

# Primordial black holes and gravitational waves from long-range scalar forces

Focus Week on Primordial Black Holes  
Kavli IPMU

Marcos M. Flores — 14th, Nov., 2023

# Primordial black holes & early structure formation

[MMF, A. Kusenko: PRL 126 (2021) 4, 041101]

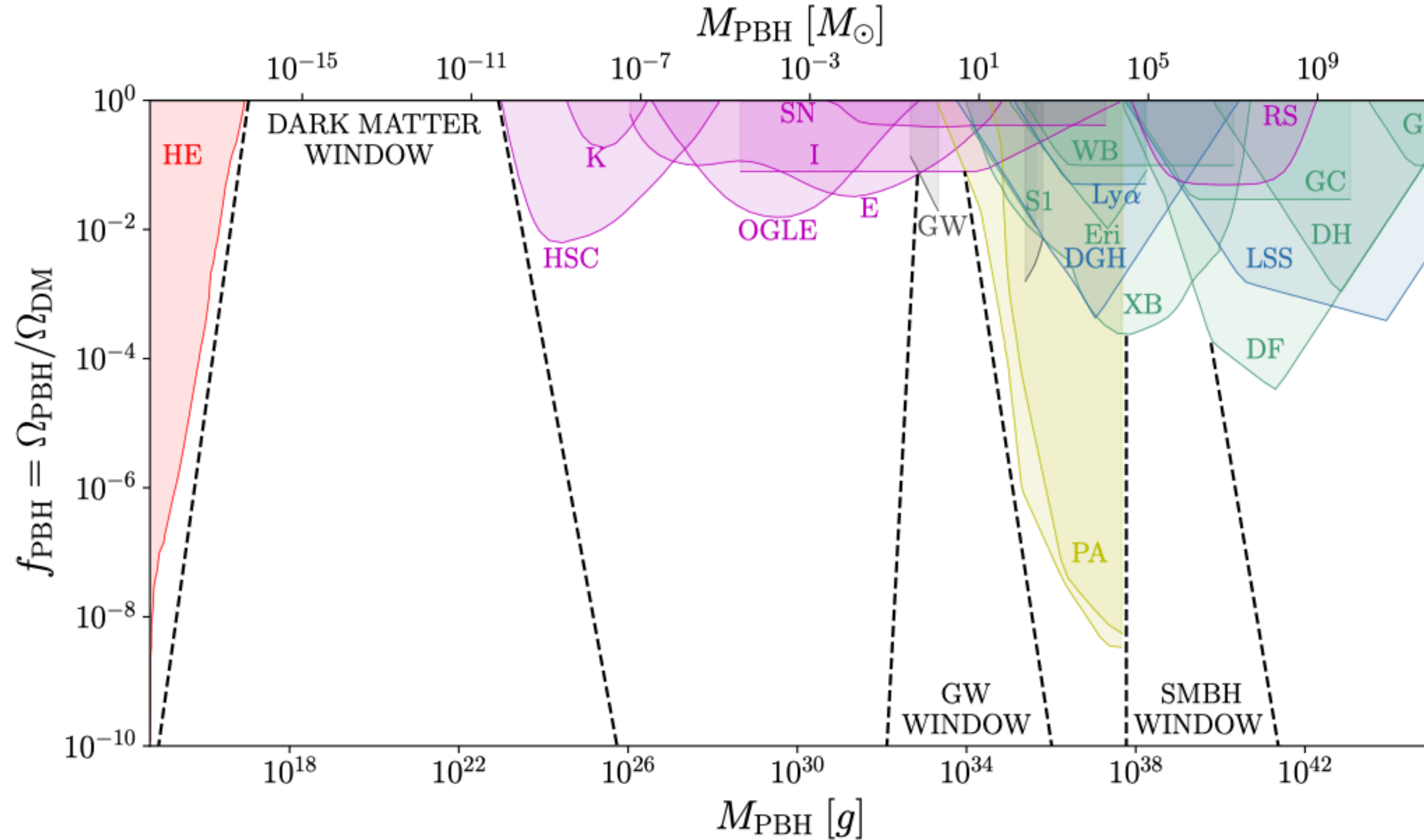
[MMF, A. Kusenko: *JCAP* 05 (2023) 013]

[MMF, Y. Lu, A. Kusenko: arXiv:2308.09094]

# Primordial black holes: An overview

- PBHs are black holes formed in the *early Universe* before the formation of stars and galaxies [Zel'dovich, Novikov (1967); Hawking (1971)]
- Can account for some or all of *dark matter*
- Astrophysical implications:
  - Can account for some LIGO events
  - Can seed supermassive black holes
  - Can account for all or part of *r*-process nucleosynthesis
  - *G* objects (discussed later)
  - Many more!

# Primordial black holes: An overview



# Primordial black holes: Formation

- PBH formation appears to be a generic feature of many existing theories
  - i.e., inflation, supersymmetry, first-order phase transitions, confinement
    - Just see the Focus Week on PBH Timetable!
- **Goal:** Develop a generic, distinguishable, scenario for PBH formation

⇒ early structure formation

The paradigm of  
*early*  
structure formation

# Cosmological timeline

*“Early”*

**Structure Formation**

10<sup>-32</sup> seconds

1 second

100 seconds

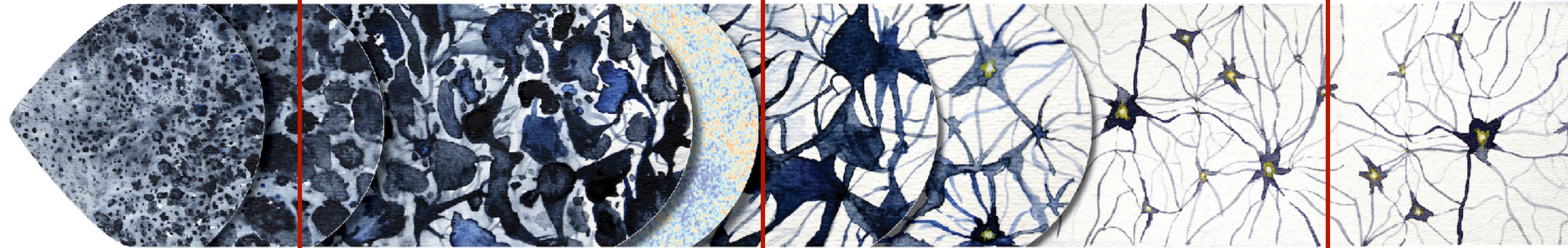
380 000 years

300–500 million years

Billions of years

13.8 billion years

Beginning of the Universe



## Inflation

Accelerated expansion of the Universe

## Formation of light and matter

## Light and matter are coupled

Dark matter evolves independently: it starts clumping and forming a web of structures

## Light and matter separate

- Protons and electrons form atoms
- Light starts travelling freely: it will become the Cosmic Microwave Background (CMB)

## Dark ages

Atoms start feeling the gravity of the cosmic web of dark matter

## First stars

The first stars and galaxies form in the densest knots of the cosmic web

## Galaxy evolution

## The present Universe

***Most interesting second in the history of the Universe***

# Conventional structure formation: Basics

$$\rho(x, t) = \bar{\rho}(t) (1 + \delta(x, t))$$

⇓

$$G_{\mu\nu} = 8\pi G T_{\mu\nu}, \quad \nabla_{\mu} T^{\mu\nu} = 0$$

⇓

System of Coupled Differential Equations

$$(\delta(x, t) \ll 1)$$



# Conventional structure formation by example

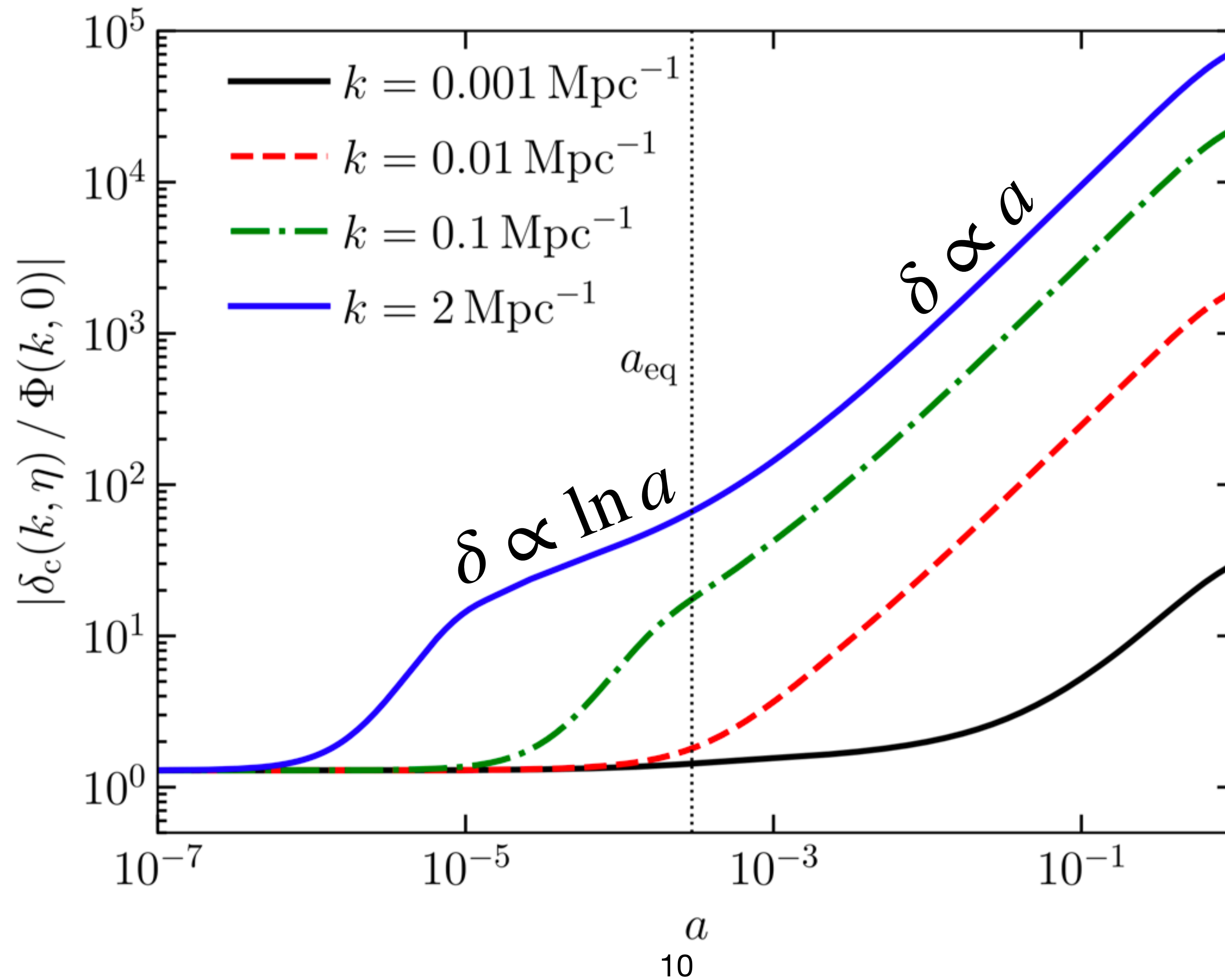
$$\ddot{\delta} + 2H\dot{\delta} = 4\pi G\bar{\rho}_m\delta, \quad H = \frac{1}{2t}, \quad \bar{\rho}_m \sim \Omega_m \sim 0$$



$$\delta(t) = c_1 + c_2 \ln t$$

**Conclusion:** *Matter perturbations only grow logarithmically during a radiation dominated era*

# Conventional structure formation by example



[Credit: Dodelson, Modern Comology]

How can you have early structure formation?

# How can you have early structure formation?

$$\mathcal{L} \supset y\chi\bar{\psi}\psi \implies V(r) = -\frac{y^2}{4\pi r} \exp(-m_\chi r)$$

$r \ll m_\chi^{-1} \iff$  long-range force

$$\implies H^{-1} \ll m_\chi^{-1}$$

# How can you have early structure formation?

$$\mathcal{L} \supset y\chi\bar{\psi}\psi \implies V(r) = -\frac{y^2}{4\pi r}\exp(-m_\chi r)$$

Yukawa interactions are *always* attractive

$$\beta \equiv y \left( M_{\text{Pl}}/m_\psi \right)$$

# Initial conditions for primordial structure formation

- Before the formation of structure can occur, we require:
  - $\bar{\psi}\psi \leftrightarrow \chi\chi$  interactions to freeze-out
  - $\psi$  particles become non-relativistic
  - $\chi$ -radiation pressure is negligible.
- We anticipate that early structure formation begins when  $T \sim m_\psi$

# Growth of perturbations

- In Fourier space, the growth of  $\psi$  overdensities, denoted  $\Delta(x, t) = \Delta n_\psi / n_\psi$  are given by a set of coupled differential equations:

$$\ddot{\delta}_k + 2H\dot{\delta}_k - \frac{3}{2}H^2(\Omega_r\delta_k + \Omega_m\Delta_k) = 0$$

$$\ddot{\Delta}_k + 2H\dot{\Delta}_k - \frac{3}{2}H^2[\Omega_r\delta_k + \Omega_m(1 + \beta^2)\Delta_k] = 0$$

[L. Amendola et. al., arXiv:1711.09915]

[S. Savastano et. al., arXiv:1906.05300]

[Domenech and Sasaki, arXiv:2104.05271]

# Growth of perturbations

- For large scalar forces, the perturbations grow quickly as demonstrated by the approximate solution:

$$\Delta_k(t) \approx \frac{\Delta_k(t_0)}{\sqrt{8\pi}} \frac{\exp\left(4\sqrt{p}(t/t_{\text{eq}})^{1/4}\right)}{p^{1/4}(t/t_{\text{eq}})^{1/8}}, \quad p = \frac{3}{8} \underline{(1 + \beta^2)}$$

For  $p \gg 1 \implies \Delta_k / \dot{\Delta}_k \ll H^{-1} \implies$  rapid structure formation



# Growth of perturbations

$$\Delta_k \ll 1 \implies \Delta_k \gtrsim 1 \iff \text{nonlinear regime} \implies \text{virialize}$$

