



# Mass distribution in galaxy clusters: strong lensing and dynamical mass analysis

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A. Zitrin, M. Meneghetti, D. Coe, J. Merten, and CLASH Team.

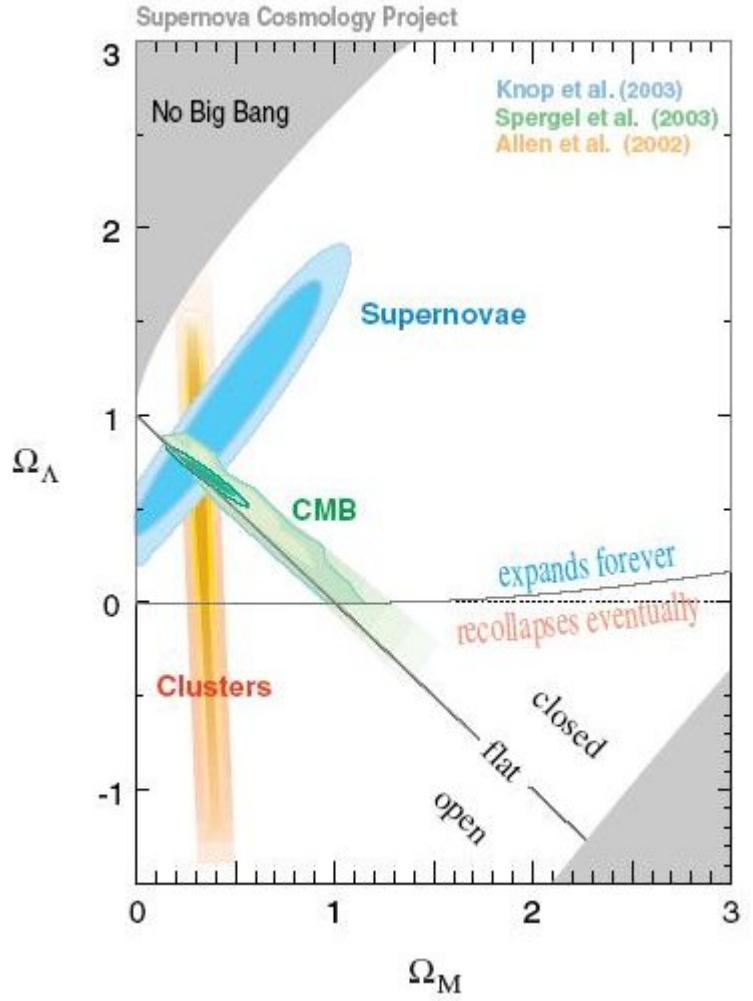
# Cosmological Framework



- Current observational constraints support:
  - flat Universe  $\Omega = \Omega_\Lambda + \Omega_M \sim 1$
  - dark energy component  $\Omega_\Lambda \sim 0.7$
  - matter density component  $\Omega_M \sim 0.3$
  - Hubble constant  $H_0 \sim 70 \text{ km s}^{-1}\text{Mpc}^{-1}$

$$H^2(z) = H_0^2 [\cancel{\Omega_r}(1+z)^4 + \Omega_M(1+z)^3 + \cancel{\Omega_k}(1+z)^2 + \Omega_\Lambda]$$

$$H^2(z) = H_0^2 [\Omega_M(1+z)^3 + \Omega_\Lambda]$$



## *Matter density component – Dark matter*

- The largest objects which are small enough to have come into dynamical equilibrium.
- The smallest objects which are big enough to contain a fair sample of the materials in the Universe, particularly of baryonic and non-baryonic matter.

**~ 80 - 85 %**  
**is Dark Matter (DM)**



## Mass measurements: velocity dispersion

- Scaling relations: the velocity distribution of galaxies can be converted into mass estimates.

$$M_{200} = \frac{10^{15}}{h(z)} \left( \frac{\sigma_{DM}}{\sigma_{15}} \right)^{1/\alpha} M_{\odot}$$

$$b_v \equiv \frac{\sigma_{gal}}{\sigma_{DM}} \Rightarrow \langle b_v \rangle_{sim} = 1.00 \pm 0.05$$

Evrard et al. (2008)

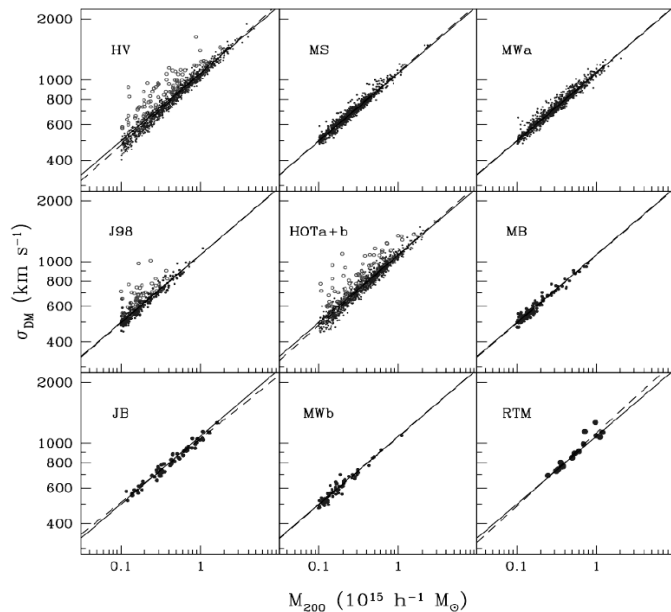
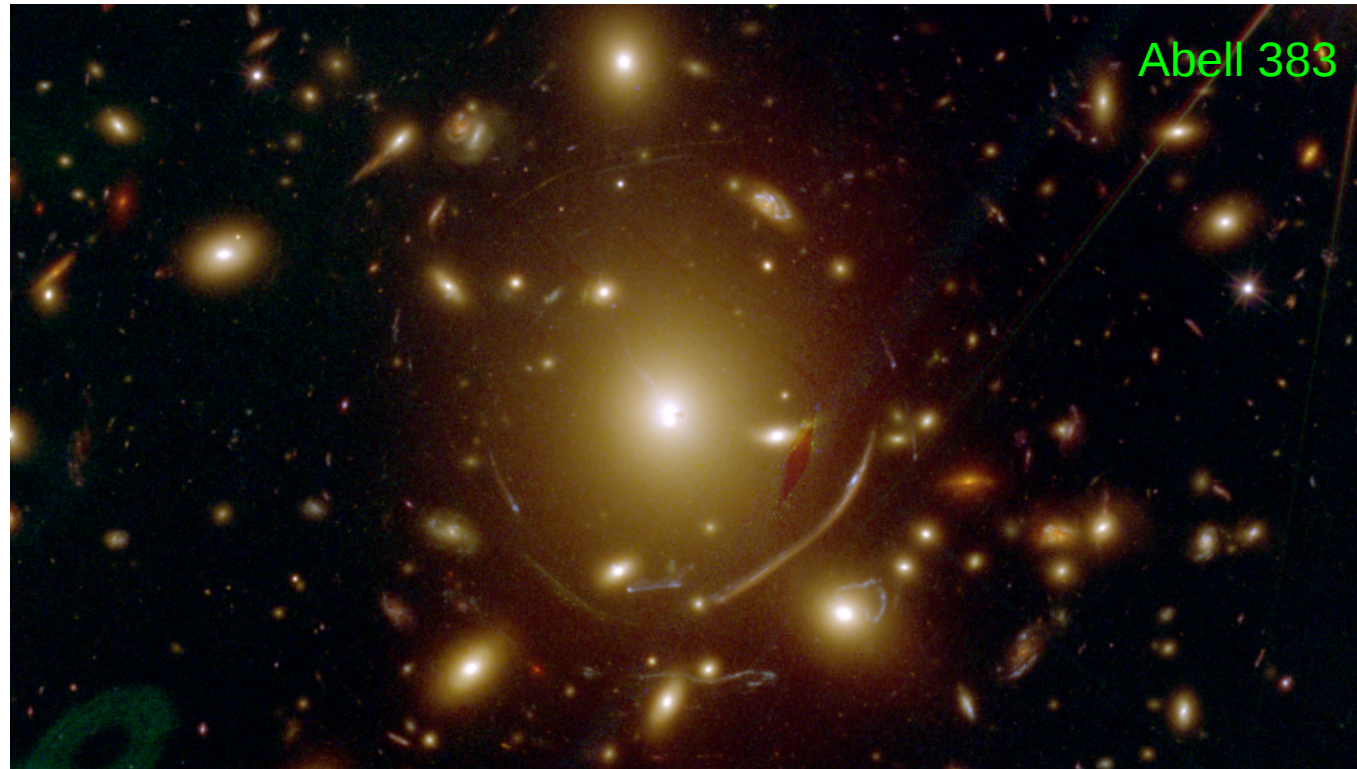
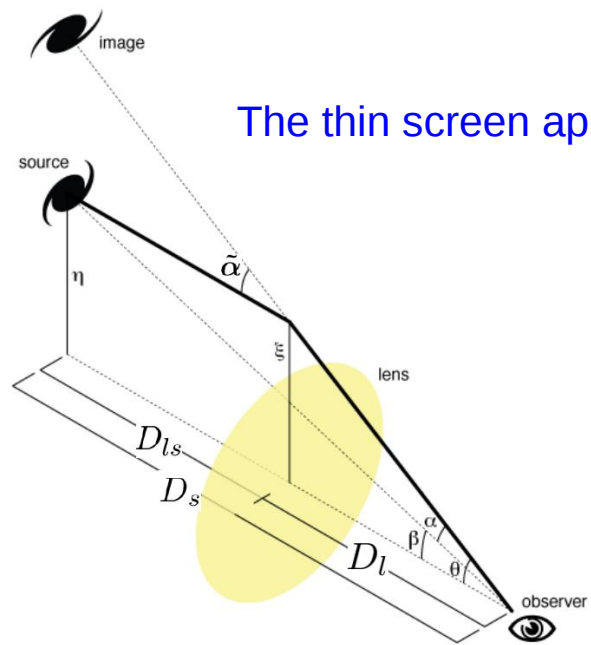


FIGURE 2.12: The figure shows the  $\sigma_{DM} - M_{200}$  relation for several cosmologies, as well as the “universal” best-fit previously described by Eq. 2.50. This figure was taken from Evrard et al. (2008)



## Mass measurements: strong lensing (SL)

- Gravitational lensing is the most robust way to probe the total matter distribution because the light deflection is independent of the nature of the matter and of its state.

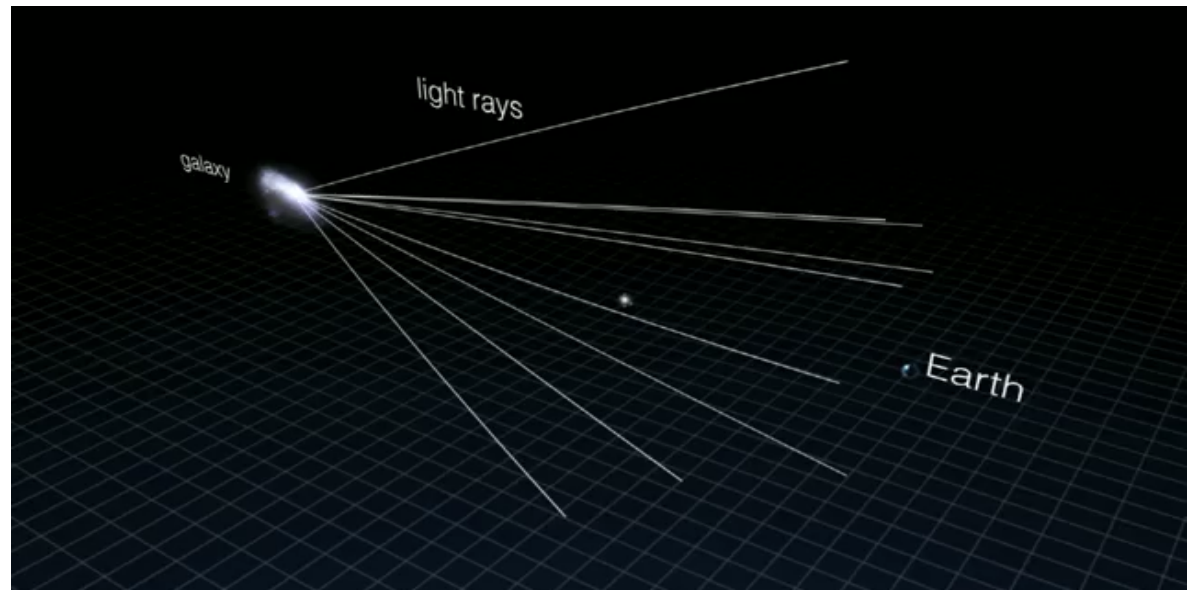


The thin screen approximation

$$\beta = \theta - \frac{D_{ls}}{D_s} \tilde{\alpha}(D_l \theta)$$

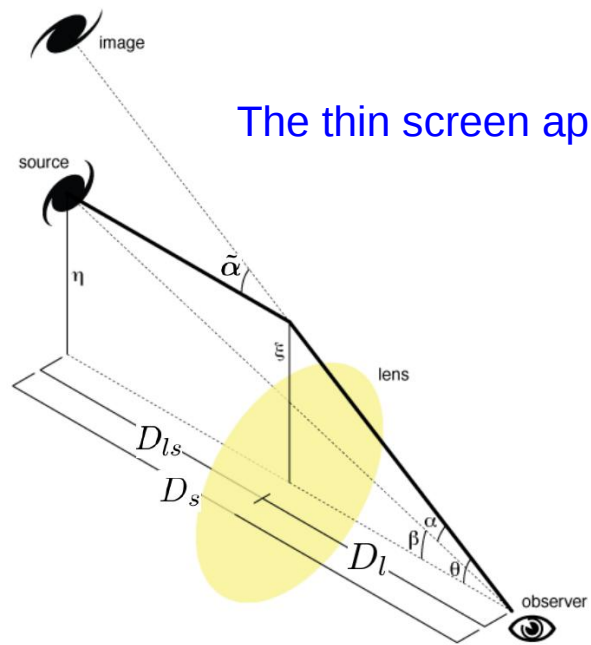
$$\tilde{\alpha}(\xi) = \frac{4G}{c^2} \int d^2 \xi' \Sigma(\xi') \frac{\xi - \xi'}{|\xi - \xi'|^2}$$

