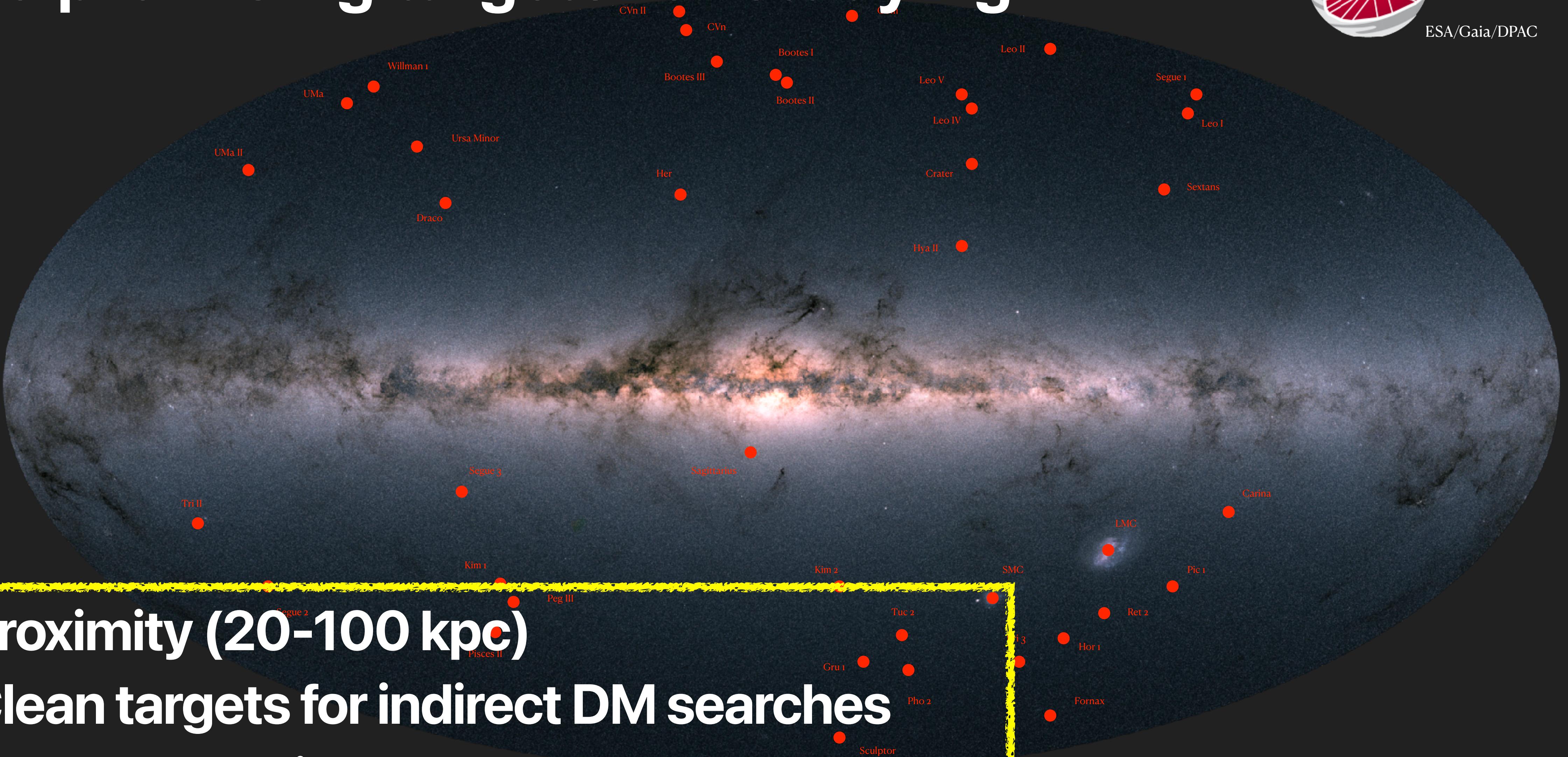


Dark Matter Searches in the Galactic dwarf spheroidals in the Subaru-PFS era

Kohei Hayashi (NIT, Sendai College)

Dwarf spheroidal galaxy (dSph): the promising targets for studying DM

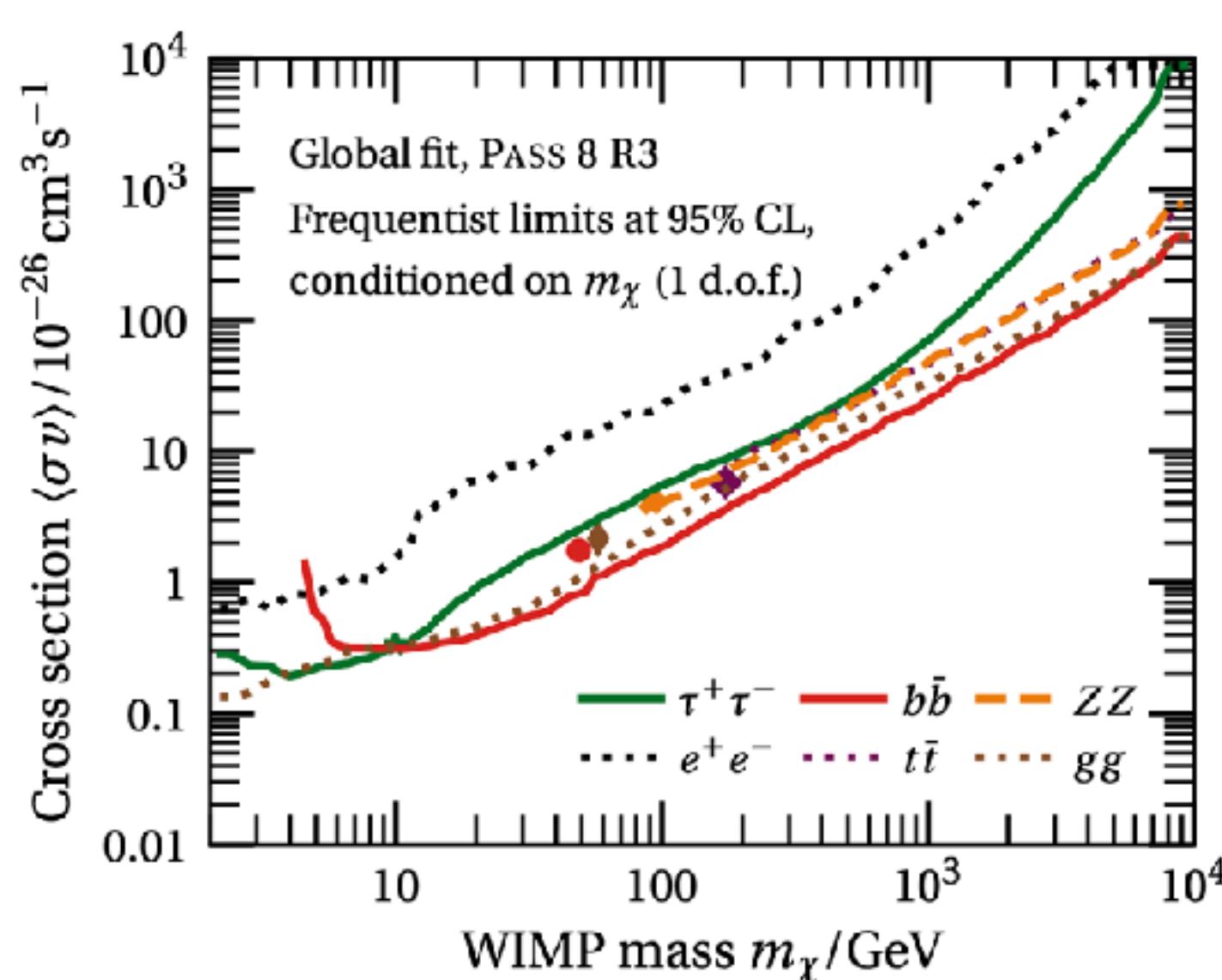


- Proximity (20-100 kpc)
Segue 2
Pisces II
 - Clean targets for indirect DM searches
 - Dark-matter rich system

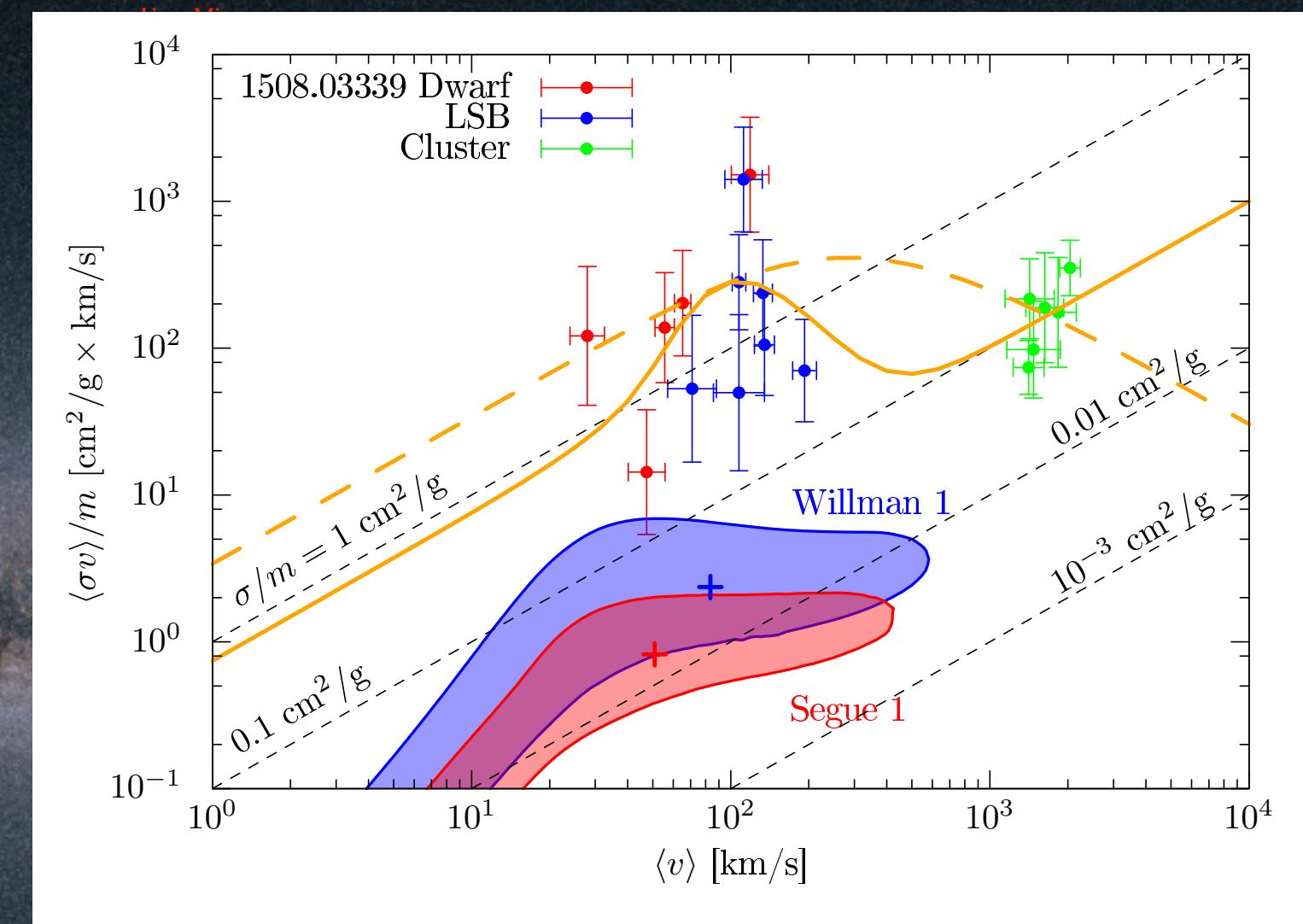
Dwarf spheroidal galaxy (dSph): the promising targets for studying DM



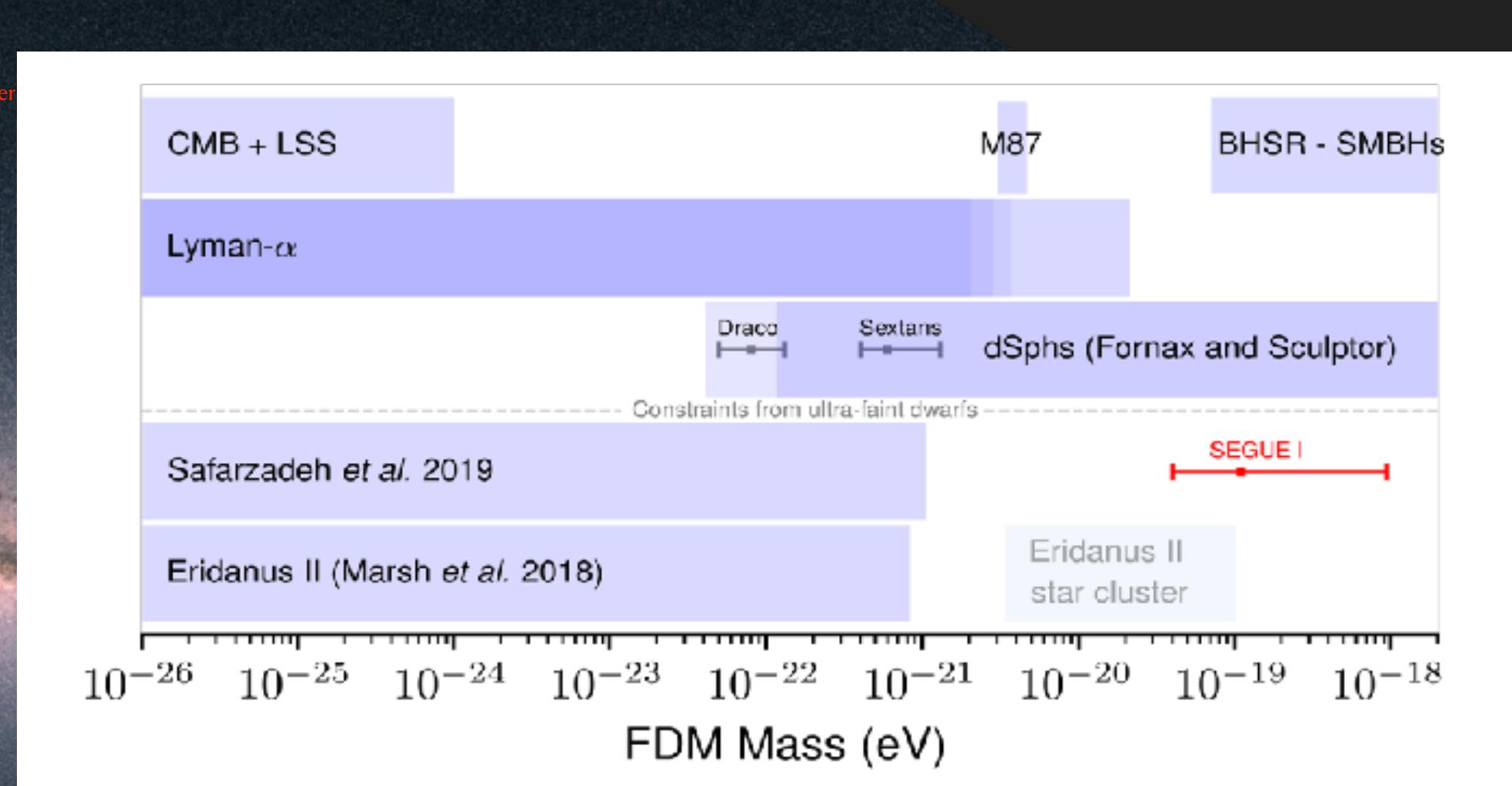
WIMP



SIDM



FDM

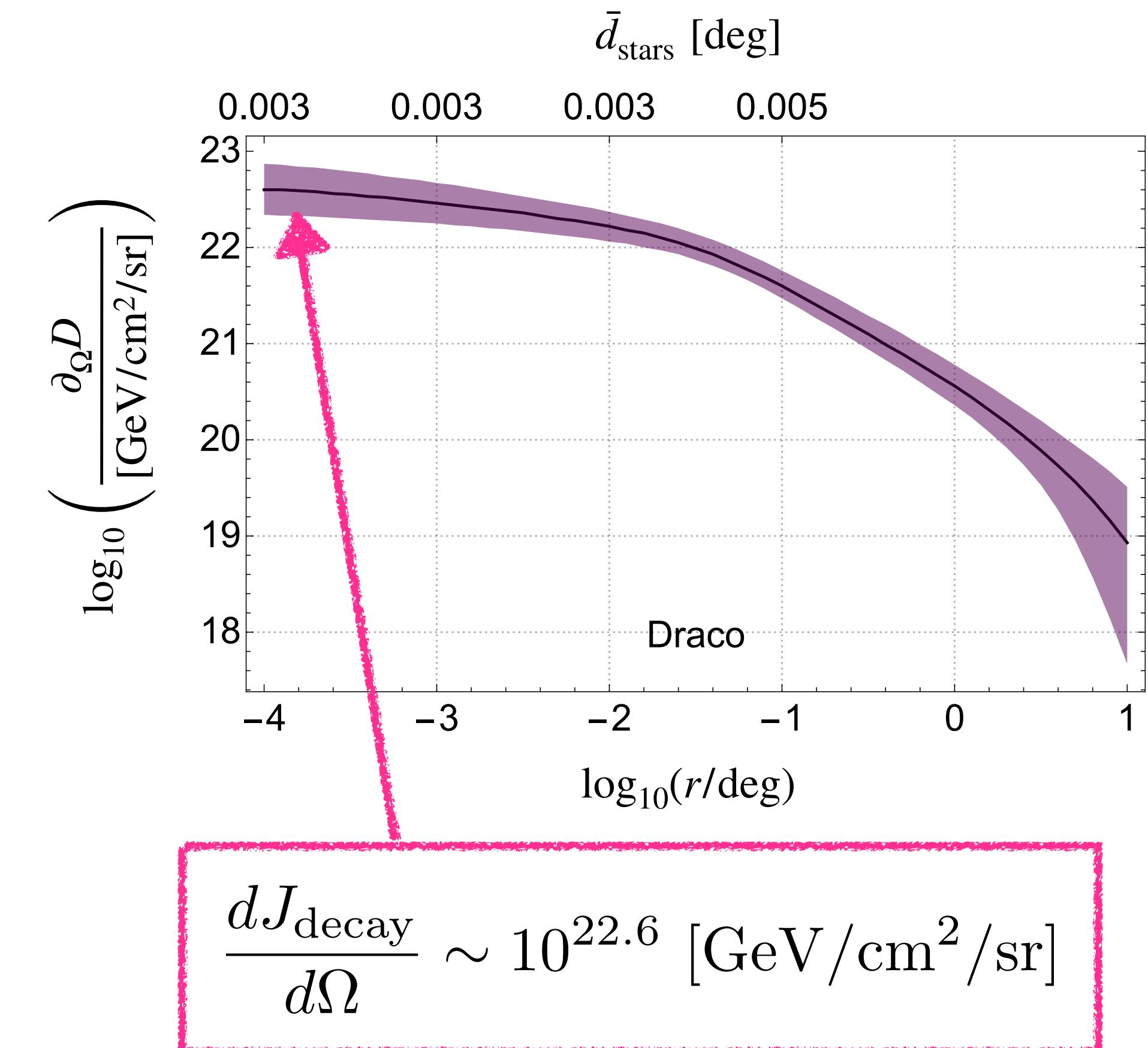
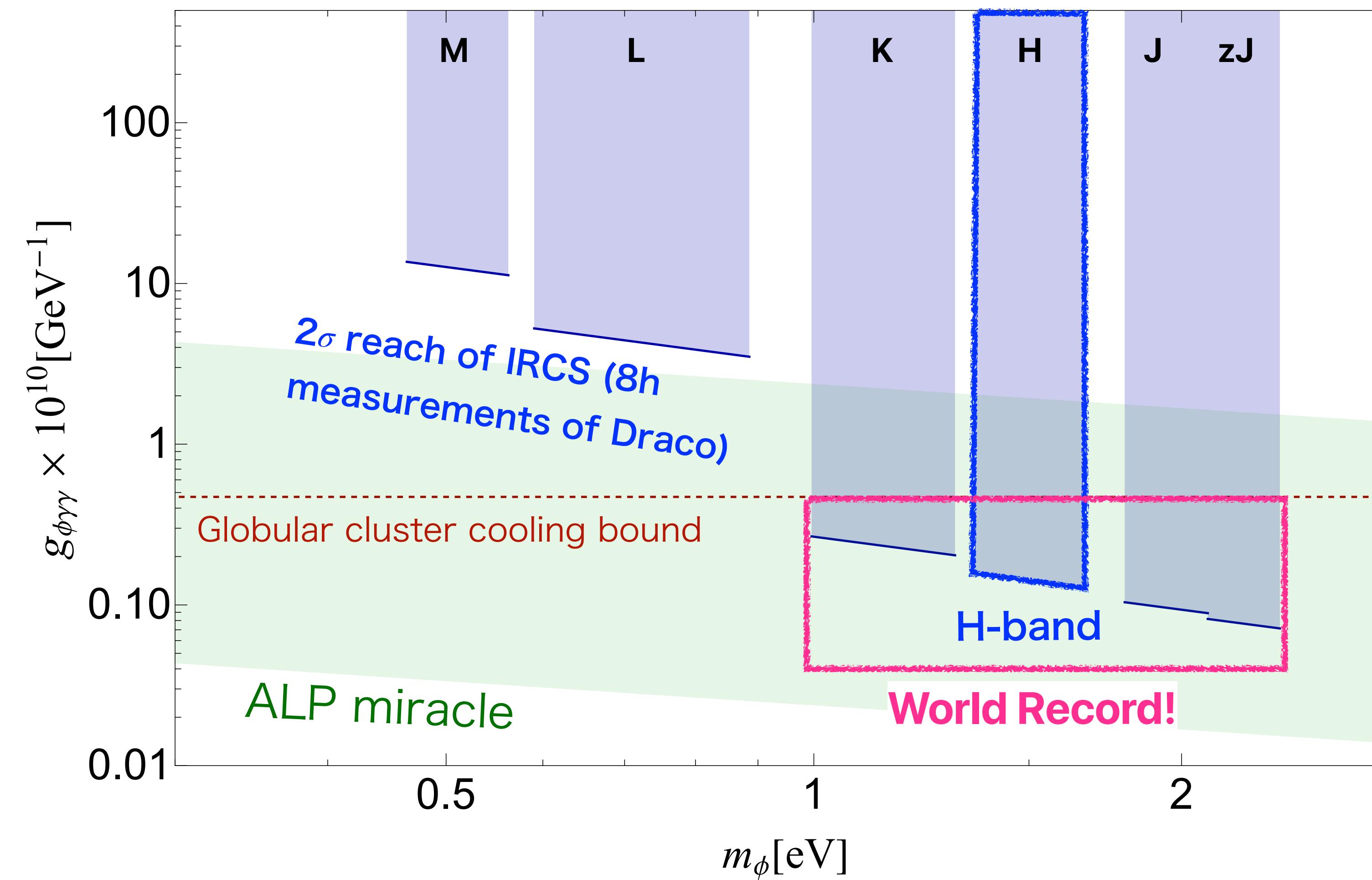


- Proximity (30-100 kpc)
- Clean targets for indirect DM searches
- Dark-matter rich system

Indirect detection of eV DM with Subaru-IRCS

Yin and KH (2024)