***Without dissipation***, halos will remain viralized until the constituent particles decay

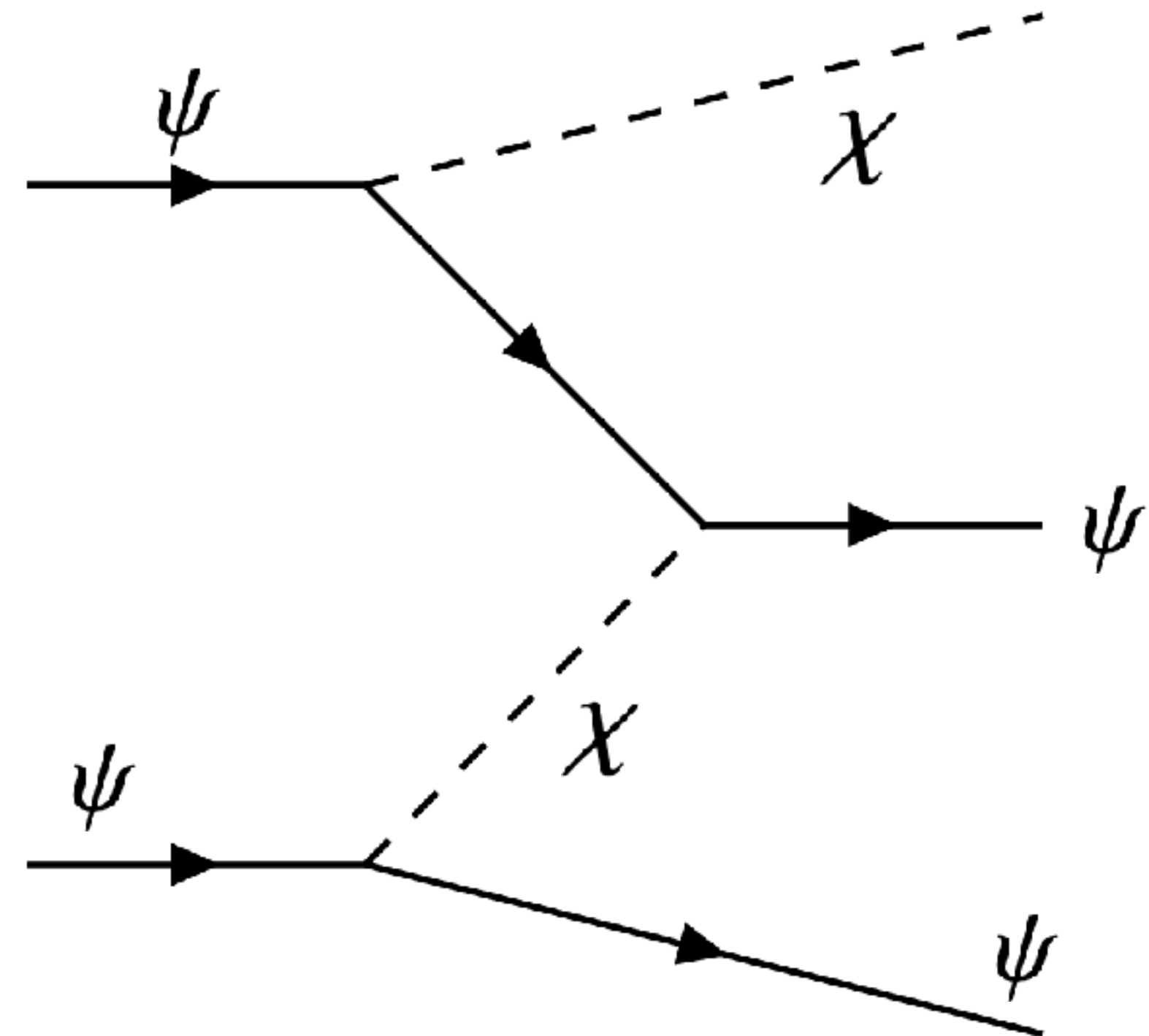
# Energy dissipation through scalar radiation

The same long-range force that cause the growth of structure will also cause accelerating particles to emit scalar waves

There are *five* possible dissipation channels:

1. Coherent motion
2. Incoherent motion
3. Bremsstrahlung (free-free) emission
4. Bound state formation
5. Surface radiation

Bremsstrahlung and surface radiation will be the most important channels for our discussion



# Energy dissipation through scalar radiation

The same long-range force that cause the growth of structure will also cause accelerating particles to emit scalar waves

There are *five* possible dissipation channels:

1. Coherent motion
2. Incoherent motion
3. Bremsstrahlung (free-free) emission
4. Bound state formation
5. Surface radiation

$$\tau_{\text{cool}} = \frac{E}{P_{\text{brem}} + P_{\text{surf}} + \dots}$$

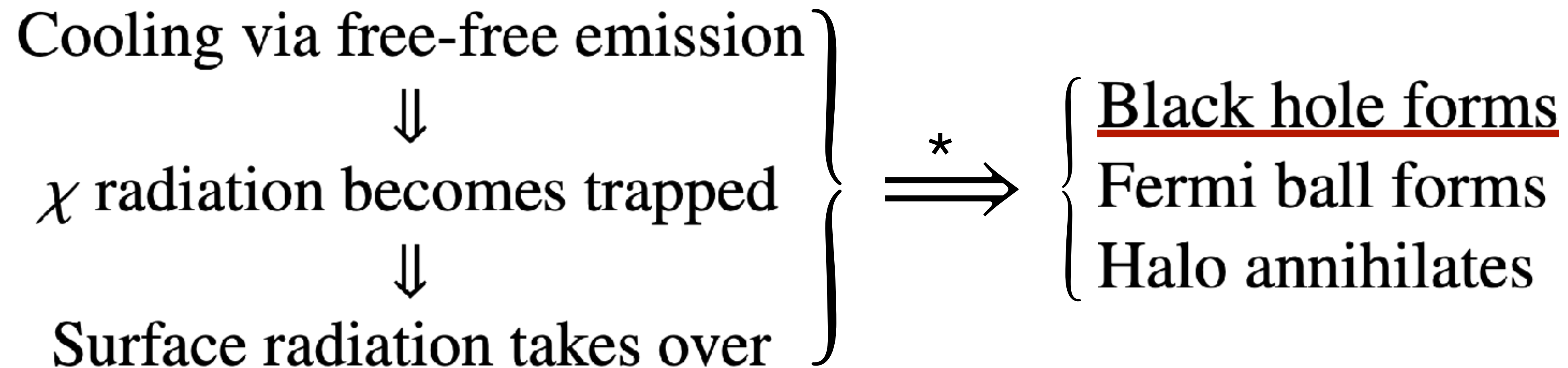
Bremsstrahlung and surface radiation will be the most important channels for our discussion

# Energy dissipation through scalar radiation

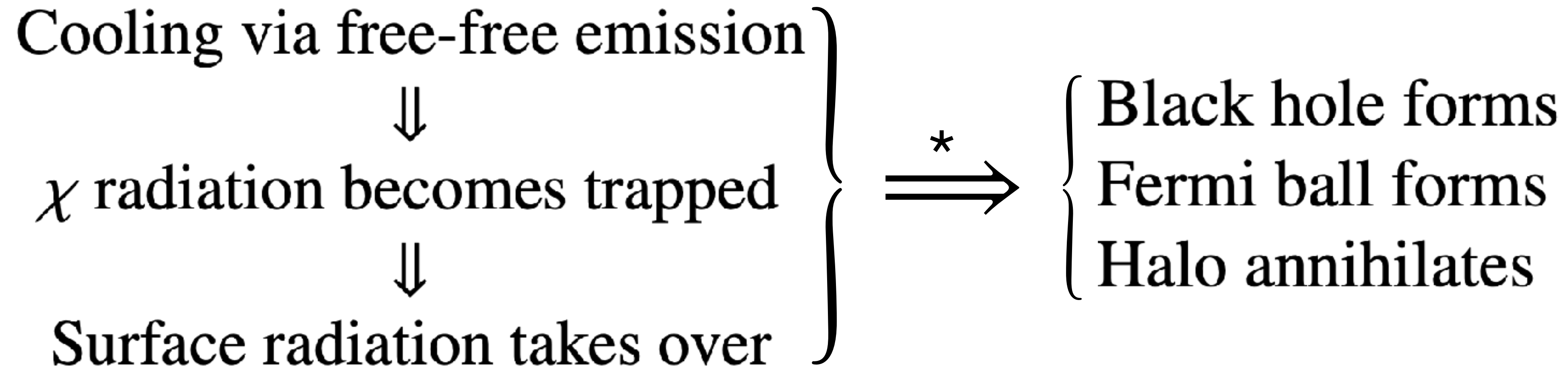
Given a halo of size  $R$  can lose energy and contract as long as,

$$\tau_{\text{cool}}(R) \ll H^{-1}$$

General algorithm for collapse:



# PBH Formation: primordial structure formation



To *ensure* that a black hole forms, we will introduce an *asymmetric dark fermion*  $\psi$

$$\mathcal{L} \supset y\chi\bar{\psi}\psi \quad \& \quad \eta_\psi = (n_\psi - n_{\bar{\psi}})/s \neq 0$$

Yukawa Interaction & Scalar Cooling + Fermion Asymmetry  $\Rightarrow$  PBHs

# PBH abundance

- The strength of the long-range force we are considering is likely strong enough to capture all of the dark matter  $\psi$  particles in halos and therefore PBHs.
- Thus, the PBH-dark matter fraction is related to the baryon density:

$$f_{\text{PBH}} = \frac{\Omega_{\text{PBH}}}{\Omega_{\text{DM}}} = 0.2 \frac{m_{\psi} \eta_{\psi}}{m_p \eta_B} = \left( \frac{m_{\psi}}{5 \text{ GeV}} \right) \left( \frac{\eta_{\psi}}{10^{-10}} \right)$$

- Our mechanism can describe the closeness of  $\Omega_{\text{DM}}$  and  $\Omega_B$ .

# PBH Mass Distribution

- Again, the strength of the scalar interaction will lead to rapid PBH formation. Thus, we expect the mass function of PBHs to represent the structure of the  $\psi$  - fluid at the time of formation.
- We need  $N$ -body simulations to accurately describe the details of  $\psi$  - structure formation.
- In the absence of this, we will approximate the mass function using the Press-Schechter function:

$$M^2 \frac{dN_h}{dM} \propto \frac{1}{\sqrt{\pi}} \left( \frac{M}{M_*} \right)^{1/2} e^{-M/M_*}$$

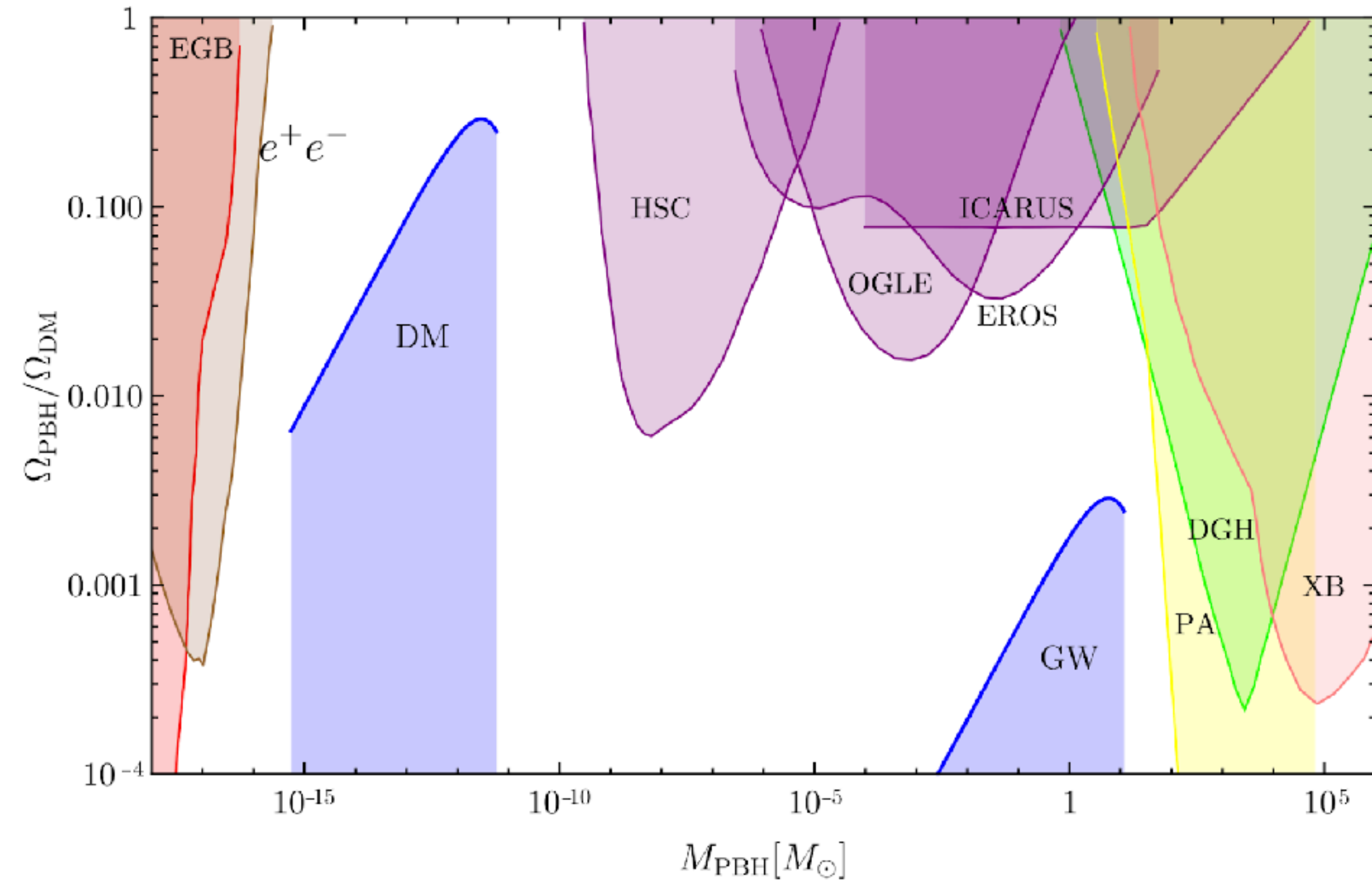
# Illustrative examples

- PBH dark matter:

$$\left. \begin{array}{l} \eta_\psi \sim \eta_B \sim 10^{-10} \\ m_\psi = 5 \text{ GeV} \end{array} \right\} f_{\text{PBH}} = 1$$

- Relevant to LIGO

$$\left. \begin{array}{l} \eta_\psi \sim 10^{-9} \\ m_\psi = 5 \text{ MeV} \end{array} \right\} f_{\text{PBH}} \sim 10^{-3}$$