Abell 383



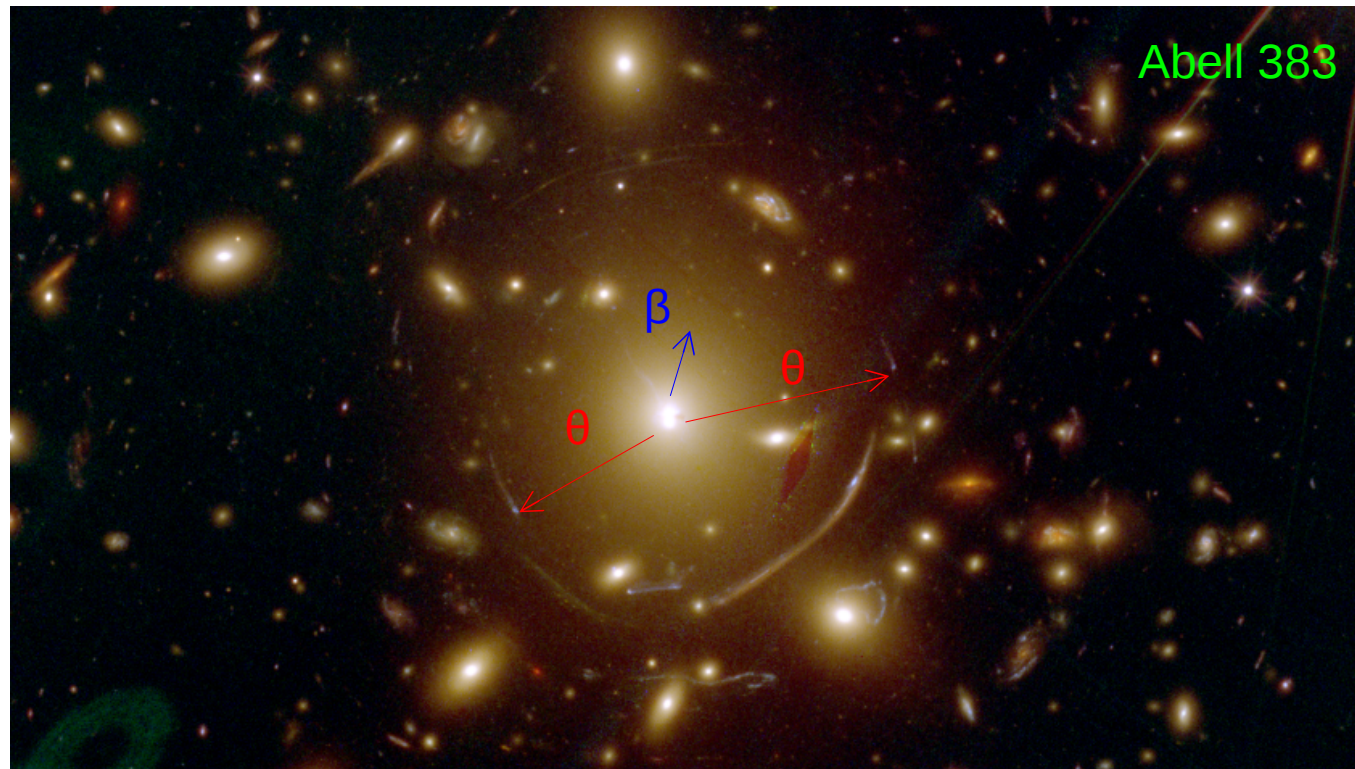
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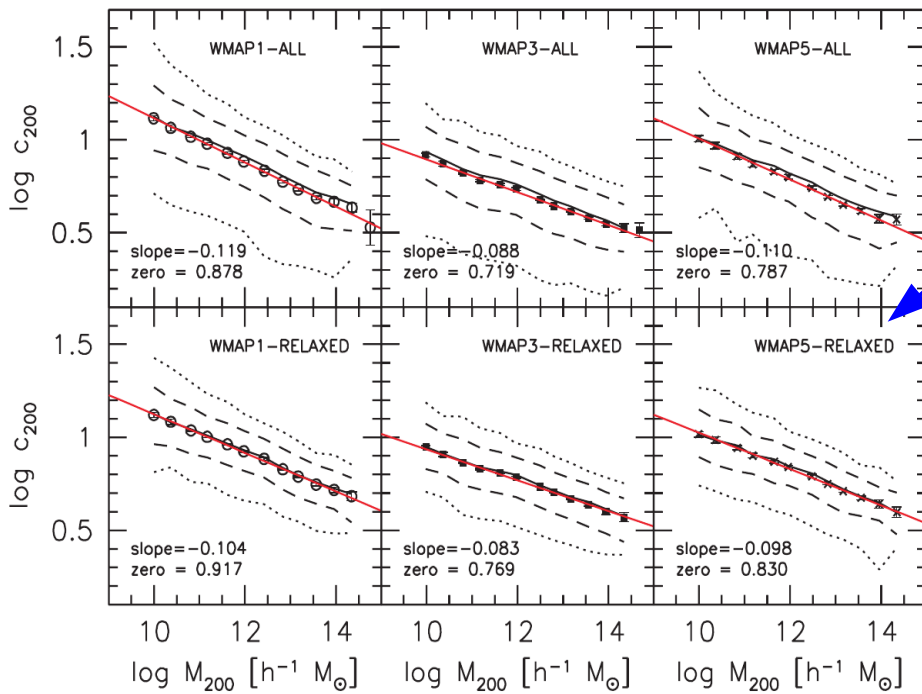
$$\tilde{\alpha}(\xi) = \frac{4G}{c^2} \int d^2 \xi' \Sigma(\xi') \frac{\xi - \xi'}{|\xi - \xi'|^2}$$



## Matter density component: Concentration – mass relation

- In the  $\Lambda$ CDM cosmological framework, numerical simulations have shown a very well-defined correlation between the concentration of the halos and their masses

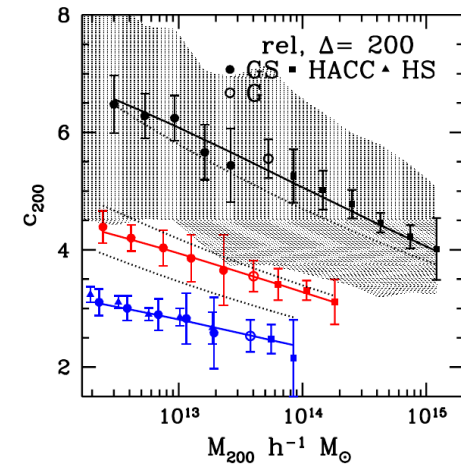
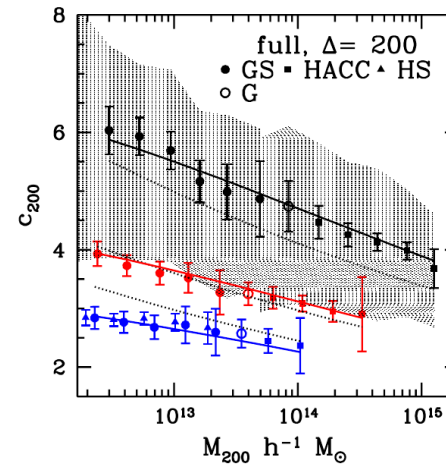
⇒ c – M relation: less massive halos are expected to be more concentrated than more massive ones



Macciò et al. (2008)

$$c_{200}(M_{200}) = c_n \times \left( \frac{M_{200}}{M_{piv} h^{-1} M_{\odot}} \right)^{\alpha}$$

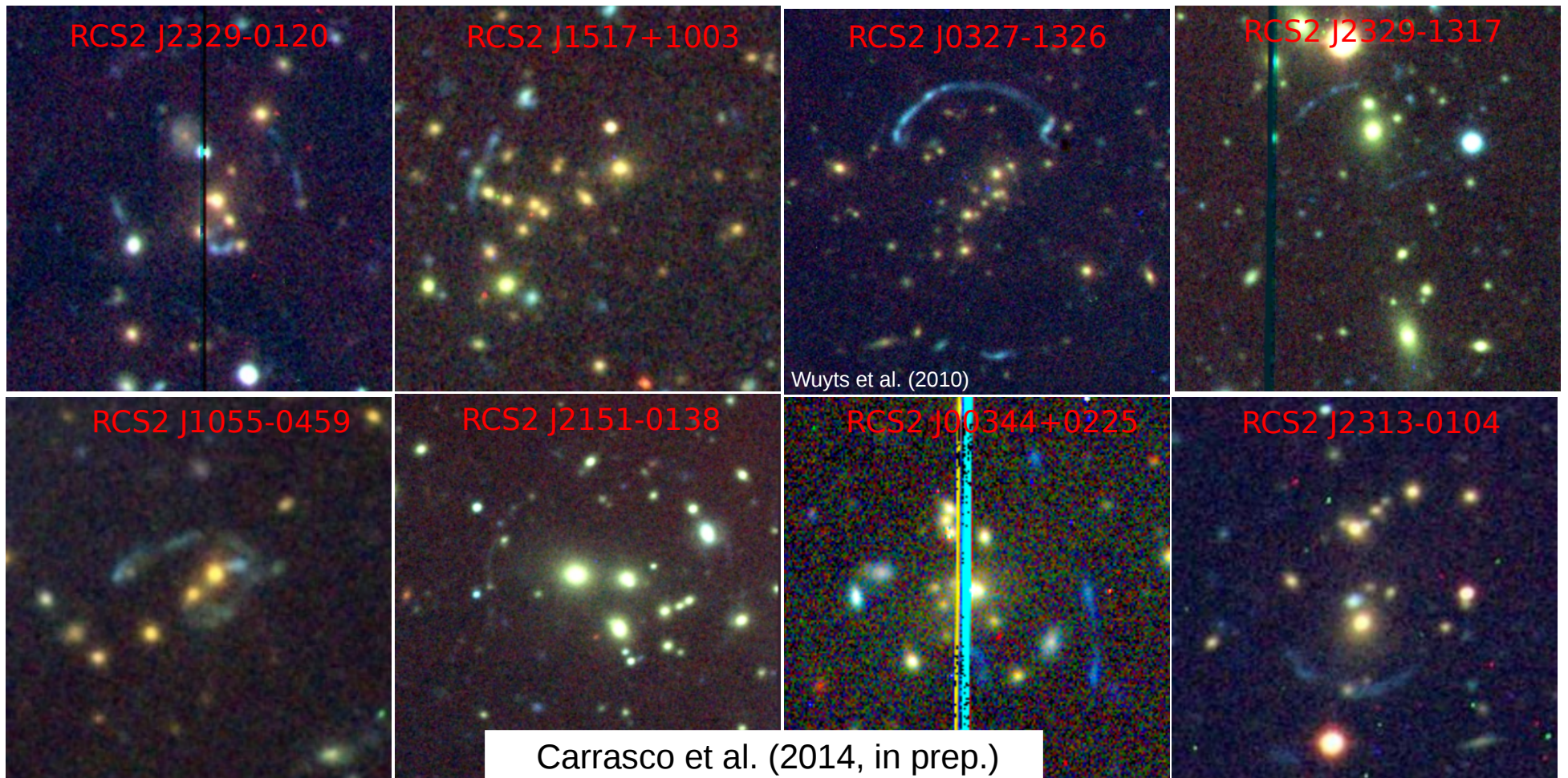
$\sigma_8$



Bhattacharya et al. (2013)

## RCSGA: 29 SL selected galaxy clusters

- Red-sequence Cluster Survey Giant Arcs → RCSGA survey (Gladders et al in prep)
  - Visual inspection of the Red-sequence Cluster Survey 2 (RCS2)





