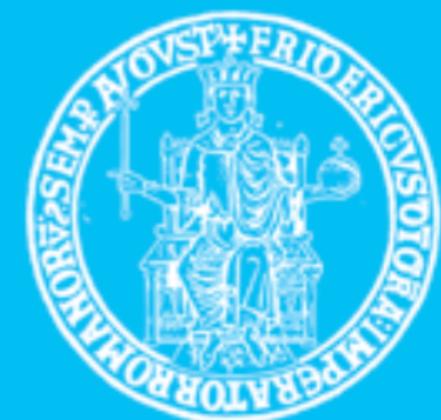


FRANCESCO SANNINO

# SOLVING (Q)FT: FROM WEAK GRAVITY CONJECTURE TO PANDEMICS



# Solving QFT

# Collaborators



... the privilege to work with amazing people

**Asymptotic safety guaranteed**

D. Litim and F. Sannino, JHEP 12 (2014) 178

**A safe CFT at large charge**

D. Orlando, S. Reffert and F. Sannino, JHEP08 (2019)

**Near-Conformal Dynamics at Large Charge**

D. Orlando, S. Reffert and F. Sannino, *Phys.Rev.D* 101 (2020) 6, 065018

**Charting the O(N) model**

Antipin, Bersini, Sannino, Wang, Zhang *Phys.Rev.D* 102 (2020) 4, 045011

**Charging the Conformal Window**

D. Orlando, S. Reffert and F. Sannino, *Phys.Rev.D* 103 (2021) 10, 105026

**Charging the non-Abelian Higgs theories**

Antipin, Bersini, Sannino, Wang, Zhang Phys.Rev.D 102 (2020) 12, 125033

**Charting the O(N) model**

Antipin, Bersini, Sannino, Wang, Zhang Phys.Rev.D 102 (2020) 4, 045011

**Untangling scaling dimensions of fixed charge operators in Higgs theories**

Antipin, Bersini, Sannino, Wang, Zhang Phys.Rev.D 103 (2021) 12, 125024

**More on the cubic versus quartic interaction equivalence in the O(N) model**

Antipin, Bersini, Sannino, Wang, Zhang submitted to Phys.Rev.D

**Asymptotically free and safe fate of symmetry nonrestoration**

Bajc, Lugo, Sannino, Phys.Rev.D 103 (2021) 096014

# Standard model

$$\mathcal{L} = -\frac{1}{4} G_{\mu\nu} G^{\mu\nu} + i \bar{\psi} D^\mu \psi + \partial_\mu H \partial^\mu H^* \\ + \gamma \bar{\psi} H \psi + \lambda (H^+ H)^2 + m_H^2 H^+ H + \Lambda^4$$

# Standard model

well tested

$$\mathcal{L} = -\frac{1}{4} G_{\mu\nu} G^{\mu\nu} + i \bar{\psi} \not{D} \psi + \partial_\mu H \partial^\mu H^* + i \theta g \gamma_5$$
$$+ \lambda \underbrace{\bar{\psi} H \psi}_{\text{}} + \lambda (H^+ H)^2 + \mu_H^2 H^+ H + \Lambda^4$$

$\gamma$  = flavor physics LHC(b), Bell,  $g^{-2}$ , ...

$\lambda$  = future colliders

Accidental Symmetries

# Standard model

$$\mathcal{L} = -\frac{1}{4} G_{\mu\nu} G^{\mu\nu} + i \bar{\psi} \not{D} \psi + \partial_\mu H \partial^\mu H^* + i \theta g \gamma_5$$
$$+ \gamma \bar{\psi} H \psi + \lambda (H^+ H)^2 + \mu_H^2 H^+ H + \Lambda^4$$

$$\mu_H^2 H^+ H$$
$$\Lambda^4$$

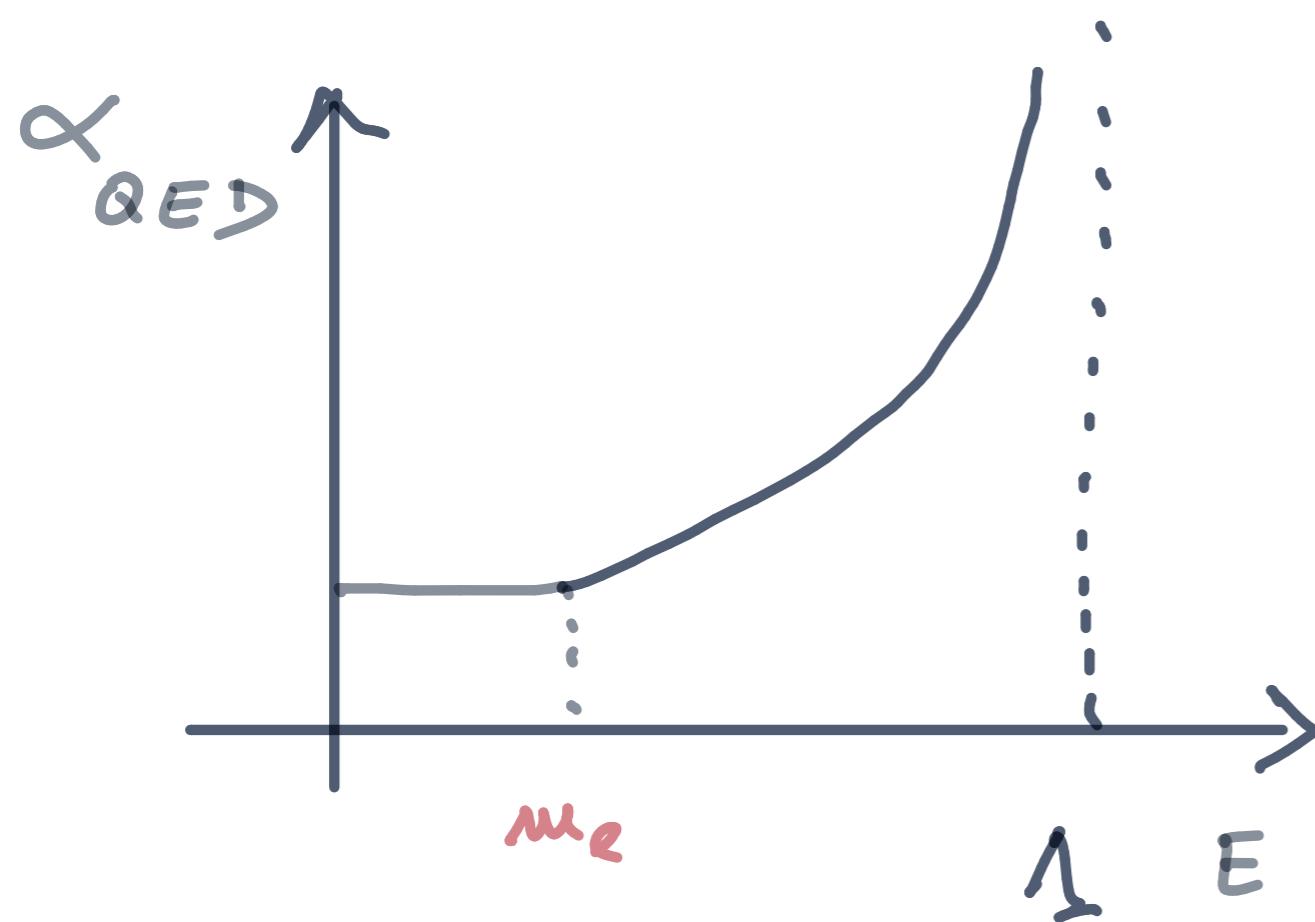
Super renormalizable operators

Technical unnaturality  
Cosmological constant problem

well tested

# Example of Effective theory

\* QED

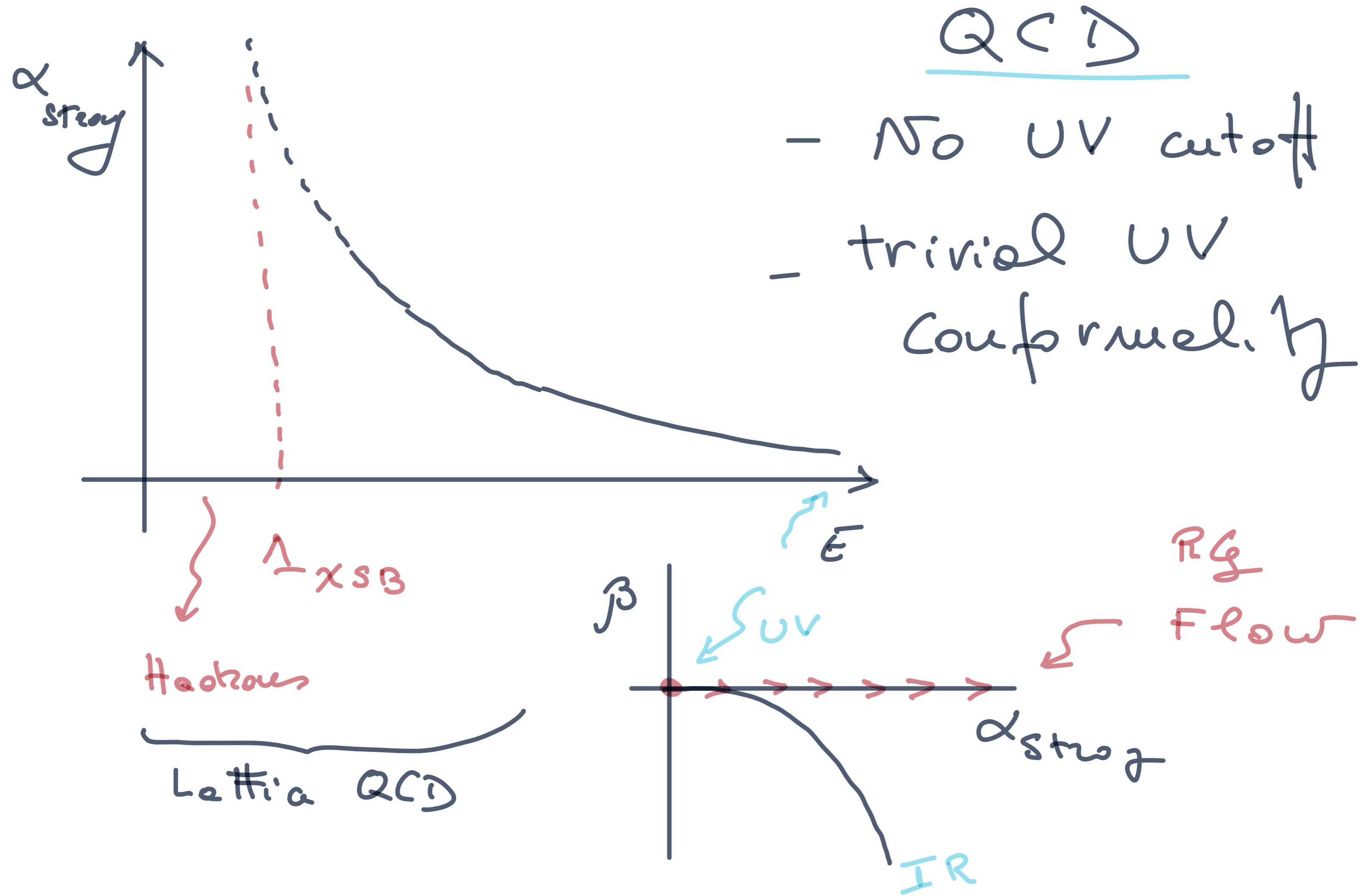


$$\Lambda \rightarrow \infty \Rightarrow \alpha_{QED} \Rightarrow 0$$

Proven at all orders  
in PT at leading  
order in  $\frac{1}{N_f}$

1709.02354

# Example of fundamental theory



# Complete Asymptotic Freedom

All marginal couplings vanish in the UV

CAF conditions obtained at 1-loop

Gauge coupling drives CAF

IR conformal or dyn. scale generated

$$\mu \frac{d\alpha_H}{d\mu} = \alpha_H [c_2 \alpha_H + c_1 \alpha_g]$$

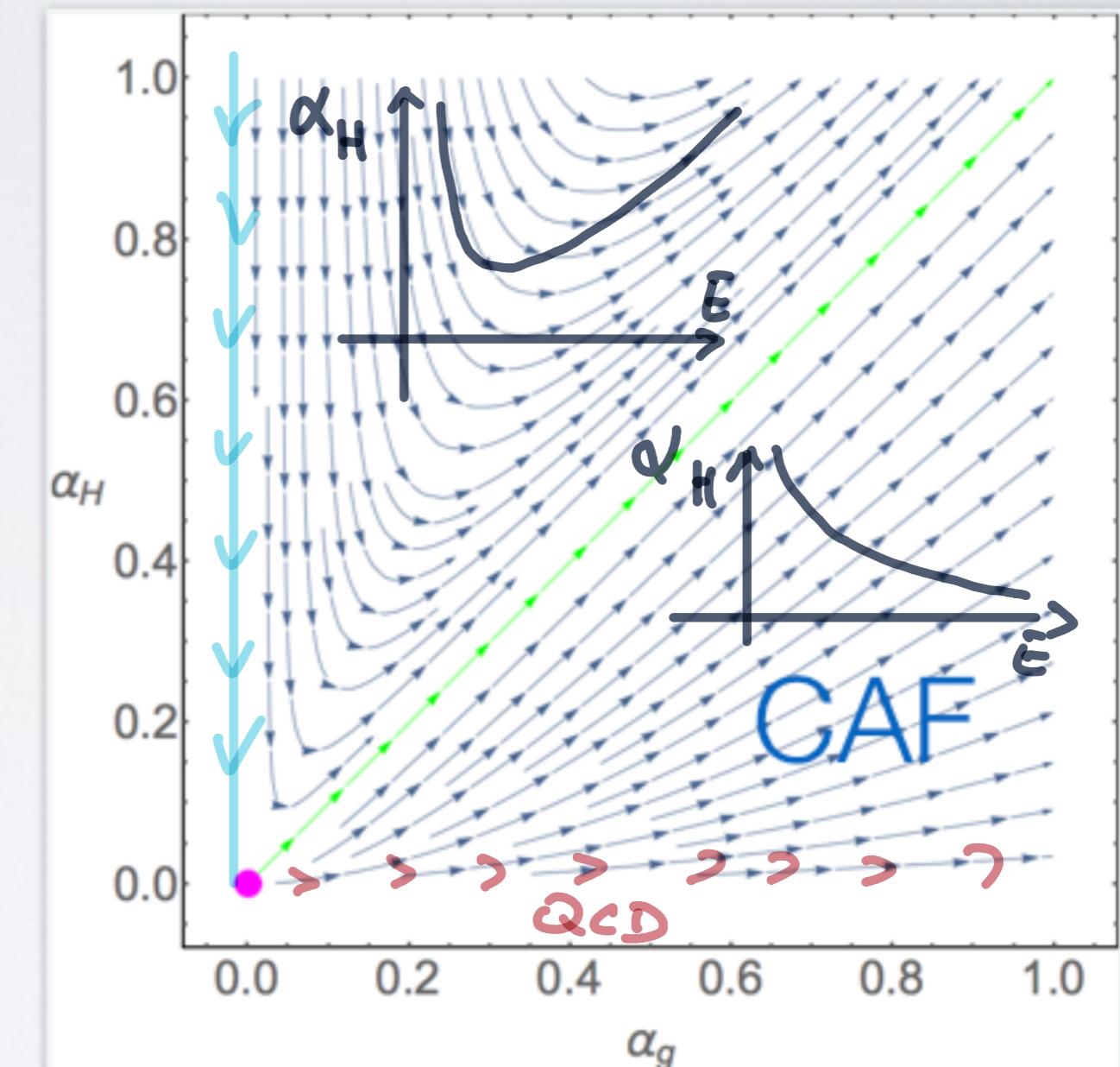
$$c_1 < 0 \quad c_2 > 0$$

Cheng, Eichten, Li, PRD 9, 2259 (1974)

Callaway, Phys. Rept. 167, 241

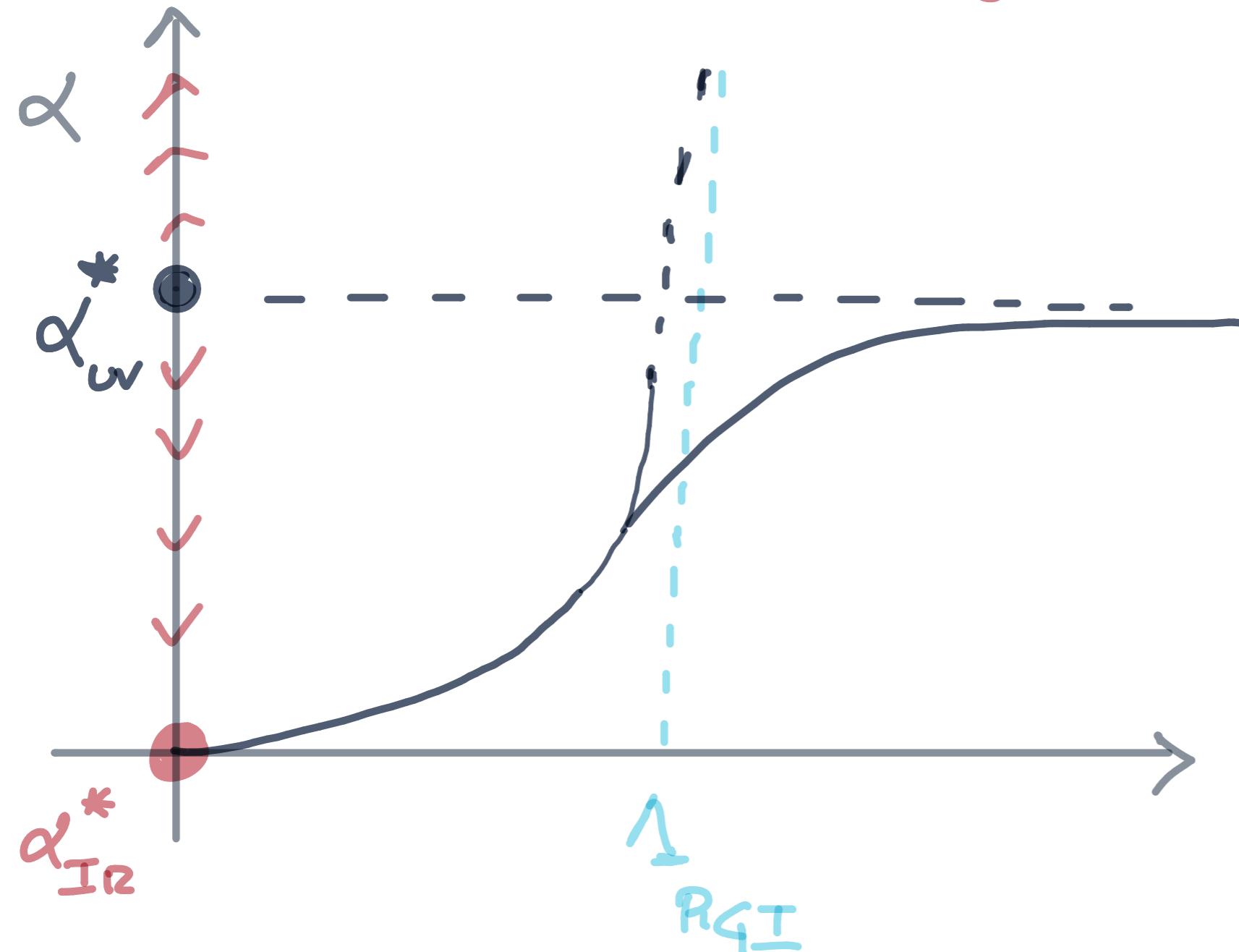
Holdom, Ren, Zhang, 1412.5540

Giudice, Isidori, Salvio, Strumia, 1412.2769

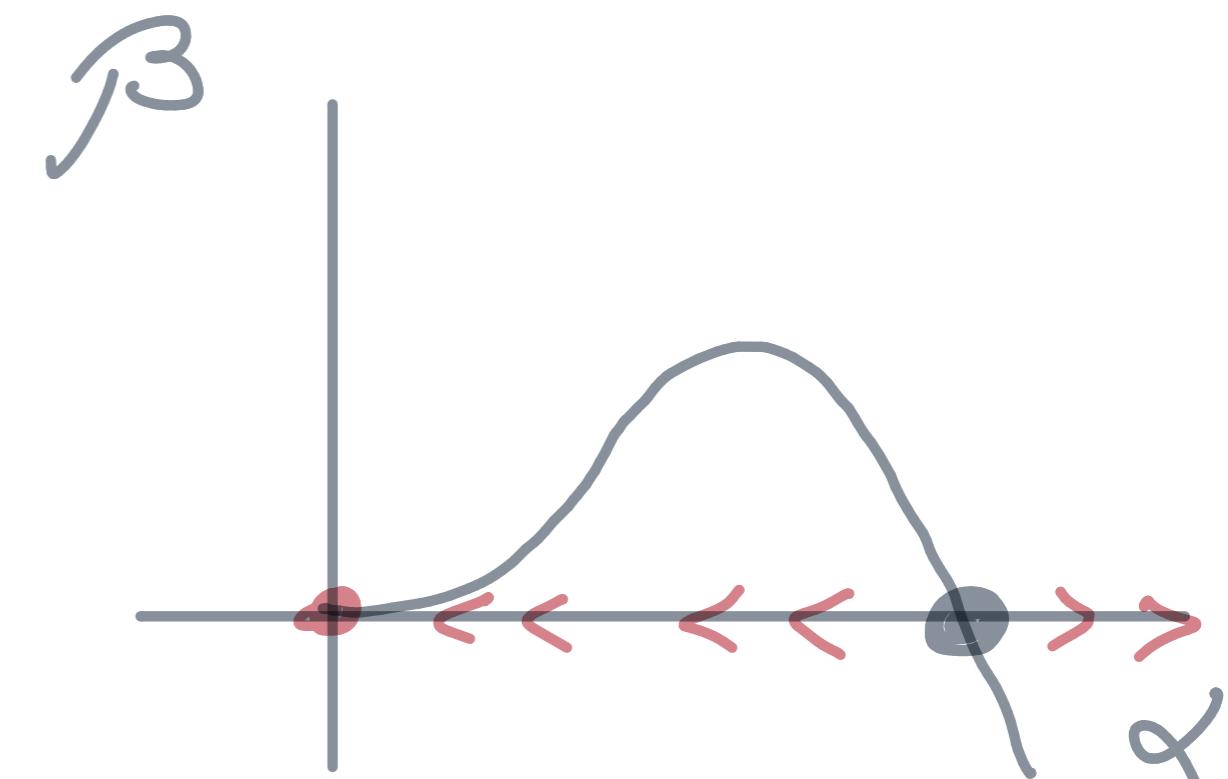


Pica, Ryttov, Sannino, 1605.04712 +  
higher orders for IR conformality

Can we save a theory  
w. HouT freedom?



