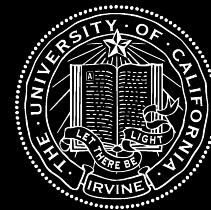


Bounds on Long-lived Dark Matter Mediators from Neutron Stars

Thong. T.Q. Nguyen^{1,2,}

In collaboration with Tim M.P. Tait³
arXiv:2212.12547 and 23xx.xxxx

1. Institute of Physics, Academia Sinica
2. Sorbonne University, Jussieu, Paris, France
3. Department of Physics and Astronomy, University of California, Irvine



Workshop on Very Light Dark Matter 2023

Outline

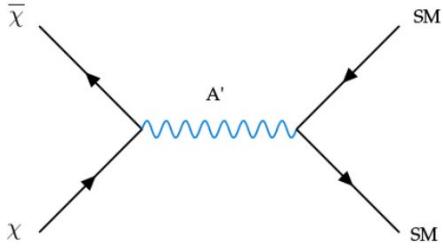
Neutron Stars in
Galactic Center.

Preview: Dark Matter
Detections

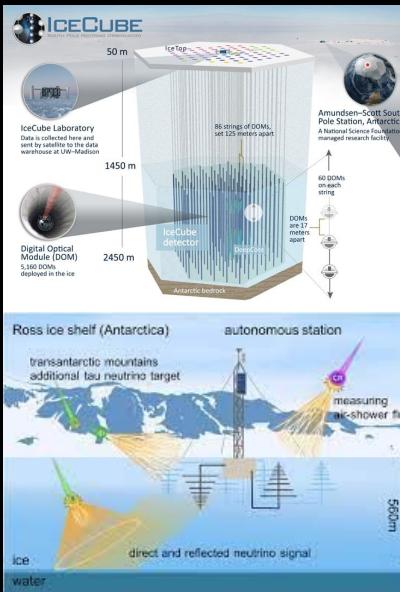


Available on Amazon!

Free High Energy Colliders!!



IceCube



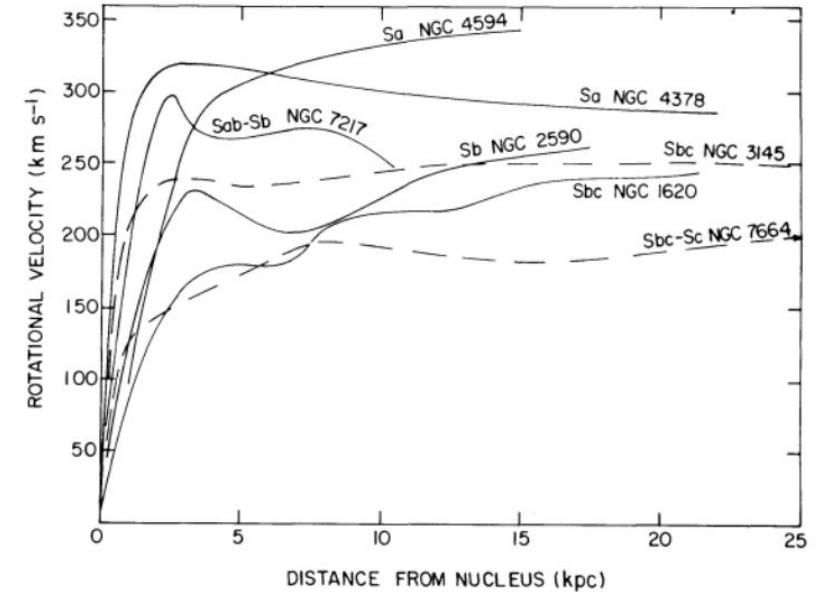
ARIA

→ New bounds:
 $\sigma_{\chi n}(m_\chi)$

arXiv:2212.12547

Why Dark Matter?

	mass → $\approx 2.3 \text{ MeV}/c^2$	charge → 2/3	spin → 1/2
QUARKS	u	c	t
	up	charm	top
GAUGE BOSONS			
d	s	b	g
down	strange	bottom	gluon
e	μ	τ	γ
electron	muon	tau	photon
ν_e	ν_μ	ν_τ	Z boson
electron neutrino	muon neutrino	tau neutrino	W boson
LEPTONS			



