



Constraining ultra-light dark matter *with small scales observations*

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Kavli IPMU & University of Sao Paulo

*"What is dark matter? --Comprehensive study of the huge discovery space in
dark matter" Symposium,
March 30 2022*

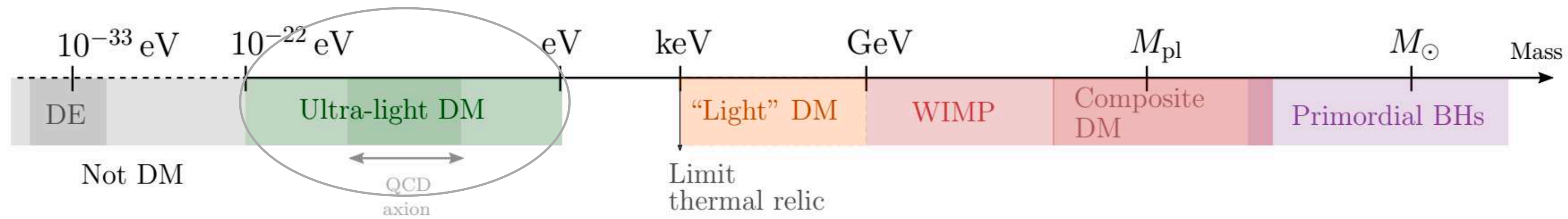
Status of the "art"

- What is DM? What is the nature of DM?

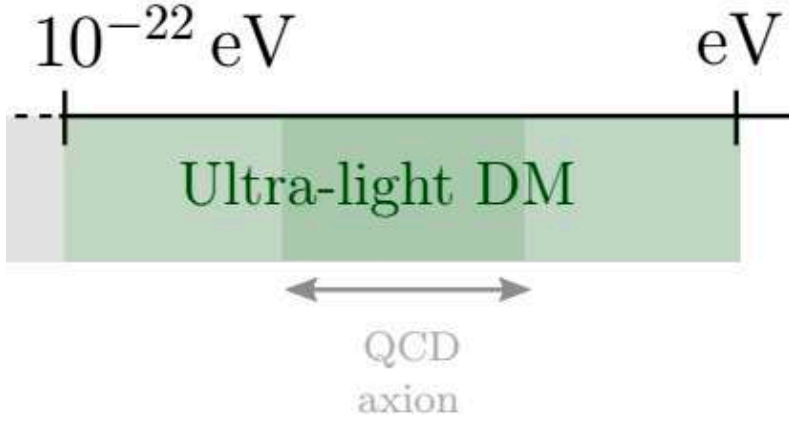


Mass scale of DM

80 orders of magnitude

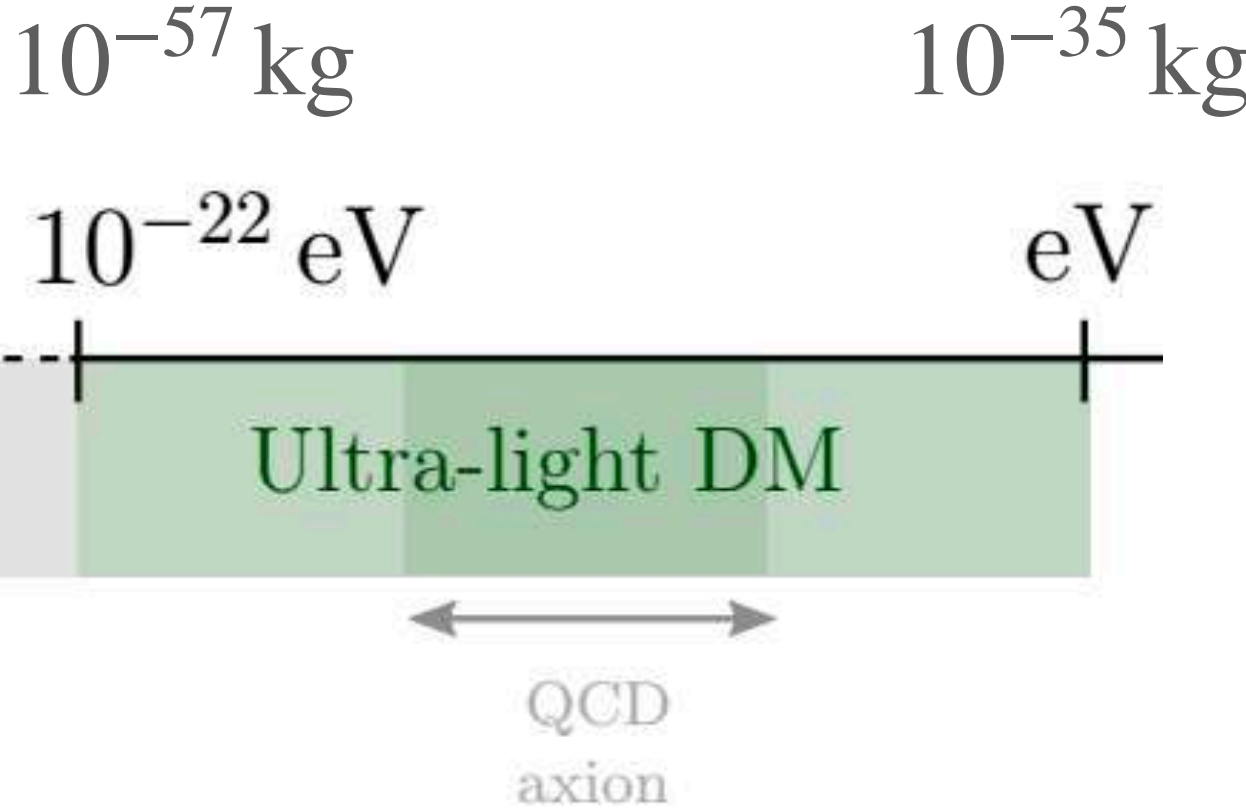
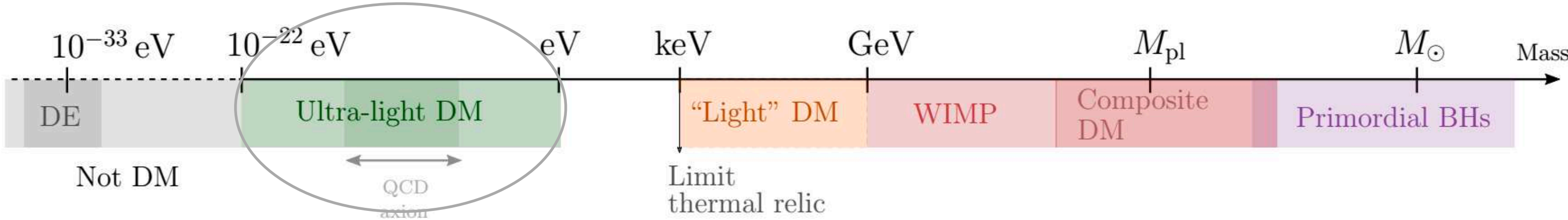


Ultra-light Dark Matter



Ultra-light candidate, cold \longrightarrow Large $\lambda_{\text{dB}} \sim 1/mv$

Lightest possible candidate for DM

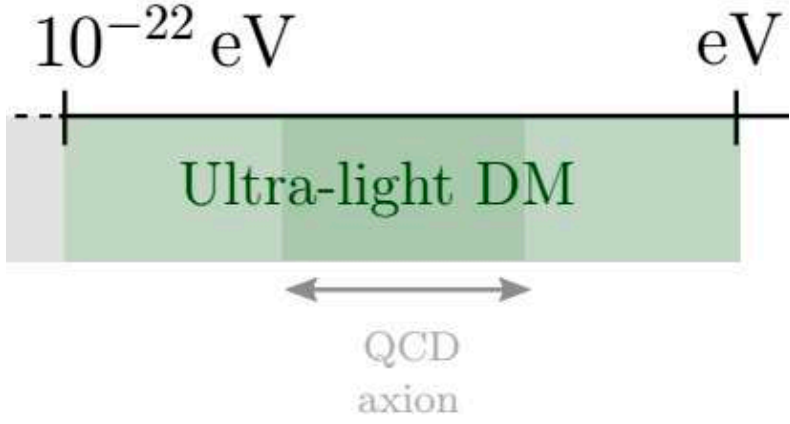


\longrightarrow

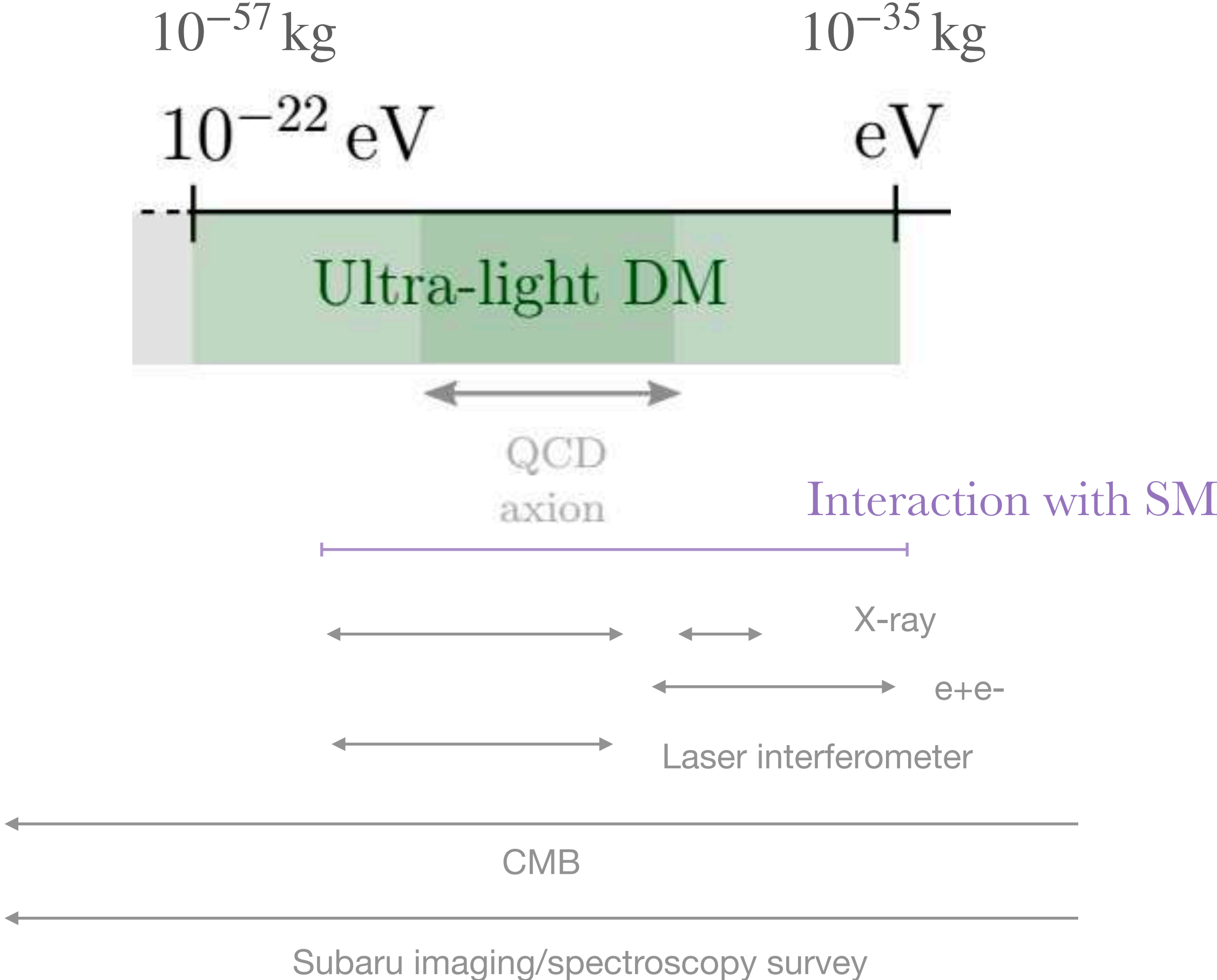
Bosons

Non-thermally produced

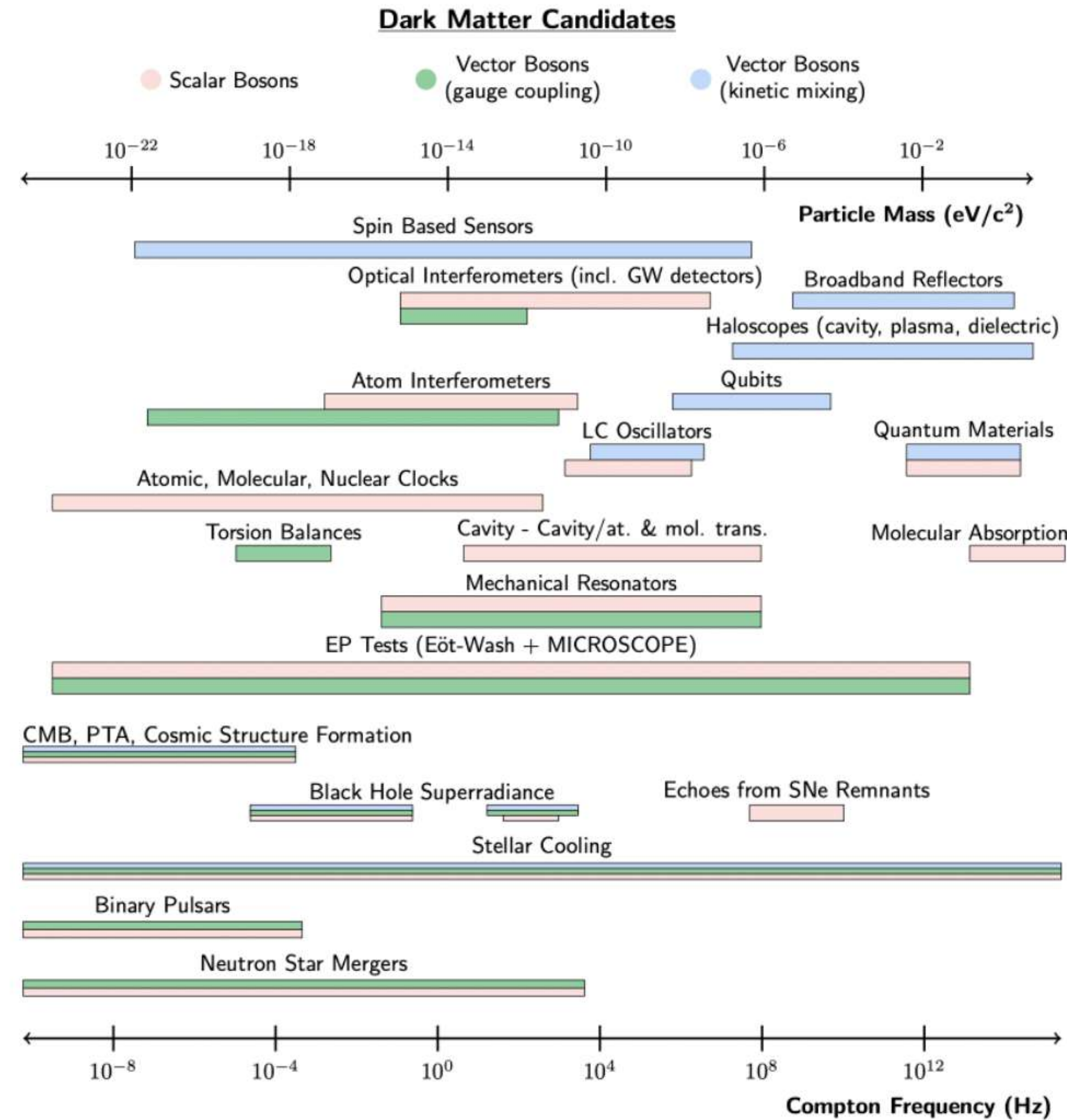
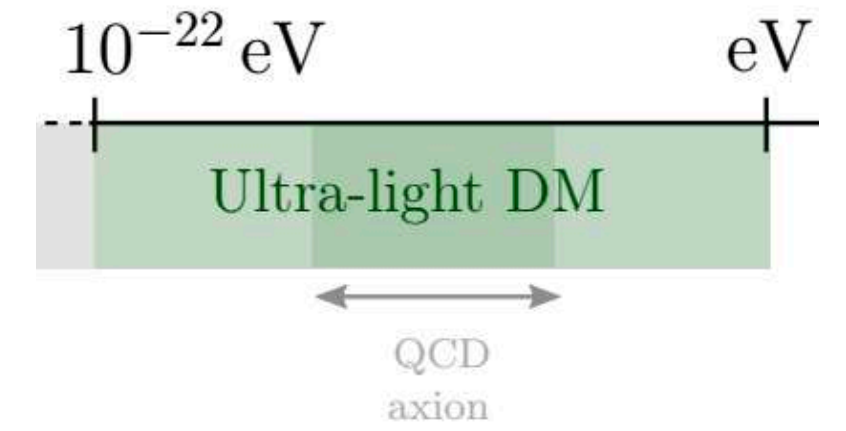
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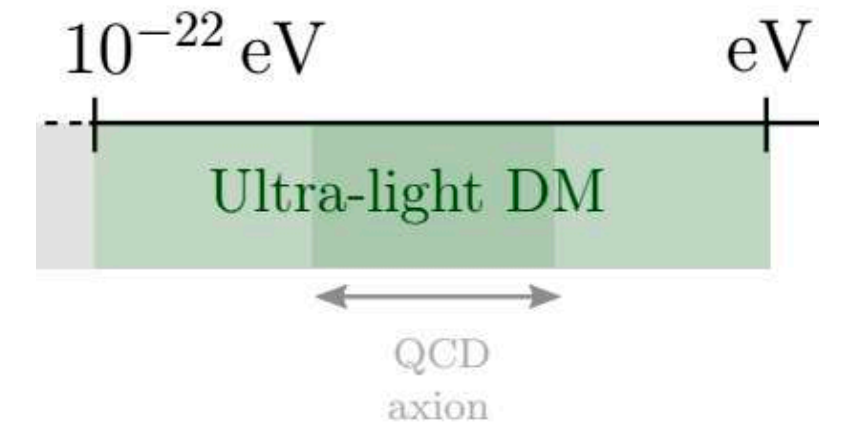


Ultra-light Dark Matter

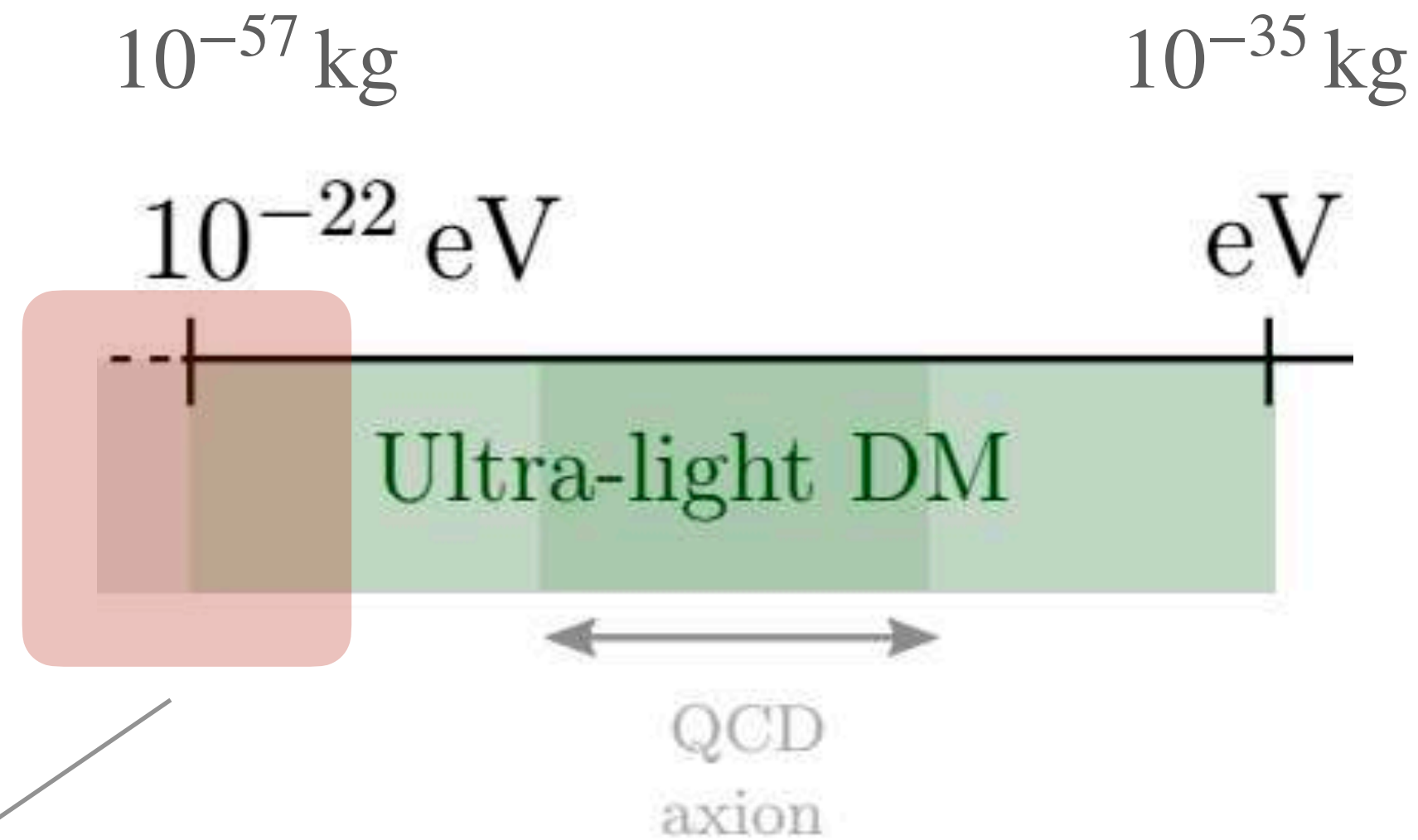


Adapted from "Snowmass 2021 White Paper
New Horizons: Scalar and Vector Ultralight Dark
Matter", 2203.14915

Ultra-light Dark Matter

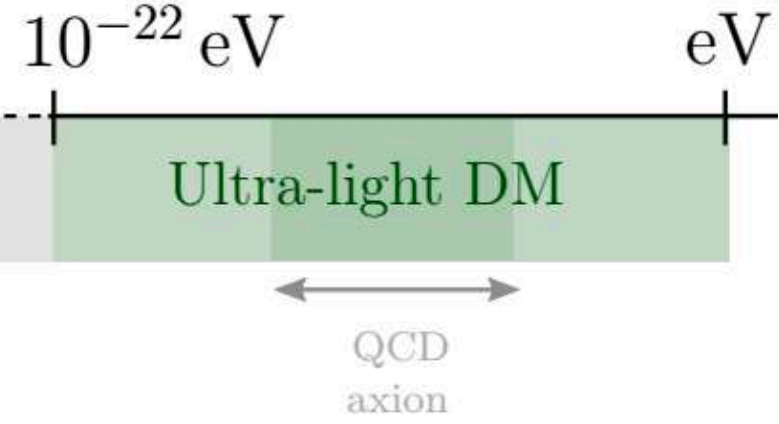


Ultra-light candidate, cold \longrightarrow Large $\lambda_{\text{dB}} \sim 1/mv$



$$10^{-24} \text{ eV} \lesssim m_{\text{fdm}} \lesssim 10^{-18} \text{ eV}$$

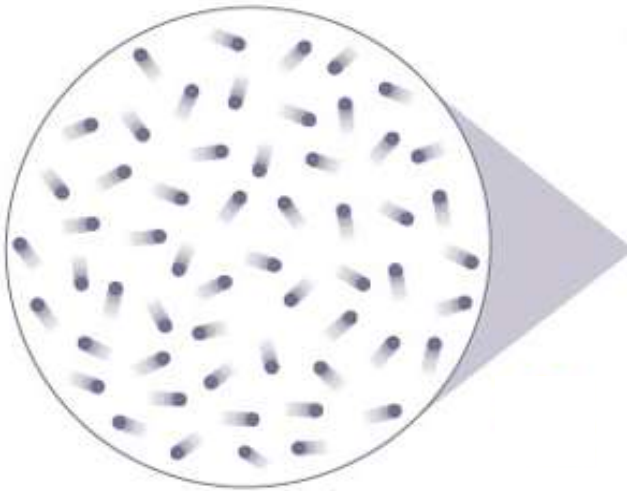
Ultra-light Dark Matter



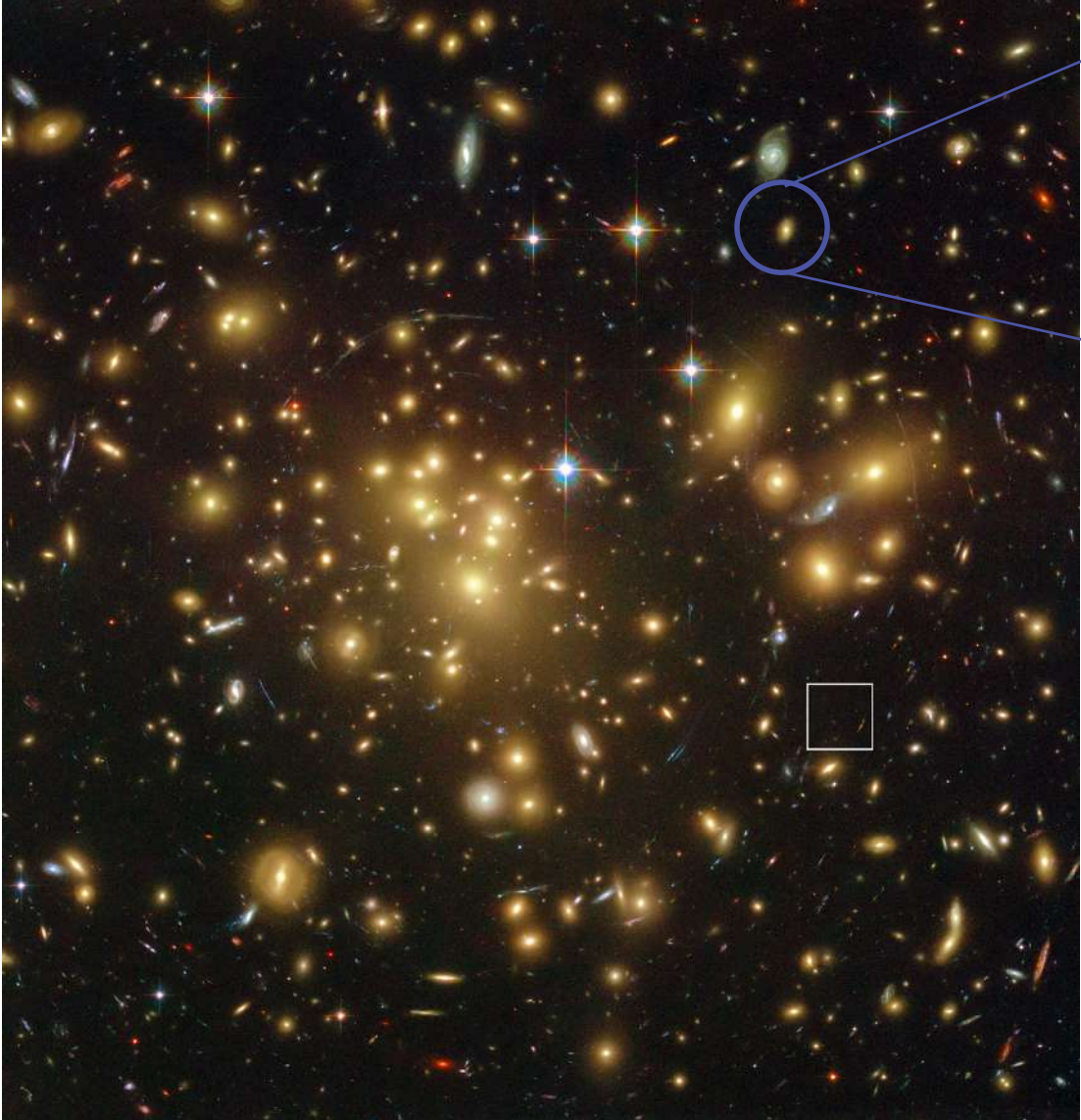
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Lightest possible candidate for DM

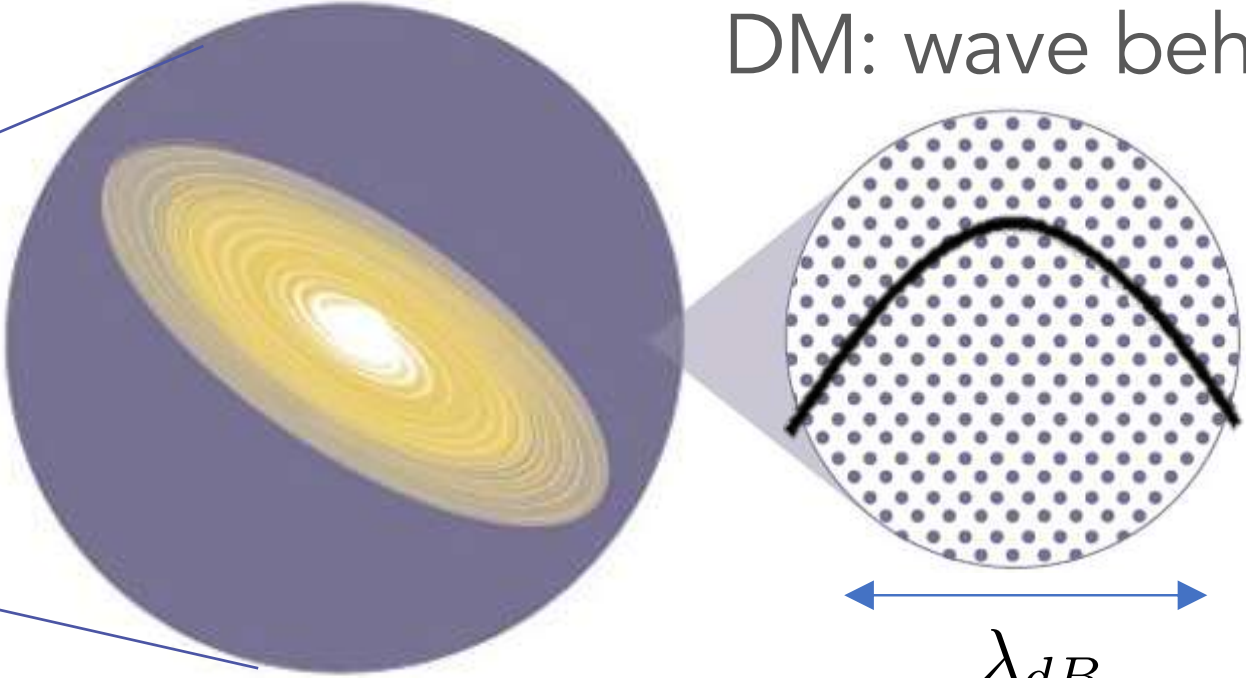
Large scales:
DM behaves like standard particle DM (**CDM**).



DM: particles
 $d \gg \lambda_{dB}$



Adapted from Quanta



Galaxy halo

DM: wave behaviour

λ_{dB}
 $d \ll \lambda_{dB}$

Small scales:
DM behaves like a **wave**

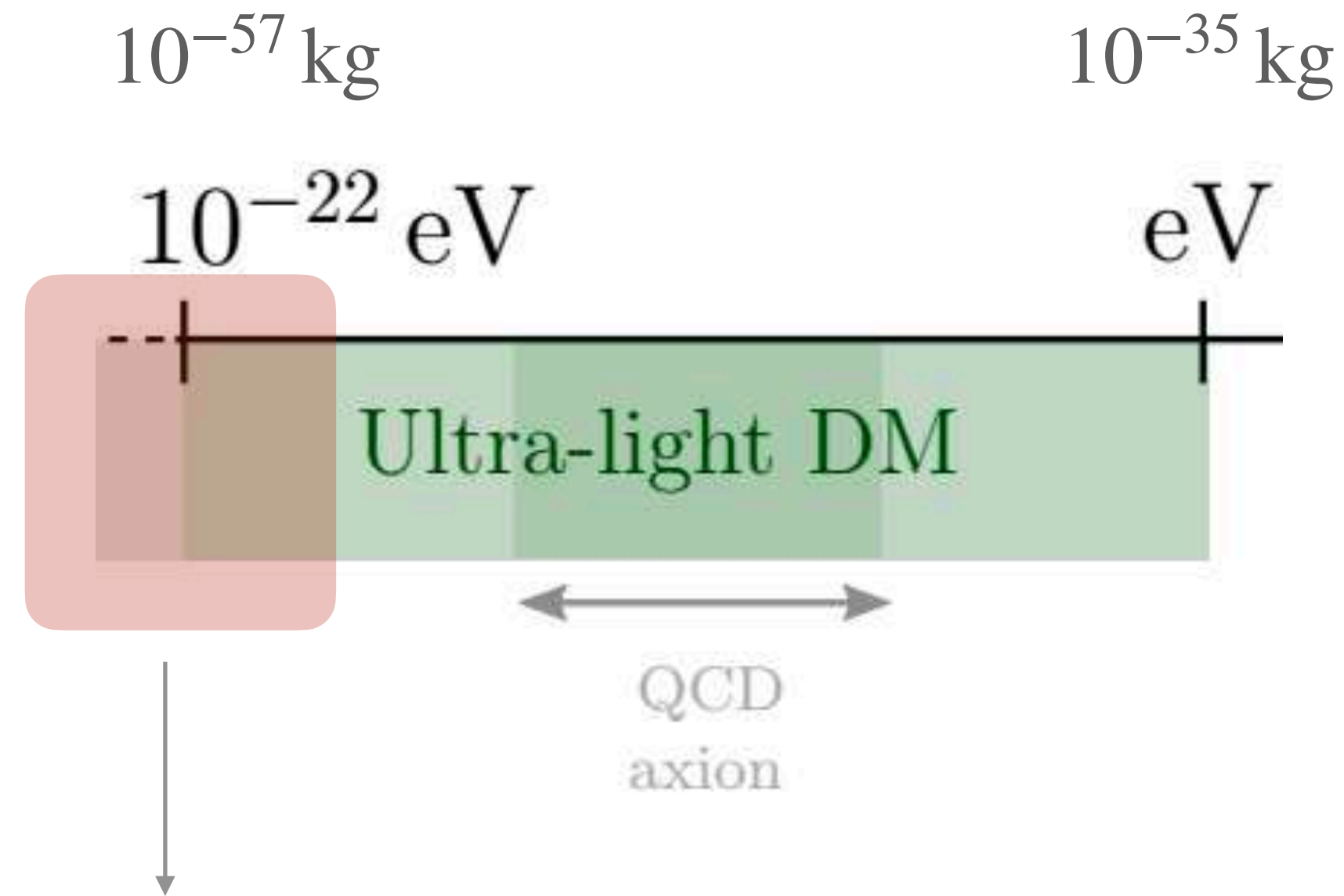
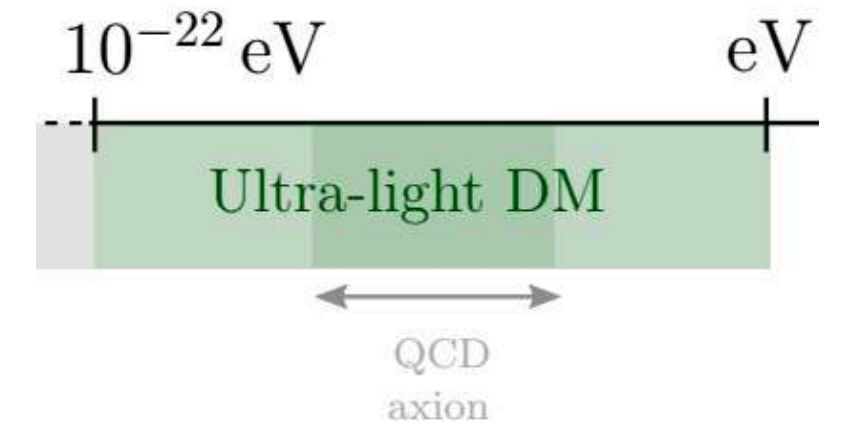
$$10^{-60} \text{ kg} \quad 10^{-35} \text{ kg}$$

$$10^{-22} \text{ eV} \lesssim m \lesssim \text{eV}$$

$$\lambda_{dB}^{ULDM} \sim \text{pc} - \text{kpc}$$

Ultra-light Dark Matter

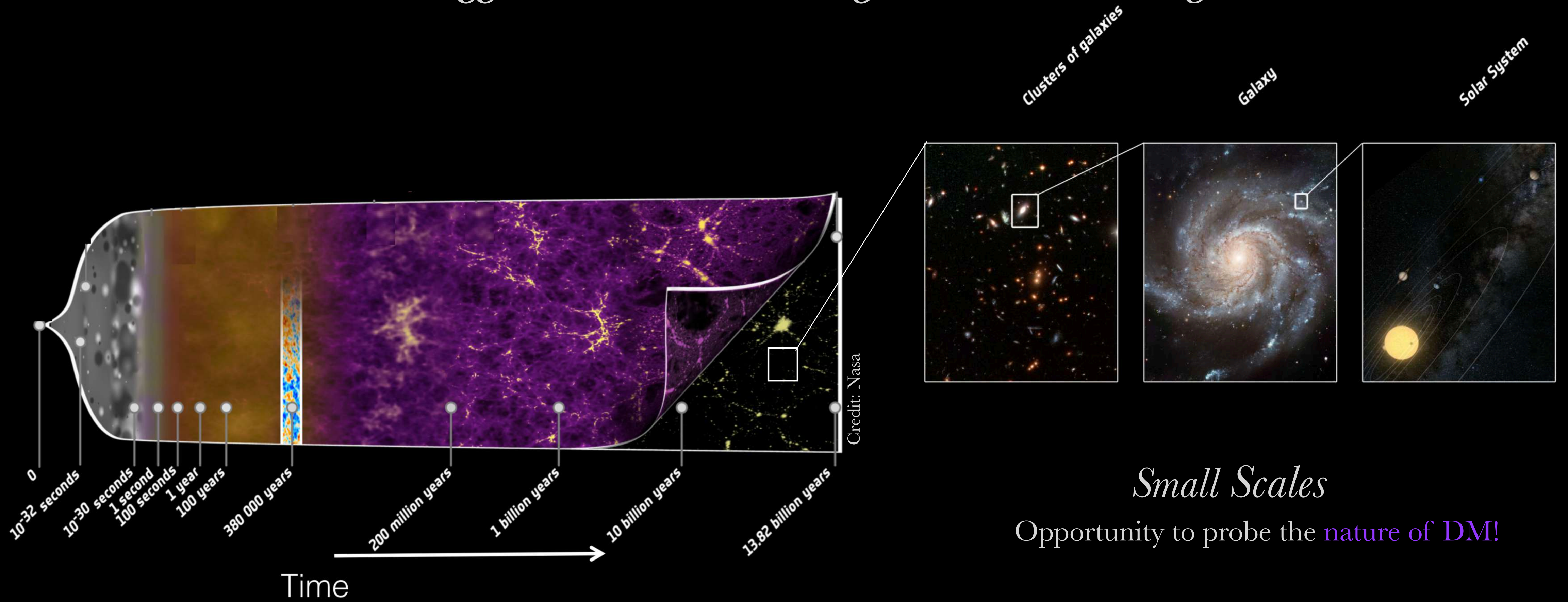
Ultra-light candidate, cold \longrightarrow Large $\lambda_{\text{dB}} \sim 1/mv$



Gravitational probes

$$10^{-24} \text{ eV} \lesssim m_{\text{fdm}} \lesssim 10^{-18} \text{ eV}$$

Small scales can offer some *hints* of the nature of DM



Astrophysical
Observables

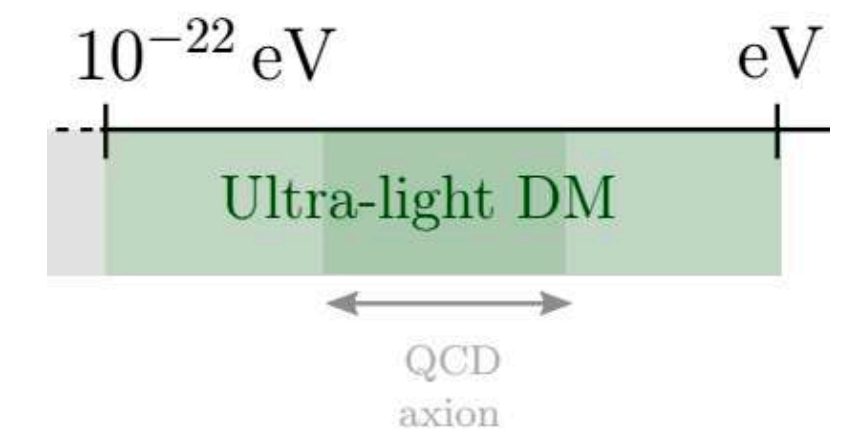


DM
Distribution

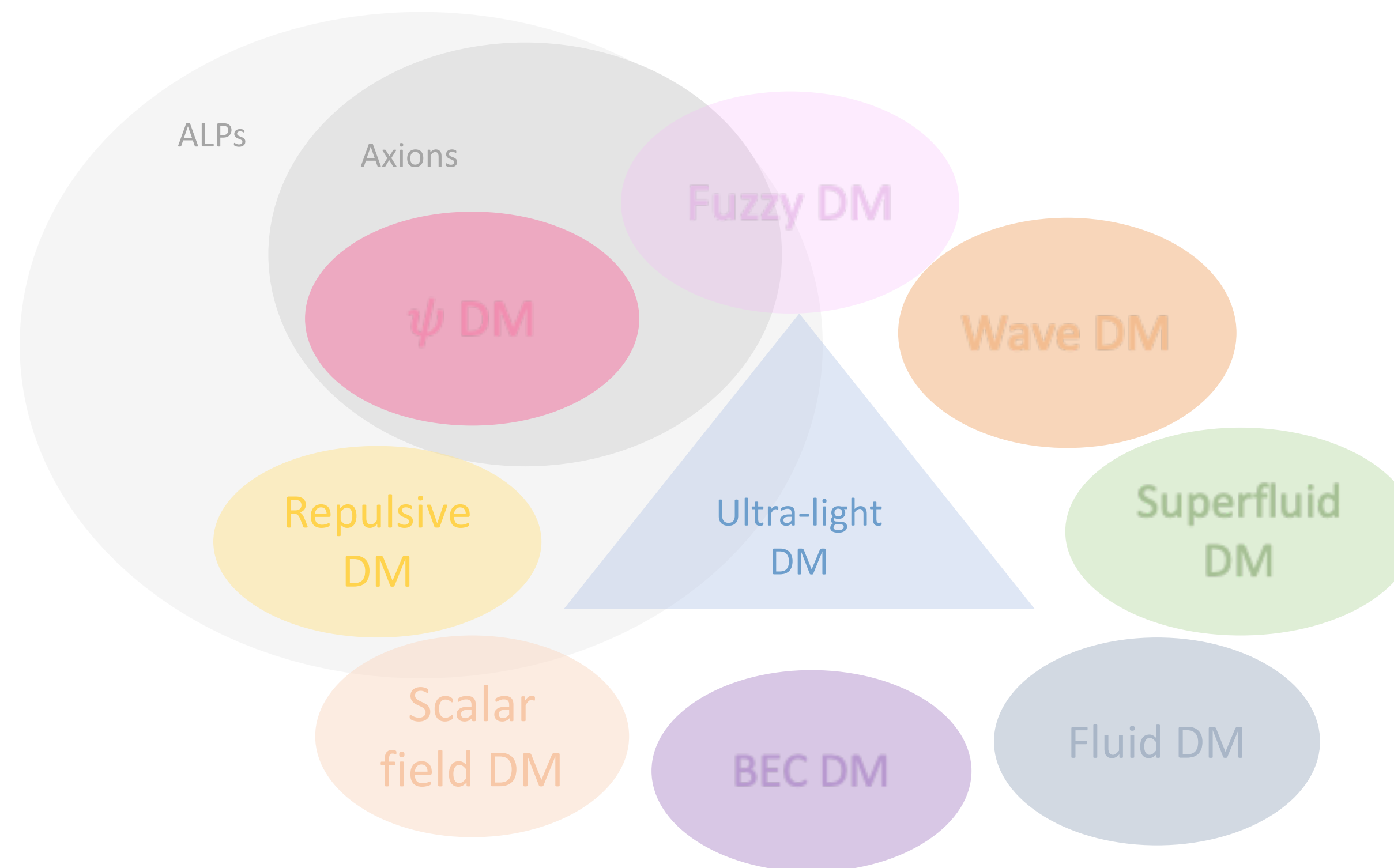


Nature of DM
Microphysics
Particle physics

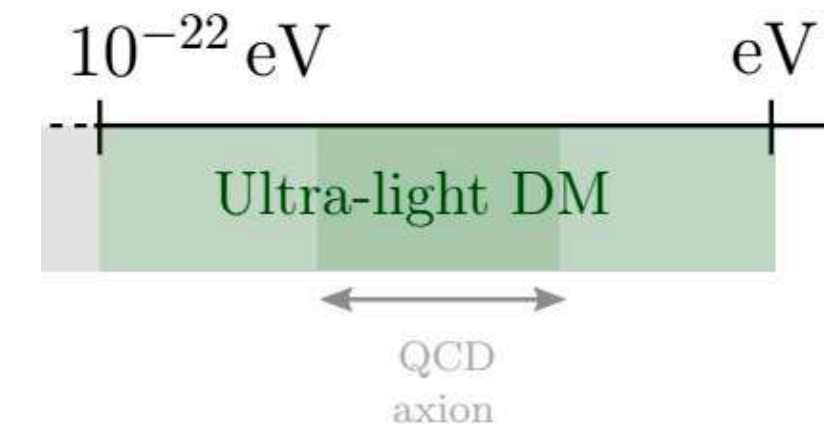
Ultra-light Dark Matter - models



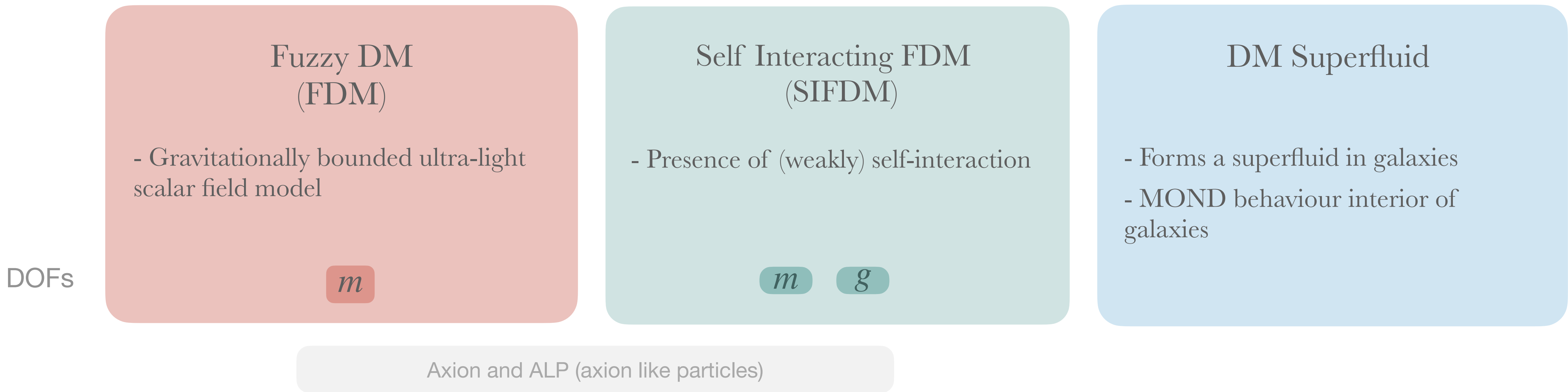
There are many ways to have a DM with this property \rightarrow many ULDM models in the literature
However, each of these models presents a different dynamics on small scales - different **phenomenology**



Ultra-light Dark Matter -classes



3 classes:



$$i\dot{\psi} = \left(-\frac{1}{2m} \nabla^2 + \frac{g}{8m^2} |\psi|^2 - m\Phi \right) \psi$$

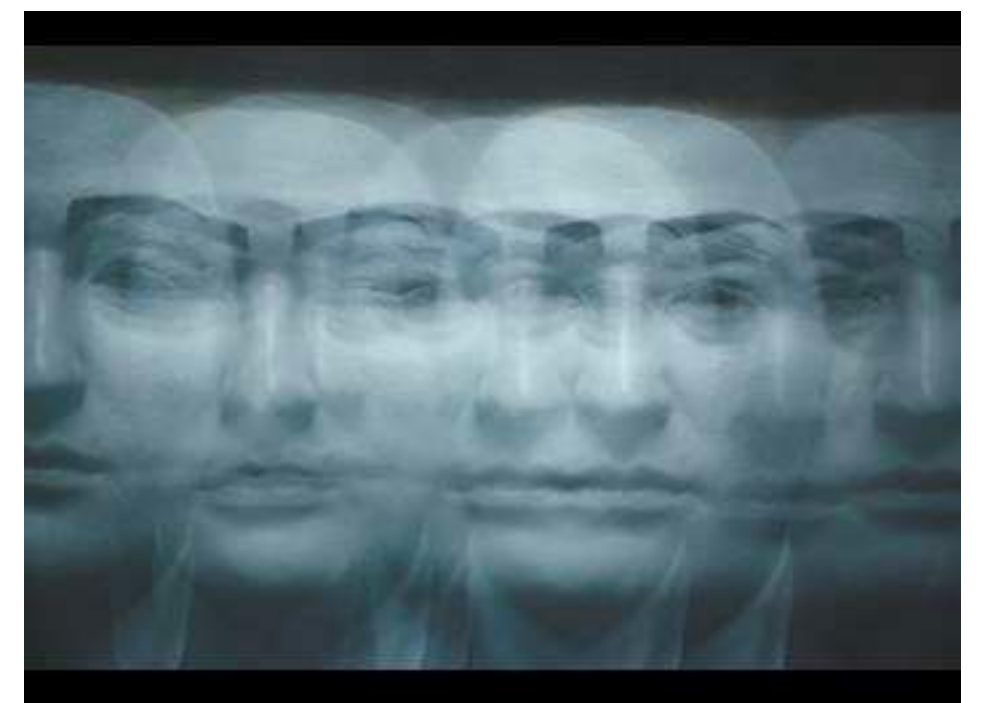
$$\mathcal{L} = P(X)$$

→ Formation mechanism: see Satoshi Shirai's talk!