1 RGI



1<sup>st</sup> rigorous example  
1406.2337

Asymptotic safety is the freedom  
of the ego.

# Exact 4D Interacting UV Fixed Point

Litim and Sannino, 1406.2337, JHEP

$$L = -F^2 + i\bar{Q}\gamma \cdot DQ + y(\bar{Q}_L H Q_R + \text{h.c.}) +$$

$$\text{Tr} [\partial H^\dagger \partial H] - u \text{Tr} [(H^\dagger H)^2] - v \text{Tr} [(H^\dagger H)]^2$$

Fields	$SU(N_c)$	$SU_L(N_f)$	$SU_R(N_f)$	$U_V(1)$
$G_\mu$	Adj	1	1	0
$Q_L$	$\square$	$\bar{\square}$	1	1
$Q_R^c$	$\bar{\square}$	1	$\square$	-1
$H$	1	$\square$	$\bar{\square}$	0

# Veneziano Limit

Litim and Sannino, 1406.2337, JHEP

Litim, Mojaza, Sannino, 1501.03061, JHEP

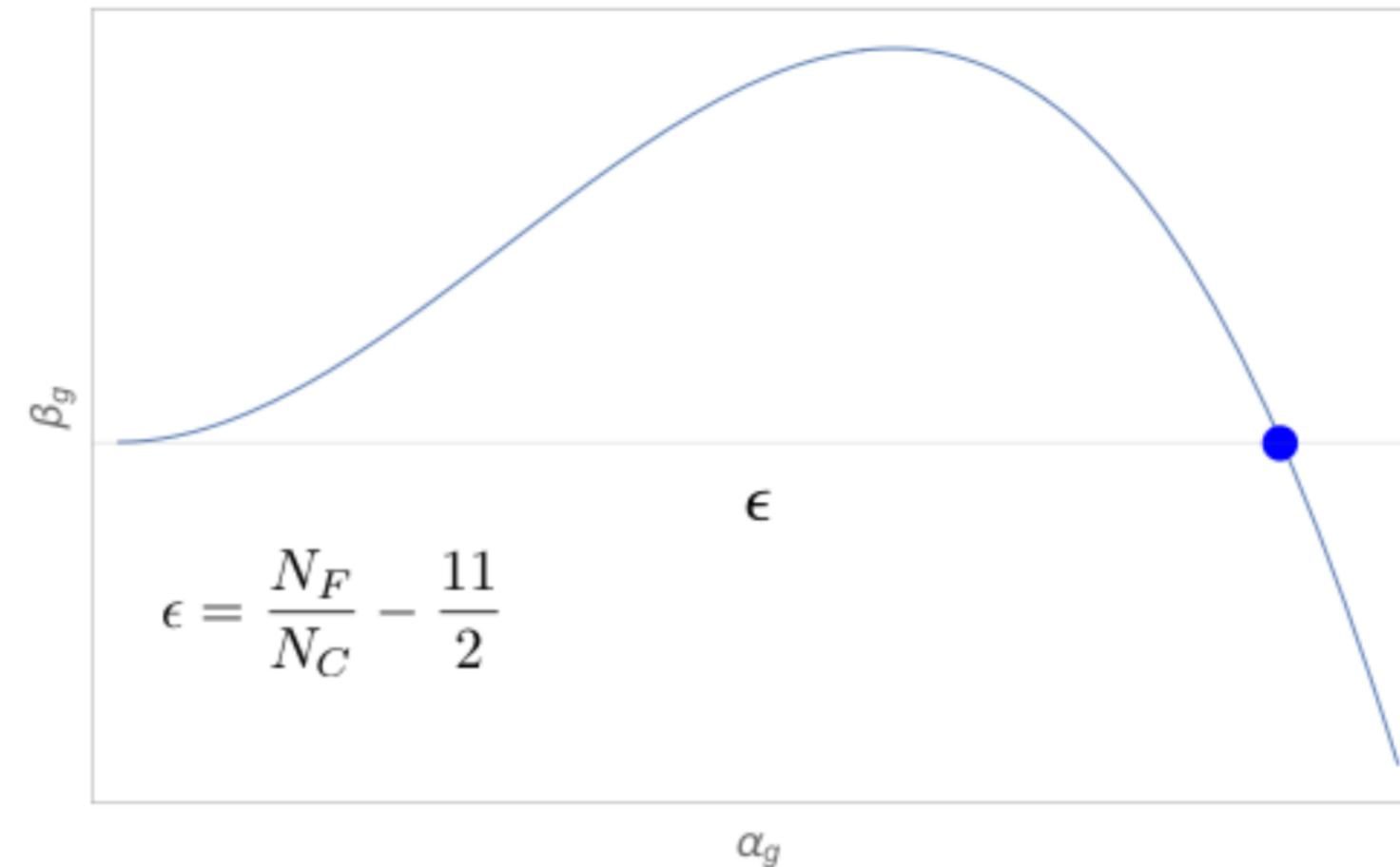
- ◆ Normalised couplings

$$\alpha_g = \frac{g^2 N_C}{(4\pi)^2}, \quad \alpha_y = \frac{y^2 N_C}{(4\pi)^2}, \quad \alpha_h = \frac{u N_F}{(4\pi)^2}, \quad \alpha_v = \frac{v N_F^2}{(4\pi)^2}$$

$$\frac{v}{u} = \frac{\alpha_v}{\alpha_h N_F}$$

At large  $N$

$$\frac{N_F}{N_C} \in \Re^+$$



Impossible in Gauge Theories with Fermions alone

Caswell, PRL 1974

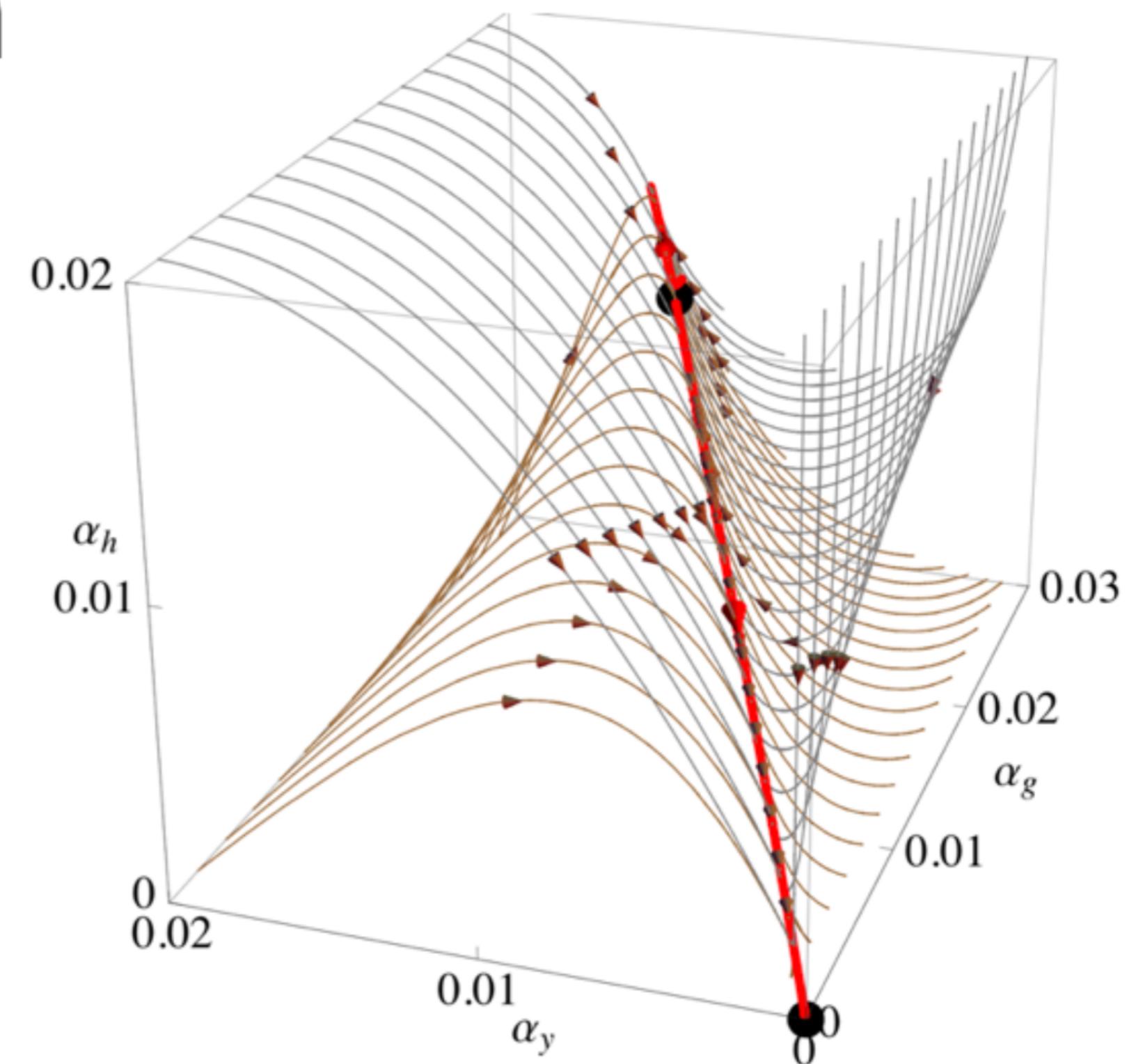
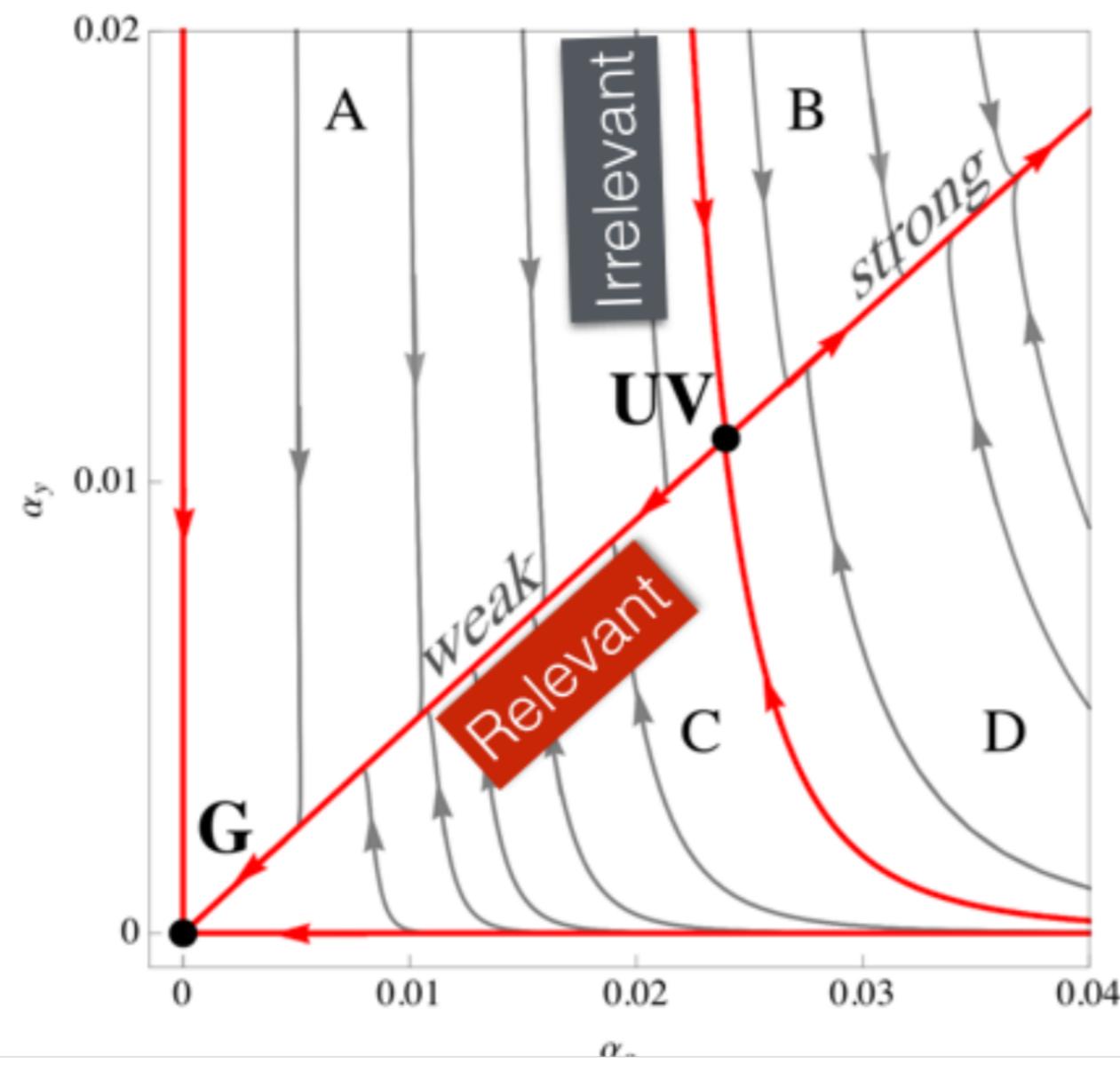
# Phase Diagram

$$\vartheta_1 = -0.608 \epsilon^2 + \mathcal{O}(\epsilon^3)$$

$$\vartheta_2 = 2.737 \epsilon + \mathcal{O}(\epsilon^2)$$

$$\vartheta_3 = 4.039 \epsilon + \mathcal{O}(\epsilon^2)$$

$$\vartheta_4 = 2.941 \epsilon + \mathcal{O}(\epsilon^2).$$

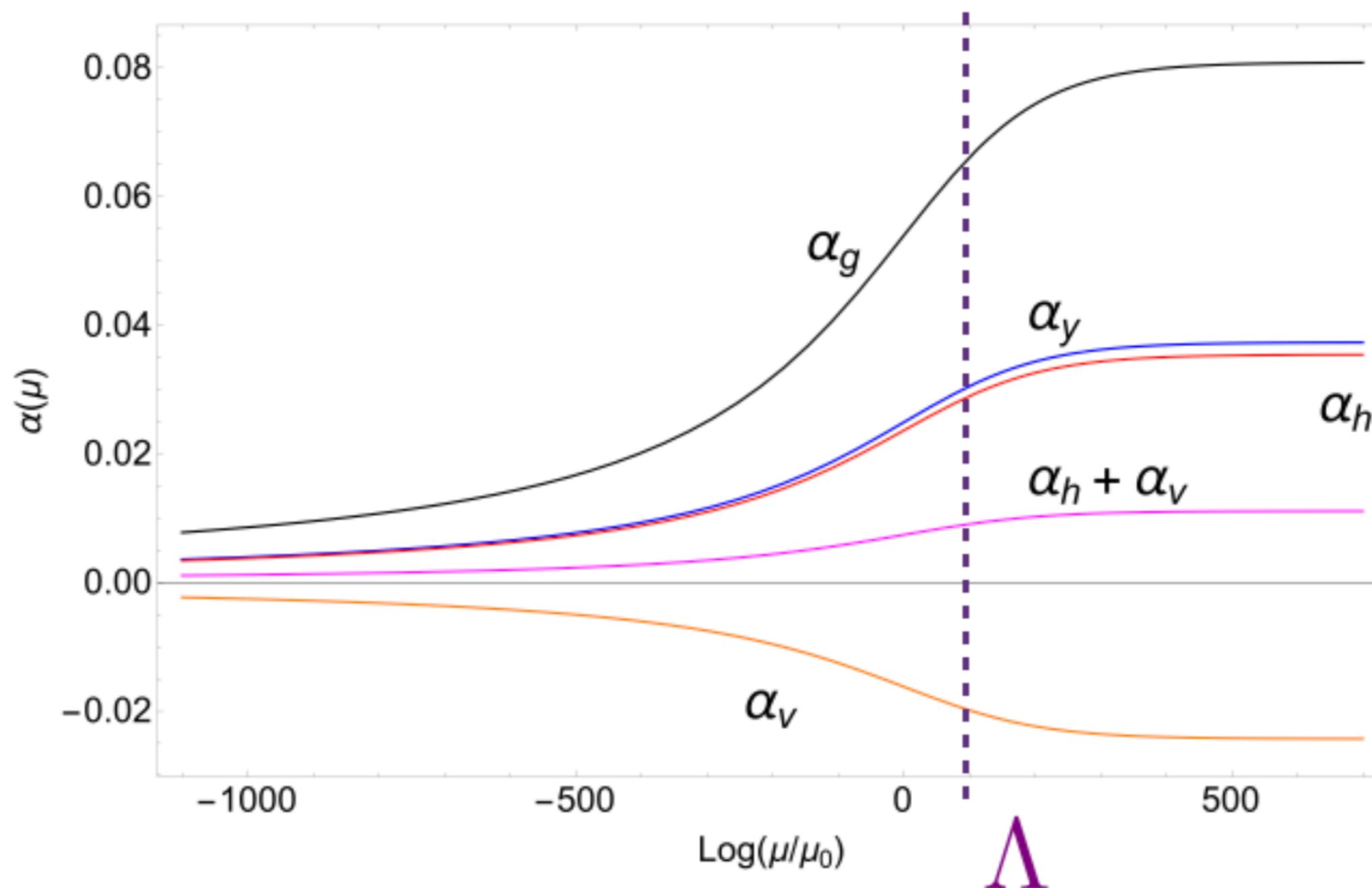


$$\vartheta_1 < 0 < \vartheta_2 < \vartheta_4 < \vartheta_3$$

# Complete asymptotic safety

Litim and Sannino, 1406.2337, JHEP

Gauge + fermion + scalars theories can be fund. at any energy scale



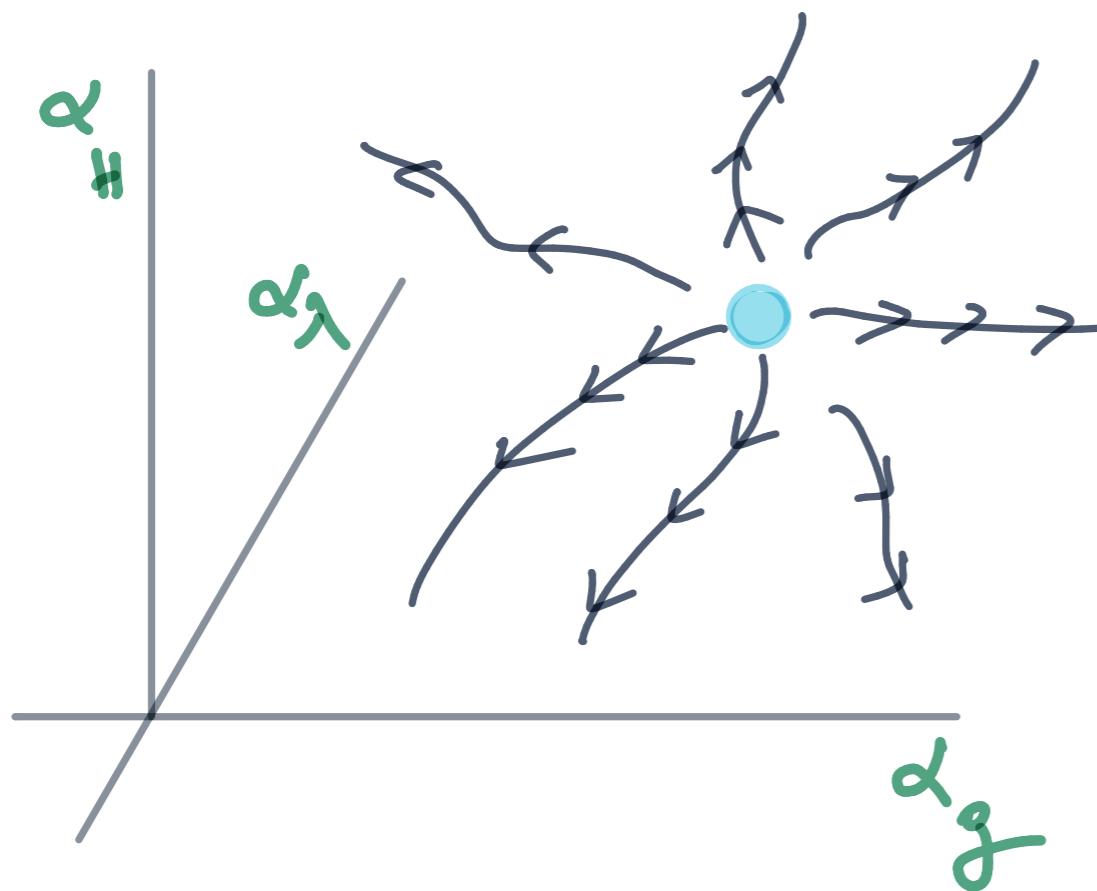
Scalars are needed perturbatively to make the theory fundamental