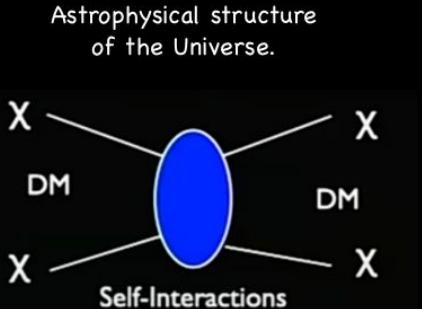
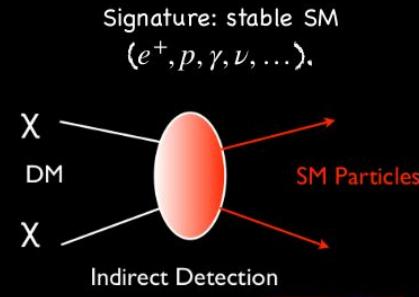
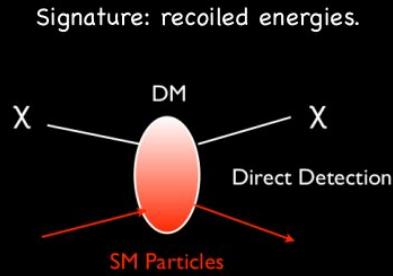
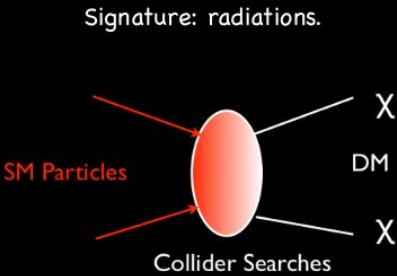
$$v(r) = \sqrt{\frac{G_N M(r)}{r}}$$

Dark Matter interactions: via Gravity and ???

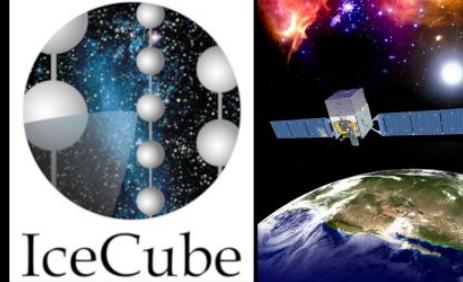
Assumption!!!



Dark Matter Detection Methods



$$\sigma_{\chi n}$$

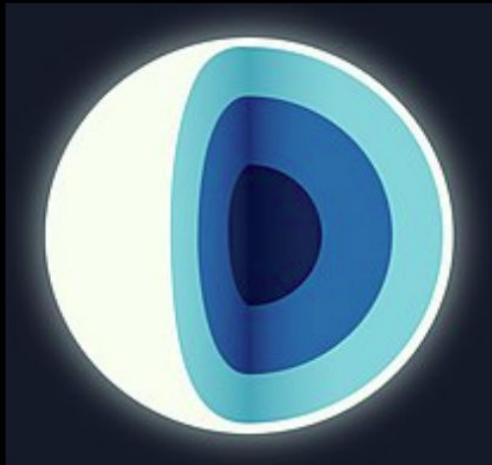


$$\langle \sigma_{\chi\chi} \rangle$$

Van Que Tran, Thong T.Q. Nguyen,
Tim M.P. Tait, Tzu-Chiang Yuan, in preparation

$$\sigma_{\chi n} \quad \text{arXiv:2212.12547}$$

Neutron Stars in Galactic Center



$$m_n = 1 \text{ GeV} \quad M \simeq 1.5M_\odot \quad R_\star \simeq 10 \text{ km}$$

Escape velocity: $v_{\text{esc}} \simeq 2 \times 10^5 \text{ km/s}$

Saturation Cross Section:

$$\sigma_{\text{sat}} = \pi R_n^2 / N_n \approx 1.87 \times 10^{-45} \text{ cm}^2$$

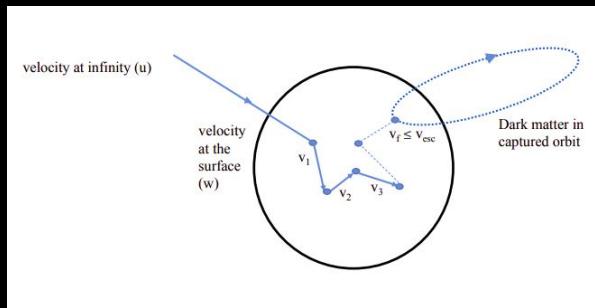
Neutron Star's number density¹ in Galactic Center:

$$n_{\text{ns}}(r) = 5.98 \times 10^3 \left(\frac{r}{1\text{pc}} \right)^{-1.7} \text{ pc}^{-3} \quad (0.1\text{pc} < r < 2\text{pc})$$

$$= 2.08 \times 10^4 \left(\frac{r}{1\text{pc}} \right)^{-3.5} \text{ pc}^{-3} \quad (r > 2\text{pc}).$$