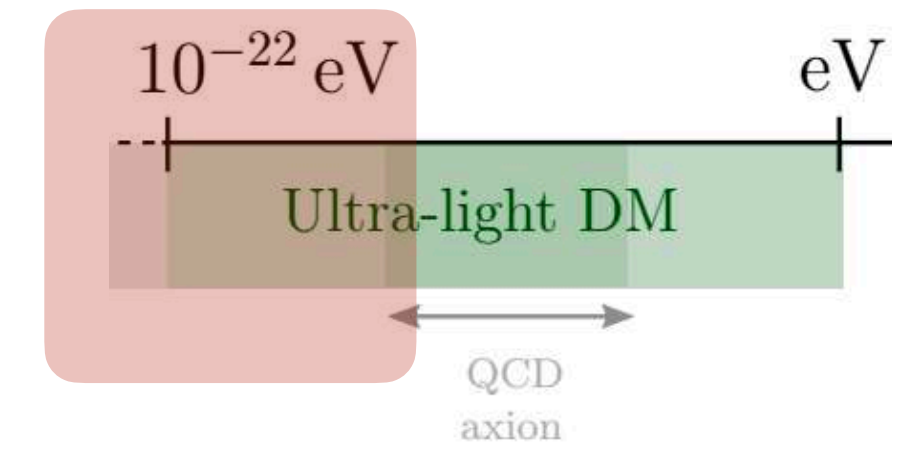
“Ultra-light dark matter”, **E.Ferreira**, 2020. *The Astronomy and Astrophysics Review*.

Fuzzy dark matter

Self interacting fuzzy dark matter



Fuzzy dark matter



Fuzzy DM (FDM)

- Gravitationally bounded ultra-light scalar field model

m

Wave DM Ultra-light axions

Focus in spin 0 particles here!

(Some of the grav. phenom. is carried for vectors, for example)

*Vector DM: Tomohiro
Fugita's talk!*

Idea:

$$m_{\text{fdm}} \sim 10^{-22} \text{ eV}$$

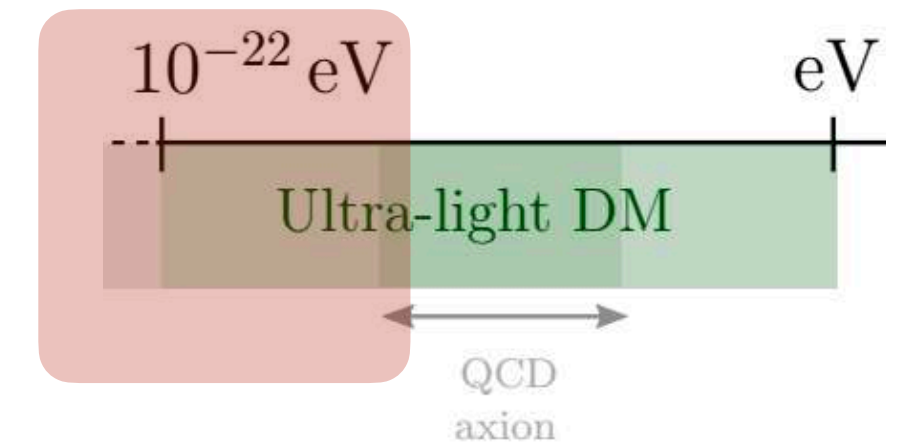
address the small scale problems+ rich phenom.

Hu W, Barkana R, Gruzinov A (2000 a,b)

(Reviews: EF (2021), J. Niemeyer (2019), L. Hui (2021))

Formation mechanism: see Satoshi Shirai's talk!

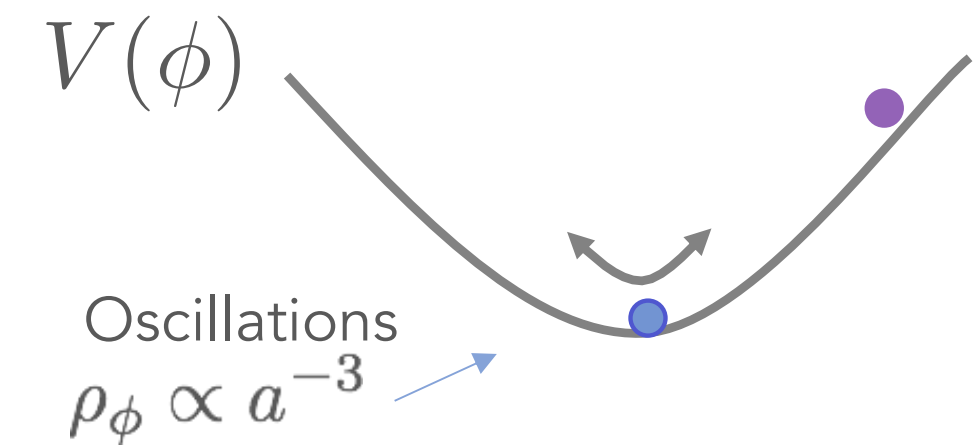
Cosmological evolution



$$\ddot{\phi} + 3H\dot{\phi} + m^2\phi = 0$$

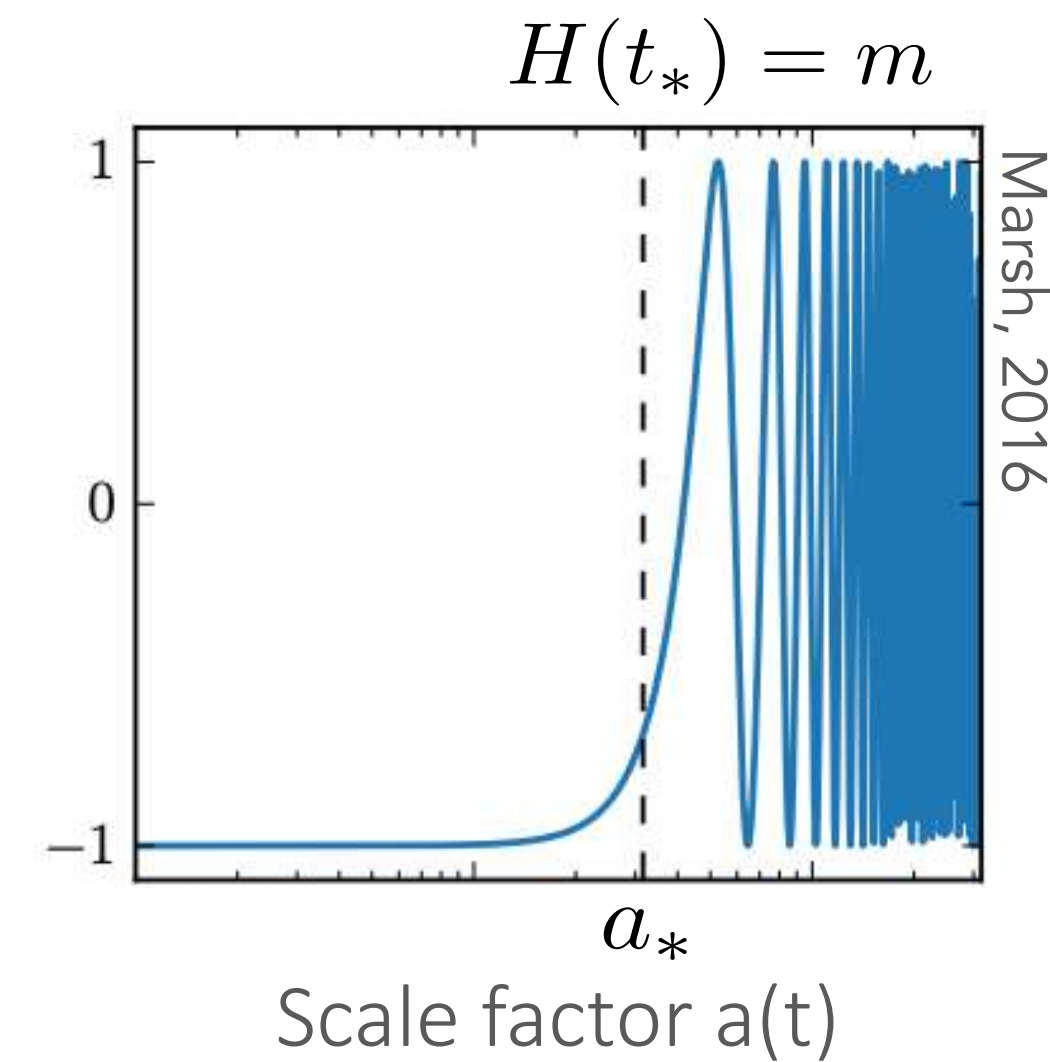
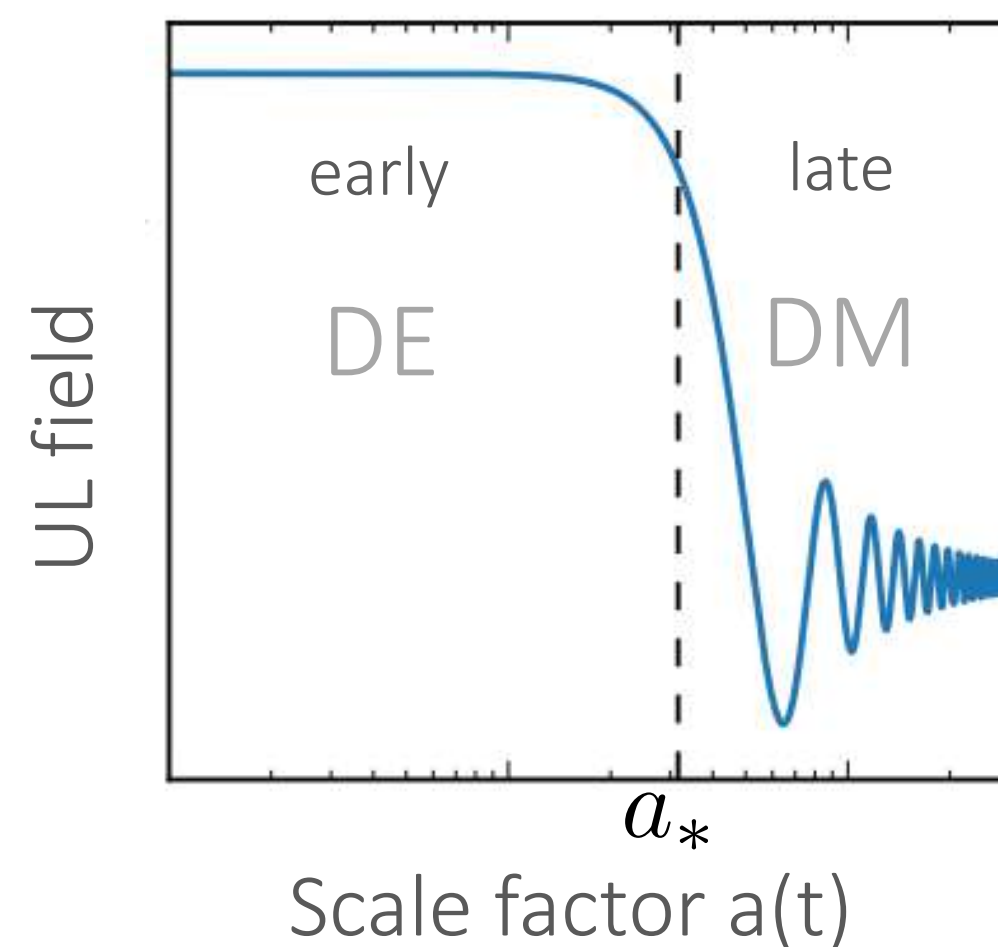
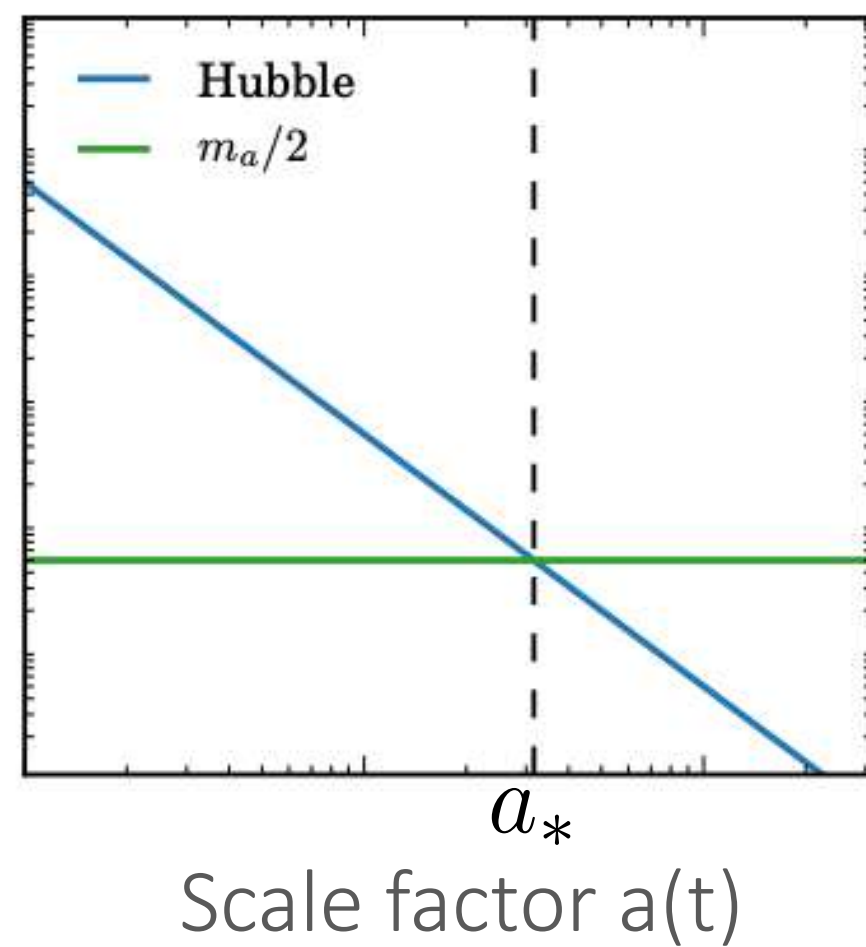
FDM

{	$H \gg m$	\implies	$\phi_{\text{early}} = \phi(t_i)$	\longrightarrow	$\omega = -1$	DE
	$H \ll m$	\implies	$\phi_{\text{late}} \propto e^{imt}$	\longrightarrow	$\langle \omega \rangle = 0$	DM



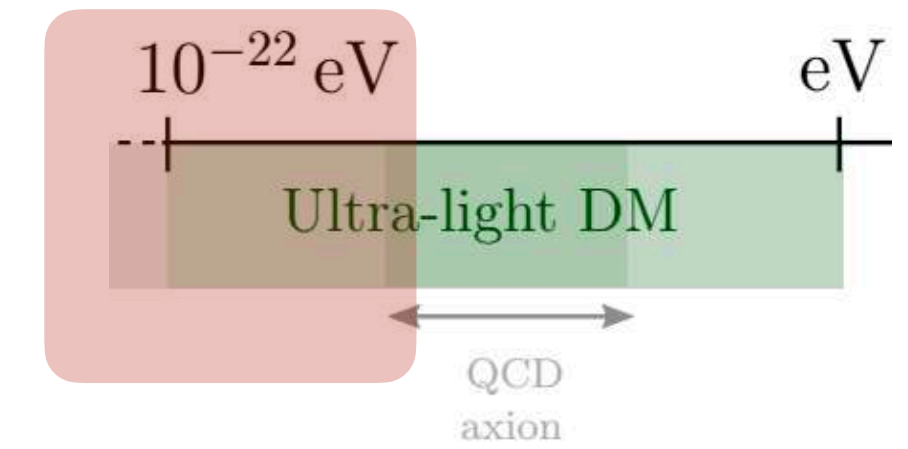
$$V(\phi) = \Lambda_a^4 [1 - \cos(\phi/f_a)]$$

$$\rightarrow \frac{1}{2}m^2\phi^2 + \frac{g}{4}\phi^4$$



In order to **behave like DM**: start oscillating before matter-radiation equality $m > 10^{-28} \text{ eV} \sim H(a_{\text{eq}})$

Structure formation - *non-relativistic regime*



Evolution on small scales: take non-relativistic regime of the theory, relevant for structure formation.

Schrödinger-Poisson system : describe the FDM and the SIFDM

$$\left\{ \begin{array}{l} i\dot{\psi} = \left(-\frac{1}{2m}\nabla^2 + \frac{g}{8m^2}|\psi|^2 - m\Phi \right) \psi \\ \nabla^2\Phi = 4\pi G(m|\psi|^2 - \bar{\rho}) \end{array} \right.$$

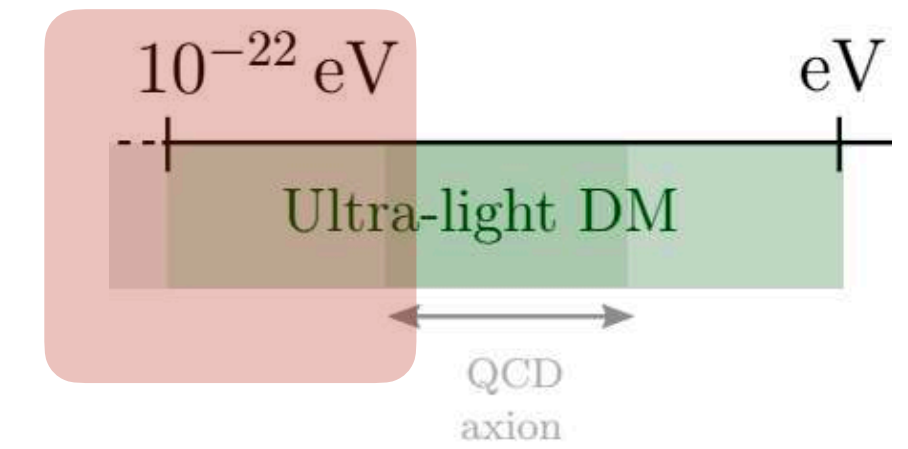
Schrödinger equation
(Gross-Pitaevskii)

Poisson equation

$g = 0 \longrightarrow$ FDM
 $g \neq 0 \longrightarrow$ SIFDM

Fundamentally different than
CDM/WDM/SIDM!

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Madelung equations

$(\psi \equiv \sqrt{\rho/m} e^{i\theta} \text{ and } \mathbf{v} \equiv \nabla\theta/m)$

$$\dot{\rho} + \nabla \cdot (\rho \mathbf{v}) = 0$$

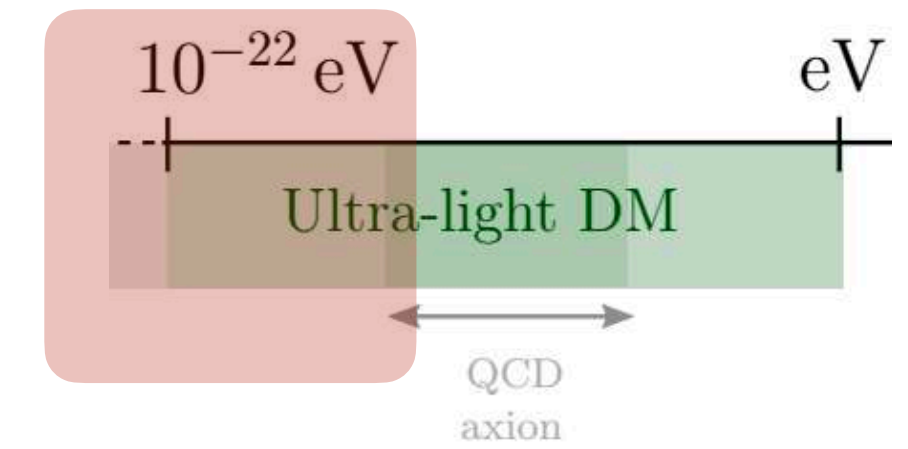
$$\dot{\mathbf{v}} + (\mathbf{v} \cdot \nabla)\mathbf{v} = -\frac{1}{m} \left(V_{grav} - P_{int} - \frac{1}{2m} \frac{\nabla^2 \sqrt{\rho}}{\sqrt{\rho}} \right)$$

$$P_{int} = K\rho^{(j+1)/j} = \frac{g}{2m^2}\rho^2$$

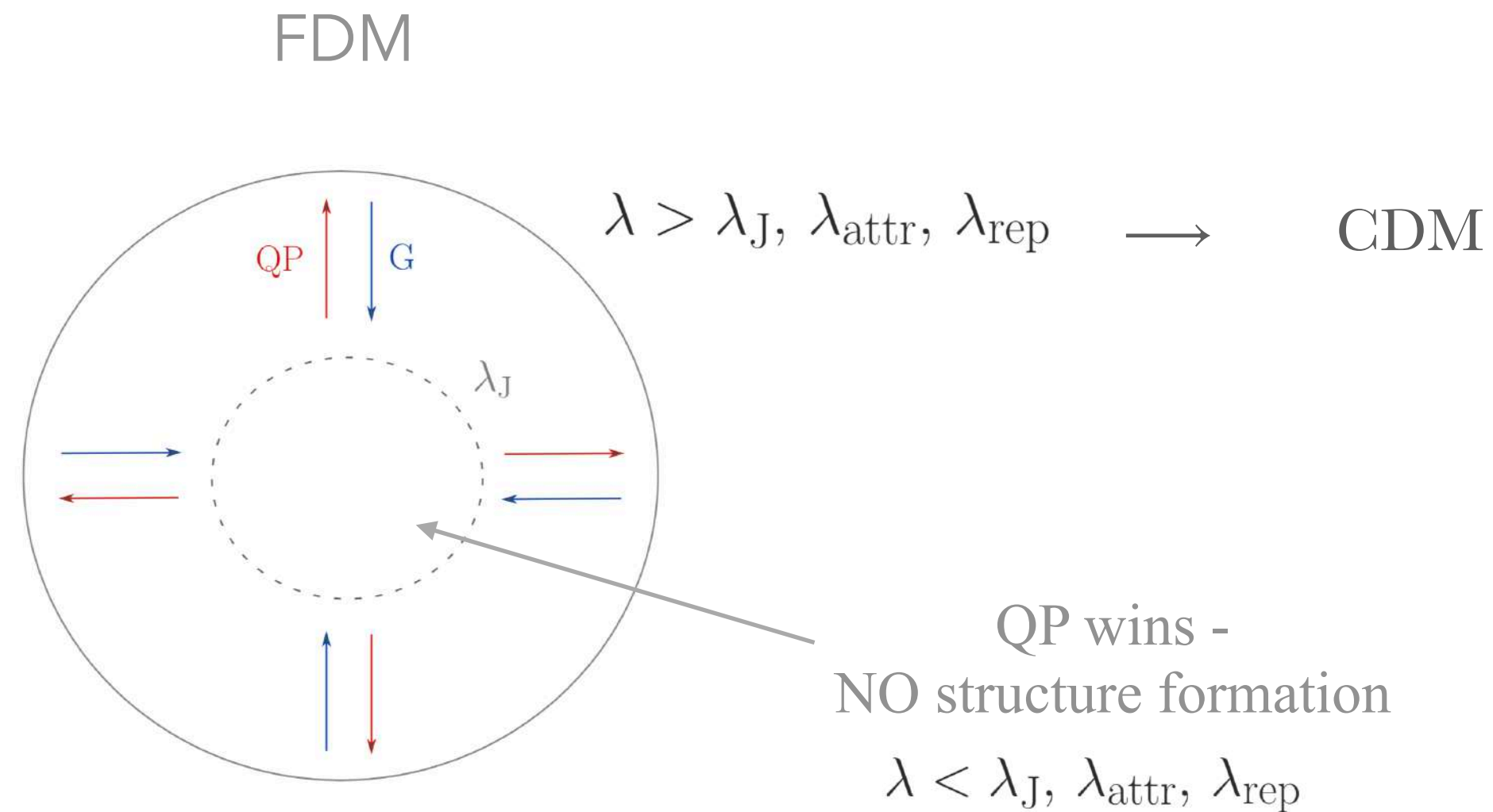
Quantum pressure

FLUID
DESCRIPTION

Structure formation - perturbation and stability



Finite clustering scale - no structure formation on small scales



Finite size coherent core – Bose stars

$$\lambda_J = 55 \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-1/2} \left(\frac{\rho}{\bar{\rho}} \right)^{-1/4} (\Omega_m h)^{-1/4} \text{ kpc}$$

$$m \leq 10^{-20} \text{ eV} \Rightarrow \lambda_{dB} > \mathcal{O}(\text{kpc})$$

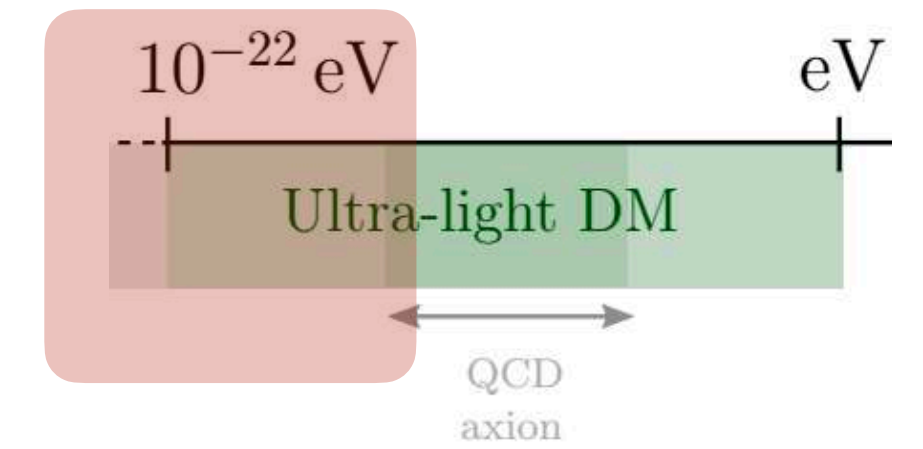
Galactic scales

$$\dot{\rho} + \nabla \cdot (\rho \mathbf{v}) = 0$$

$$\dot{\mathbf{v}} + (\mathbf{v} \cdot \nabla) \mathbf{v} = -\frac{1}{m} \left(V_{\text{grav}} - \overset{P_{\text{int}} = \frac{g}{2m^2} \rho^2}{\boxed{P_{\text{int}}}} - \underbrace{\frac{1}{2m} \frac{\nabla^2 \sqrt{\rho}}{\sqrt{\rho}}}_{\text{Quantum pressure}} \right)$$