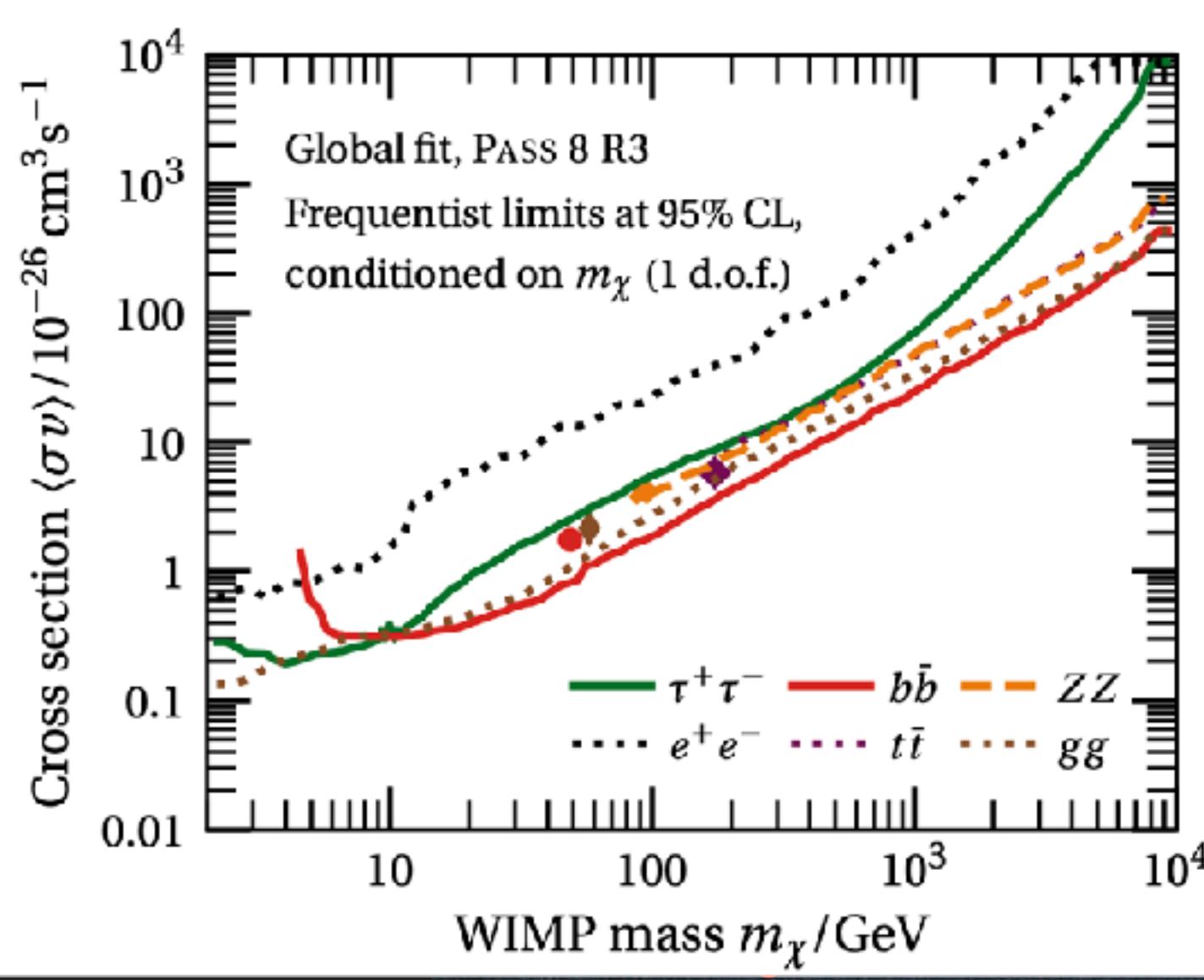
Subaru-IRCS observation can place more stringent constraints on $g_{\phi\gamma\gamma}$ of eV DM than the GC cooling.



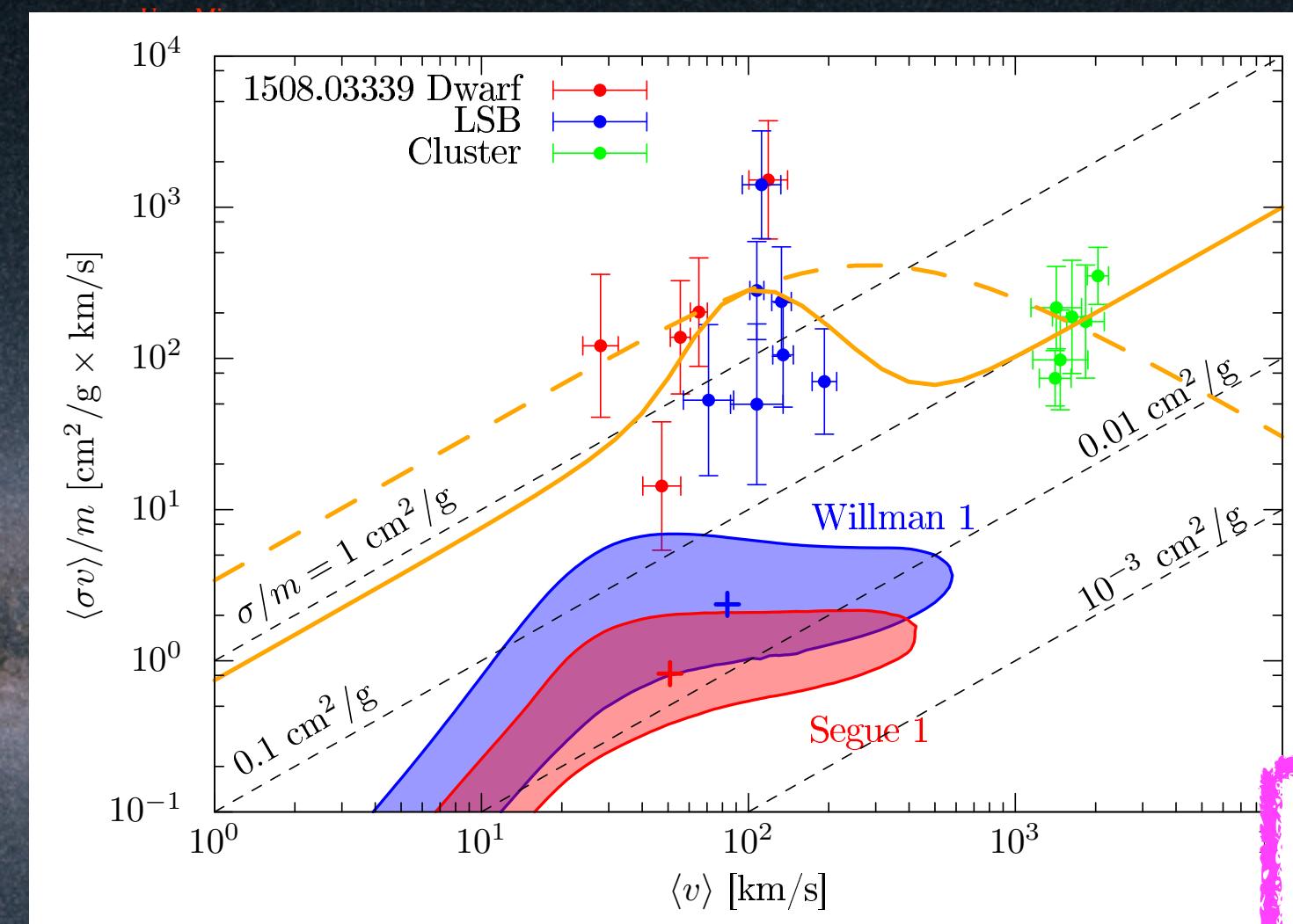
Dwarf spheroidal galaxy (dSph): the promising targets for studying DM



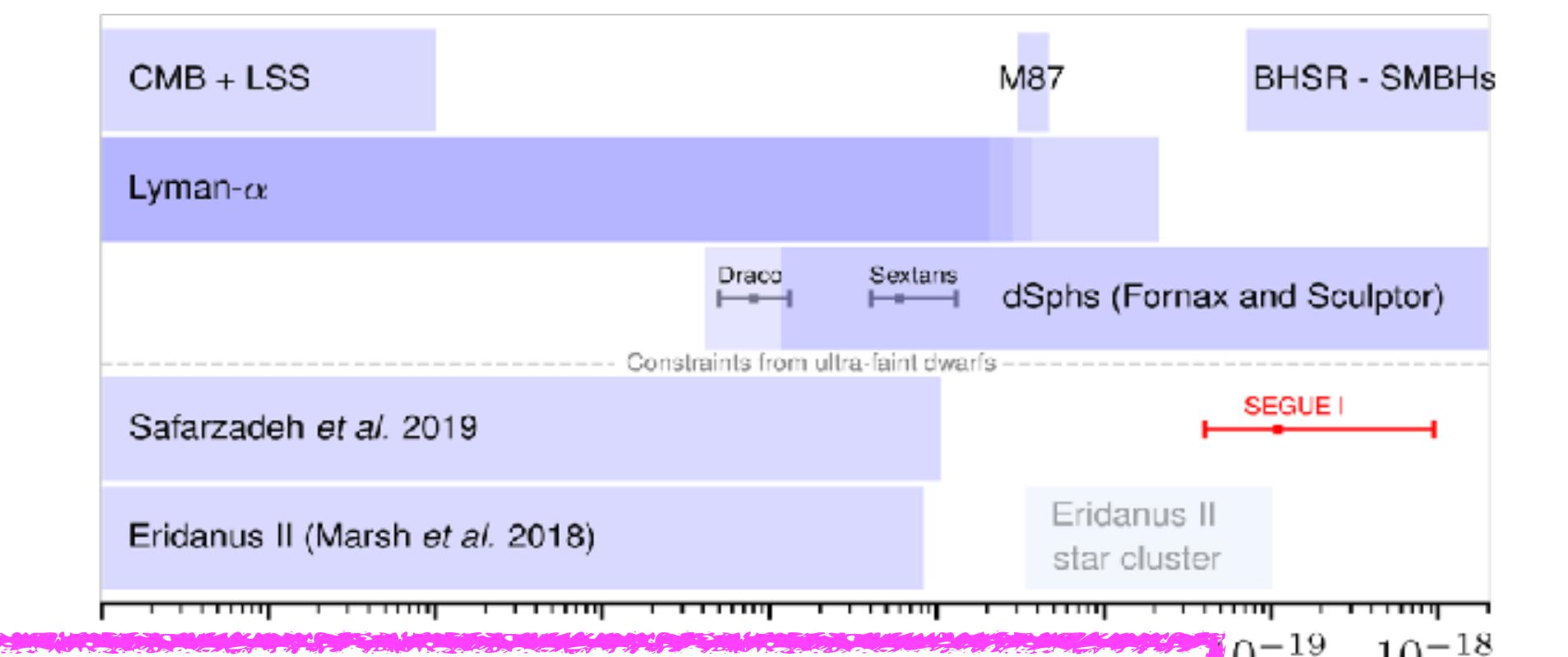
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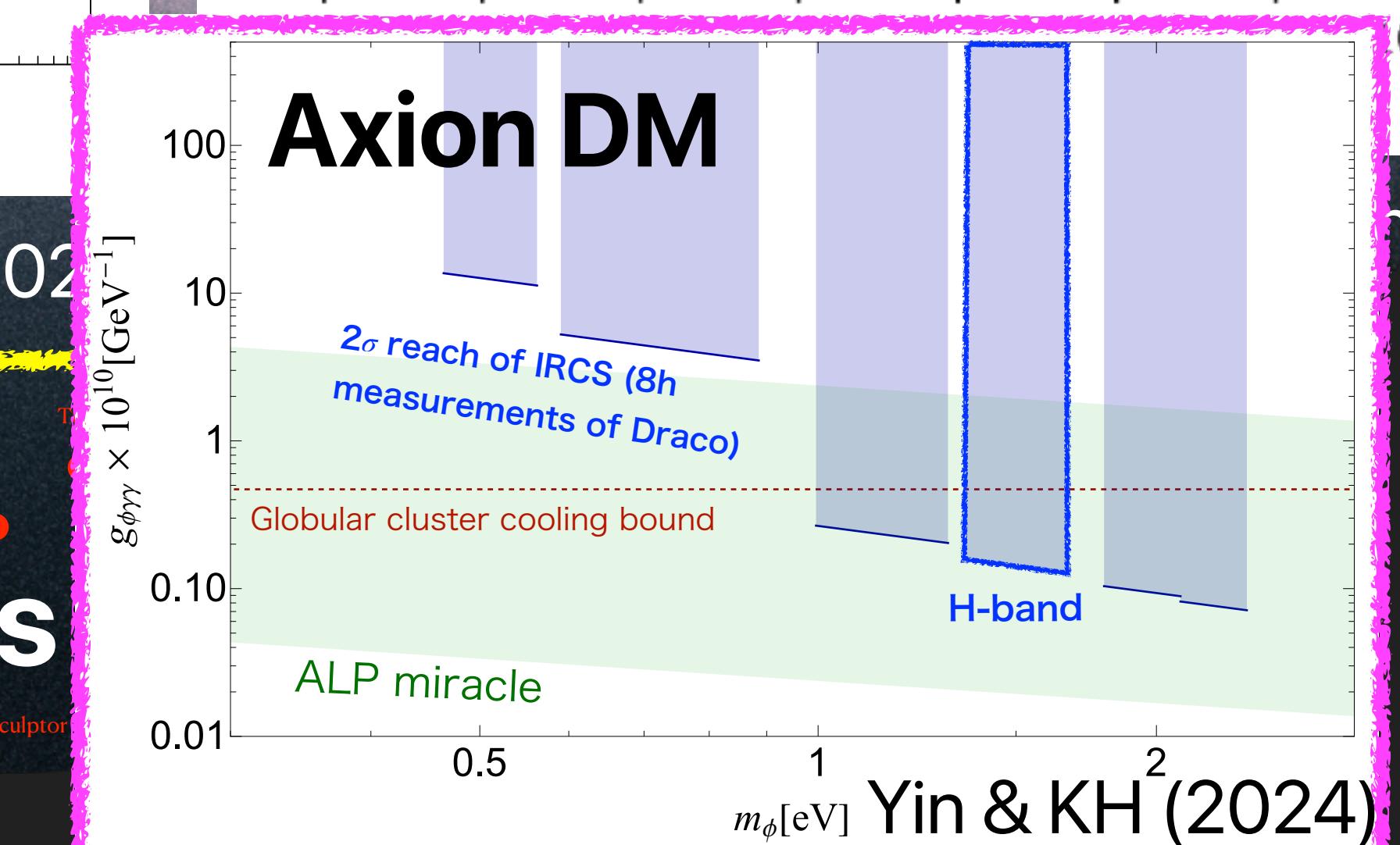
SIDM



FDM



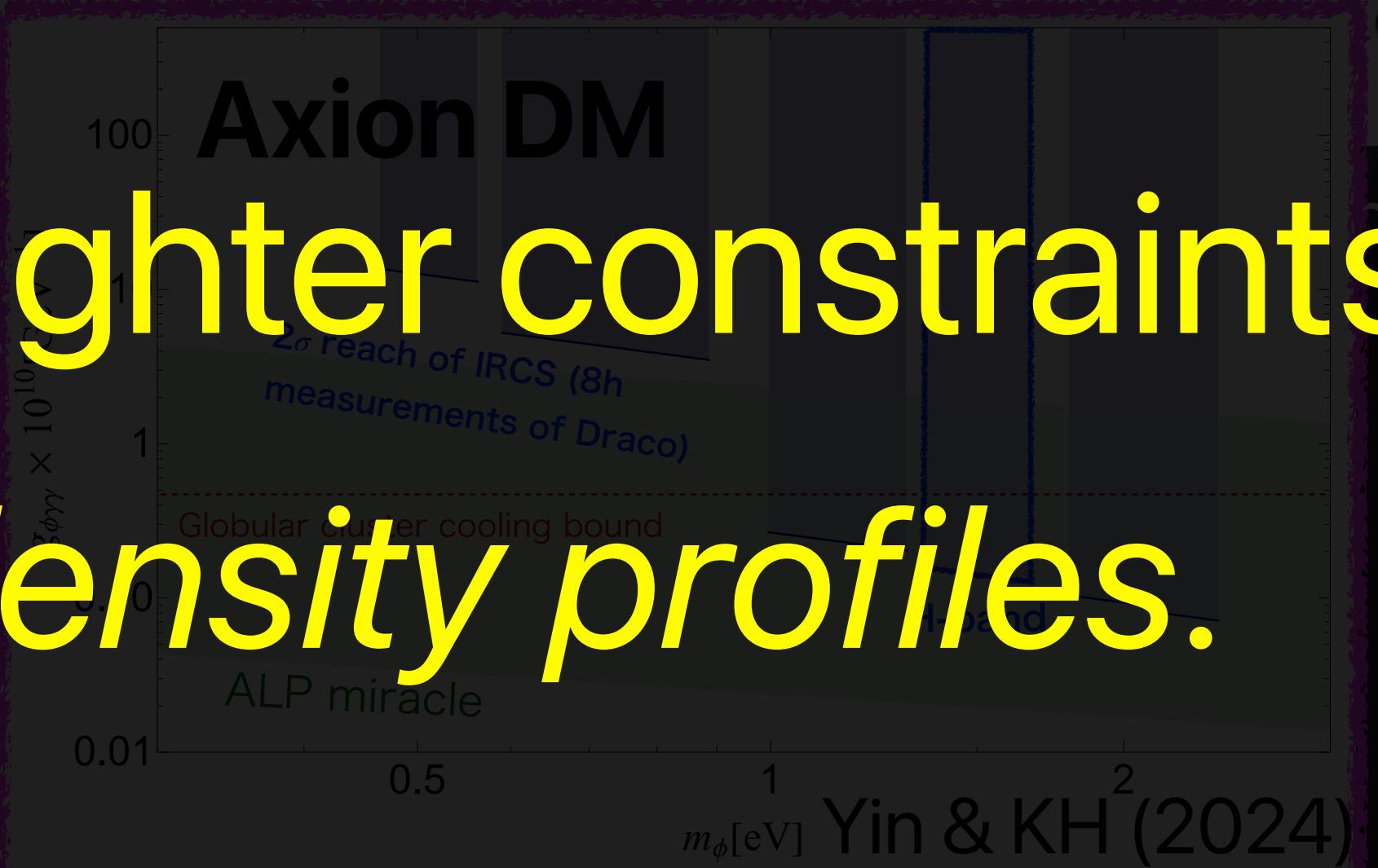
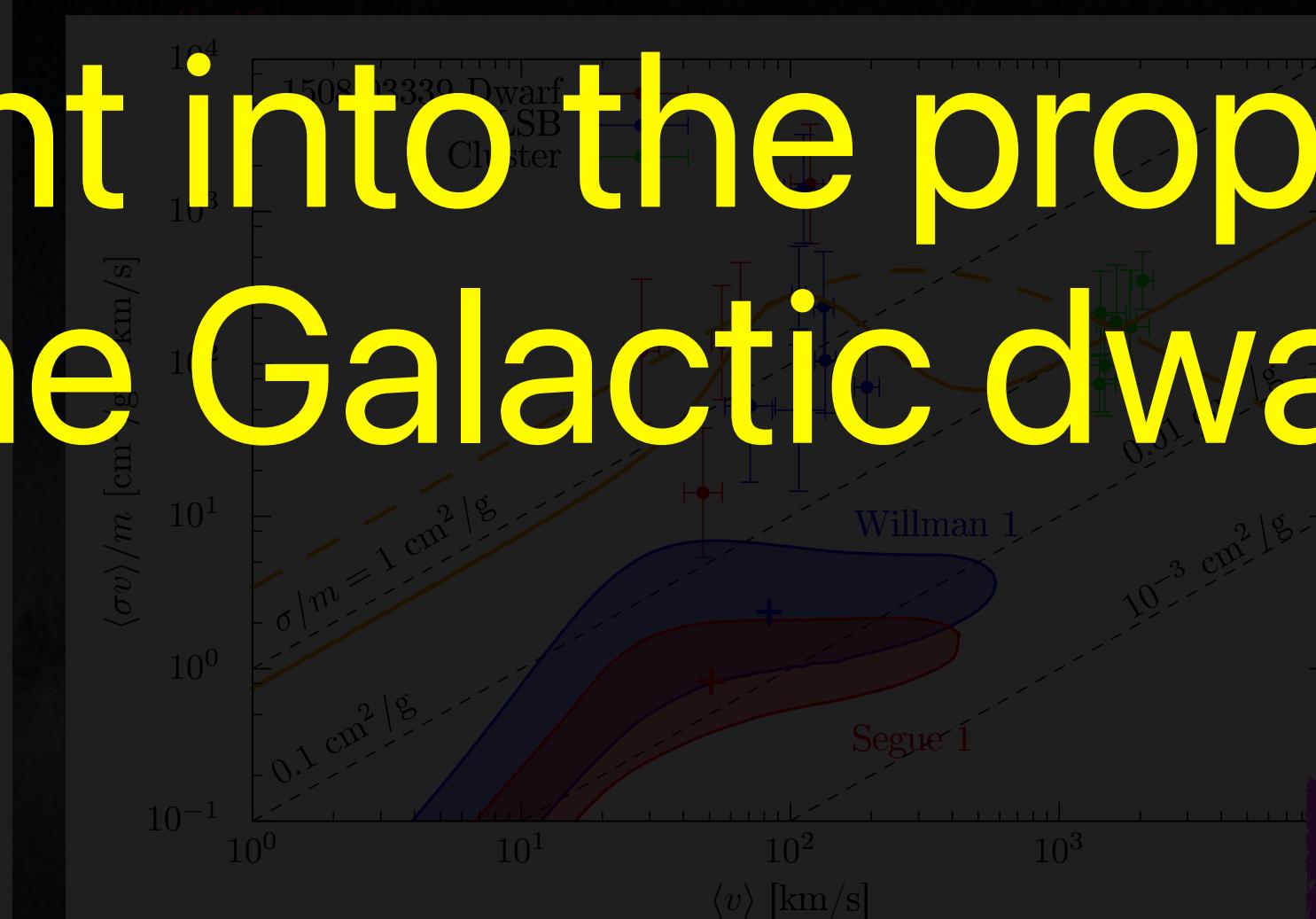
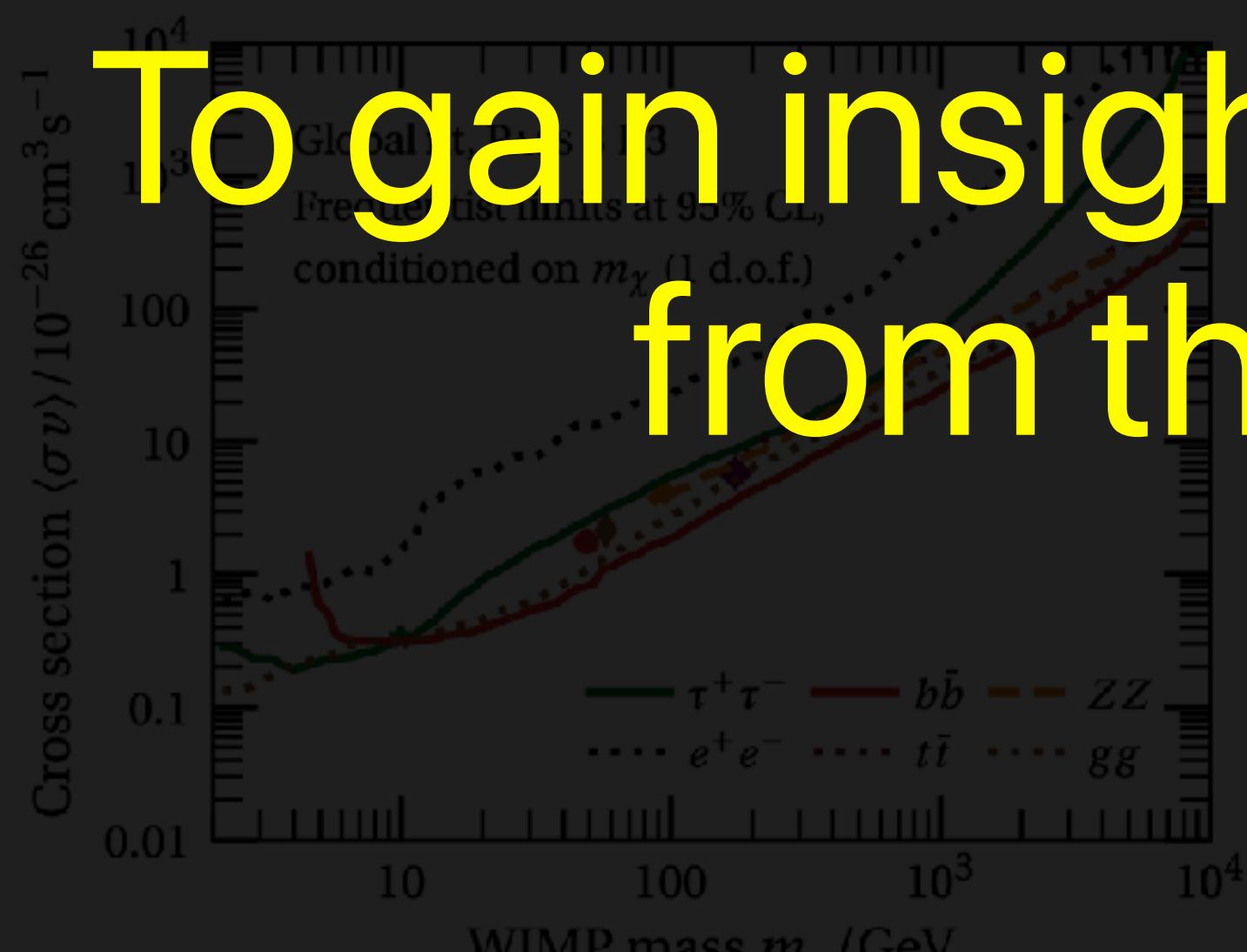
- Proximity (30-100 kpc)
- Clean targets for indirect DM searches
- Dark-matter rich system



