

Production of light dark photon dark matter in the early universe

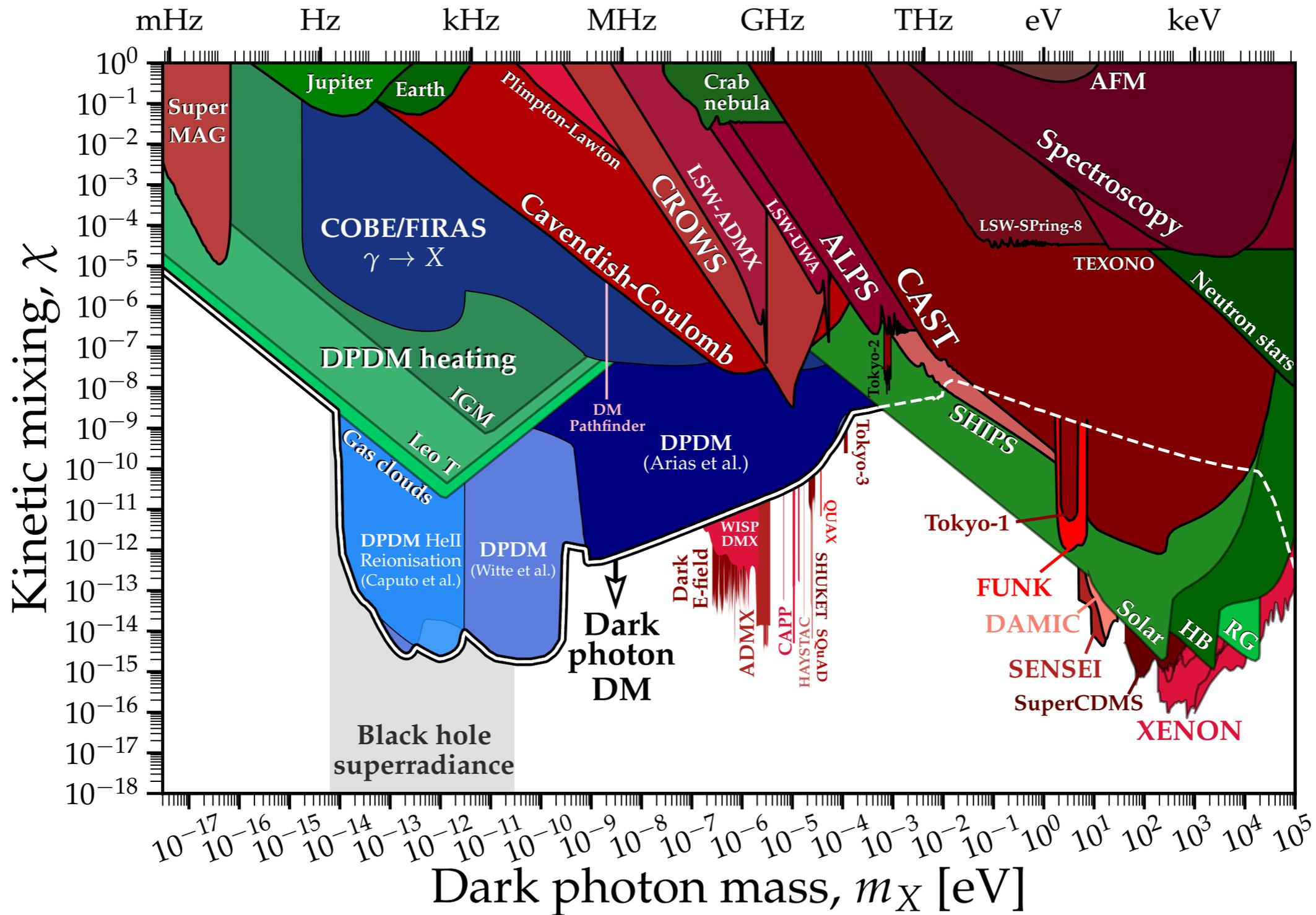
Naoya Kitajima (A01)



FY2022 “What is dark matter? - Comprehensive study of the huge discovery space in dark matter”

March 7-9, 2023, Kavli IPMU

Dark photon dark matter : current status



$$\mathcal{L} \ni \frac{1}{2} \chi F^{\mu\nu} X_{\mu\nu}$$

Dark photon dark matter production

- Gravitational particle production during inflation / reheating

Graham, Mardon, Rajendran (2016) / Ema, Nakayama, Tang (2019)

Requirement : High scale inflation / high reheating temperature

- Resonant production from axion oscillation

Agrawal, NK, Reece, Sekiguchi, Takahashi (2020)

Co, Pierce, Zhang, Zhao (2019), Bastro-Gil, Santiago, Ubaldi, Vega-Morales (2019)

Requirement : Large axion-dark photon coupling

- Resonant production from dark Higgs oscillation Harigaya, Narayan (2019)

Requirement : Extremely small Higgs self-coupling and gauge coupling

- Misalignment production Nakayama (2019), Nakayama (2020)

Requirement : non-trivial dynamics of gauge kinetic function during inflation

- Production from the decay of cosmic string loop

Long, Wang (2019), NK, Nakayama (2022)

Resonant dark photon DM production from axion

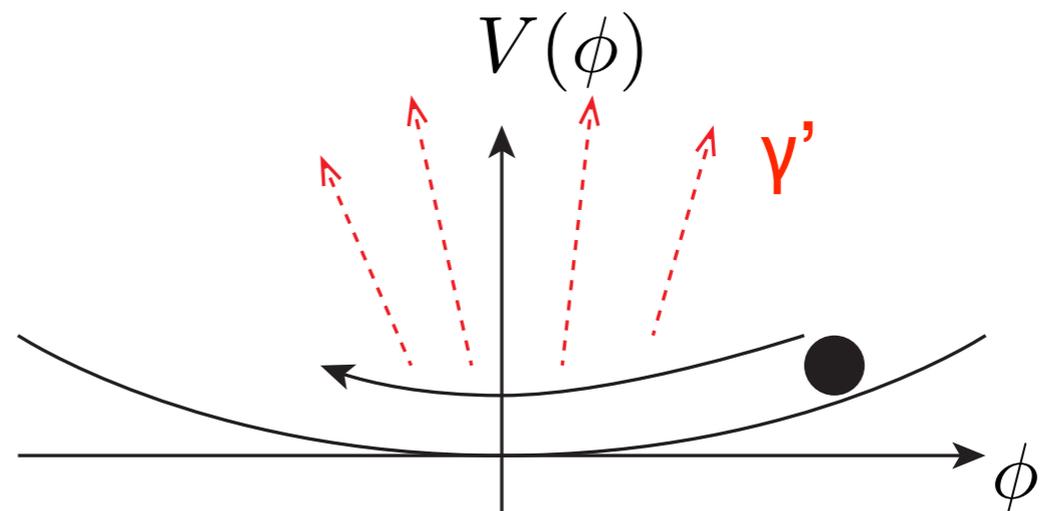
Agrawal, NK, Reece, Sekiguchi, Takahashi, 1810.07188

Co, Pierce, Zhang, Zhao, 1810.07196

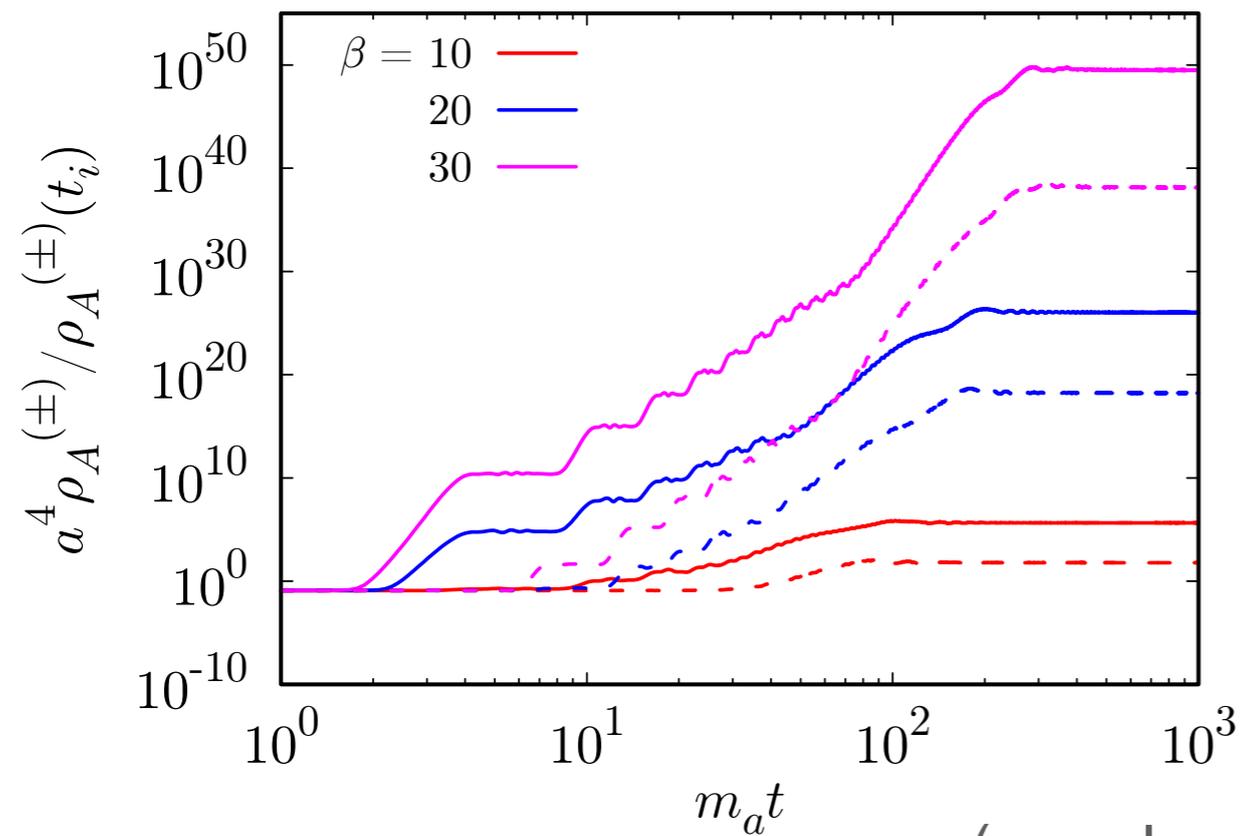
Bastero-Gil, Santiago, Ubaldi, Vega-Morales, 1810.07208

$$\mathcal{L} = \frac{1}{2} \partial^\mu \phi \partial_\mu \phi - V(\phi) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{2} m_{\gamma'}^2 A_\mu A^\mu - \frac{\beta}{4f_a} \phi F_{\mu\nu} \tilde{F}^{\mu\nu}$$

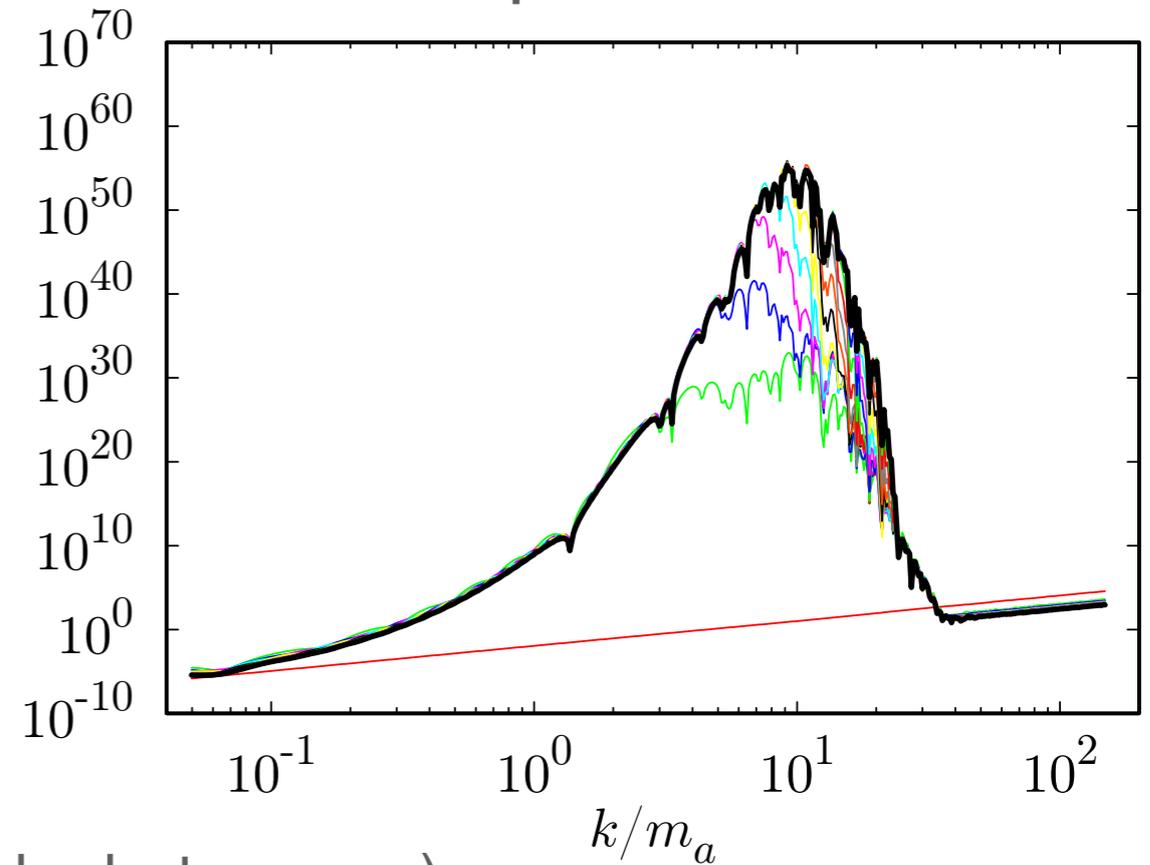
$$\longrightarrow \ddot{\mathbf{A}}_{\mathbf{k},\pm} + H \dot{\mathbf{A}}_{\mathbf{k},\pm} + \left(m_{\gamma'}^2 + \frac{k^2}{a^2} \mp \frac{k}{a} \frac{\beta \dot{\phi}}{f_a} \right) \mathbf{A}_{\mathbf{k},\pm} = 0$$