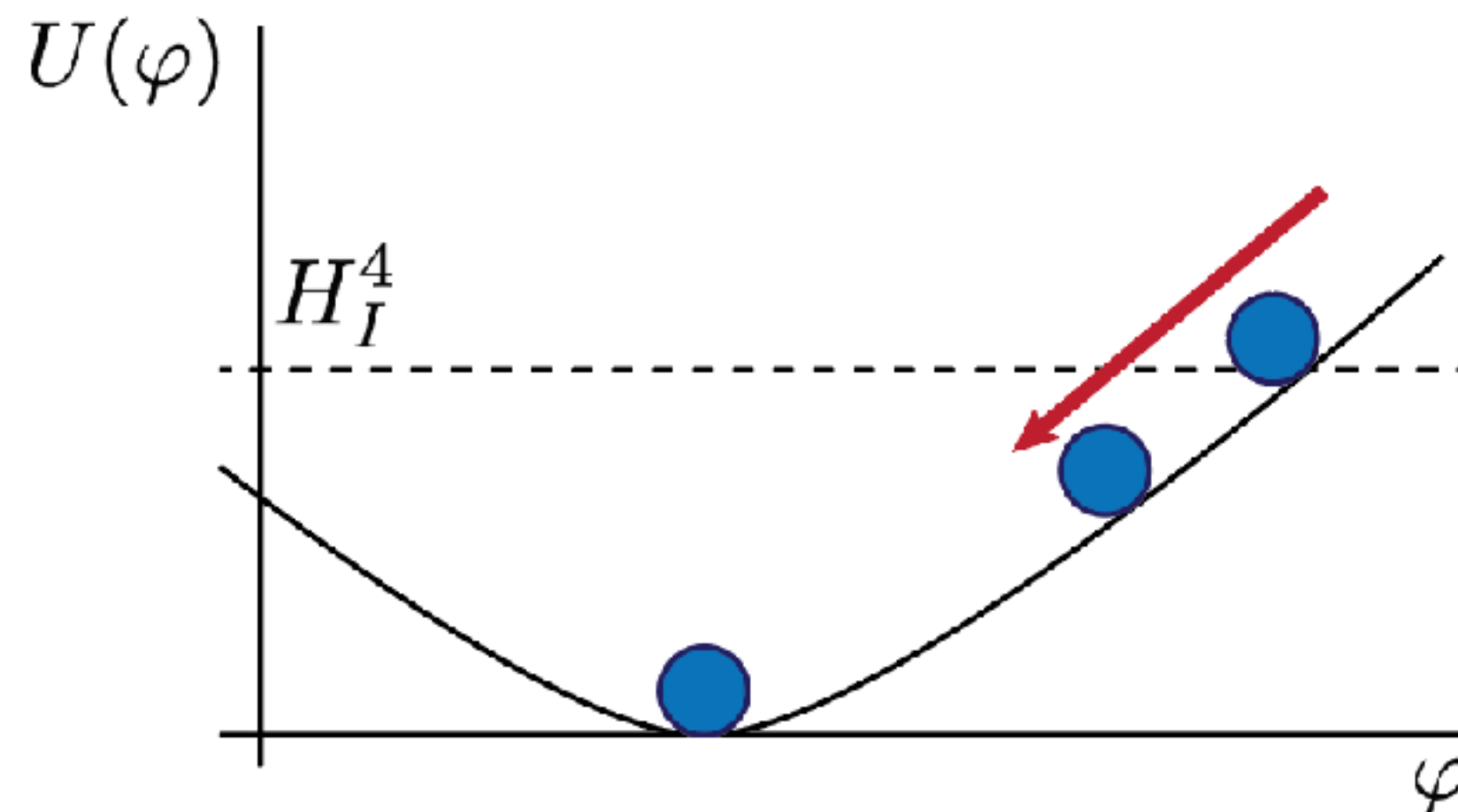
# Primordial black holes, scalar forces & supersymmetry

[MMF, A. Kusenko: *JCAP* 05 (2023) 013]

[MMF, A. Kusenko, L. Pearce, Y. F. Perez-Gonzales, G. White: arXiv: 2308.15522, Accepted PRD]

# PBHs from Scalar Forces & SUSY Q-balls

- Utilize well understood dynamics of scalar fields in early Universe
  - The initial conditions of this scenario are *very similar* to Affleck-Dine baryogenesis. See [M. Dine, A. Kusenko hep-ph/0303065]
  - Scalar fields are generic inclusion if BSM physics
  - In particular, supersymmetry — contains many scalar fields with 100+ flat directions [Gherghetta et. al '95] which are *lifted* by SUSY breaking terms



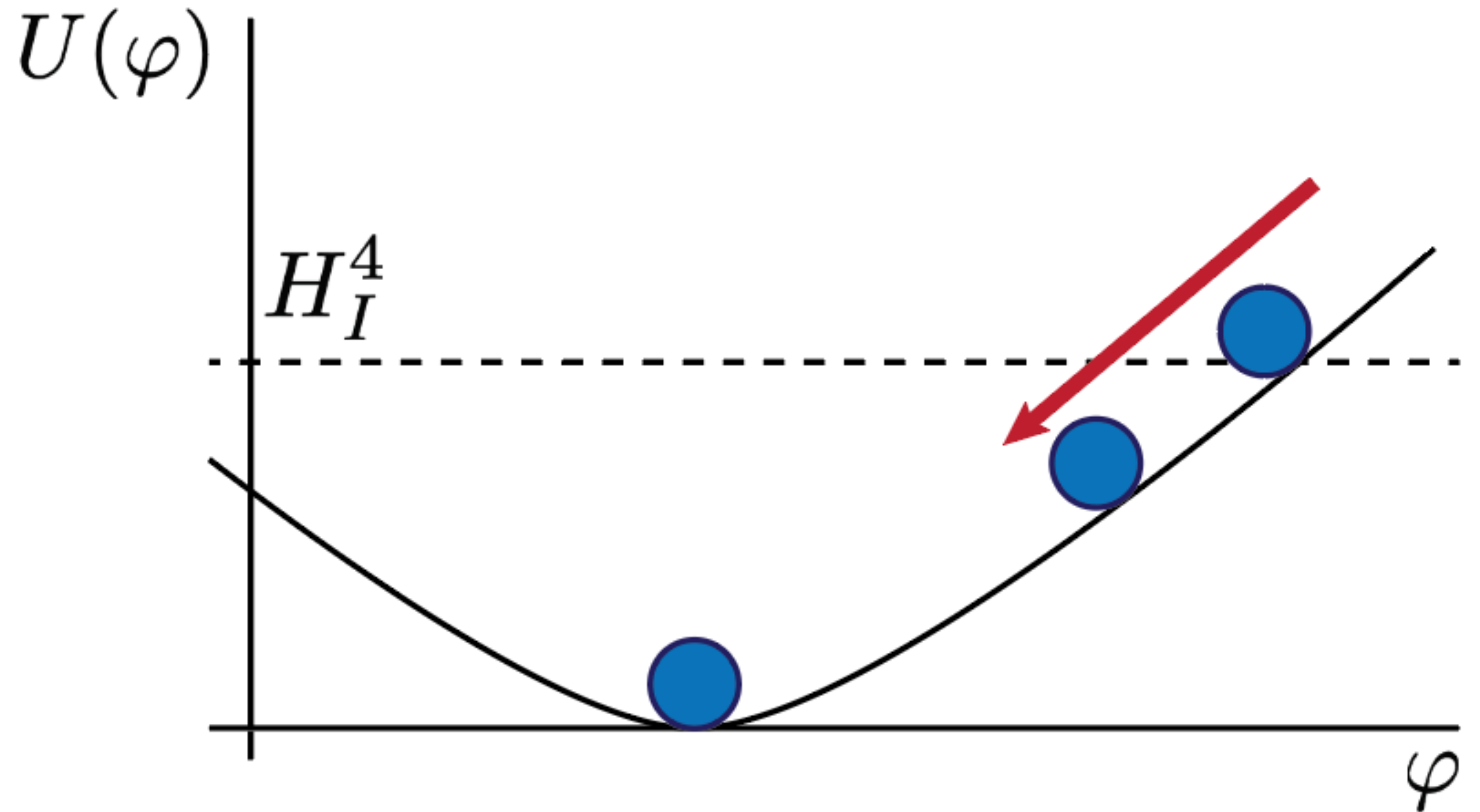
**Key:** Scalar fields acquire a VEV in de Sitter space during inflation

# Scalar fields in de Sitter space during inflation

$$U(\langle\varphi\rangle) \sim H_I^4$$

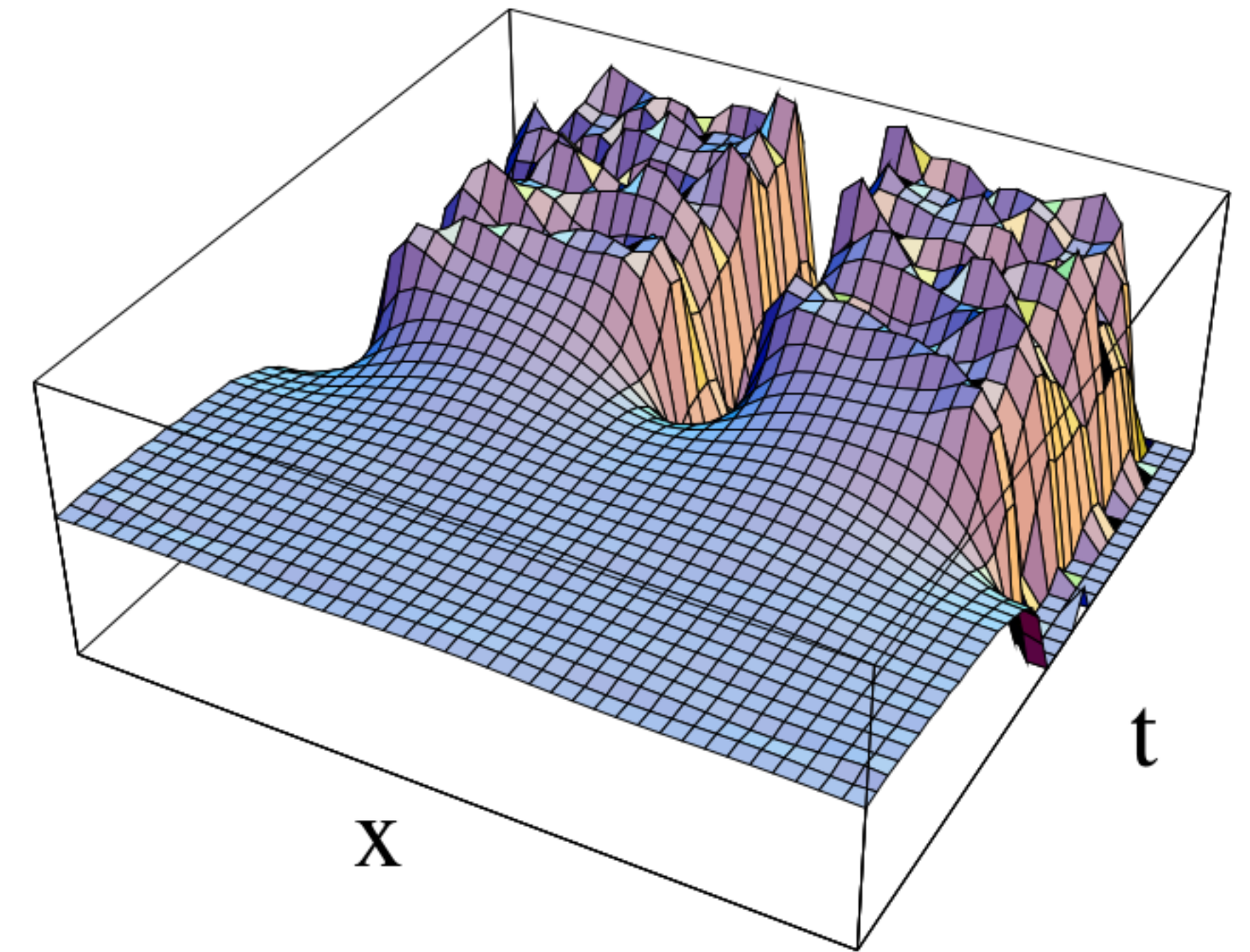
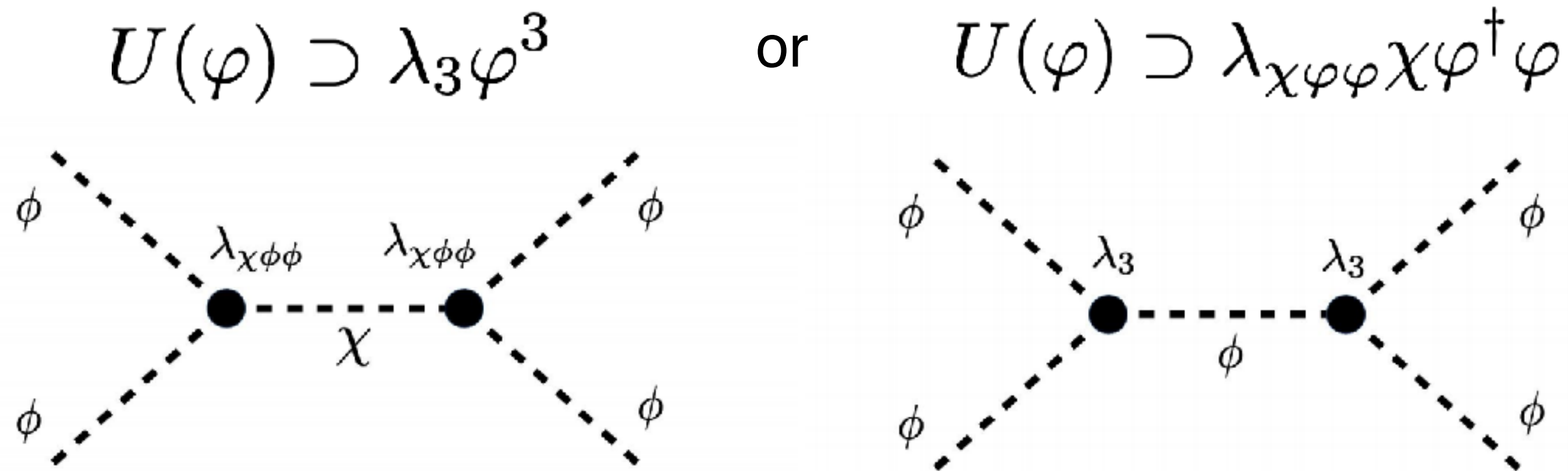
&

$$H_I = \sqrt{\frac{U_{\text{tot}}}{3M_{\text{Pl}}^2}} \approx \sqrt{\frac{U_I(\Phi_I)}{3M_{\text{Pl}}^2}}$$



