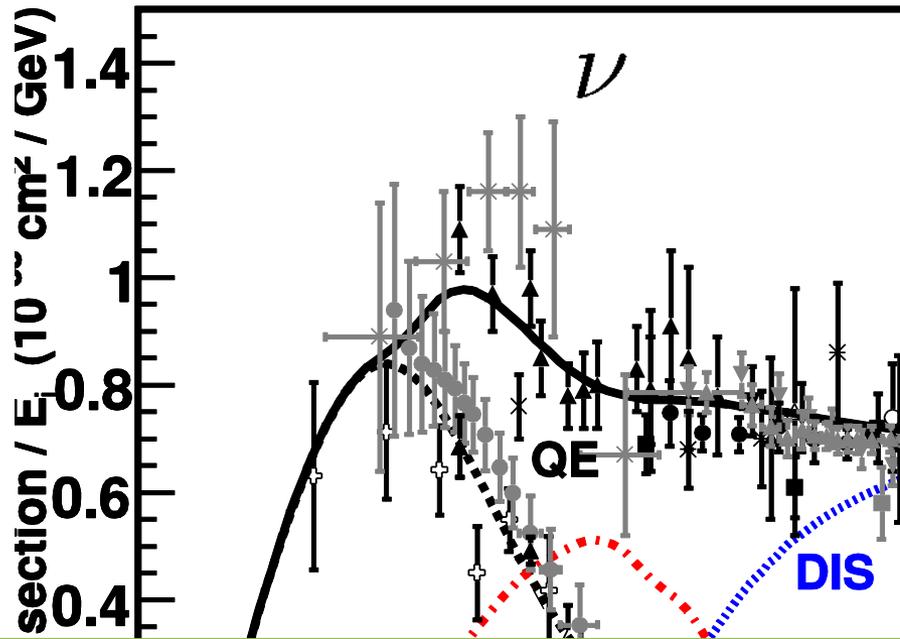


ν -Deuteron Reactions In the $\Delta(1232)$ Region

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σ_{Tot} of BNL Neutrino Experiments

J.A.Formaggio G.P.Zeller
RMP84(2012)

Resonance (RES) Excitation is dominated by $\Delta(1232)$ at 1-3 GeV



A necessary task for neutrino experiments at few-GeV:

Develop theoretical models for calculating the nuclear effects in the $\Delta(1232)$ region

A necessary task for neutrino experiments at **few-GeV**:

Our approach:

1. Construct a model for the **electroweak** excitation of the $\Delta(1232)$ to describe :
 - a. data on the proton target
 - b. data on the **deuteron** target (This talk)
 determine cross sections on the **neutron**

2. Apply the constructed model to calculate nuclear effects by using
 - a. multiple-scattering theory for deuteron (This talk)
 - b. The Δ -hole model for heavy nuclei

Nakamura, Sato, Lee, Szczerbinska, Kubodera, PR C81,035502 (2010)

Excitation of $\Delta(1232)$ is dominated by single pion production



Need a model to describe the data of :

$$\gamma + p \rightarrow \pi^0 + p$$

$$\gamma + p \rightarrow \pi^+ + n$$

$$\gamma + n \rightarrow \pi^0 + n$$

$$\gamma + n \rightarrow \pi^- + p$$

$$e + p \rightarrow e' + \pi^0 + p$$

$$e + p \rightarrow e' + \pi^+ + n$$

$$e + n \rightarrow e' + \pi^0 + n$$

$$e + n \rightarrow e' + \pi^- + p$$

$$\nu + p \rightarrow l^- + \pi^+ + p$$

$$\nu + n \rightarrow l^- + \pi^0 + p$$

$$\nu + n \rightarrow l^- + \pi^+ + n$$

$$\bar{\nu} + n \rightarrow l^+ + \pi^- + n$$

$$\bar{\nu} + p \rightarrow l^+ + \pi^0 + n$$

$$\bar{\nu} + p \rightarrow l^+ + \pi^- + p$$

Achieved by the **SL Model** (1996-2005)

Nucleon target :

T. Sato , T.-S. H. Lee, Phys. Rev. C 54, 2660 (1996)

T. Sato, T.-S. H. Lee, Phys. Rev. C 63, 055201 (2001)

T. Sato, I. Uno, T.-S. H. Lee, Phys, Rev. C67,065201 (2003)

I. Uno, T. Sato, T.-S. H. Lee, Phys. Rev. C72, 025204 (2005)

Deuteron target:

K. Hafidi, T.-S. H. Lee, Phys. Rev. C (2001)

J. Wu, T. Sato, T.-S. H. Lee, Phys. Rev. C 91, 035203 (2014)

Approach of SL model:

Apply the **Osaka** unitary transformation method

M. Kobayashi, T.Sato, H.Ohtsubo, Prog. Theor. Phys. 98 927 (1997)



Construct an **energy independent** Hamiltonian with π , N, Δ hadronic degrees of freedom from phenomenological **Lagrangians** of relativistic quantum field theory

SL Model

(Sato, Lee, PR C 54, 2660 (1996);C63,055201 (2001))

$$H'_1 = \boxed{v_{\pi N, \pi N}} + h_{\Delta, \pi N} + v_{\pi N, \gamma N} + h_{\Delta, \gamma N}$$

Determined by
 $\pi N \rightarrow \pi N$
 $\gamma N \rightarrow \pi N$
 $N(e, e' \pi) N$

Meson-exchange

$$\langle \Delta | J^{em} | N \rangle$$

Determined by data

Solve

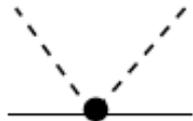
$$T_{ab}(E) = V_{ab} + \sum_c V_{ac} G_c(E) T_{cb}(E)$$

a, b, c = $\pi N, \gamma N$

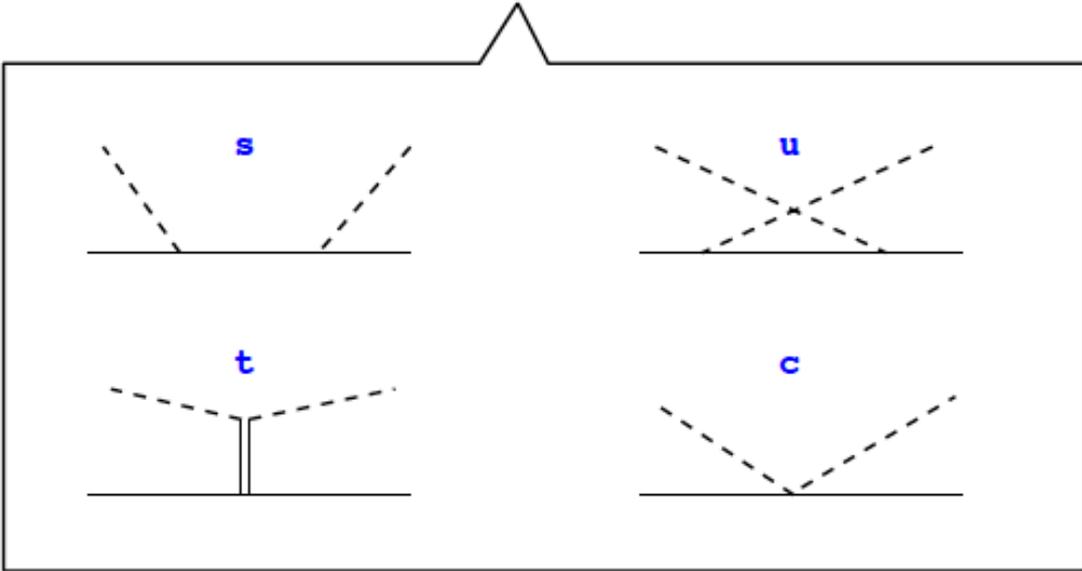
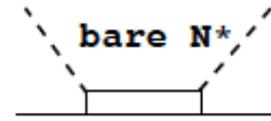
only Δ