Fundamental theories as  $CFT_4$

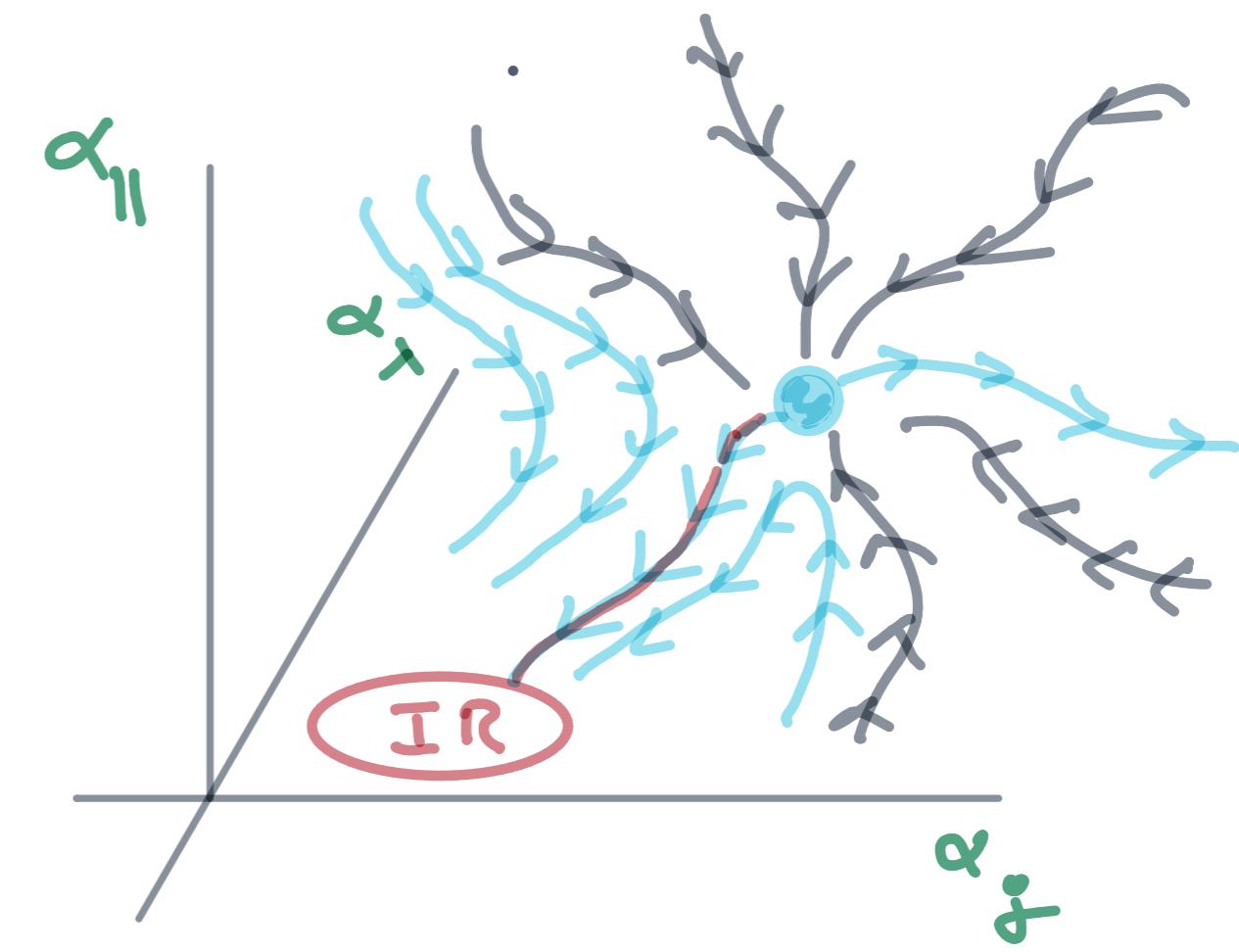
or

$CFT_4$  as lamposts

IR unprecede



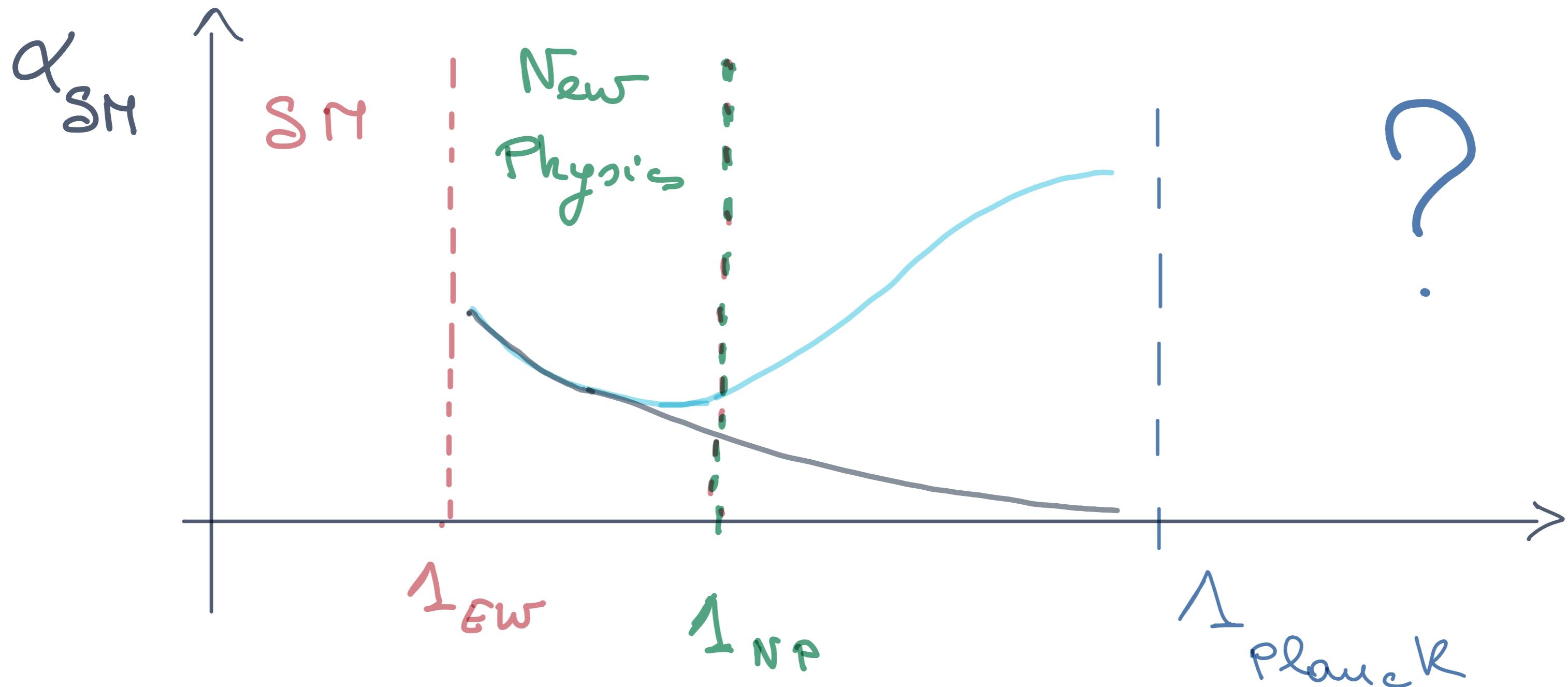
IR predition



# QFT<sub>8</sub>

Fundamental  
CFT in UV

# Quantum Grav.?



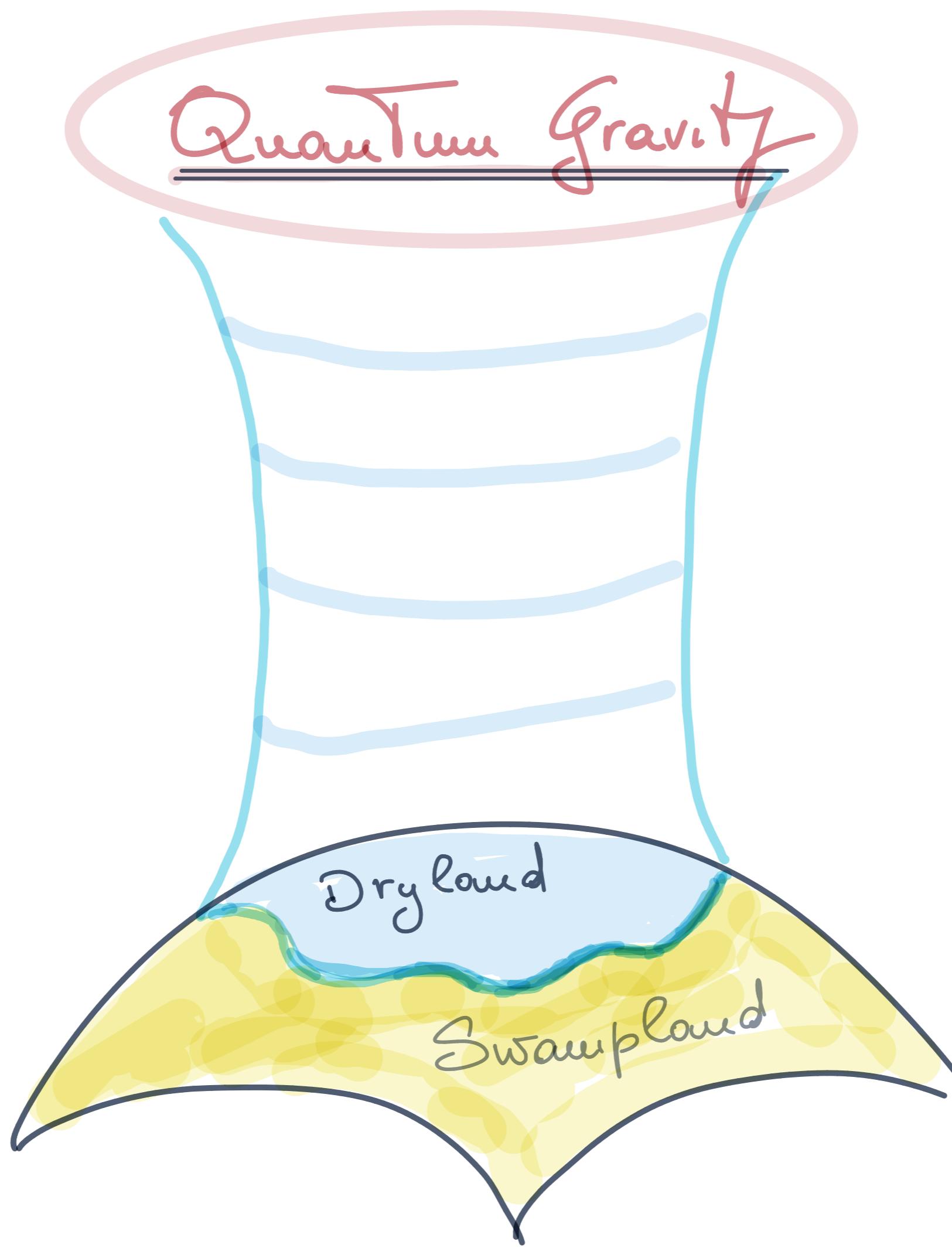
- If  $R^2$  gravity no effect on QFT
- Follow Swampland program [Palti's review]

# Swamp land

Claudia  
Prommegger

Energy

Quantum Gravity



Distance  
Palti's  
Review

# Conjectures

- No global symmetries
- Completeness conjecture  
[Theories featuring a gauge symmetry coupled to quantum gravity must exhibit states of all charges]
- Distance conjecture

$$m(B) \sim m(A) e^{-\alpha \delta(A, B)}$$

- Species scale conjecture

$$\Lambda < \Lambda_s = \frac{M_p}{N^{1/d-2}}$$

$M_p$  = d-dim Planck  
scale

$N$  particle states  
below a give  
cutoff  $\Lambda_s$

- Weak gravity conjecture

gravity is the weakest force

$$g^2 g^2 \gg \frac{m^2}{M_p^2} \Rightarrow m \leq g g M_p$$

# On Convexity of Charged Operators in CFTs and the Weak Gravity Conjecture

Ofer Aharony<sup>1</sup> and Eran Palti<sup>2</sup>

<sup>1</sup> Department of Particle Physics and Astrophysics, Weizmann Institute of Science,  
Rehovot 7610001, Israel

<sup>2</sup> Department of Physics, Ben-Gurion University of the Negev, Beer-Sheva 84105, Israel

e-mail: [ofar.aharony@weizmann.ac.il](mailto:ofar.aharony@weizmann.ac.il), [palti@bgu.ac.il](mailto:palti@bgu.ac.il)

The Weak Gravity Conjecture is typically stated as a bound on the mass-to-charge ratio of a particle in the theory. Alternatively, it has been proposed that its natural formulation is in terms of the existence of a particle which is self-repulsive under all long-range forces. We propose a closely related, but distinct, formulation, which is that it should correspond to a

Sharp version of the WGC

$$\Delta(q_1 + q_2) \geq \Delta(q_1) + \Delta(q_2)$$

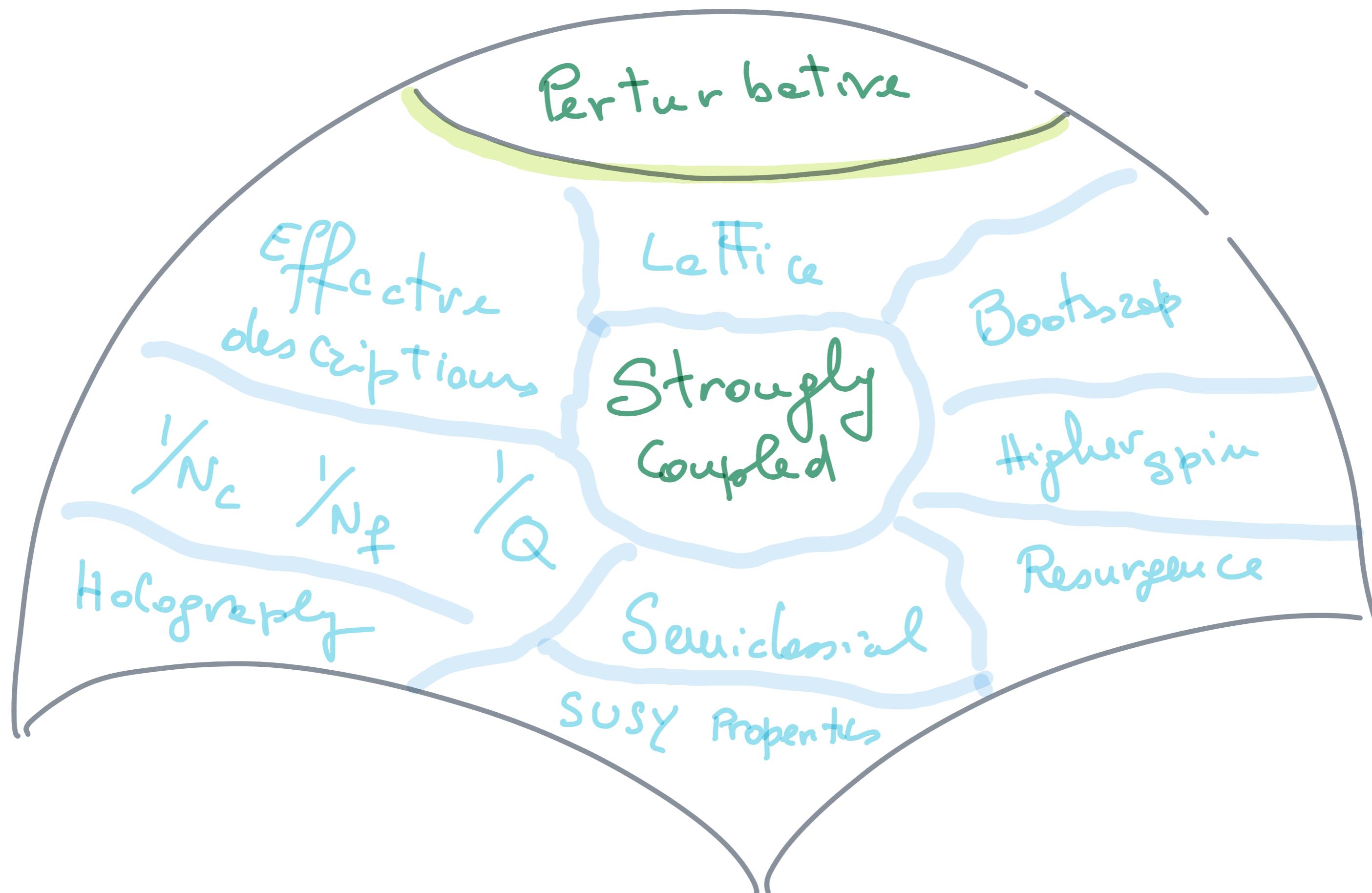
$\Delta(q)$  := Conformal dimension

of operators of charge  $q$

\* Physical interpretation  
Positive binding energy

\* Non-abelian case  $\approx$  Most attractive channel (MAC)  
of the SO'?

