

# Red hydrodynamic model of quark matter in nuclear collisions

Akihiko Monnai (Osaka Institute of Technology)

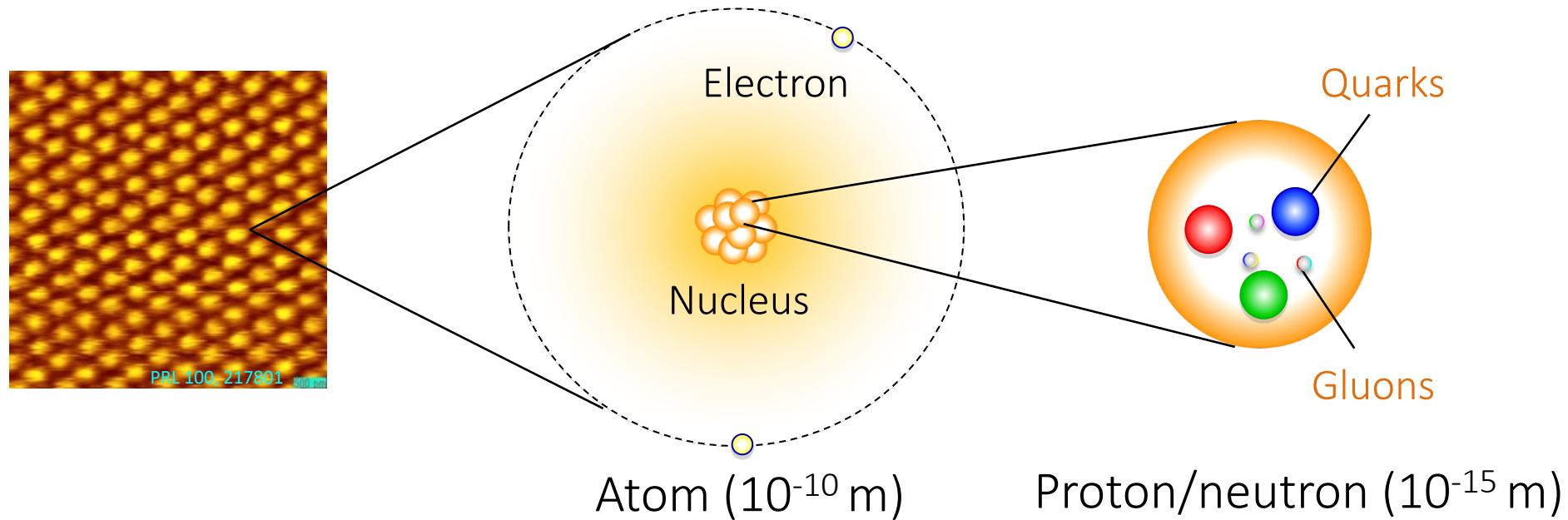
AM, arXiv:2301.00588 [nucl-th] 

Interdisciplinary Science Conference in Okinawa (ISCO 2023)

1<sup>st</sup> March 2023, OIST, Japan

# Introduction

## ■ The subatomic world



Matter is composed of elementary particles called **quarks**, bound by the strong force mediated by **gluons**

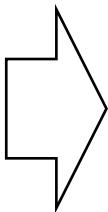
# Introduction

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## ■ Phases of matter



Ice (solid phase)



Water (liquid phase)



Vapor (gas phase)

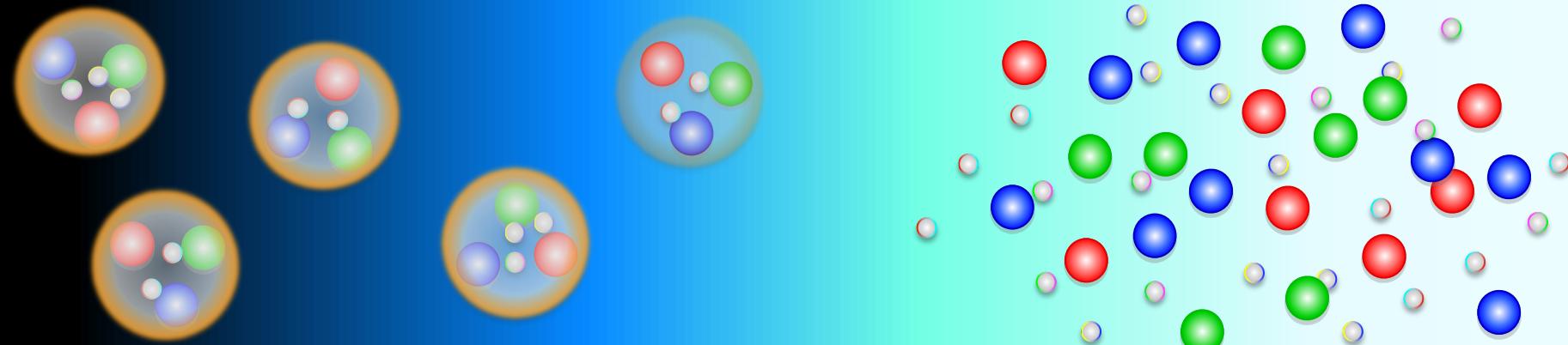
Matter takes different states (**phases**) depending on temperature, pressure, etc.

A change from one phase to another is called **phase transition**

# Introduction

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## ■ Phase transition of quarks