## RCSGA: 29 SL selected galaxy clusters

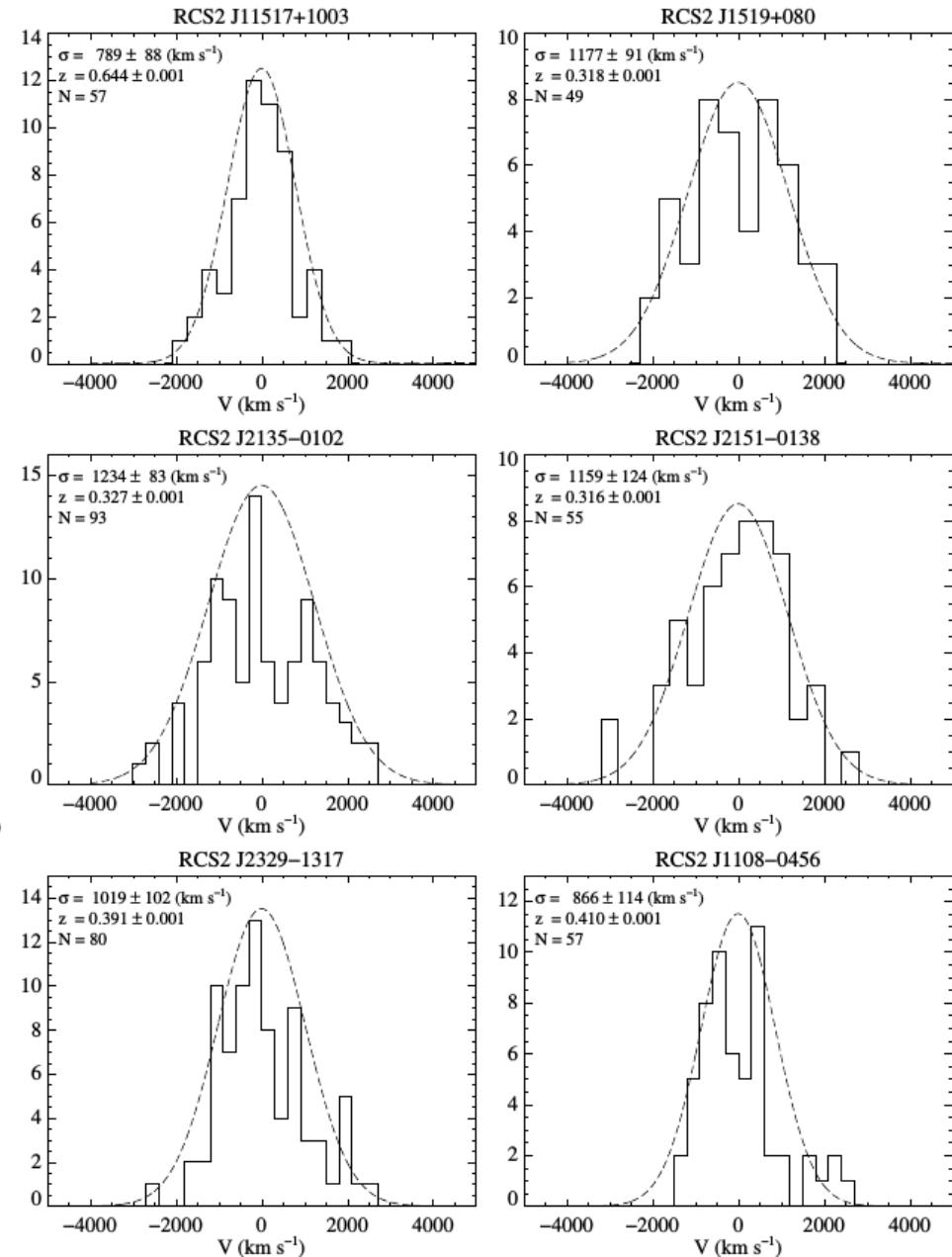
- VLT / Magellan / Gemini spectroscopic data
  - > 2500 spectra
  - ~ 1100 cluster members
  - $\langle N \rangle \sim 38$  members per clusters
  - only 5 clusters with  $N < 20$
- Velocity dispersion  $\Rightarrow$  Dynamical mass

Evrard et al. (2008)  $\rightarrow M_{200} = \frac{10^{15}}{h(z)} \left( \frac{\sigma_{DM}}{\sigma_{15}} \right)^{1/\alpha} M_{\odot}$

$$2.80 \times 10^{13} \leq M_{200}/h^{-1}M_{\odot} \leq 2.84 \times 10^{15}$$

$$0.22 < z < 1.01$$

Carrasco et al. (2014, in prep.)

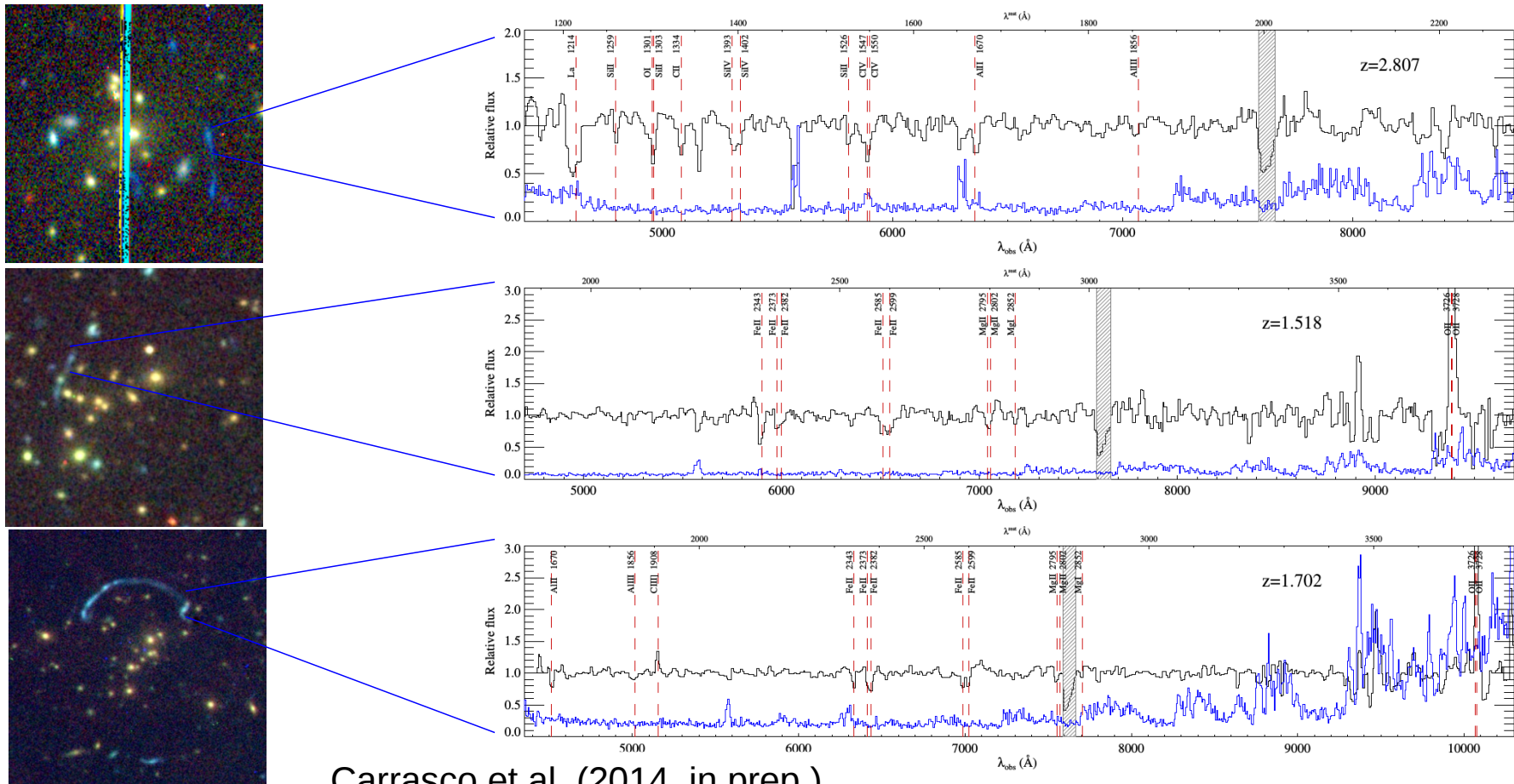


## RCSGA: 51 lensed galaxies

- VLT / Magellan / Gemini spectroscopic analysis has also confirmed 51 lensed galaxies

→ 34 background sources

$$0.8 < z < 3.2$$



Carrasco et al. (2014, in prep.)

# Mass distribution reconstruction



*Lenstool: Parametric method – 8 free parameters* (Jullo et al. 2007)

- Main halos → eNFW profile

$$\rho(r) = \frac{\rho_s}{r/r_s(1+r/r_s)^2} \quad c_{200} := \frac{r_{200}}{r_s}$$

$c_{200}, r_s, (\text{R.A.}, \text{Dec.}), e_\Sigma, \theta_e$

6 free parameters

- Galaxy halos → PIEMD profile

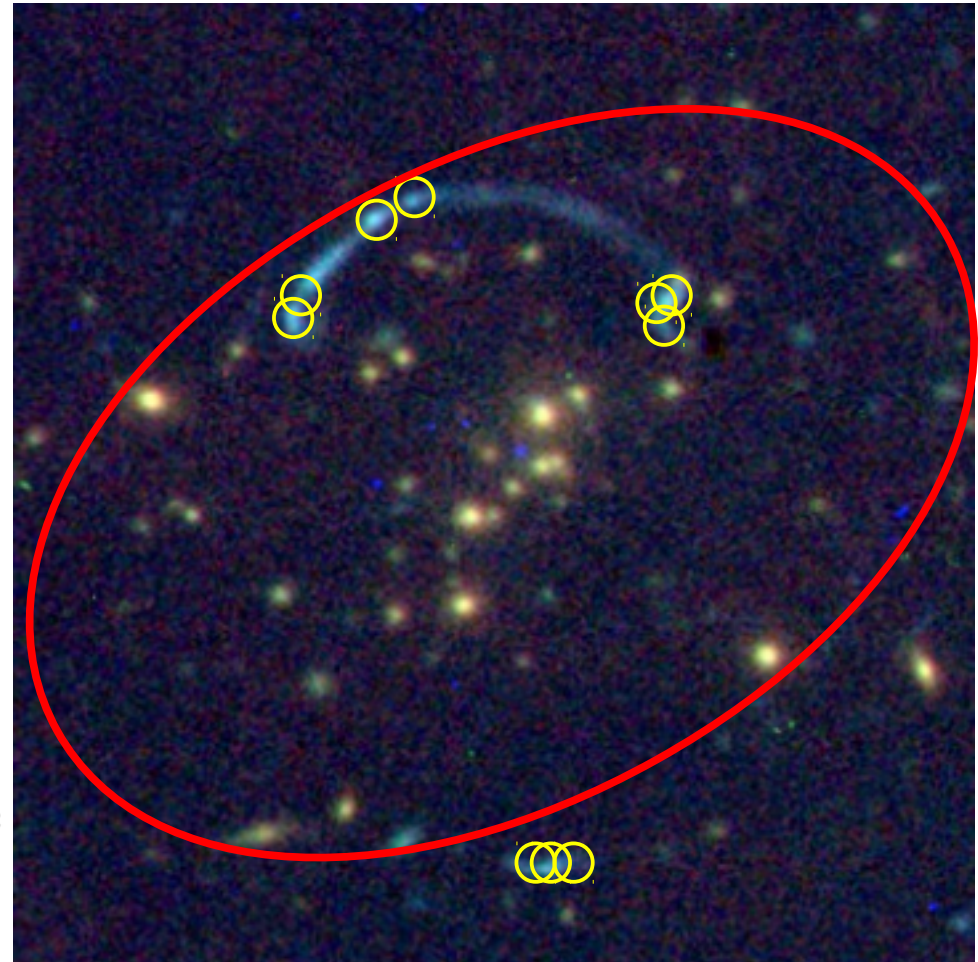
$$\rho(r) = \frac{\rho_0}{(1+r^2/r_{core}^2)(1+r^2/r_{cut}^2)}$$

$\sigma_0^*, r_{cut}^*, r_{core}^*$

$r_{core}^* \Rightarrow 0.15 - 0.30 \text{ kpc}$

2 free parameters

RCS2 J0327-1326



Wuyts et al. (2010), Sharon et al. (2012)