Dwarf spheroidal galaxy (dSph): the promising targets for studying DM



in insight into the properties of dark matter from the Galactic dwarf spheroidals



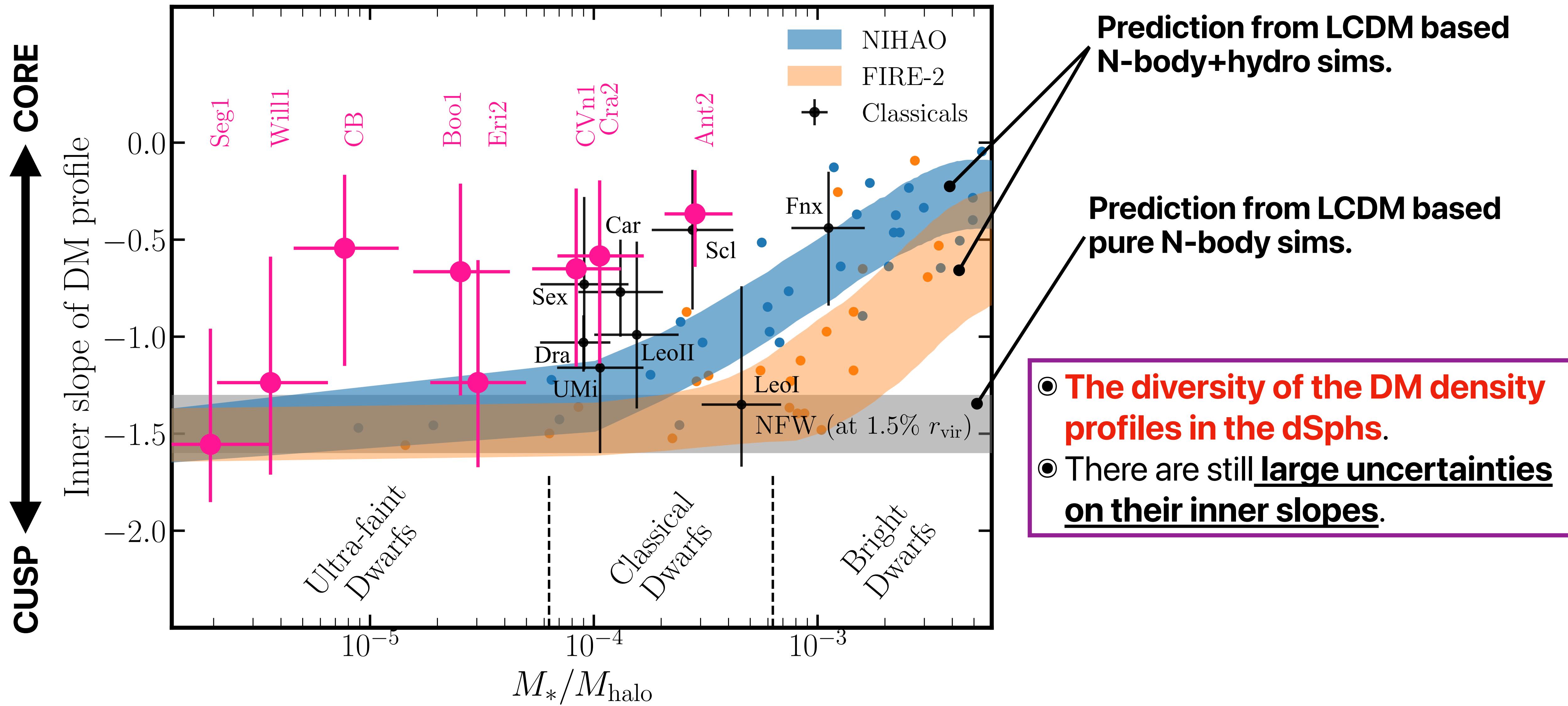
it is necessary to place tighter constraints⁺
on their dark matter density profiles.

- Proximity (30-100 kpc)
 - Clean targets for indirect D
 - Dark-matter rich system

on their *dark*

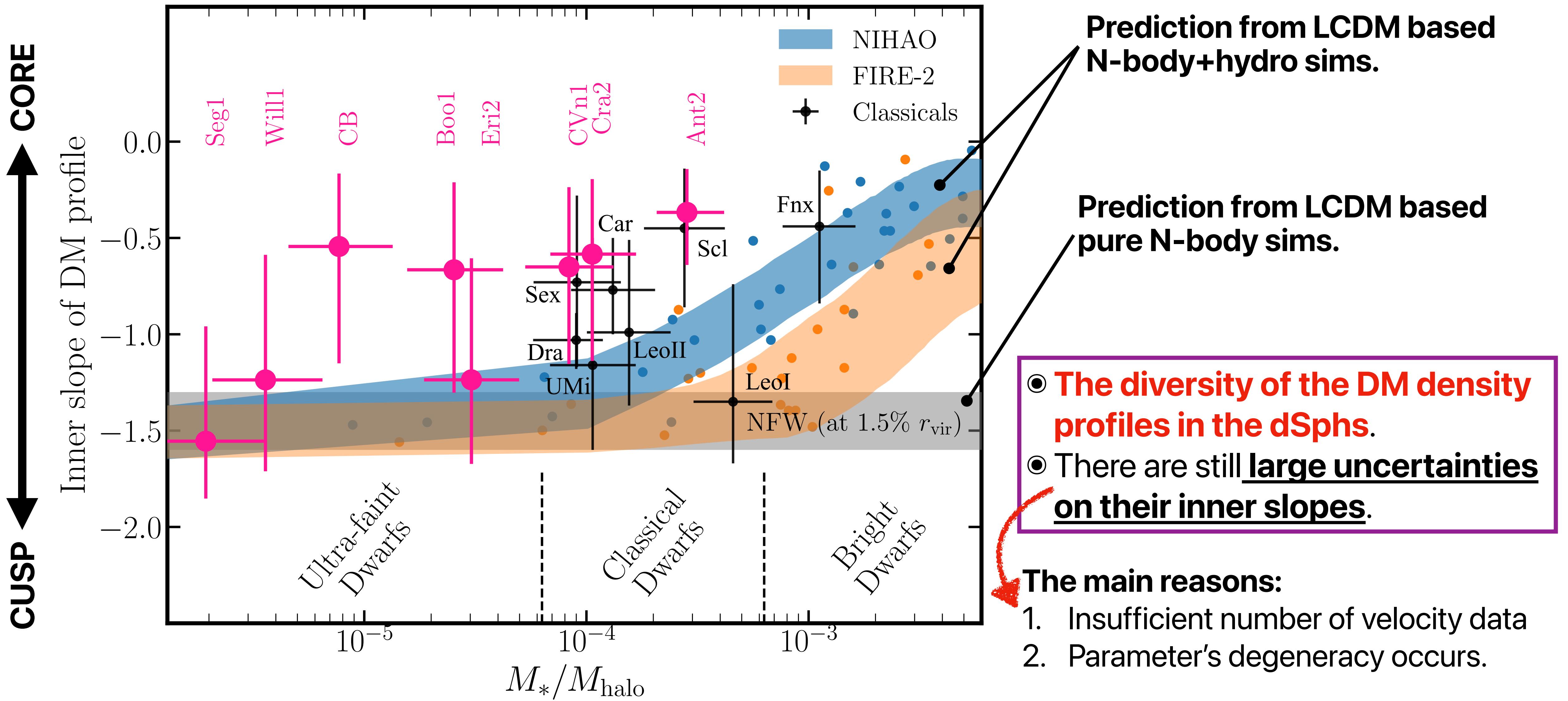
Diversity of the DM distributions?

KH, Chiba & Ishiyama (2020)
KH, Hirai, Chiba & Ishiyama (2023)



Diversity of the DM distributions?

KH, Chiba & Ishiyama (2020)
KH, Hirai, Chiba & Ishiyama (2023)



$\rho_{\text{DM}} - \beta_{\text{ani}}$ degeneracy

Ex. Spherical Jeans eq.

$$\frac{\partial[\nu(r)\sigma_r^2(r)]}{\partial r} + \frac{2\nu(r)\beta_{\text{ani}}(r)\sigma_r^2(r)}{r} = -\nu(r)\frac{GM_{\text{DM}}(r)}{r^2}$$

$$M_{\text{DM}}(r) = \int_0^r 4\pi s^2 \rho_{\text{DM}}(s) ds$$
$$\beta_{\text{ani}}(r) = 1 - \frac{\sigma_t^2(r)}{2\sigma_r^2(r)}$$

$\rho_{\text{DM}} - \beta_{\text{ani}}$ degeneracy

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Degeneracy occurs between velocity anisotropy parameter and density distribution.

$\rho_{\text{DM}} - \beta_{\text{ani}}$ degeneracy

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How to break the degeneracy?

$\rho_{\text{DM}} - \beta_{\text{ani}}$ degeneracy

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Degeneracy occurs between velocity anisotropy parameter and density distribution.

How to break the degeneracy?

- Higher-order velocity moments
- New observational data such as proper motions of each member star
- ...

$\rho_{\text{DM}} - \beta_{\text{ani}}$ degeneracy

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$$\frac{\partial[\nu(r)\sigma_r^2(r)]}{\partial r} + \frac{2\nu(r)\beta_{\text{ani}}(r)\sigma_r^2(r)}{r} = -\nu(r) \frac{GM_{\text{DM}}(r)}{r^2}$$

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How to break the degeneracy?

- Higher-order velocity moments
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- ...

Fourth order velocity moments and kurtosis

Wardana, Chiba, KH (2024, in prep.)

The shape of velocity distribution should be sensitive to velocity anisotropy.

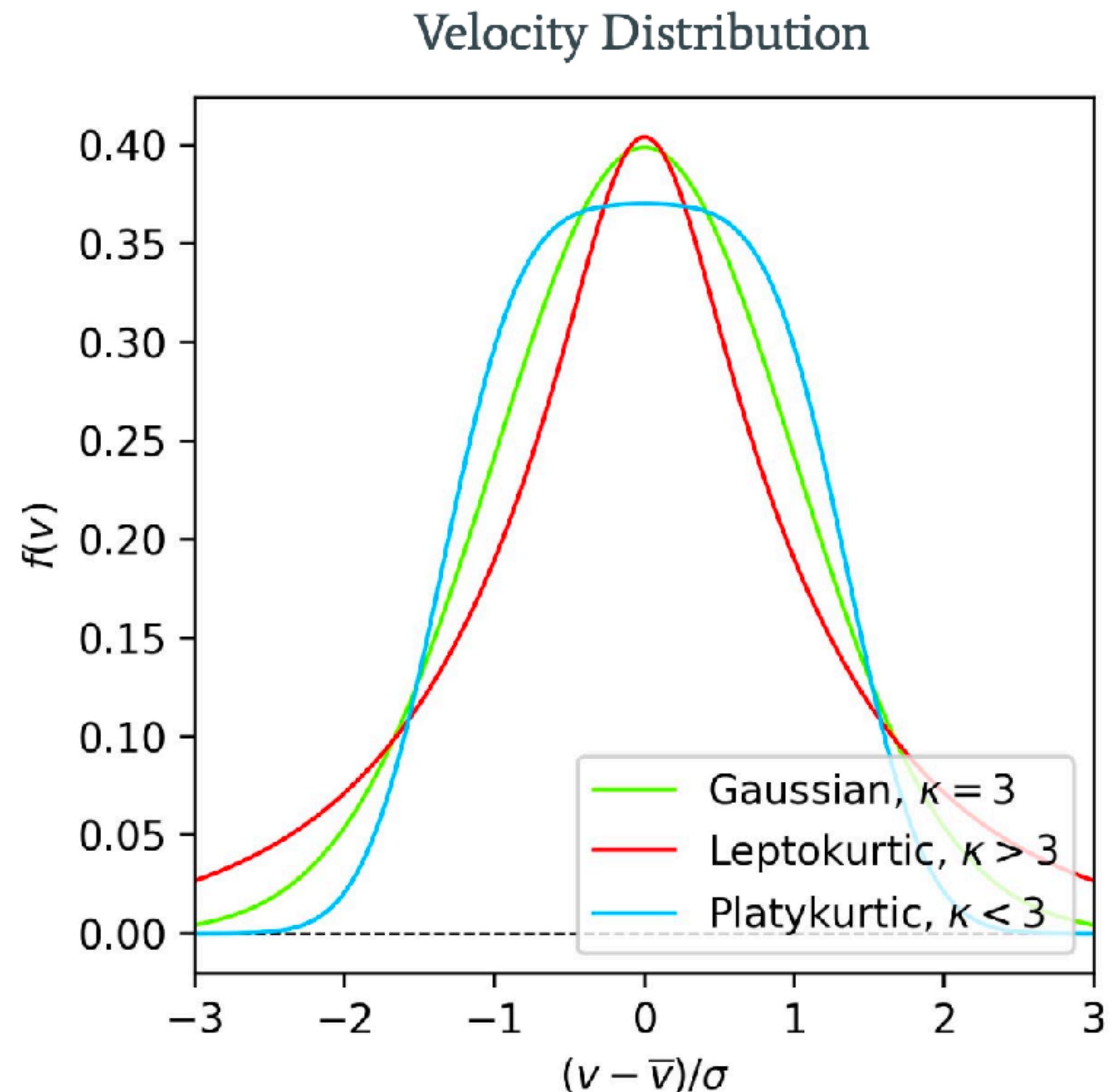
The 4th order velocity moments (spherically symmetry):

$$\overline{v_{\text{los}}^4}(R) = \frac{2}{I(R)} \int_R^\infty dr \left[1 - 2\beta \frac{R^2}{r^2} + \frac{1}{2}\beta(1+\beta) \frac{R^4}{r^4} \right] \frac{\nu v_r^4 r}{\sqrt{r^2 - R^2}}.$$

Kurtosis:

$$\kappa = \frac{\overline{v_{\text{los}}^4}}{(\sigma_{\text{los}}^2)^2}$$

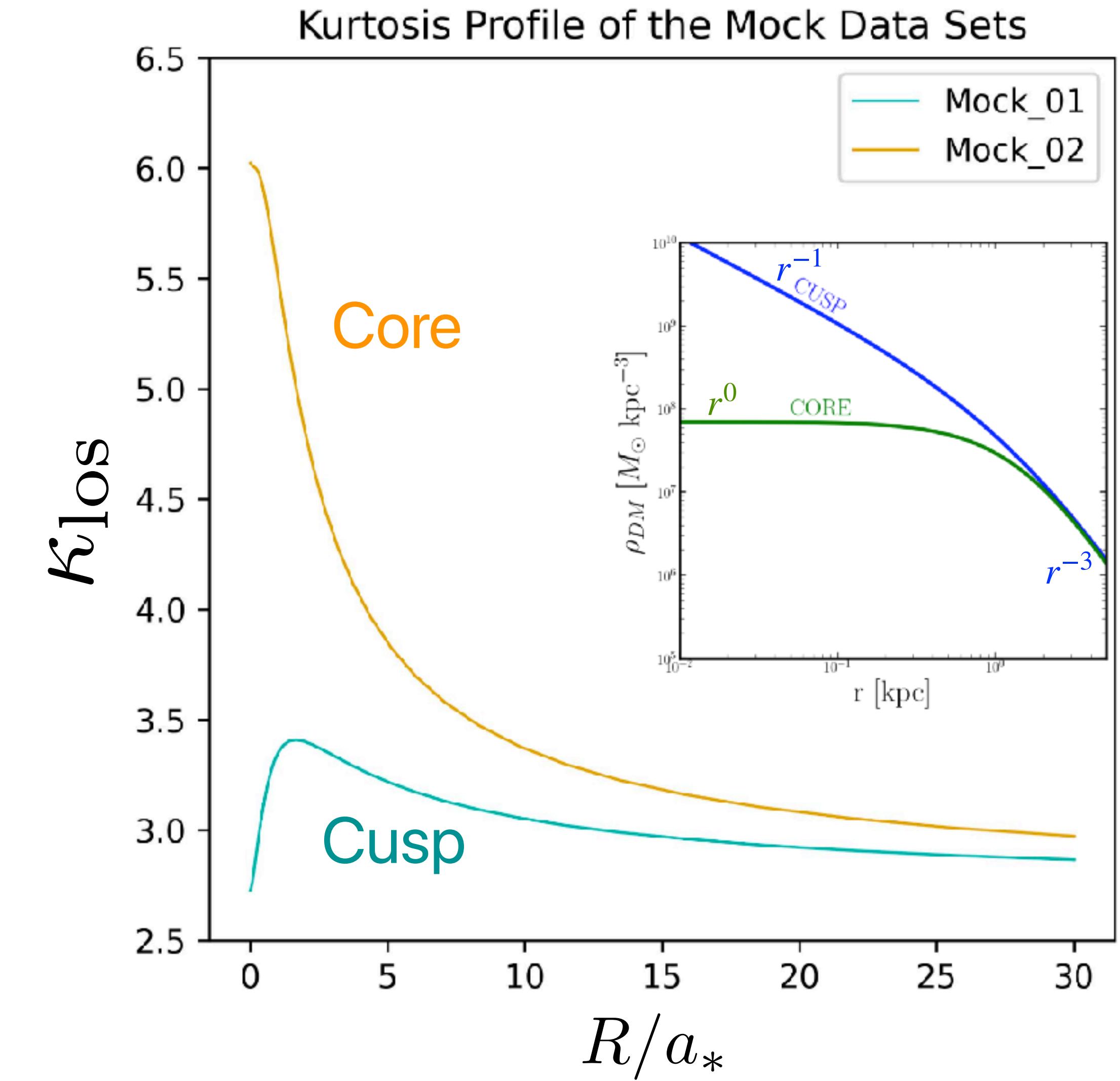
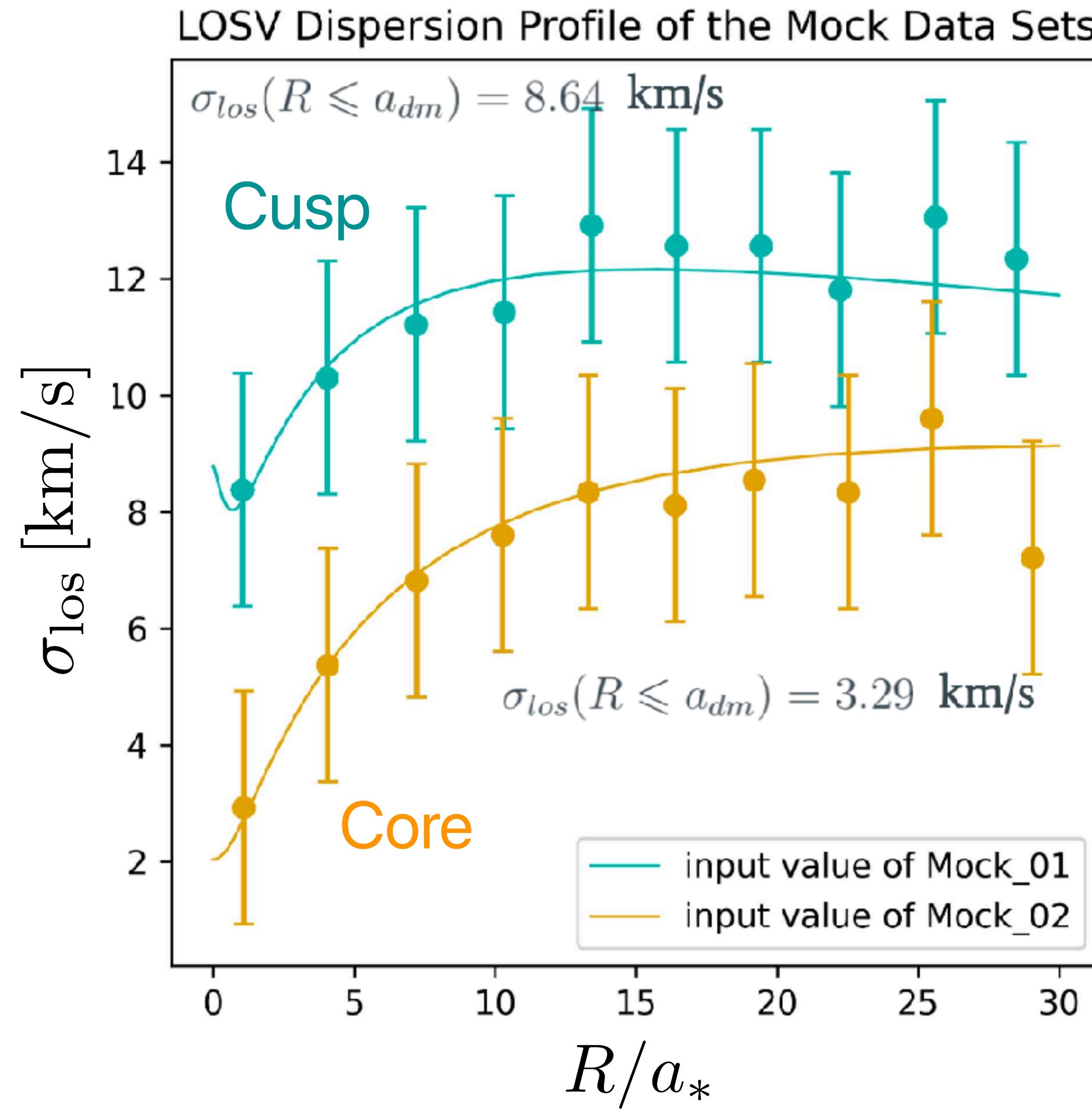
e.g., Lokas (2002), Richardson & Fairbairn (2012)



Application to mock data sets

Wardana, Chiba, KH (2024, in prep.)