V_{ab}

=

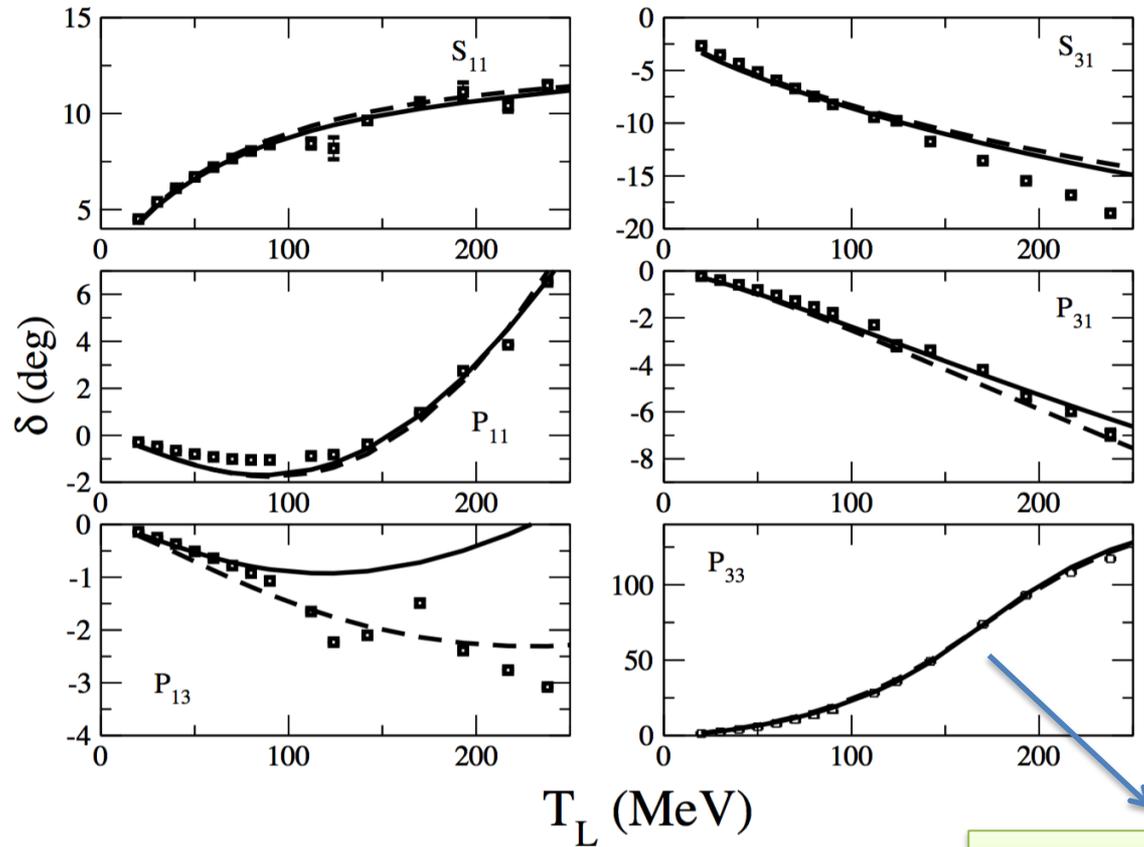


+



Procedures:

- Fit $\pi N \rightarrow \pi N$ phase shift



$\Delta \rightarrow \pi N$ is determined

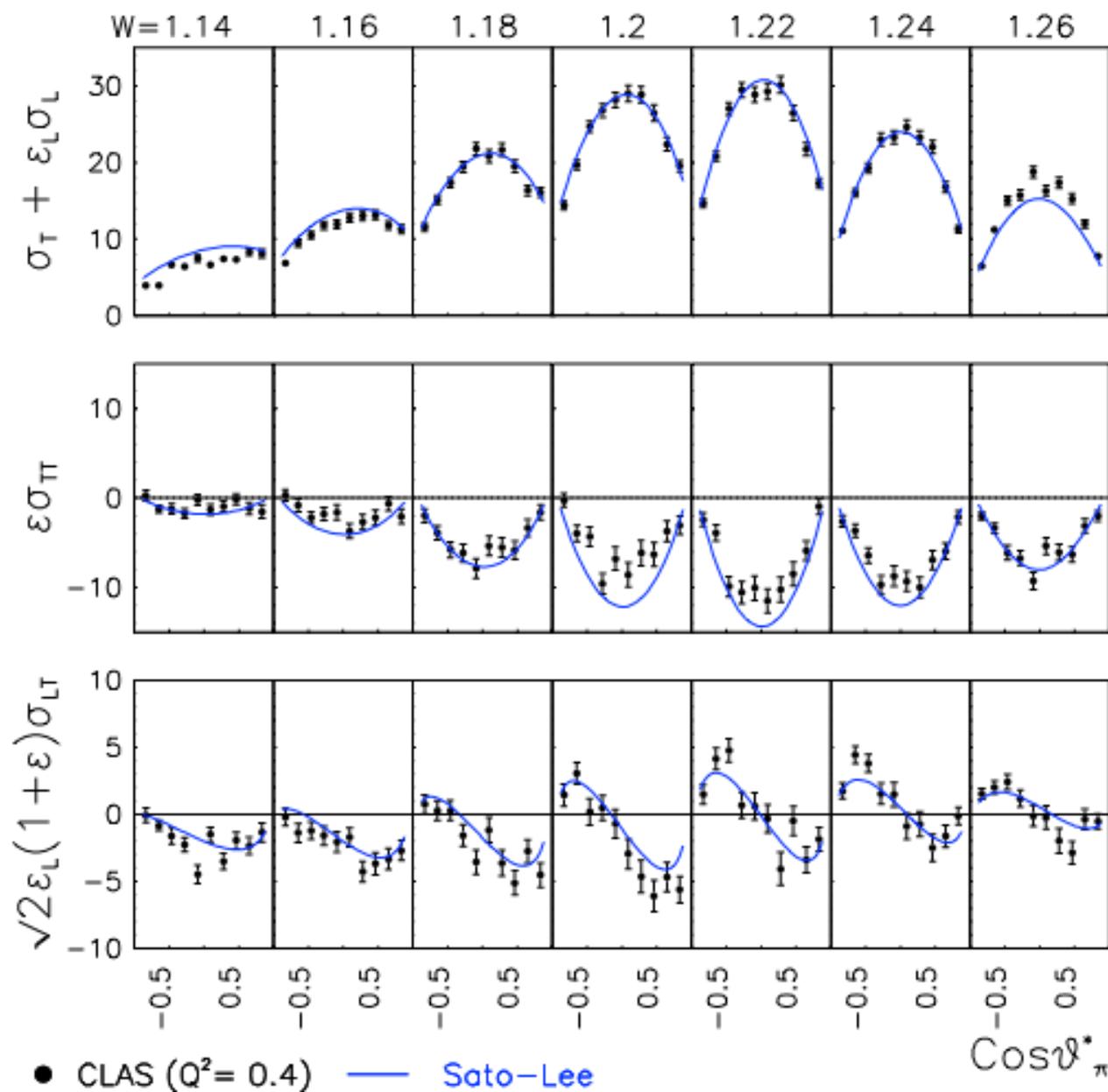
Procedures:

