

Modularity of BPS indices on Calabi-Yau threefolds (Boris Pioline)

Tuesday, 14 February 2023 09:30 (1h 30m)

Unlike in cases with maximal or half-maximal supersymmetry, the spectrum of BPS states in type II string theory compactified on a Calabi-Yau threefold with generic $SU(3)$ holonomy remains partially understood. Mathematically, the BPS indices coincide with the generalized Donaldson-Thomas invariants associated to the derived category of coherent sheaves, but they are rarely known explicitly. String dualities indicate that suitable generating series of rank 0 Donaldson-Thomas invariants counting D4-D2-D0 bound states should transform as vector-valued mock modular forms, in a precise sense. I will spell out and test these predictions in the case of one-modulus compact Calabi-Yau threefolds such as the quintic hypersurface in P^4 , where rank 0 DT invariants can (at least in principle) be computed from Gopakumar-Vafa invariants, using recent mathematical results by S. Feyzakhsh and R. Thomas.