Two sets of new mock data: cuspy (green) and core (orange) (isotropic: $\beta = 0.$)



Result: The power of 4th-order moments

Wardana, Chiba,
KH (2024, in prep.)

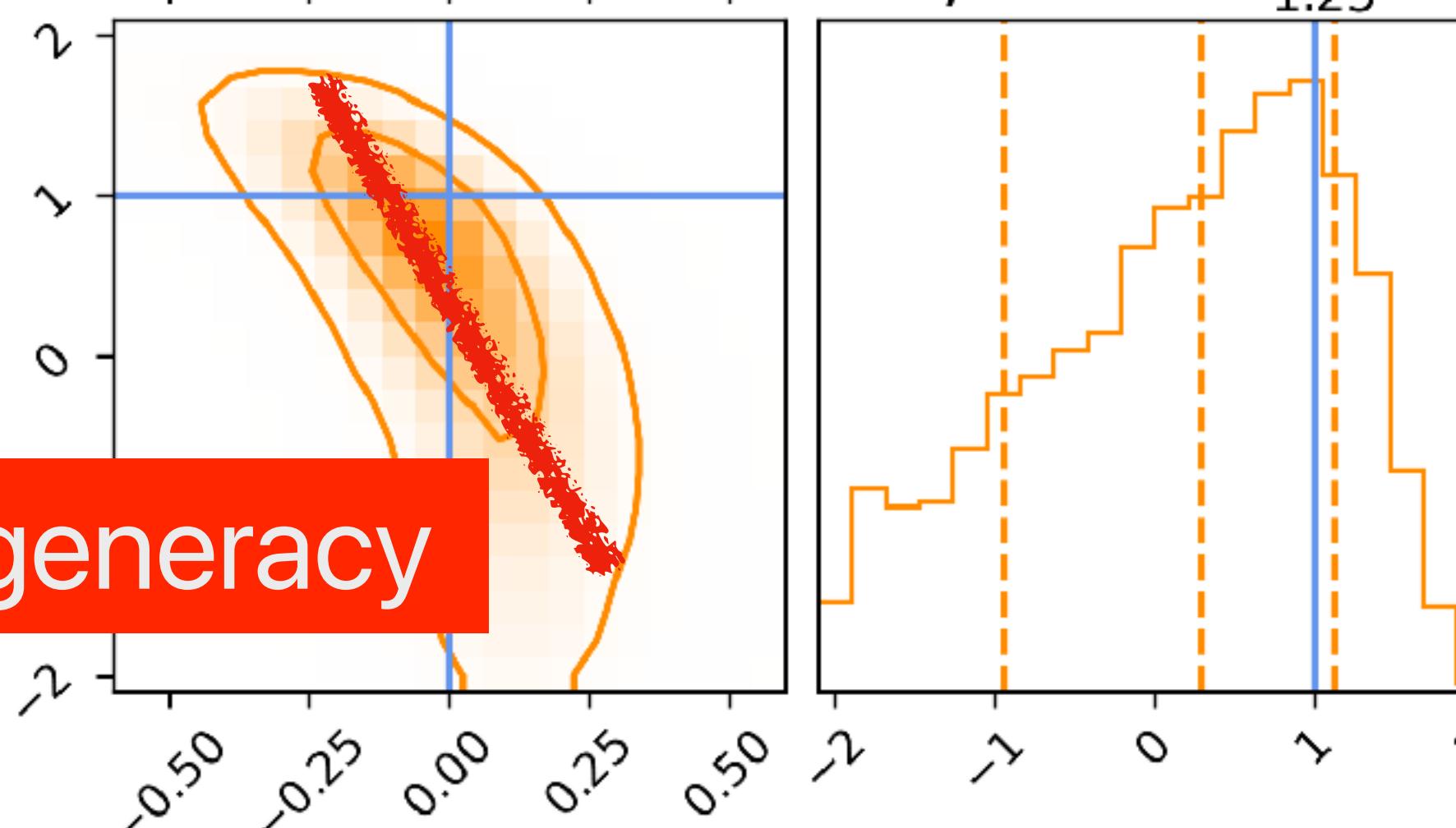
$N_{\text{star}} = 500$ stars, $v_{\text{err}} = 2$ km/s (Similar to the typically available data for MW's dSphs)



$$-\log(1 - \beta) = 0.01^{+0.16}_{-0.18}$$

2nd-order only

Dafa Wardana



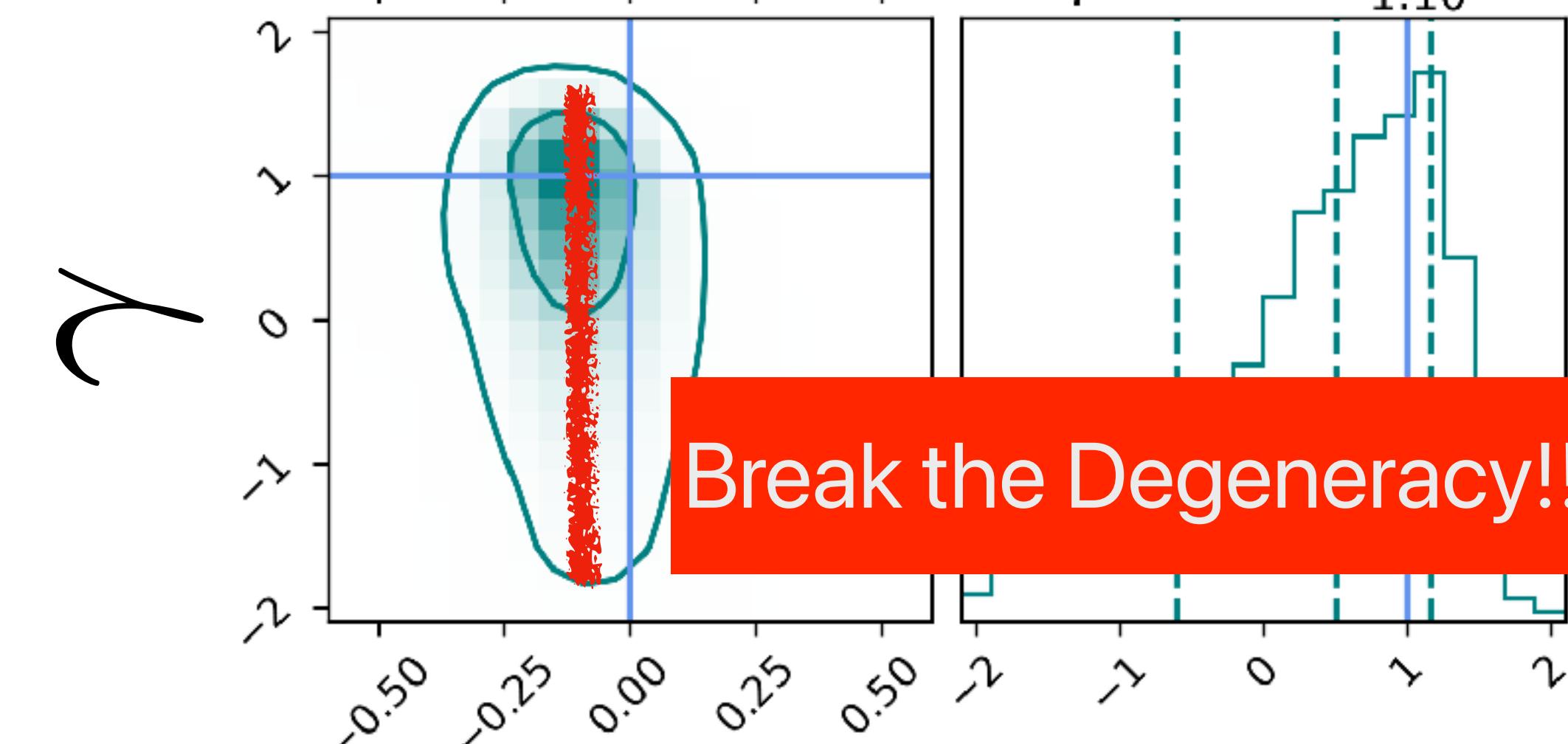
Degeneracy

$$-\log_{10}(1 - \beta)$$

$$\gamma$$

$$-\log(1 - \beta) = -0.11^{+0.11}_{-0.11}$$

2nd & 4th-order



Break the Degeneracy!!

$$-\log_{10}(1 - \beta)$$

$$\gamma$$

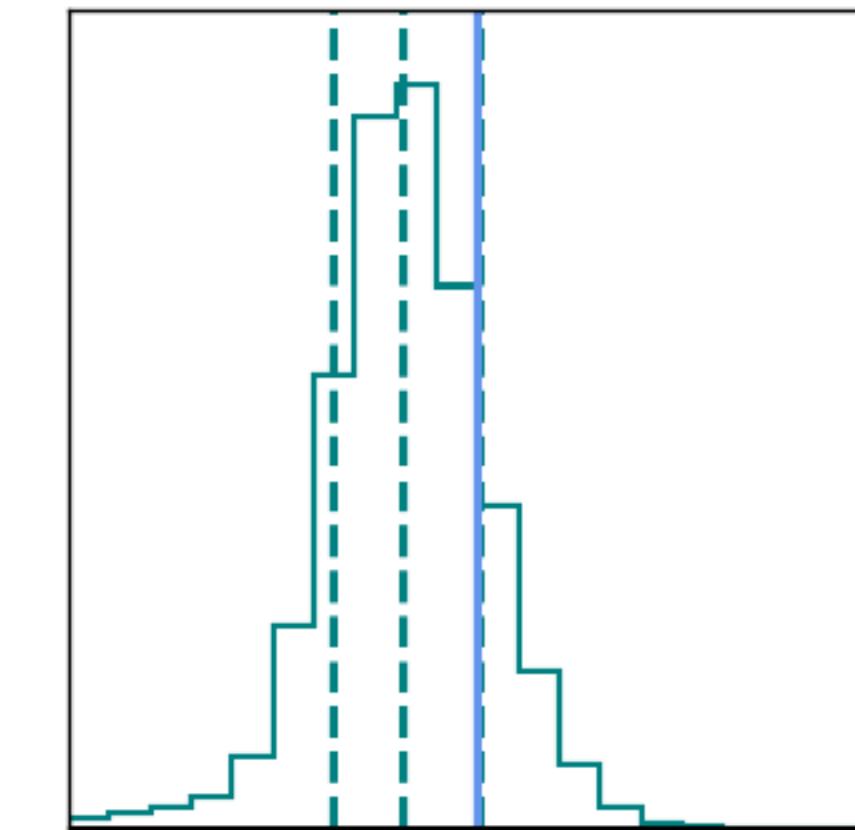
Result: Dependence of N_{star}

Wardana, Chiba, KH (2024, in prep.)

2nd & 4th-order moments analysis, $v_{\text{err}} = 2 \text{ km/s}$ is fixed.

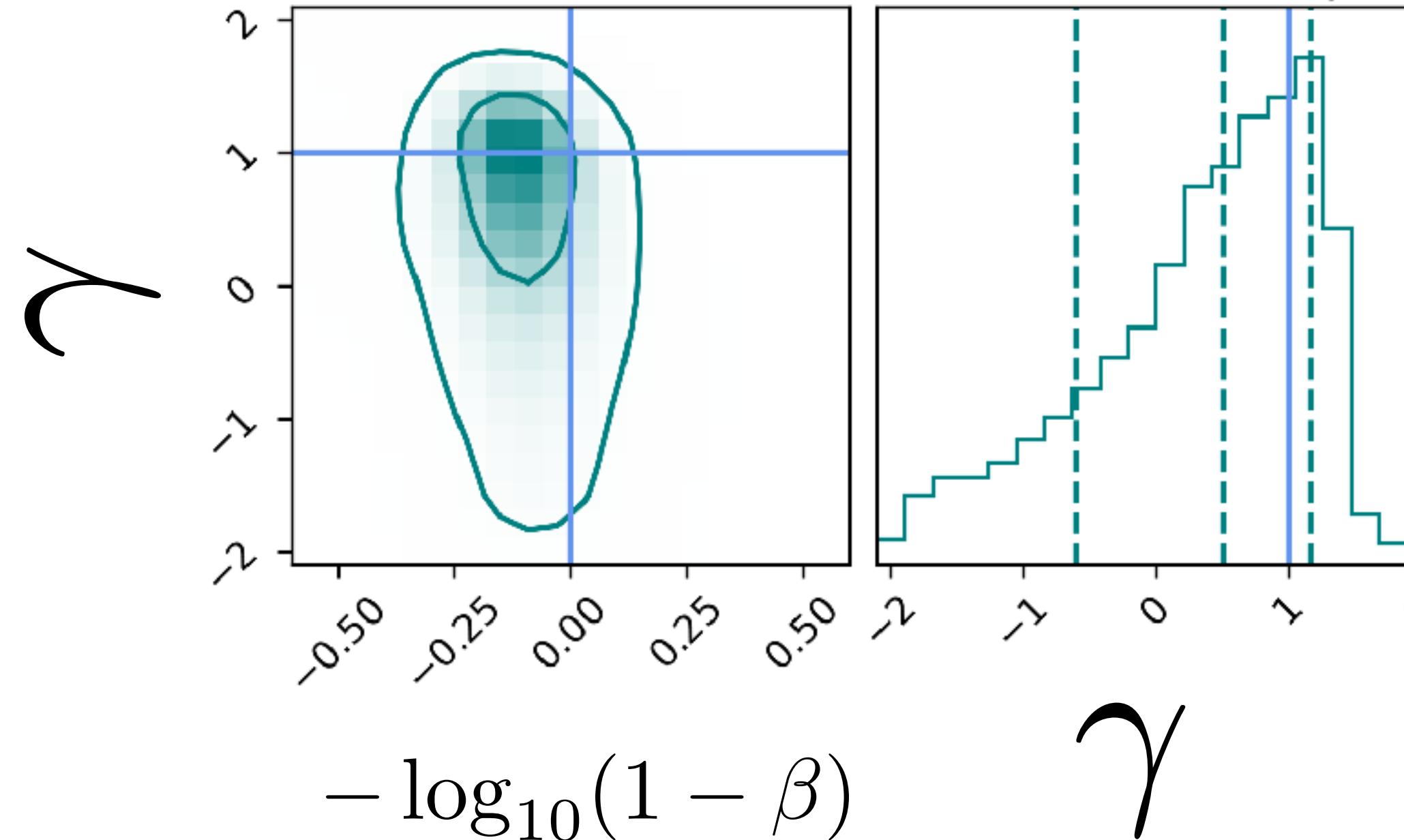


$$-\log(1 - \beta) = -0.11^{+0.11}_{-0.11}$$

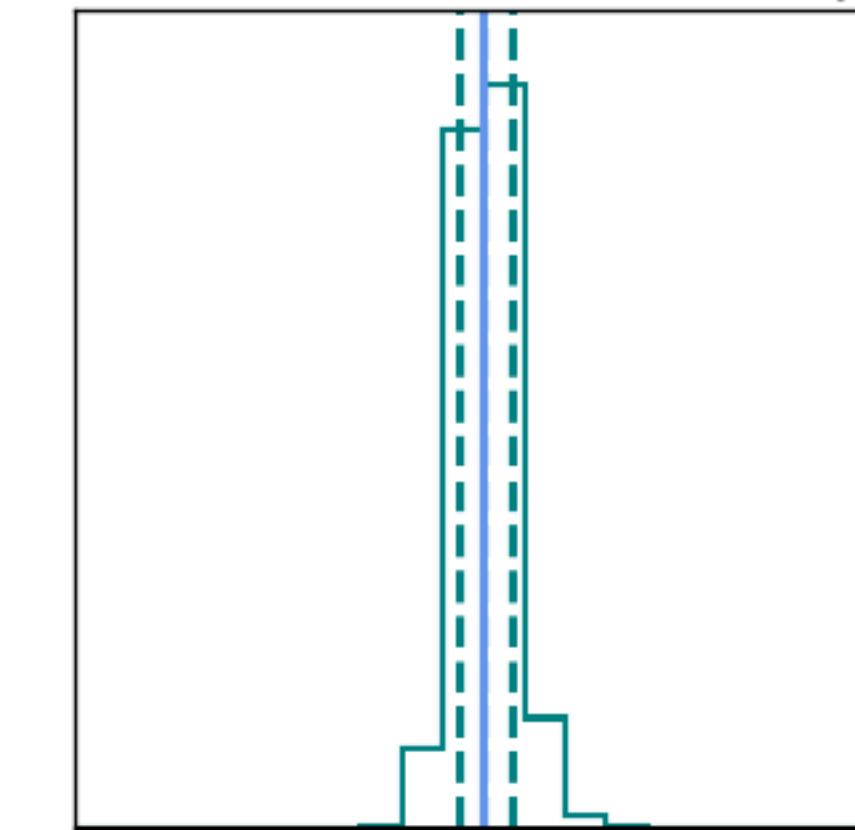


500 stars

$$\gamma = 0.50^{+0.66}_{-1.10}$$

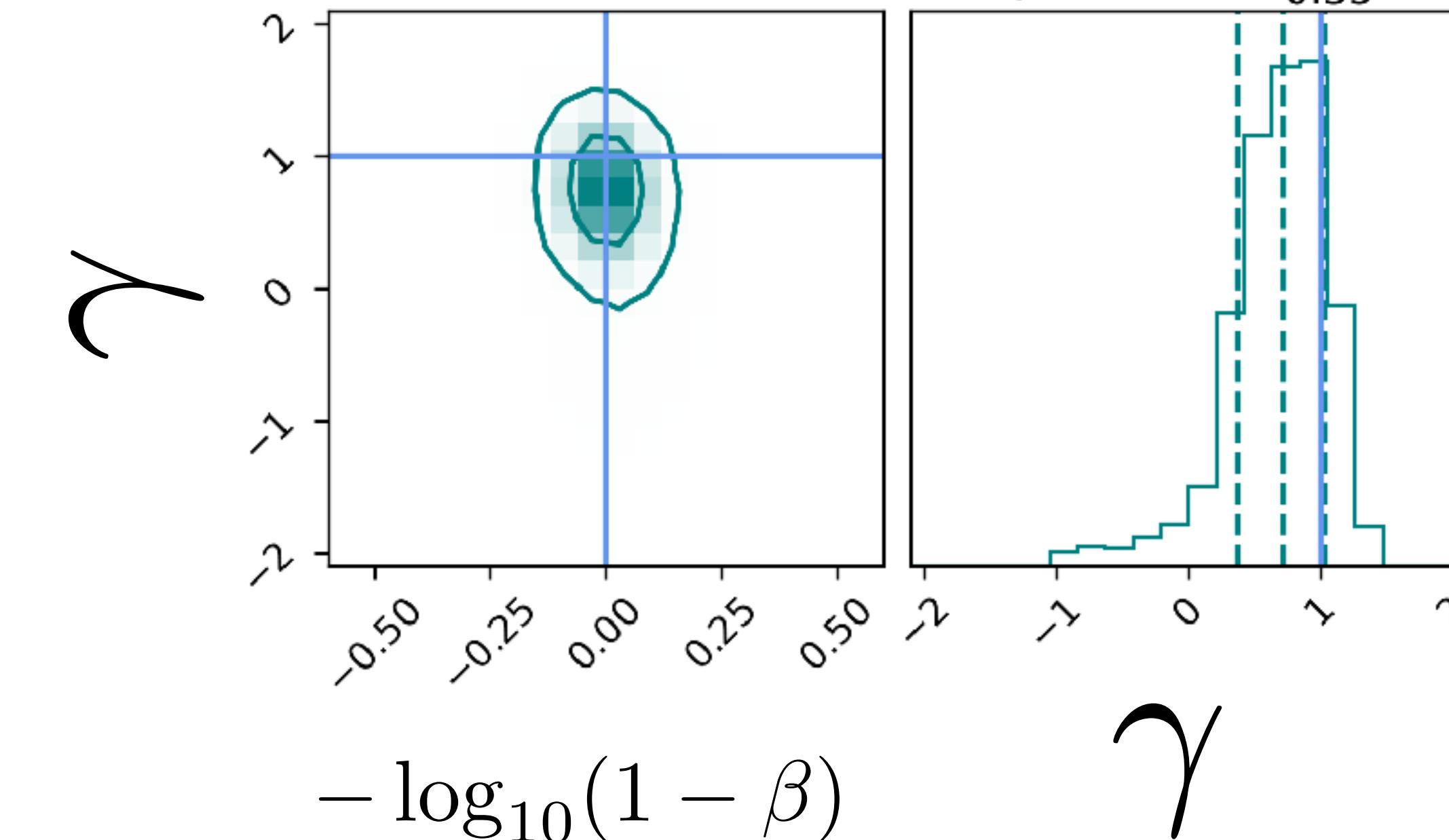


$$-\log(1 - \beta) = 0.00^{+0.04}_{-0.04}$$



5000 stars

$$\gamma = 0.72^{+0.31}_{-0.35}$$



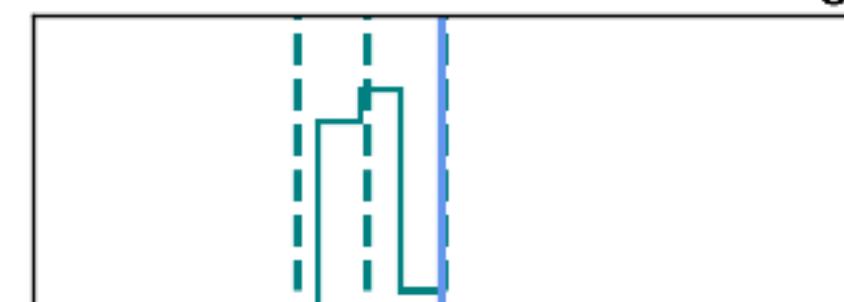
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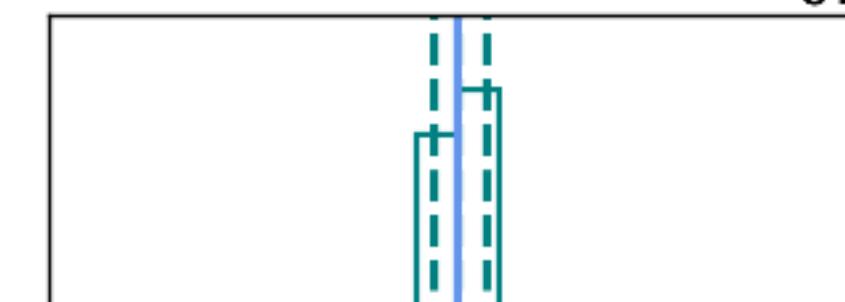


