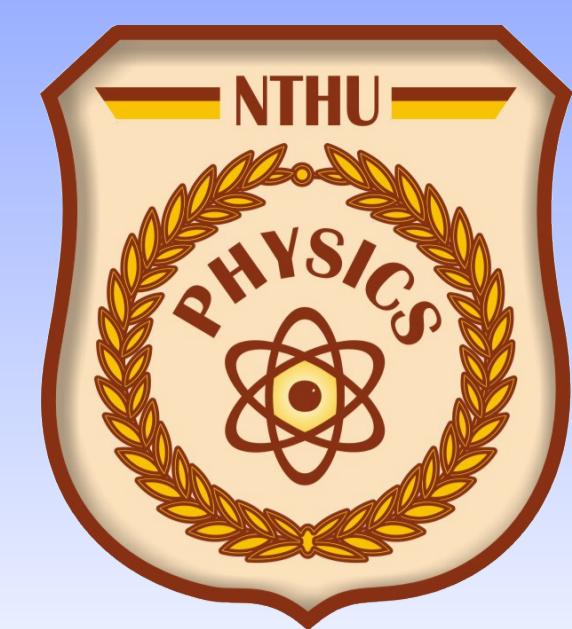




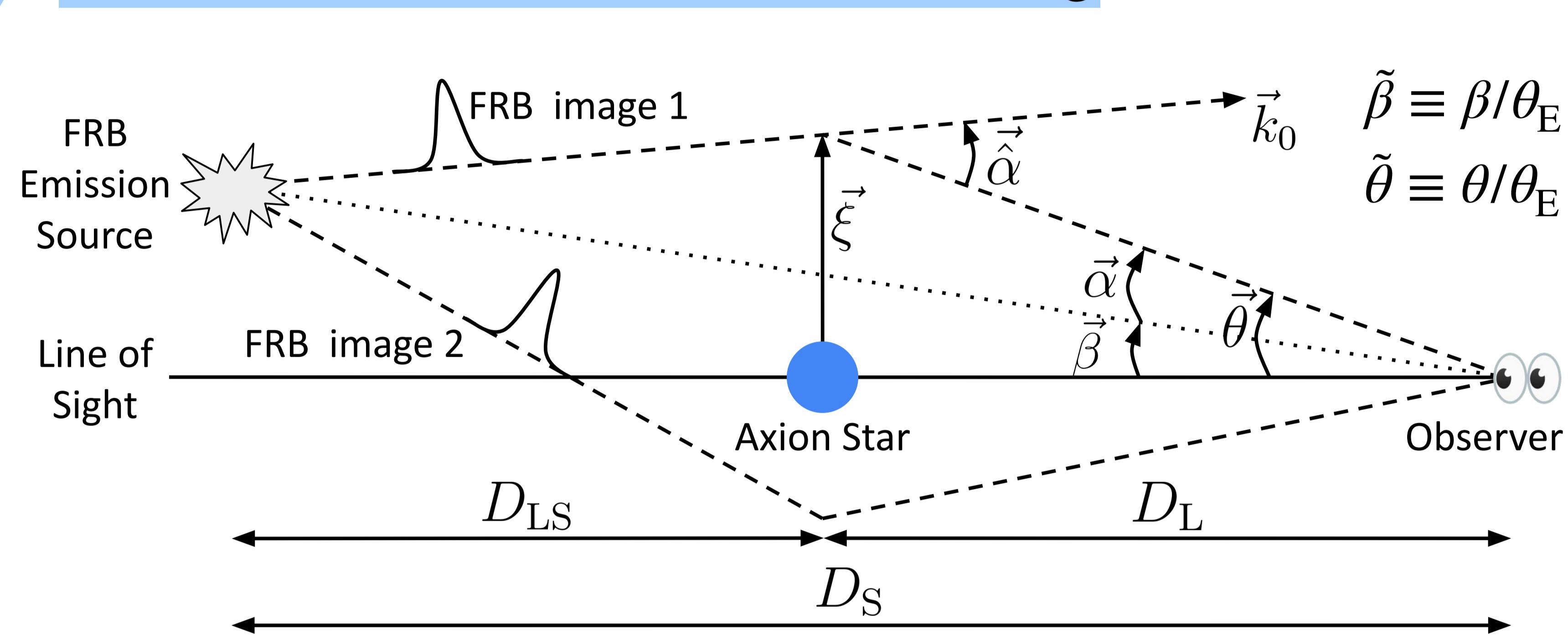
# Constraints on Extended Axion Structures from Lensing Effects of Fast Radio Burst

Jan Tristram Acuña, Kuan-Yen Chou\* Po-Yen Tseng  
 Department of Physics, National Tsing Hua University, Hsinchu, Taiwan  
 \*Email: kychou@gapp.nthu.edu.tw