# Methodologies



# Methodologies

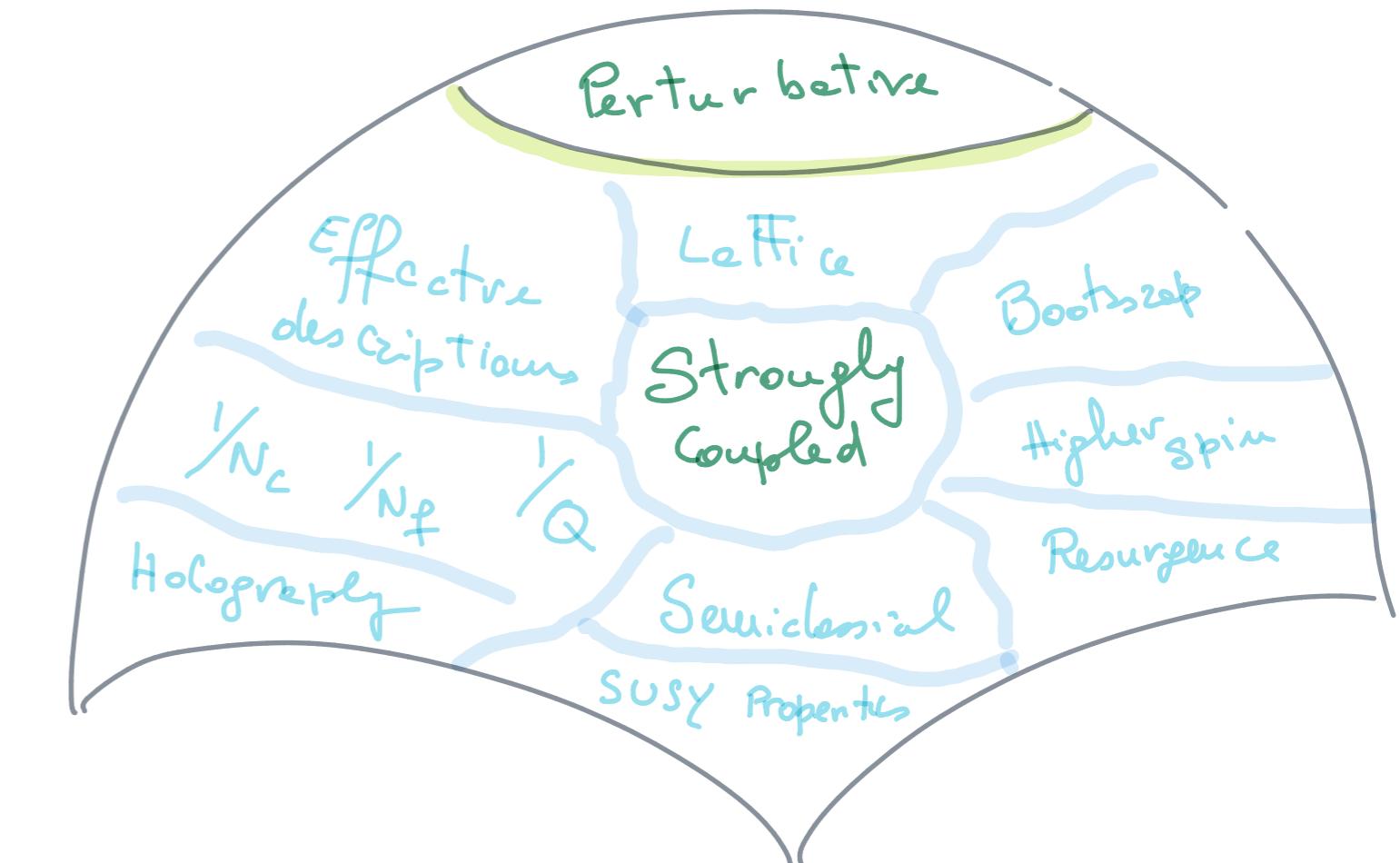
## Perturbation theory

- \* Valid up to order

$$\alpha^{\frac{1}{\alpha}}$$

- \* With multiple couplings must respect Weyl Consistency Conditions (WCC)

- \* Feynman Diagrams  $\rightarrow$  amplitudes



# $O(N)$ model, charged

$\mathcal{O}(N)$  scalar theory in  $d=4-\epsilon$

↓

WF fixed point

$$S = \int d^d x \left[ \frac{(\partial \phi_i)^2}{2} + \frac{(4\pi)^2 g_0}{4!} (\phi_i \phi_i)^2 \right] \quad g^*(\epsilon) = \frac{3\epsilon}{8+N} + \mathcal{O}(\epsilon^2)$$

Fix  $N/2$  charges (rank of  $\mathcal{O}(N)$ ) with  $N$  even

$$\epsilon = 0 \quad N = 4$$

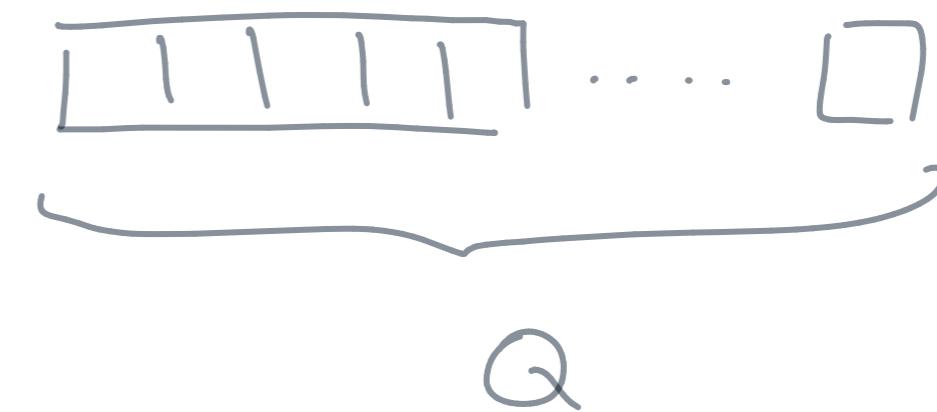
$$\epsilon \rightarrow 1$$

Magnets, Superfluid  $\text{He}^4$ , ...

$8N$  Higgs

# Minimal scaling dimensions

$$Q = \sum_{i=1}^{N/2} Q_i$$



$$Q(\phi_i) = 1$$

$$Q(\phi_i \phi_j - \frac{\delta_{ij}}{N} \phi^2) = 2$$

Anisotropic perturbations

$\Delta \vec{q}$   $\rightarrow$  stability of the system vs  
anisotropic perturbations

# Ground state

homogeneous classical solution

$$\varphi_i = \frac{1}{\sqrt{2}} (\phi_{2i-1} + i\phi_{2i}) = \frac{1}{\sqrt{2}} \sigma_i e^{i\chi_i}$$

$$\sigma_i = A_i$$

$\downarrow$   
VEV

$$\chi_i = -i\mu^\sim$$

$\downarrow$   
chemical potential

$$\vec{Q} = (Q_1, \dots, Q_{N/2}) \rightarrow (Q, 0, \dots, 0)$$

$$\langle Q | e^{-H\tau} | Q \rangle = \frac{1}{Z} \int D^{N/2} r D^{N/2} x e^{-S_{\text{eff}}}$$

$$S_{\text{eff}} = S + \mu Q + \underbrace{\frac{1}{2} \left( \frac{d-2}{2R} \right)^2 \sigma_i \sigma_j}_{\text{Conformal coupling}}$$

$$\Delta_Q = \sum_{\kappa=-1}^8 \frac{1}{Q^\kappa} \Delta_\kappa(\mathcal{A})$$

$$d=gQ$$

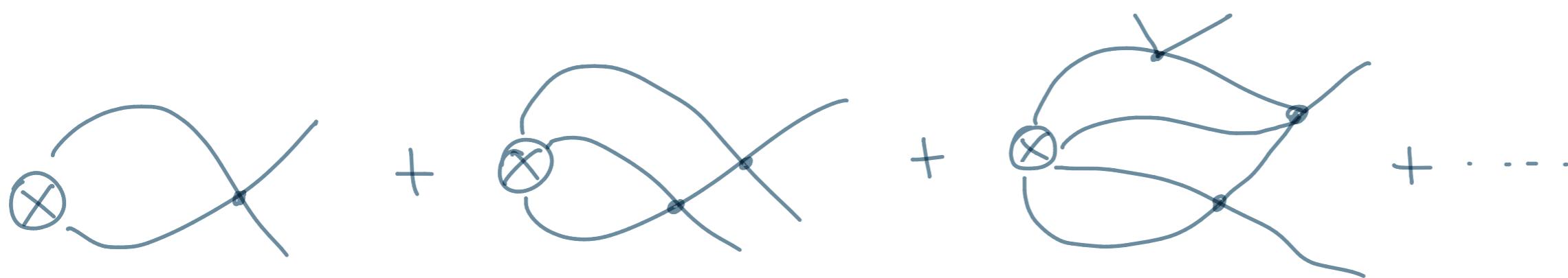
$\Delta_{-1}$

$$S = S(\phi_0) + \frac{1}{2} (\phi - \phi_0)^2 S''(\phi_0) + \dots$$

EOM

$$\frac{4 \Delta_{-1}(A)}{A} = \frac{3^{2/3} x^{1/3}}{3^{1/3} + x^{2/3}} + \frac{3^{1/3} (3^{1/3} + x^{2/3})}{x^{1/3}} ; \quad x = 6A + \sqrt{-3 + 36A^2}$$

Resum an infinite class of diagrams



$\Delta_0$  is trickier

$$S = S(\phi_0) + \frac{1}{2} (\phi - \phi_0)^2 S''(\phi_0) + \dots$$

Determinant fluctuation

$$\Delta_0 = \frac{R}{2} \sum_{\ell=0}^{\infty} n_{\ell} [\omega_+(\ell) + \omega_-(\ell) + \left(\frac{N}{2} - 1\right)(\omega_{++}(\ell) + \omega_{--}(\ell))]$$

$\ell$  labels momentum eigenvalues with degeneracy  $n_{\ell}$

Dispersion Relations	
	Mass
$\omega_+$	$6\mu$
$\omega_-$	$0$
$\omega_{++}$	$2\mu$
$\omega_{--}$	$2\mu$

$c_s = \frac{1}{\sqrt{d-1}}$  (phonon)

non relativistic (magnon)

# Perturbation Theory

$$A = g Q$$

Expand  $\Delta_K$  for  $A \rightarrow 0$

$$\Delta_{-1}$$

$$\Delta_0$$

$$\begin{aligned}
 \Delta_Q = & Q + \left( \frac{Q^2}{8+N} - \frac{(N+10)}{2(8+N)} Q \right) \epsilon \\
 & - \left[ \frac{2}{(8+N)^2} Q^3 + \frac{(N-22)(N+6)}{2(8+N)^3} Q^2 + \frac{184+N(14-3N)}{4(8+N)^3} Q \right] \epsilon^2 \\
 & + \left[ \frac{8}{(8+N)^3} Q^4 + \frac{-456-64N+N^2+2(8+N)(14+N)\zeta(3)}{(8+N)^4} Q^3 \right. \\
 & \left. - \frac{-31136-8272N-276N^2+56N^3+N^4+24(N+6)(N+8)(N+26)\zeta(3)}{4(N+8)^5} Q^2 \right. \\
 & \left. + \frac{-65664-8064N+4912N^2+1116N^3+48N^4-N^5+64(N+8)(178+N(37+N))\zeta(3)}{16(N+8)^5} Q \right] \epsilon^3 \\
 & + [c_5 Q^5 + c_4 Q^4 + c_3 Q^3 + c_2 Q^2 + c_1 Q] \epsilon^4 + [e_6 Q^6 + e_5 Q^5 + e_4 Q^4 + e_3 Q^3 + e_2 Q^2 + e_1 Q] \epsilon^5 +
 \end{aligned}$$

Full 4-loop  $\Theta(\epsilon^4)$  combining with p.v. for  $Q=1, 2, 4$

Infinite # of checks for diagrammatic computations

$$d=4 \quad \epsilon = 0$$

$$\Delta_Q = Q + \frac{1}{3}gQ(Q-1) - \frac{g^2}{18}(4Q^3 + (N-6)Q^2 + \frac{1}{2}(2-3N)Q) + \mathcal{O}(g^3)$$

$$CFT \Rightarrow QFT$$

Anomalous dimensions of Higgs operators

SM Higgs for  $N=4$

Work in progress...

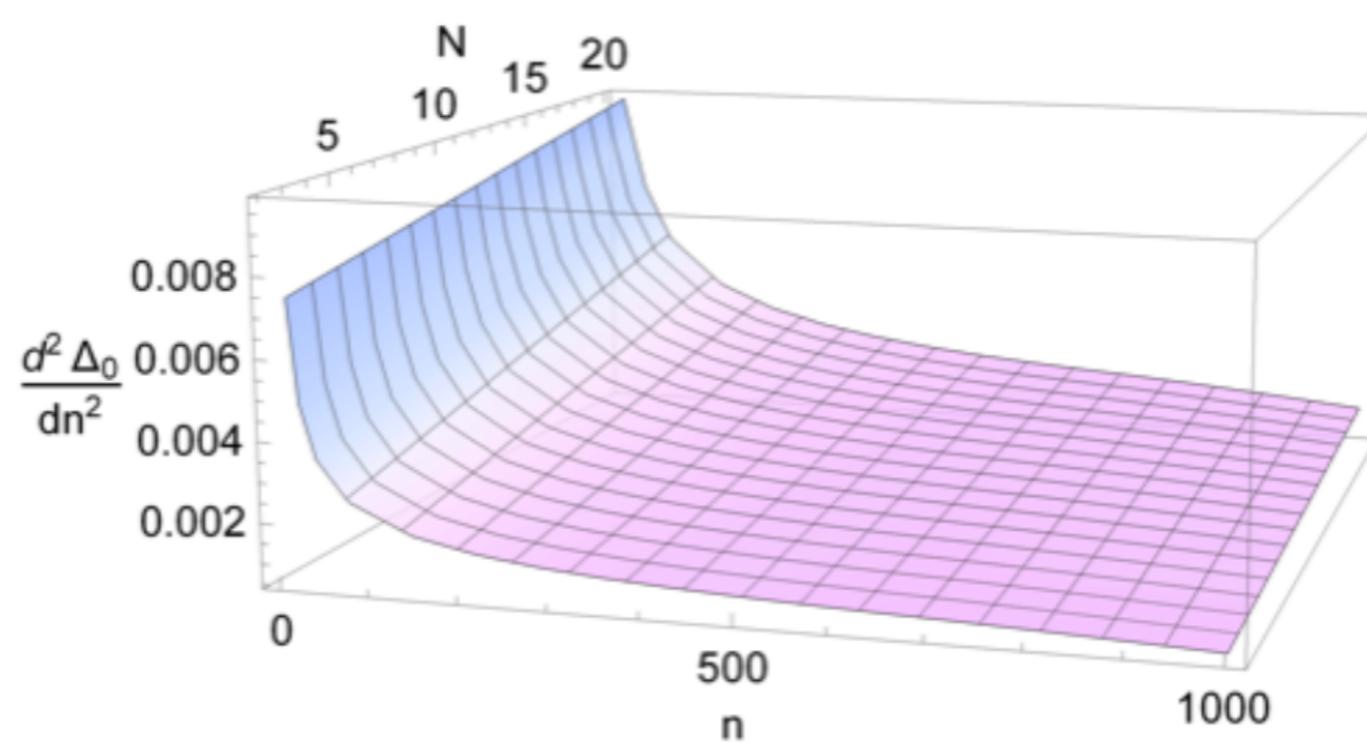
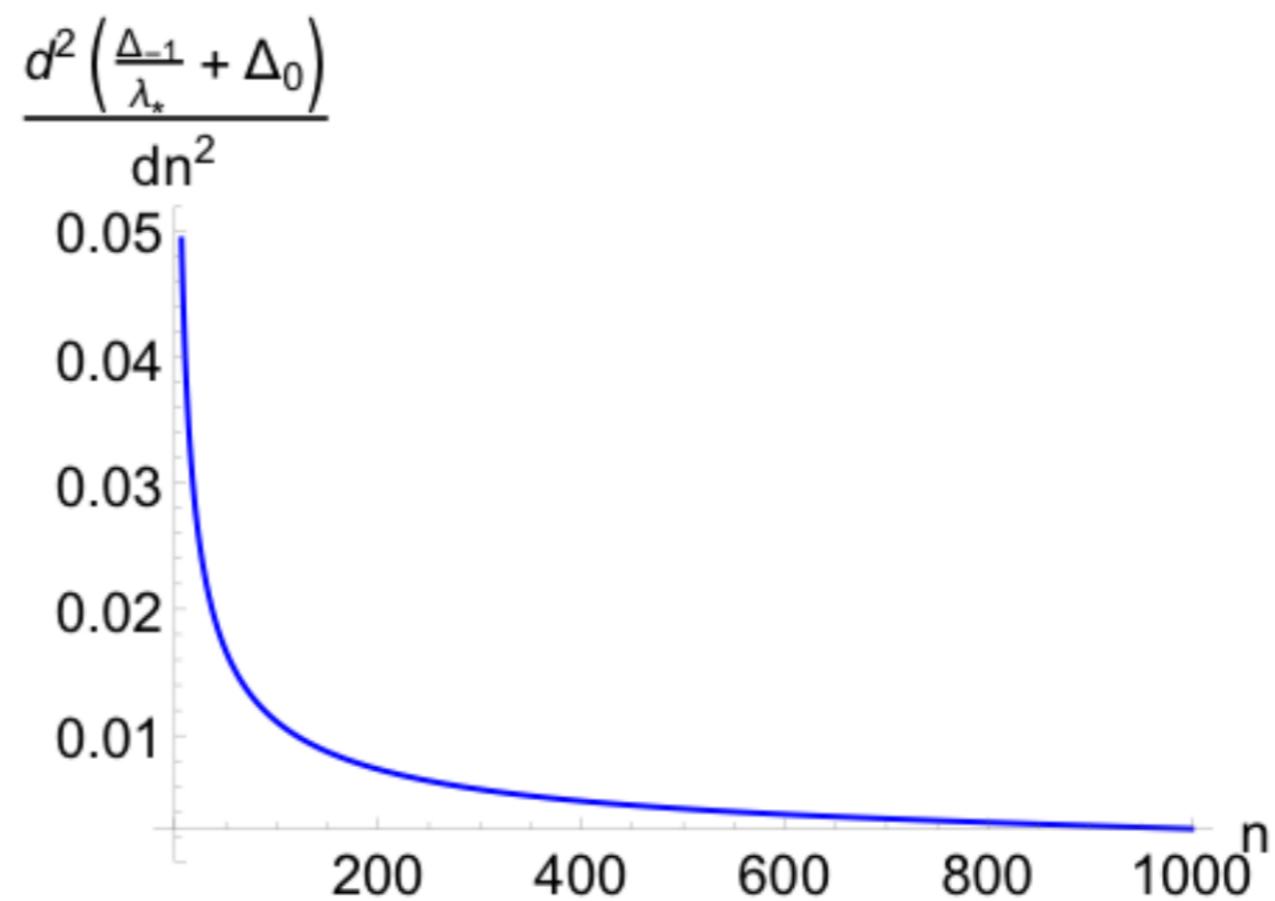
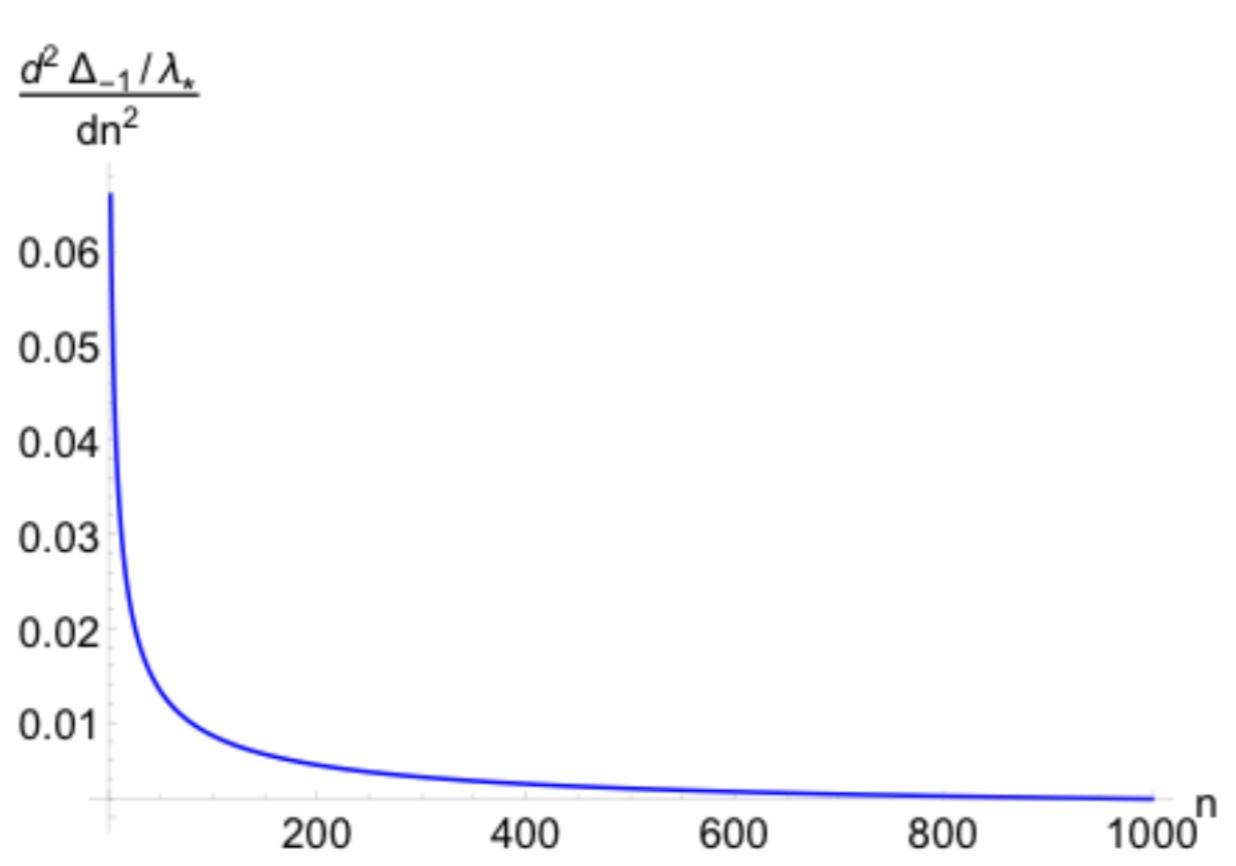
$Q = n$  Aharony and Palti:  $\mathcal{D}(N)$  4- $\epsilon$  test

$$\chi_{n_1, n_2} = \Delta(\varphi^{n_1+n_2}) - \Delta(\varphi^{n_1}) - \Delta(\varphi^{n_2}) > 0 \quad \Theta(\epsilon^3)$$

$$\Delta_\theta = \frac{1}{\lambda_*} \Delta_{-1}(\lambda_* h) + \Delta_0(\lambda_* h) + \dots$$