Dark matter captured by neutron stars

Basudeb Dasgupta, Arita Gupta, Anupam Ray, JCAP 08 (1906.04204)



$v_f \leq v_{\text{esc}} \Rightarrow \text{Captured!}$

Dark Matter Capture Rate after Nth times [GeV]:

$$C_N = \frac{\pi R_\star p_N(\tau)}{1 - 2G_N M_\star / R_\star} \frac{\sqrt{6} n_\chi}{3\sqrt{\pi}\bar{v}} \times \left[2\bar{v}^2 + 3v_{\text{esc}}^2 - (2\bar{v}^2 + 3v_N^2) \exp\left(-\frac{3(v_N^2 - v_{\text{esc}}^2)}{2\bar{v}^2}\right) \right]$$

- DM velocity dispersion: \bar{v} .
- DM velocity (Nth-time scattering): v_N .
- DM density profile: n_χ .

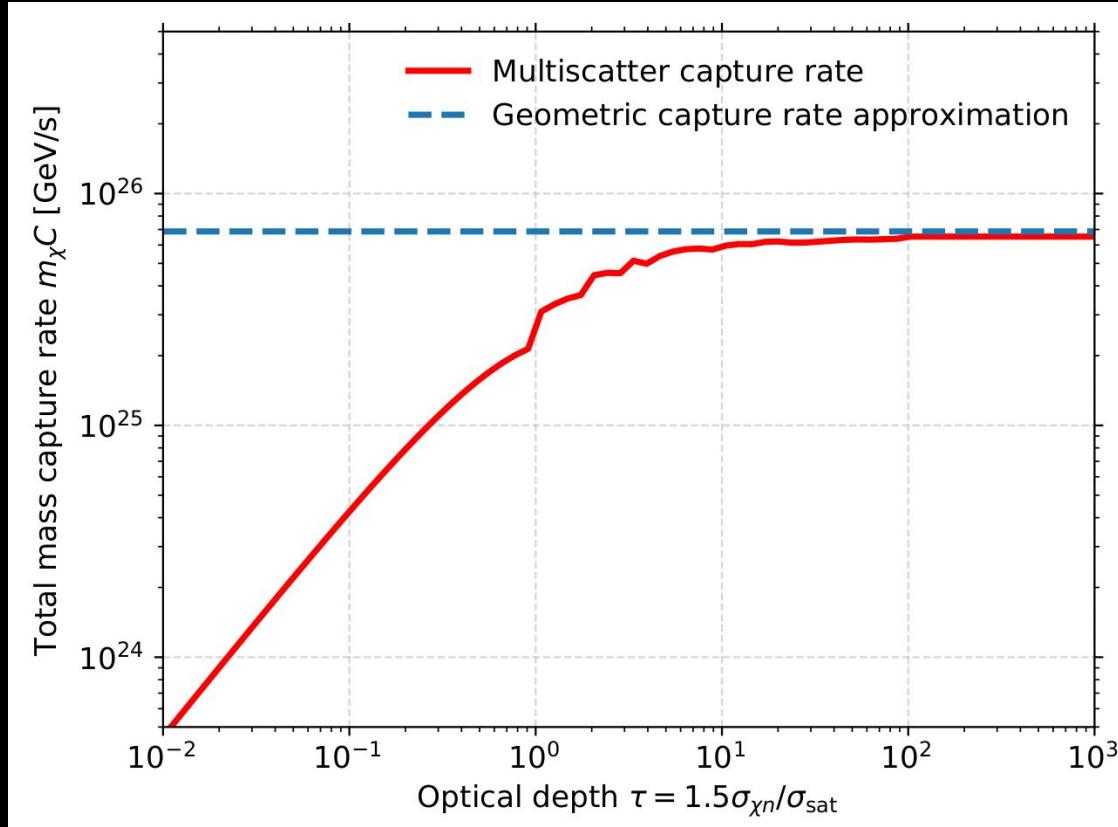
• Probability scattering N-time:

$$p_N(\tau) = 2 \int_0^\infty dy \frac{ye^{-y\tau}(y\tau)^N}{N!}.$$

Optical Depth: $\tau = 1.5 \frac{\sigma_{\chi n}}{\sigma_{\text{sat}}} \longrightarrow \begin{array}{l} \text{DM model.} \\ \text{Celestial object.} \end{array}$

