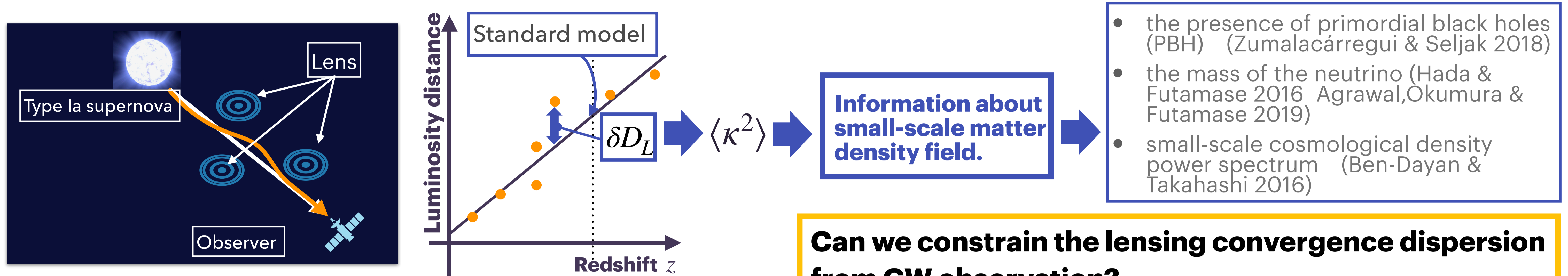




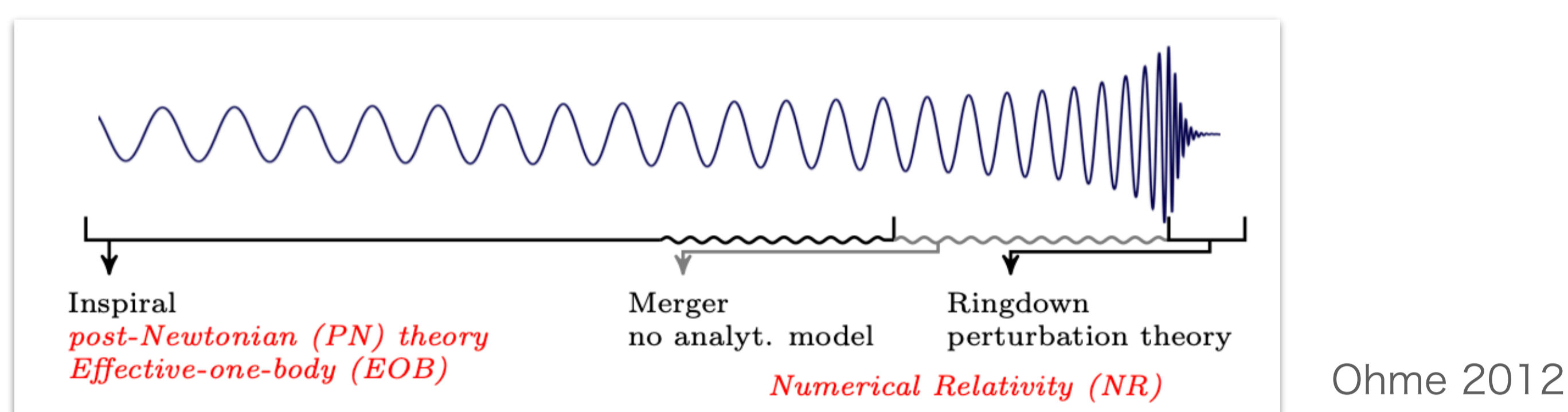
Introduction

Cosmology using the lensing convergence dispersion $\langle \kappa^2 \rangle$ with Type A Supernova



Can we constrain the lensing convergence dispersion from GW observation?