- Fit $\gamma N \rightarrow \pi N$, $N(e, e' \pi)N$ data



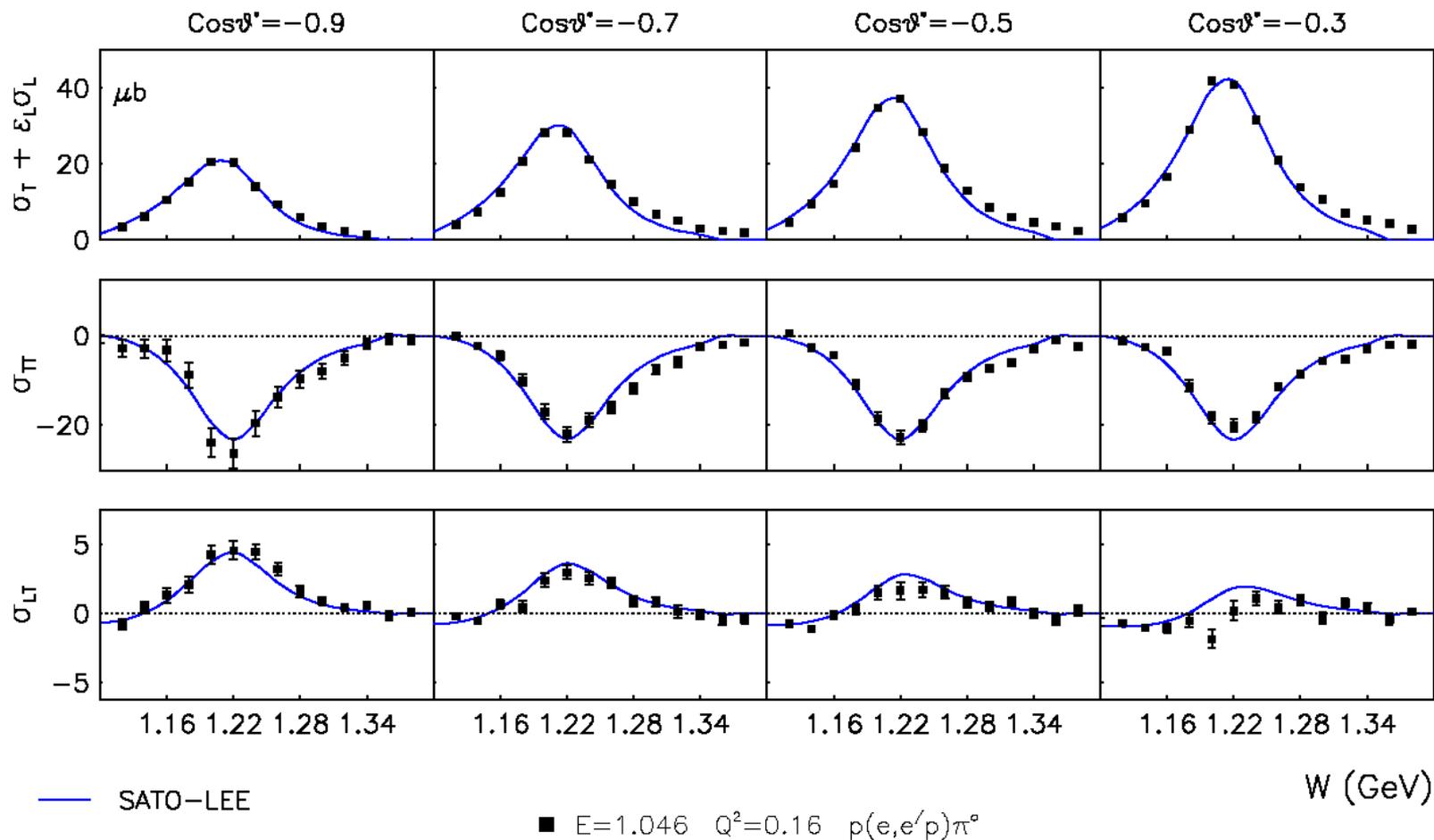
$\Delta \rightarrow \gamma N$ form factors are determined

Structure functions of $p(e, e' \pi^0) p$

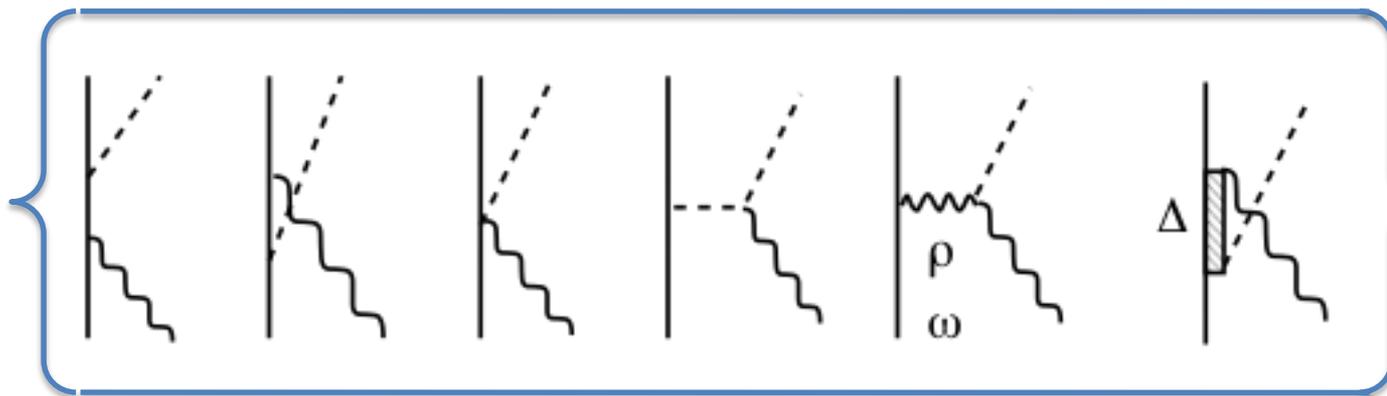
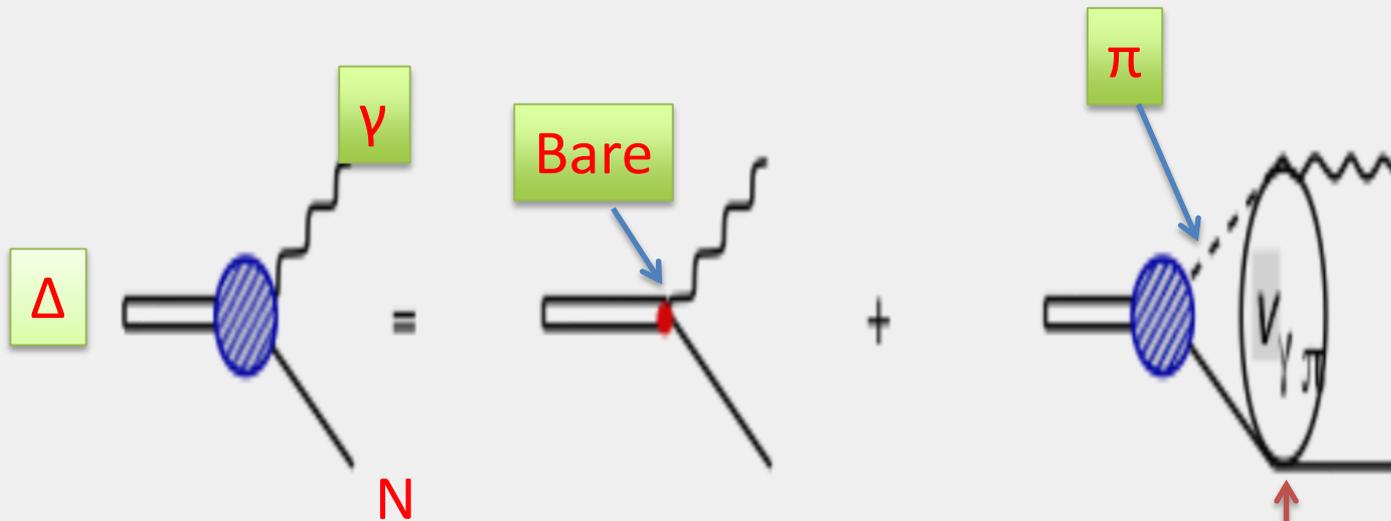


Pion electroproduction Structure functions

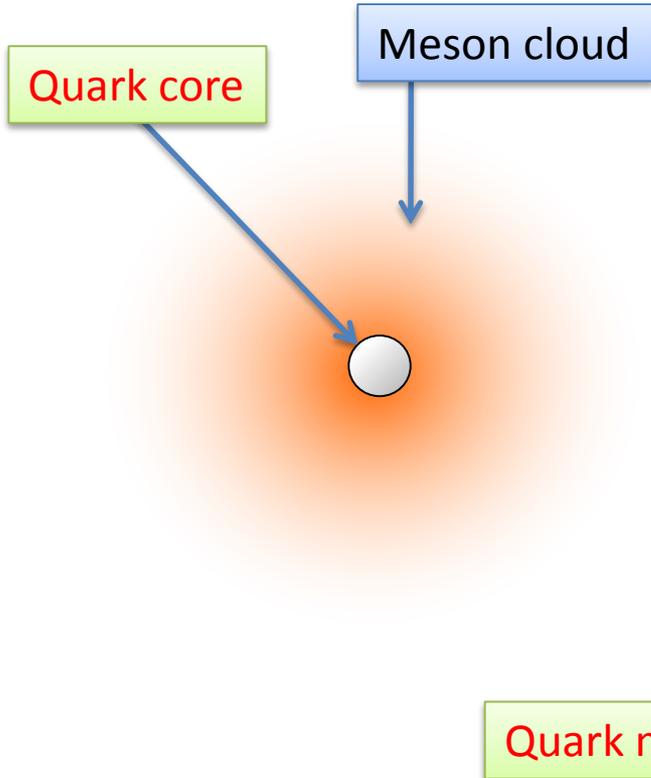
(data CLAS from C. Smith, 2004)