**Sub-solar mass axion stars may be constrained by FRB lensing with non-negligible finite-size and axion-induced lensing effects.**

## Geometrical Schematic of FRB Lensing

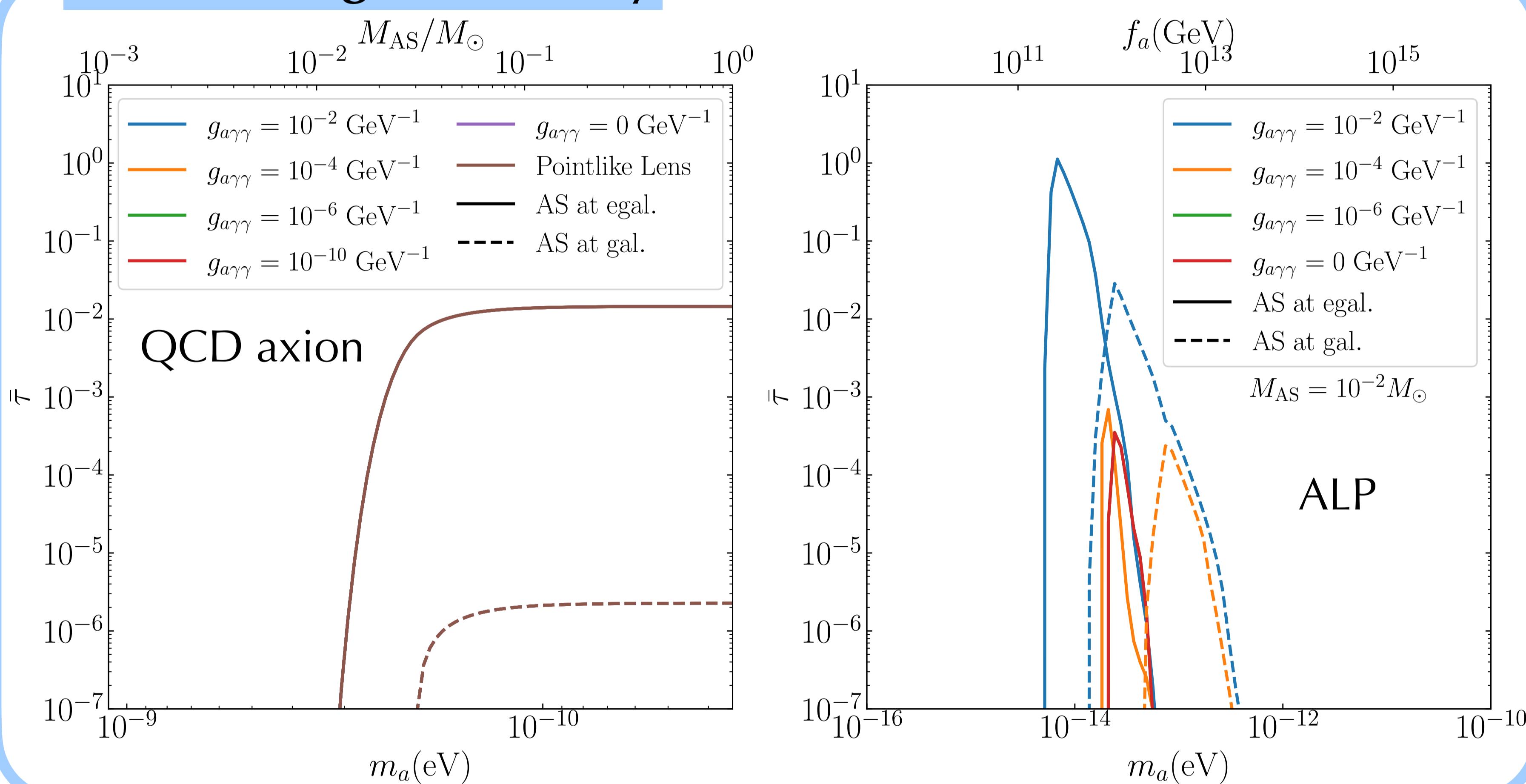


- Lensing probability: Assume ASs at extragalaxy and the Milky Way.

$$\bar{\tau}(M_{AS}) = \int dz_S \mathcal{N}_{FRB}(z_S) \int_0^{z_S} d\chi(z_L) (1+z_L)^2 n_{AS}(M_{AS}, \sigma(M_{AS}, z_L)),$$

$$\sigma(M_{AS}, z_L) \propto (\tilde{\beta}_{\max}^2 - \tilde{\beta}_{\min}^2) \quad \Delta t_{\text{thres}} \leq \Delta t(\tilde{\beta}_{\min} \leq \tilde{\beta}) \quad R_f(\tilde{\beta} \leq \tilde{\beta}_{\max}) \leq R_{f,\max}$$