$$-\log(1 - \beta) = -0.11^{+0.11}_{-0.11}$$



500 stars

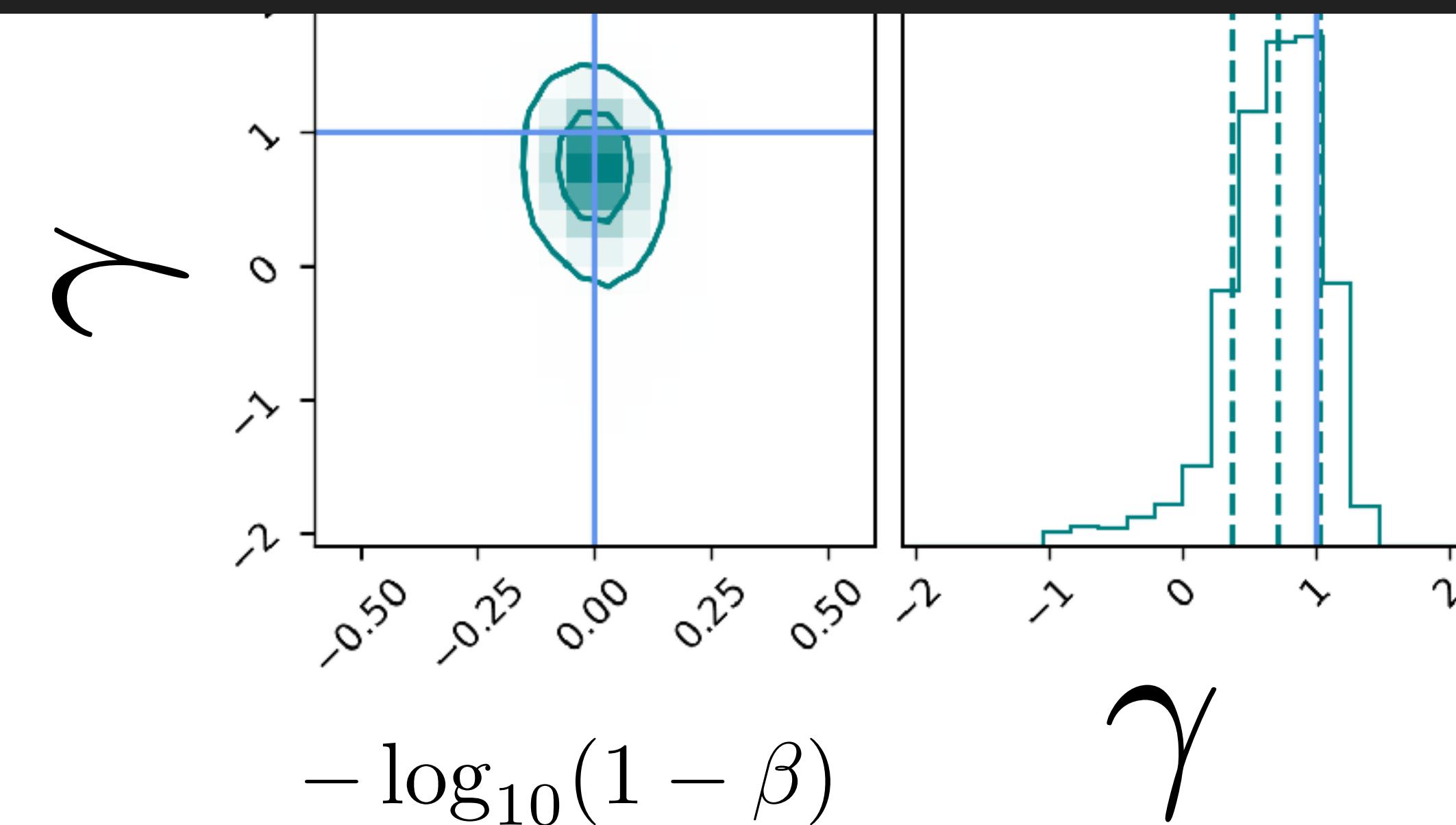
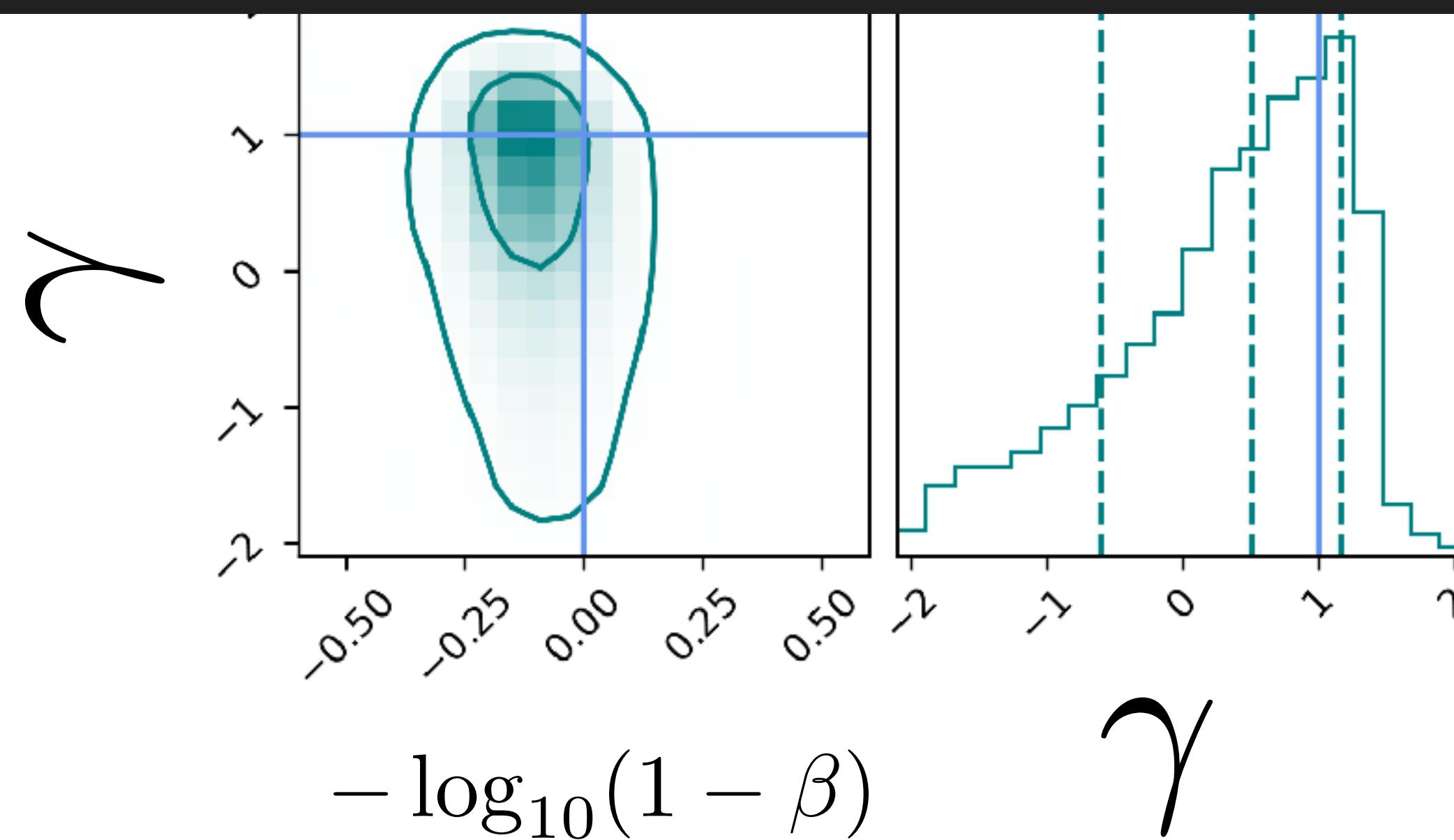
$$-\log(1 - \beta) = 0.00^{+0.04}_{-0.04}$$



5000 stars

Daf

Numerous kinematic data should be required to place constraints on the DM profile!



Result: Dependence of V_{err}

Wardana, Chiba, KH (2024, in prep.)

2nd & 4th-order moments analysis, $N_{\text{star}} = 5000$.



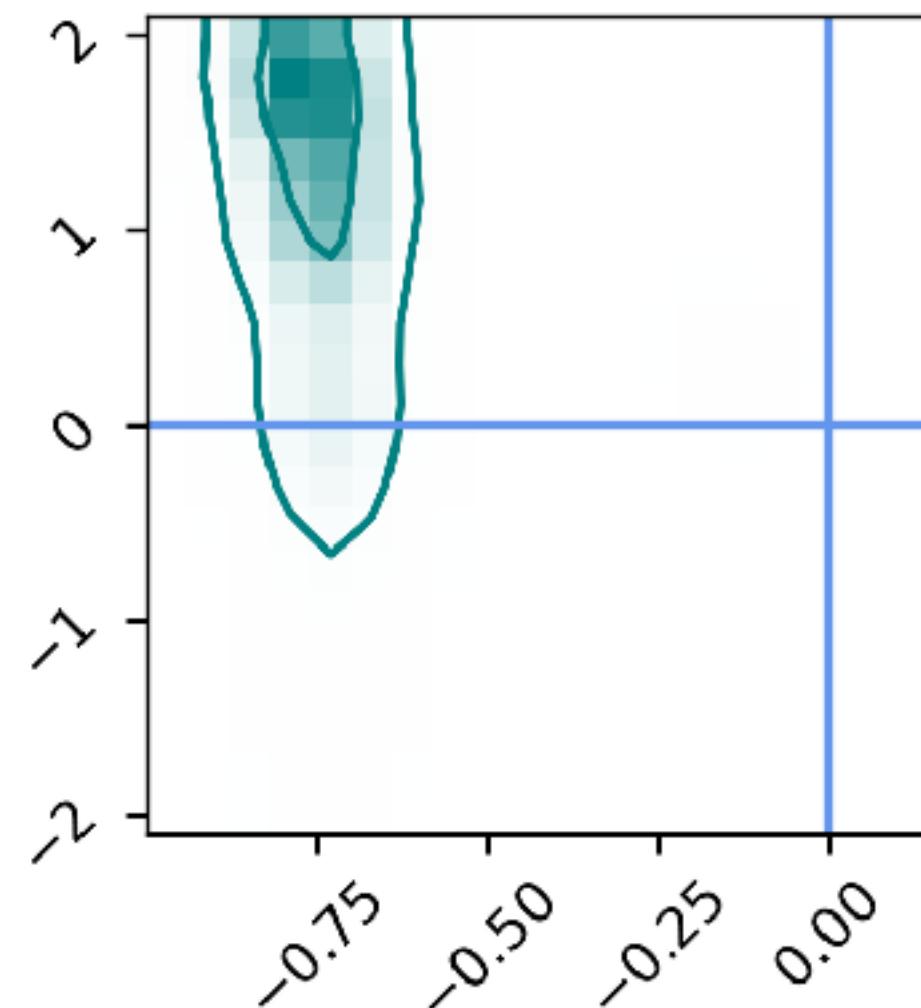
$$-\log(1 - \beta) = -0.75^{+0.03}_{-0.04}$$

$$\frac{\sigma_{\text{dSph}}}{v_{\text{err}}} \sim 1$$

$$v_{\text{err}} \sim 2.0 \text{ km/s}$$

$$\gamma = 1.24^{+0.57}_{-1.09}$$

γ



$$-\log_{10}(1 - \beta)$$

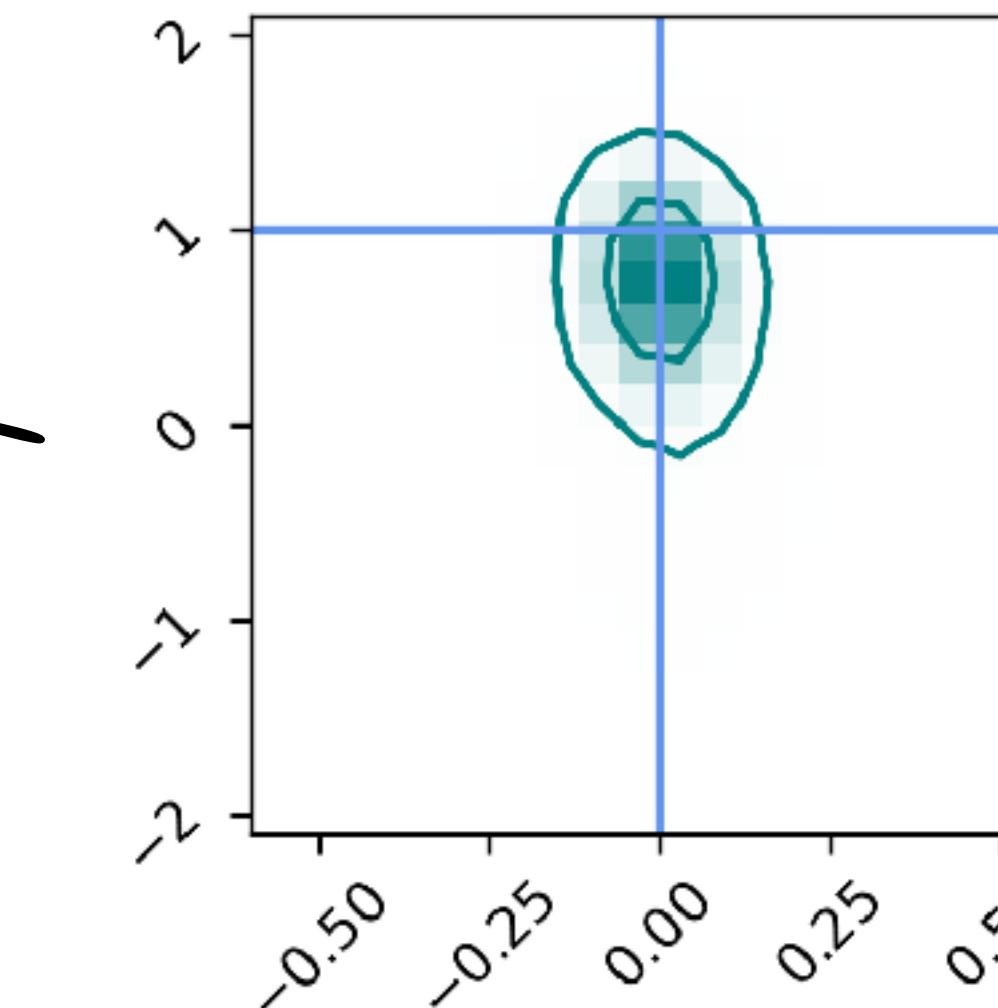
γ

$$-\log(1 - \beta) = 0.00^{+0.04}_{-0.04}$$

$$\frac{\sigma_{\text{dSph}}}{v_{\text{err}}} \sim 100$$

$$v_{\text{err}} \sim 0.01 \text{ km/s}$$

$$\gamma = 0.72^{+0.31}_{-0.35}$$



$$-\log_{10}(1 - \beta)$$

γ

Result: Dependence of V_{err}

Wardana, Chiba, KH (2024, in prep.)

2nd & 4th-order moments analysis, $N_{\text{star}} = 5000$.



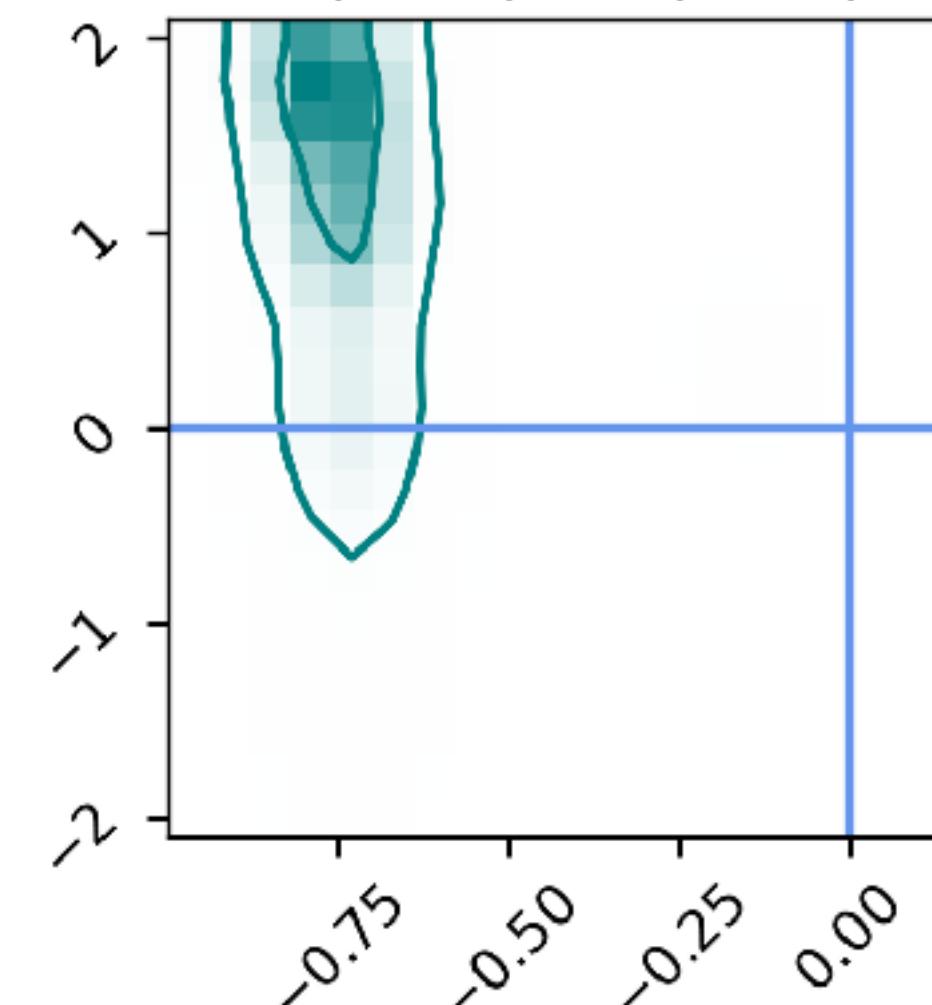
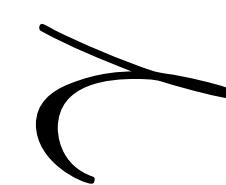
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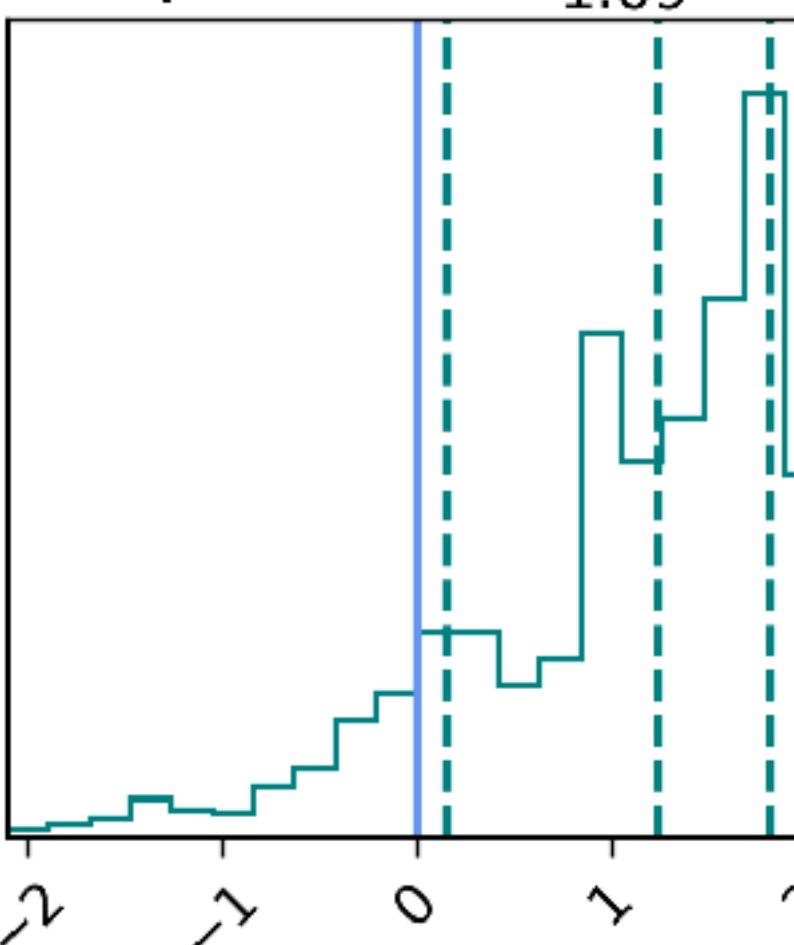
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Dafa Wardana



$$-\log_{10}(1 - \beta)$$

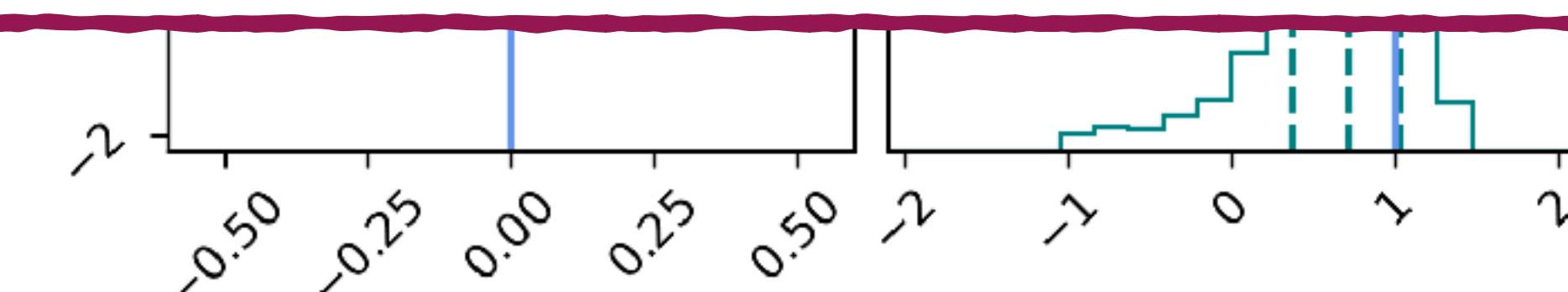
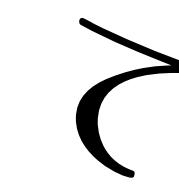
$$\gamma$$



$$-\log(1 - \beta) = 0.00^{+0.04}_{-0.04}$$

The systematic bias cannot be eliminated by increasing the number of stars.
It starts to be smaller than the velocity error when

$$\frac{\sigma_{\text{dSph}}}{v_{\text{err}}} \gtrsim 4$$



$$-\log_{10}(1 - \beta)$$

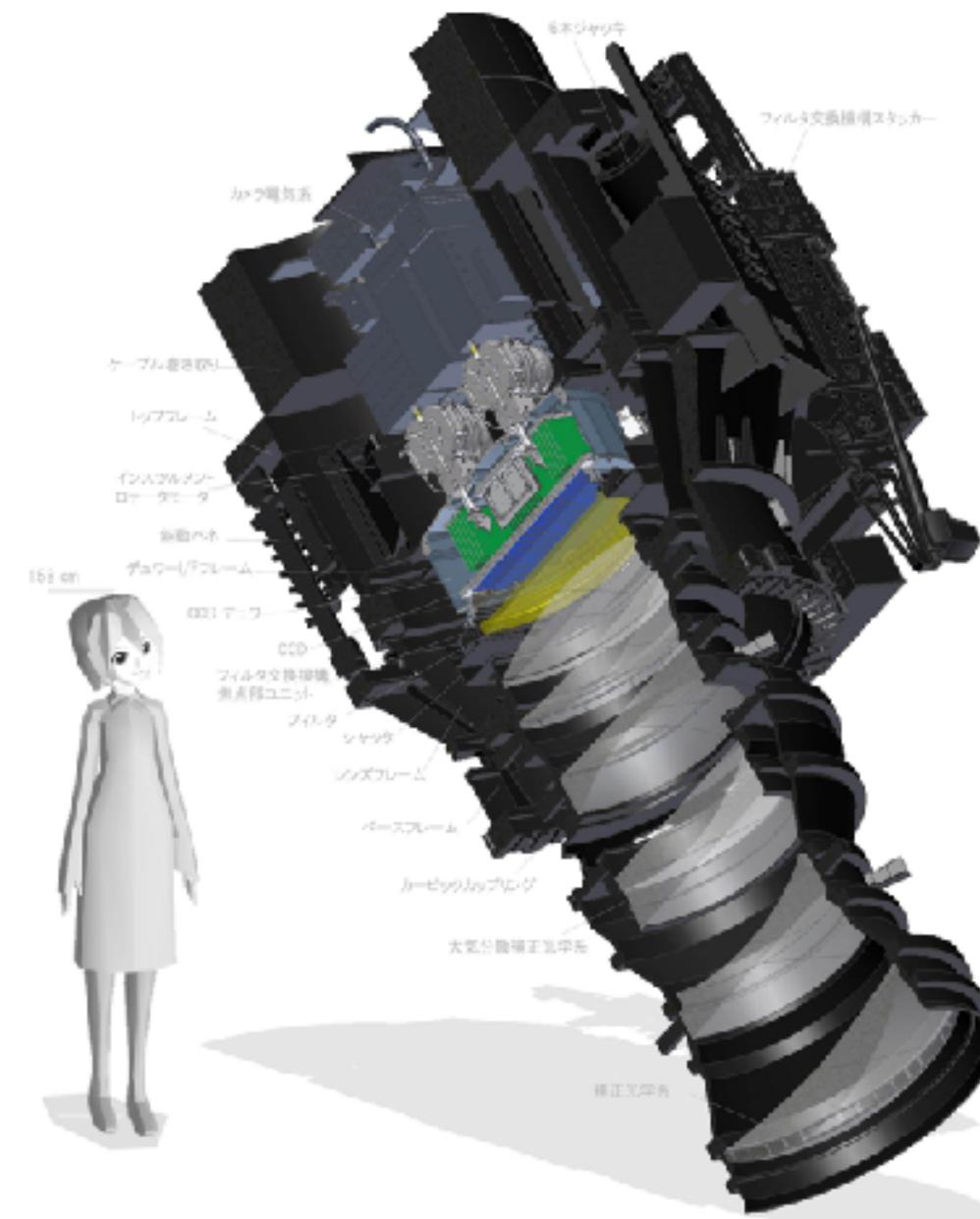
$$\gamma$$

Fourth order velocity moments and kurtosis

Wardana, Chiba, KH (2024, in prep.)