resonant amplification



spectrum



- Produced dark photons can stabilize the dark Higgs

—> secondary inflation (like thermal inflation) or early dark energy

NK, Nakagawa, Takahashi, 2111.06696

next talk by S. Nakagawa

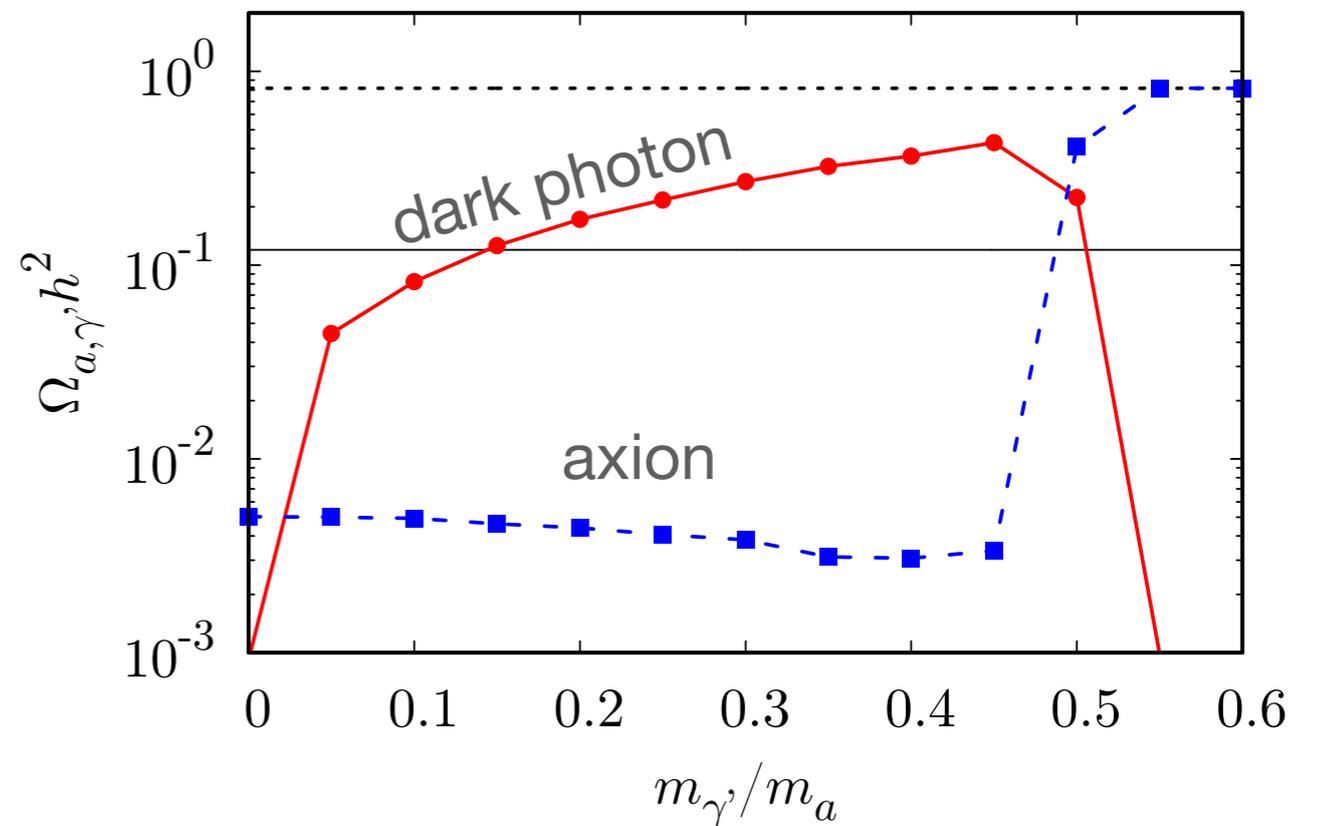
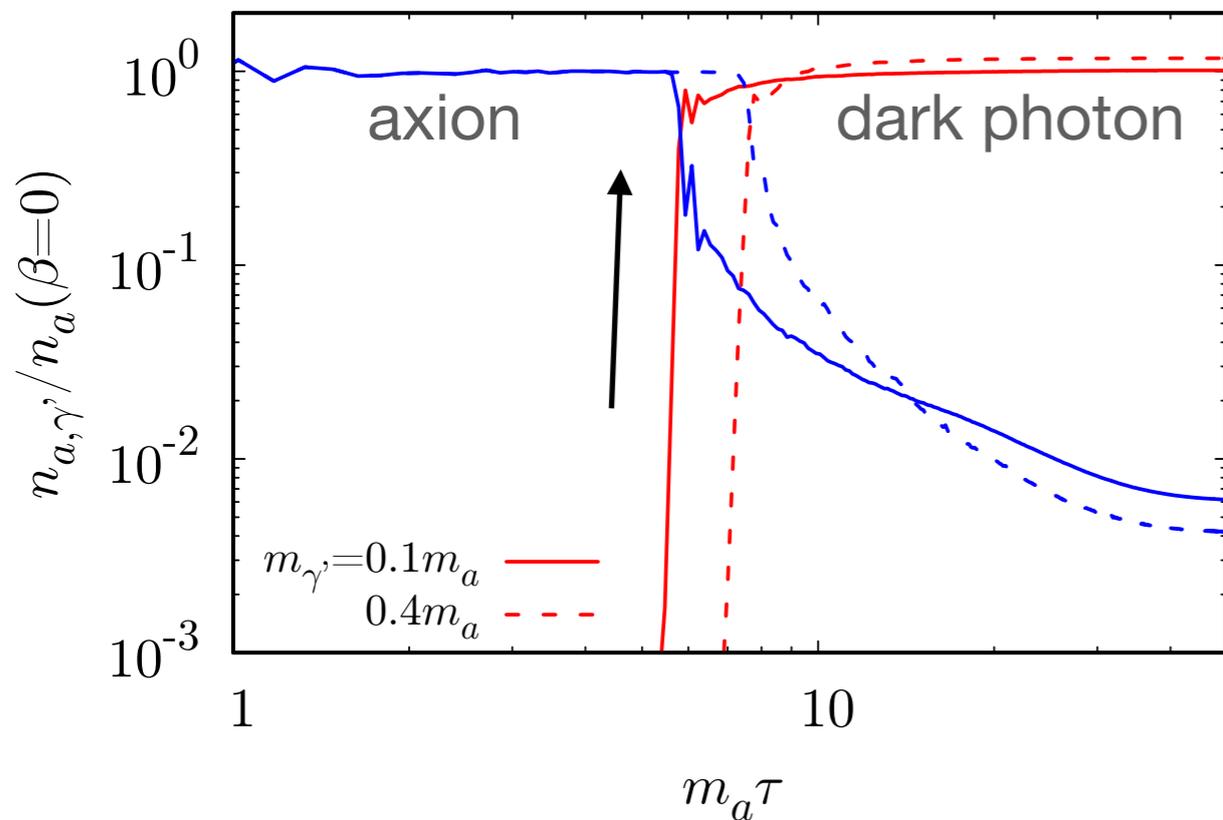
Nakagawa, Takahashi, Yin, 2209.01107

- GW emission with circular polarization NK, Soda, Urakawa, 2010.10990

see also Machado+ (2019), Salehian+ (2020), Ratzinger+ (2020), Namba+ (2020)

Relic abundance of dark photon DM and axion

Agrawal, NK, Reece, Sekiguchi, Takahashi, 1810.07188



Axion abundance is suppressed due to the backreaction

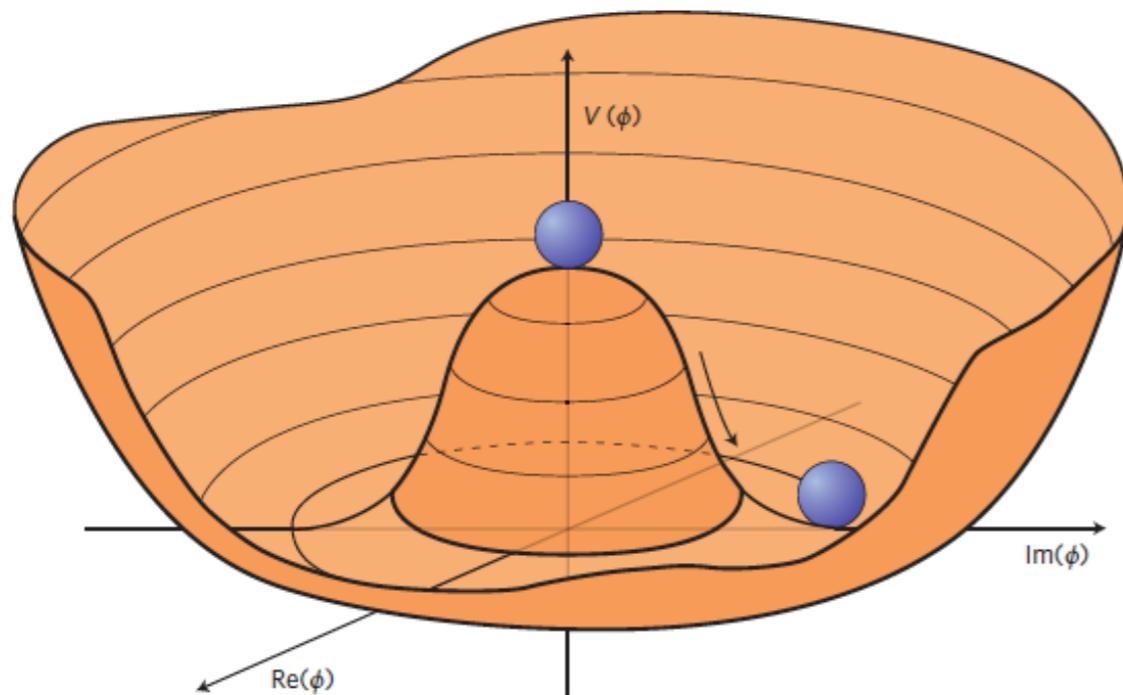
(see also NK, T. Sekiguchi, F. Takahashi, 1711.06590)

& dark photon can be the dominant DM component

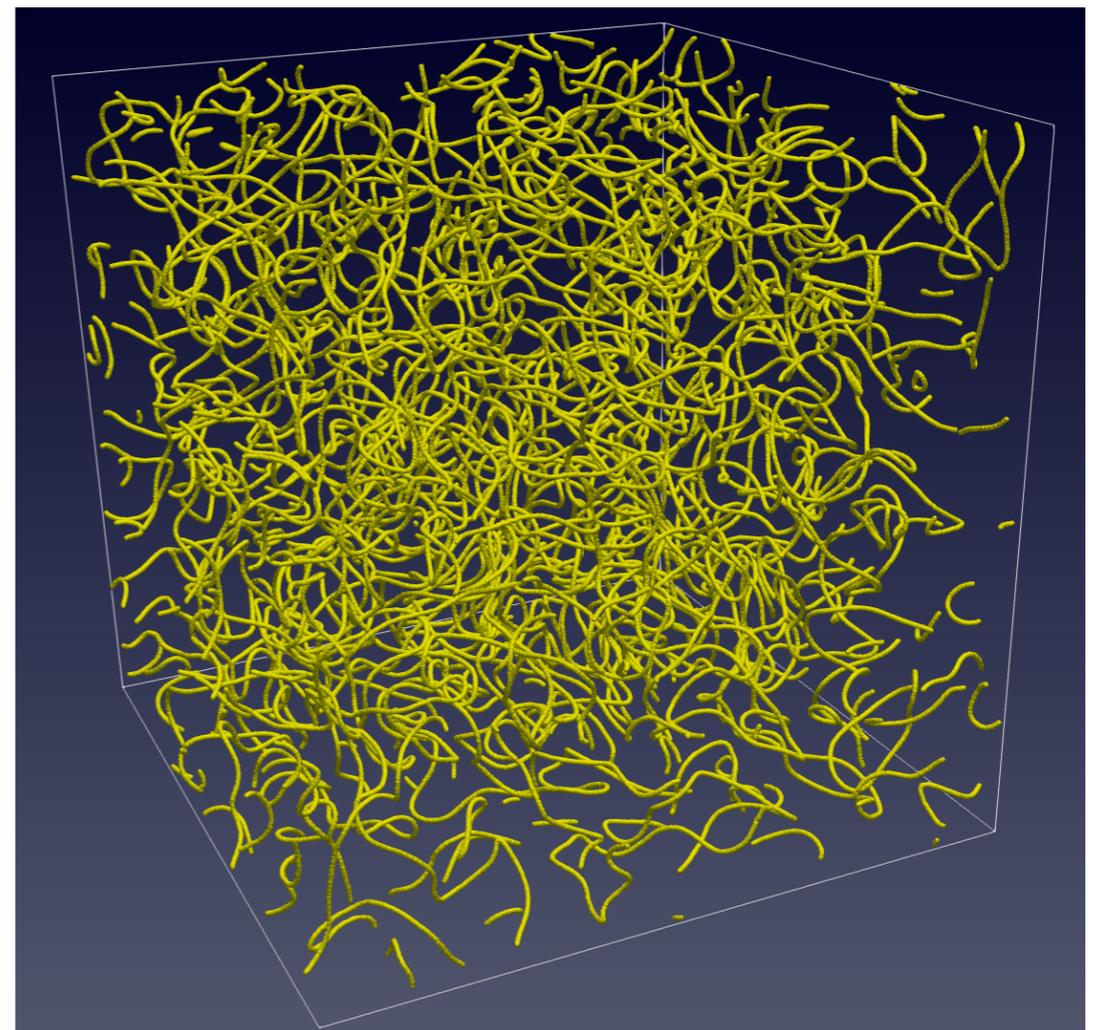
Dark photon DM from Abelian-Higgs cosmic strings

Long, Wang 1901.03312, NK, Nakayama 2212.13573

$$\mathcal{L} = (\mathcal{D}_\mu \Phi)^* \mathcal{D}^\mu \Phi - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - V(\Phi), \quad V(\Phi) = \frac{\lambda}{4} (|\Phi|^2 - v^2)^2$$
$$(\mathcal{D}_\mu = \partial_\mu - ieA_\mu, \quad F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu)$$