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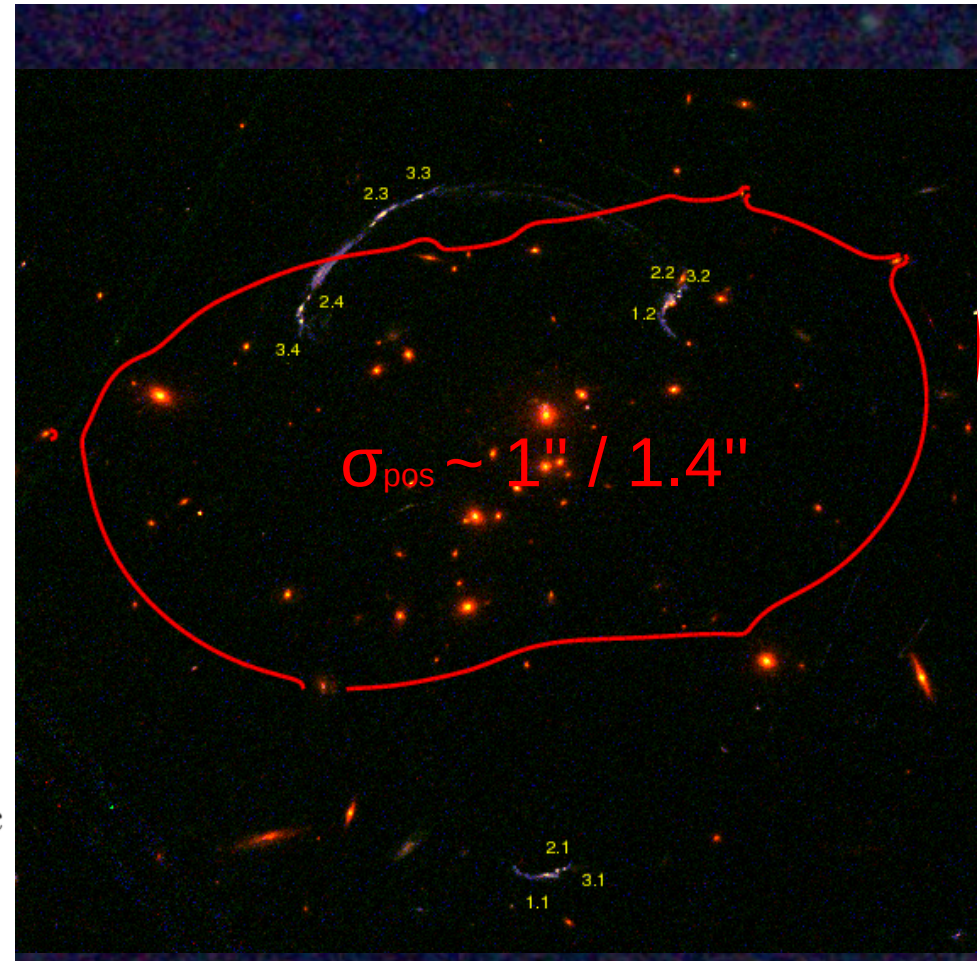
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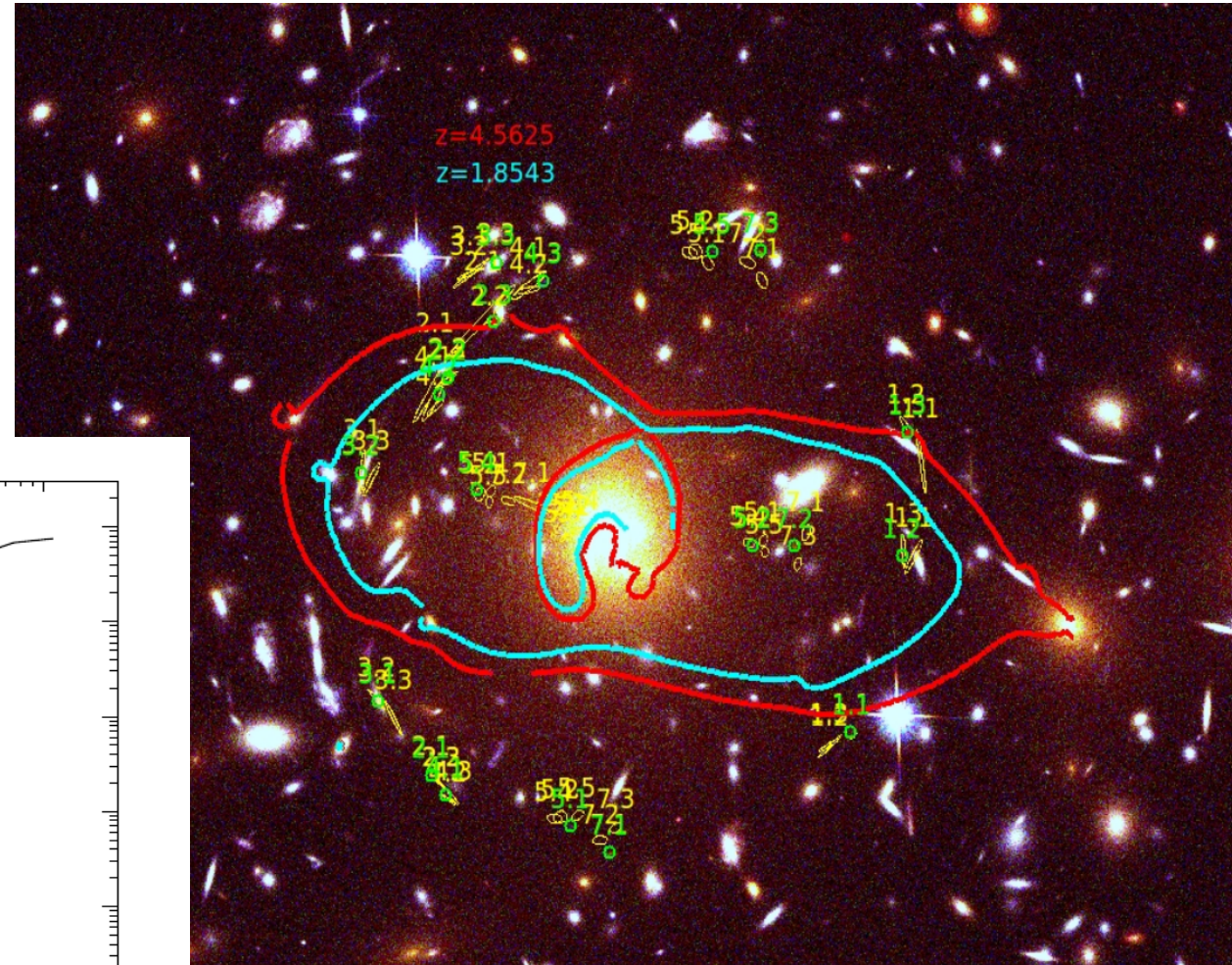
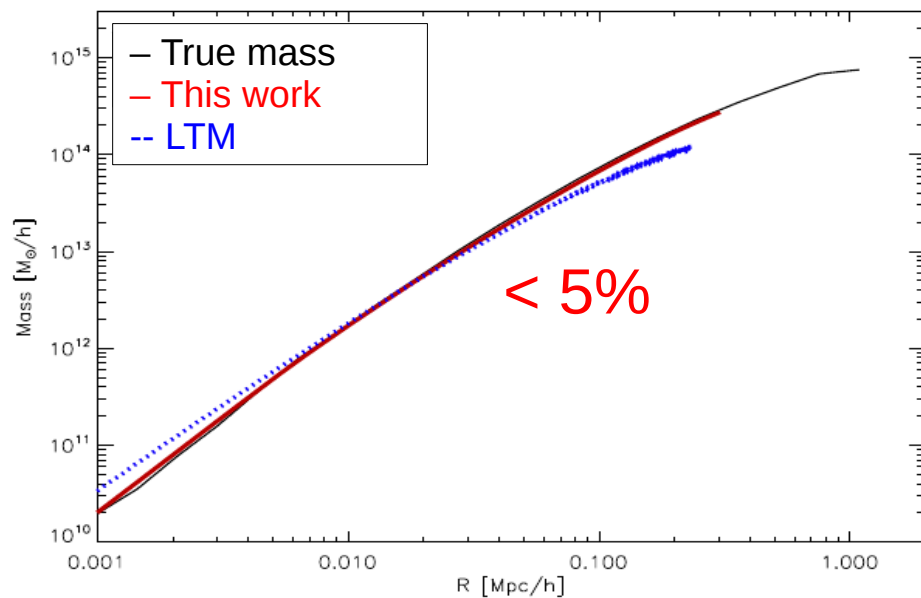


*Lenstool: Parametric method – 8 free parameters* (Jullo et al. 2007)

G1 projection XZ

- Massimo's simulated clusters

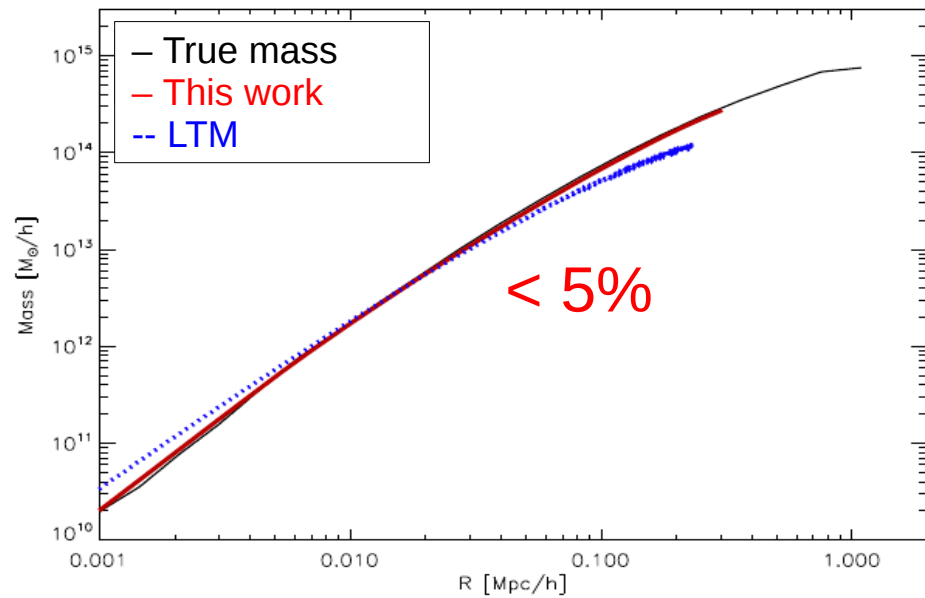
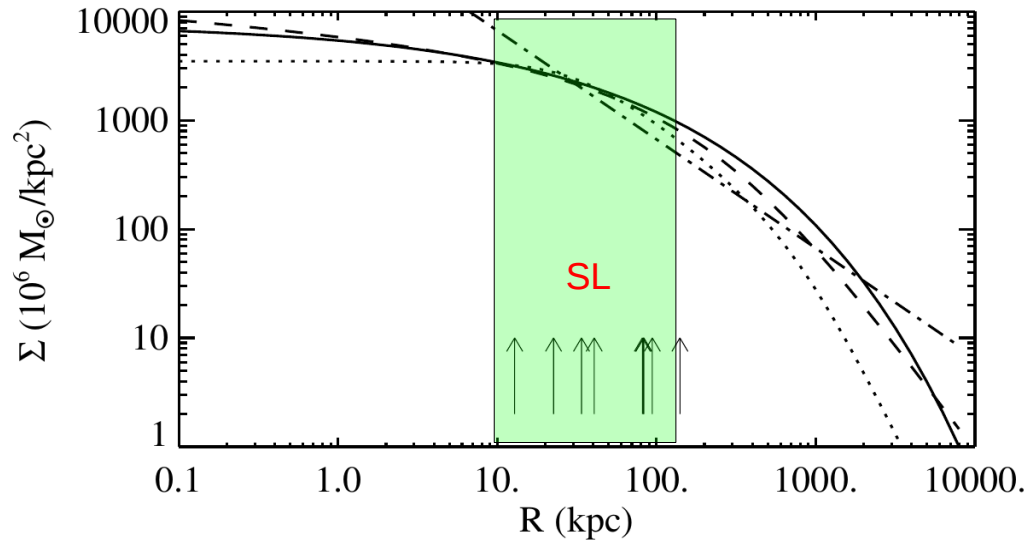
- ➔ MOKA + SkyLens (Giocoli et al. 2010)
- ➔  $\Sigma \sim 1'' / 1.4''$