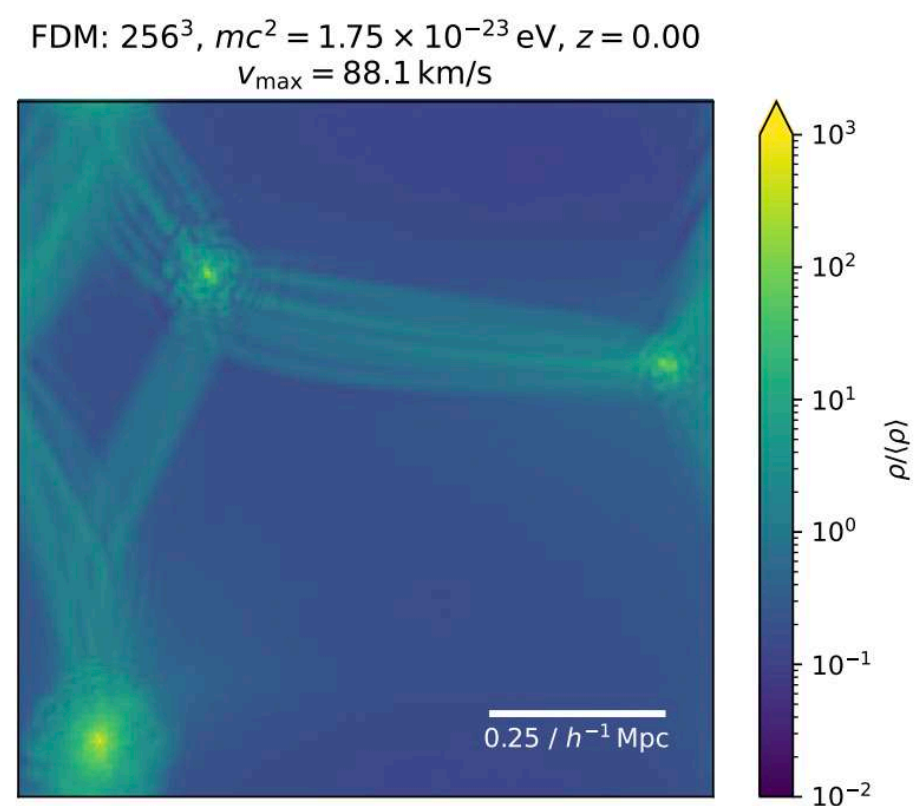
Phenomenology

RICH PHENOMENOLOGY ON SMALL SCALES

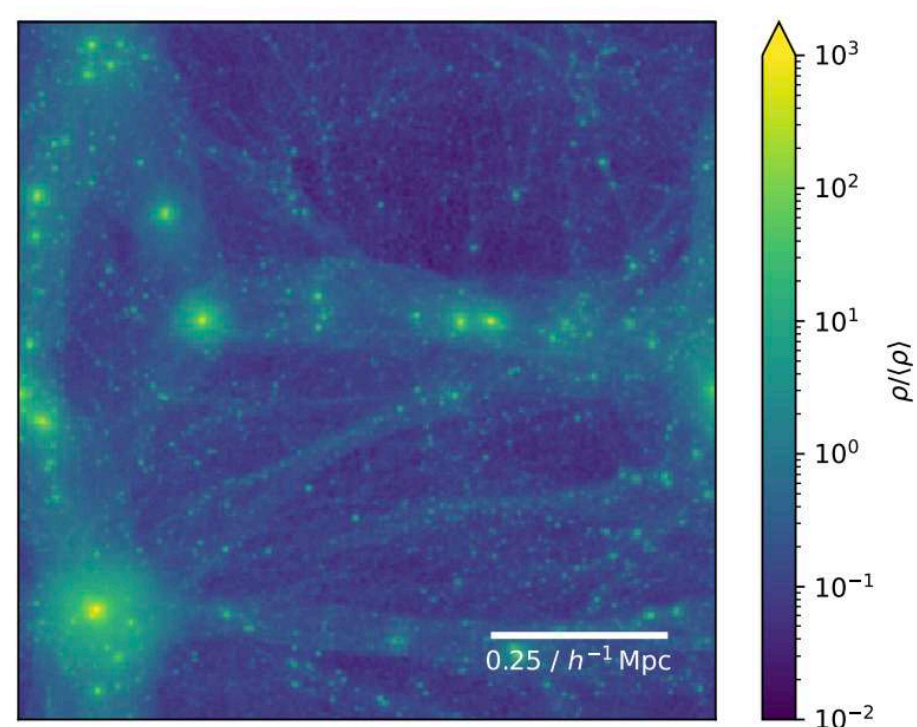


* Focus only in gravitational signatures

Suppression of small structures

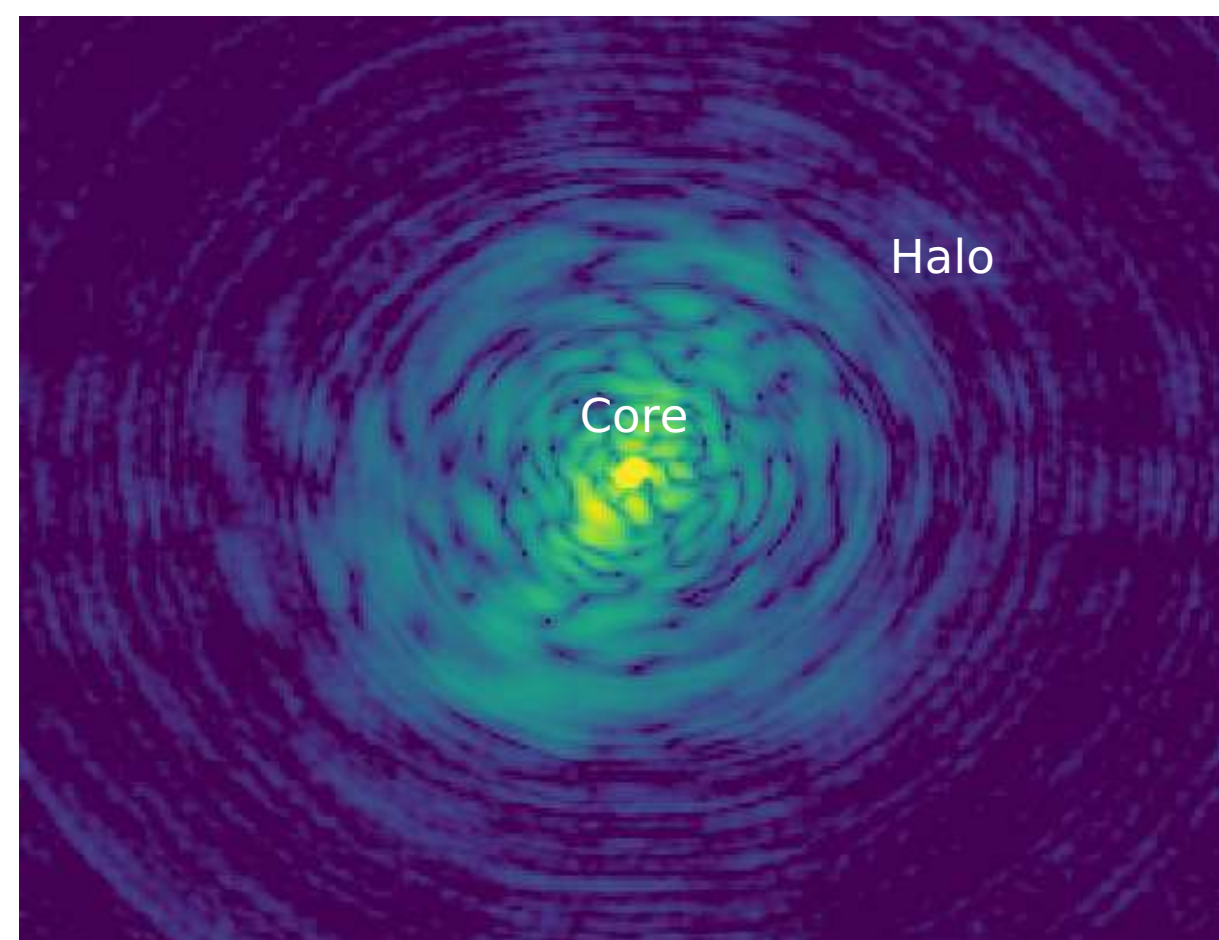


CDM: 256^3 , $z = 0.00$

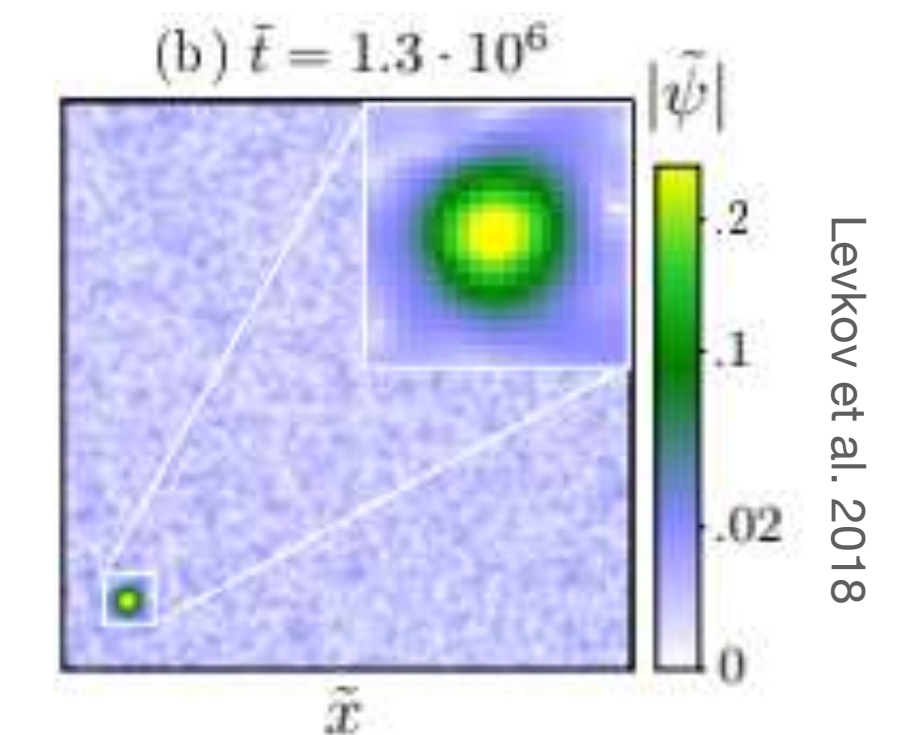


S. May et al. 2021

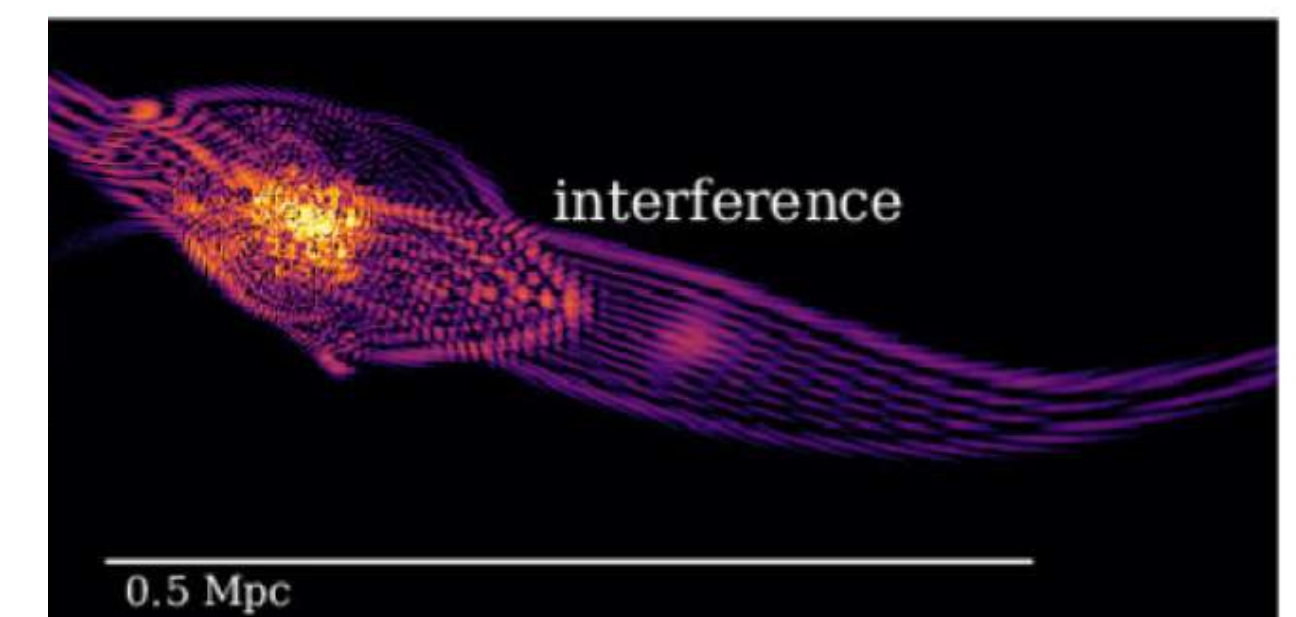
Formation of a solitonic core



Dynamical effects

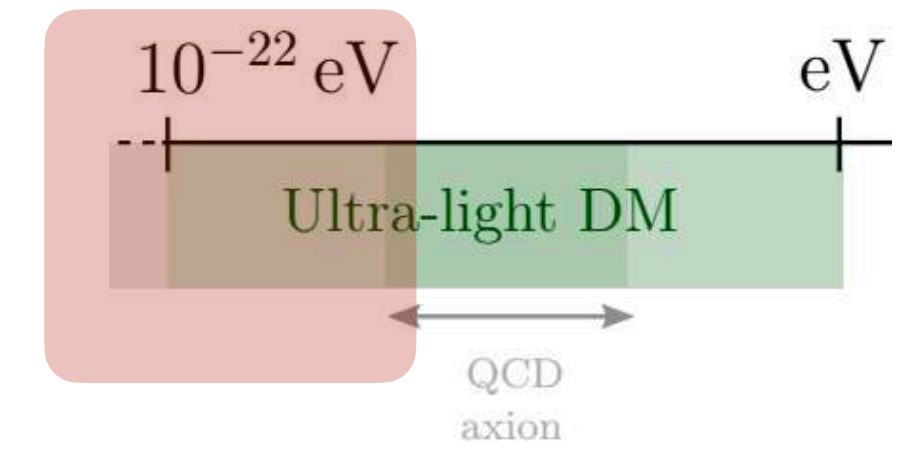


Wave interference



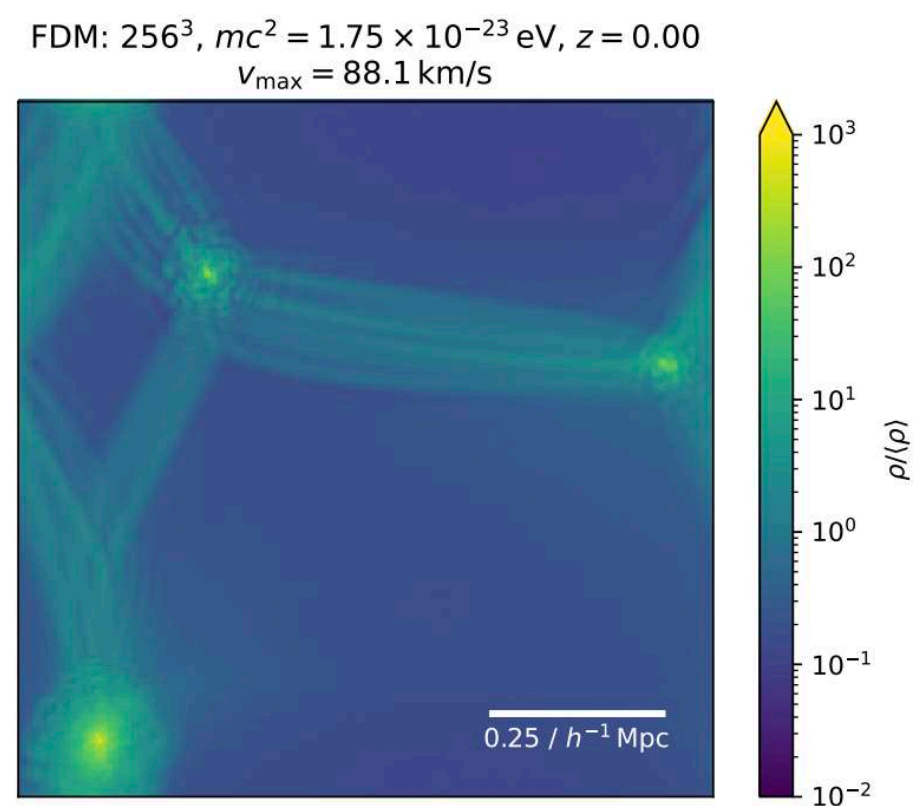
Mocz et al. 2017

Phenomenology

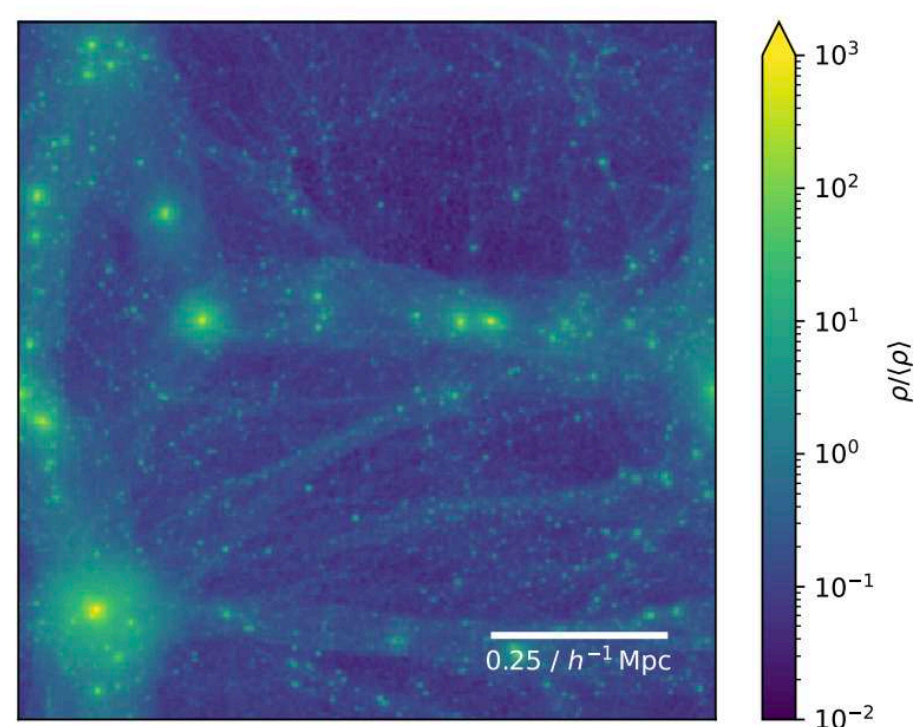


RICH PHENOMENOLOGY ON SMALL SCALES

Suppression of small structures

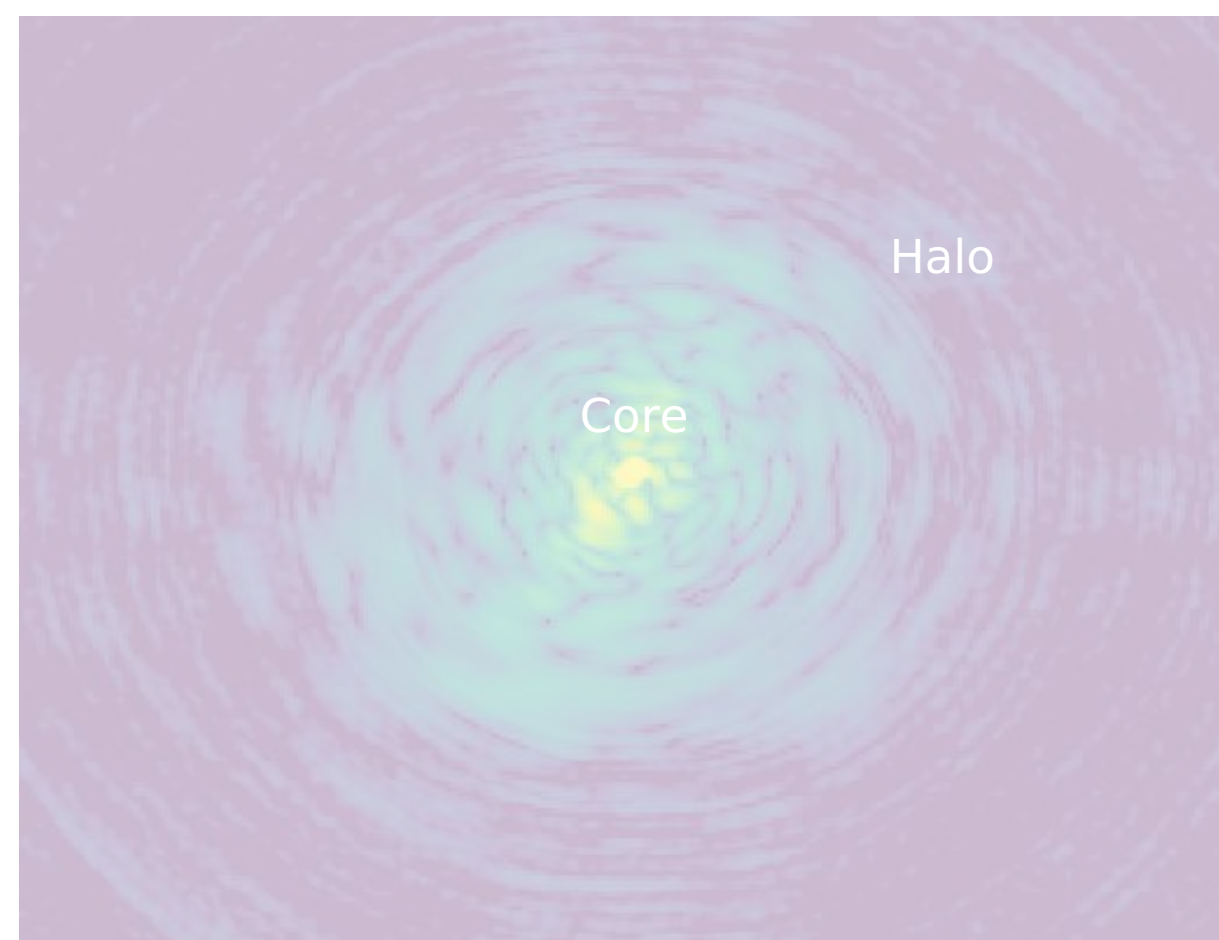


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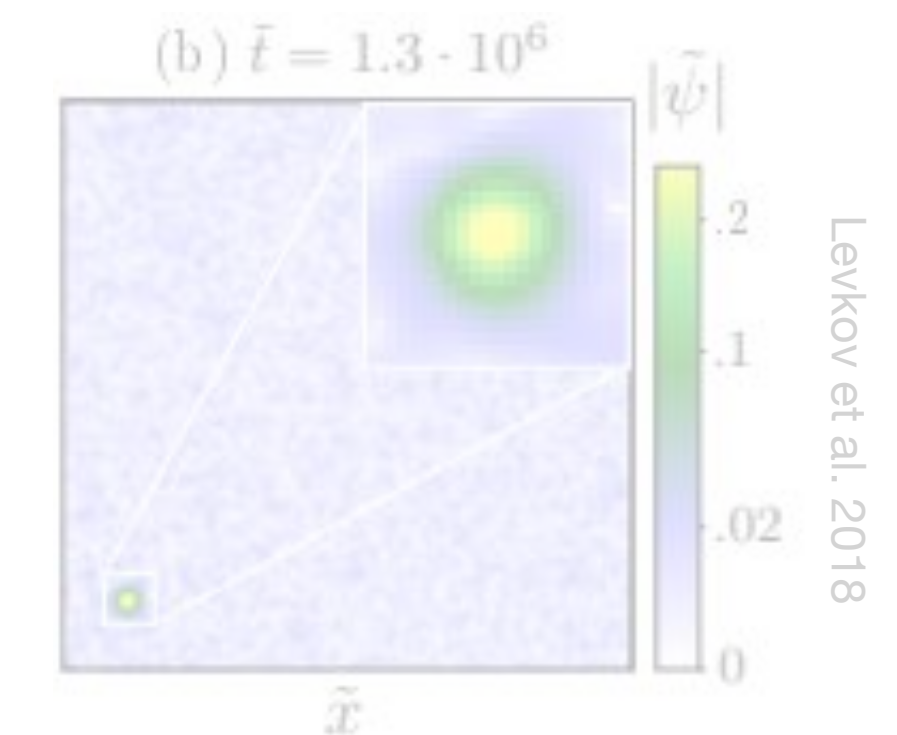


S. May et al. 2021

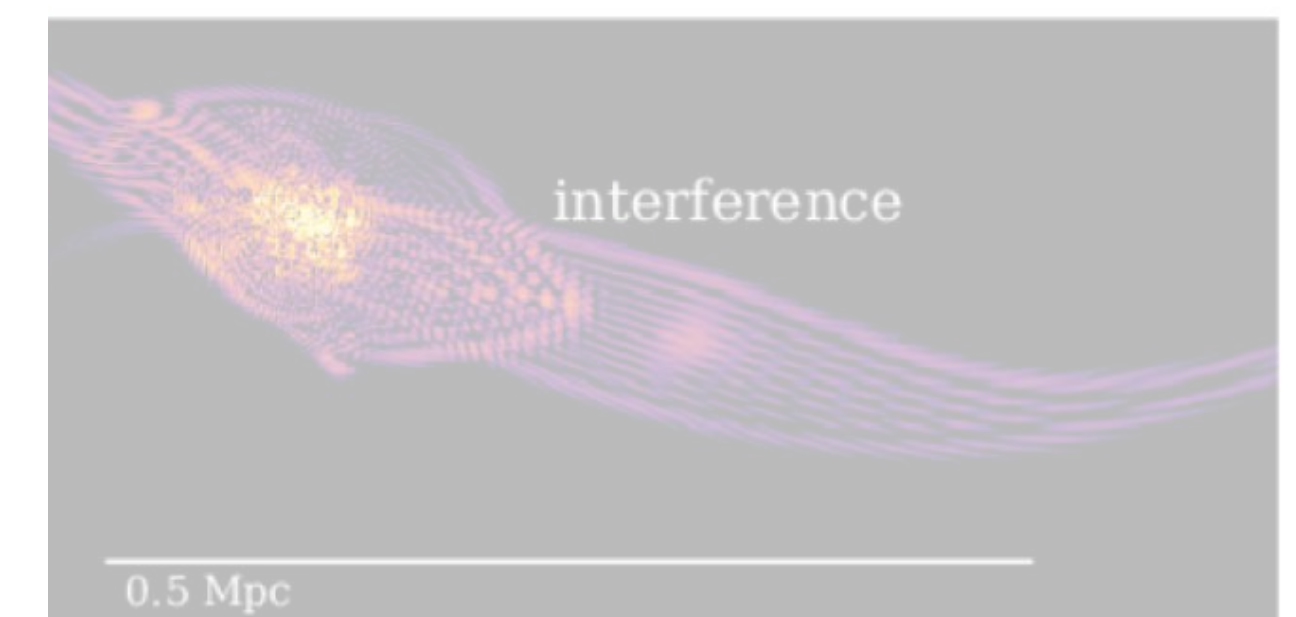
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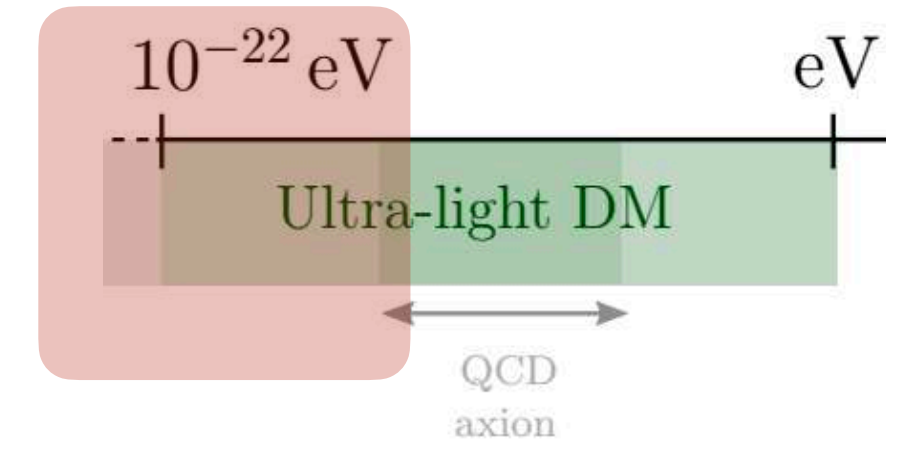
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Phenomenology

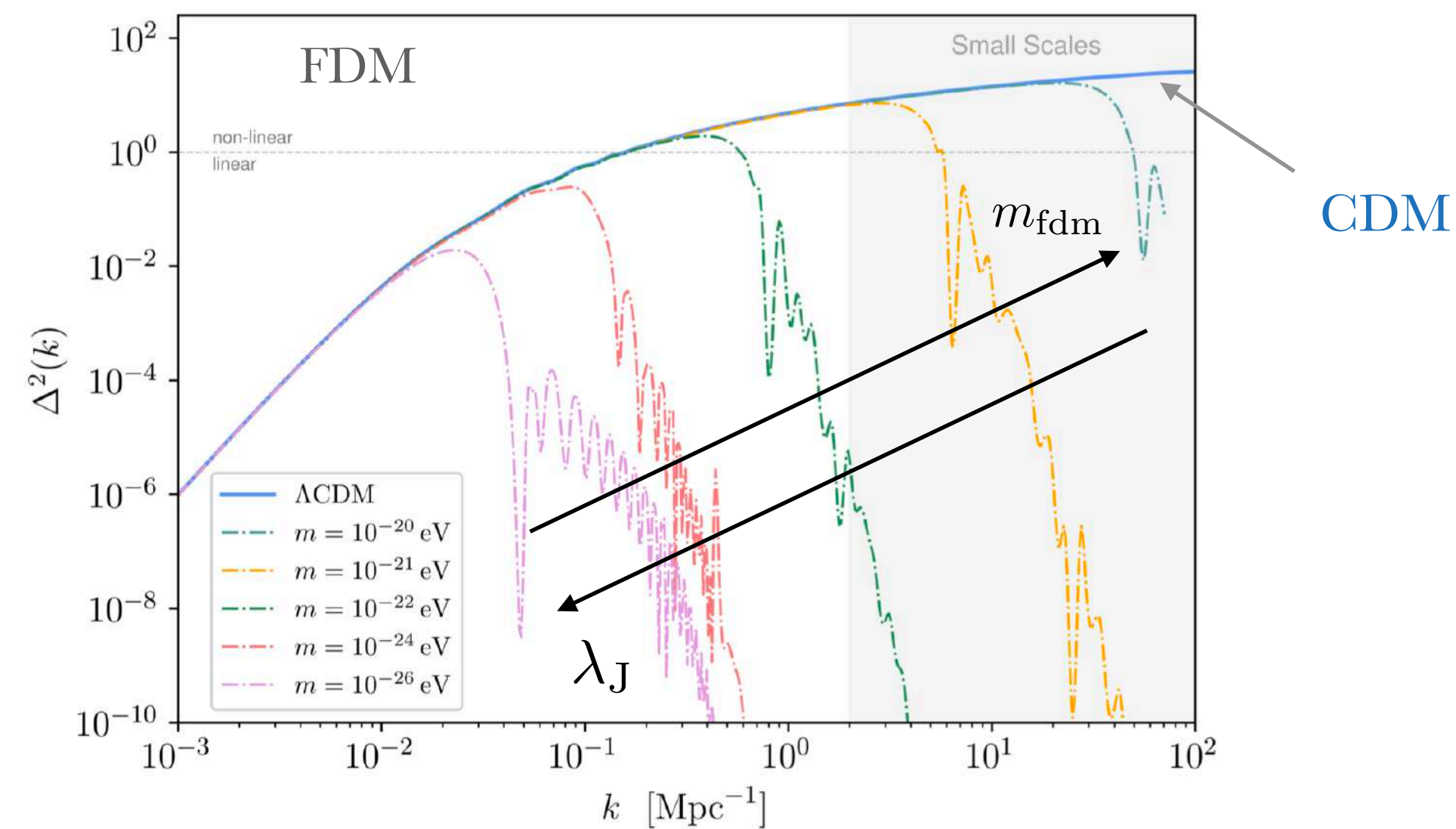
Suppression of small structures



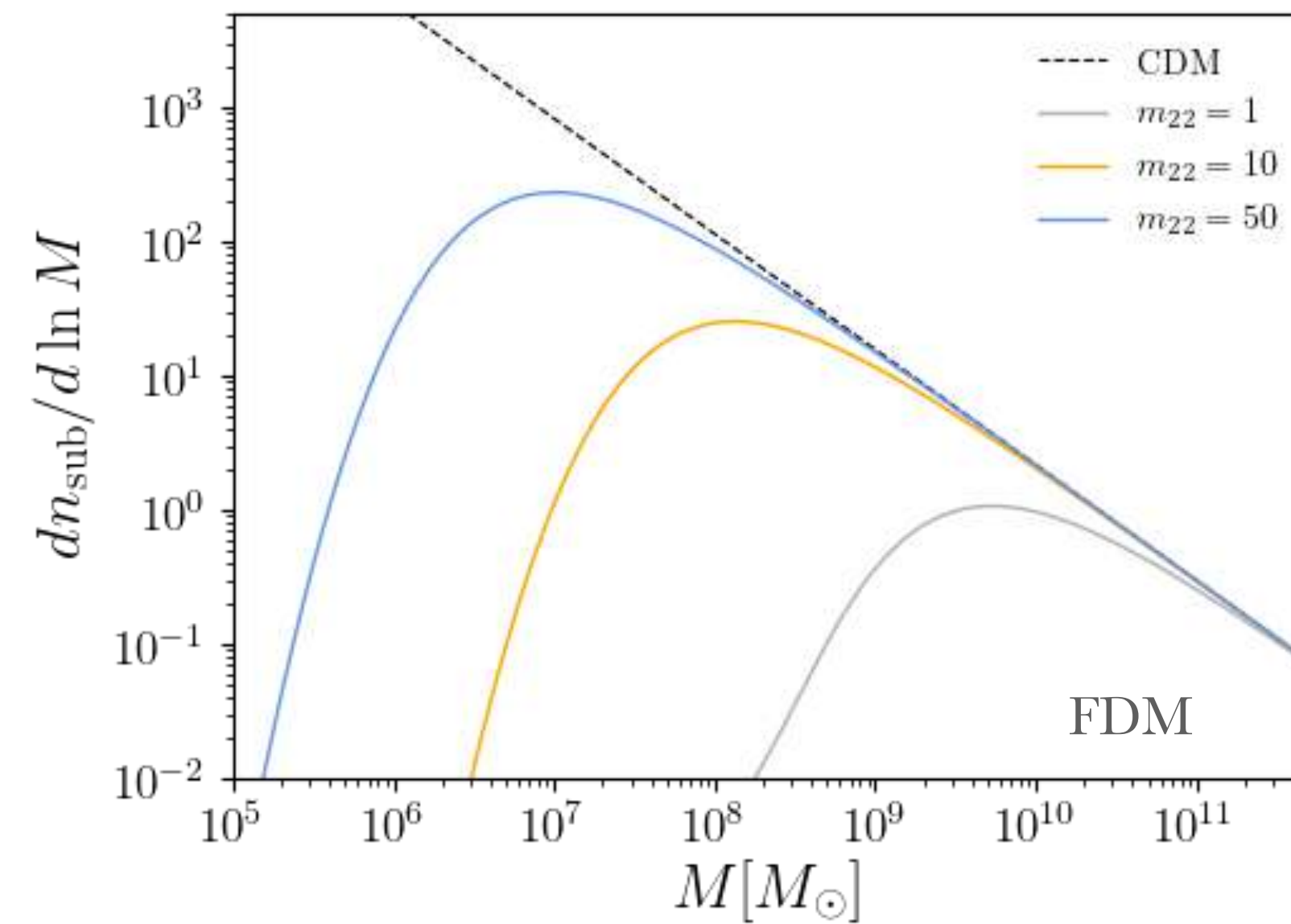
Finite Jeans length λ_J or $\lambda_{\text{attr}}, \lambda_{\text{rep}}$ \longrightarrow

Suppresses small scale structure

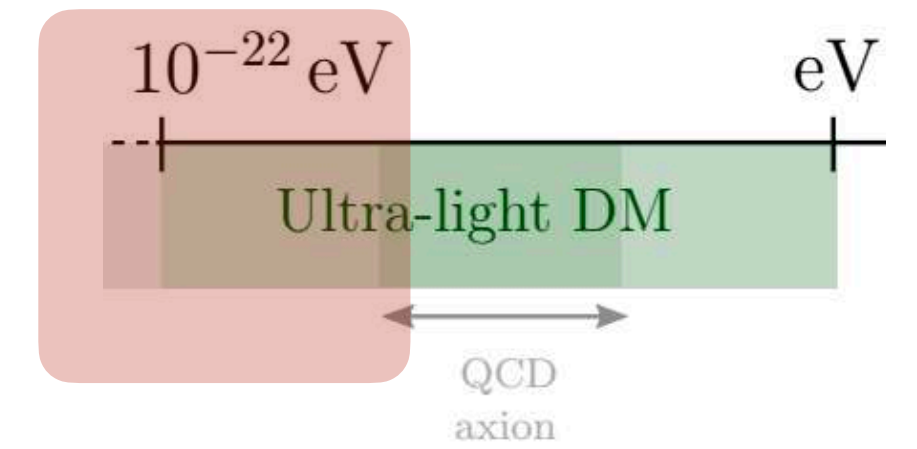
POWER SPECTRUM



(sub) HALO MASS FUNCTION

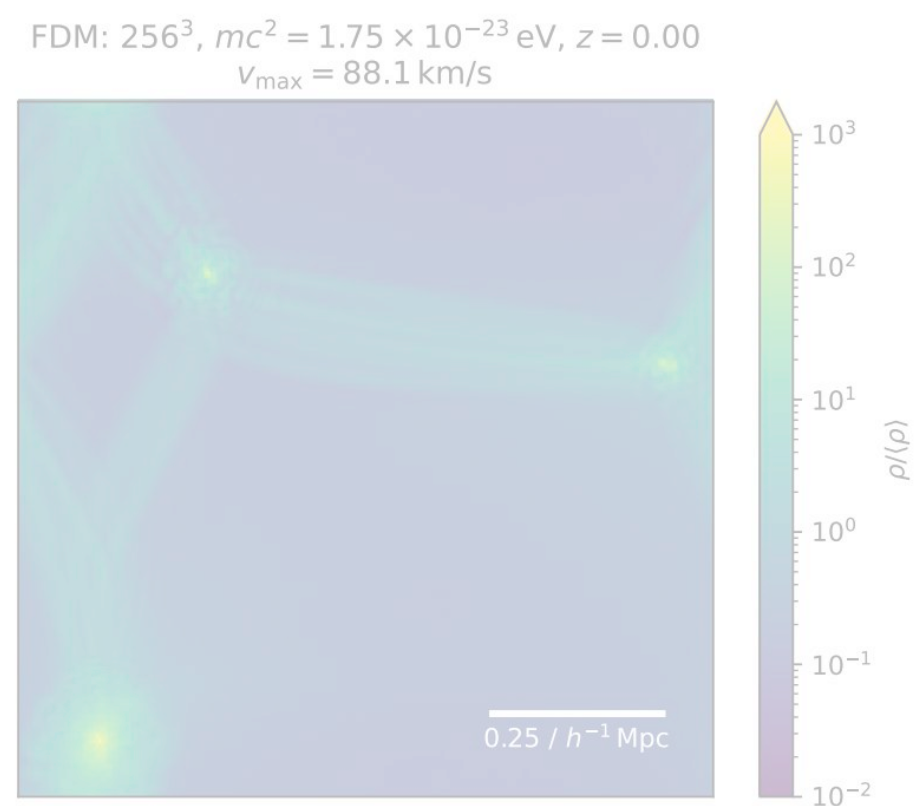


Phenomenology

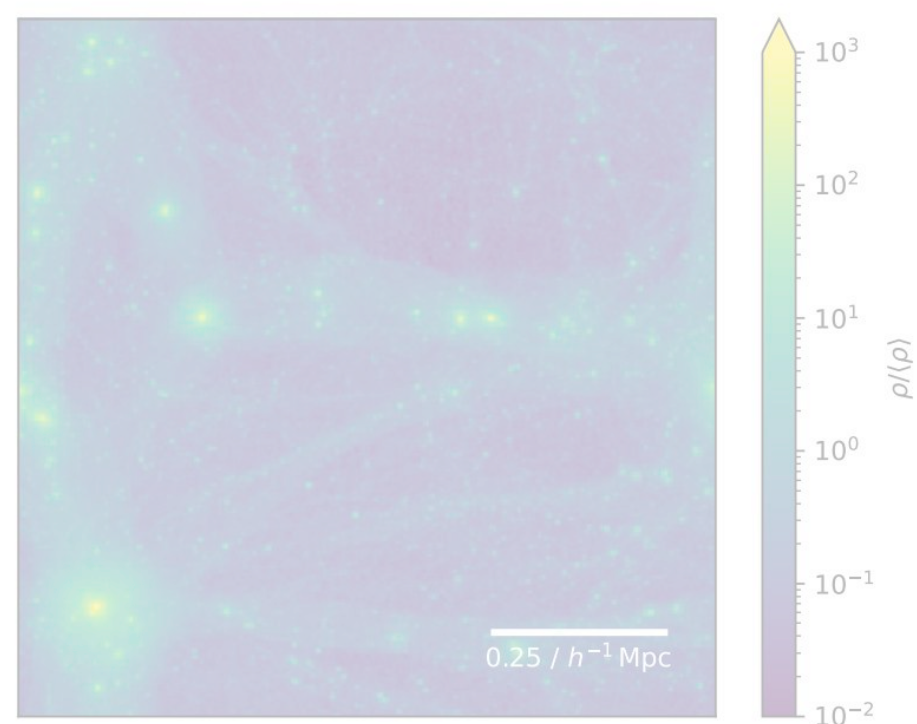


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Suppression of small structures

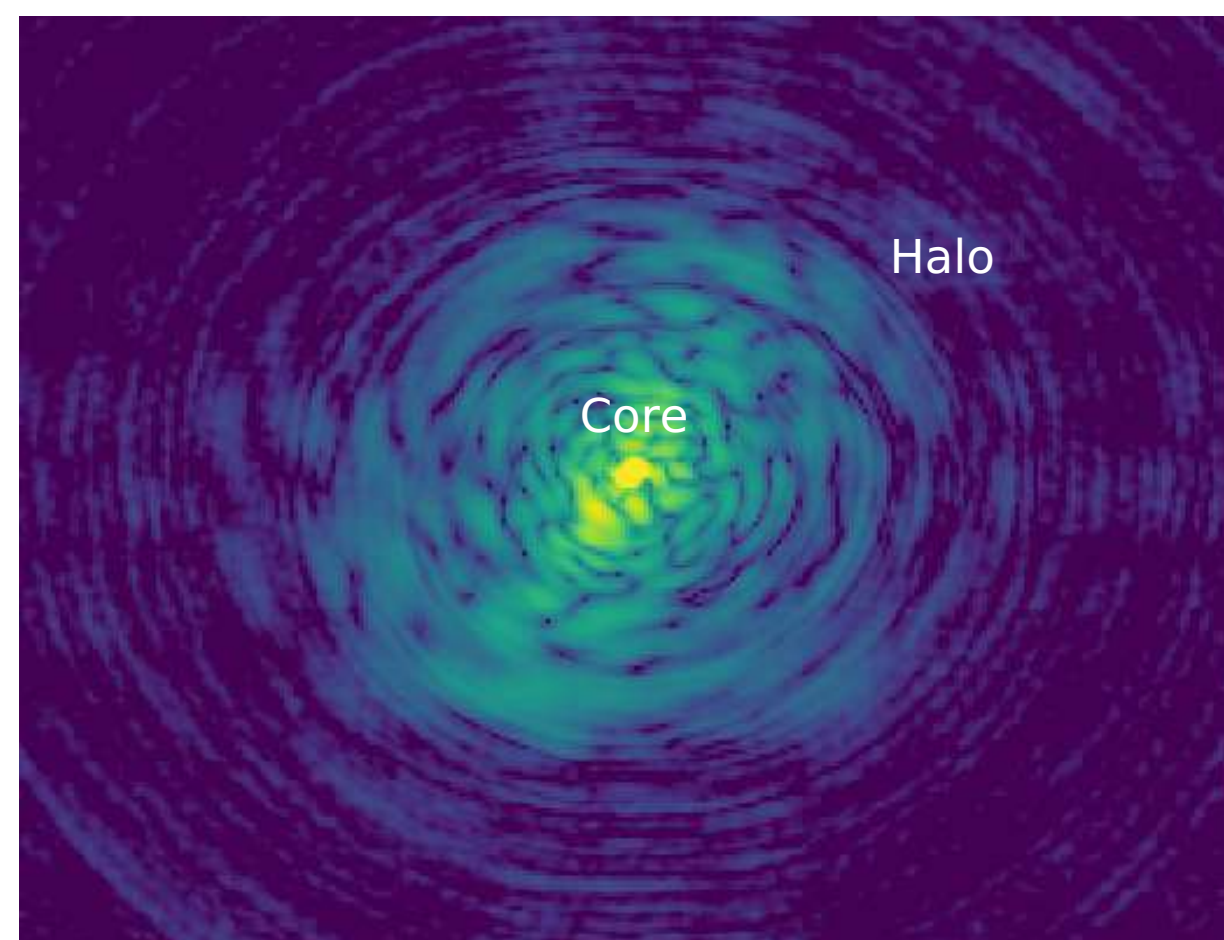


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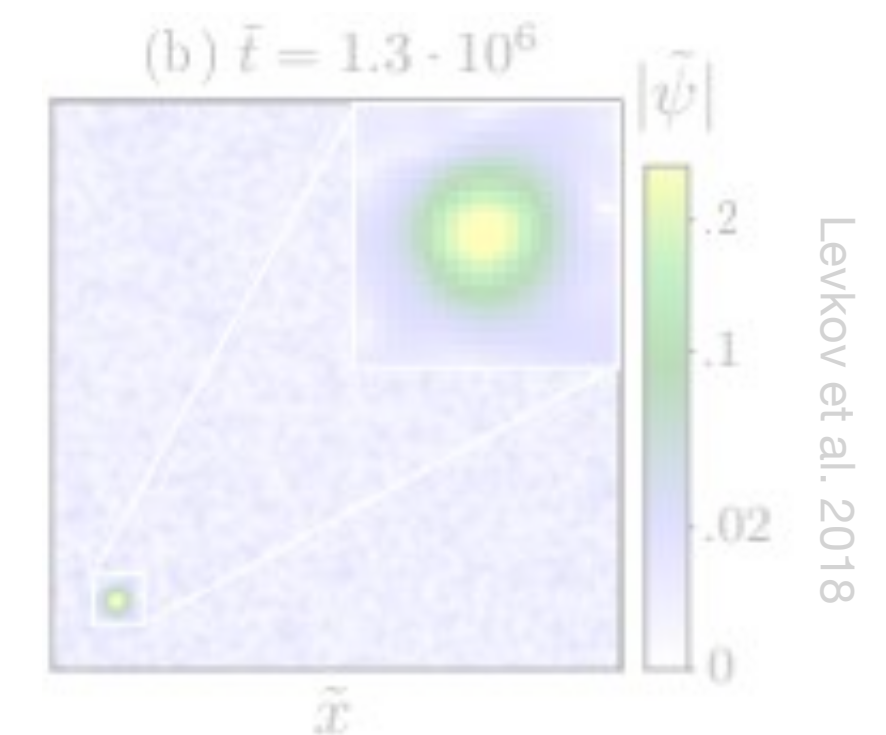


S. May et al. 2021

Formation of a solitonic core



Dynamical effects



Wave interference



Mocz et al. 2017

Phenomenology

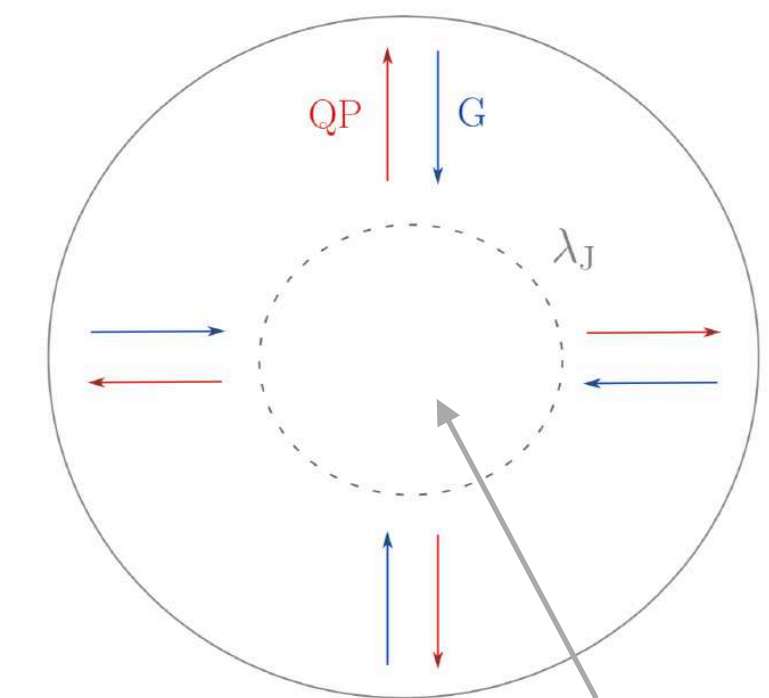
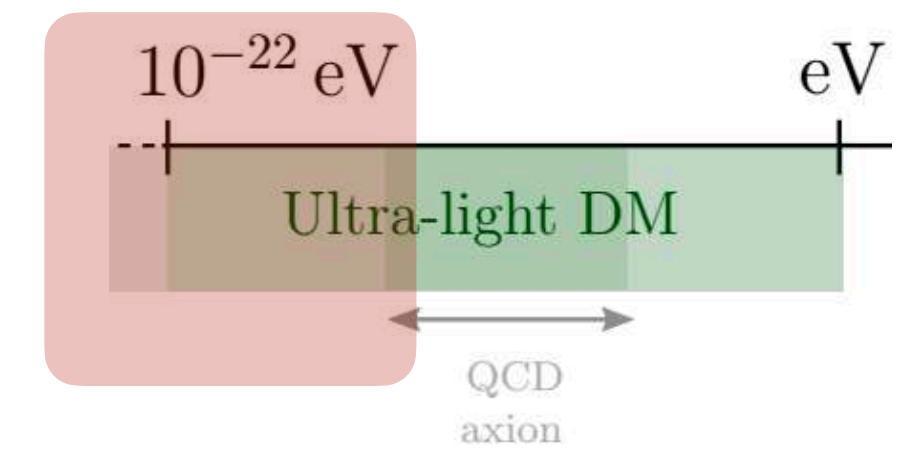
Formation of **cores**

NON-LINEAR
evolution: need
simulations

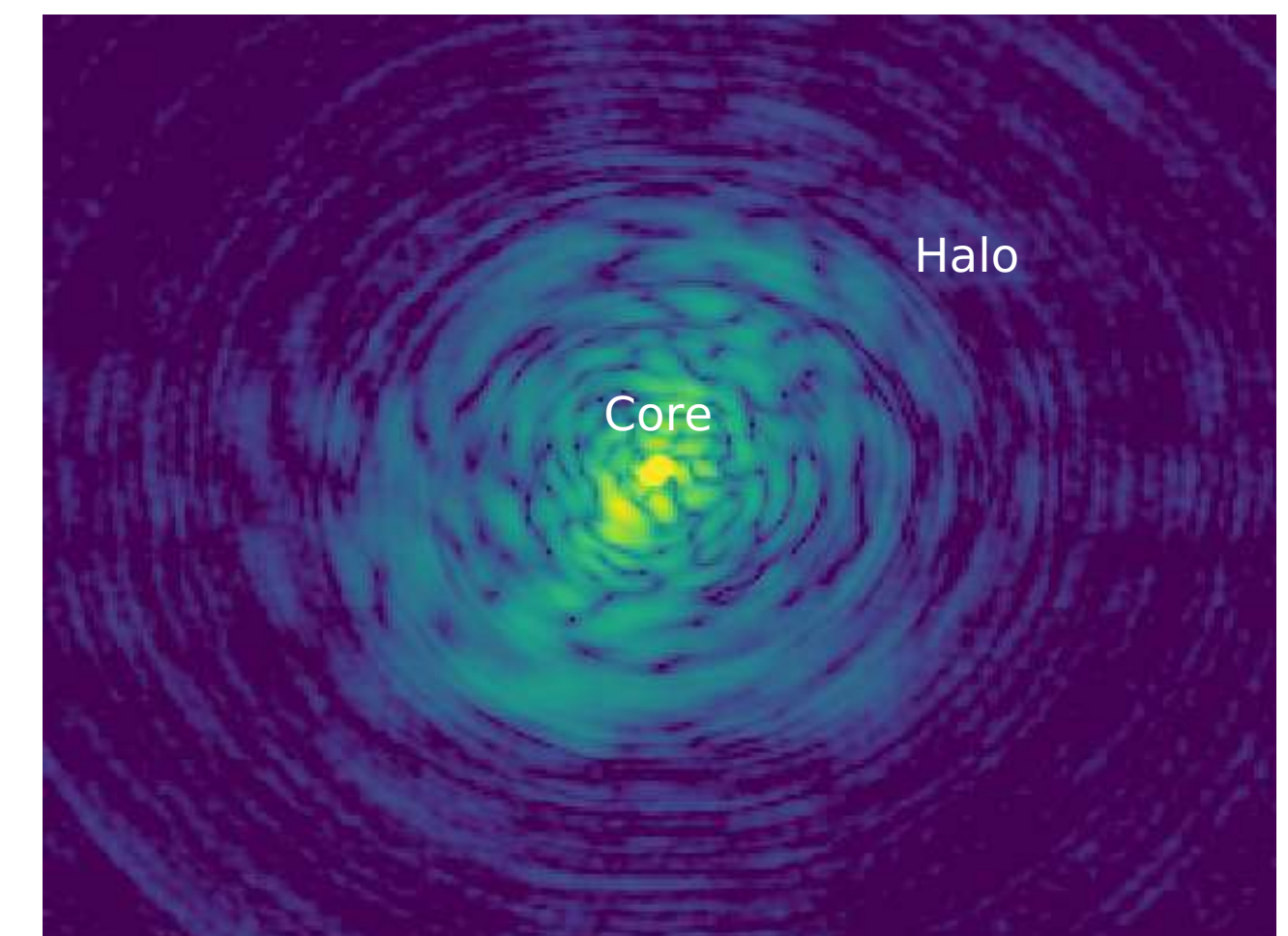
$m = 10^{-22}$ eV $N = 512^3$ $L = 300$ kpc



Simulation by Jowett Chan

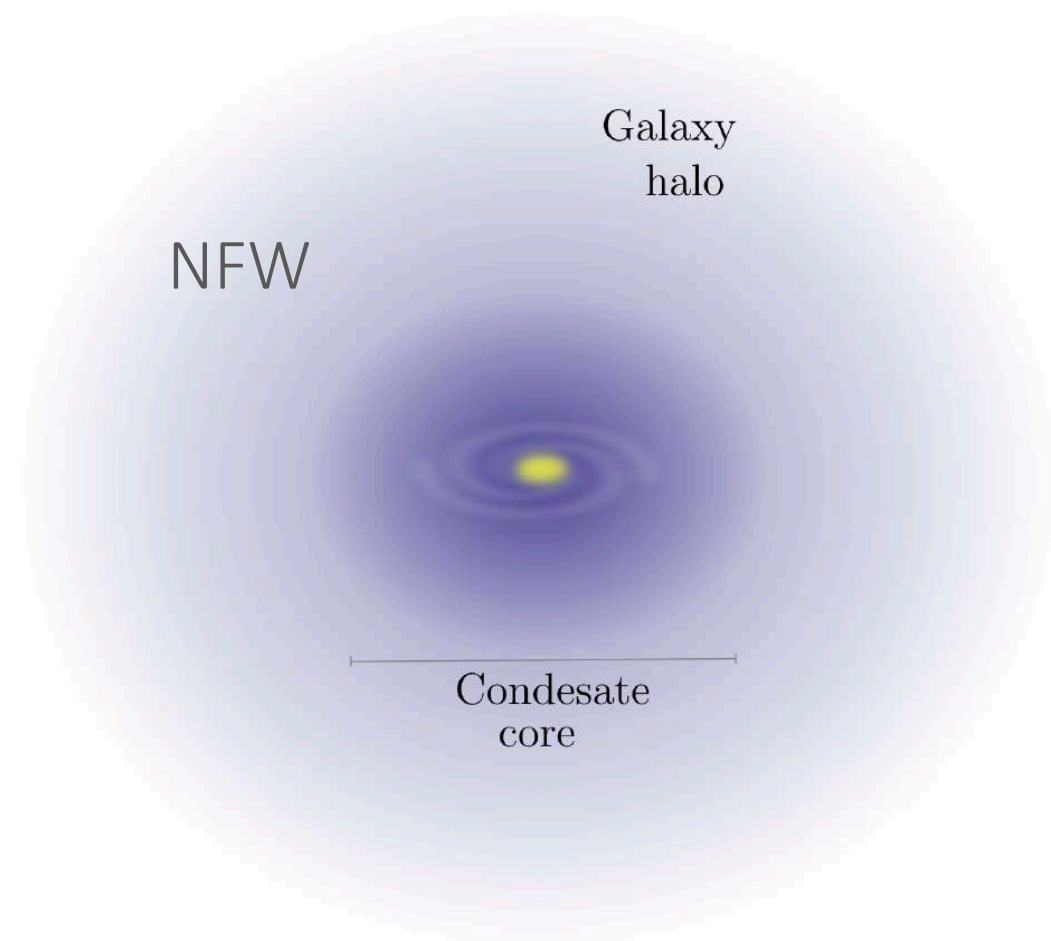


NO structure formation
Stable, oscillating solution

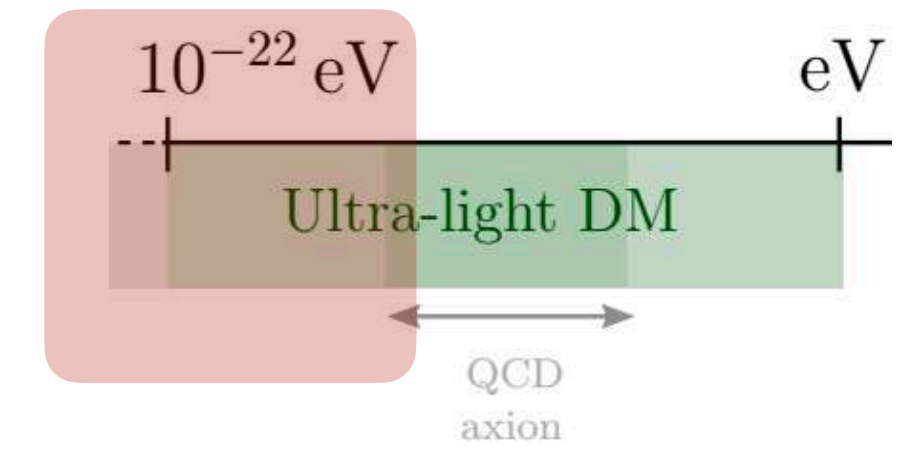


Phenomenology

Formation of **cores**



$$\rho(r) \simeq \begin{cases} \rho_c & \text{for } r \leq r_c \\ \rho_{\text{NFW}} & \text{for } r \geq r_c \end{cases}$$

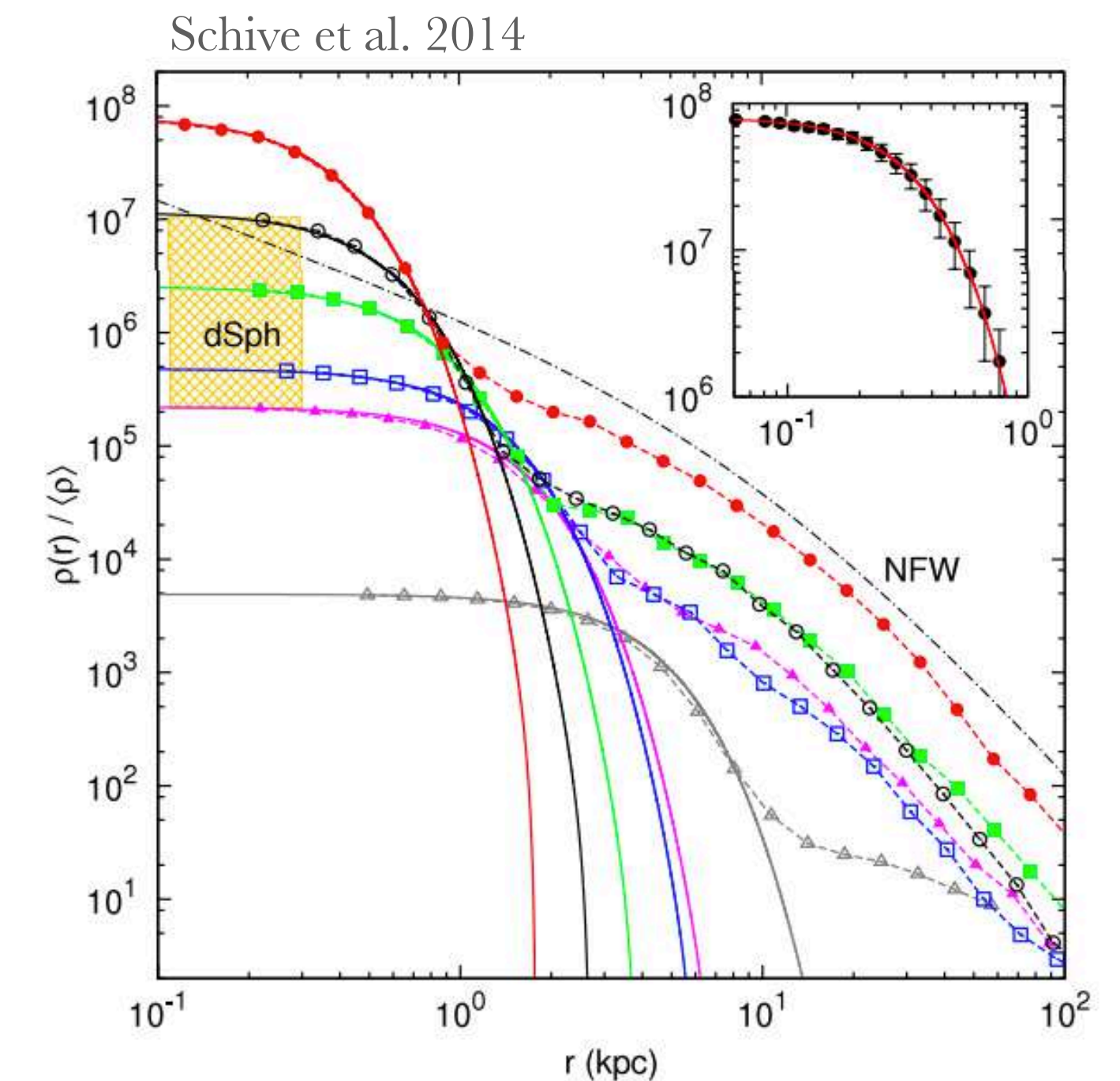


FDM

From simulations Schive et al. 2014, fitting function: Stable core solution

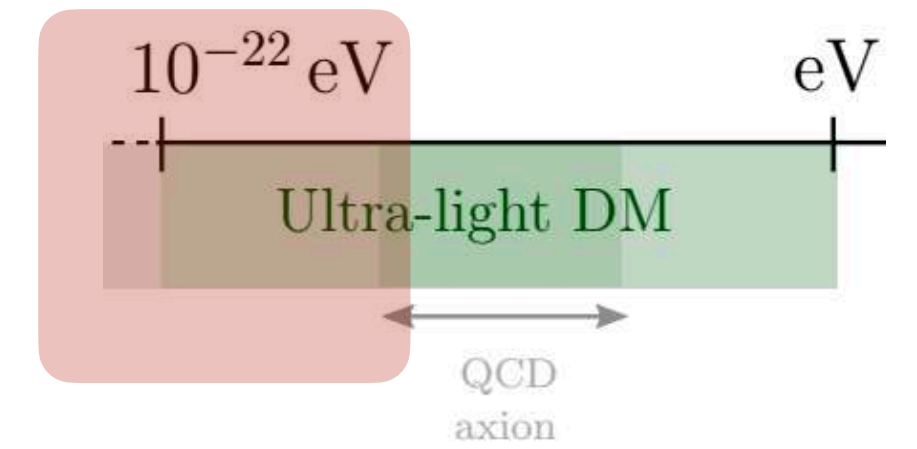
$$\rho_c \simeq \frac{1.9 \times 10^{-2}}{[1 + 0.091 (r/R_{1/2,c})^2]^8} \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-2} \left(\frac{r_c}{\text{kpc}} \right)^{-4} M_\odot \text{ pc}^{-3},$$

$$r_c \simeq 0.16 \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-1} \left(\frac{M}{10^{12} M_\odot} \right)^{-1/3} \text{ kpc}.$$



