

HELAS, Toponium and the ILC

Kaoru Hagiwara (KEK)

Hitoshi Fest @ Kavli IPMU
2024.12.20

MULTIPLE WEAK BOSON PRODUCTION VIA GLUON FUSION

#1

Kaoru Hagiwara (Durham U.), Hitoshi Murayama (Tokyo U.) (Jun, 1989)

Published in: *Phys.Rev.D* 41 (1990) 1001[pdf](#)[DOI](#)[cite](#)[claim](#)[reference search](#)

14 citations

SSC

SUPERSYMMETRIC CONTRIBUTIONS TO GAMMA ($Z \rightarrow$ HADRONS)

#2

Kaoru Hagiwara (KEK, Tsukuba), Hitoshi Murayama (Tokyo U.) (Apr, 1990)

Published in: *Phys.Lett.B* 246 (1990) 533-536[DOI](#)[cite](#)[claim](#)[reference search](#)

22 citations

LEP

Search for the Yukawa interaction in the process $e^+ e^- \rightarrow t \bar{t} Z$ at TeV

#3

linear colliders

Kaoru Hagiwara (KEK, Tsukuba), H. Murayama (Tokyo U.), I. Watanabe (Hiroshima U.) (Oct, 1990)

Published in: *Nucl.Phys.B* 367 (1991) 257-286[DOI](#)[cite](#)[claim](#)[reference search](#)

83 citations

Single weak boson production at TeV $e^+ e^-$ colliders

#4

Kaoru Hagiwara (Durham U. and KEK, Tsukuba), H. Iwasaki (Hiroshima U.), A. Miyamoto (KEK, Tsukuba), H. Murayama (Tokyo U.), D. Zeppenfeld (Wisconsin U., Madison) (Dec, 1990)

Published in: *Nucl.Phys.B* 365 (1991) 544-596[DOI](#)[cite](#)[claim](#)[reference search](#)

55 citations

HELAS

JLC physics

#23

H. Murayama (Tokyo U.) (1990)

Contribution to: 2nd Workshop on Japan Linear Collider (JLC), 135-149

[cite](#)[reference search](#)

0 citations

HELAS: HELicity amplitude subroutines for Feynman diagram evaluations

#6

H. Murayama (Tohoku U.), I. Watanabe (Hiroshima U.), Kaoru Hagiwara (KEK, Tsukuba) (Jan, 1992)

[pdf](#)[cite](#)[claim](#)[reference search](#)

71 citations

JLC

Top quark pair production near threshold

#7

Y. Sumino (Tokyo U.), K. Fujii (KEK, Tsukuba), Kaoru Hagiwara (KEK, Tsukuba and Durham U.), H. Murayama (Tohoku U.), C.K. Ng (SLAC) (Mar, 1992)

Published in: *Phys.Rev.D* 47 (1993) 56-81[pdf](#)[links](#)[DOI](#)[cite](#)[claim](#)[reference search](#)

149 citations

① Jun 1989

② Apr 1990

③ Oct 1990

④ Dec 1990

⑤ Nov 1990

⑥ Jan 1992

⑦ Mar 1992

1987

M2

↑ I gave weekly lectures @ UTokyo
(Hitoshi was a M2 student)

1988

D1

Oct 8-19 I met Hitoshi @ UTokyo.

1989

D2

• paper ①

↑ I was in
Durham

1990

D3

Mar 2-16 Phenomenology school @ KEK with K. Hikasa

• papers ②, ③, ④

Many projects @ KEK

• JLC WS2 ⑤

↑
Durham

1991

↓ Ph.D.

Tohoku U

• HELAS manual ⑥

• Toponium paper with J. Srimino ⑦

1992 Tim Stelzer visited KEK & learned HELAS \Rightarrow MadGraph (1994).

Multiple weak-boson production via gluon fusion

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(Received 25 September 1989)

We note here that this chiral transformation produces no anomaly for a degenerate quark doublet in the QCD sector. The resulting Yukawa Lagrangian is simply

$$\begin{aligned} \mathcal{L}_{\text{Yukawa}} = & -f \frac{1}{\sqrt{2}} \sqrt{(v+H)^2 + (\chi^3)^2 + 2\chi^+\chi^-} \\ & \times (\bar{U}, \bar{D}) \begin{pmatrix} U \\ D \end{pmatrix}. \end{aligned} \quad (3)$$

This form exhibits explicitly the SO(4) symmetry of the fields $(v+H, \chi^1, \chi^2, \chi^3)$ where $\chi^\pm = (\chi^1 \pm i\chi^2)/\sqrt{2}$. This symmetry is a reflection of the $SU(2)_L \times SU(2)_R$ symme-

$$\mathcal{L}_{\text{eff}} = \frac{\alpha_s}{24\pi} G_{\mu\nu}^a G^{a\mu\nu} \ln \left[\left(1 + \frac{H}{v} \right)^2 + 2 \frac{\chi^+\chi^-}{v^2} + \frac{(\chi^3)^2}{v^2} \right]. \quad (4)$$

This is our main result.

The “Feynman rules” for $gg \rightarrow$ multiple W and Z bosons are obtained by expanding the effective action (4). From its form, we see immediately that only even numbers of W/Z are produced, which is analogous to the G -parity selection rule for the pions. The vertex for $2n$ W/Z ’s which contain m pairs of W^+W^- and $(2n-2m)$ Z ’s is

$$\frac{\alpha_s}{3\pi} \delta^{ab} [k_2^\mu k_1^\nu - (k_1 \cdot k_2) g^{\mu\nu}] \frac{1}{v^{2n}} \frac{(-1)^{n-1}}{n} 2^m (2n-2m)! m! m! n! C_m, \quad (5)$$

where the colors of gluons are denoted by a, b , and their four-momenta by k_1^μ, k_2^ν . These “vertices” correspond to the infinitely-heavy-quark loop with Goldstone-boson legs [we call these direct amplitudes; see Fig. 1(a)]. The cross sections averaged over colors and helicities of two gluons are

$$\sigma(gg \rightarrow (W^+W^-)^m Z^{2n-2m}) = \frac{1}{2} \frac{1}{8} \frac{\alpha_s^2}{9\pi^2} \frac{\hat{s}}{8} (2n-2m)! \left(\frac{2^m n!}{nv^{2n} (n-m)!} \right)^2 V_{\text{ph}}, \quad (6)$$

Supersymmetric contributions to $\Gamma(Z \rightarrow \text{hadrons})$

Kaoru Hagiwara

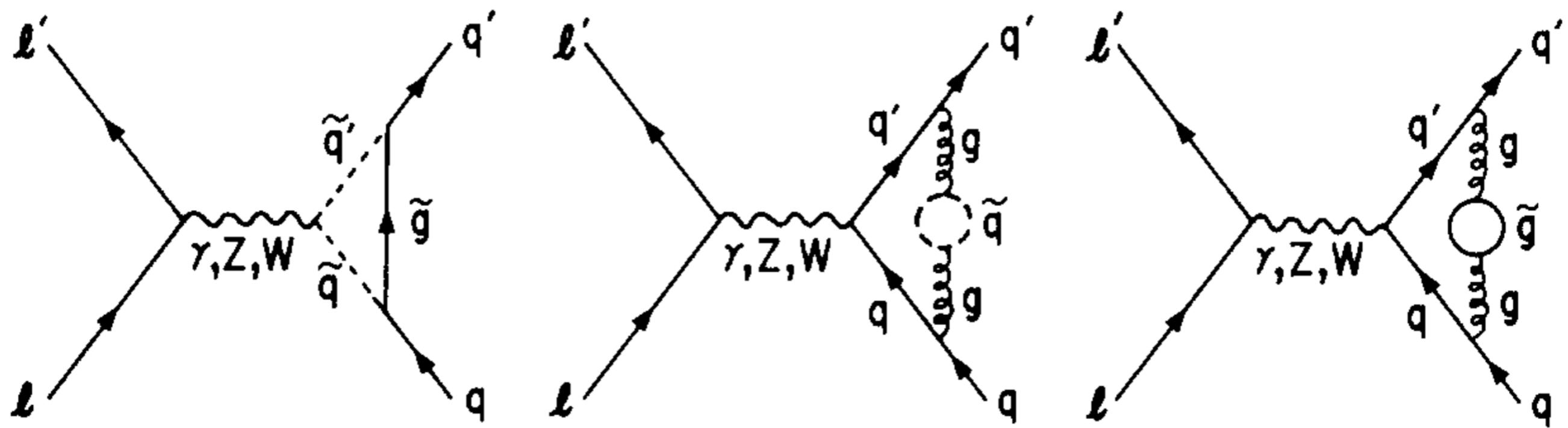
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Received 27 May 1990



Search for the Yukawa interaction in the process $e^+e^- \rightarrow t\bar{t}Z$ at TeV linear colliders

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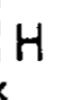
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Received 29 October 1990

(a) $f \xleftarrow{\quad} f = -i \langle f | H | f \rangle$



(b) $f \xleftarrow{\quad} f = D_H(p_H^2) \langle f | H | f \rangle$



(c) $Z \sim \sim Z = -i \Gamma_{ZZH}(Z, Z)$



(d) $Z \sim \sim Z = D_H(p_H^2) \Gamma_{ZZH}(Z, Z)$



(e) $W^- \sim \sim W^+ = -i \Gamma_{WWH}(W^-, W^+)$



(f) $W^- \sim \sim W^+ = D_H(p_H^2) \Gamma_{WWH}(W^-, W^+)$



Fig. 3. Additional HELAS Feynman rules including a Higgs boson which is represented by a dashed line.

SINGLE WEAK BOSON PRODUCTION AT TeV e^+e^- COLLIDERS

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²*KEK, Tsukuba, Ibaraki 305, Japan*

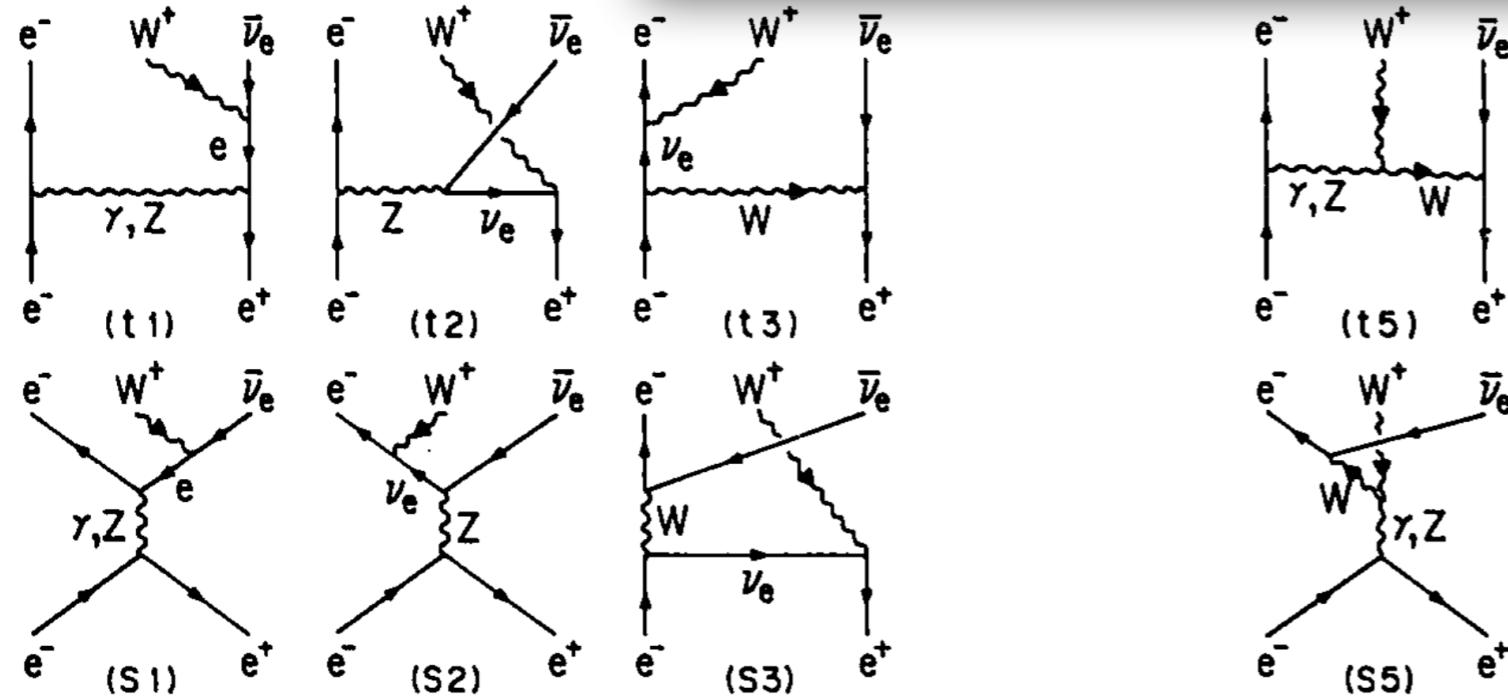
³*Department of Physics, Hiroshima University, Hiroshima 730, Japan*

