

Thermal Leptogenesis in the Minimal Gauged $U(1)_{L_\mu - L_\tau}$ Model

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@Barkeley Week



SCHOOL OF SCIENCE
THE UNIVERSITY OF TOKYO

Based on JHEP 09 (2023) 079 [hep-ph 2305.18100]

Alessandro Granelli, Koichi Hamaguchi, Natsumi Nagata, Maura E. Ramirez-Quezada, and JW

Leptogenesis

M. Fukugita, T. Yanagida Phys. Lett. B 174 45-47 (1986)

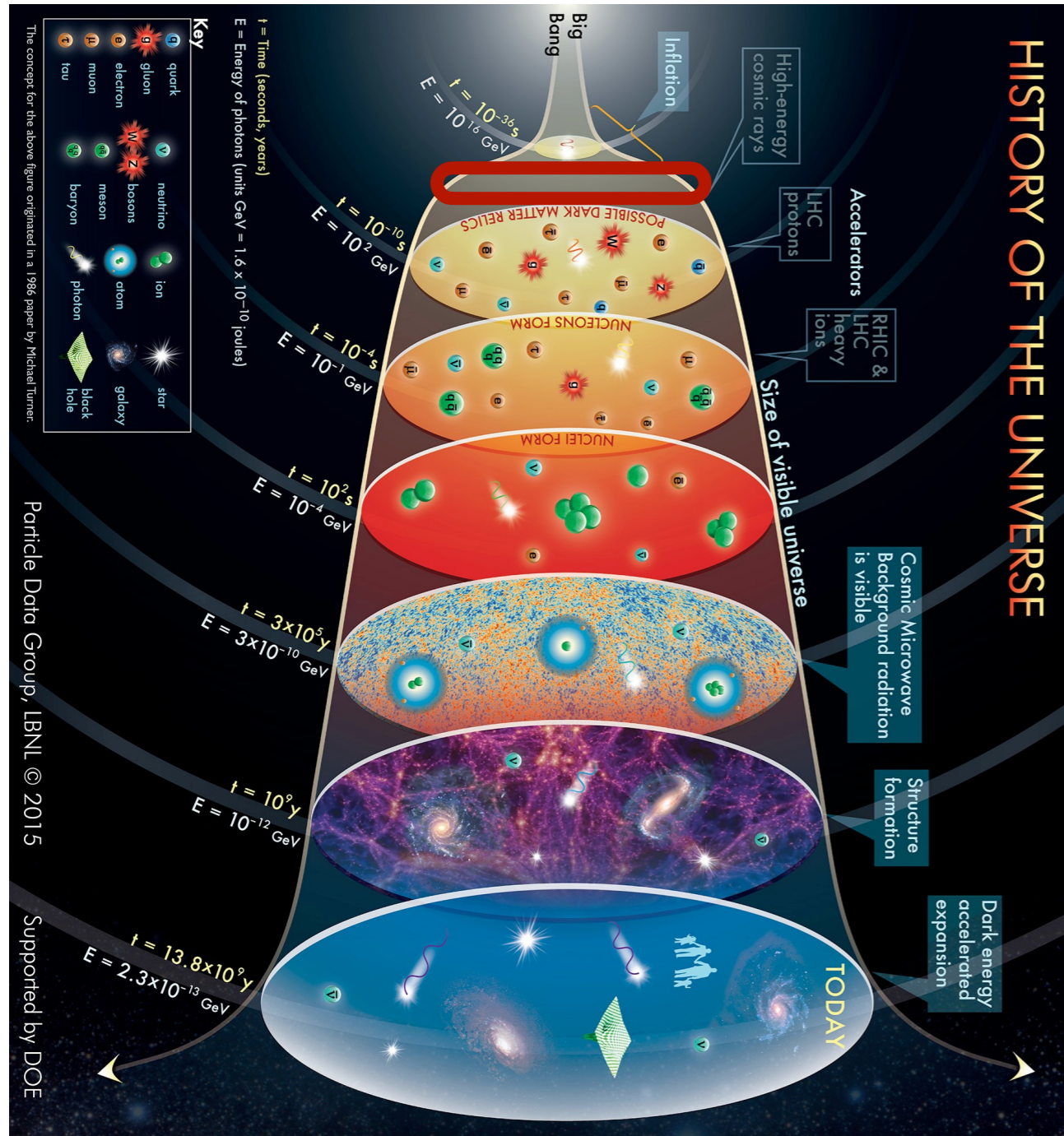
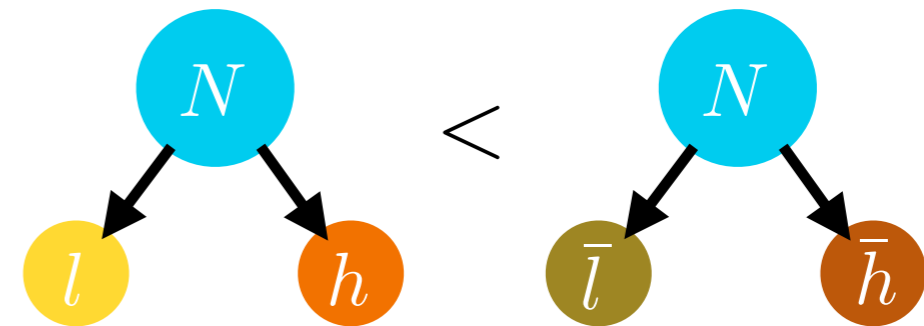


Fig from PDG

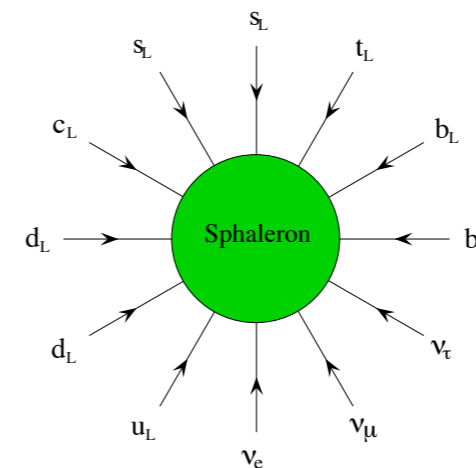
RH ν decay



$> 10^{10}$ GeV

Sphaleron process

V.A. Kuzmin et al., Phys. Rev. B 155 36-42 (1985)

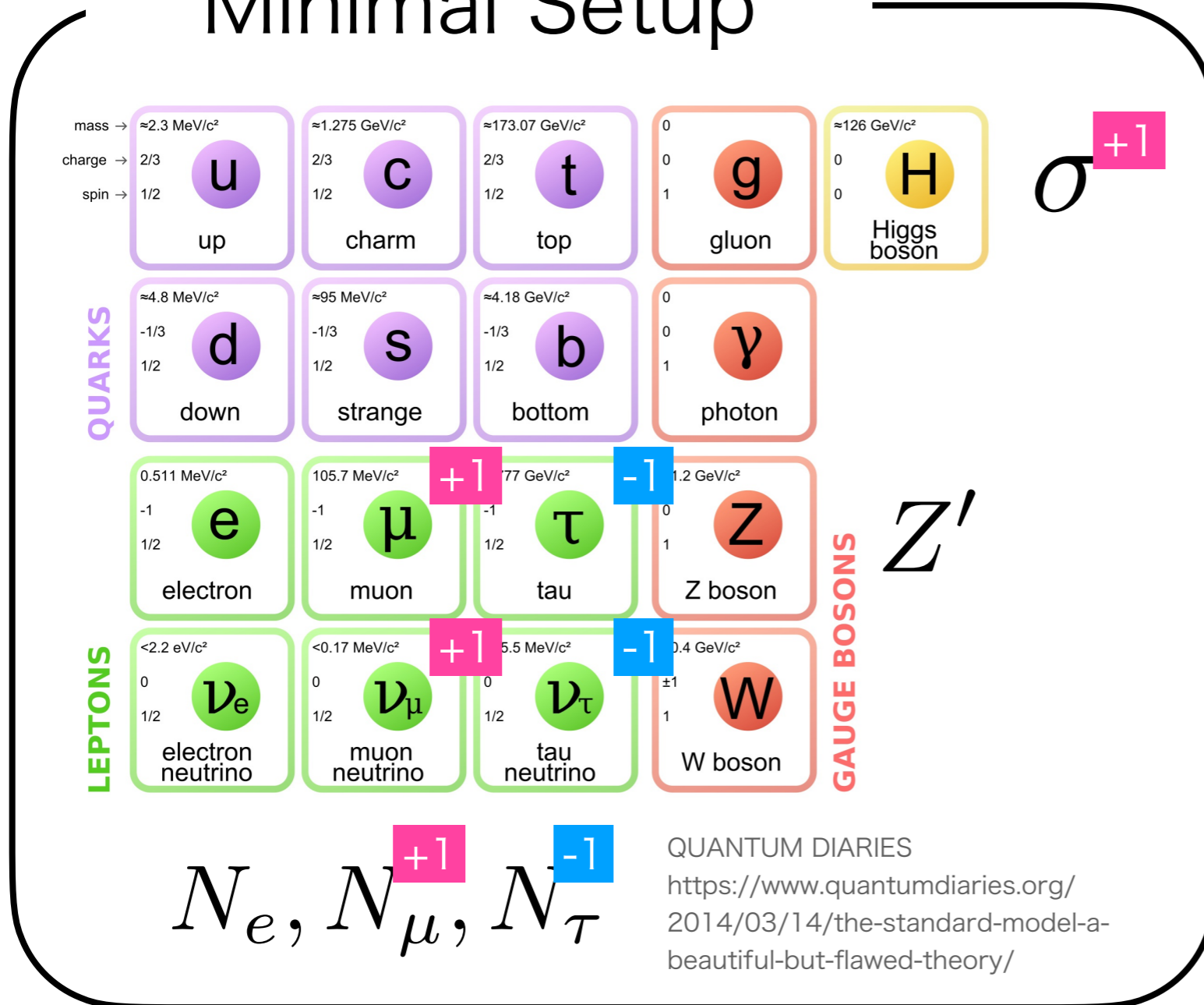


$> 10^3$ GeV

Fig from W. Buchmüller, Nucl. Phys. B Proc.Suppl. 235-236 329-335 (2013)

$U(1)_{L_\mu - L_\tau}$ gauge symmetry

Minimal Setup



K. Asai, et.al., Eur. Phys. J.C 77 (2017) 11, 763

K. Asai, et.al., Phys.Rev.D 99 (2019) 5, 055029

$U(1)_{L_\mu - L_\tau}$ gauge symmetry

Minimal Setup

SM singlet
Breaking symmetry

mass →	≈2.3 MeV/c ²	≈1.275 GeV/c ²	≈173.07 GeV/c ²	0	≈126 GeV/c ²
charge →	2/3	2/3	2/3	0	0
spin →	1/2	1/2	1/2	1	0
	u up	c charm	t top	g gluon	H Higgs boson
QUARKS					
	≈4.8 MeV/c ²	≈95 MeV/c ²	≈4.18 GeV/c ²	0	
	-1/3	-1/3	-1/3	0	
	1/2	1/2	1/2	1	
	d down	s strange	b bottom	γ photon	
	0.511 MeV/c ²	105.7 MeV/c ²	1.777 GeV/c ²	12.1 GeV/c ²	
	-1	-1	-1	0	
	1/2	1/2	1/2	1	
	e electron	μ muon	τ tau	Z Z boson	
LEPTONS					
	<2.2 eV/c ²	<0.17 MeV/c ²	5.5 MeV/c ²	80.4 GeV/c ²	
	0	0	0	±1	
	1/2	1/2	1/2	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	

σ^{+1}

► Predictive power for neutrino oscillation parameter

$$N_e, N_\mu^{+1}, N_\tau^{-1}$$

QUANTUM DIARIES
<https://www.quantumdiaries.org/2014/03/14/the-standard-model-a-beautiful-but-flawed-theory/>

K. Asai, et.al., Eur. Phys. J.C 77 (2017) 11, 763
 K. Asai, et.al., Phys.Rev.D 99 (2019) 5, 055029

$U(1)_{L_\mu - L_\tau}$ gauge symmetry

Minimal Setup

SM singlet
Breaking symmetry

mass →	≈2.3 MeV/c ²	≈1.275 GeV/c ²	≈173.07 GeV/c ²	0	≈126 GeV/c ²	
charge →	2/3	2/3	2/3	0	0	0
spin →	1/2	1/2	1/2	1	0	0
	u up	c charm	t top	g gluon	H Higgs boson	σ^{+1}
QUARKS						
	≈4.8 MeV/c ²	≈95 MeV/c ²	≈4.18 GeV/c ²	0		
	-1/3	-1/3	-1/3	0		
	1/2	1/2	1/2	1		
	d down	s strange	b bottom	γ photon		
	0.511 MeV/c ²	105.7 MeV/c ²	1.777 GeV/c ²	1.2 GeV/c ²		
	-1	-1	-1	0		
	1/2	1/2	1/2	1		
	e electron	μ muon	τ tau	Z Z boson		
LEPTONS						
	<2.2 eV/c ²	<0.17 MeV/c ²	5.5 MeV/c ²	80.4 GeV/c ²		
	0	0	0	±1		
	1/2	1/2	1/2	1		
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson		