Ellis, Gaillard, Nanopoulos 1504.07217

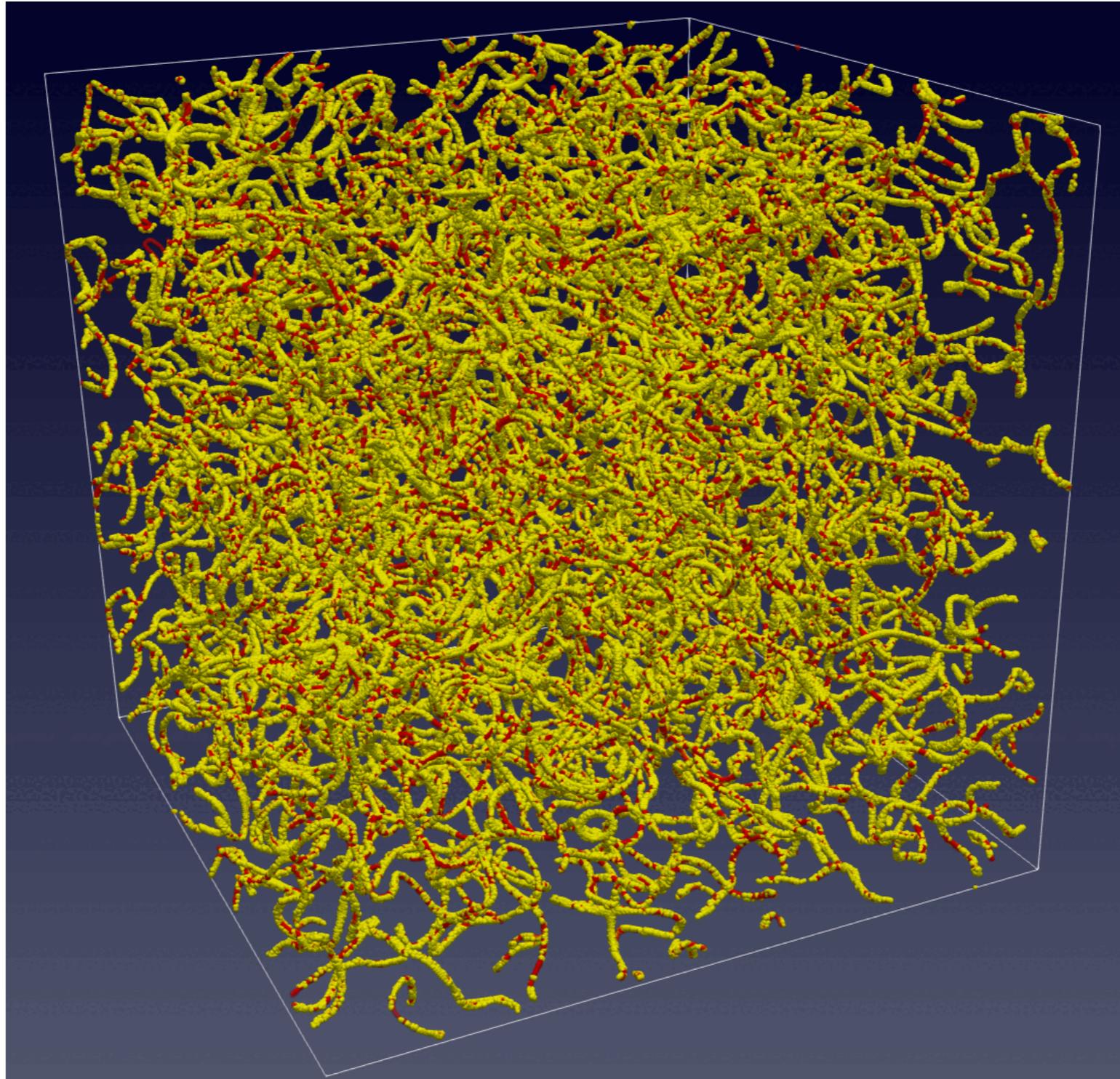


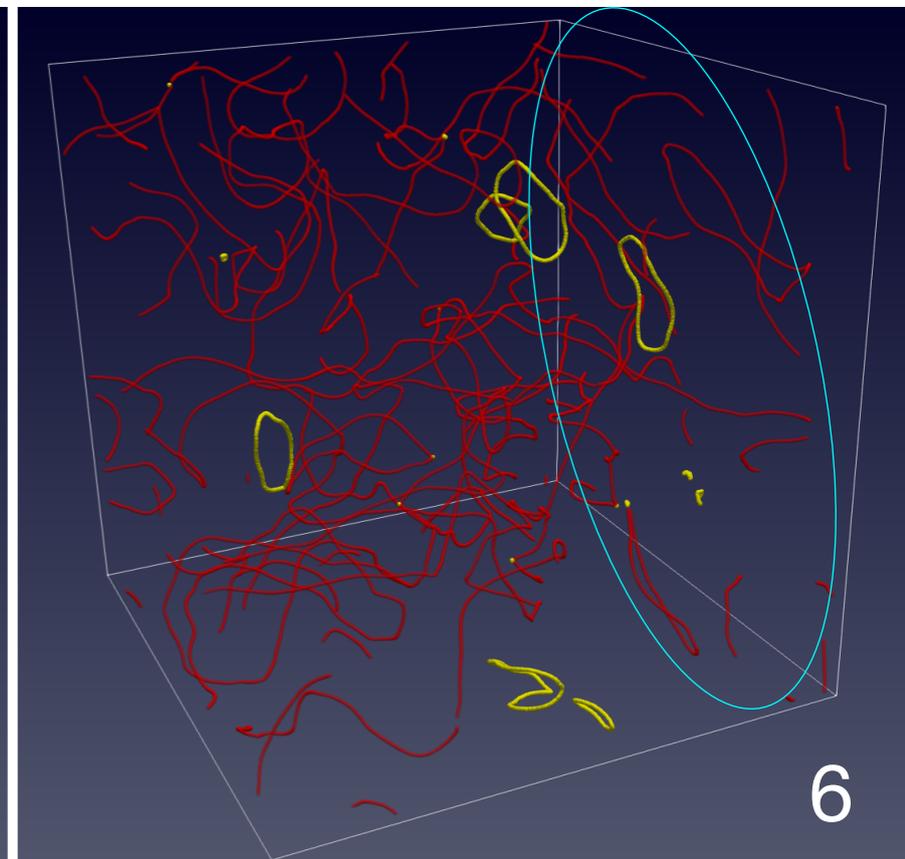
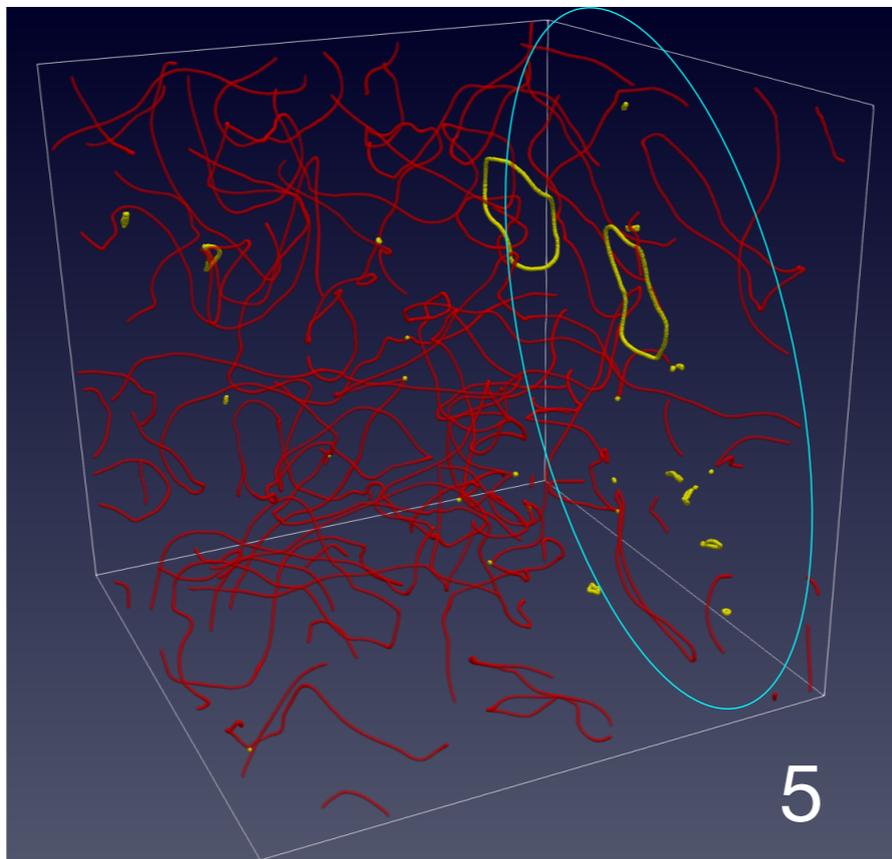
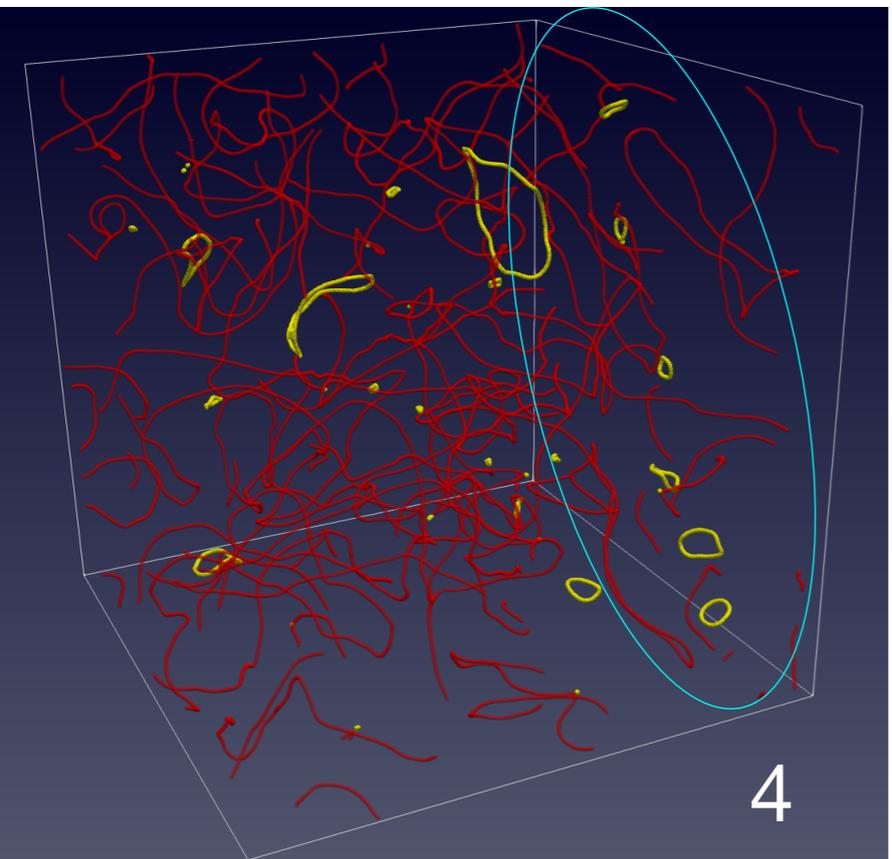
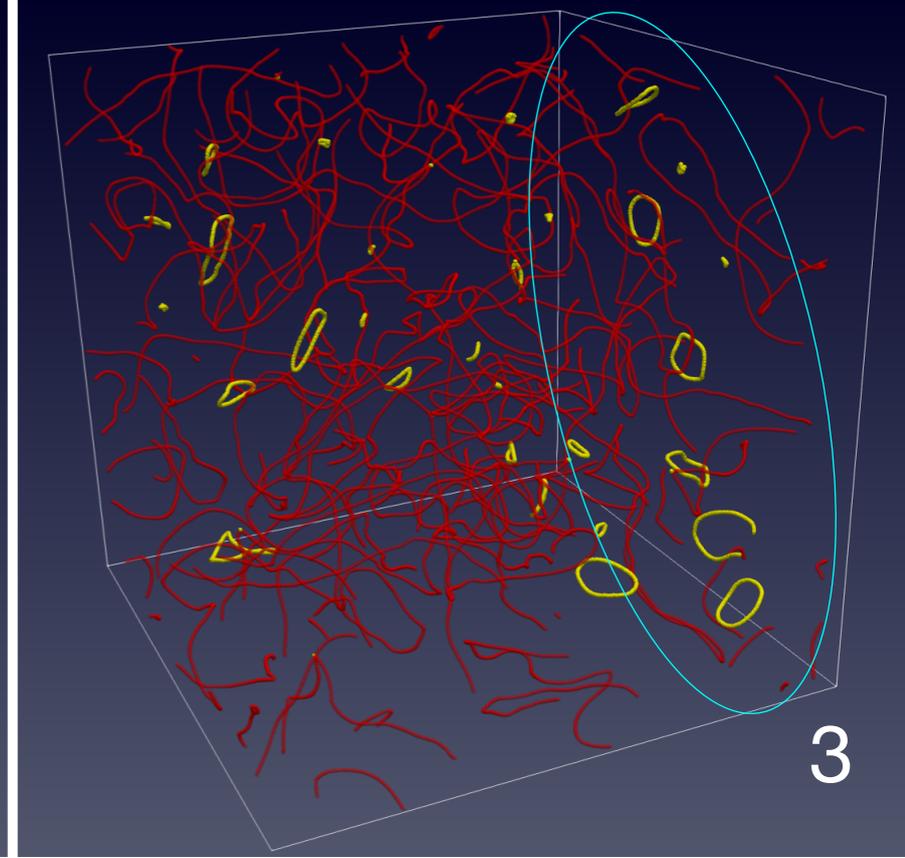
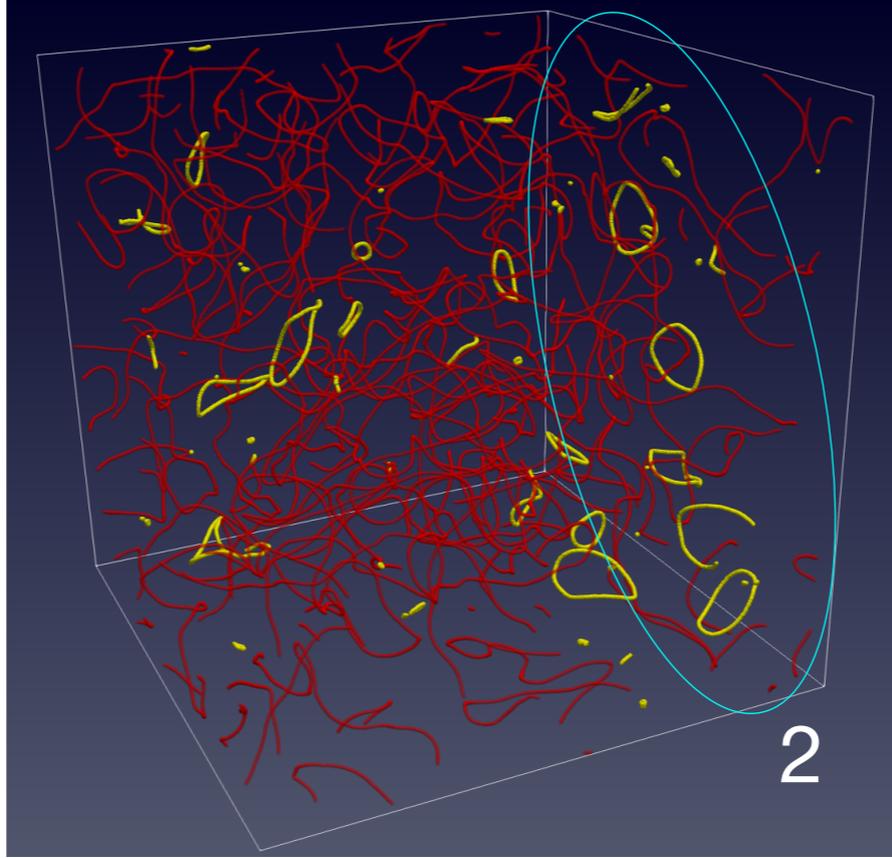
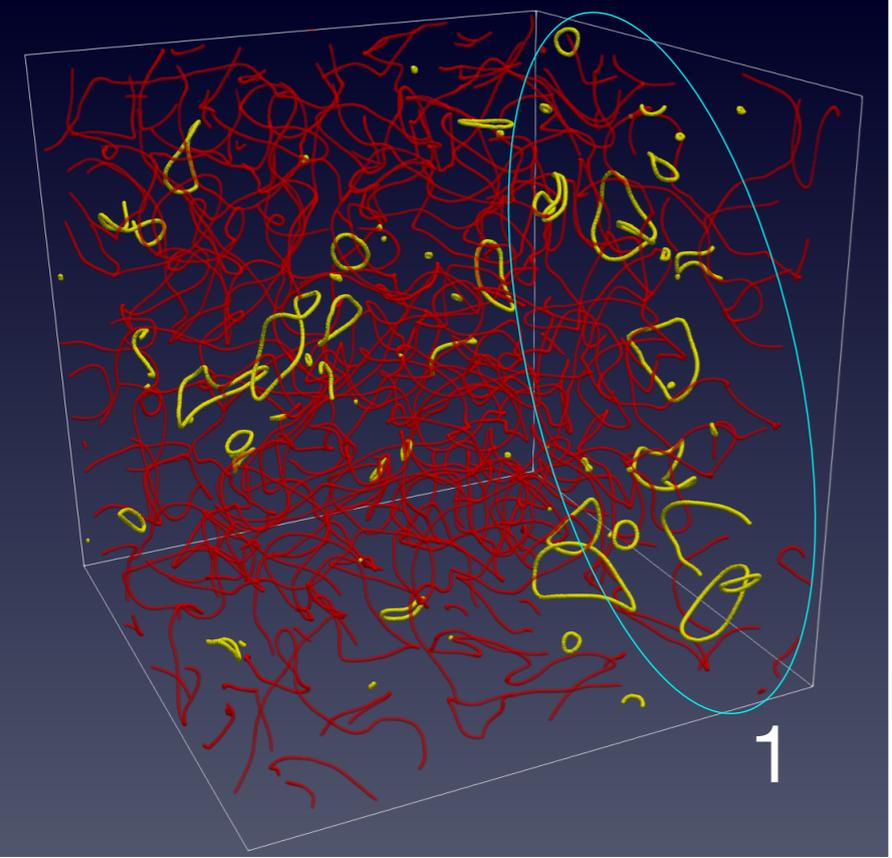
Scenario

- We are interested in very light dark photon (i.e. extremely small gauge coupling) in order to give the observed relic abundance.
 - > cosmic string is almost global (Type-II string)
e = 0 limit corresponds to the global string case
- Dark photon is continuously produced by the collapse of loops.
(similar to the axion emission from global strings)
- Dark photon production becomes inefficient for $\ell_{\text{loop}} \gtrsim m_A^{-1}$
(i.e. loop oscillation frequency becomes smaller than the mass) or $H \lesssim m_A$
- After that, string behaves like local string
(network loses the energy only through the GW emission)