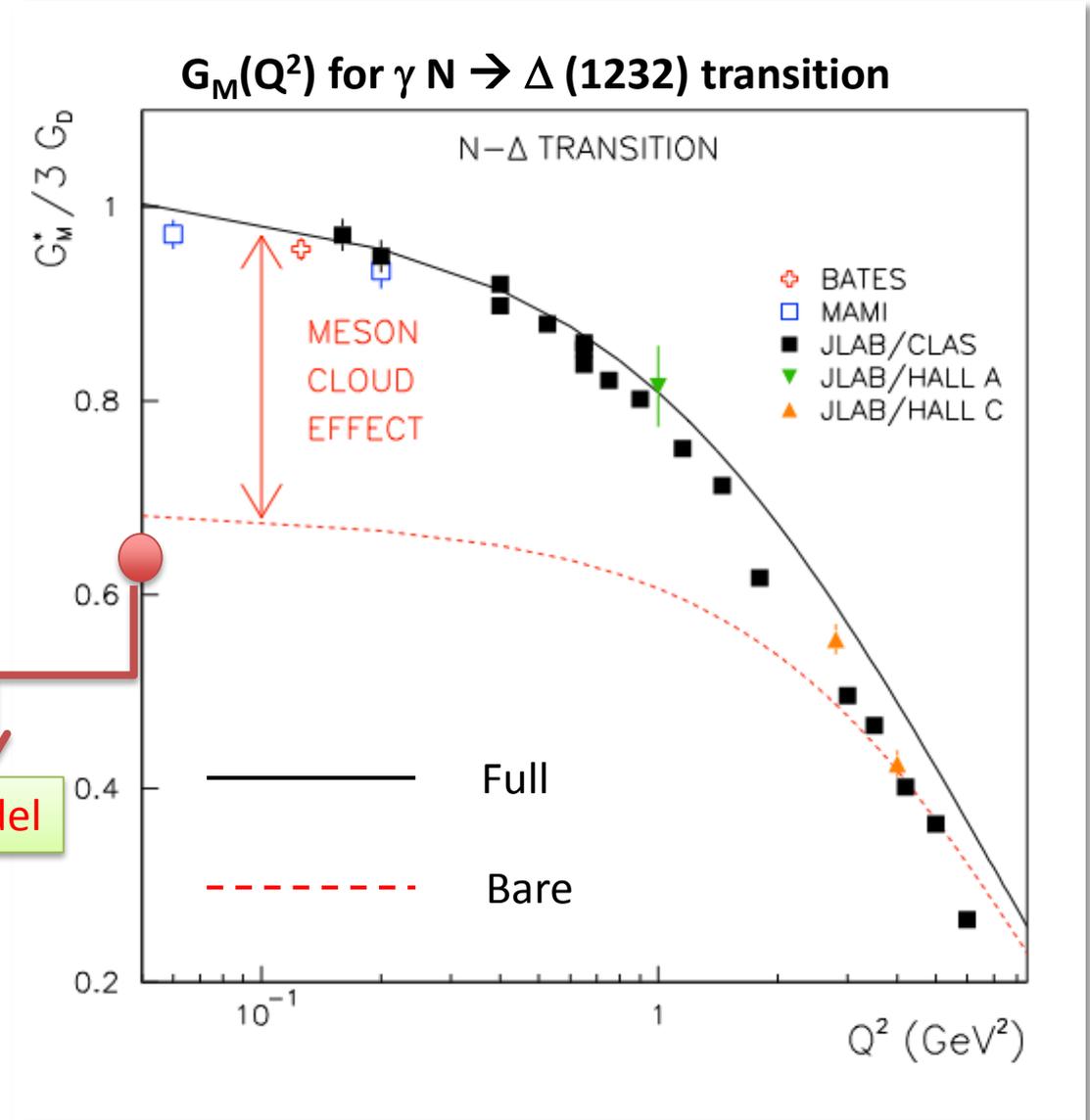
$\Delta \rightarrow \gamma N$ Form factor



Meson cloud effect in $\gamma N \rightarrow \Delta(1232)$ form factors



Note:
Most of the available static hadron models give $G_M(Q^2)$ close to “Bare” form factor.



Extend SL Model to include J^{CC} and J^{NC}

- Charged current

$$J^{CC} = (V^1 + i V^2) - (A^1 + i A^2)$$

- Neutral current

$$J^{NC} = (1 - 2\sin^2\theta_w) J^{em} - V_{\text{isoscalar}} - A^3$$

Objective:

Extract $N - \Delta$ axial form factors from

- $N(\nu, \mu \pi)$ reactions
- Parity-violating asymmetry of inclusive $N(e, e')$

Procedures:

- Charged current

$$J^{\text{CC}} = (V^1 + i V^2) - (A^1 + iA^2)$$

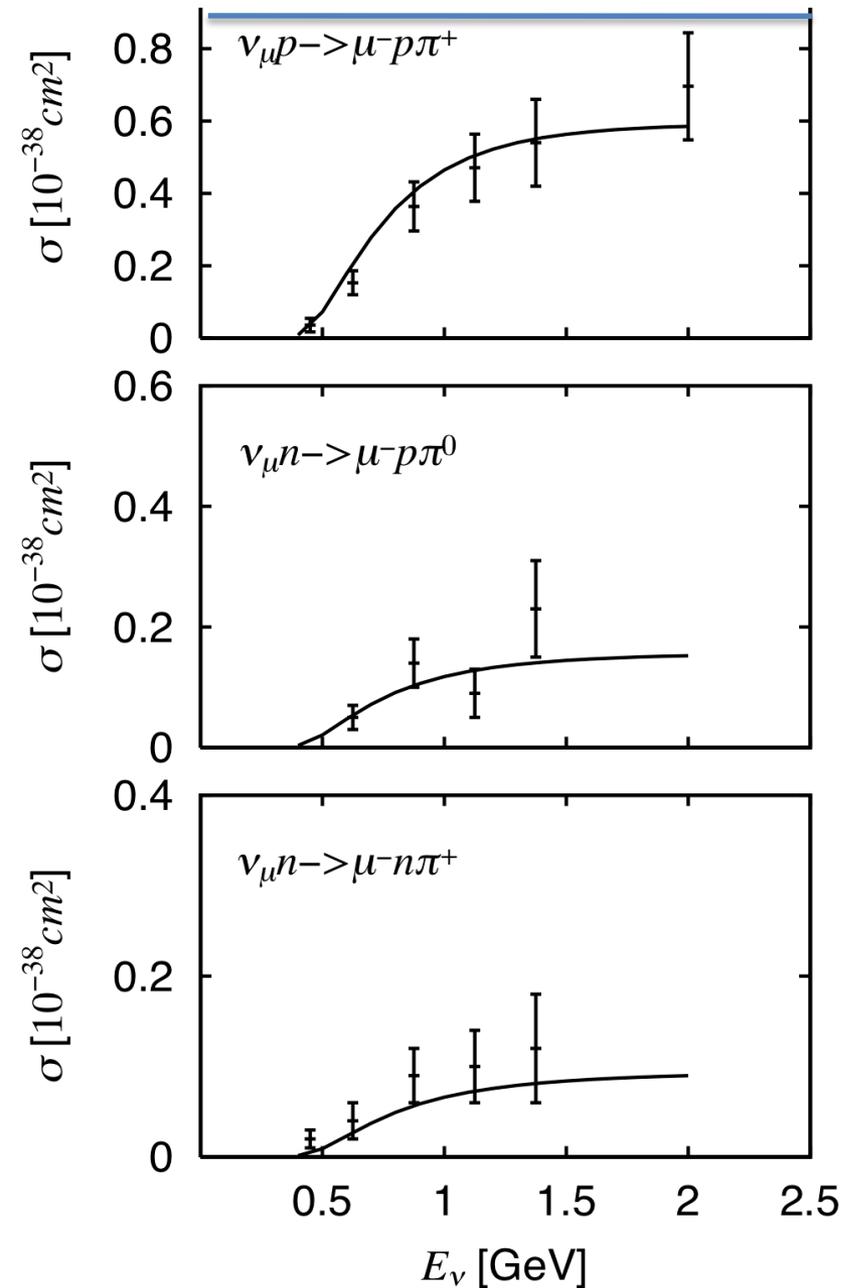
determined in $(e, e' \pi)$

- **Non-resonant** axial current (A^1, A^2, A^3) are **derived** from effective Lagrangians