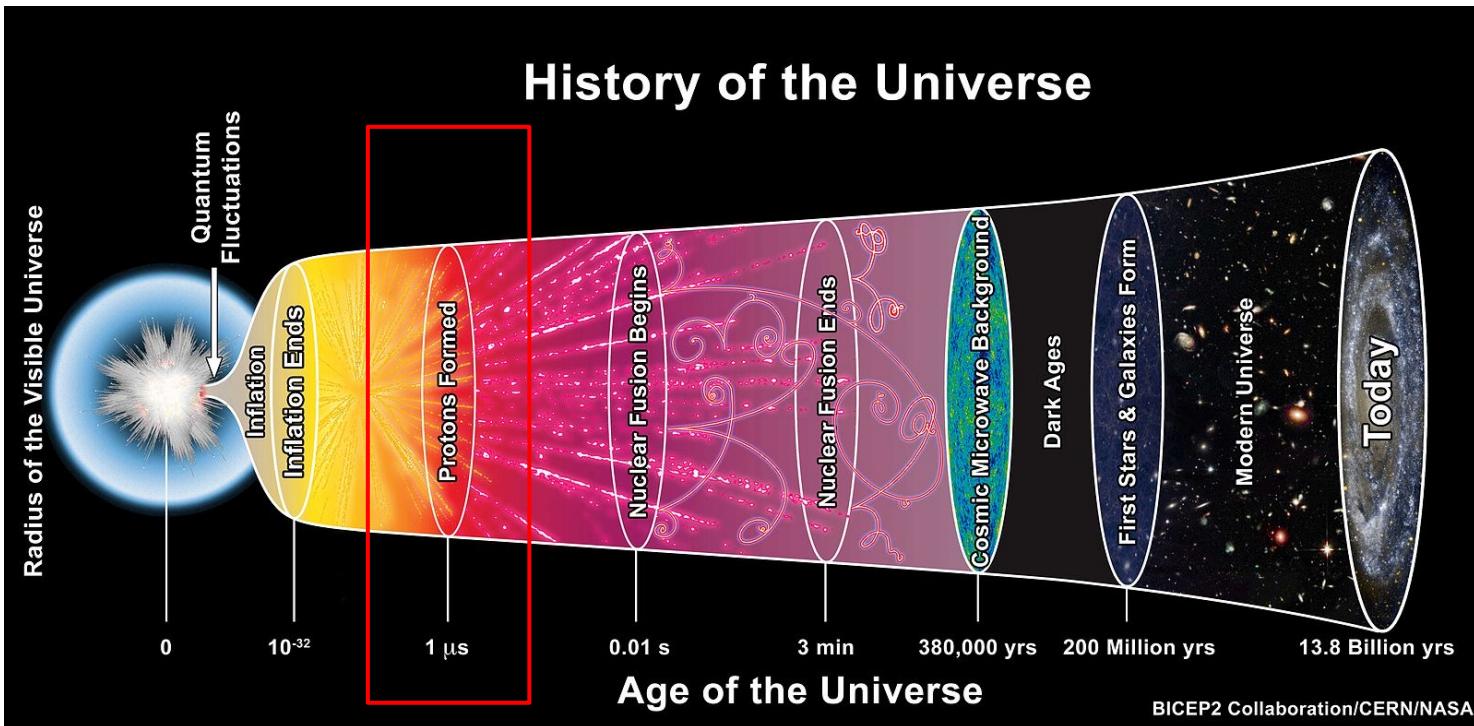


Protons and neutrons “melt” into **quark-gluon plasma** (QGP)  
above around 2 trillion degrees Kelvin

# Introduction

- Where is the quark-gluon plasma?

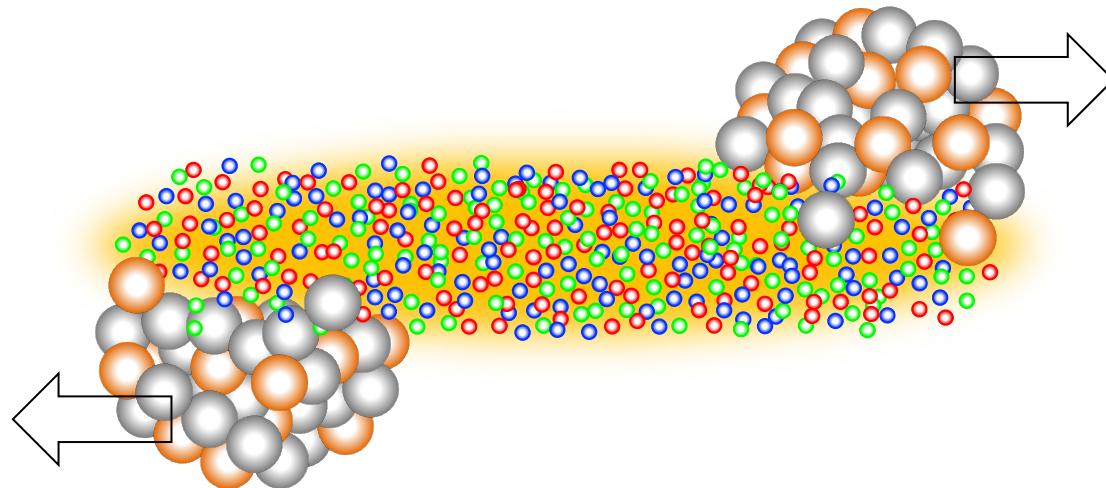
The QGP had filled the Universe around  $10^{-5}$  seconds after the Big Bang



# Introduction

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- How to make the quark-gluon plasma **on earth**



Smash two big nuclei (such as gold or lead) almost at the speed of light

BNL Relativistic Heavy Ion Collider (2000-)  
CERN Large Hadron Collider (2010-)



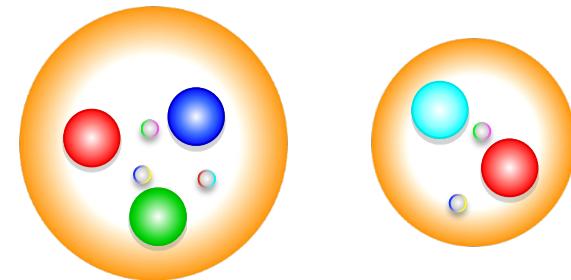
# Introduction

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## ■ What can be observed in experiments?

- ▶ **Hadrons**

Quarks are frozen back into “quark ice” called hadrons (include protons and neutrons)



- ▶ **Photons**

“Particles of light” are also produced

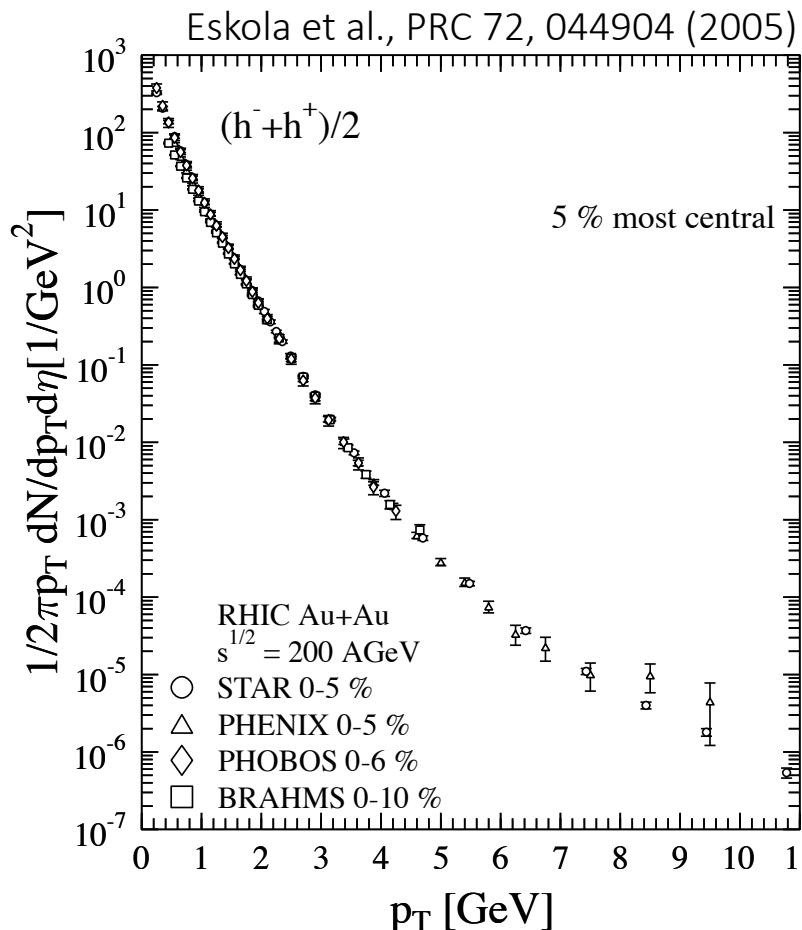


- ▶ Charged leptons, weak bosons, etc.