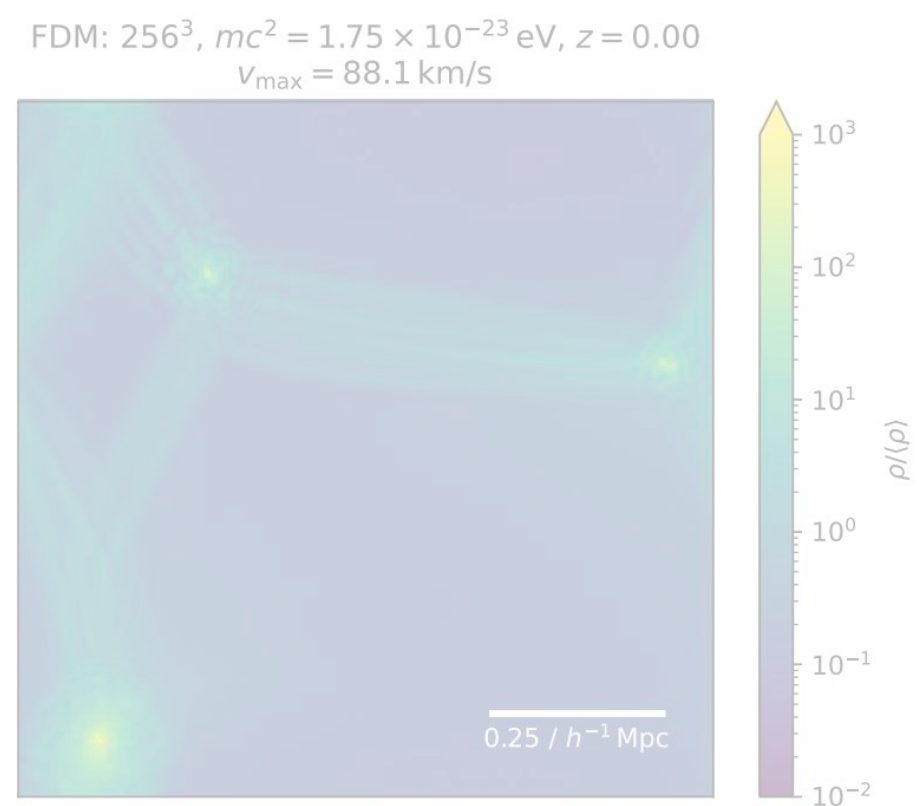
Relations used to compare with **observations**

Phenomenology

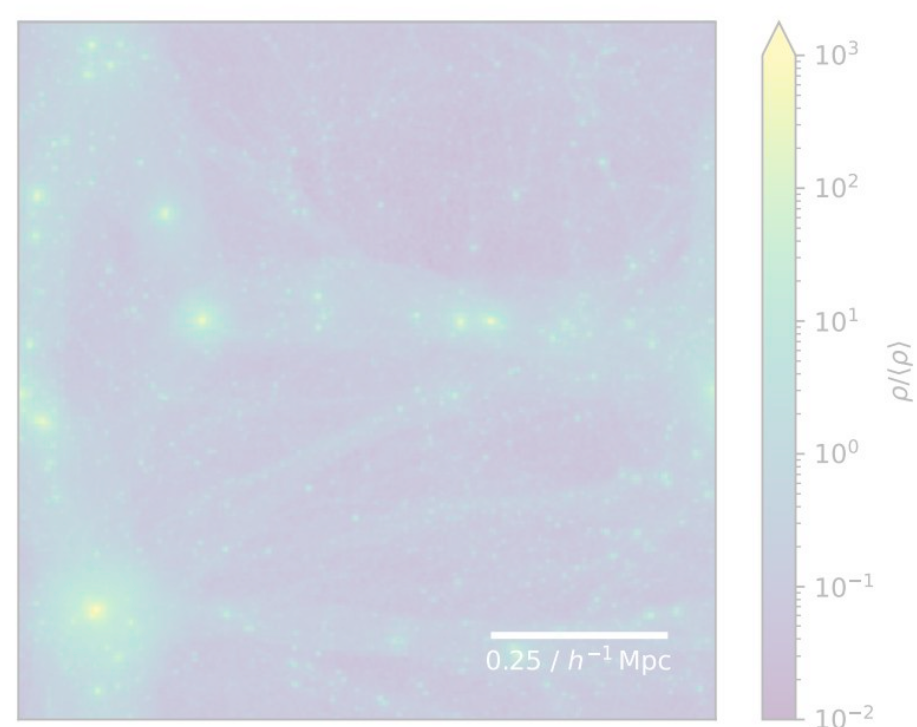


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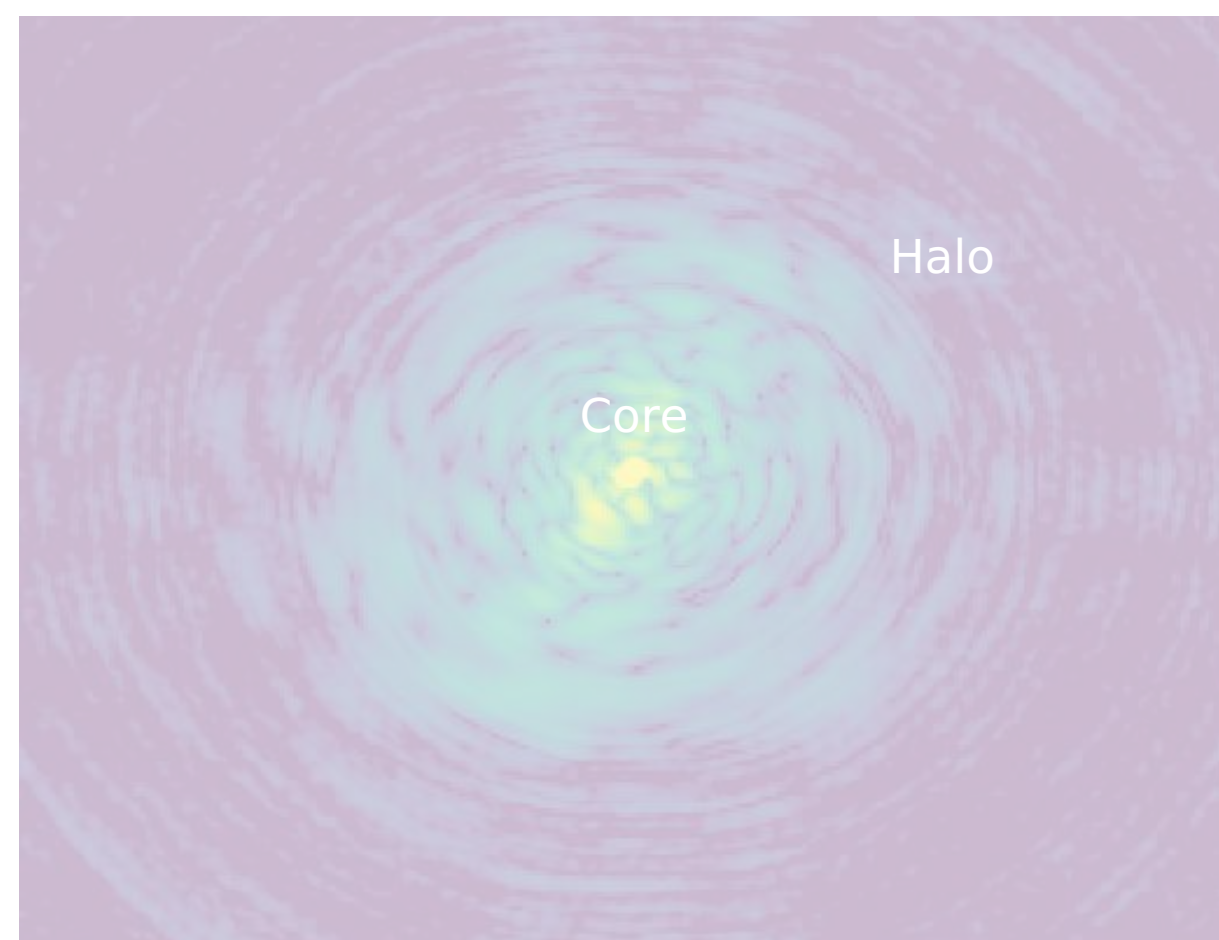


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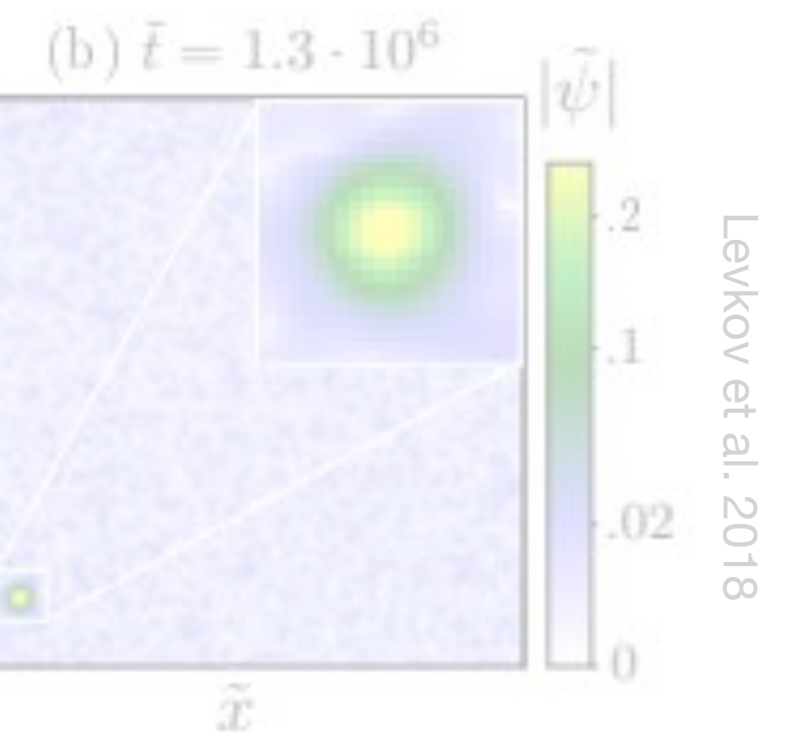


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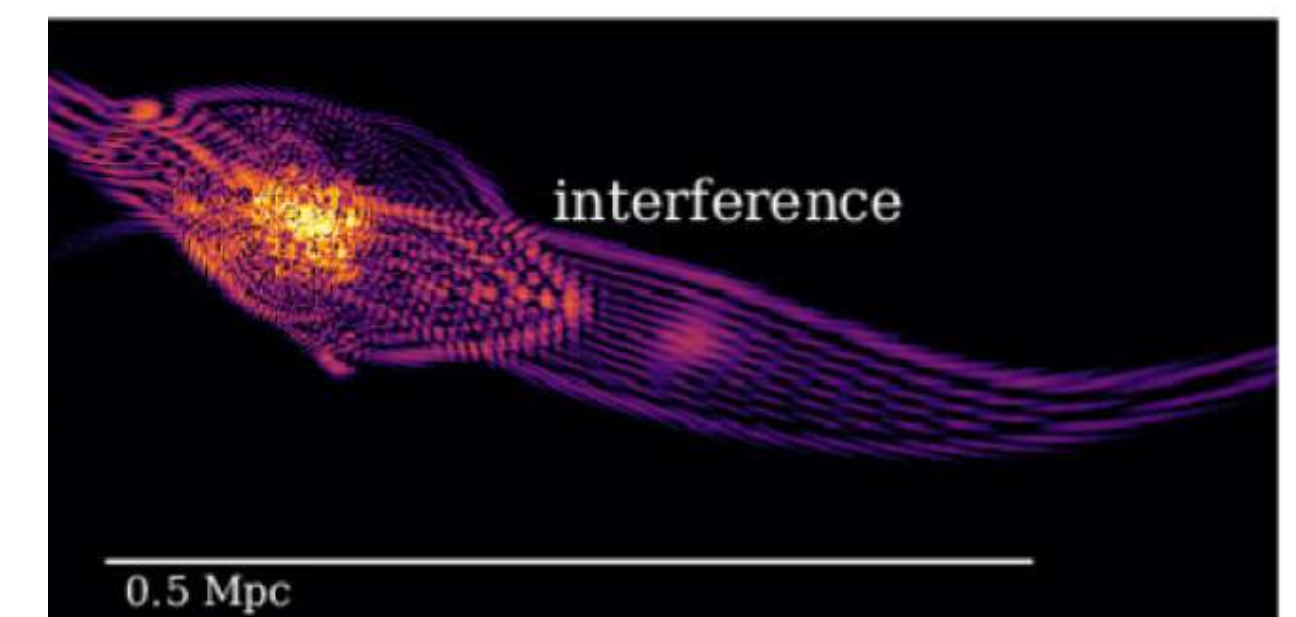
Formation of a solitonic core



Dynamical effects



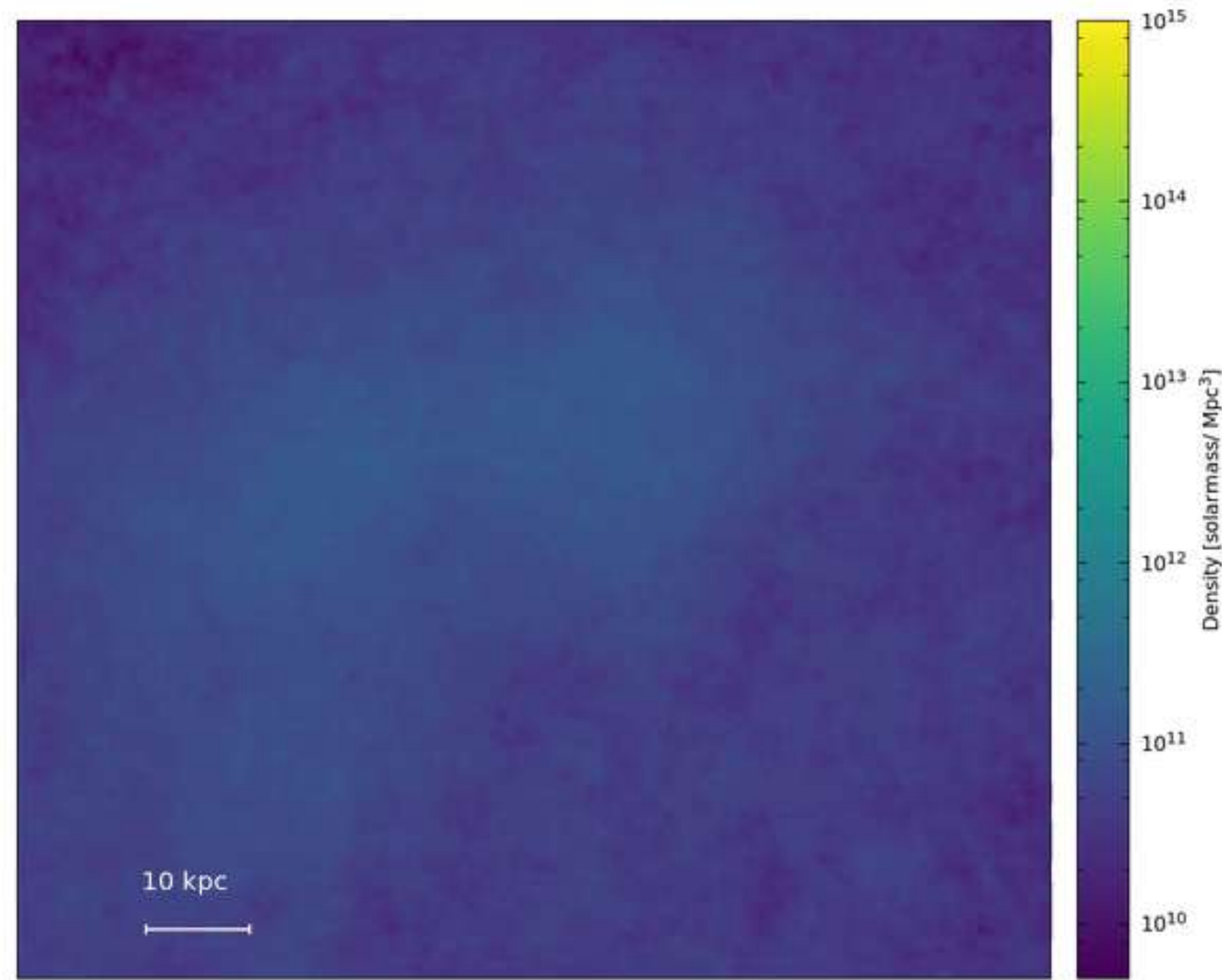
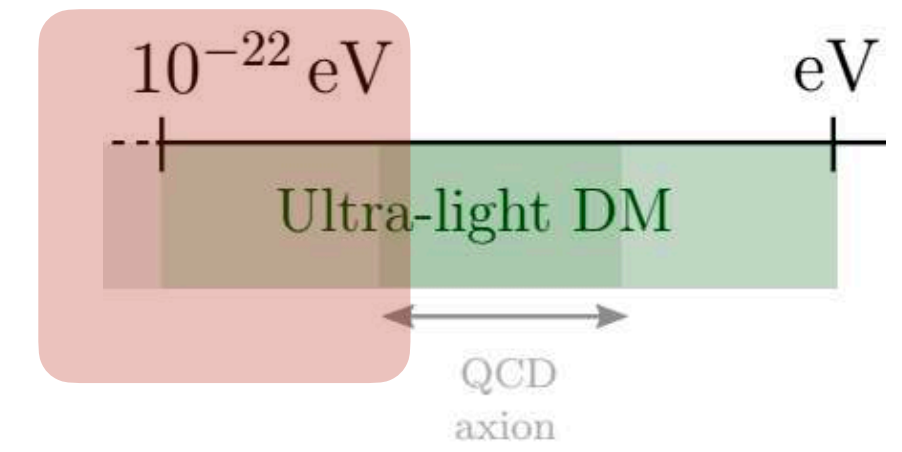
Wave interference



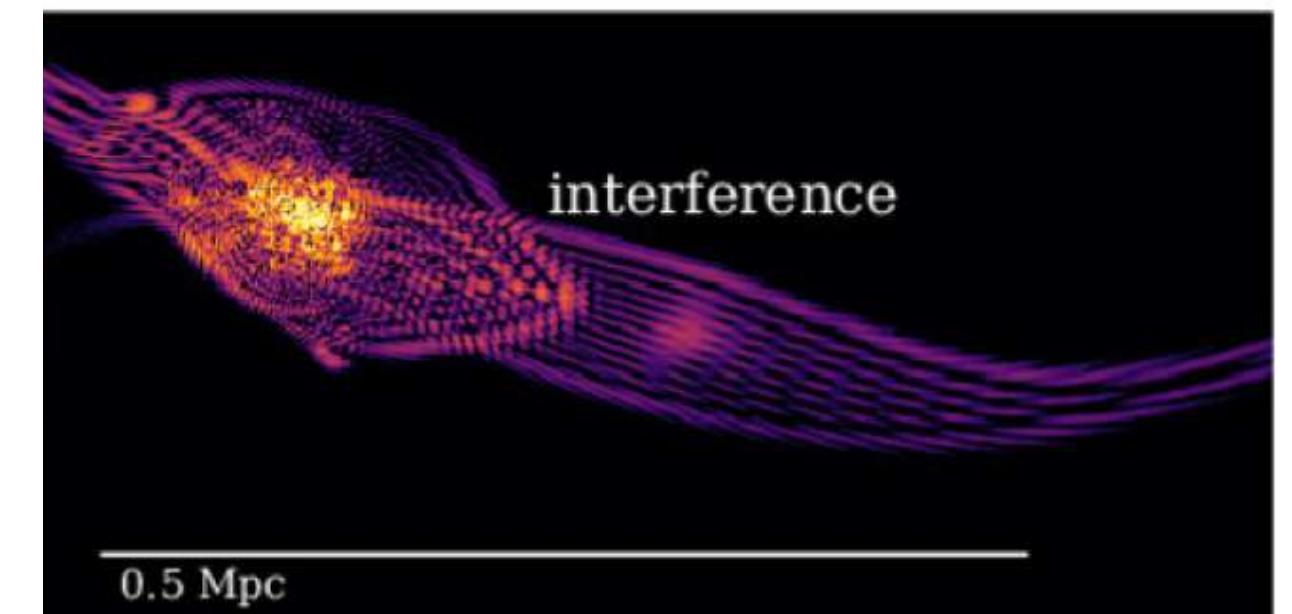
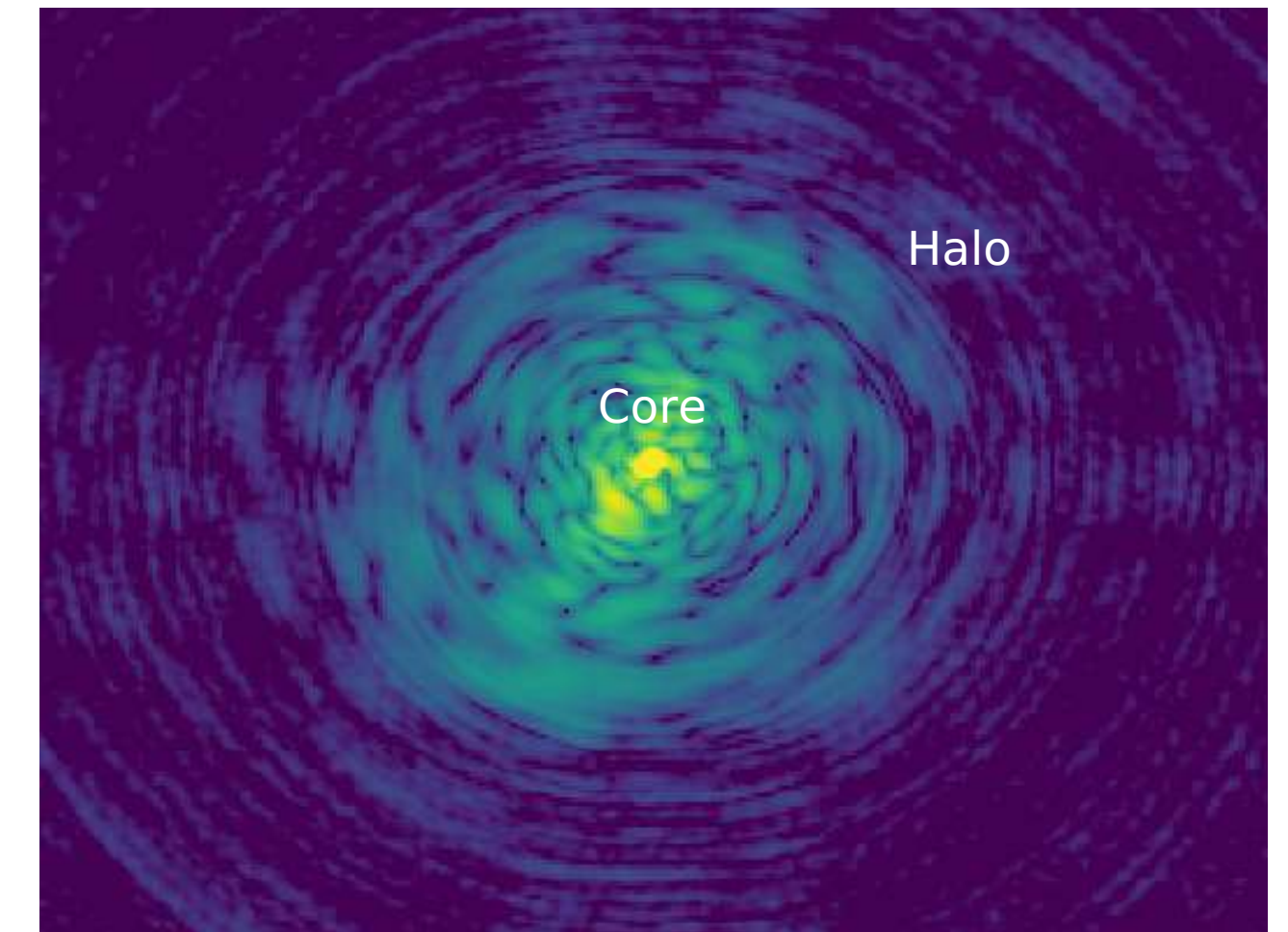
Mocz et al. 2017

Phenomenology

Wave interference: granules and vortices



Simulation by Jowett Chan



Mocz et al. 2017

Order one fluctuations in density \longrightarrow

Constructive interference: **granules**

Destructive interference

$\sim \lambda_{dB}$

Hard to observe!

Phenomenology

Vortices

Vortices are sites where the fluid velocity has a non-vanishing curl

Two ways:

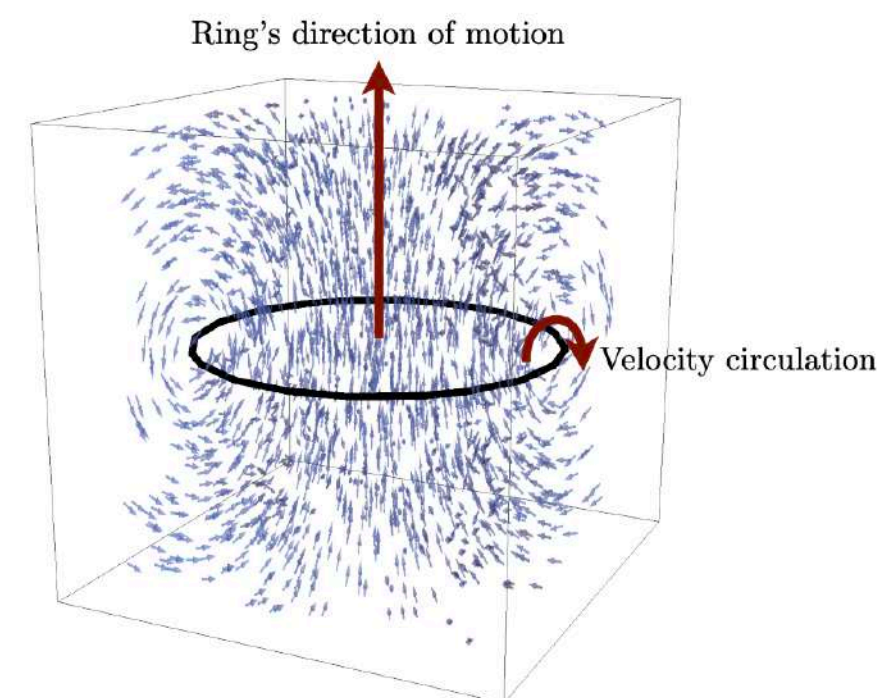
- regions where the density vanishes
- transfer of angular momentum (superfluids only)

Fuzzy DM

Interference of waves leads to **vortices** - where there is **destructive interference**

General defect in 3D

$$c = \frac{1}{m} \oint_{\partial A} d\theta = \frac{2\pi n}{m}$$



$$(\psi \equiv \sqrt{\rho/m} e^{i\theta} \text{ and } \mathbf{v} \equiv \nabla\theta/m)$$

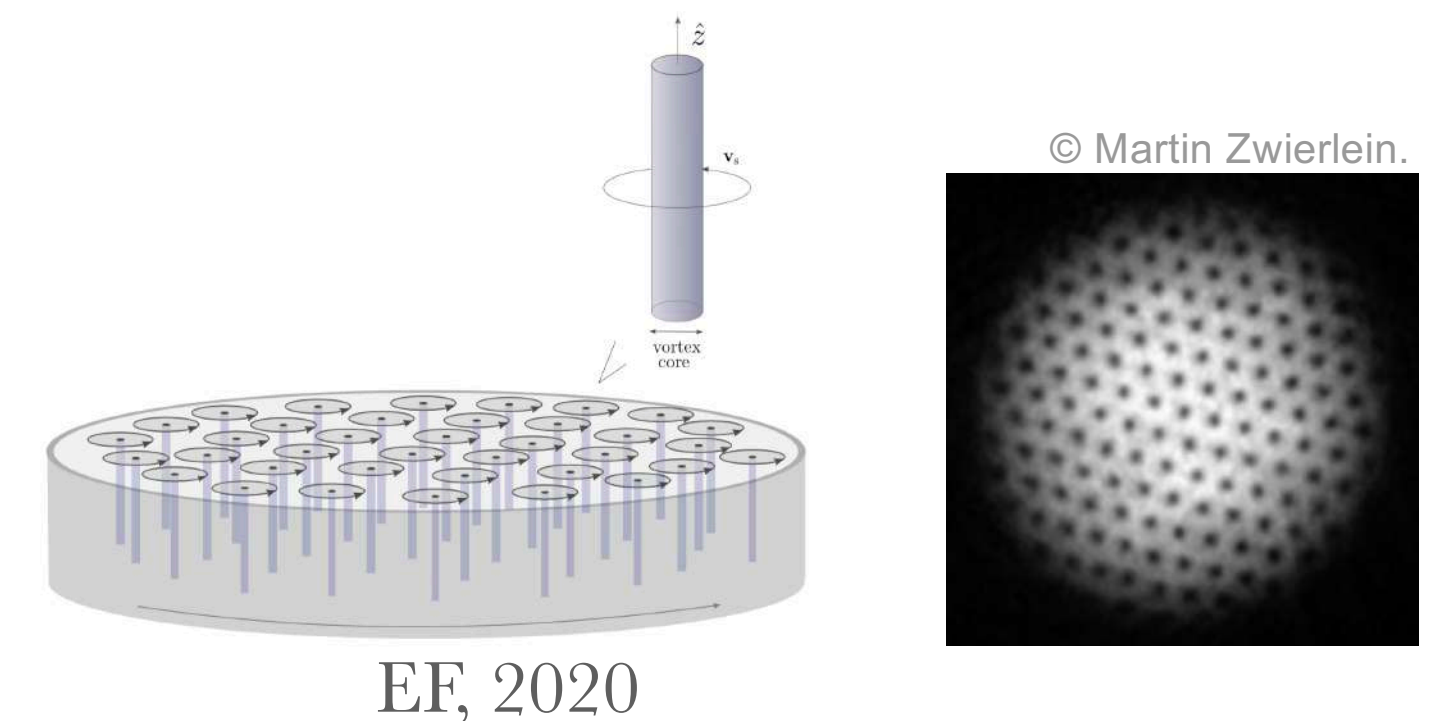
$$\dot{\rho} + \nabla \cdot (\rho \mathbf{v}) = 0$$

$$\dot{\mathbf{v}} + (\mathbf{v} \cdot \nabla)\mathbf{v} = -\frac{1}{m} \left(V_{grav} - P_{int} - \frac{1}{2m} \frac{\nabla^2 \sqrt{\rho}}{\sqrt{\rho}} \right)$$

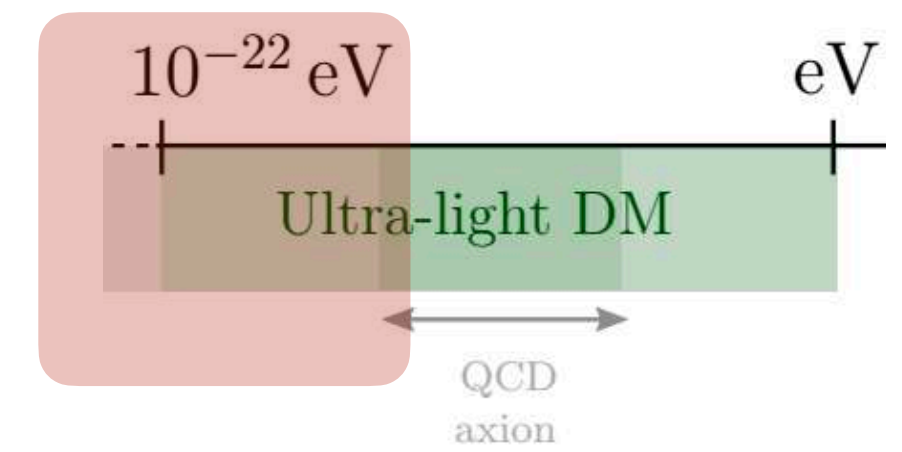
Vel. field is a gradient flow \longrightarrow irrotational fluid, no vorticity

Self-interacting Fuzzy DM

Superfluid cannot rotate uniformly. If the superfluid rotates faster than the critical vel., network of vortices are formed.

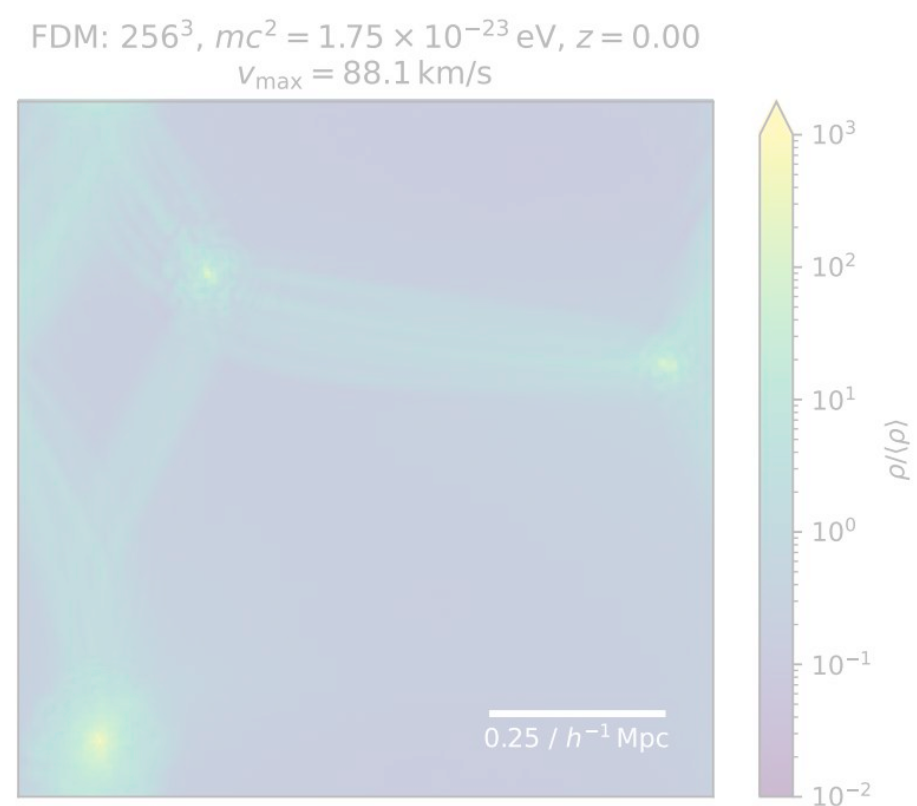


Phenomenology

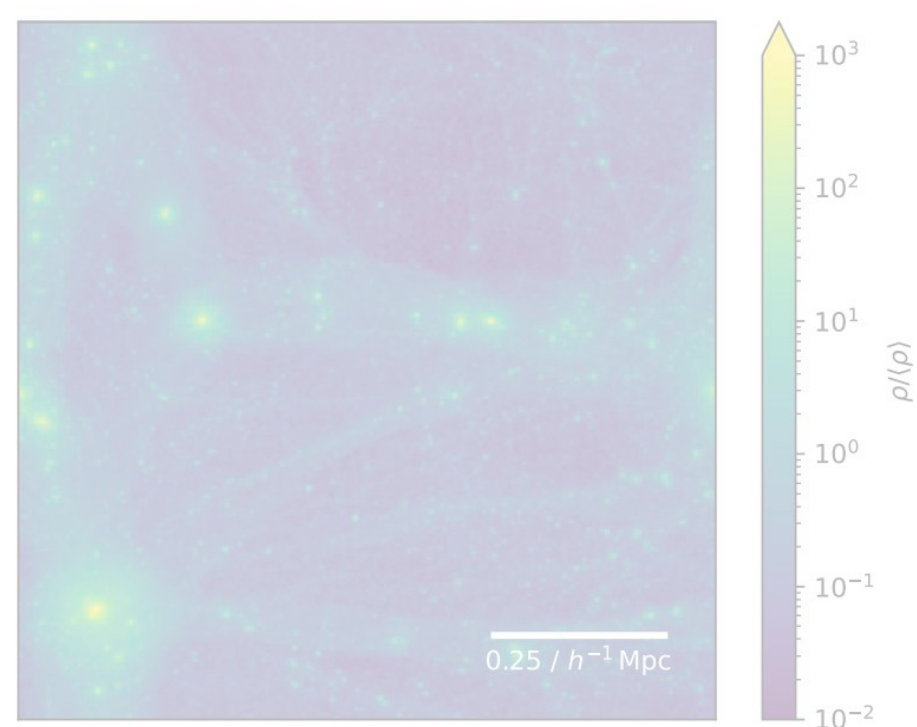


RICH PHENOMENOLOGY ON SMALL SCALES

Suppression of small structures

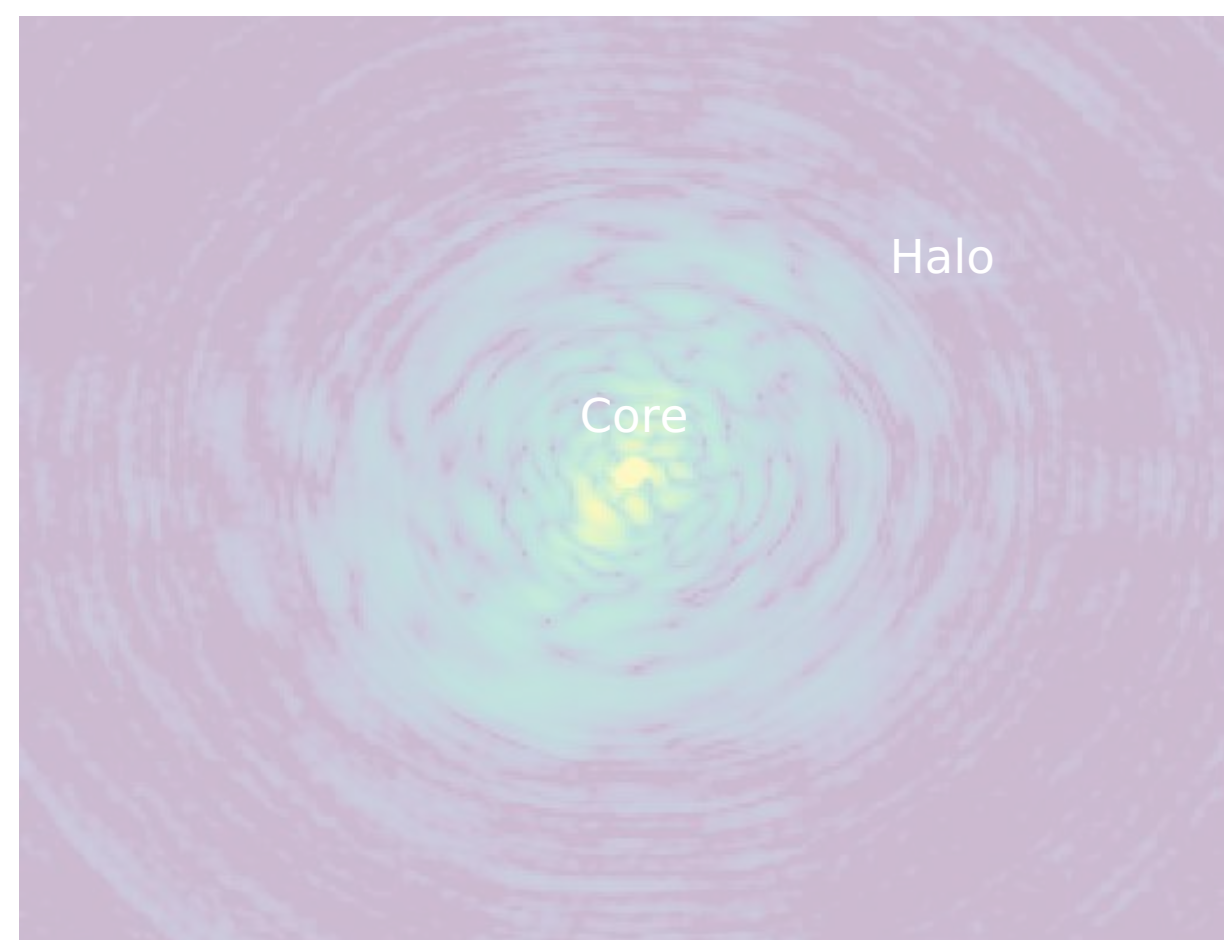


CDM: 256^3 , $z = 0.00$

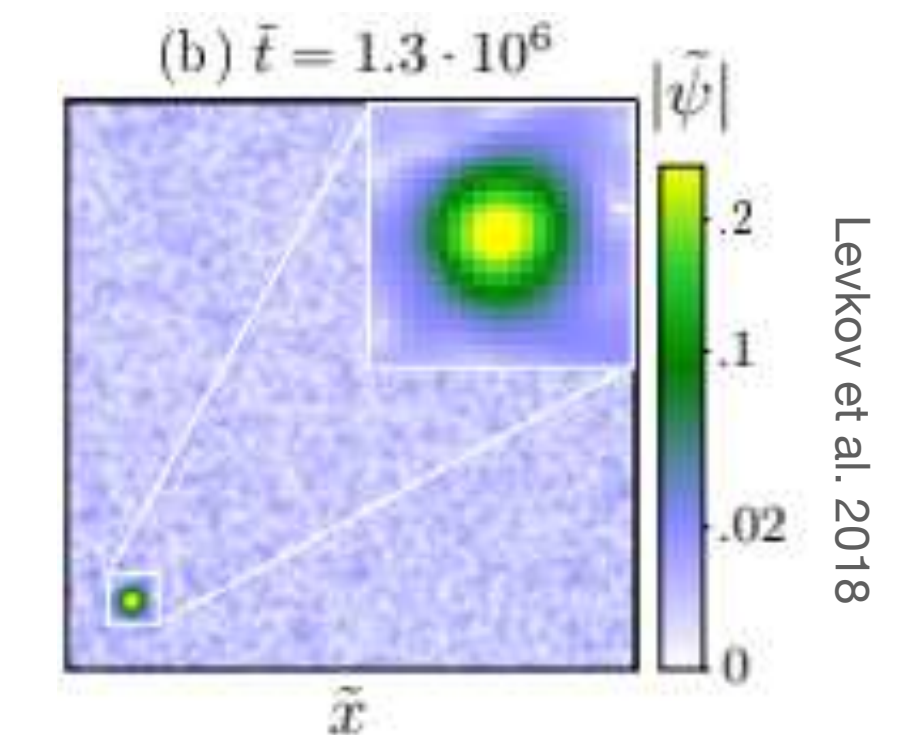


S. May et al. 2021

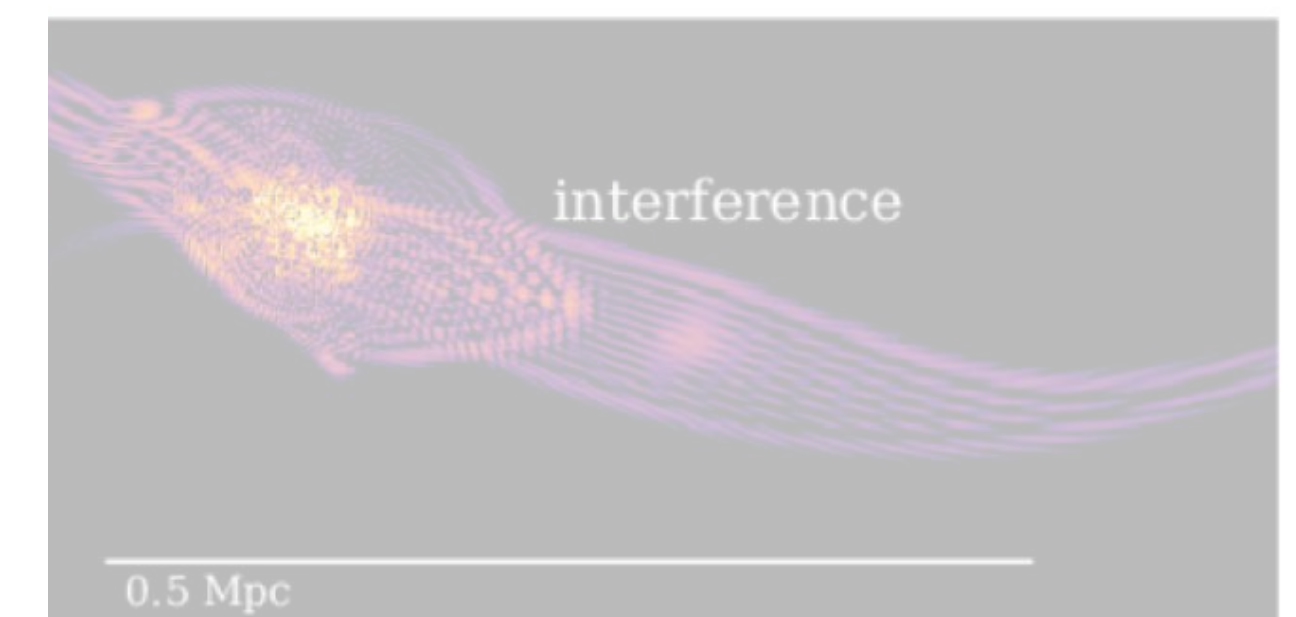
Formation of a solitonic core



Dynamical effects



Wave interference

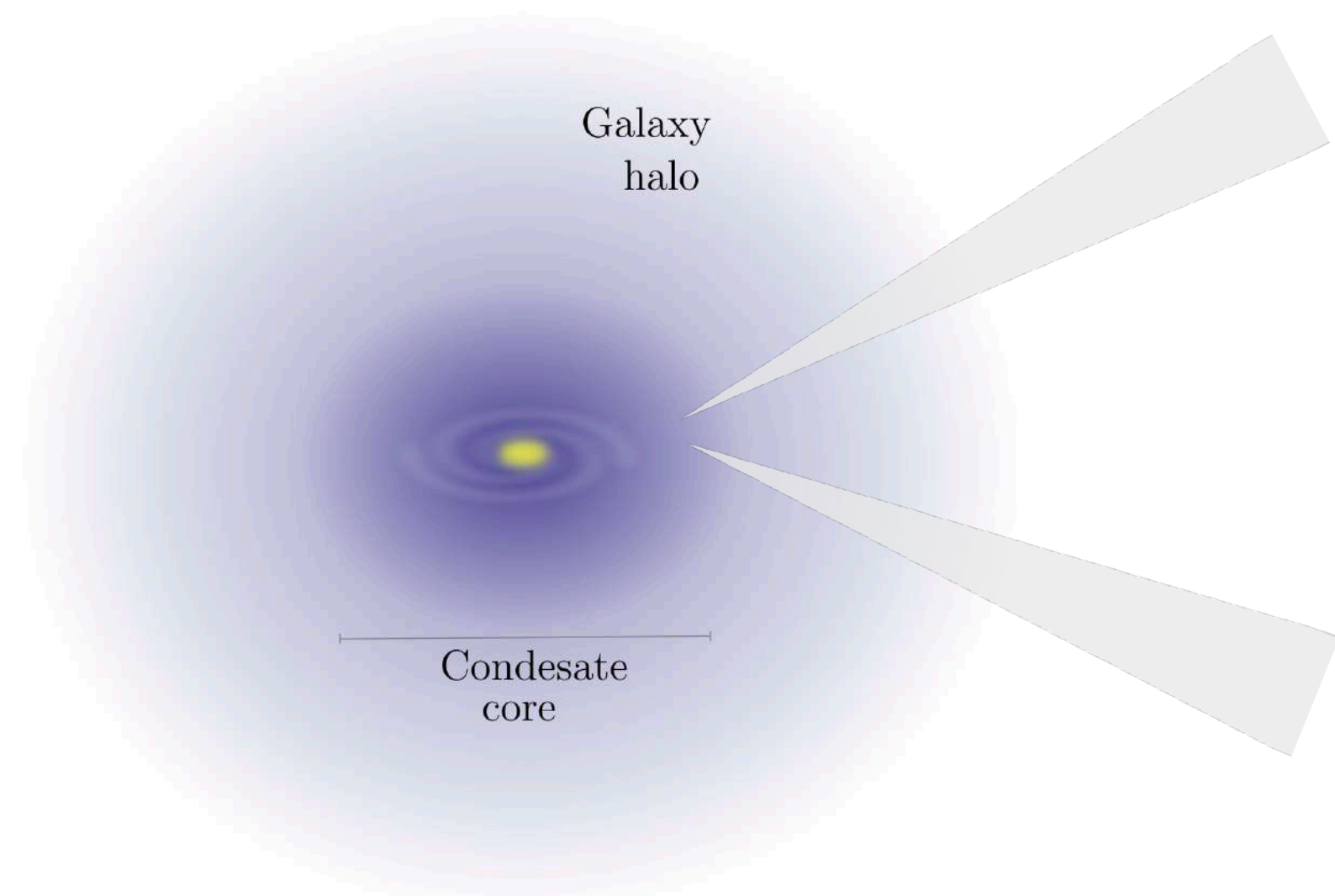
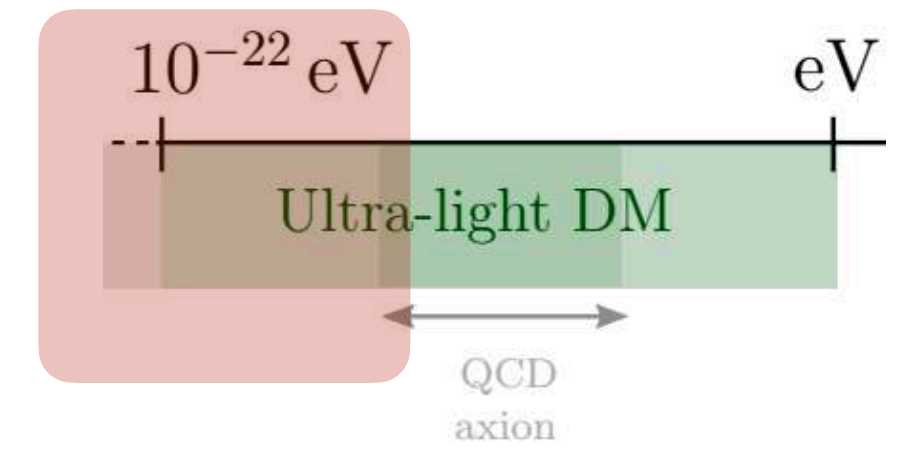