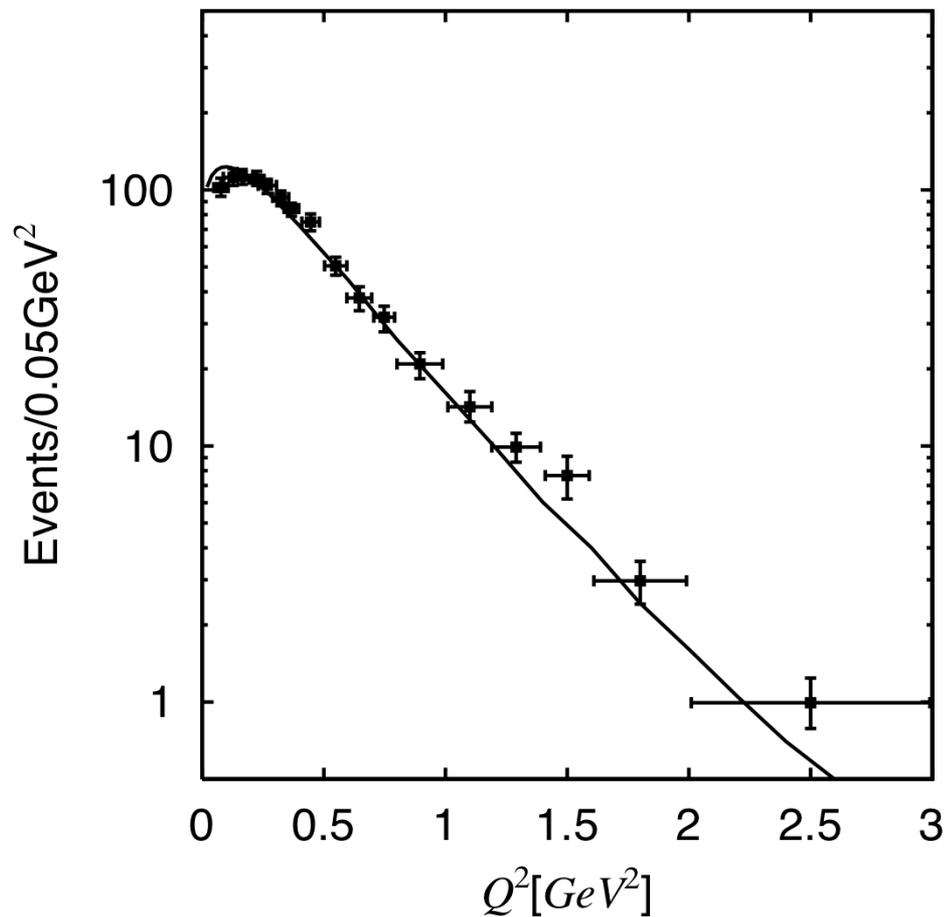


Adjust $G_{N,\Delta}^A(Q^2) = \langle \Delta | (A^1 + iA^2) | N \rangle$ to fit $N(\nu, \mu \pi)$ data

ν -N Total cross sections



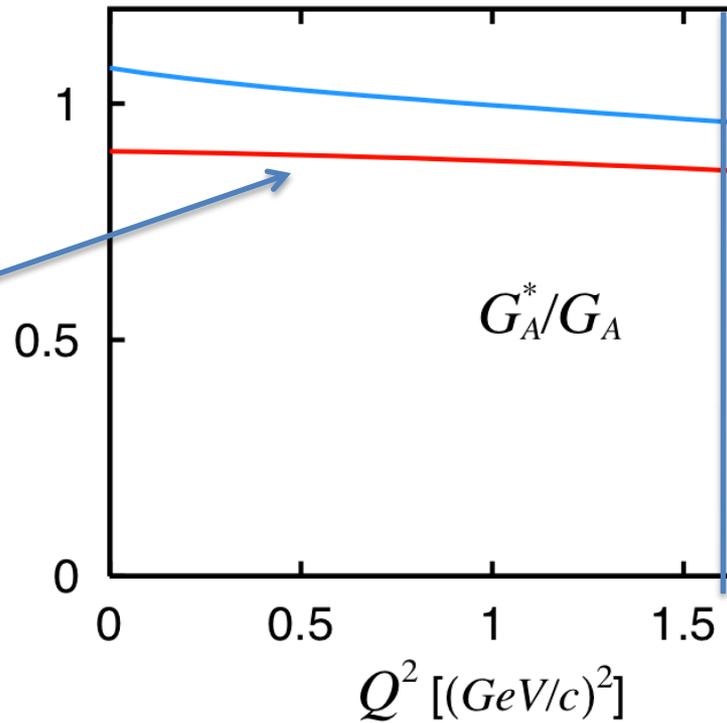
Sato, Uno, Lee, PR C67,065201(2003)



$d\sigma/dQ^2$ of $p(\nu, \mu^- \pi^+)$

$G_{N,\Delta}^A(Q^2) = \langle N | A^1 + iA^2 | \Delta \rangle$ is determined

Bare $\langle N | A^{CC} | \Delta \rangle$



Neutral current

$$J^{\text{NC}} = (1 - 2\sin^2\theta_w) J^{\text{em}} - V_{\text{isoscalar}} - A^3$$

determined in $(e, e' \pi)$



Test A^3 and $G_{N,\Delta}^A(Q^2)$ by Parity-violating inclusive $N(e, e')$

Experimental test (2011) of SL prediction (2005)

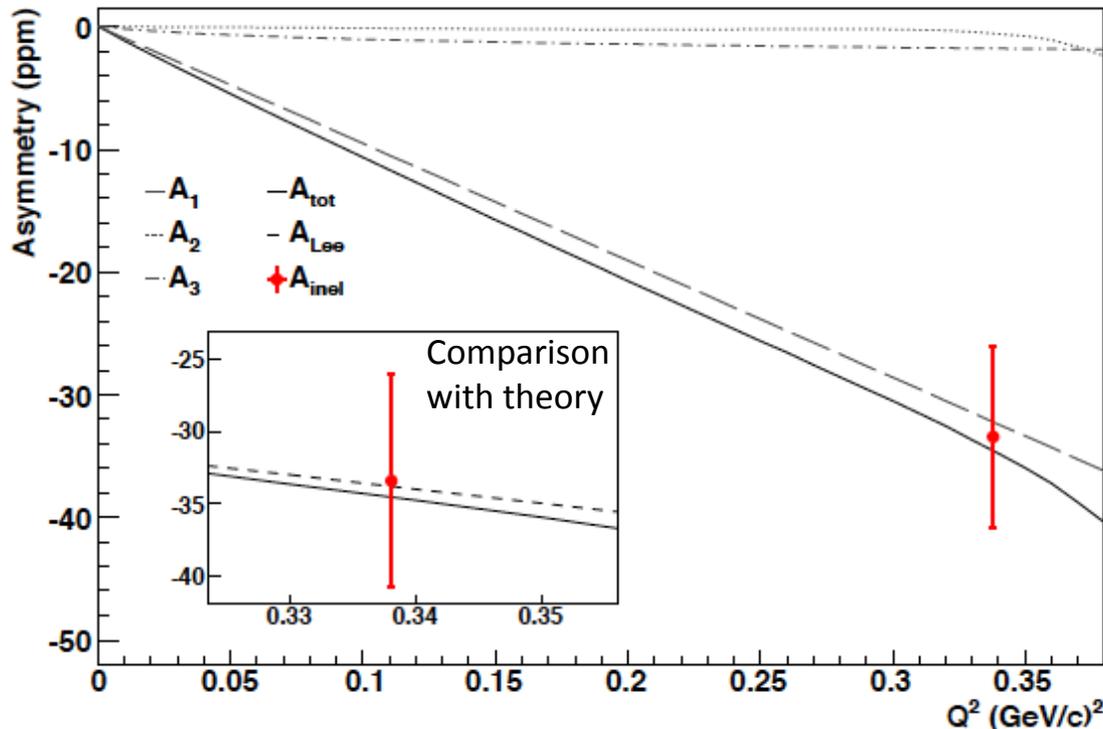
Electron data : parity violation asymmetry