⁴*Department of Physics, University of Tokyo, Tokyo 113, Japan*

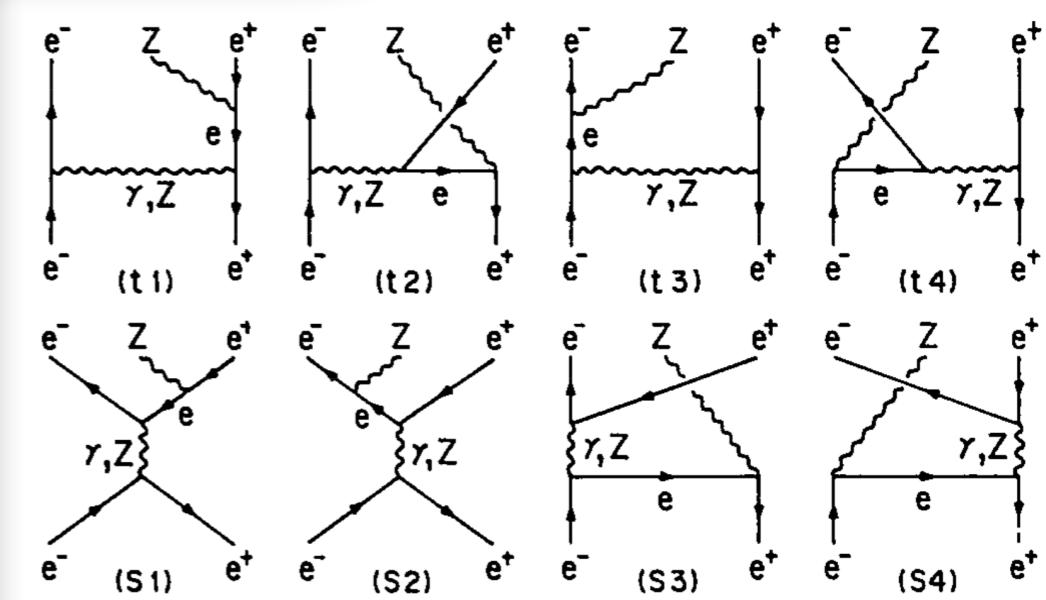
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Received 27 December 1990

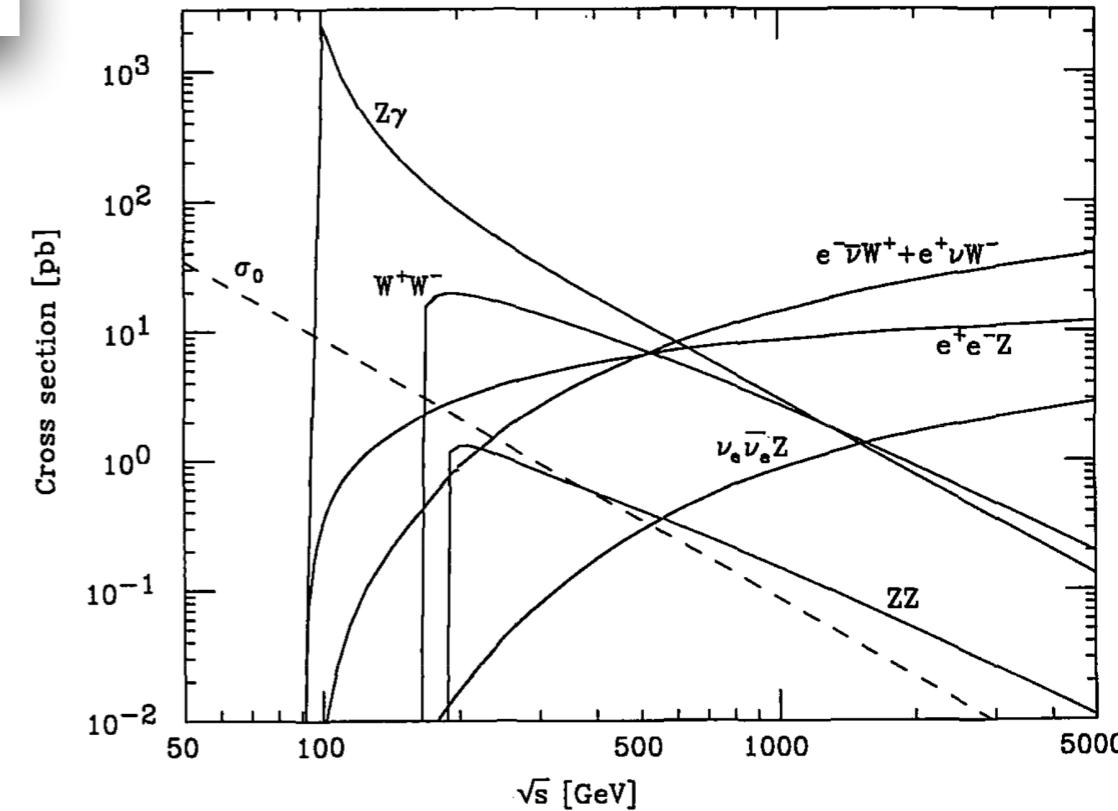
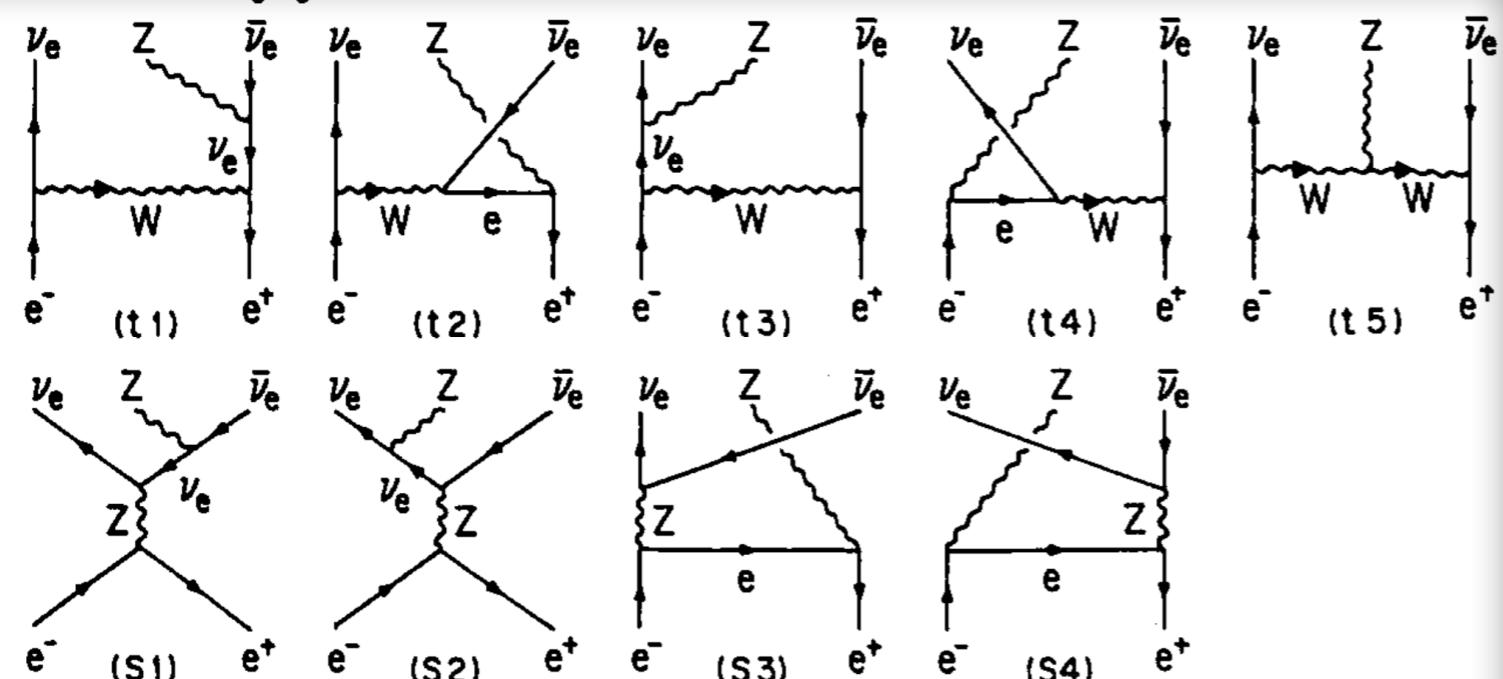
(a) $e^-e^+ \rightarrow e^-\bar{\nu}_e W^+$



(b) $e^-e^+ \rightarrow e^-\bar{e}^+ Z$



(c) $e^-e^+ \rightarrow \nu_e\bar{\nu}_e Z$





KEK Report 91-11
January 1992
H

HELAS: HELicity Amplitude Subroutines for Feynman Diagram Evaluations

H. MURAYAMA, I. WATANABE and K. HAGIWARA



Chapter 2

How to use HELAS

2.1 Basic Idea

The basic idea of HELAS is to begin with the external lines by creating the wavefunctions explicitly using a fixed notation, and to give rules to join the lines. You may suppose that there are too many possibilities for a complete set of joining rules but in fact they can all be classified into a finite set in renormalizable theories. We will show all the possible rules of renormalizable theories in Table 2.1.