Each Term is convex

$$\lambda_* = 0.1$$
$$N = 4$$



## What I did not present

- Charged (Complex) CFTs
- $\Theta(N)$  cubic duality (Bersini's talk)
- $U(N) \times U(M)$  [Intriguing for WGC]
- $d=4$  Safety at large charge
- $d=4$  QCD (near) conformal dynamics  
the dilaton story

Reorganising Epidemiology via CFTs

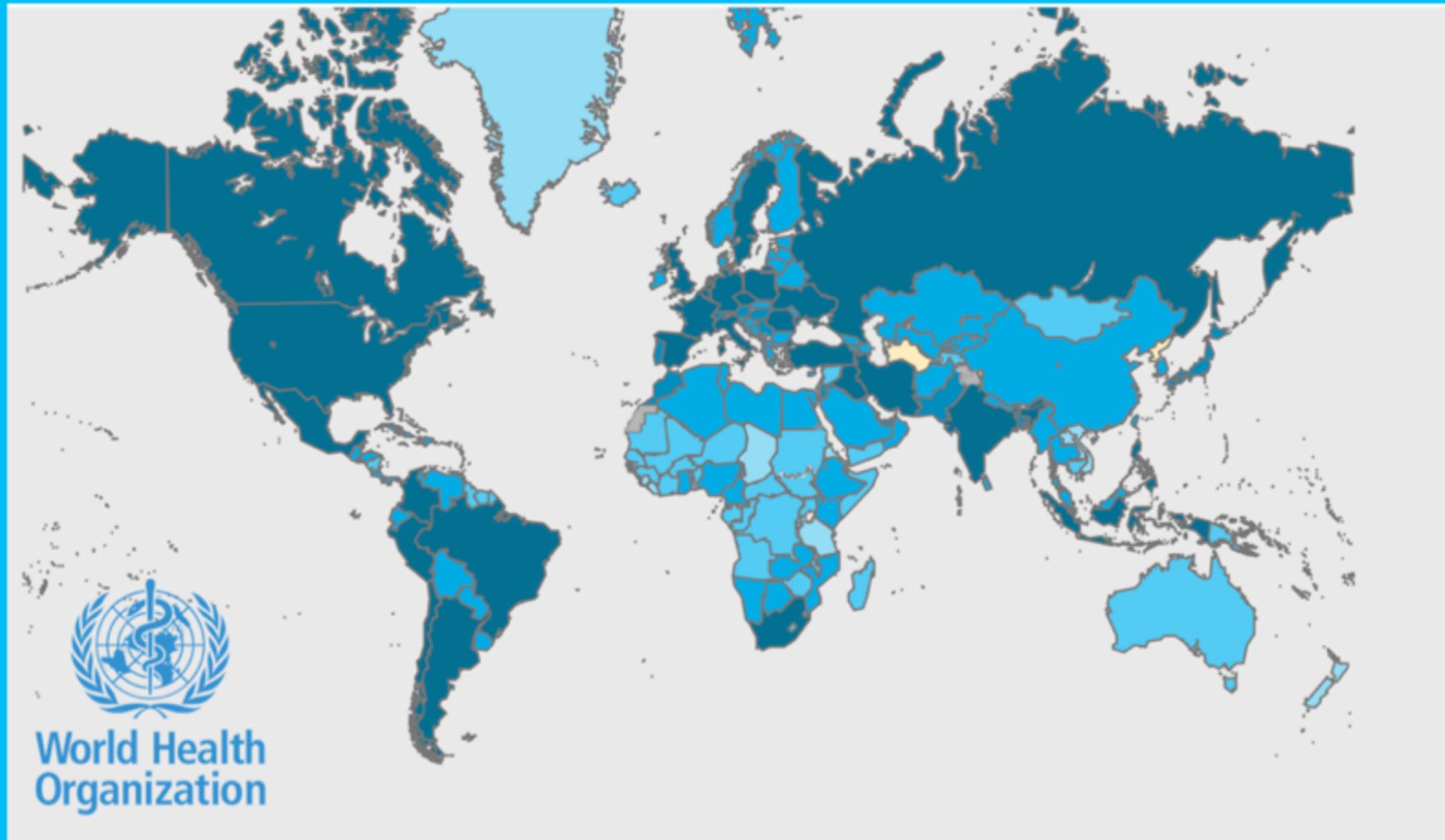
## World wide situation

New cases: 515,104

Deaths: 3,386,825

Confirmed: 163,312,429

Vaccine doses: 1,407,945,776

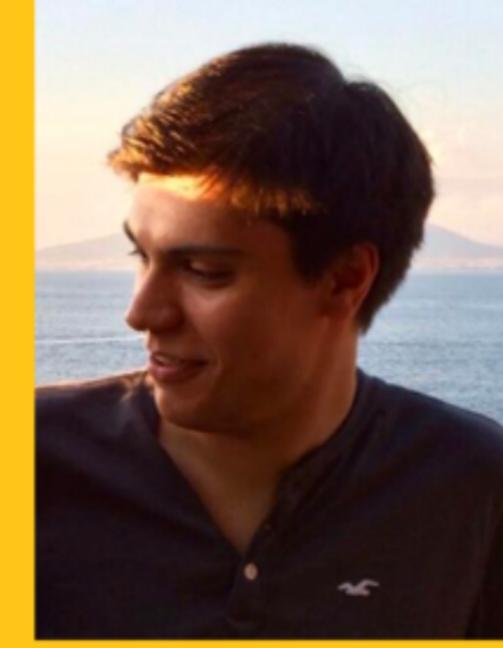


# FROM STRING THEORY TO PANDEMICS



... the privilege to work with amazing people

# FROM HEP-TH AND -EXP TO PANDEMICS & ARTIFICIAL INTELLIGENCE



... the privilege to work with amazing people

# PAPERS



## Renormalisation Group Approach to Pandemics...

M. Della Morte, D. Orlando and F. Sannino, Frontiers of Physics 8, 144 (2020)



## Interplay of social distancing and border restrictions....

G. Cacciapaglia and F. Sannino Sci Rep 10, 15828 (2020)



## RG approach to pandemics as a time-dependent SIR model

M. Della Morte and F. Sannino Frontiers of Physics 8 (2021) 583

# PAPERS



**Second wave COVID-19 pandemics in Europe: A temporal...**  
G. Cacciapaglia, C. Cot and F. Sannino Sci Rep 10, 15514 (2020)



**Multiwave pandemic dynamics explained: How to tame ....**  
G. Cacciapaglia, C. Cot and F. Sannino Sci Rep 11, 6638 (2021)



**Mining Google and Apple mobility data: Temporal anatomy for..**  
G. Cacciapaglia, C. Cot and F. Sannino Sci Rep 11, 4150 (2021)

# PAPERS

nature

SCIENTIFIC  
REPORTS

THE LANCET



## Impact of US vaccination strategy on COVID-19 wave dynamics

C. Cot, G. Cacciapaglia, A.S. Islind, M. Oskarsdottir, F. Sannino Sci Rep to appear

## Calling for pan-European commitment for rapid and sustained reduction in SARS-CoV-2 infections

V. Priesemann, F. Sannino et al. The lancet 397 (10269), 92-93

## Evidence for complex fixed points in pandemic data

G. Cacciapaglia and F. Sannino article/rs-70238/v1 (accepted)



## Invited review

### The field theoretical ABC of epidemic dynamics

**Giacomo Cacciapaglia<sup>1,2</sup>, Corentin Cot<sup>1,2</sup>, Michele Della Morte<sup>3</sup>, Stefan Hohenegger<sup>1,2</sup>, Francesco Sannino<sup>4,5</sup>, Shahram Vatani<sup>1,2</sup>**

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<sup>3</sup> IMADA & CP<sup>3</sup>-Origins. Univ. of Southern Denmark, Campusvej 55, DK-5230 Odense, Denmark

<sup>4</sup> CP<sup>3</sup>-Origins and D-IAS, Univ. of Southern Denmark, Campusvej 55, DK-5230 Odense, Denmark

<sup>5</sup> Dipartimento di Fisica, E. Pancini, Univ. di Napoli, Federico II and INFN sezione di Napoli  
Complesso Universitario di Monte S. Angelo Edificio 6, via Cintia, 80126 Napoli, Italy

# Epidemiological theory of virus variants

Giacomo Cacciapaglia<sup>1,2\*</sup>, Corentin Cot<sup>1,2†</sup>, Adele de Hoffer<sup>3‡</sup>,  
Stefan Hohenegger<sup>1,2§</sup>, Francesco Sannino<sup>4,5,6¶</sup> and Shahram Vatani<sup>1,2||</sup>

June 16, 2021

<sup>1</sup> Institut de Physique des 2 Infinis (IP2I) de Lyon, CNRS/IN2P3, UMR5822,  
69622 Villeurbanne, France

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<sup>3</sup> Politecnico di Torino, Torino, Italy

<sup>4</sup> Scuola Superiore Meridionale, Largo S. Marcellino, 10, 80138 Napoli NA, Italy

<sup>5</sup> Dipartimento di Fisica, E. Pancini, Univ. di Napoli, Federico II and INFN sezione di Napoli,  
Complesso Universitario di Monte S. Angelo Edificio 6, via Cintia, 80126 Napoli, Italy

<sup>6</sup> CP<sup>3</sup>-Origins and D-IAS, Univ. of Southern Denmark, Campusvej 55, DK-5230 Odense,  
Denmark

## Abstract:

We propose a physical theory underlying the temporal evolution of competing virus variants that relies on the existence of (quasi) fixed points capturing the large time scale invariance of the dynamics. To motivate our result we first modify the time-honoured compartmental models of the SIR type to account for the existence of competing variants and then show how their evolution can be naturally re-phrased in terms of flow equations ending at quasi fixed points. As the natural next step we employ (near) scale invariance to organise the time evolution of the competing variants within the effective description of the *epidemic Renormalization Group* framework. We test the resulting theory against the time evolution of COVID-19 virus variants that validate the theory empirically.

arXiv.org > q-bio > arXiv:2106.14982

# PAPERS



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## Variant-driven multi-wave pattern of COVID-19 via Machine Learning clustering of spike protein mutations

Adele de Hoffer, Shahram Vatani, Corentin Cot, Giacomo Cacciapaglia, Francesco Conventi, Antonio Giannini, Stefan Hohenegger, Francesco Sannino

doi: <https://doi.org/10.1101/2021.07.22.21260952>

Submitted

# **“WHEN COULD WE TRAVEL AGAIN?”**

**AT THE END OF JANUARY WE WERE TOLD TO POSTPONE OUR TRIPS**

# RENORMALISATION GROUP



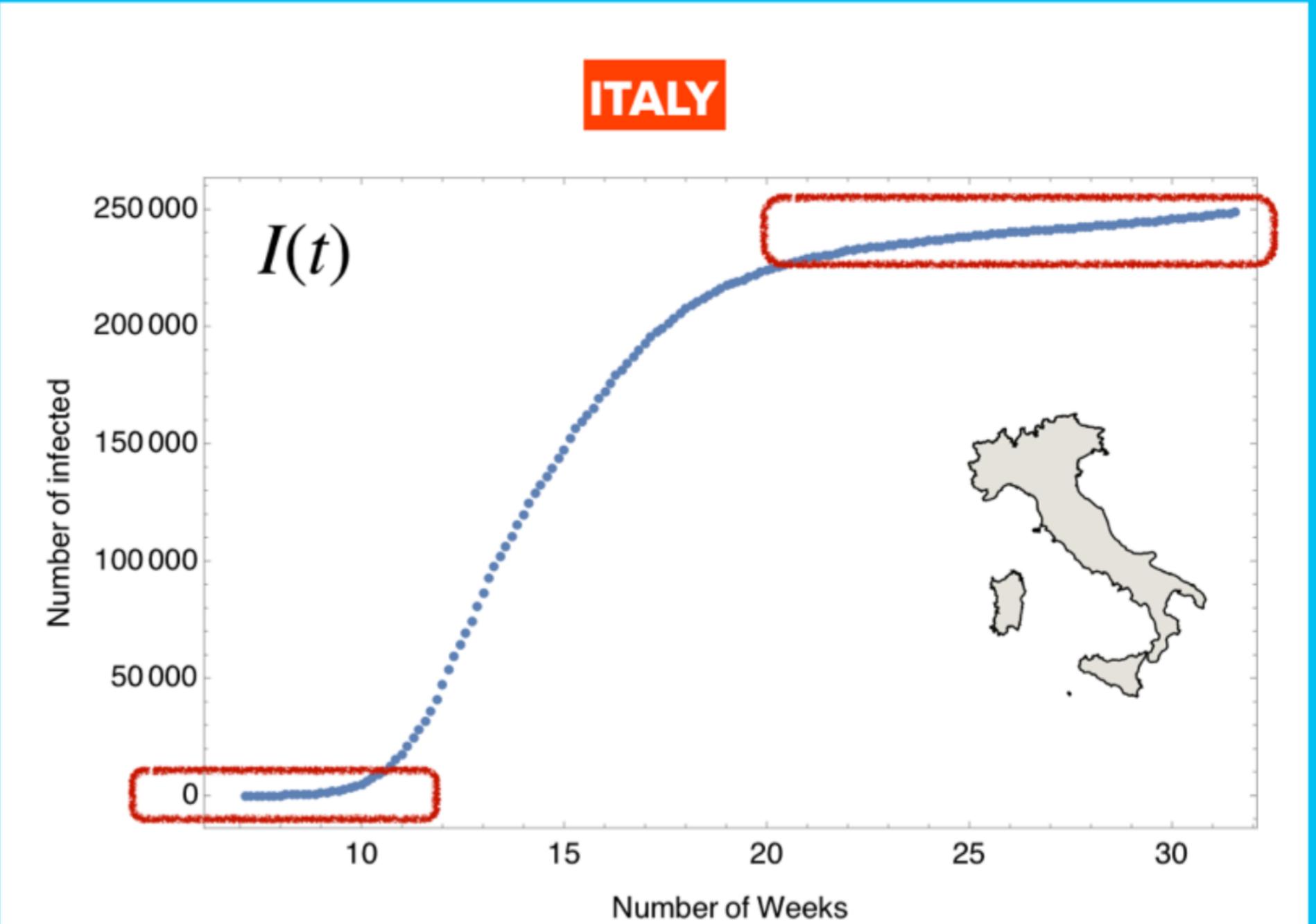
**Renormalisation Group Approach to Pandemics...**  
*M. Della Morte, D. Orlando and F. Sannino, Frontiers of Physics 8, 144*

## EPIDEMIC

# LARGE AND SHORT TIME SCALE INVARIANCE

- Short times = obvious time invariance
- Long time = approx time invariance
- Approx time dilation can be encoded in an effective interaction strength

$$\alpha(t) = \ln I(t)$$



# EPIDEMIC RENORMALISATION GROUP (eRG) IN A NUTSHELL

- The **beta function** encodes the underlying (pandemic) dynamics

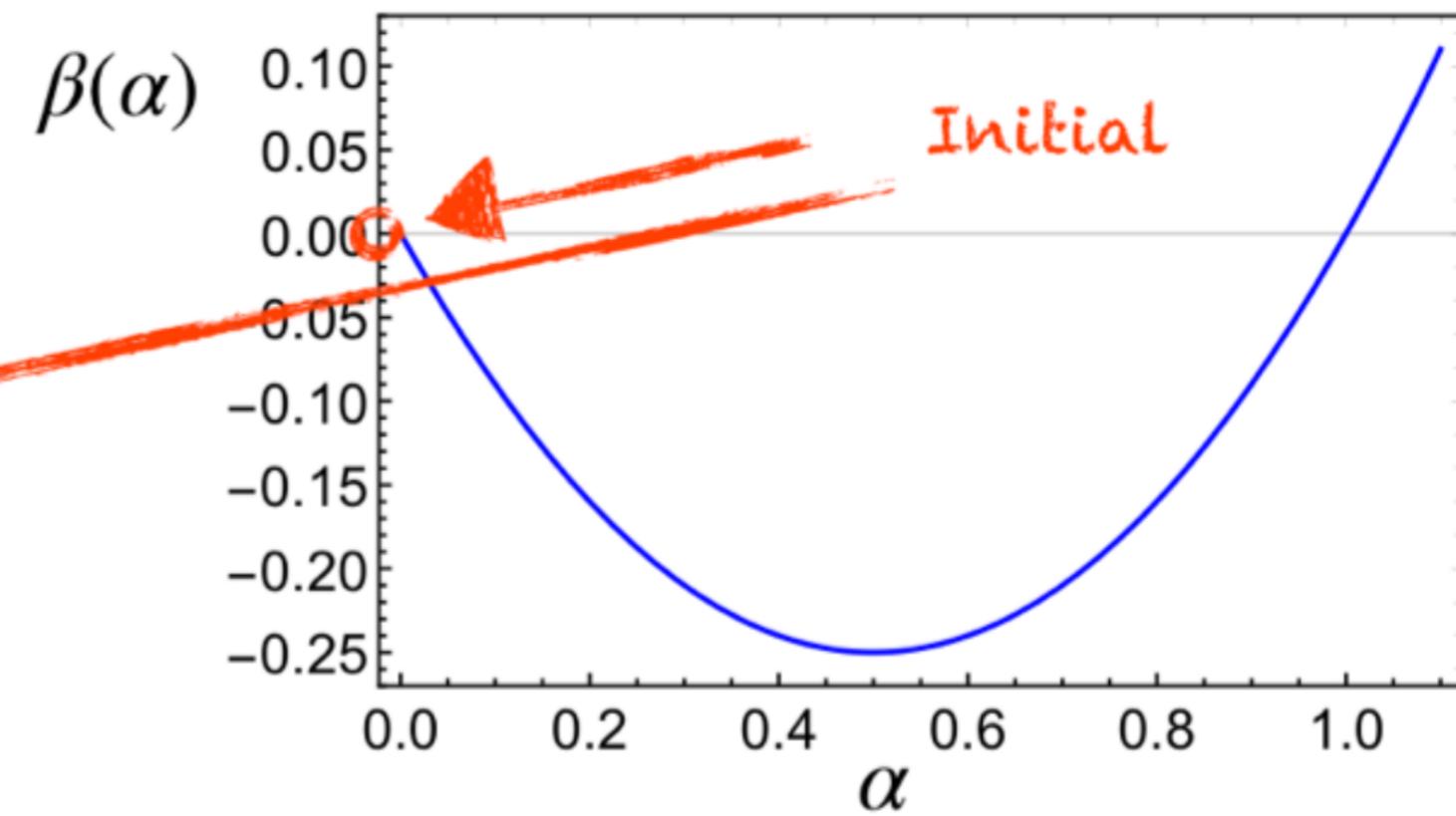
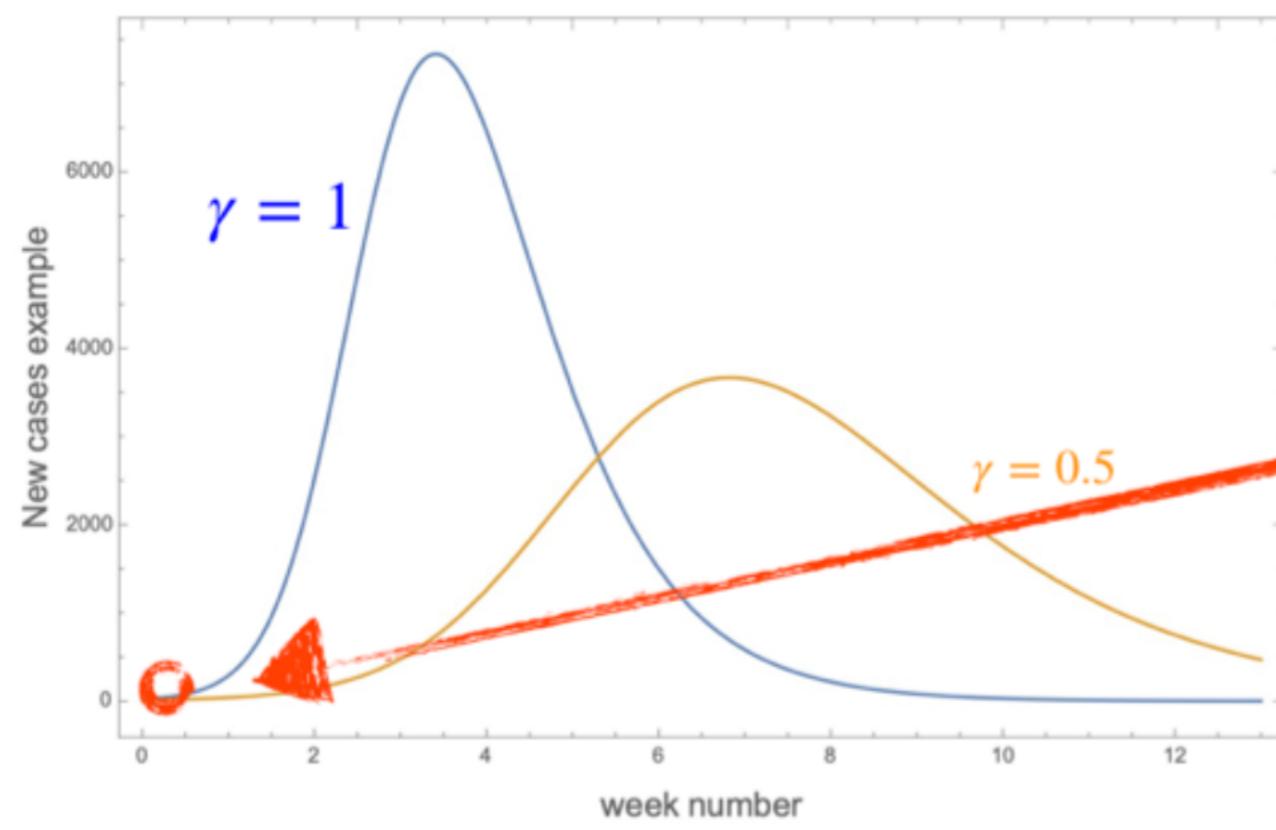
$$-\beta(\alpha) \equiv \frac{d\alpha}{dt} = \gamma \alpha \left( 1 - \frac{\alpha}{a} \right)$$