Loop production & decay

Type-II string with $e=0.01$ and $\lambda=2$





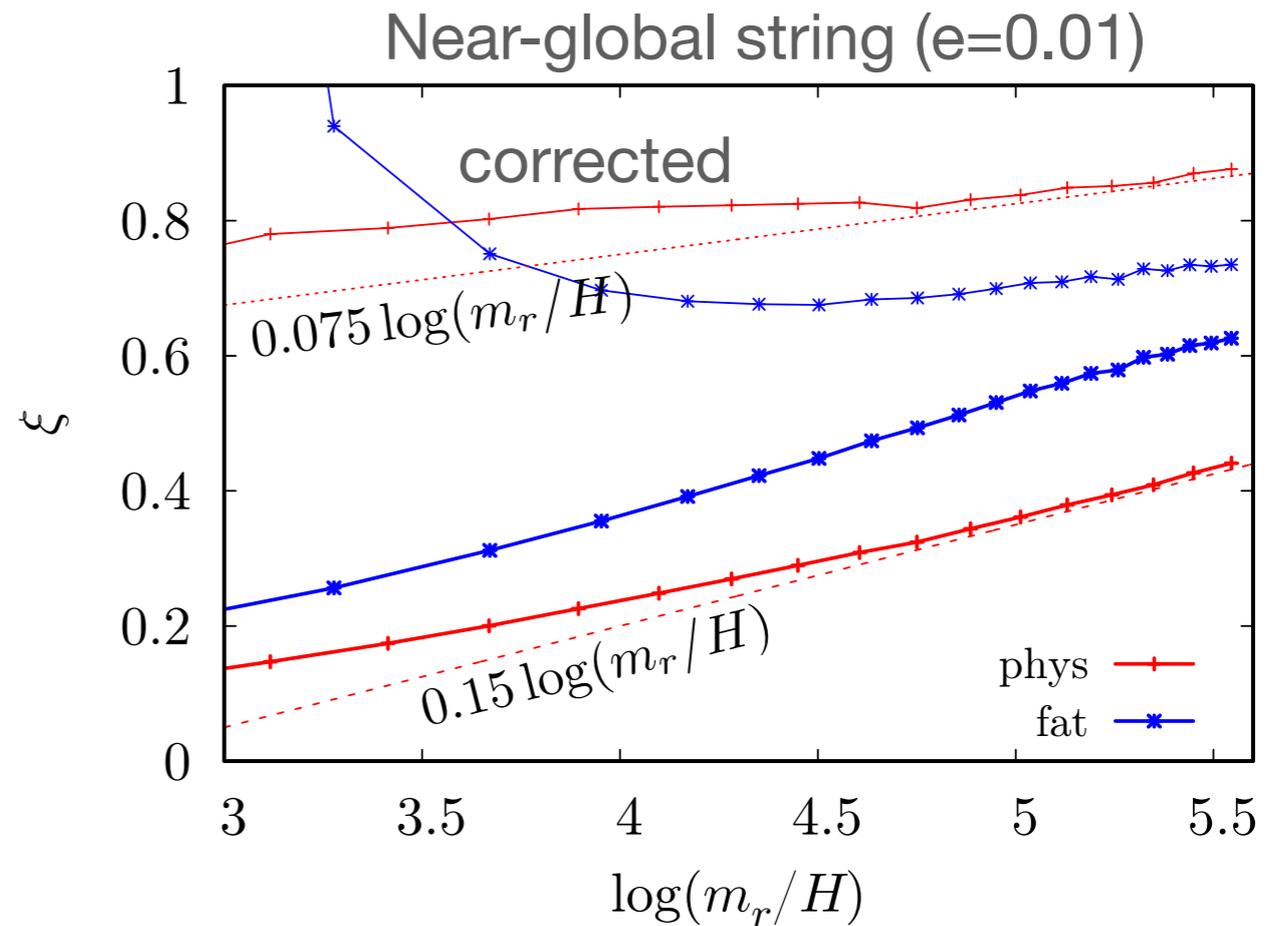
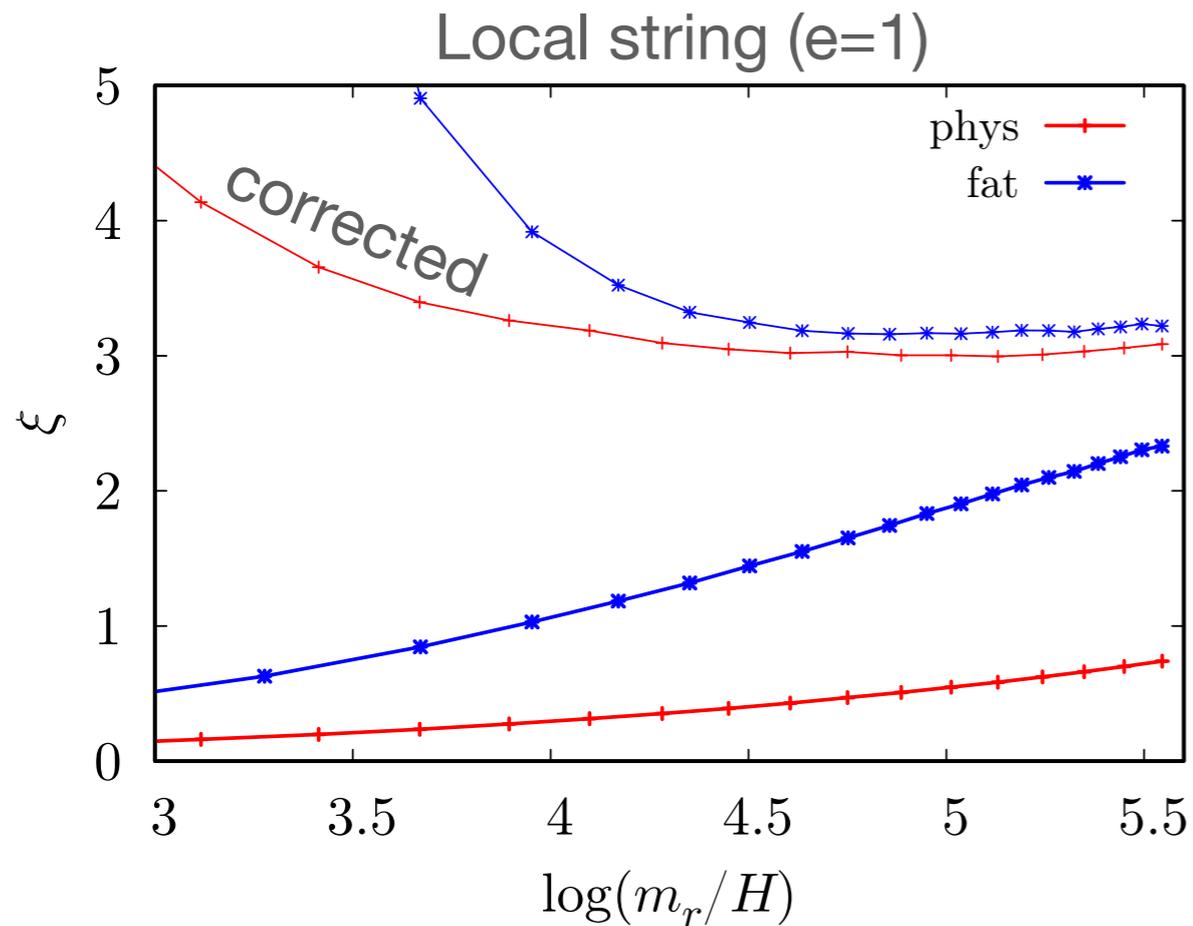
Scaling law/violation

number of strings
per Hubble patch:

$$\xi = \frac{\ell_{\text{str}} t^2}{V}$$

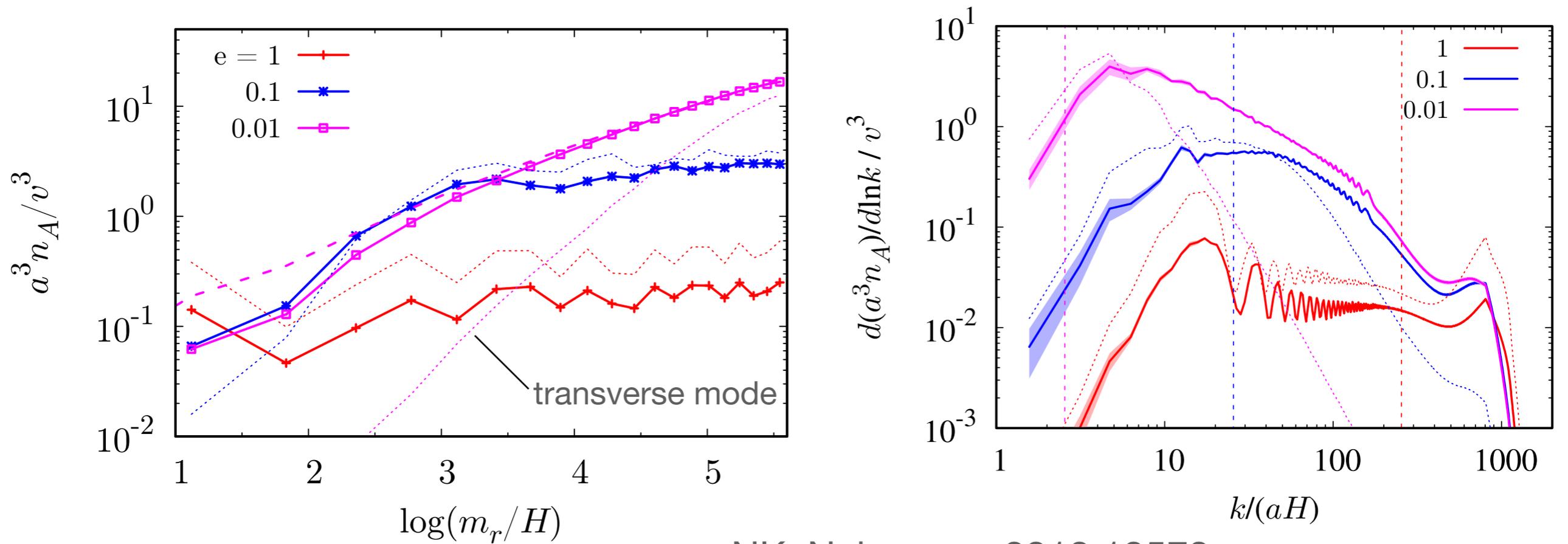
V : volume

ℓ_{str} : total string length



scaling violation can be seen (similar to the axion string case)

Dark photon DM abundance & spectrum

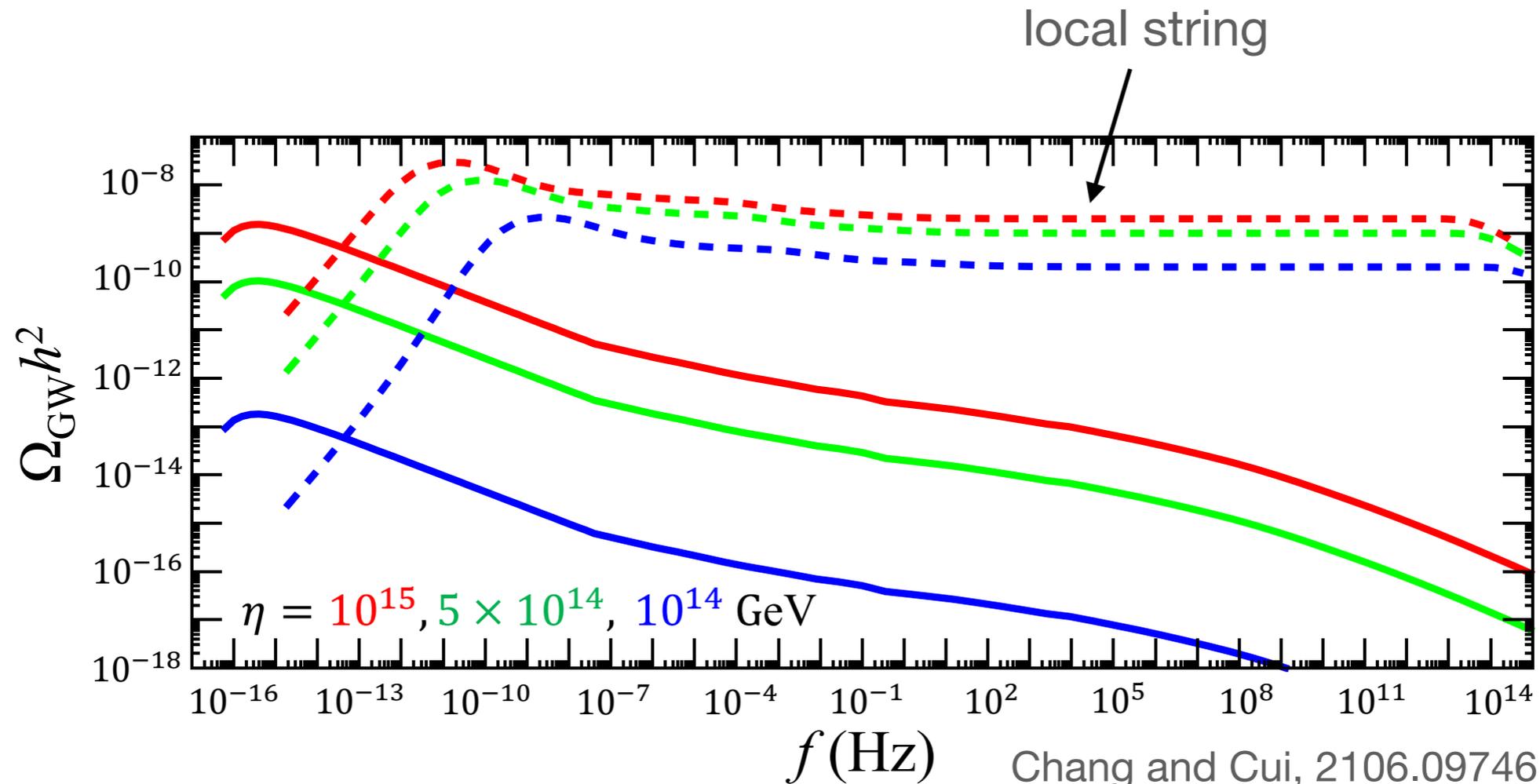


NK, Nakayama 2212.13573

$$\Omega_A h^2 = \frac{m_A (n_{A,0}/s_0) h^2}{\rho_{\text{cr},0}/s_0} \simeq 0.091 \left(\frac{\xi}{12} \right) \left(\frac{m_A}{10^{-13} \text{ eV}} \right)^{1/2} \left(\frac{v}{10^{14} \text{ GeV}} \right)^2$$

$$\xi = 0.15 \log \left(\frac{m_r}{m_A} \right) \simeq 12 + 0.15 \log \left[\left(\frac{m_r}{10^{14} \text{ GeV}} \right) \left(\frac{10^{-13} \text{ eV}}{m_A} \right) \right]$$