To place further constraints on DM profiles in the dSphs via 4th order analysis,

- Large number of kinematic data
- Precise velocity measurements



Subaru-HSC

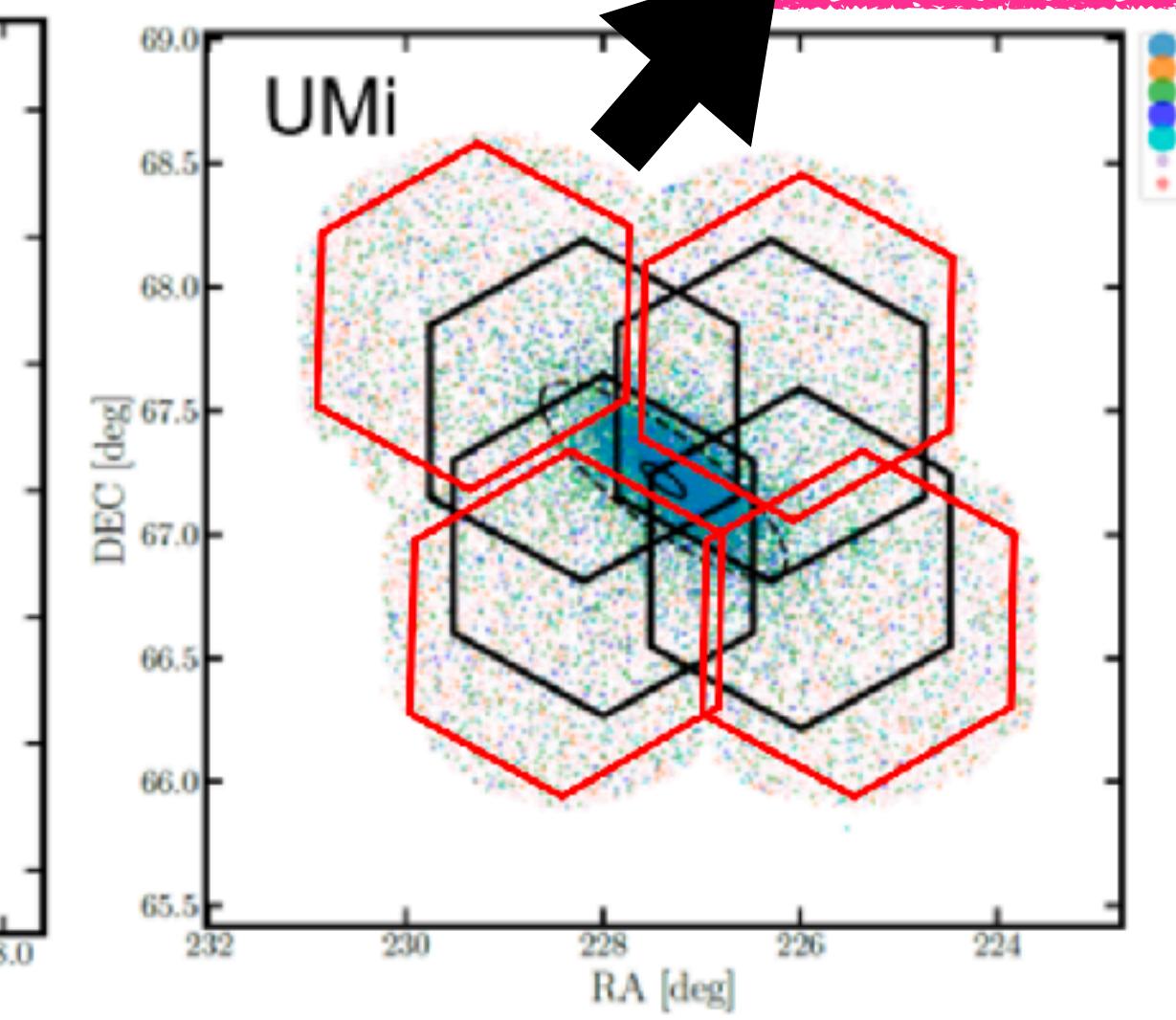
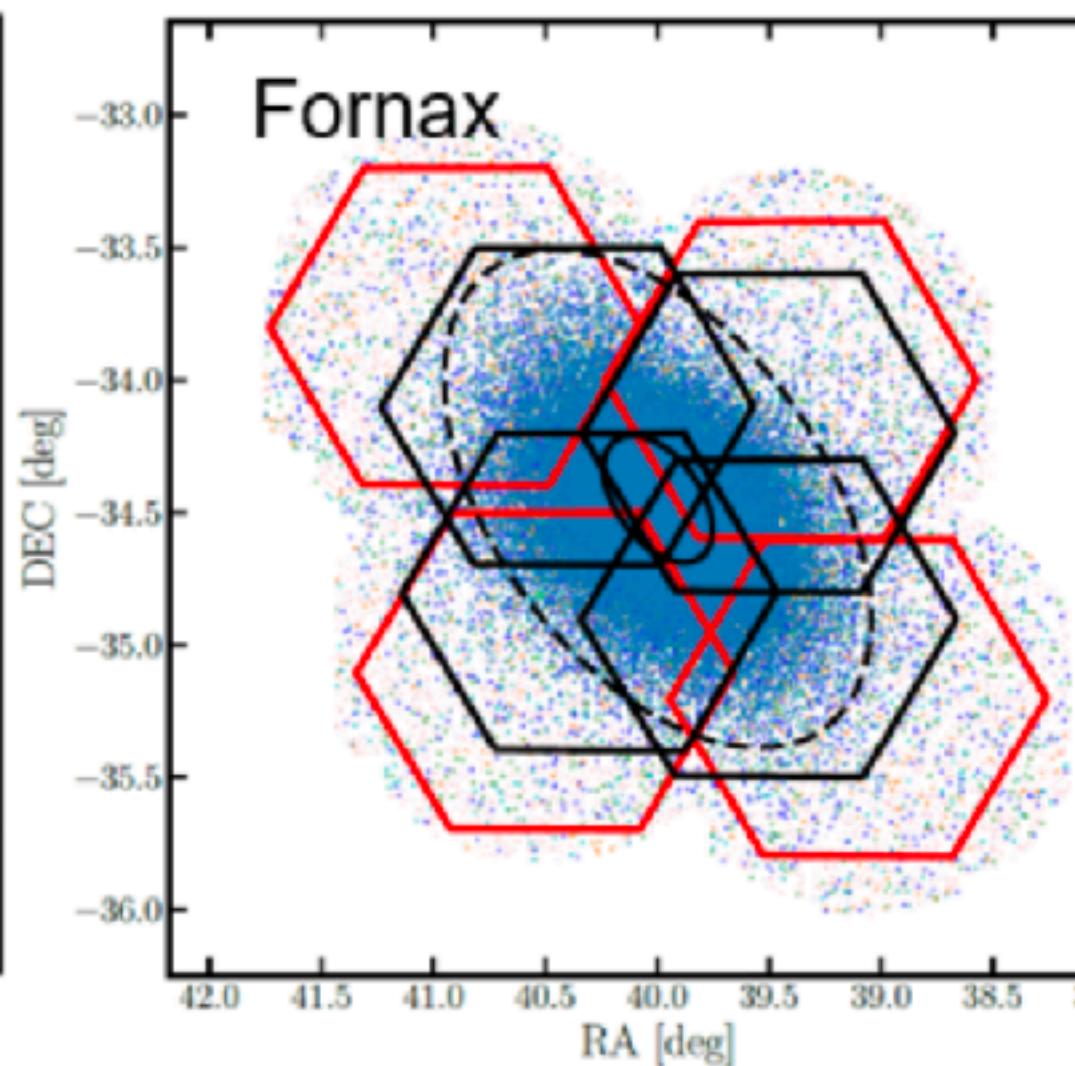
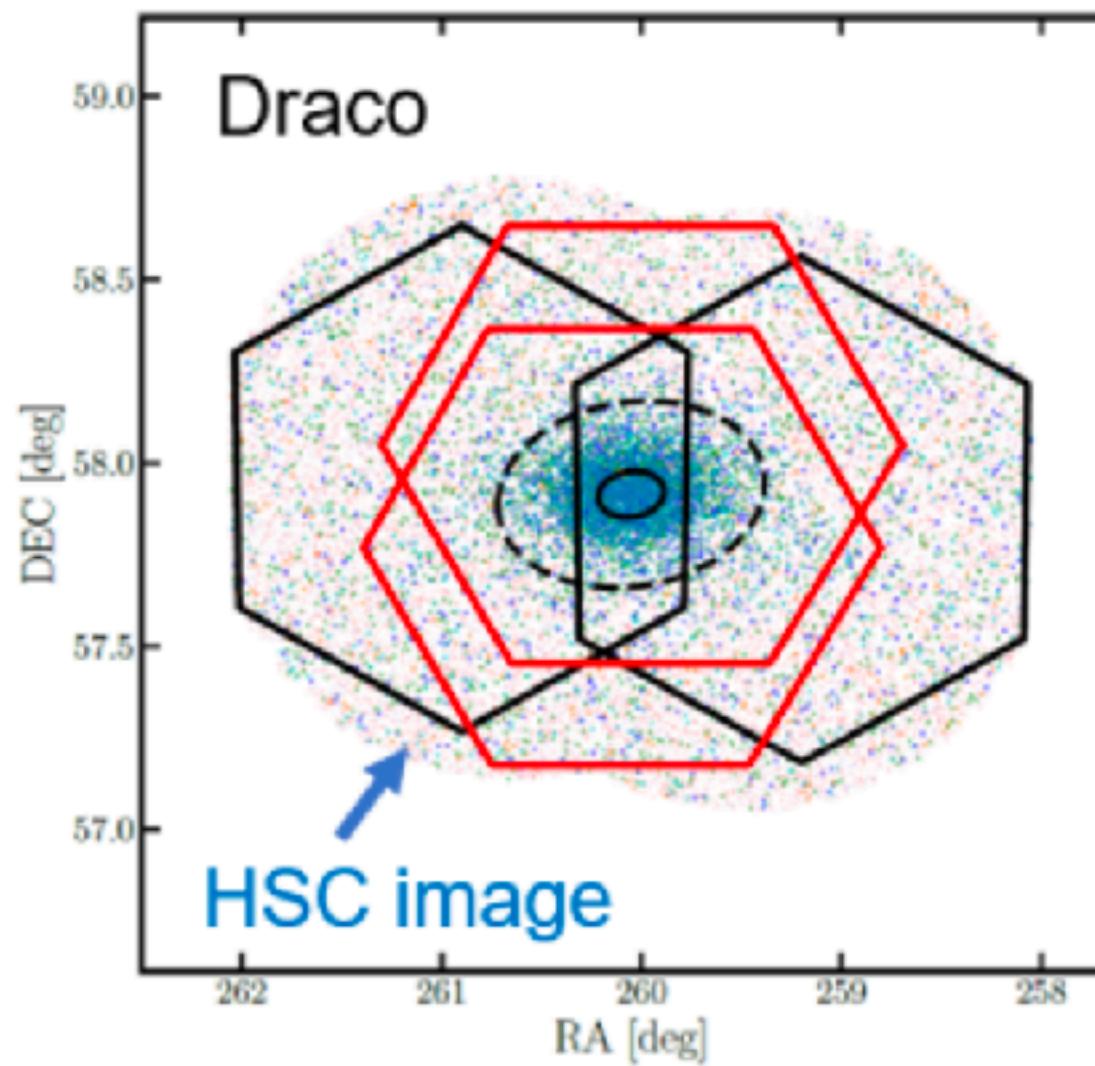


Subaru-PFS

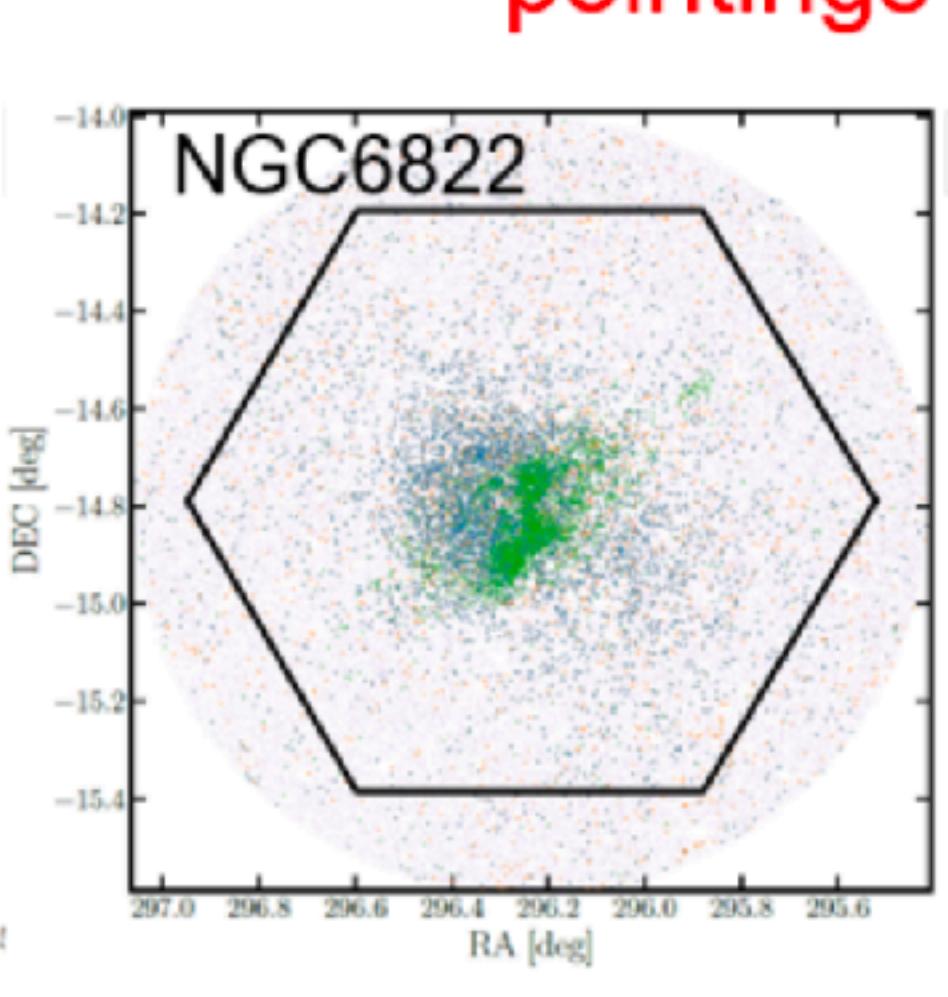
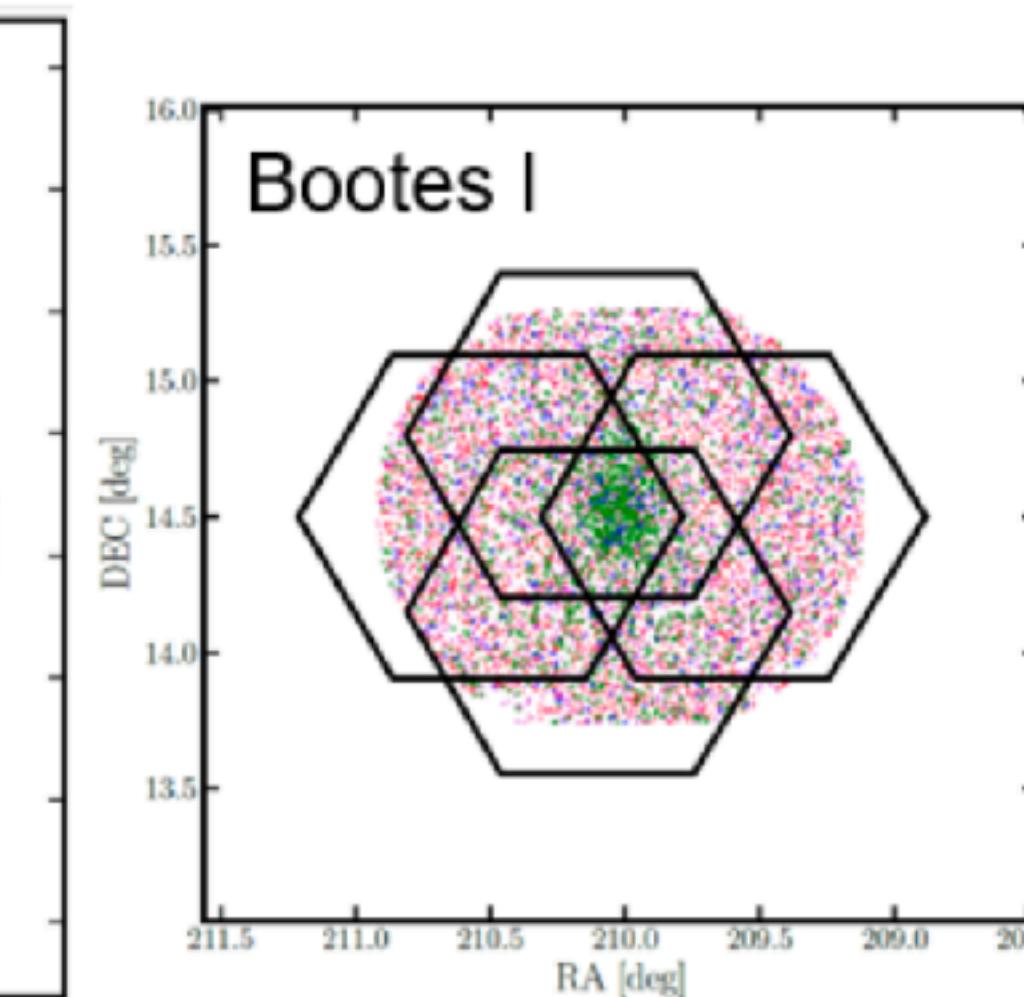
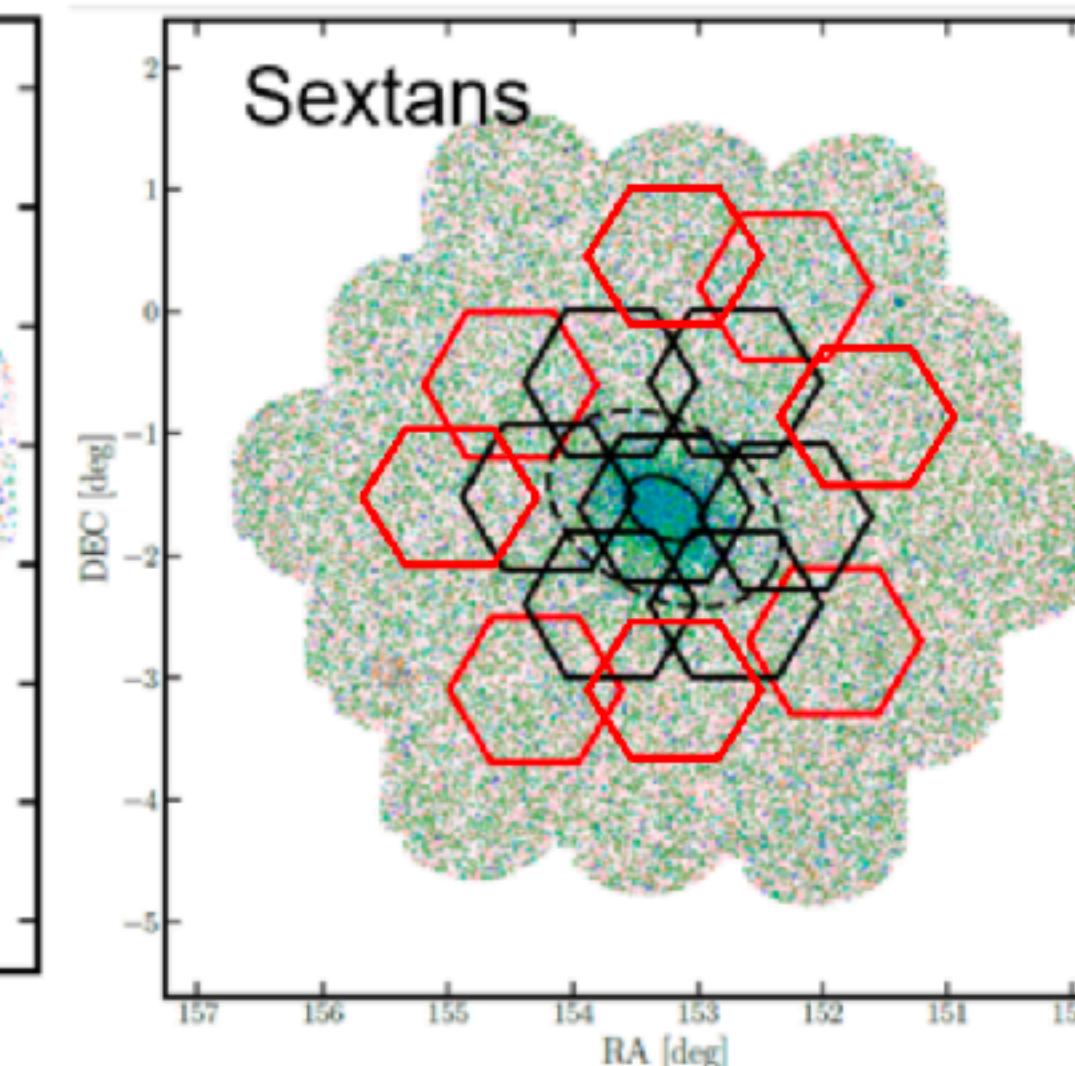
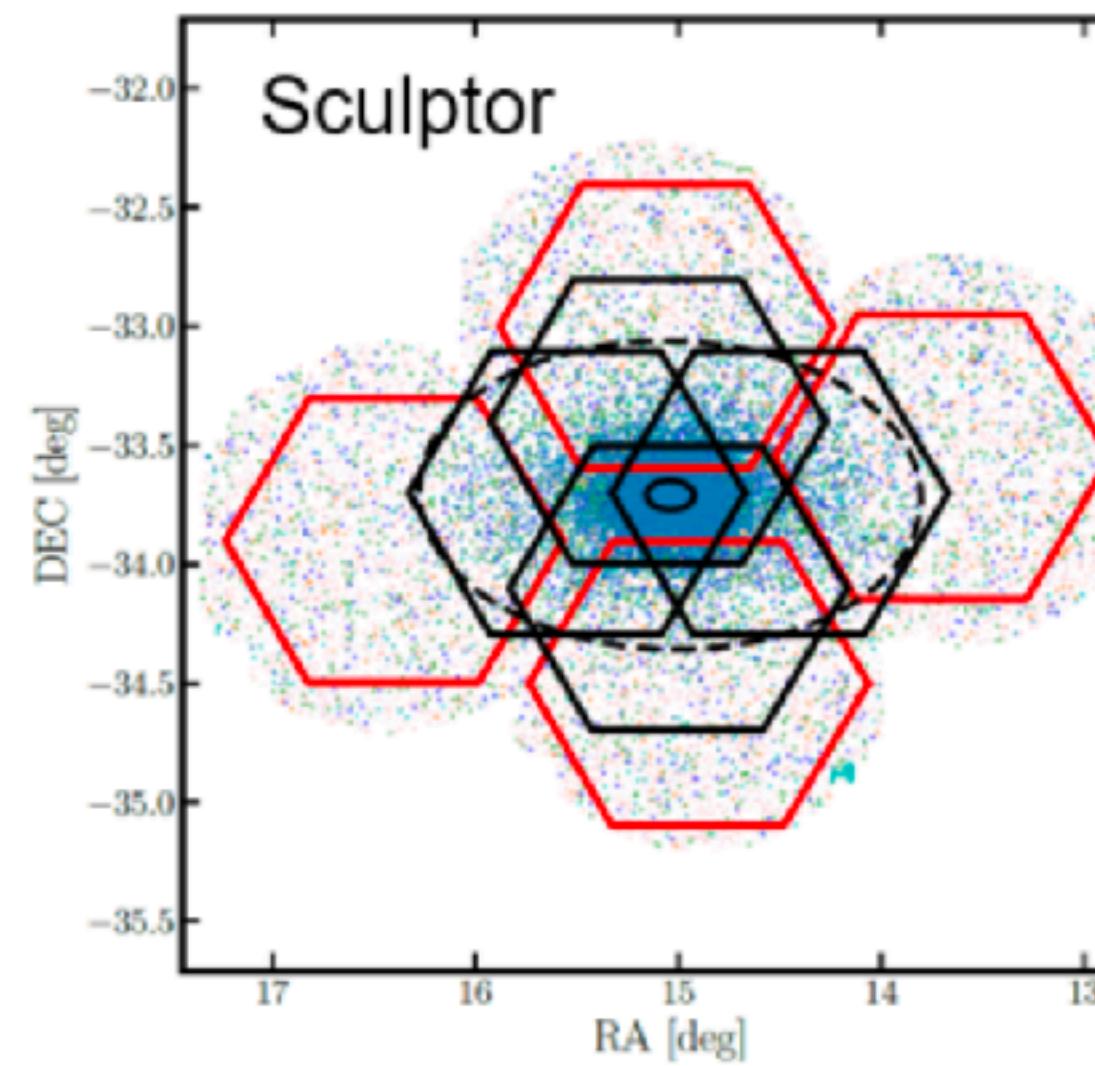
Subaru-PFS is coming soon.

