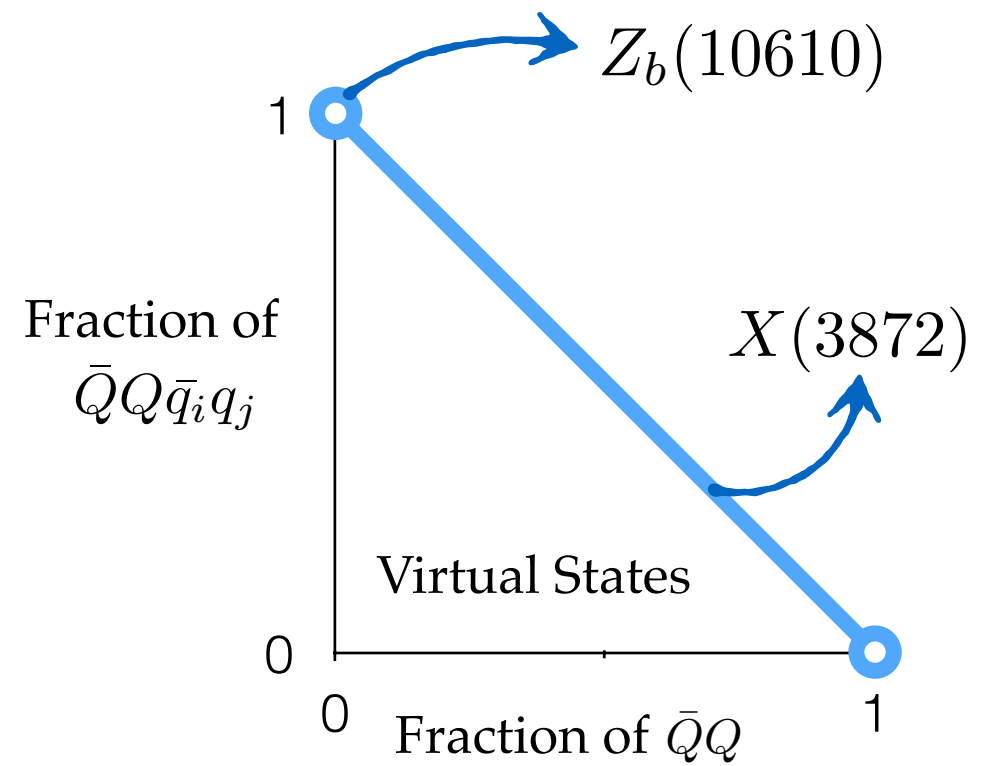
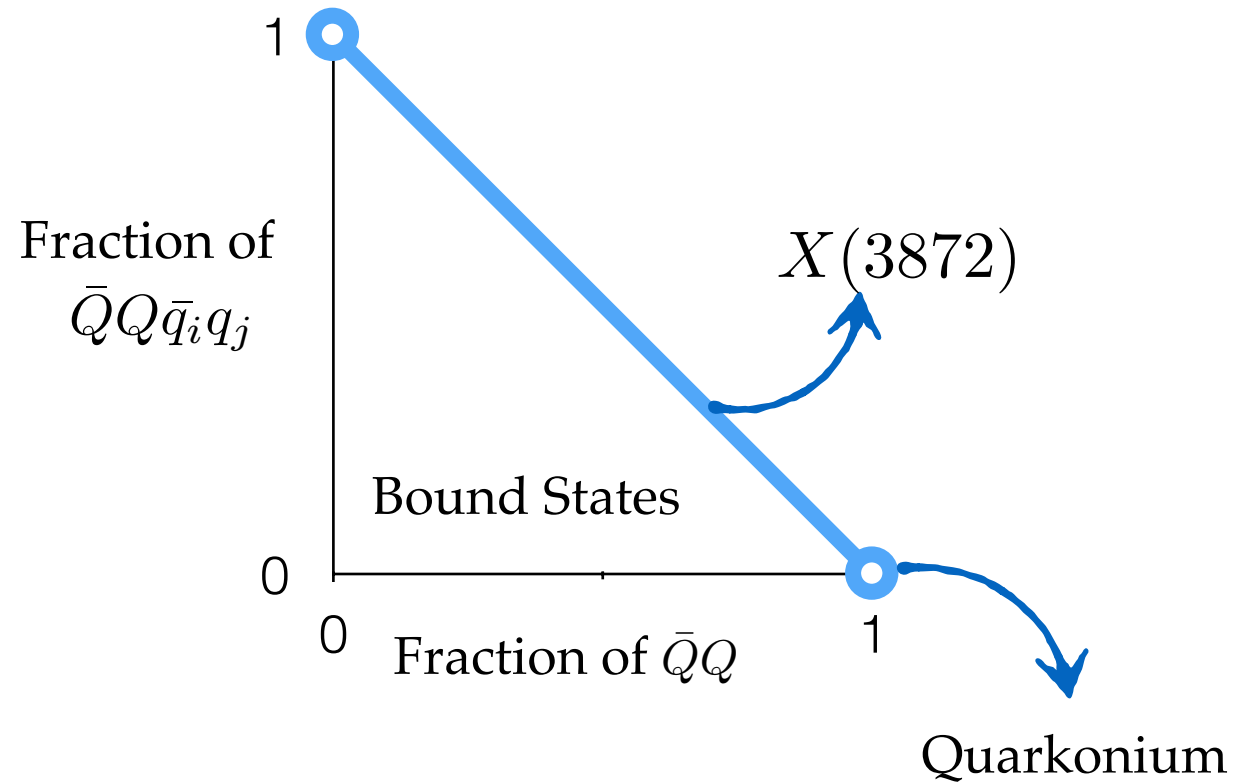
