

Constraints on dark-matter (and galaxy structure) from strong gravitational lensing

Léon Koopmans
(Kapteyn Astronomical Institute)

The Einstein radius of the system is much larger than can be explained by stars alone for any reasonable IMF, lens or dynamical model.



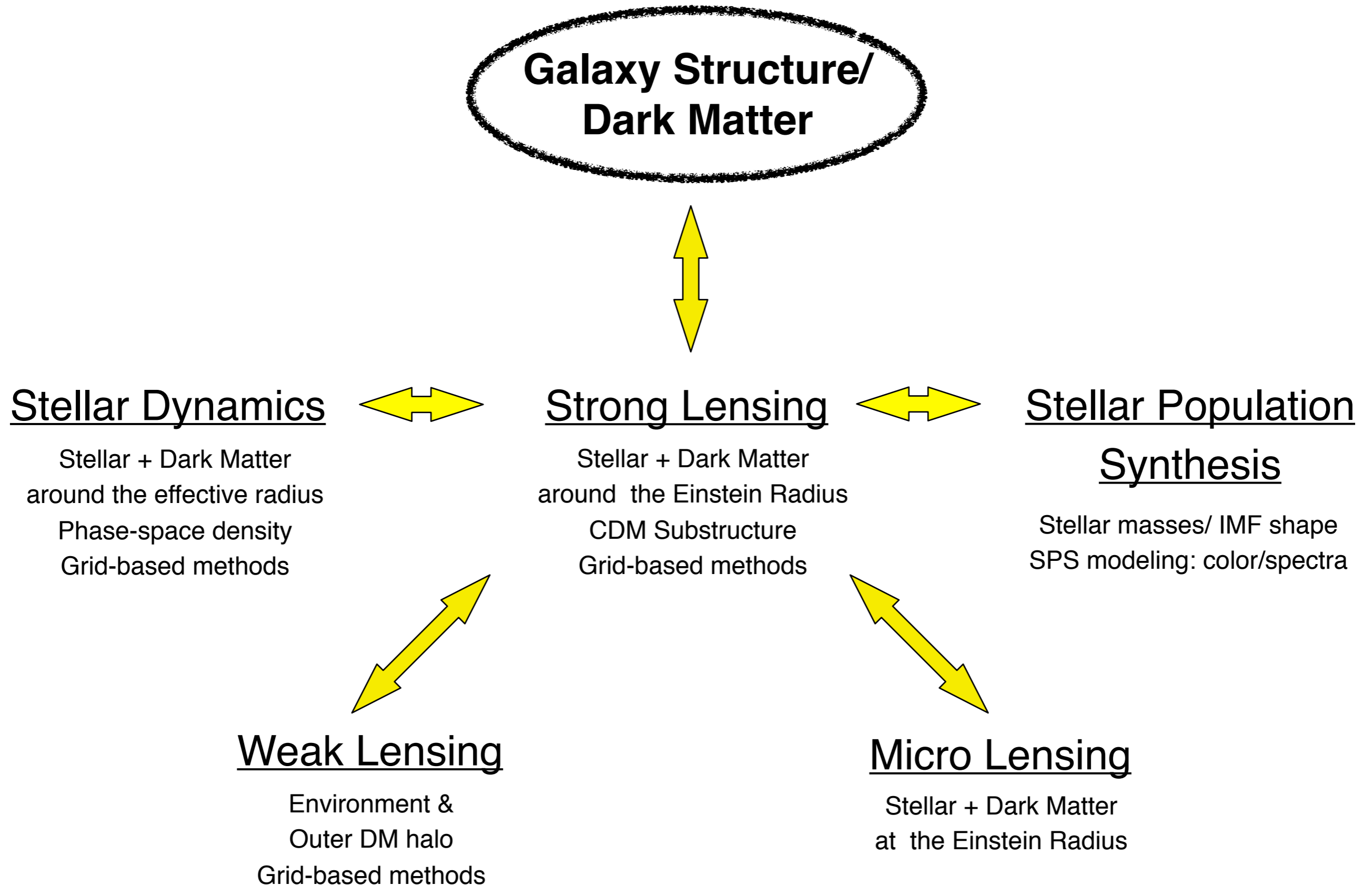
Lensed Source

Stars

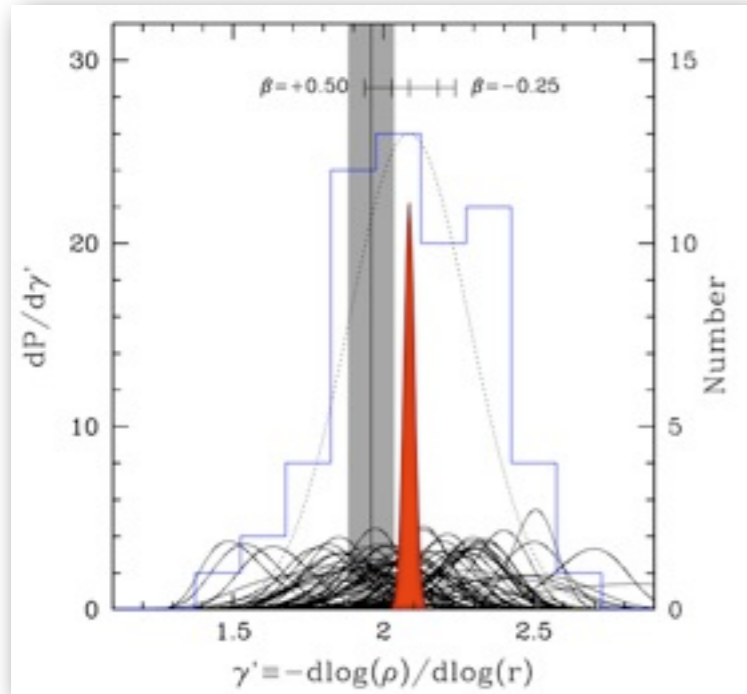
Satellites

Dark Matter

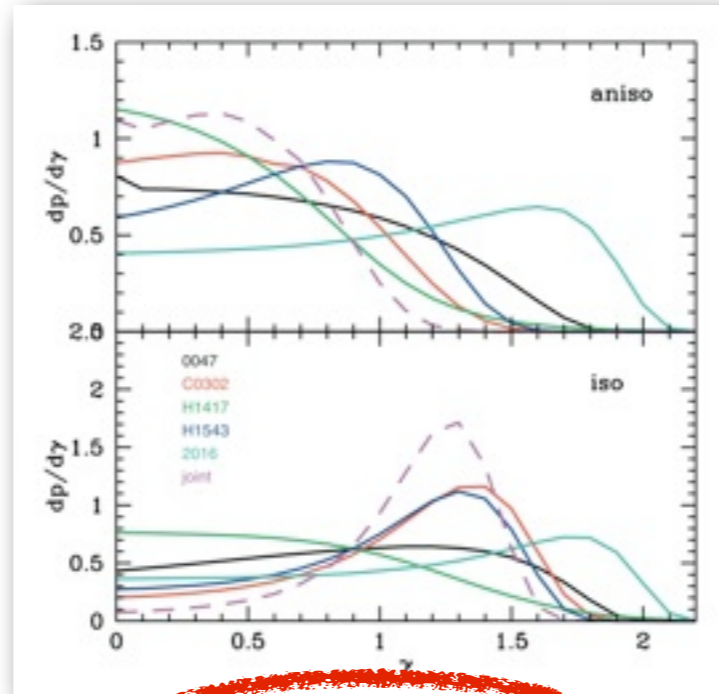
Strong Lens Galaxies: Integrated Approach



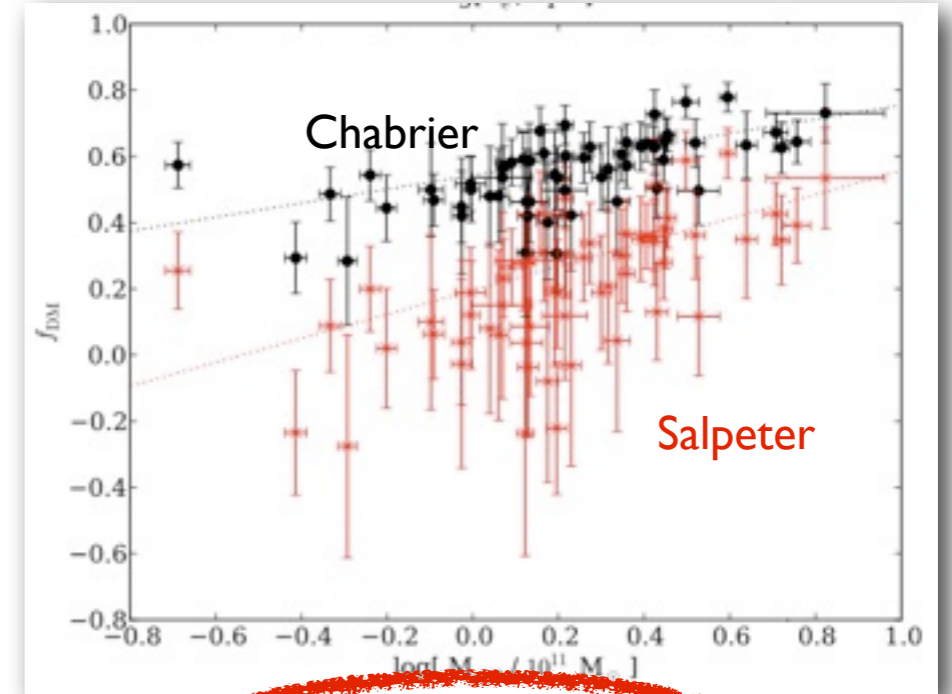
Galaxy Structure & Evolution



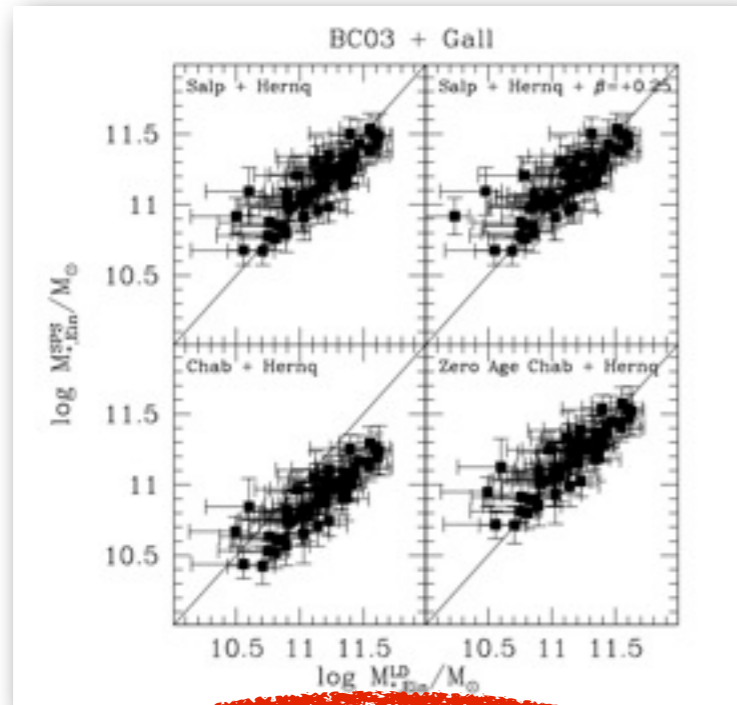
Total Density Profile



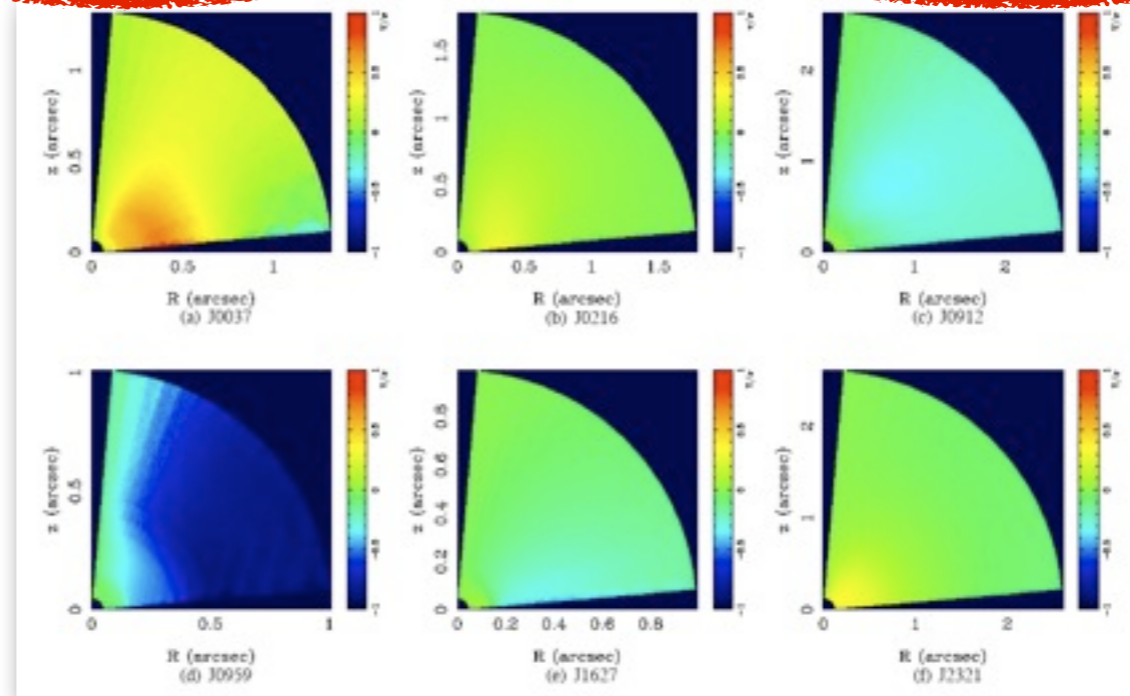
DM Density Profile



Stellar/DM Mass Fractions



Stellar IMF



Kinematic Structure

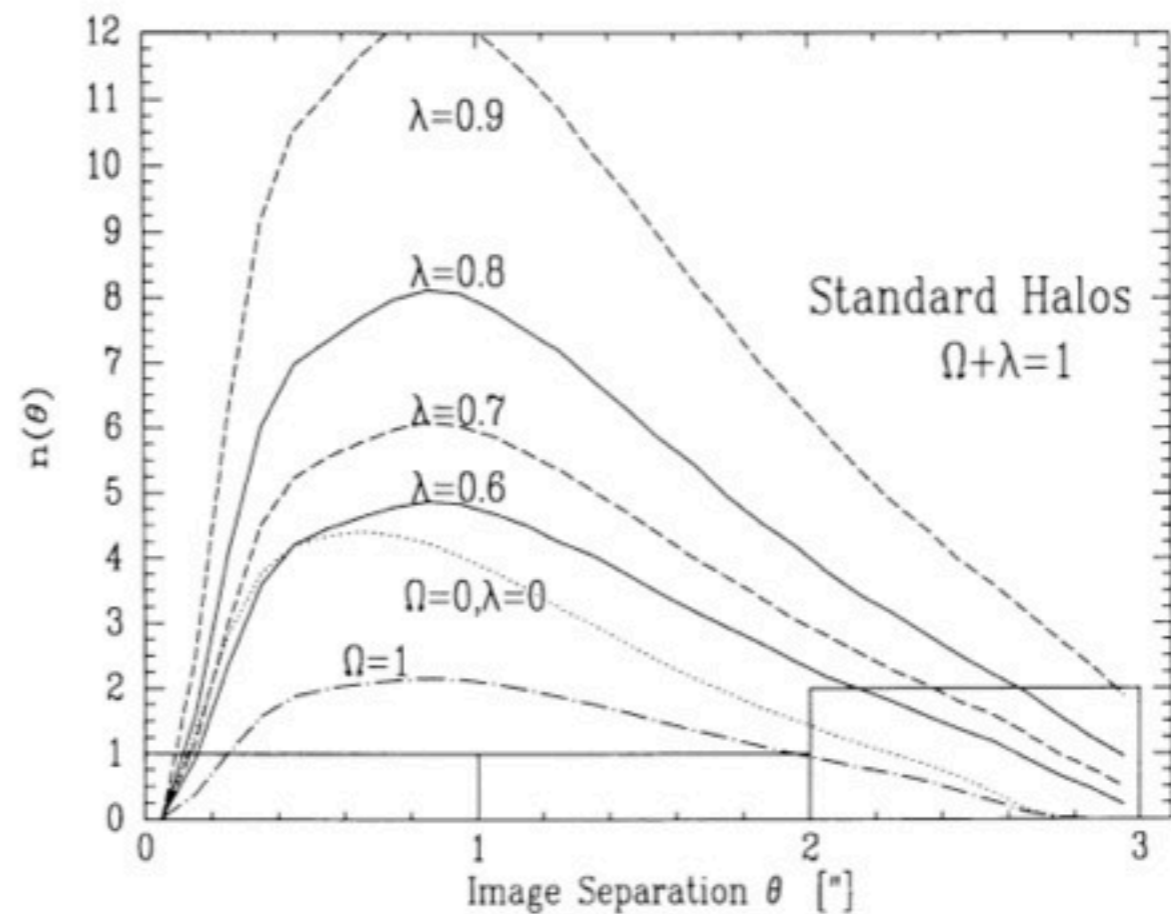
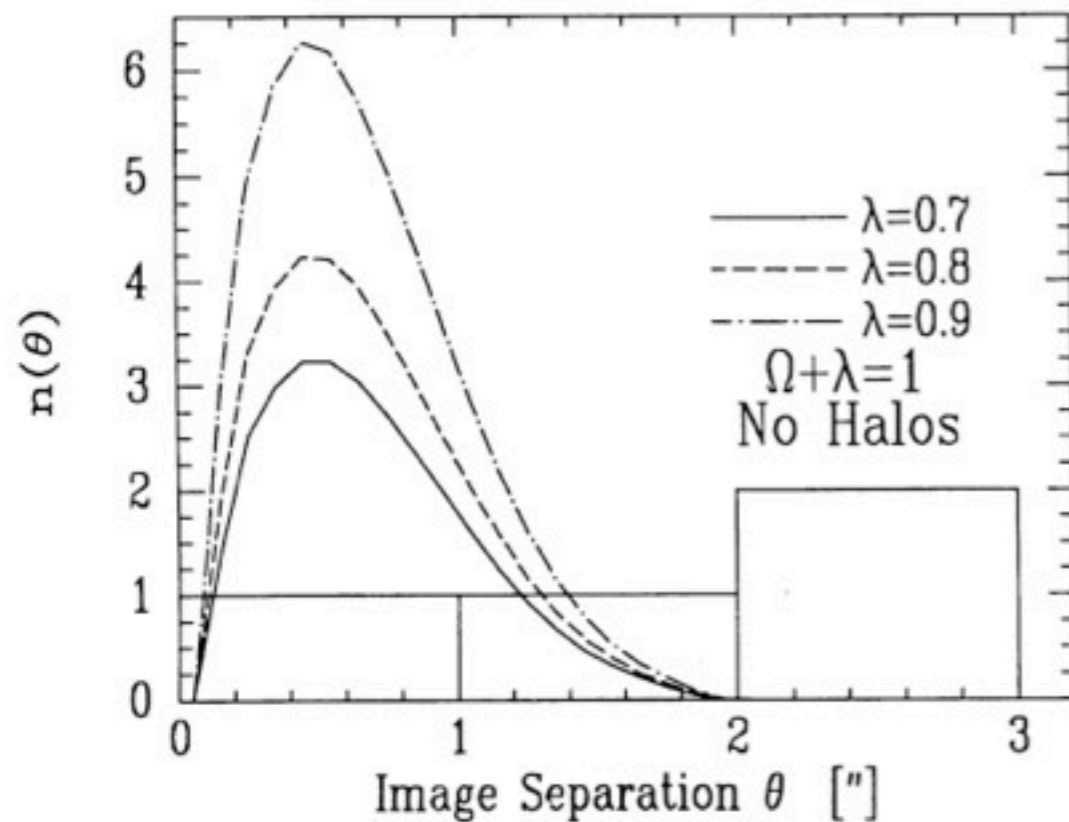
Early-type Galaxies:

Evidence Against Constant
M/L Mass Models from
Strong Lensing (+ Dynamics)

Some Early Evidence for DM in Galaxies from Strong Lensing

Observed lenses sometimes have image separations $>2''$, which should not happen in case of constant stellar M/L models (e.g. deV).

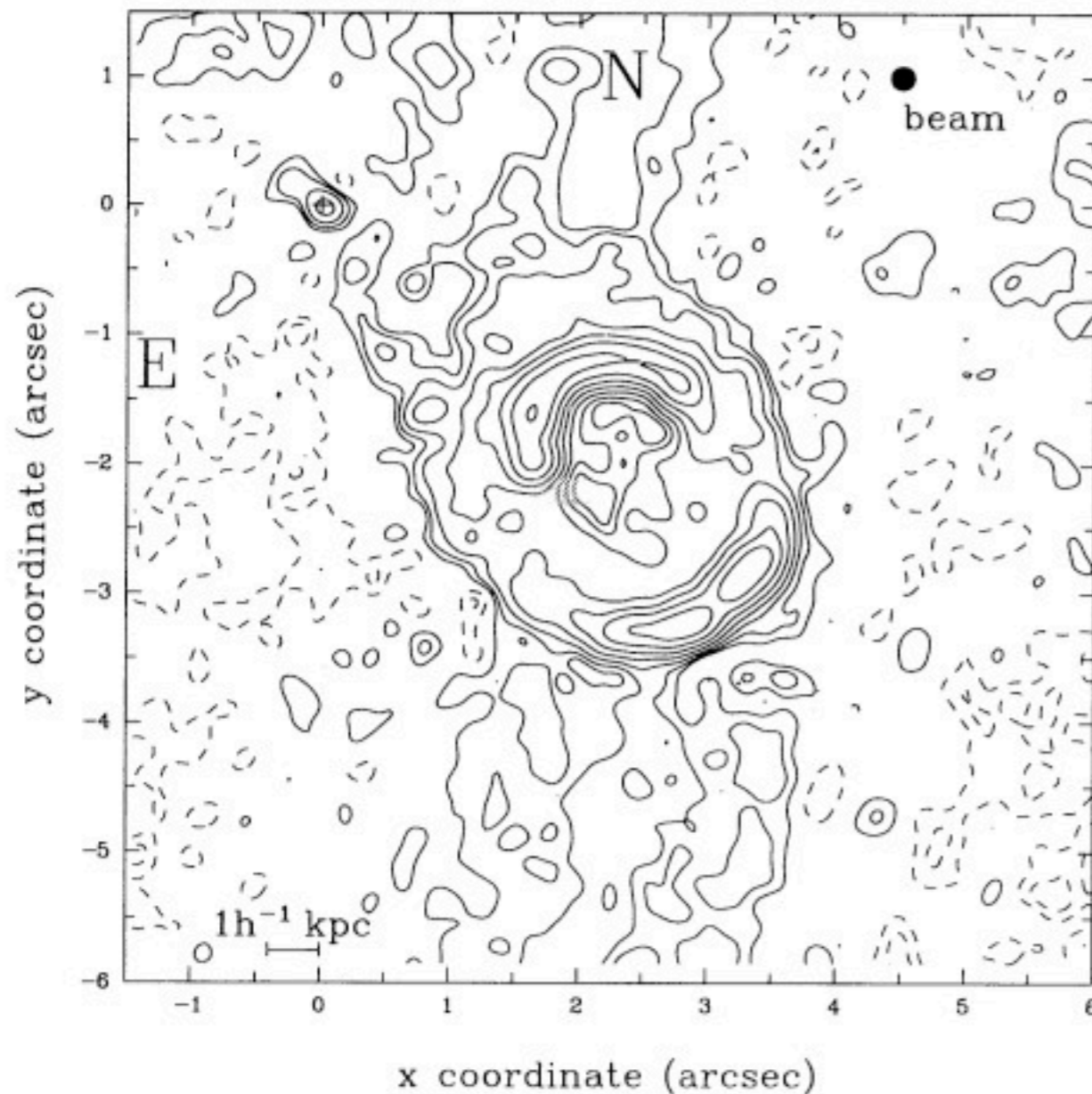
When a massive DM halo is added and $\rho \sim r^{-2}$, then lensing statistics matches observations (this is confirmed in many studies).



Maoz et al. 1993

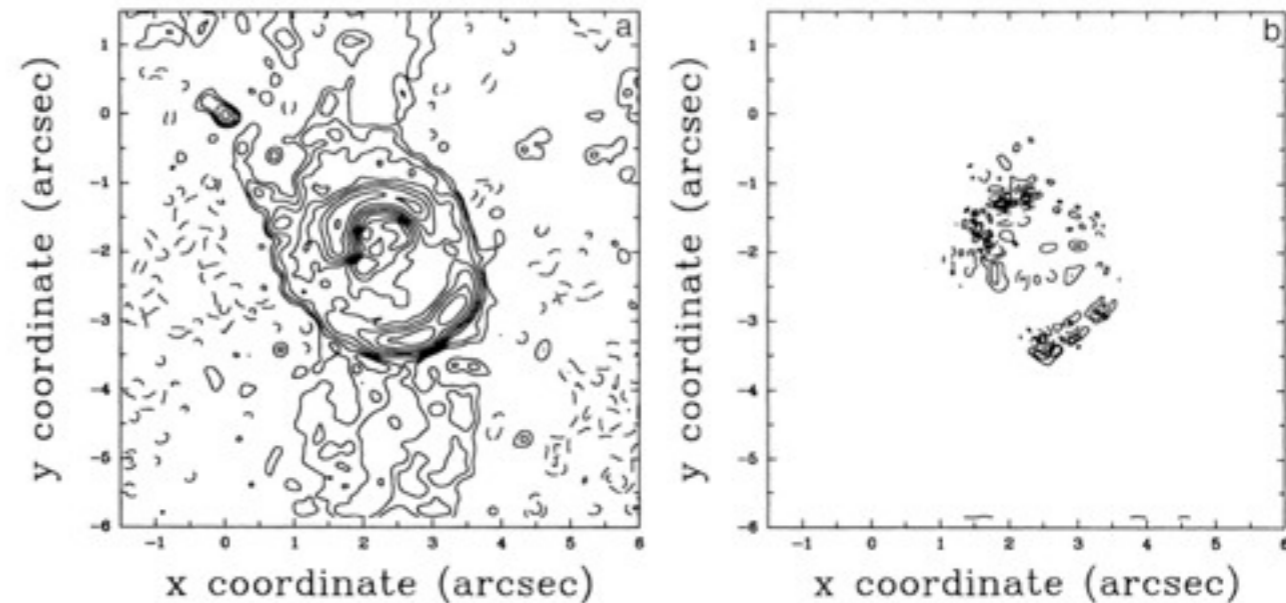
Some Early Evidence for DM in Galaxies from Strong Lensing

Data: Radio Einstein ring MG1654+134



Using LENSCLEAN one can determine a fit to the extended Einstein ring and obtain a model of the source and mass distribution

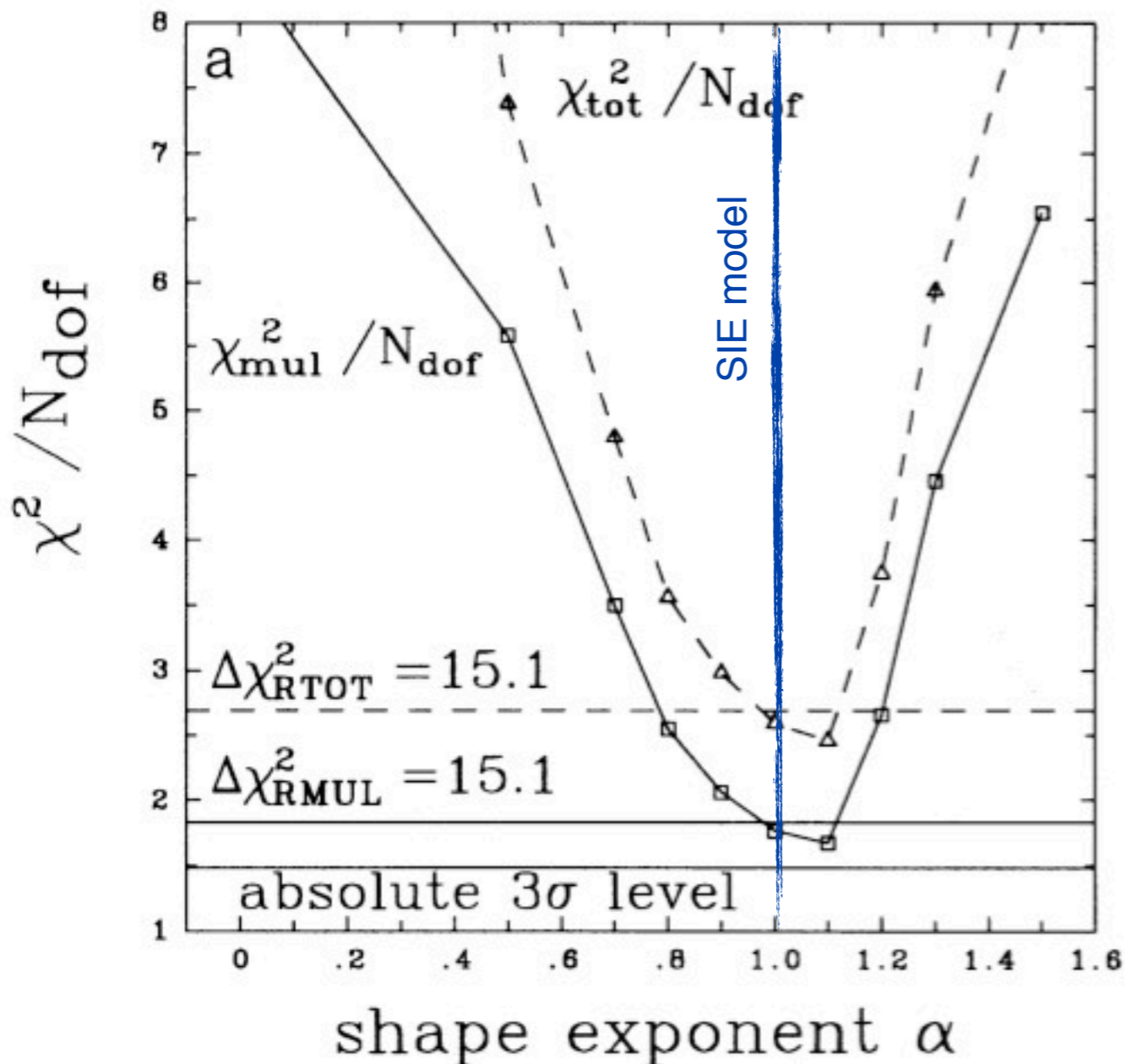
Best model with residuals



Kochanek 1995

Some Early Evidence for DM in Galaxies from Strong Lensing

$$\rho \propto (r^2 + s^2)^{(\alpha-3)/2}$$



Constant M/L models (deVaucouleurs) are only marginally consistent with data:

- (i) very large $M/L_B \sim 20$, taking passive evolution into account.
- (ii) R_{eff} exceeding observations

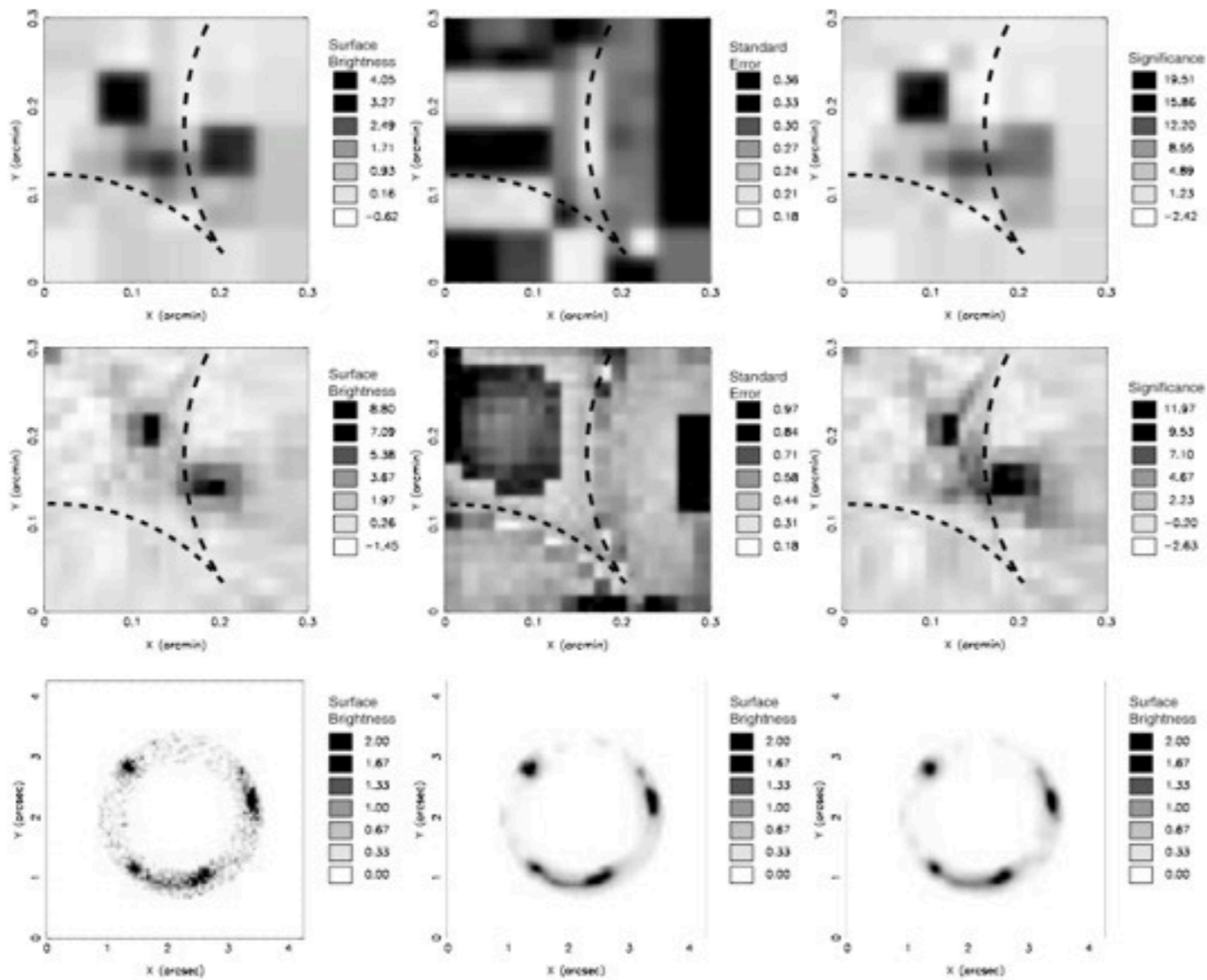
The M/L is $\sim 3x$ larger than locally observed and expected from SPS models

SIE model fits the data very well and predicted stellar dispersion matches FP.