► Predictive power for neutrino oscillation parameter

► We can evaluate BAU with three parameters in thermal LG

A. Granelli, K. Hamaguchi, N. Nagata, M E. Ramirez-Quezada, and JW, JHEP 09 (2023) 079 [hep-ph 2305.18100]

$$N_e, N_\mu^{+1}, N_\tau^{-1}$$

QUANTUM DIA
<https://www.quantumdiary.com/2014/03/14/the-beautiful-but-flawed>

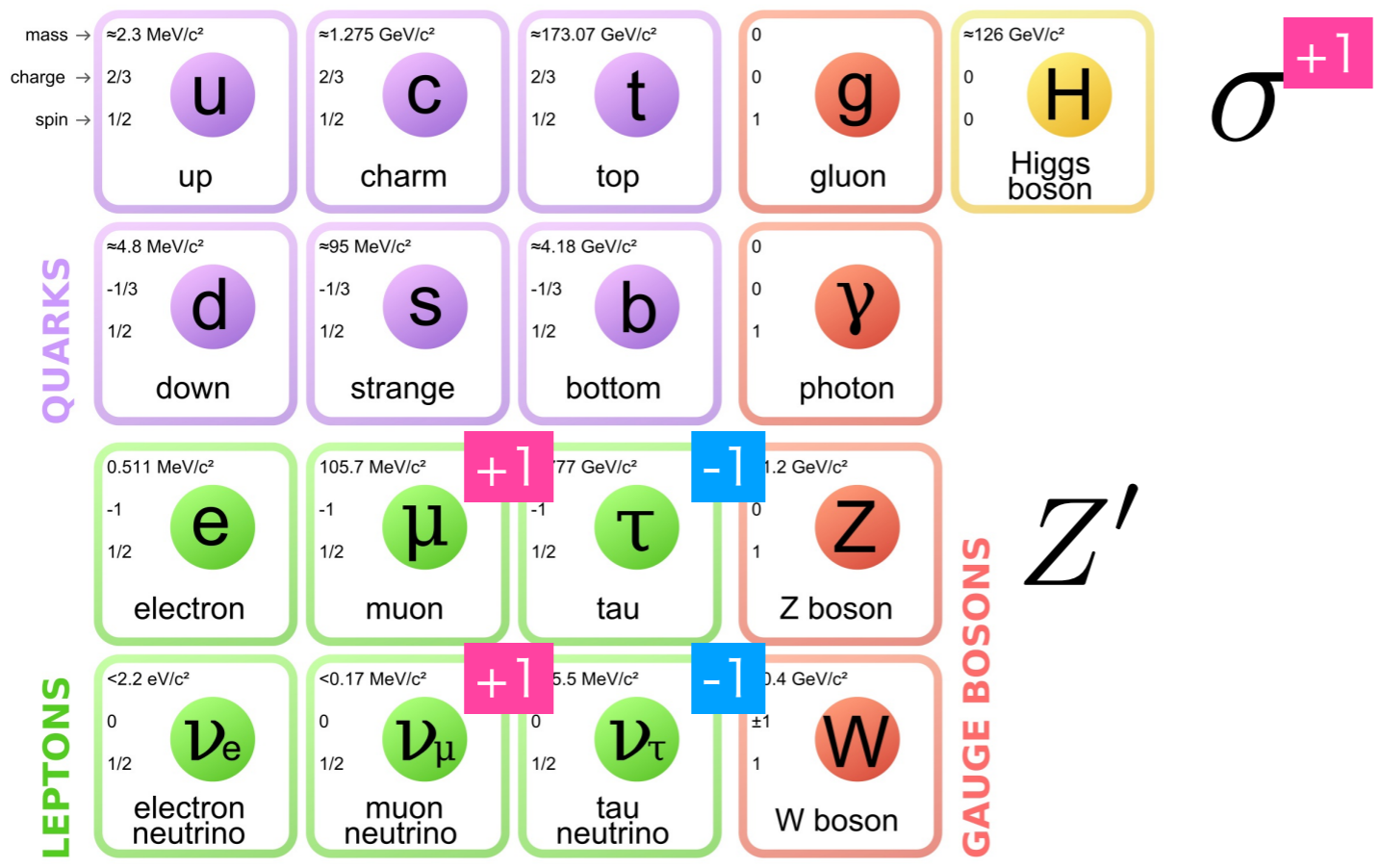
K. Asai, et.al., Eur. Phys. J.C 77 (2017) 11, 763
K. Asai, et.al., Phys.Rev.D 99 (2019) 5, 055029

Outline

- ✓ Introduction
- ▶ Minimal Gauged $U(1)_{L_\mu - L_\tau}$ Model
- ▶ Thermal LG in $U(1)_{L_\mu - L_\tau}$ model
- ▶ Result
- ▶ Summary

$U(1)_{L_\mu - L_\tau}$ gauge symmetry

Minimal Setup



$\langle \sigma \rangle \gg 10^{10} \text{ GeV}$
 Interacting with Sterile neutrino

N_e, N_μ, N_τ

QUANTUM DIARIES
<https://www.quantumdiaries.org/2014/03/14/the-standard-model-a-beautiful-but-flawed-theory/>

K. Asai, et.al., Eur. Phys. J.C 77 (2017) 11, 763
 K. Asai, et.al., Phys.Rev.D 99 (2019) 5, 055029

$U(1)_{L_\mu - L_\tau}$ gauge symmetry

$$\Delta\mathcal{L} = -\lambda_e N_e^c (L_e \cdot H) - \lambda_\mu N_\mu^c (L_\mu \cdot H) - \lambda_\tau N_\tau^c (L_\tau \cdot H) \\ - \frac{1}{2} M_{ee} N_e^c N_e^c - M_{\mu\tau} N_\mu^c N_\tau^c - \lambda_{e\mu} \sigma N_e^c N_\mu^c - \lambda_{e\tau} \sigma^* N_e^c N_\tau^c + h.c$$

After H and σ getting VEVs...

$$\mathcal{L}_{mass} = -(\nu_e, \nu_\mu, \nu_\tau) \mathcal{M}_D \begin{pmatrix} N_e^c \\ N_\mu^c \\ N_\tau^c \end{pmatrix} - \frac{1}{2} (N_e^c, N_\mu^c, N_\tau^c) \mathcal{M}_R \begin{pmatrix} N_e^c \\ N_\mu^c \\ N_\tau^c \end{pmatrix} + h.c.$$

Where

$$\mathcal{M}_D = \frac{v}{\sqrt{2}} \begin{pmatrix} \lambda_e & 0 & 0 \\ 0 & \lambda_\mu & 0 \\ 0 & 0 & \lambda_\tau \end{pmatrix} \quad \mathcal{M}_R = \begin{pmatrix} M_{ee} & \lambda_{e\mu} \langle \sigma \rangle & \lambda_{e\tau} \langle \sigma \rangle \\ \lambda_{e\mu} \langle \sigma \rangle & 0 & M_{\mu\tau} \\ \lambda_{e\tau} \langle \sigma \rangle & M_{\mu\tau} & 0 \end{pmatrix}$$

$U(1)_{L_\mu - L_\tau}$ gauge symmetry

Because of this symmetry, structure of both Dirac and Majorana mass terms are tightly restricted.

→ Strong predictive power for the neutrino sector

$$\mathcal{M}_{\nu L} \simeq -\mathcal{M}_D \mathcal{M}_R^{-1} \mathcal{M}_D^T$$

$$U_{PMNS}^T \mathcal{M}_{\nu L} U_{PMNS} = \text{diag}(m_1, m_2, m_3)$$

Input

$$\Delta m^2, \delta m^2,$$

$$\theta_{12}, \theta_{23}, \theta_{31}$$

Output

$$\delta, \alpha_1, \alpha_2,$$

$$m_1, m_2, m_3$$

Where

$$\mathcal{M}_D = \frac{v}{\sqrt{2}} \begin{pmatrix} \lambda_e & 0 & 0 \\ 0 & \lambda_\mu & 0 \\ 0 & 0 & \lambda_\tau \end{pmatrix} \quad \mathcal{M}_R = \begin{pmatrix} M_{ee} & \lambda_{e\mu} \langle \sigma \rangle & \lambda_{e\tau} \langle \sigma \rangle \\ \lambda_{e\mu} \langle \sigma \rangle & 0 & M_{\mu\tau} \\ \lambda_{e\tau} \langle \sigma \rangle & M_{\mu\tau} & 0 \end{pmatrix}$$

$U(1)_{T_{12} - T_{13}}$ gauge symmetry

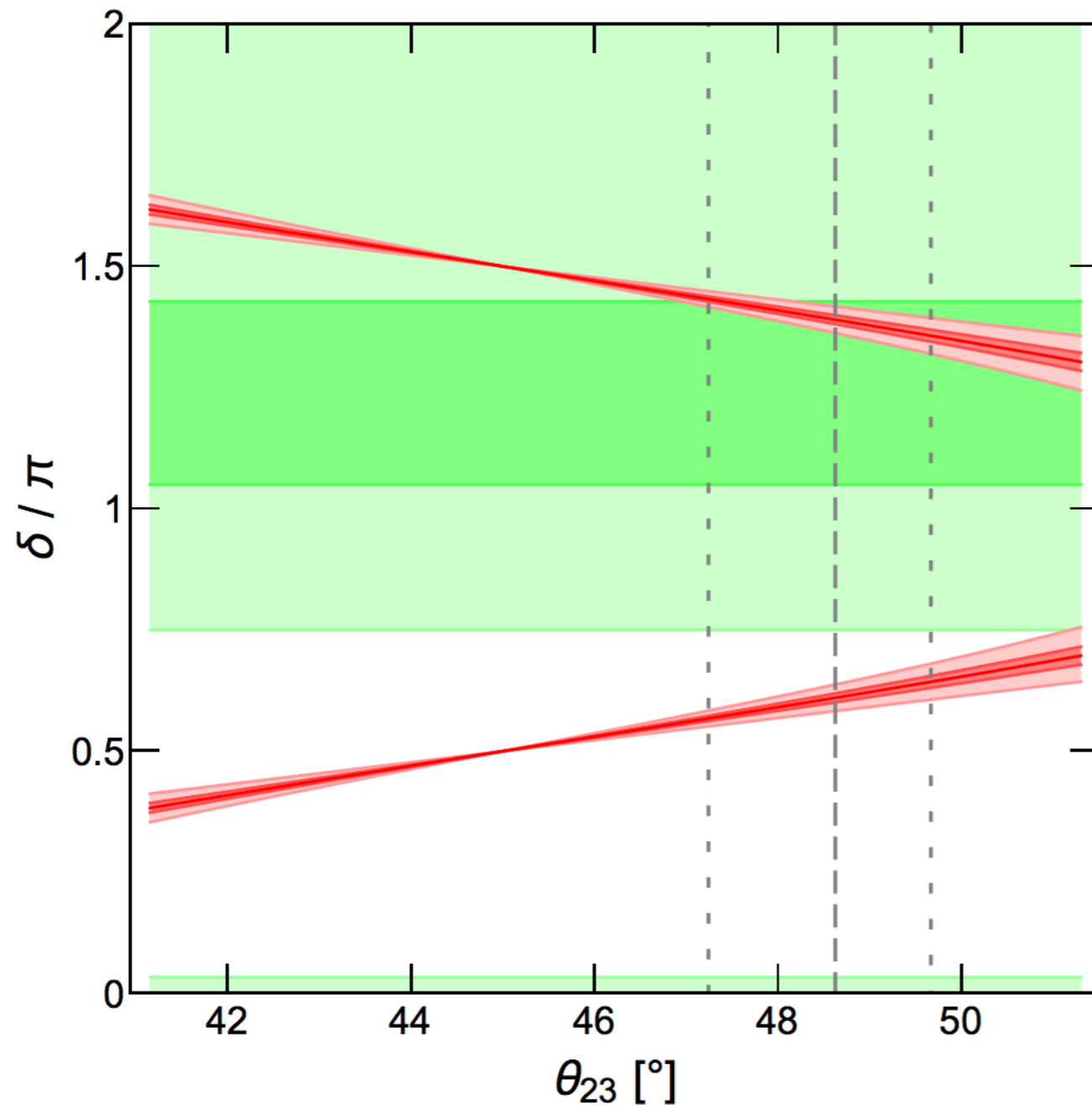


Fig taken from K. Asai et.al., JCAP 11 (2020) 013

K. Asai, et.al., Eur. Phys. J.C 77 (2017) 11, 763

K. Asai, et.al., Phys.Rev.D 99 (2019) 5, 055029

structure of both Dirac and
slightly restricted.