$$\text{Capture rate (1 NS): } C = \sum_{N=1}^{\infty} C_N.$$

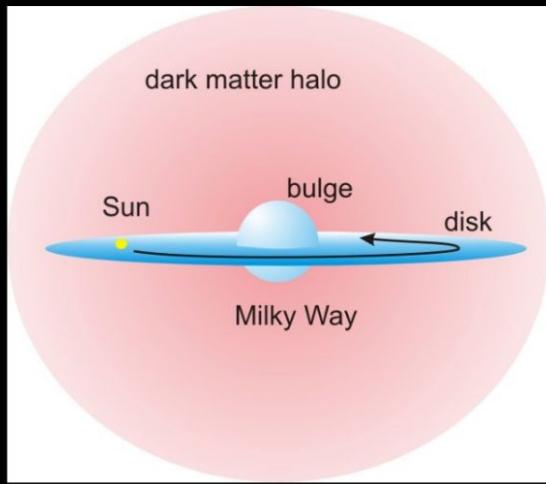
$$\text{Total capture rate (All NSs): } C_{\text{tot}} = 4\pi \int_{r_1=0.1\text{pc}}^{r_2=100\text{pc}} r^2 n_{\text{ns}} C dr.$$



$$C_{\max} = \pi R^2 n_\chi(r) v_0 \left(1 + \frac{3}{2} \frac{v_{\text{esc}}^2}{\bar{v}(r)^2} \right) \xi(v_p, \bar{v}(r)),$$

Milky Way Galaxy

(Credit: <https://scienceblogs.com>)



Y. Sofue, *Publ.Astron.Soc.Jap.* 65 (1307.8241)

Mass Component	Total mass (M_{\odot})	Scale radius (kpc)	Center density ($M_{\odot} \text{ pc}^{-3}$)
Black hole	4×10^6	—	—
Inner bulge (core)	5×10^7	0.0038	3.6×10^4
Main Bulge	8.4×10^9	0.12	1.9×10^2
Disk	4.4×10^{10}	3.0	15
Dark halo	5×10^{10}	$h = 12.0$	$\rho = 0.011$

$$M(r) = M_{\text{BH}} + 4\pi \int_0^r (\rho_{\text{inner}} + \rho_{\text{outer}} + \rho_{\text{disk}} + \rho_{\chi}) r^2 dr,$$

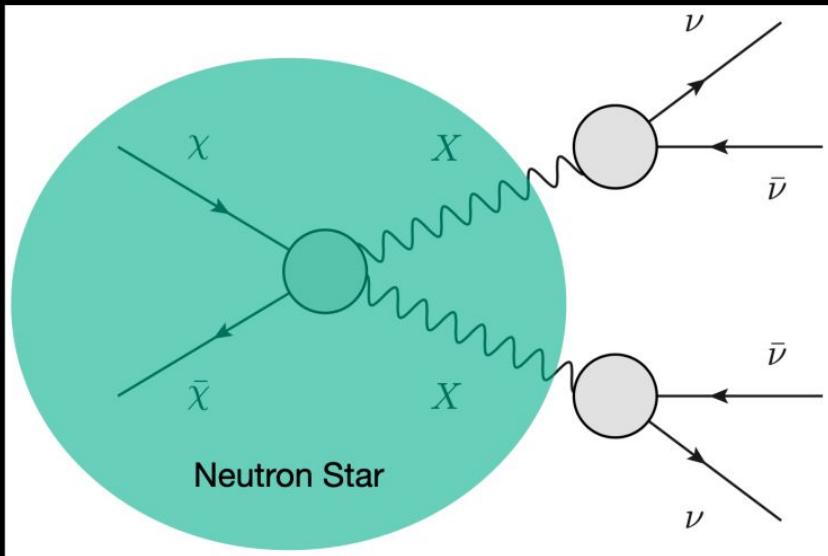
$$\text{DM velocity dispersion: } \bar{v}(r) = \sqrt{\frac{3}{2}} v_c(r) = \sqrt{\frac{3}{2}} \sqrt{\frac{G_N M(r)}{r}}.$$

$$\rho_{\chi}(r) = \rho_{\text{NFW}}(r) = m_{\chi} n_{\chi}(r) = \frac{\rho_0}{(r/r_s)^{\gamma} (1+r/r_s)^{3-\gamma}}.$$

- ⊗ $\rho_0 = 0.42 \text{ GeV/cm}^3$.
- ⊗ $r_s = 12.0 \text{ kpc}$.