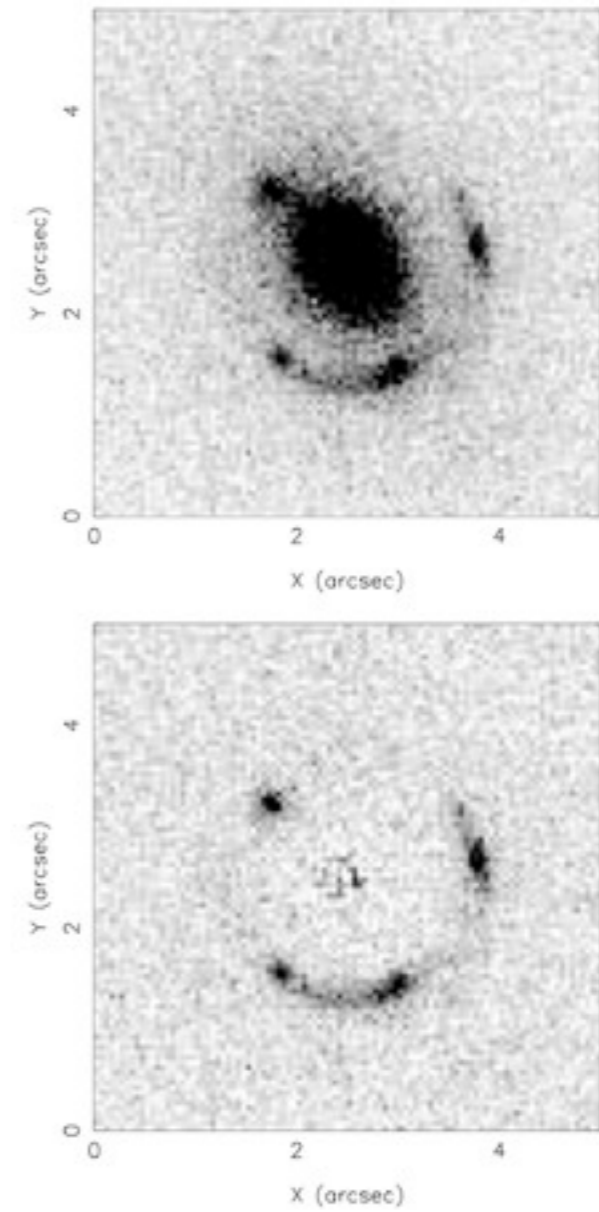
Conclusion: Constant M/L models fail to fit the data and DM is needed in this galaxy.

Two-Component Models: Stars + DM

Grid-based inversion of the lensed images makes use of all information: tight constraints on density profile



Q0047-2808

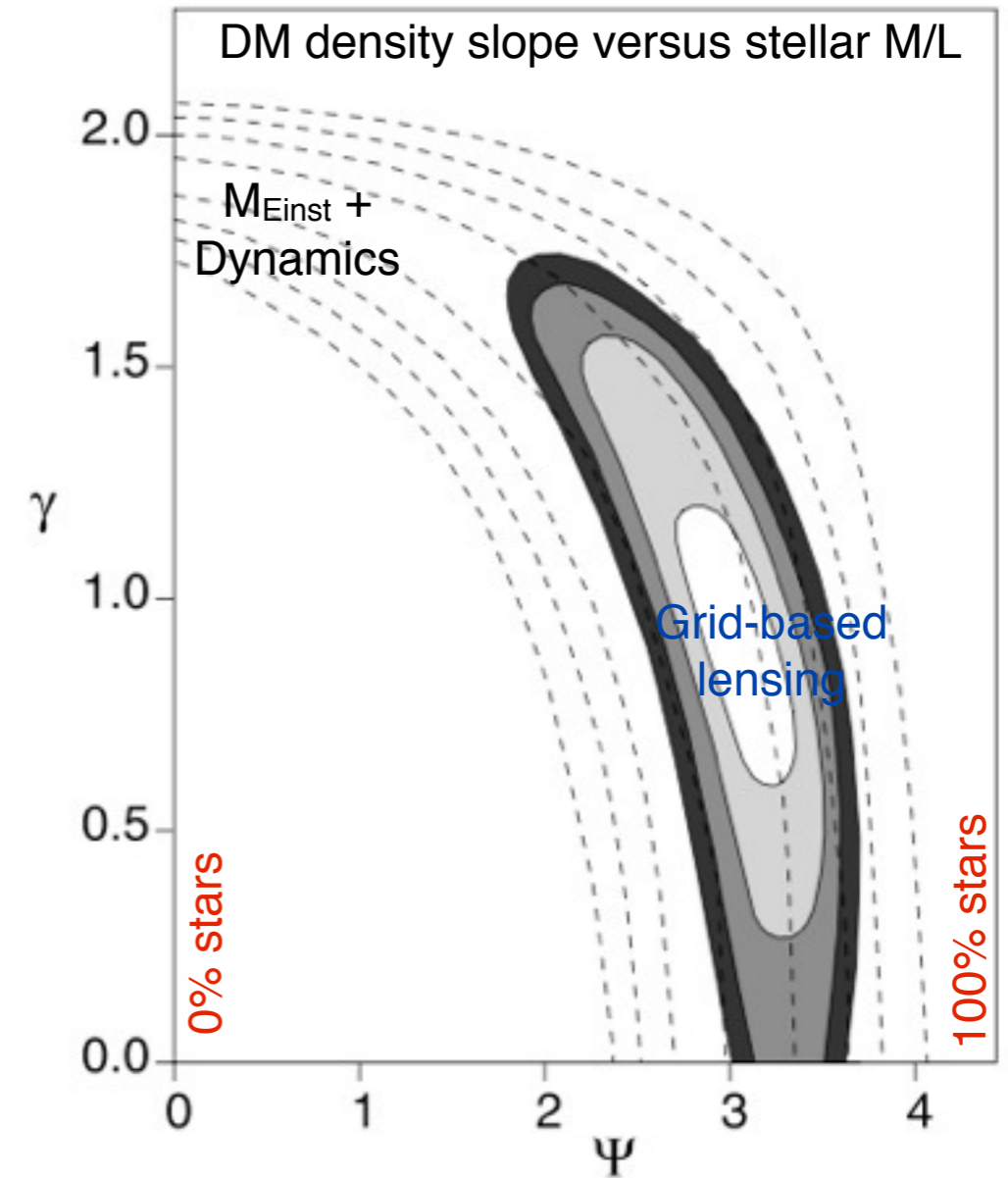
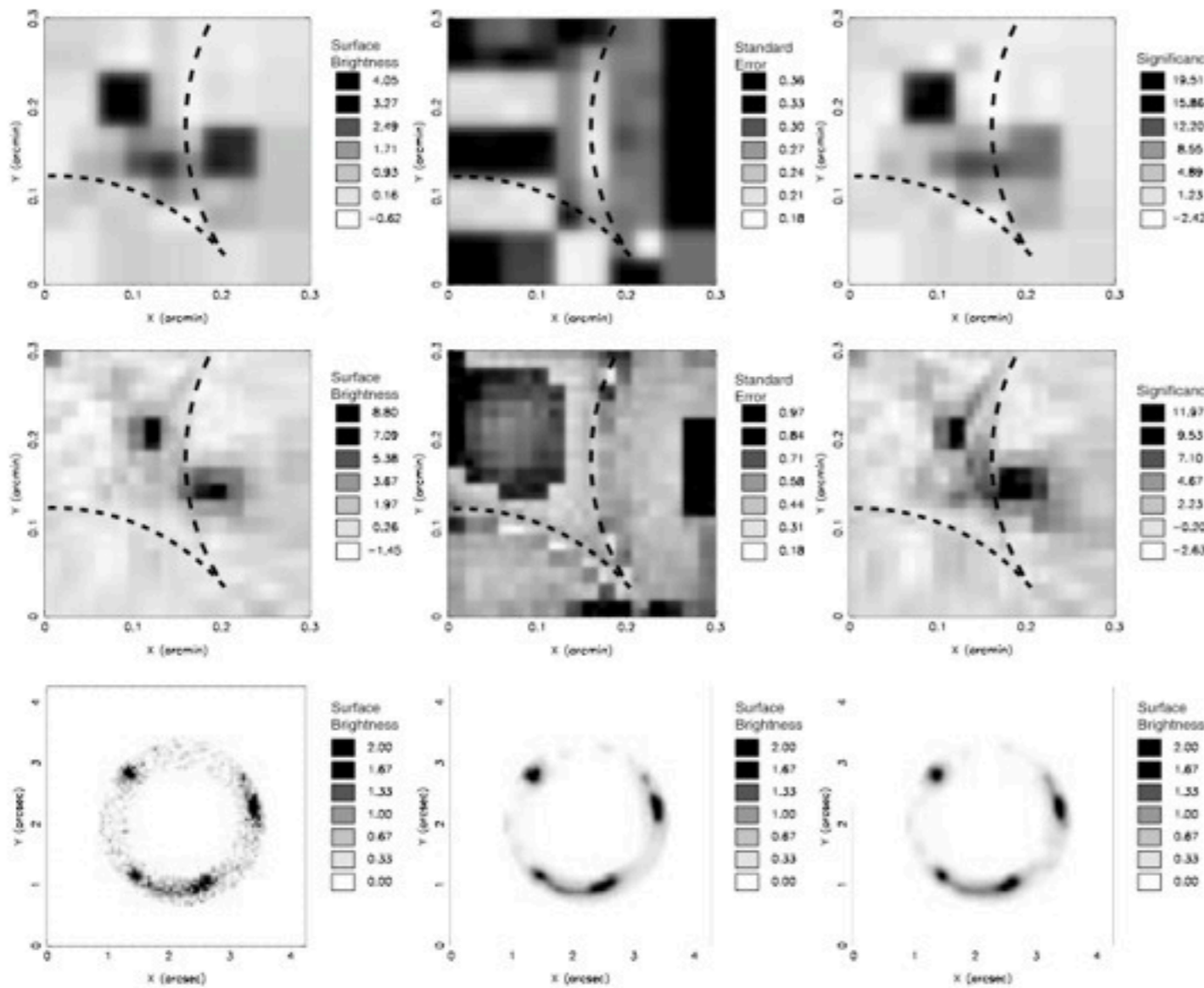


Dye & Warren 2005

Two-Component Models: Stars + DM

Grid-based inversion of the lensed images makes use of all information: tight constraints on density profile

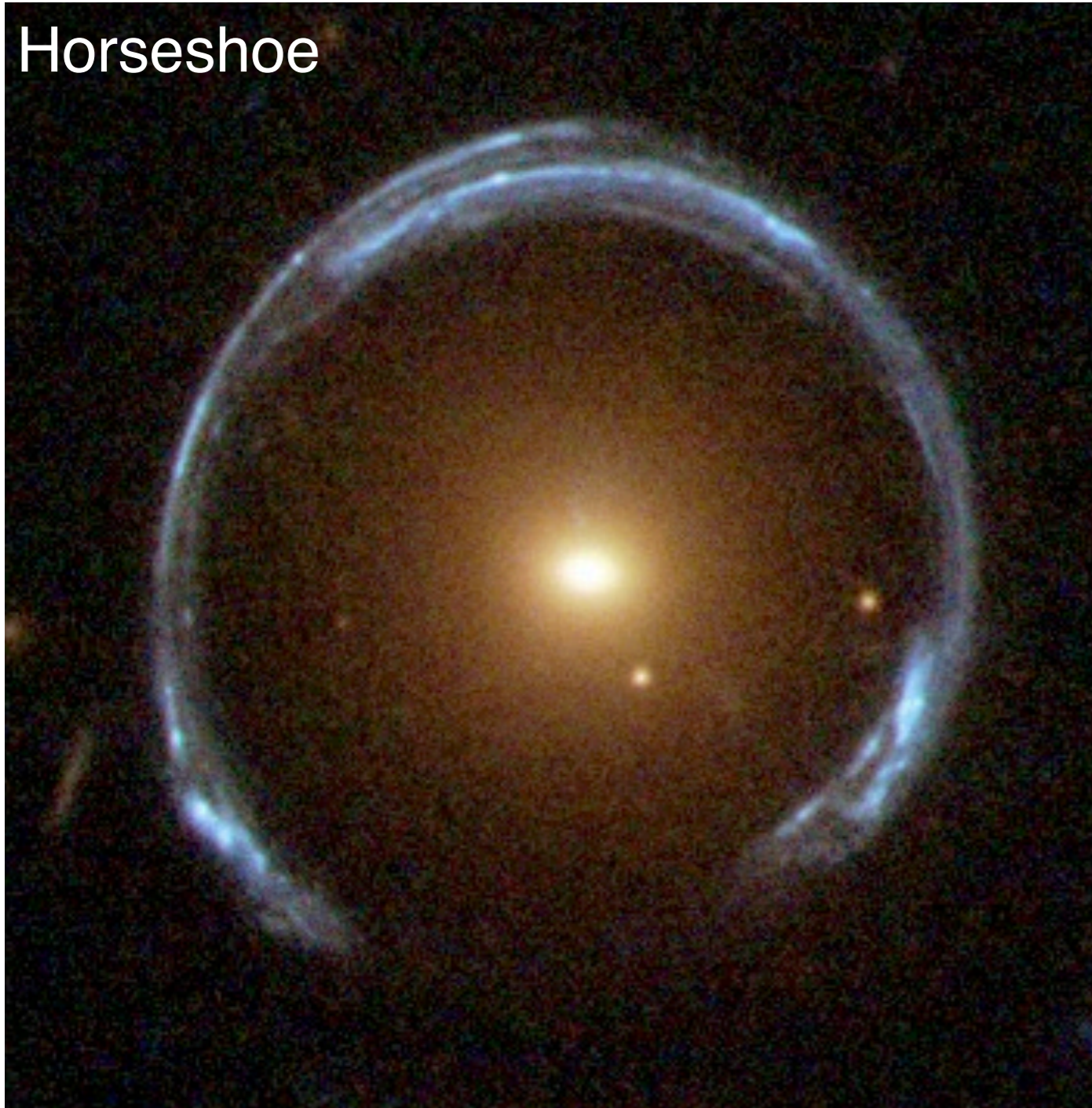
Q0047-2808



Dye & Warren 2005

Single-Component Mass Models

Horseshoe



The Horseshoe system has a very large $R_{\text{Einst}}=30$ kpc but only a single galaxy in the center suggesting an extremely massive DM halo.

Table 1. Properties of the cosmic Horseshoe¹.

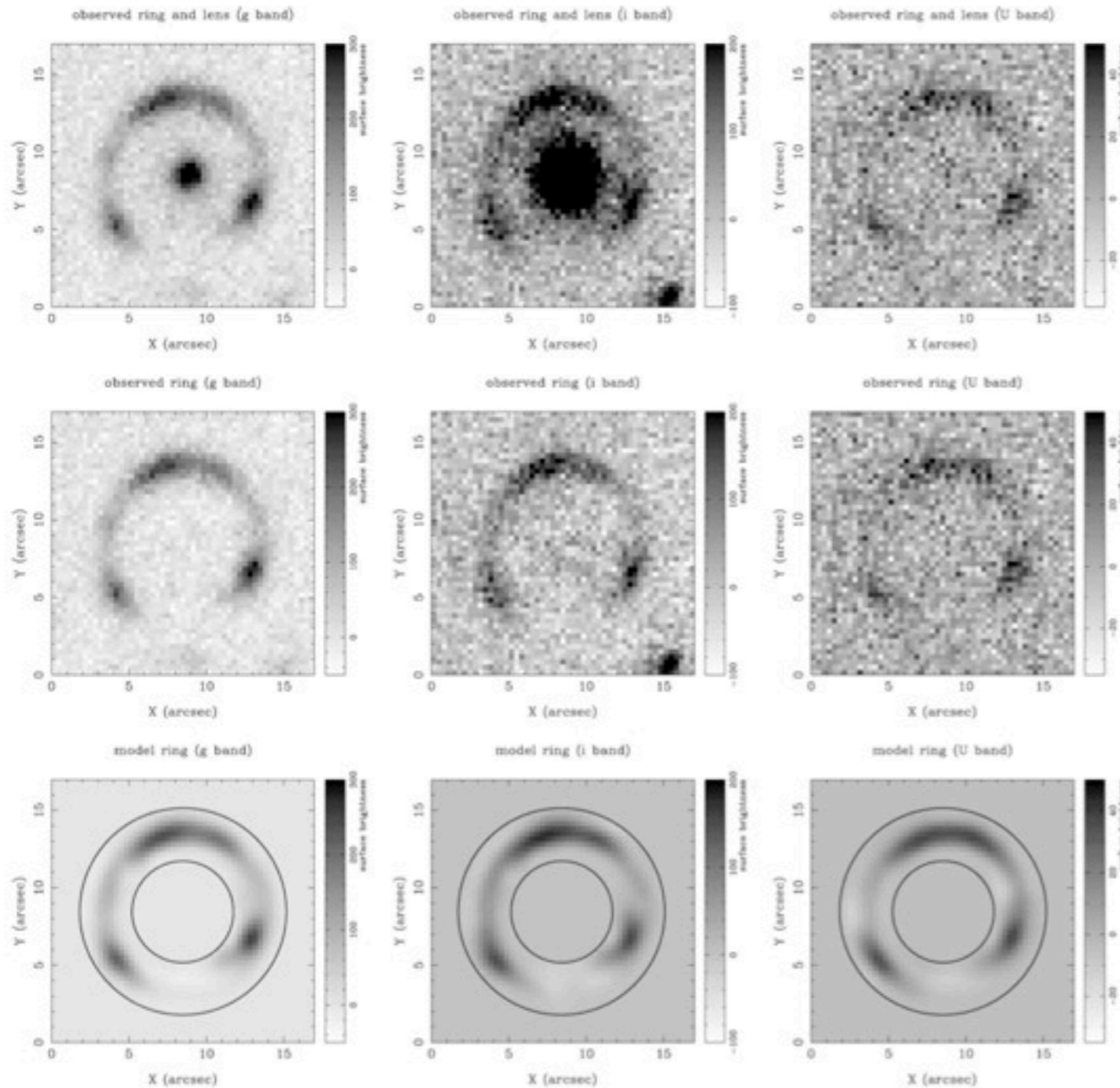
	Parameter	Values
Lens	RA	11h 48m 33.15s
	Galaxy Dec	19° 30' 03''5
	Redshift	0.444
	Effective radii	1''96 ± 0''02
	g_L	(20.84 ± 0.06) mag
	r_L	(19.00 ± 0.02) mag
	i_L	(18.22 ± 0.01) mag
	z_L	(17.75 ± 0.04) mag
	Axis ratio, g	0.8 ± 0.1
Source	Redshift ²	2.38115 ± 0.00012
	Star formation rate	~ 100 M_{\odot} yr ⁻¹
	Dynamical mass	$M_{\text{vir}} \simeq 10^{10} M_{\odot}$
Ring	Diameter	10''2
	Length	~ 300°
	u_L	21.6 mag
	g_L	20.1 mag
	i_L	19.7 mag
	Mass enclosed ³	$(5.02 \pm 0.09) \times 10^{12} M_{\odot}$

¹ Belokurov et al. (2007) measured the redshift of the source to be $z = 2.379$. We find a systematic shift that brings the source redshift to be $z = 2.3811$ in agreement with Quider et al. (2009).

² The mass within the Einstein radius or, more precisely, within the ring diameter, is taken from Dye et al. (2008).

³ Parameters obtained from images taken with the 2.5 m Isaac Newton Telescope (INT). Magnitudes are taken from SDSS DR7. See Belokurov et al. (2007)

Single-Component Mass Models



Dye et al. 2008

The Horseshoe system has a very large $R_{\text{Einst}}=30$ kpc but only a single galaxy in the center suggesting an extremely massive DM halo.

Table 1. Properties of the cosmic Horseshoe¹.

	Parameter	Values
Lens	RA	11h 48m 33.15s
	Dec	19° 30' 03''.5
Galaxy	Redshift	0.444
	Effective radii	1''.96 ± 0''.02
	g_L	(20.84 ± 0.06) mag
	r_L	(19.00 ± 0.02) mag
	i_L	(18.22 ± 0.01) mag
	z_L	(17.75 ± 0.04) mag
	Axis ratio, g	0.8 ± 0.1
	Source	Redshift ²
	Star formation rate	~ 100 $M_\odot \text{ yr}^{-1}$
	Dynamical mass	$M_{\text{vir}} \simeq 10^{10} M_\odot$
Ring	Diameter	10''.2
	Length	~ 300°
	u_L	21.6 mag
	g_L	20.1 mag
	i_L	19.7 mag
	Mass enclosed ³	$(5.02 \pm 0.09) \times 10^{12} M_\odot$

¹ Belokurov et al. (2007) measured the redshift of the source to be $z = 2.379$. We find a systematic shift that brings the source redshift to be $z = 2.3811$ in agreement with Quider et al. (2009).

² The mass within the Einstein radius or, more precisely, within the ring diameter, is taken from Dye et al. (2008).

³ Parameters obtained from images taken with the 2.5 m Isaac Newton Telescope (INT). Magnitudes are taken from SDSS DR7. See Belokurov et al. (2007)

Single-Component Mass Models

Parameter	SIE	NFW	PL
κ_0	2.50 ± 0.03	0.118 ± 0.002	2.30 ± 0.03
θ	46.5 ± 2.7	55.5 ± 3.1	49.2 ± 3.0
q	0.76 ± 0.03	0.89 ± 0.02	0.78 ± 0.03
x_c	-0.12 ± 0.04 arcsec	-0.10 ± 0.04 arcsec	-0.11 ± 0.04 arcsec
y_c	0.05 ± 0.03 arcsec	0.04 ± 0.03 arcsec	0.02 ± 0.03 arcsec
α	–	–	1.96 ± 0.02
$\ln \epsilon$	–4237.7	–4262.7	–4235.4
Param.	SIE+ γ	NFW+ γ	PL+ γ
κ_0	2.58 ± 0.03	0.116 ± 0.002	2.37 ± 0.03
θ	49.8 ± 2.7	47.9 ± 3.1	50.8 ± 3.1
q	0.81 ± 0.02	0.86 ± 0.02	0.83 ± 0.02
x_c	-0.10 ± 0.04 arcsec	-0.09 ± 0.04 arcsec	-0.11 ± 0.04 arcsec
y_c	0.03 ± 0.03 arcsec	0.04 ± 0.03 arcsec	0.04 ± 0.03 arcsec
α	–	–	1.95 ± 0.02
γ	0.017 ± 0.005	0.011 ± 0.006	0.020 ± 0.005
θ_γ	38.2 ± 9.4	46.1 ± 12.4	37.7 ± 8.6
$\ln \epsilon$	–4239.0	–4272.0	–4240.2

Different models can be compared via the Bayesian Evidence:

$$\mathcal{E} \approx \mathcal{L}_{\max} \times \frac{V_{\text{post}}}{V_{\text{prior}}}$$

i.e. the marginalization over all model-parameters of the posterior PDF: Probability of the data, given the model-family

Residuals: SIE

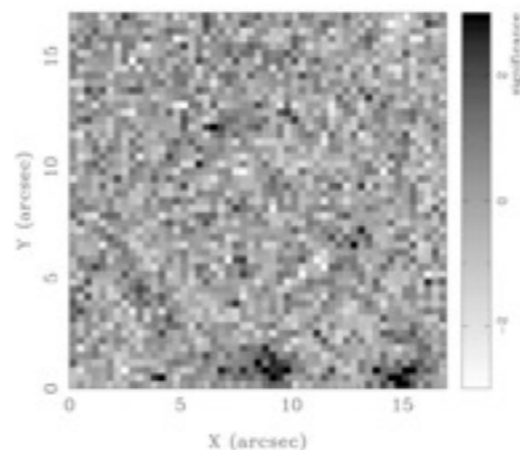
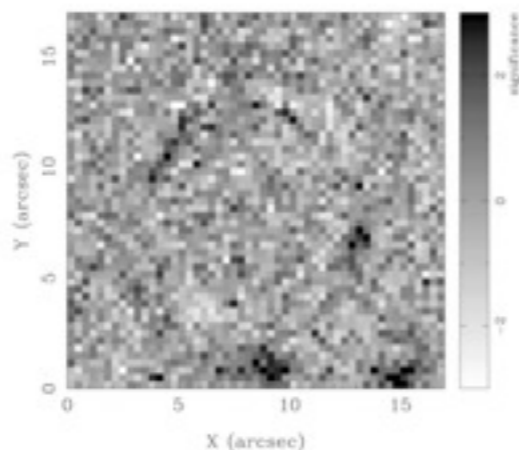
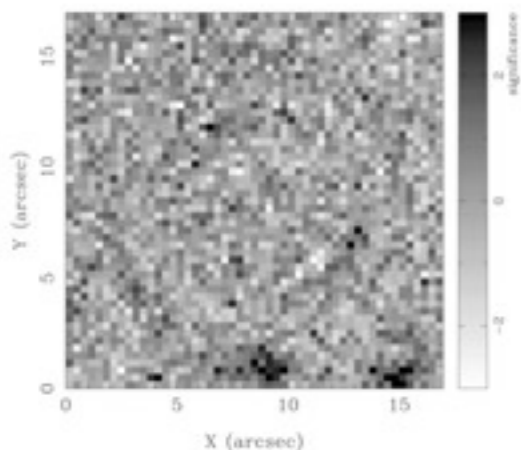
NFW

Power-law

SIE: significance of residuals (g band)

NFW: significance of residuals (g band)

PL: significance of residuals (g band)

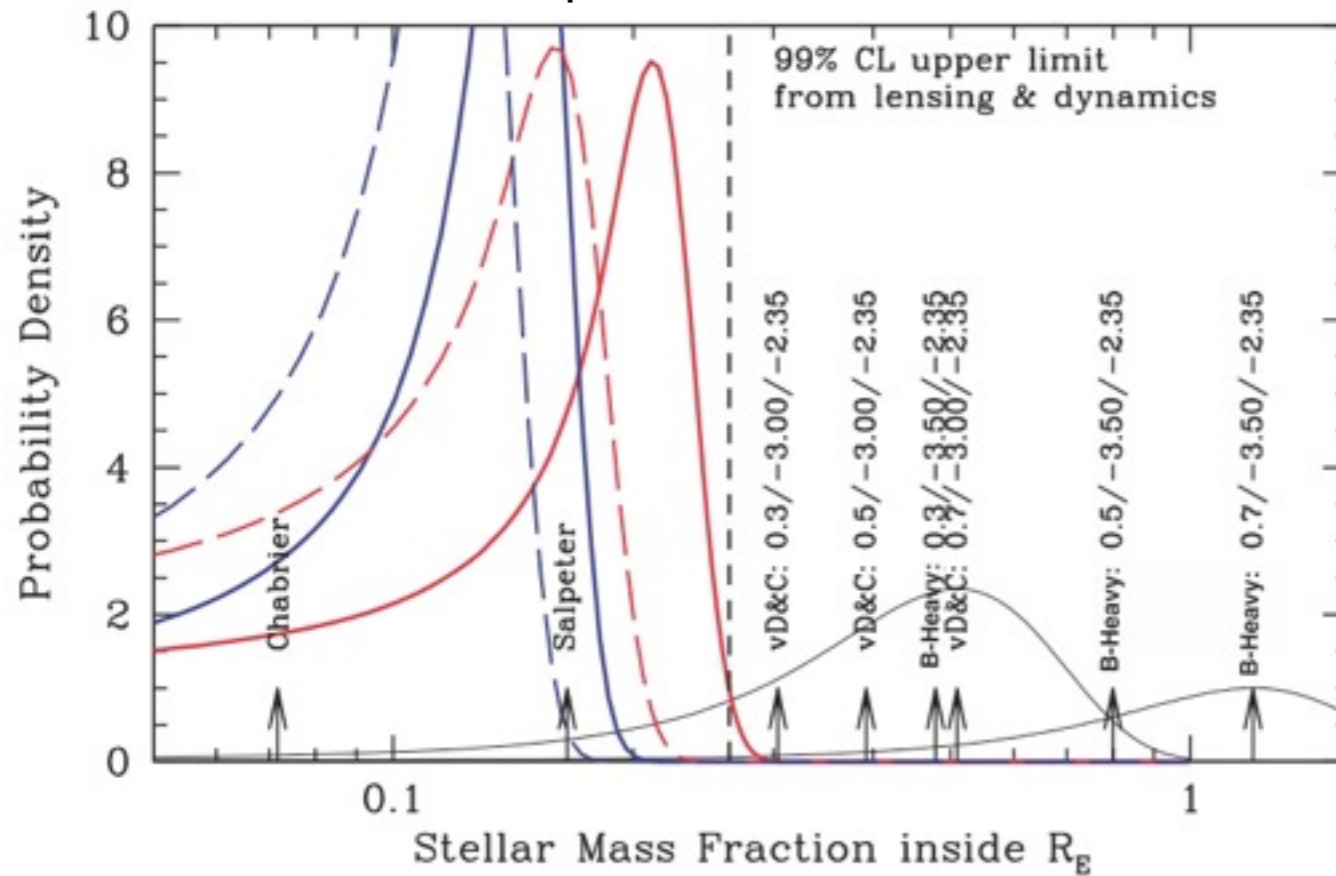


Dye et al. 2008

A SIE/PL model leaves nearly no residuals and has an evidence exceeding that of the NFW model [this is a massive group-like system]

Two-Component L&D Mass Models

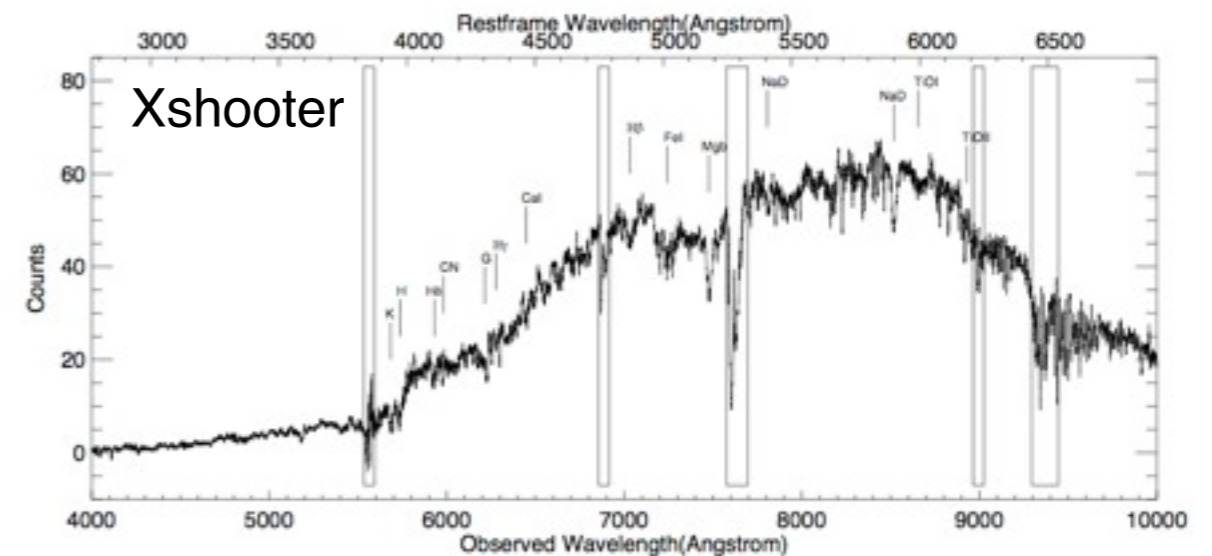
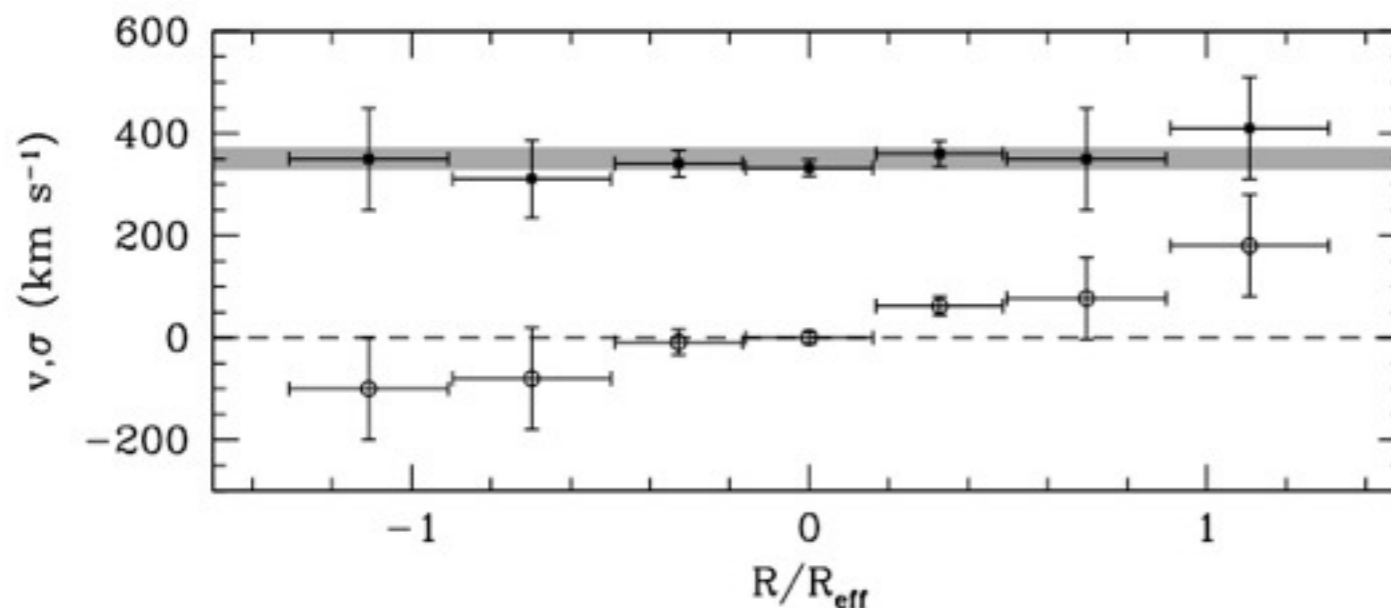
Spiniello et al 2011



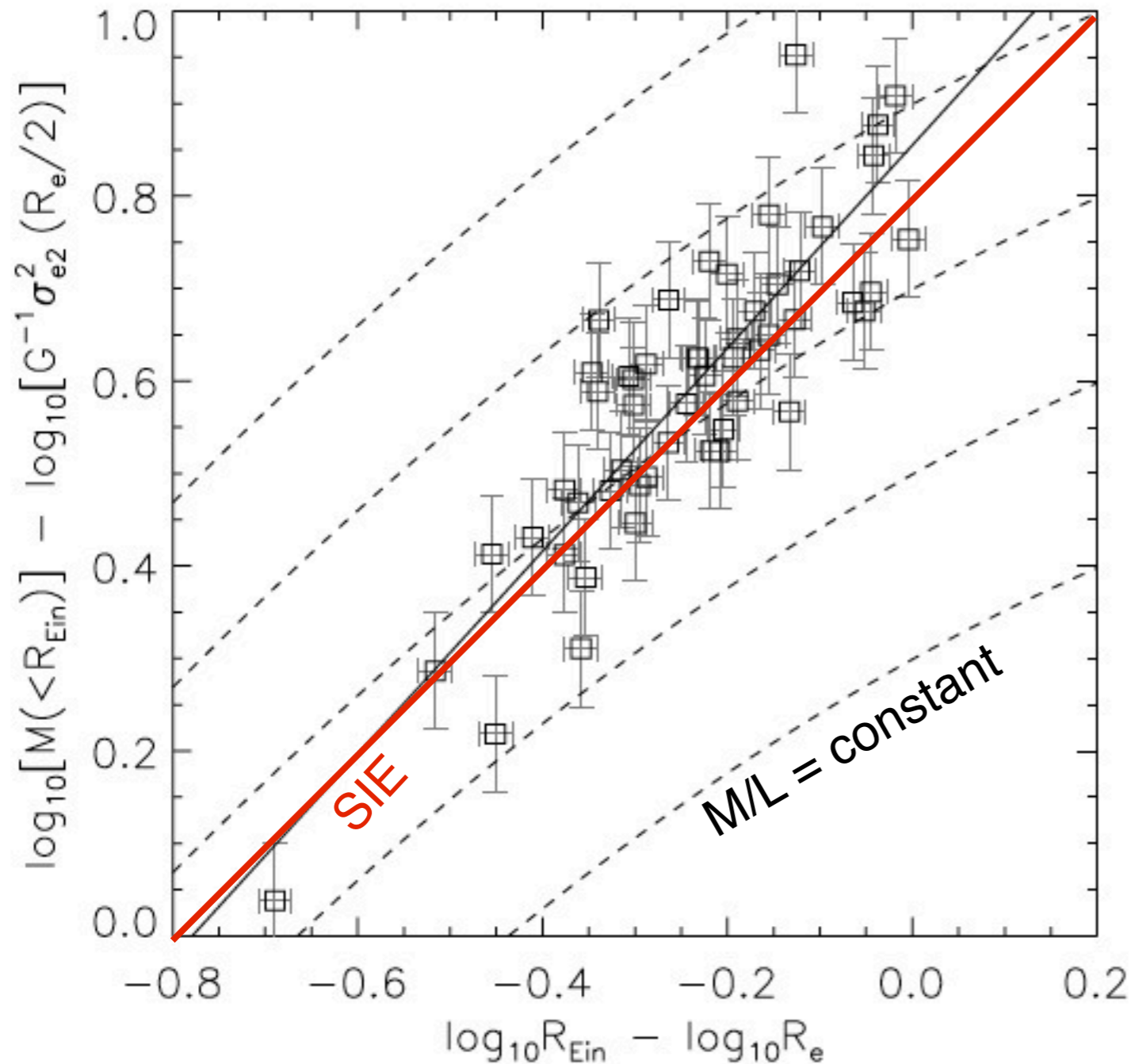
When the mass inside R_{inst} is combined with an extended kinematic profile, only a small subset of models still fits the data.