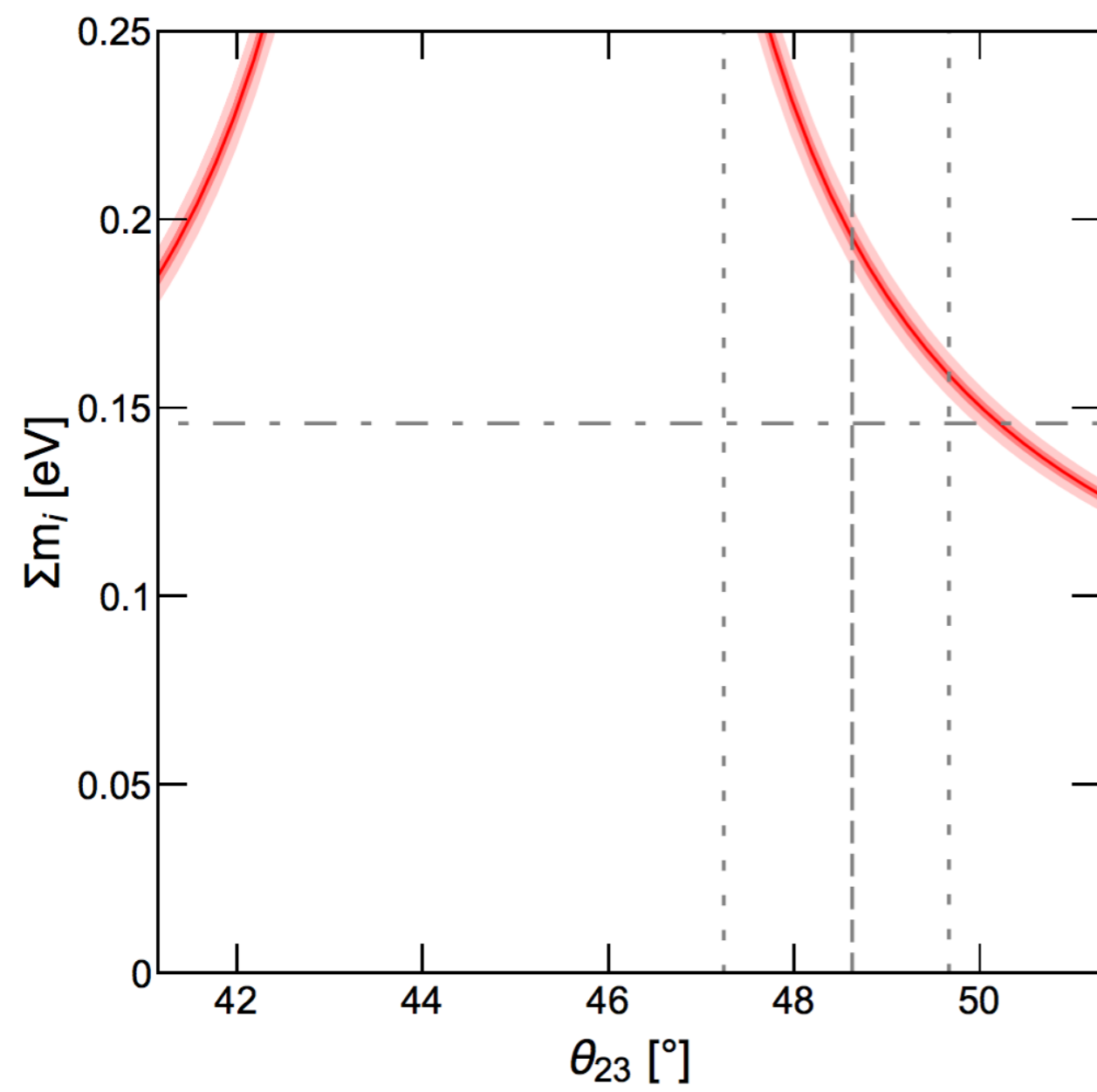
for the neutrino sector

Input $\Delta m^2, \delta m^2,$
 $\theta_{12}, \theta_{23}, \theta_{31}$ \rightarrow Output $\delta, \alpha_1, \alpha_2,$
 m_1, m_2, m_3

$$\cos \delta \simeq \frac{\cot \theta_{12} \cot \theta_{23}}{\sin \theta_{13}}$$

Two solutions $\delta, 2\pi - \delta$

$U(1)_{L_\mu - L_\tau}$ gauge symmetry



structure of both Dirac and Majorana phases is tightly restricted.

• for the neutrino sector

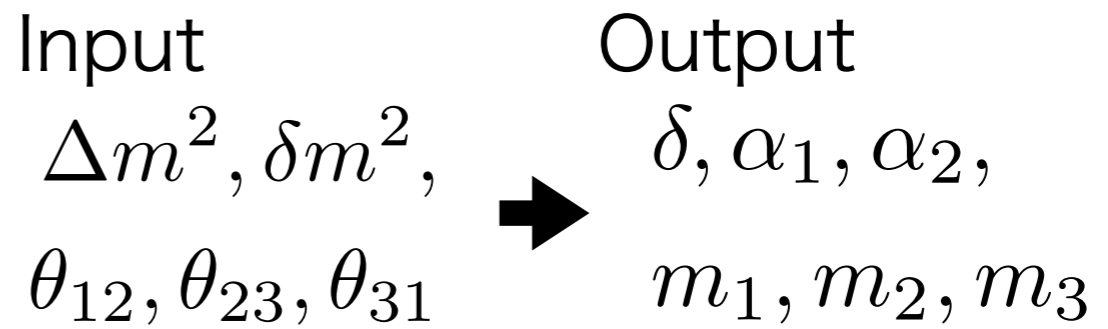


Fig taken from K. Asai et.al., JCAP 11 (2020) 013

K. Asai, et.al., Eur. Phys. J.C 77 (2017) 11, 763

K. Asai, et.al., Phys.Rev.D 99 (2019) 5, 055029

$U(1)_{L_{\mu} - L_{\tau}}$ gauge symmetry

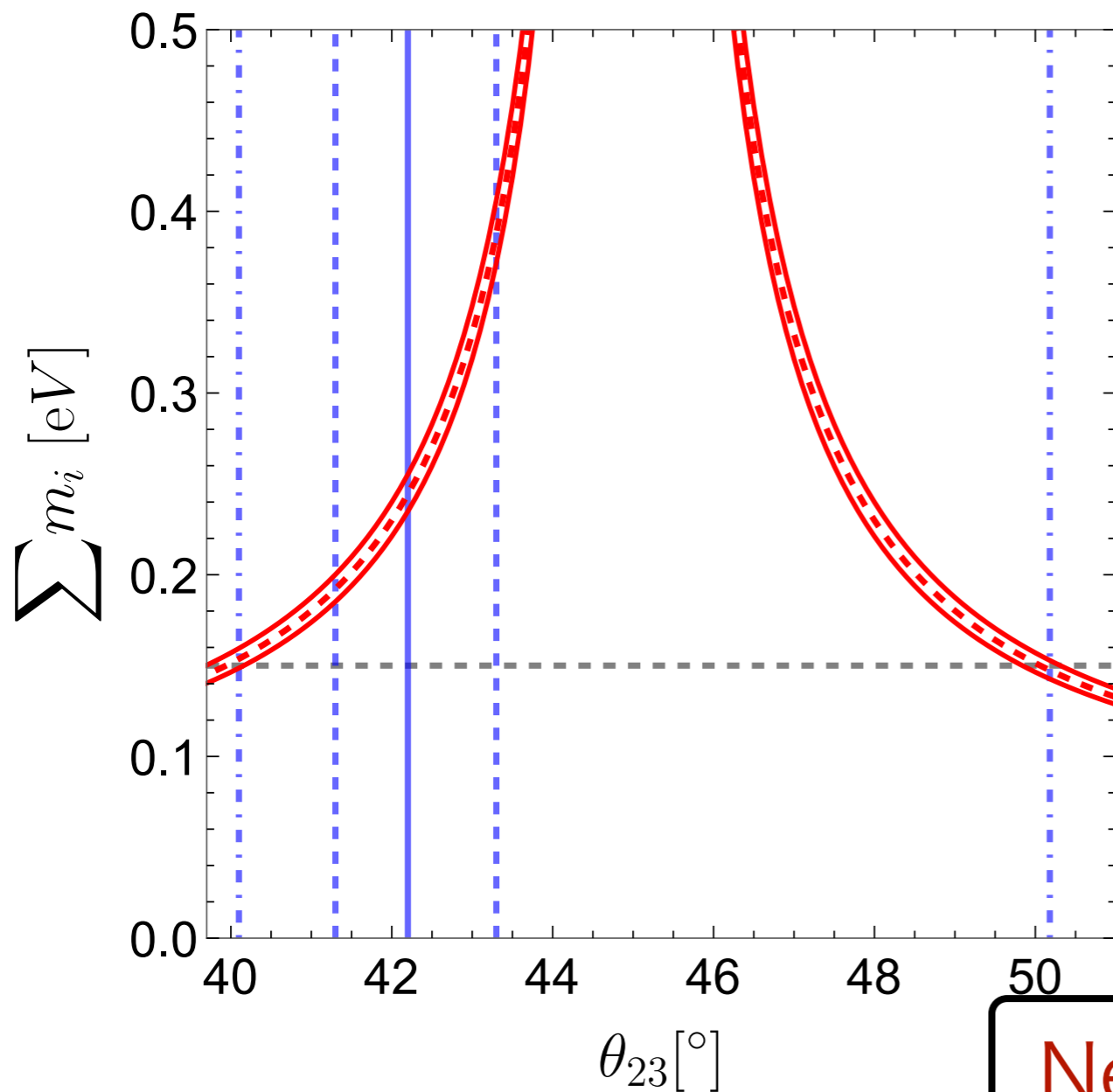


Fig taken from K. Asai et.al., [hep-ph 2401.17613]

K. Asai, et.al., Eur. Phys. J.C 77 (2017) 11, 763

K. Asai, et.al., Phys.Rev.D 99 (2019) 5, 055029

structure of both Dirac and γ restricted.

the neutrino sector

Input
 μ
 $n^2, \delta m^2,$
 θ_{23}, θ_{31} \rightarrow Output
 $\delta, \alpha_1, \alpha_2,$
 m_1, m_2, m_3

Newest analysis released
 in this January

Outline

- ✓ Introduction
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Thermal LG in $U(1)_{L_\mu - L_\tau}$ model ¹⁴

To evaluate baryon asymmetry,

Input	Output	
$\Delta m^2, \delta m^2,$ $\theta_{12}, \theta_{23}, \theta_{31}$	$\delta, \alpha_1, \alpha_2,$ m_1, m_2, m_3	$\Rightarrow \mathcal{M}_{\nu L} = U_{PMNS}^* \text{diag}(m_1, m_2, m_3) U_{PMNS}^{-1}$

$$\mathcal{M}_D = \frac{v}{\sqrt{2}} \begin{pmatrix} \lambda_e & 0 & 0 \\ 0 & \lambda_\mu & 0 \\ 0 & 0 & \lambda_\tau \end{pmatrix} \Rightarrow \mathcal{M}_R \simeq -\mathcal{M}_D^T \mathcal{M}_{\nu L}^{-1} \mathcal{M}_D$$

$$\mathcal{M}_D, \mathcal{M}_R \Rightarrow \eta_b \quad \text{baryon asymmetry}$$

Thermal LG in $U(1)_{L_\mu - L_\tau}$ model

To evaluate baryon as

Input $\Delta m^2, \delta m^2, \theta_{12}, \theta_{23}, \theta_{31}$ \rightarrow Output $\delta, \alpha_1, \alpha_2, m_1, m_2, m_3$

Cf) Neutrino parameters in CI parameterization
 J. A. Casas and A. Ibarra. Nucl.Phys.B 618 (2001) 171-204
 $m_1, \Delta m^2, \delta m^2, \theta_{12}, \theta_{23}, \theta_{31},$
 $\delta, \alpha_1, \alpha_2, M_1, M_2, M_3,$
 $x_1, x_2, x_3, y_1, y_2, y_3$

$$\mathcal{M}_D = \frac{v}{\sqrt{2}} \begin{pmatrix} \lambda_e & 0 & 0 \\ 0 & \lambda_\mu & 0 \\ 0 & 0 & \lambda_\tau \end{pmatrix} \rightarrow \mathcal{M}_R \simeq -\mathcal{M}_D^T \mathcal{M}_{\nu L}^{-1} \mathcal{M}_D$$

$\mathcal{M}_D, \mathcal{M}_R \rightarrow \eta_b$ baryon asymmetry

Thermal LG in $U(1)_{L_\mu - L_\tau}$ model ¹⁶

$$M_i \simeq 6 \times 10^{14} \text{ GeV} \left(\frac{0.05 \text{ eV}}{m_1} \right) \lambda^2 \beta_i(\theta, \phi)$$

$$(\lambda_e, \lambda_\mu, \lambda_\tau) = \lambda(\cos \theta, \sin \theta \cos \phi, \sin \theta \sin \phi)$$

$n_3) U_{PMNS}^{-1}$

$\nu_{12}, \nu_{23}, \nu_{31}$ $\nu_{\sigma 1}, \nu_{\sigma 2}, \nu_{\sigma 3}$

$$\mathcal{M}_D = \frac{v}{\sqrt{2}} \begin{pmatrix} \lambda_e & 0 & 0 \\ 0 & \lambda_\mu & 0 \\ 0 & 0 & \lambda_\tau \end{pmatrix} \quad \rightarrow \quad \mathcal{M}_R \simeq -\mathcal{M}_D^T \mathcal{M}_{\nu_L}^{-1} \mathcal{M}_D$$