Vertex	interaction
FFV	vector or axial vector couplings
FFS	Yukawa couplings
VVV	Yang-Mills couplings
VVS	Higgs interaction
SSV	scalar gauge couplings
SSS	scalar self-couplings
VVVV	Yang-Mills couplings
VVSS	scalar gauge couplings (seagull)
SSSS	scalar self-couplings

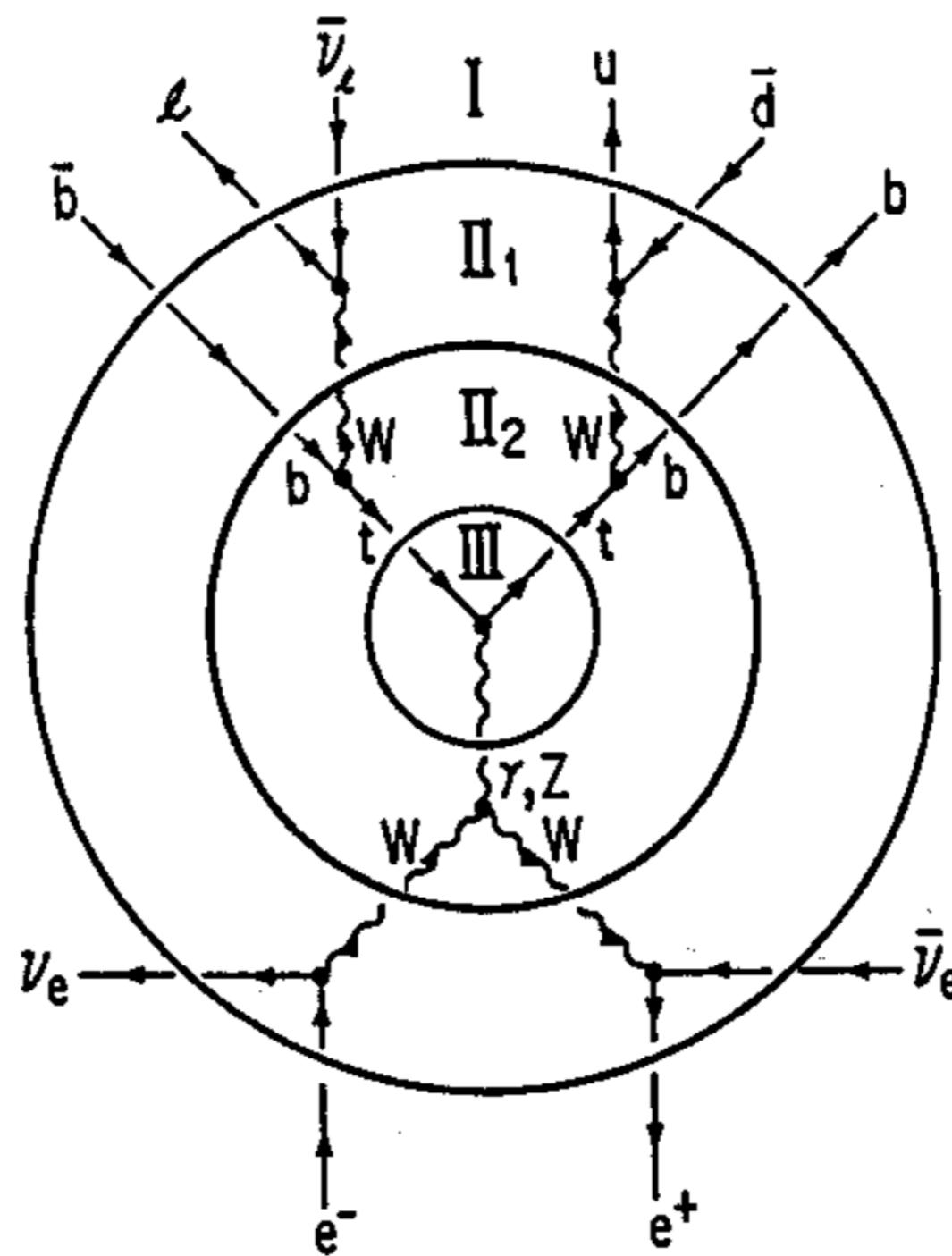


Figure 5: The steps you follow when coding with HELAS . The shown example is an extended version of Fig. 4(a), where the final W^+ decays into $u\bar{d}$, and W^- into $l\bar{\nu}_l$.

2.9.3 Goldstone bosons and the BRS invariance tests

What we find most efficient in testing the helicity amplitudes with one or more external vector bosons is the BRS identity [4]

$$\langle phys; \text{out} | (\partial^\mu V_\mu - \xi_V m_V \chi_V) | phys; \text{in} \rangle = 0, \quad (2.35)$$

where ξ_V is the covariant R_ξ gauge parameter and χ_V the Goldstone mode associated with the vector boson V . The states $\langle phys; \text{out} |$ and $| phys; \text{in} \rangle$ are arbitrary physical states of on-shell external particles. By using the reduction formula, the identity (2.35) leads to an exact relationship between the S -matrix elements of the four-divergence of the vector boson and those of the associated Goldstone boson

$$\langle phys, V_S; \text{out} | phys; \text{in} \rangle = -\langle phys, \chi_V; \text{out}, | phys; \text{in} \rangle, \quad (2.36)$$

where V_S denotes the 'scalar' component of the vector boson. Eq. (2.36)

A.4 Collinear Singularities

The output of the JEEXXX is simply

$$\hat{J}_A^\mu(\langle e' |, |e \rangle) = (-e)\bar{u}(p, \sigma')\gamma^\mu u(k, \sigma), \quad (\text{A.24})$$

for the t -channel photon emission from the electron current. Since the problem is

For the helicity non-flip case $\sigma = \sigma'$, the truncated current reads

$$\hat{J}_A^\mu = (-e)\sqrt{x}(2E) \left(\cos \frac{\theta}{2}, \sin \frac{\theta}{2} e^{-i\sigma\phi}, i\sigma \sin \frac{\theta}{2} e^{-i\sigma\phi}, \cos \frac{\theta}{2} \right), \quad (\text{A.27})$$

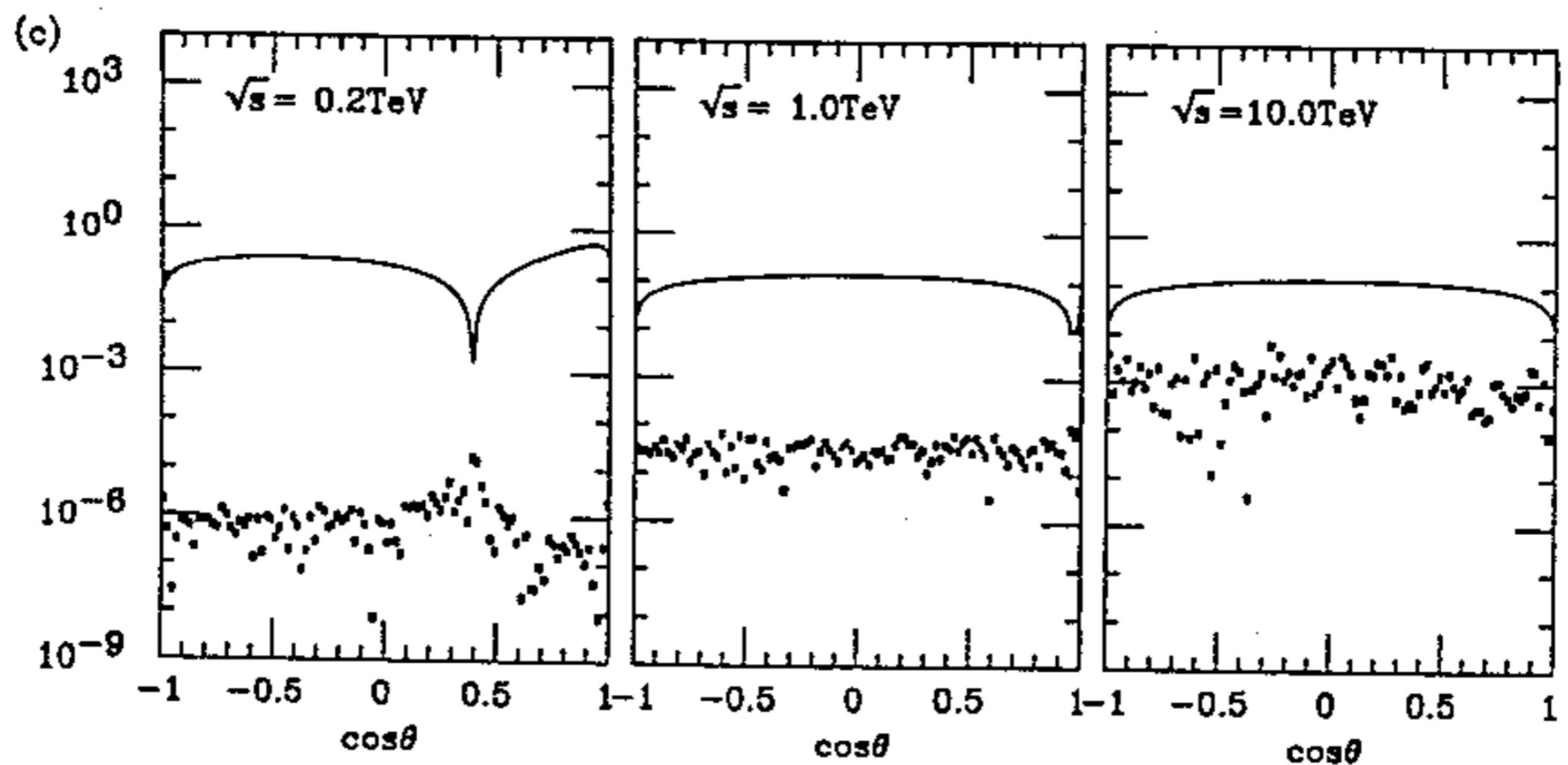
where the terms of order $O(m_e^2/E^2)$ are neglected. One can check the conservation of the current by contracting with the four-momentum of the photon

$$\begin{aligned} p_A^\mu &= k^\mu - p^\mu \\ &= E(1-x, -x\beta' \sin \theta \cos \phi, -x\beta' \sin \theta \sin \phi, \beta - x\beta' \cos \theta) \\ &= E(1-x, -x \sin \theta \cos \phi, -x \sin \theta \sin \phi, 1-x \cos \theta) + O\left(\frac{m_e^2}{E}\right), \end{aligned} \quad (\text{A.28})$$

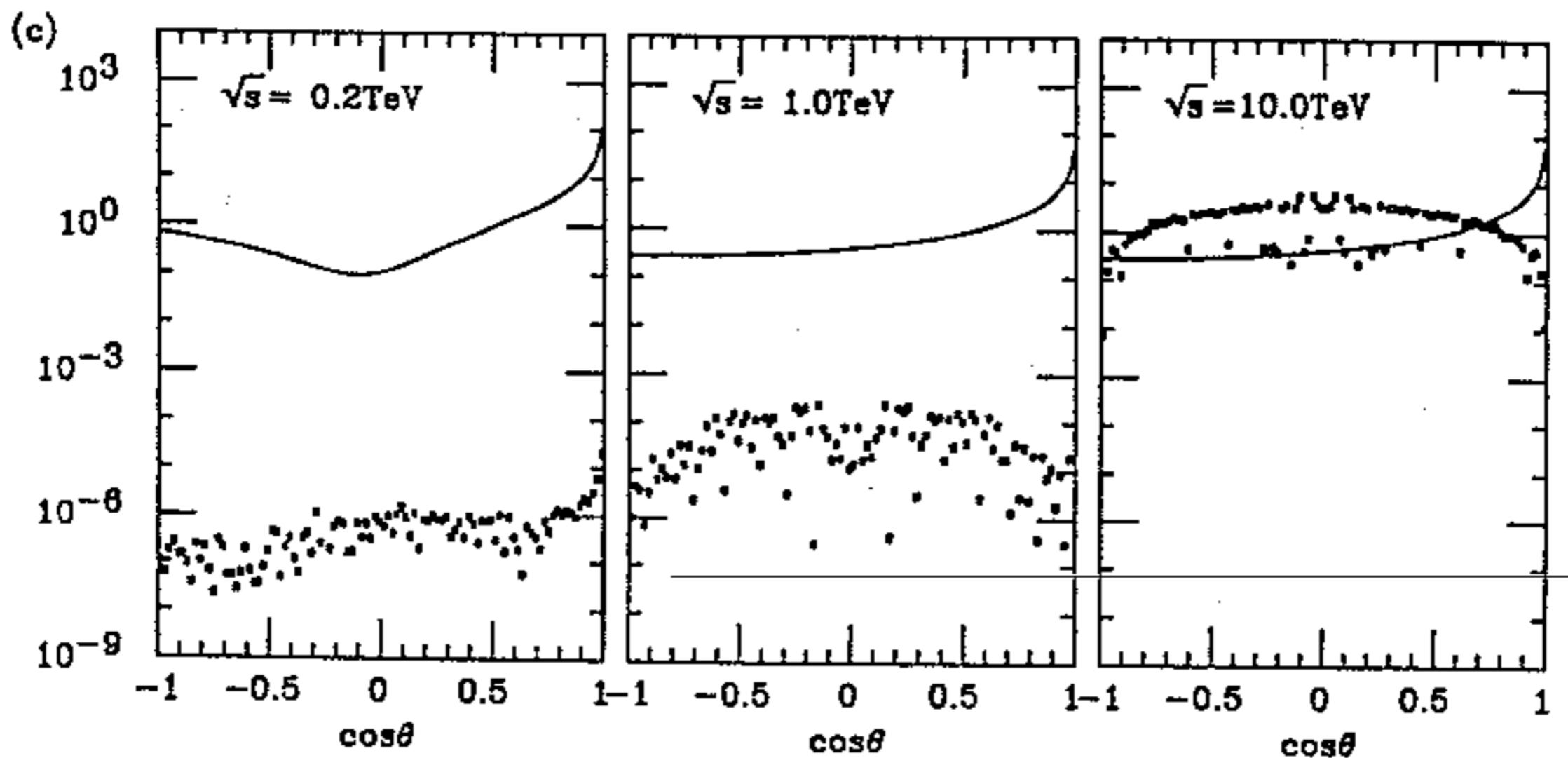
Since the problem lies in the collinear limit $\cos \theta \rightarrow 1$, it is instructive to give the expression in the limit,