For a Hernquist ($\beta=0$) stellar component embedded in a gNFW DM halo, the posterior PDF for M_{star} gives:

$$f_{\text{DM}}(\hat{< R}_{\text{eff}}) = 0.60^{+0.15}_{-0.06} \pm 0.1$$



Scaling Relations versus Constant Stellar M/L Models



Under homology conditions, one can rescale (i) $R_{\text{Einst}}/R_{\text{eff}}$ and (ii) $M_{\text{Einst}}/(\sigma^2 R_{\text{eff}})$.

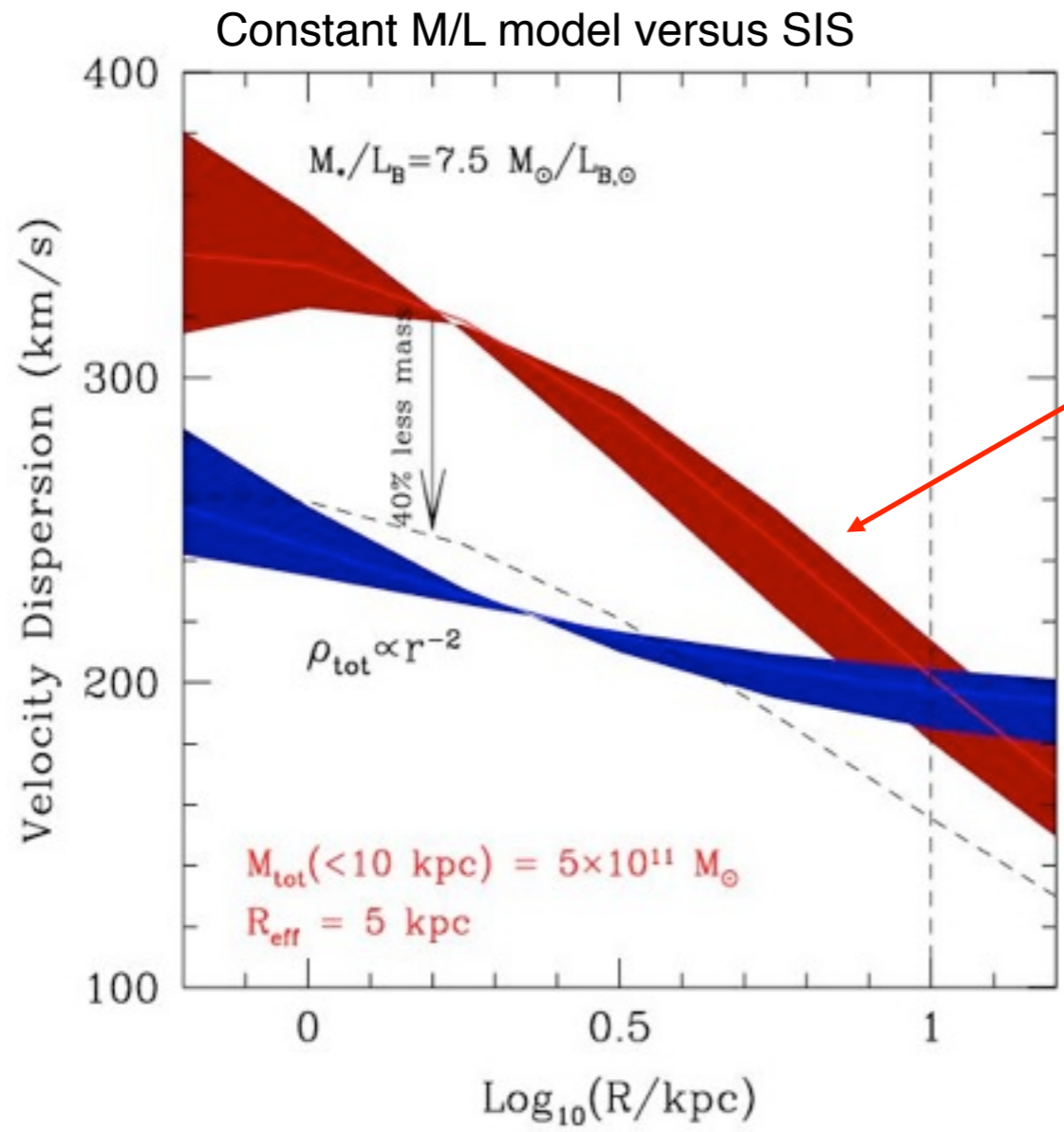
One finds that lenses follow a power-law density distribution.

Constant M/L models can be excluded at >99.9% CL and $\langle f_{\text{DM}} \rangle = 0.38 \pm 0.07$ (68%) inside R_{eff} .

Bolton et al. 2008; also Koopmans et al. 2009

DM Density Slopes inside $R_{\text{Einst/eff}}$

Combination with Stellar Dynamics



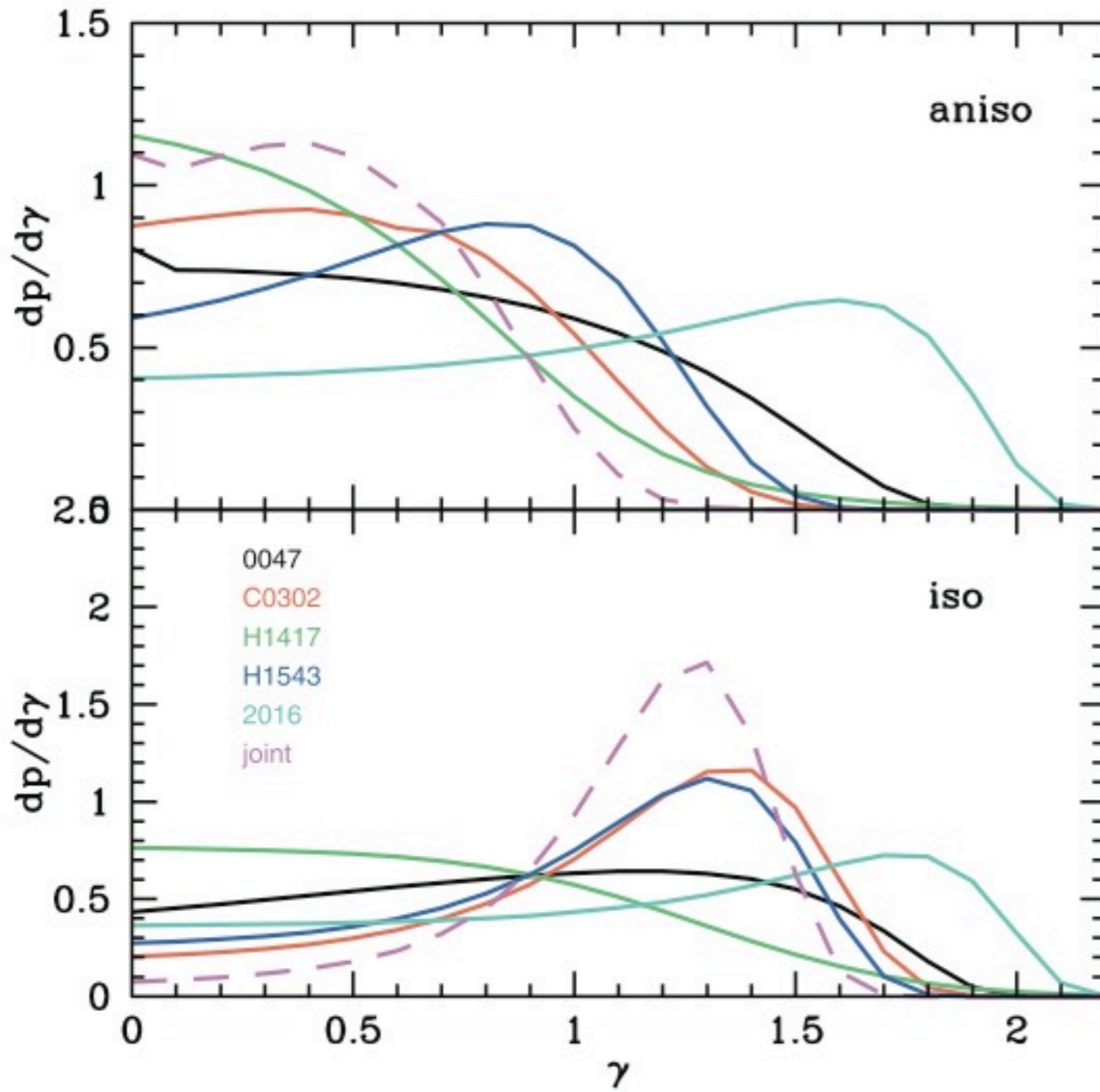
$R^{1/4}$ constant M/L
density profile

Lensing mass is
the same

SIS density profile
with stellar M/L=0

$$\langle v_{\parallel}^2 \rangle (\leq R_A) = \frac{1}{\pi} \left[\frac{GM_E}{R_E} \right] f(\gamma', \delta, \beta) \times \left(\frac{R_A}{R_E} \right)^{2-\gamma'}$$

DM: Lensing & Dynamics



Treu & Koopmans 2004

Applying this technique through the spherical Jeans equations ($w/\beta \ll 0$) to five lens systems with lensing and kinematics (from Keck) at $z \sim 0.5-1.0$, it was found for two-component models (HQ/JF+gNFW) that for $\beta=0$.

$$\langle \gamma_{\text{DM}} \rangle = 1.3^{+0.2}_{-0.4} \quad (68\% \text{CL})$$

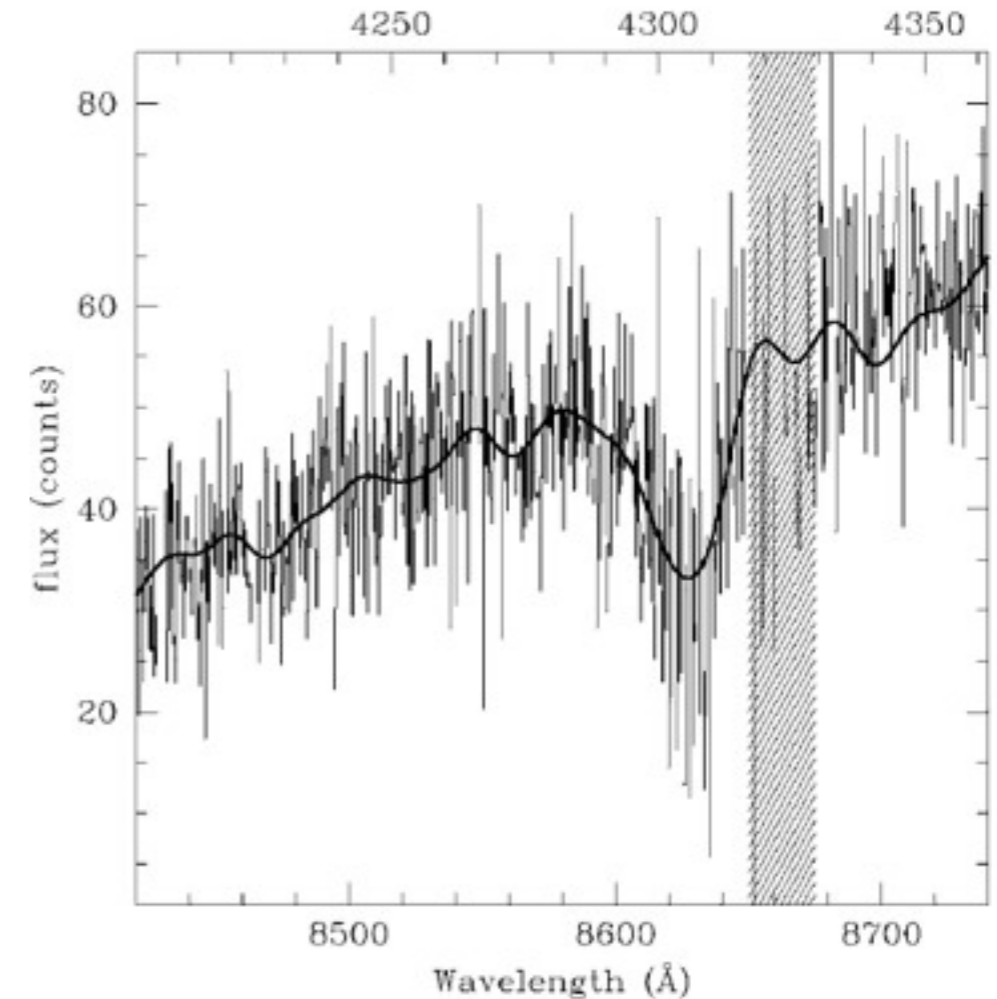
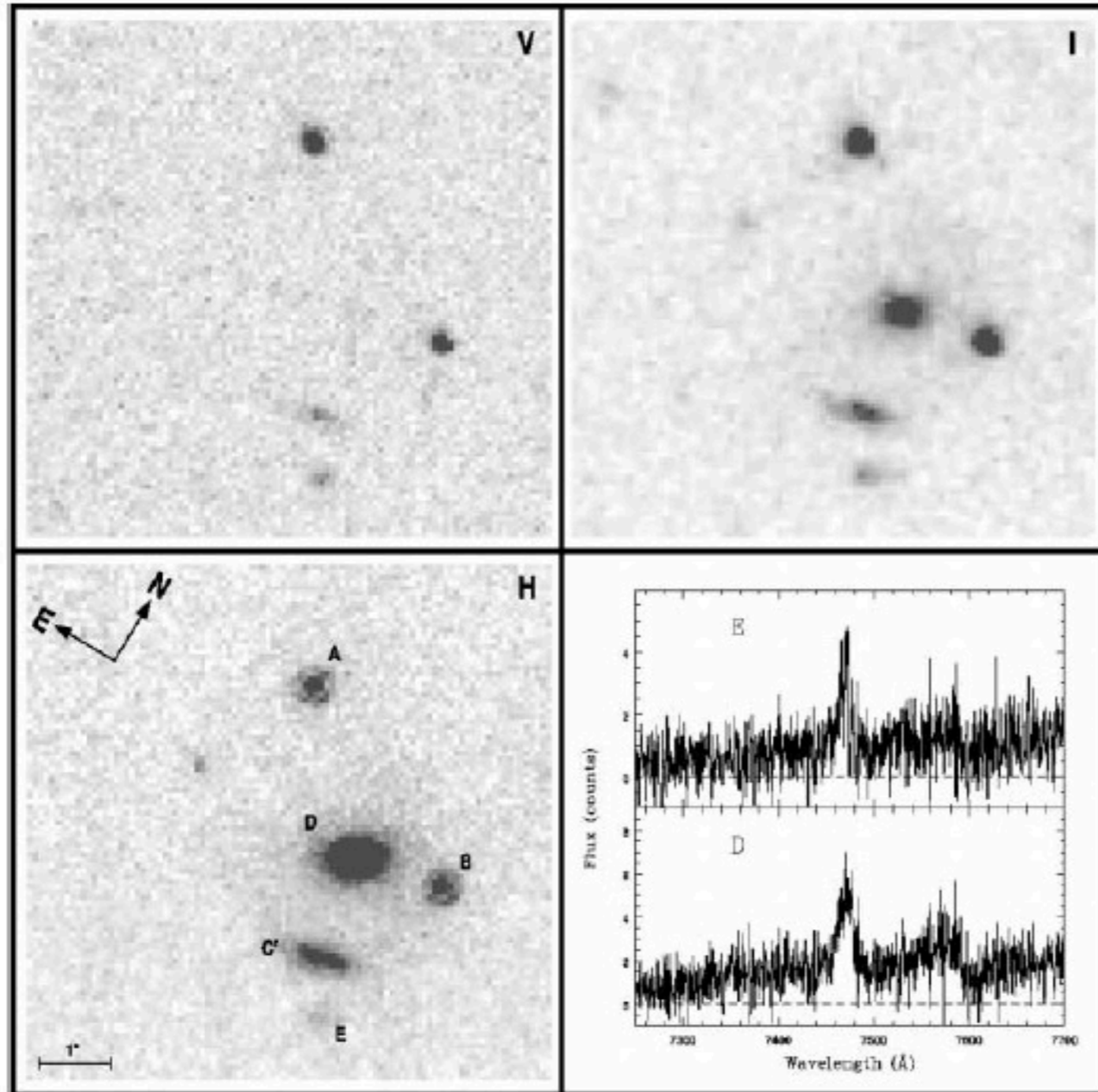
$$f_{\text{DM}} = 0.15 - 0.65 \quad \text{inside } R_{\text{eff}}$$

And for Osipkov-Merritt model with $r_i = R_{\text{eff}}$

$$\langle \gamma_{\text{DM}} \rangle < 0.6 \quad (68\% \text{CL})$$

[Slope total mass is 0.45-0.90 steeper]

Adiabatic Contraction

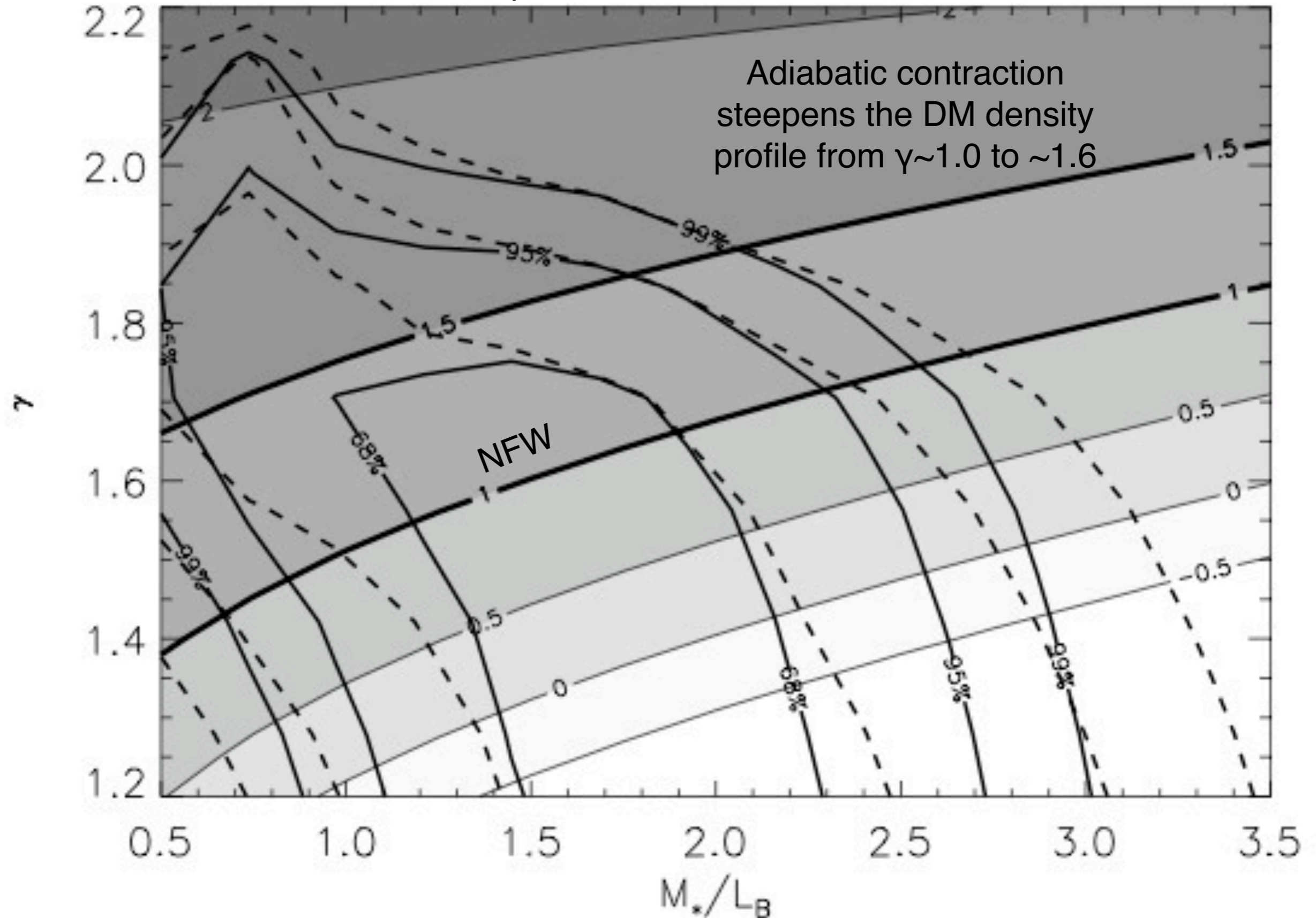


MG2016+112: ETG at $z=1.01$.
 $R_{\text{eff}} \sim 2.7$ kpc; Stellar dispersion of 330 ± 32 km/s; 80% DM inside
 $R_{\text{Einst}} \sim 14$ kpc

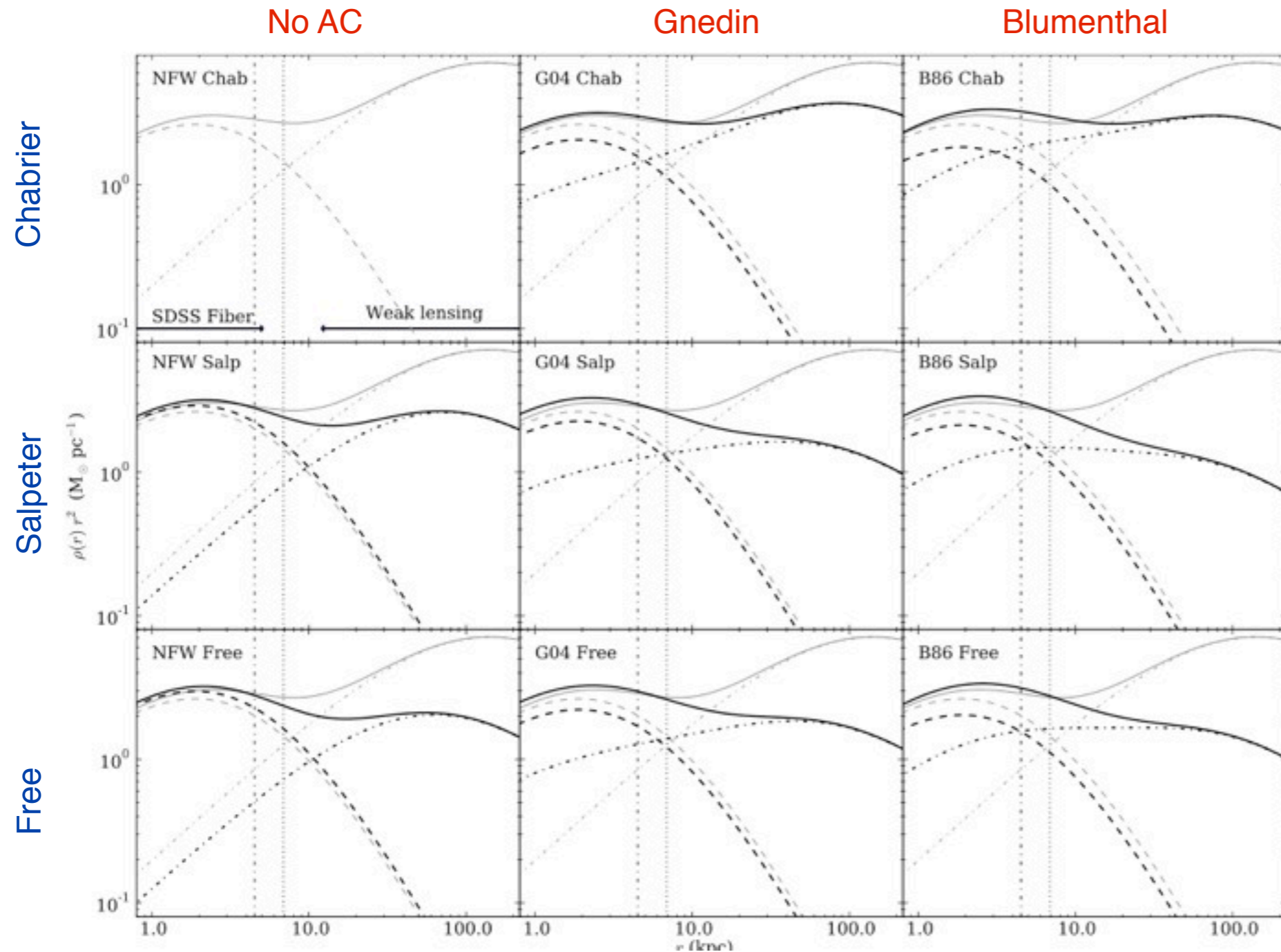
Treu & Koopmans 2002

Adiabatic Contraction

Impact of adiabatic contraction



Adiabatic Contraction

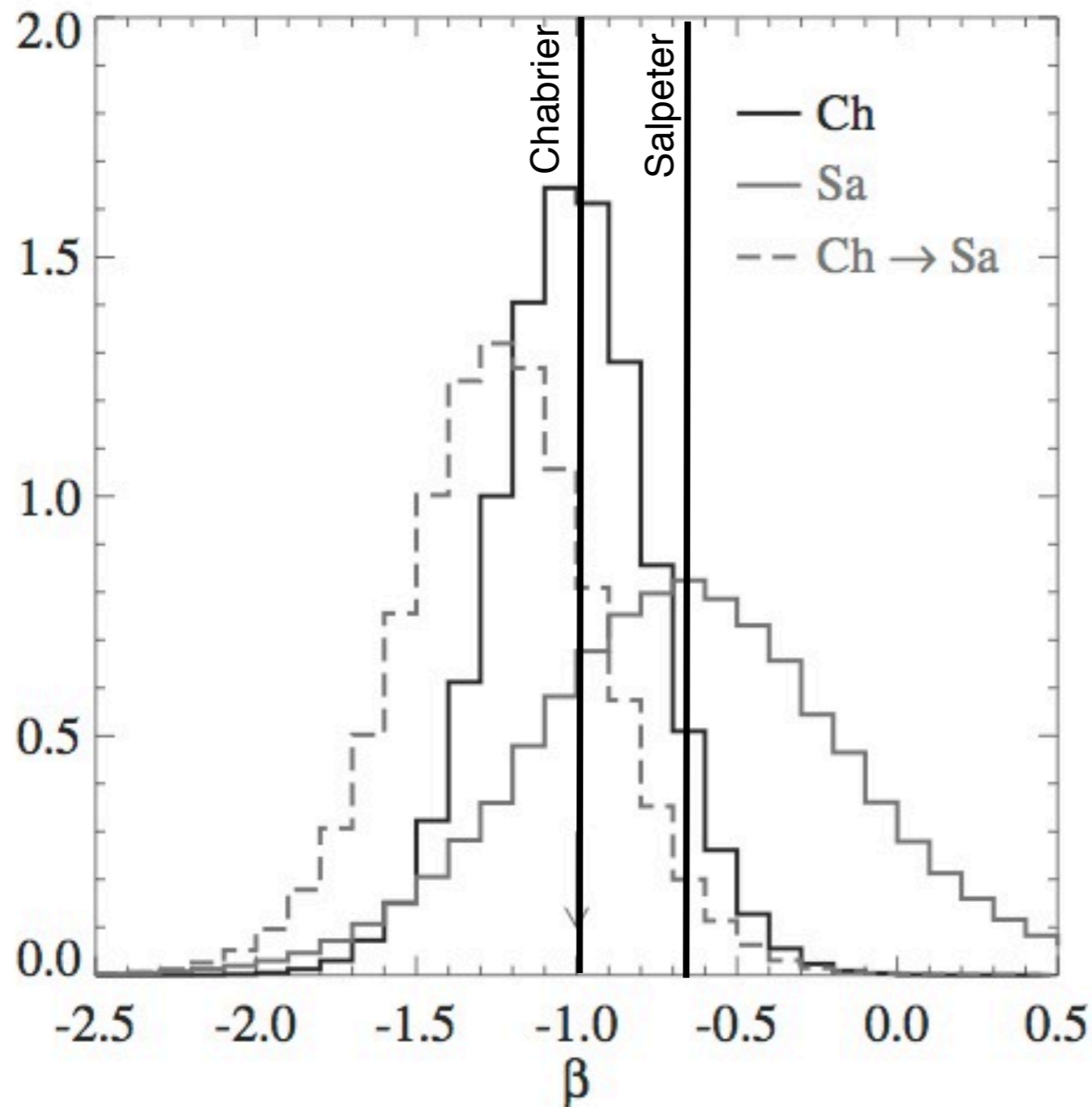


Contraction & IMF have major impact on the halo shape and required halo mass.

Constraints from WL, SL and dynamics prefer a heavy Salpeter-like IMF with some moderate AC.

Auger et al. 2010

Similarly: Scaling Relations for DM



Rescaling lenses to a common DM mass-scale (subtracting stellar mass) as function of $R_{\text{inst}}/R_{\text{eff}}$ allows its density profile to be inferred.