# Introduction

$$1 \text{ GeV} \simeq 1.6 \times 10^{-10} \text{ J}$$
$$1 \text{ GeV}/c \simeq 5.3 \times 10^{-19} \text{ kg} \cdot \text{m/s}$$

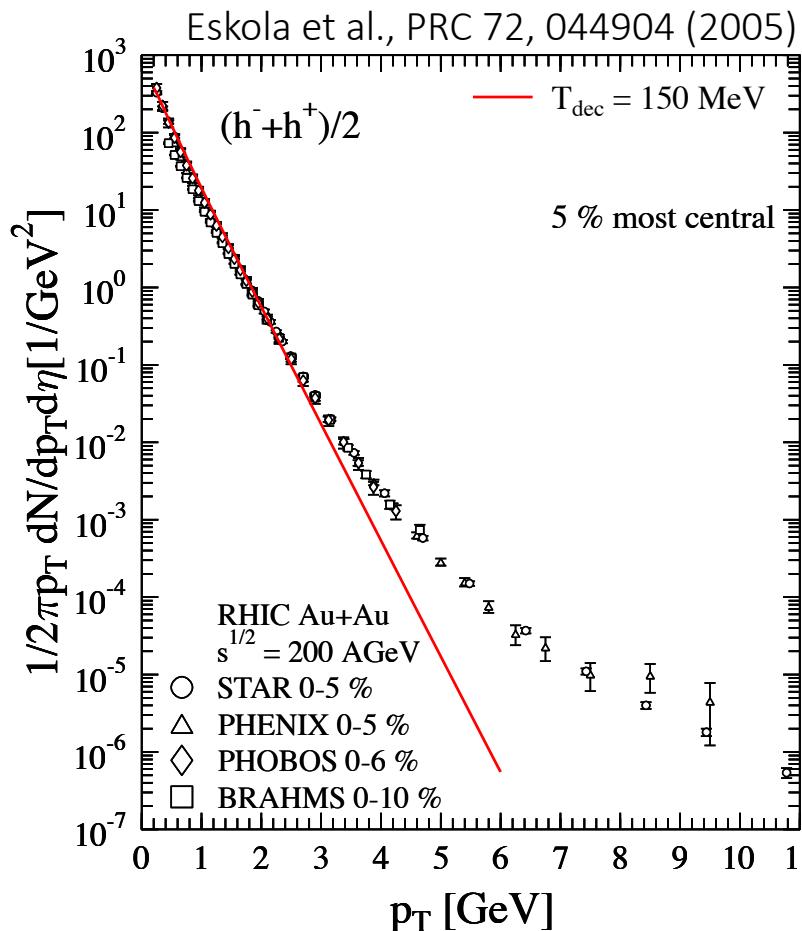
## ■ Interpretation of the momentum distribution



# Introduction

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## ■ Interpretation of the momentum distribution

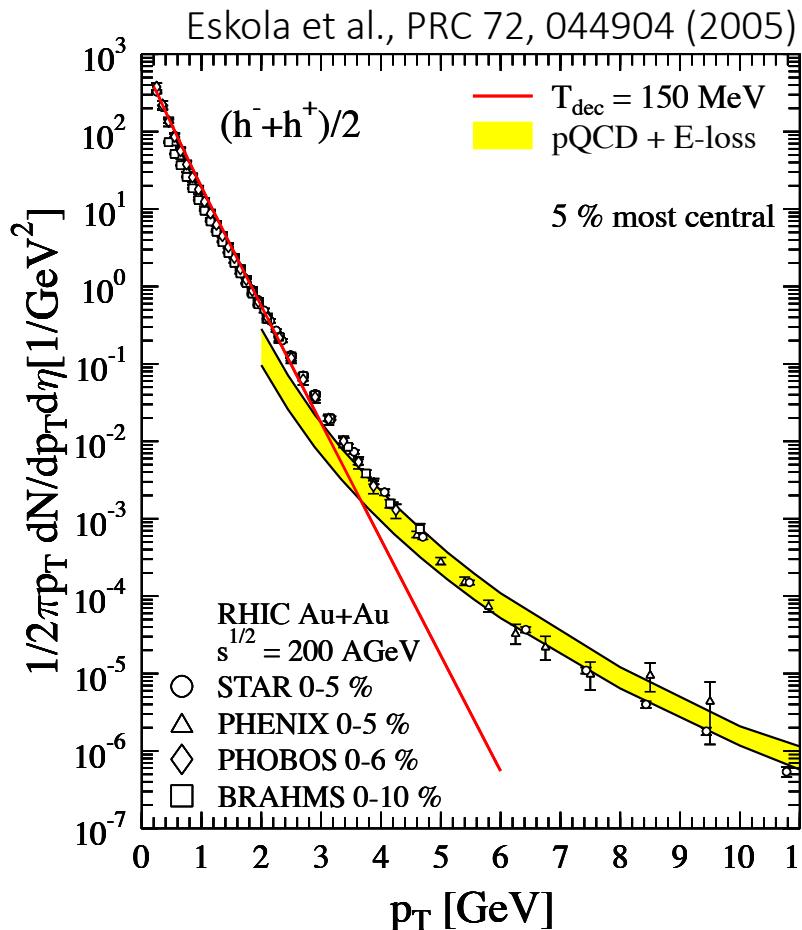


Low momentum region (< 2-4 GeV)  
Hydrodynamic model (strongly-coupled)