$$\begin{aligned} \hat{J}_A^\mu &= \sqrt{x}(2E)(1, 0, 0, 1), \\ p_A^\mu &= E(1-x, 0, 0, 1-x). \end{aligned} \quad (\text{A.29})$$

$$\begin{aligned} \hat{J}_A^\mu - \hat{J}_A^0 \frac{p_A^\mu}{p_A^0} &= (-e)\sqrt{x}(2E) \sin \frac{\theta}{2} \left(0, e^{-i\sigma\phi} + \frac{2x}{1-x} \cos^2 \frac{\theta}{2} \cos \phi, \right. \\ &\quad \left. i\sigma e^{-i\sigma\phi} + \frac{2x}{1-x} \cos^2 \frac{\theta}{2} \sin \phi, -\frac{2x}{1-x} \cos \frac{\theta}{2} \sin \frac{\theta}{2} \right), \end{aligned} \quad (\text{A.30})$$

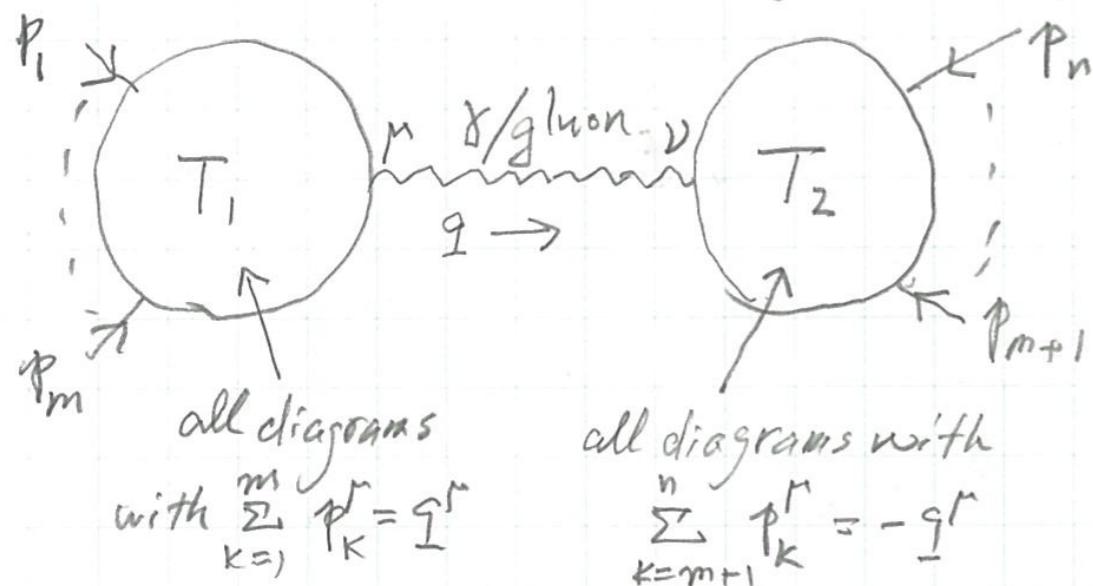


$$e_L^- e_R^+ \rightarrow W_L^- W_L^+$$



$$W_L^- W_L^+ \rightarrow W_L^- W_L^+$$

QED & QCD : Feynman gauge \Rightarrow FD gauge 2003.03.03 (KH-Kanzaki-Mawatari)



$$= T(p_1, \dots, p_n) = T_1^\mu(p_1, \dots, p_m) \frac{P_{\mu\nu}^3(\mathbf{q})}{q^2 + i\epsilon} T_2^\nu(p_{m+1}, \dots, p_n)$$

$$P_{\mu\nu}^3(\mathbf{q}) = -g_{\mu\nu} + (1-\beta) \frac{q_\mu q_\nu}{q^2}$$

$$\mathbf{q}_\mu T_1^\mu = \mathbf{q}_\nu T_2^\nu = 0 \Rightarrow \beta\text{-independence of } T.$$

(BRST)

$$P_{\mu\nu}^3(\mathbf{q}) = -g_{\mu\nu} + \frac{q_\mu q_\nu}{q^2} - \beta \frac{\mathbf{q}_\mu \mathbf{q}_\nu}{q^2}$$

$$= \sum_{h=\pm 1} E_\mu^*(\mathbf{q}, h) E_\nu(\mathbf{q}, h) + \text{sgn}(q^2) E_\mu^*(\mathbf{q}, 0) E_\nu(\mathbf{q}, 0) - \beta \frac{q_\mu q_\nu}{q^2}$$

$$E^\mu(\mathbf{q}, \pm 1) = \frac{1}{\sqrt{2}}(0, 1, \pm i, 0)$$

$$E^\mu(\mathbf{q}, 0) = \begin{cases} (\sinh y, 0, 0, \cosh y) & \text{when } q^2 > 0 : q^M = Q (\cosh y, 0, 0, \sinh y) \\ (\cosh y, 0, 0, \sinh y) & \text{when } q^2 < 0 : q^M = Q (\sinh y, 0, 0, \cosh y) \end{cases}$$

We introduce $\tilde{E}^M(\mathbf{q}, 0) = E^\mu(\mathbf{q}, 0) - \frac{q^\mu}{Q}$

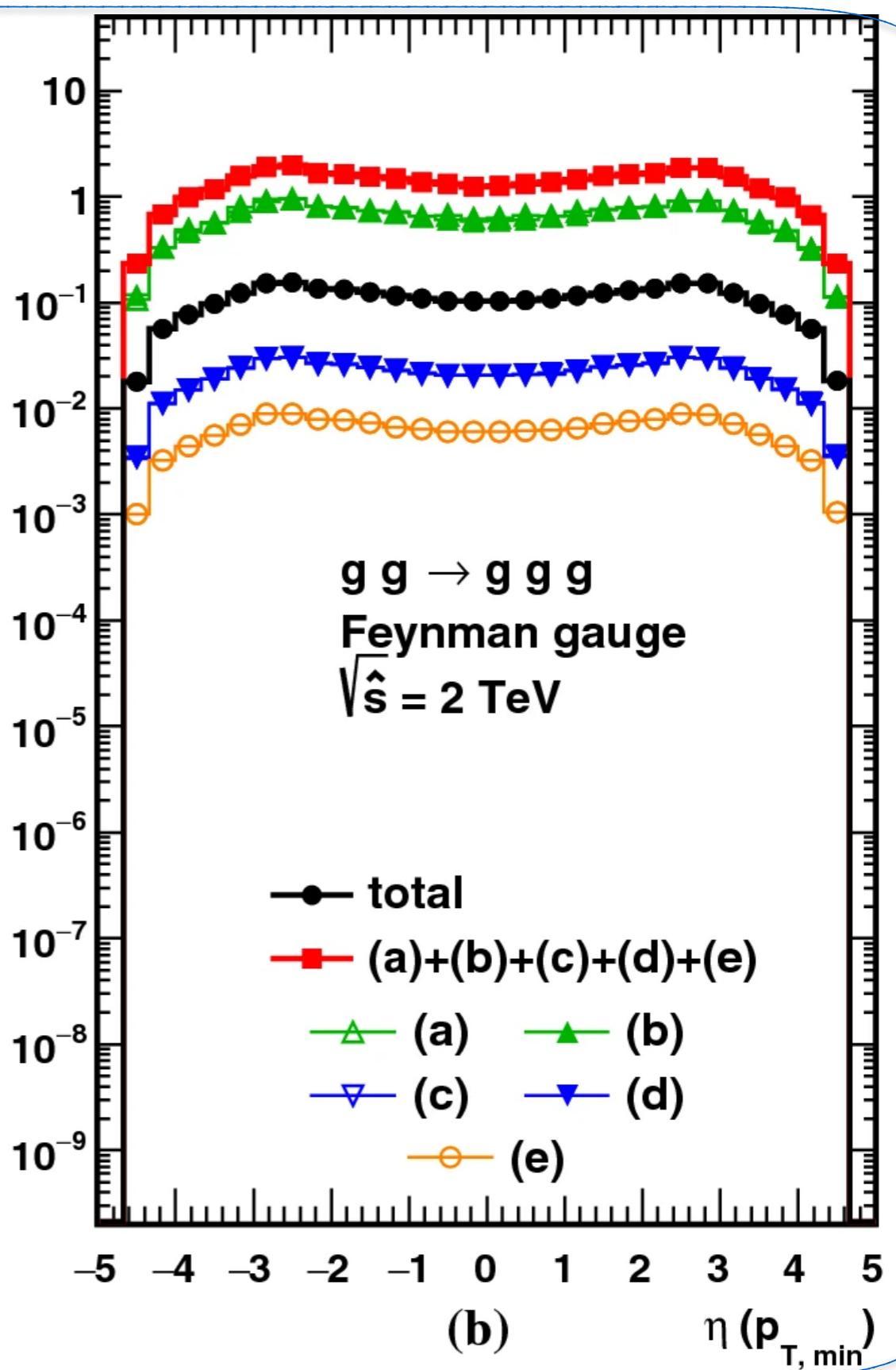
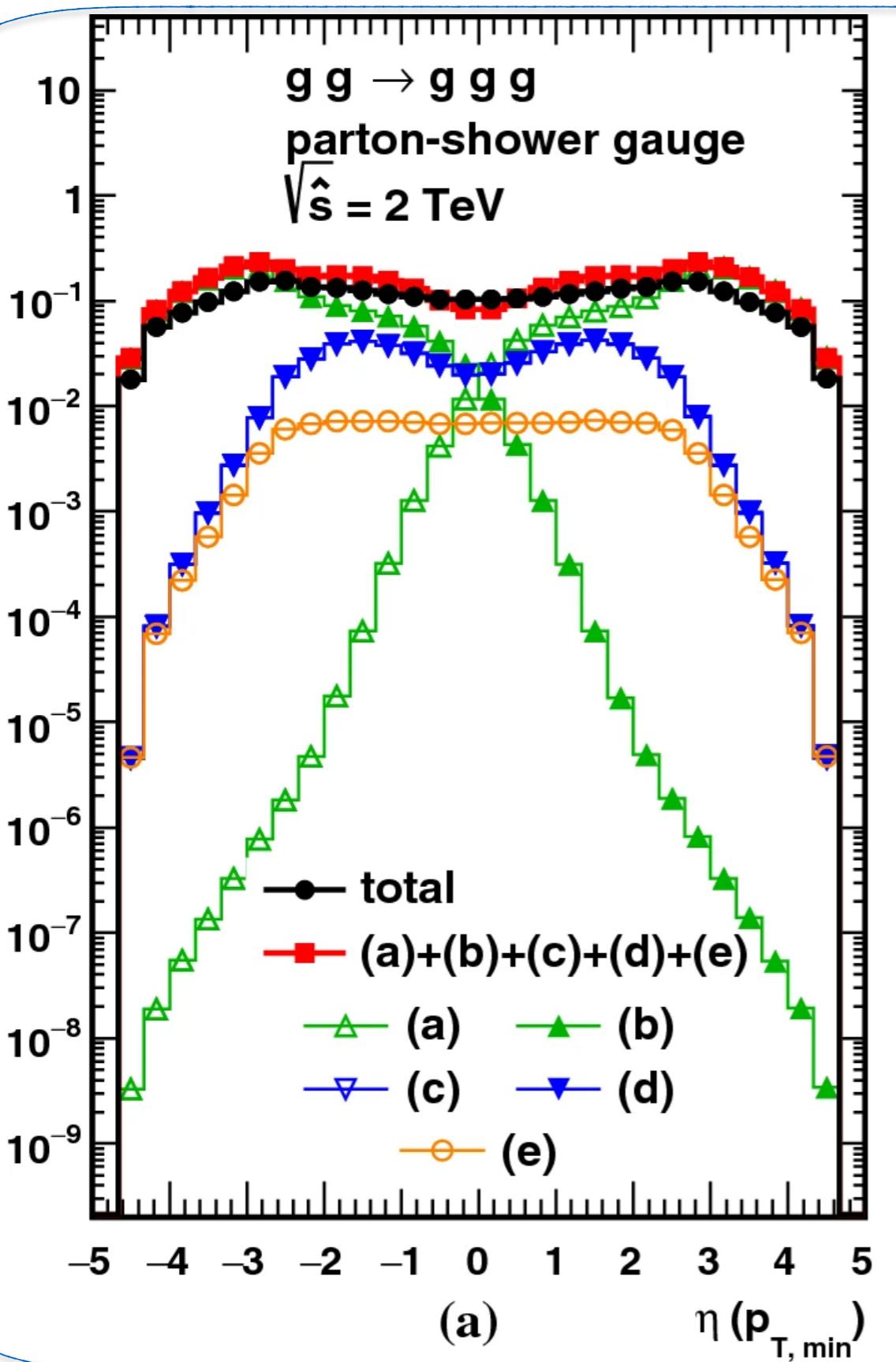
$$= \left\{ \begin{array}{l} e^{-y} (-1, 0, 0, 1) \\ e^{-y} (1, 0, 0, -1) \end{array} \right\} = -\text{sgn}(q^2) \frac{Q n^M}{n \cdot q} \quad \text{when } q^0 > 0$$