⊗ γ : Inner Slope (1-1.5).

Dark Matter annihilation in NS



$$\eta = m_\chi / m_X$$

$$L = \eta c \tau_X \geq R_\star$$

Neutron Stars in GC are expected to be old!!
Annihilation rate: $\Gamma_{\text{ann}} \rightarrow \frac{\Gamma_{\text{cap}}}{2} = \frac{C_{\text{total}}}{2}$

Number of DM e.o.m:

$$\frac{dN(t)}{dt} = C_{\text{total}} - C_A N(t)^2$$

Solution:

$$N(t) = \sqrt{C_{\text{total}}/C_A} \tanh \frac{t}{t_{\text{eq}}}$$

Equilibrium time scale:

$$t_{\text{eq}} = 1/\sqrt{C_A C_{\text{total}}}$$

$$C_A = \frac{\langle \sigma_A v \rangle}{V_\star}$$

Observable: Differential Energy Flux

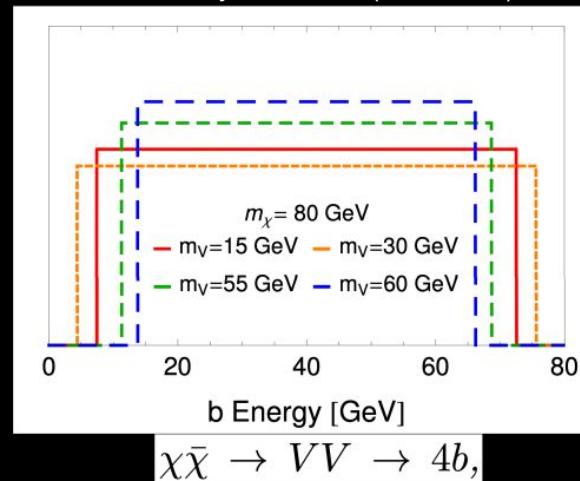
Differential Energy Flux (measured by ID Experiments):

$$E^2 \frac{d\Phi}{dE} = \frac{\Gamma_{\text{ann}}}{4\pi D^2} \times E^2 \frac{dN}{dE} \times \text{BR}(X \rightarrow \text{SM}) \times P_{\text{surv}}. \quad [\text{GeV cm}^{-2} \text{ s}^{-1}]$$

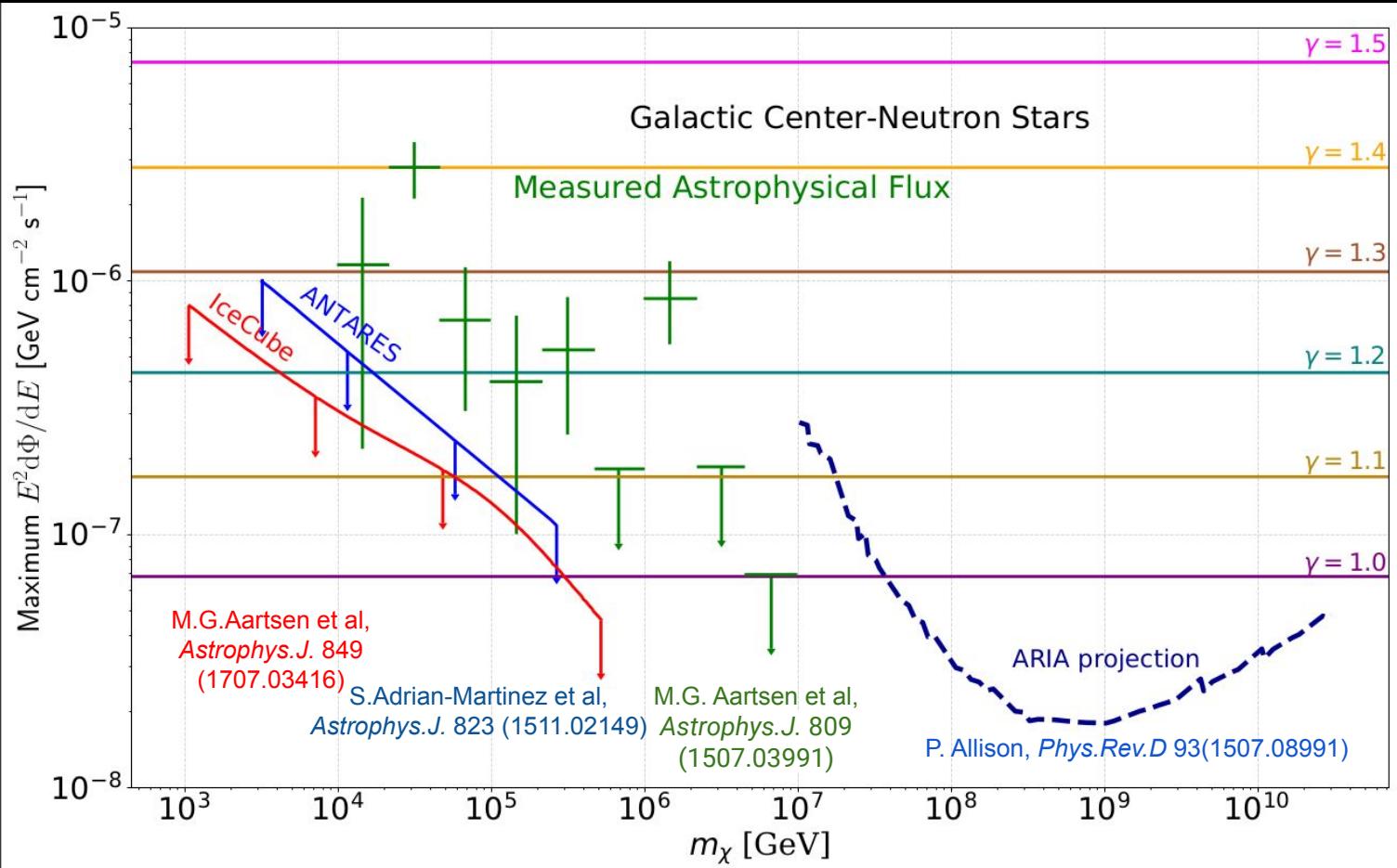
M. Abdullah, A. DiFanzo, A. Rajaraman, T.M.P. Tait, P. Tanedo, *Phys.Rev.D* 90 ([1404.6528](#))