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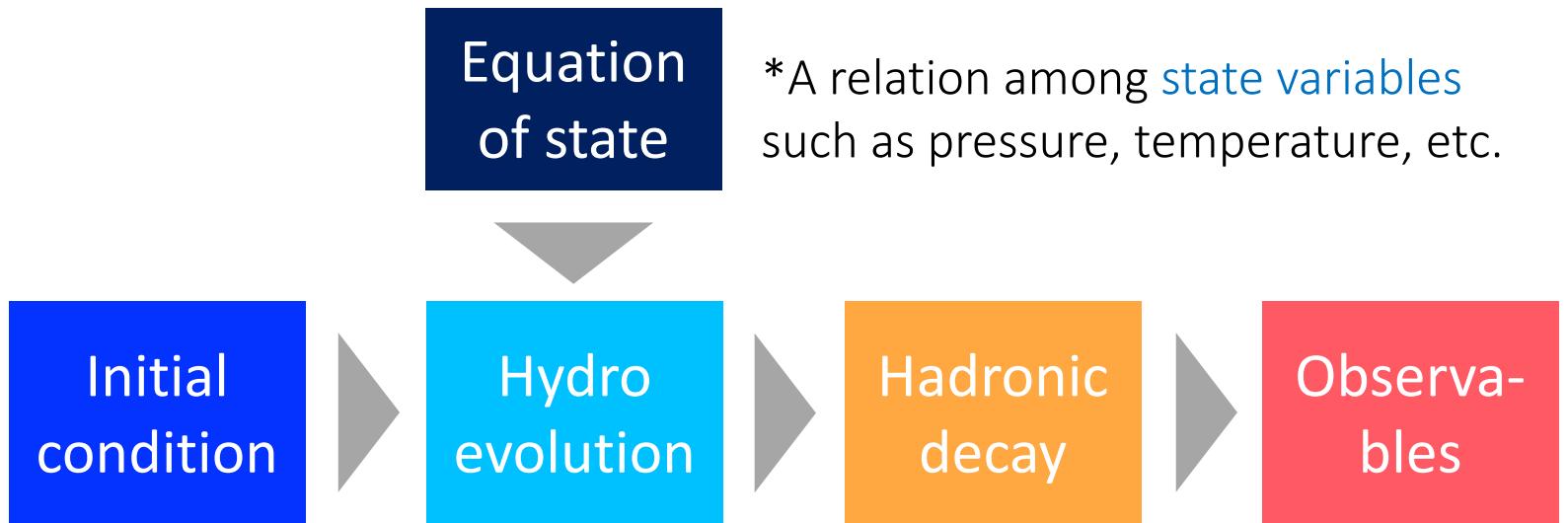
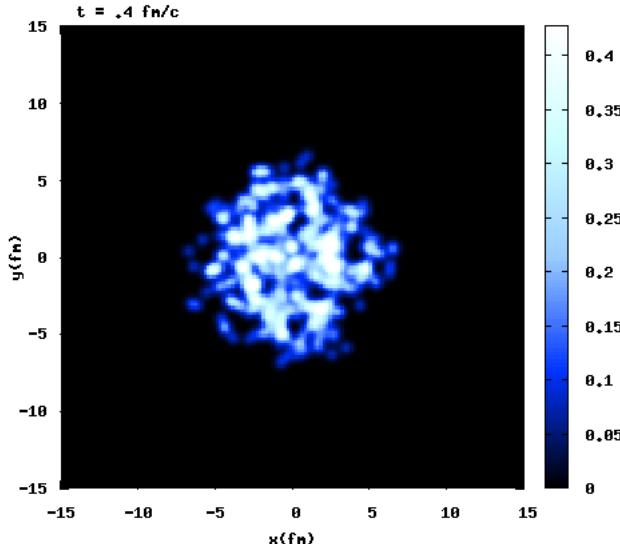
Low momentum region (< 2-4 GeV)  
Hydrodynamic model (strongly-coupled)



Mid-high momentum region (> 4-5 GeV)  
perturbative QCD (weakly-coupled)

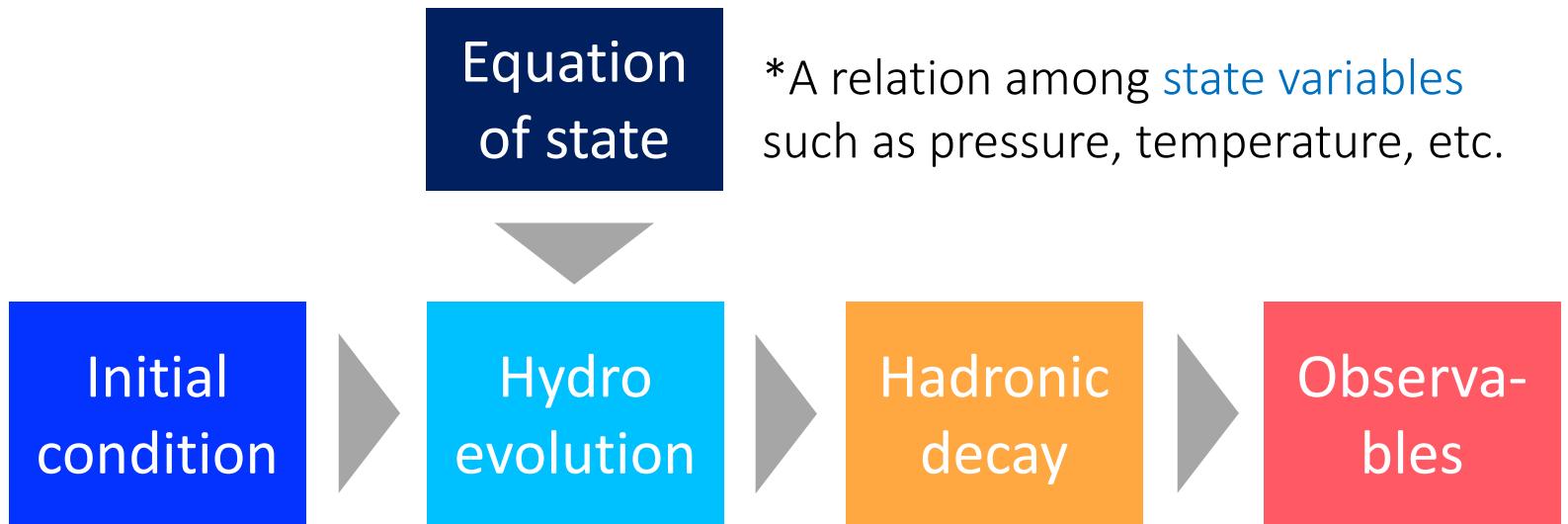
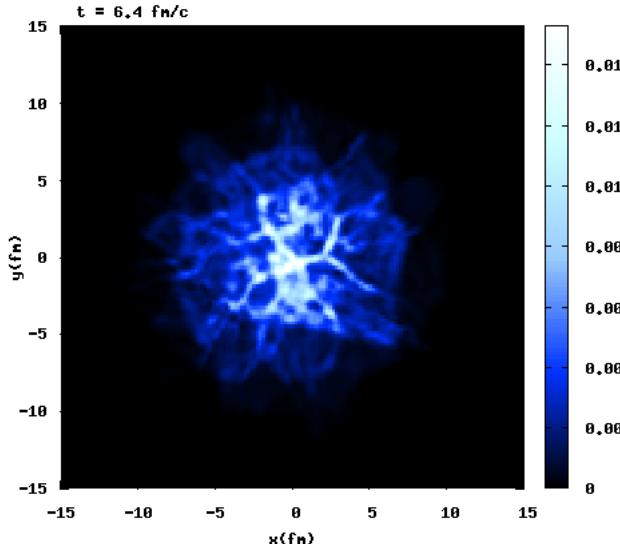
# Motivation