and define

$$P_{\mu\nu}^{FD}(\mathbf{q}) = \sum_{h=\pm 1} E_\mu^*(\mathbf{q}, h) E_\nu(\mathbf{q}, h) + \text{sgn}(q^2) \tilde{E}^M(\mathbf{q}, 0) \tilde{E}_\nu(\mathbf{q}, 0) = -g_{\mu\nu} + \frac{q_\mu n_\nu + n_\mu q_\nu}{n \cdot q}$$

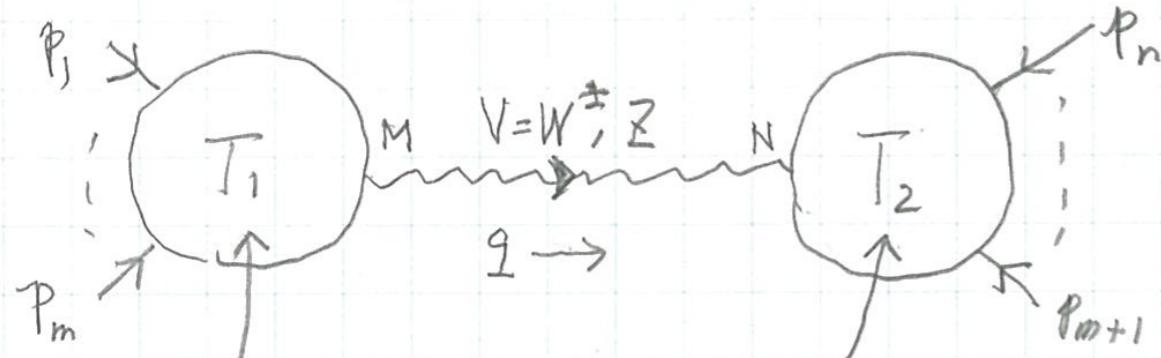
$= q^2 n^\mu n^\nu / (n \cdot q)^2$

with $n^M = (\text{sgn}(q^0), -\frac{\vec{q}}{|q|})$



Distributions of pseudorapidity of the final-state particle with minimum transverse momentum for the process $gg \rightarrow ggg$ in the PS gauge (A) and in the Feynman gauge (B). A line with filled circles denotes the total distribution, while lines with triangles (a–d) and open circles (e) show the distribution of the squared amplitudes of each type of the Feynman diagrams depicted in Fig. 4. A line with filled squares presents the distribution of the sum of the squared amplitudes of each diagram [arXiv:2003.03003, EPJC2020, KH, Kanzaki & Mawatari]

EW (W^\pm & Z of the SM): $U_{\text{gauge}} \Rightarrow F D_{\text{gauge}}$ [2203.10440] Chen-KH-Kanzaki-Manatari



all diagrams with

$$\sum_{K=1}^m p_K^\mu = q^\mu$$

all diagrams with

$$\sum_{K=m+1}^n p_K^\mu = -q^\mu$$

$$= T(p_1, \dots, p_n) = T_1^M \frac{P_V^U(q)_{MN}}{q^2 - m_V^2} T_2^N \quad M=m,4 \quad N=2,4$$

$$P_V^U(q)_{\mu\nu} = -g_{\mu\nu} + \frac{q_\mu q_\nu}{m_V^2} ; \quad P_V^U(q)_{\mu 4} = P_V^U(q)_{4 \nu} = P_V^U(q)_{44} = 0$$

$$\text{BRST: } \begin{cases} q_\mu T_1^\mu = i m_V \bar{T}_1^{\pi_V} \\ q_\nu T_2^\nu = -i m_V \bar{T}_2^{\pi_V} \end{cases} \quad \text{when } q^0 > 0$$

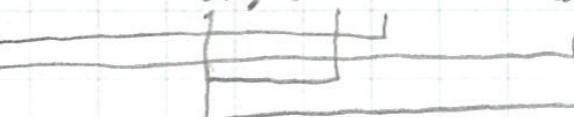
$$P_V^U(q)_{\mu\nu} = -g_{\mu\nu} + \frac{q_\mu q_\nu}{m_V^2}$$

$$= -g_{\mu\nu} + \frac{q_\mu q_\nu}{q^2} + \left(\frac{1}{m_V^2} - \frac{1}{q^2} \right) q_\mu q_\nu$$

$$= \sum_{h=\pm 1} \epsilon_\mu^*(q, h) \epsilon_\nu(q, h) + \text{sgn}(q^2) \epsilon_\mu^*(q, 0) \epsilon_\nu(q, 0) + \frac{q^2 - m_V^2}{m_V^2} \frac{q_\mu q_\nu}{q^2}$$

$$= \sum_{h=\pm 1} \epsilon_\mu^*(q, h) \epsilon_\nu(q, h) + \text{sgn}(q^2) \left[\left(\tilde{\epsilon}_\mu(q, 0) + \frac{q_\mu}{Q} \right) \left(\tilde{\epsilon}_\nu(q, 0) + \frac{q_\nu}{Q} \right) + \frac{q^2 - m_V^2}{m_V^2} \frac{q_\mu q_\nu}{Q^2} \right]$$

Apply BRST identities



The same as QED & QCD

mixing

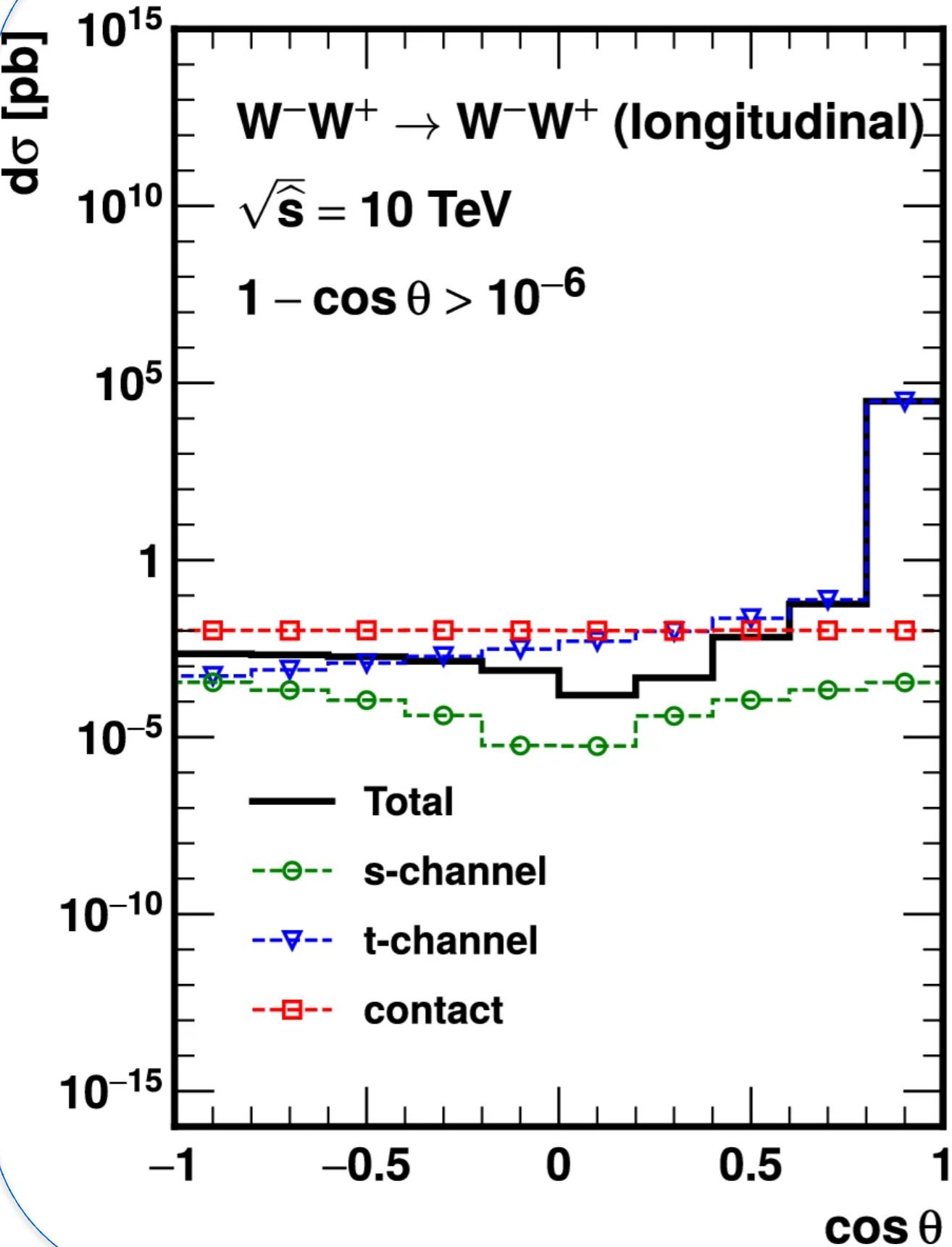
$$T = T_1^M \frac{P_V^U(q)_{\mu\nu}}{q^2 - m_V^2 + i\epsilon} T_2^\nu = T_1^M \frac{P_V^{\text{FD}}(q)_{MN}}{q^2 - m_V^2 + i\epsilon} T_2^N$$

$$\begin{aligned} : (T_1^\mu, T_1^4) &\left(-g_{\mu\nu} + \frac{q_\mu n_\nu + n_\mu q_\nu}{n \cdot q} \quad i m_V \frac{n_\mu}{n \cdot q} \right) (T_2^\nu \\ &\quad - i m_V \frac{n_\nu}{n \cdot q}) \\ T_1^4 &= \bar{T}_1^{\pi_V} \\ \bar{T}_2^4 &= \bar{T}_2^{\pi_V} \end{aligned}$$