Mocz et al. 2017

Phenomenology

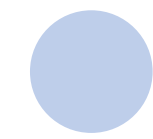
Dynamical effects

Relaxation, oscillation, friction, and heating



Heating

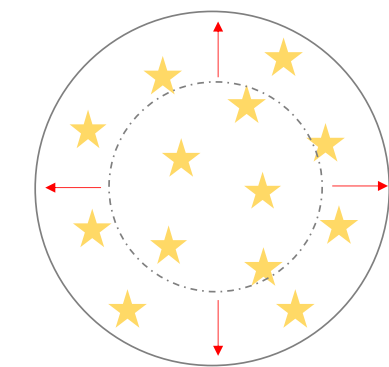
FDM granule



m_{eff}

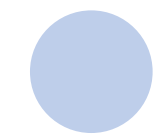


System (star)
gains energy



Friction

FDM granule



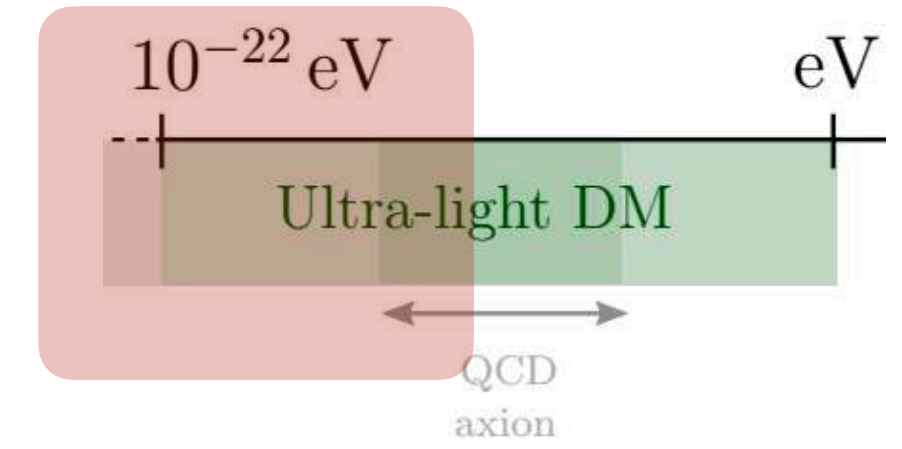
m_{eff}



Globular cluster

System (GC or BH)
loses energy

Observational implications and constraints

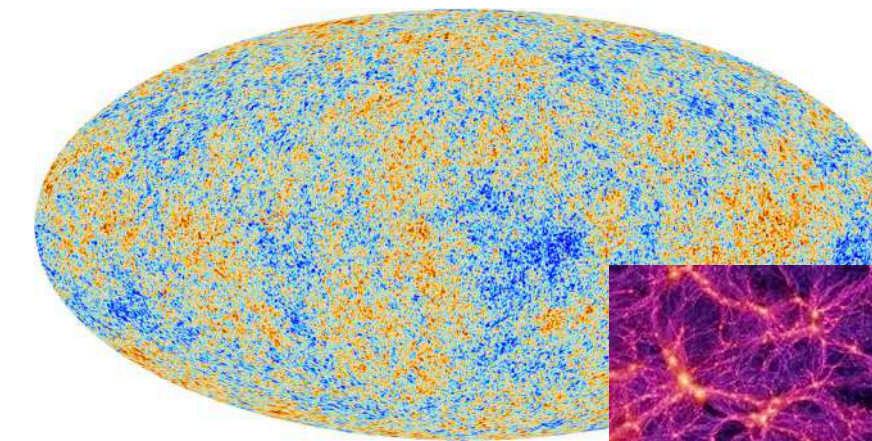


Galaxies

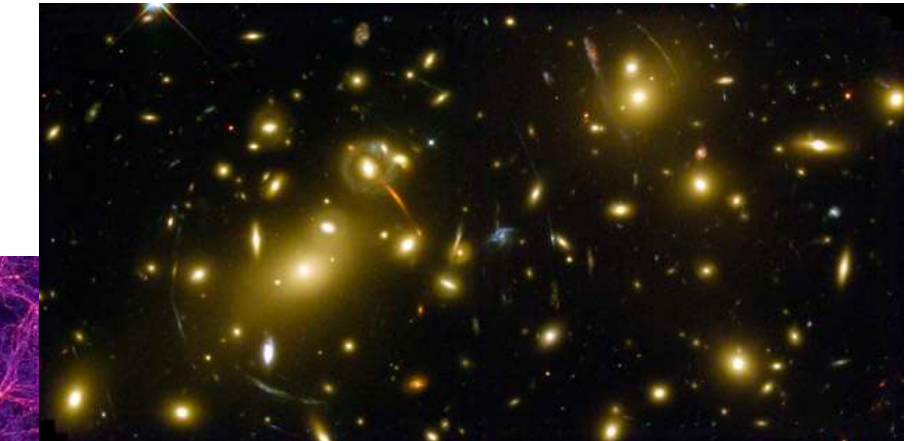


NASA and ESA

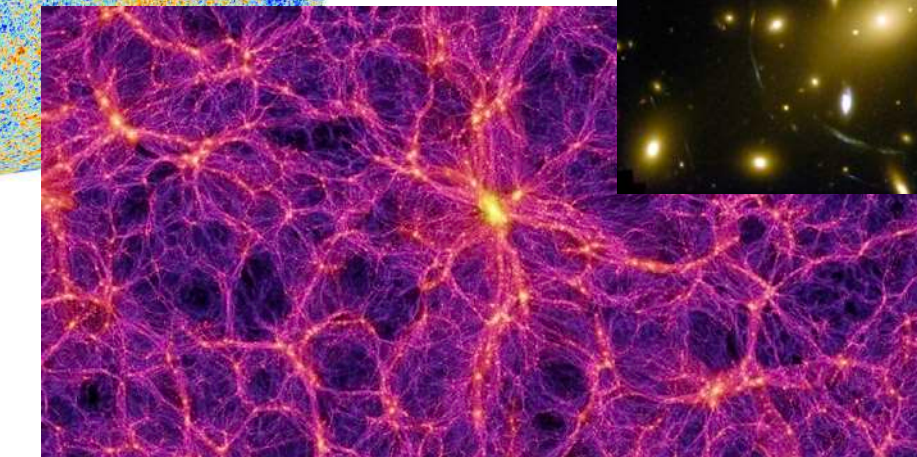
CMB+LSS



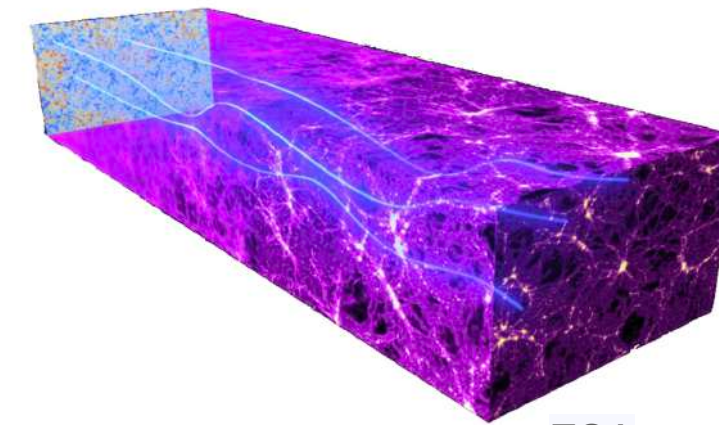
ESA and the Planck Collaboration



NASA and ESA

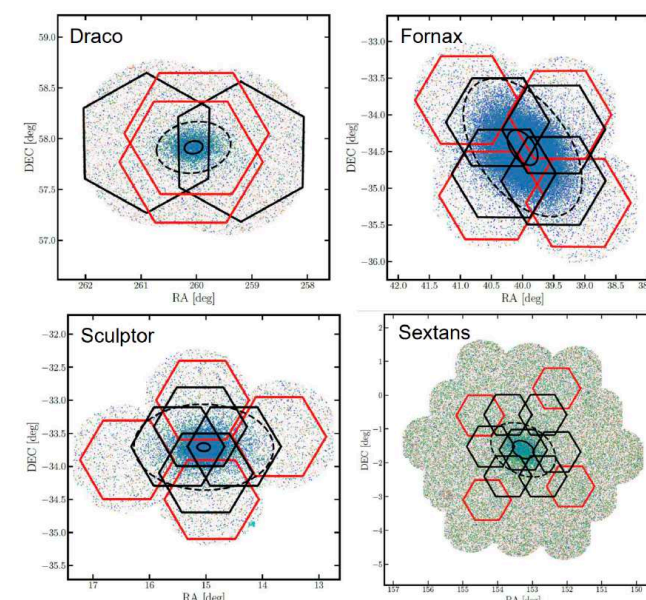


Springel & others / Virgo Consortium

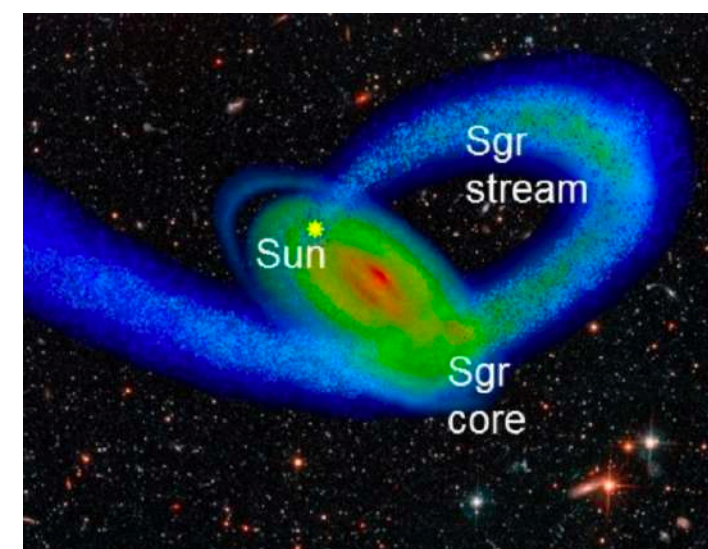


ESA

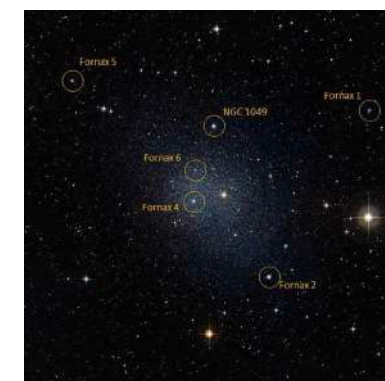
Dwarfs



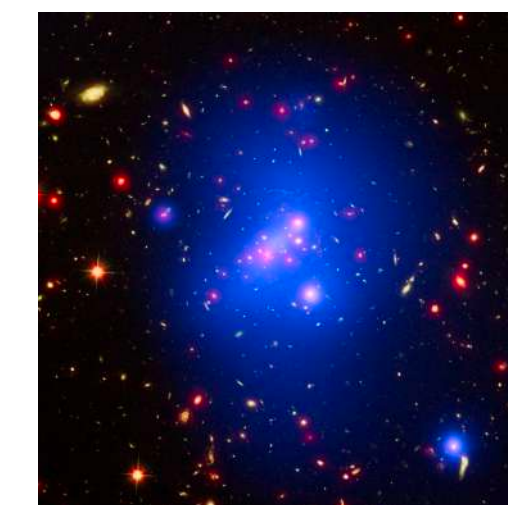
Stellar stream



Globular clusters

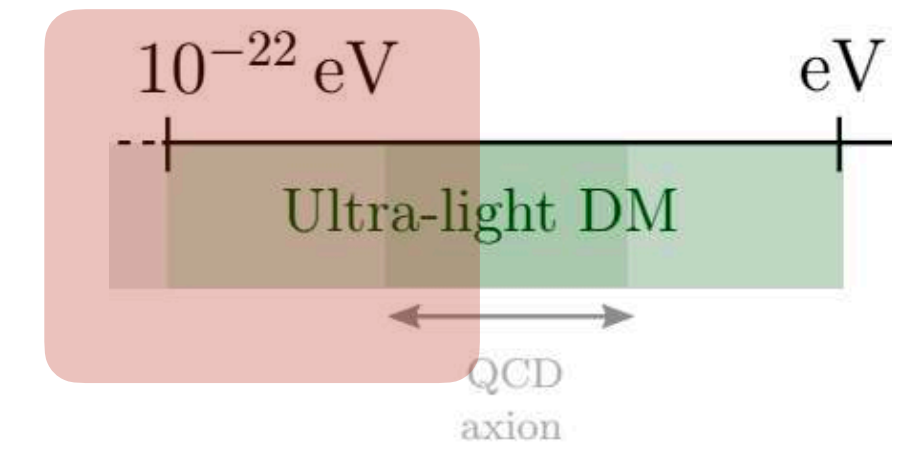


Clusters

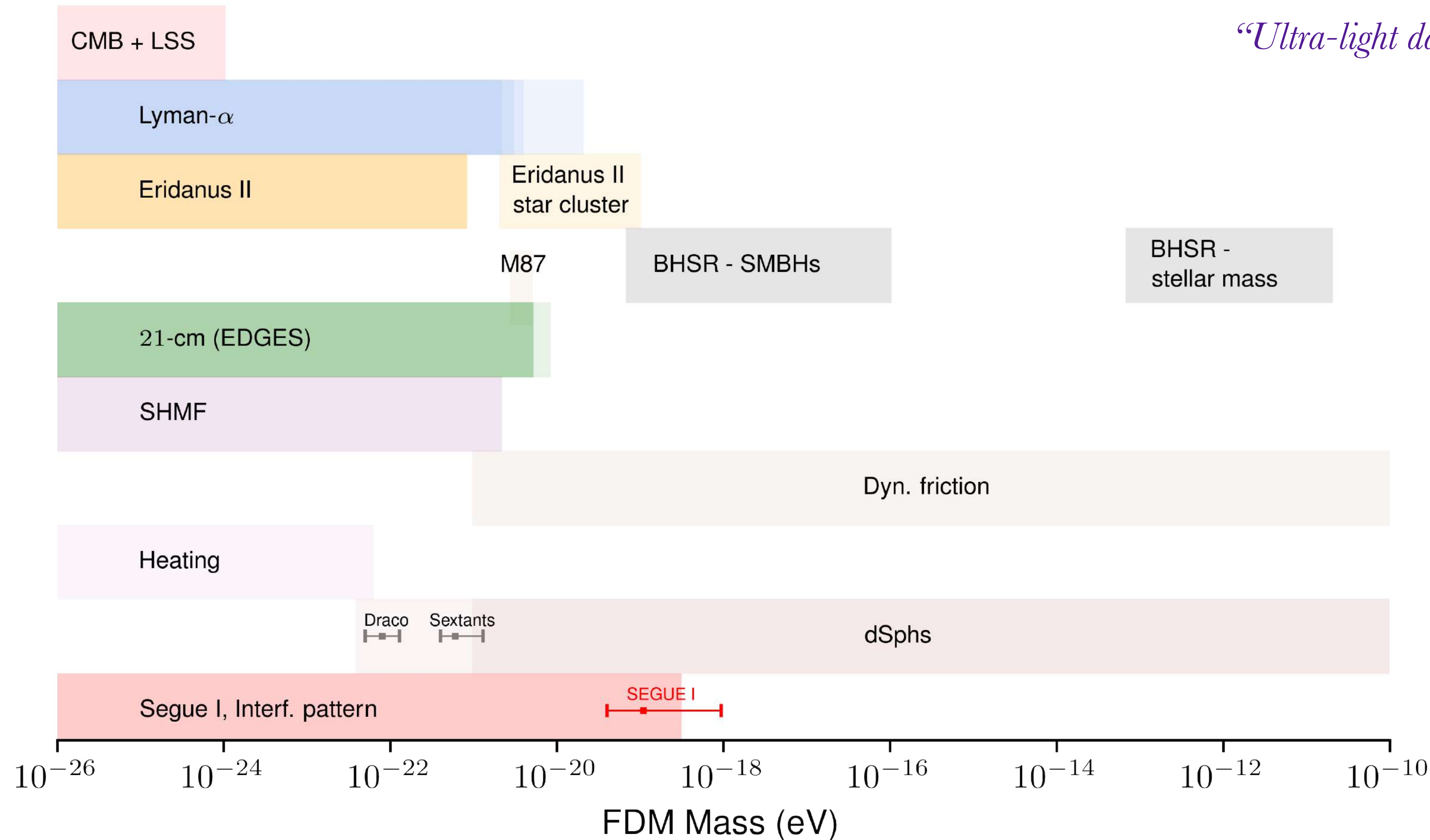


Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass



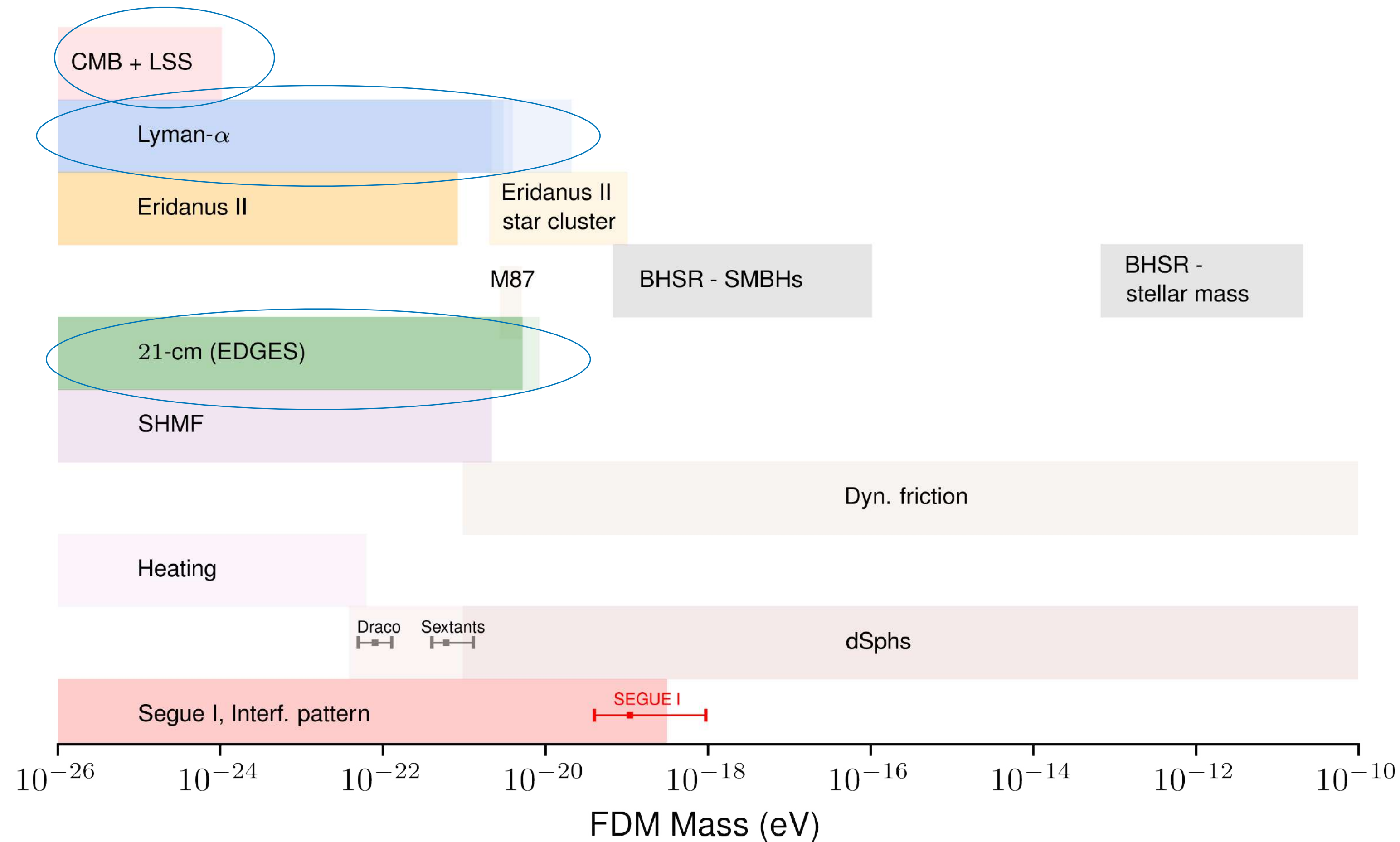
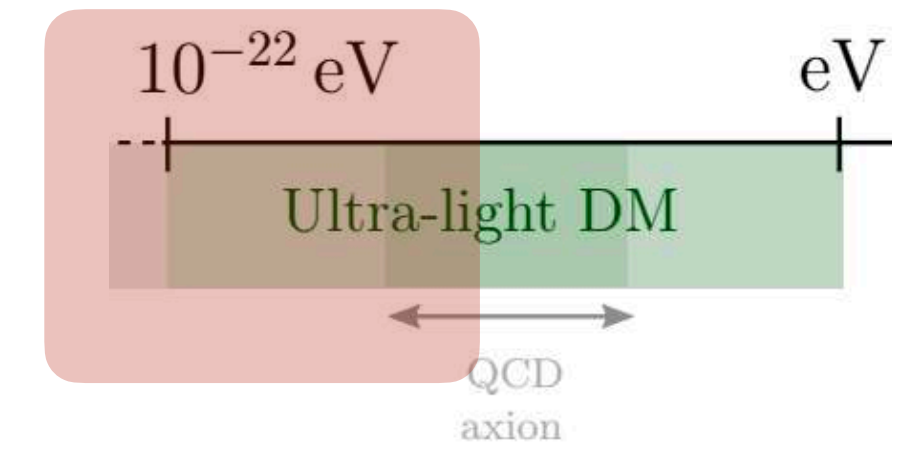
“Ultra-light dark matter”, **E.F.**, 2020. *The Astronomy and Astrophysics Review.*



Bounds consider FDM is *all* DM

Observational implications and constraints

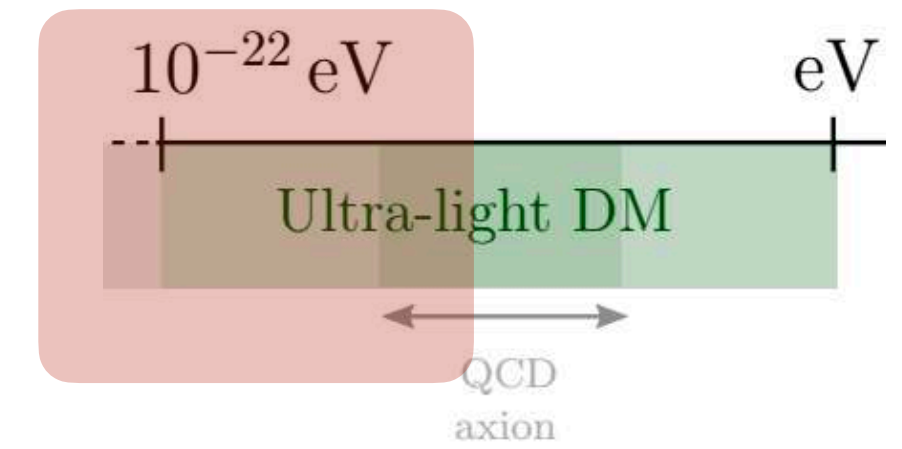
Fuzzy Dark Matter - bounds on the mass



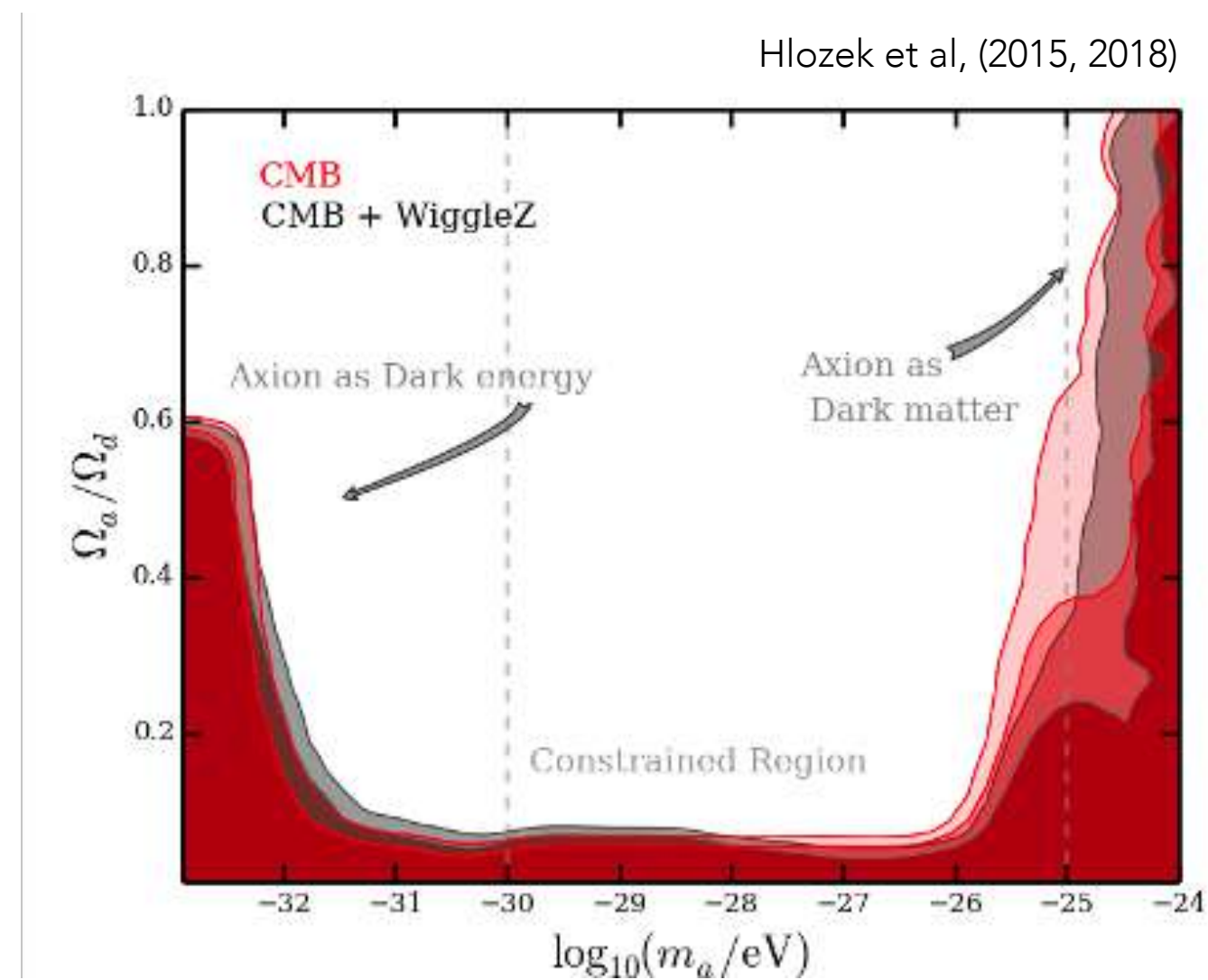
Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass

Suppression of small structures



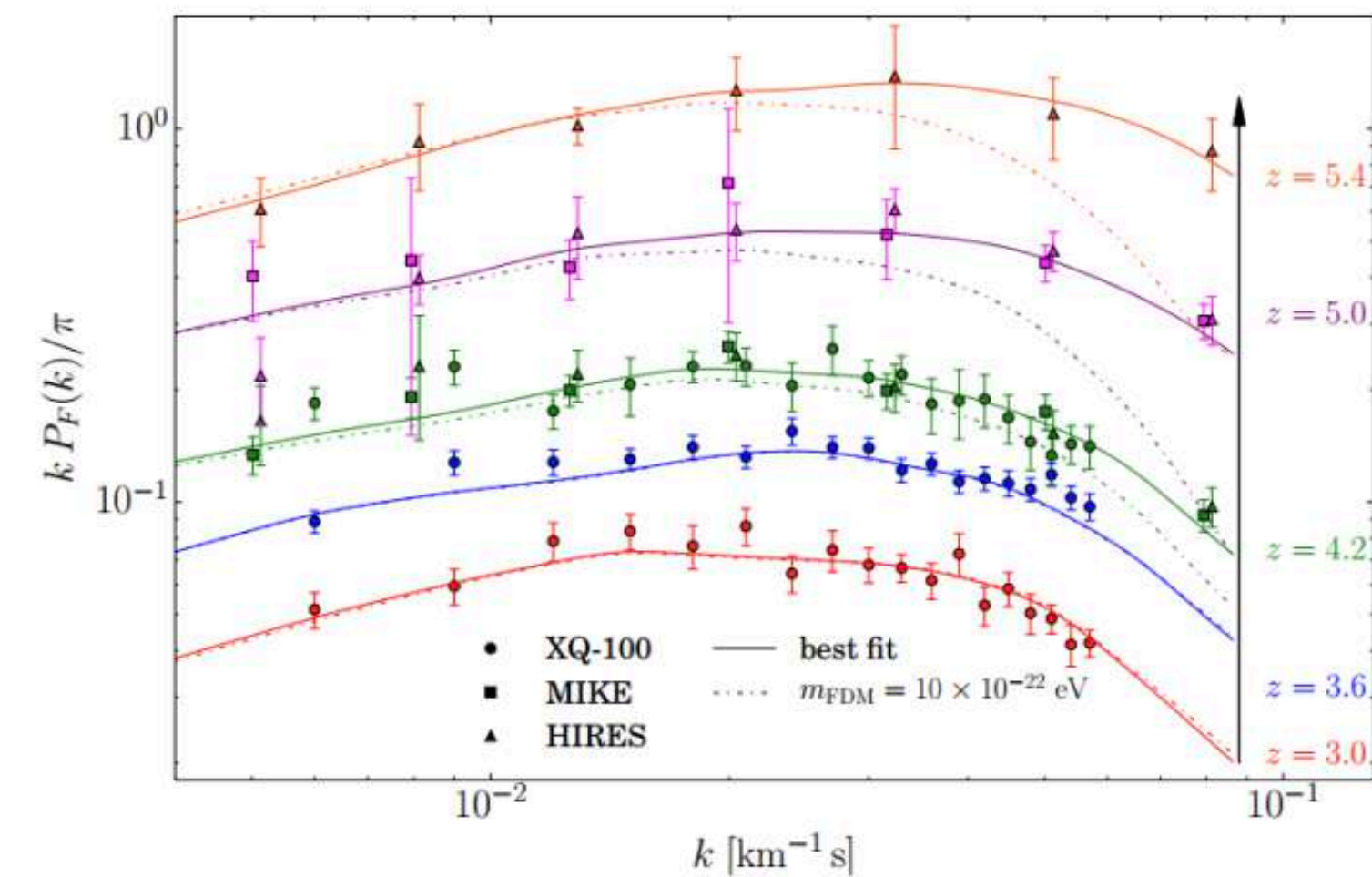
CMB/LSS



$$m \gtrsim 10^{-24} \text{ eV}$$

Lyman alpha

Armengaud et al. (2017); Iršič et al. (2017);
Rogers et al. (2020)

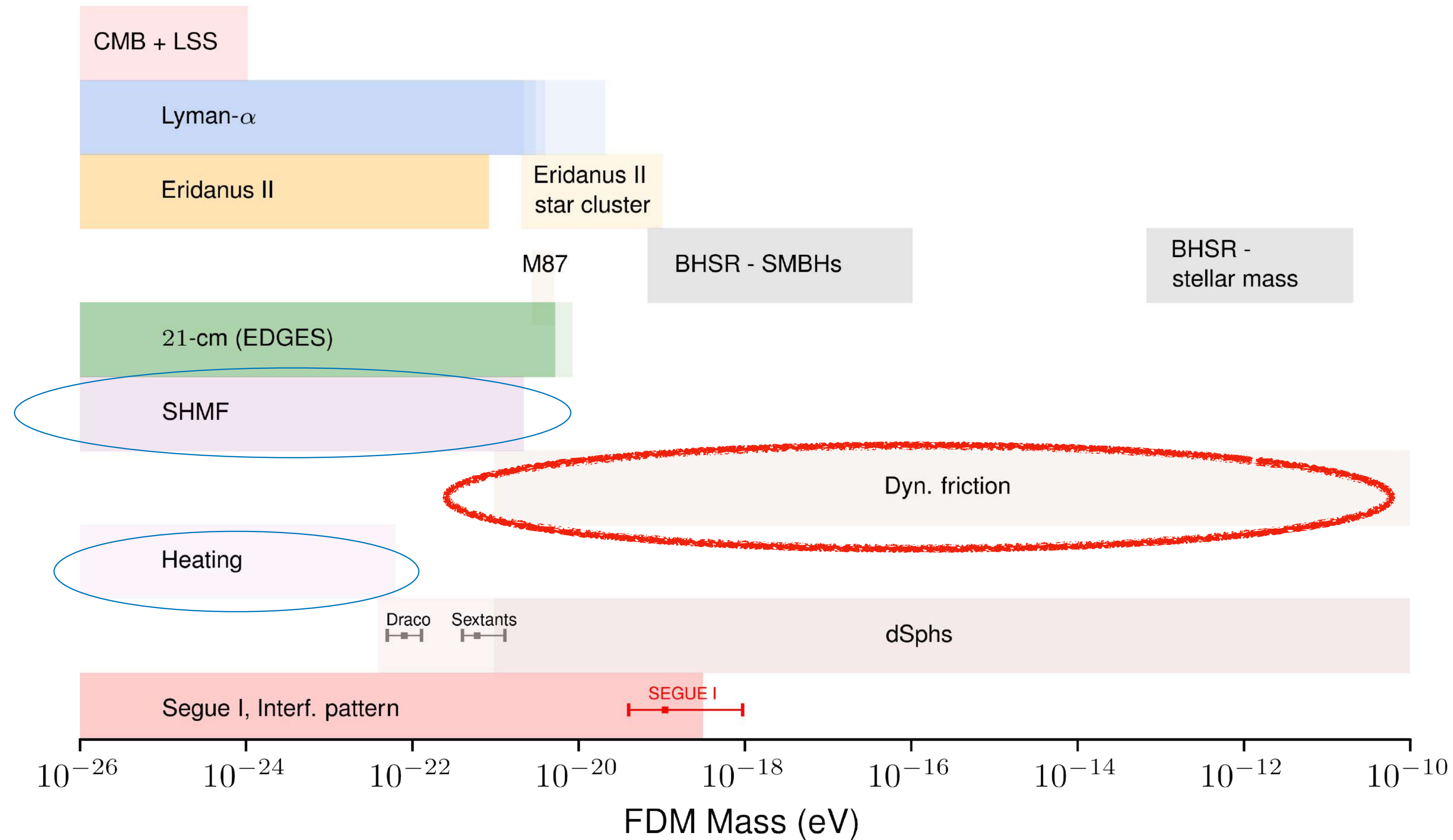


$$m \gtrsim 2 \times 10^{-20} \text{ eV}$$

so enough Mpc-scale power in Ly- α forest at $z = 5$.

Observational implications and constraints

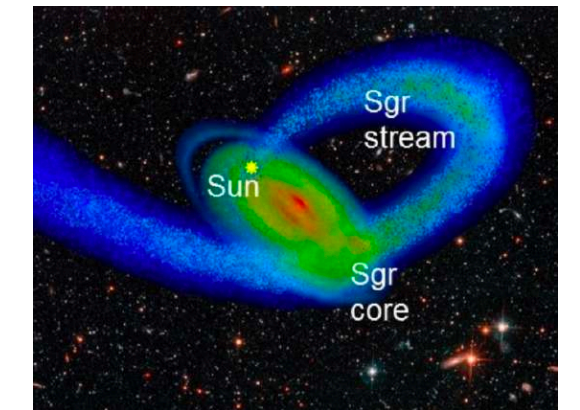
Fuzzy Dark Matter - bounds on the mass



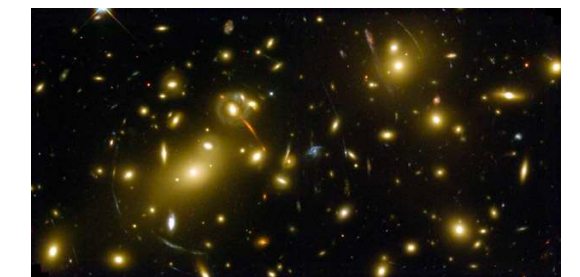
Suppression of small structures

Stellar streams

Schutz 2020: bound in the FDM SHMF using stellar streams and grav. lensing



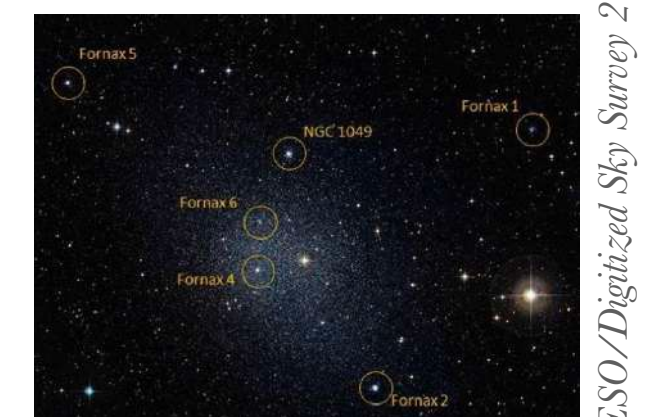
Grav. lensing



Dynamical effects

Globular clusters

$$m < 10^{-21} \text{ eV}$$



Lancaster et al. 2020

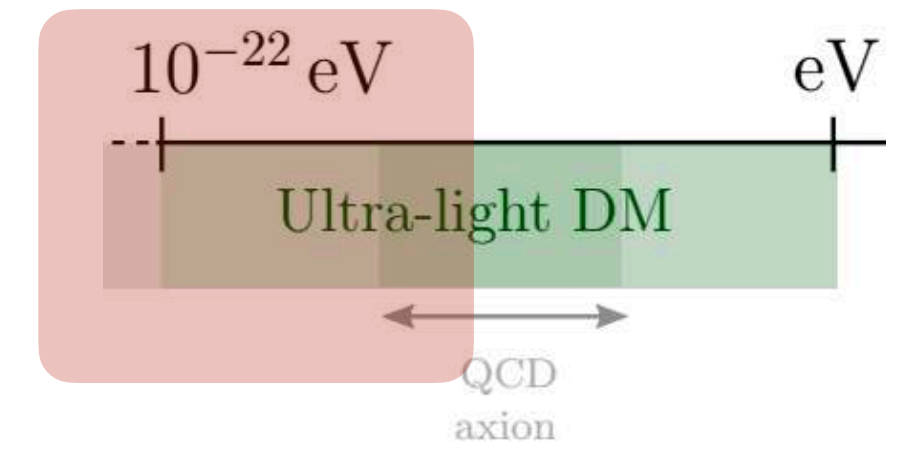
Heating of the MW disk

Church et al. 2019

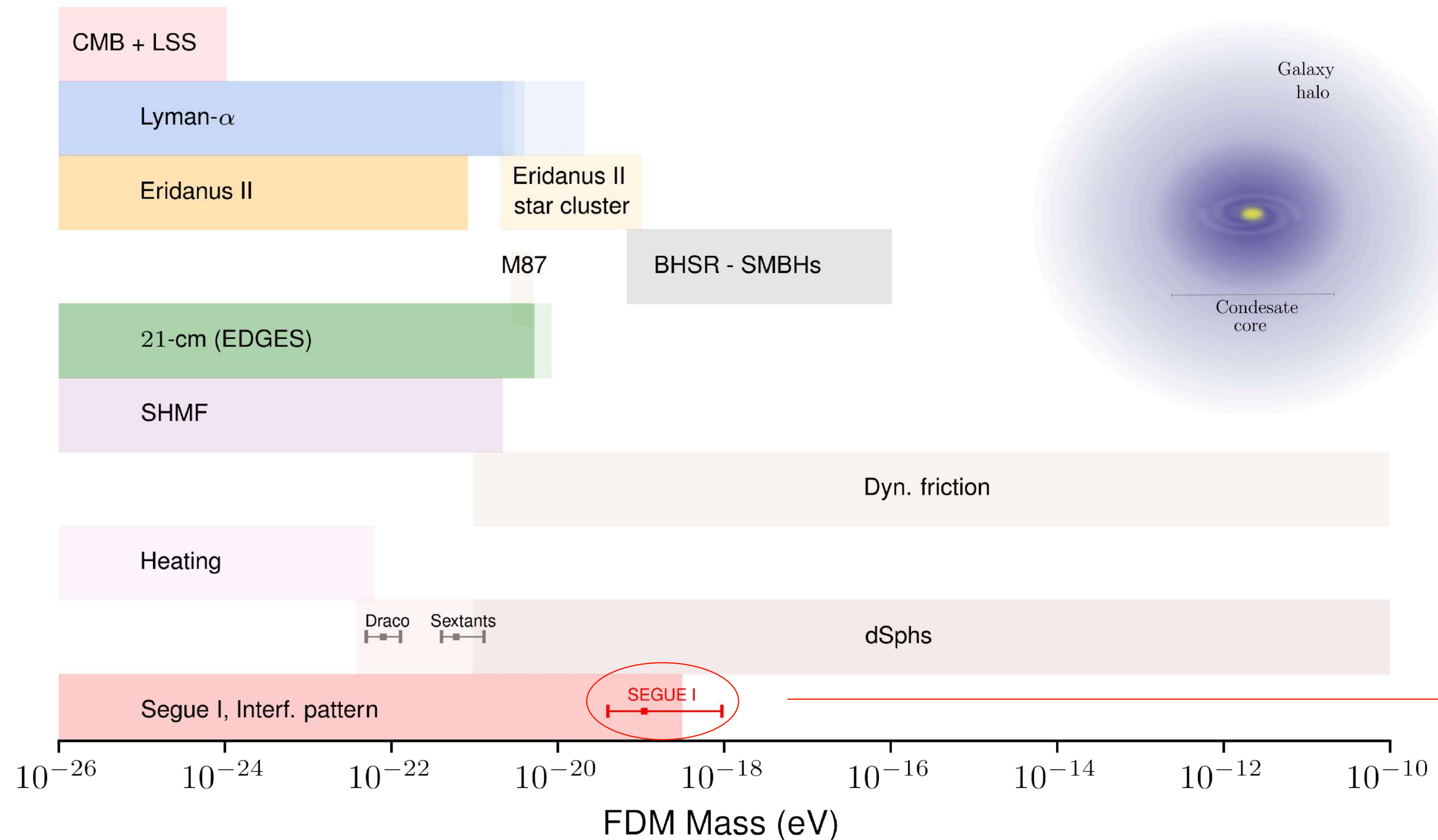
$$m > 0.6 \times 10^{-22} \text{ eV}$$

Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass



Presence of a core



FDM SIMULATIONS

$$\rho(r) = \begin{cases} \rho_{\text{soliton}} \simeq \frac{\rho_c}{[1 + 0.091(r/r_c)^2]^8}, & r < r_c \\ \rho_{\text{NFW}} = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2}, & r > r_c \end{cases}$$

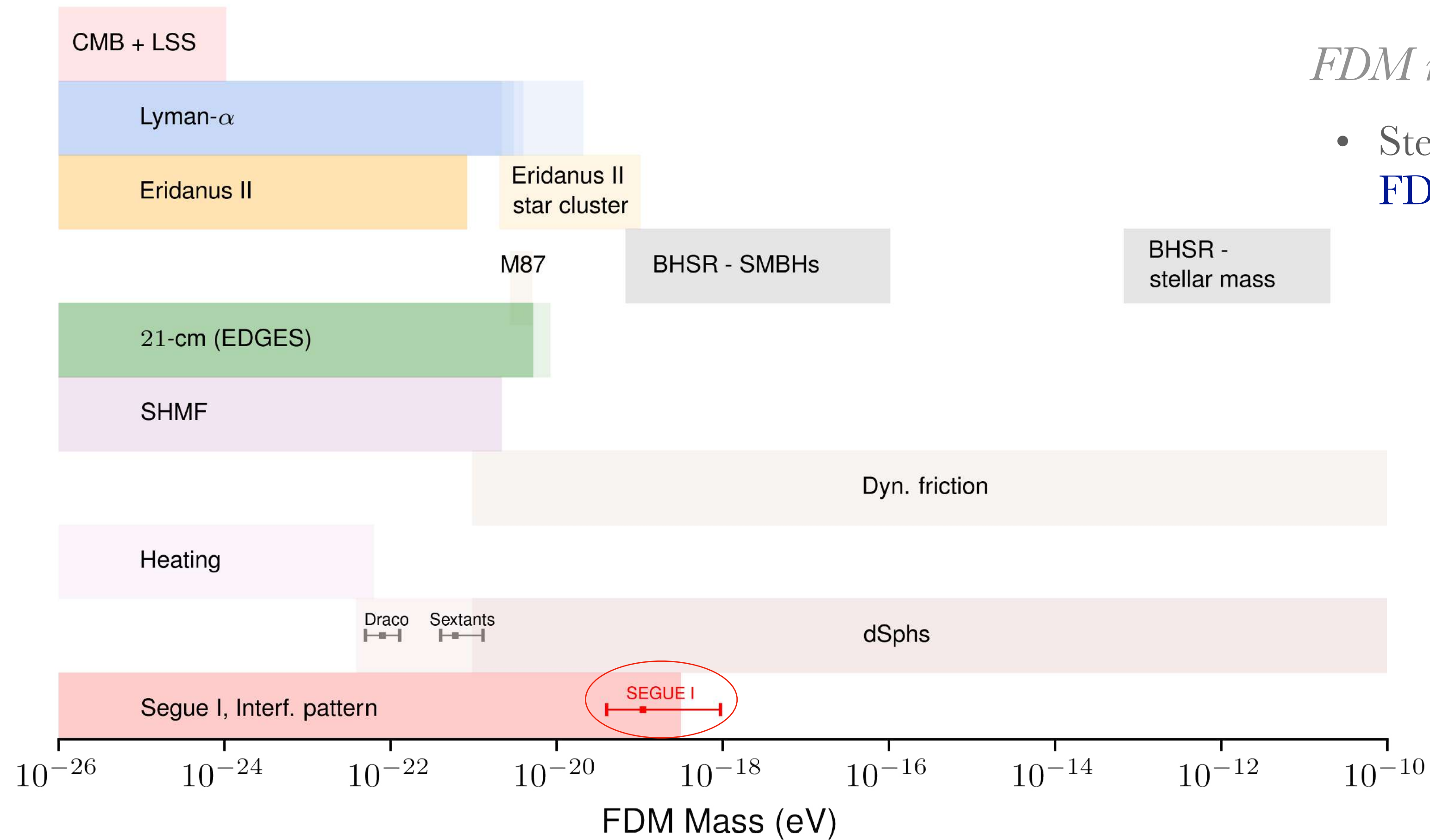
Jeans analysis like presented by Shunichi Horigome and Kohei Hayashi (and Shinichiro Ando)

“Narrowing the mass range of Fuzzy Dark Matter with Ultra-faint Dwarfs”, J. Chan, E.F., K. Hayashi, 2021.