# Scalar fields and fragmentation

- Attractive forces induce an *instability* in scalar condensate

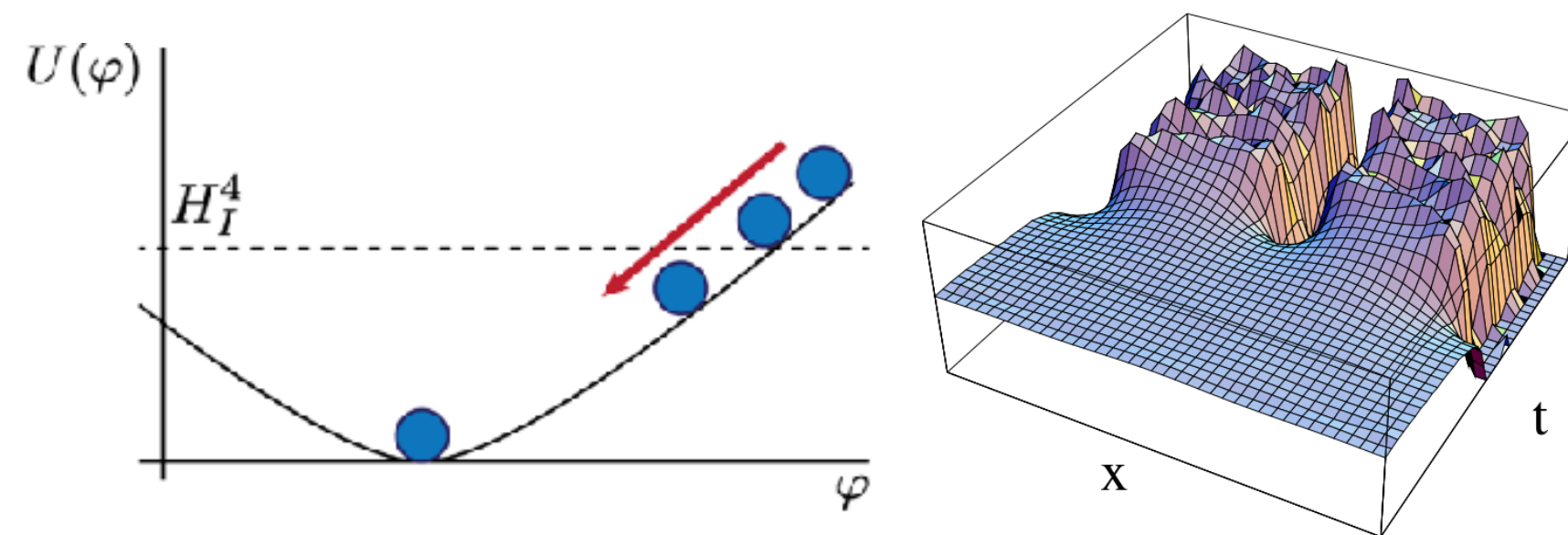


$\implies$  Leads to the formation of Q-balls

# From inflation to Q-balls

$$U(\langle\varphi\rangle) \sim H_I^4$$

Inflation  
&  
Development of Large VEV



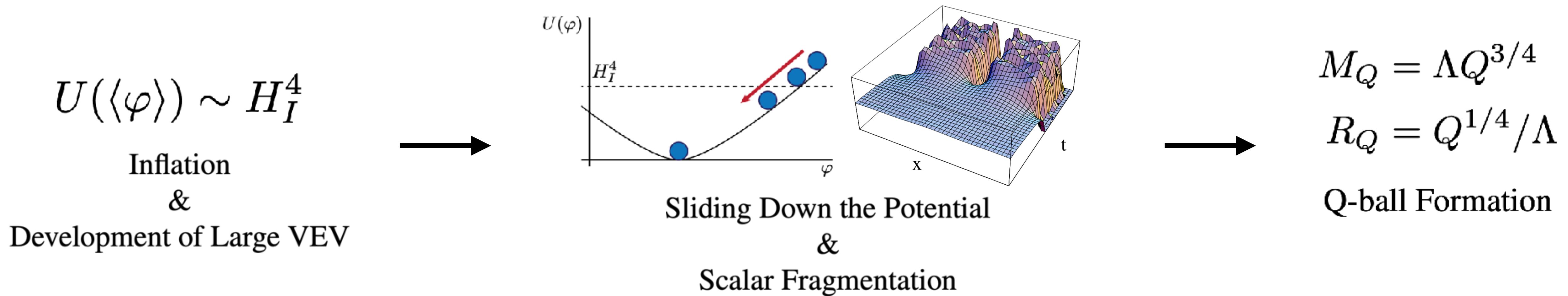
Sliding Down the Potential  
&  
Scalar Fragmentation



$$M_Q = \Lambda Q^{3/4}$$
$$R_Q = Q^{1/4} / \Lambda$$

Q-ball Formation

# From inflation to Q-balls



Intermediate matter domination & gravitational forces *can* produce PBHs

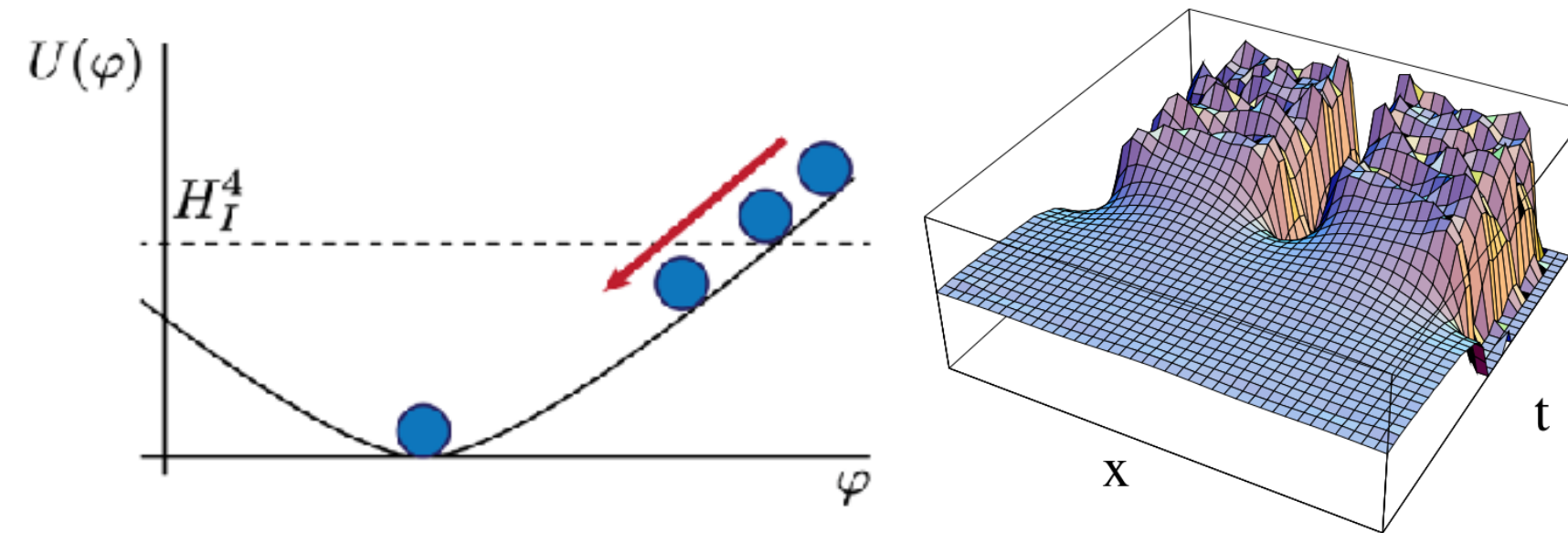
$\implies$  *but* it's very inefficient

$\implies$  need special, spherical configurations

# From inflation to Q-balls

$$U(\langle\varphi\rangle) \sim H_I^4$$

Inflation  
&  
Development of Large VEV



Sliding Down the Potential  
&  
Scalar Fragmentation



$$M_Q = \Lambda Q^{3/4}$$

$$R_Q = Q^{1/4} / \Lambda$$

Q-ball Formation



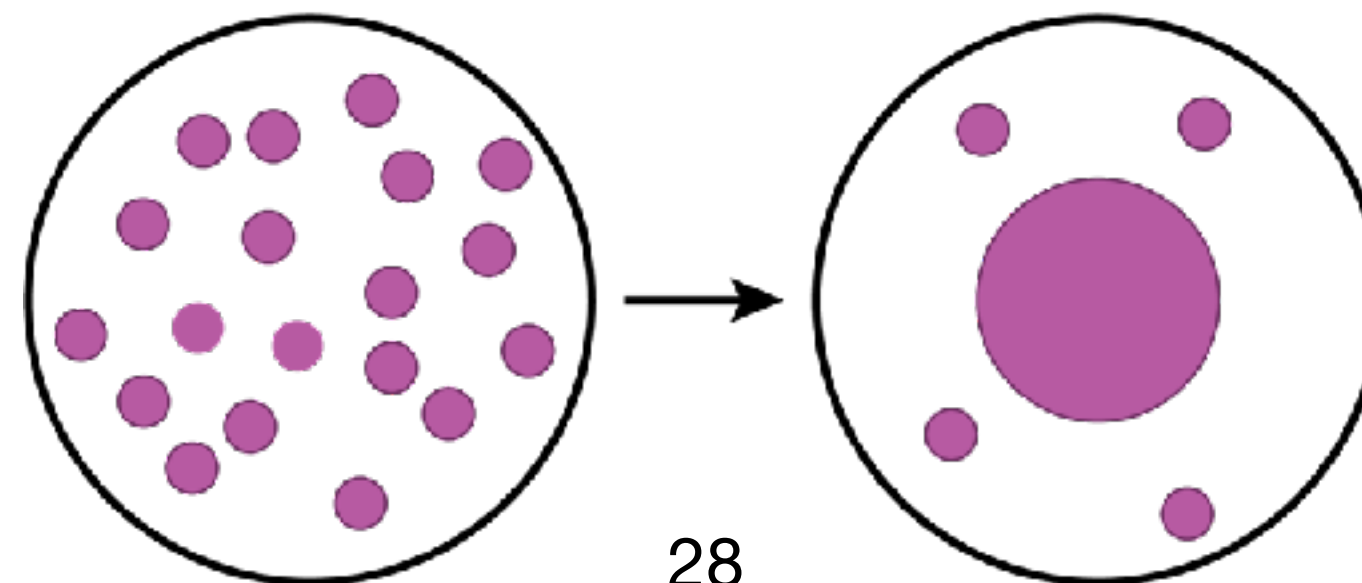
Scalar Forces  
&  
Scalar Radiation

$$\tau_{\text{cool}} = \frac{E}{dE/dt}$$

$$= \frac{E}{P_{\text{brem}} + P_{\text{surf}} + \dots}$$



Mergers lead to  
larger and larger charges



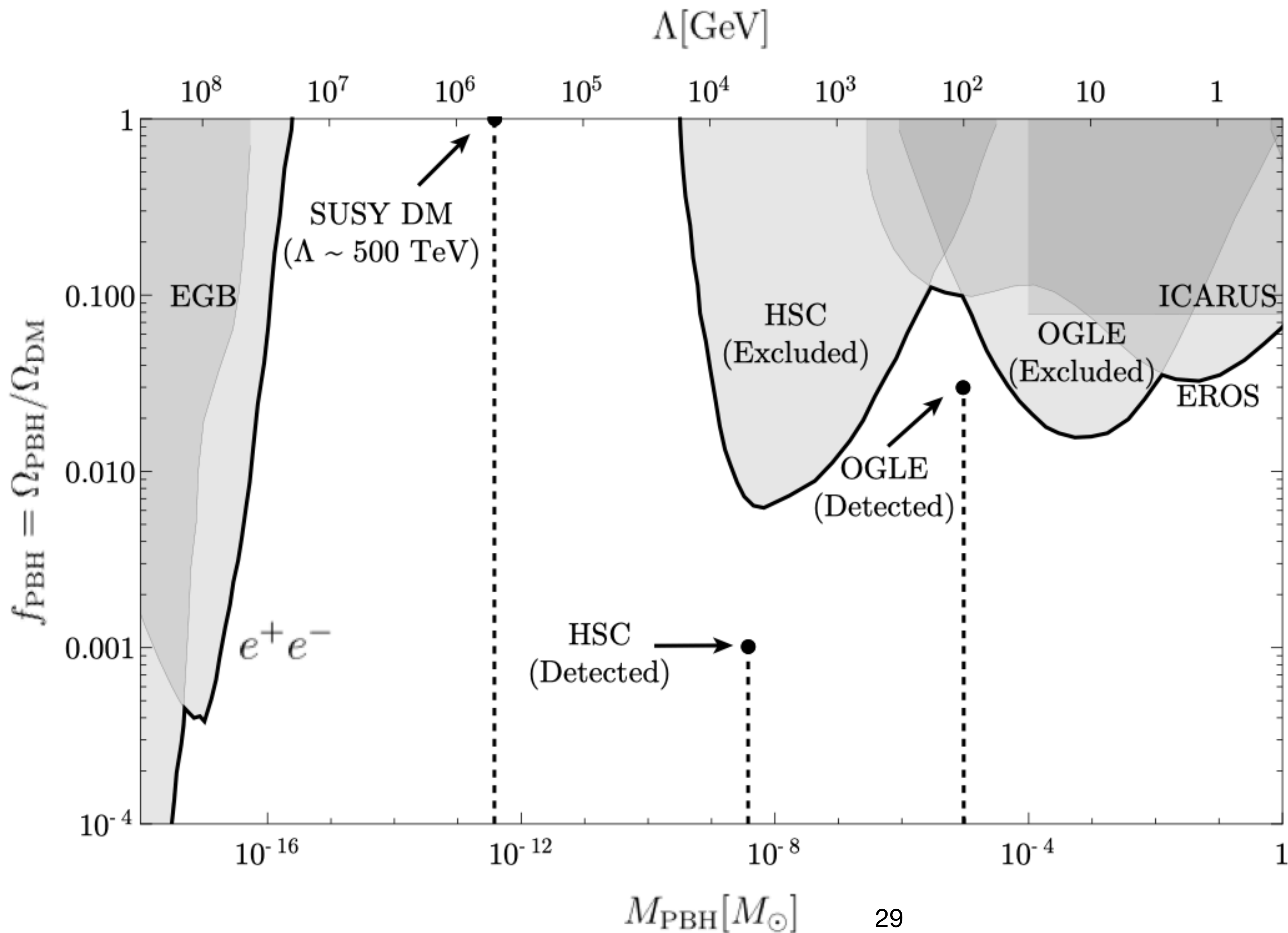
28



PBH Formation

$$M_{\text{PBH}} \sim 10^{22} g \left( \frac{100 \text{ TeV}}{\Lambda} \right)^2$$

# PBHs from Scalar Forces & SUSY Q-balls



$$M_{\text{PBH}} \sim 10^{22} \text{ g} \left( \frac{100 \text{ TeV}}{\Lambda} \right)^2$$