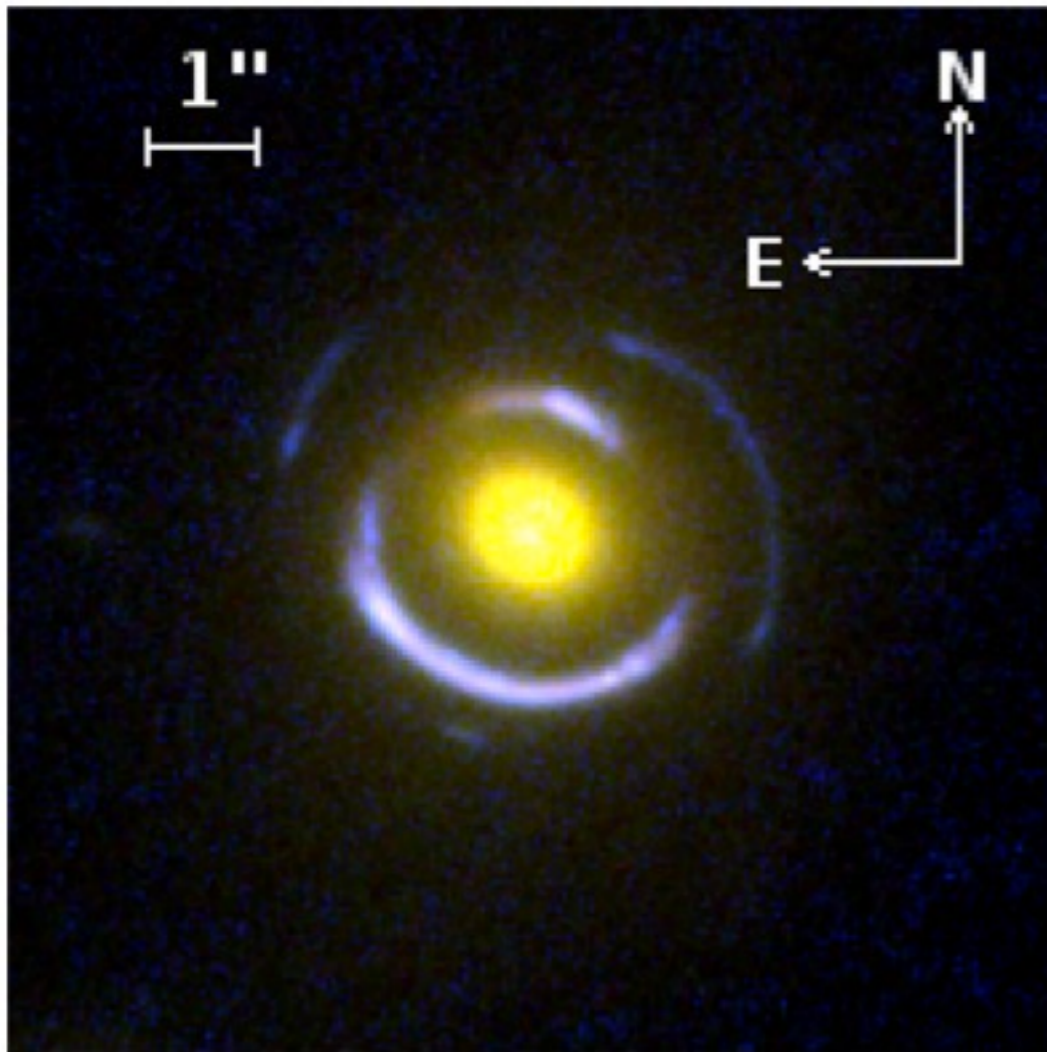
Chabrier IMFs leads to low stellar masses and DM profiles close to $\gamma'=1.7$ (SIE), whereas **Salpeter IMFs lead to more stellar mass and a more shallow DM profile ($\gamma_{\text{DM}}=1.7$)**, consistent with TK04.

Grillo et al. 2012

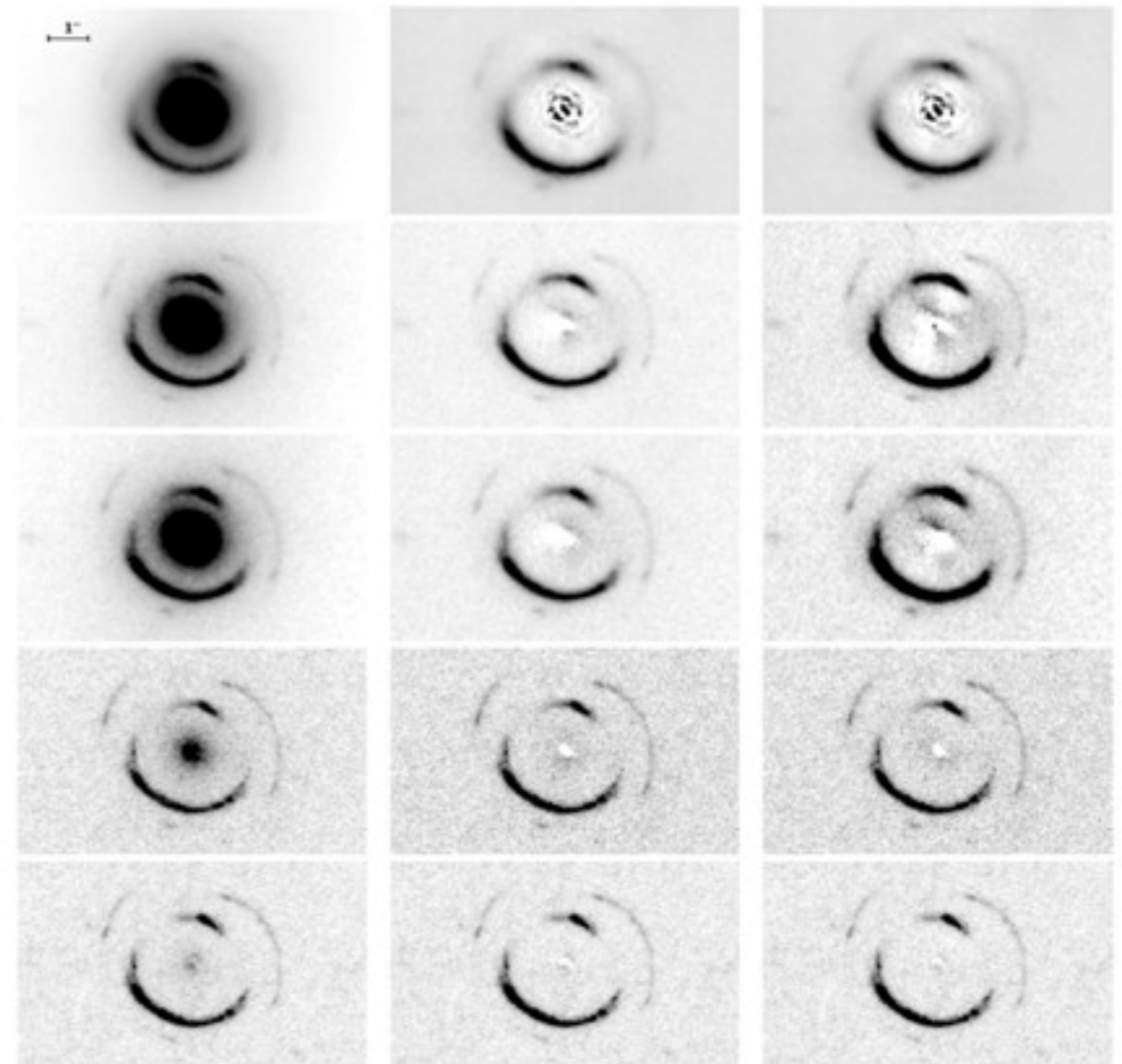
The Double Einstein Ring

If strong lensing provides M_{Einst} accurately inside R_{Einst} , then having two rings provides the density profile inside the two rings w/o hardly any assumption.

Color Composite



Multi-color HST data

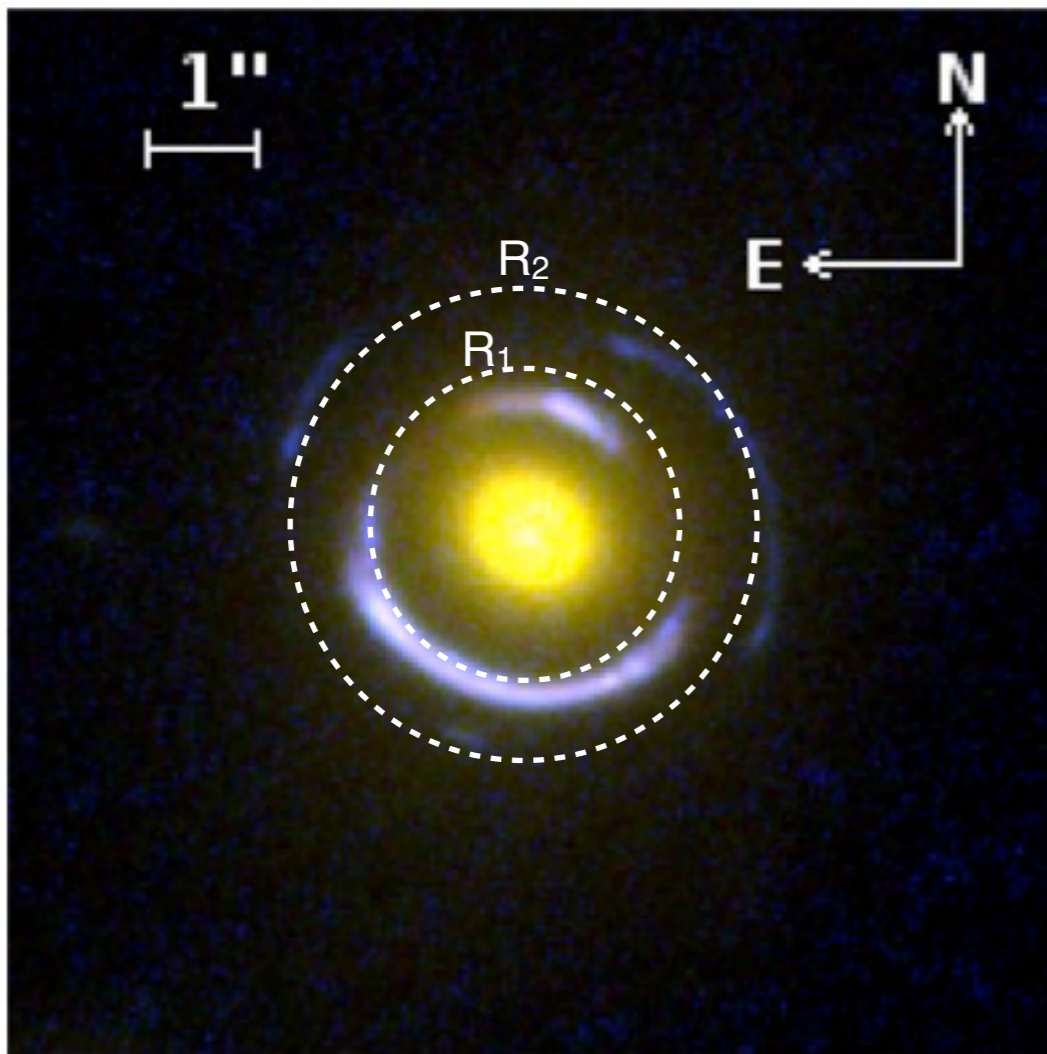


Sonnenfeld et al. 2012

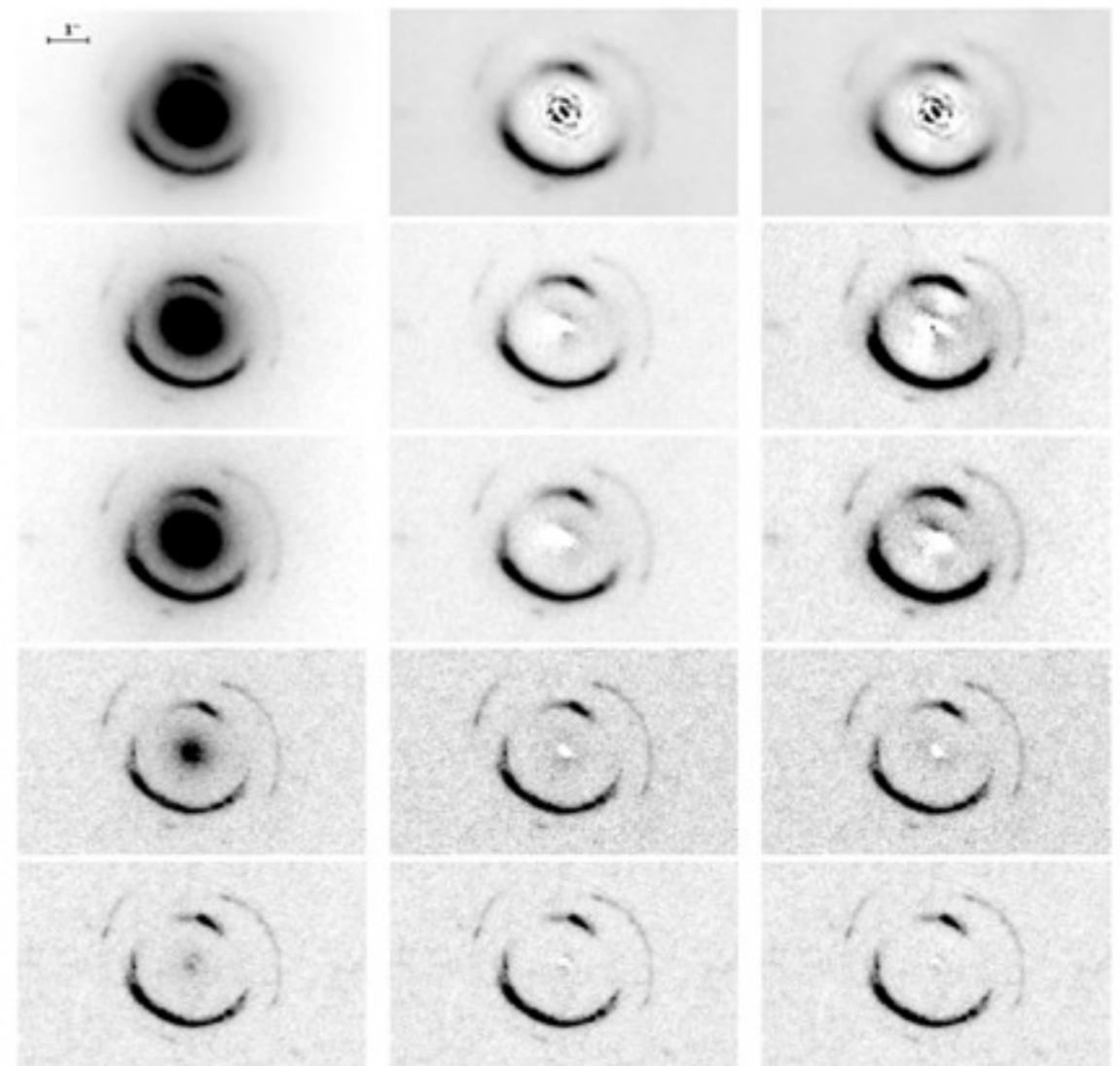
The Double Einstein Ring

If strong lensing provides M_{Einst} accurately inside R_{Einst} , then having two rings provides the density profile inside the two rings w/o hardly any assumption.

Color Composite



Multi-color HST data

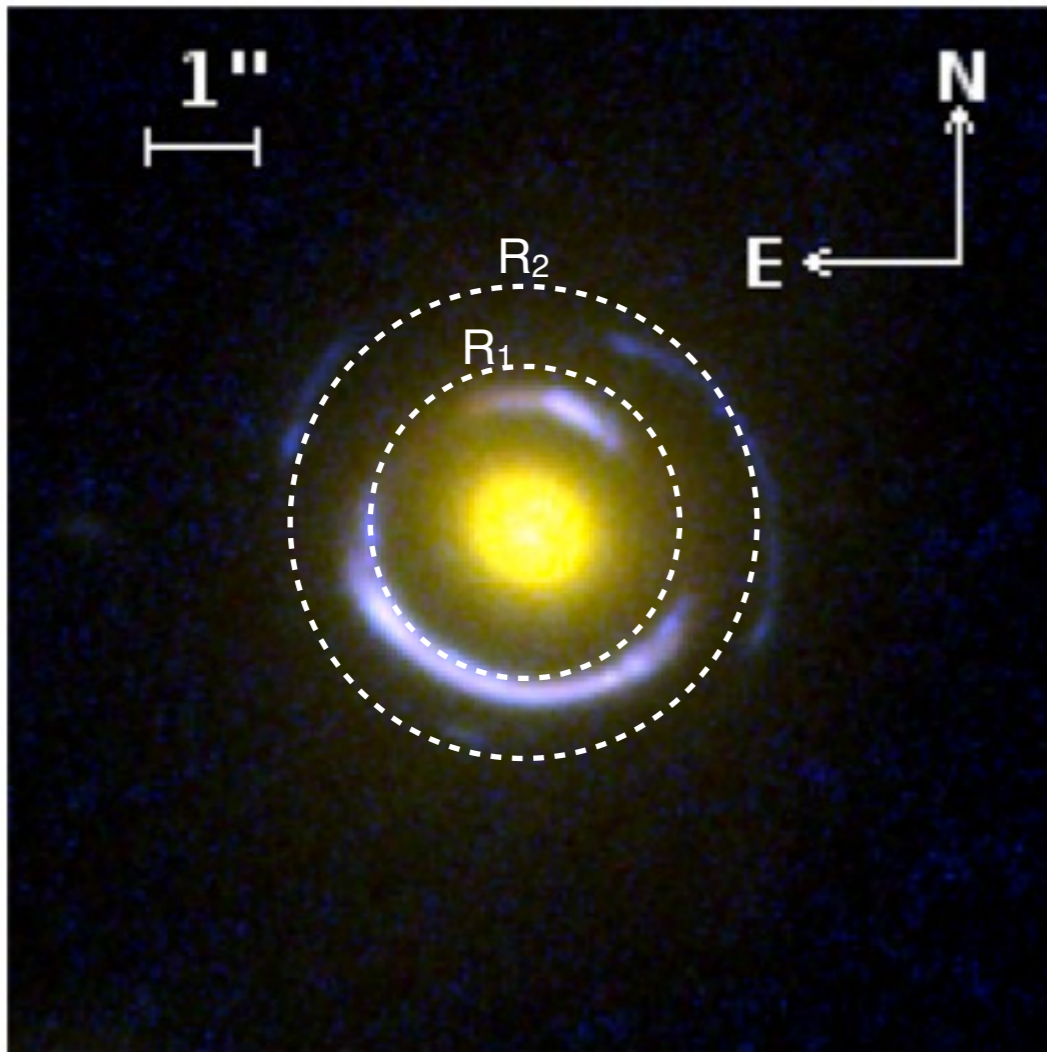


Sonnenfeld et al. 2012

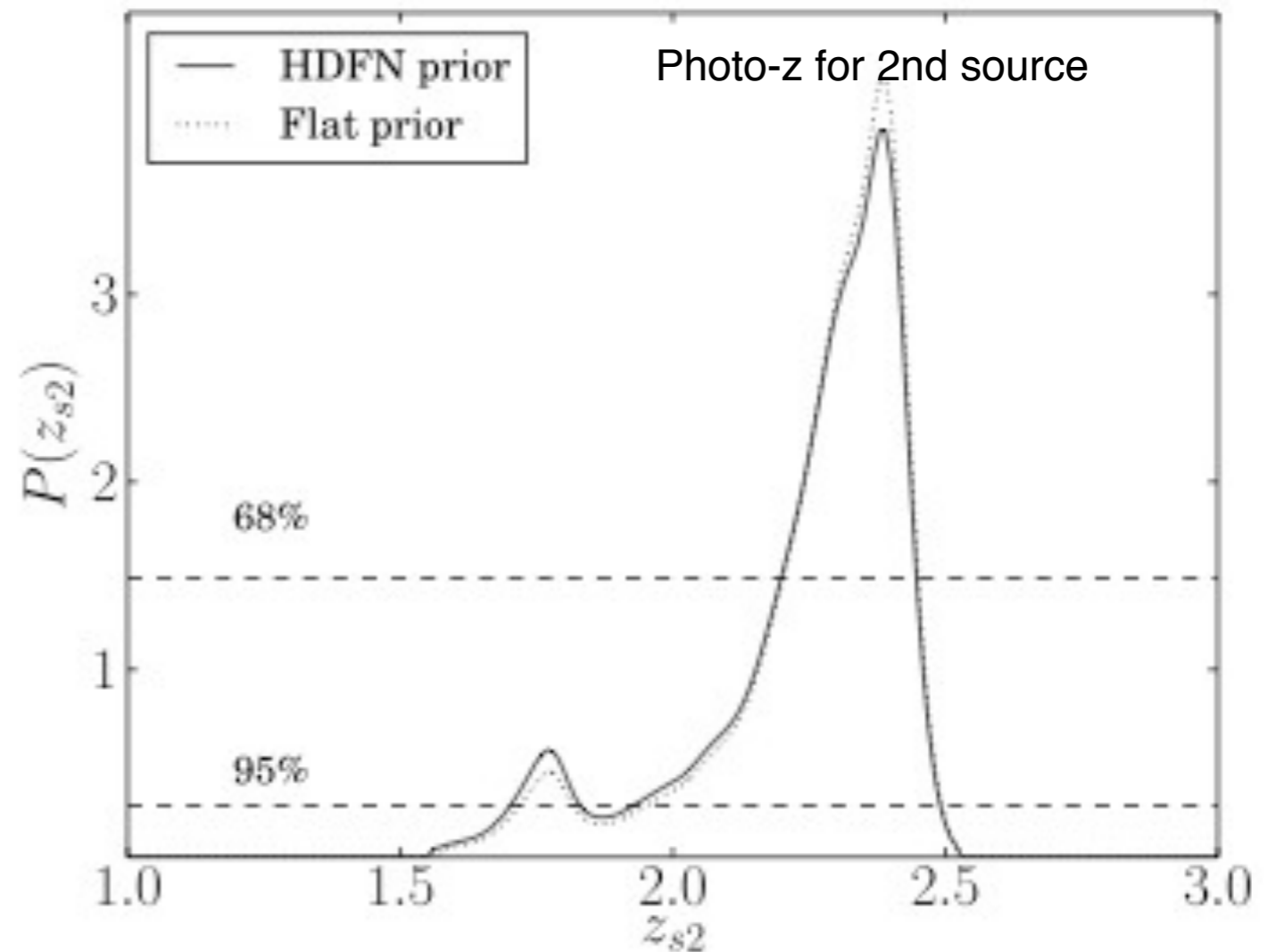
The Double Einstein Ring

If strong lensing provides M_{Einst} accurately inside R_{Einst} , then having two rings provides the density profile inside the two rings w/o hardly any assumption.

Color Composite



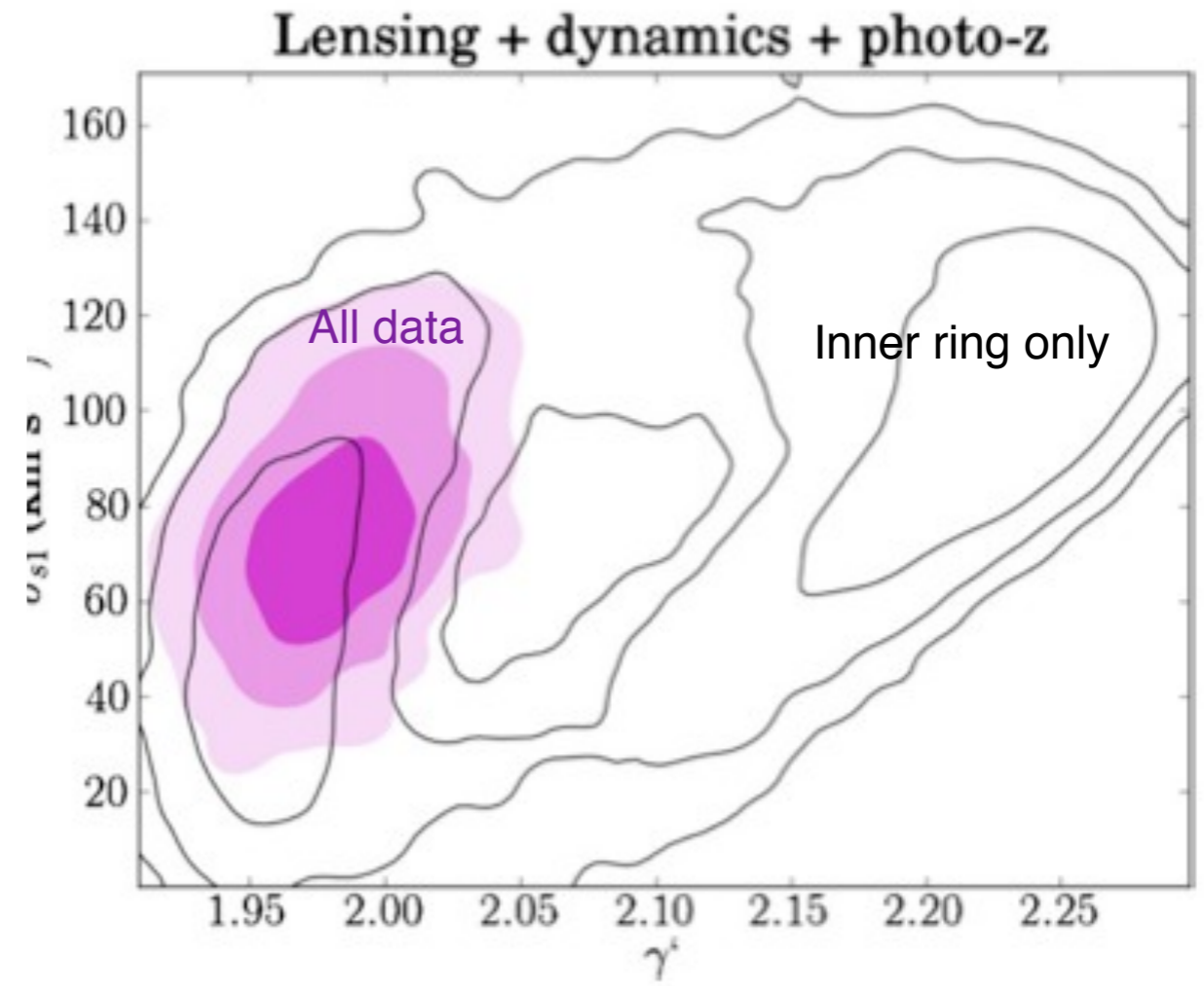
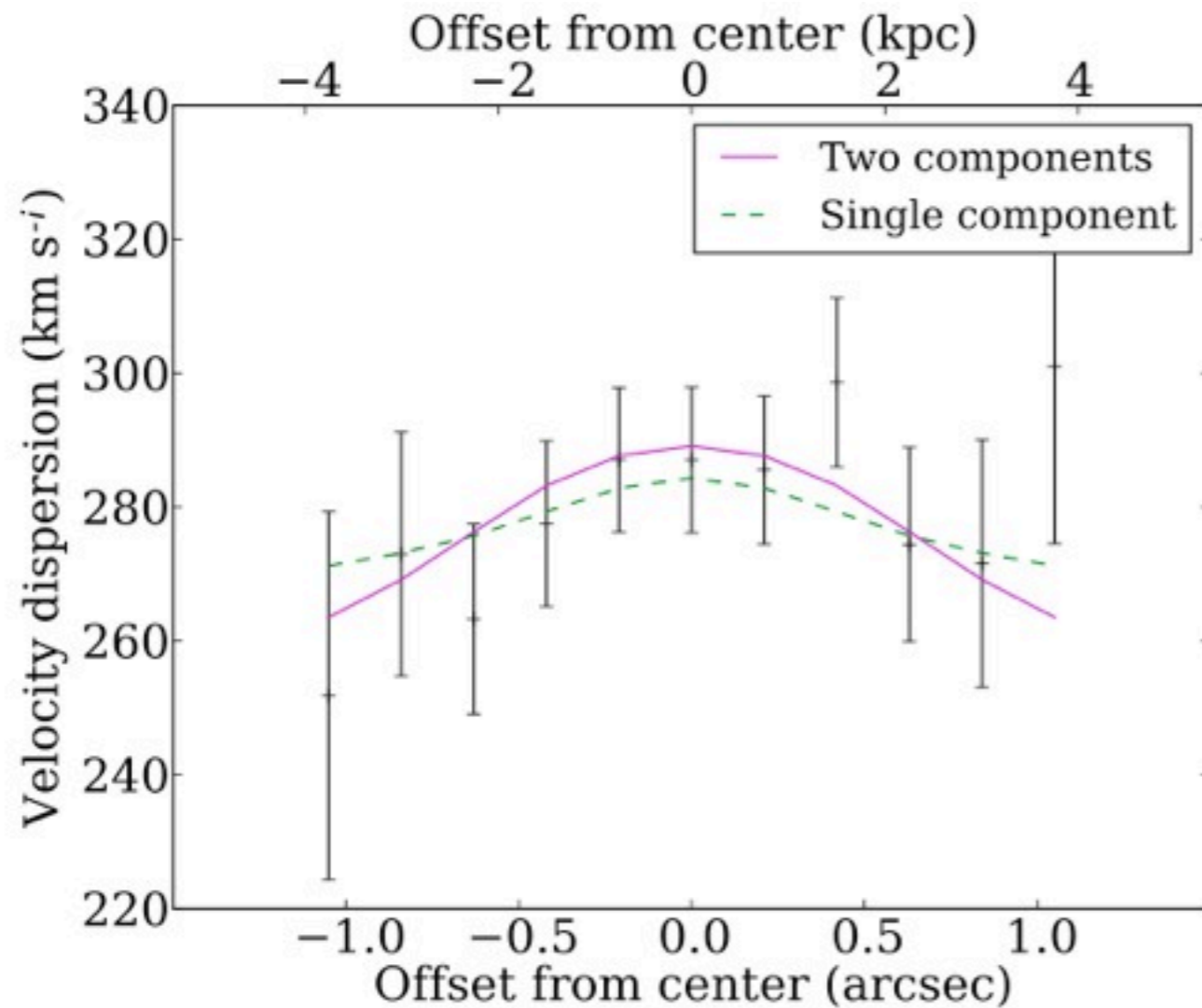
Multi-color HST data



Sonnenfeld et al. 2012

The Double Einstein Ring

Combining the double Einstein ring data with an extended kinematic profile breaks the old single-ring-only degeneracy



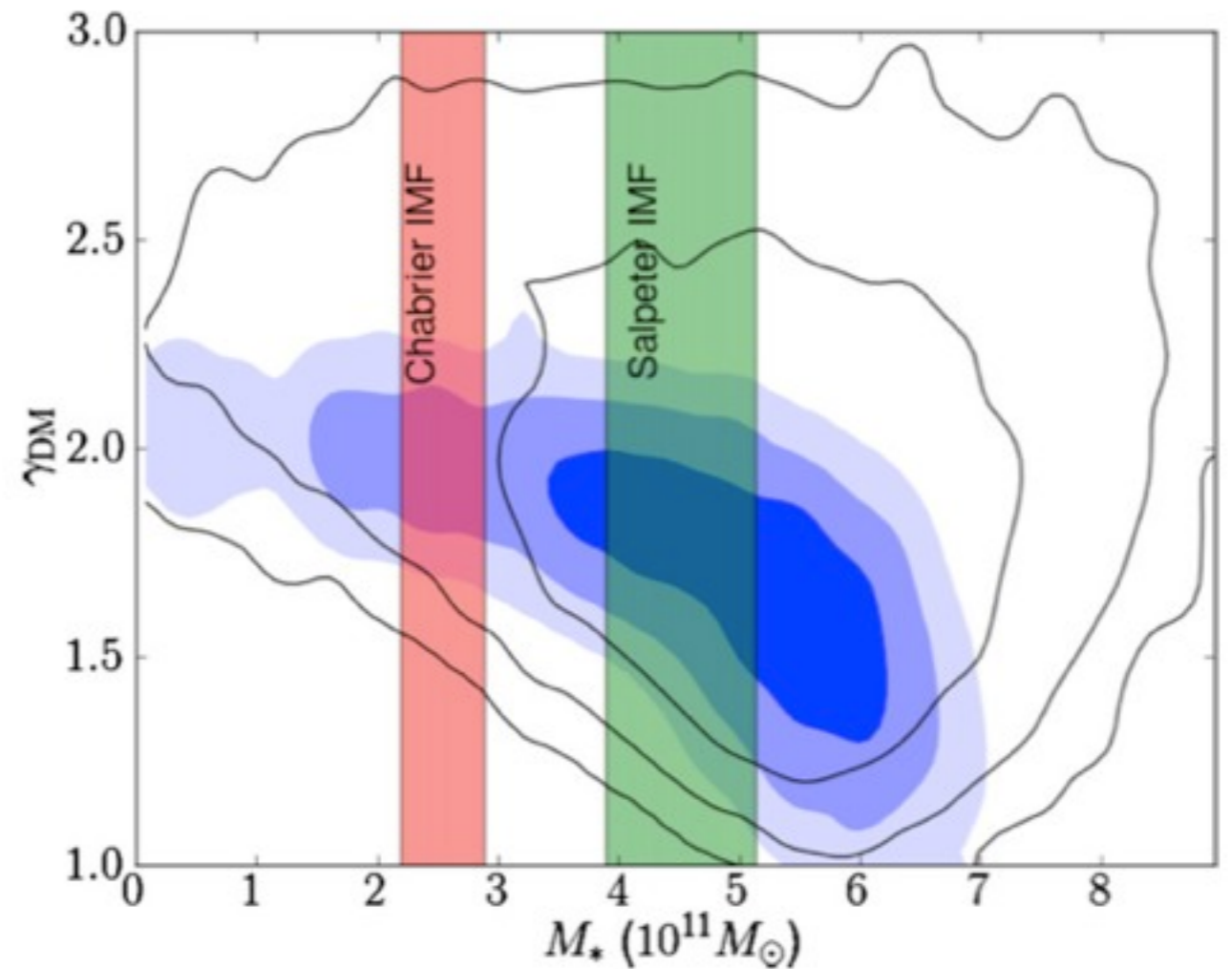
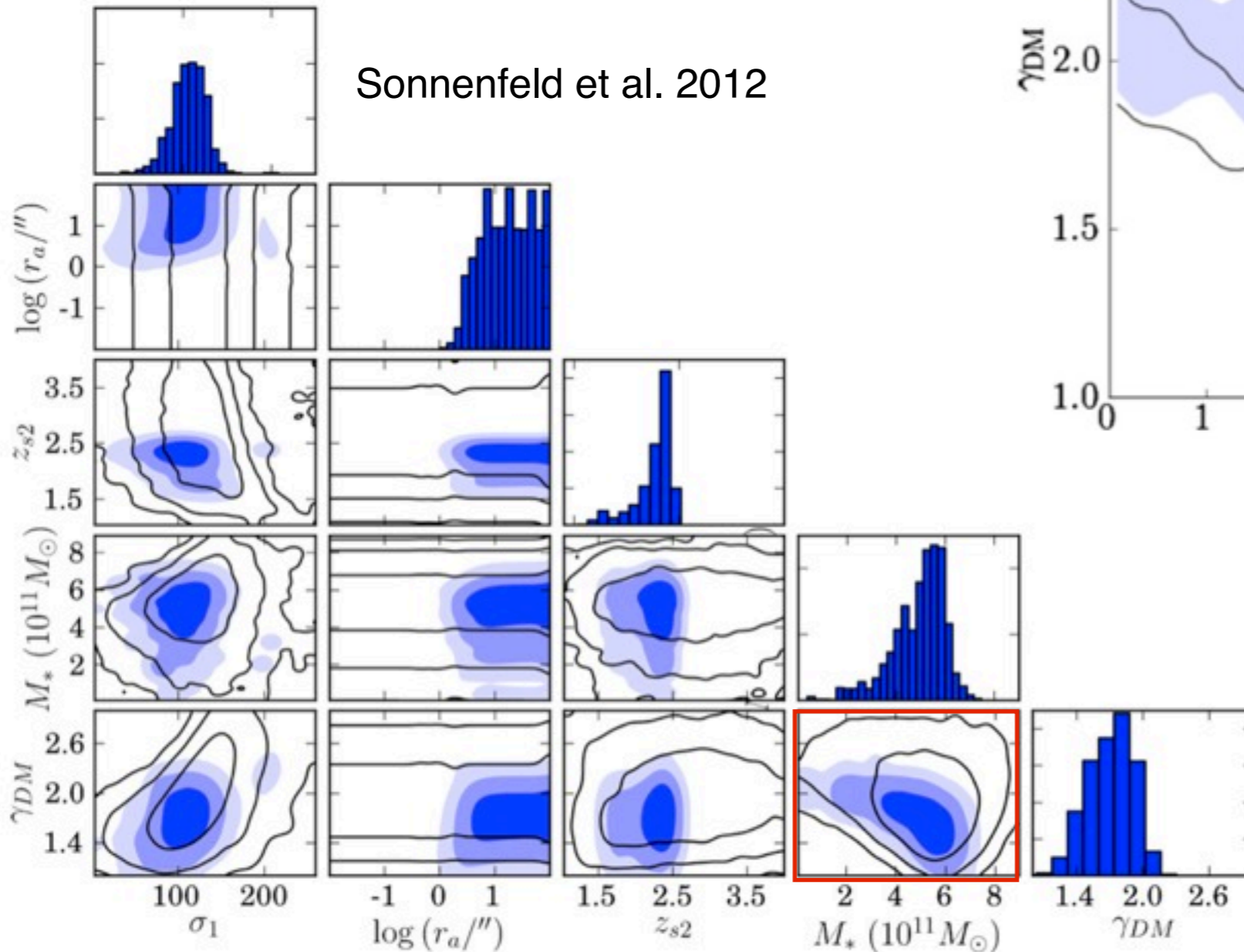
Sonnenfeld et al. 2012