Current
 $N_{\text{spec.}} \sim 300$

PFS
 $N_{\text{spec.}} \sim 5000$



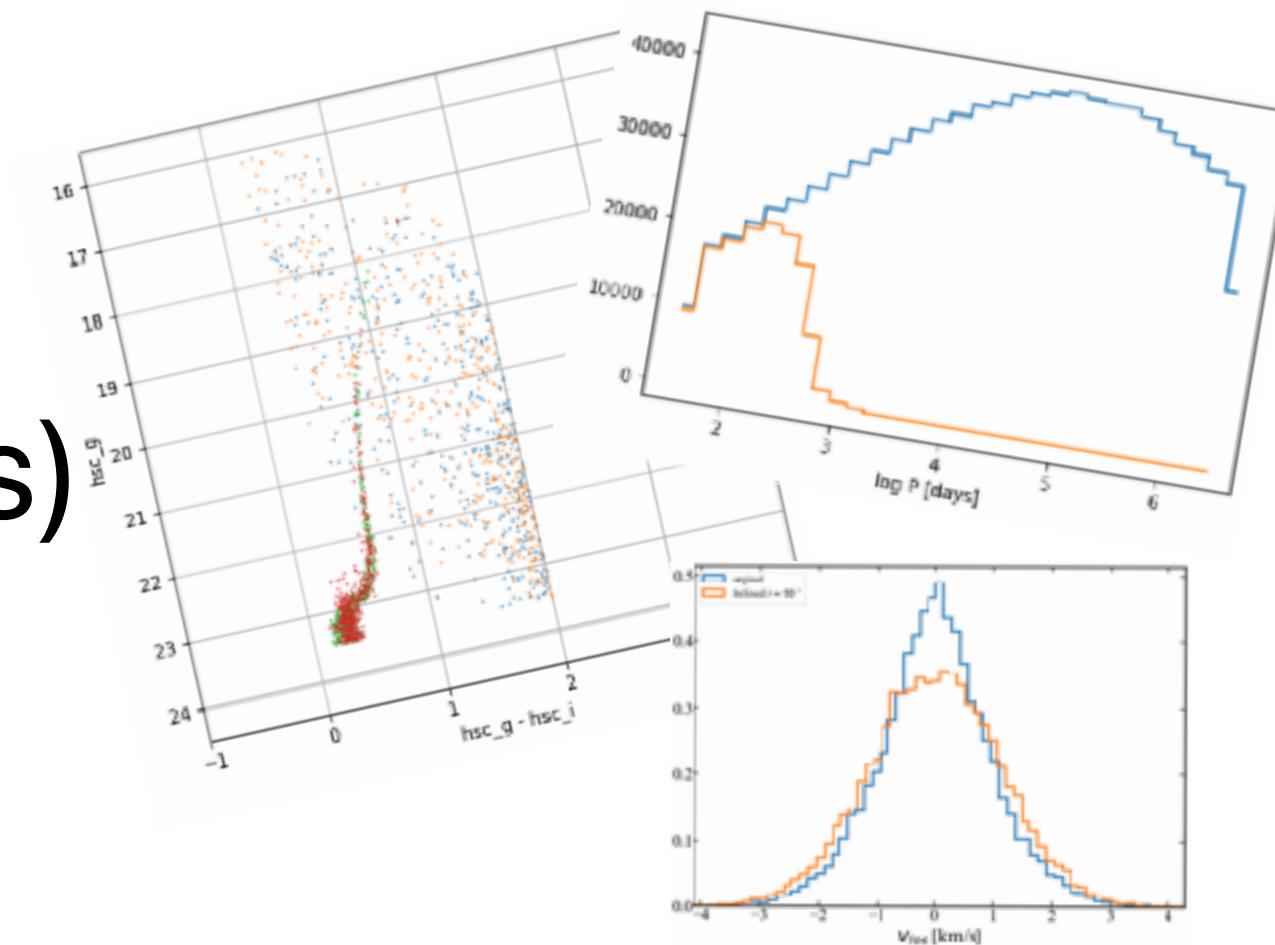
Background:
HSC image
Dashed line:
tidal radius
Red: extra
pointings



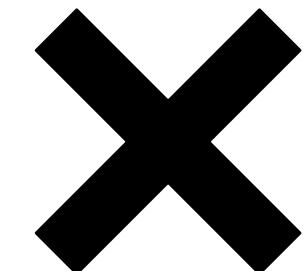
1

Non-trivial effects on dynamical analysis should be considered

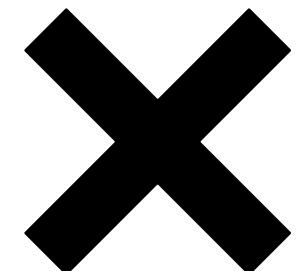
- Contamination stars (MW think disk, thin disk, and halo stars)
- Binary stars (Binary system can inflate l.o.s velocity dispersions)
- Tidal forces (Deviation from dynamical equilibrium)



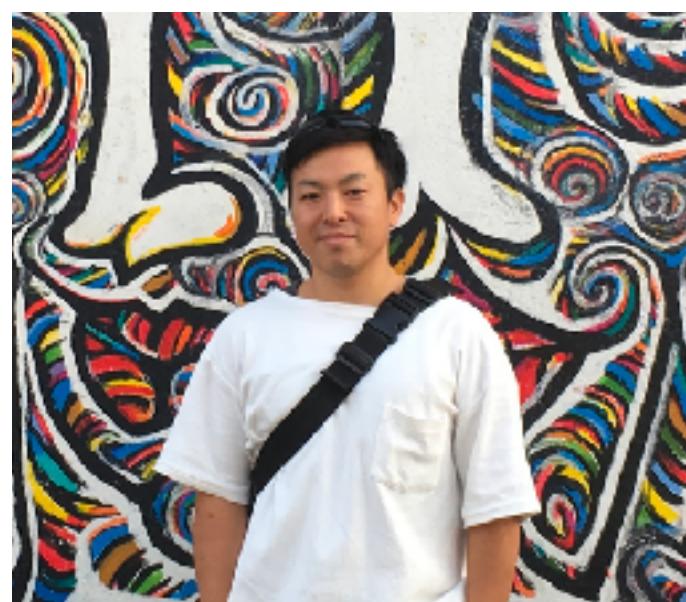
Kinematic info.
generated by DM
potential



Binary stars



Contamination stars



KH



E. Kirby (Notre Dame)



L. Dobos (JHU)



C. Filion (JHU)

DM density profile estimation through normalizing flows

Lim, KH, Nojiri et al. (2024, in prep.)

Observable informations are limited to:

- Celestial coordinate
- Line-of-sight velocity

$$(x, y, z, v_x, v_y, v_z) \longrightarrow (x, y, v_z)$$



Conventional methods introduce in order to simplify the problem and make it solvable only with limited information:

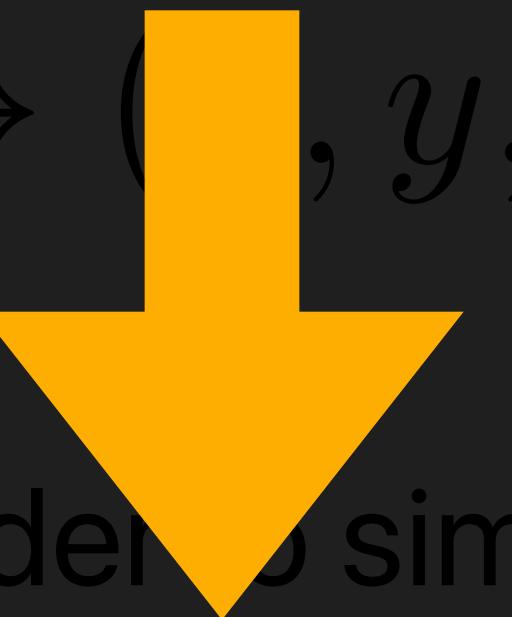
- Symmetry assumptions (e.g., spherical, axisymmetric)
- Parameterized stellar and DM density profiles
- Velocity anisotropy profile
- etc...

DM density profile estimation through normalizing flows

Lim, KH, Nojiri et al. (2024, in prep.)

We introduce model-independent, unbinned
Jeans analysis using neural density estimator.
- Line-of-sight velocity

$$(x, y, z, v_x, v_y, v_z) \longrightarrow (\cdot, y, v_z)$$



Conventional methods introduce in order to simplify the problem and make it solvable only with limited information:

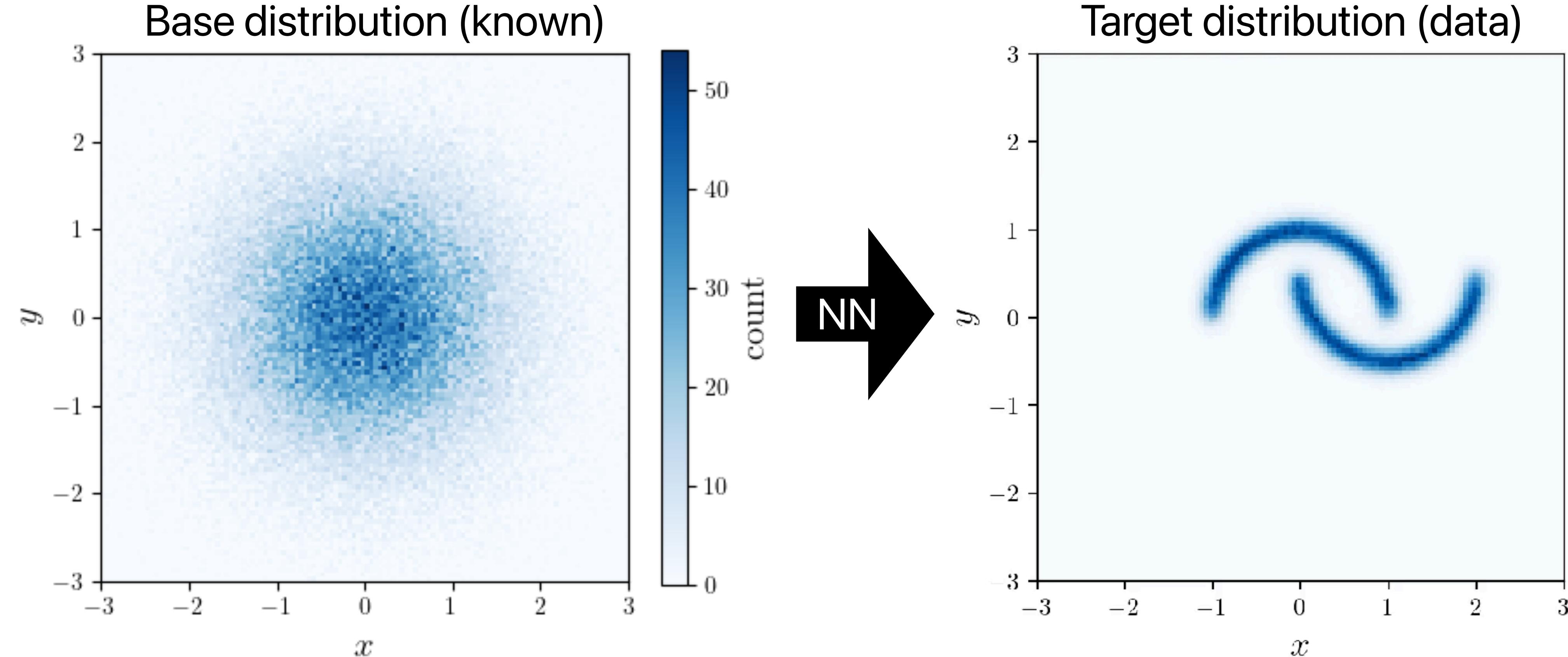
- Symmetry assumptions (e.g., spherical, axisymmetric)
- Parameterized stellar and DM density profiles
- Velocity anisotropy profile $\nu(r), \sigma_r^2(r)$
- etc...

Normalizing flows

Normalizing flows: Neural Density Estimator

Lim, KH, Nojiri et al. (2024, in prep.)

Normalizing Flows (NFs) is an artificial neural network that learns a transformation of random variables.



Normalizing flows: Neural Density Estimator

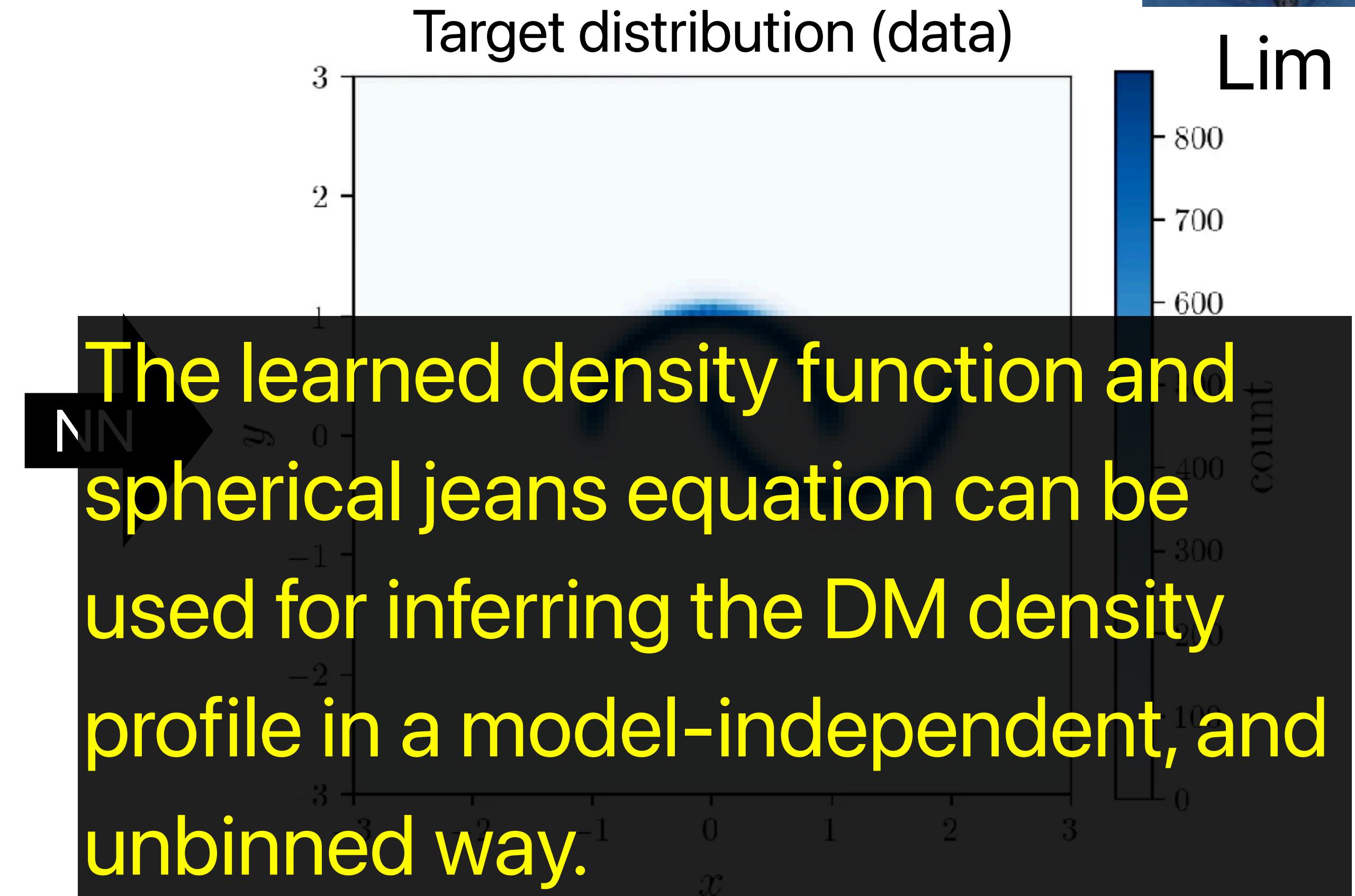
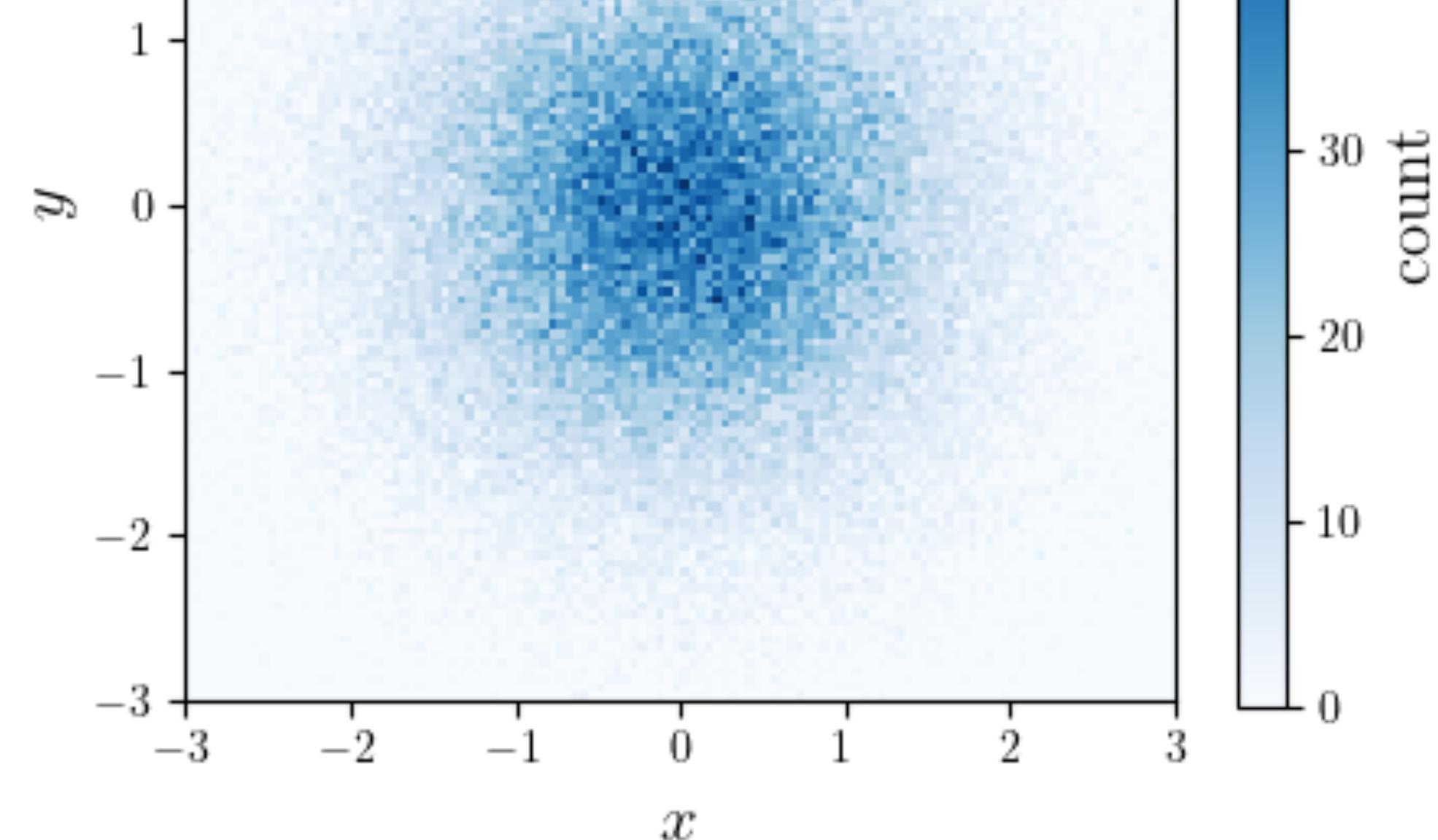
Lim, KH, Nojiri et al. (2024, in prep.)

Normalizing Flows (NFs) is an artificial neural network that

learns a transformation of random variables.

We train normalizing flows

to learn the phase-space
density of stars in dSph.