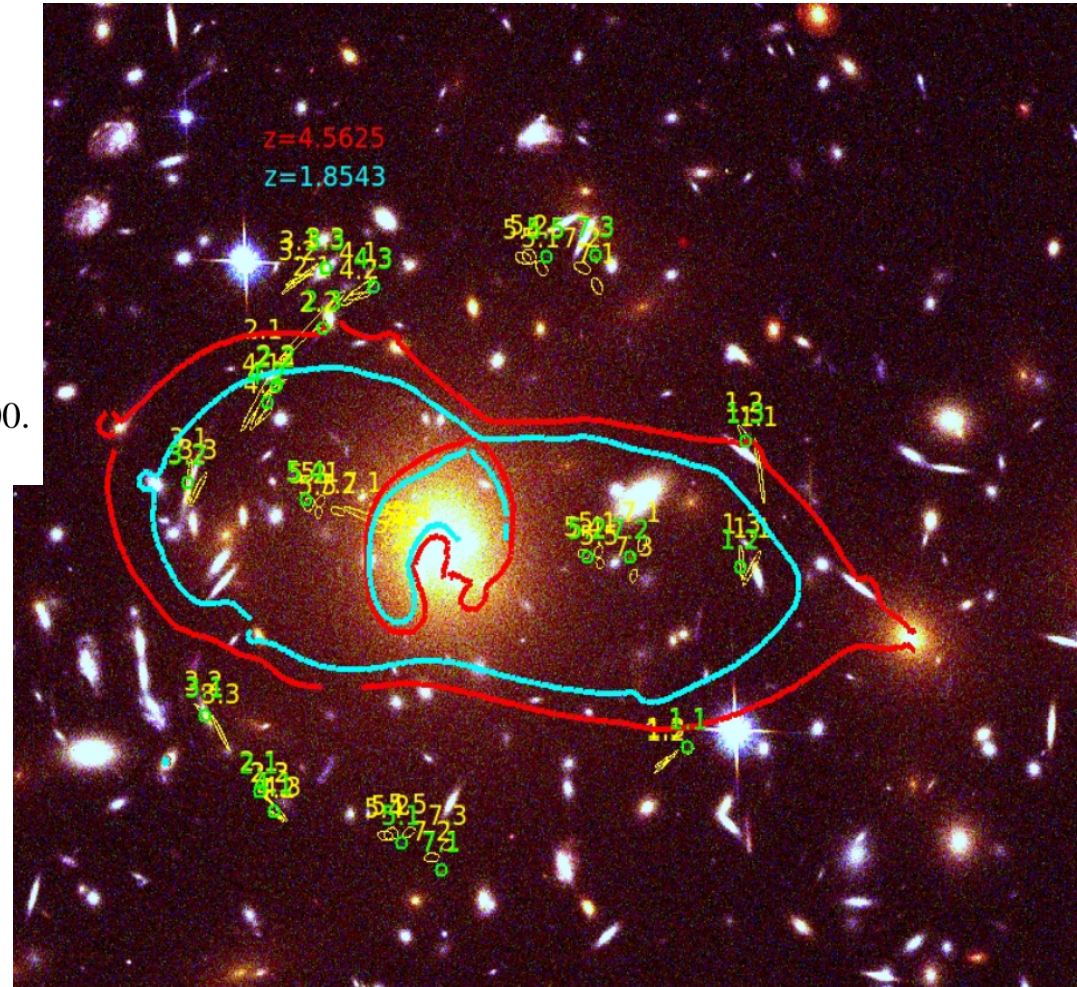
# Mass distribution reconstruction



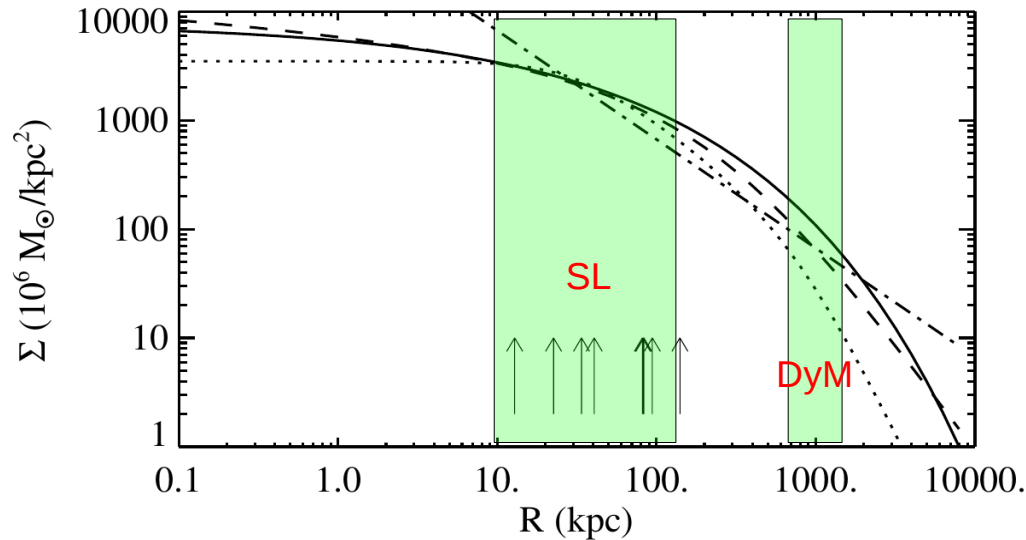
*Lenstool: Parametric method – 8 free parameters* (Jullo et al. 2007)



G1 projection XZ



## Lenstool: Parametric method – SL and Dyn constraints

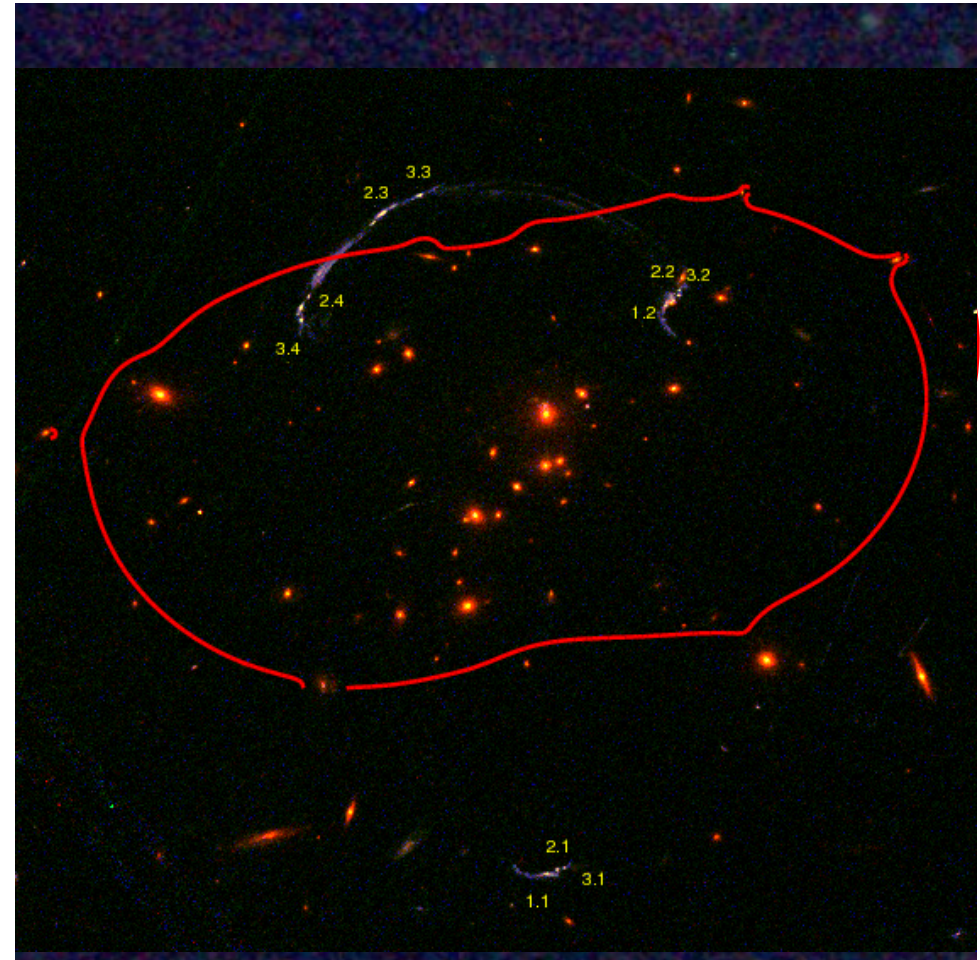


- Dynamical mass (Dyn) constraints

$$\chi_{mass}^2(M_{200}^{obs}, c_{200}, r_s) = \left( \frac{M_{200}^{obs} - M_{200}^{pred}(c_{200}, r_s)}{\Delta M} \right)^2$$

$$\chi_{tot}^2 = \chi_{SL}^2 + \chi_{mass}^2$$

RCS2 J0327-1326

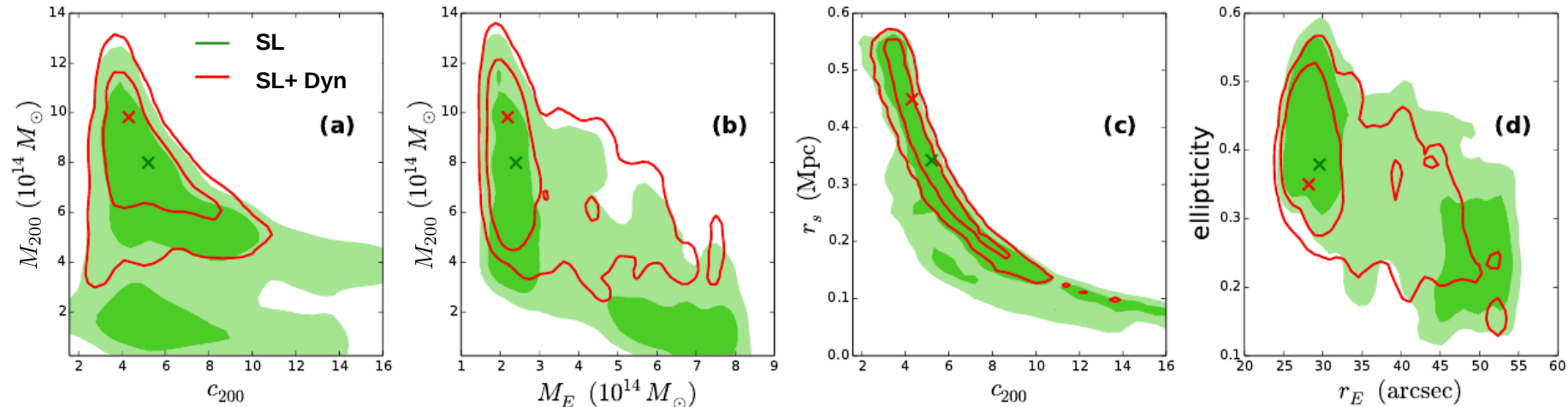
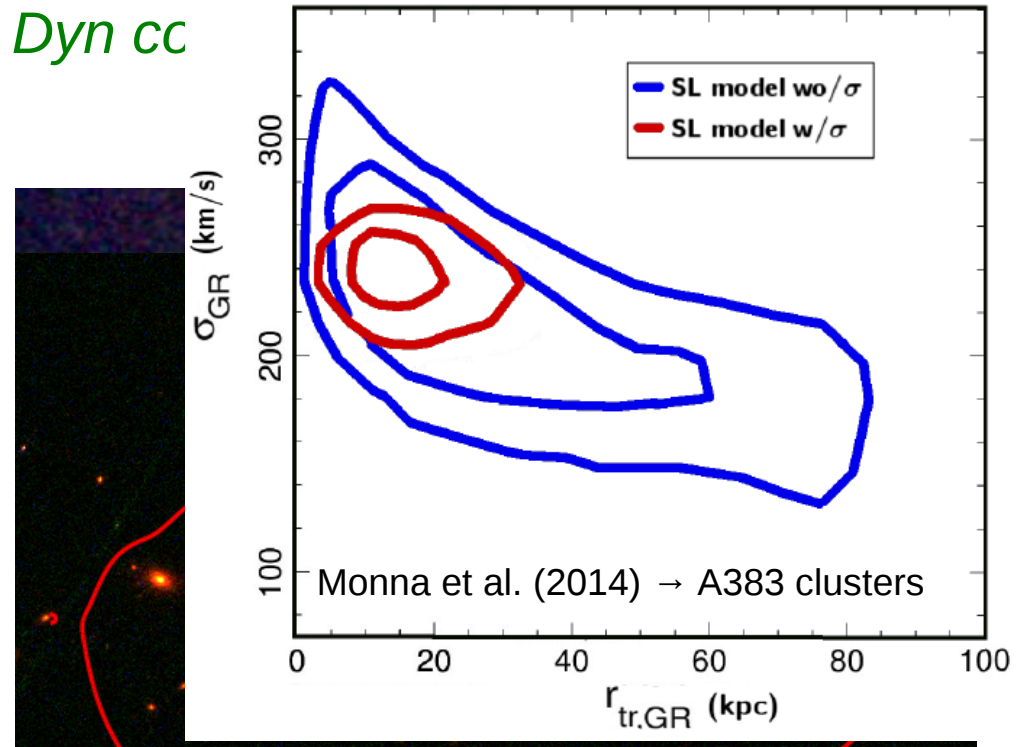
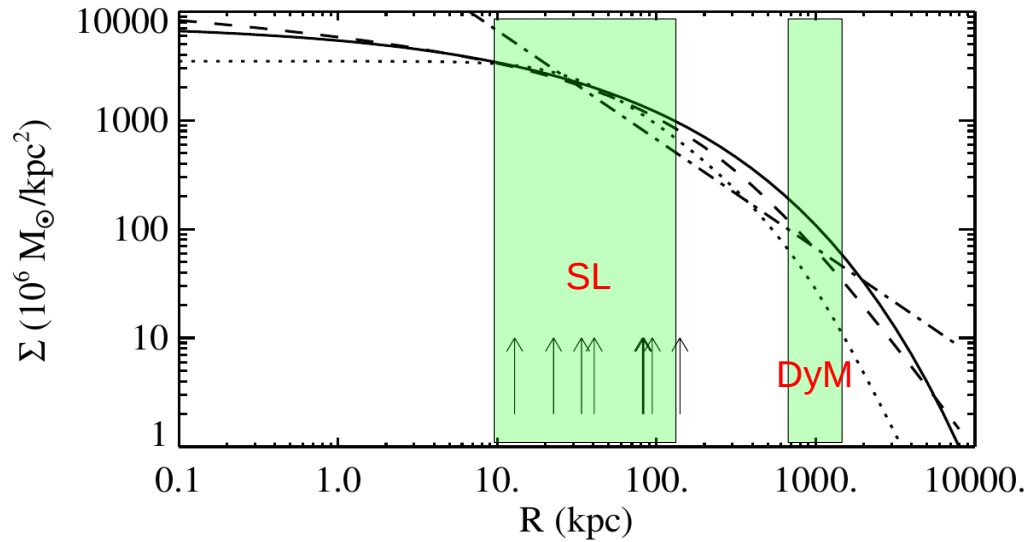


Wuyts et al. (2010), Sharon et al. (2012)