## FRB Lensing Probability



$$\hat{a}_{a\gamma\gamma} = -\frac{g_{a\gamma\gamma}^2}{8|\mathbf{k}_0|^2} \int \nabla_\perp (\partial a)^2 dt \quad t_{a\gamma\gamma} = -\frac{g_{a\gamma\gamma}^2}{8|\mathbf{k}_0|^2} \int (\partial a)^2 dt$$

- Lens equation: Assume AS spatial profile is Gaussian

$$\tilde{\beta} = \tilde{\theta} - \frac{1}{\tilde{\theta}} [1 - \exp(-w_E^2 \tilde{\theta}^2)] - Aw_E^2 \tilde{\theta} \exp(-w_E^2 \tilde{\theta}^2)$$

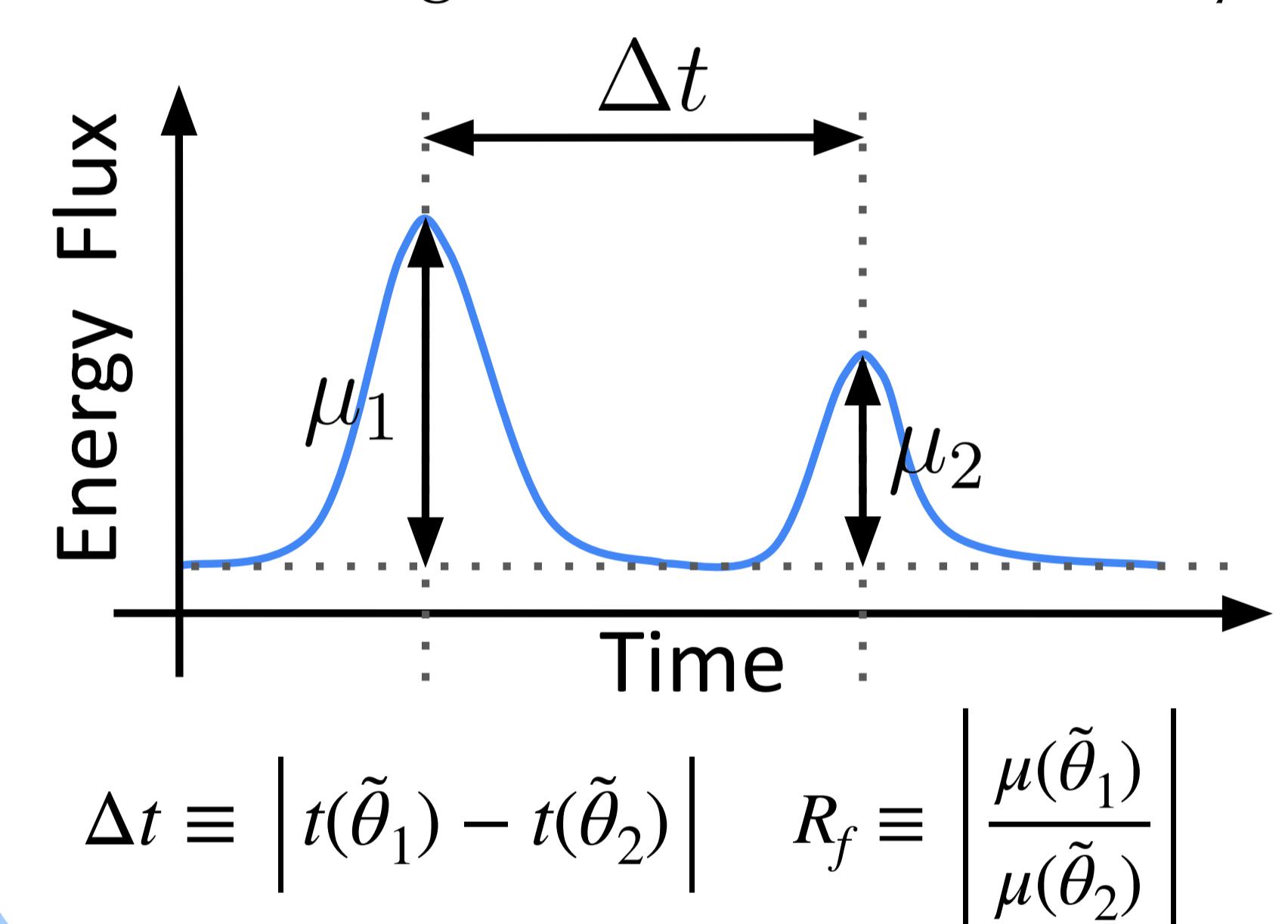
Gravitational-induced      Axion-induced