GW spectrum from local/global strings



Chang and Cui, 2106.09746

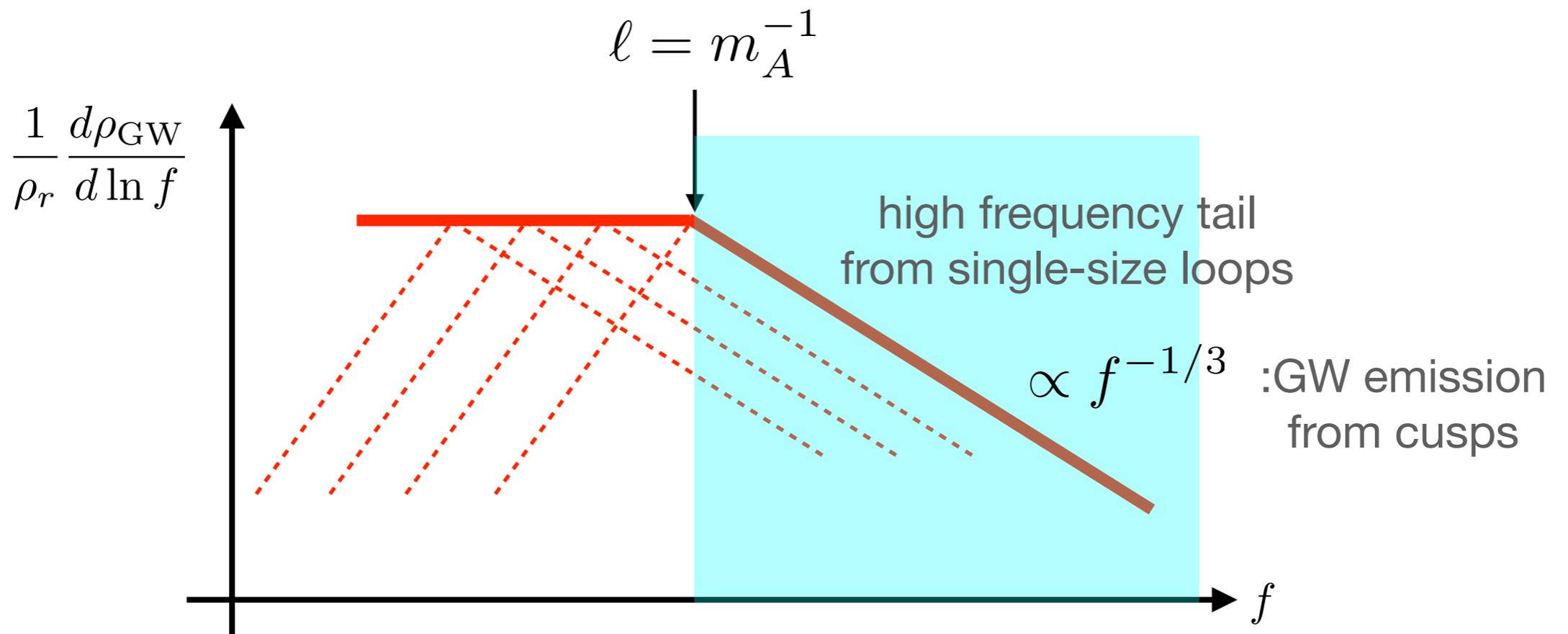
(see also Gorghetto et al, 2101.11007)

Energy loss of loops = GW emission + vector boson emission

$$\frac{dE_\ell}{dt} = -\Gamma_{\text{GW}} G\mu^2 - \Gamma_{\text{vec}} v^2 \theta(1 - m_A \ell) \quad (\Gamma_{\text{GW}} \sim \Gamma_{\text{vec}} \sim 50)$$

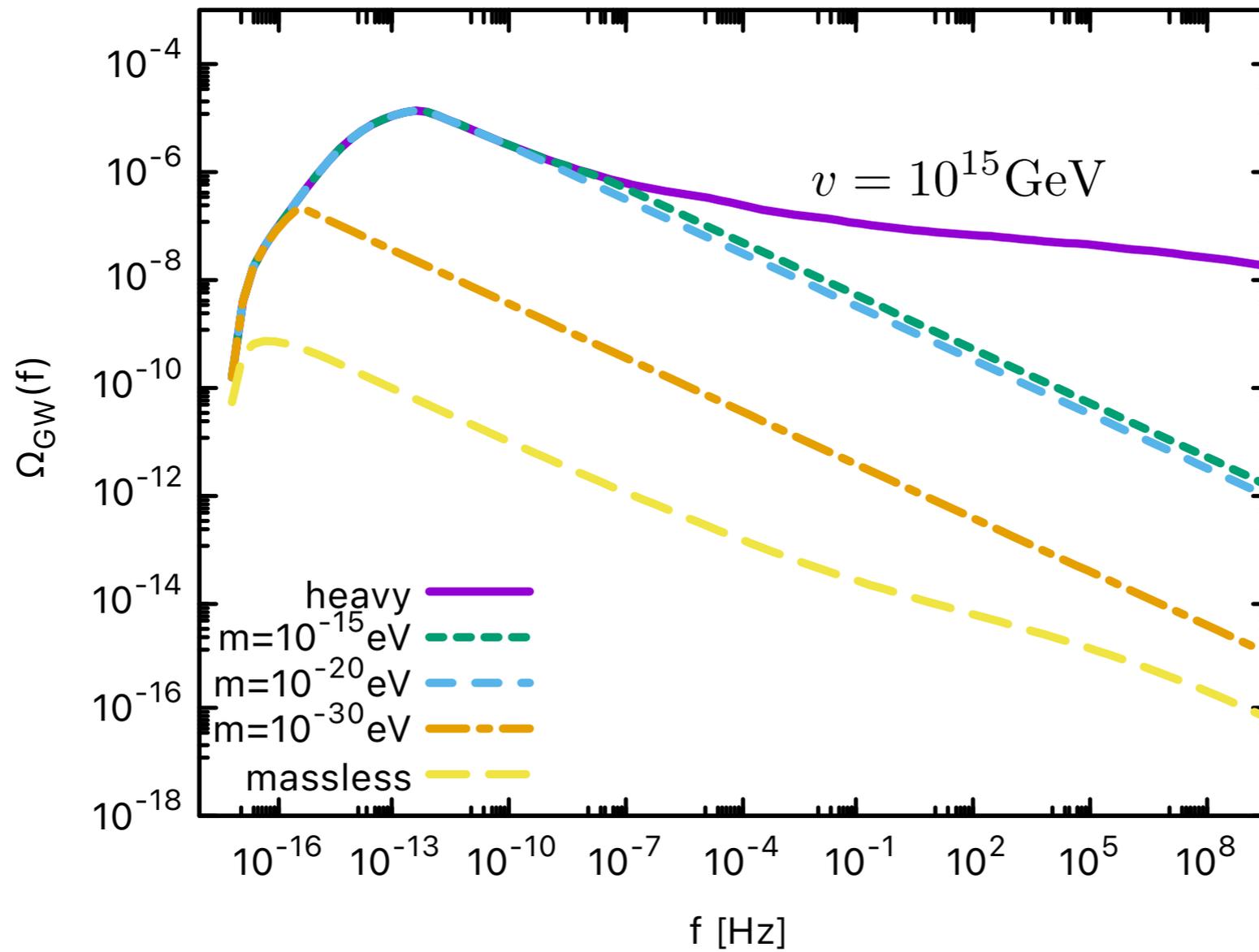
Loops shorter than m_A^{-1} can emit dark photons

→ short lived & GW emission is suppressed



GW spectrum

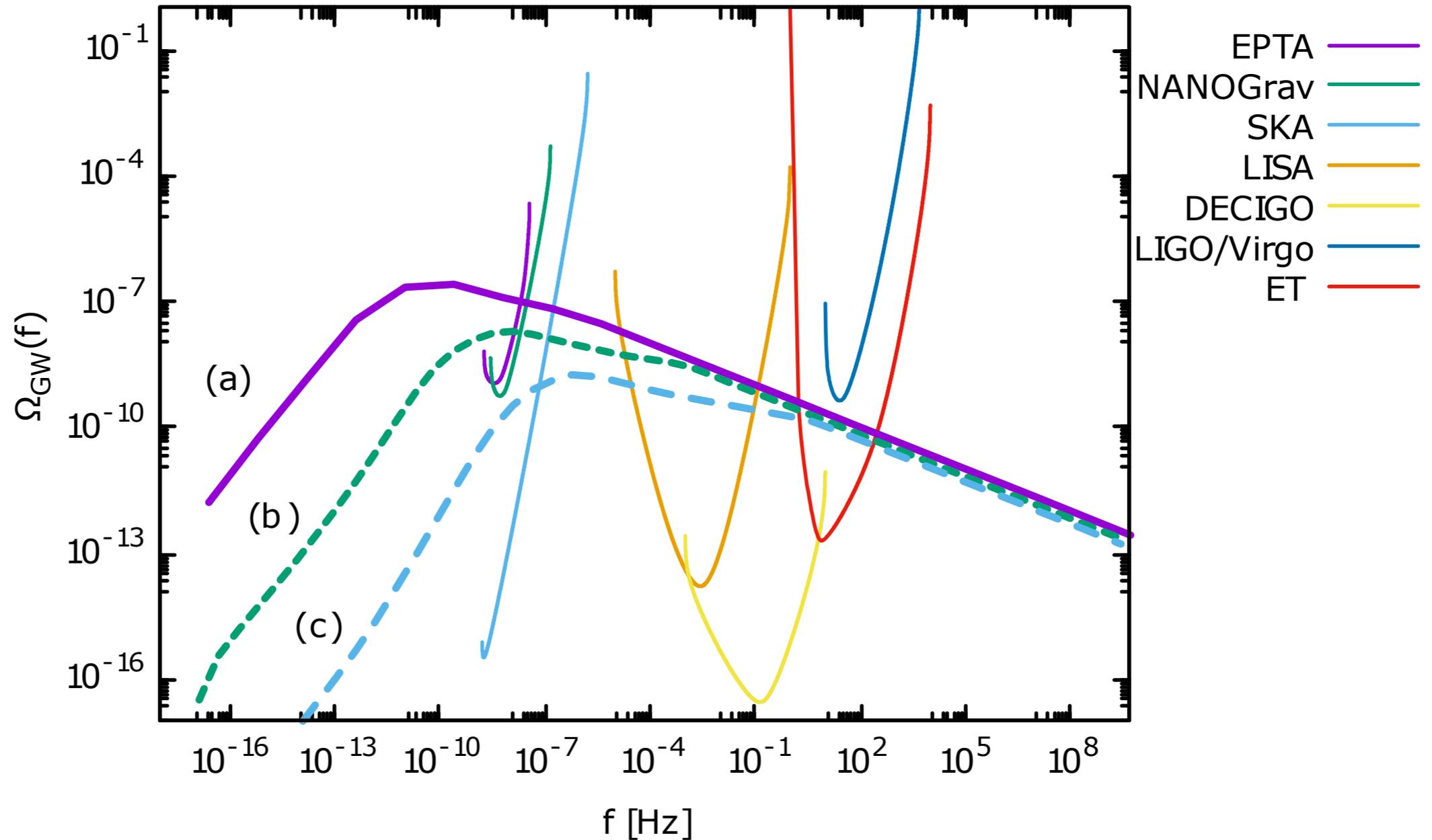
NK, Nakayama 2212.13573



scaling violation (Log-dependence) is taken into account

Detectability

NK, Nakayama 2212.13573



(a) $v = 10^{15}$ GeV, $m_A = 10^{-14}$ eV

(b) $v = 10^{13}$ GeV, $m_A = 10^{-10}$ eV

(c) $v = 10^{12}$ GeV, $m_A = 10^{-5}$ eV

Discussion

More precise study is necessary for

- Scaling violation
- Time-dependence of the tension
- Loop and dark photon production rate
especially near the transition : global \rightarrow local
- Initial loop size distribution (monochromatic or extended?)
- Spectral function of GW from individual loop (cusp- or kink-like?)
(because it is crucial for high frequency region)
- Loop lifetime (deviation from Nambu-Goto string)

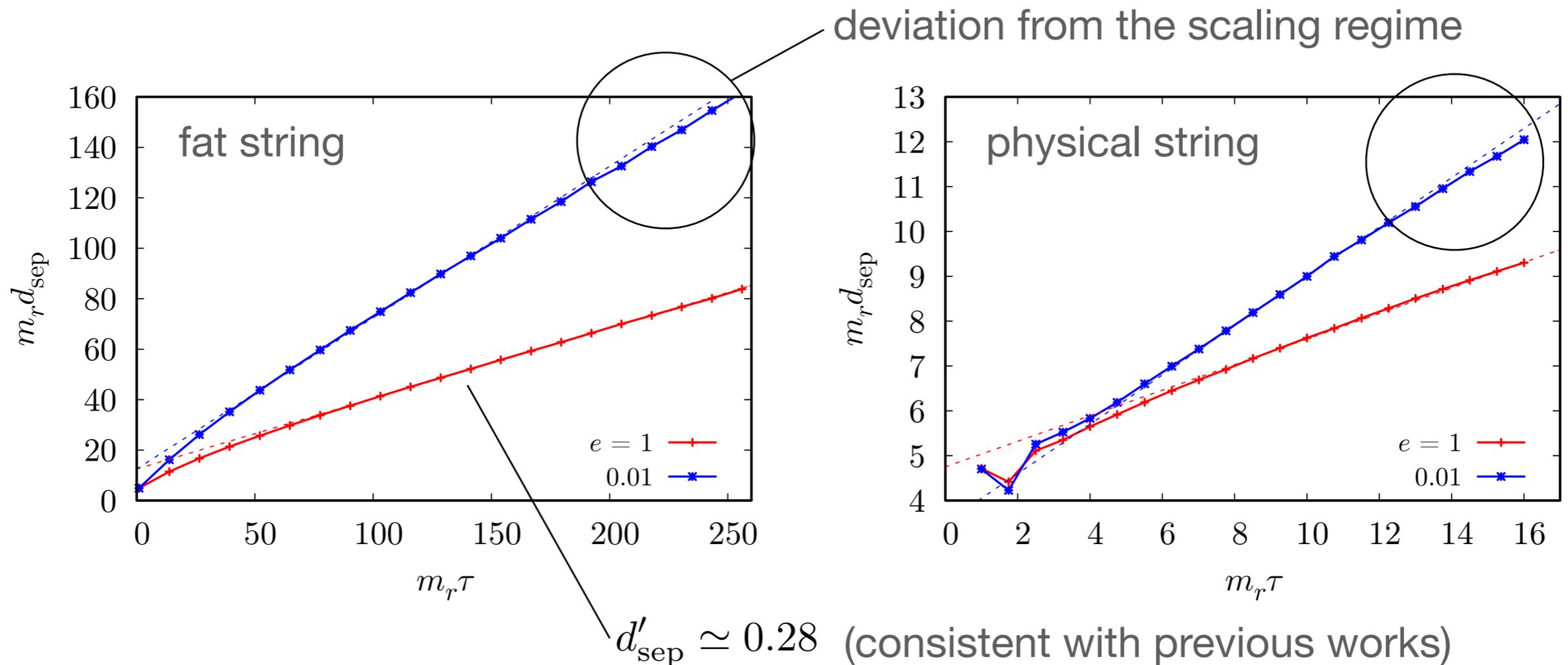
discussed in Hindmarsh et al (2017), Matsunami et al (2019)

Summary

- Dark photon can be produced from the network of cosmic strings
 - efficient loop collapse continuously produces dark photons
 - dark photon production stops when $H < m_A$
 - (i.e. the dark photon emission is kinematically suppressed)
 - > relic abundance is fixed at that time
 - observed abundance can be obtained for e.g.
 - $v \sim 10^{12}-10^{14}\text{GeV}, m_A \sim 10^{-14}-10^{-5}\text{eV}$
- Gravitational waves are emitted as a signal of this scenario
 - Spectrum is different from both local and global one
 - It can be tested by combining pulsar timing and direct detection