- The zeros at  $\alpha = 0$  and  $\alpha = a$  enforce time-scale invariance at these two points
- The solution is
$$\alpha(t) = \frac{a e^{\gamma t}}{b + e^{\gamma t}}$$
- With  $b$  an integration constant

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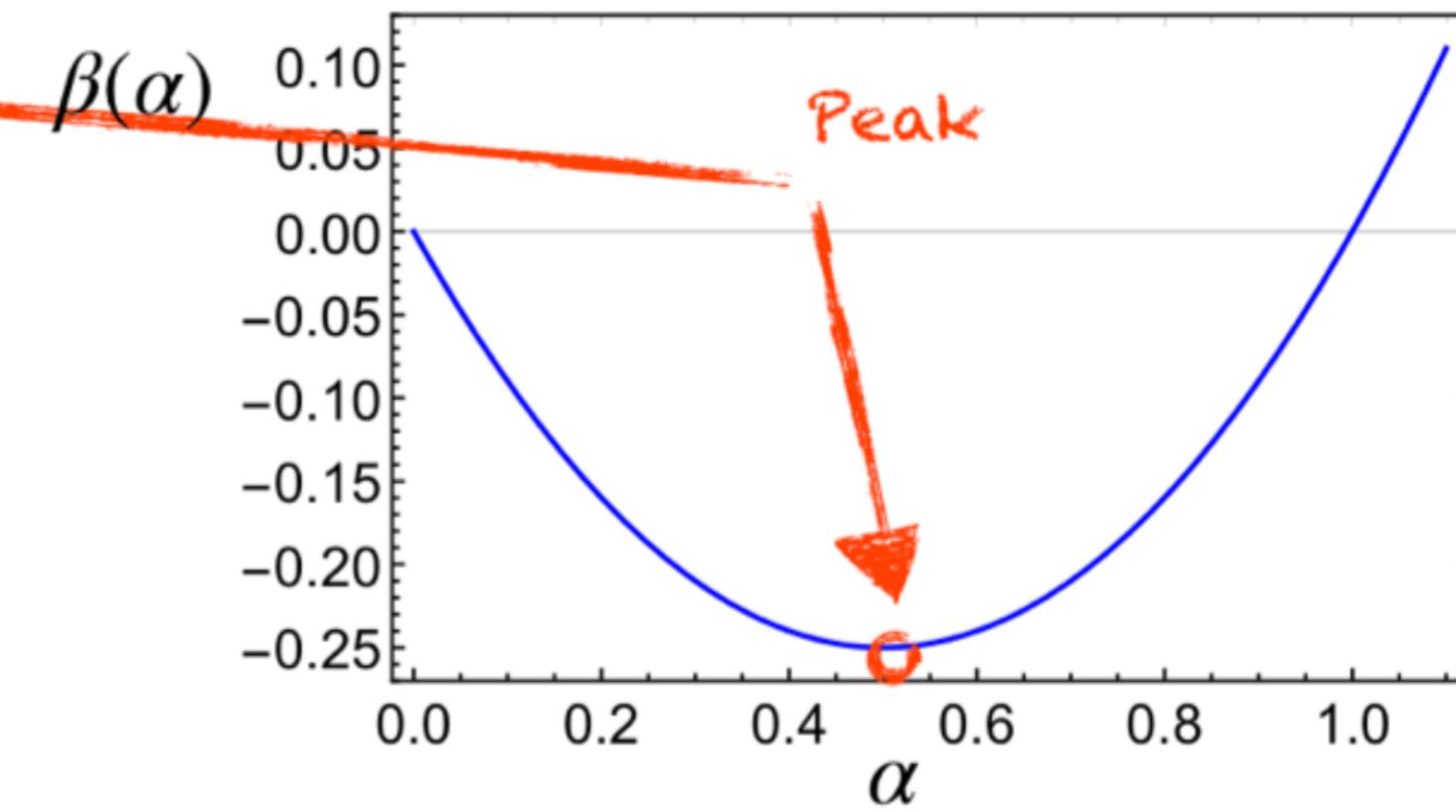
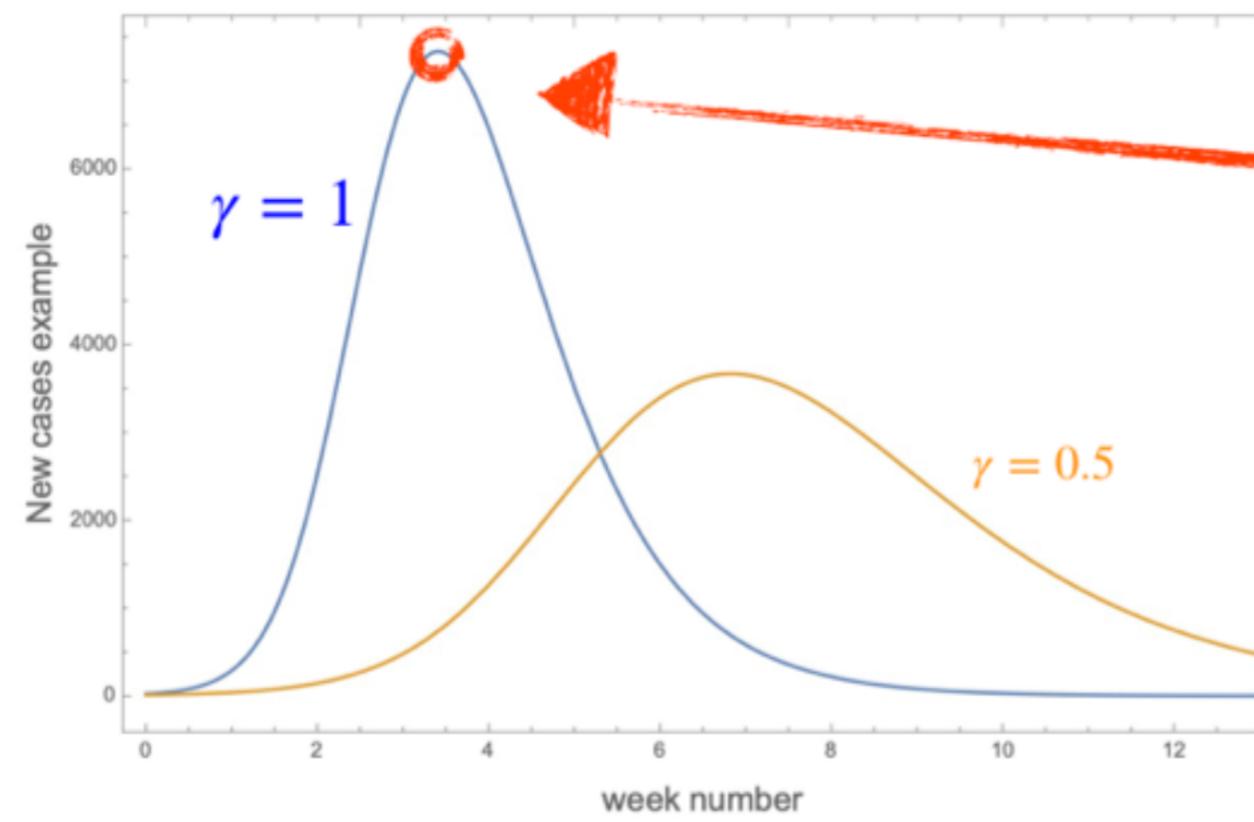
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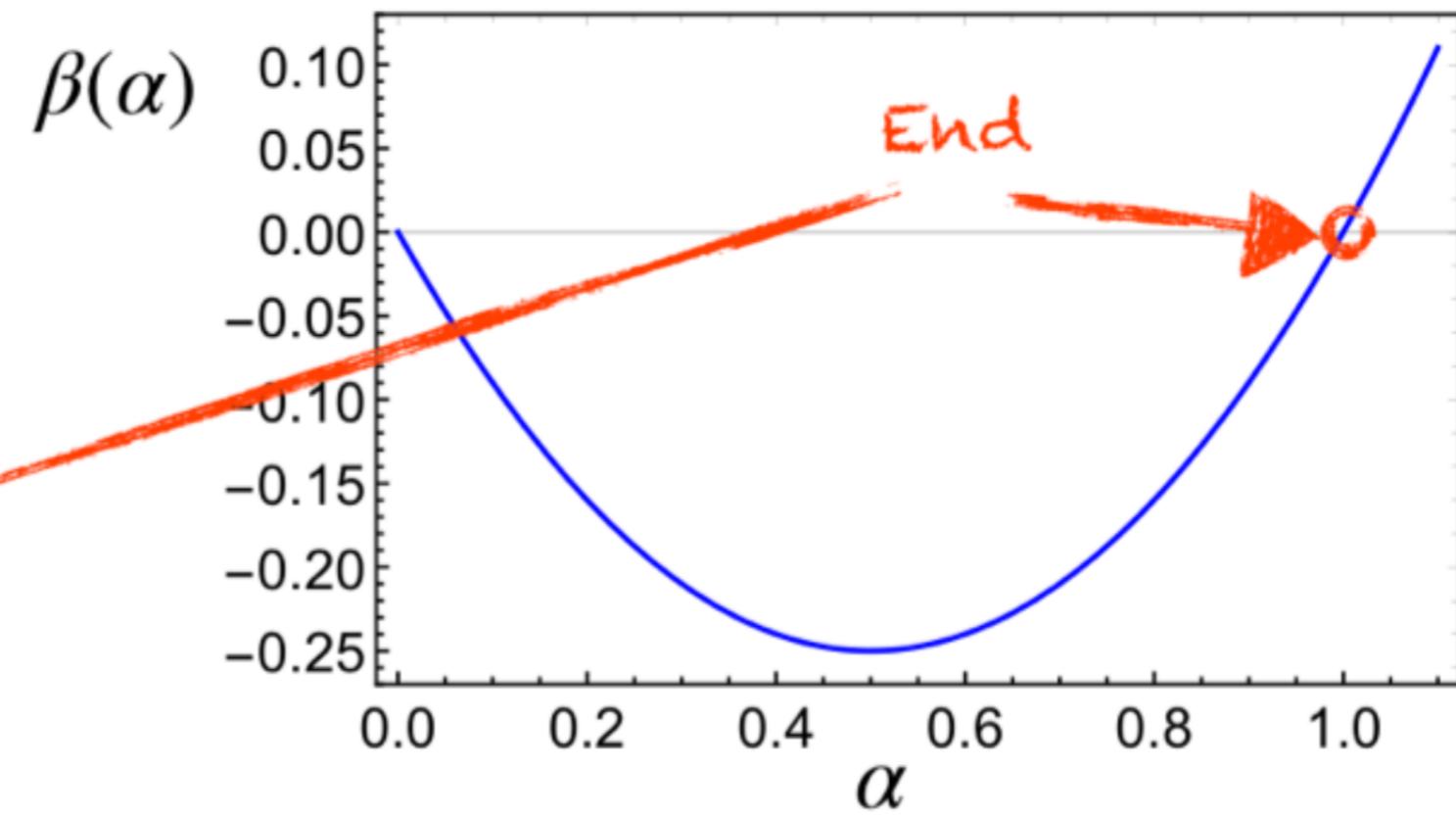
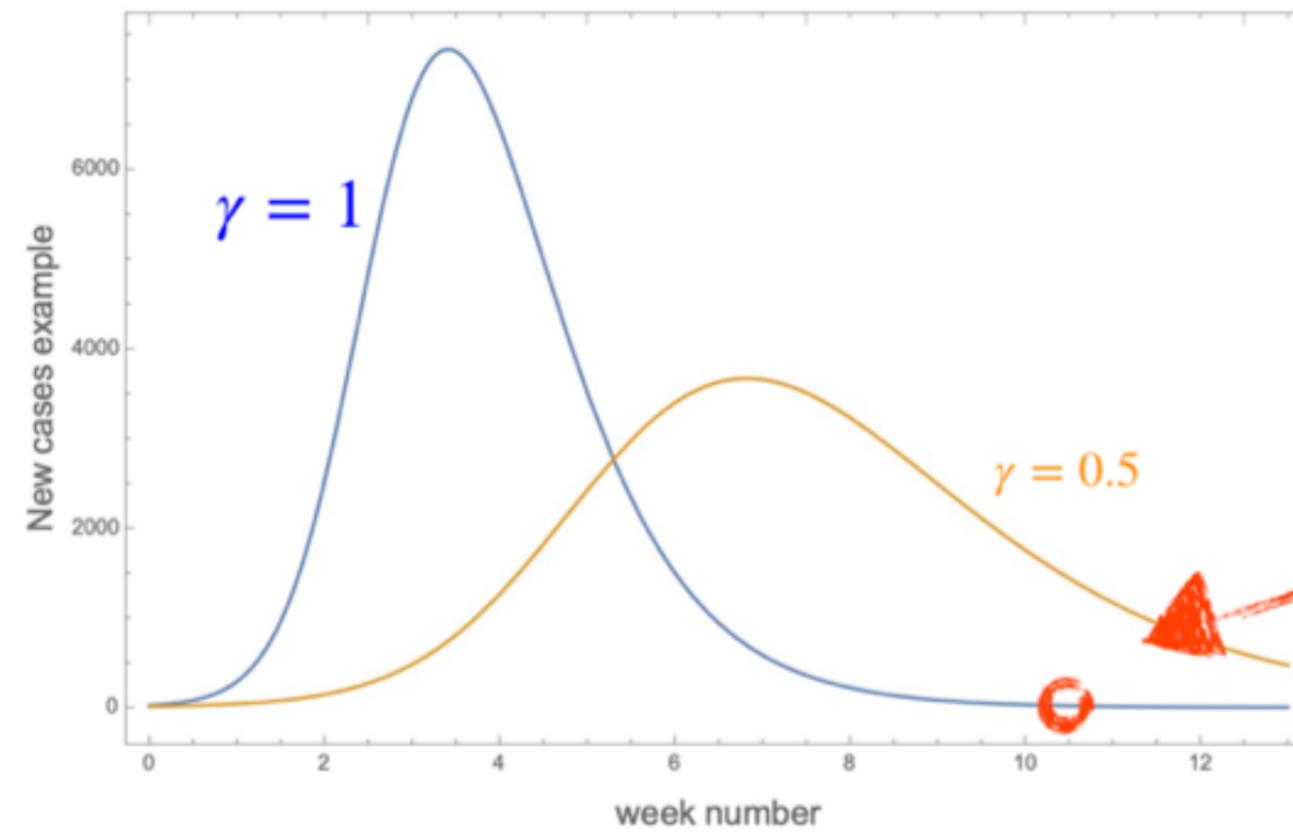
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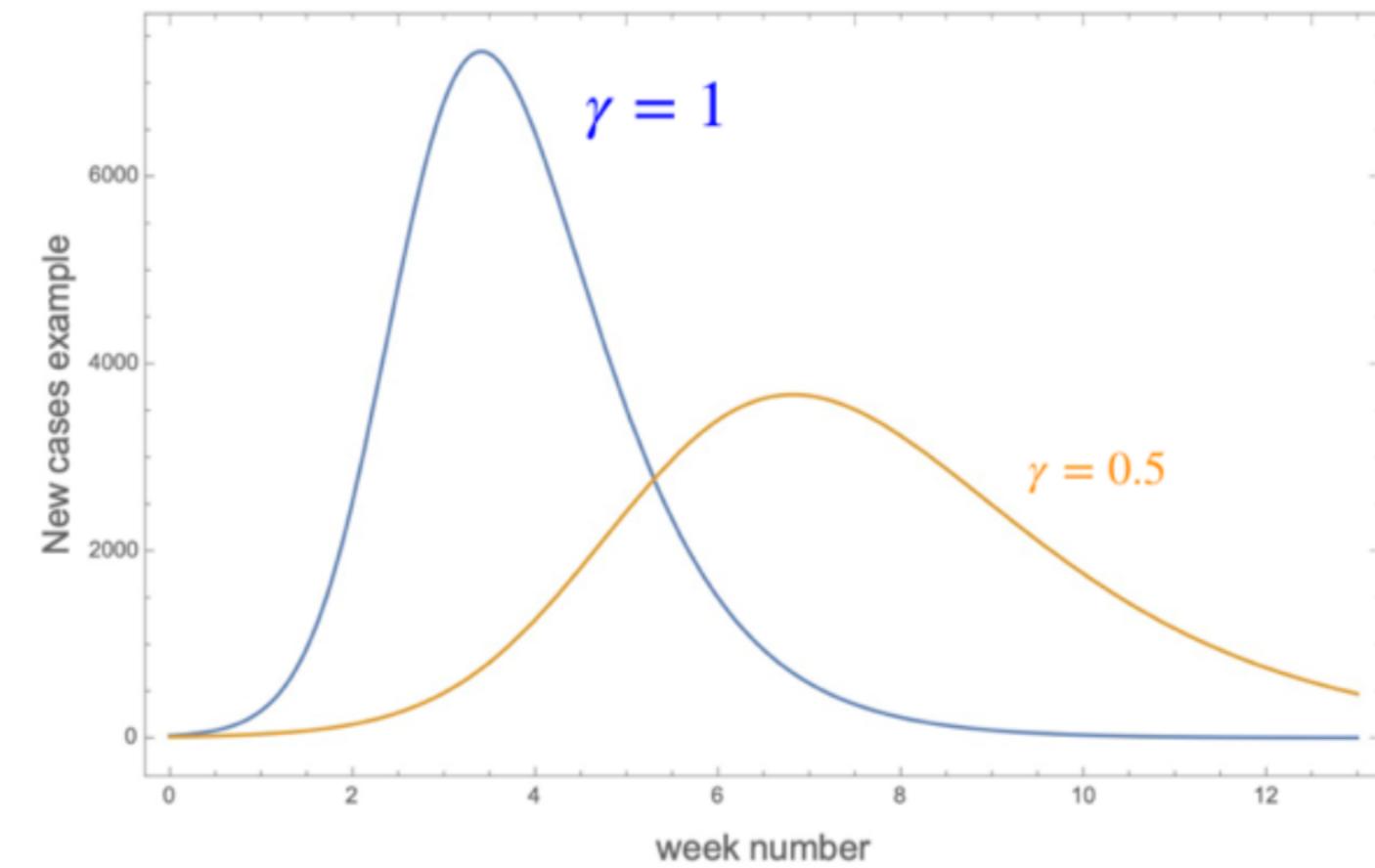
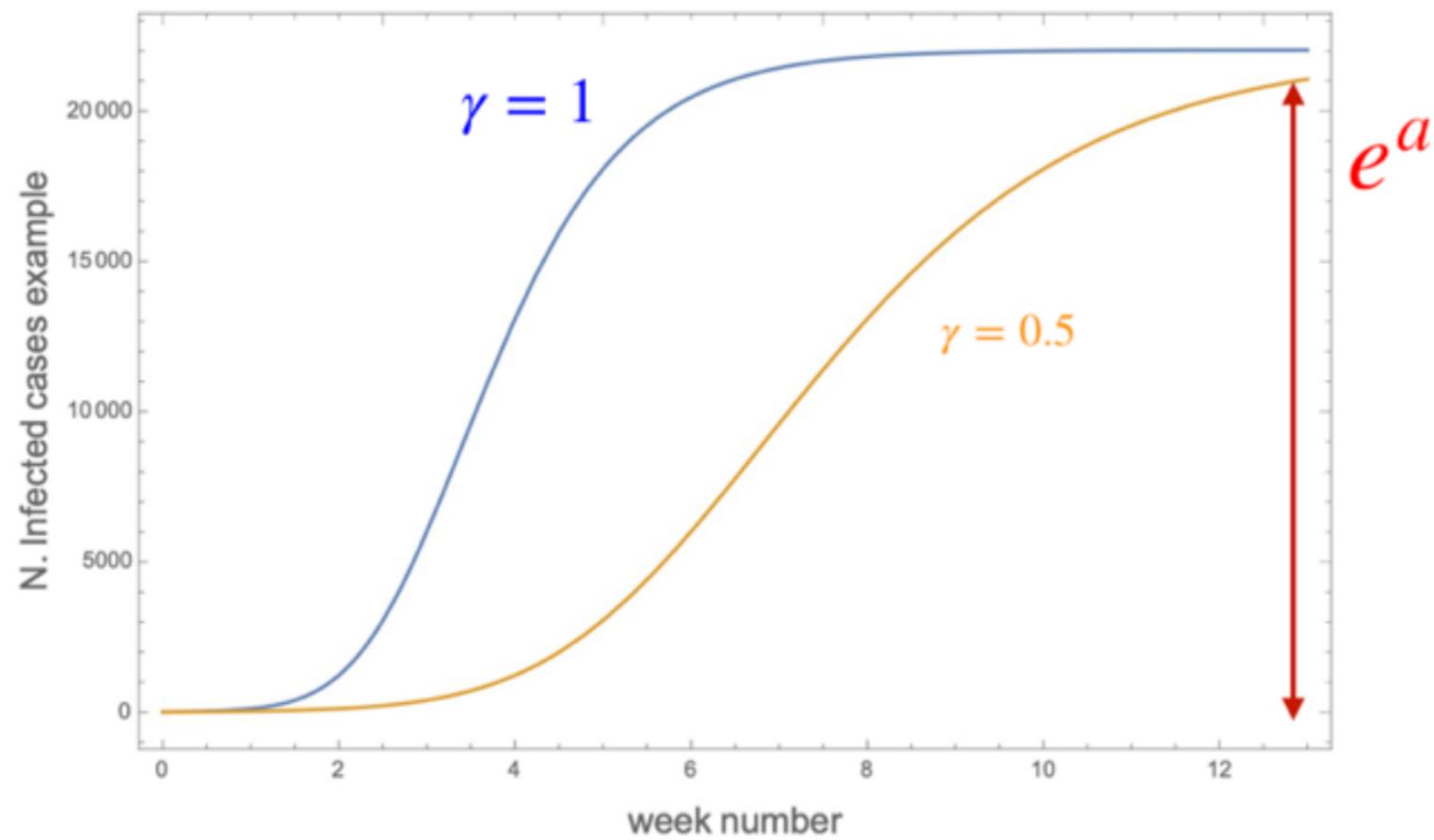
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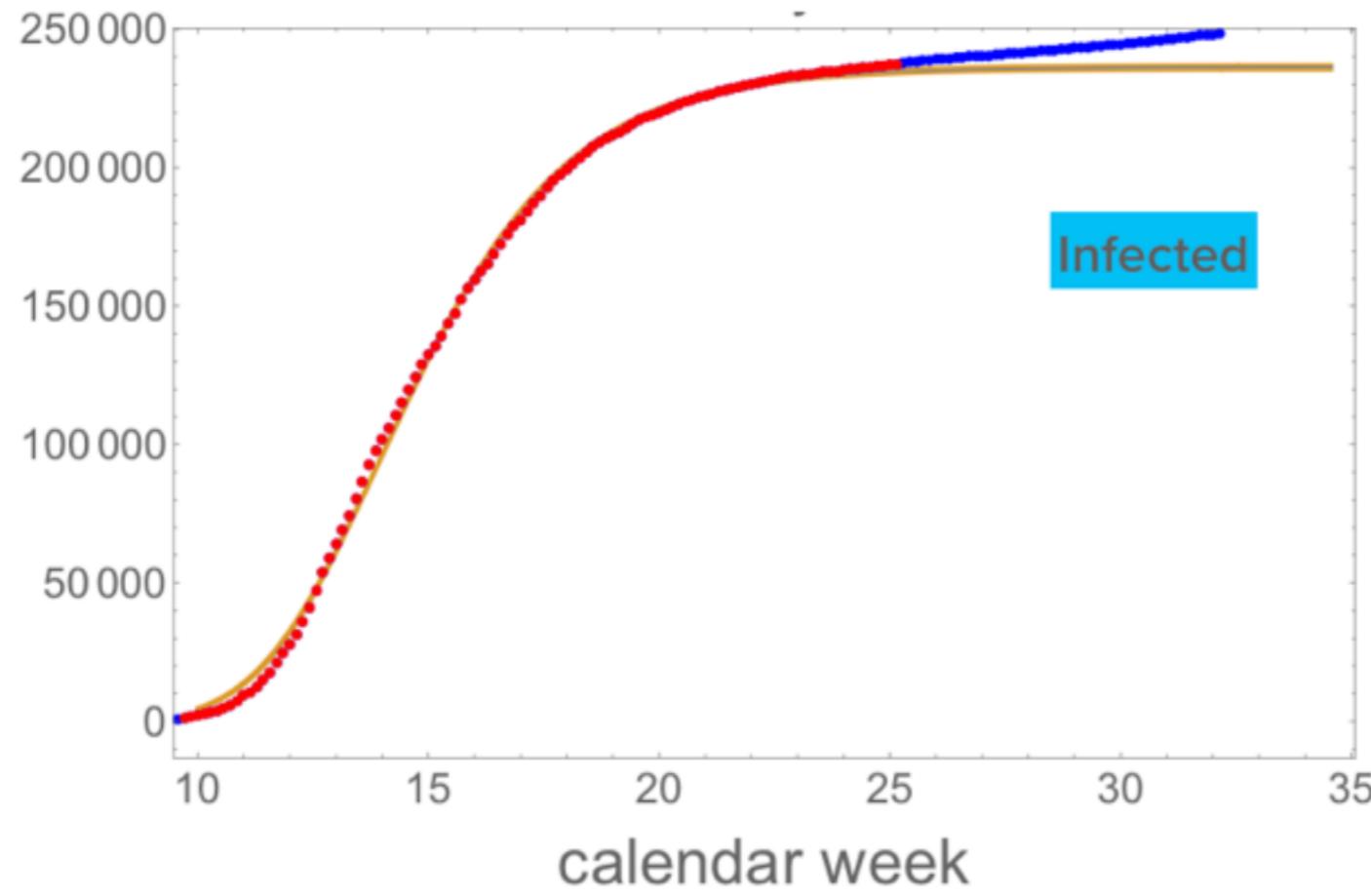
$$\alpha(t) = \frac{a e^{\gamma t}}{b + e^{\gamma t}}$$