The Double Einstein Ring

Full Bayesian MCMC exploration of parameter space:

$$\gamma_{DM} = 1.7 \pm 0.2$$

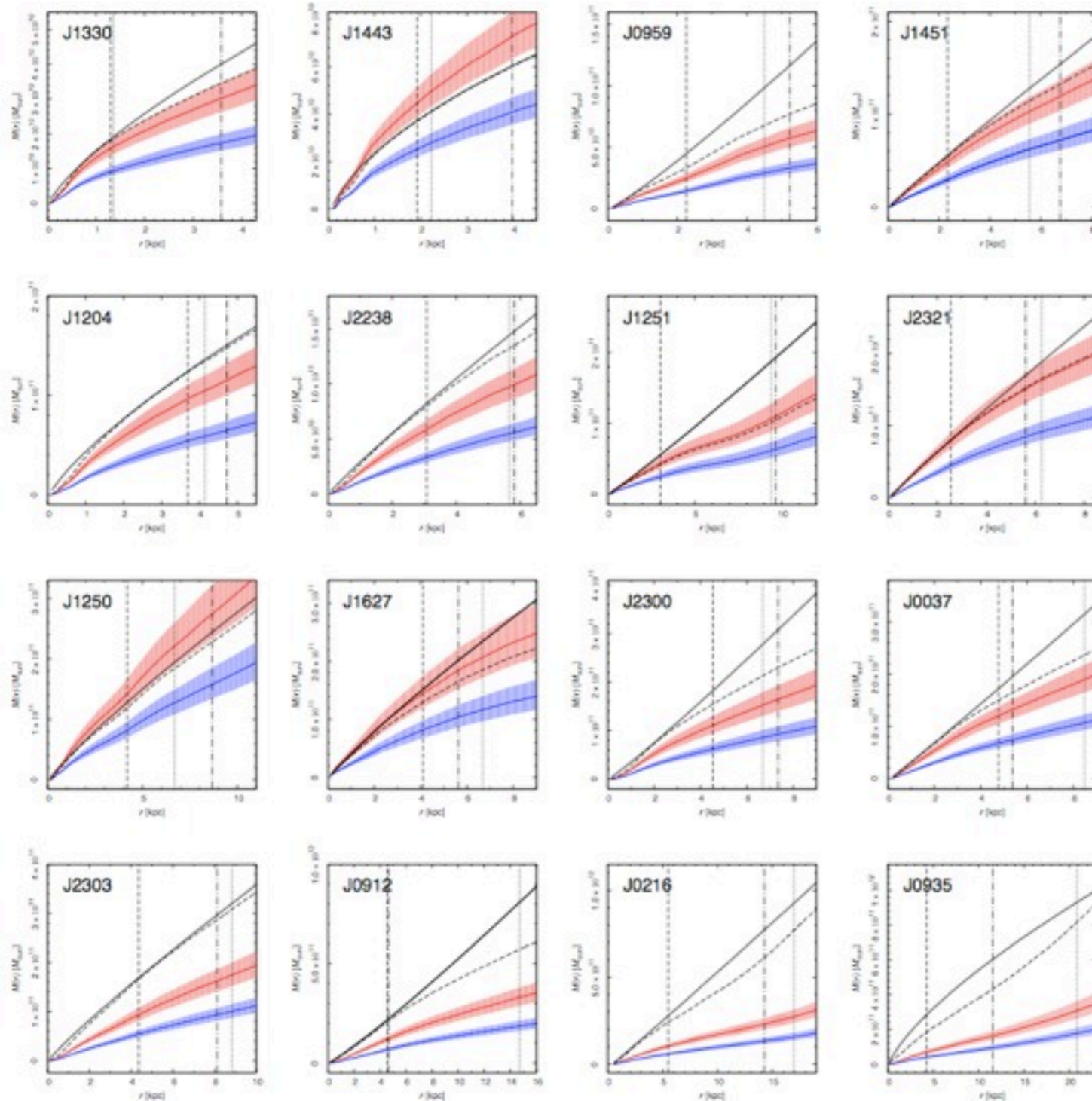
Sonnenfeld et al. 2012



SPS models (B&C) based on broad-band colors from all HST filters.

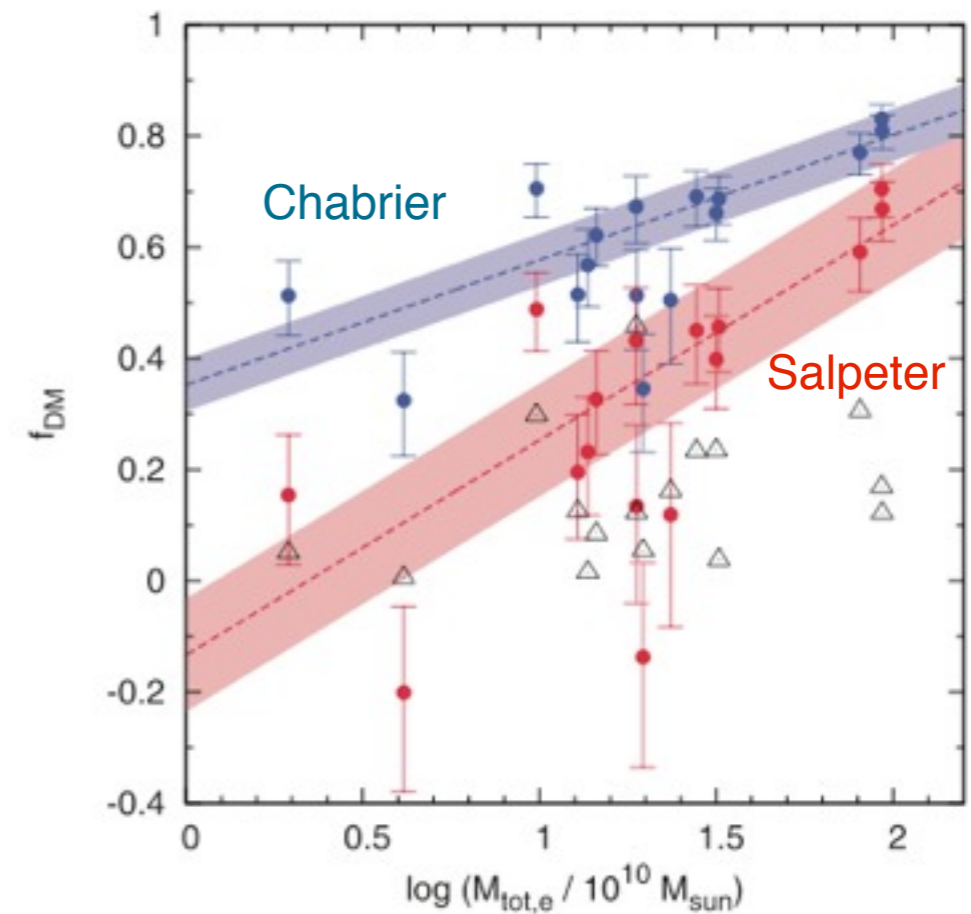
Salpeter IMF is preferred

Self-consistent 2D L&D



Fully self-consistent L&D sets very tight constraints on the density profiles using all information from 2D lensing and 2D kinematic data.

DM fraction f_{DM} increases rapidly with ETG mass/dispersion



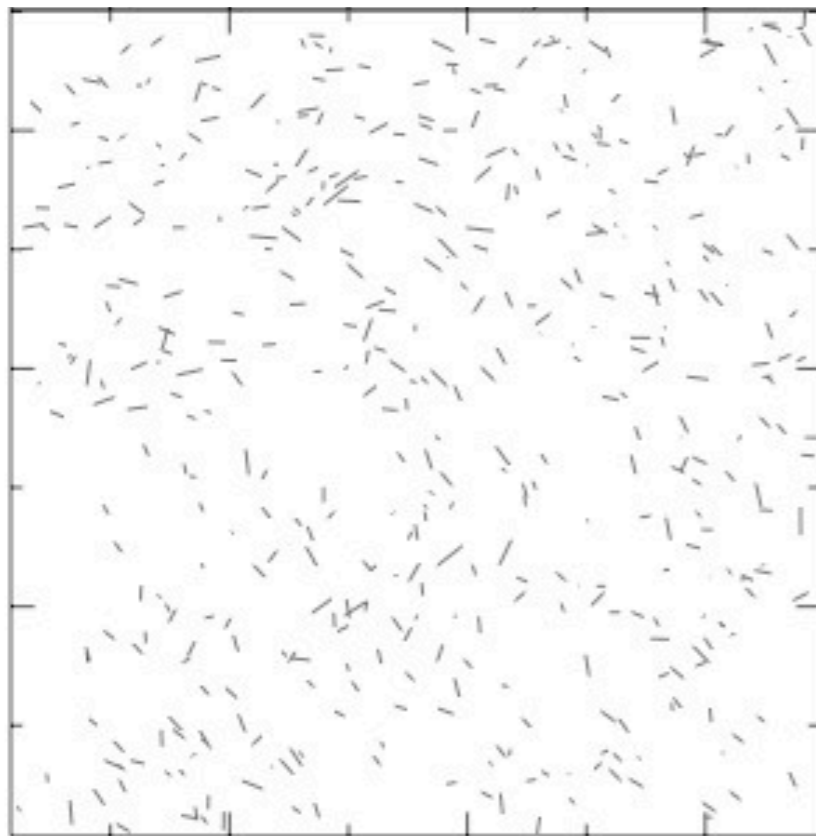
Barnabe et al. 2011

Extended Halos: 1-100 R_{eff}

Connection between SL & WL

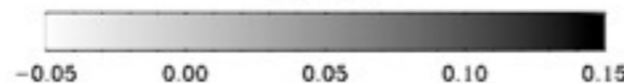
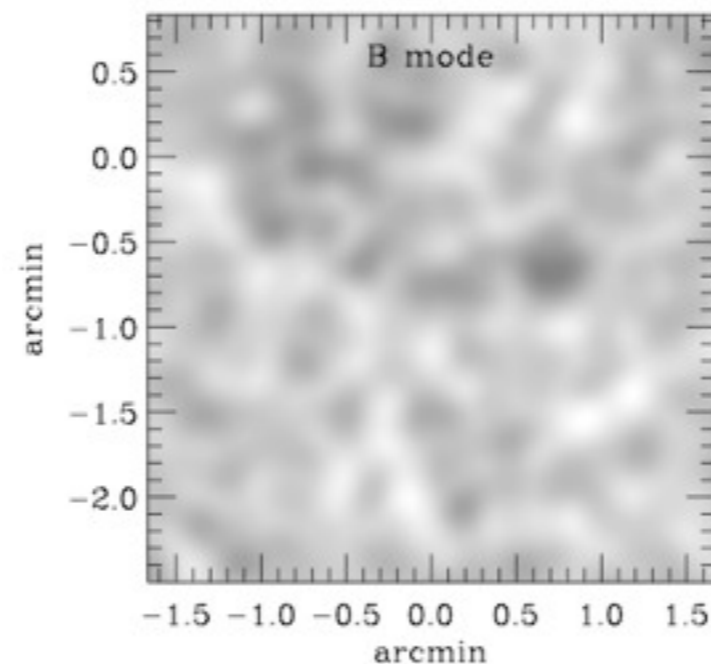
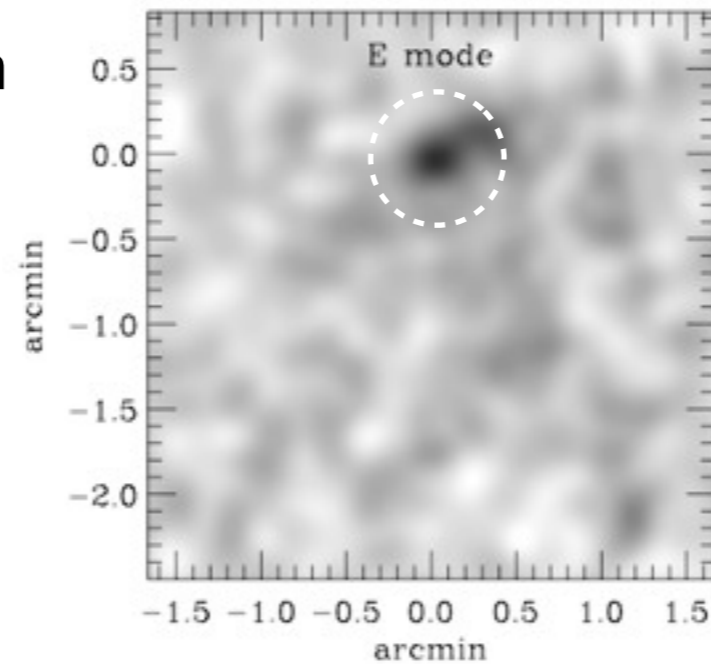
Weak Lensing of Strong Lenses

Shear field after PSF correction
using 22 SLACS ETGs



Gavazzi et al. 2007

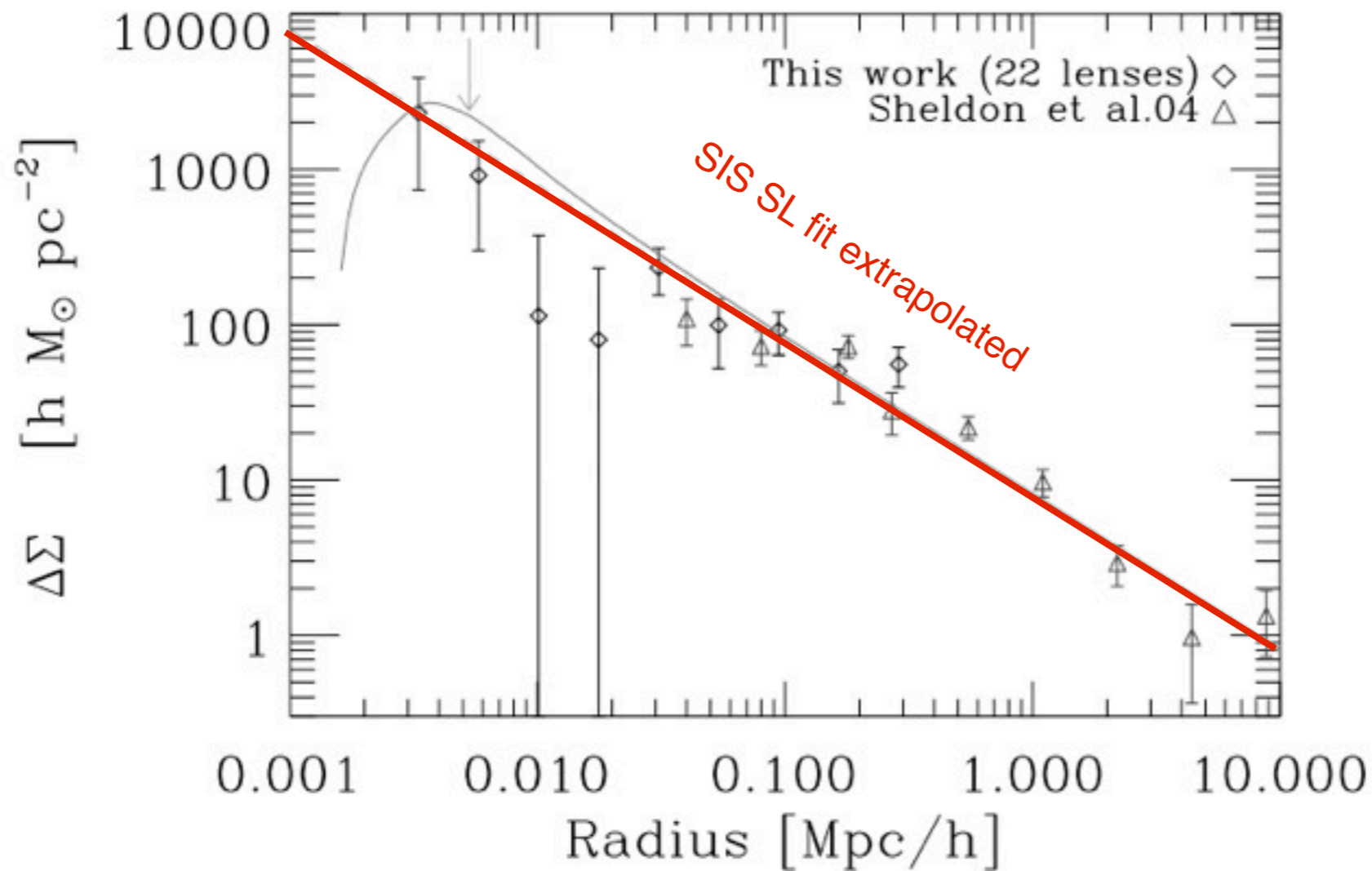
SLACS galaxies are centered in the
middle of the upper CCD of ACS



All lens galaxies are centered
at the same position on the
CCD and the shear signals can
be stacked to obtain a **mass-
averaged convergence map**.

Systematics (B-modes) seem
under control

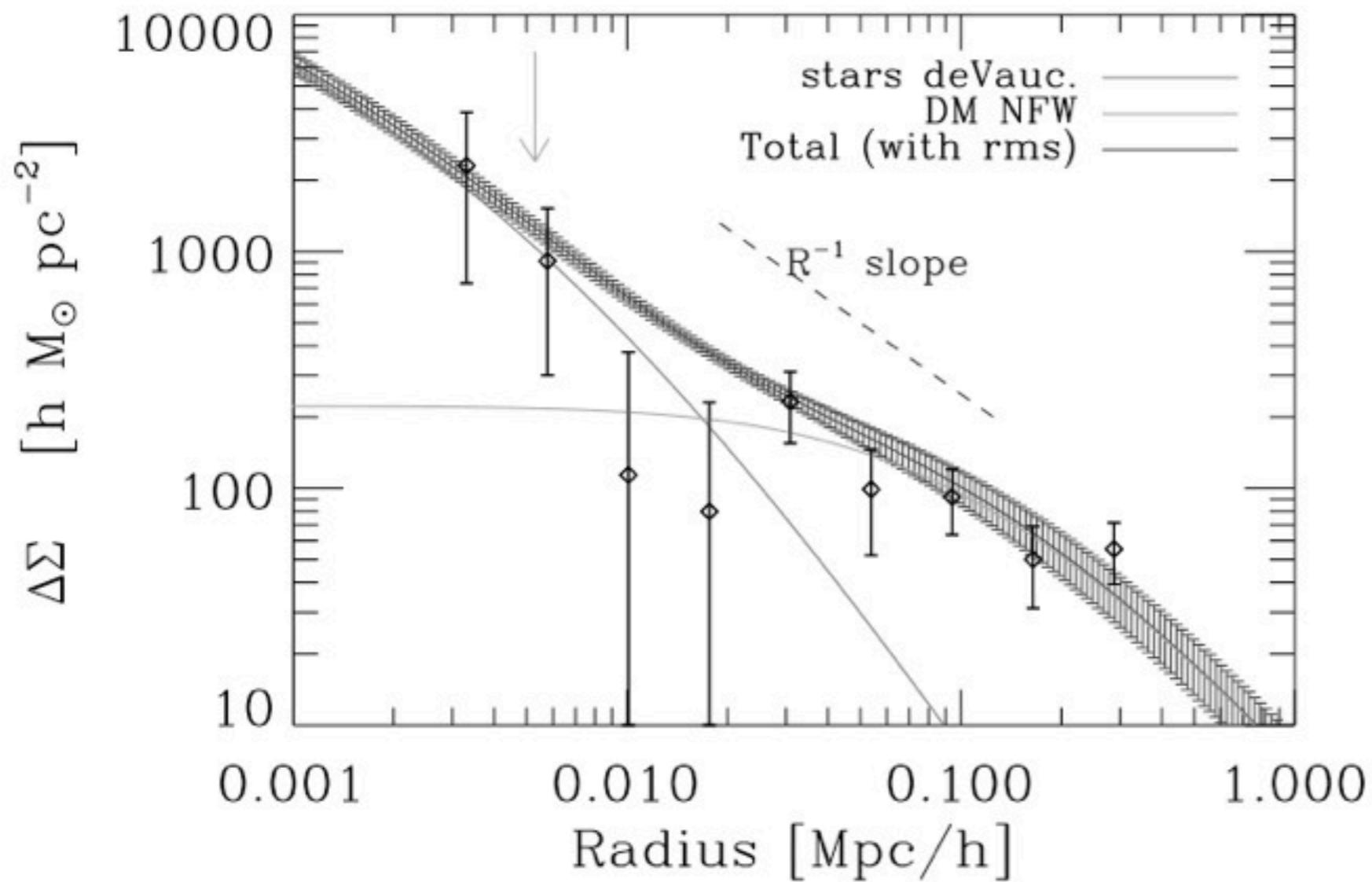
Weak Lensing of Strong Lenses



The best SL-SIS model can fit the WL data all the way over 1-100 R_{eff} .

Gavazzi et al. 2007

Weak Lensing of Strong Lenses



The best SL-SIS model can fit the WL data all the way over 1-100 R_{eff} .

Two-component mass model: deV+NFW with stellar M/L and M_{vir} as the only free parameters:

$$M^*/L_V = 4.5 \pm 0.5 h$$

$$M_{\text{vir}}/L_V = 250 \pm 95 h$$

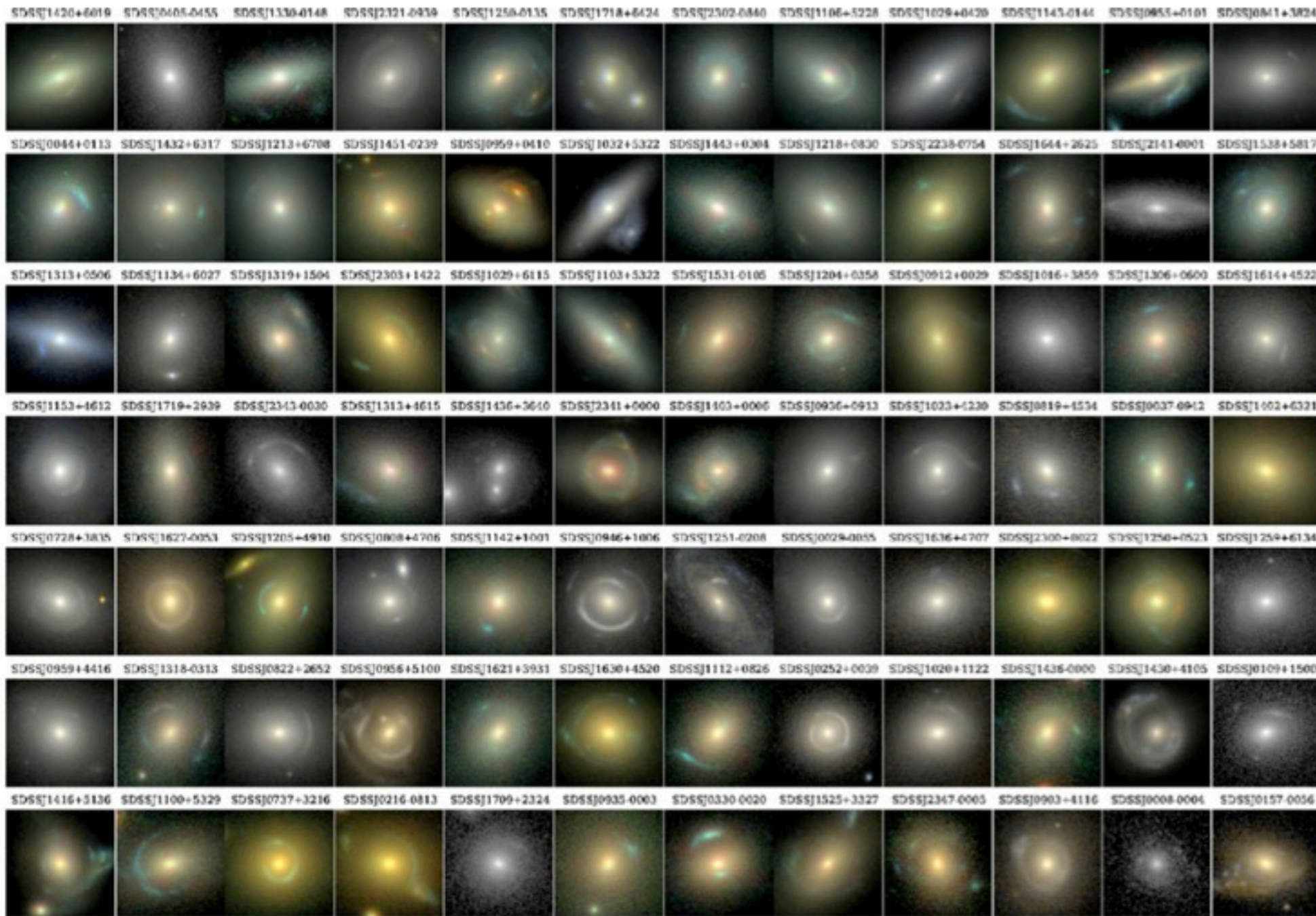
$$f_{\text{DM}}(<R_{\text{vir}}) = 0.02 \pm 0.01$$

$$f_{\text{DM}}(R_{\text{eff}}) = 0.27 \pm 0.04$$

Gavazzi et al. 2007

The Inclusion of Stellar Population Synthesis: Impact on DM inferences

Multi-color SLACS Sample

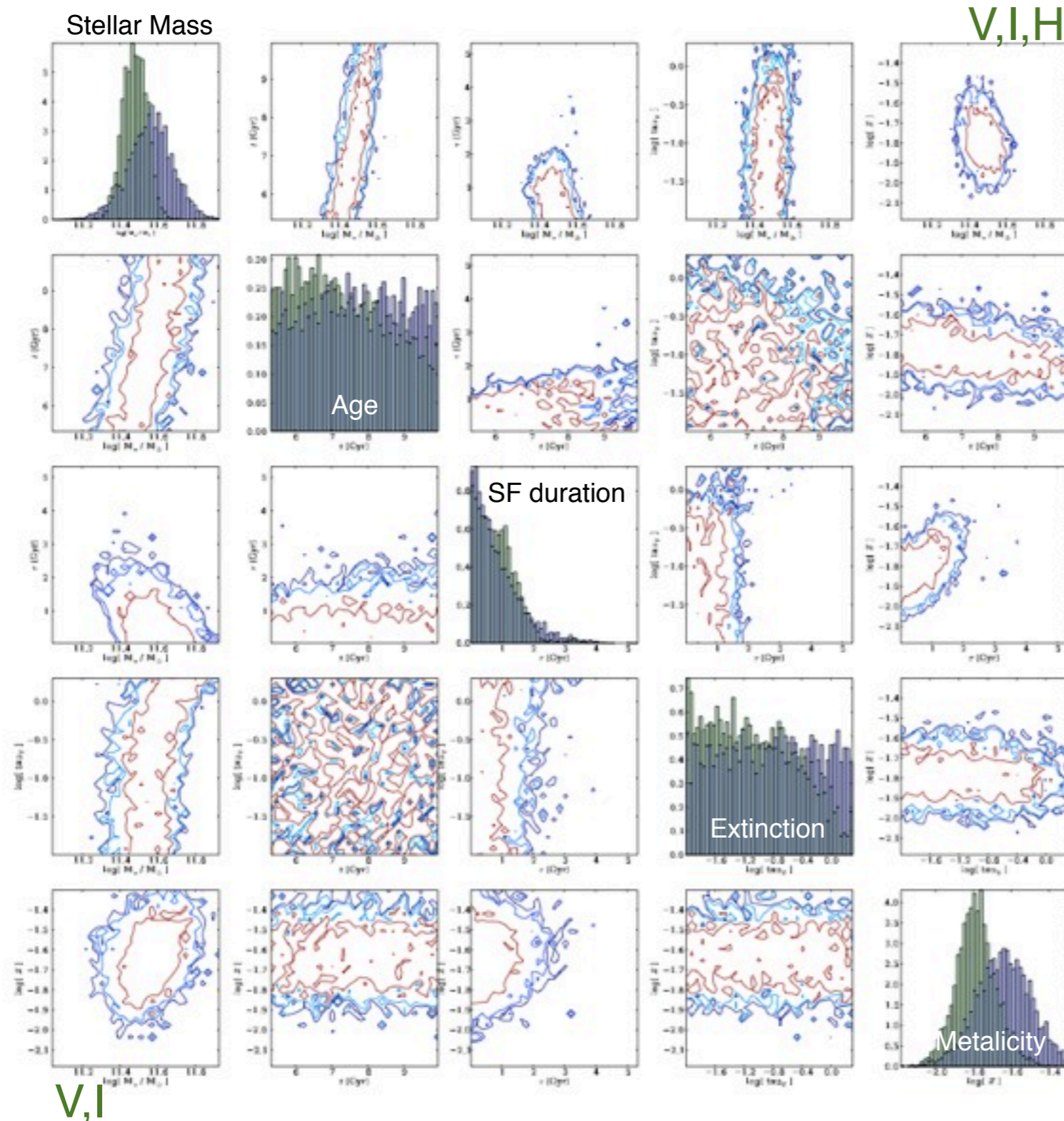


V, I & H-band HST data allow one to measure stellar masses using SPS and subtract this from the total lensing mass inside $R_{\text{Einst/eff}}$

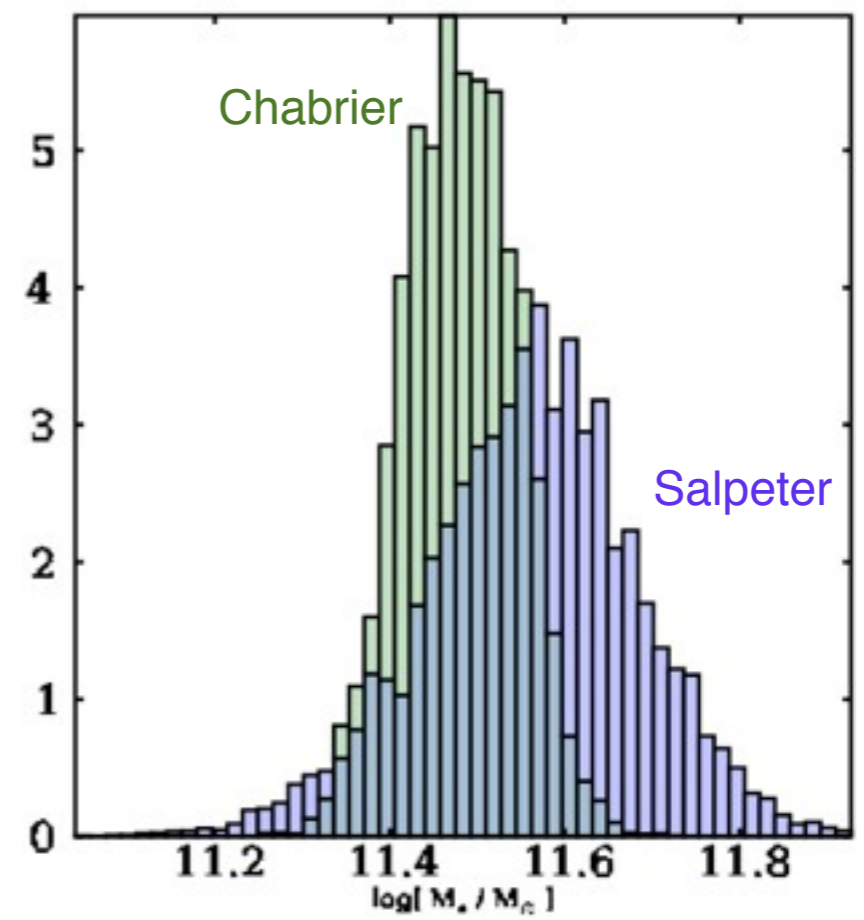
SPS codes: B&C03, MIUSCAT, CvD12, etc

Auger et al. 2009

CSP Constraints on Stellar Mass

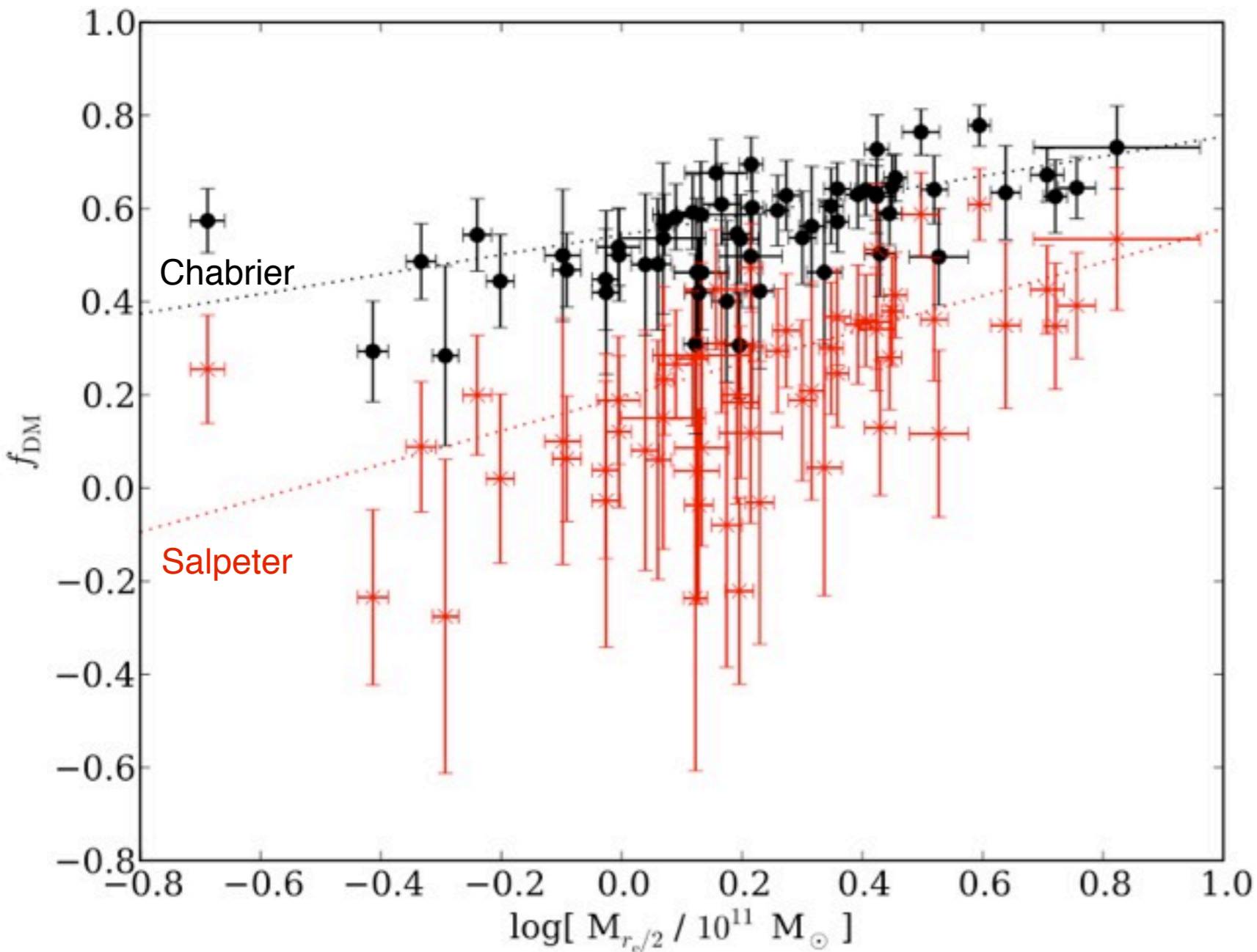


B&C03 SPS models provides strong constraints on the stellar mass PROVIDED the IMF is given (e.g. Chabrier, Salpeter)