Mean separation of neighboring strings

$$d_{\text{sep}} = \sqrt{\frac{V(c)}{\ell_{\text{str}}^{(c)}}}$$



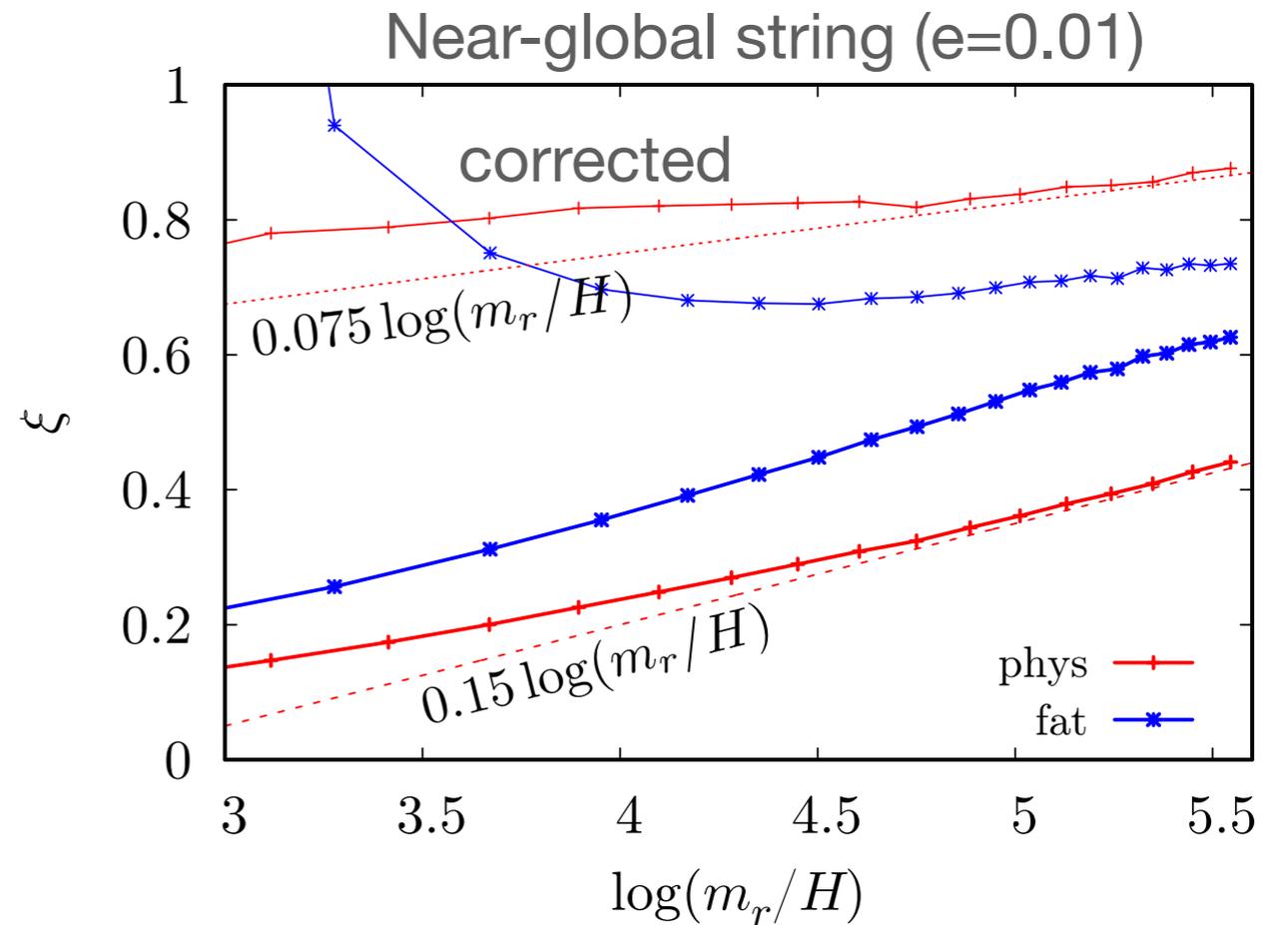
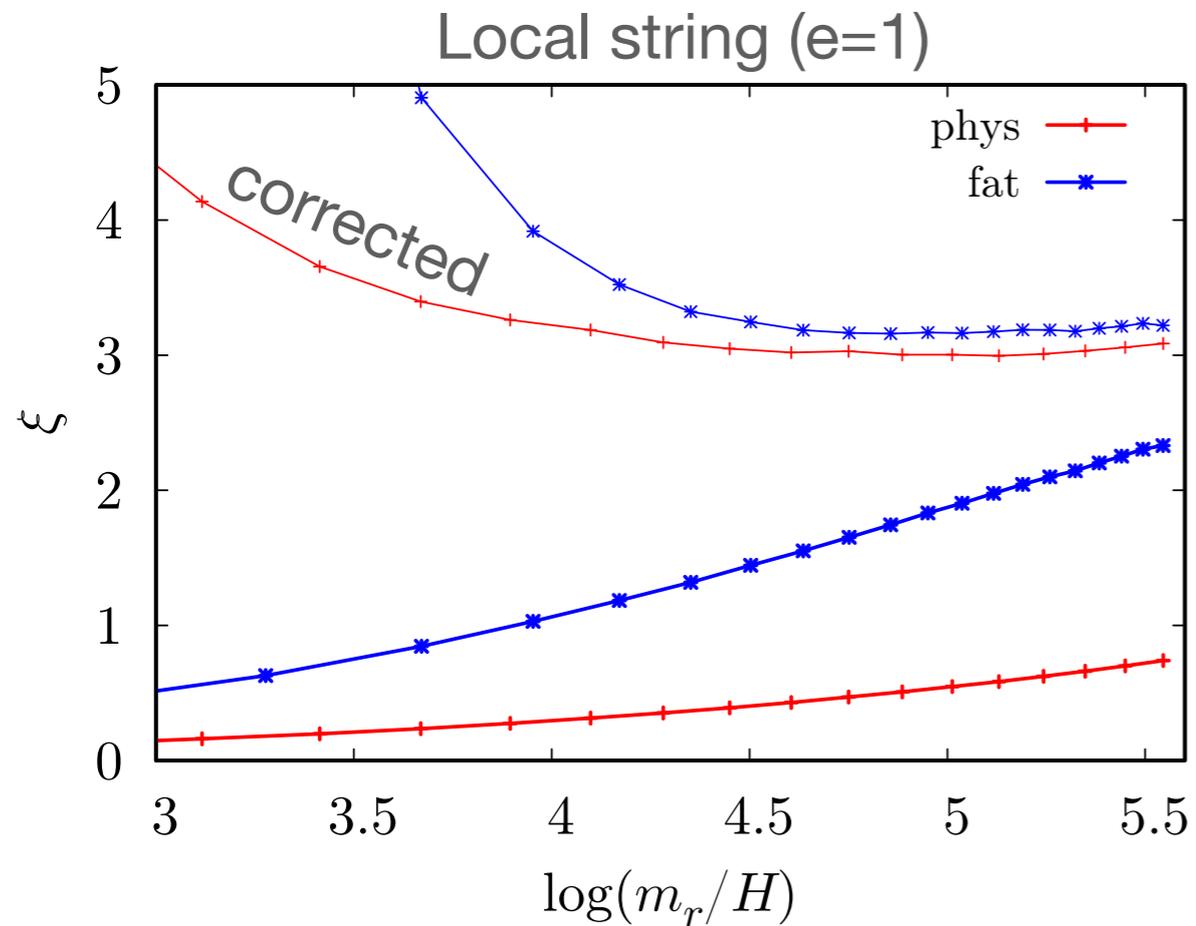
Near-global string is more sparse than local string
(as pointed out by Yamaguchi et al (1999))

Number of strings per Hubble patch

$$\xi = \frac{\ell_{\text{str}} t^2}{V}$$

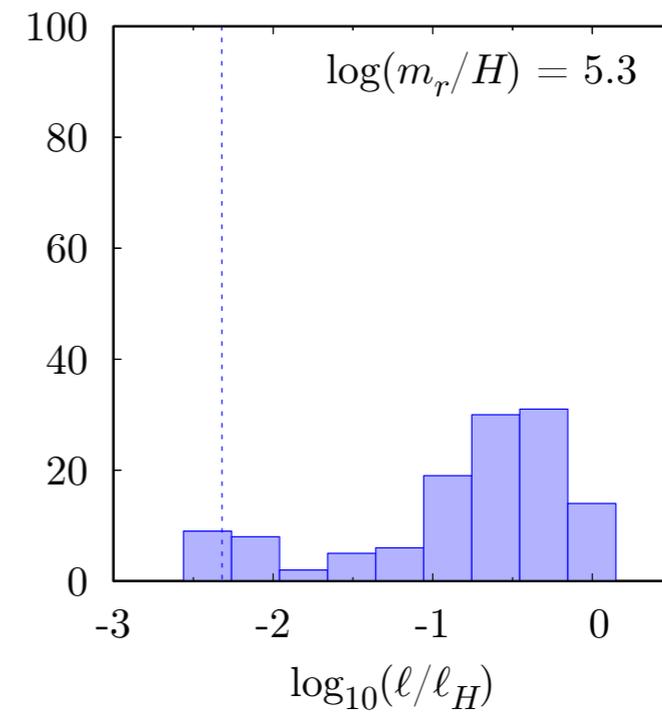
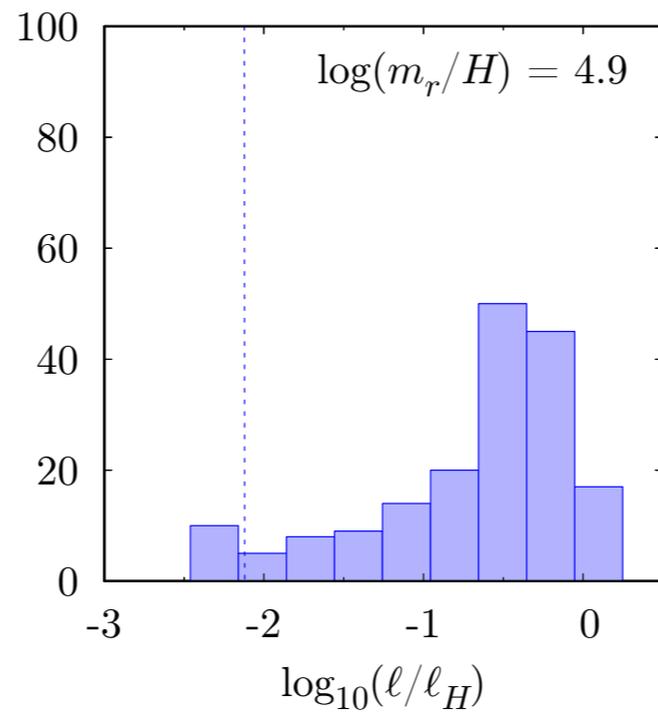
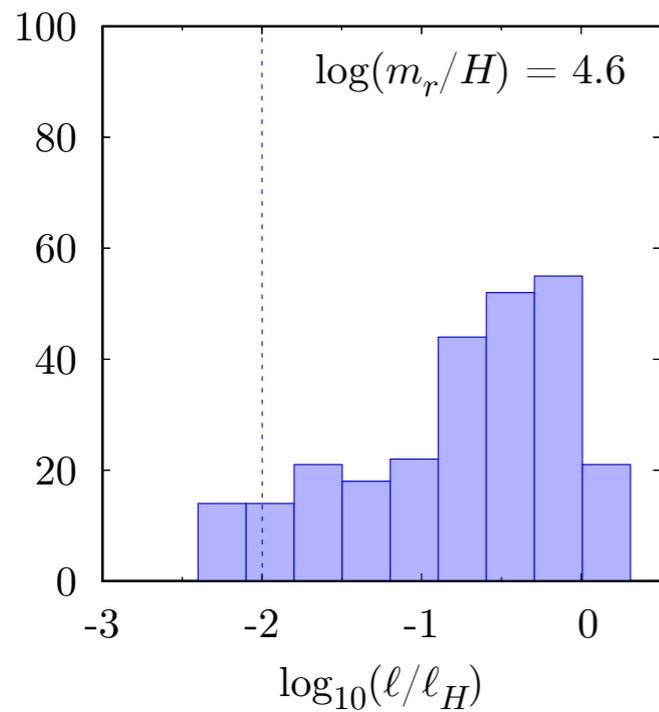
correction: $d_{\text{sep}} = a\tau + b \rightarrow \tilde{d}_{\text{sep}} \equiv d_{\text{sep}} - b = a\tau$

$$\tilde{d}_{\text{sep}} = \sqrt{\frac{V(c)}{\tilde{\ell}_{\text{str}}(c)}} \rightarrow \tilde{\xi} = \frac{\tilde{\ell}_{\text{str}} t^2}{V}$$



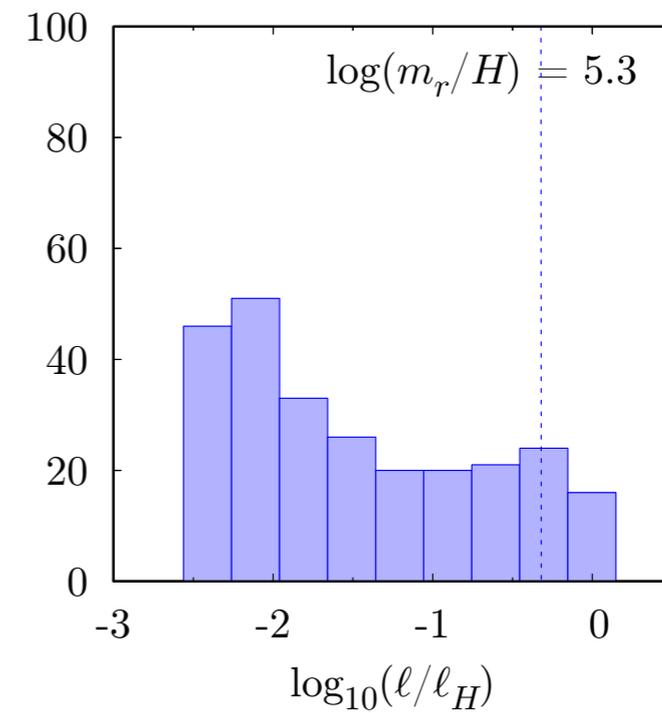
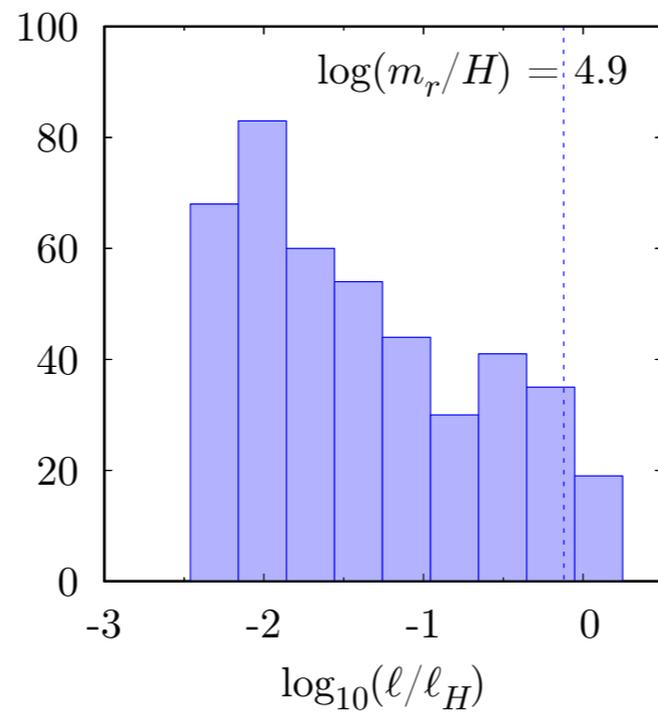
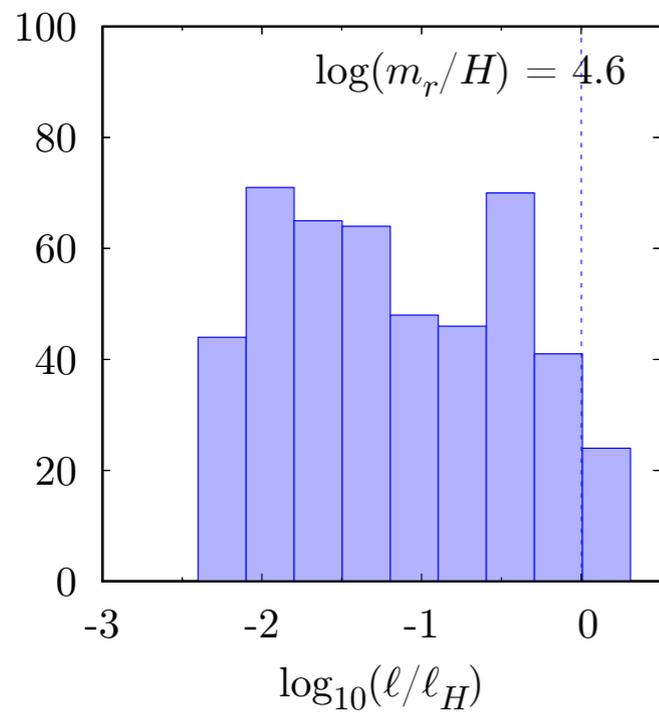
loop size distribution

local (e=1)