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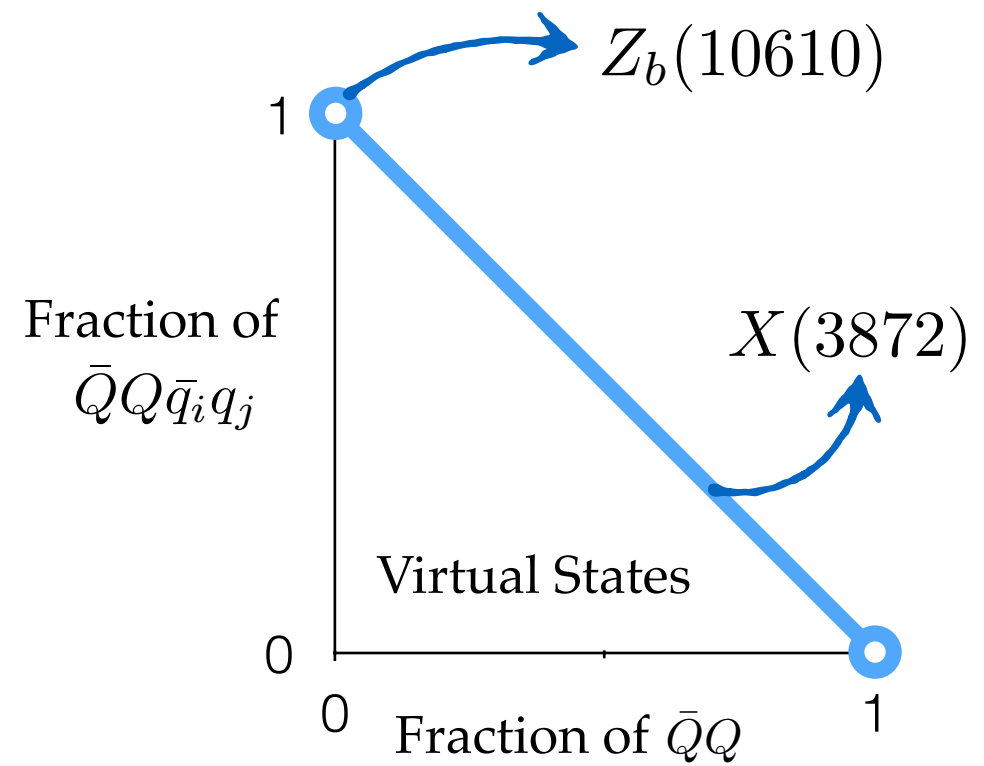
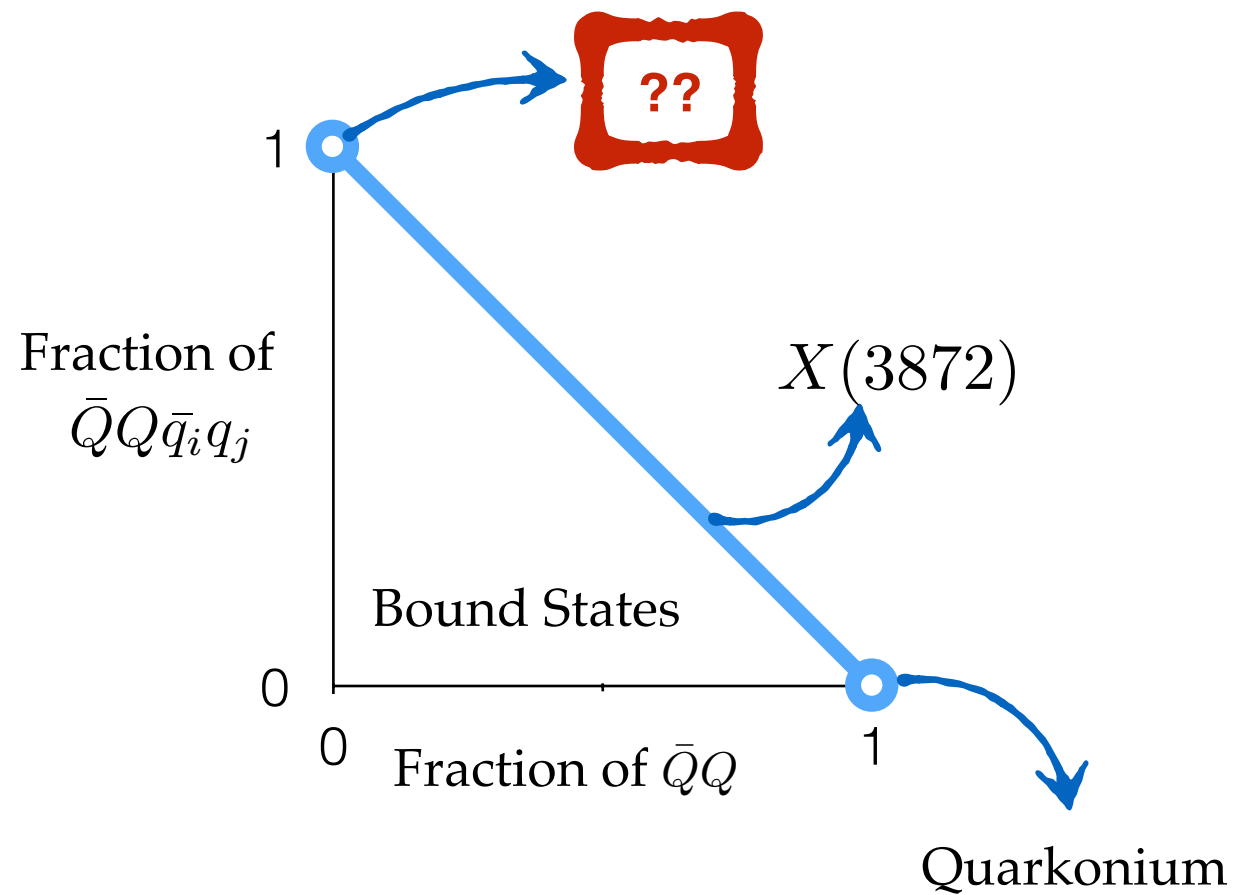