$$w_E \equiv D_L \theta_E / R_{AS}$$

$$A \propto g_{a\gamma\gamma}^2 f_0^{-2}$$

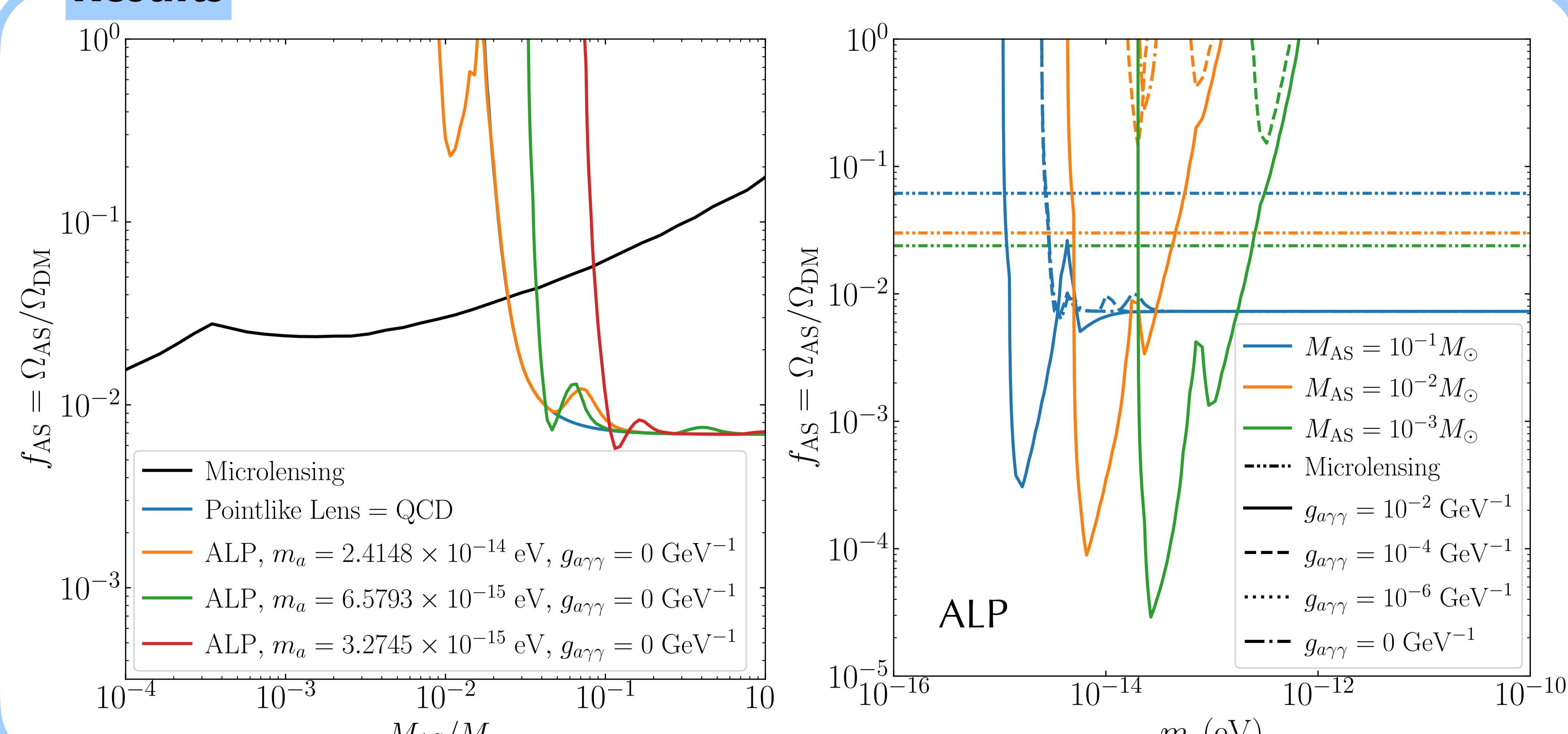
## FRB Lensing Signatures

- Flux Magnification + Time delay



- Estimated # of lensed FRB:  $N_{\text{lensed}} = (1 - e^{-\bar{\tau}}) N_{\text{obs}}$   
 Parameters with  $N_{\text{lensed}} > 1$  are excluded by CHIME.

## Results



## References

- Jamie I. McDonald and Luís B. Ventura. *Phys. Rev. D* 101 (2020), no. 12, 123503, arXiv: 1911.10221.
- K. Fujikura et al.. *Phys. Rev. D* 104 (2021), no. 12, 123012, arXiv: 2109.04283.
- Julian B. Muñoz et al.. *Phys. Rev. Lett.*, 117(9):091301, 2016, arXiv: 1605.00008.