- D : Average distance from GC to detectors (Earth).
- dN/dE : Signal (neutrino) spectrum.
- Signal surviving probability: $P_{\text{surv}} = e^{-R_\star/L} - e^{-D/L}$.
- Limit: $L \leq D \approx 8.0$ kpc.

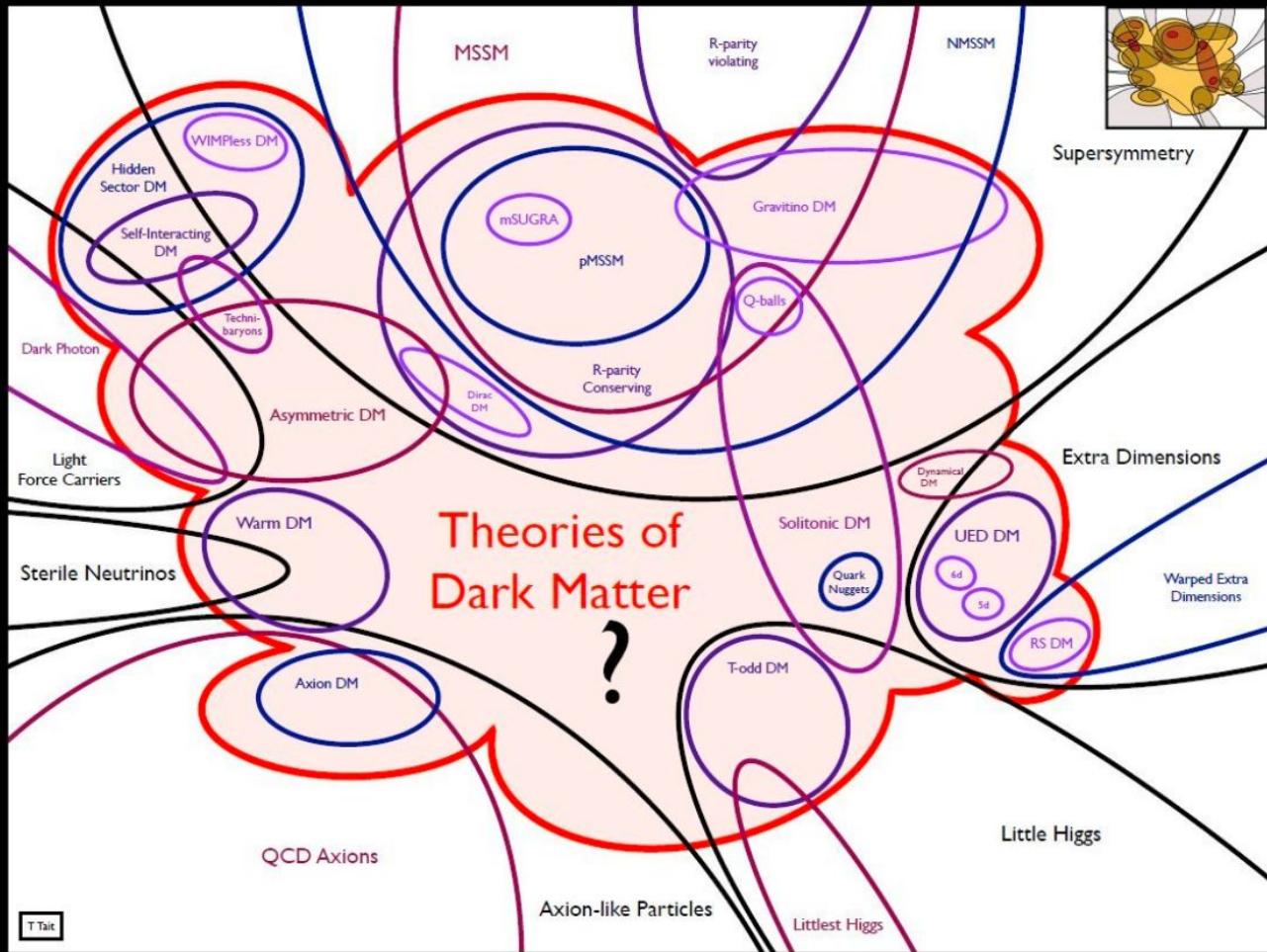
$$\frac{dN_\nu}{dE_\nu} = \frac{4}{m_\chi} \Theta(E_\nu) \Theta(m_\chi - E),$$