# Mass distribution reconstruction



## Lenstool: Parametric method – SL and Dyn cc



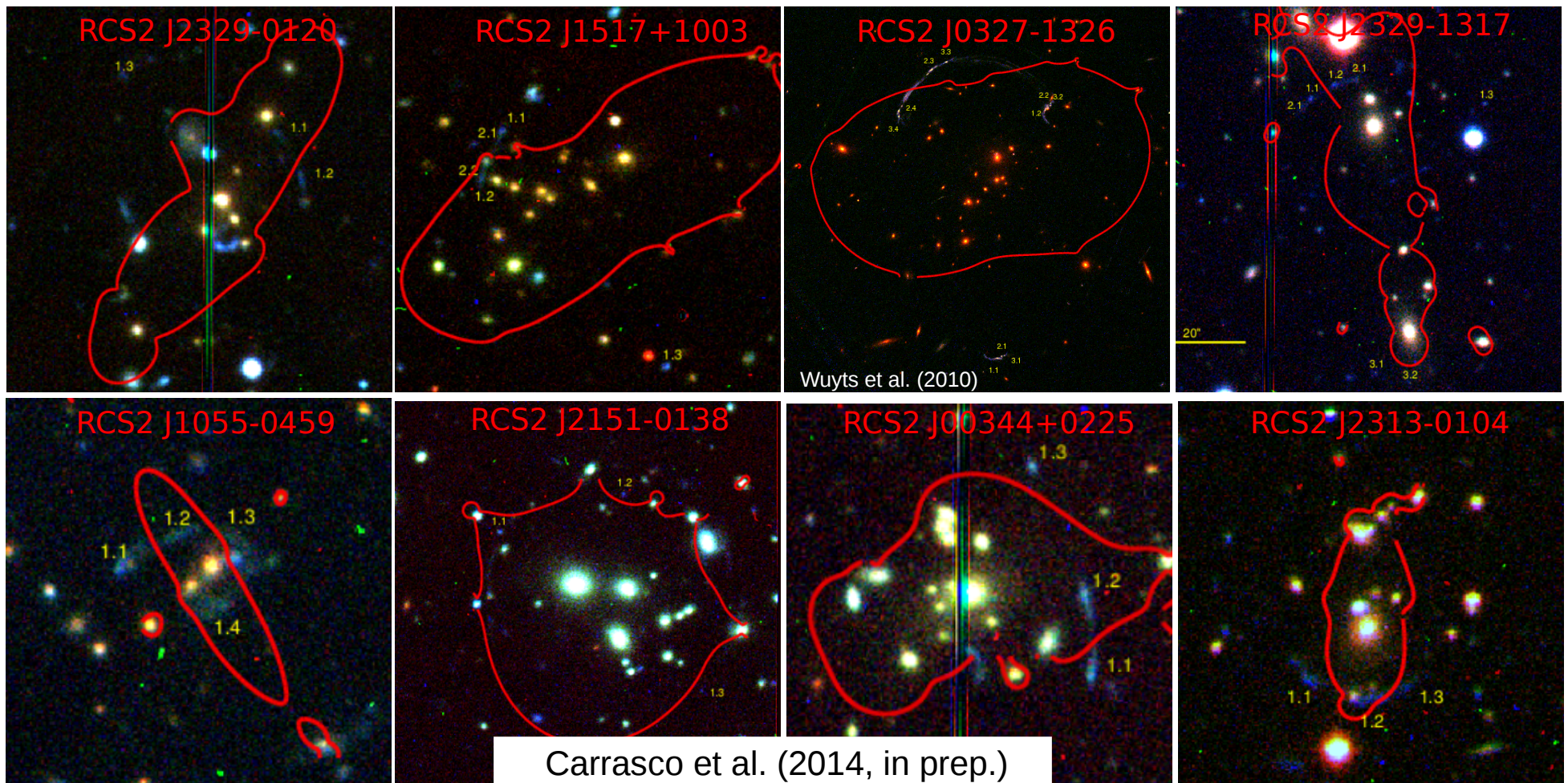
Sifon et al. (2013) → PLCK G004.5 – 19.5 clusters



# Mass distribution reconstruction

## *Lenstool: Parametric method – SL and Dyn constraints*

- 29 SL & DyM mass reconstructions



# Concentration – mass relation

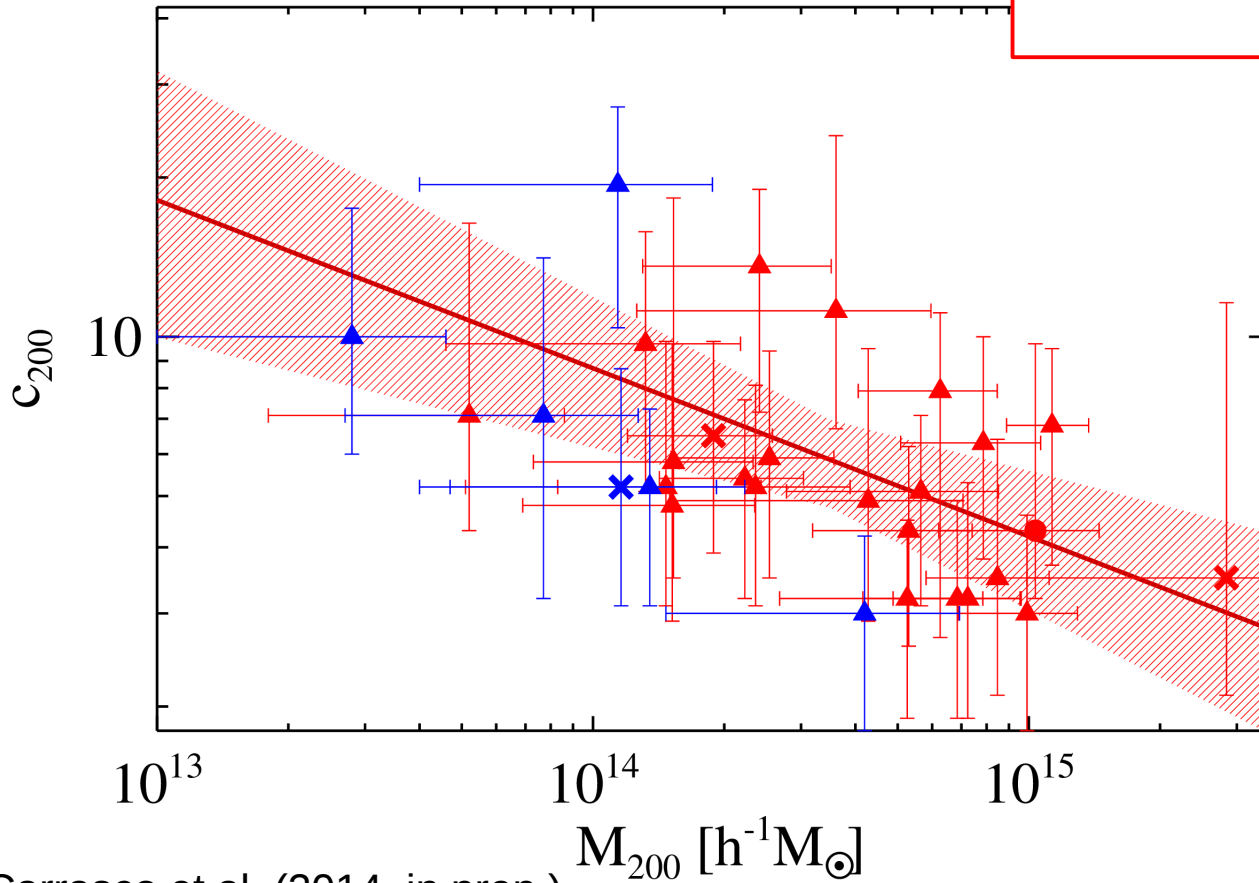


## *c – M relation for 27 RCSGA clusters*

- 26 clusters from RCSGA survey + 1 from Sifón et al. (2014)

27 SL selected galaxy clusters

$$c_{200} = (5.80 \pm 1.08) \times \left( \frac{M_{200}}{3.61 \times 10^{14} h^{-1} M_{\odot}} \right)^{-0.32 \pm 0.11}$$



Carrasco et al. (2014, in prep.)

# Concentration – mass relation

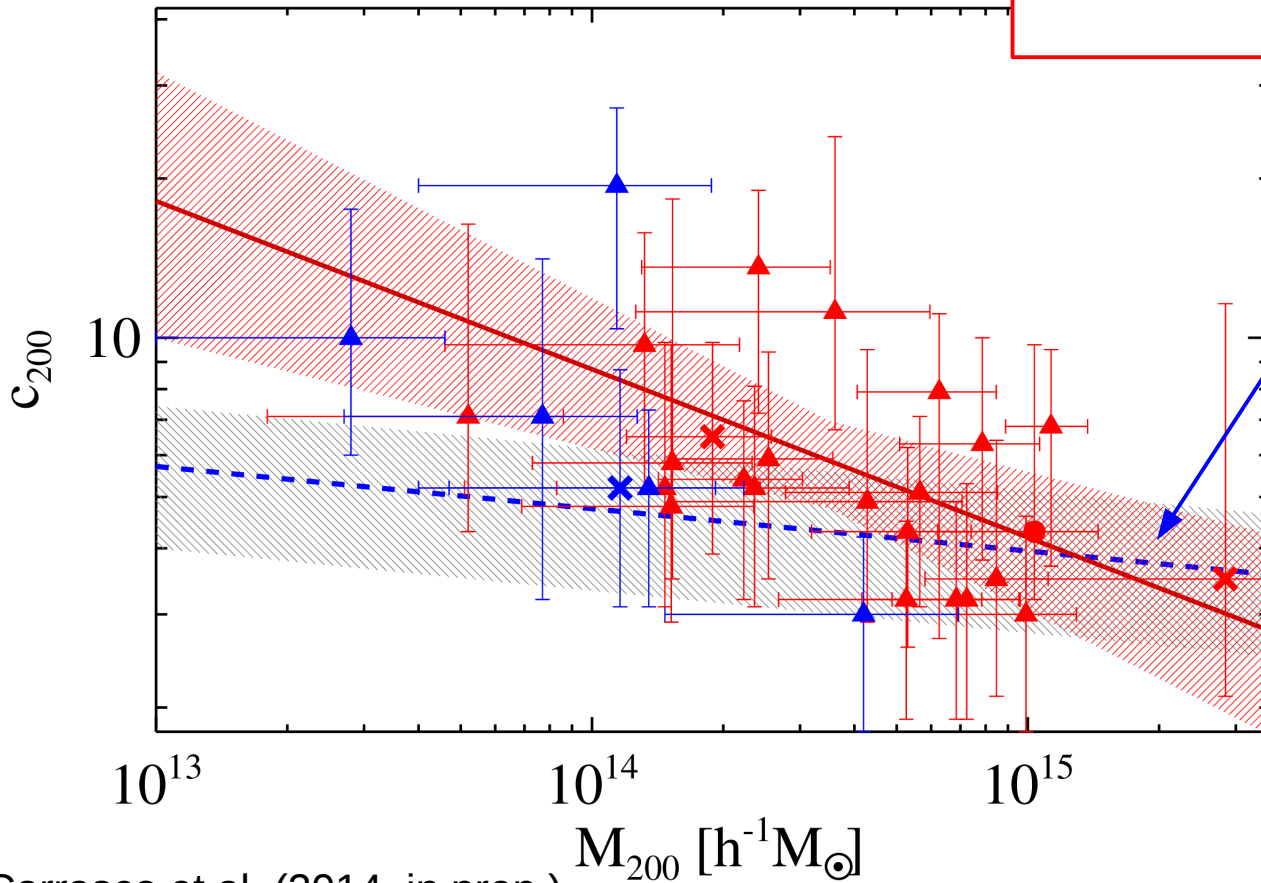


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Battacharya et al. (2013)

→ Normal population at  $z = 0$

$$M_{200} \sim 8 \times 10^{14} h^{-1} M_{\odot}$$

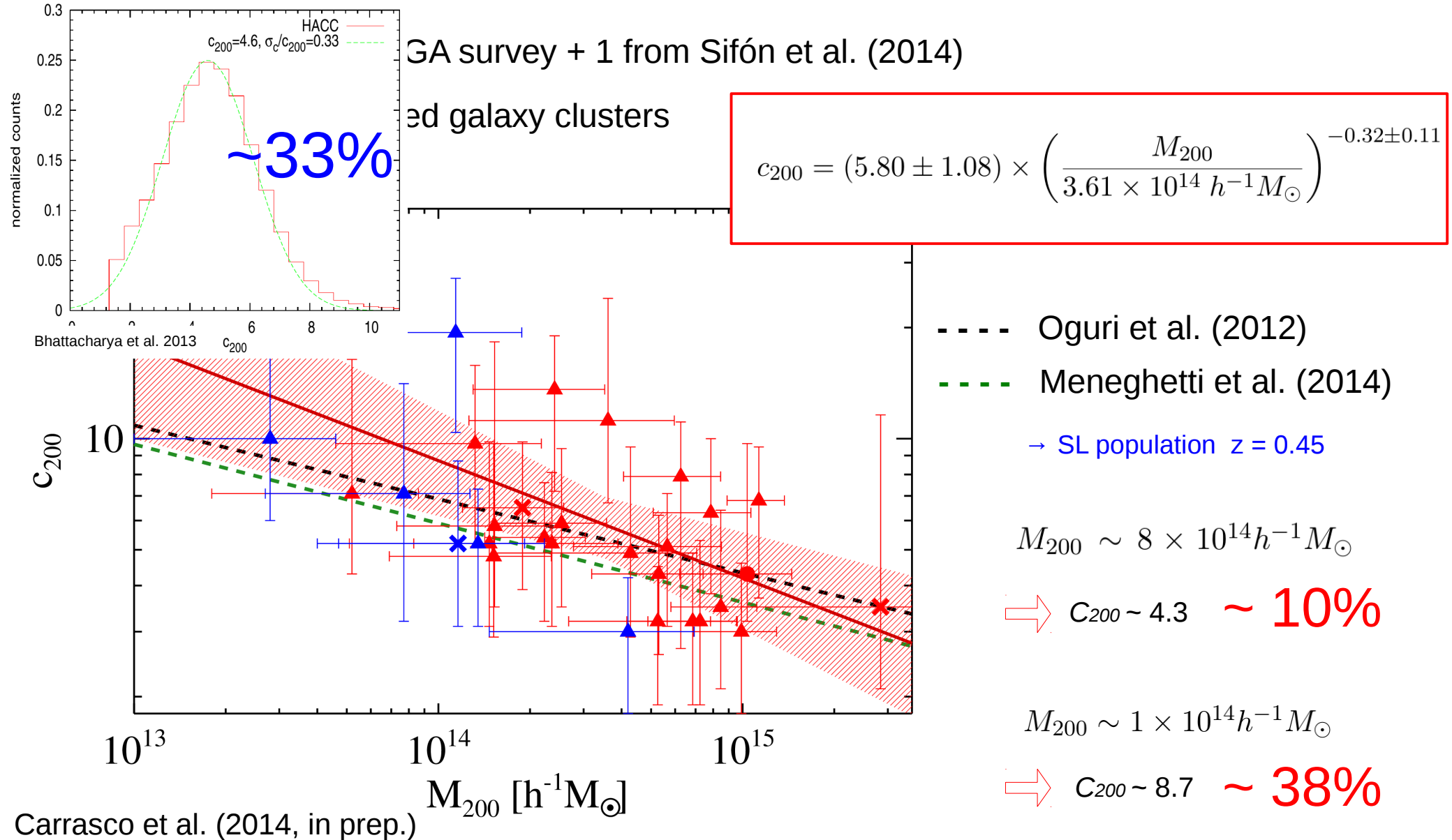
⇒  $C_{200} \sim 4.3 \sim 11\%$

Carrasco et al. (2014, in prep.)