## ■ Relativistic hydrodynamic model



# Motivation

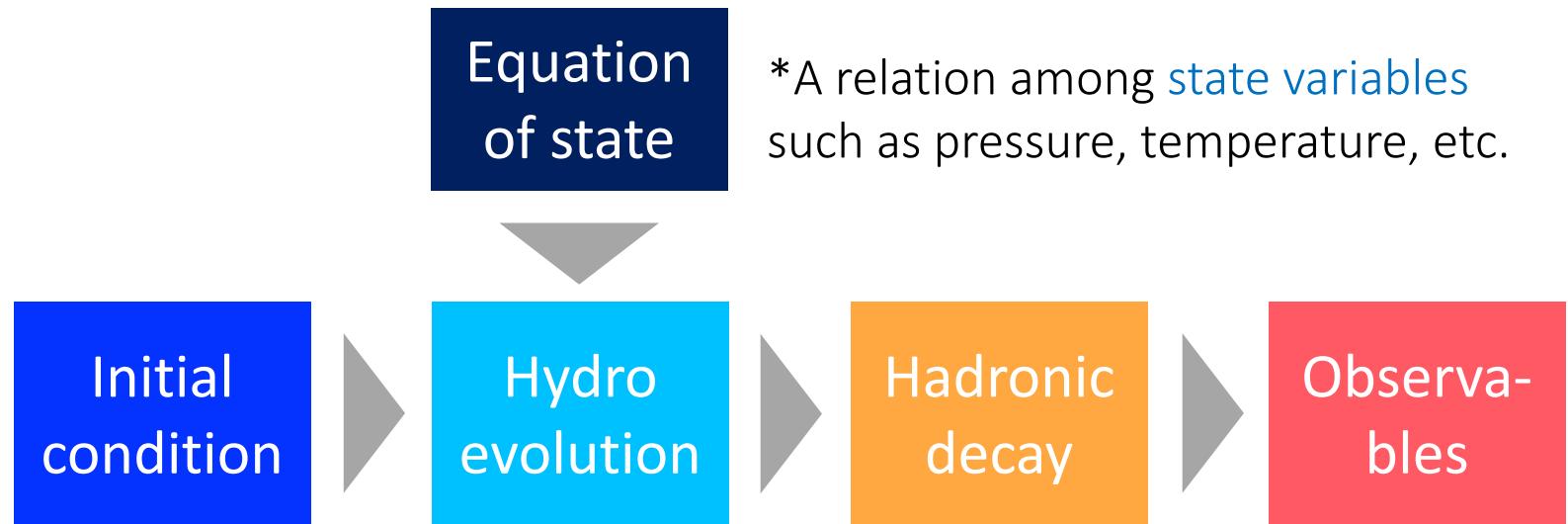
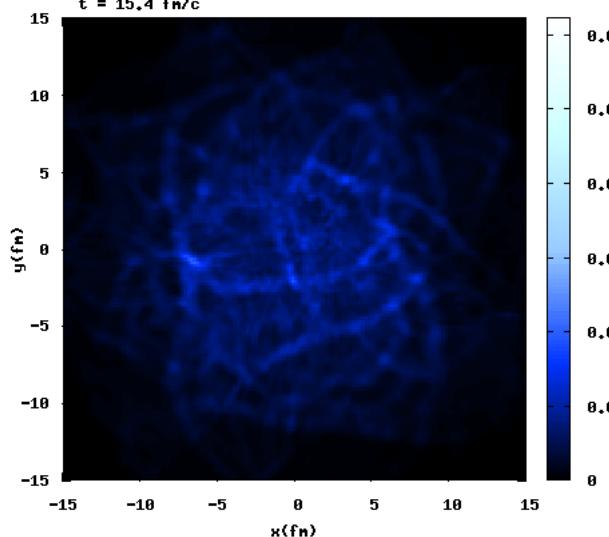
## ■ Relativistic hydrodynamic model



\*A relation among **state variables** such as pressure, temperature, etc.

# Motivation

## ■ Relativistic hydrodynamic model



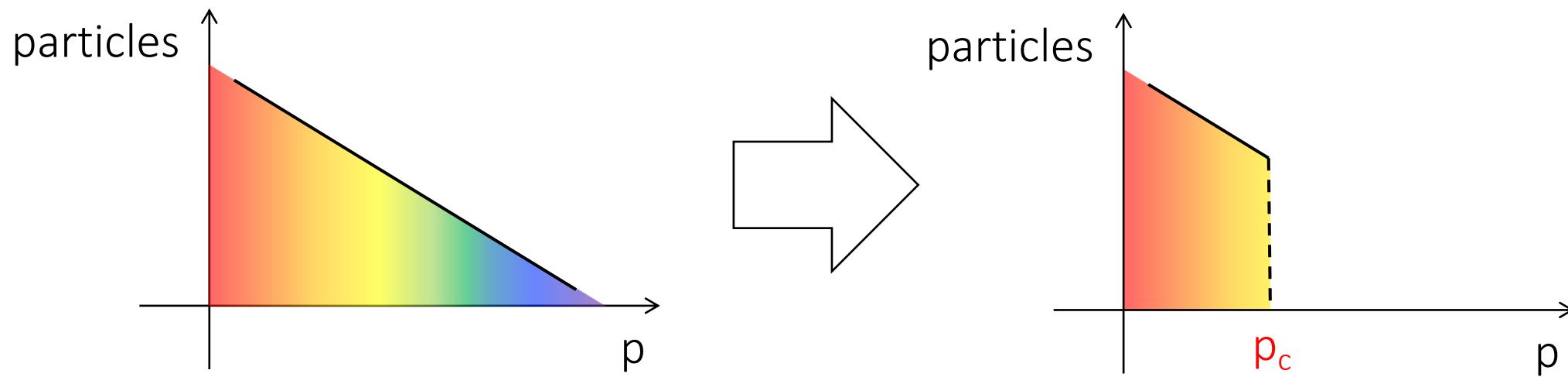
A caveat of the conventional model:  
Equation of state & particle production include the contribution  
of **high-momentum particles**



# This work

- “Red” hydrodynamic model

\*low momentum = long wavelength = “red”

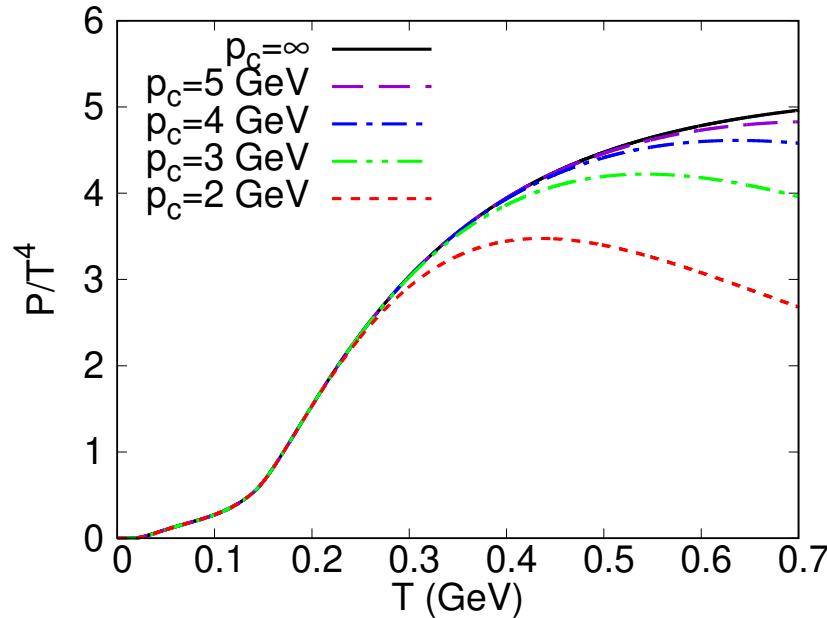


We introduce an **upper limit ( $p_c$ )** for the momenta of  
strongly-coupled components