$\mathcal{M}_D, \mathcal{M}_R \rightarrow \eta_b$ baryon asymmetry

Thermal LG in $U(1)_{L_\mu - L_\tau}$ model ¹⁷

$$M_i \simeq 6 \times 10^{14} \text{ GeV} \left(\frac{0.05 \text{ eV}}{m_1} \right) \lambda^2 \beta_i(\theta, \phi)$$

Thermal LG works when

$$10^{11-12} \text{ GeV} \lesssim M_1$$

$n_3) U_{PMNS}^{-1}$

$$\mathcal{M}_D = \frac{v}{\sqrt{2}} \begin{pmatrix} \lambda_e & 0 & 0 \\ 0 & \lambda_\mu & 0 \\ 0 & 0 & \lambda_\tau \end{pmatrix} \quad \rightarrow \quad \mathcal{M}_R \simeq -\mathcal{M}_D^T \mathcal{M}_{\nu_L}^{-1} \mathcal{M}_D$$

$\mathcal{M}_D, \mathcal{M}_R \rightarrow \eta_b$ baryon asymmetry

Thermal LG in $U(1)_{L_\mu - L_\tau}$ model ¹⁸

$$M_i \simeq 6 \times 10^{14} \text{ GeV} \left(\frac{0.05 \text{ eV}}{\lambda^2 \beta_i(\theta, \phi)} \right)$$

Thermal LG works when

$$10^{11-12} \text{ GeV} \lesssim M_1$$

y_τ in thermal equilibrium at

$$T \sim 10^{12} \text{ GeV}$$

Flavor effect affects thermal LG

$$\mathcal{M}_D = \frac{v}{\sqrt{2}} \begin{pmatrix} \lambda_e & 0 & 0 \\ 0 & \lambda_\mu & 0 \\ 0 & 0 & \lambda_\tau \end{pmatrix}$$

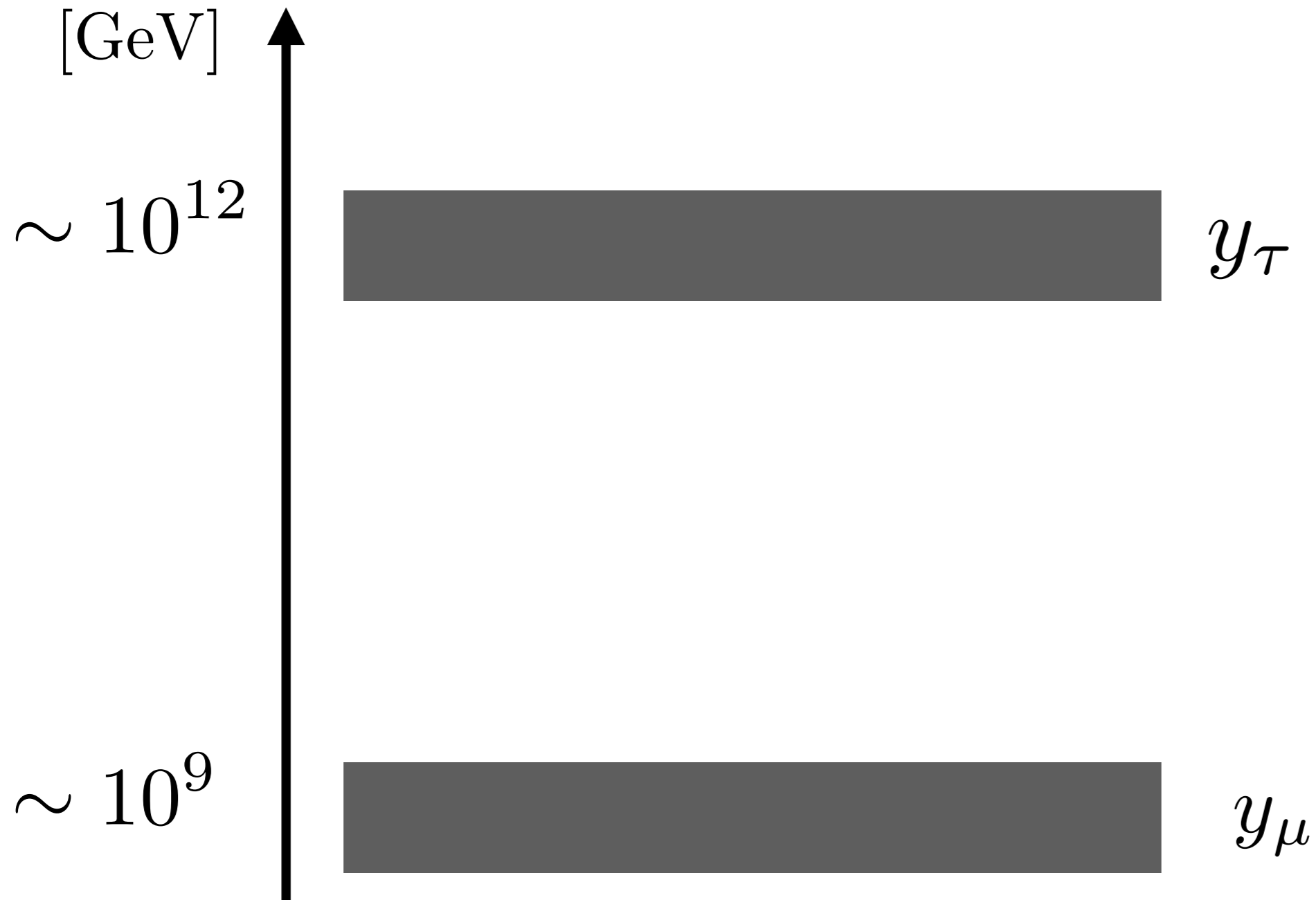
R. Barbieri, et.al., Nucl.Phys.B 575 (2000) 61-77

E. Nardi, et.al., JHEP 01 (2006) 164

A. Abada, et.al., JCAP 04 (2006) 004

$\mathcal{M}_D, \mathcal{M}_R \rightarrow \eta_b$ baryon asymmetry

Flavor effect on LG

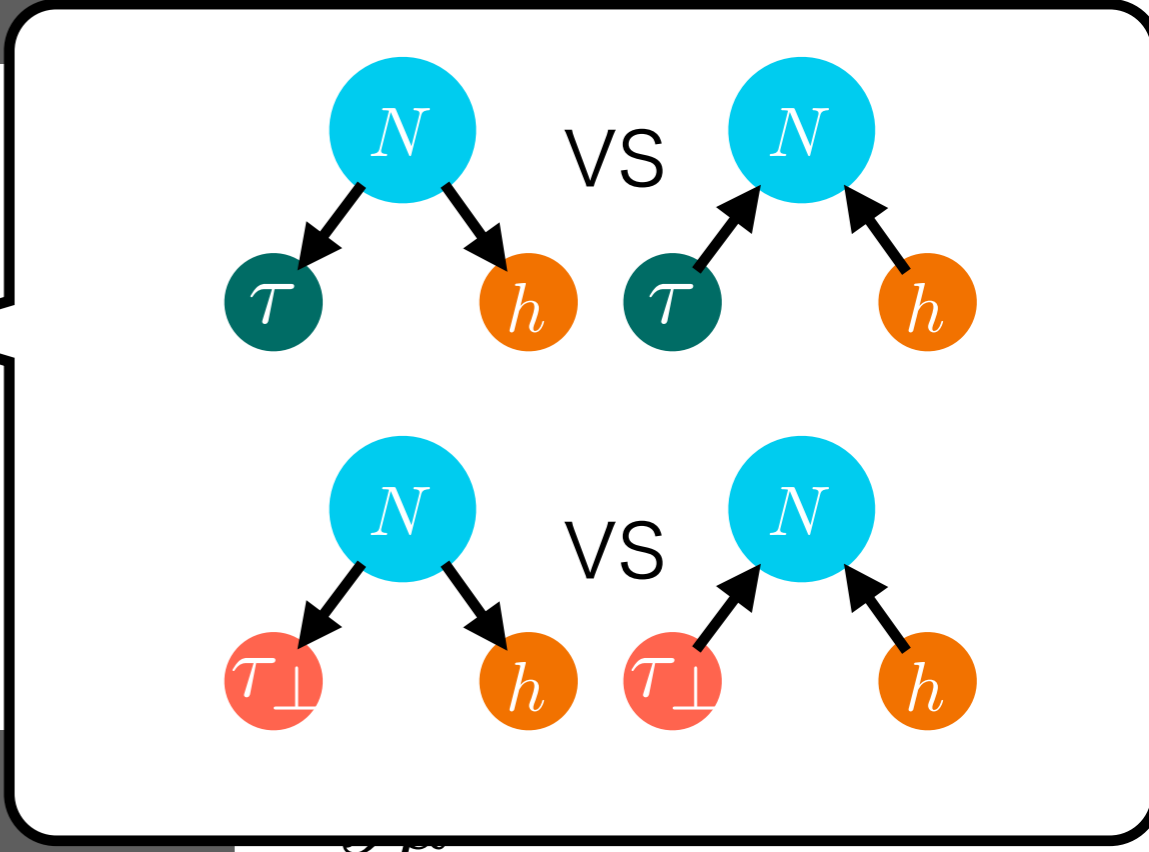
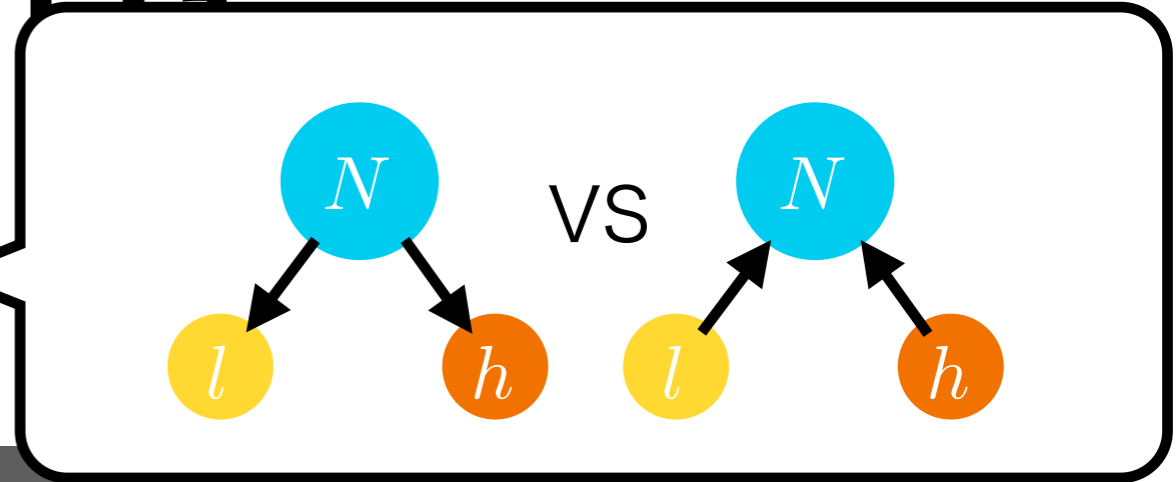
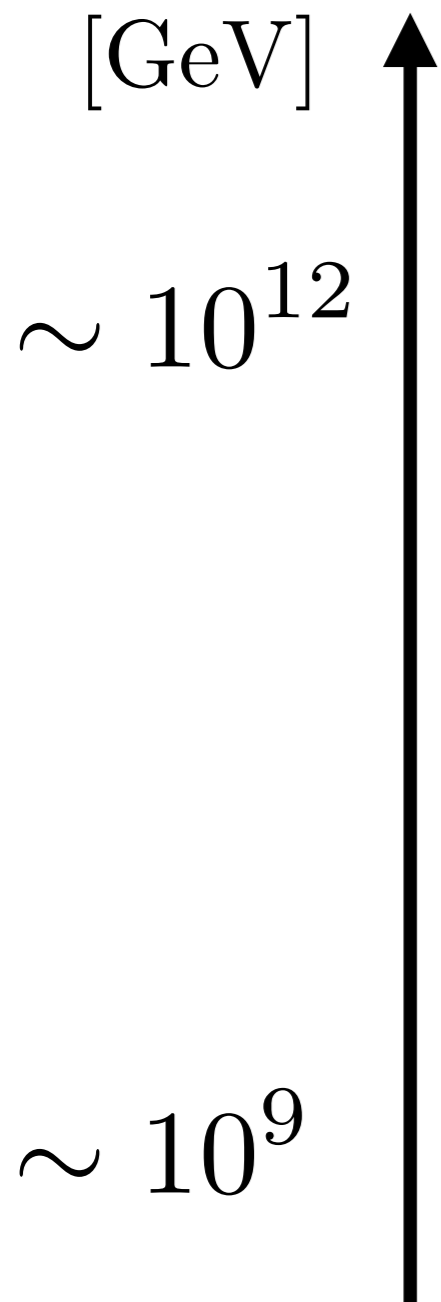