Ultra-light Dark Matter

Fuzzy Dark Matter - bounds on the mass

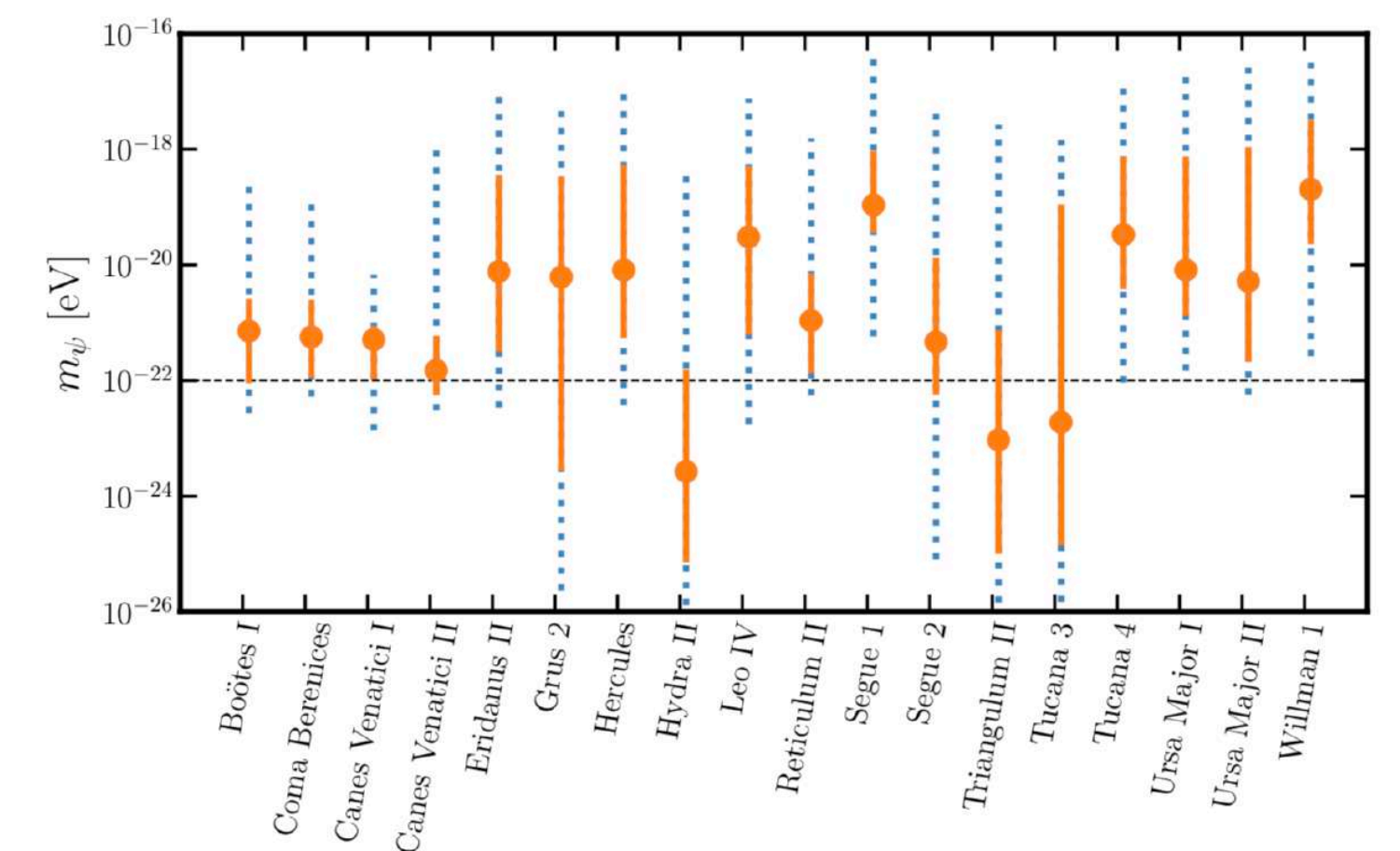
Hayashi, E.F, Chan, 2021.



FDM mass from Ultra-faint dwarfs

- Stellar kinematic data from 18 UFDs to fit the FDM profile from simulations

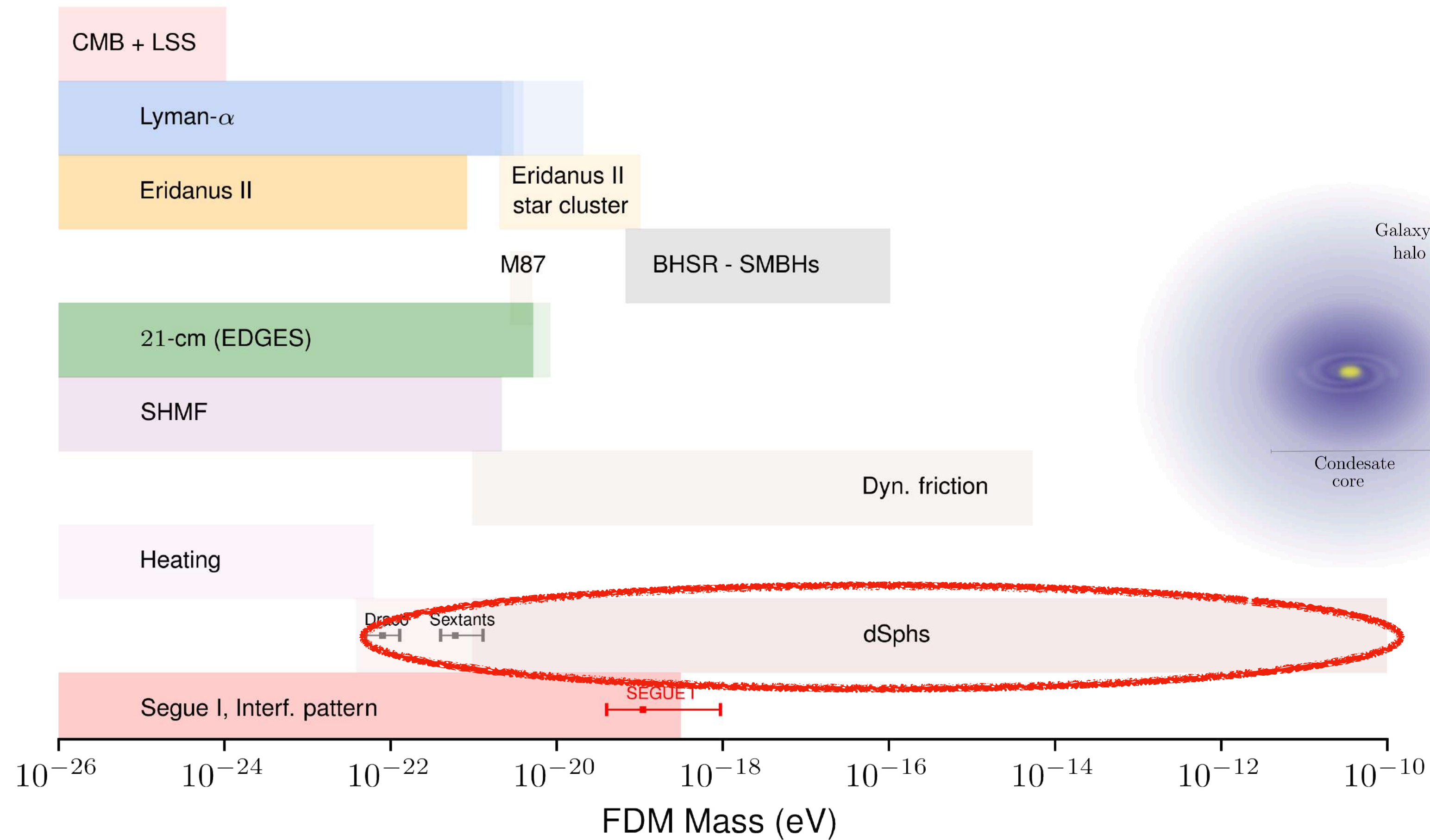
$$m_{\text{FDM}}^{(\text{Seg1})} = 1.1_{-0.7}^{+8.3} \times 10^{-19} \text{ eV}$$



Preference for higher mass

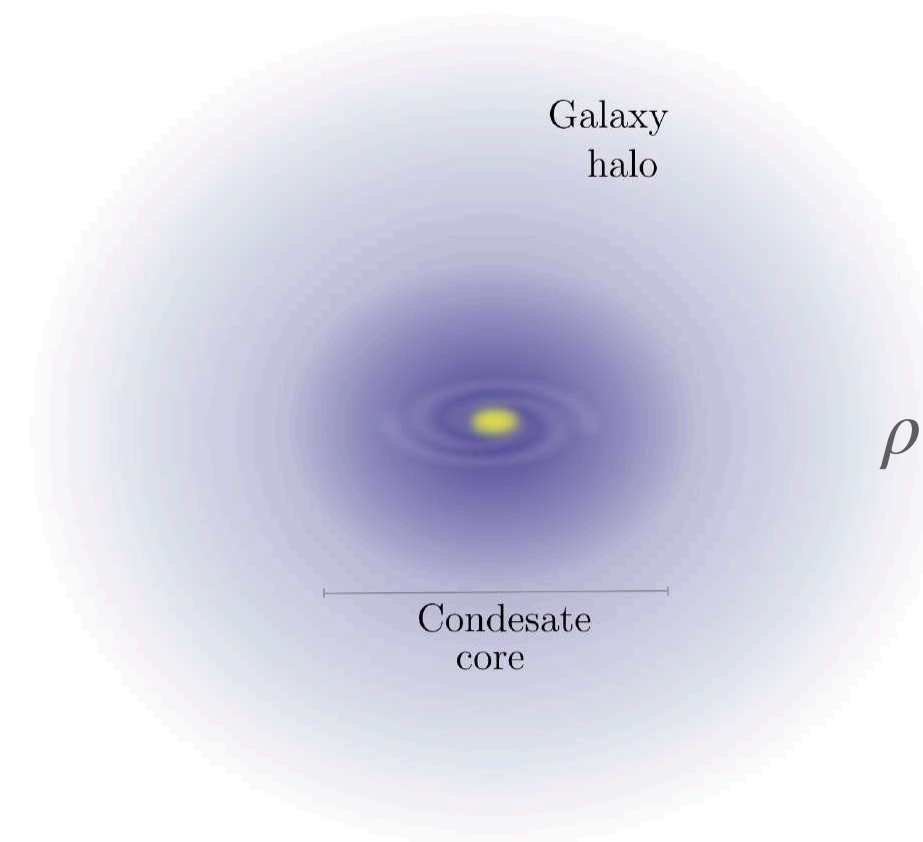
Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass



DWARFS

Dwarf Spheroidals (dSphs)



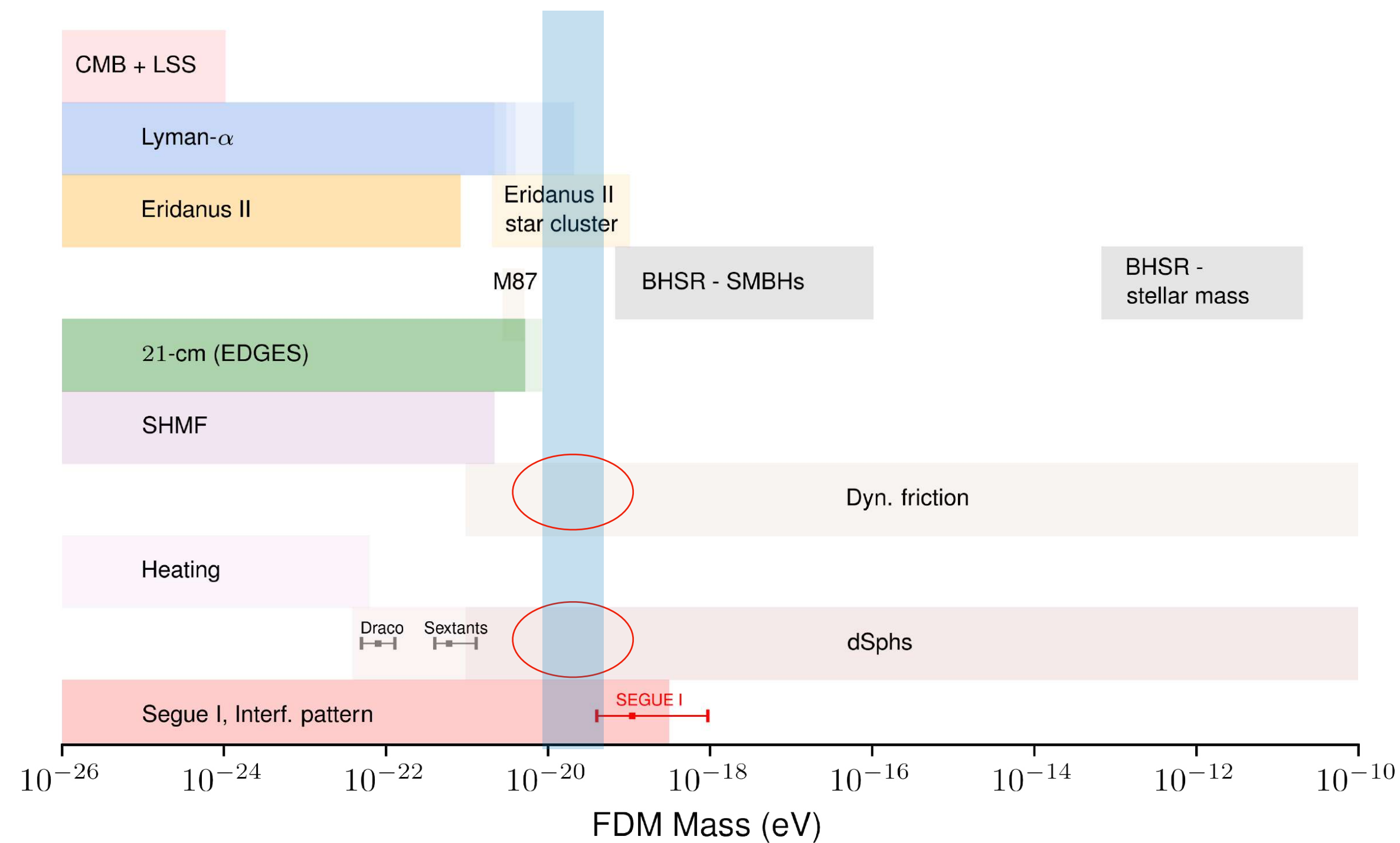
FDM SIMULATIONS

$$\rho(r) = \begin{cases} \rho_{\text{soliton}} \approx \frac{\rho_c}{[1 + 0.091(r/r_c)^2]^8}, & r < r_c \\ \rho_{\text{NFW}} = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2}, & r > r_c \end{cases}$$

Fornax - Sculptor

$$m < 0.8 \times 10^{-22} \text{ eV}$$

Constraints on the mass



$$m_{\text{FDM}}^{(\text{Seg1})} = 1.1^{+8.3}_{-0.7} \times 10^{-19} \text{ eV}$$

Incompatibility between all bounds and the dSphs
(Fornax and Sculptor) bounds

Possible reasons for this *incompatibility*:

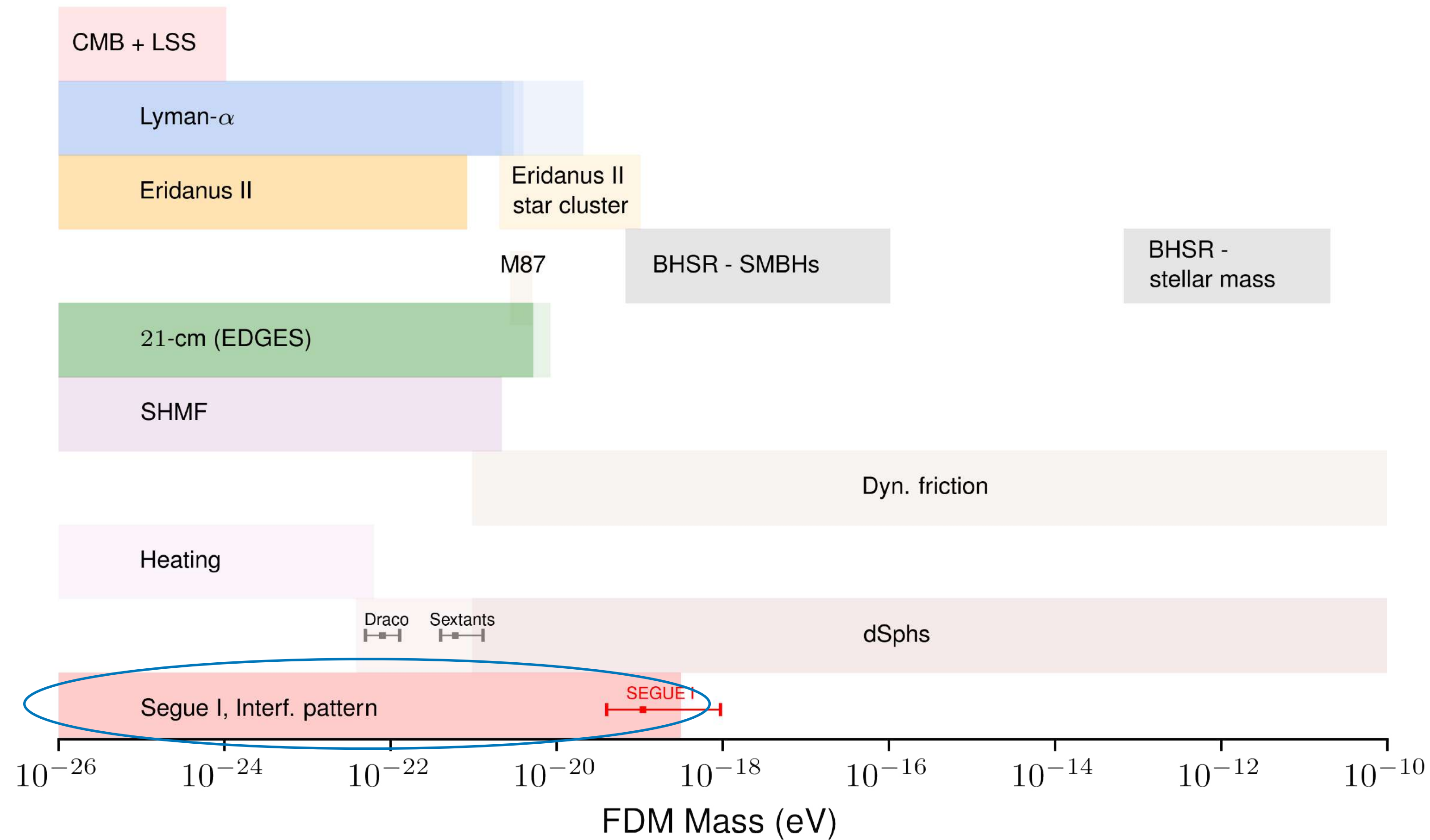
- *Influence of baryons*: baryonic processes can change the density structure of their halo - we are not probing the intrinsic DM profile.
- *Universality of the core profile*: FDM soliton profile might be too simplistic, could change for different systems (might also depend on baryons)
- *Core-mass relation*: might need to be better understood. \neq relation in \neq simulations
- *Challenge for the FDM model*

*Jowett Chan's and
Masashi Chiba's talks!*

Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass

Shinichiro Ando's presentation



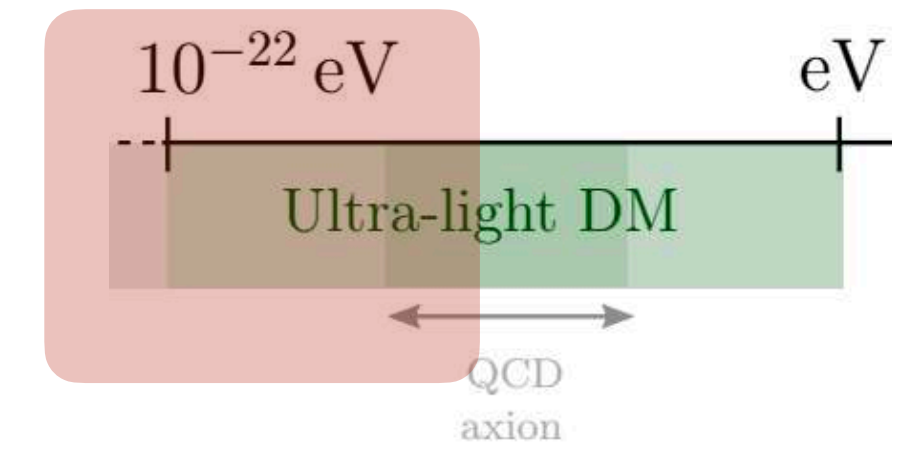
INTERFERENCE PATTERNS

N. Dalal, A. Kravtsov, 2203.05750

$$m_{\text{FDM}} > 1 \times 10^{-19} \text{eV}$$

Current status

Fuzzy Dark Matter - bounds on the mass

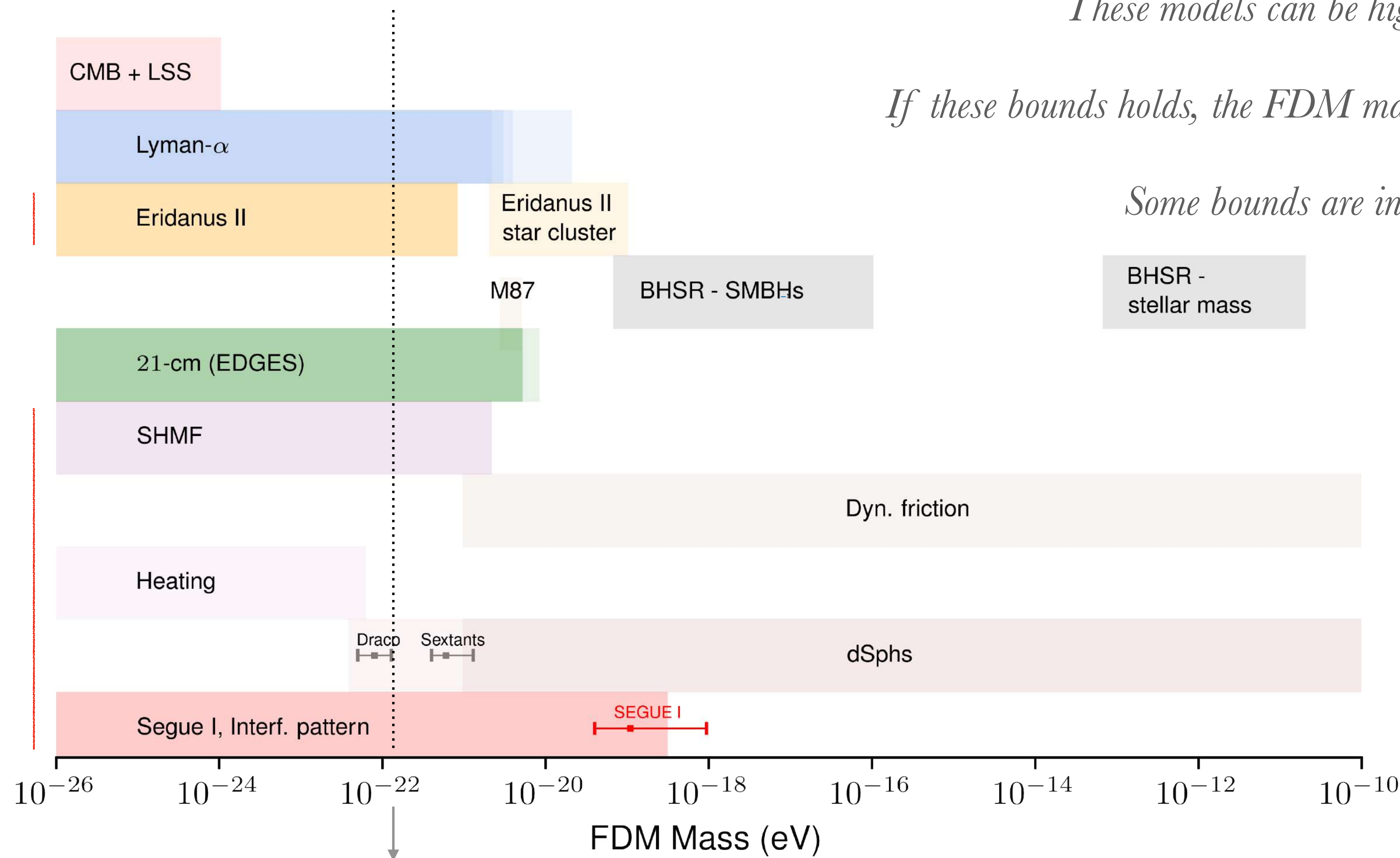


These models can be highly constrained

If these bounds hold, the FDM mass range is narrowing down

Some bounds are incompatible!

BUT: systematic effects!!



Sweet spot for solving small scale problems

Need:

- Observations
- Improve sims
- New observables
- New probes

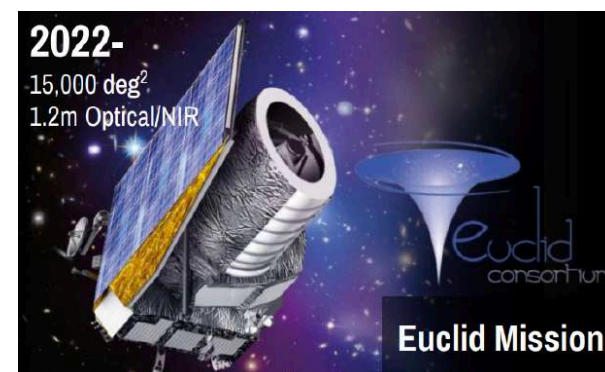
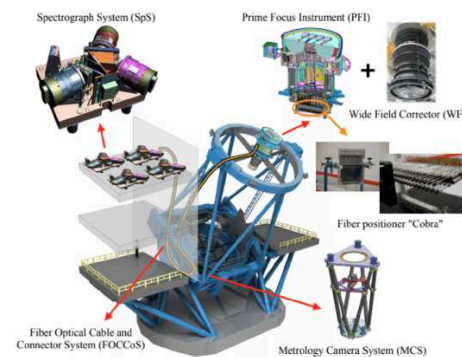
FUTURE

Observations

Photometric and spectroscopic surveys



Prime Focus Spectrograph (PFS)



CMB

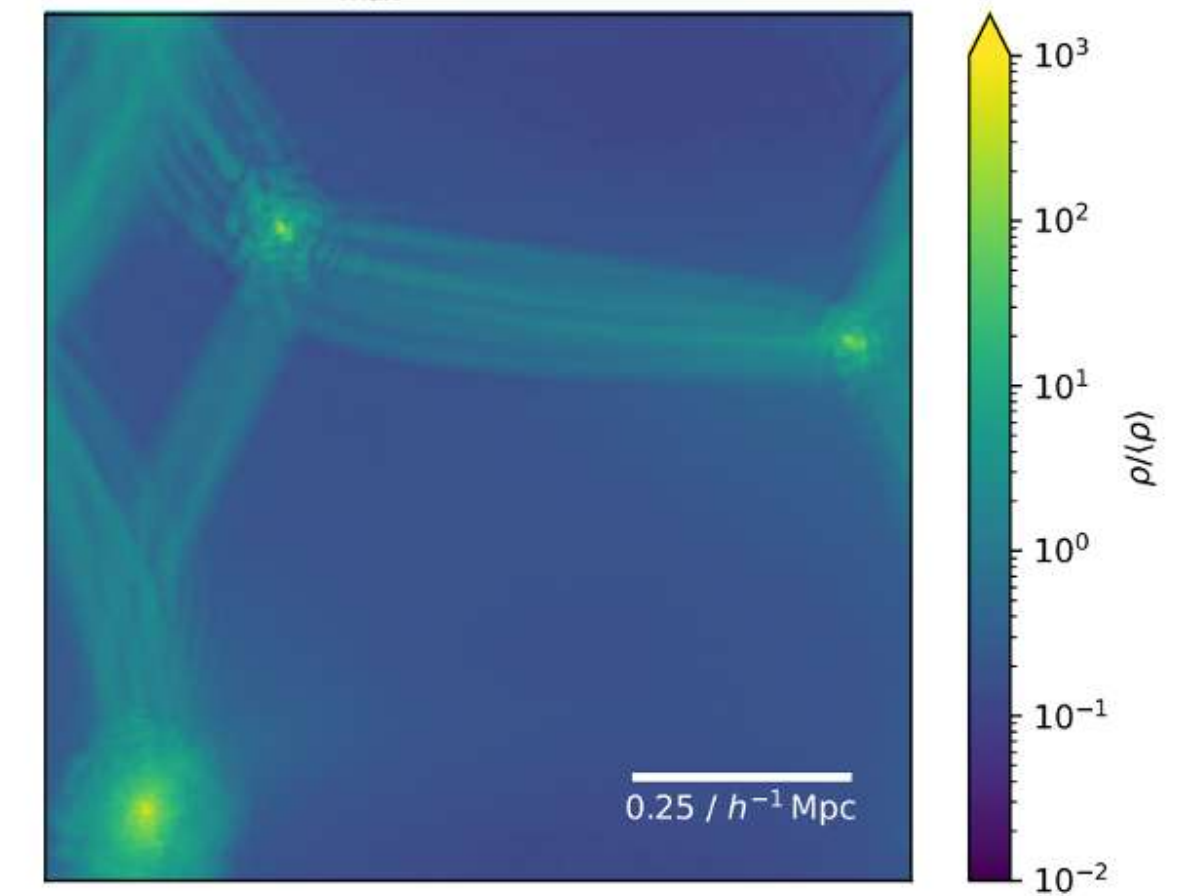


21cm



Simulations

FDM: 256^3 , $mc^2 = 1.75 \times 10^{-23}$ eV, $z = 0.00$
 $v_{\max} = 88.1$ km/s



New observables

Ex.: - interference pattern
- vortices

New probes

Sub-galactic power spectrum

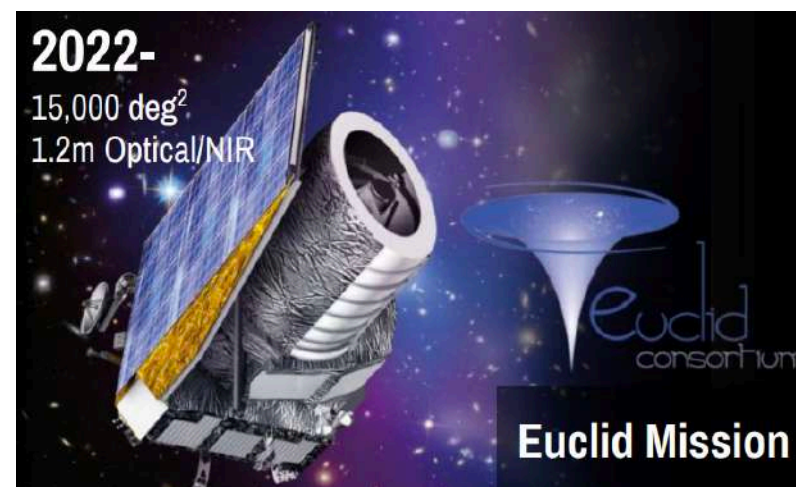
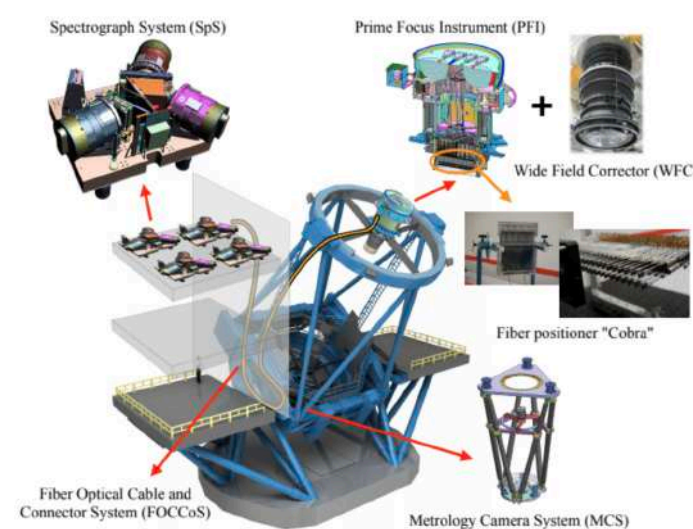
Future - signals in cosmology

Observations

Photometric and spectroscopic surveys



Prime Focus Spectrograph (PFS)



GWs

21cm



CMB



CMB-S4
Next Generation CMB Experiment

PFS (Prime Focus Spectrograph)

B02 group (Subaru spectroscopy)

PFS is going to be exquisite to measure the properties of DM

DM with PFS → synergy between science goals

Galaxy archeology

- Nature of DM (dSphs)
- Structure of MW dark halo
- Streams
- Stellar kinematics and chemical abundances – MW & M31

Cosmology

- Power spectrum
- HSC+PFS
- Linear growth (RSD)

Galaxy evolution

- Small-scale tests of structure growth
- Halo-galaxy connection M_*/M_{200}
- Physics of cosmic reionization via LAEs & 21cm studies
- Tomography of gas and DM

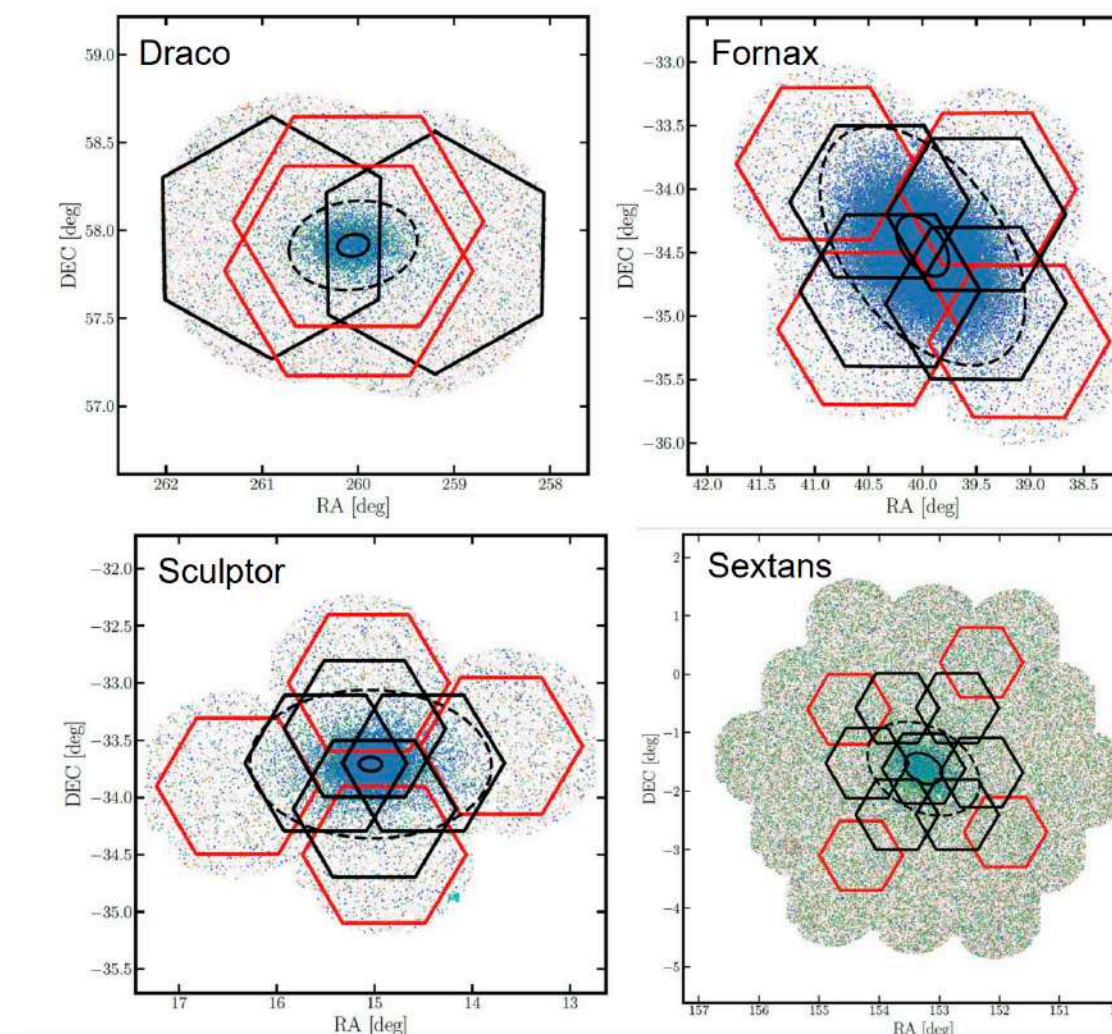
PFS - Galactic Archaeology

TESTING ULTRA LIGHT DM/DM with PFS

Galaxy archeology

- Nature of DM (dSphs)
- Structure of MW dark halo
- Streams
- Stellar kinematics and chemical abundances – MW & M31

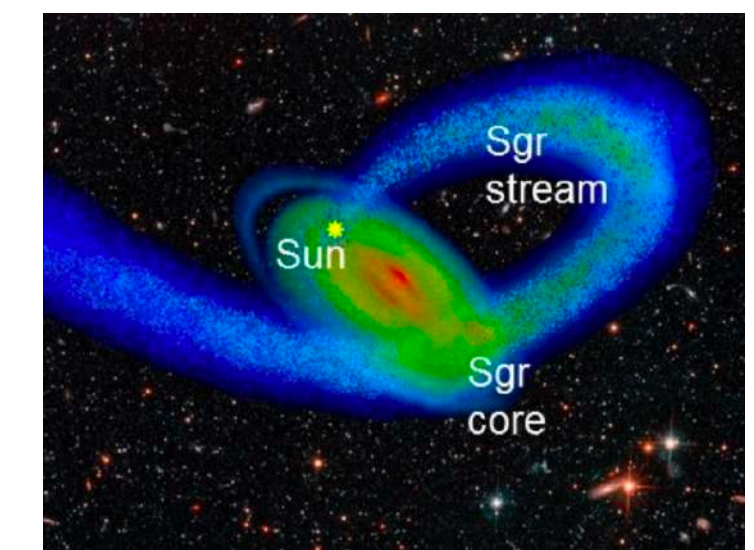
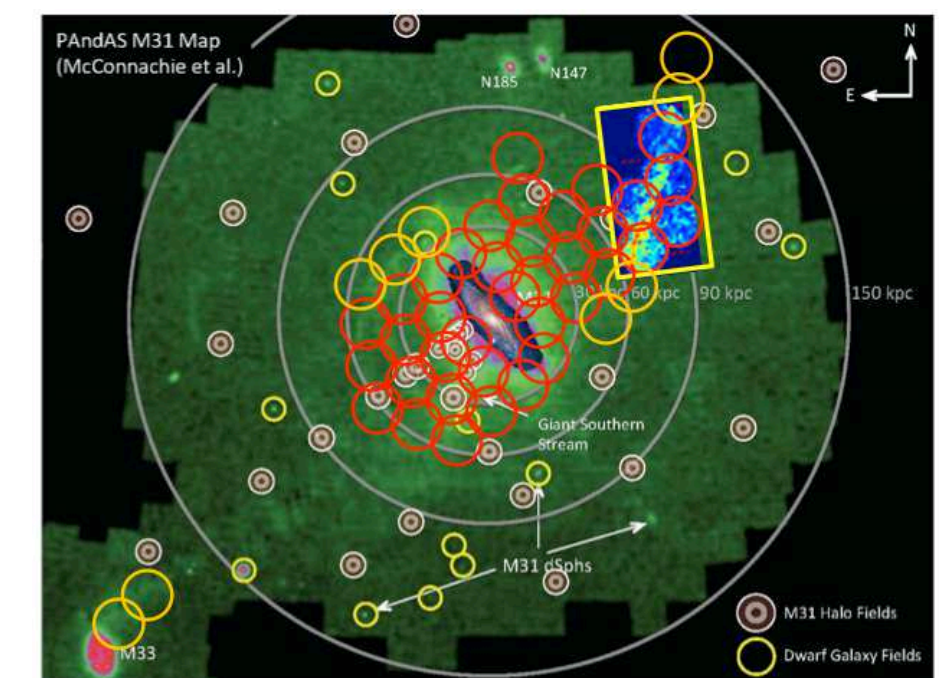
Wide & deep survey of MW dwarf galaxies w. Subaru/PFS



dSphs

B02 group (Subaru spectroscopy)

M31



MW outer disk

- MW dwarf satellites - DM halo profile and $[Fe/H]$ & $[\alpha/Fe]$ over largest areas \longrightarrow Unique & high impact
- M31 halo - DM subhalos, chemo-dynamics with spectroscopic $[Fe/H]$ and $[\alpha/Fe]$
- MW halo/streams/disks - Chemo-dynamics of the MW outer disks, halo dynamics, constraints on the Galactic potential \longrightarrow Unique: beyond reach of *Gaia* and VLT

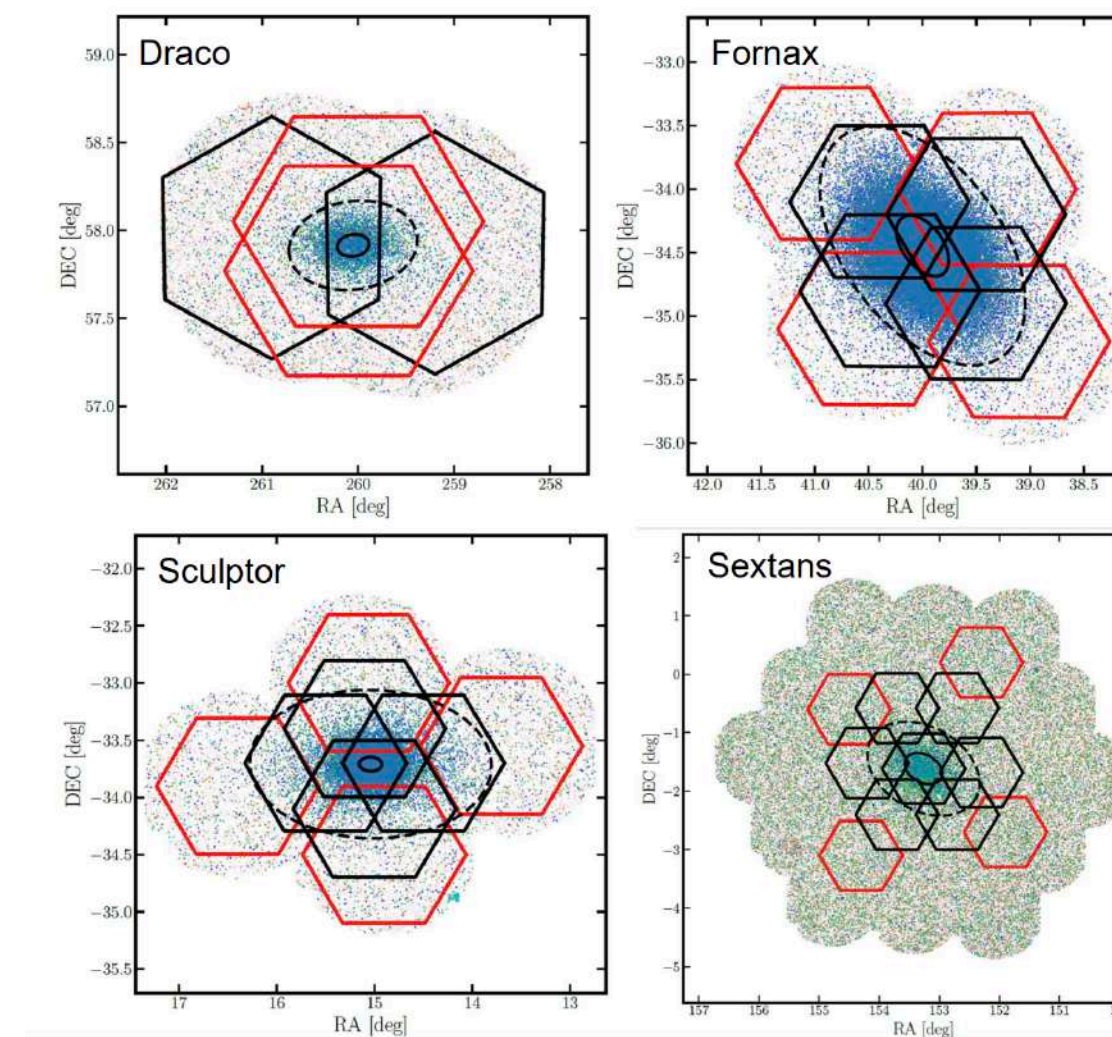
PFS - Galactic Archaeology

TESTING ULTRA LIGHT DM/DM with PFS

Galaxy archeology

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- Streams
- Stellar kinematics and chemical abundances – MW & M31

Wide & deep survey of MW dwarf galaxies w. Subaru/PFS

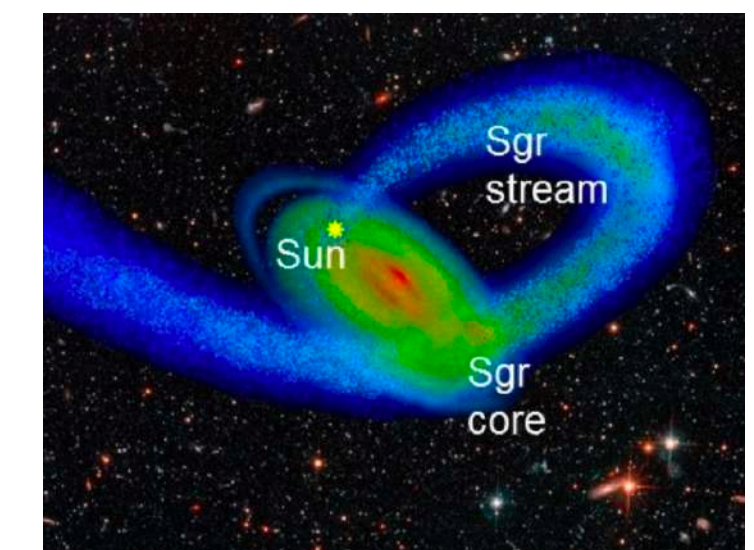
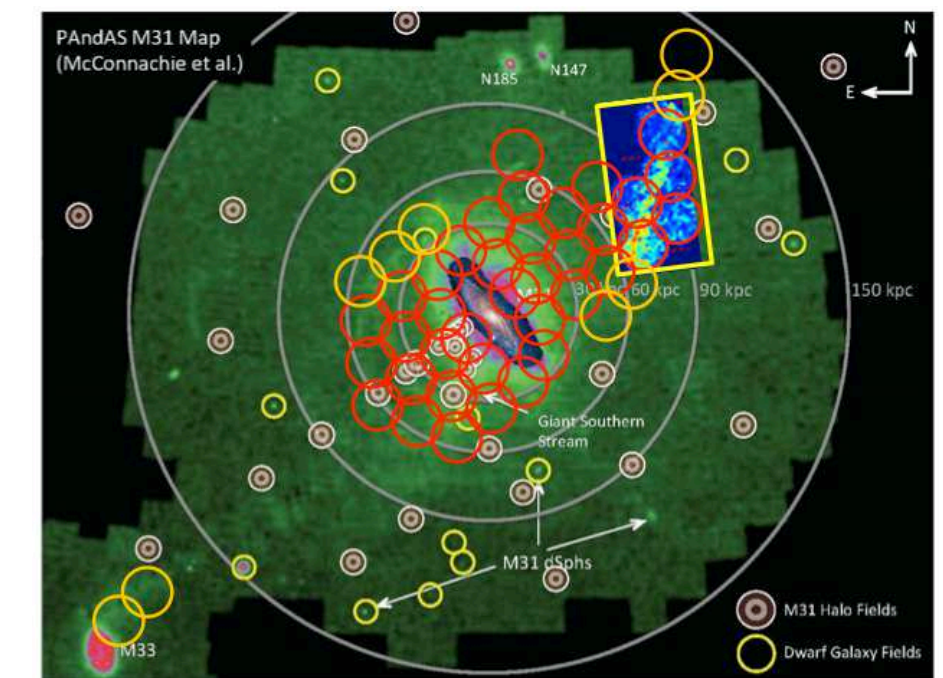


dSphs

Stellar streams

B02 group (Subaru spectroscopy)

M31



MW outer disk

Dwarf galaxies:

- (1) Sample sizes in excess of 1000 stars per dSph,
- (2) Wide-area coverage well suited for dSphs,
- (3) Velocity precision much smaller than the velocity dispersion of a dSph,
- (4) Abundance measurements
- (5) Synergy with Subaru/HSC pre-imaging.