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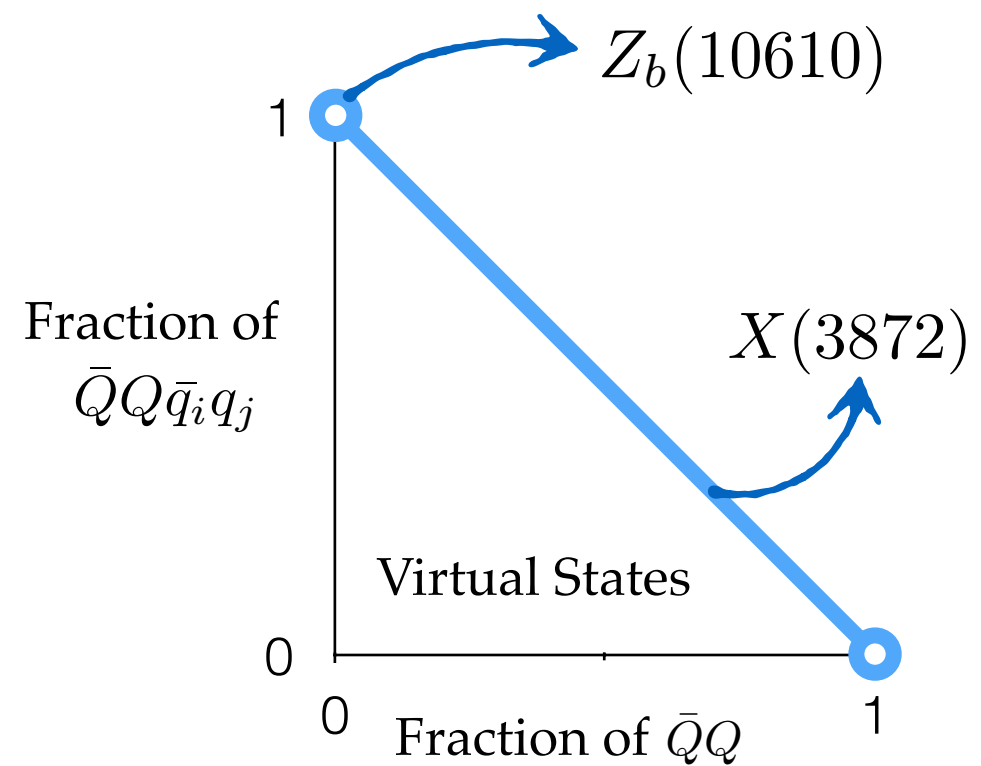