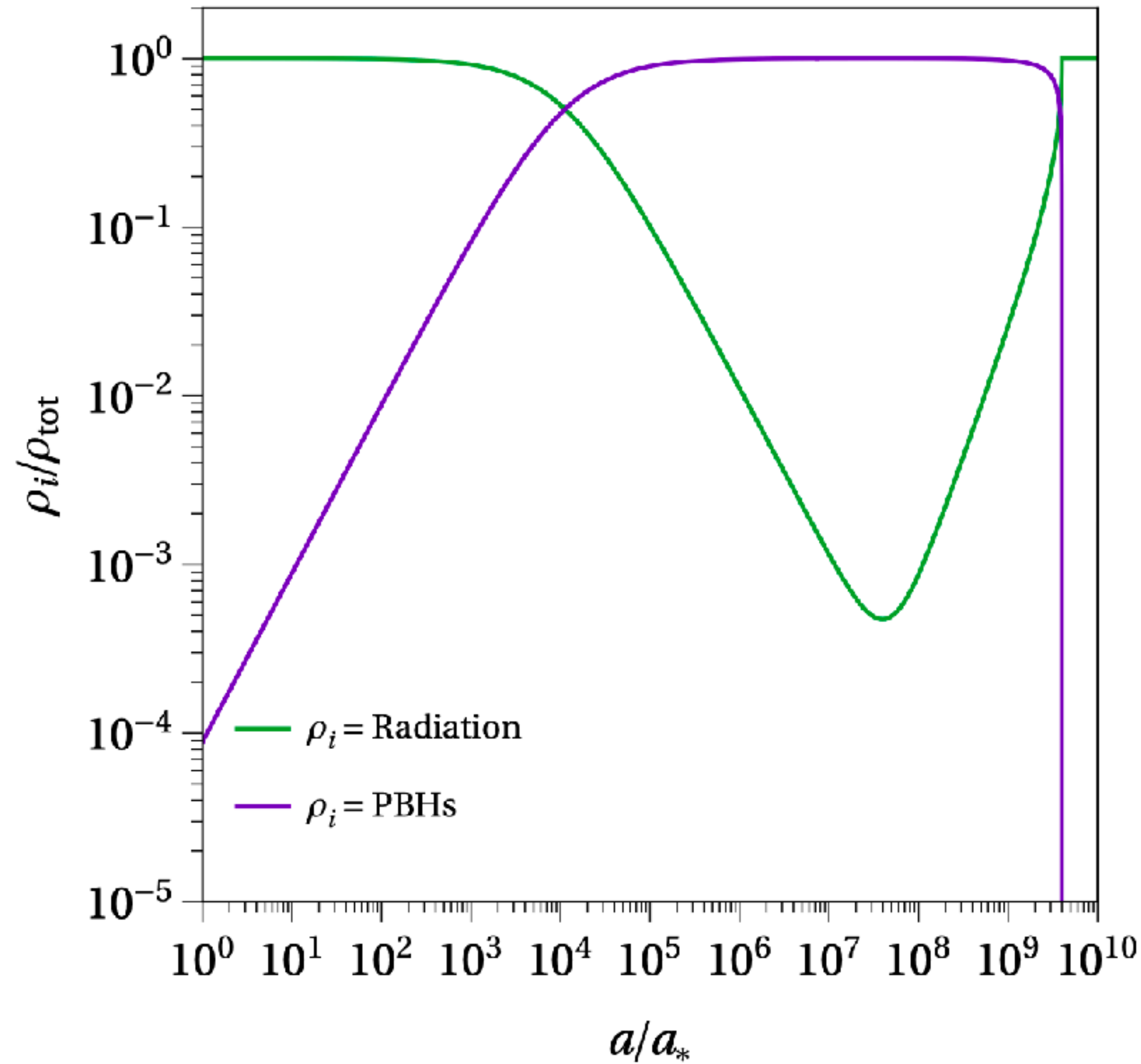
# Evaporating PBHs & the poltergeist mechanism

- The *poltergeist mechanism* realized in numerous physical scenarios:
  - PBH evaporation
    - [K. Inomata, M. Kawasaki, K. Mukaida, T. Terada, T. T. Yanagida]
  - Q-ball evaporation
    - [G. White, D. Vagie, A. Kusenko, L. Pearce]
  - Axion poltergeist
    - [K. Harigaya, K. Inomata, T. Terada]
  - Many more...

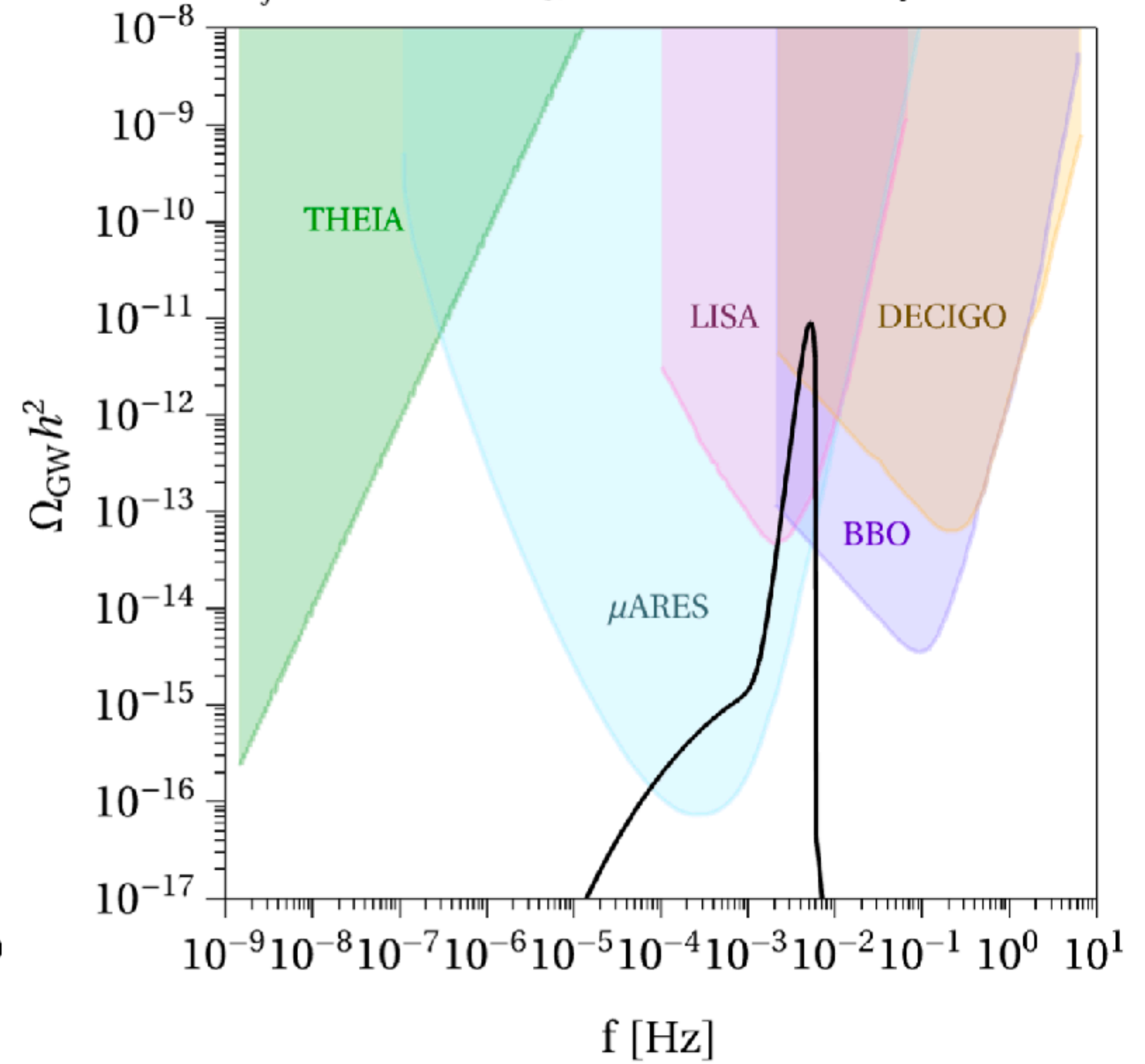
$$M_{\text{PBH}} \sim 10^{22} g \left( \frac{100 \text{ TeV}}{\Lambda} \right)^2$$

# Evaporating PBHs as a test of high-scale SUSY

$$\Lambda = 5.25 \times 10^{13} \text{ GeV}, \beta = 5 \times 10^{-5}$$



$$H_f = 10^5 \text{ GeV}, Q_c = 10^{32}, N = 10^6, y = 1 \text{ GeV}$$



[MMF, A. Kusenko, L. Pearce, Y. F. Perez-Gonzales, G. White: arXiv: 2308.15522]

# Observational implications: PBH spin

[MMF, A. Kusenko PRD 104 (2021) 6, 063008]

# Scalar radiation and angular momentum dissipation

- For PBHs to form, scalar radiation needs to remove both energy and angular momentum from dark matter halos.
- Angular momentum losses can be considered in two contexts:
  - Oscillatory channels (coherent/incoherent)
  - Non-oscillatory channels (bremsstrahlung/surface)

See also:

Harada et. al. [arXiv:1707.03595]

Harada et. al. [arXiv:2011.00710]

# Angular momentum losses for oscillatory channels

- For oscillatory charge distributions, we can find decompose the outgoing waves in a spherical basis. The energy losses and angular momentum losses for a given mode are:

$$\frac{dE_{\ell m}}{dt} = \frac{1}{2} |\Lambda_{\ell m}|^2, \quad \frac{dJ_{\ell m}}{dt} = \frac{m}{2\omega} |\Lambda_{\ell m}|^2 = \frac{m}{\omega} \left( \frac{dE_{\ell m}}{dt} \right)$$

- Here,  $m = -\ell, \dots, \ell$ . This shows that if the  $\ell = 0$  mode dominates, angular momentum losses are not significant.

$\implies$  Different for electromagnetism

# Angular momentum losses for non-oscillatory channels

- For non-oscillatory motion, radiation escapes isotropically when the viewed from the co-rotating frame of the dark matter halo.
- In the lab frame, scalar quanta are **blueshifted** (**redshifted**) when emitted in the direction parallel (antiparallel) to the motion of the halo

$$\frac{dJ}{dt} = -R \frac{dE}{dt} f(v)$$

# Angular momentum losses for non-oscillatory channels

- We can compare the angular momentum loss to the cooling rate (i.e. the energy loss):

$$\frac{\tau_{\text{cool}}}{\tau_J} = \mathcal{A} \left( \frac{R_0}{R} \right) \frac{f(v)}{v}, \quad \mathcal{A} \equiv \frac{M_h}{R_0} \left( \frac{\beta}{M_{\text{Pl}}} \right)^2 \gg 1$$

- For  $v \ll 1$  and  $R \ll R_0$  then we find that,

$$J(R) = J_0 \left( \frac{R}{R_0} \right) \exp \left[ -\mathcal{A} \left( \frac{R_0}{R} \right) \right]$$

- Angular momentum is removed very efficiently. Black holes formed will be spinless.

# Primordial black holes: Spins

Formation Mechanism	Mass Range	Spins
Inflationary Perturbations [A. Green review: arXiv:2007.10722]	DM, LIGO, supermassive	Small
SUSY flat directions, Q-balls & IMD [1612.02529, 1706.09003, 1907.10613]	DM	Large
Light scalar Q-balls (not SUSY) [1612.02529, 1706.09003, 1907.10613]	DM, LIGO, supermassive	Large
First order phase transitions [2106.05637, 2212.14037, 2307.11639]	DM, LIGO, supermassive	Small
Multiverse bubbles [1512.01819, 1710.02865, 2001.09160]	DM, LIGO, supermassive	Small
<b><i>Early structure formation and collapse</i></b> [MMF, A. Kusenko: PRL 126 (2021) 4, 041101] [MMF, A. Kusenko: JCAP 05 (2023) 013] [MMF, Y. Lu, A. Kusenko: arXiv:2308.09094]	DM, LIGO, supermassive	Small [MMF, A. Kusenko PRD 104 (2021) 6, 063008]



# Observational implications of early structure formation: gravitational waves

[MMF, A. Kusenko, M. Sasaki; PRL 131 (2023) 1, 1]

# Primordial structure formation & GWs

- Generically, the collapse of dark matter  $\psi$  halos will be *aspherical*
  - $\implies$  Time changing mass quadrupole moment
- It's still not obvious which methodology is best suited to tackling this problem
  - Standard methods, like cosmological perturbation theory *do not* include forces which couple to charge/number density as a means of generating perturbations
- We utilized the *Zel'dovich approximation* to directly determine the quadrupole moment, allowing for a calculation of the expected GW spectrum

See also:

I. Dalianis, C. Kouvaris [arXiv:2106.06023]

# Zel'dovich Approximation

$\delta$  enters the horizon -  $t_q$



Overdensity increases to maximum size -  $t_{\max}$



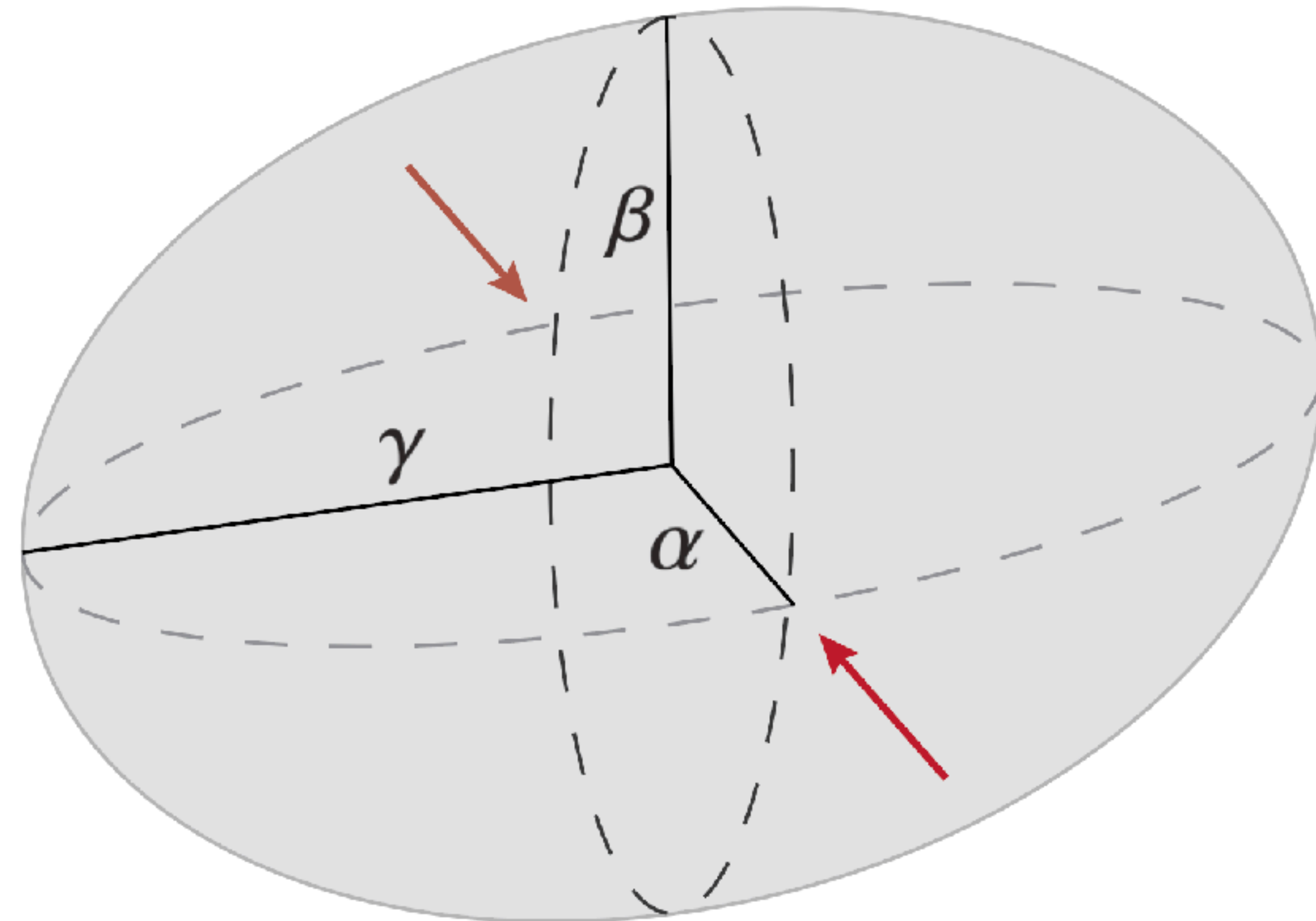
Collapse begins



“Pancake” forms and shell crossing occurs -  $t_{\text{col}}$



BH formation or halo annihilation



See also:

I. Dalianis, C. Kouvaris [arXiv:2106.06023]

# Growth of perturbations

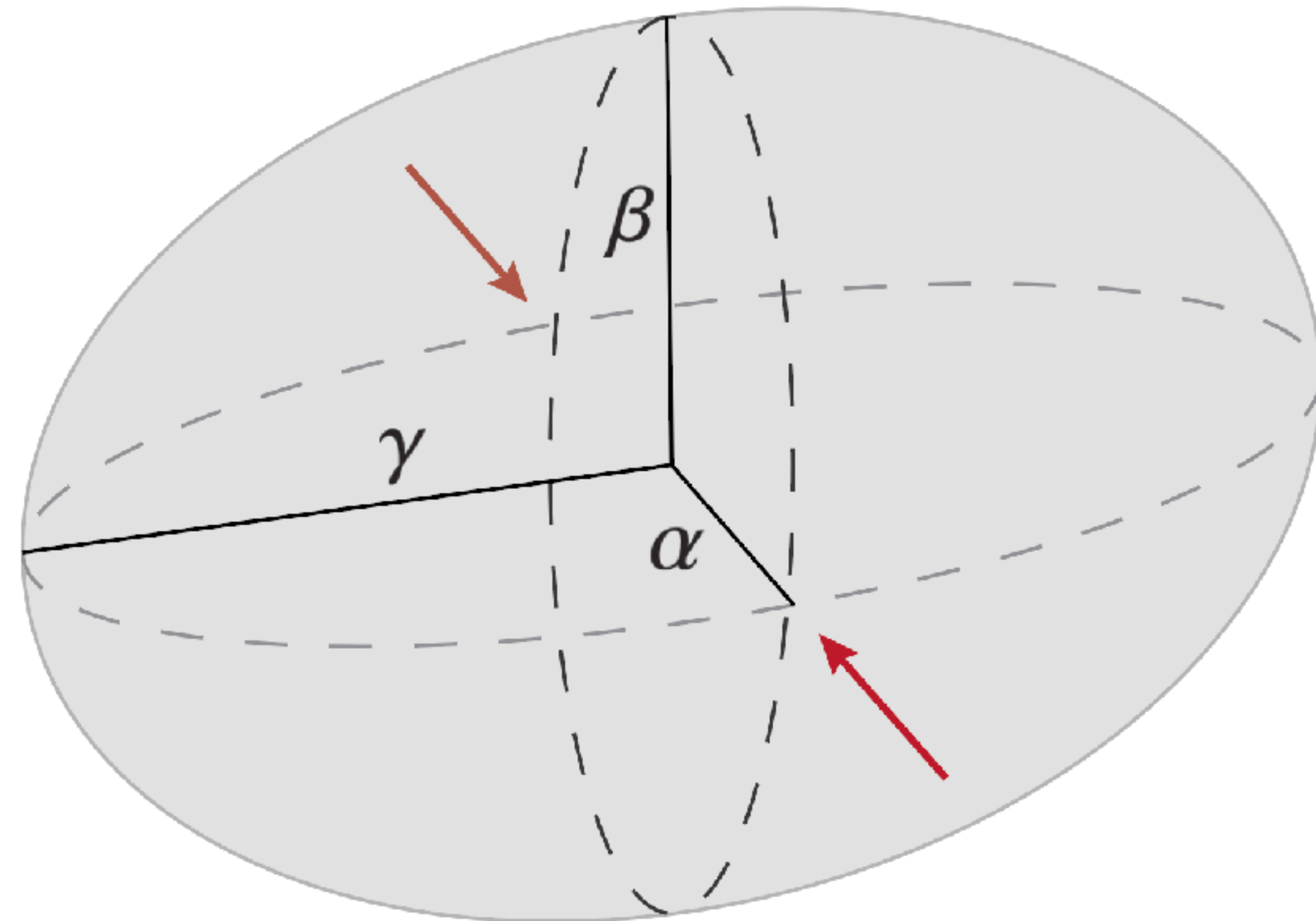
A reminder of the traditional result:

$$\delta \propto \begin{cases} \ln a & \text{for (RD)} \\ a & \text{for (MD)} \end{cases}$$

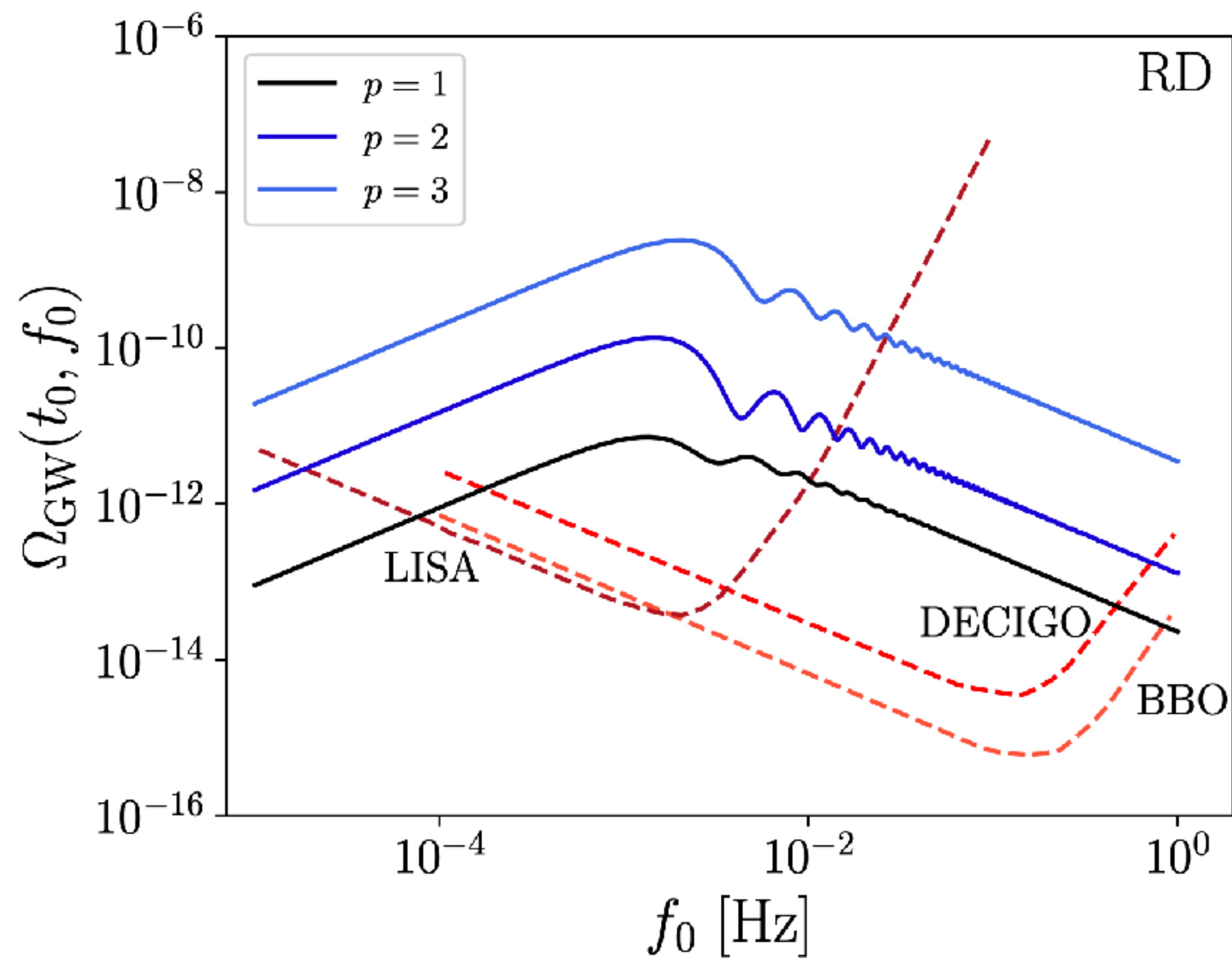
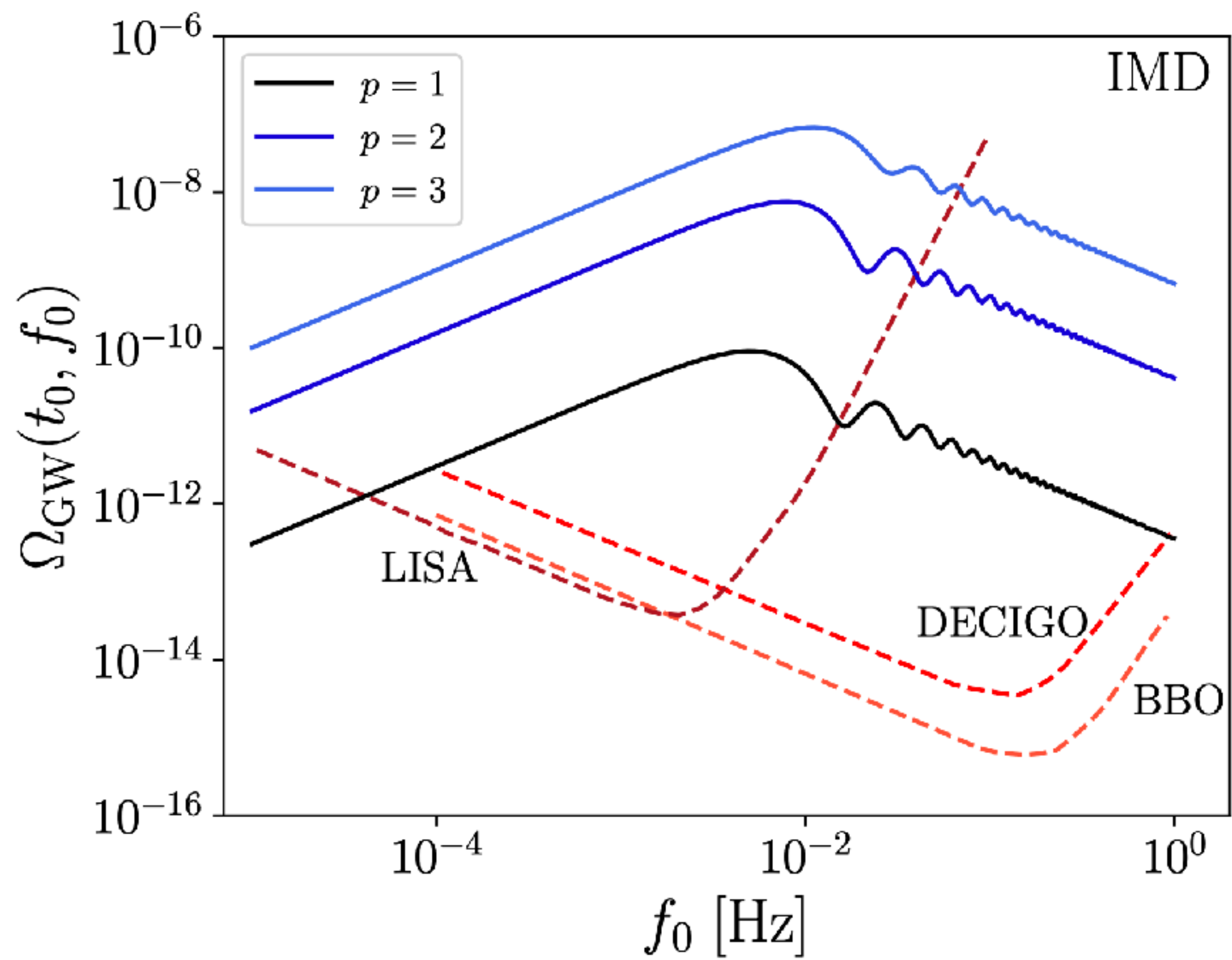
Here, **our fundamental assumption will be that**

$$\delta \propto a^p, \quad p \geq 1$$

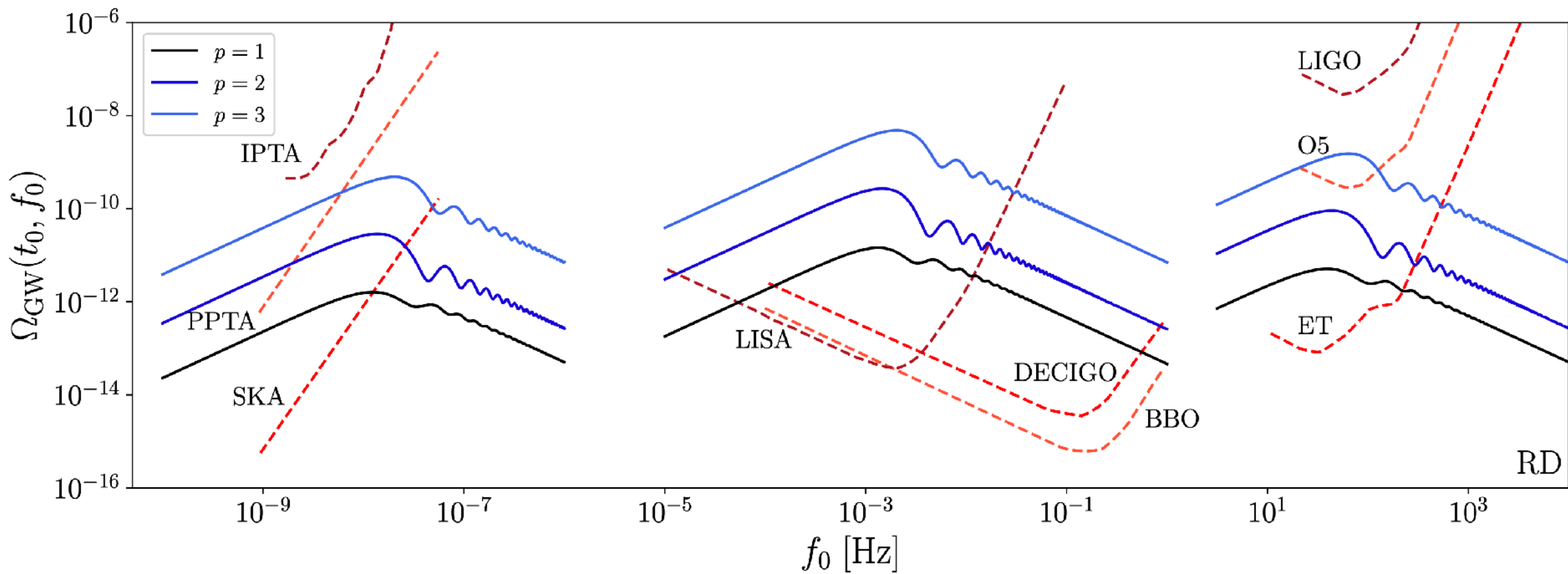
As before  $p$  characterizes the strength of the force.