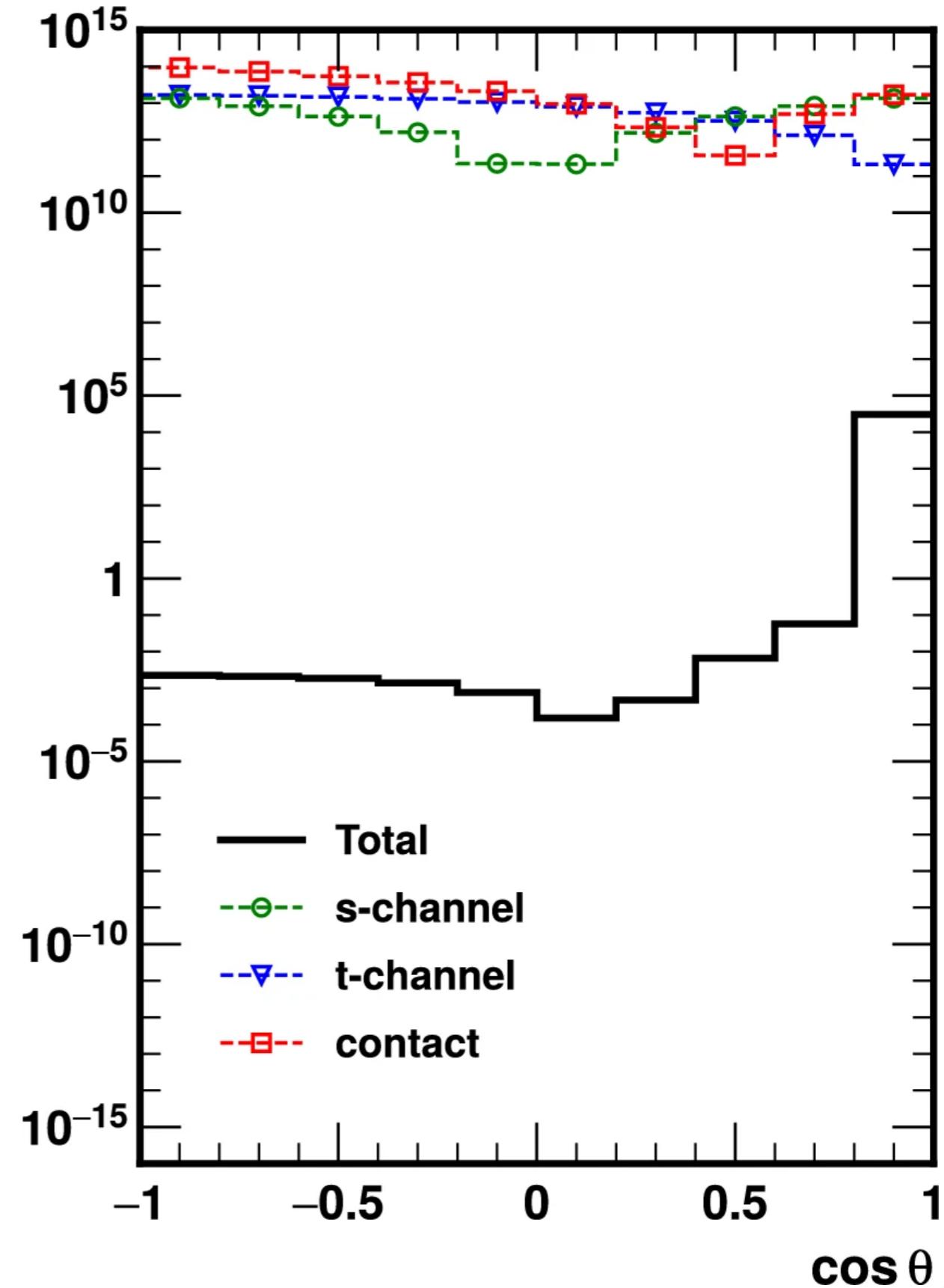
Δ mixing

$\mathbb{E.B.}(\pi_V)$

New HELAS

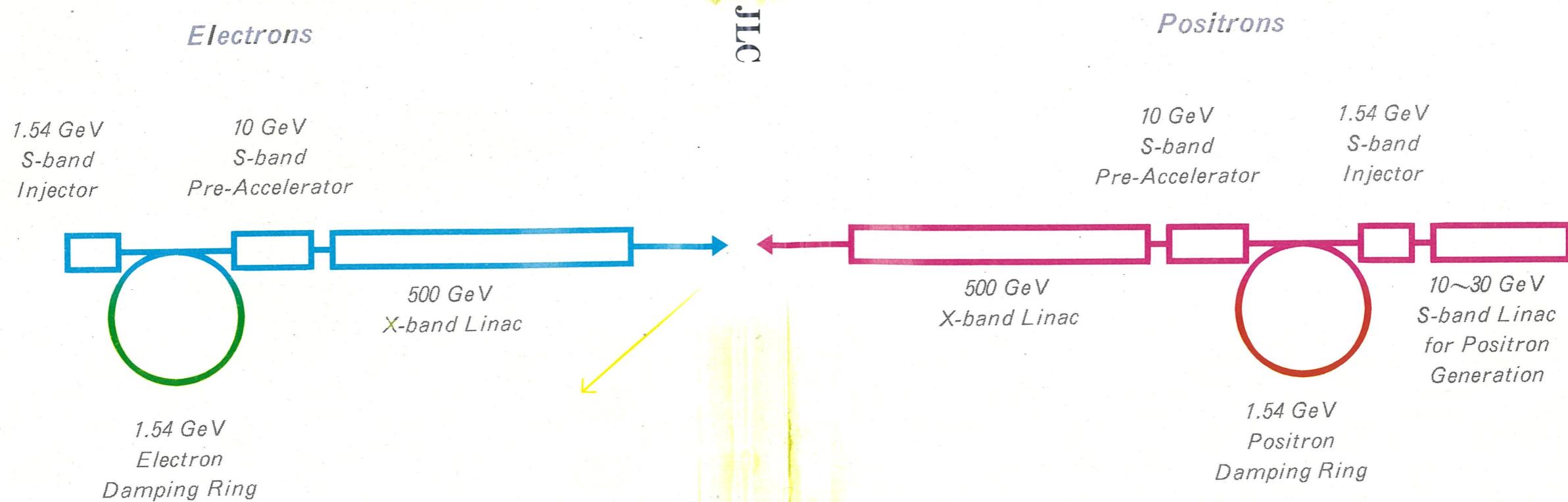


HELAS



Proceedings
of
the Second Workshop
on
Japan Linear Collider
(JLC)

KEK, November 6 - 8, 1990



Togai.



NATIONAL LABORATORY FOR HIGH ENERGY PHYSICS, KEK

JLC Physics

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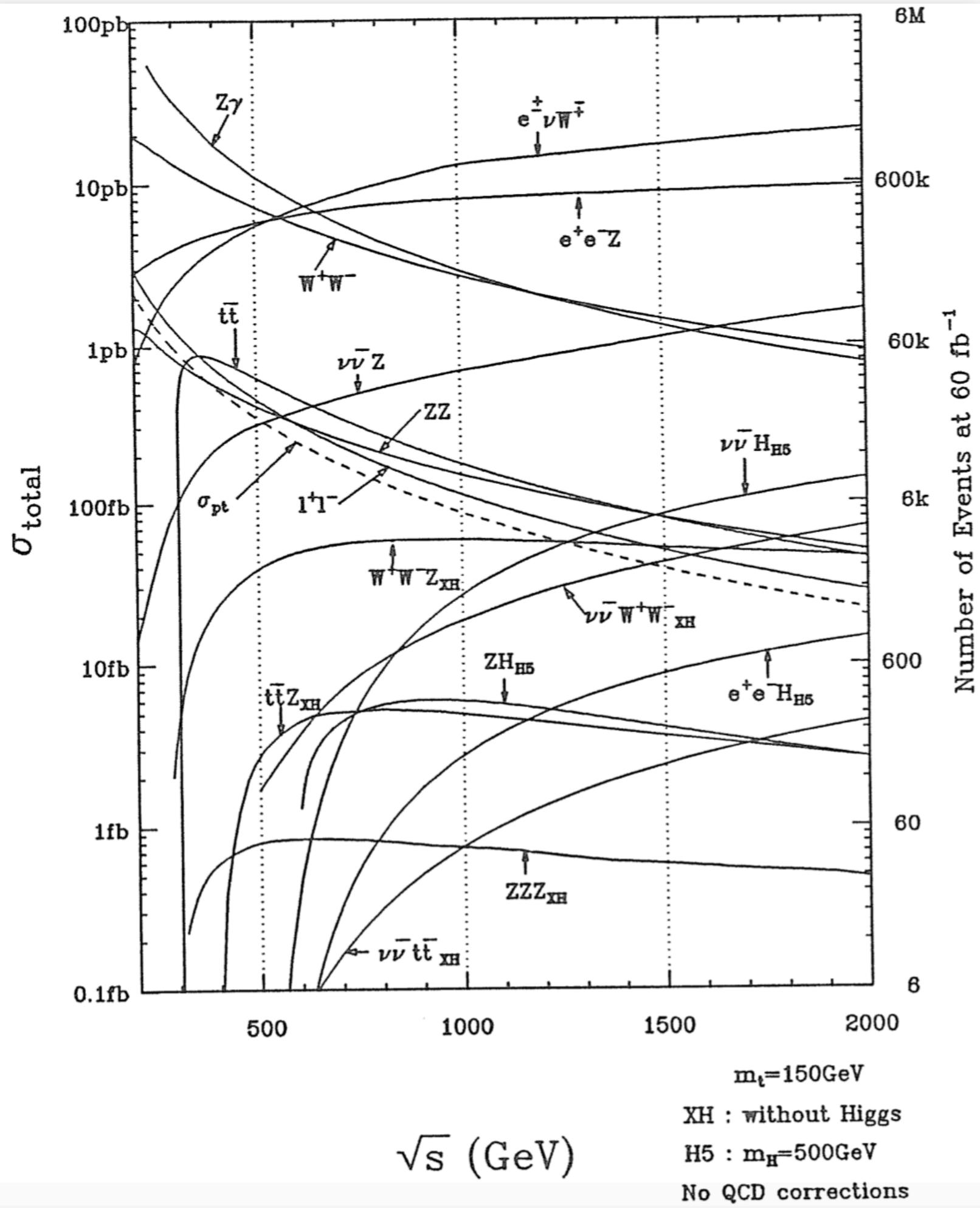
Abstract

We discuss what will be the physics goal of JLC. We briefly summarize our status of electroweak physics. Possible scenarios at and beyond Fermi scale are listed, one is the $SU(2)_L \times U(1)_Y$ gauge theory and the other is the composite scenario. The experimental consequences of each scenarios are discussed. Some suggestions on minimal requirements on the detector and the accelerator to achieve the physics goals are given.