GA → potential to put unprecedented constraints on ULDM.

PFS - Galactic Archaeology

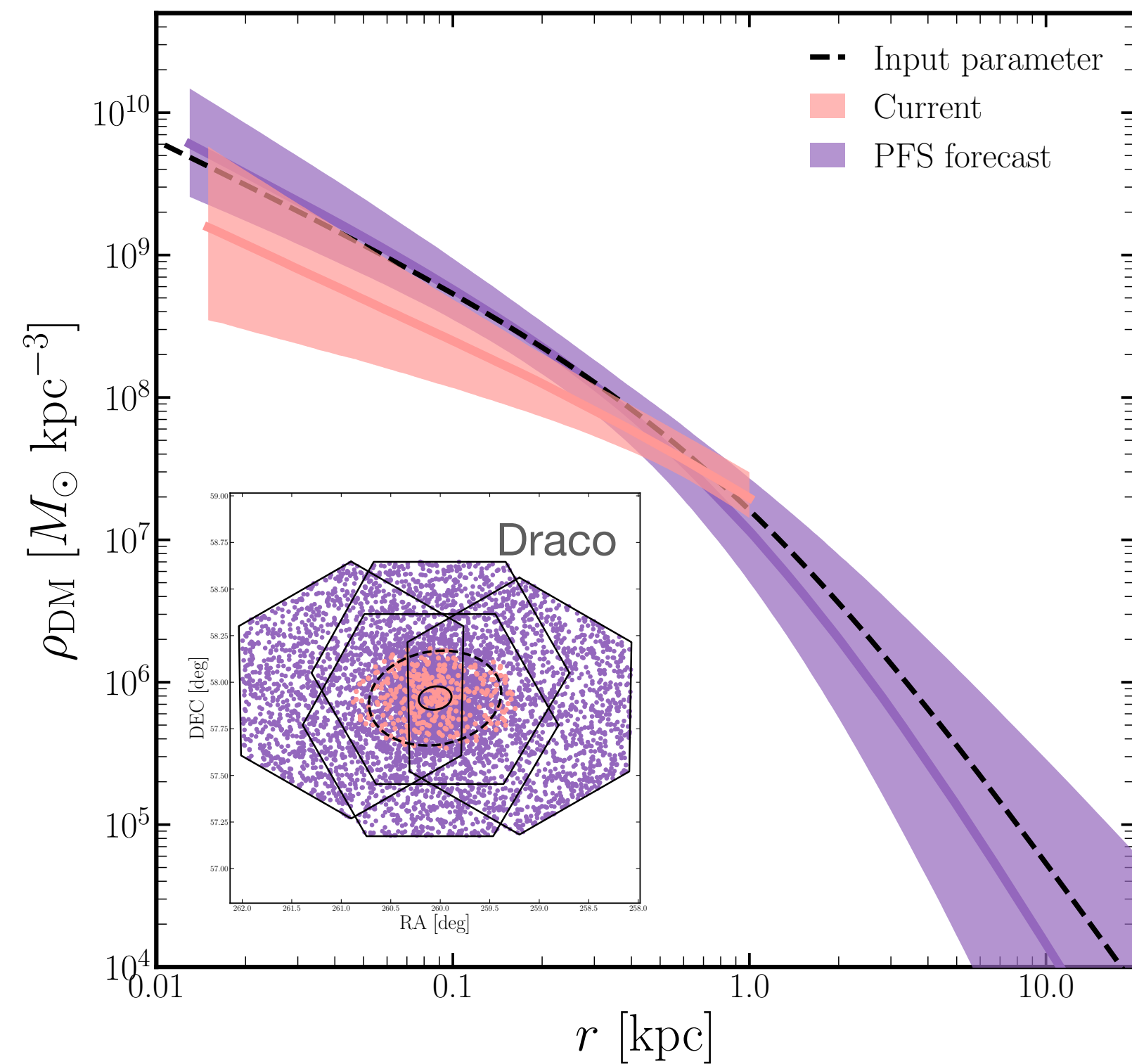
B02 group (Subaru spectroscopy)

DM searches with PFS-GA

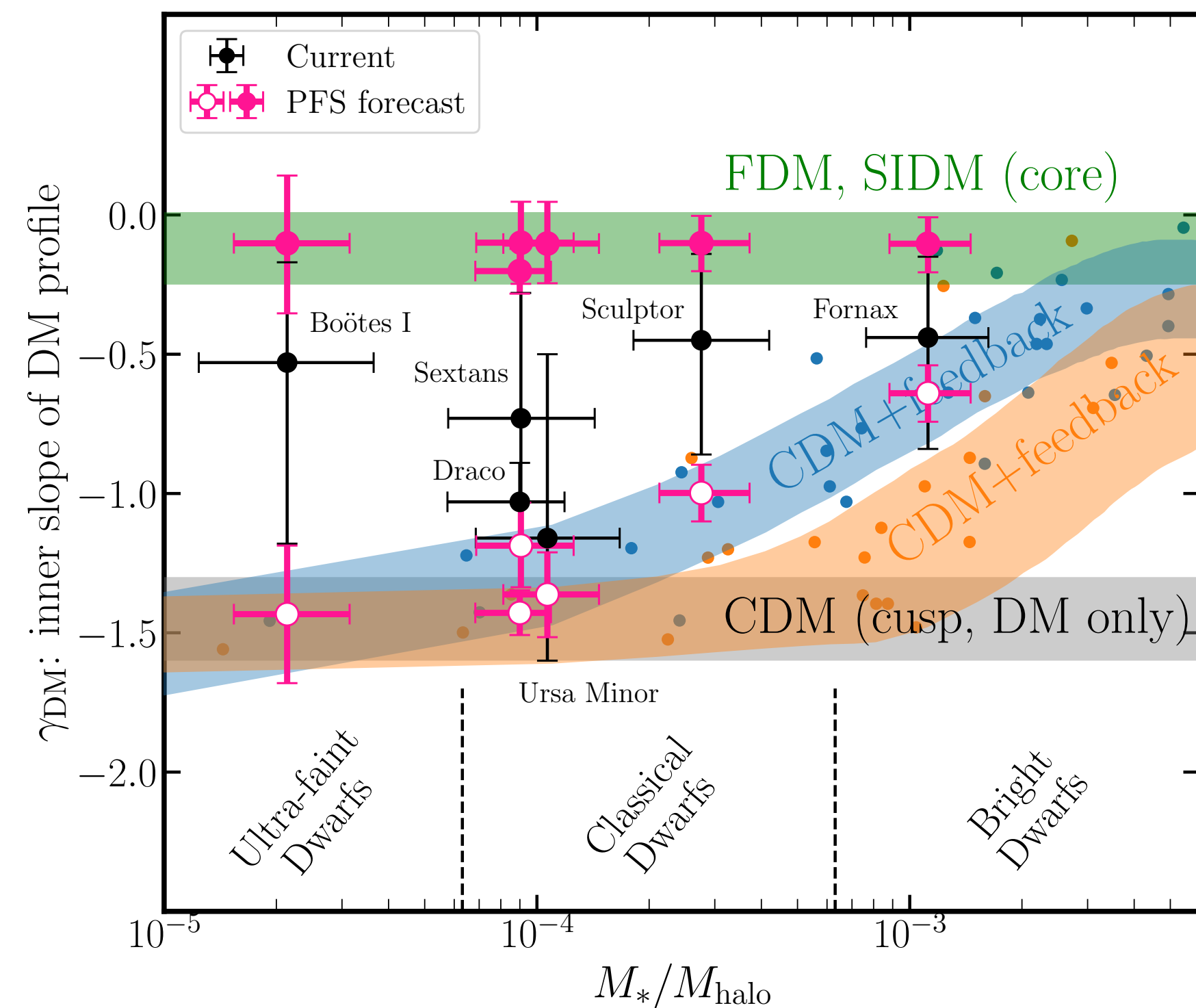
Leader: Kohei Hayashi

Figures by Kohei Hayashi

Dark matter density profile



Inner dark-matter density profile slope derived for PFS-GA selected sample of dSphs vs. their stellar-to-halo mass ratio



“Current” (N = 500) and “PFS forecast” (N = 5, 000 stars) samples

Adapted from Kohei Hayashi, Masashi Chiba, Tomoaki Ishiyama, ApJ (2022)

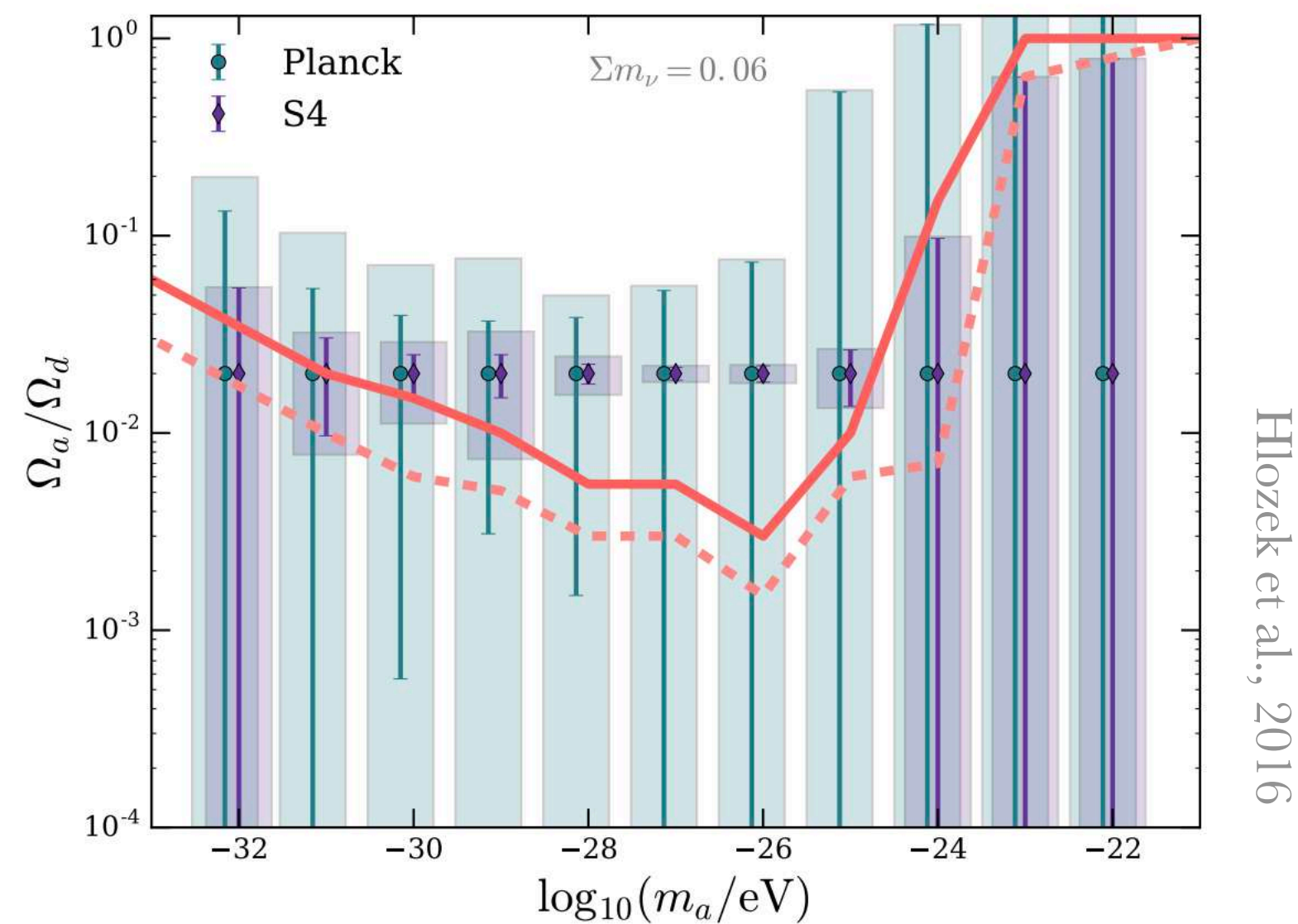
Future - Cosmic Microwave Background

CMB working group

TESTING ULTRA LIGHT DM CMB

CMB - S4

Constraints on Ω_a/Ω_d



Significantly improve constraints on the composition of the dark sector!

Constraints on the *optical depth*

$\tau(r_{\text{rec}})$

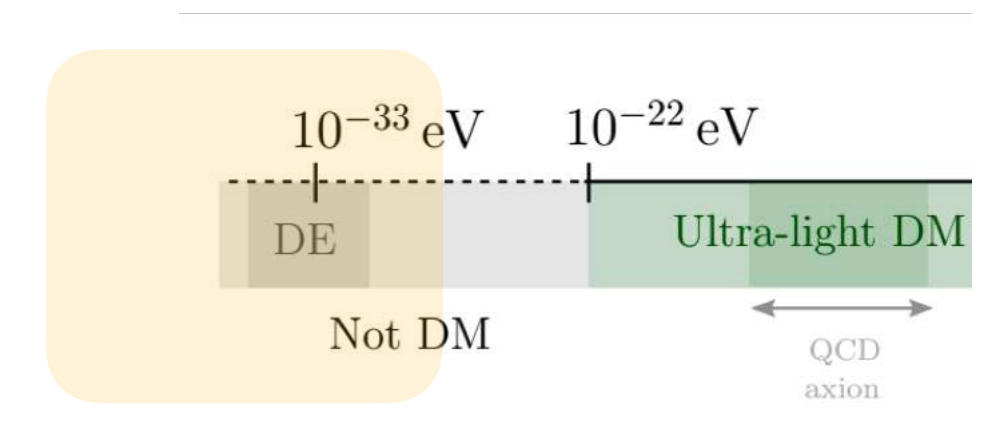
Constraint the ULDM mass

Kinematic Sunyaev-Zel'dovich effect: sensitive to the duration of the reionization

- *LiteBIRD*
- *Advances ACTPol*
- *CMB-S4*

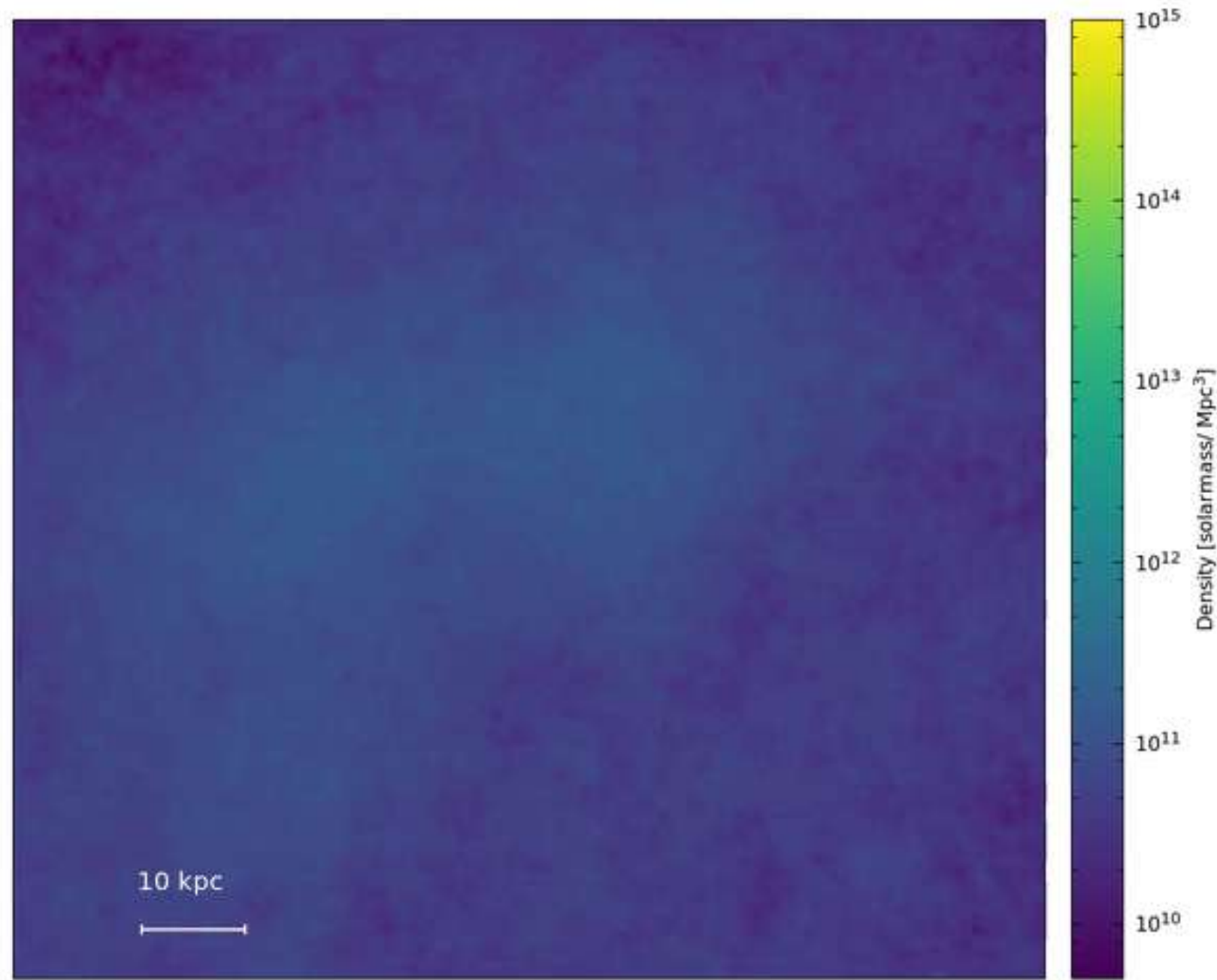
Cosmic Birefringence

CMB and light DM groups' talks!



New probes

Interference pattern



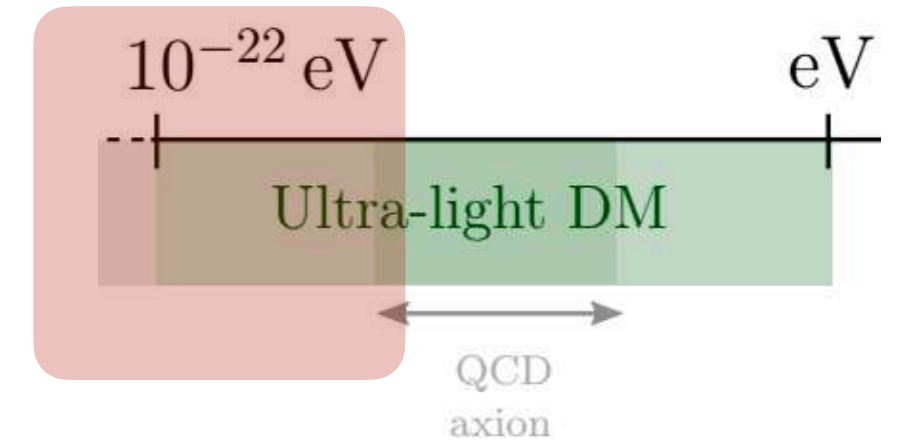
Simulation by Jowett Chan

@(1) fluctuations in density →

Constructive interference: **granules**

Destructive interference

→ $\sim \lambda_{dB}$



ONGOING

In collaboration with Jowett Chan and Simon May

- Characterizing the interference patterns using full simulations

- Strong lensing *In collaboration with MPA group: Simona Vegetti, Simon White, Devon Powel*

- Stellar streams *In collaboration with MPA group: Sten Delos and Fabian Schmidt*

Previous studies:

Strong lensing:

J. Chan, H. Schive, S.g. Wong, T. Chiueh, T. Broadhurst, 2020

Stellar streams:

Neal Dalal, Jo Bovy, Lam Hui, Xinyu Li, 2020

Sub-galactic power spectrum:

Hezaveh et al. (2016)

Sub-galactic power spectrum

Kawai, Oguri (2021)

M. Oguri's talk!

Dwarfs

N. Dalal, A. Kravtsov, 2022



What is the predicted **size and abundance** of vortices in the halo?

Are they **observable**?

Strong lensing? Stellar streams?

Can they be formed in the filaments?

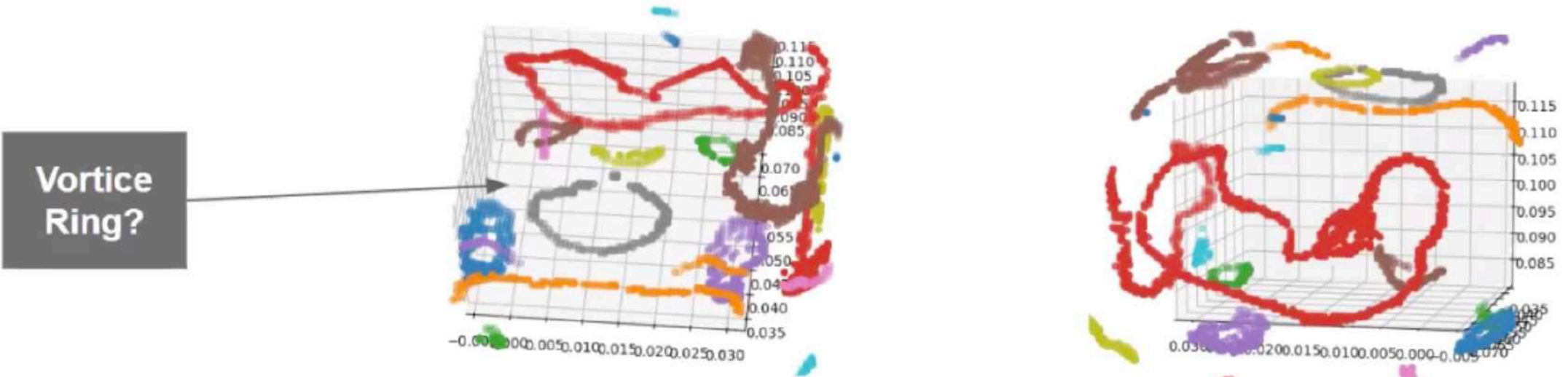
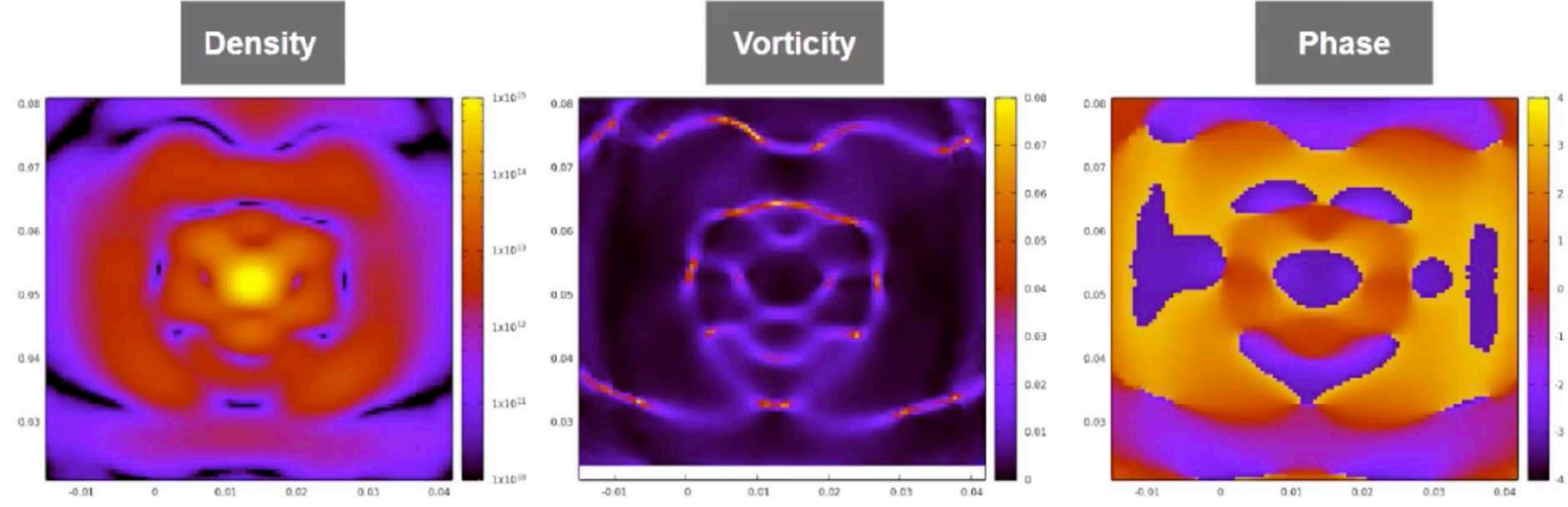
New probes

Ongoing: Vortices

PRELIMINARY

Fuzzy DM

Might be interesting to the C02 (simulation) group!

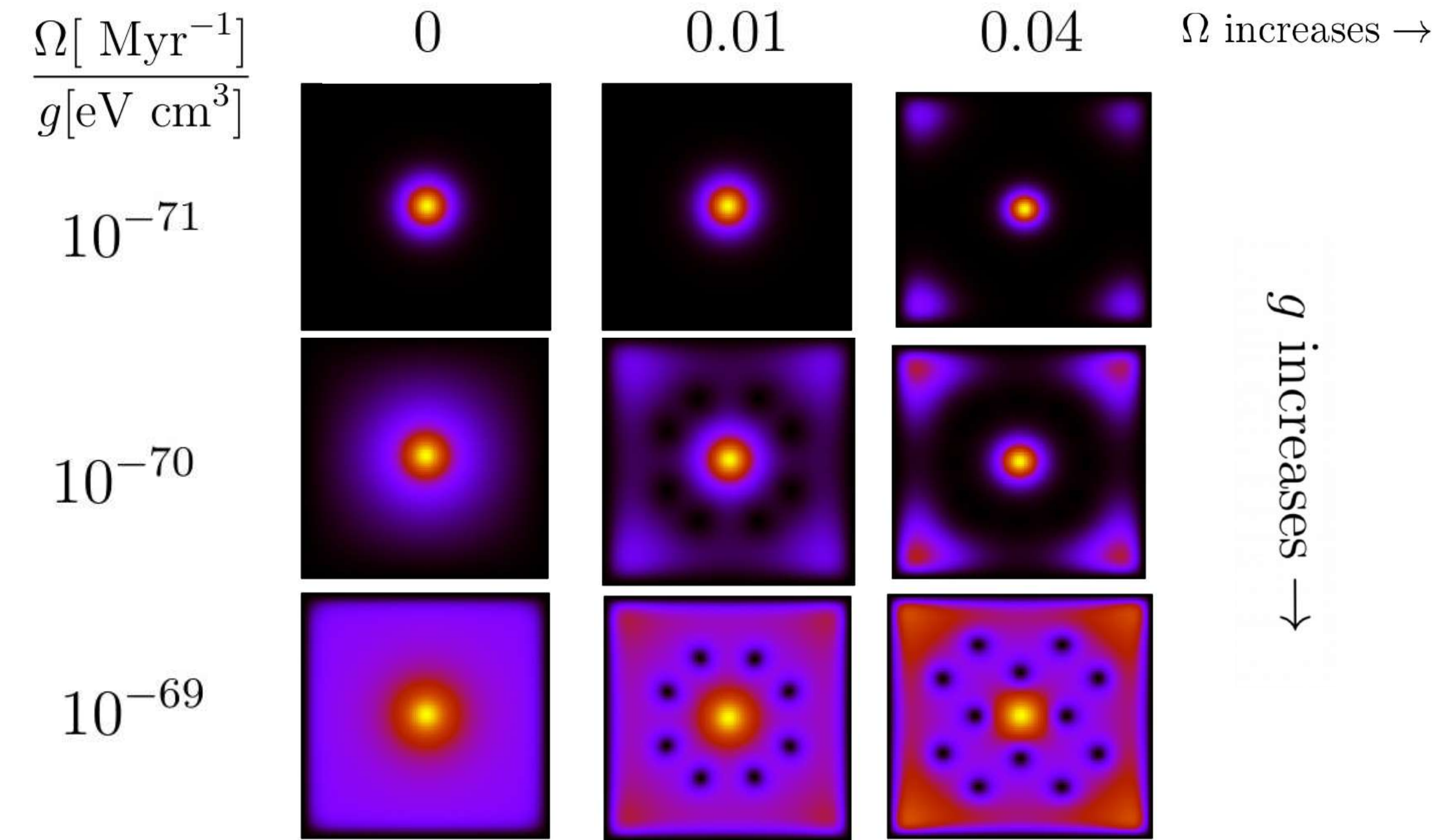


+ Improve theoretical understanding of these DM vortices
In collaboration with P. Bittar



In collaboration with Jowett Chan
 (some aspects with Noam Libeskind and S. May)

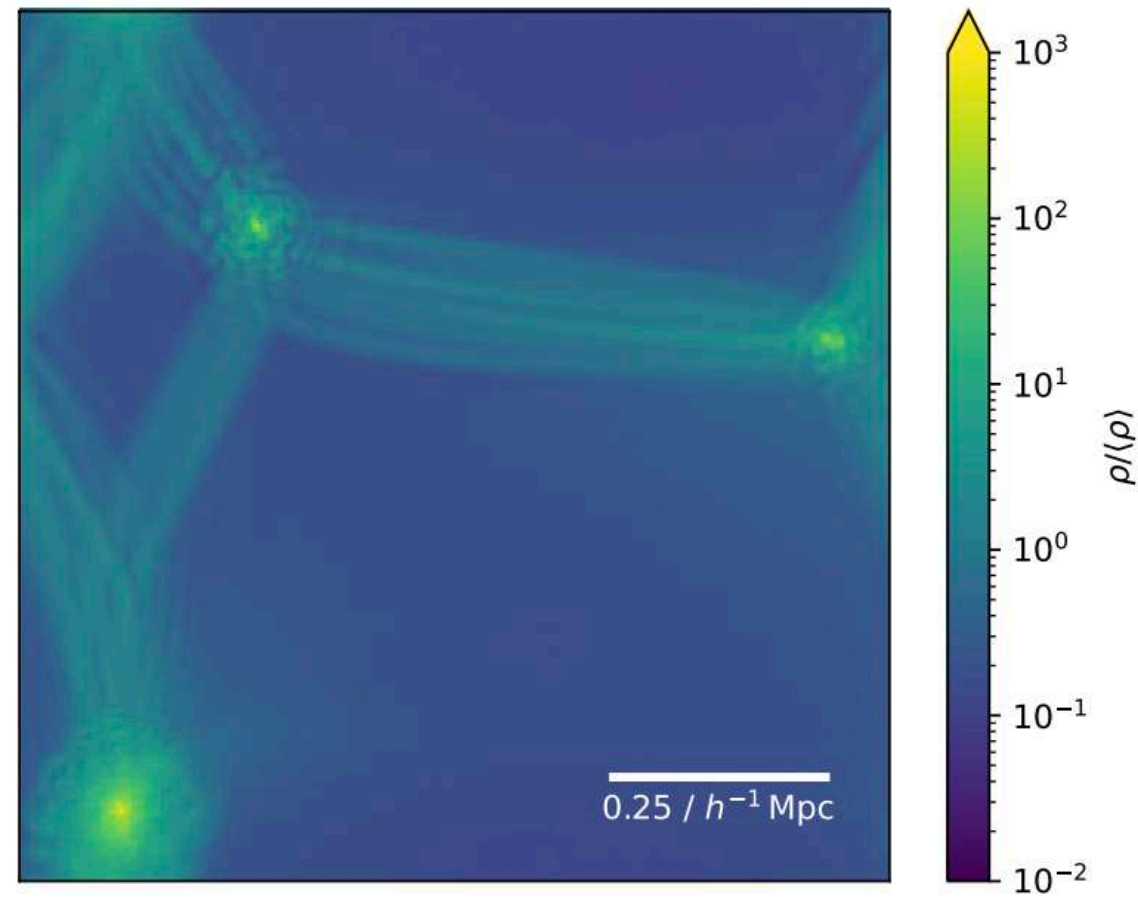
Self-interacting Fuzzy DM



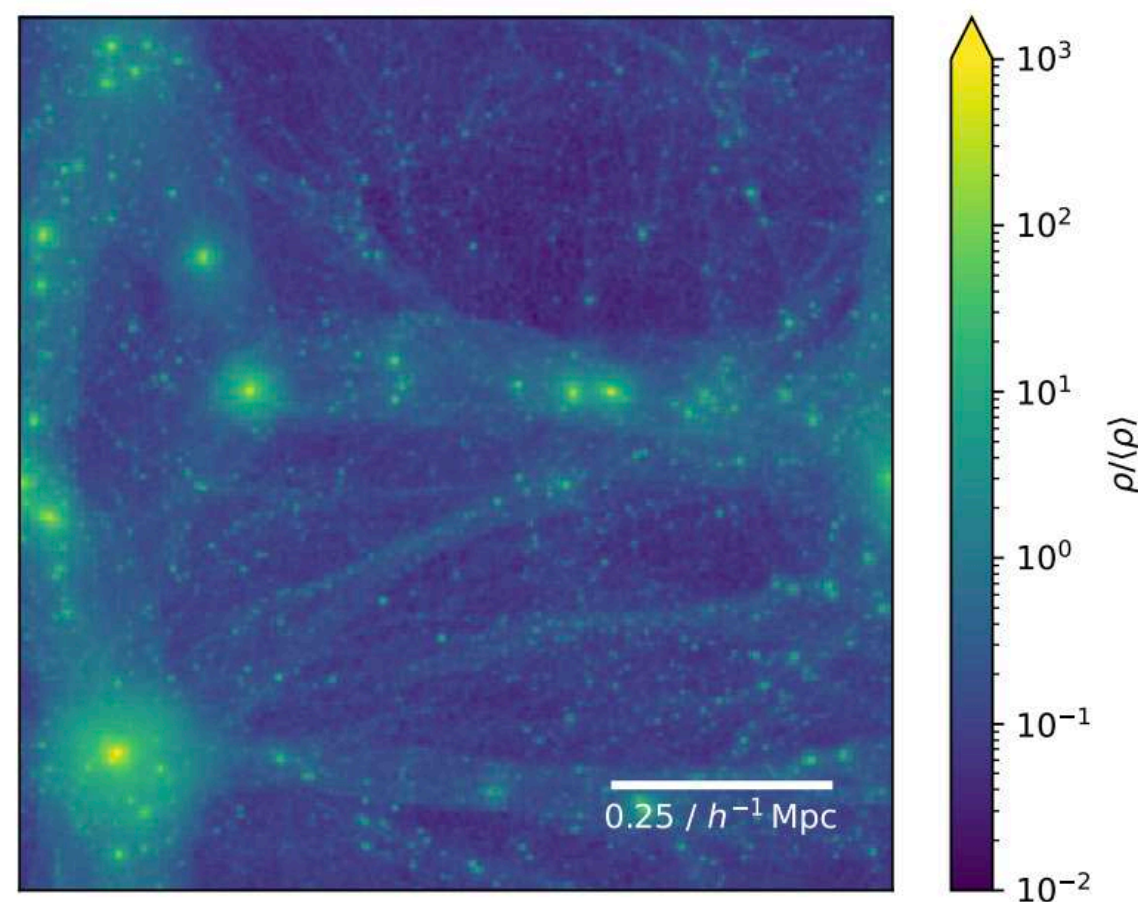
Might be interesting to the A01 (light DM) group!

Filaments in FDM

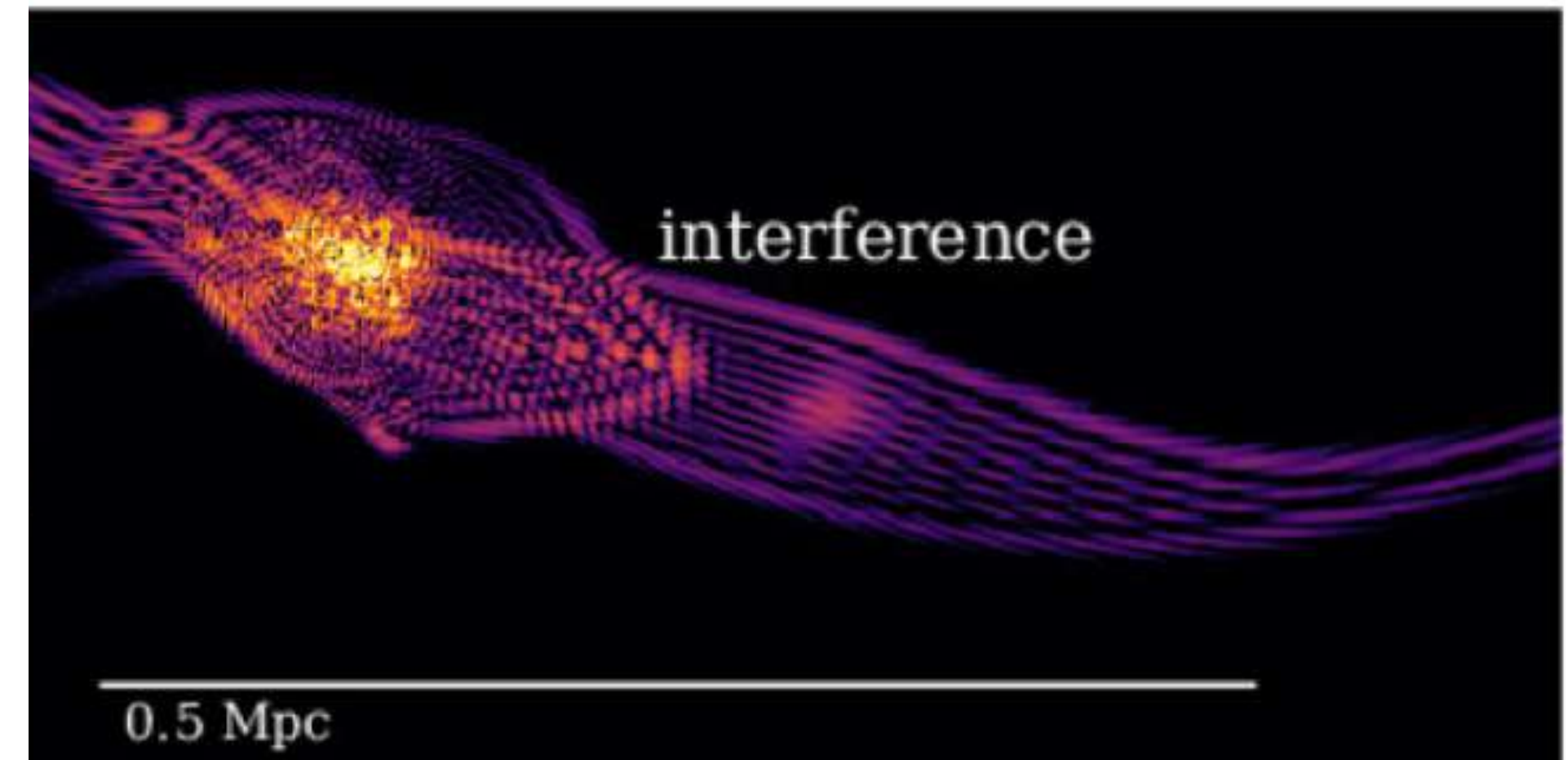
FDM: 256^3 , $mc^2 = 1.75 \times 10^{-23}$ eV, $z = 0.00$
 $v_{\max} = 88.1$ km/s



CDM: 256^3 , $z = 0.00$



S. May et al. 2021



Mocz et al. 2017

Vortices in filaments

"Cosmic Filament Spin from Dark Matter Vortices",
S. Alexander, C. Capanelli, EF, and E. McDonough (2021)

Simulations of *ULDM*

Very challenging!

Might be interesting to the C02 (simulation) group!

- Hybrid simulations: large scales (hydro) + small scales (SP-sims)
- Zoom-in
- Soliton mergers
 - Soliton oscillations
- Adding baryons



Jowett Chan

(See works from S. May & V. Springel, L. Hui, Veelmat, Niemeyer & Schwabe, Schive, Chiueh & Broadhurst, Mocz et al., ...)