Auger et al. 2009

Dark-Matter Fraction versus Mass



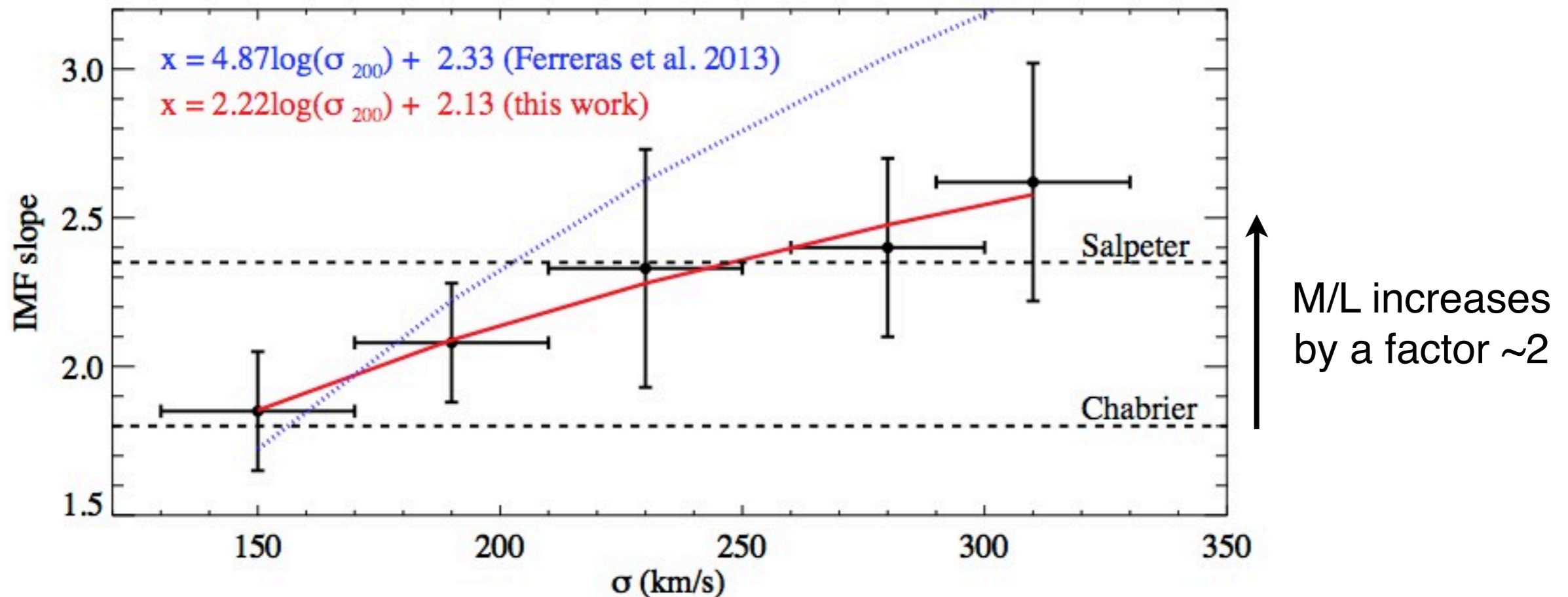
Subtracting the SPS stellar mass from the mass inside $R_{\text{eff}/2} \sim R_{\text{Einst}}$, suggests that the DM fraction in ETG increases with galaxy mass, assuming a fixed IMF.

This has implications for feedback models in Λ CDM, increasing as galaxies get more massive.

Auger et al. 2010

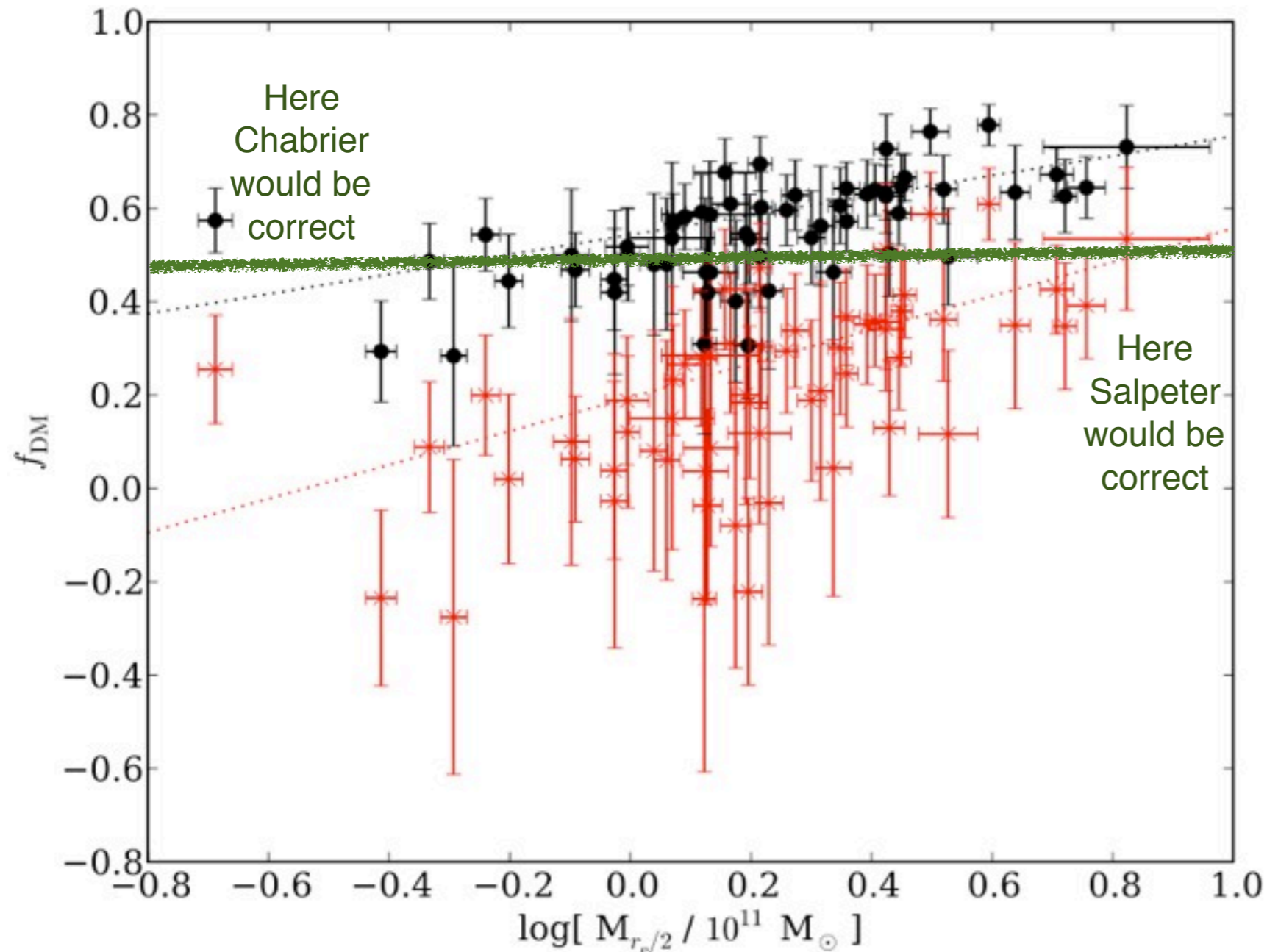
However! Impact of IMF variations on the inference of DM in ETGs

A full SPS modeling of SDSS galaxies suggest a trend in the IMF slope between 150-300 km/s, doubling the stellar M/L over this range. If confirmed (e.g. Conroy et al. 2013), this implies a tilting of the f_{DM} trend with galaxy mass



Spiniello et al. 2013

Impact of IMF variations on the inference of DM in ETGs



The amazing conclusion seems to be that f_{DM} does NOT depend on galaxy mass anymore and is constant over 150-300 km/s.

And $f_{DM} \sim 0.5$ inside $R_{eff}/2$.

Spiniello et al. 2013, in prep.

Auger et al. 2010

The Slope and Lower Mass Limit of the IMF from L&D+SSP.

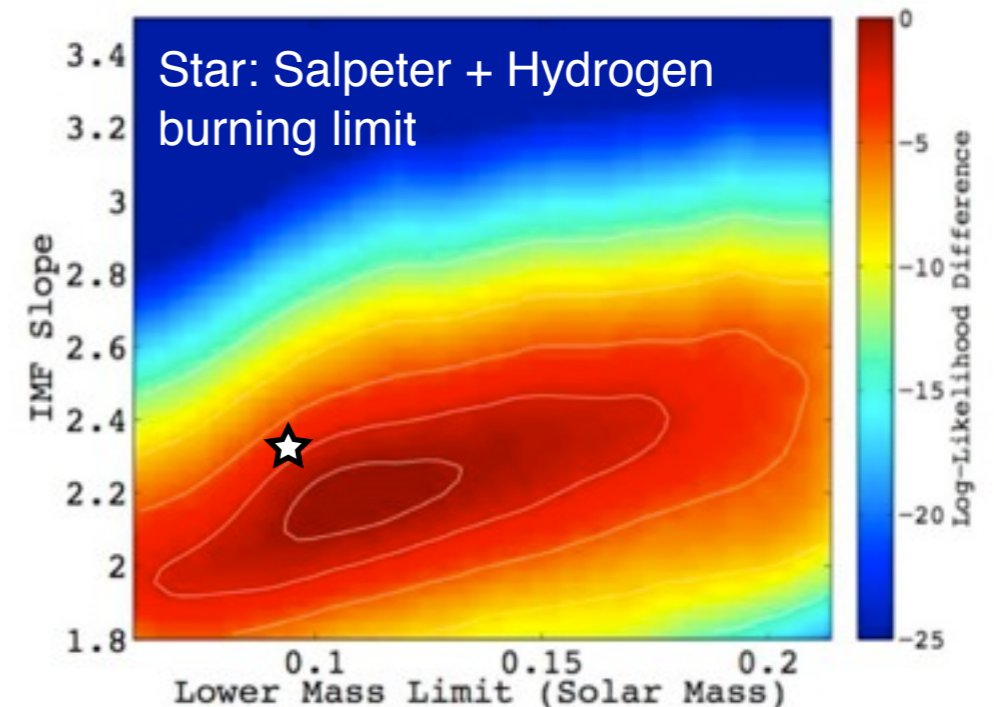
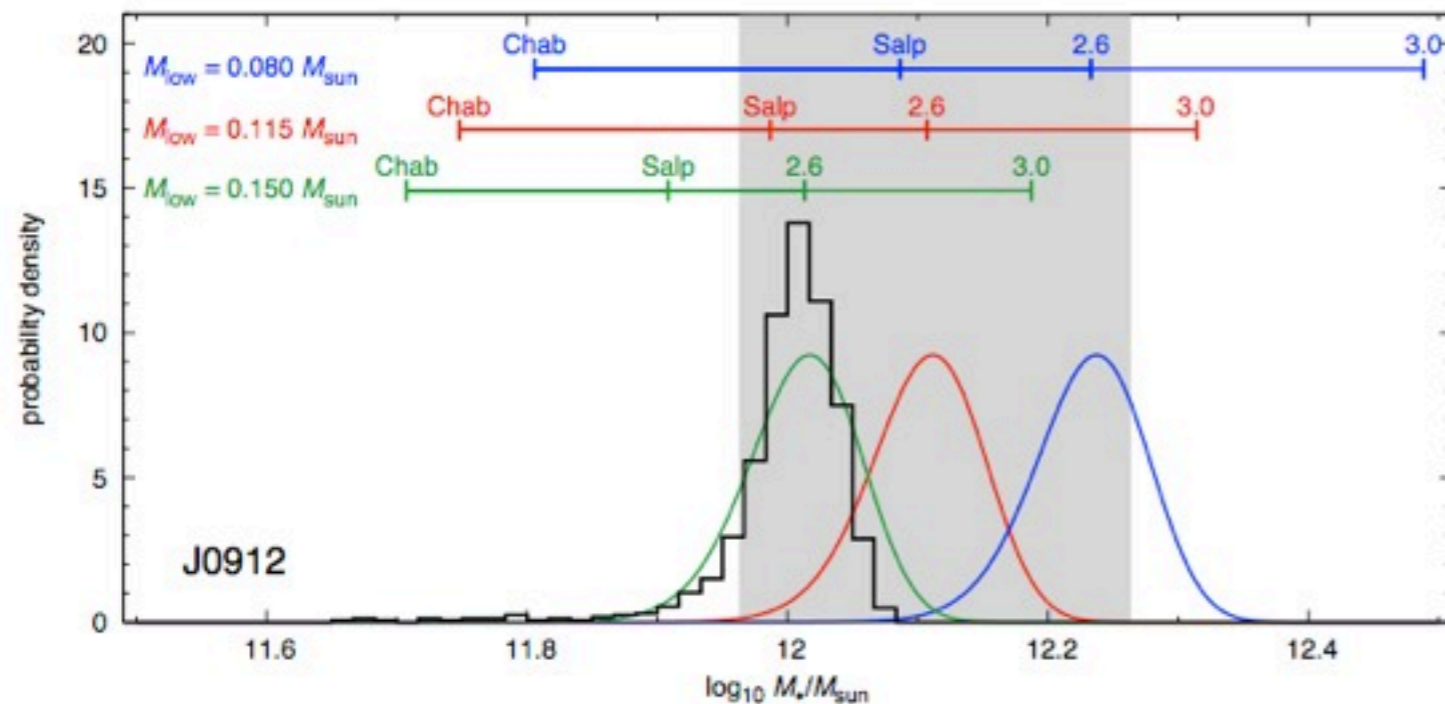
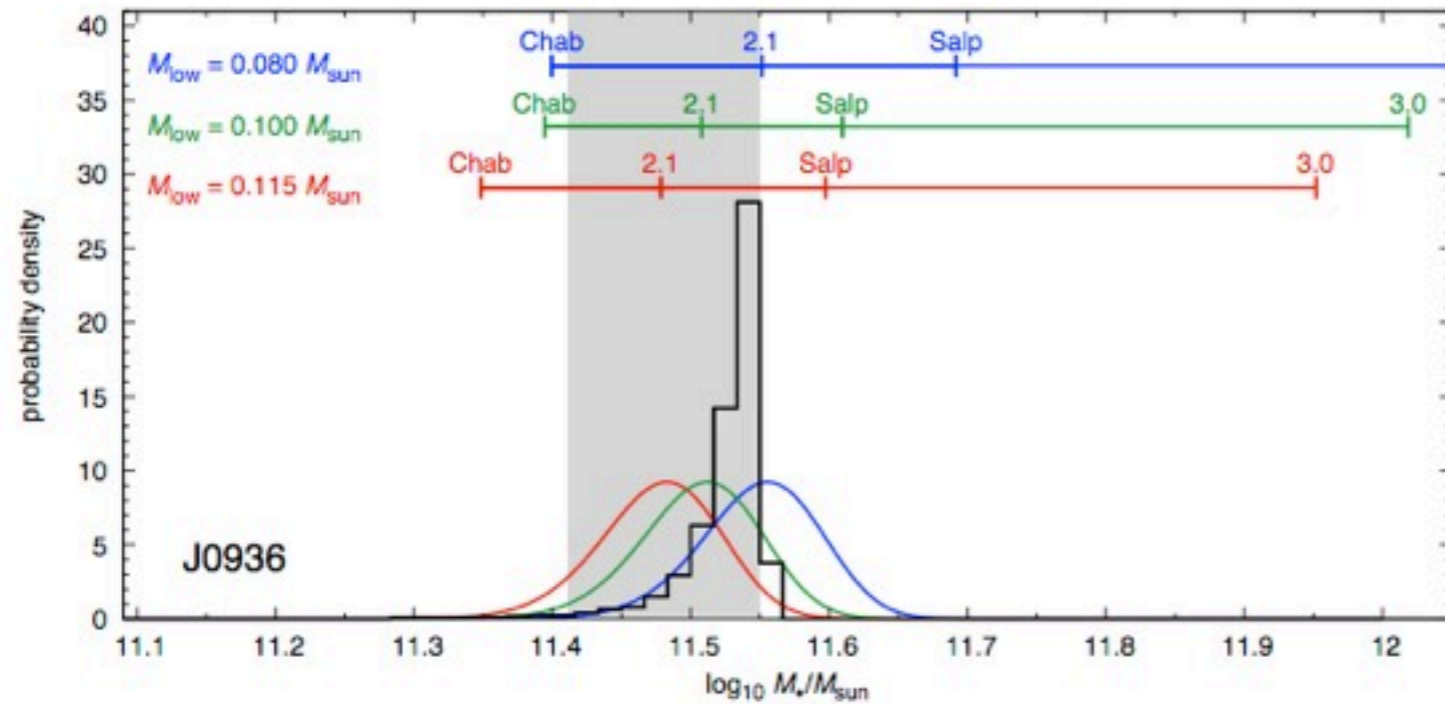
(see talk Barnabe)

L&D provides an excellent constraint on the stellar mass independent of M/L.

SSP provides a slope, but no lower mass cutoff. Combined M_{low} of the IMF can be determined.

$$\text{IMF } M_{\text{low}} = 0.12 \pm 0.03 M_{\text{sun}}$$

$$\text{IMF slope} = 2.21 \pm 0.14$$



Barnabe et al. 2013

Disk/Spiral Lens Galaxies

B1933+503: A disk-galaxy at $z=0.76$

Power-law models fit best. Only deV with $R_{\text{eff}}=19 \text{ kpc } h^{-1}$ fits, but that is much larger than observed.

2 quads + double

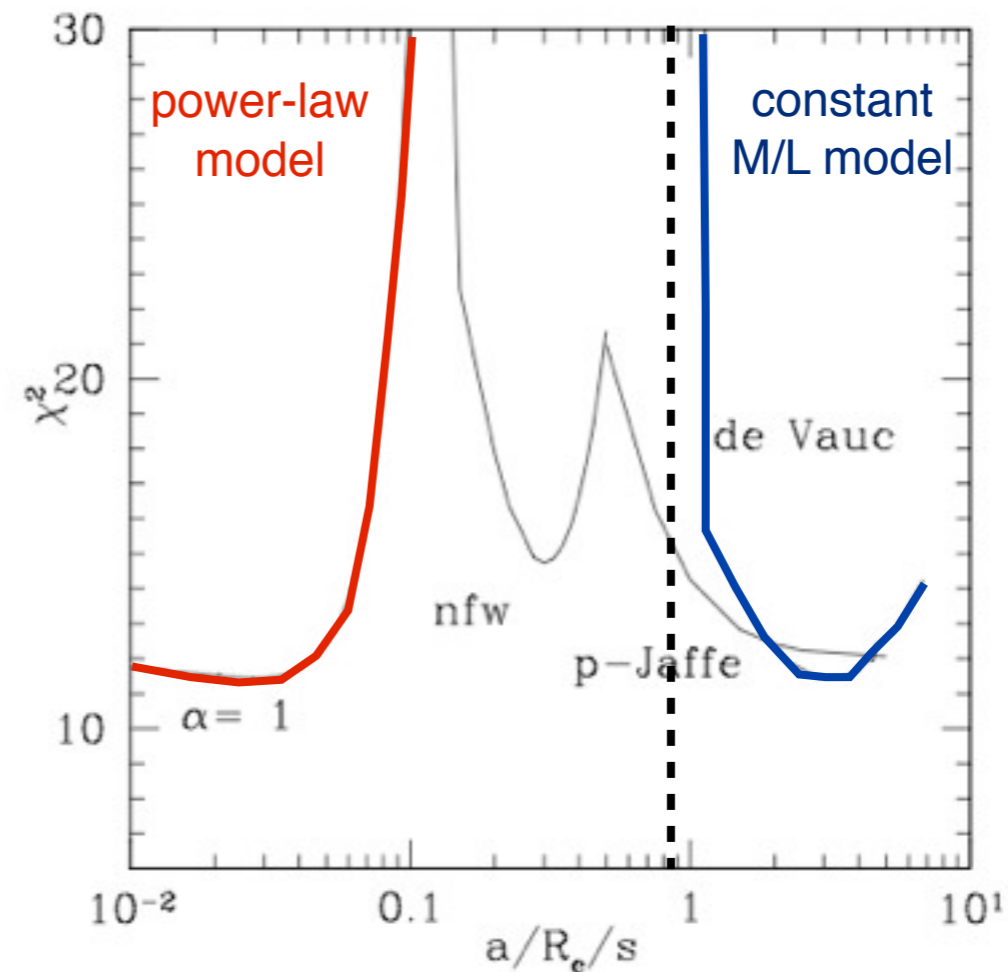
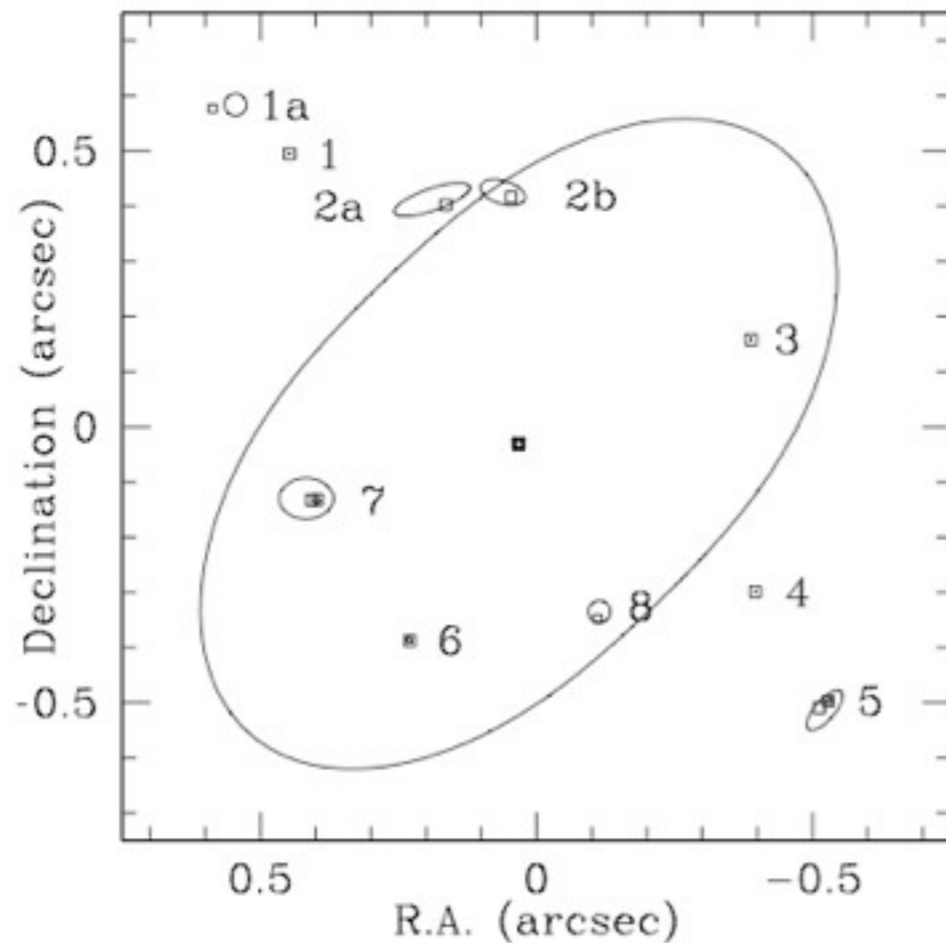
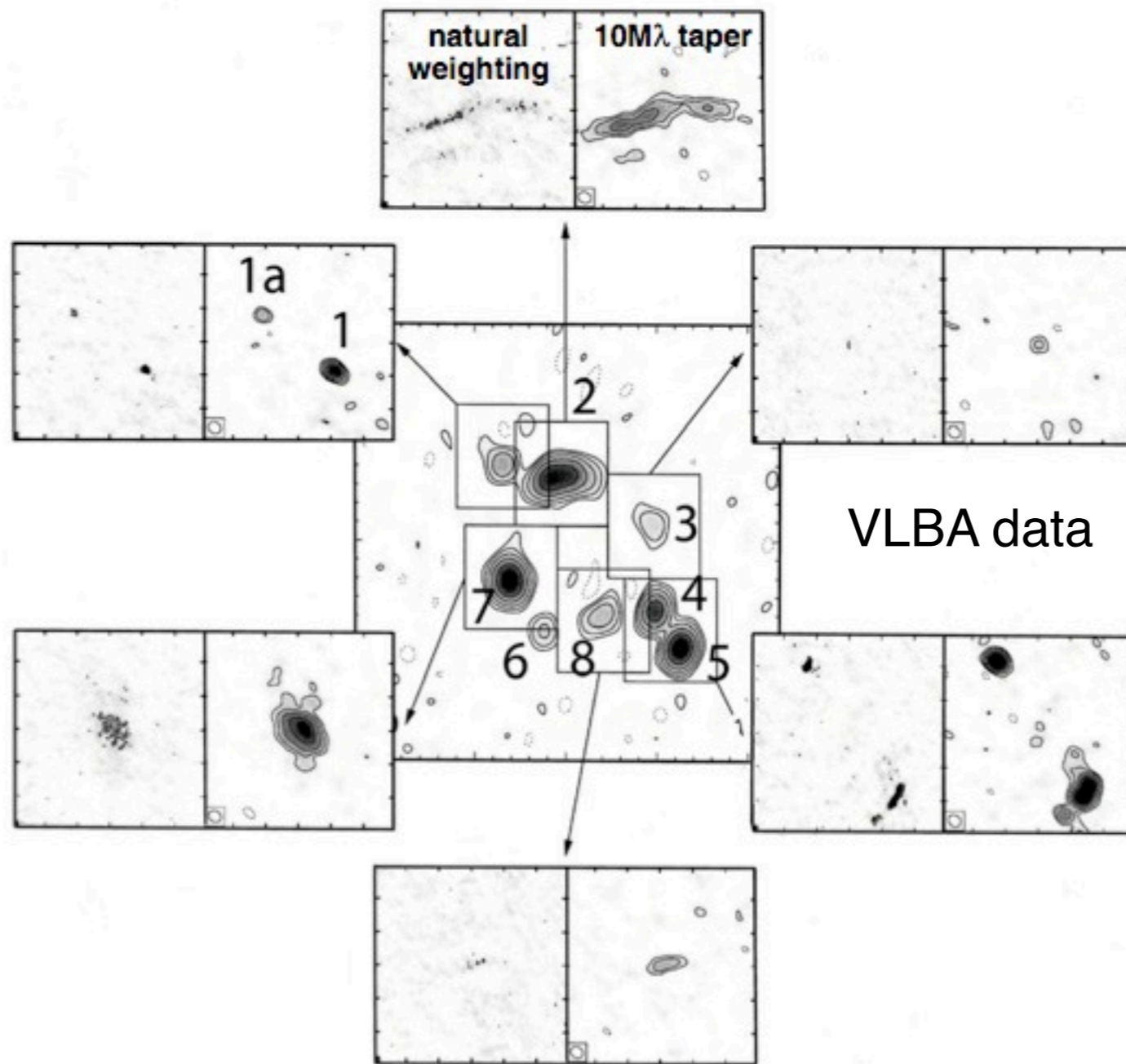


Table 2
Lens Galaxy Light

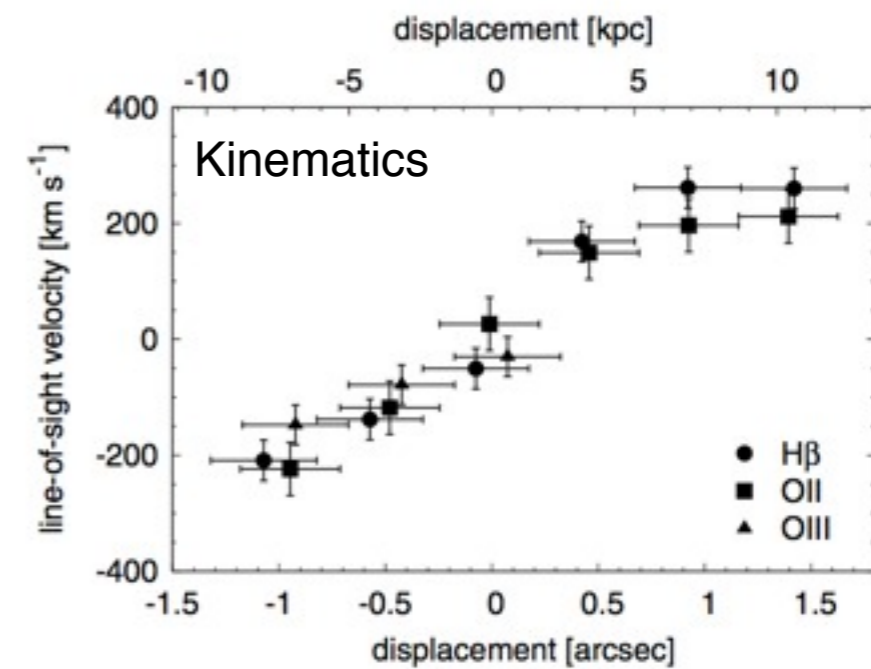
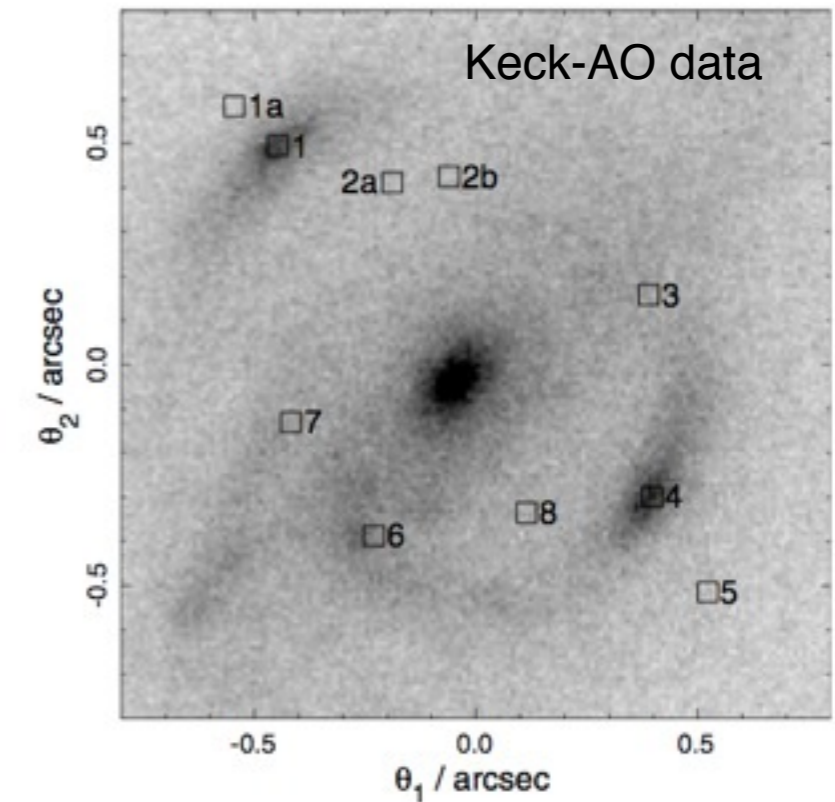
	$\Delta R.A.$ (arcsec)	$\Delta Decl.$ (arcsec)	R_c (arcsec)	n_{seraic}	q	ϕ ($^\circ$)
Disk	0.040 ± 0.005	-0.036 ± 0.005	0.85 ± 0.05	≈ 1	0.63 ± 0.06	138.0 ± 1.5
Bulge	0.040 ± 0.005	-0.036 ± 0.005	0.055 ± 0.006	≈ 1	0.41 ± 0.02	147 ± 3

Cohn et al. 2001

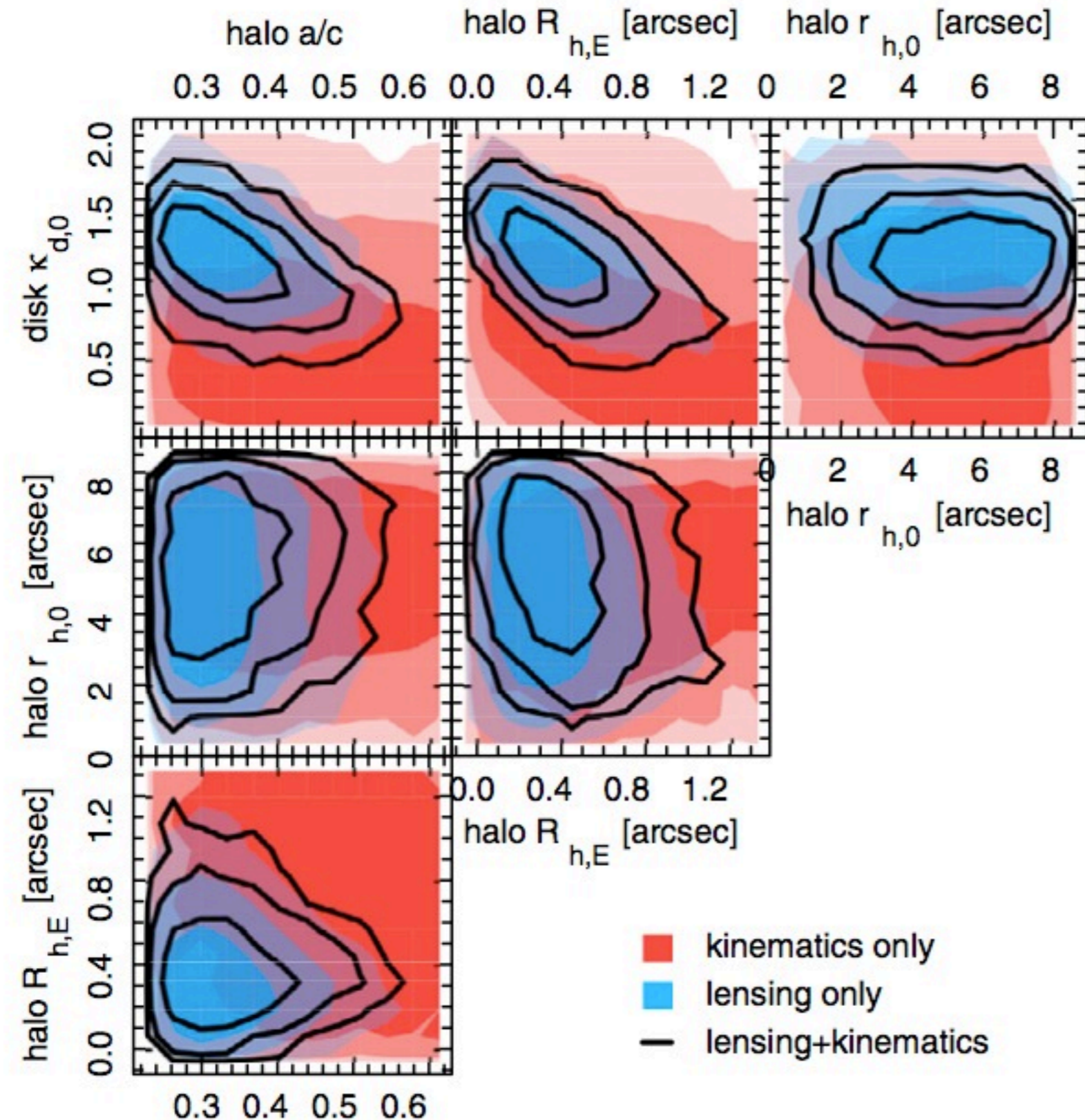
B1933+503: A disk-galaxy at $z=0.76$



Suyu et al. 2012



B1933+503: A disk-galaxy at z=0.76



Given both high-resolution VLBA and Keck-AO data plus kinematics, a disk+bulge+halo model can be constructed.