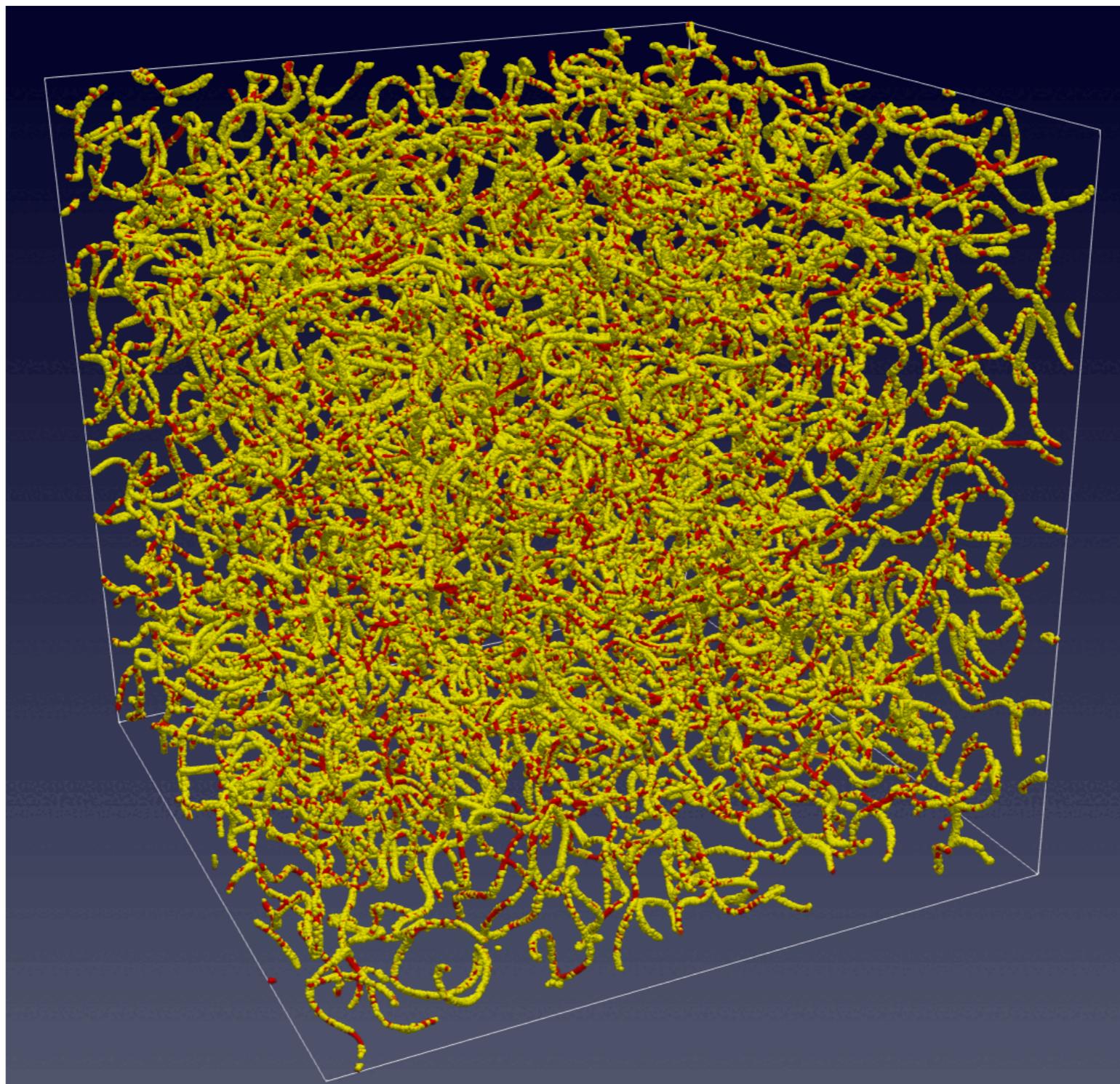
time →

near-global (e=0.01)

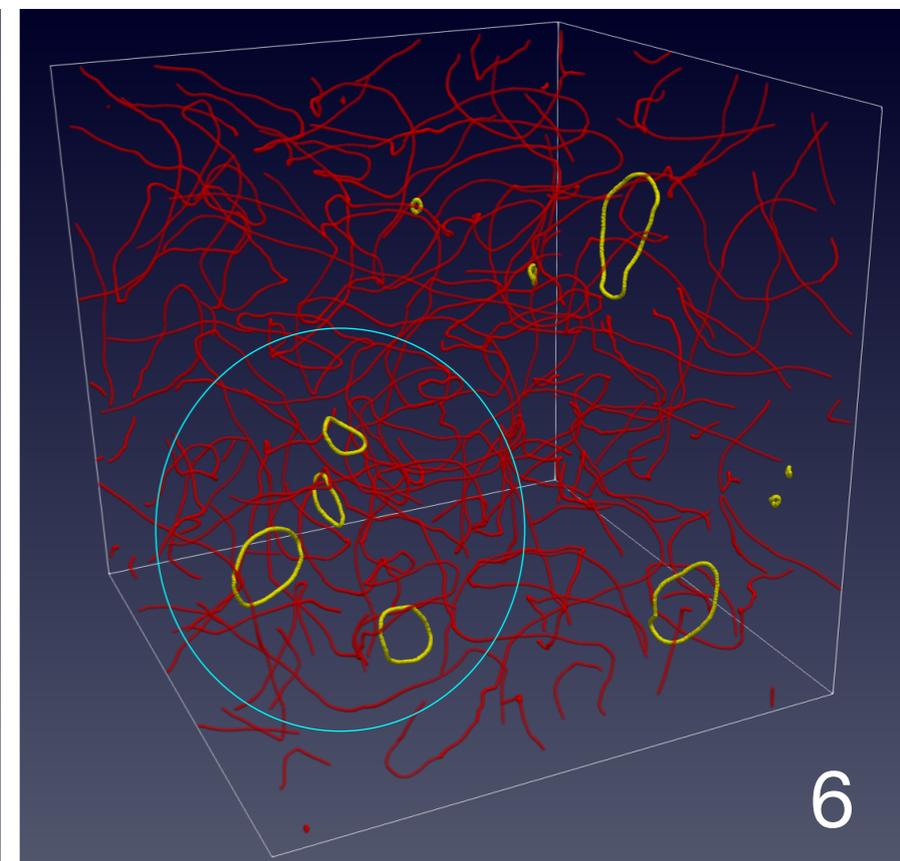
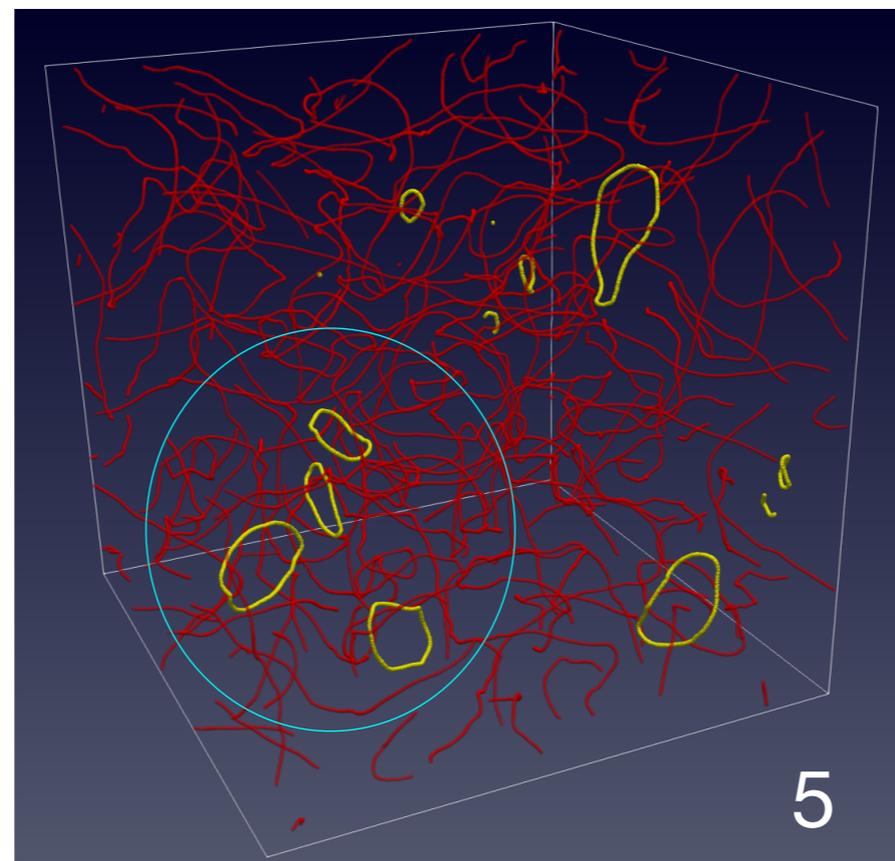
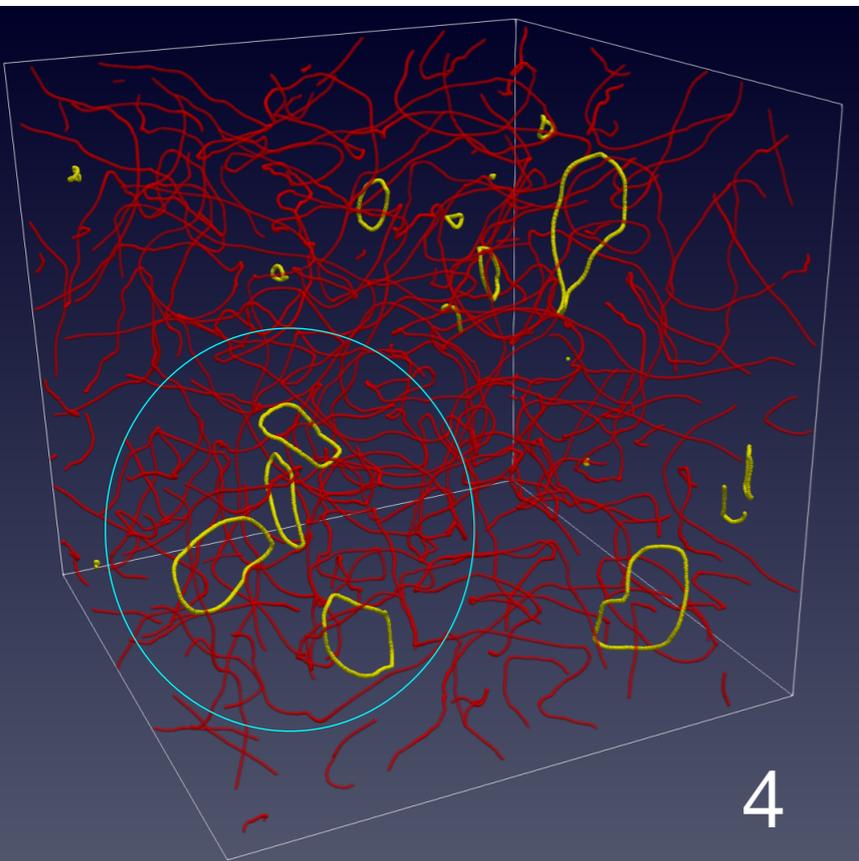
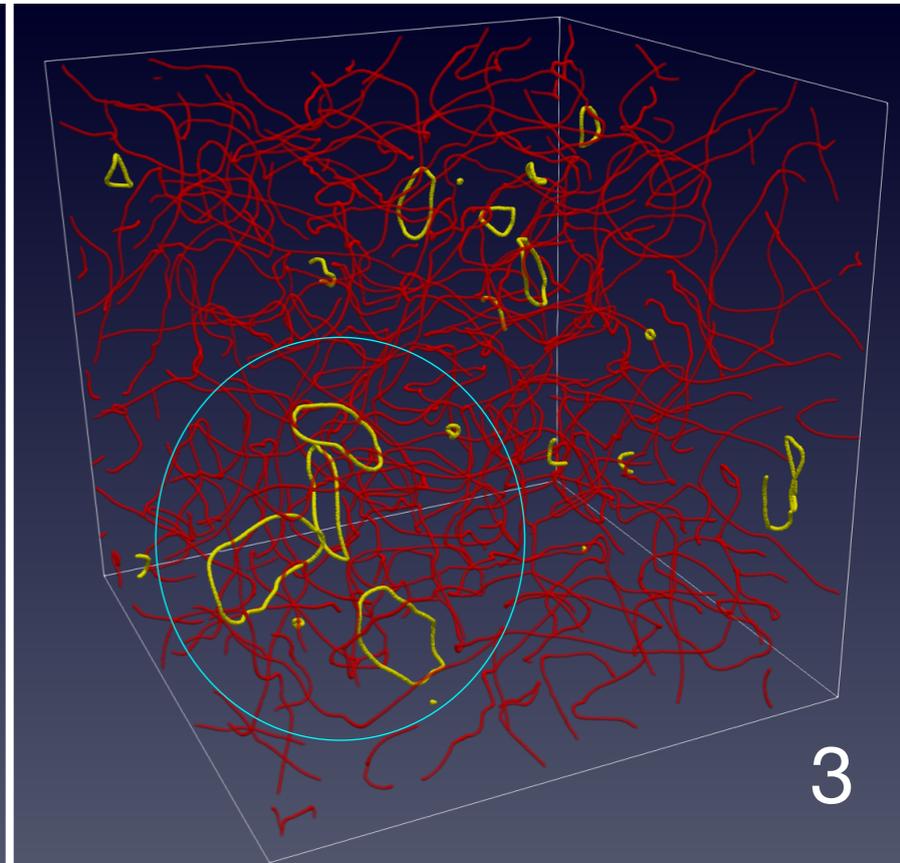
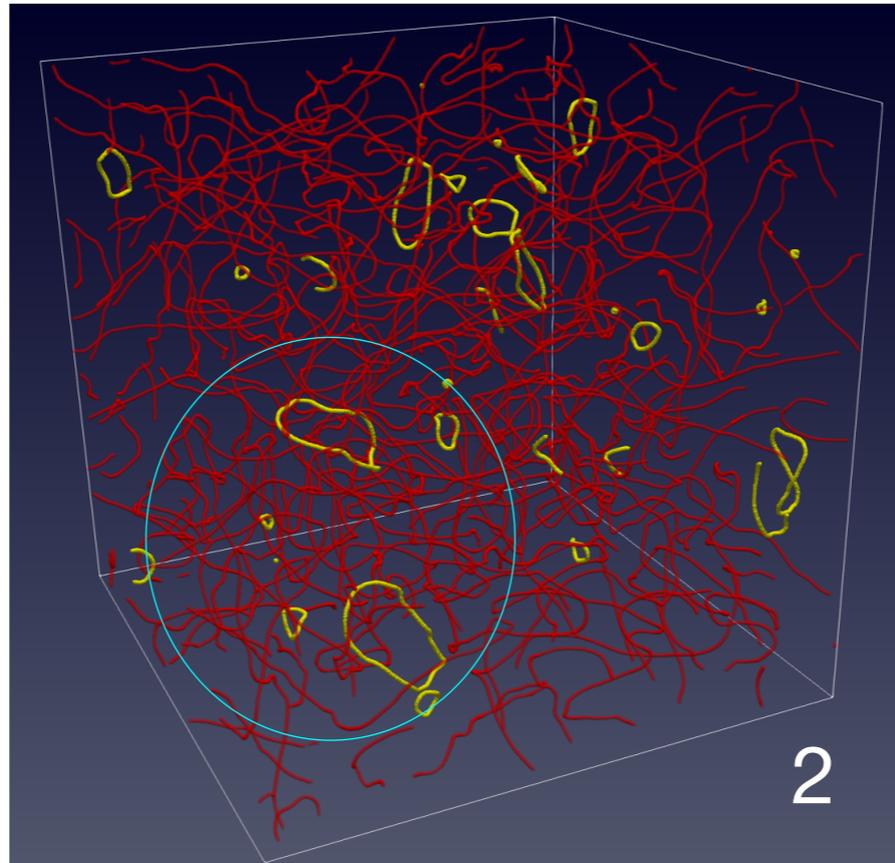
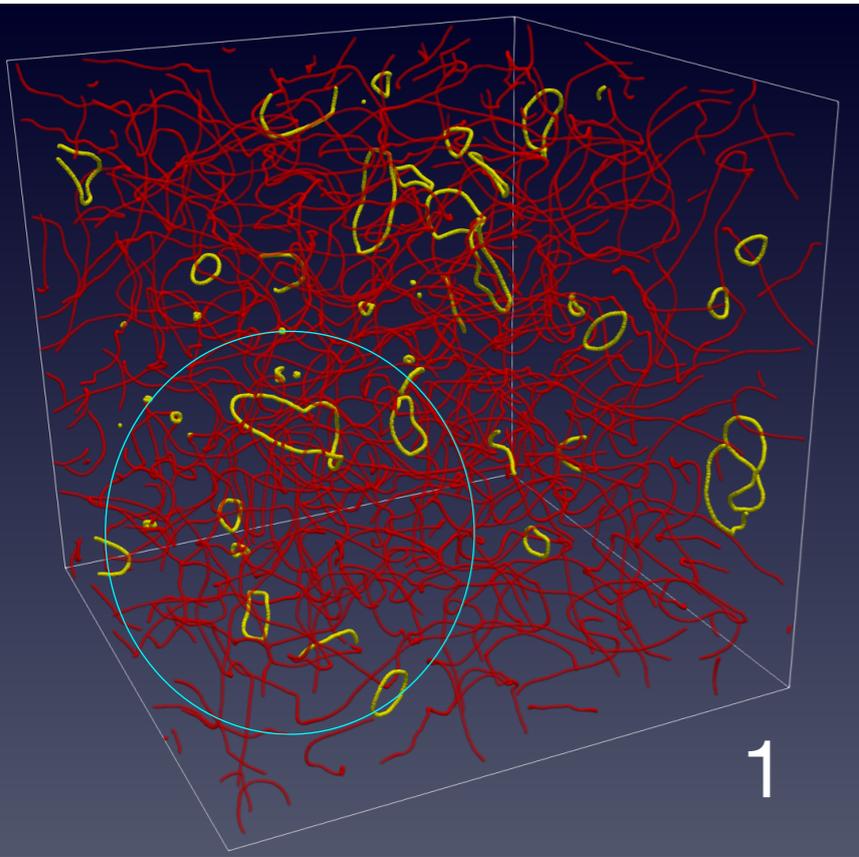