R. Barbieri, et.al., Nucl.Phys.B 575 (2000) 61-77

E. Nardi, et.al., JHEP 01 (2006) 164

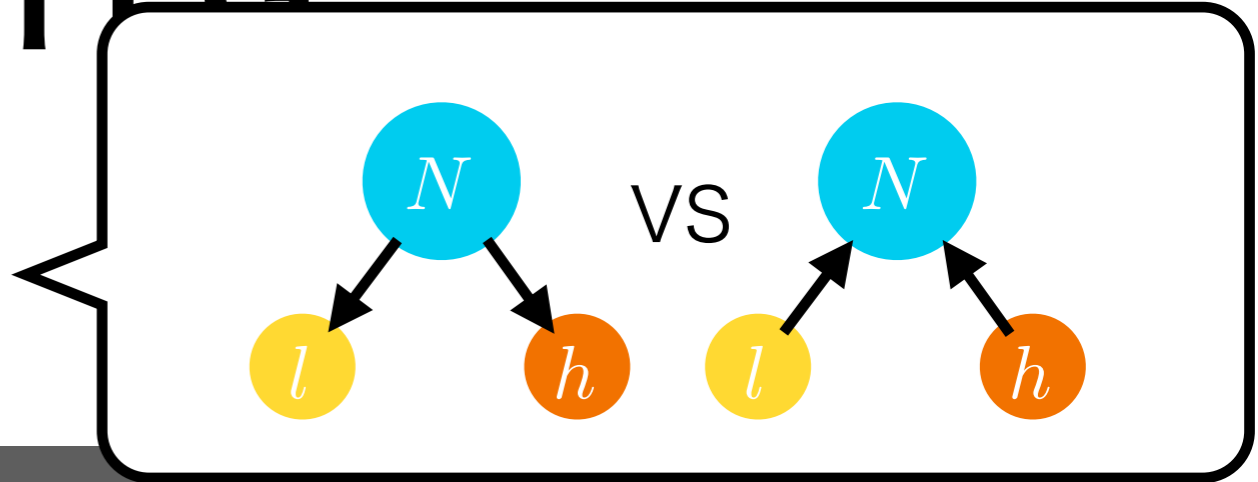
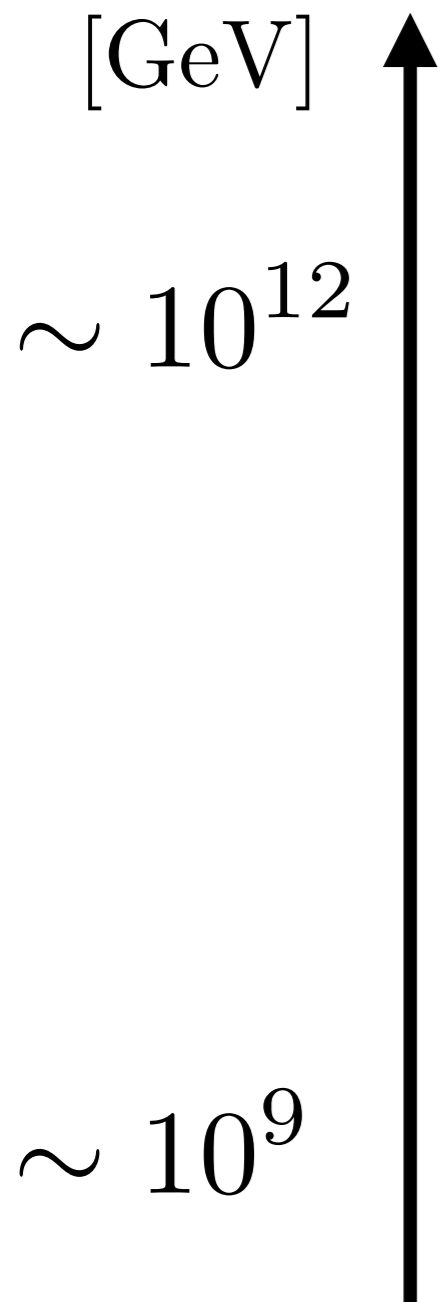
A. Abada, et.al., JCAP 04 (2006) 004

Flavor effect on U_1



R. Barbieri, et.al., Nucl.Phys.B 575 (2000) 61-77
 E. Nardi, et.al., JHEP 01 (2006) 164
 A. Abada, et.al., JCAP 04 (2006) 004

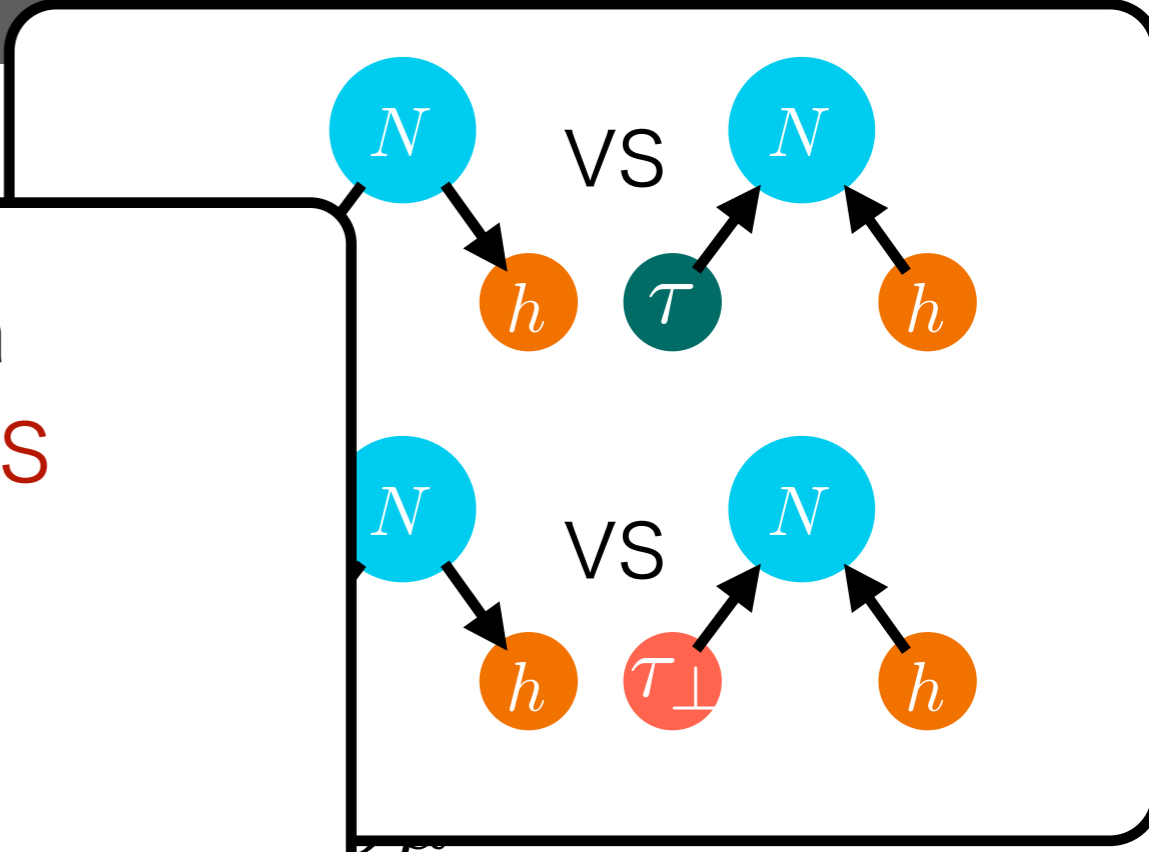
Flavor effect on LG



Numerical calculation
with DME by **ULYSSES**

A. Granelli, et.al., Comput.Phys.Commun.
262 (2021) 107813

A. Granelli, et.al., Comput.Phys.Commun.
291 (2023) 108834



R. Barbieri, et.al., Nucl.Phys.B 575 (2000) 61-77
 E. Nardi, et.al., JHEP 01 (2006) 164
 A. Abada, et.al., JCAP 04 (2006) 004

Thermal LG in $U(1)_{L_\mu - L_\tau}$ model ²²

$$M_i \simeq 6 \times 10^{14} \text{ GeV} \left(\frac{0.05 \text{ eV}}{m_1} \right) \lambda^2 \beta_i(\theta, \phi)$$

Thermal LG works when

$$10^{11-12} \text{ GeV} \lesssim M_1$$

Numerical calculation
with DME by **ULYSSES**

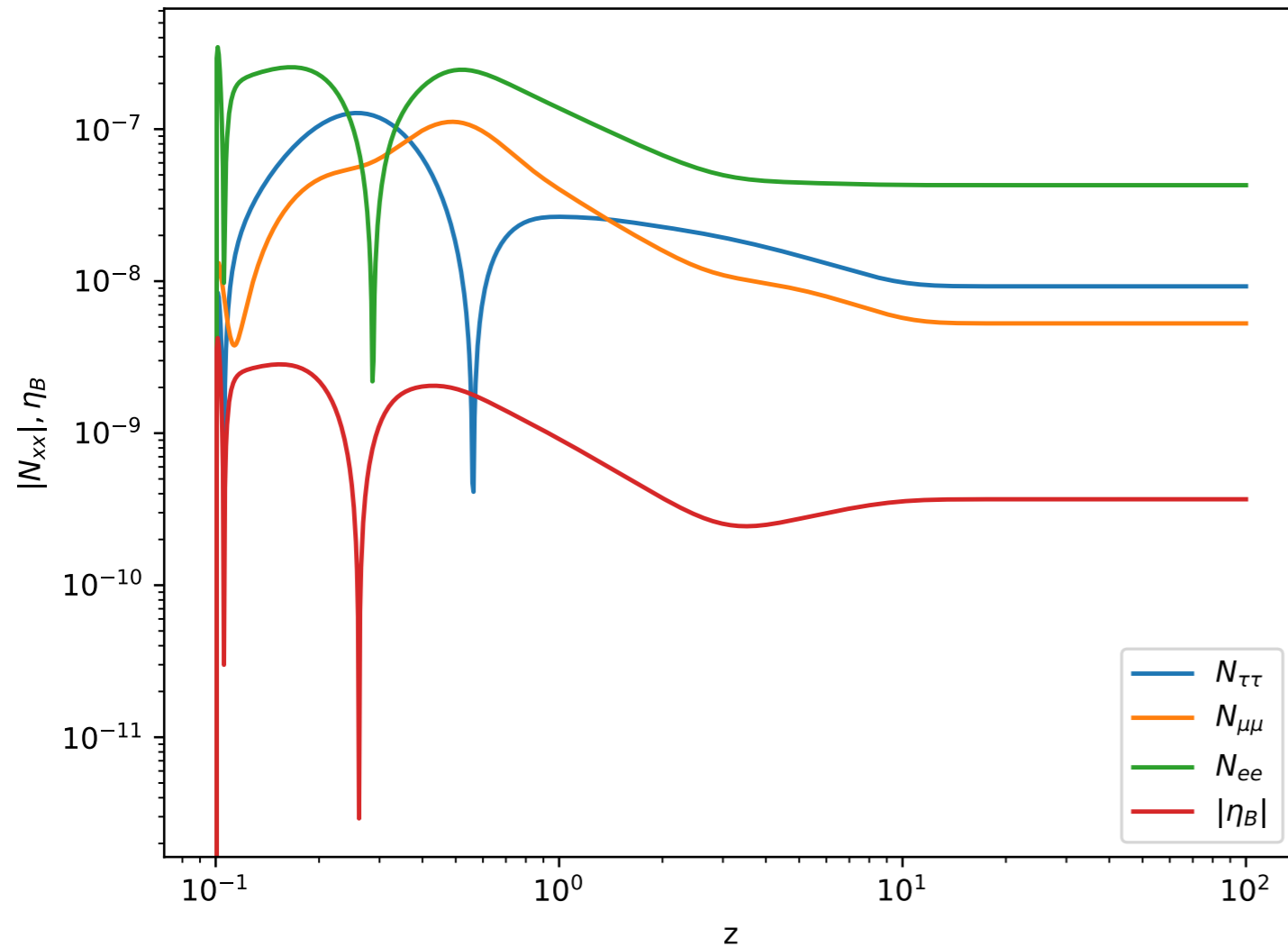
A. Granelli, et.al., Comput.Phys.Commun.
262 (2021) 107813

A. Granelli, et.al., Comput.Phys.Commun.
291 (2023) 108834

$$\mathcal{M}_D = \frac{v}{\sqrt{2}} \begin{pmatrix} \lambda_e & 0 & 0 \\ 0 & \lambda_\mu & 0 \\ 0 & 0 & \lambda_\tau \end{pmatrix}$$

$\mathcal{M}_D, \mathcal{M}_R \rightarrow \eta_b$ baryon asymmetry

Thermal LG in $U(1)_{L_\mu - L_\tau}$ model ²³



$$\lambda^2 \beta_i(\theta, \phi)$$

ical calculation

ME by **ULYSSES**

al., Comput.Phys.Commun.
07813

al., Comput.Phys.Commun.
08834

-1
PMNS

$\mathcal{M}_D, \mathcal{M}_R \rightarrow \eta_b$ baryon asymmetry

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Benchmark Point

Set I

$$\theta_{12} = 33.41^\circ$$

$$\theta_{13} = 8.58^\circ$$

$$\theta_{23} = 39.7^\circ$$

$$\Delta m_{21}^2 = 7.41 \times 10^{-5} \text{ eV}^2$$

$$\Delta m_{31}^2 = 2.507 \times 10^{-3} \text{ eV}^2$$

Set II

$$\theta_{12} = 33.41^\circ$$

$$\theta_{13} = 8.54^\circ$$

$$\theta_{23} = 51.9^\circ$$

$$\Delta m_{21}^2 = 7.41 \times 10^{-5} \text{ eV}^2$$

$$\Delta m_{31}^2 = 2.511 \times 10^{-3} \text{ eV}^2$$

We have taken 3σ ranges of the neutrino mixing angle θ_{23} to avoid constraint on sum of neutrino mass.