1 Introduction

To my understanding, the aim of this workshop is to discuss the following three points.

1. How we can build JLC.
2. What we can do at JLC.
3. What the *goal* of JLC is.



Top-quark pair production near threshold

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(Received 15 April 1992)

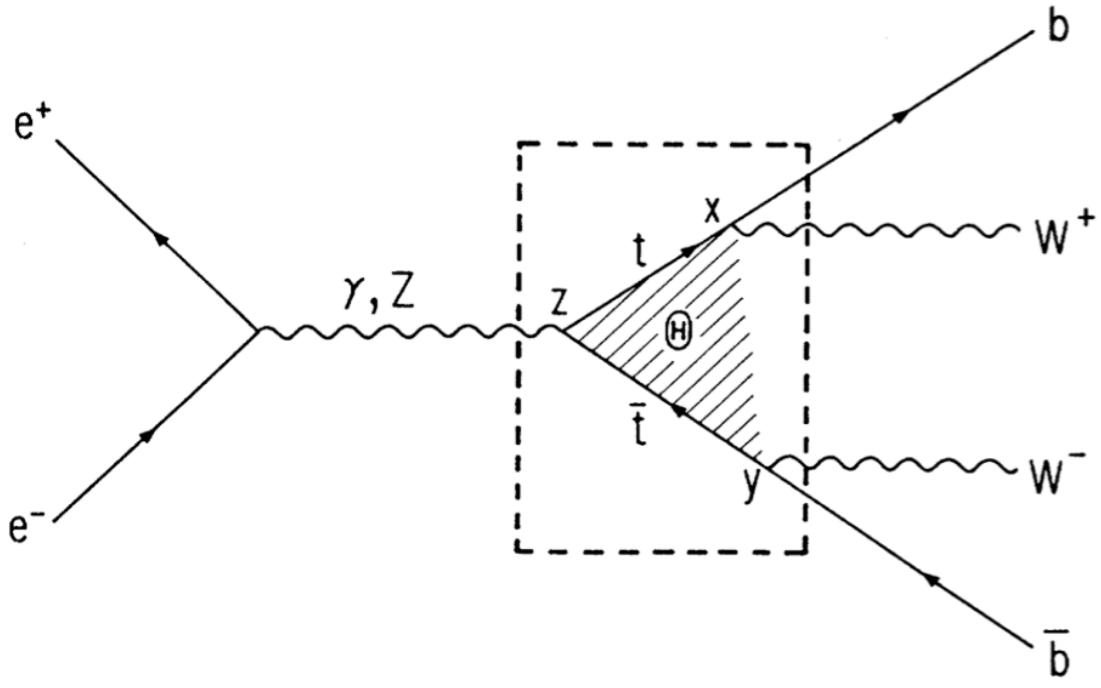


FIG. 1. The diagram for the $t\bar{t}$ pair production process and their subsequent decays into bW 's. The box with the dashed line shows the three-point function $K(x,y,z)$ that carries the information of the toponium resonance.

The nontrivial and interesting part of the process is contained in the three-point Green's function

$$K(x,y,z)_{\alpha\gamma,\delta\beta} = \langle 0 | T t_\alpha(x) \bar{t}_\beta(y) : \bar{t}_\gamma(z) t_\delta(z) : | 0 \rangle , \quad (2.6)$$

which expresses the amplitude where a $t\bar{t}$ pair is created at a space-time point z and the $t(\bar{t})$ quark decays at another point $x(y)$, see Fig. 1. This three-point function contains the effect of full QCD interactions, in the ab-

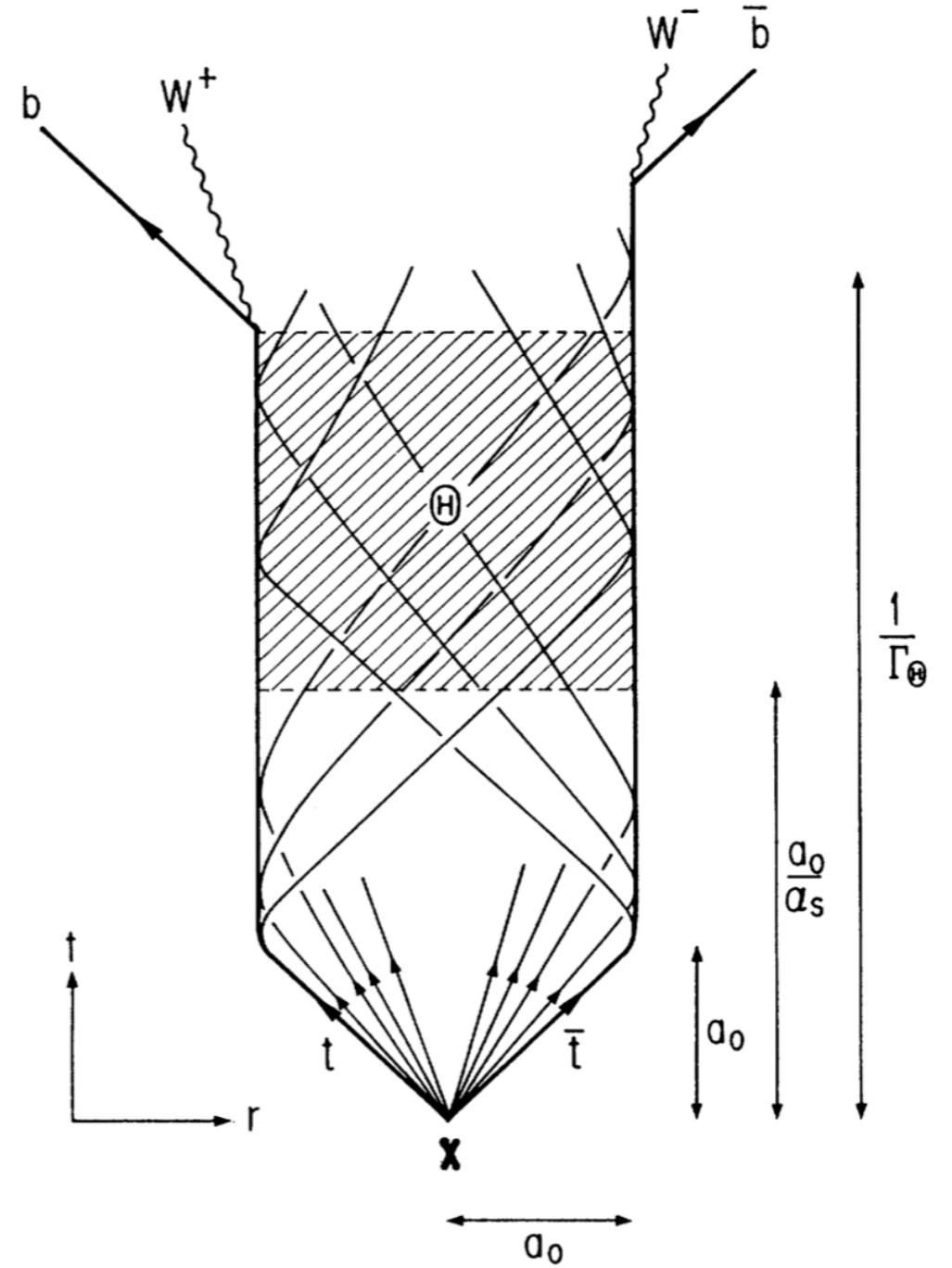
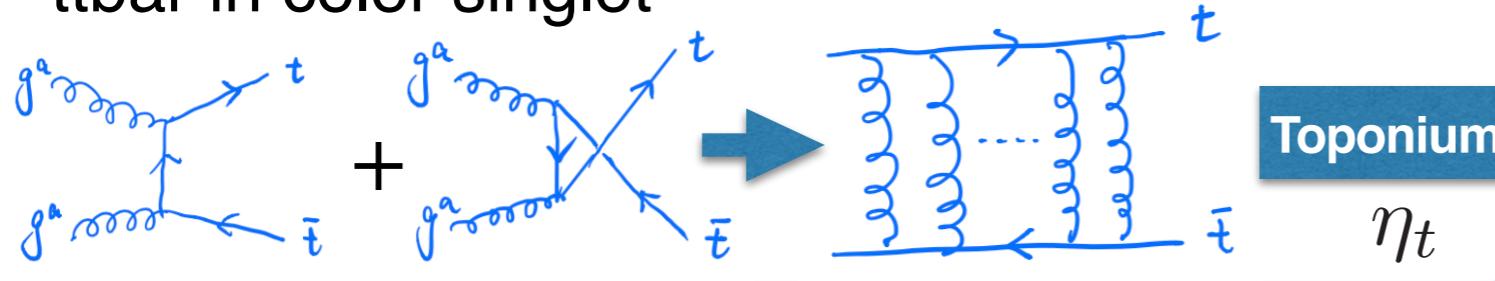


FIG. 2. A figure that shows the time evolution of the non-relativistic $t\bar{t}$ system.