# GW Spectrum

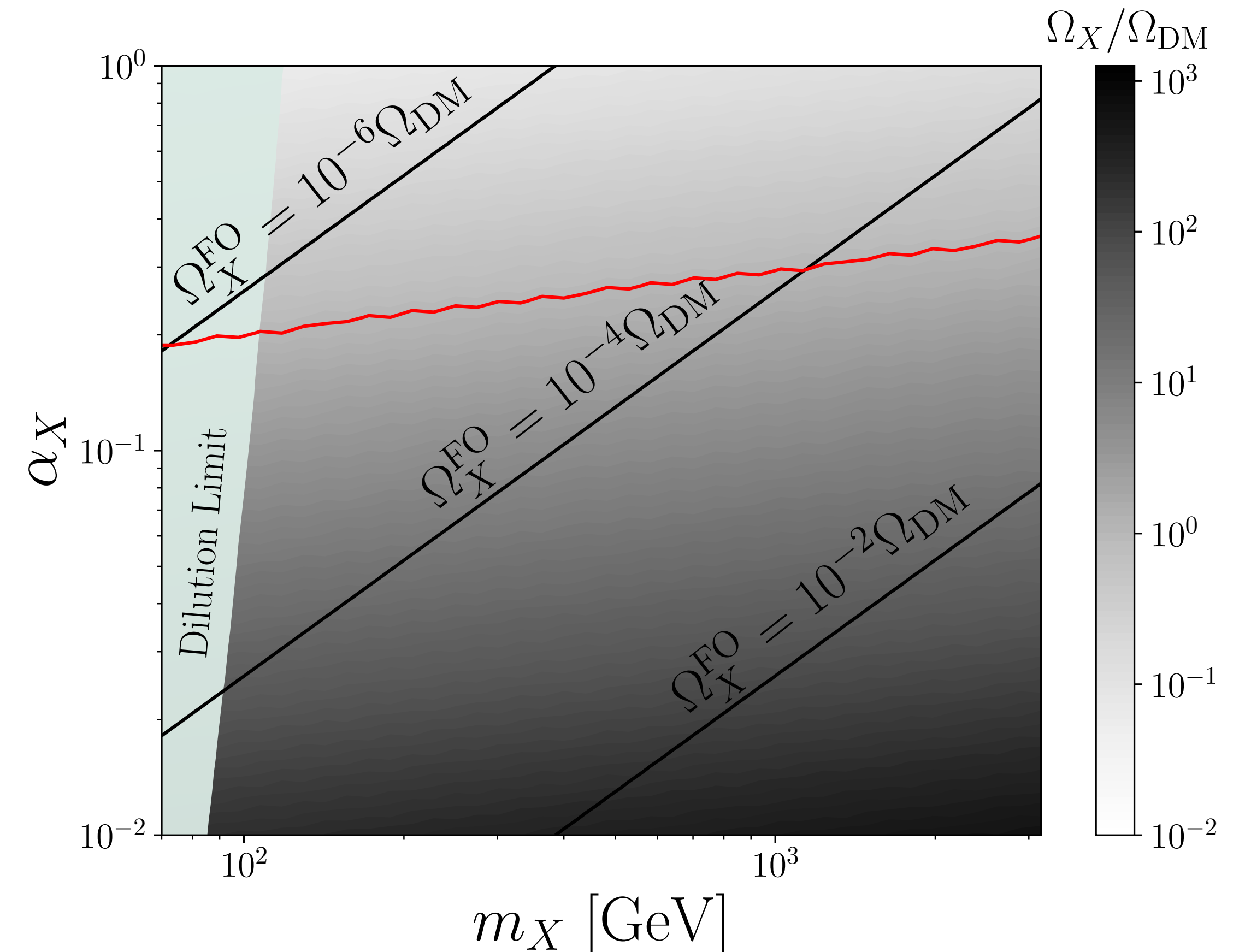


# GW Spectrum



# Before moving on...

- Early structure formation has proven useful in areas of cosmology *outside of PBH formation*:
  - Matter-antimatter asymmetry
    - [MMF, A. Kusenko, L. Pearce, G. White, 2208.09789]
  - Dark matter production ( $\implies$ )
    - [MMF, C. Kouvaris, A. Kusenko, 2306.04056]
  - Large-scale magnetic fields
    - [R. Durrer, A. Kusenko; 2209.13313]



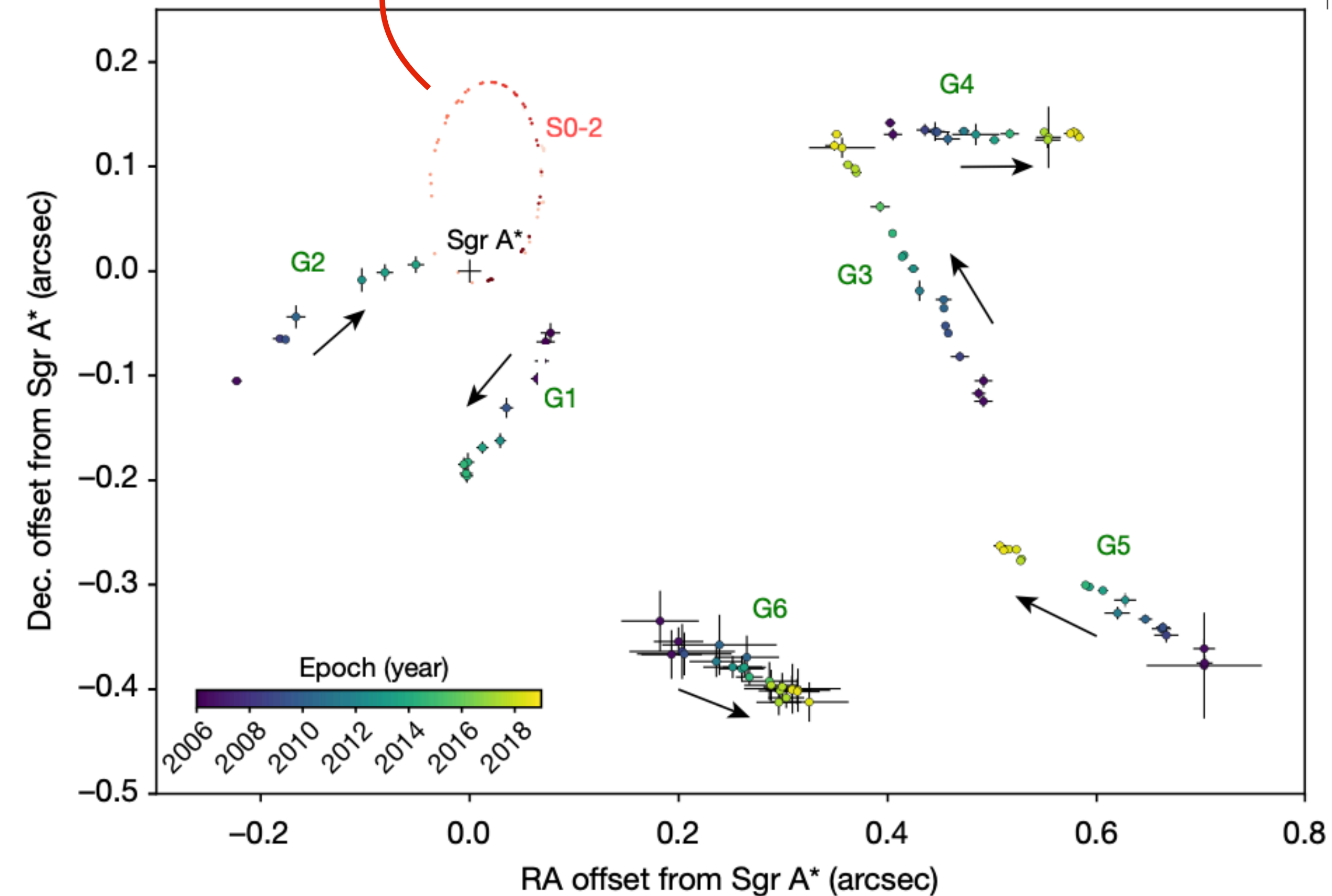
# Primordial black holes and the Galactic Center

[MMF, A. Kusenko, A. M. Ghez, S. Naoz; PRD 108 (2023) 6, L061301]



# Brief review of $G$ objects

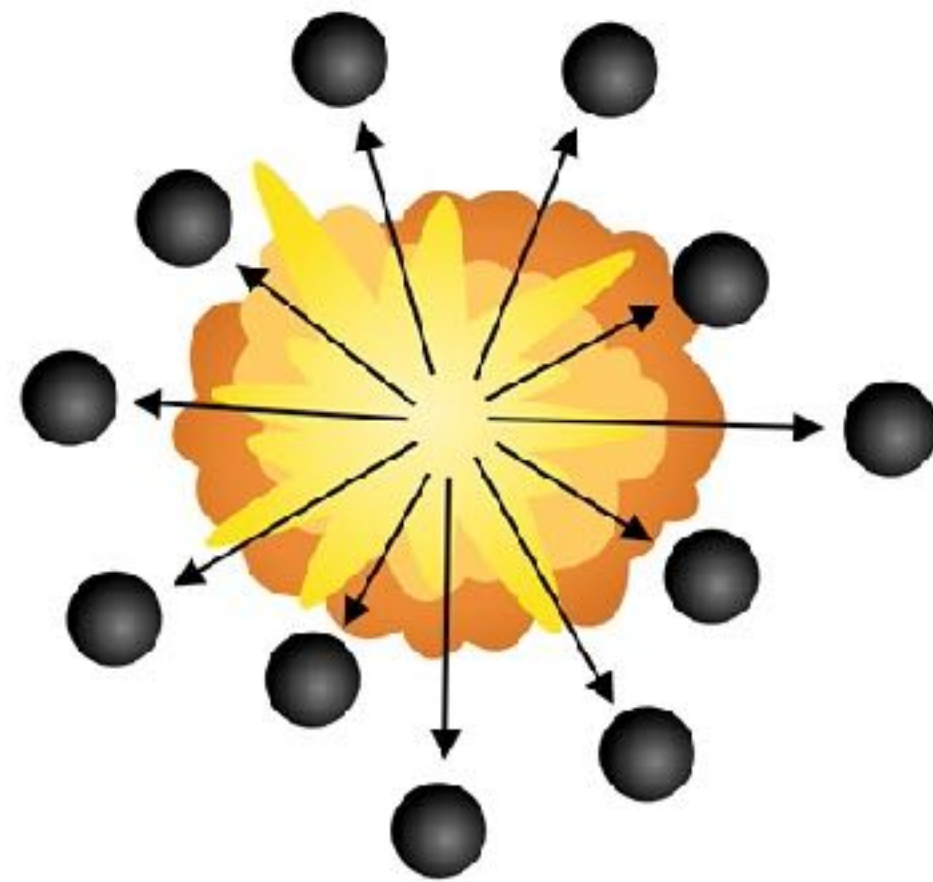
- Population of unresolved objects which show both ***thermal and dust emission***.
- Simultaneously, they display the ***dynamical properties of stellar-mass objects***
- These objects, particularly  $G2$ , seem ***resilient*** to tidal disruption
- Various proposed formation mechanisms:
  - **Merger of binary systems**
  - See Prodan, S., Antonini, F. & Perets (2015), Stephan, A. P. et al. (2016)
  - **Low-mass star that has retained a protoplanetary disk**
    - Murray-Clay, R. A. & Loeb, A; (2015)



[Ciurlo et. al. 2020]

# PBH-Neutron star interactions

1. Primordial black holes produced in Big Bang make up part or all of dark matter.

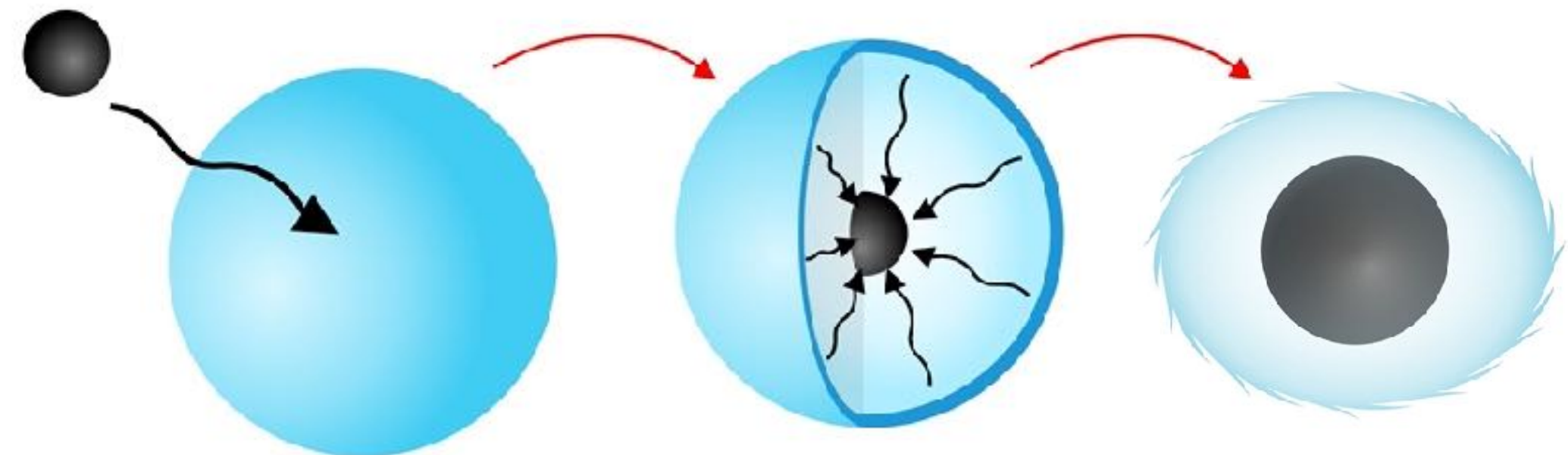


⇒  $r$  – process nucleosynthesis

⇒ stellar – mass black holes surrounded by gas  $\stackrel{?}{\rightleftharpoons}$   $G$  objects

2. A microscopic black hole falls into a neutron star, eats it from the inside, and creates a 1-2 solar mass black hole

Microscopic  
primordial  
black hole



# ***G* objects as converted neutron stars**

$$N_{\text{NS} \rightarrow \text{BH}} \quad \& \quad l = \frac{L_B}{L_{\text{Ed}}}$$

# PBH-Neutron star interactions

$$\langle t_{\text{NS}} \rangle = F^{-1} + t_{\text{loss}} + t_{\text{con}}$$

Time for PBH to settle  
in core of NS

↓

PBH-NS  
capture rate

↓

Accretion  
timescale

The diagram illustrates the components of the average time  $\langle t_{\text{NS}} \rangle$  for a Primordial Black Hole (PBH) to interact with a Neutron Star (NS). The equation is  $\langle t_{\text{NS}} \rangle = F^{-1} + t_{\text{loss}} + t_{\text{con}}$ . An arrow points from  $F^{-1}$  down to the text 'PBH-NS capture rate'. Another arrow points from  $t_{\text{con}}$  down to the text 'Accretion timescale'. A third arrow points from  $t_{\text{loss}}$  up to the text 'Time for PBH to settle in core of NS'.