Cf) NuFit data

NuFIT Collaboration, NuFIT v5.2, <http://www.nu-fit.org>.

I. Esteban, et.al., JHEP 09 (2020) 178

Neutrino Masses and Mixing Parameters					
Parameters (units)	θ_{12} ($^\circ$)	θ_{13} ($^\circ$)	θ_{23} ($^\circ$)	Δm_{21}^2 (10^{-5} eV^2)	Δm_{31}^2 (10^{-3} eV^2)
With SK	$33.41^{+0.75}_{-0.72}$	$8.58^{+0.11}_{-0.11}$	$42.2^{+1.1}_{-0.9}$	$7.41^{+0.21}_{-0.20}$	$2.507^{+0.026}_{-0.027}$
3σ range	[31.31, 35.74]	[8.23, 8.91]	[39.7, 51.0]	[6.82, 8.03]	[2.427, 2.590]
Without SK	$33.41^{+0.75}_{-0.72}$	$8.54^{+0.11}_{-0.12}$	$49.1^{+1.0}_{-1.3}$	$7.41^{+0.21}_{-0.20}$	$2.511^{+0.028}_{-0.027}$
3σ range	[31.31, 35.74]	[8.19, 8.89]	[39.6, 51.9]	[6.82, 8.03]	[2.427, 2.590]

Benchmark Point

Fig taken from K. Asai et.al., JCAP 11 (2020) 013

Set I

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$$\theta_{13} = 8.58^\circ$$

$$\theta_{23} = 39.7^\circ$$

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$$\Delta m_{31}^2 = 2.507 \times 10^{-3} \text{ eV}^2$$

Set II

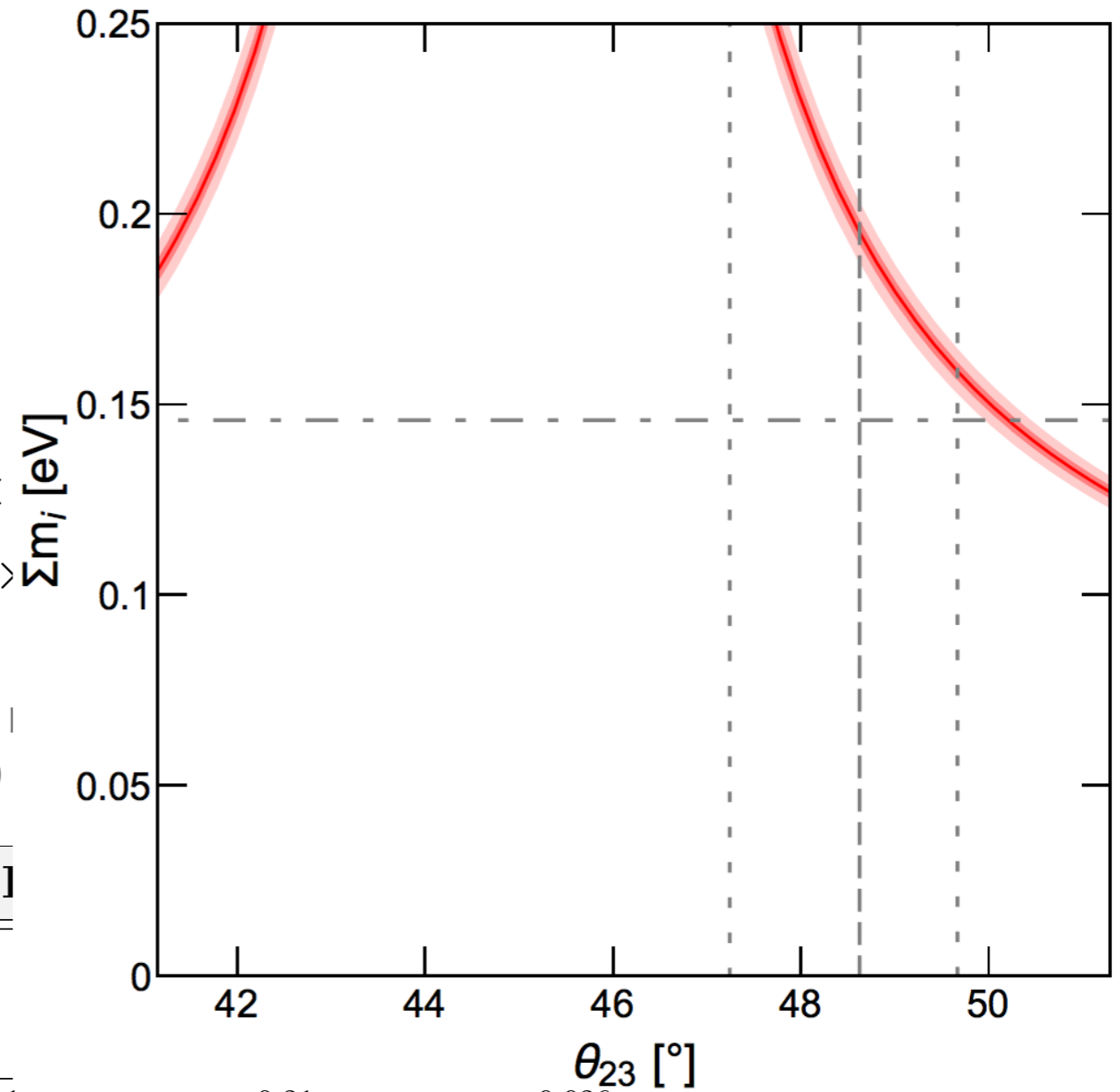
$$\theta_{12} = 33.41^\circ$$

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$$\theta_{23} = 51.9^\circ$$

$$\Delta m_{21}^2 = 7.41 \times 10^{-5} \text{ eV}^2$$

$$\Delta m_{31}^2 = 2.511 \times 10^{-3} \text{ eV}^2$$



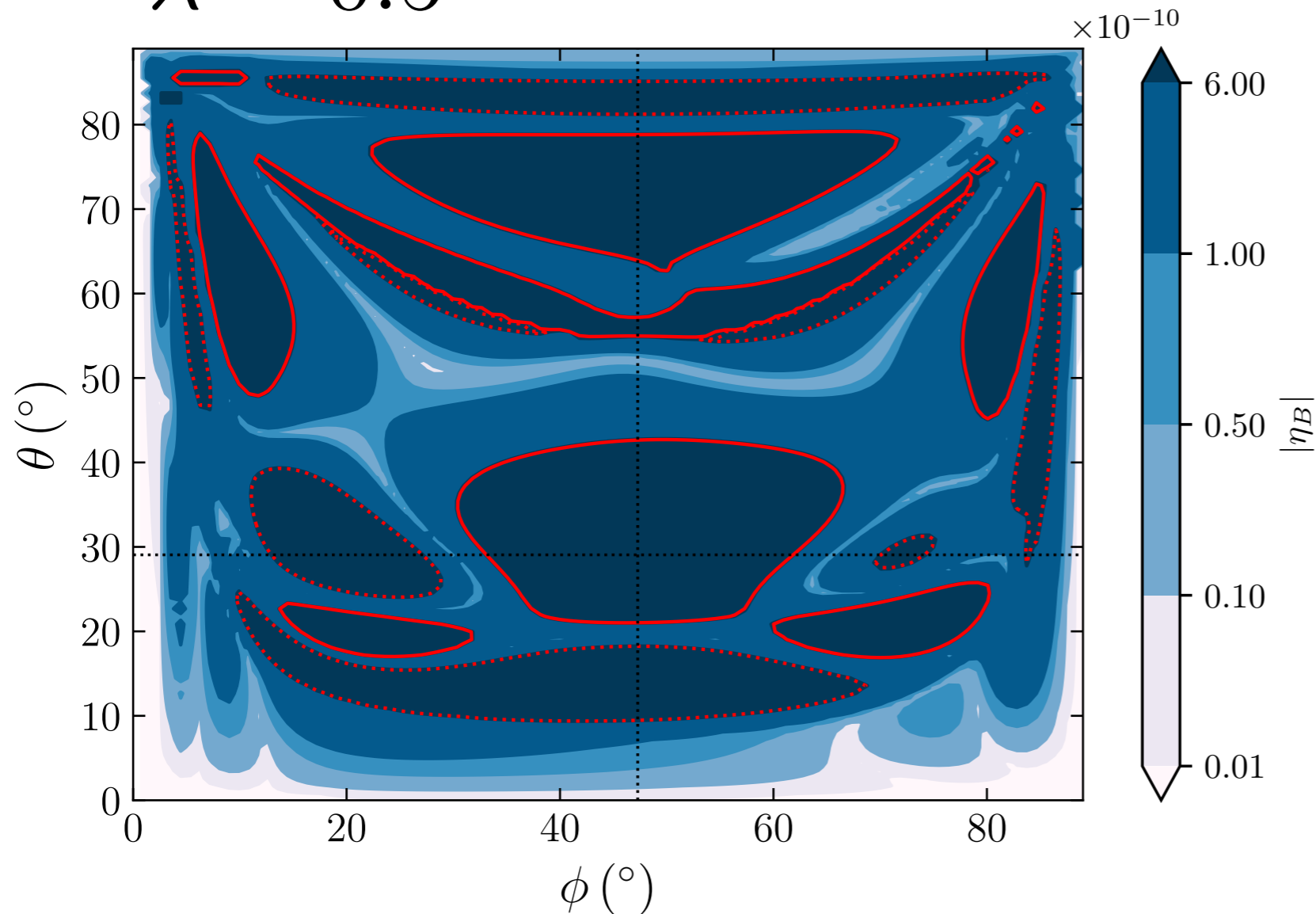
Cf) NuFit data

NuFIT Collaboration, NuFIT v5.2, I
I. Esteban, et.al., JHEP 09 (2020)

Neutrino Masses and Mixing I					
Parameters (units)	θ_{12} ($^\circ$)	θ_{13} ($^\circ$)	θ_{23} ($^\circ$)	Δm_{21}^2 (eV^2)	Δm_{31}^2 (eV^2)
With SK	$33.41^{+0.75}_{-0.72}$	$8.58^{+0.11}_{-0.11}$	$42.2^{+1.1}_{-0.9}$	$7.41^{+0.21}_{-0.20}$	$2.507^{+0.026}_{-0.027}$
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3σ range	[31.31, 35.74]	[8.19, 8.89]	[39.6, 51.9]	[6.82, 8.03]	[2.427, 2.590]