When marginalizing over disk+bulge one finds:

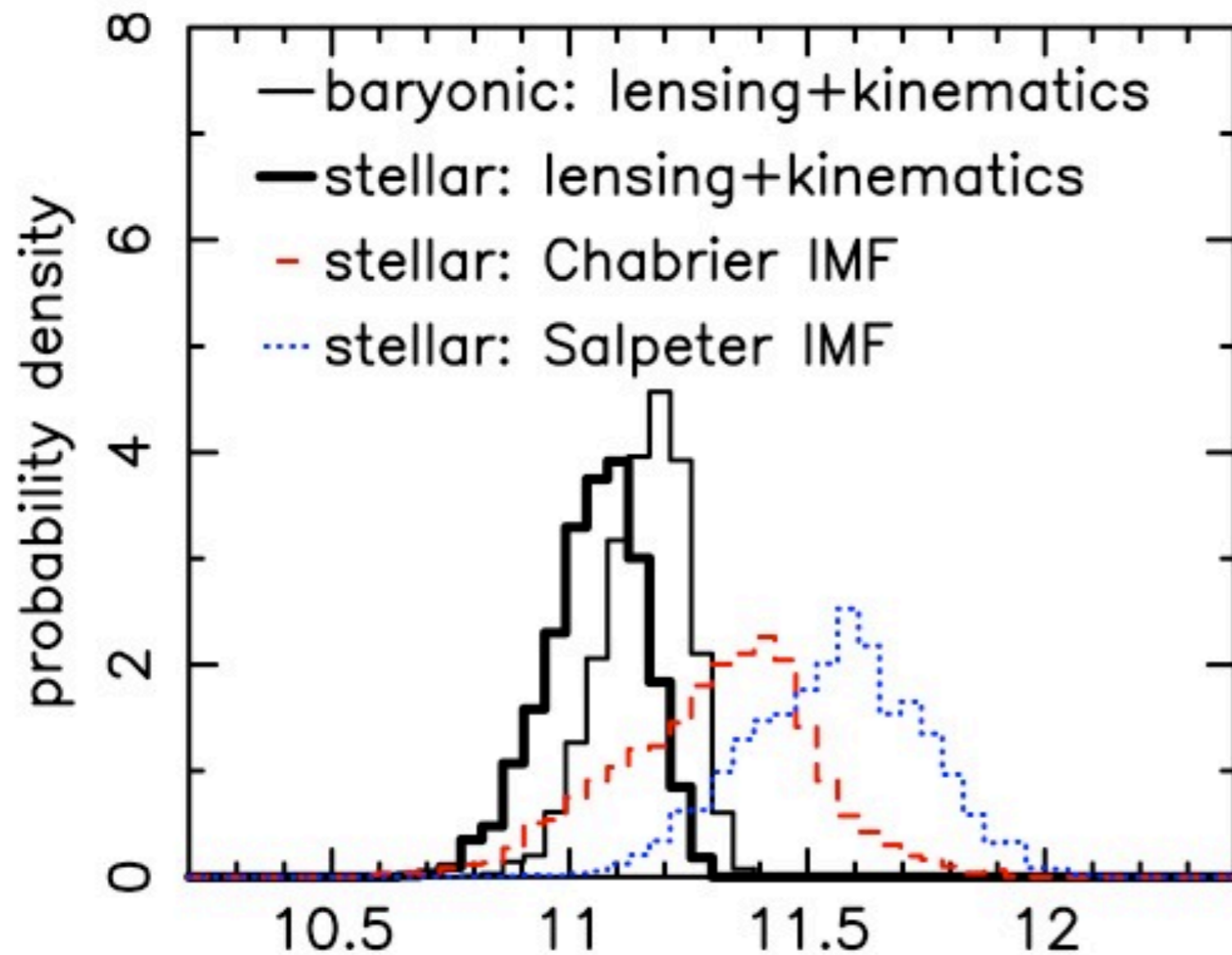
- (1) Disk contributed 0.76 ± 0.05 to V at $2.2 R_d$ and hence is marginally sub-max.
- (2) $f_{DM} = 0.43/0.37 \pm 0.09$ inside $2.2R_d/R_{eff}$
- (3) $(c/a)=0.3$ and $r_{h,0} > 16$ kpc
- (4) Chabrier IMF is preferred over Salpeter by 7.2 LH ratio.

$$\rho_h(r) = \frac{\rho_{h,0}}{(r/r_{h,0})(1+r/r_{h,0})^2},$$

$$r^2 = c^2 \left(\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} \right), \quad a \leq b \leq c.$$

Suyu et al. 2012

B1933+503: A disk-galaxy at $z=0.76$



Given both high-resolution VLBA and Keck-AO data plus kinematics, a disk+bulge+halo model can be constructed.

When marginalizing over disk+bulge one finds:

- (1) Disk contributed 0.76 ± 0.05 to V at $2.2 R_d$ and hence is marginally sub-max.
- (2) $f_{DM} = 0.43/0.37 \pm 0.09$ inside $2.2R_d/R_{eff}$
- (3) $(c/a)=0.3$ and $r_{h,0} > 16$ kpc
- (4) Chabrier IMF is preferred over Salpeter by 7.2 LH ratio.

$$\rho_h(r) = \frac{\rho_{h,0}}{(r/r_{h,0})(1+r/r_{h,0})^2},$$

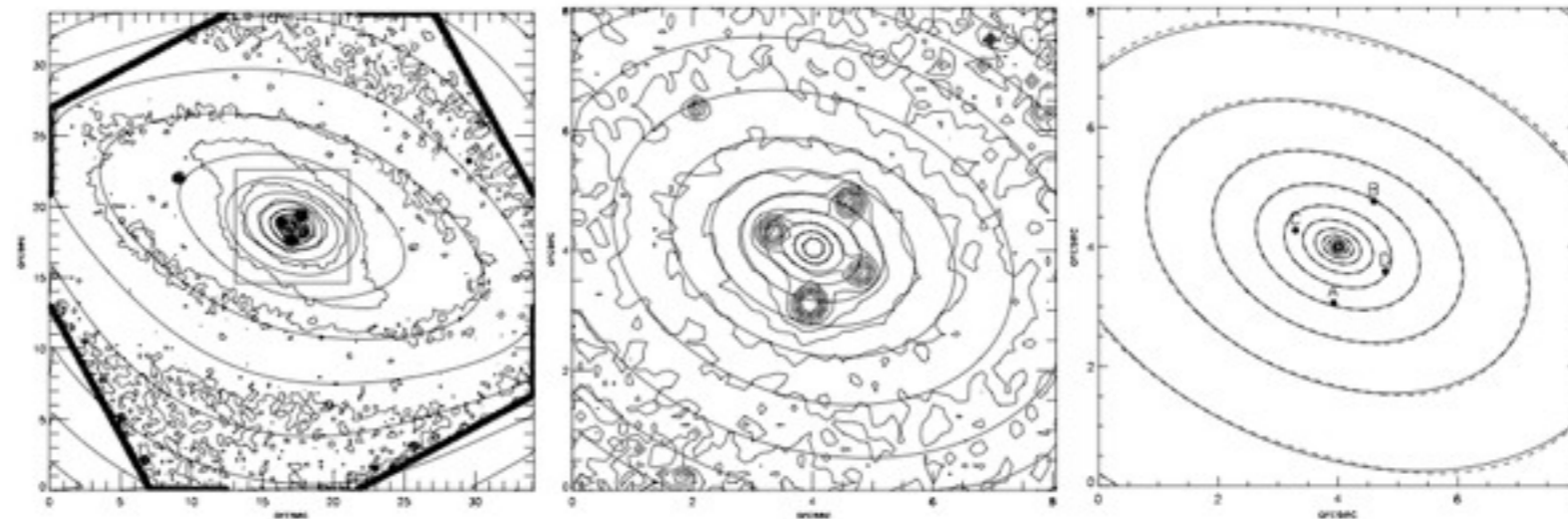
$$r^2 = c^2 \left(\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} \right), \quad a \leq b \leq c.$$

Suyu et al. 2012

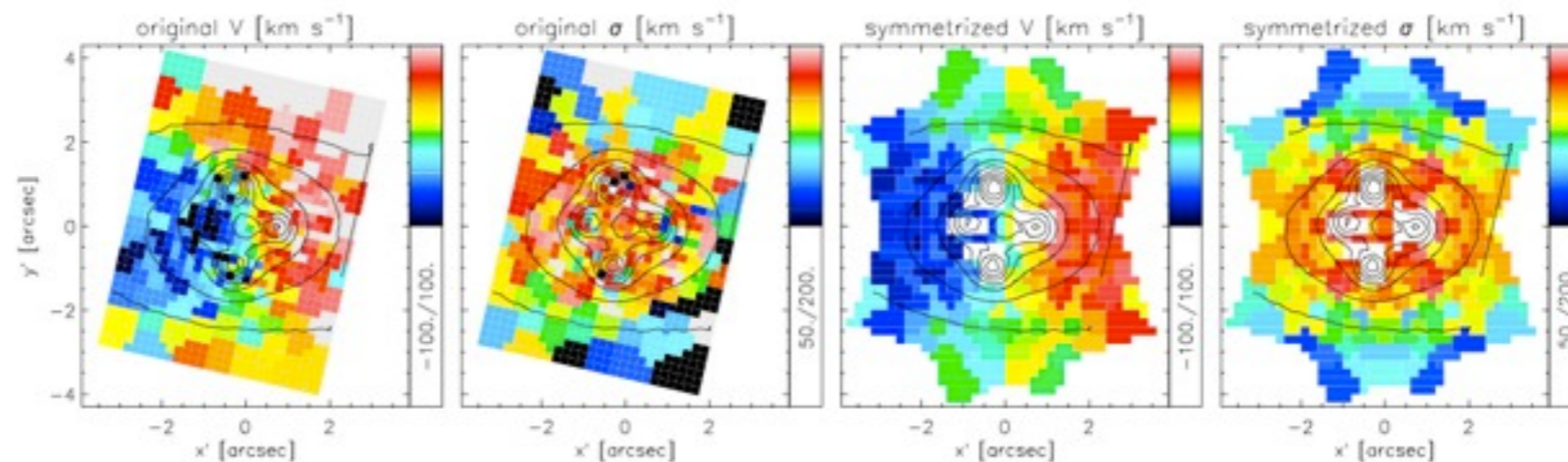
Q2237+0305: A disk-galaxy at $z=0.04$

The Einstein Cross is a spiral galaxy with a lensing bulge. DM should (in principle) play a minor role in the inner regions of this system

HST data



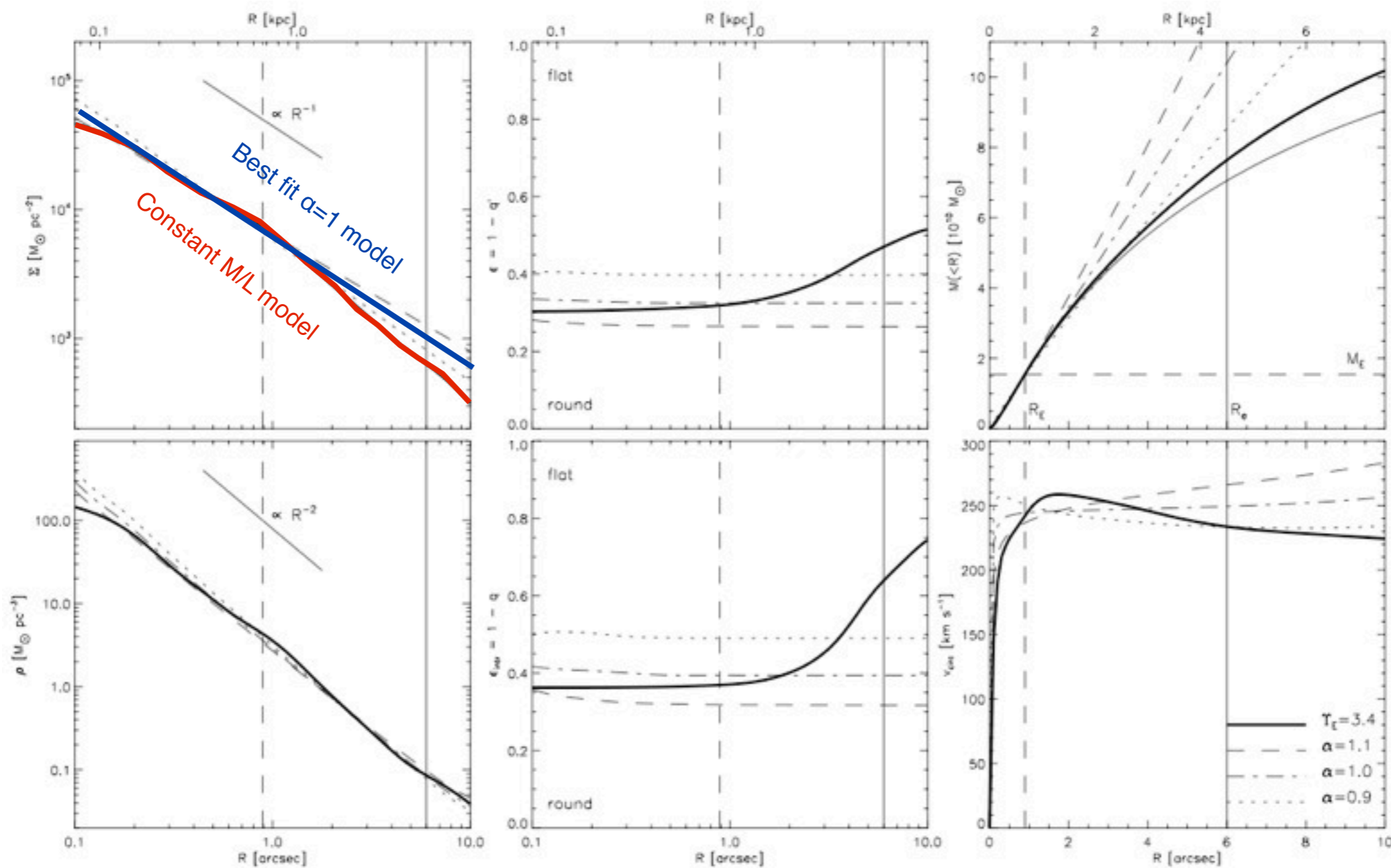
Sauroon data



van de Ven et al. 2010

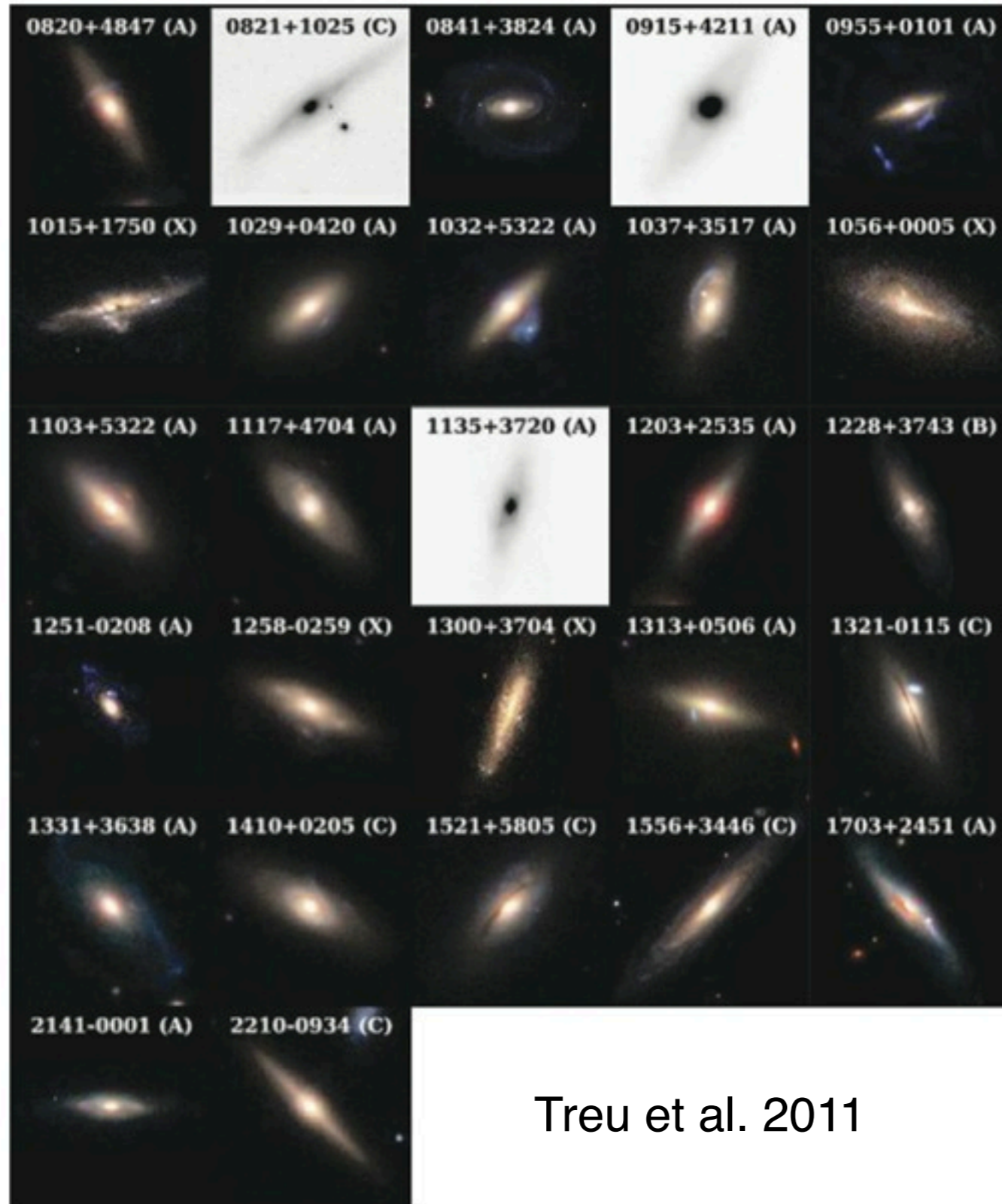
Q2237+0305: A disk-galaxy at $z=0.04$

Very little dark matter (<20%) in the bulge:
a sanity check on methodology.



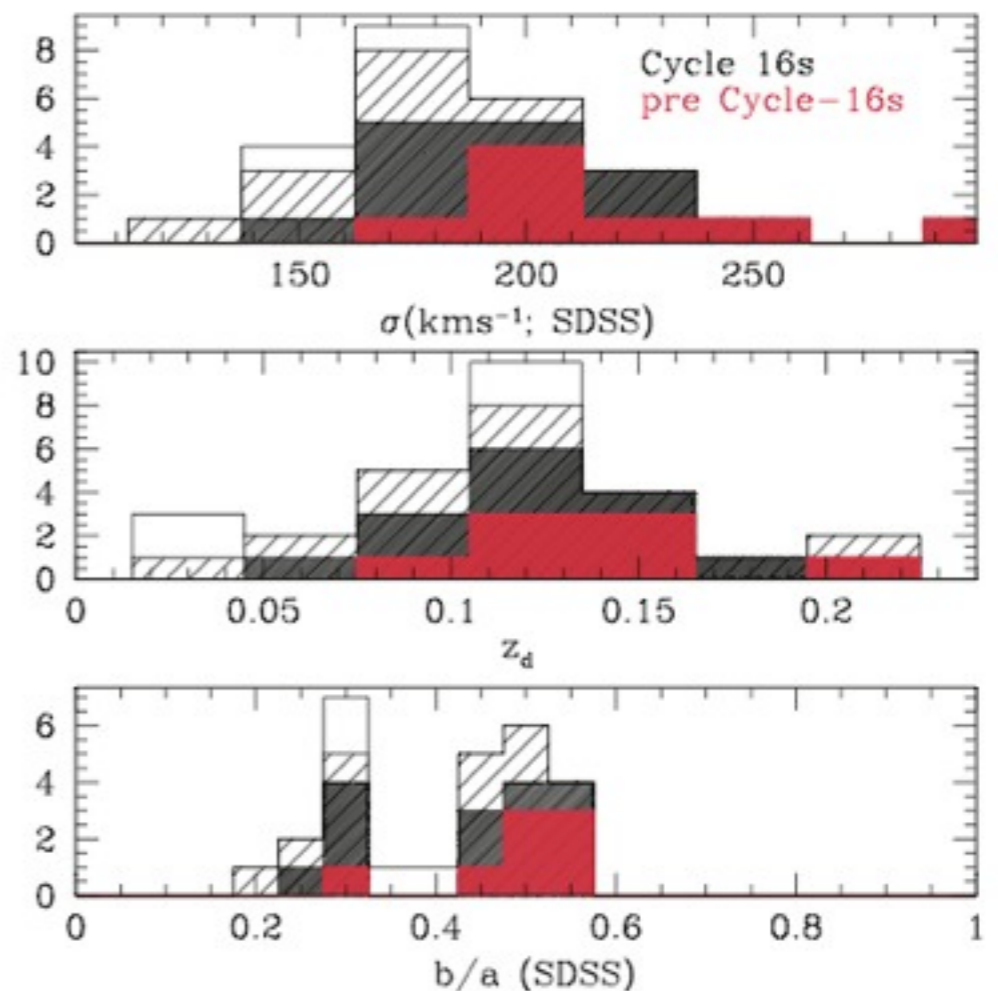
van de Ven et al. 2010

The SWELLS Survey - Disk-Galaxy Lenses



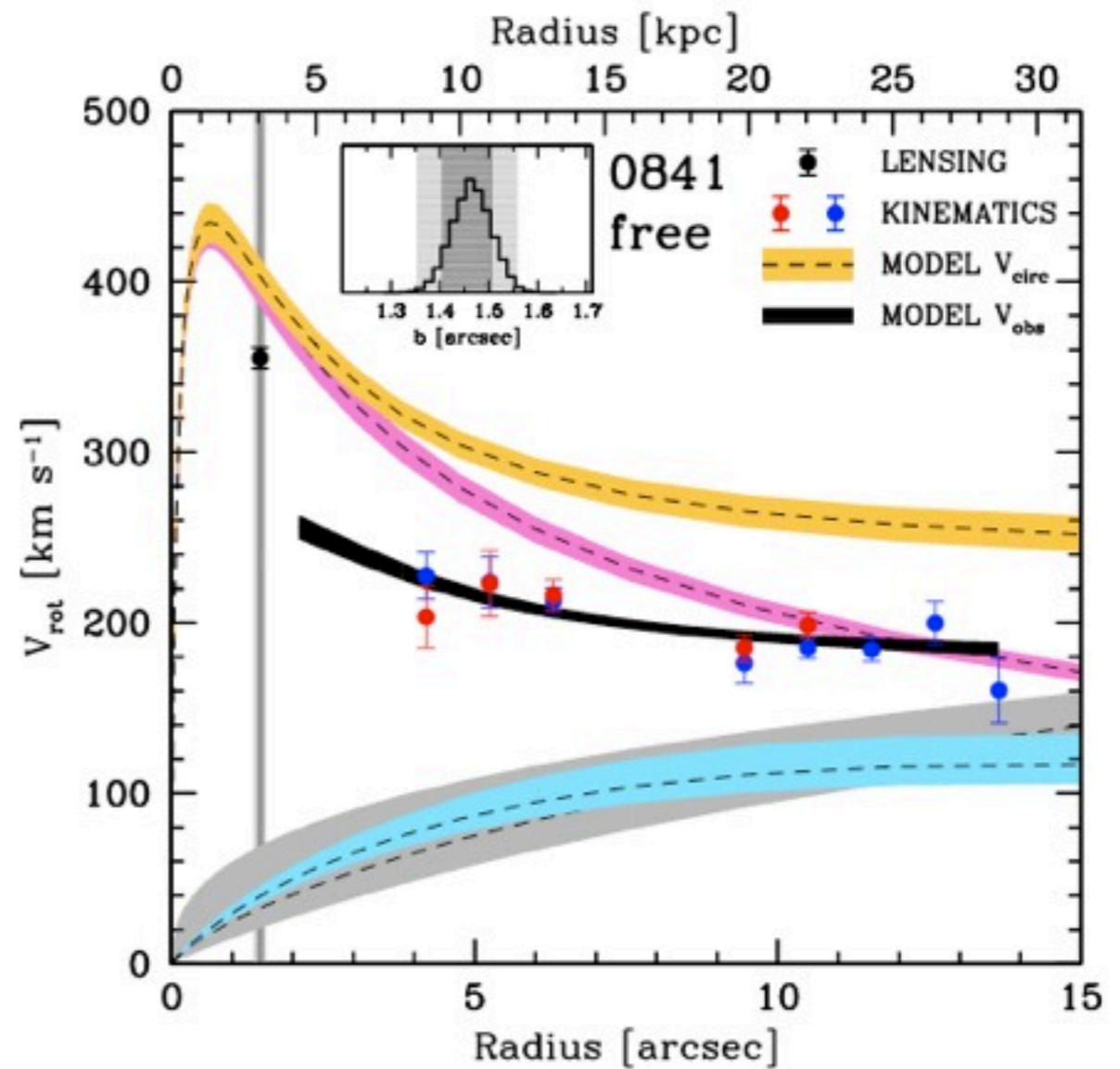
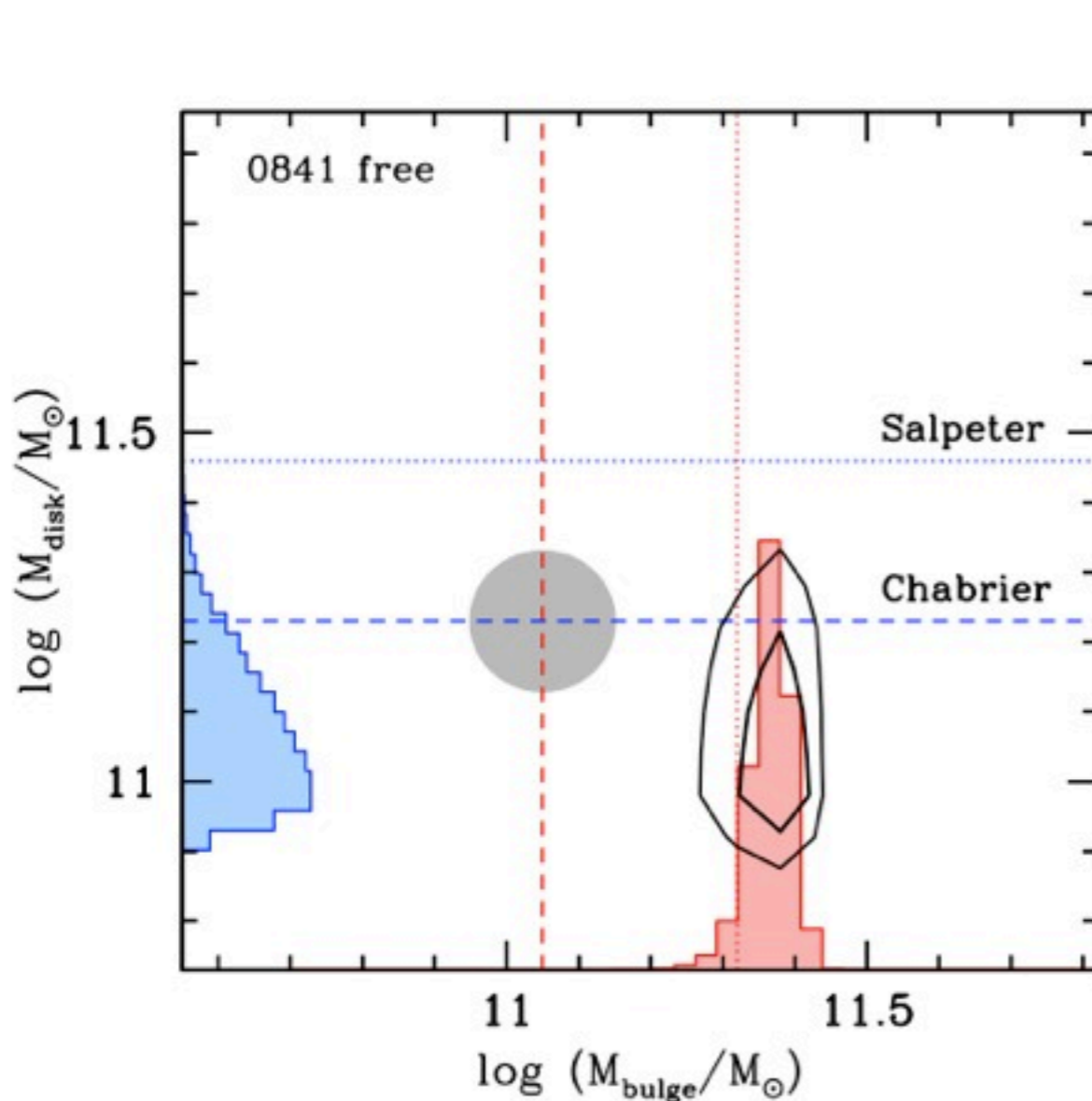
Treu et al. 2011

Highly-inclined disk galaxies selected from SDSS. Follow-up with HST, Keck-AO and Keck-spectroscopy.