# Concentration – mass relation



## $c - M$ relation for 27 RCSGA clusters



# Concentration – mass relation of 73 galaxy clusters



## The largest robust dataset of concentration parameters

- SGAS survey (Oguri et al. 2012)

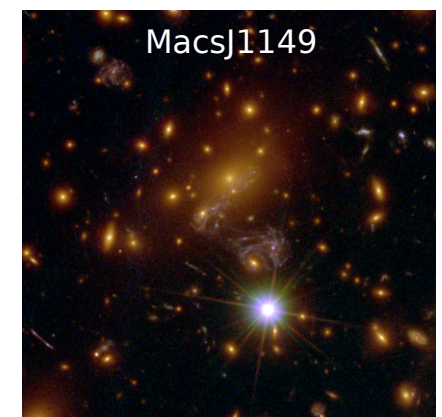
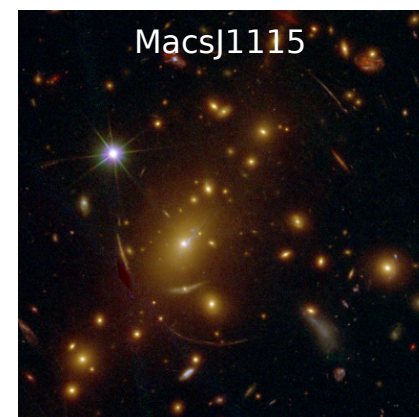
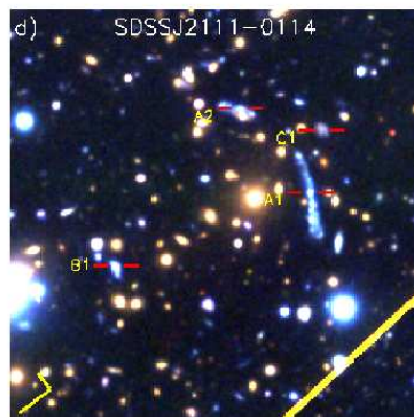
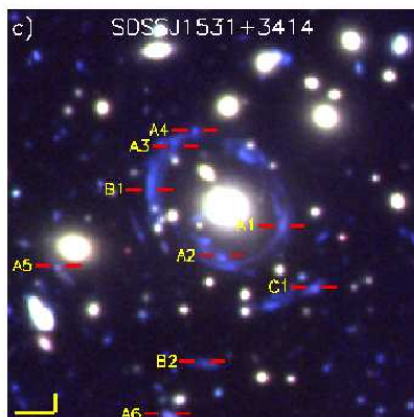
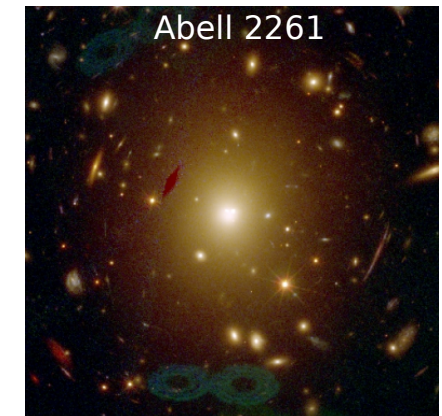
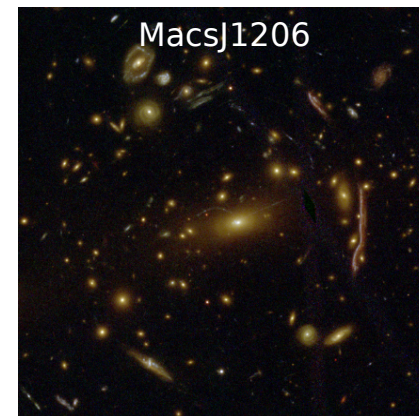
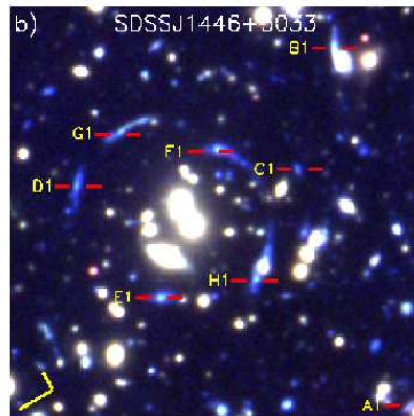
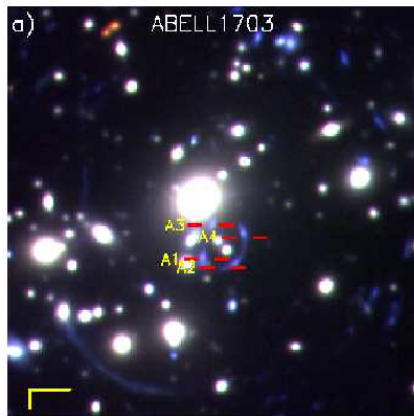
- SDSS
- SL selected

} 27 clusters

- CLASH survey (Merten et al. 2014)

- HST
- X-ray selected

} 19 clusters



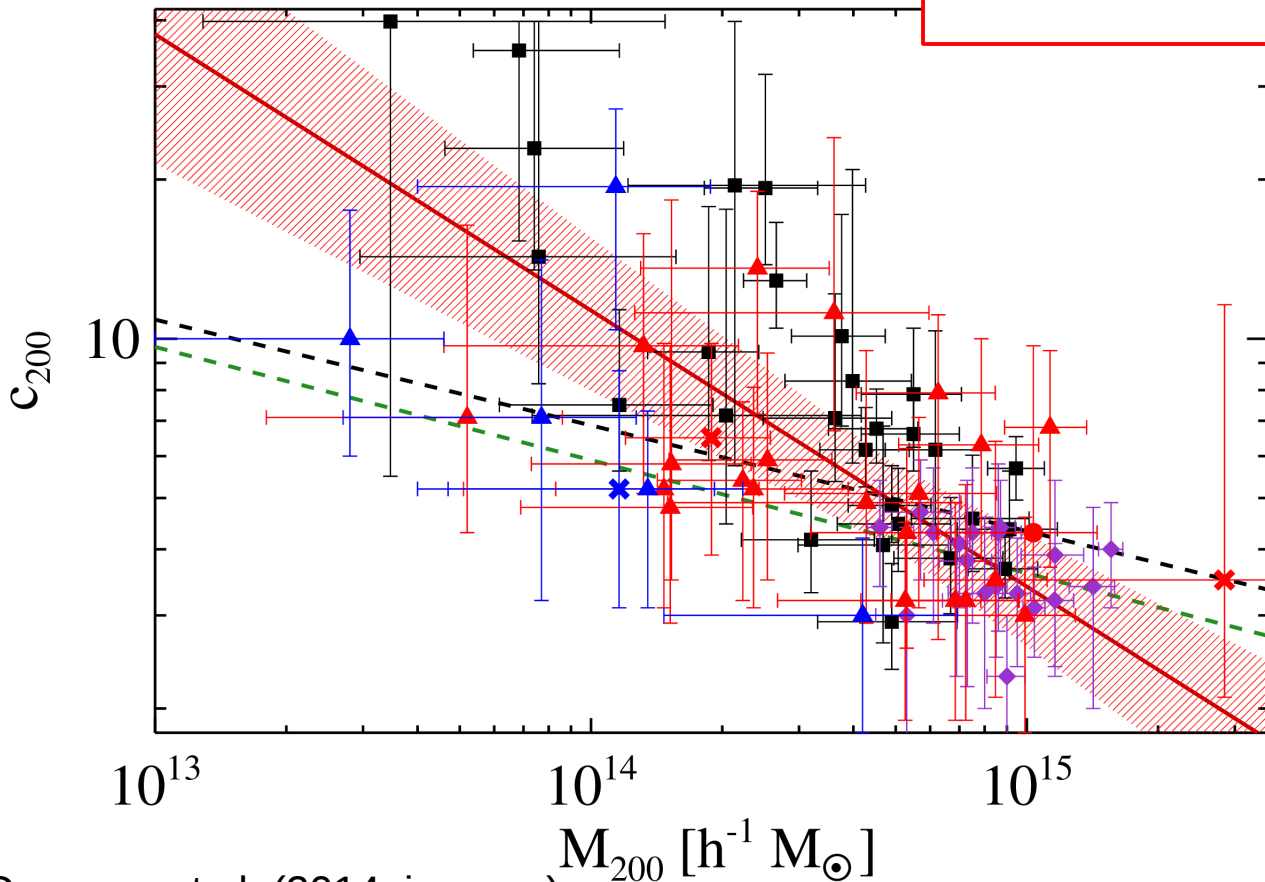
# Concentration – mass relation of 73 galaxy clusters



*The largest robust dataset of concentration parameters*

- ▲▲ This work
- 27 SL selected clusters from Oguri et al. (2012)
- ◆ 19 X-ray selected clusters from Merten et al. (2014)

$$c_{200} = (4.75 \pm 0.84) \times \left( \frac{M_{200}}{5.26 \times 10^{14} h^{-1} M_{\odot}} \right)^{-0.52 \pm 0.09}$$



- Oguri et al. (2012)
- - - Meneghetti et al. (2014)

→ SL population  $z = 0.45$   
 $M_{200} \sim 8 \times 10^{14} h^{-1} M_{\odot}$

⇒  $C_{200} \sim 3.9 \sim 6\%$

$M_{200} \sim 1 \times 10^{14} h^{-1} M_{\odot}$

⇒  $C_{200} \sim 11 \sim 78\%$

Carrasco et al. (2014, in prep.)

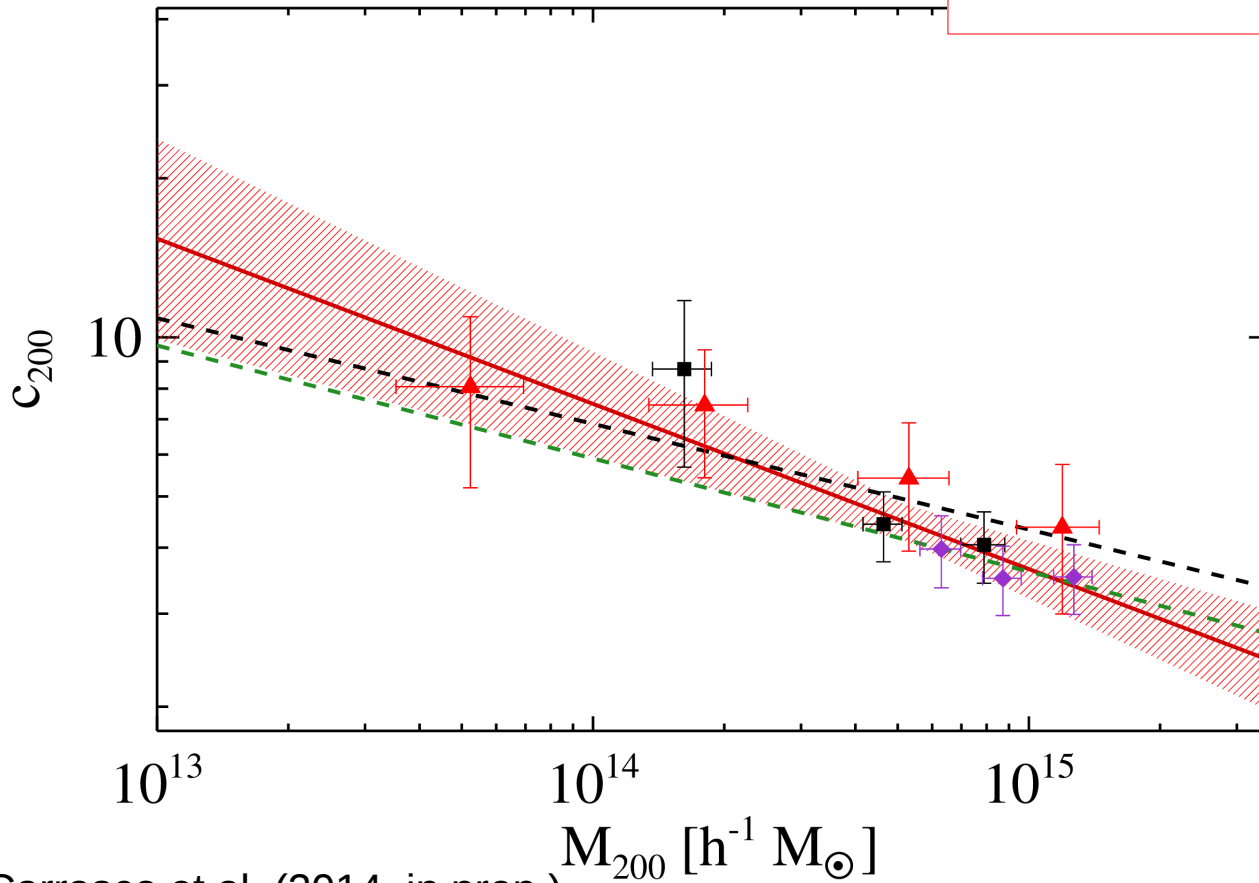
# Concentration – mass relation



## Stacking analysis

- ▲ This work
- 27 SL selected clusters from Oguri et al. (2012)
- ◆ 19 X-ray selected clusters from Merten et al. (2014)

$$c_{200} = (4.21 \pm 0.26) \times \left( \frac{M_{200}}{6.30 \times 10^{14} h^{-1} M_{\odot}} \right)^{-0.31 \pm 0.09}$$



- - - Oguri et al. (2012)
- - - Meneghetti et al. (2014)

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$$M_{200} \sim 1 \times 10^{14} h^{-1} M_{\odot}$$

⇒  $C_{200} \sim 7.5 \sim 17\%$

Carrasco et al. (2014, in prep.)