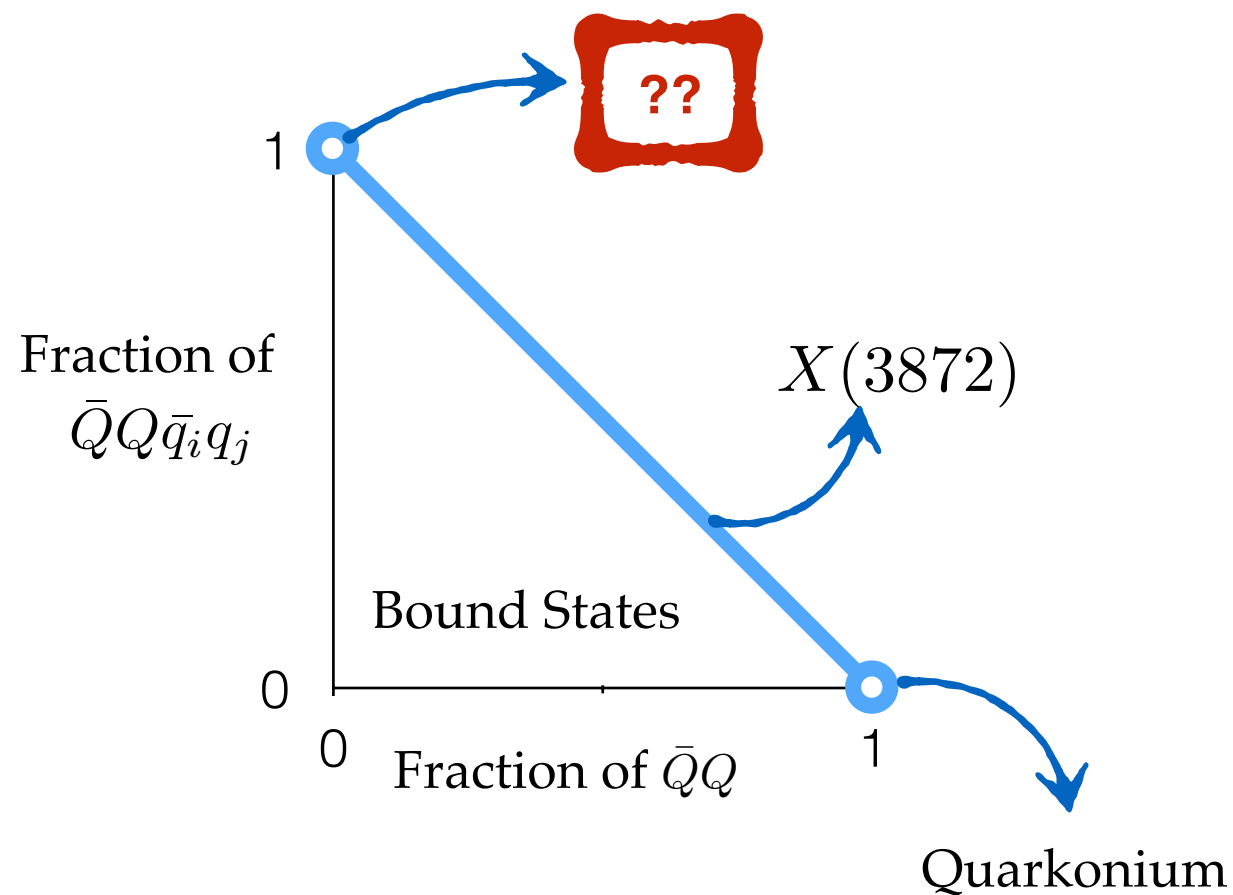
Classification