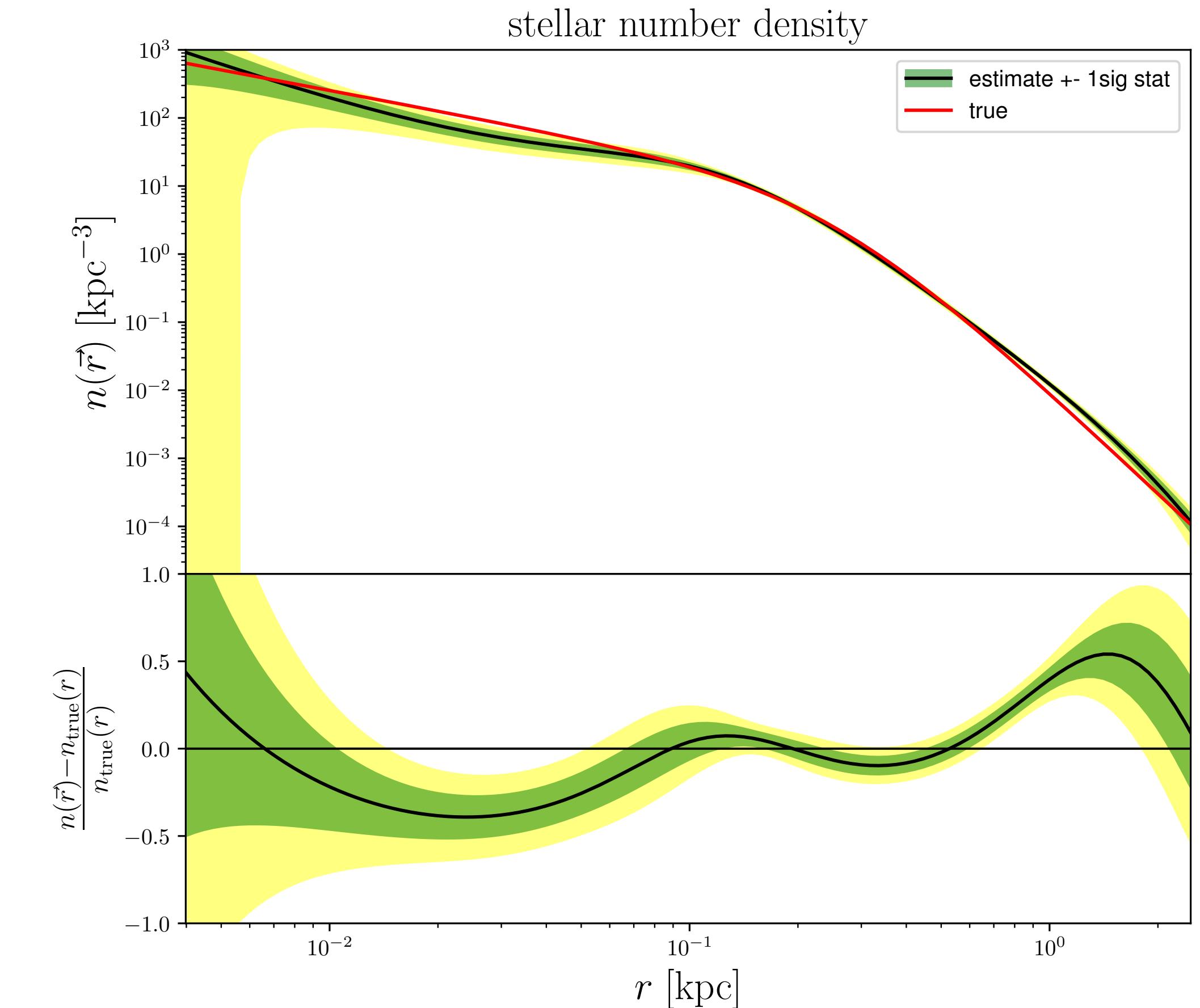
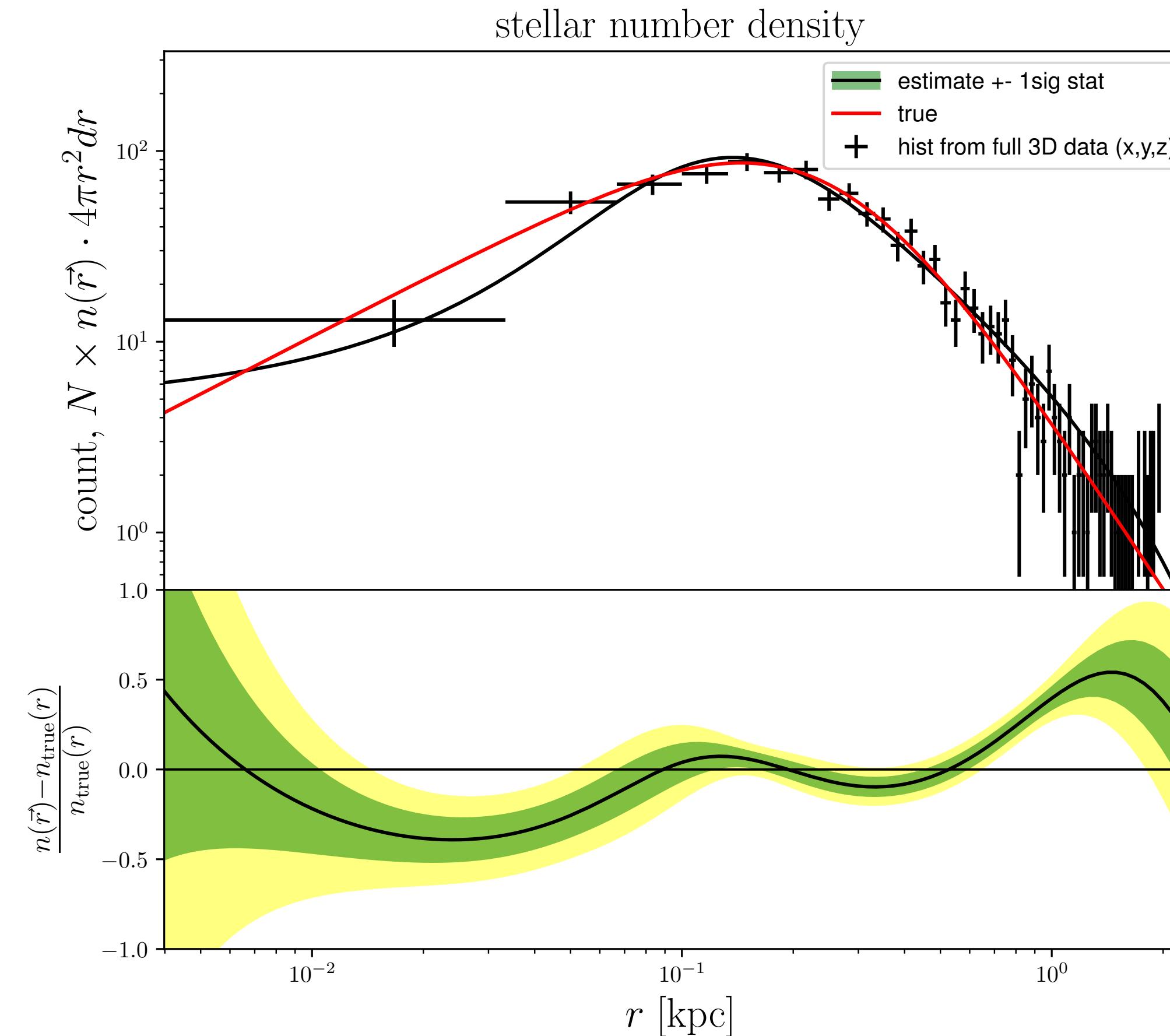


Results: Stellar number density

Lim, KH, Nojiri et al. (2024, in prep.)

Inferred stellar number density trained on 2D position (x,y).

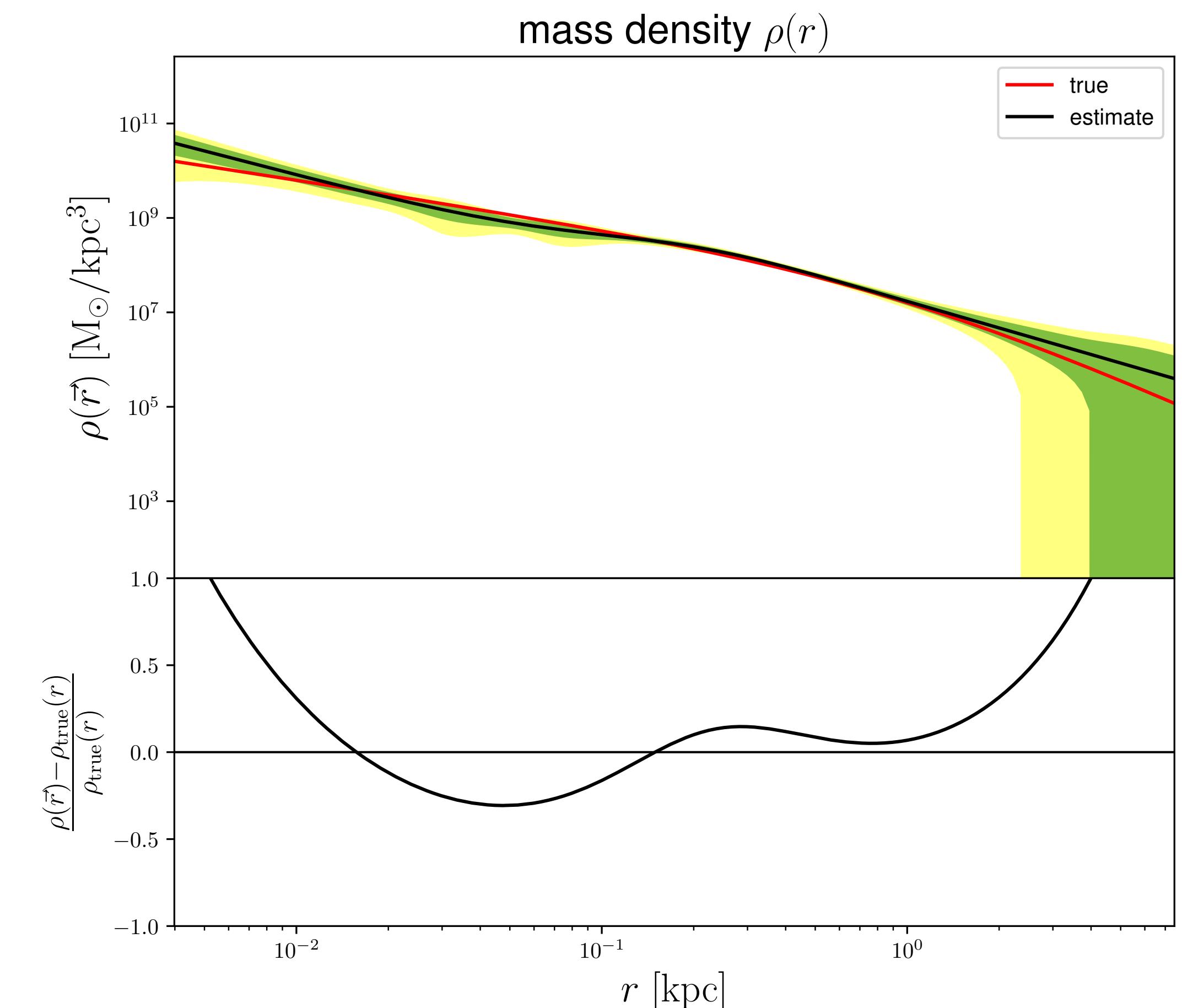
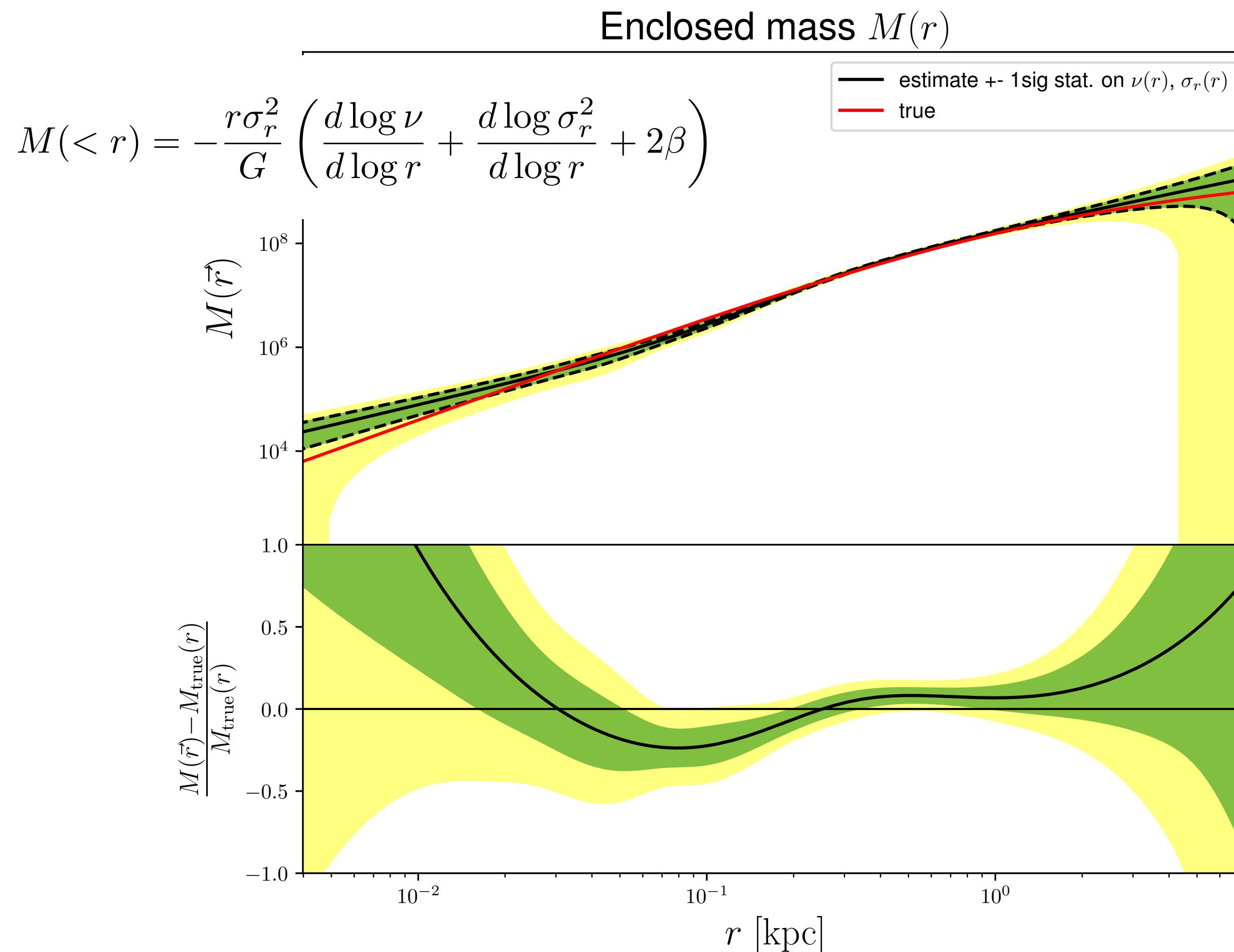
Mock 1000 stars are taken from GaiaChallenge with cusp DM, isotropic: $\beta = 0$.



Results: Dark matter density

Lim, KH, Nojiri et al. (2024, in prep.)

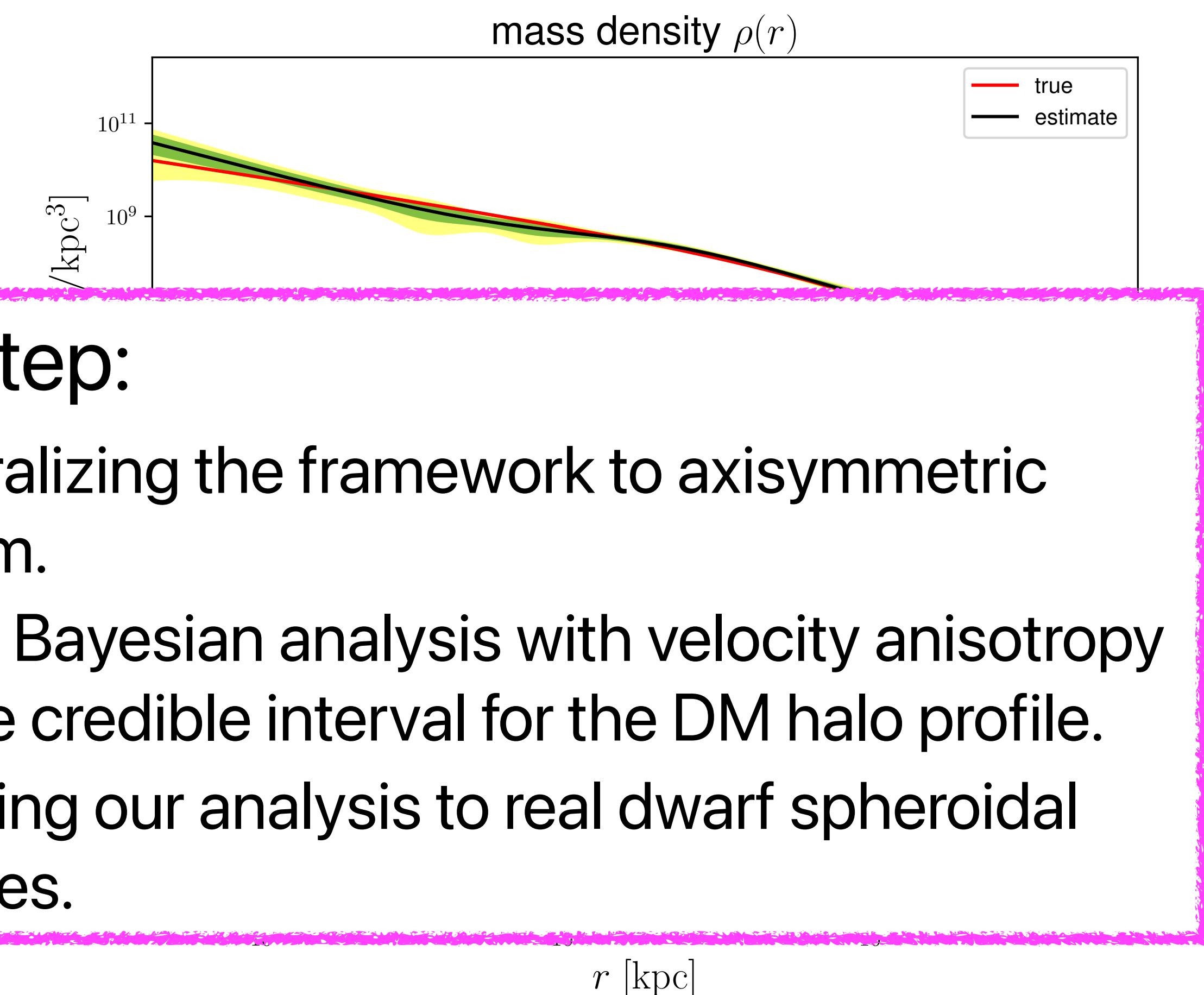
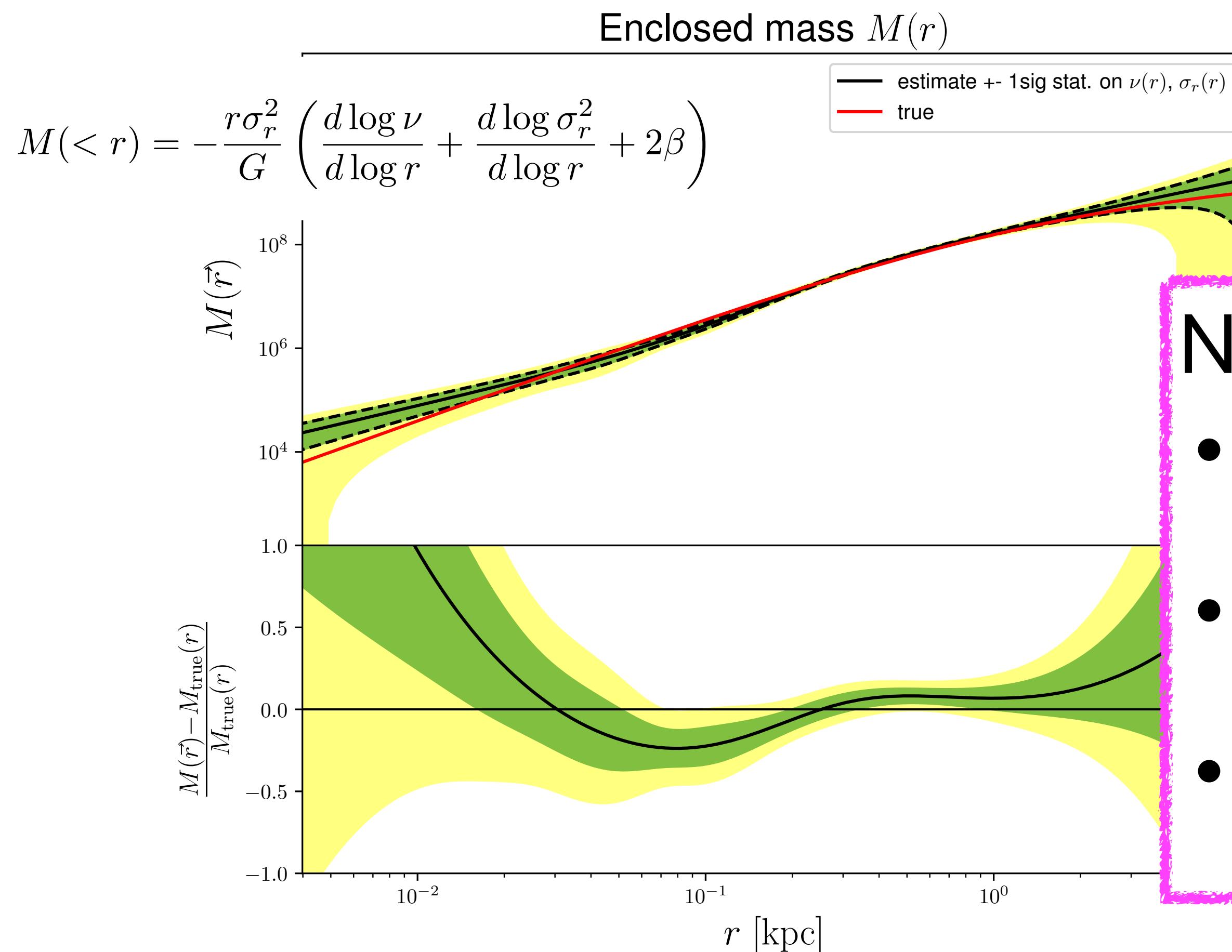
Inferred mass density calculated from stellar density and velocity dispersion trained on 3D infomation (x,y,vz).



Results: Dark matter density

Lim, KH, Nojiri et al. (2024, in prep.)

Inferred mass density calculated from stellar density and velocity dispersion trained on 3D infomation (x,y,vz).



Next step:

- Generalizing the framework to axisymmetric system.
- Doing Bayesian analysis with velocity anisotropy to give credible interval for the DM halo profile.
- Applying our analysis to real dwarf spheroidal galaxies.

Take Home Message

- The Galactic dwarf spheroidal galaxies are ideal target for studying the basic properties of dark matter.
- The current constraints on their DM density profiles still have large uncertainties, even though several dSphs favor cusped DM halo.
- Our teams are now developing new dynamical analysis to place further constraints on dSph's DM density profile.
- **Subaru HSC/PFS** enable us to hunt a huge number of dSph's stars out to their outskirts, and thereby placing tighter constraints on their DM density profiles.