Direct measurement of luminosity distance from GW



$$\dot{f}(t) \propto M_z^{5/3} f^{11/3} \quad h_{+,\times}(t) \propto \frac{M_z^{5/3} f^{2/3}}{D_L}$$

M_c : chirp mass
 h_+, h_\times : strain of plus mode, cross mode
 f, \dot{f} : frequency, frequency evolution
 $(M_z \equiv (1+z)M_c)$

The luminosity distance can be measured **directly** and **accurately** from the gravitational wave waveform.

$$\delta D_L / D_L \lesssim 1\% \text{ ! (Holz 2005)}$$

Challenges in obtaining redshift information

- No redshift information from gravitational waveform
- BH-BH merger has no EM counterpart
- Wide error area \rightarrow Large-scale follow-up

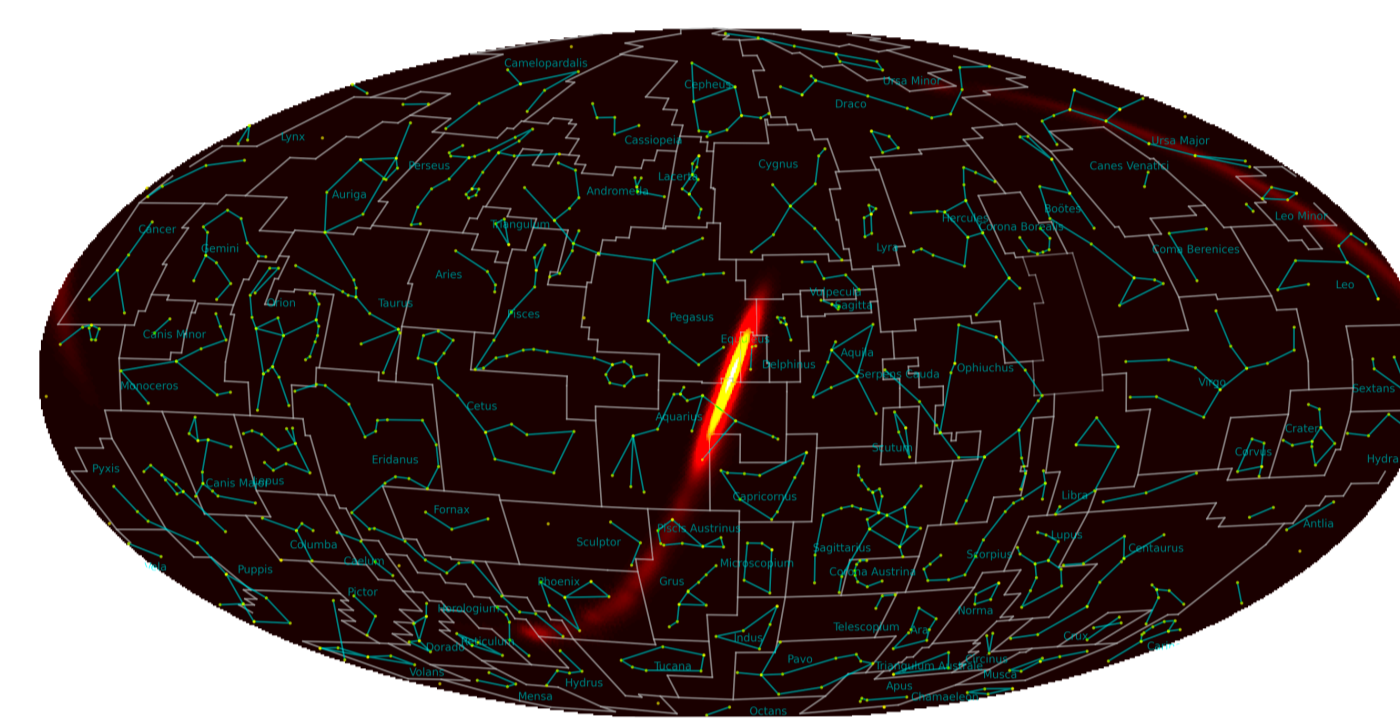