- Need a classification system like “Periodic Table of Exotics”



Classification

- Need a classification system like “Periodic Table of Exotics”
- Need no mixing, deeply bound, and experimentally testable.
=> Clean and simple system to understand, which can be used to understand more complicated XYZ



$\psi(4230)$ aka $Y(4230)$ aka $Y(4260)$

Quantum Numbers

$$J^{PC} = 1^{--}$$

$$Q = 0$$

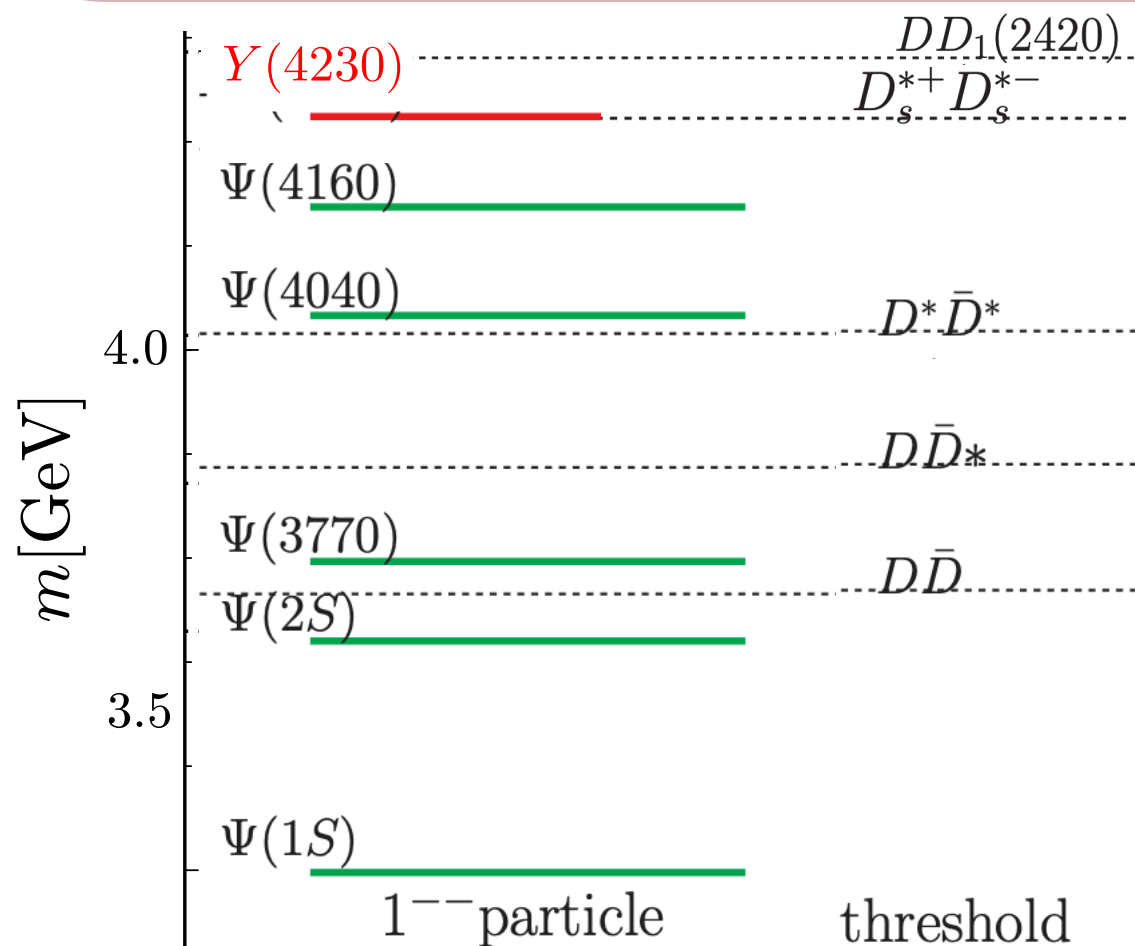
$$I^G = 0^-$$

Notable Decays

- Seen $\mathcal{B}(\pi^+\pi^-J/\psi)$ $\mathcal{B}(\pi^+\pi^-h_c)$ $\mathcal{B}(\pi^+D^{*-}D^0)$ $\mathcal{B}(\gamma X(3872))$
- Not Seen: Any Open-Charm Decays, e.g, $\mathcal{B}(D\bar{D})$

- $M_{PDG} = 4220 \pm 15 \text{ MeV}$

- $\Gamma_{PDG} = 20 - 100 \text{ MeV}$



Scenario 3: $Y(4230) = \psi(4160)$ ([arxiv:1902.09268](https://arxiv.org/abs/1902.09268))

- $Y(4230)$ is not a new state at all!
 - $\psi(4160)$ is strongly coupled to
 - $D_s^*\bar{D}_s^*$ threshold (+30 MeV above)