- $\gamma$  controls the infection rate and the flattening of the epidemic curve.



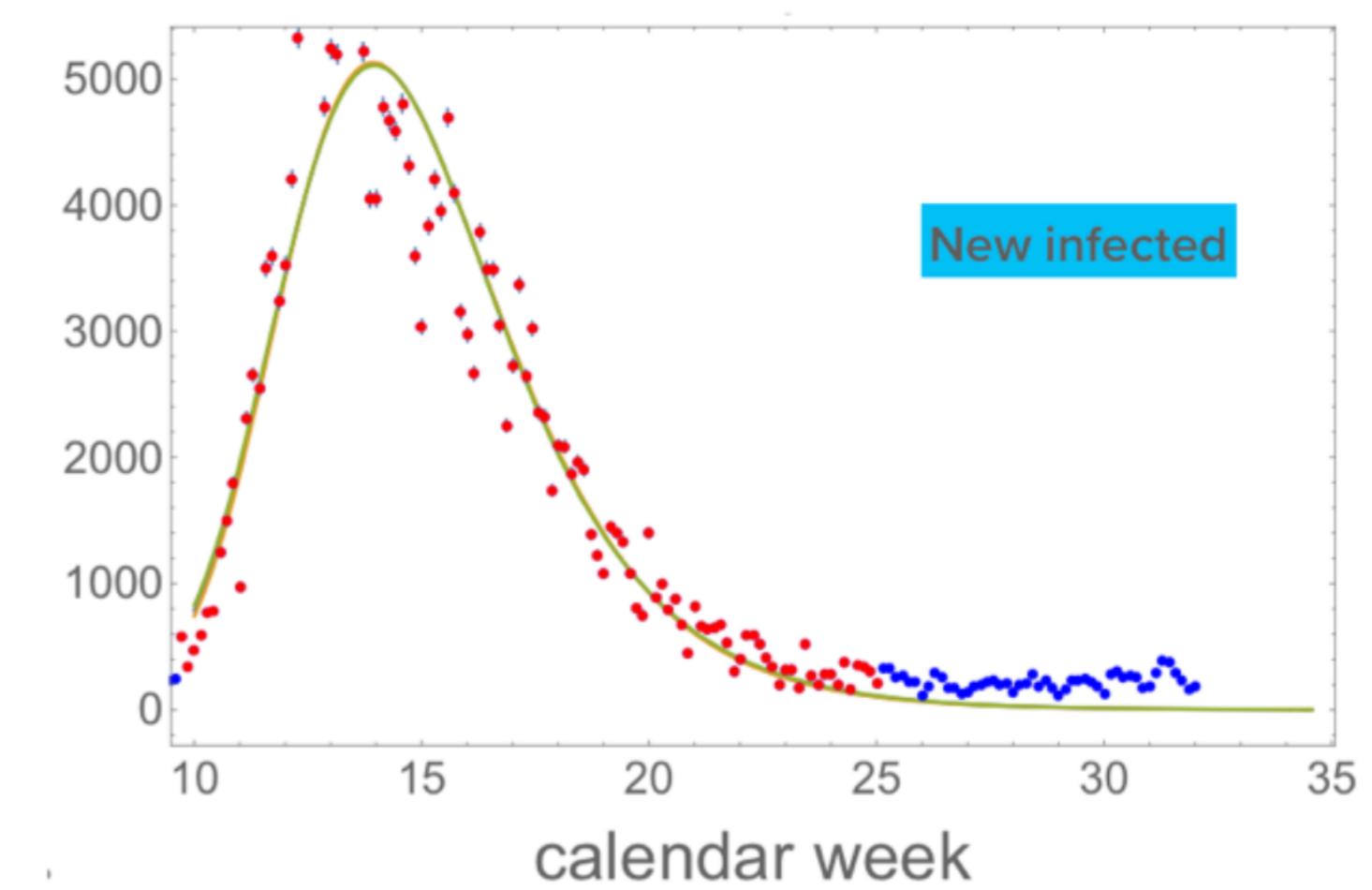
- $e^a$  is the total number of infected
- $b$  is a temporal shift

*Time structure well reproduced*



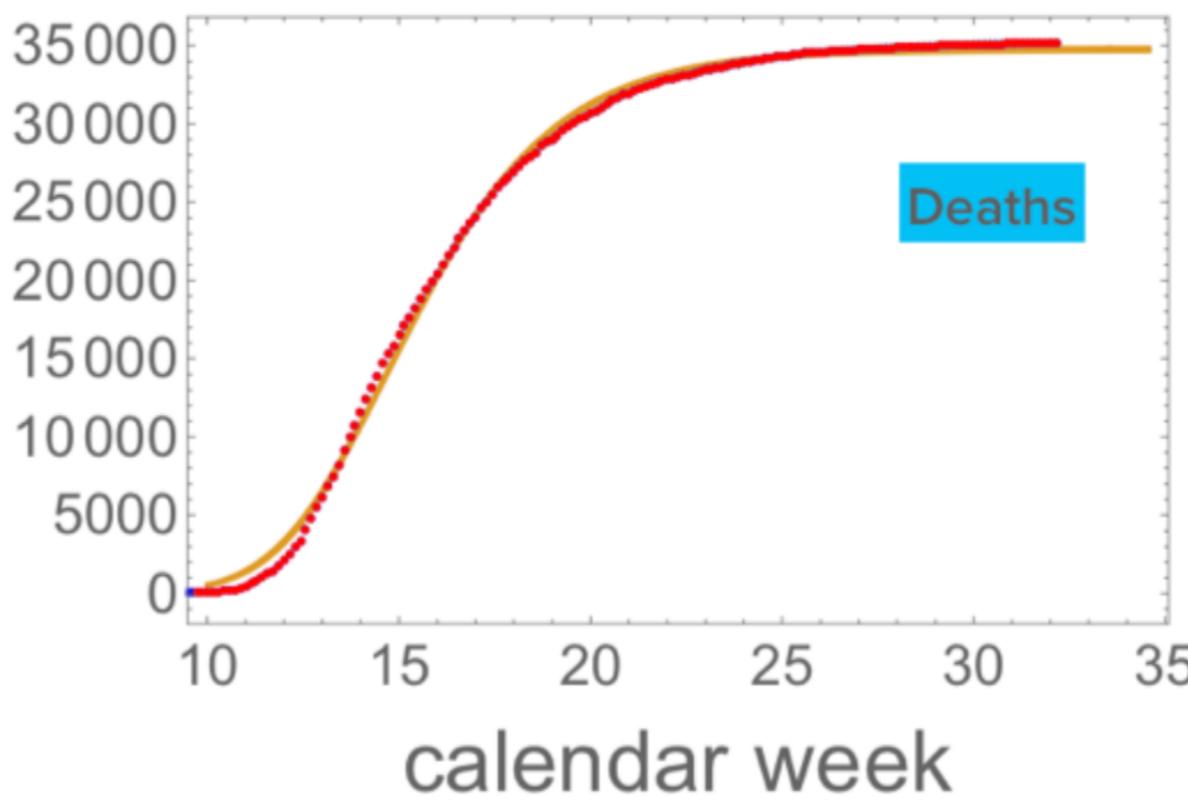
ITALY

Infected



New infected

$$a = 12.373 \pm 0.005$$
$$\gamma = 0.447 \pm 0.009$$
$$b = 41 \pm 5$$



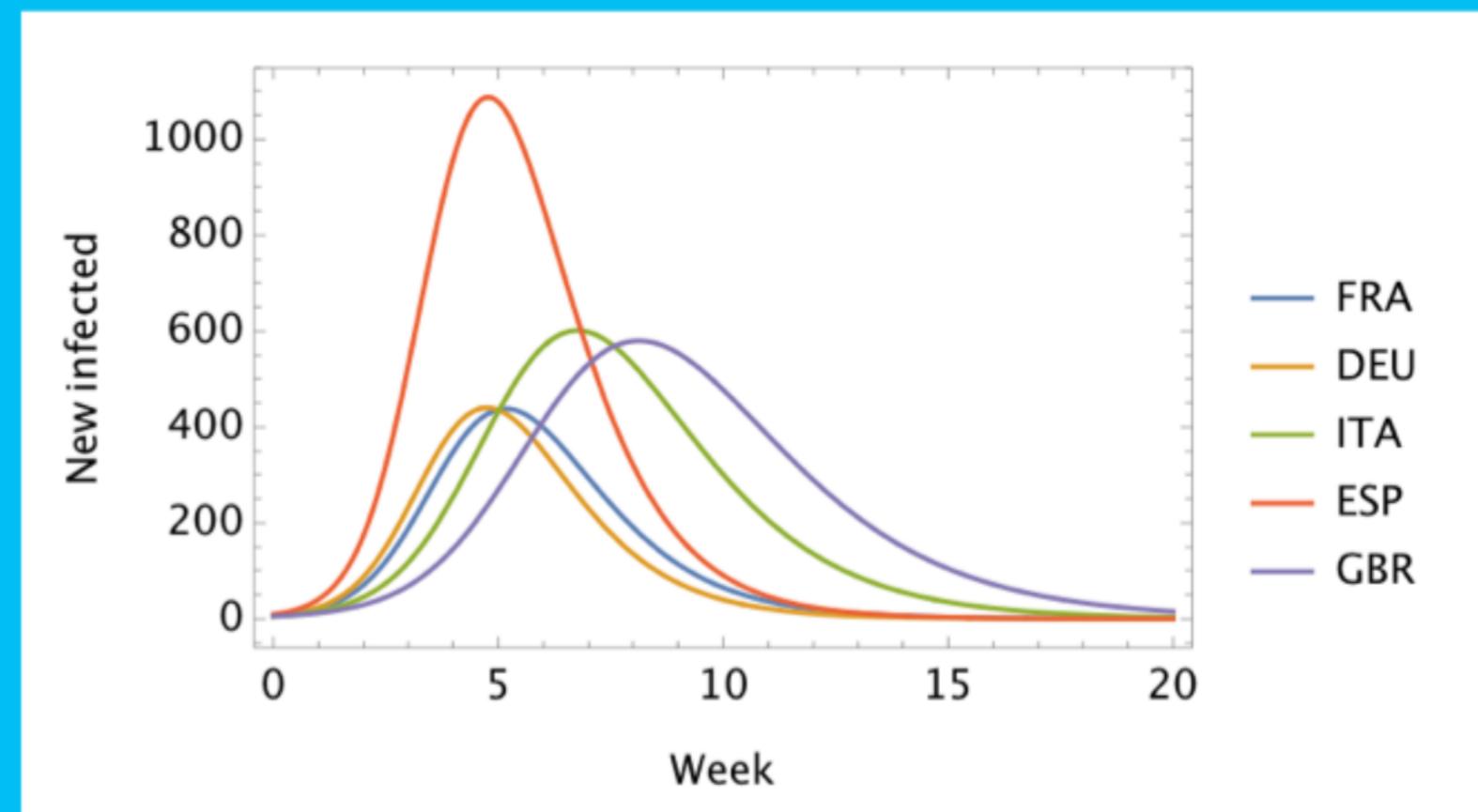
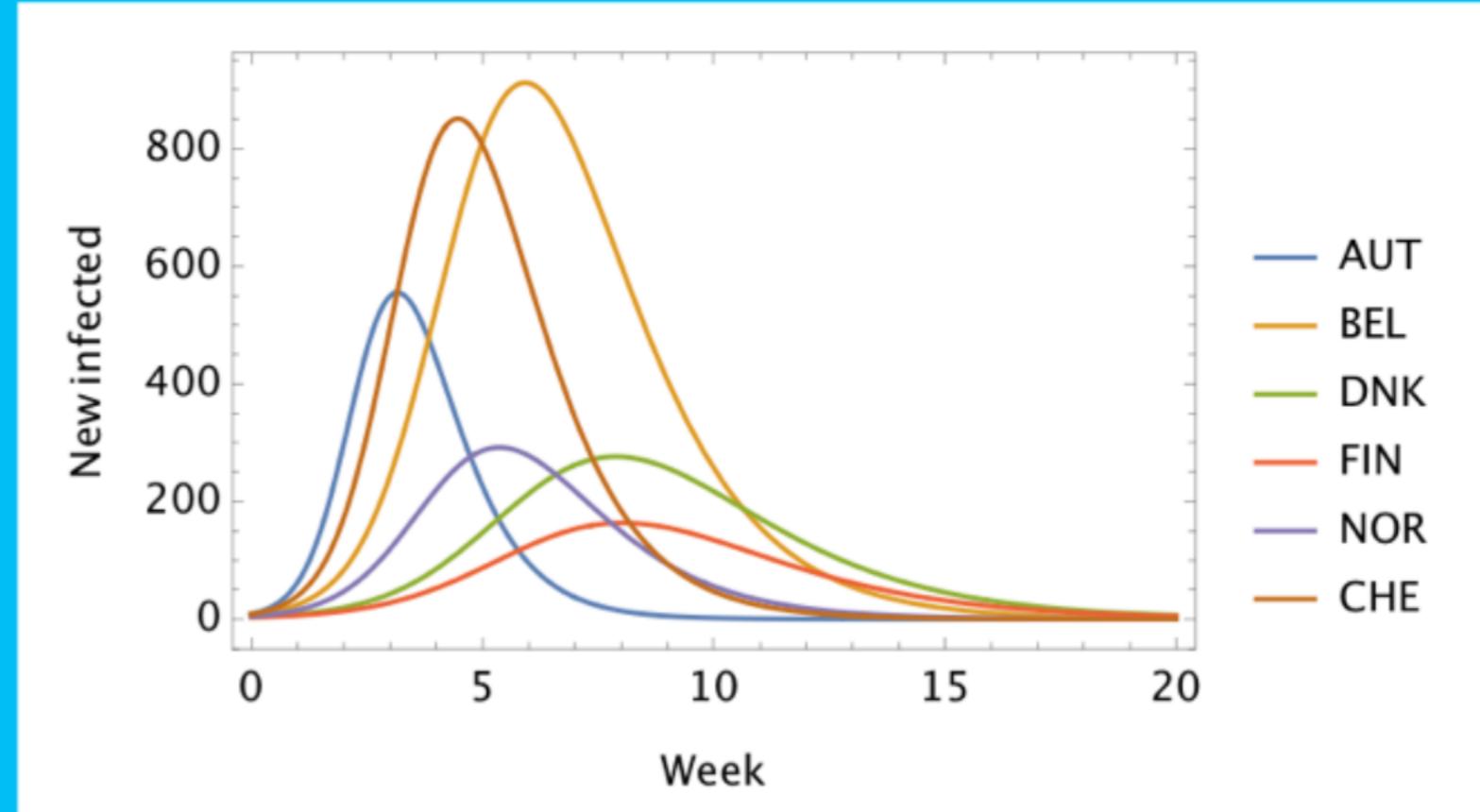
Deaths