[Takhistov, Fuller, Kusenko, PRL 119 (2017) 6, 061101]

[Takhistov, Fuller, Kusenko, PRL 126, 071101 (2021)]

[Takhistov, arXiv:1707.05849]

# PBH-Neutron star interactions

Capture rate is given by:

$$F = \frac{\Omega_{\text{PBH}}}{\Omega_{\text{DM}}} F_0^{\text{MW}}$$

where

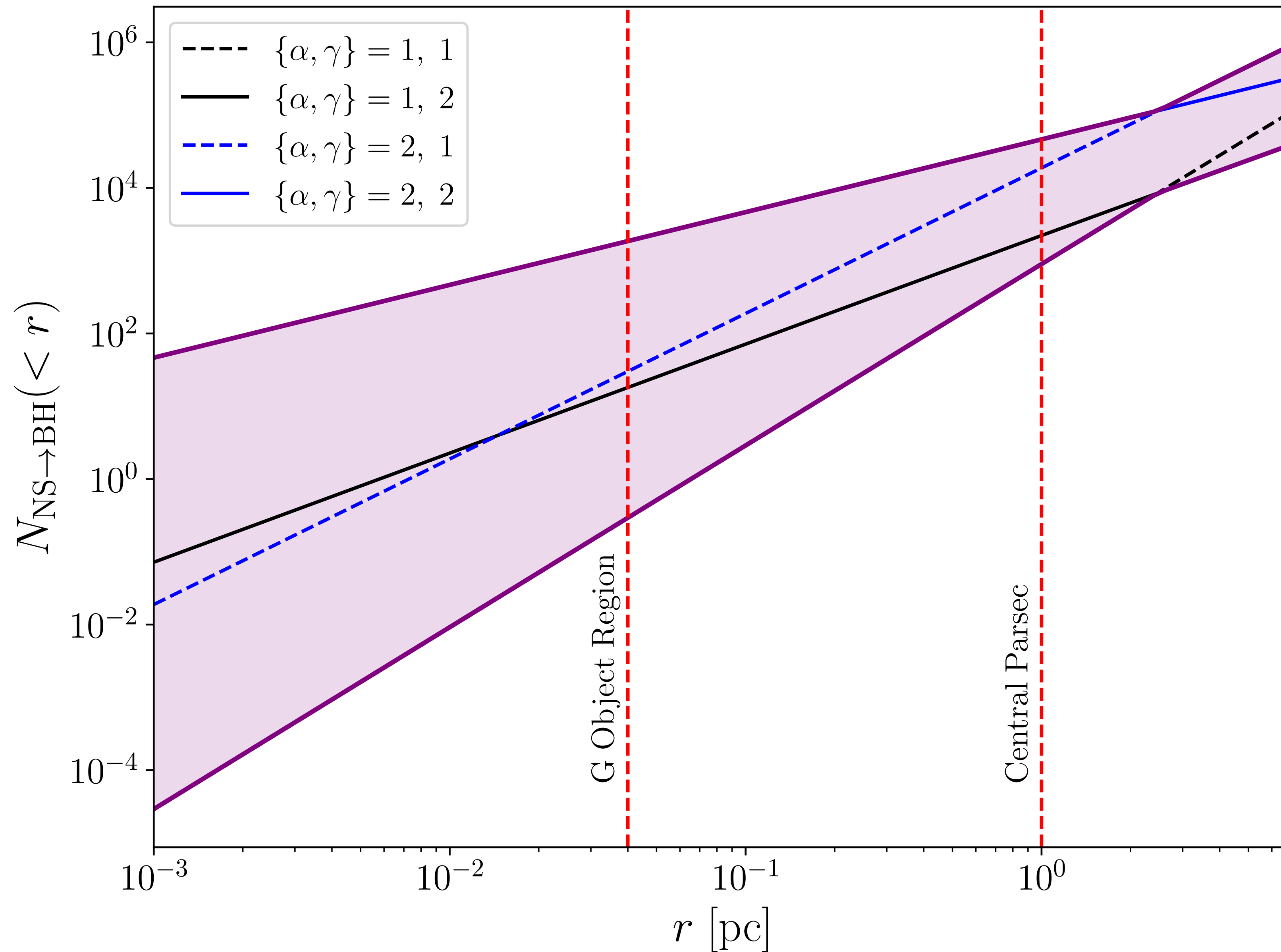
$$F_0^{\text{MW}} = \sqrt{6\pi} \frac{\rho_{\text{DM}}}{m_{\text{PBH}} \bar{v}} \left( \frac{2GM_{\text{NS}} R_{\text{NS}}}{1 - 2GM_{\text{NS}} R_{\text{NS}}} \right) \left( 1 - e^{-3E_{\text{loss}}/(m_{\text{PBH}} \bar{v}^2)} \right).$$

[Takhistov, Fuller, Kusenko, PRL 119 (2017) 6, 061101]

[Takhistov, Fuller, Kusenko, PRL 126, 071101 (2021)]

[Takhistov, arXiv:1707.05849]

# Number of Converted NS



$$\rho_{\text{DM}}(r) \simeq \rho_{\odot} \left( \frac{r}{r_{\odot}} \right)^{-\alpha}$$

$$n_{\text{NS}}(r) \simeq n_{\text{NS},0} \left( \frac{r}{r_{\text{NS}}} \right)^{-\gamma}$$

# PBH-Neutron star interactions

For simplicity, we will assume spherical Bondi accretion.

$$\dot{m} \equiv \frac{\dot{M}_B}{\dot{M}_{\text{Ed}}} = 1.7 \times 10^{-7} \left( \frac{M}{M_\odot} \right) \left( \frac{n_\infty}{1 \text{ cm}^{-3}} \right) \left( \frac{T_\infty}{10^4 \text{ K}} \right)^{-3/2}$$

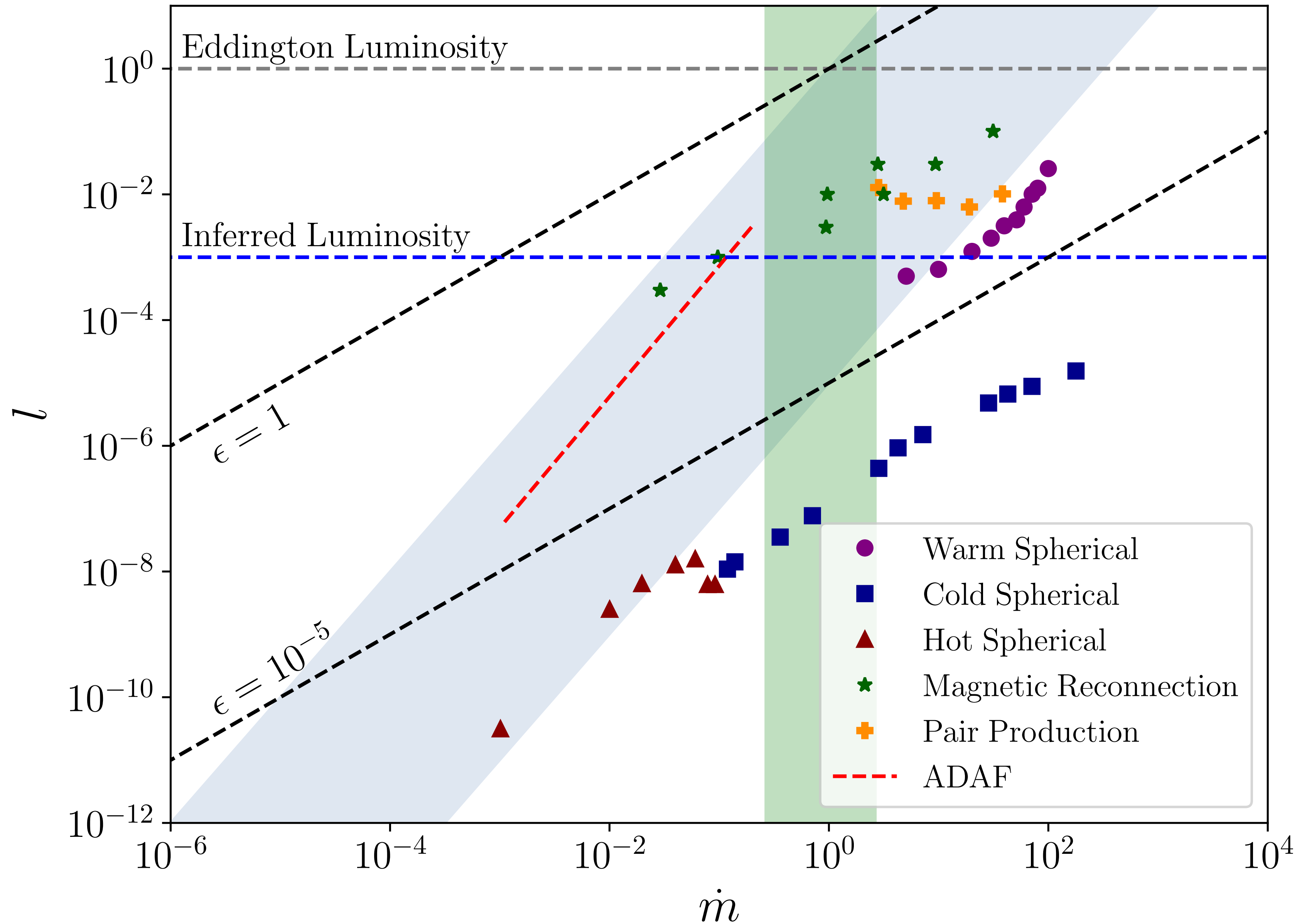
Define the efficiency,

$$l \equiv \epsilon \dot{m}, \quad l = \frac{L_B}{L_{\text{Ed}}}$$

Generally,  $\epsilon = \eta \dot{m} \implies l = \eta \dot{m}^2$

**Key:** Parameterize theoretical and observational uncertainty in  $\eta$

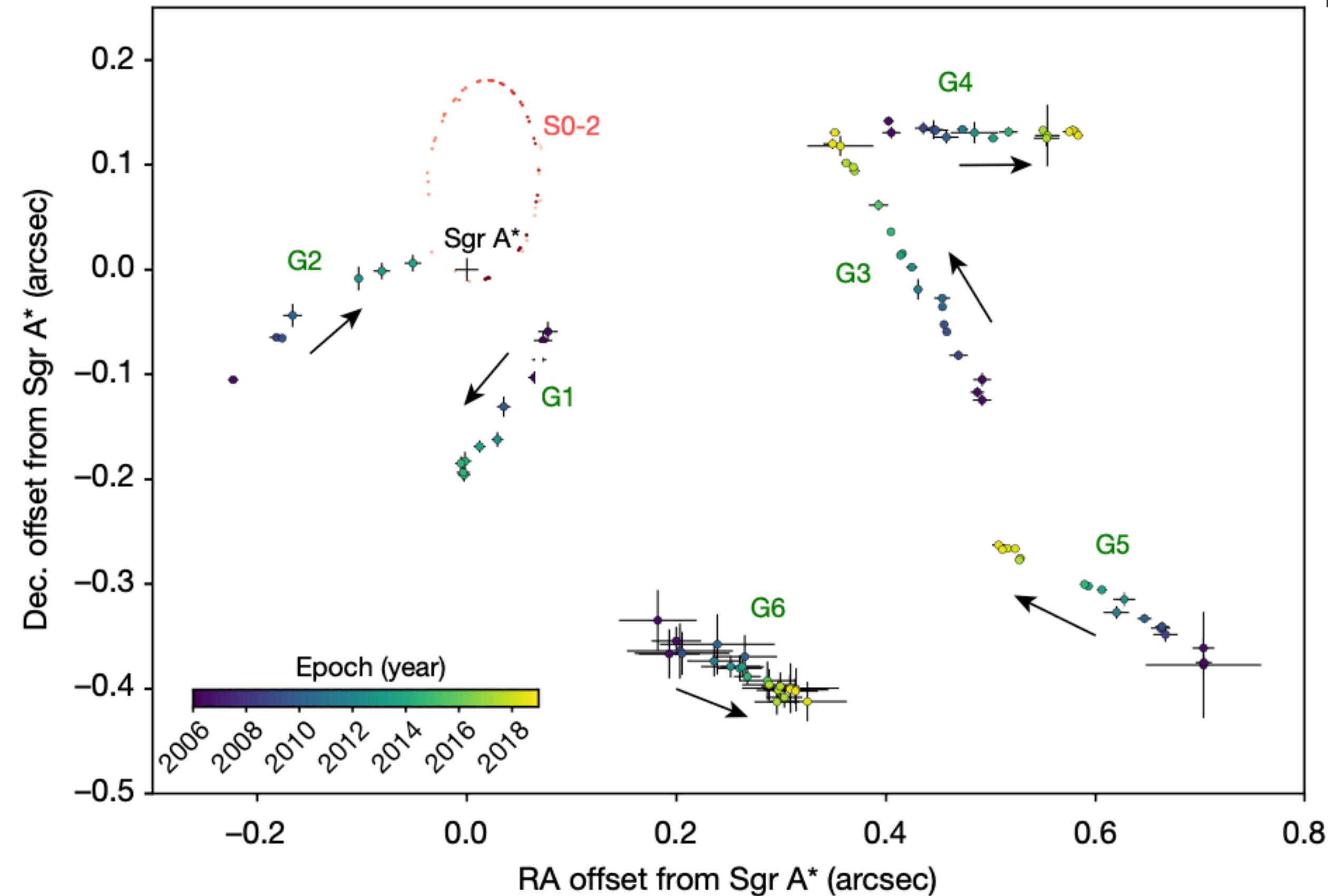
# Accretion Estimates





# Benefits of the PBH – $G$ objects interpretation

- Relates
  - Dark matter as PBHs
  - Mysterious nature of  $G$  objects
  - Missing pulsar problem
    - Observed absence of pulsars within the Galactic Center



[Ciurlo et. al. 2020]

# Conclusion

- Early structure formation can occur and has many interesting phenomenological implications
  - Primordial black holes
  - Matter-antimatter asymmetry
  - Generation of DM
  - Gravitational waves
- PBHs are a compelling DM candidate with numerous interesting astrophysical and cosmological implications
  - $G$  objects
  - Many more out there!