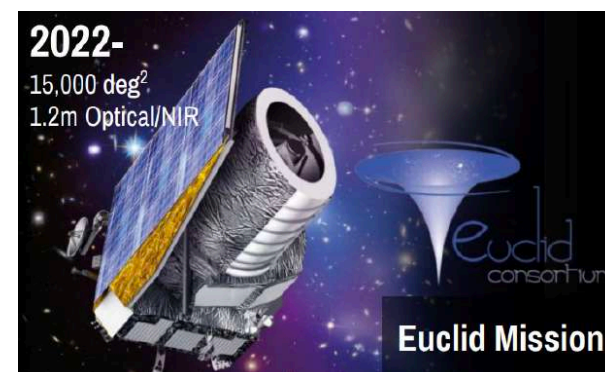
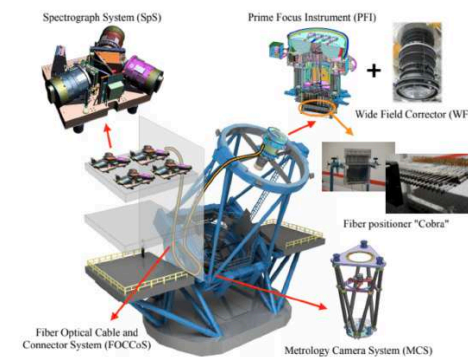
Future - signals in cosmology

Observations

Photometric and spectroscopic surveys



Prime Focus Spectrograph (PFS)



CMB

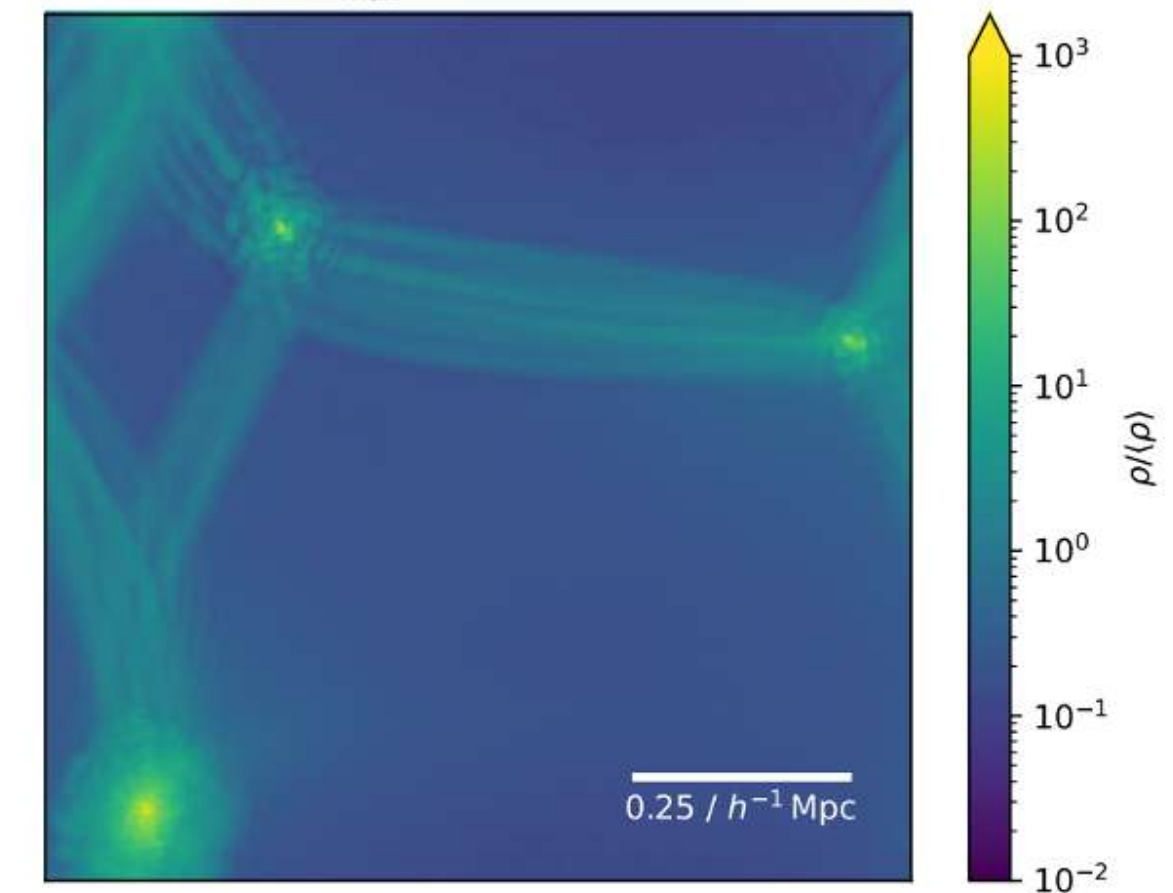


21cm



Simulations

FDM: 256^3 , $mc^2 = 1.75 \times 10^{-23}$ eV, $z = 0.00$
 $v_{\max} = 88.1$ km/s



New probes

Substructures

- strong lensing
- stellar streams

Small scale information from PS
- substructure convergence PS

Summary

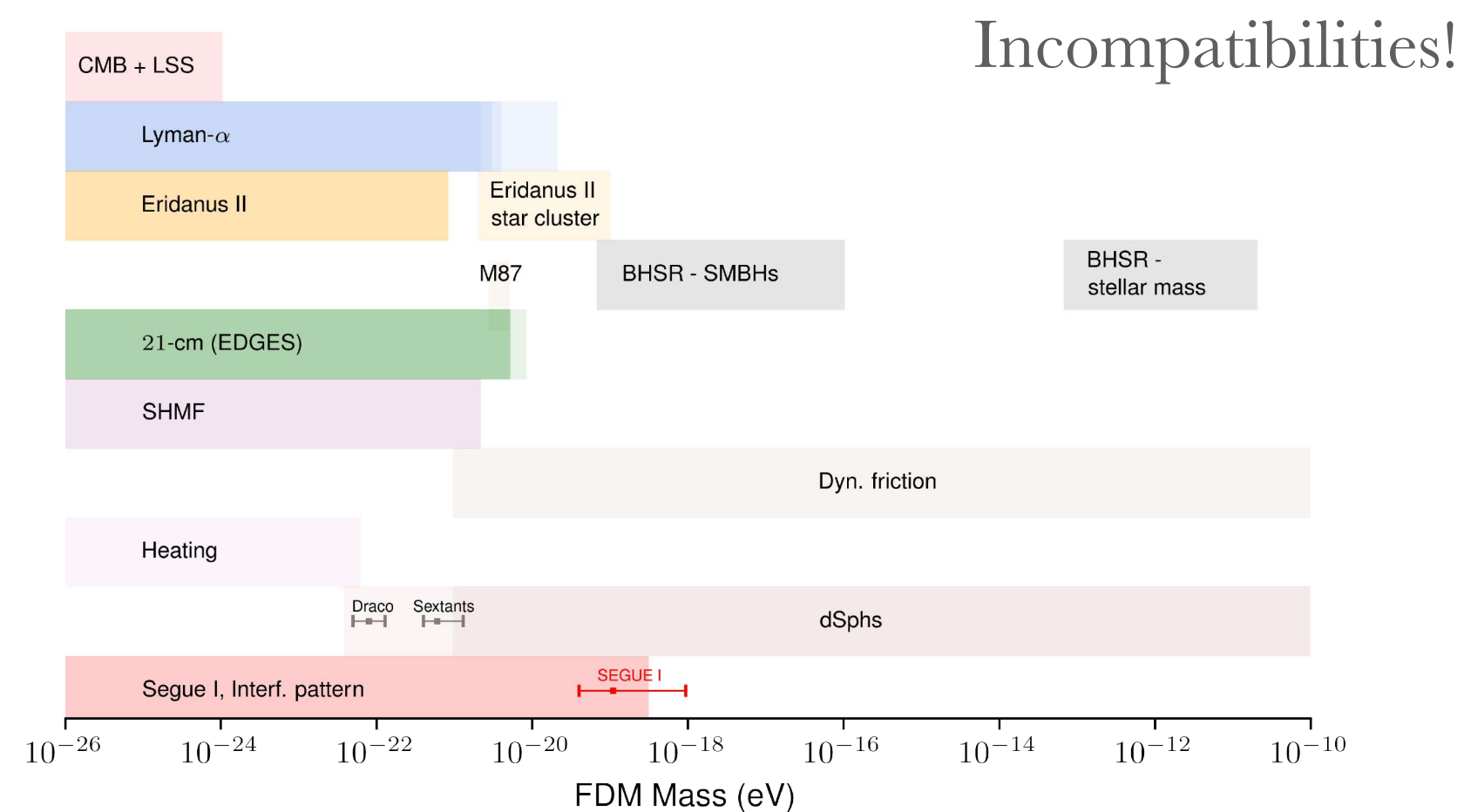
Ultra-Light Dark Matter

- Well motivated DM models
- Rich and distinct phenomenology on small scales
- Testable prediction

Small Scales

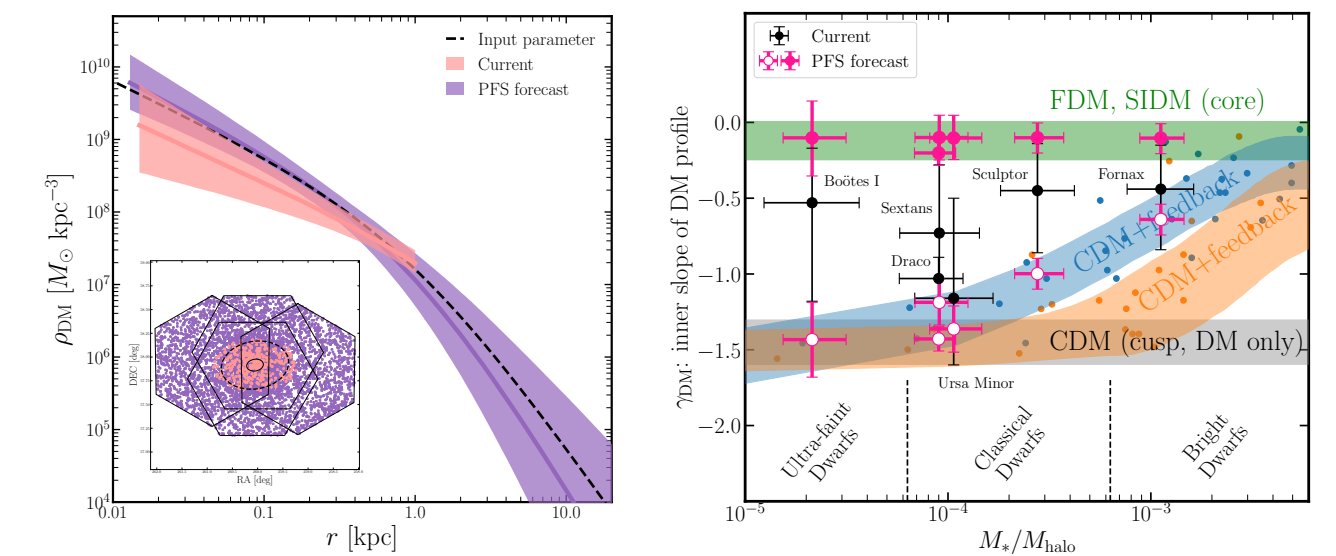
- Opportunity to probe the microphysics, particle physics properties of DM
- Small scales provide strong constraints in these models
- FDM mass being narrowed down
- Incompatibility between dwarf bounds

Current status



Future

Observations: **PFS**
PFS-GA



- Simulations: cosmological
- New observables: interference patterns and vortices
- New probes

Thank you very much!



Extra slides

Ultra-light Dark Matter

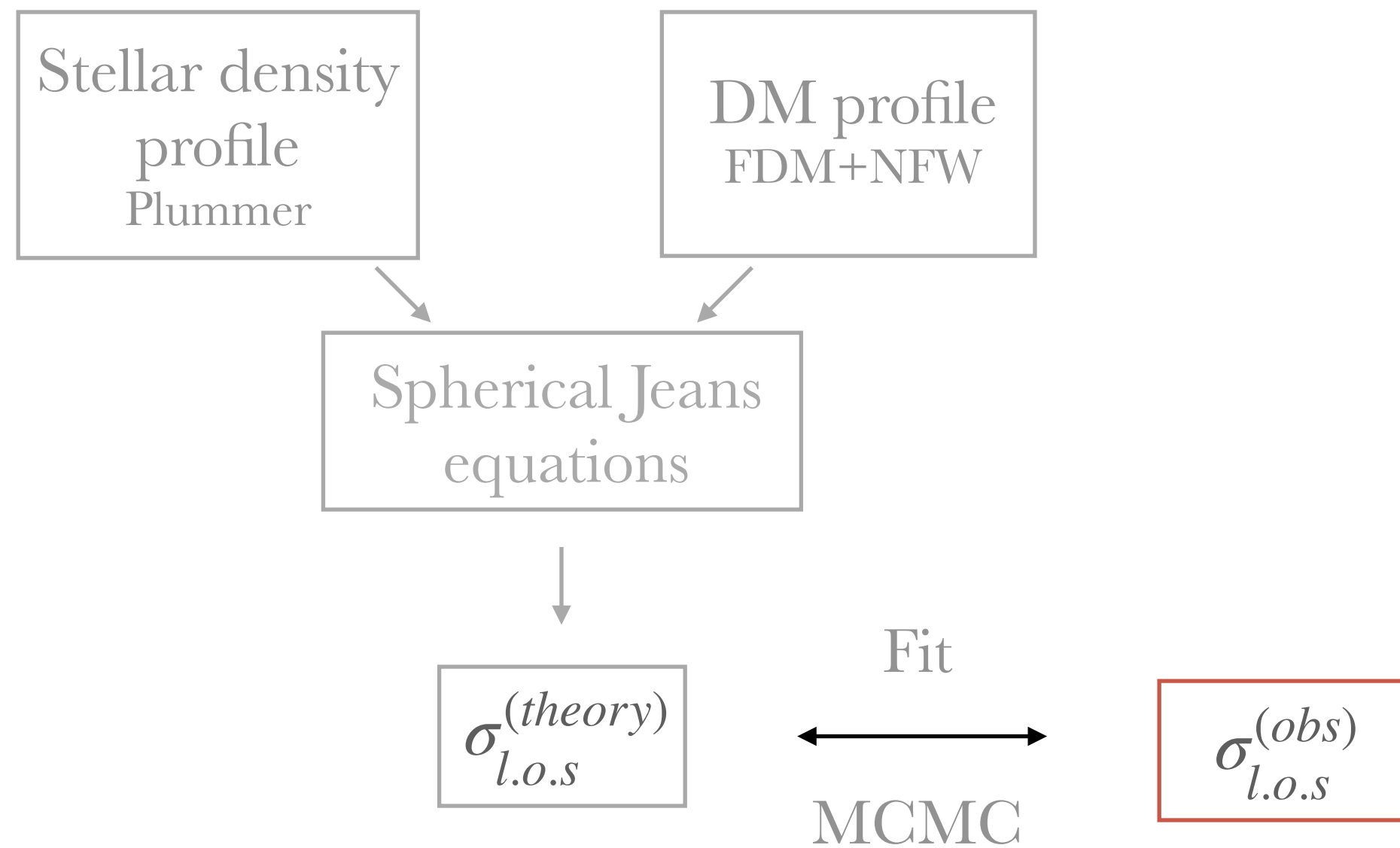
FDM mass from Ultra-faint dwarfs

Hayashi, E.F, Chan, 2021.

Ultra-faint dwarfs (UFD): ideal laboratory to study DM

Stellar kinematic data from 18 UFDs to fit the FDM profile:

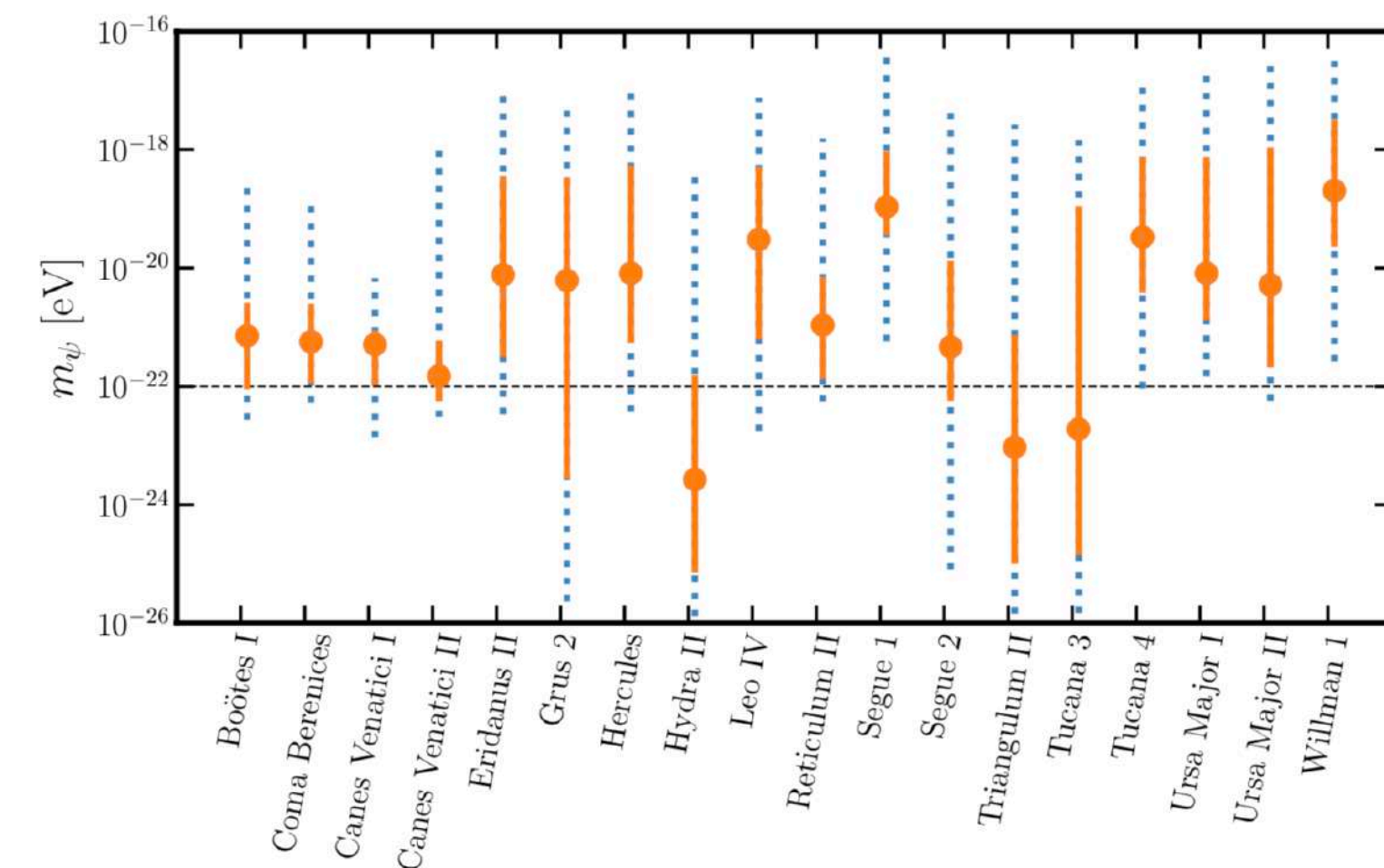
FDM SIMULATIONS



$$\rho(r) = \begin{cases} \rho_{\text{soliton}} \simeq \frac{\rho_c}{[1 + 0.091(r/r_c)^2]^8}, & r < r_c \\ \rho_{\text{NFW}} = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2}, & r > r_c \end{cases}$$

$$\rho_c(r) = 1.9 \times 10^{12} \left(\frac{m}{10^{-23} \text{ eV}} \right)^{-2} \left(\frac{r_c}{\text{pc}} \right)^{-4} [M_\odot \text{ pc}]$$

$$r_c \simeq 1600 \left(\frac{m}{10^{-23} \text{ eV}} \right)^{-1} \left(\frac{M_{\text{halo}}}{10^{12} M_\odot} \right)^{-1/3} [\text{pc}]$$



Parameter space: $\left\{ m, M_{\text{halo}}, r_c, r_s, r_\beta, \beta_0, \beta_\infty, \eta, r_h, v_{\text{sys}} \right\}$
 Velocity anisotropy

Strongest constraint on m_{FDM} to date!

FDM simulation

Spectral technique to solve the SP system

$$i\hbar\partial_t\psi_c(t, \mathbf{x}) = -\frac{\hbar^2}{2m a(t)^2}\nabla_c^2\psi_c(t, \mathbf{x}) + \frac{m}{a(t)}\Phi_c\psi_c(t, \mathbf{x})$$

$$\nabla_c^2\Phi_c(t, \mathbf{x}) = 4\pi Gm (|\psi_c(t, \mathbf{x})|^2 - \langle|\psi_c|^2\rangle(t))$$

Time evolution of the wave function

$$\Psi(\mathbf{x}, t + \Delta t) = T \exp\left[-\frac{i\Delta t}{\hbar} \int dt' \left(-\frac{\hbar^2}{2m}\nabla^2 + mV(\mathbf{x}, t')\right)\right] \Psi(\mathbf{x}, t)$$

Small Δt :

$$\Psi(\mathbf{x}, t + \Delta t) = \exp\left(\frac{i\hbar\Delta t}{2m}\nabla^2 - \frac{im\Delta t}{2\hbar}V(\mathbf{x}, t + \Delta t) - \frac{im\Delta t}{2\hbar}V(\mathbf{x}, t)\right) \Psi(\mathbf{x}, t),$$

Split into 3 operations (Baker-Campbell-Hausdorff formula)

$$\Psi(\mathbf{x}, t + \Delta t) = \exp\left(-\frac{im\Delta t}{2\hbar}V(\mathbf{x}, t + \Delta t)\right) \exp\left(\frac{i\hbar\Delta t}{2m}\nabla^2\right) \exp\left(-\frac{im\Delta t}{2\hbar}V(\mathbf{x}, t)\right) \Psi(\mathbf{x}, t)$$

Operator Splitting Spectral Method

$$\psi_c^{n+1} \approx \underbrace{e^{i\Phi_c \Delta t/2}}_{3^{\text{rd}}} \underbrace{\mathcal{F}^{-1} \left[e^{ik^2 \Delta t} \mathcal{F}^{-1} \left[e^{i\Phi_c \Delta t/2} \psi_c^n \right] \right]}_{2^{\text{nd}}} \underbrace{\left[\right]}_{1^{\text{st}}}$$

$$\Delta t \sim \Delta x^2$$

Timestep criteria

FDM simulation

Spectral technique to solve the SP system

$$i\hbar\partial_t\psi_c(t, \mathbf{x}) = -\frac{\hbar^2}{2m a(t)^2} \nabla_c^2\psi_c(t, \mathbf{x}) + \frac{m}{a(t)}\Phi_c\psi_c(t, \mathbf{x})$$
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$$\Delta t \sim \Delta x^2$$

Timestep criteria

FDM simulation

The fields ψ and Φ are discretised on a uniform Cartesian mesh with N^3 grid points - allow numerical computations using Fast Fourier transform. It follows the operations:

- Calculate the potential

- $\psi_c \leftarrow e^{-i \frac{m}{\hbar} \frac{1}{a} \frac{\Delta t}{2} \Phi_c} \psi_c$ (kick) (20a)

- $\psi_c \leftarrow \text{FFT}^{-1} \left(e^{-i \frac{\hbar}{m} \frac{1}{a^2} \frac{\Delta t}{2} k^2} \text{FFT}(\psi_c) \right)$ (drift) (20b)

- $\Phi_c \leftarrow \text{FFT}^{-1} \left(-\frac{1}{k^2} \text{FFT} \left(4\pi G m \left(|\psi_c|^2 - \langle |\psi_c|^2 \rangle \right) \right) \right)$
(update potential) (20c)

- $\psi_c \leftarrow e^{-i \frac{m}{\hbar} \frac{1}{a} \frac{\Delta t}{2} \Phi_c} \psi_c$ (kick) (20d)

- Go to step (20a) (20e)

Schrödinger-Poisson system

$$i\hbar\partial_t\psi_c(t, \mathbf{x}) = -\frac{\hbar^2}{2m a(t)^2} \nabla_c^2 \psi_c(t, \mathbf{x}) + \frac{m}{a(t)} \Phi_c \psi_c(t, \mathbf{x})$$

$$\nabla_c^2 \Phi_c(t, \mathbf{x}) = 4\pi G m \left(|\psi_c(t, \mathbf{x})|^2 - \langle |\psi_c|^2 \rangle(t) \right)$$

May et al. 2020

Steps (20a) to (20e) implemented as a module in the AREPO code

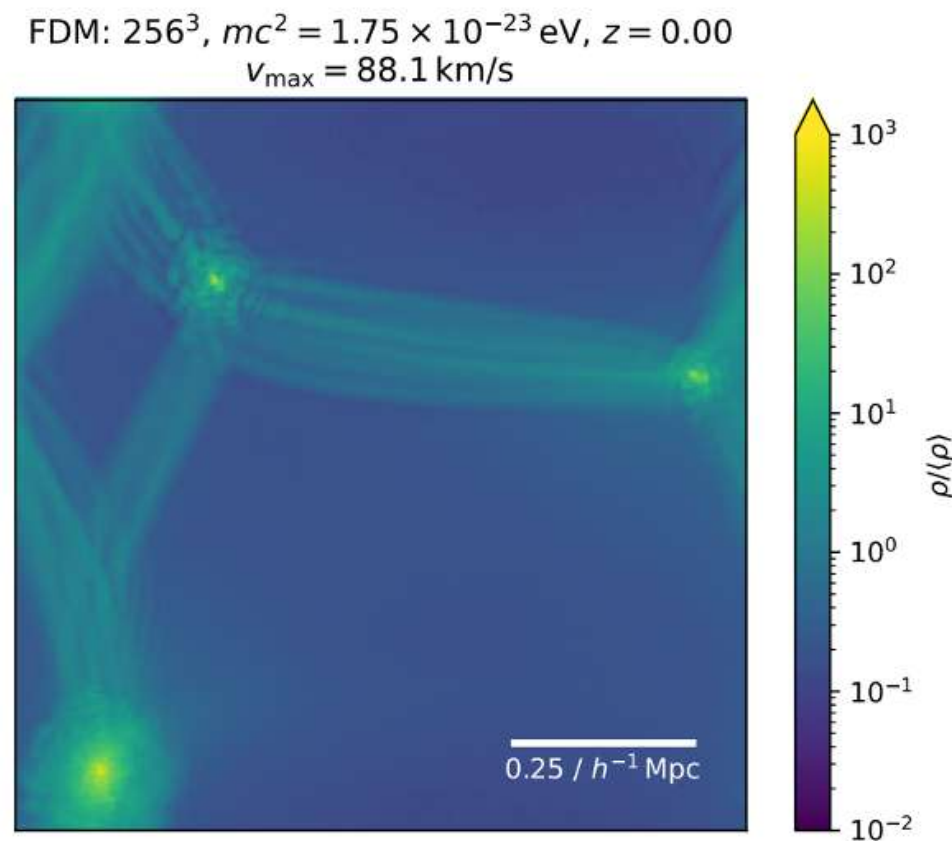
Jowett

Own implementation

FDM simulation

May et al 2020: Box size and resolution

Largest three-dimensional cosmological simulations of FDM structure formation to low redshifts



Type	Res. el.	L / h^{-1} Mpc	mc^2 / eV	Resolution
FDM	8640^3	10	7×10^{-23}	$1.16 h^{-1}$ kpc
FDM	4320^3	10	$(3.5, 7) \times 10^{-23}$	$2.31 h^{-1}$ kpc
FDM	3072^3	10	$(3.5, 7) \times 10^{-23}$	$3.26 h^{-1}$ kpc
FDM	2048^3	10	$(3.5, 7) \times 10^{-23}$	$4.88 h^{-1}$ kpc
FDM	4320^3	5	7×10^{-23}	$1.16 h^{-1}$ kpc
FDM	3072^3	5	$(3.5, 7) \times 10^{-23}$	$1.63 h^{-1}$ kpc
FDM	2048^3	5	$(3.5, 7) \times 10^{-23}$	$2.44 h^{-1}$ kpc
FDM	1024^3	5	$(3.5, 7) \times 10^{-23}$	$4.88 h^{-1}$ kpc
CDM	2048^3	10	—	$9.69 \times 10^3 h^{-1} M_{\odot}$
CDM	1024^3	10	—	$7.75 \times 10^4 h^{-1} M_{\odot}$
CDM	512^3	10	—	$6.20 \times 10^5 h^{-1} M_{\odot}$
CDM	1024^3	5	—	$9.69 \times 10^3 h^{-1} M_{\odot}$
CDM	512^3	5	—	$7.75 \times 10^4 h^{-1} M_{\odot}$

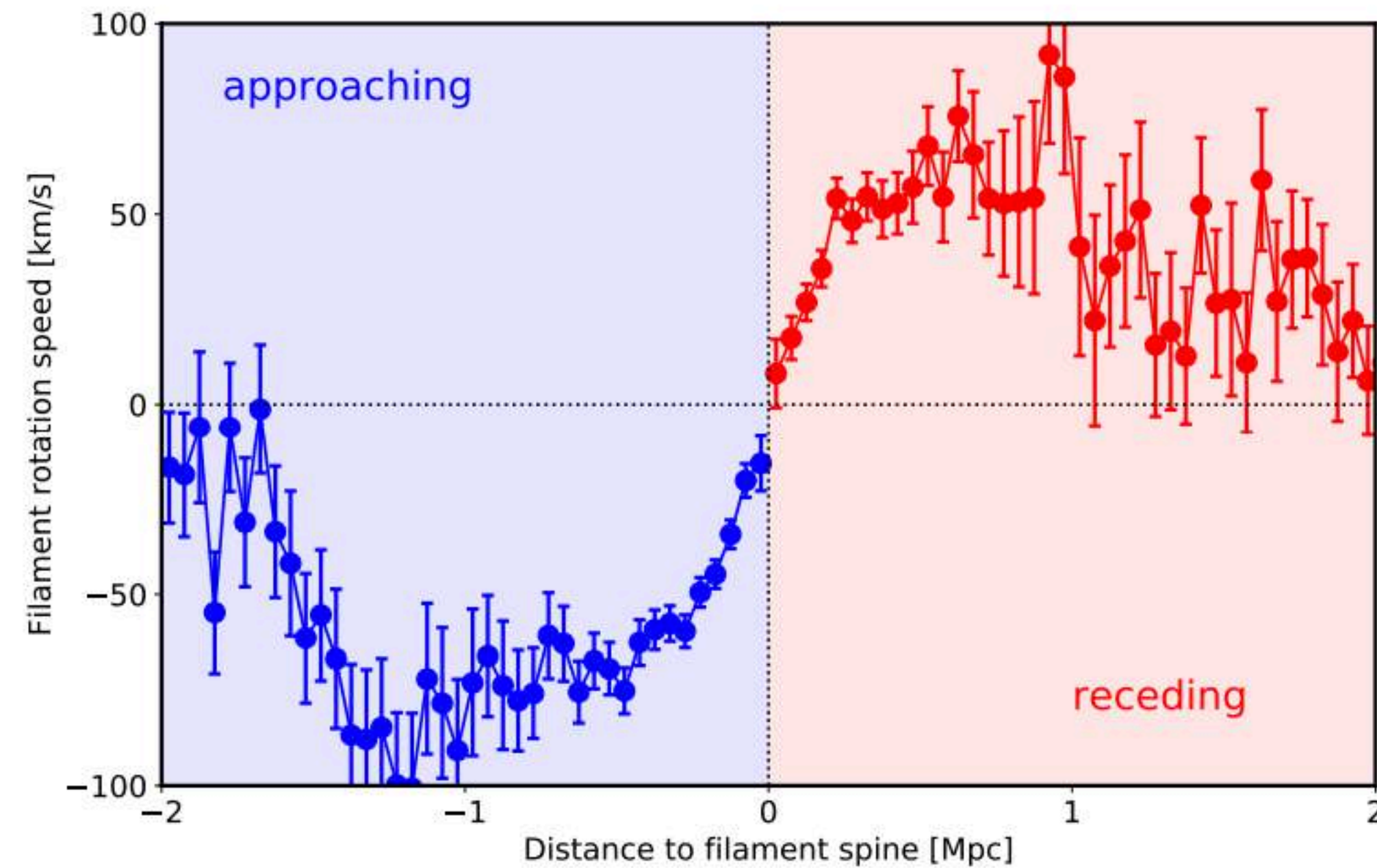
Table 1. List of performed simulations with important characteristics. The lengths given for the box sizes and resolutions are comoving.

Simulations: $\{\Omega_m = 0.3, \Omega_b = 0, \Omega_{\Lambda} = 0.7, H_0 = 70 \text{ km s}^{-1} (h = 0.7), \sigma_8 = 0.9\}$

IC: $z = 127$

Rotation of filaments: vortices

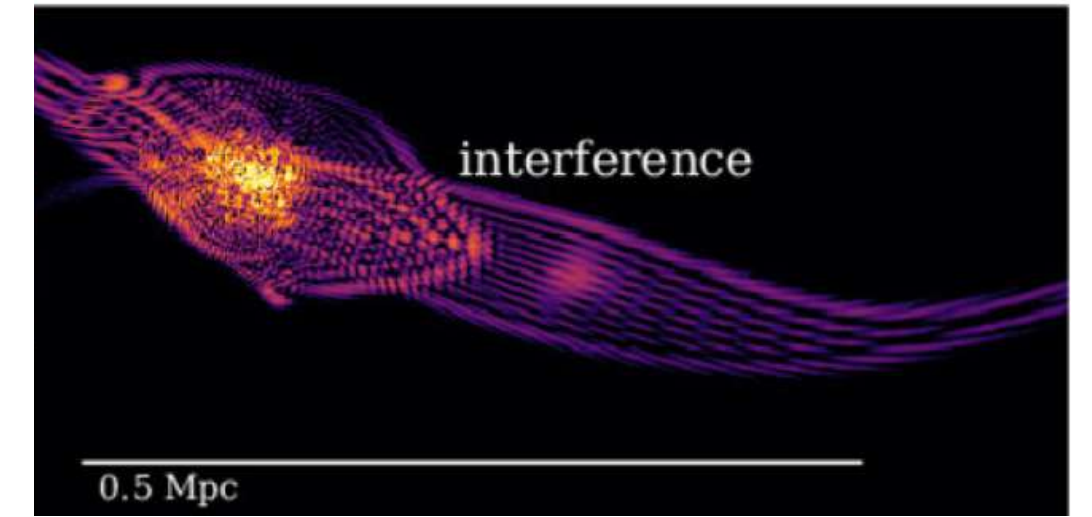
Peng Wang, Noam I. Libeskind, Elmo Tempel, Xi Kang, Quan Guo, "*Possible observational evidence that cosmic filaments spin*", Nature Astronomy (2021)



- Stacking thousands of filaments and examining the velocity of galaxies perpendicular to the filament's axis (via their red and blue shift)
- Found that filaments display motion consistent with rotation → largest objects known to have angular momentum

Rotation of filaments: vortices

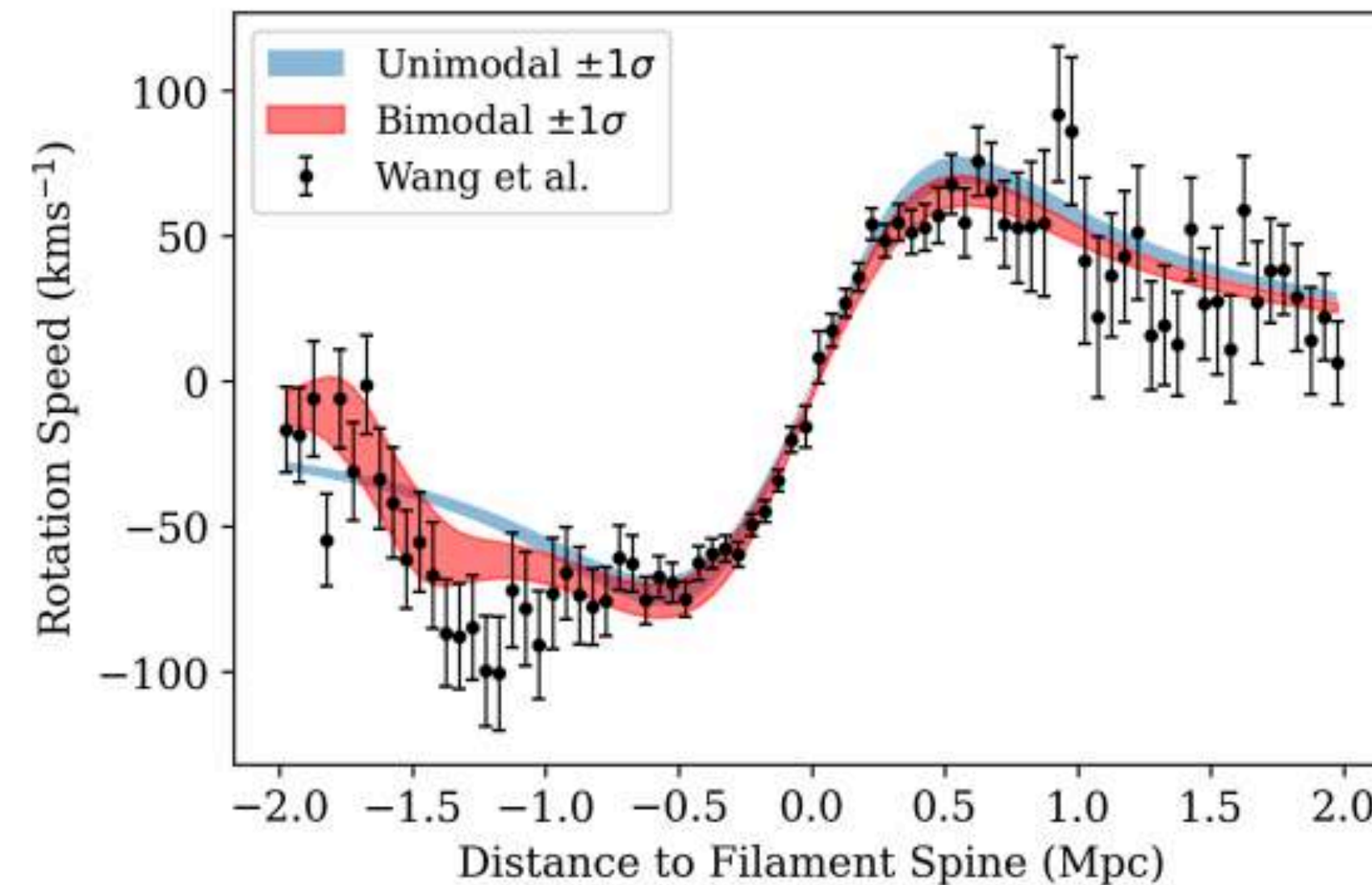
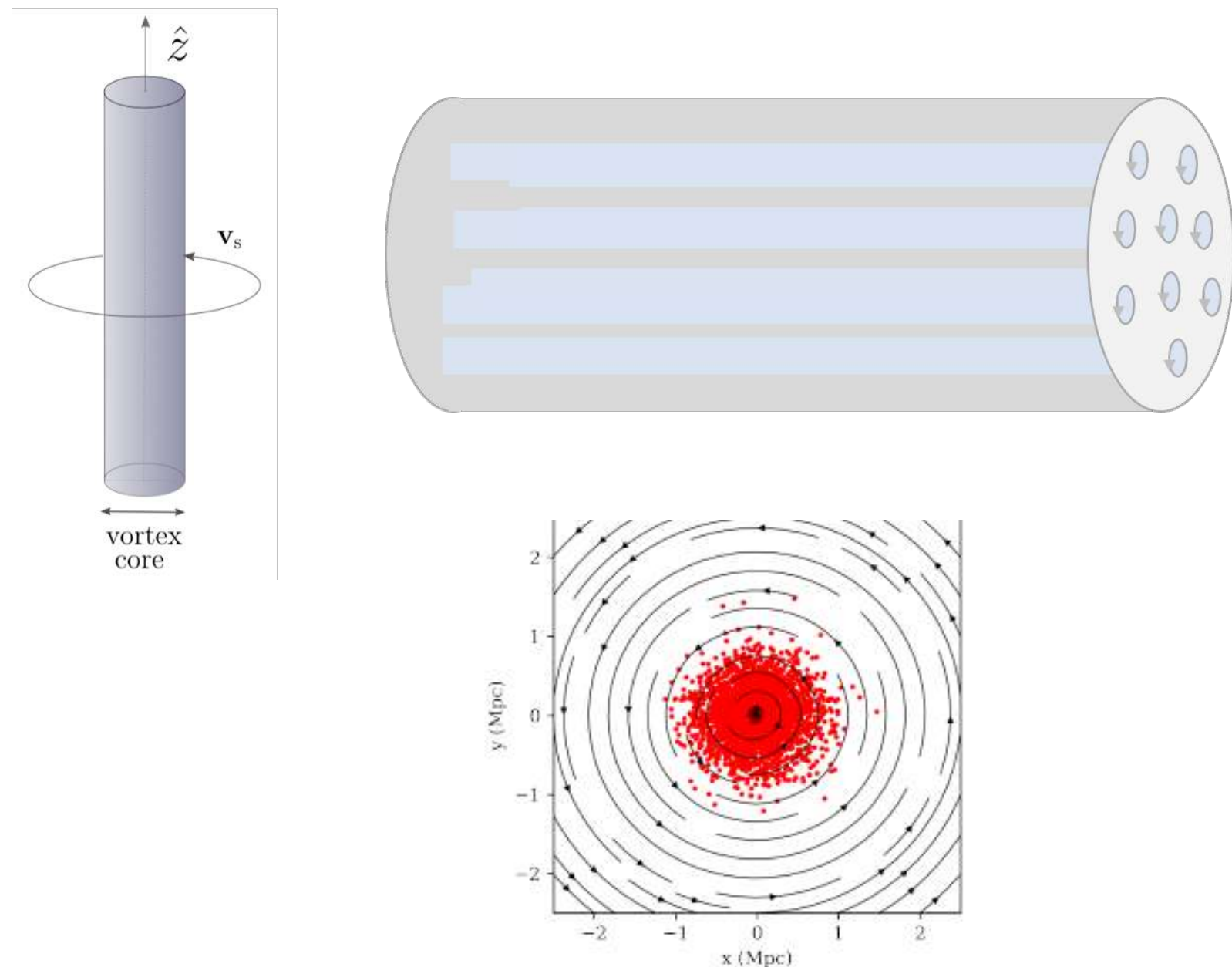
- Not clear that we can get spinning cosmic filaments in LCDM
 - Seems to be difficult to theoretically explain the acquisition of angular momentum on megaparsec scales
 - Some simulations seem to be finding spinning cosmic filaments



Mocz et al. 2017

"Cosmic Filament Spin from Dark Matter Vortices", Stephon Alexander, Christian Capanelli, Elisa G. M. Ferreira, and Evan McDonough (2021)

- Suggest that a collection of (dark) vortices enclosed in a cylindrical volume aligned with the axis of a filament are able to generate rotations at the Mpc scale and reproduce the result of Wang et al (2021)

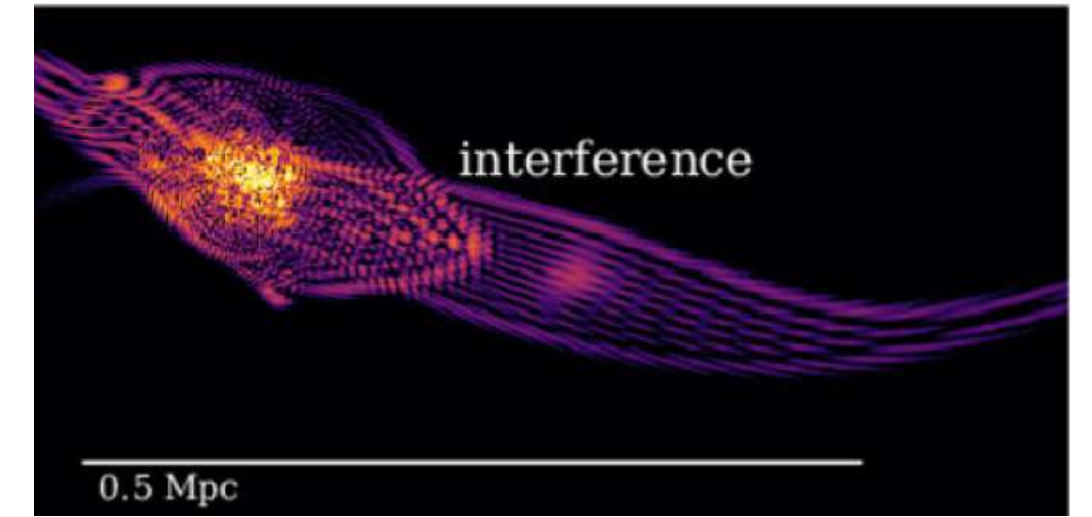


$$R = 0.51_{0.02}^{+0.02} \text{ Mpc}$$

$$\frac{N_V}{m} = 2.9_{-0.2}^{+0.2} \text{ eV}^{-1}$$

Independent on the formation mechanism of these vortices!

Rotation of filaments: vortices

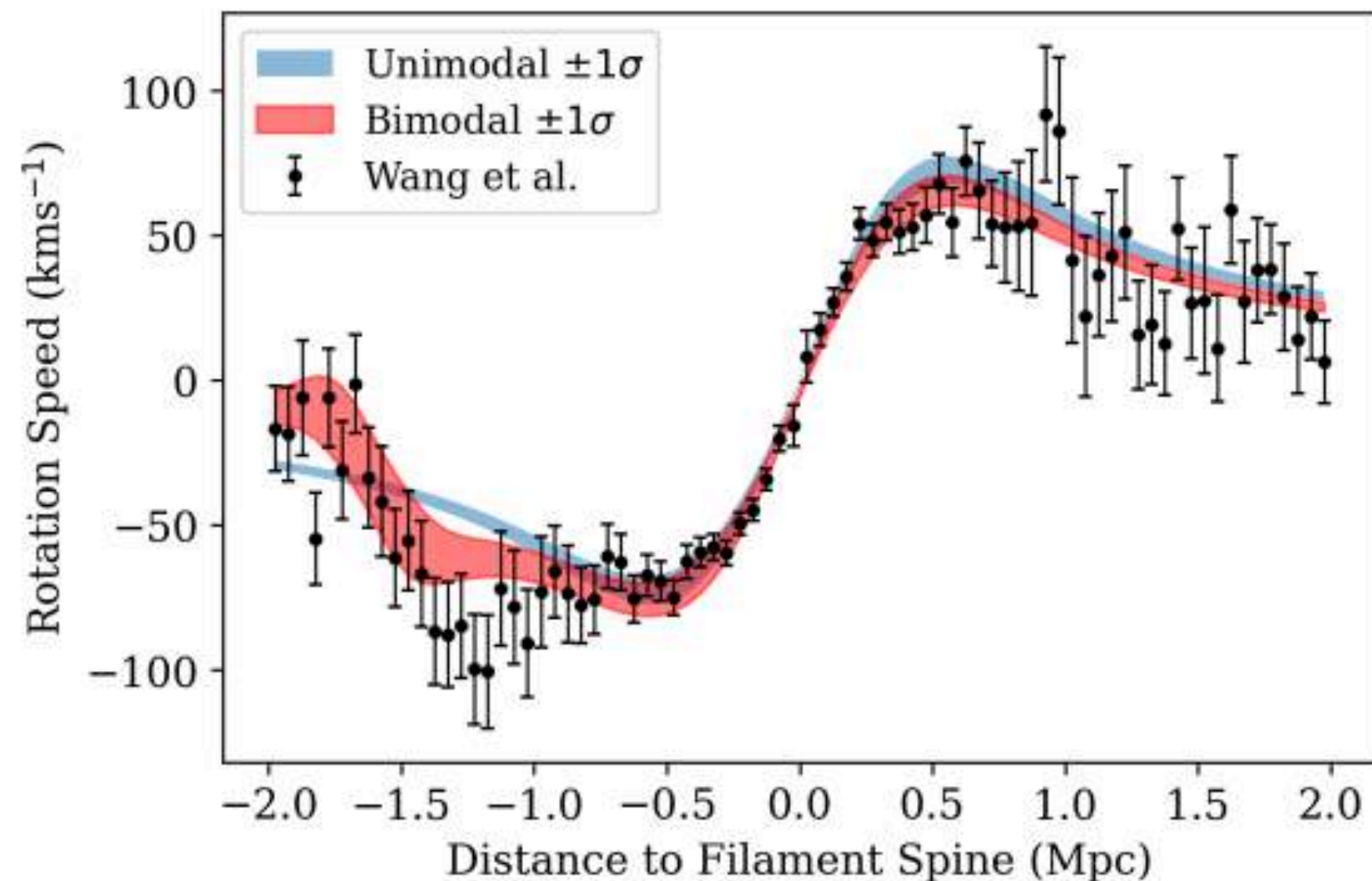


Mocz et al. 2017

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$$R = 0.51_{0.02}^{+0.02} \text{ Mpc}$$

$$\frac{N_V}{m} = 2.9_{-0.2}^{+0.2} \text{ eV}^{-1}$$

For example, for a $m \sim 10^{-22} \text{ eV} \longrightarrow N_V \sim 3000$

Possible formation mechanisms:

- in regions where the density vanishes (*Hui et al 2020*, *Lague et al 2020*)
- Transfer of angular momentum (*Berezhiani, 2015*)

Compatible with those!

* In CDM - formation of vortices