G⁰@JLab, arXiv:1212.1637

$$A = \frac{d\sigma_R - d\sigma_L}{d\sigma_R + d\sigma_L}$$

Exp :

$$G_{N\Delta}^A(Q^2) = -0.05 \pm (0.35)_{\text{stat}} \pm (0.34)_{\text{sys}} \pm (0.06)_{\text{th}}$$



$$G_{N\Delta}^A(Q^2) = -0.196$$

SL model prediction (2005)

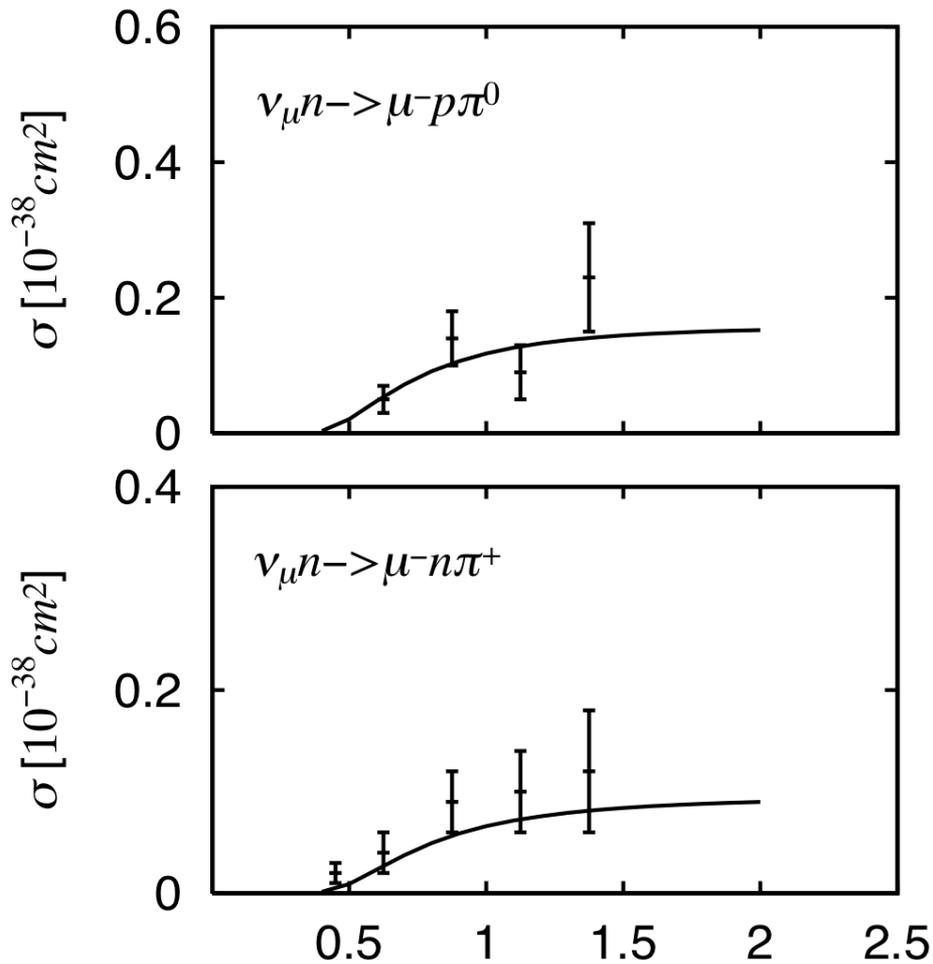
SL Model can describe almost all available data of electroweak pion production in the $\Delta(1232)$ region



It can be used to calculate the nuclear effects to analyze neutrino experiments

But

the predicted amplitudes on **neutron** are not well checked

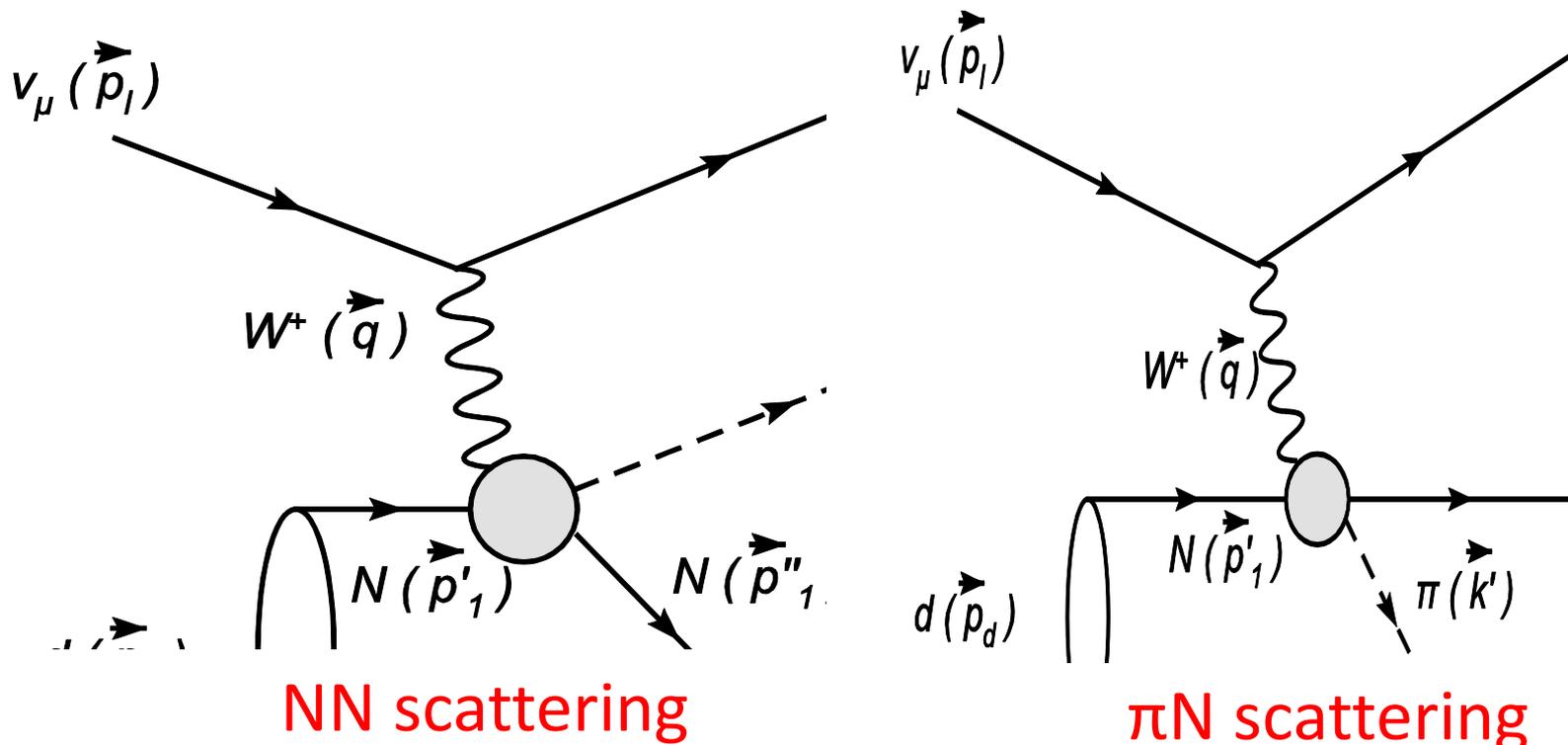


From data on **deuteron**

SL model does not describe the data on **neutron** well

Possible reason:

Previous analysis of data on deuteron target **did not** include final π NN interaction



Need to study final state interaction (**FSI**) effects

Study of FSI using **SL model**:

1. $d(e, e' \pi^+) pp$: search for pion excess in nuclei

K. Hafidi, T.-S. H. Lee, Phys. Rev. C (2001)

2. $\gamma + d \rightarrow \pi \ n p, \ \pi \ p p$
 $\nu + d \rightarrow \mu \ \pi \ p p, \ \mu \ \pi \ n p$ }

J. Wu, T. Sato, T.-S. H. Lee, Phys. Rev. C 91, 035203 (2014)

Motivated by the neutrino experiments

Approach:

Apply the multiple scattering theory to calculate γ_d and ν_d reaction amplitudes from a Hamiltonian with N , π and Δ

Model Hamiltonian with N, π, Δ

$$H = H_0 + H'_1 + H'_2 + J^{CC} + J^{NC}$$

$$H'_2 = V_{NN,NN} + V_{N\Delta,NN} + V_{N\Delta,N\Delta}$$

$$H'_1 = v_{\pi N,\pi N} + h_{\Delta,\pi N} + v_{\pi N,\gamma N} + h_{\Delta,\gamma N}$$

Lee, Matsuyama (1985-1992)

Determined by
 $\pi N \rightarrow \pi N$
 $NN \rightarrow NN, \pi NN$

Determined by
 $\gamma N \rightarrow \pi N$
 $N(e, e'\pi) N$

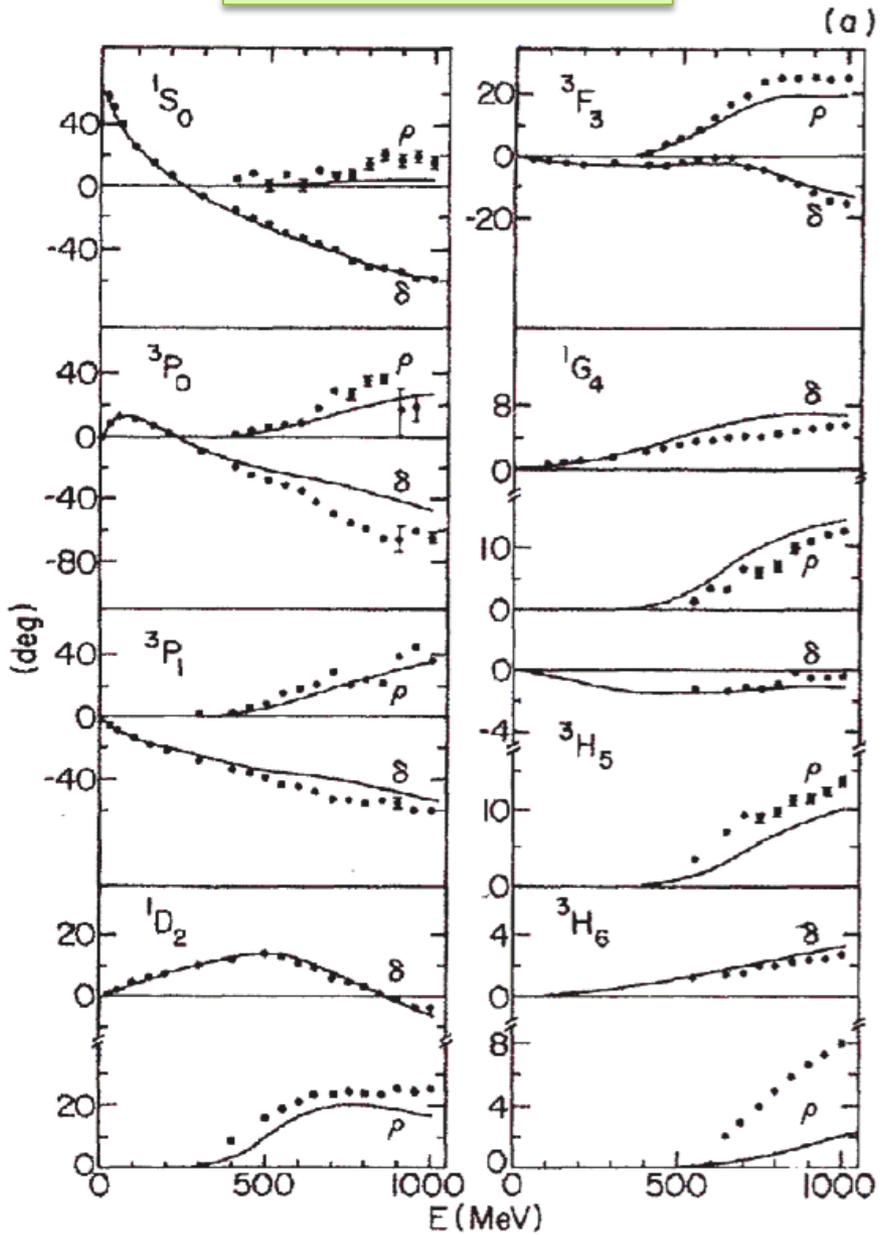
Sato, Lee (1996-2001)

$J^{CC} + J^{NC}$

Determined by $\nu N \rightarrow \mu \pi N$

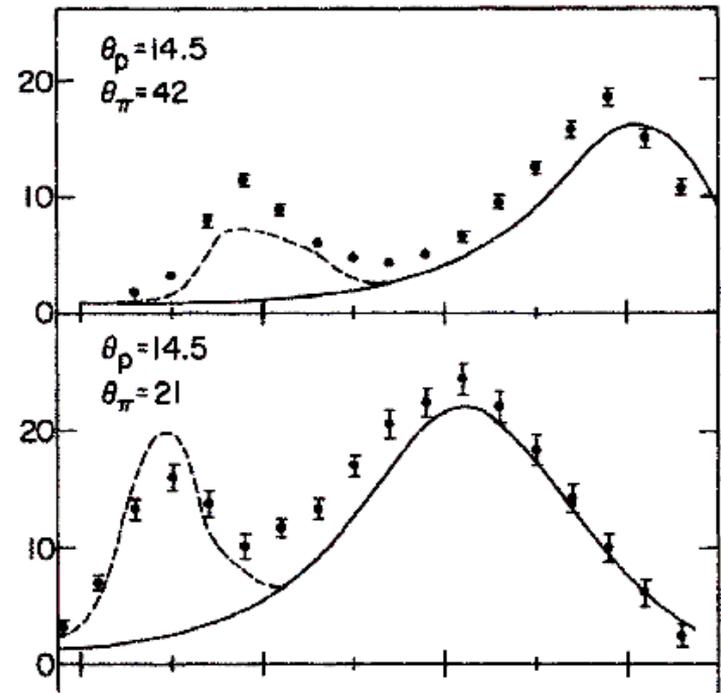
Sato, Uno, Matsui, Lee, (2003-2005)

NN phase shifts



Lee, Matsuyama (1985-1992)