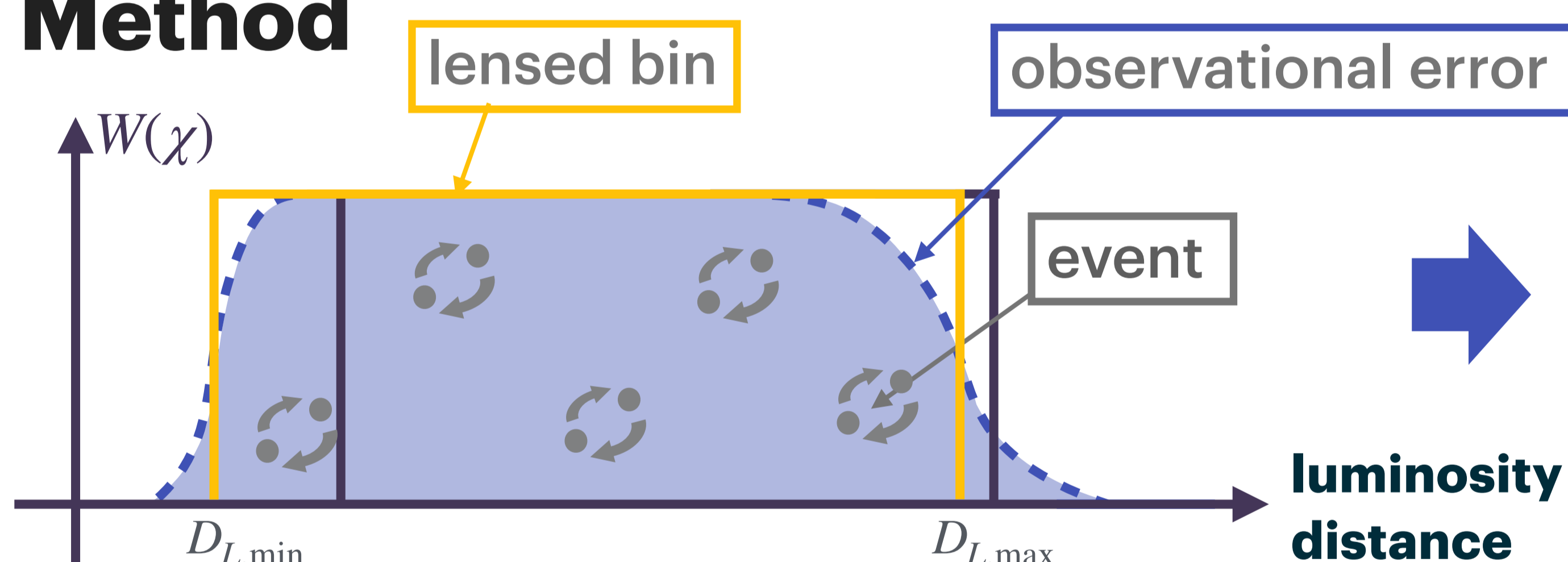
Fig: The error area of GW from BH-BH merger (S240530a)
<https://gracedb.ligo.org/superevents/S240530a/>

It is challenging to derive redshift information from black hole gravitational waves.

Aims

To develop methods for extracting the lensing convergence dispersion from GW of BBH without relying on redshift information.

Method



$$W(D_L) = \frac{1}{N_{GW}} \frac{dN_{GW}}{dD_L} \quad (D_{L,min} < D_{L,obs} < D_{L,max})$$

auto-correlation power spectrum

$$C^{ww}(\ell) = C^{ss}(\ell) + C^{st}(\ell) + C^{su}(\ell) + C^{tt}(\ell)$$

original term dispersion term $\leftarrow \langle \kappa^2 \rangle$
translation term $\leftarrow \langle \kappa^2 \rangle$