Experimental limits



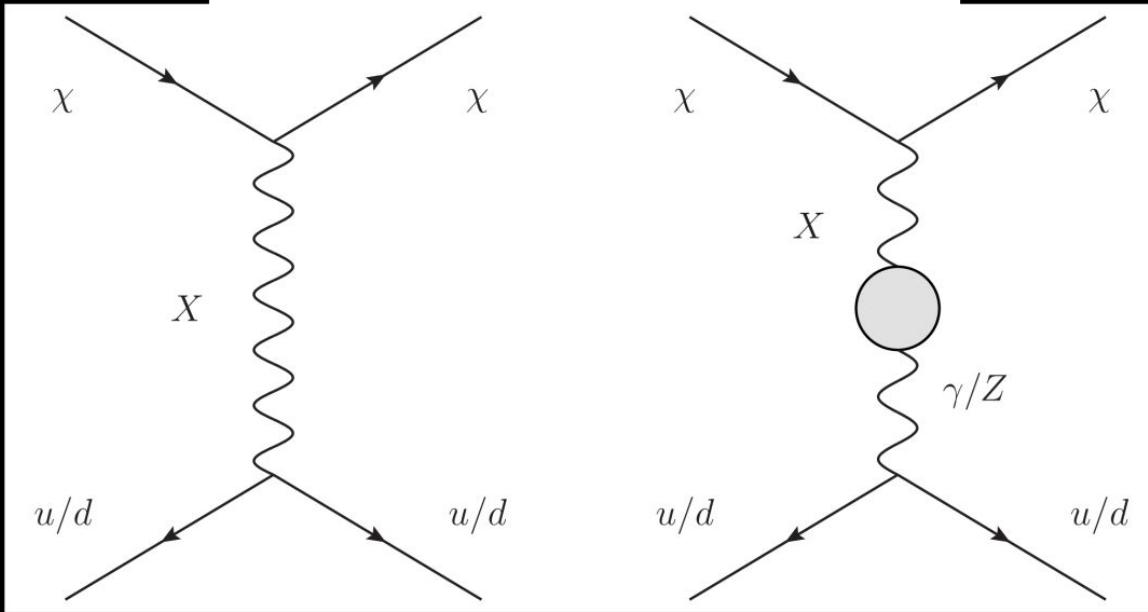
What DM model?