eRG

# ADVANTAGES

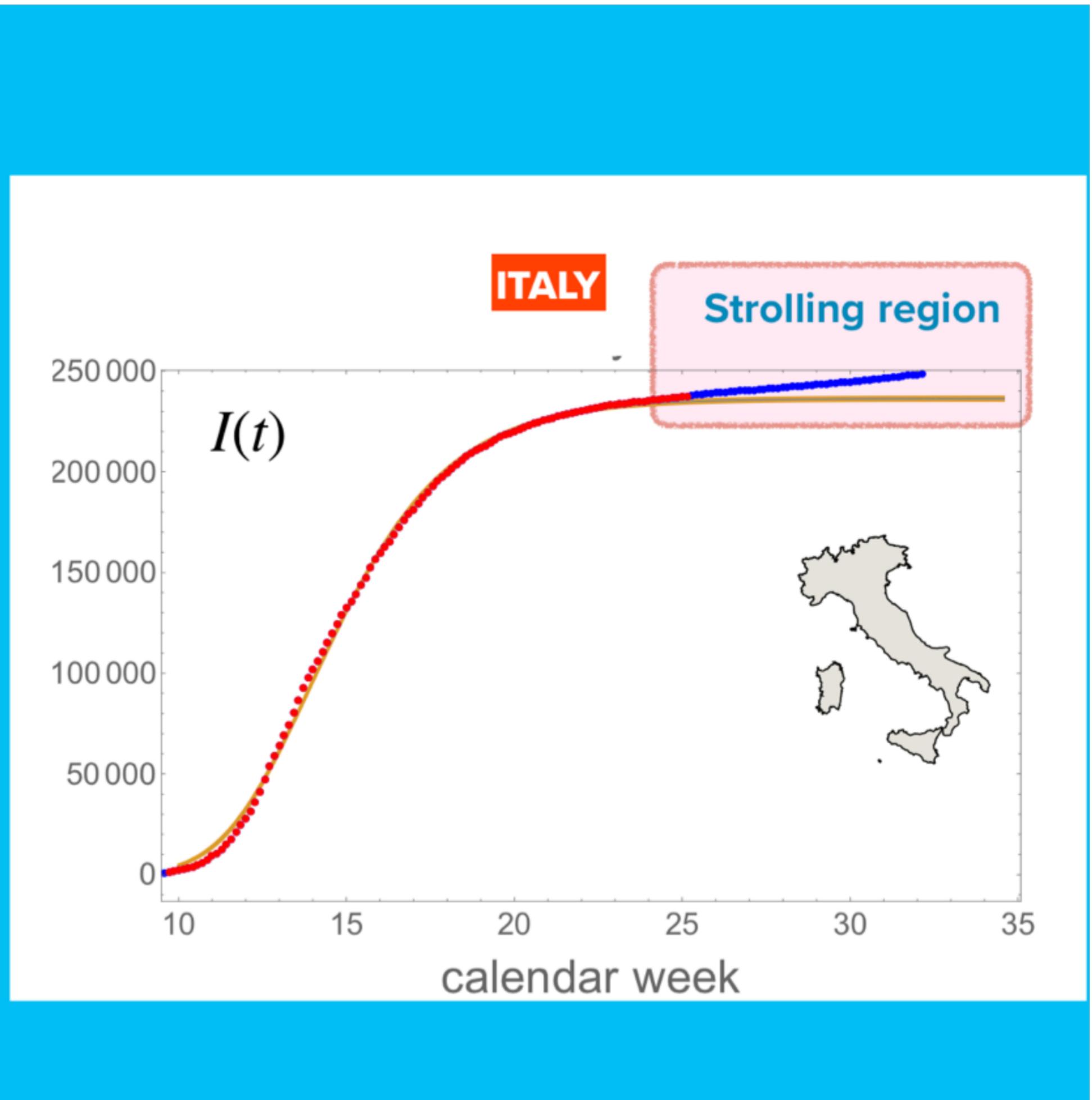
- Analytic expressions
- Symmetry based
- 2 parameters per country
- Time structures well described
- Predictive near peak of new infected



NEAR TIME SCALE INVARIANCE

# EXPLAINS STROLLING PANDEMIC

- **Approx** time scale invariance
- Strolling pandemic (**Sp**) = linear growth
- **eRG**: natural framework for **Sp**



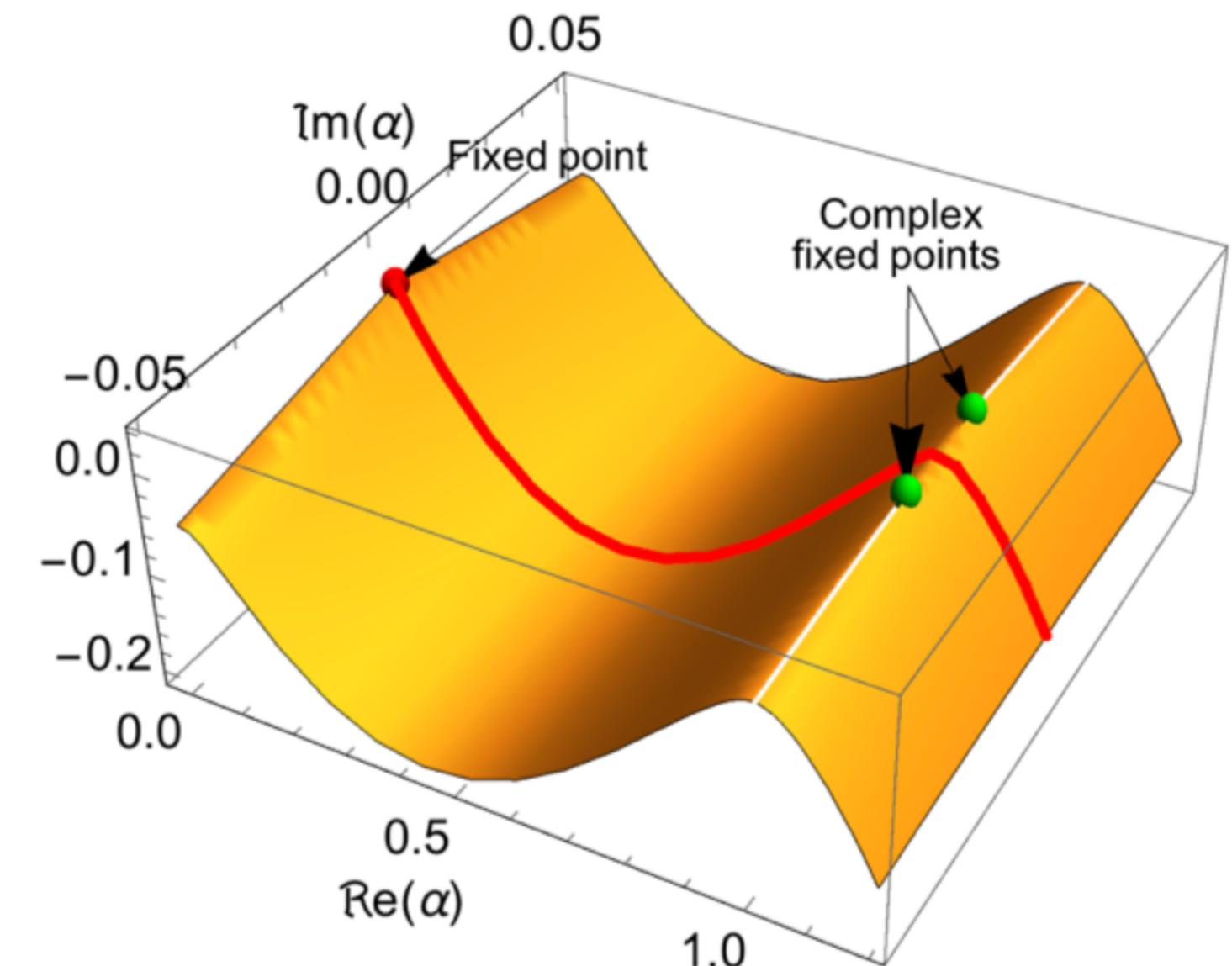
# COMPLEX eRG = CeRG [it reads “Serge”]

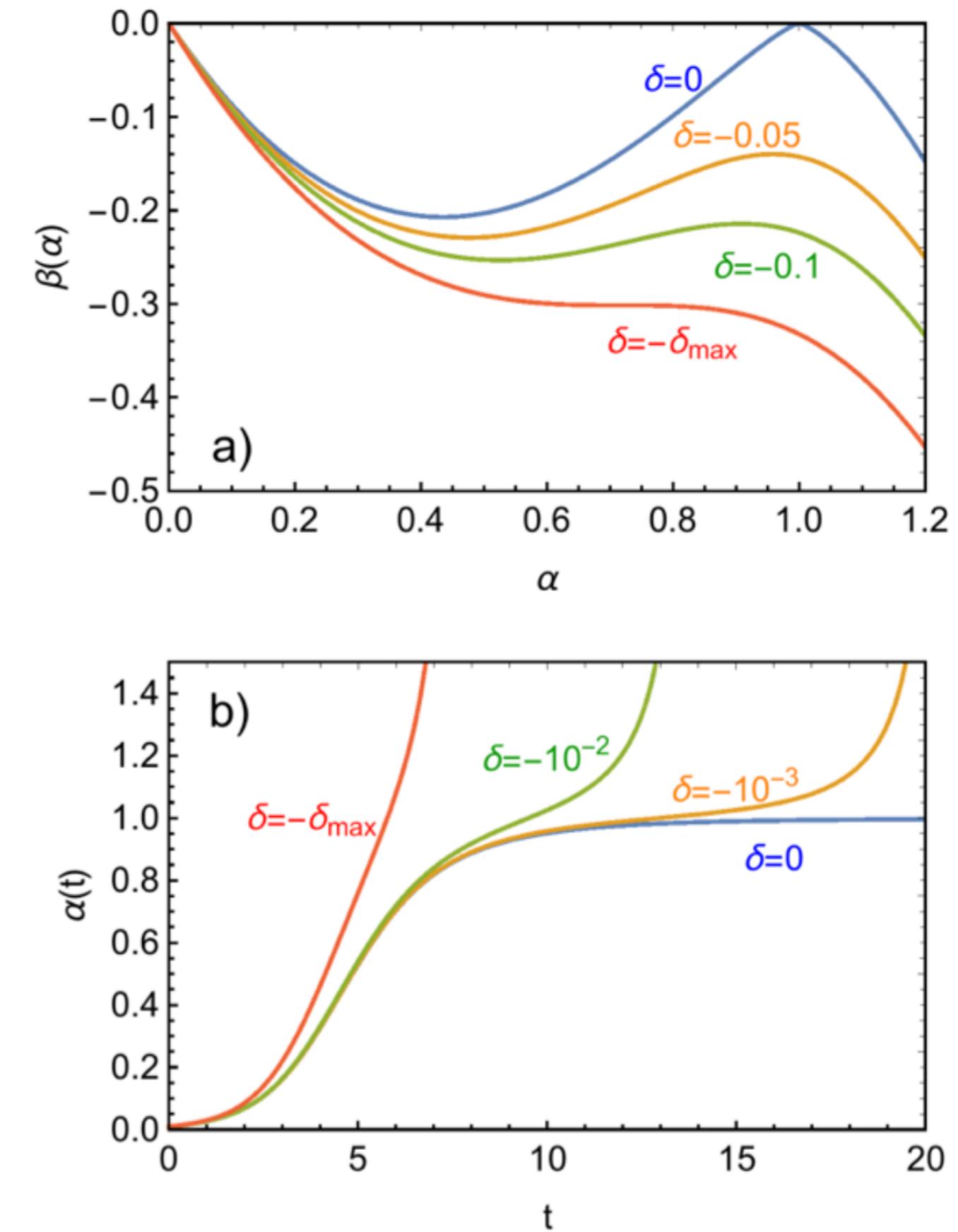
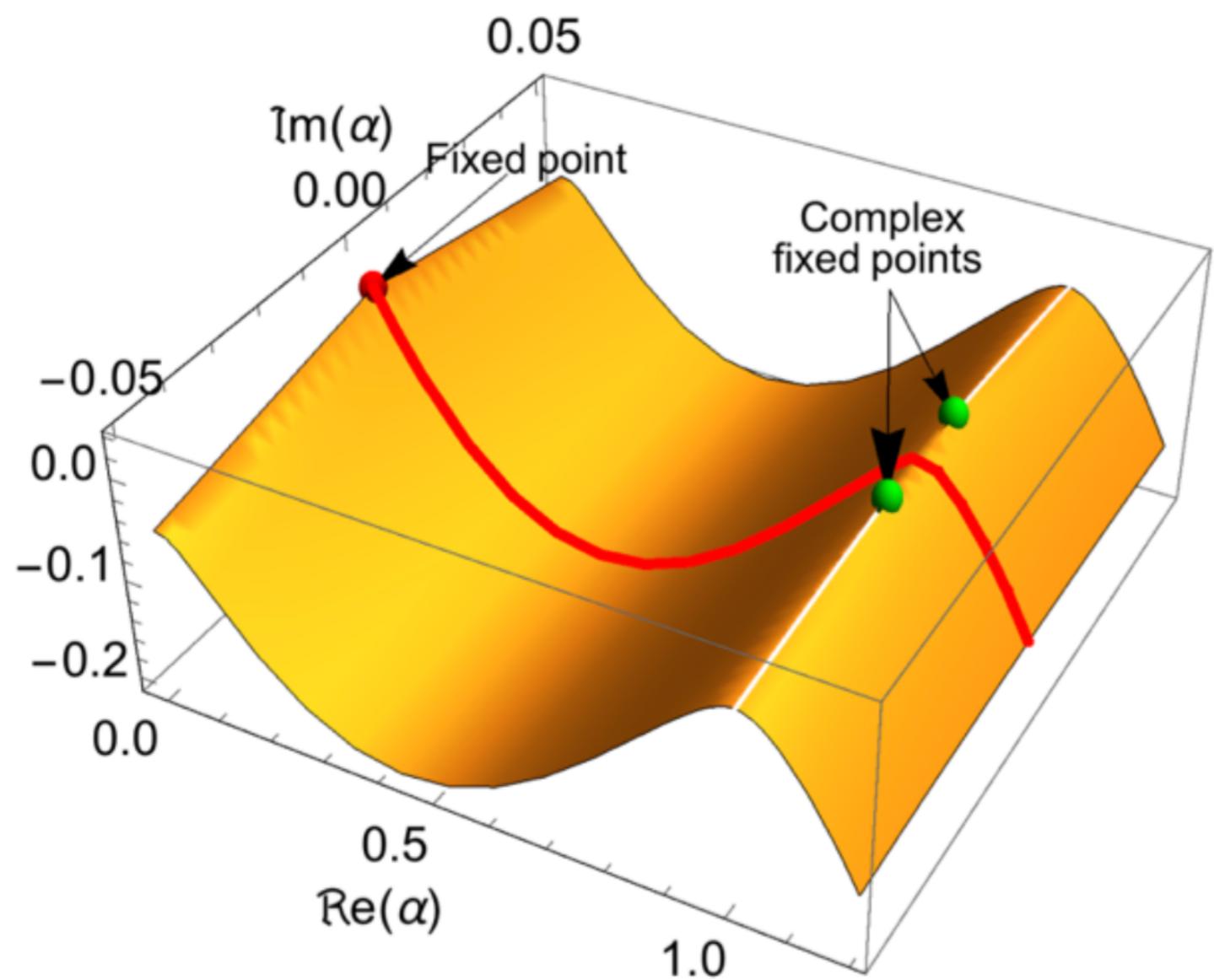
- A tiny violation of large time scale invariance can be achieved via

$$-\beta_{\text{CeRG}}(\alpha) = \frac{d\alpha}{dt} = \alpha \left[ (1 - \alpha)^2 - \delta \right]^p$$

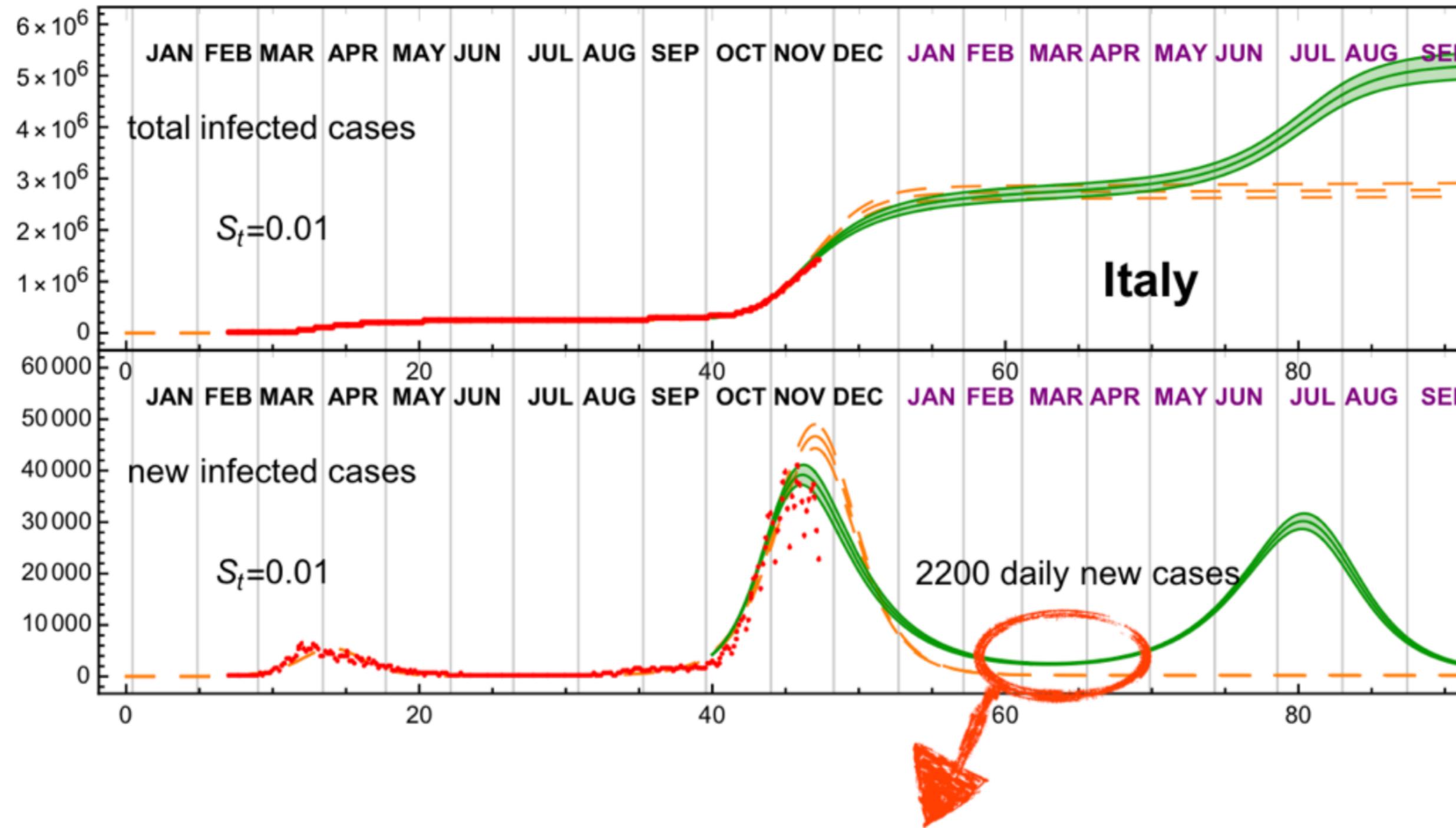
- with  $|\delta| \ll 1$
- For  $p = 1/2$  and  $\delta = 0$  it reproduces eRG
- Complex fixed points for negative  $\delta$

$$\alpha_0 = 0 , \quad \alpha_1 = 1 - i\sqrt{|\delta|} , \quad \alpha_2 = 1 + i\sqrt{|\delta|}$$





## A predicting example:



Crucial to keep the number of new cases as low as possible!

Prieseman, Sannino et al, The Lancet 397, P92-93

## What next?

- Dilatonic dynamics / Conformal winds
- Beyond scalars
- Deeper relation to gravity
- CFT to reorganize understanding of infectious diseases. (Large virological change?)
- . . .