The SWELLS Survey - Disk-Galaxy Lenses

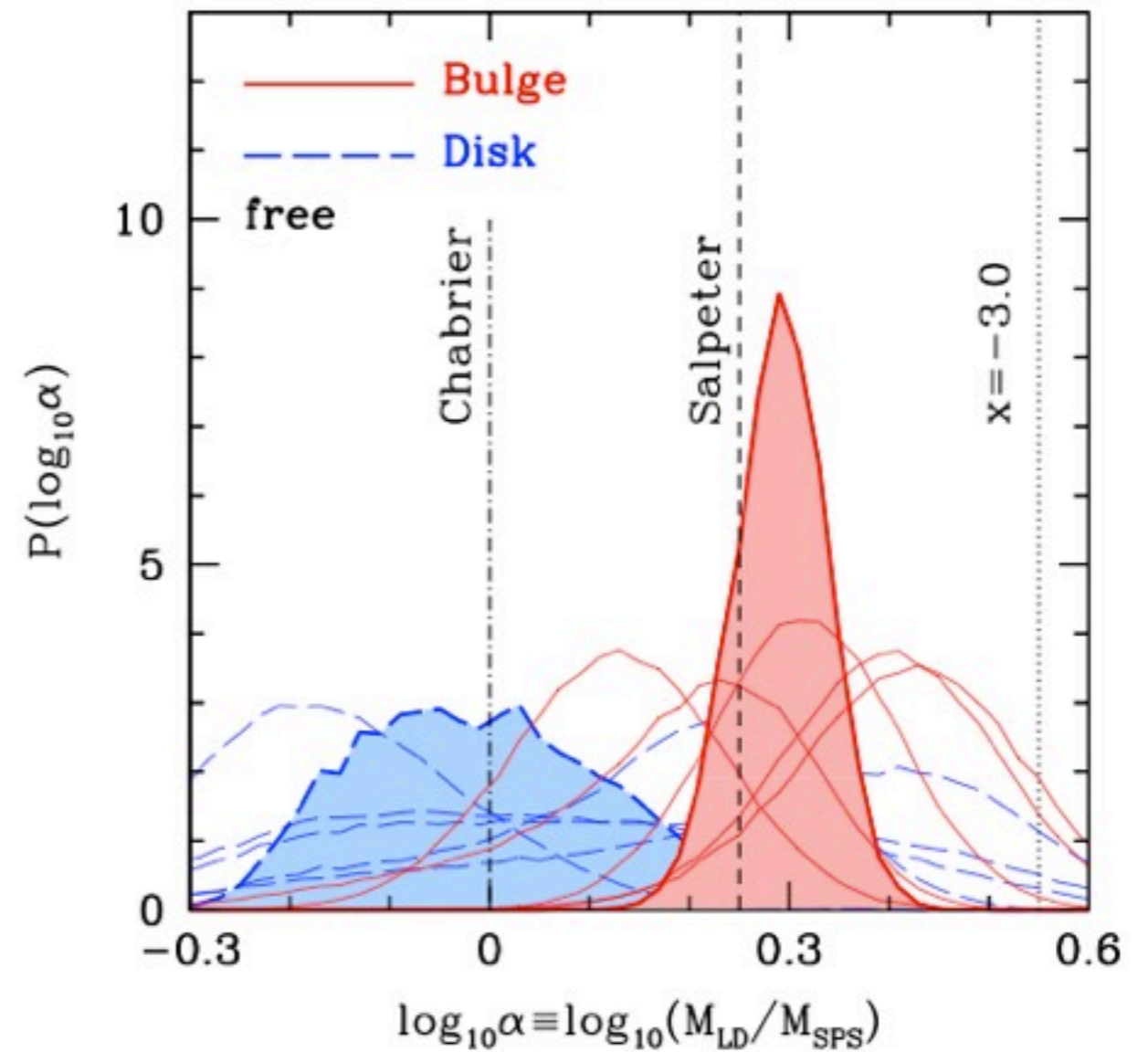
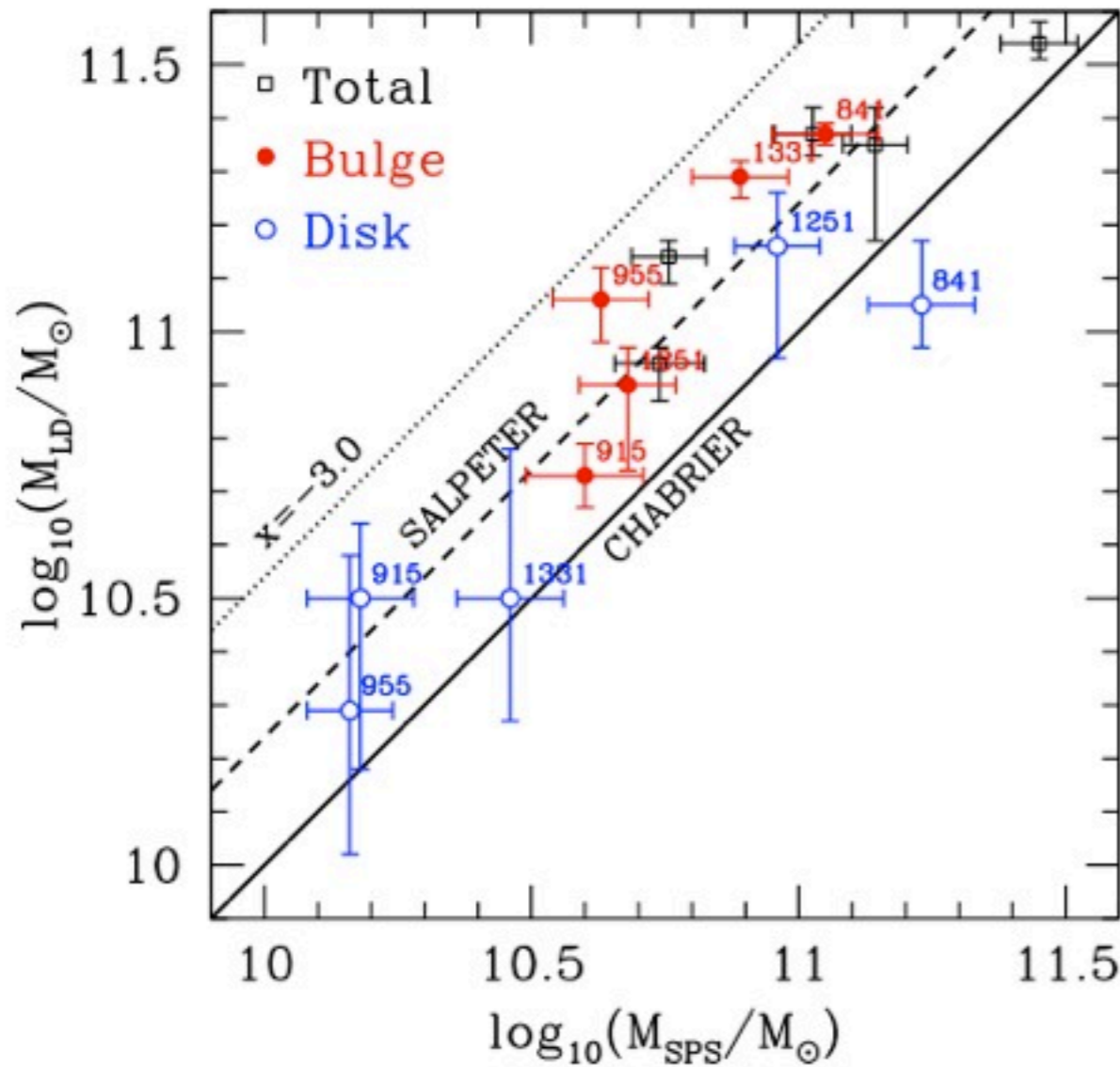
Joint lensing & dynamical provide a stellar mass for the disk and the bulge. SPS modeling predict M/L value.



Dutton et al. 2012

The SWELLS Survey - Disk-Galaxy Lenses

Constraints on the **bulge** are quite tight and show a **Salpeter IMF**.
Disk masses are less well measured but jointly **Chabrier** is preferred.



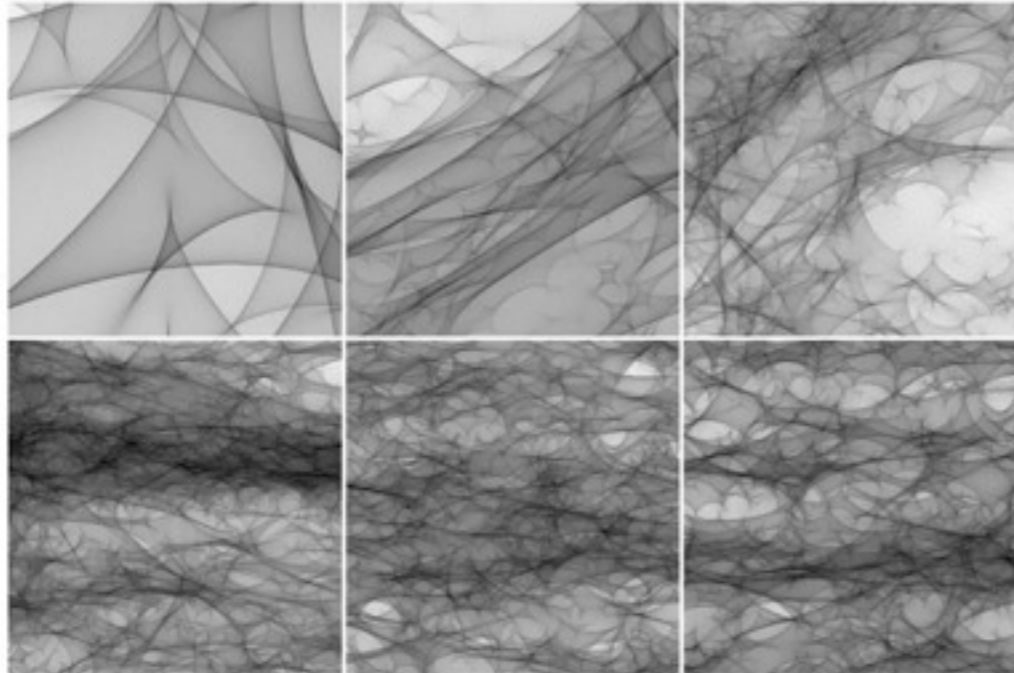
Dutton et al. 2012

Constraint on Stellar & Dark Matter from Microlensing in Strong lenses

Strong-lensing+Microlensing evidence for dark-matter in galaxies

At the lensed image position, the magnification PDF due to stellar ML depends strongly on the fraction of DM in the line-of-sight for FIXED total surface density (from SL).

Caustic networks with increasing microlensing optical depth but fixed surface density (DM+stars)



High ML optical depth

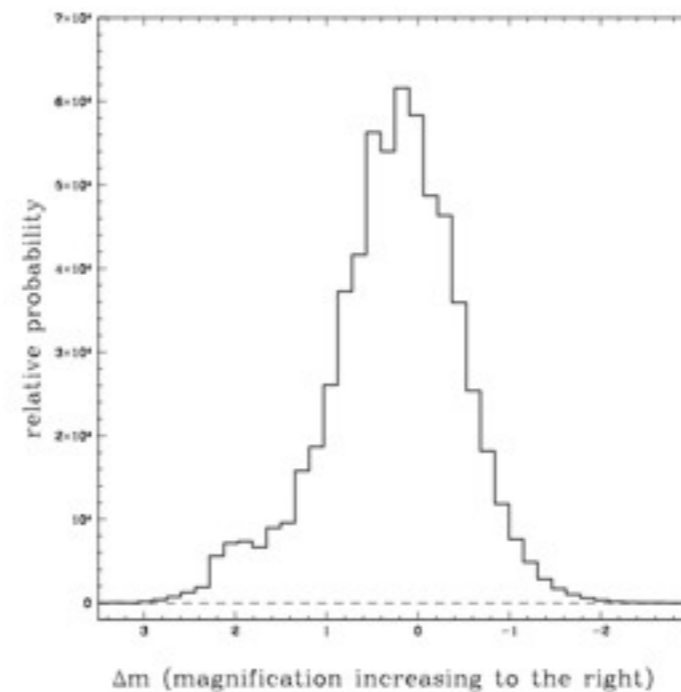


FIG. 2a

Low ML optical depth

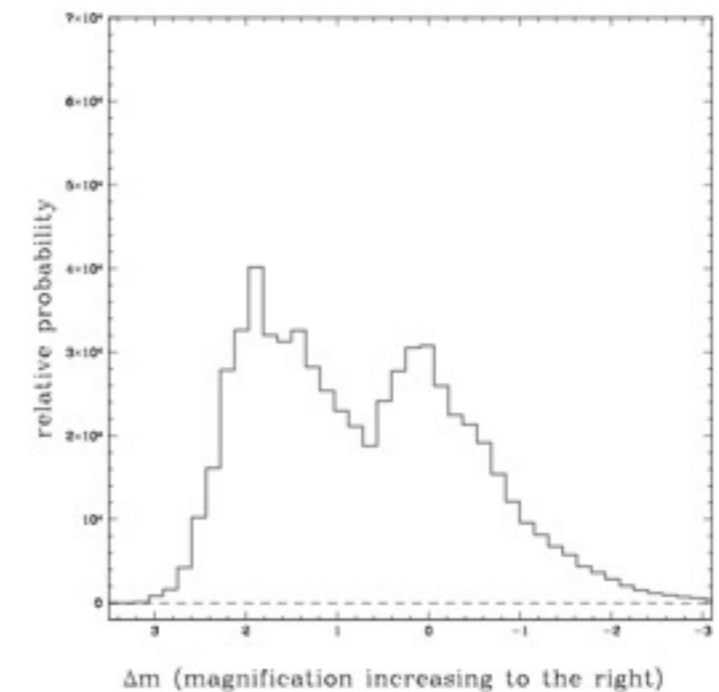


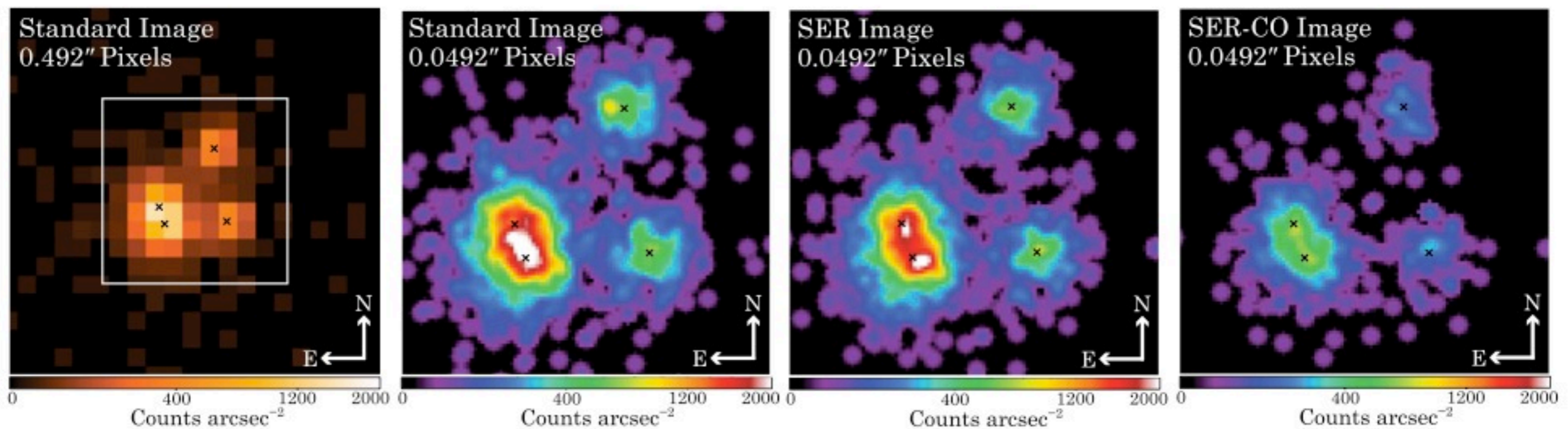
FIG. 2b

Schechter & Wambsganss 2004

Strong-lensing+Microlensing evidence for dark-matter in galaxies

This technique can be applied to either ML light curves of single systems or to an ensemble of single-epoch observations of a sample of lenses.

PG1115+080

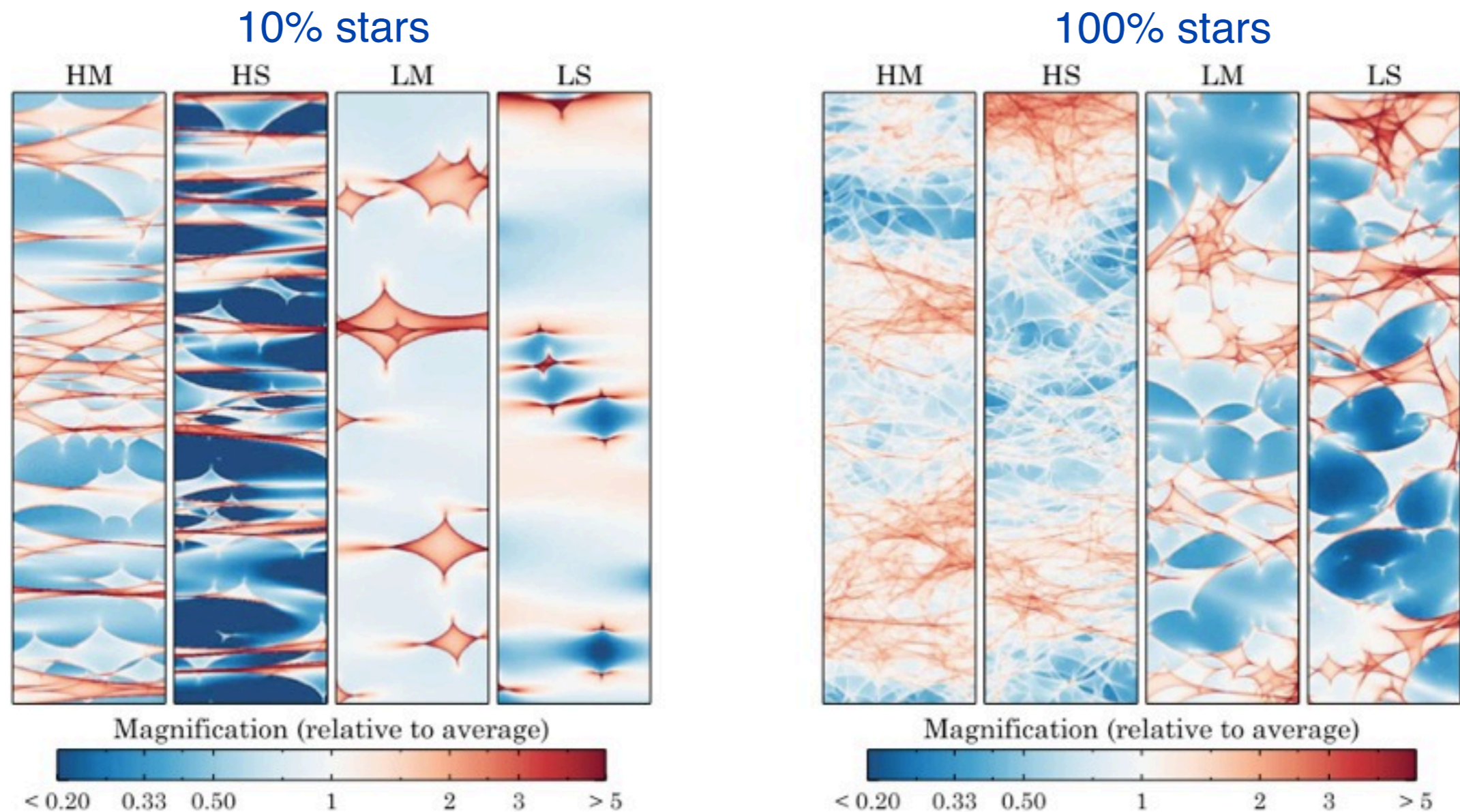


Pooley et al. 2012

Strong-lensing+Microlensing evidence for dark-matter in galaxies

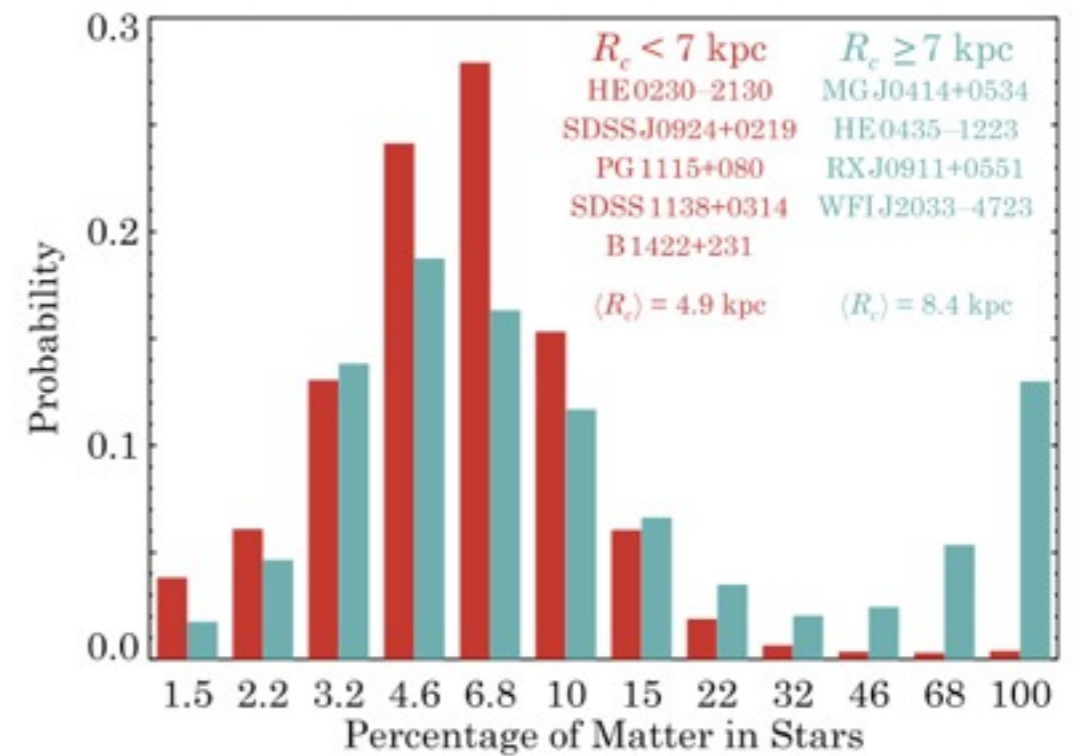
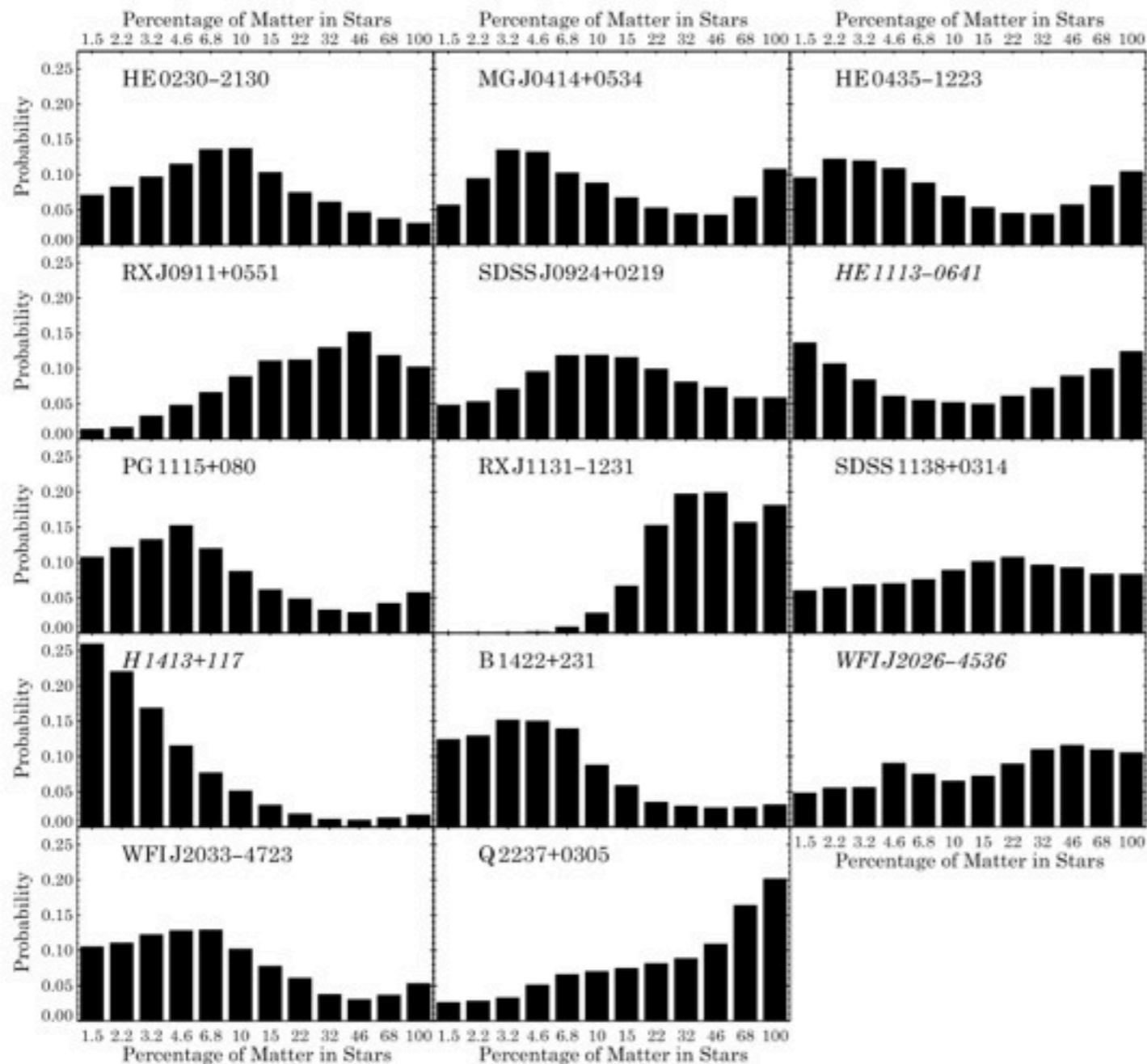
Caustic patterns for all 4 lensed images in PG1115+080 for two different stellar surface densities (the total density is obtained from the SL model).

PG1115+080



Pooley et al. 2012

Strong-lensing+Micro-lensing evidence for dark-matter in galaxies

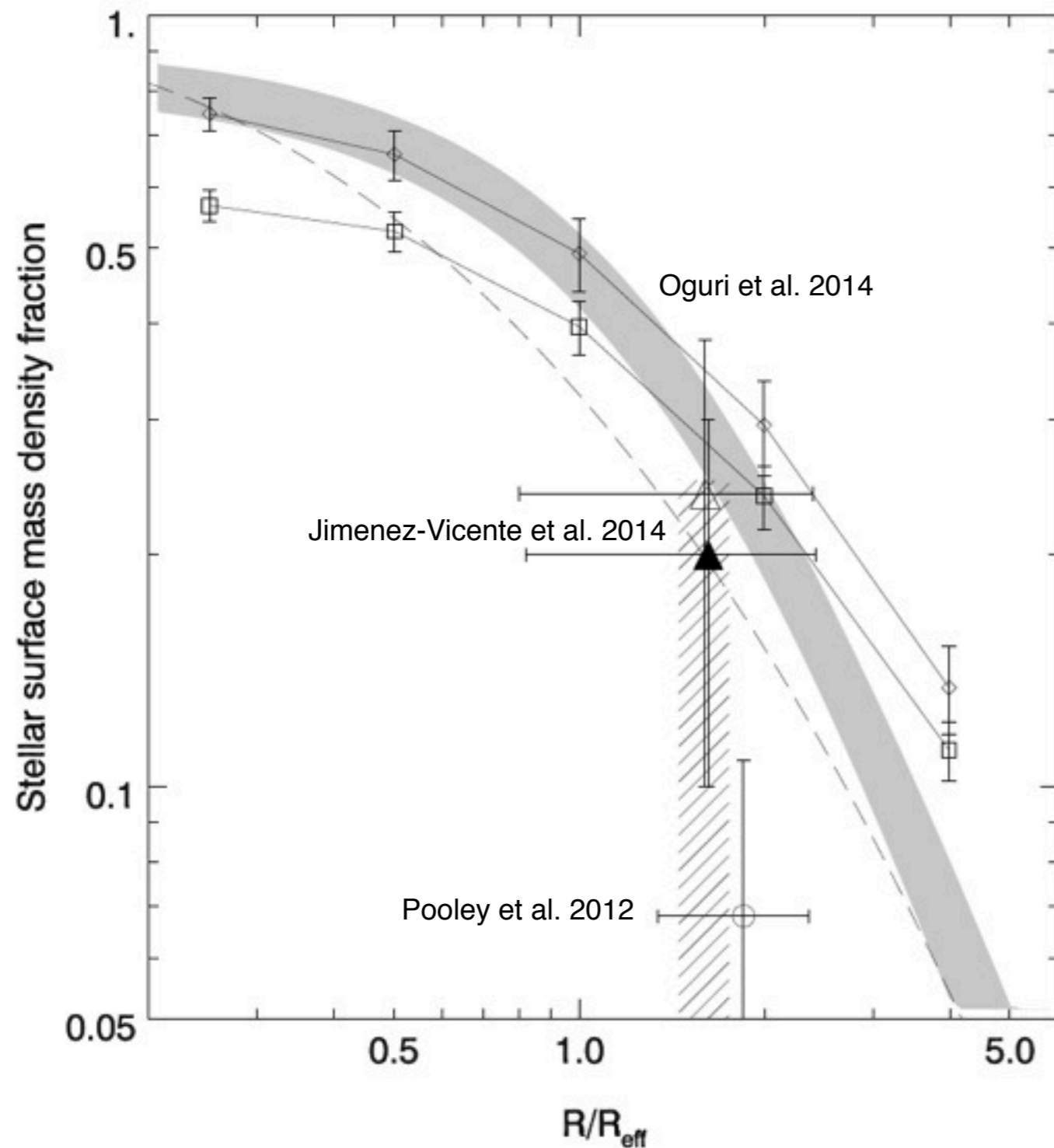


Based on 14 systems and 61 epochs, a Bayesian analysis give that 93% of the surface density is in DM at $\langle R \rangle = 6.6$ kpc.

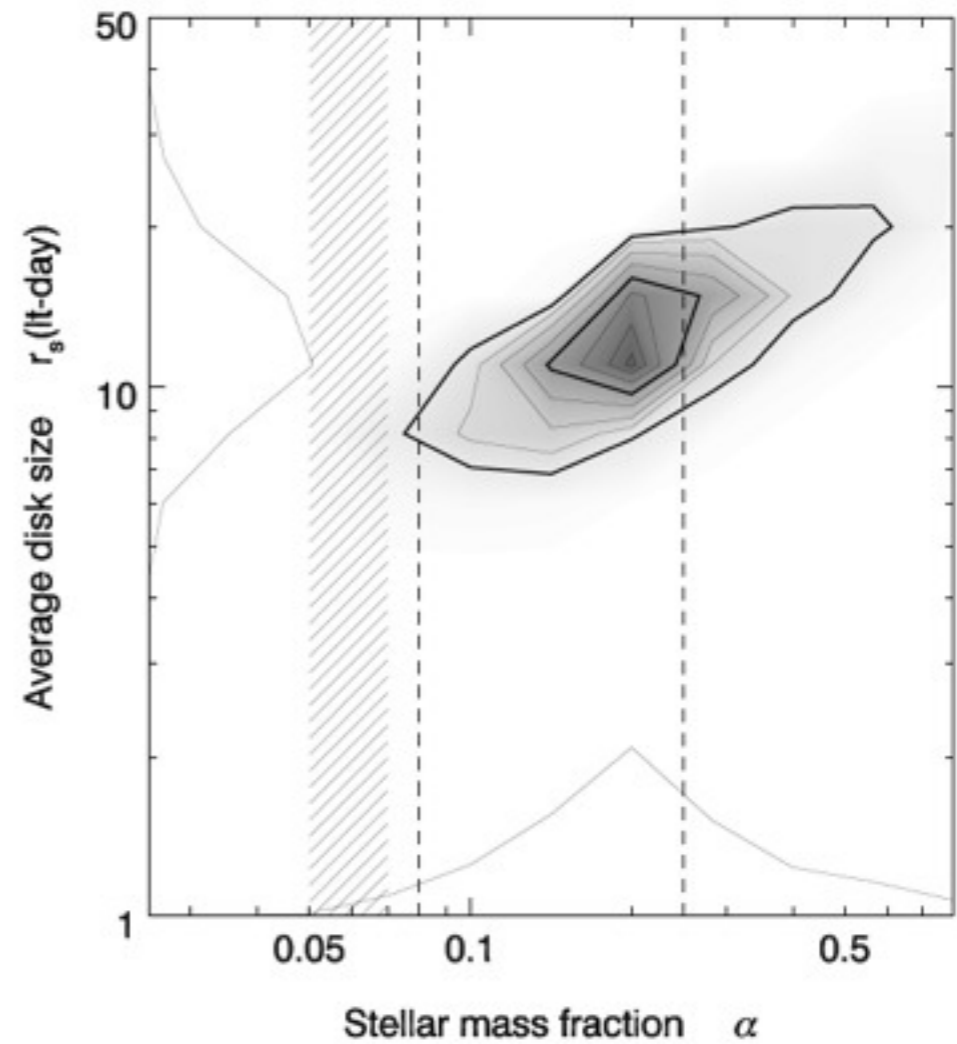
Pooley et al. 2012

Percentage of matter in stars

Strong-lensing+Micro-lensing evidence for dark-matter in galaxies



Accretion disk size degeneracy



Projected DM fraction at $R_{\text{eff}} \sim 80\%$

Jimenez-Vicente et al. 2014

Conclusions

- There is conclusive evidence for DM from strong lenses in both early and late-type galaxies from lensing alone, even more so in combination with dynamics, stellar population studies and micro-lensing.
- In ETG the fraction of DM inside R_{eff} seems to increase with galaxy mass and ranges between 40-80% inside $R_{\text{eff}}/2$ in projection for a fixed/universal IMF.
- Evidence is strong that the IMF varies over the $\sigma^*=150\text{-}350$ km/s range for ETGs which has implications for lensing DM studies and scaling relations.
- Evidence for a varying IMF with galaxy mass flattens the f_{DM} trend to a fraction of $f_{\text{DM}}=40\pm 10\%$ inside $R_{\text{eff}}/2$ from $\sigma^*=150\text{-}350$ km/s
- The DM density slope inside $R_{\text{Einst/eff}}$ is around 1.3-1.7, steeper than NFW.
- The overall stellar+DM profile is consistent with an adiabatically contracted NFW for Salpeter-like IMFs.
- SL+WL suggest an approximate deV+NFW = $\rho \sim r^{-2}$ total density profile over $1\text{-}100R_{\text{eff}}$

The future of SL studies of galaxies is bright but it (i) requires much larger sample for continual progress and (ii) must possibly re-focus on more unique or complementary science cases.



Lensed Source

Thanks

Stars

Satellites

Dark Matter

19 November 2014, IPMU Tokyo, Japan