

Excited dark states matter

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Abstract

- In many dark matter models bound state transitions are fast.
- In a thermal bath, excited states contribute significantly to the effective annihilation cross section.
- Preliminary results indicate a dramatic change to the unitarity bound.

Introduction

- Solving full chemical network in Fig. 1 is daunting
- When transitions amongst bound states are fast compared to the decay of the ground state, the effective annihilation rate is controlled by

$$\langle \sigma^{\text{bsf}} v \rangle_{\text{eff}} \equiv \frac{\left(\sum_{ij} \langle \sigma_{ij}^{\text{bsf}} v \rangle_{\mathcal{B}} \right) \left(\sum_{\mathcal{B}} \Gamma_{\mathcal{B}}^{\text{dec}} n_{\mathcal{B}}^{\text{eq}} \right)}{\sum_{\mathcal{B}} \left[\Gamma_{\mathcal{B}}^{\text{dec}} + \Gamma_{\mathcal{B}}^{\text{dis}} \right] n_{\mathcal{B}}^{\text{eq}}} \quad (1)$$

- Excited states make a contribution.

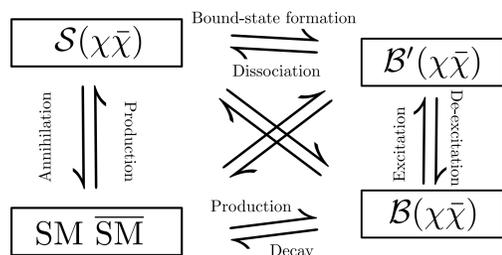


Figure 1: Full chemical network including excited states

Infrared enhancements

- At next to leading order include self energy diagram Fig. 2
 - For dark U(1) in a thermal bath
- $$(\sigma_{\chi\bar{\chi}}^{\text{bsf}} v)_{\mathcal{B}}^{\text{NLO}} = (\sigma_{\chi\bar{\chi}}^{\text{bsf}} v)_{\mathcal{B}}^{\text{LO}} [1 + \alpha n_f R(\Delta E/T)] \quad (2)$$
- The function R gets large in the infrared, meaning excited states make a major contribution

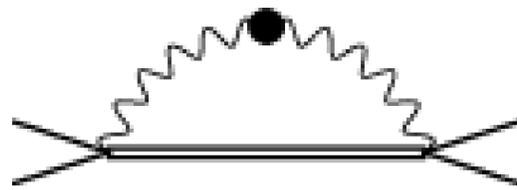


Figure 2: Self energy diagram to calculate NLO corrections

Dark U(1)

- For dark U(1) the effective cross section is approximately the ionization equilibrium x-section until the temperature reaches the binding energy

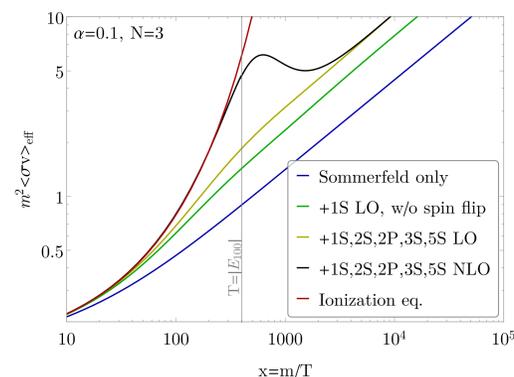


Figure 4: Dark U(1) in a bath

Squark coannihilation

- For squark co-annihilation transitions yet to be calculated but assumed to be fast through photon exchange
 - For squarks in a thermal bath
- $$(\sigma_{\chi\bar{\chi}}^{\text{bsf}} v)_{\mathcal{B}}^{\text{NLO}} \approx (\sigma_{\chi\bar{\chi}}^{\text{bsf}} v)_{\mathcal{B}}^{\text{LO}} \left[1 + \alpha \left(N_c + \frac{n_f}{2} \right) R(\Delta E/T) \right] \quad (3)$$
- preliminary results: amplification even more dramatic!

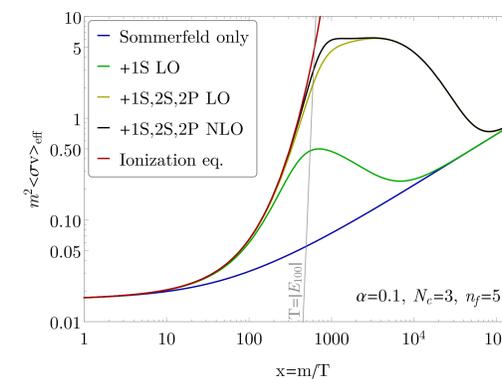


Figure 3: Squark co-annihilation effective cross section

Melted bound states

- Remaining mystery: how to treat melted bound states.
- See Fig. 5 for example where first 3 energy levels exist but then the energy spectrum becomes continuous.

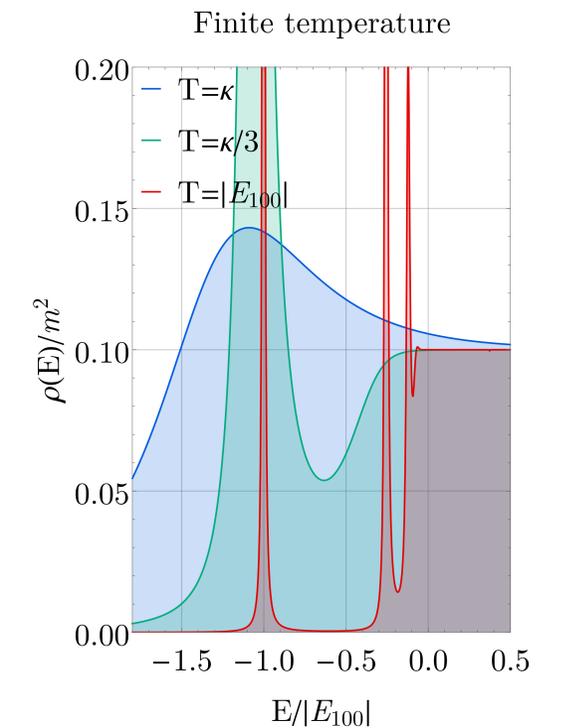


Figure 5: Melted bound states

Conclusion

- Excited states matter
- Thermal field theory effects at NLO matter
- Potentially large consequences in some models, particularly in calculating the unitarity bound