# Equation of state

$0.1 \text{ GeV} \simeq 1.16 \times 10^{12} \text{ K}$

## ■ Results



$$\text{Pressure: } P = \pm T \sum_i \int_0^{\textcolor{red}{p_c}} \frac{g_i d^3 p}{(2\pi)^3} \ln \left[ 1 \pm \exp \left( -\frac{E_i}{T} \right) \right]$$

i: index for particle species

Hadronic phase   

QGP phase   

} Smoothly connect the  
pressures of the 2 phases

Effects of momentum cutoff is larger at higher temperatures;  
mostly negligible in the hadronic phase

# Hydrodynamic evolution

- (2+1)-dimensional inviscid model

AM, PRC 90, 021901(R) (2014)

Initial condition: Monte-Carlo Glauber model (event-averaged)

2.76 TeV Pb+Pb collisions at  $b = 4.6 \text{ fm}$  ( $\sim 0\text{-}20\%$ )

Initial time:  $\tau_{\text{ini}} = 0.4 \text{ fm/c}$

Freezeout temperature:  $T_f = 140 \text{ MeV}$

Thermal photon estimated down to:  $T_{\text{ph}} = 110 \text{ MeV}$

Hadronic decay: Sollfrank, Koch, and Heinz, Phys. Lett. B 252, 256 (1990)

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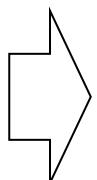
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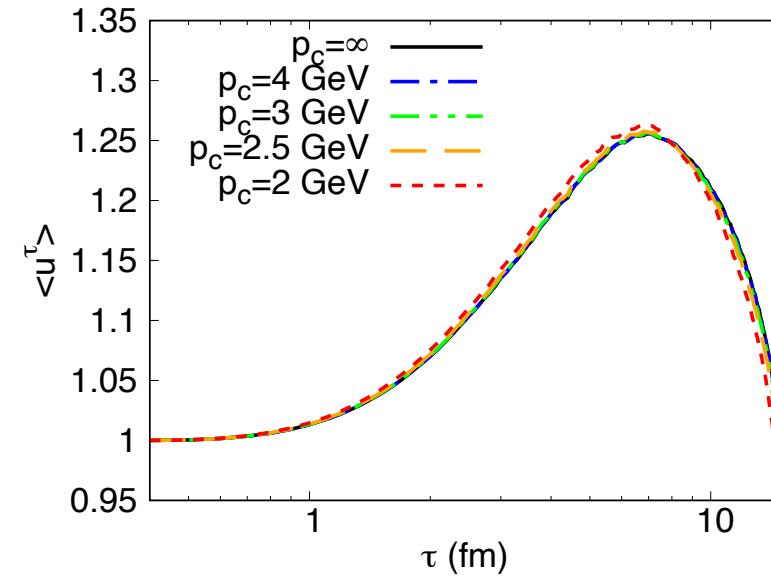
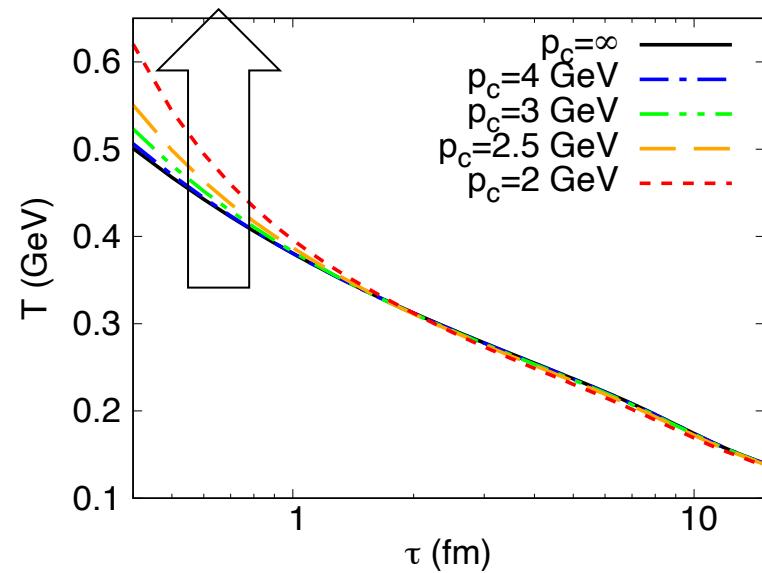
Simulations of nuclear collisions at the Large Hadron Collider



# Hydrodynamic evolution

$$1 \text{ fm}/c \simeq 3.3 \times 10^{-24} \text{ s}$$

## ■ Numerical results



Initial temperature is **higher with lower cutoff momentum**; the flow development is mostly unaffected

# Photons

Review: AM, Int. J. Mod. Phys. A 37(11n12), 2230006 (2022) 

## ■ Sources of direct photons (conventional)



# Photons

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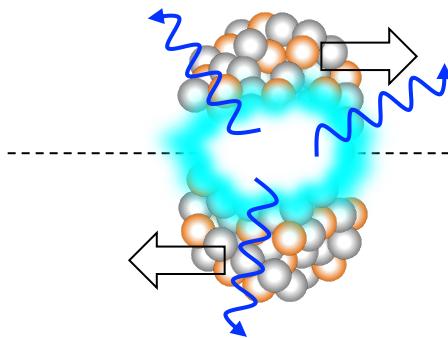
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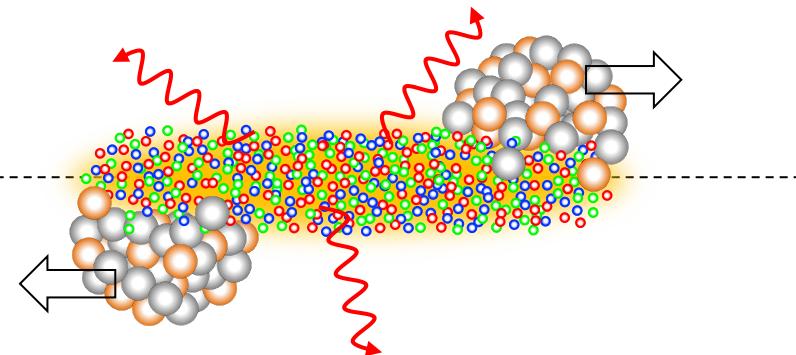
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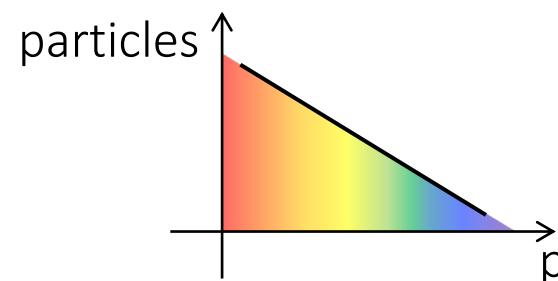