$\psi(4230)$ aka $Y(4230)$ aka $Y(4260)$

Quantum Numbers

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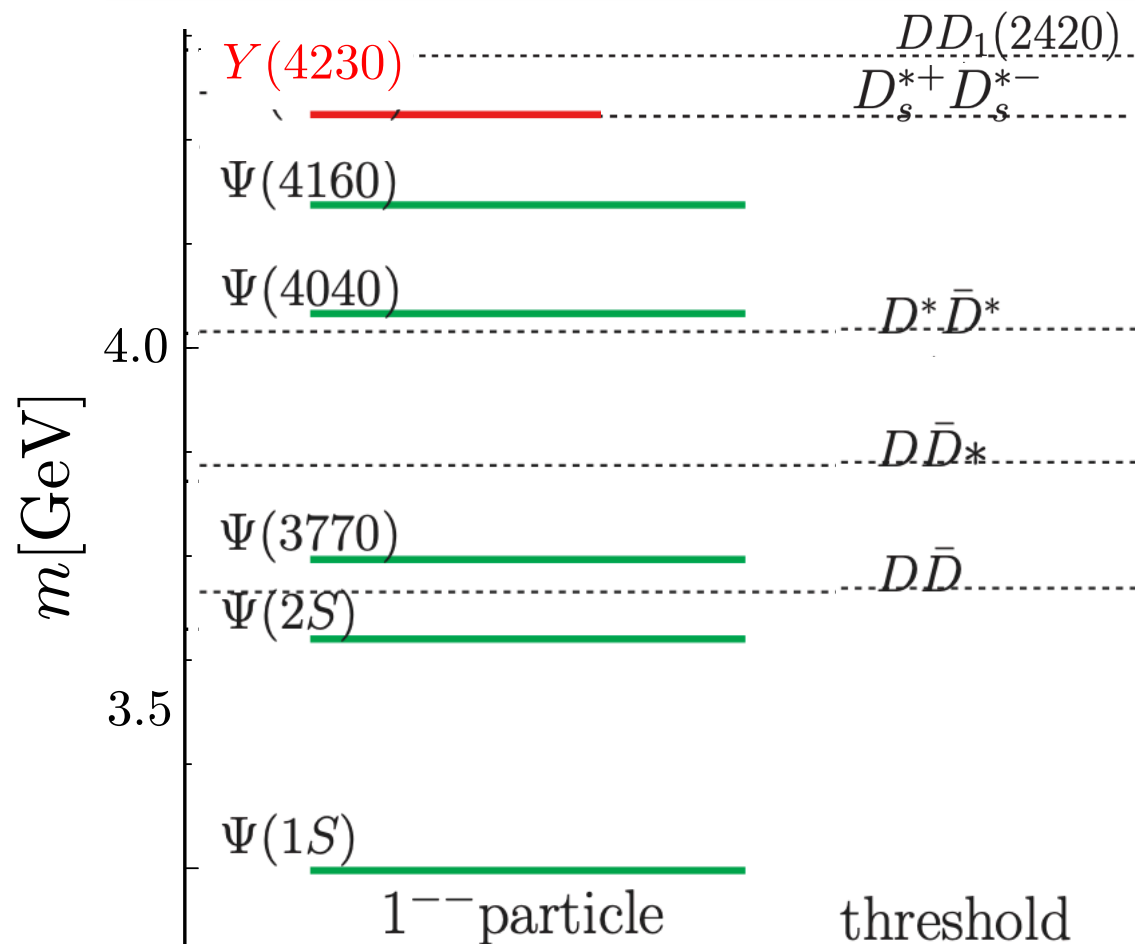
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Notable Decays

- Seen $\mathcal{B}(\pi^+\pi^-J/\psi)$ $\mathcal{B}(\pi^+\pi^-h_c)$ $\mathcal{B}(\pi^+D^{*-}D^0)$ $\mathcal{B}(\gamma X(3872))$
- Not Seen: Any Open-Charm Decays, e.g, $\mathcal{B}(D\bar{D})$

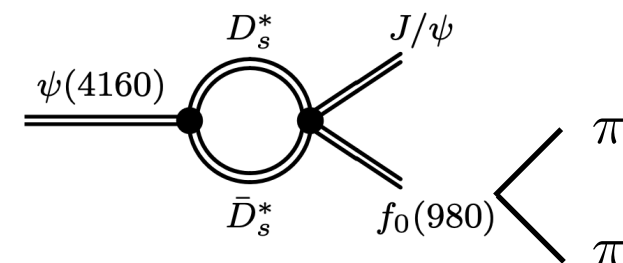
- $M_{PDG} = 4220 \pm 15 \text{ MeV}$

- $\Gamma_{PDG} = 20 - 100 \text{ MeV}$



Scenario 3: $Y(4230) = \psi(4160)$ ([arxiv:1902.09268](https://arxiv.org/abs/1902.09268))

- $Y(4230)$ is not a new state at all!
 - $\psi(4160)$ is strongly coupled to
 - $D_s^*\bar{D}_s^*$ threshold (+30 MeV above)