Result

$$\lambda = 0.5$$



Set I

$$\theta_{12} = 33.41^\circ$$

$$\theta_{13} = 8.58^\circ$$

$$\theta_{23} = 39.7^\circ$$

$$\Delta m_{21}^2 = 7.41 \times 10^{-5} \text{ eV}^2$$

$$\Delta m_{31}^2 = 2.507 \times 10^{-3} \text{ eV}^2$$

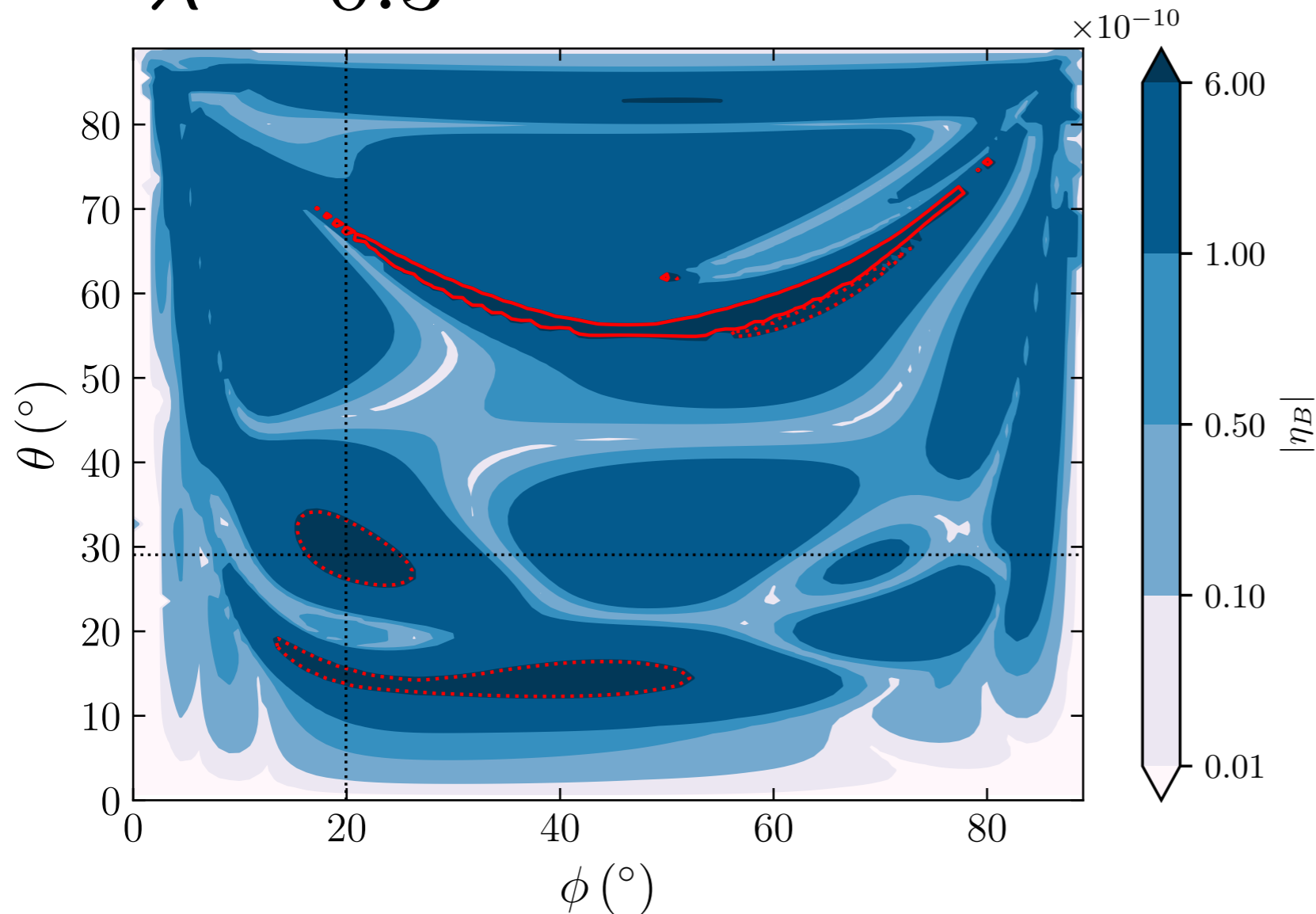
Input parameters are taken from NuFit ver 5.2

NuFIT Collaboration, NuFIT v5.2, <http://www.nu-fit.org>.

I. Esteban, et.al., JHEP 09 (2020) 178

Result

$$\lambda = 0.3$$



Set I

$$\theta_{12} = 33.41^\circ$$

$$\theta_{13} = 8.58^\circ$$

$$\theta_{23} = 39.7^\circ$$

$$\Delta m_{21}^2 = 7.41 \times 10^{-5} \text{ eV}^2$$

$$\Delta m_{31}^2 = 2.507 \times 10^{-3} \text{ eV}^2$$

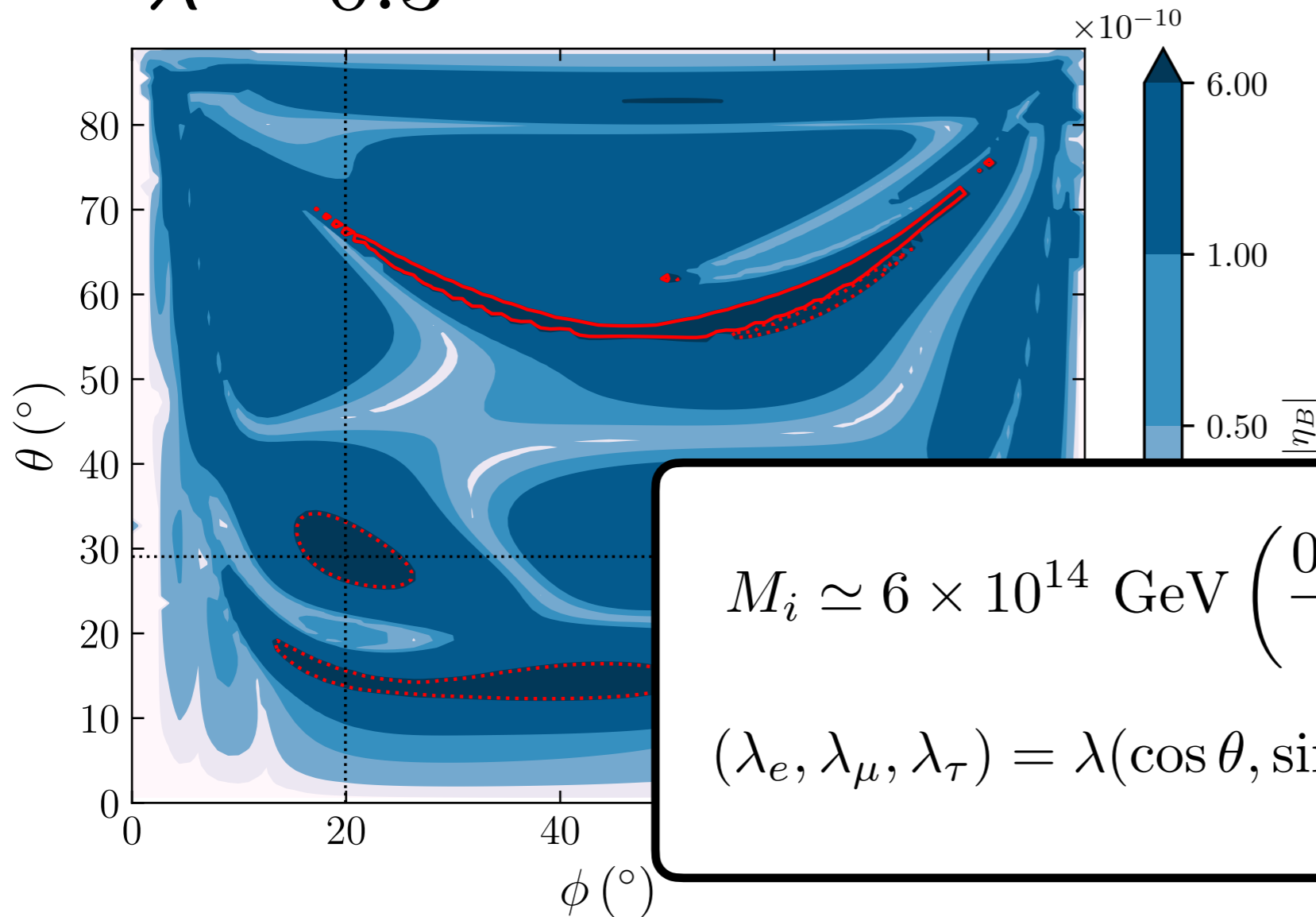
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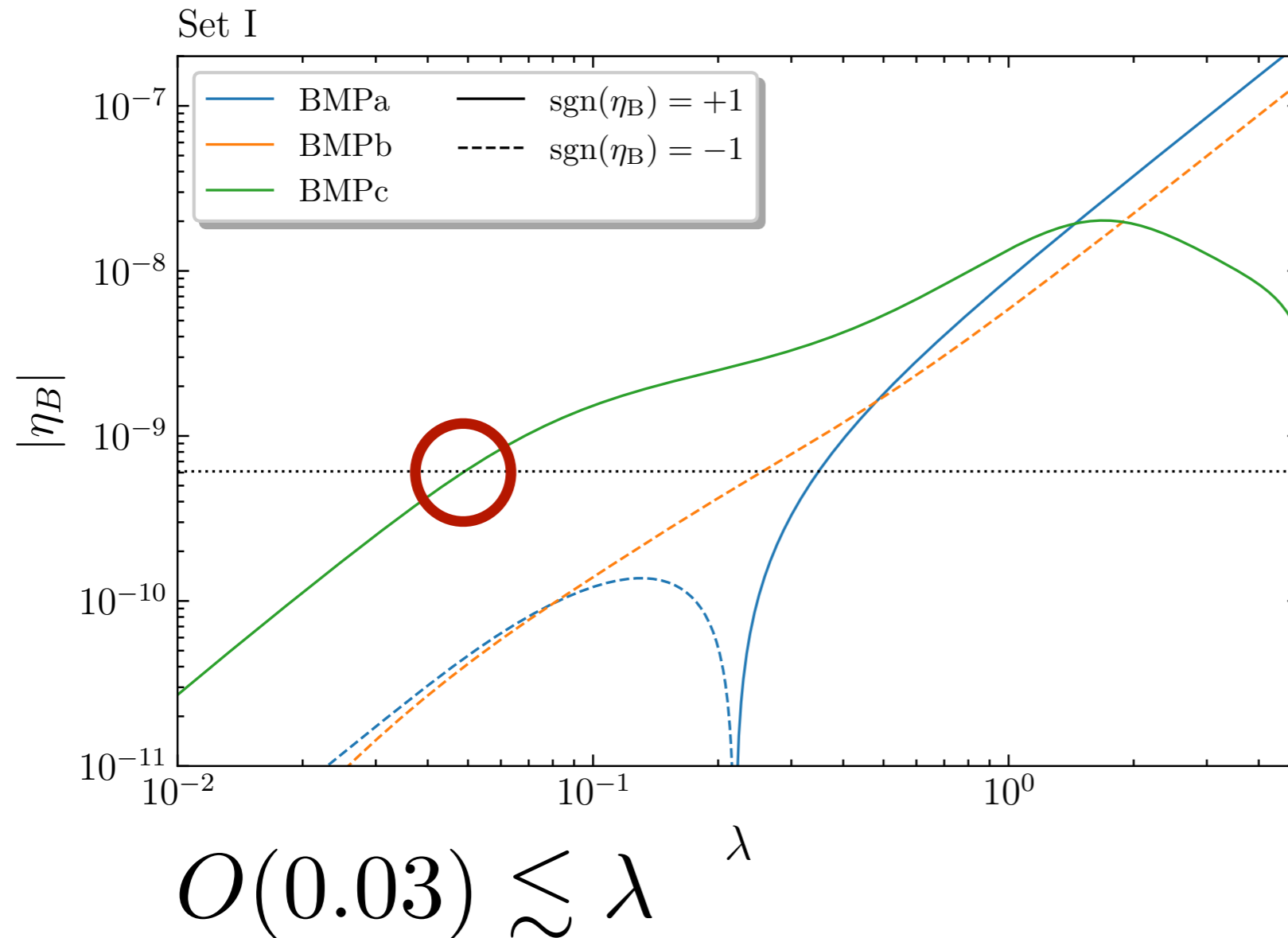
$$\Delta m_{21}^2 = 7.41 \times 10^{-5} \text{ eV}^2$$

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$$M_i \simeq 6 \times 10^{14} \text{ GeV} \left(\frac{0.05 \text{ eV}}{m_1} \right) \lambda^2 \beta_i(\theta, \phi)$$

$$(\lambda_e, \lambda_\mu, \lambda_\tau) = \lambda(\cos \theta, \sin \theta \cos \phi, \sin \theta \sin \phi)$$

Result



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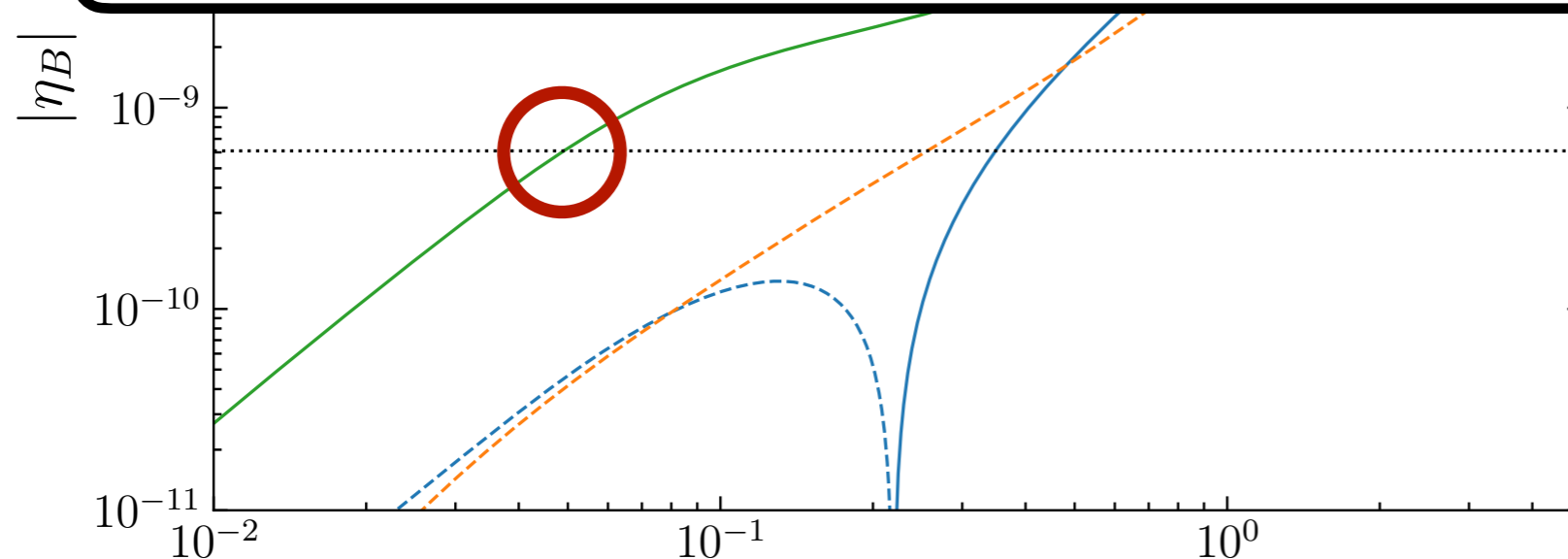
This is larger than those obtained in the context of non-thermal LG

K. Asai, K. Hamaguchi, N. Nagata, and S. Tseng, JCAP 11 (2020) 013

Result

$$M_i \simeq 6 \times 10^{14} \text{ GeV} \left(\frac{0.05 \text{ eV}}{m_1} \right) \lambda^2 \beta_i(\theta, \phi)$$

$$\blacktriangleright 10^{11-12} \text{ GeV} \lesssim M_1$$



$$O(0.03) \lesssim \lambda$$

Set I

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Assumption

- ▶ $U(1)_{L_\mu - L_\tau}$ gauge symmetry is never restored after the reheating
- ▶ singlet scalar field associated σ and Z' are sufficiently heavy so that these fields are always absent from the thermal bath

▶ $\langle \sigma \rangle \gg T_R$

- ▶ The masses of all three right-handed neutrinos are smaller than the reheating temperature.