Prompt photons  
produced at the collision



Thermal photons  
produced from the medium

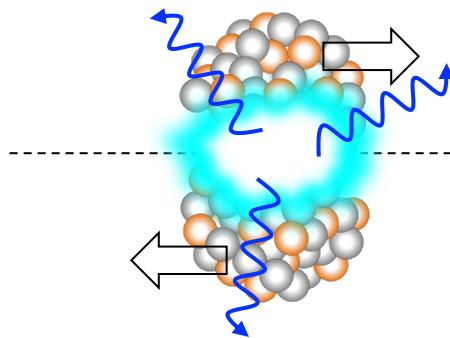
Turbide, Rapp and Gale, PRC 69, 014903  
Heffernan, Hohler, and Rapp, PRC 91, 027902  
Holt, Hohler, and Rapp, NPA 945, 1  
Berges et. al., PRC 95, 054904 (2017)  
Tanji and Venugopalan PRD 95, 094009 (2017)



# Photons

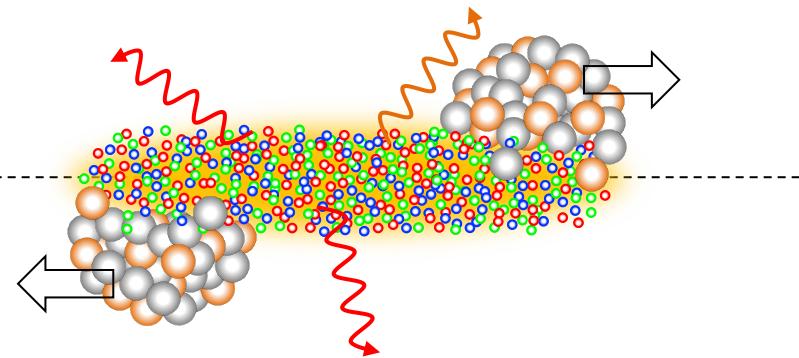
Review: AM, Int. J. Mod. Phys. A 37(11n12), 2230006 (2022) 

## ■ Sources of direct photons (this work)

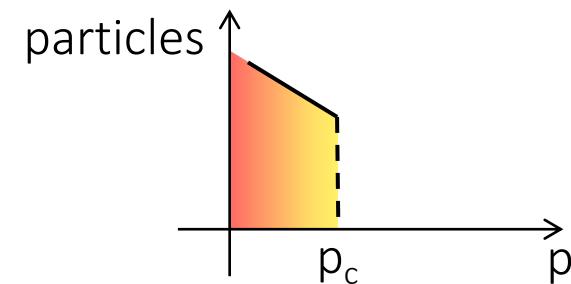


Prompt photons  
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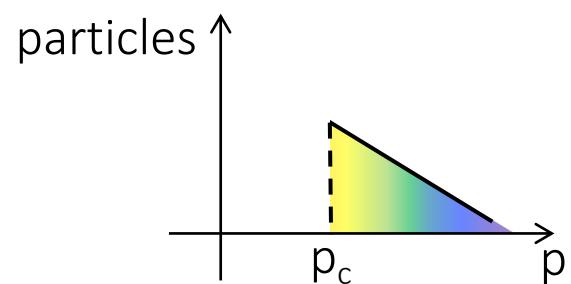
Turbide, Rapp and Gale, PRC 69, 014903  
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Berges et. al., PRC 95, 054904 (2017)  
Tanji and Venugopalan PRD 95, 094009 (2017)



Thermal photons  
produced from the medium  
(low momentum only)



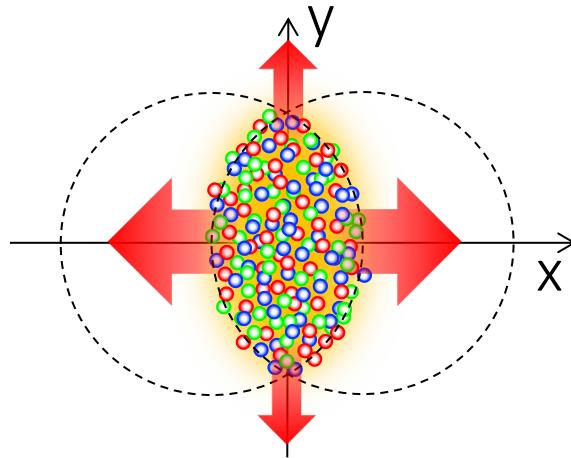
High  $p_T$  photons  
produced from the non-  
thermal components



# Elliptic flow

Ollitrault, PRD 46, 229 (1992)  
Poskanzer and Voloshin, PRC 58, 1671 (1998)

## ■ From spatial anisotropy to momentum anisotropy



Pressure gradients drive particles **faster** in the direction of the minor axis

→ The momentum distribution of hadrons has anisotropy (**elliptic flow  $v_2$** )