$\psi(4230)$ aka $Y(4230)$ aka $Y(4260)$

Quantum Numbers

$$J^{PC} = 1^{--}$$

$$Q = 0$$

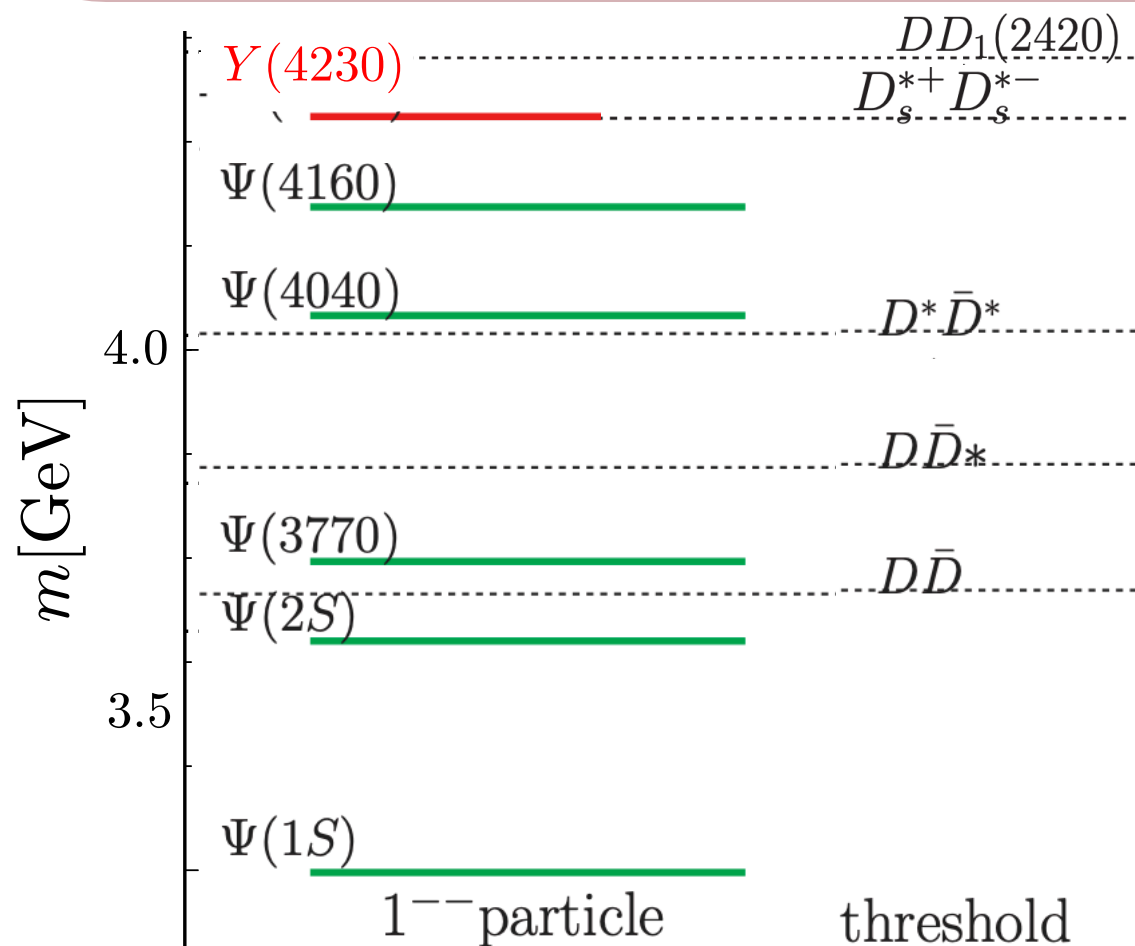
$$I^G = 0^-$$

Notable Decays

- Seen $\mathcal{B}(\pi^+\pi^-J/\psi)$ $\mathcal{B}(\pi^+\pi^-h_c)$ $\mathcal{B}(\pi^+D^{*-}D^0)$ $\mathcal{B}(\gamma X(3872))$
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- $Y(4230)$ is not a new state at all!
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 - $D_s^*\bar{D}_s^*$ threshold (+30 MeV above)
 - Causing $Y(4230)$ structure in data, but only one pole from $\psi(4160)$