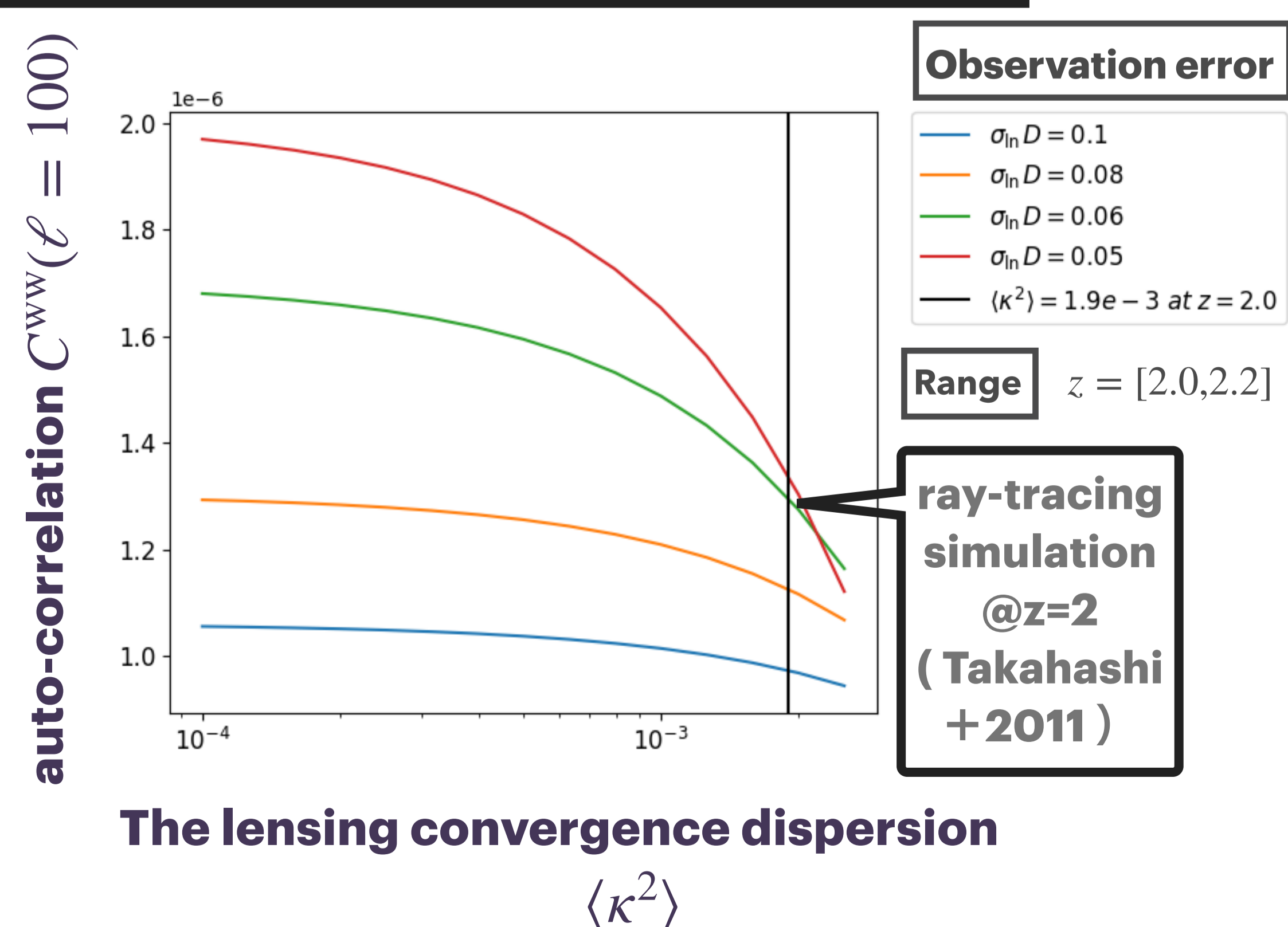
cross-correlation power spectrum

$$C^{wg}(\ell) = C^{sg}(\ell) + C^{tg}(\ell) + C^{ug}(\ell)$$

Relation between $\langle \kappa^2 \rangle$ and $C^{ww}(\ell)$

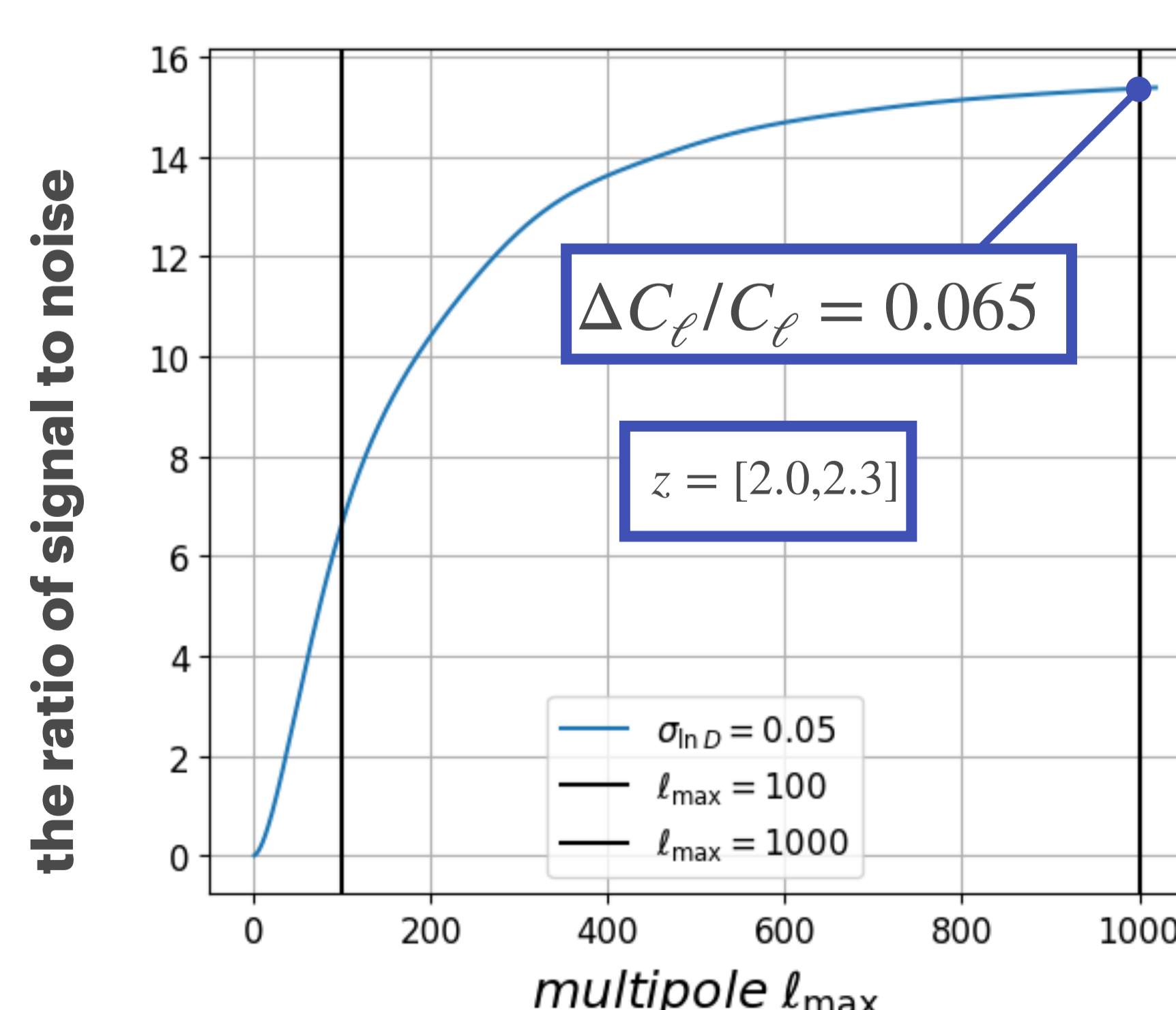
Result

Relation between $\langle \kappa^2 \rangle$ and $C^{ww}(\ell)$



anti-correlation between $C^{ww}(\ell)$ and $\langle \kappa^2 \rangle$

Signal to noise ratio



$$\Delta \langle \kappa^2 \rangle / \langle \kappa^2 \rangle \sim 0.30$$

Take Home Message !

- The lensing convergence dispersion contains a wealth of cosmological information.
- It is challenging to derive redshift from black hole gravitational waves.
- The anti-correlation between $C^{ww}(\ell)$ and $\langle \kappa^2 \rangle$ enables us to measure $\langle \kappa^2 \rangle$ from GW without depending on redshift.