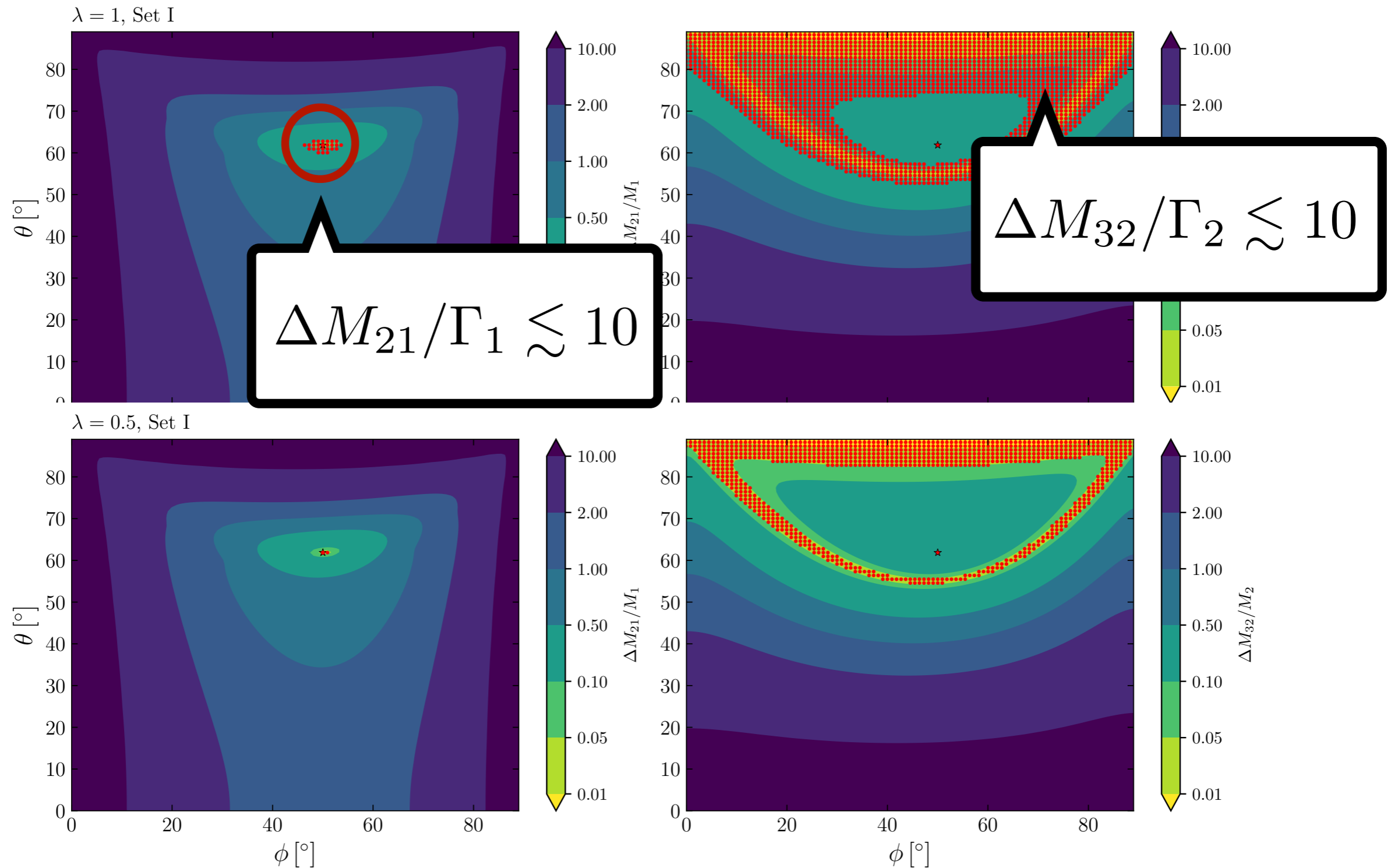
▶ $|M_{ee, \mu\tau}|, |\lambda_{e\mu, e\tau} \langle \sigma \rangle| < T_R$

Summary

- ▶ In Minimal gauged $U(1)_{L_\mu-L_\tau}$ model, the phases and the sum of the light neutrino masses are predictable because of a restricted neutrino mass matrix structure.
- ▶ Additionally, in the context of thermal leptogenesis, the BAU can be computed in terms of the three remaining free variables
- ▶ Mass of the lightest RH ν , $M_1 \gtrsim 10^{11-12}$ GeV setting LG scale in the considered model which is higher than that of the non-thermal scenario.

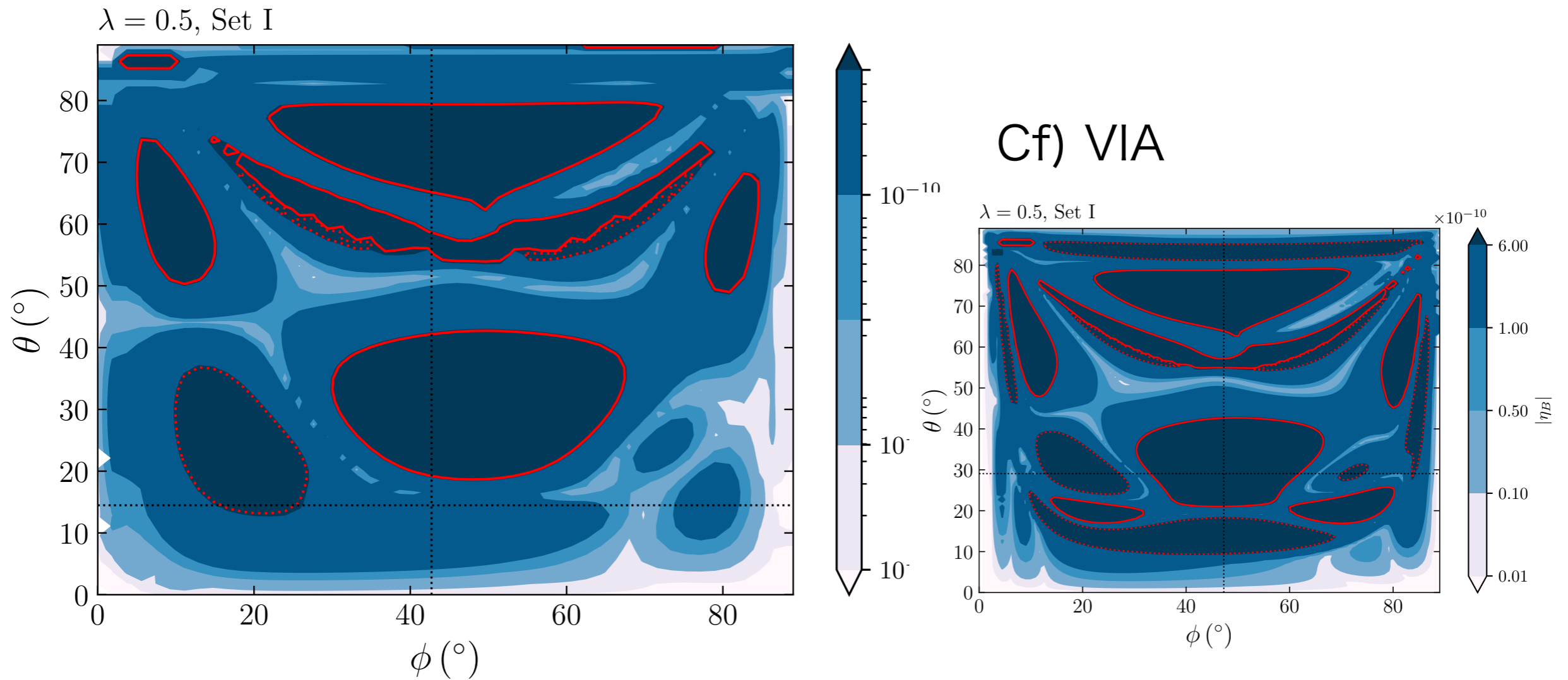
Backup

Impact of Resonance Effects



Dependence of initial condition

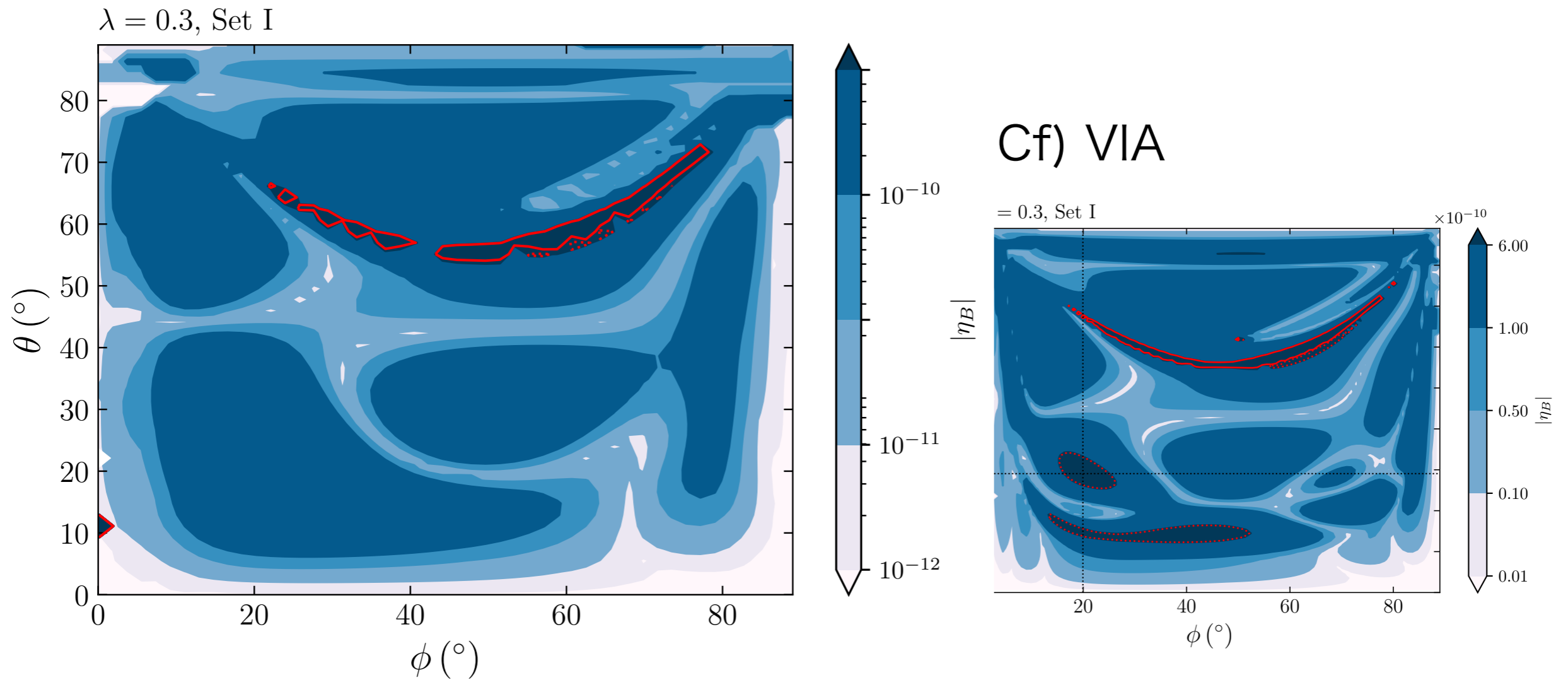
When we take thermal initial abundance (TIA),



$$(\lambda_e, \lambda_\mu, \lambda_\tau) = \lambda(\cos \theta, \sin \theta \cos \phi, \sin \theta \sin \phi)$$

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