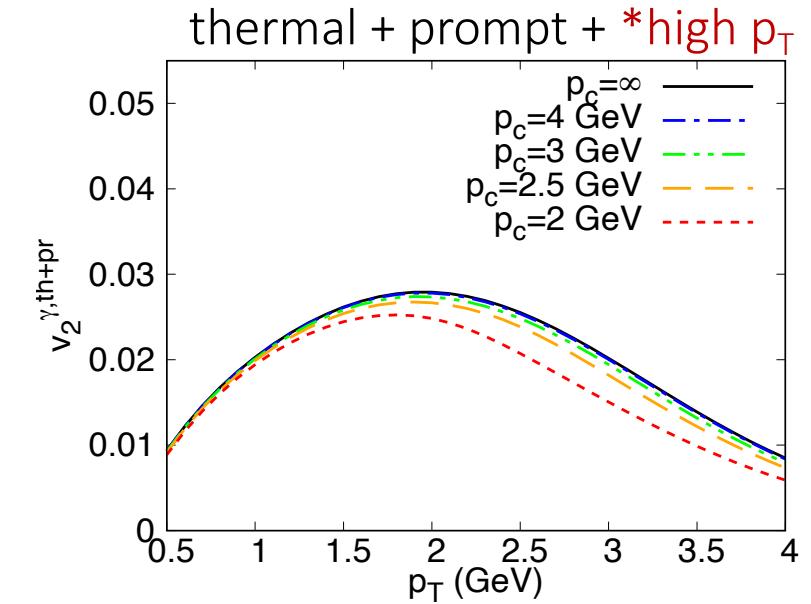
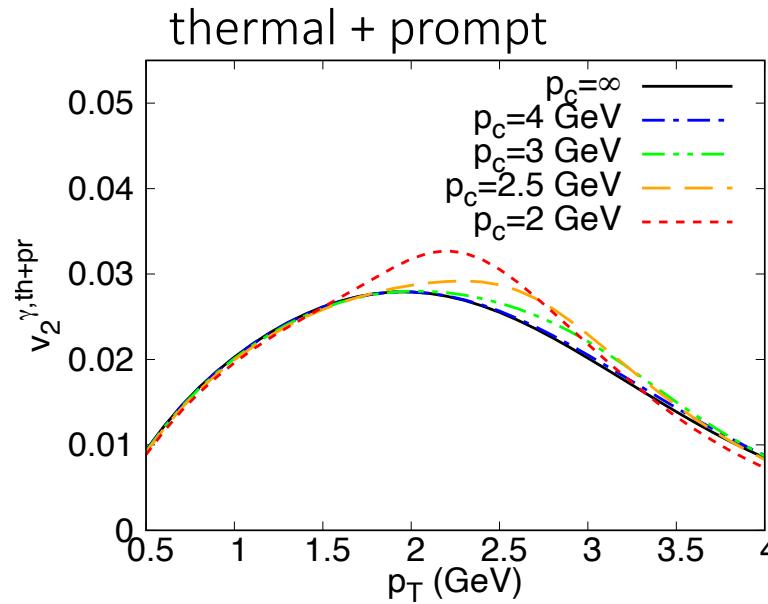
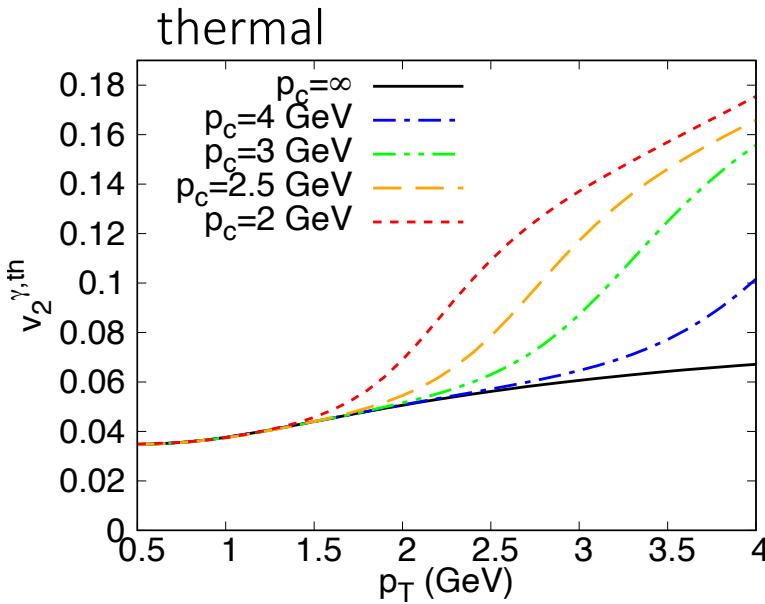
Direct photons are also **anisotropic**

Prompt photons: isotropic  
Thermal photons: **anisotropic**  
High  $p_T$  photons: isotropic

\**High  $p_T$  photons are conjectured as thermal photons with no anisotropy in this study*

# Elliptic flow

## ■ Numerical results

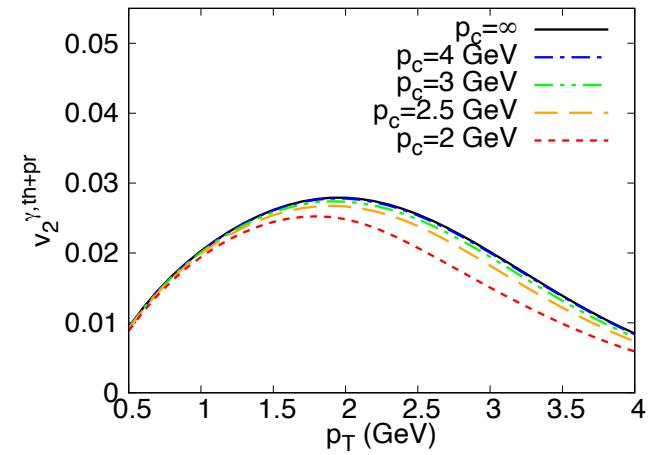
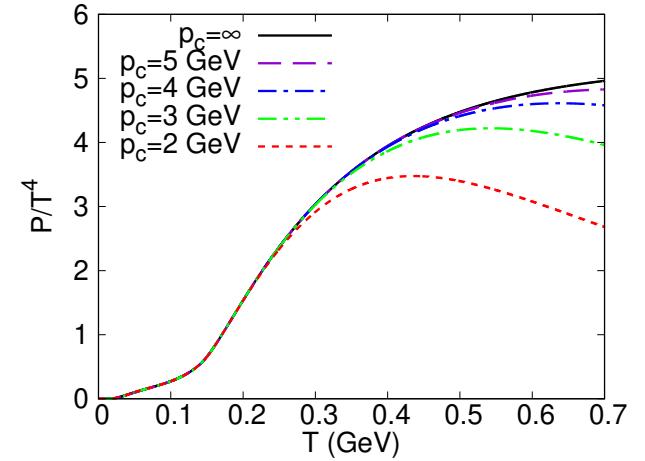


Photon  $v_2$  is **sensitive** to the choice of  $p_c$ ; whether it is enhanced or not depends on the **high  $p_T$  contributions**

# Summary

- We developed a “red” hydrodynamic model of the QGP

- ▶ Equation of state is constructed only with **low momentum components**
- ▶ High  $p_T$  photon emission is assumed to be non-thermal
- ▶ Initial temperature can be higher
- ▶ Direct photon elliptic flow can be sensitive to the cutoff momentum  $p_c$



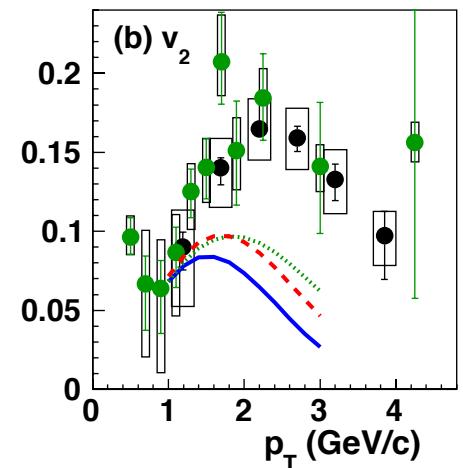
# Outlook

## ■ Future directions

- ▶ Introduction of viscous corrections (including estimation of transport coefficients)
- ▶ Event-by-event estimation for quantitative analyses of elliptic flow
- ▶ Comparison with the experimental data for understanding the *photon puzzle*\*

\*The discrepancy between the theoretical estimations and experimental data of direct photon  $v_2$

PHENIX, Phys. Rev. C 94,  
064901 (2016)



# The end

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Thank you for listening!