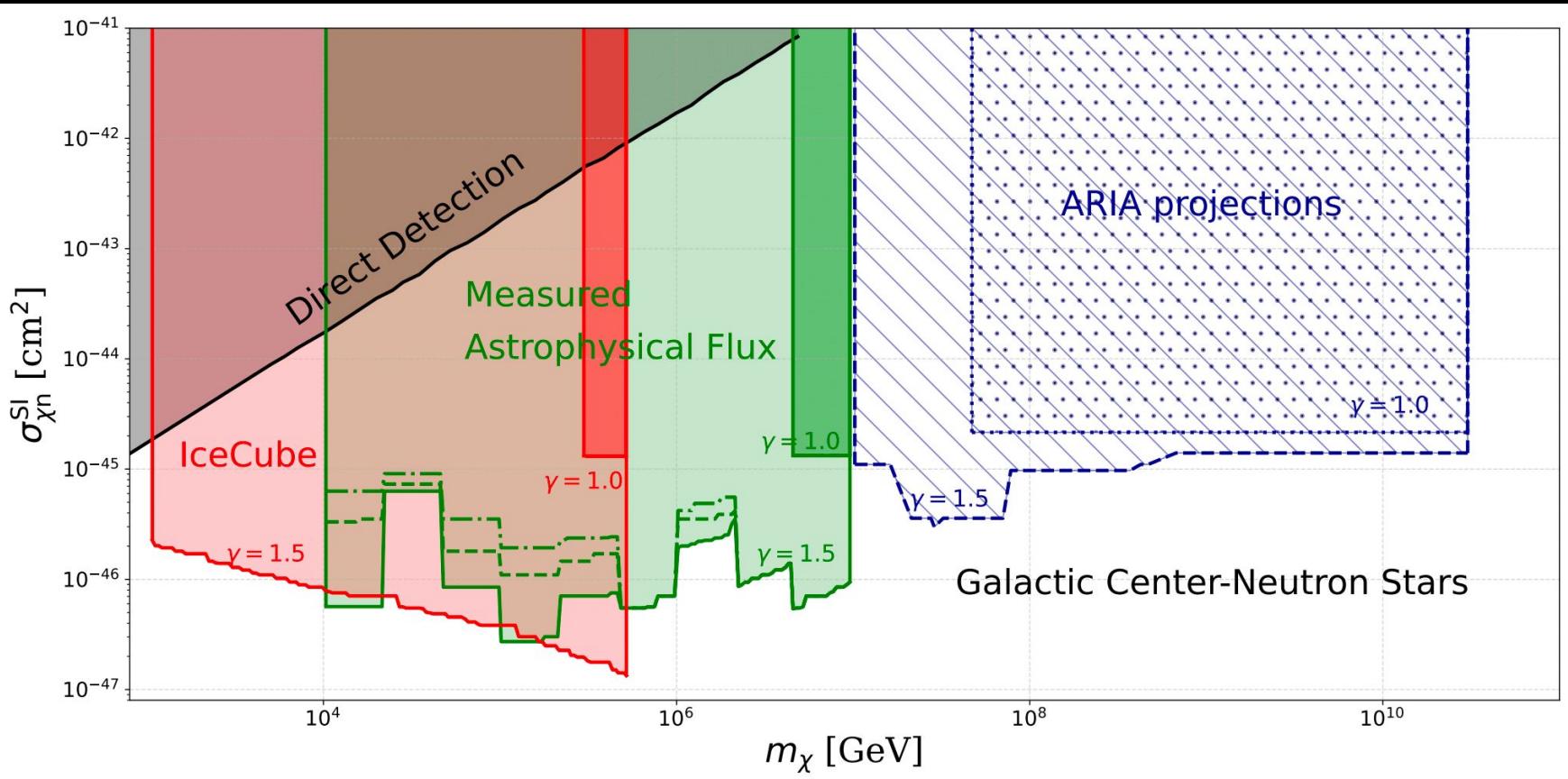
Dark Photon model

 $SU(2)_L \times U(1)_Y \times U(1)_X$

$$\begin{aligned}\mathcal{L} \supset & -\frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{\epsilon}{2} X_{\mu\nu} B^{\mu\nu} \\ & - \frac{1}{2} m_X^2 X_\mu X^\mu + \bar{\chi} (i \not{D}_{U(1)_X} - m_\chi) \chi,\end{aligned}$$



Spin-Independent Cross Section limits



Take home message

- Neutron Stars can help us investigate Long-lived Dark Matter Mediator models.
- With Light Dark Photon model and current IceCube result, the bounds for SI Cross Section of DM-neutron can be pushed down to $10^{-46} - 10^{-47}$ cm² (TeV - PeV mass range).
- Can use other celestial objects with large number in Galactic Center: Brown Dwarfs, White Dwarfs, ...
- Motivation for experimental results: ARIANNA, KM3Net, IceCube Gen2, ...

Thank you for listening!

Chiao is searching
for Dog-matter
too!