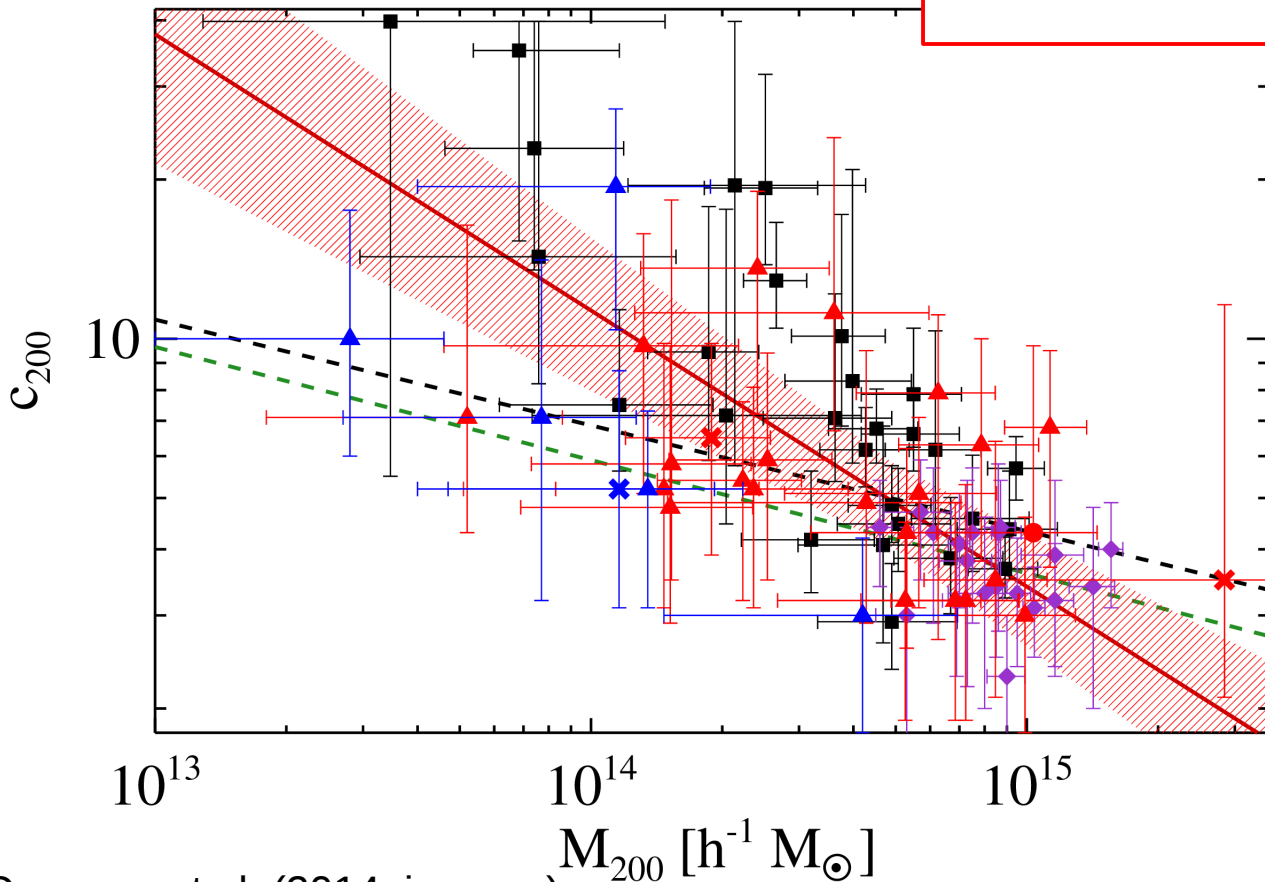
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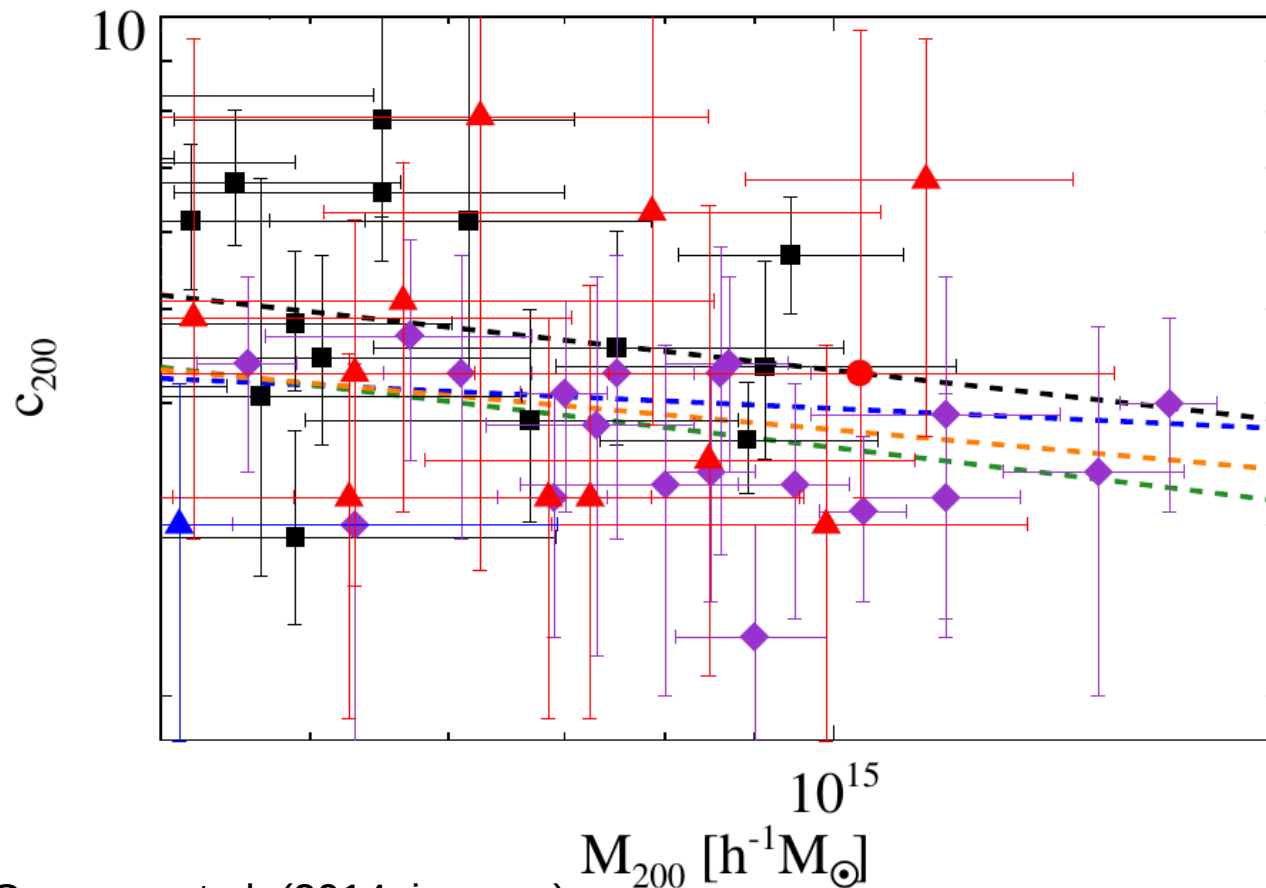


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- Bhattacharya et al. (2013)
- Oguri et al. (2012)-SL
- Meneghetti et al. (2014)-SL
- Meneghetti et al. (2014)-X-ray

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Carrasco et al. (2014, in prep.)

## New non-parametric method

Merten et al. (2009)

$$\chi_{\text{total}}^2 = \chi_{\text{weak}}^2 + \chi_{\text{strong}}^2 + \chi_{\text{reg}}^2 + \dots$$

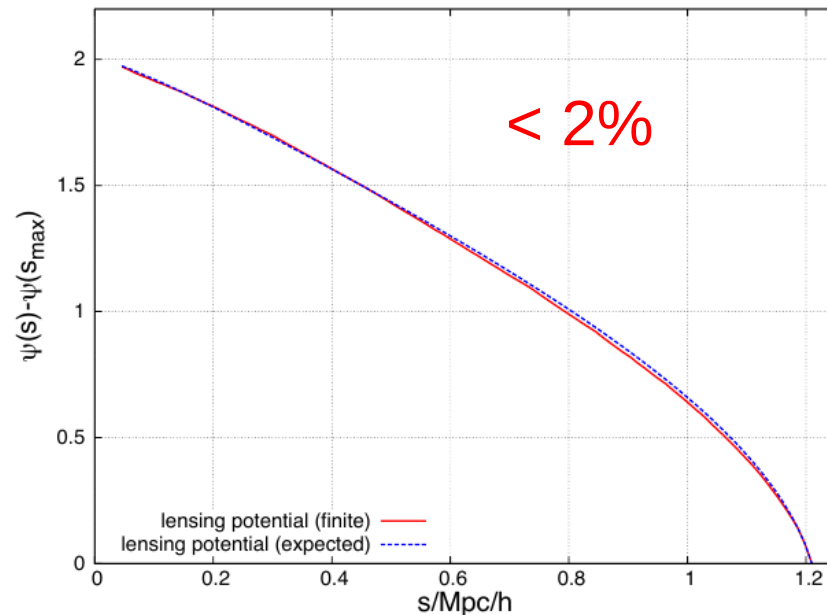
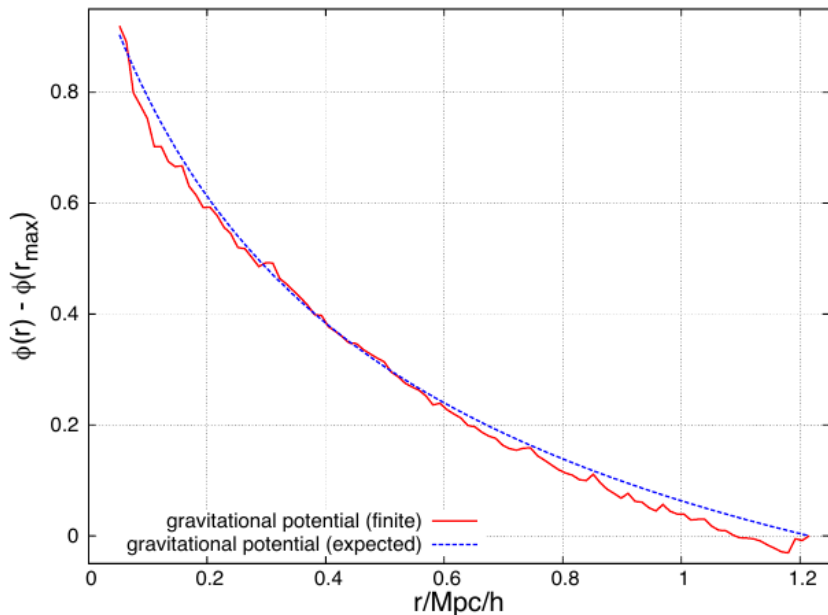
$$+ \chi_{\text{X-ray}}^2 + \chi_{\text{tSZ}}^2 + \chi_{\text{kinematics}}^2 + \chi_{\text{ext. mult. im.}}^2$$

(Red arrows point from  $\chi_{\text{reg}}^2$  to Konrad et al. (2013), from  $\chi_{\text{X-ray}}^2$  to Majer et al. (2014), and from  $\chi_{\text{kinematics}}^2$  to Sarli et al. (2014).)

Huber et al. (2014, in prep)

Deprojections  
→ Richardson-Lucy algorithm

$$\chi_{\nu}^2 = (\mathbf{d}_{\nu} - \mathcal{O}_{\nu}\psi)^T \mathcal{C}_{\nu}^{-1} (\mathbf{d}_{\nu} - \mathcal{O}_{\nu}\psi)$$



# Conclusions

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- We are lucky... there's a lot of work to do.