Loop production & decay

local string ($e=1$)



local string (e=1)

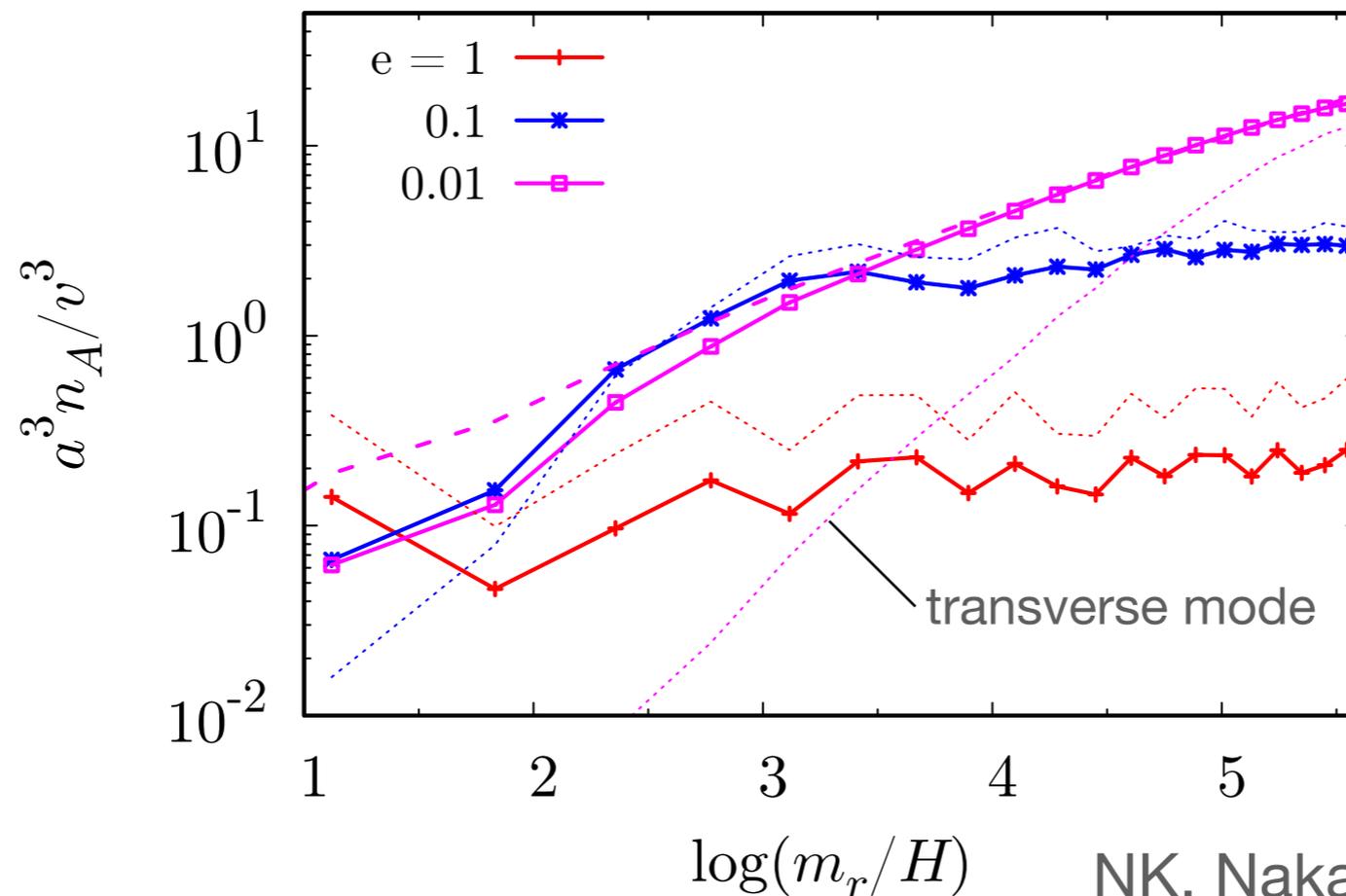


Emission of longitudinal vector boson

$$\rho_A^{(L)} = \frac{|\Phi|^2}{v^2} \left[\frac{2}{a^2} \left(\frac{\text{Im}(\Phi^* \Phi')}{|\Phi|} \right)^2 + \frac{1}{a^4} \left(E_i^{(L)} \right)^2 \right].$$

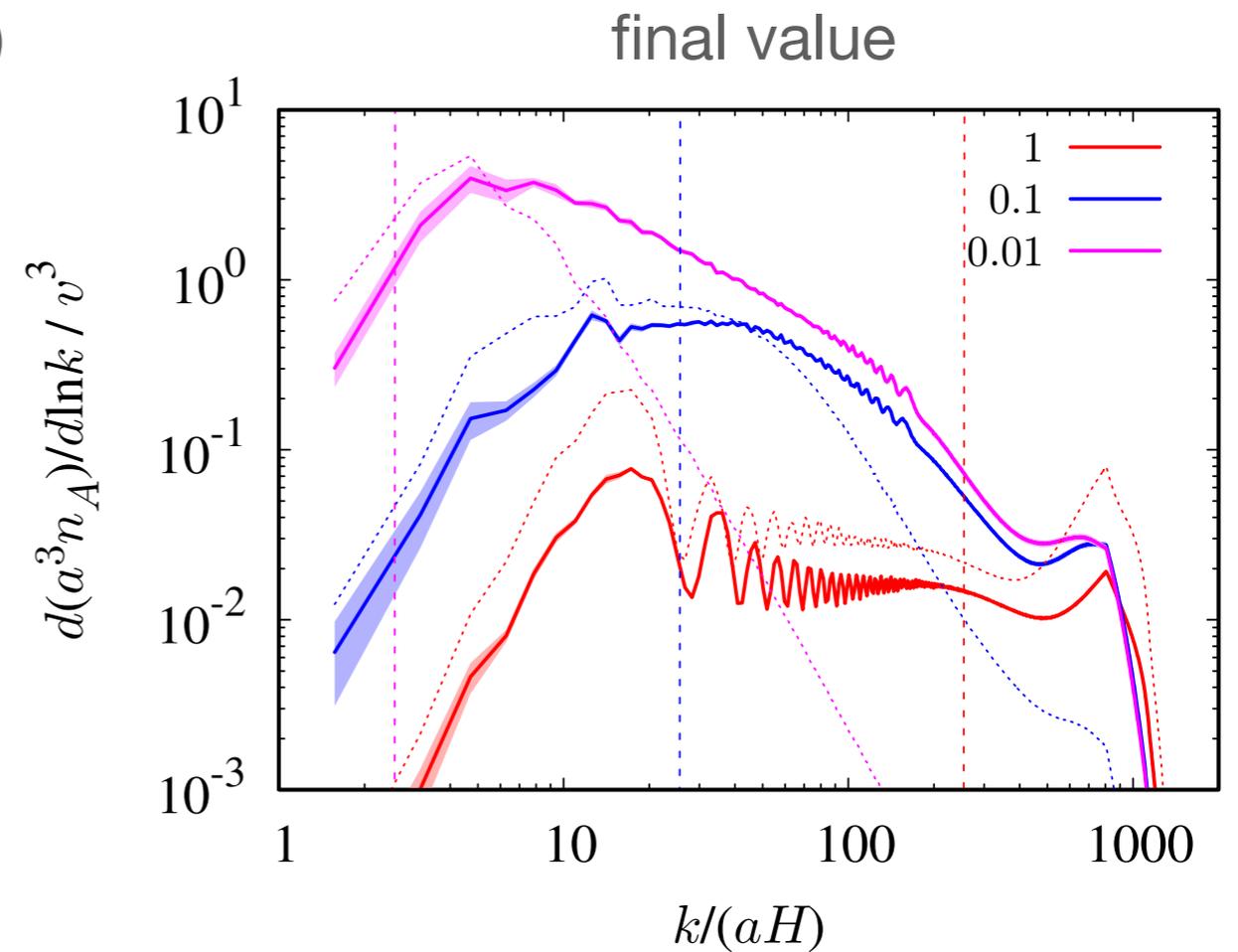
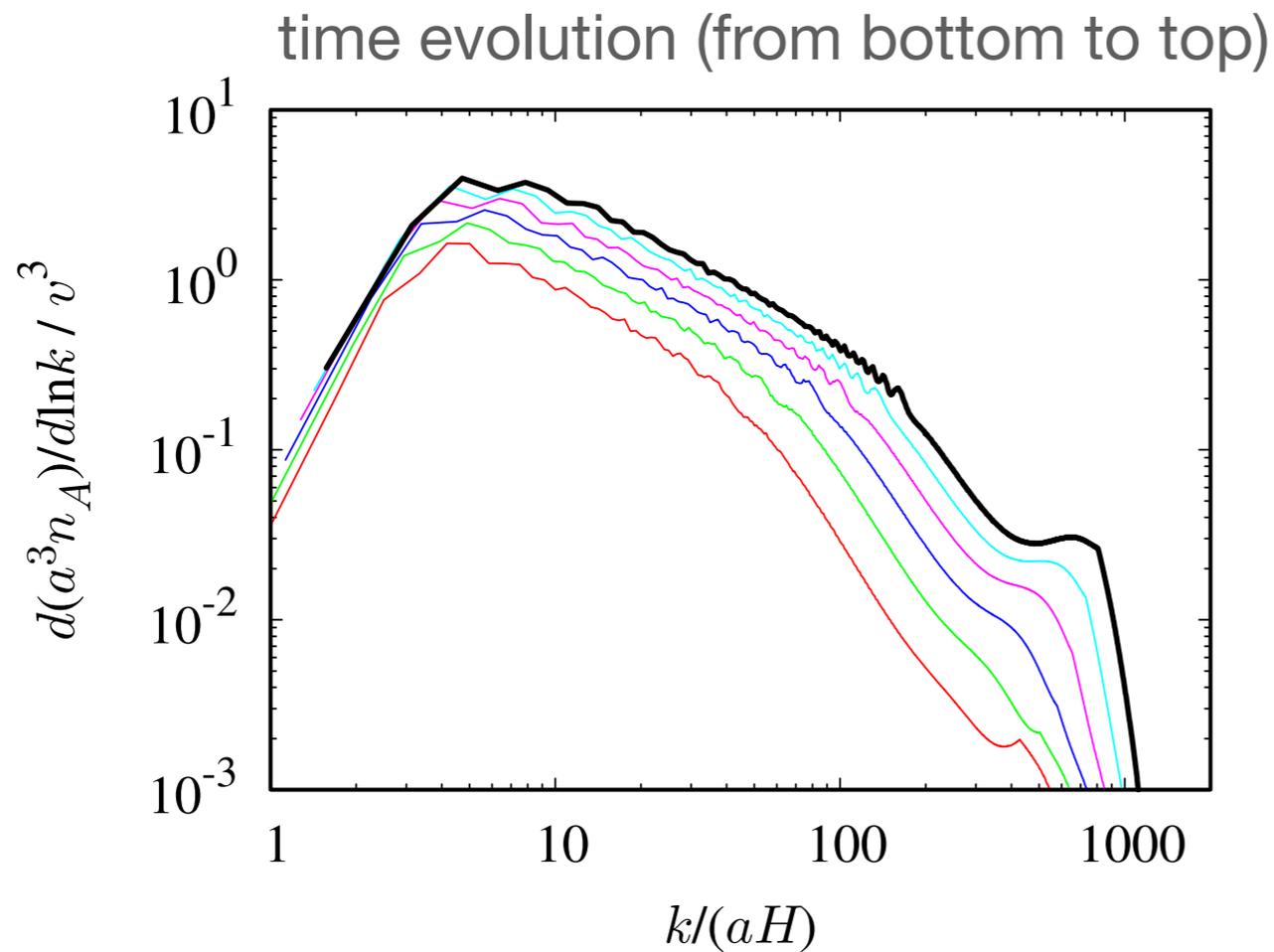
$$n_A = \int dk \frac{dn_A}{dk} = \int dk \frac{1}{E_A(k)} \frac{d\rho_A}{dk} \quad n_A^{(L)}(t) \simeq \frac{8\xi\mu H}{\bar{E}_A/H}$$

(analytic estimation)



Spectrum of emitted dark photon

NK, Nakayama 2212.13573



peak wavenumber: $k/a \sim 10H$ \longleftrightarrow typical loop size: $\ell \sim 0.1H^{-1}$