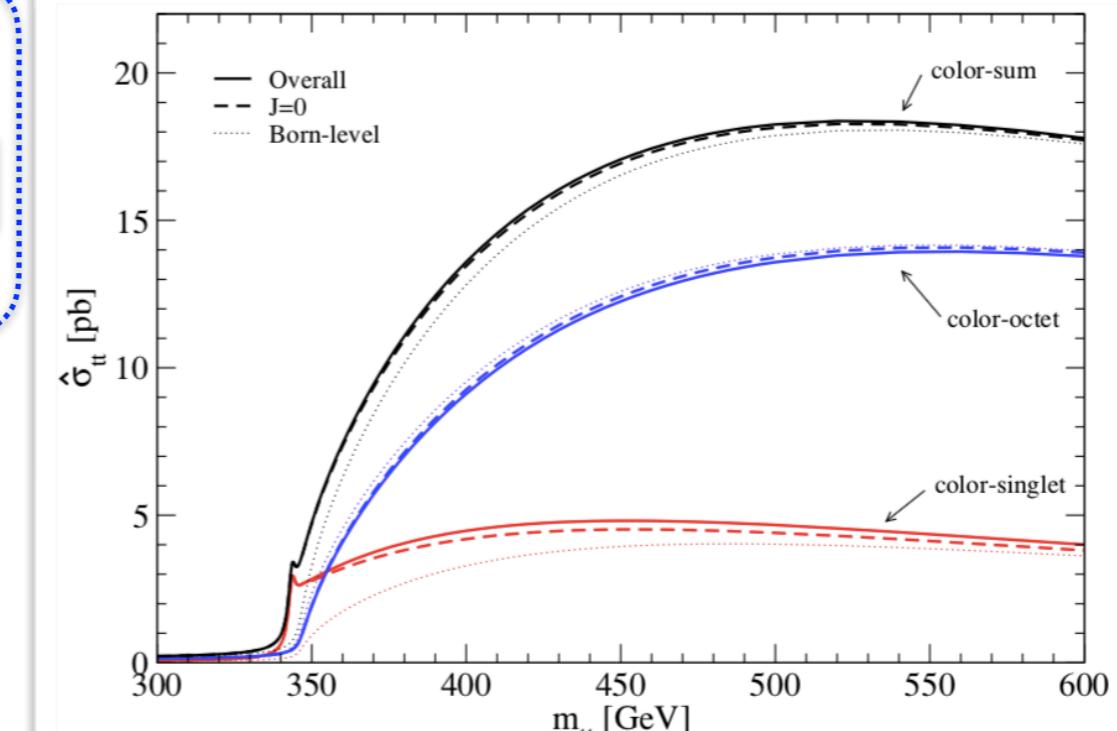
Toponium formation

Production at the LHC

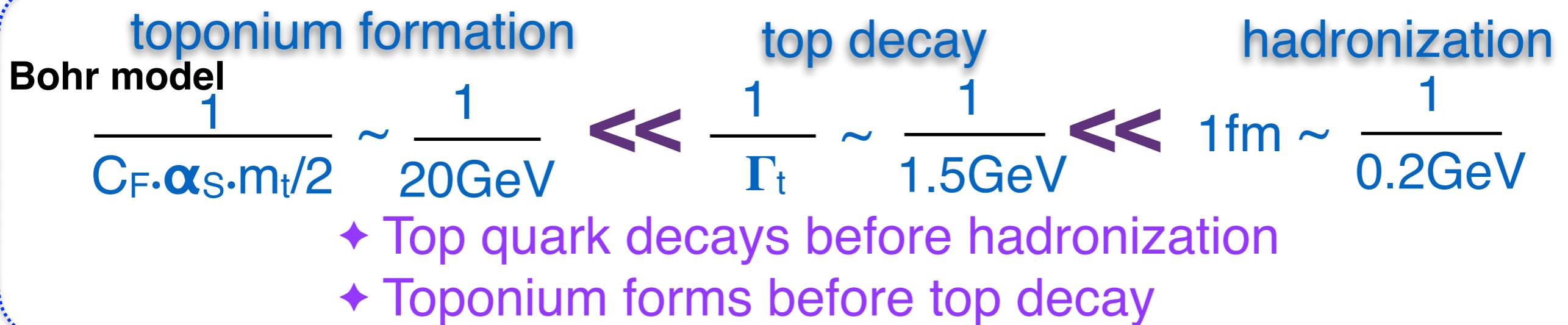
- ttbar in color singlet



- The colour-singlet dominates at the threshold
 - the gg-singlet channel dominates
- The J=0 state dominates
 - $L=S=0$
- The toponium η_t couples to 2 gluons ($C=+$) .

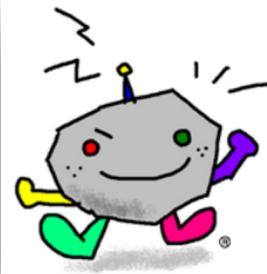


Y.Sumino and H.Yokoya. JHEP 2010

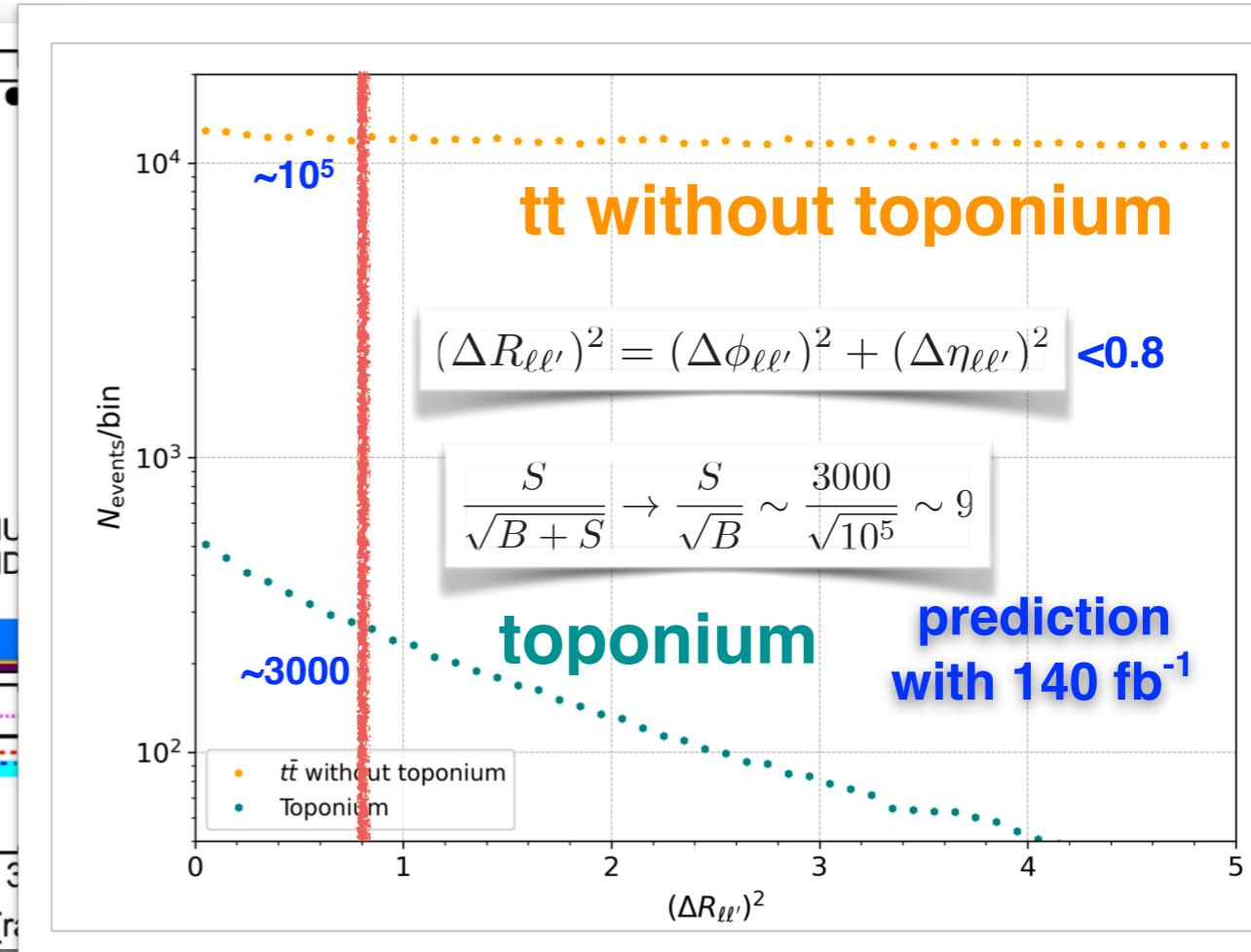
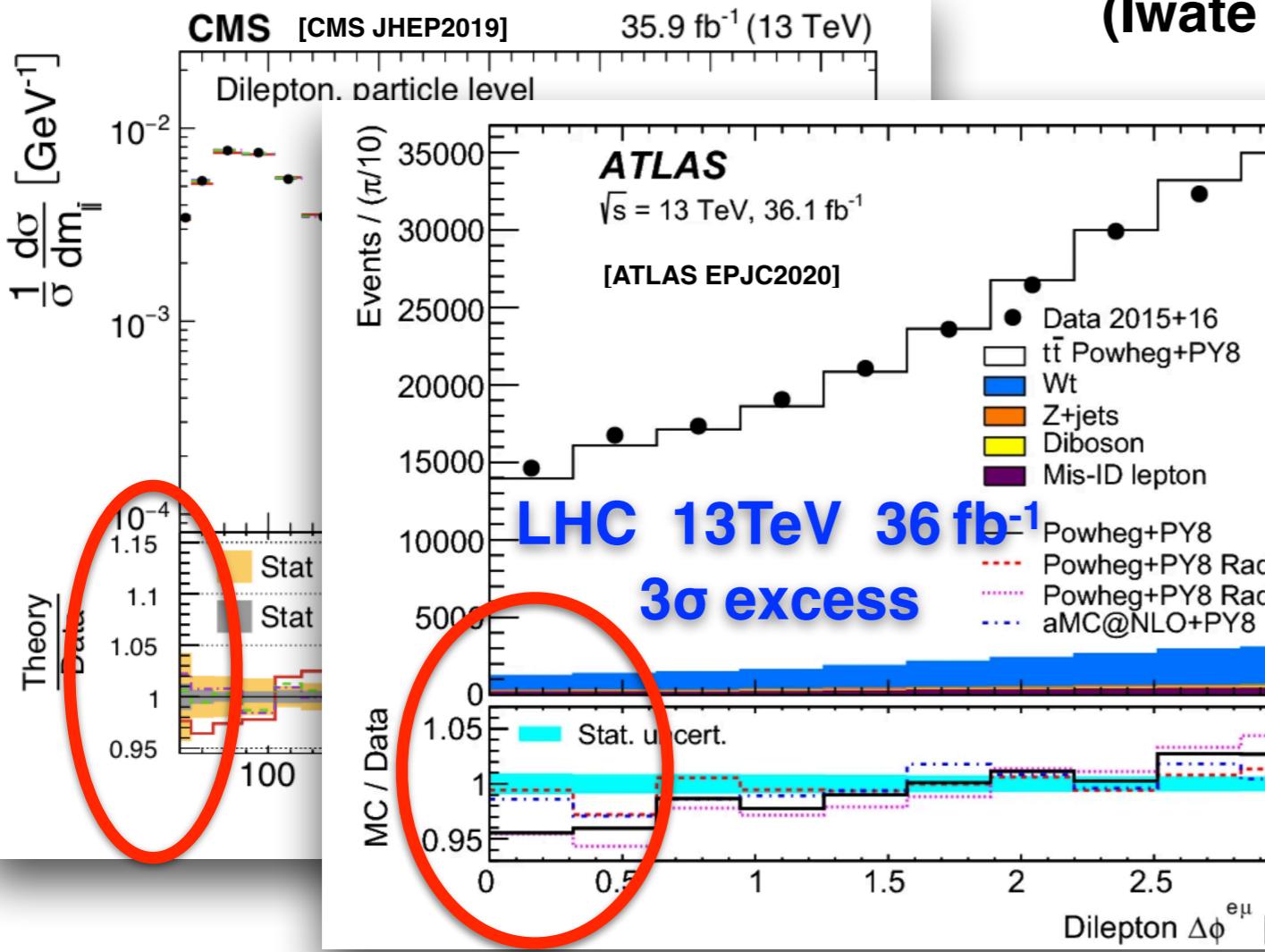




Toponium at the LHC



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- In the ttbar cross section measurement, both ATLAS and CMS observed excess of Data over the 'SM' prediction at low $\phi(l'l')$, $m(l'l')$ bins.
 - This may suggest that either ttbar production MC underestimates dileptons in small angle region, or new physics.
 - The standard ttbar MC does not have toponium.
- We include the toponium effect in the simulation, in the small separation region between the two final state leptons, 9 sigma significance is expected with integrated luminosity 140/fb.

Workshop for Tera-Scale Physics and Beyond, KEK, December 18, 2024

Based on

- [1] Benjamin Fuks, Kaoru Hagiwara, Kai Ma and YJZ, 'Signatures of toponium formation in LHC run 2 data', Phys. Rev.D 104 (2021) 3, 034023.
- [2] Benjamin Fuks, Kaoru Hagiwara, Kai Ma and YJZ, 'Simulating toponium formation signals at the LHC', arXiv:2411.18962.

Excavating the Road to the ILC

A decade ago, our goal was to have the ILC running concurrently with the LHC. Today, I think we need to uncover hints of new physics within the LHC data that could guide future explorations at the ILC.

A Lesson from the Toponium ‘Discovery’ at the LHC

New physics can easily be obscured by subtle adjustments to SM event simulation programs, particularly if we assume that "nothing beyond the SM is within reach."

Instead, we should adopt the opposite bias: assume that new physics is hiding within the data—from the LHC, flavor physics experiments, and precision measurements—and actively seek evidence for it.

The key question is: **How do we look for this evidence?**

It may be our imagination that paves the way to the ILC.