$pp \rightarrow \pi^+ np$

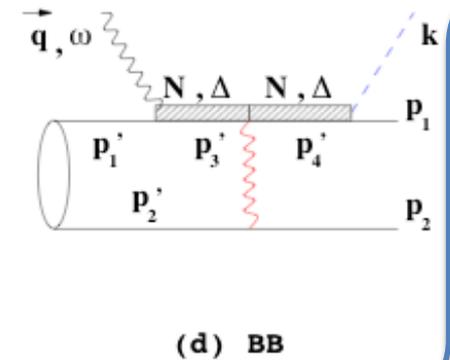
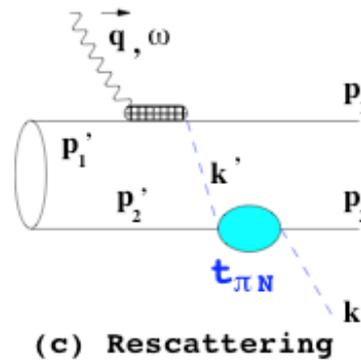
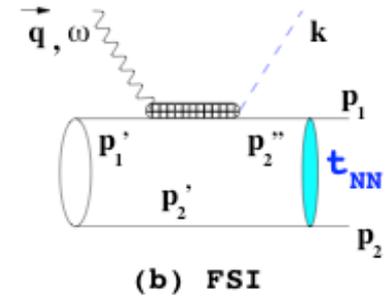
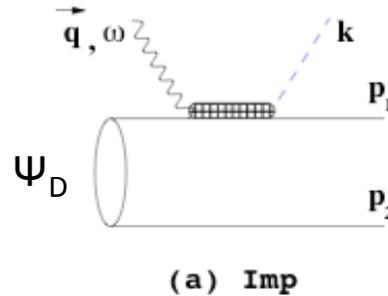


Model Hamiltonian with N, π, Δ

multiple scattering theory

$$\langle \pi NN | T | \gamma^* \Psi_d \rangle$$

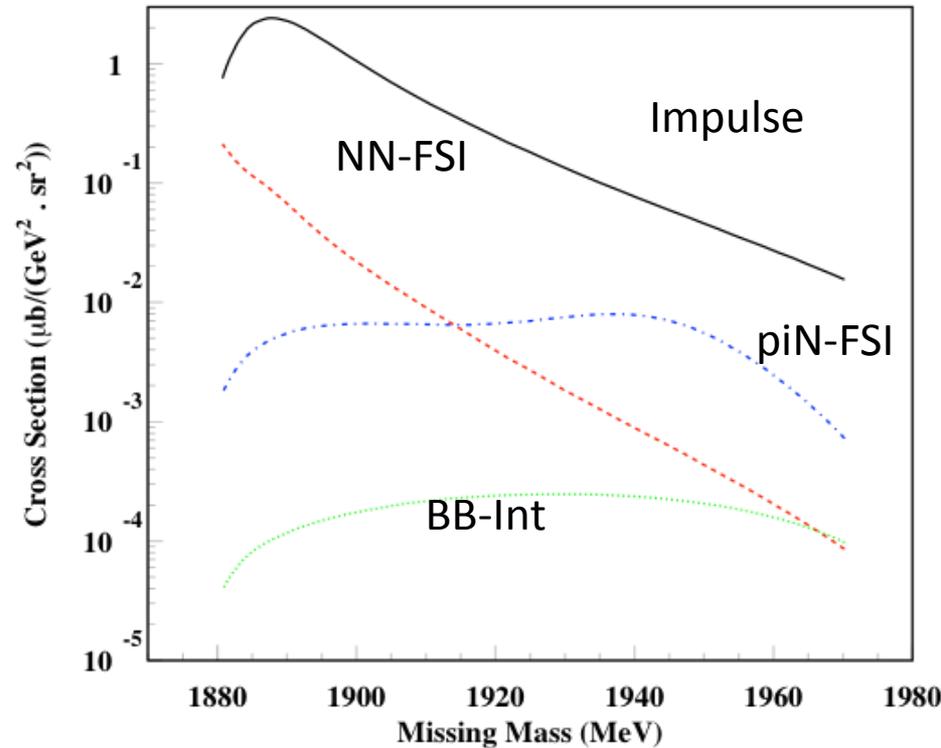
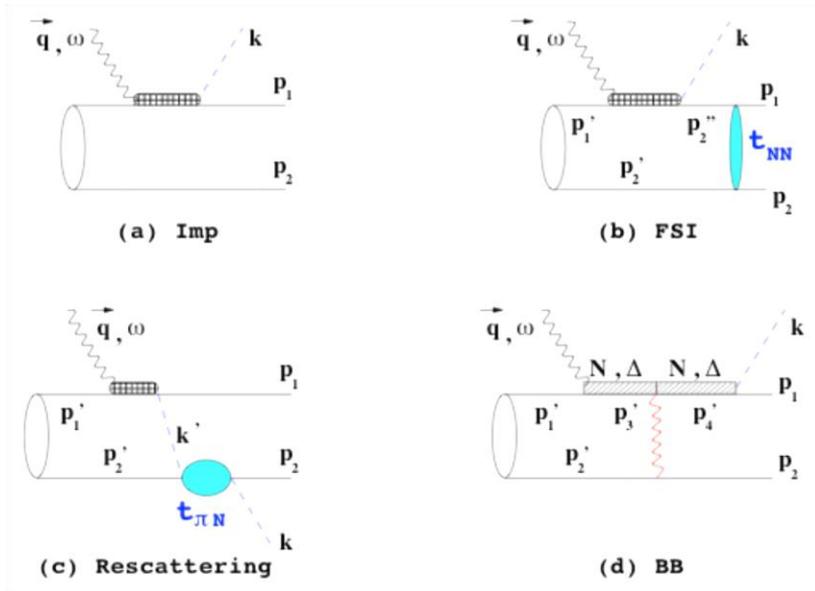
$$\sigma (\gamma^* d \rightarrow \pi NN)$$



Calculations include :

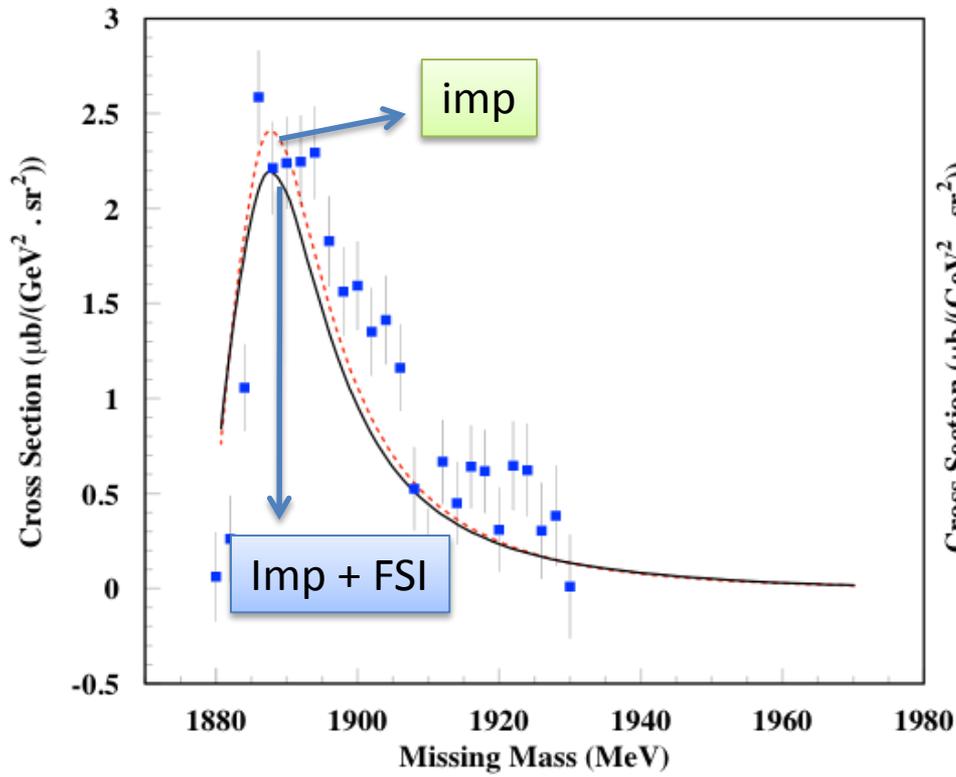
- Fermi motion effects
- Spin rotation effects
$$|p_L, m_s\rangle_d = R_w(\Lambda) |p_c, m_s\rangle$$
- Lorentz transformation of currents
$$[J]_d = \Lambda [j]_N \Lambda^{-1}$$
- Exact loop-integrations of FSI terms

$d(e, e' \pi^+) nn$



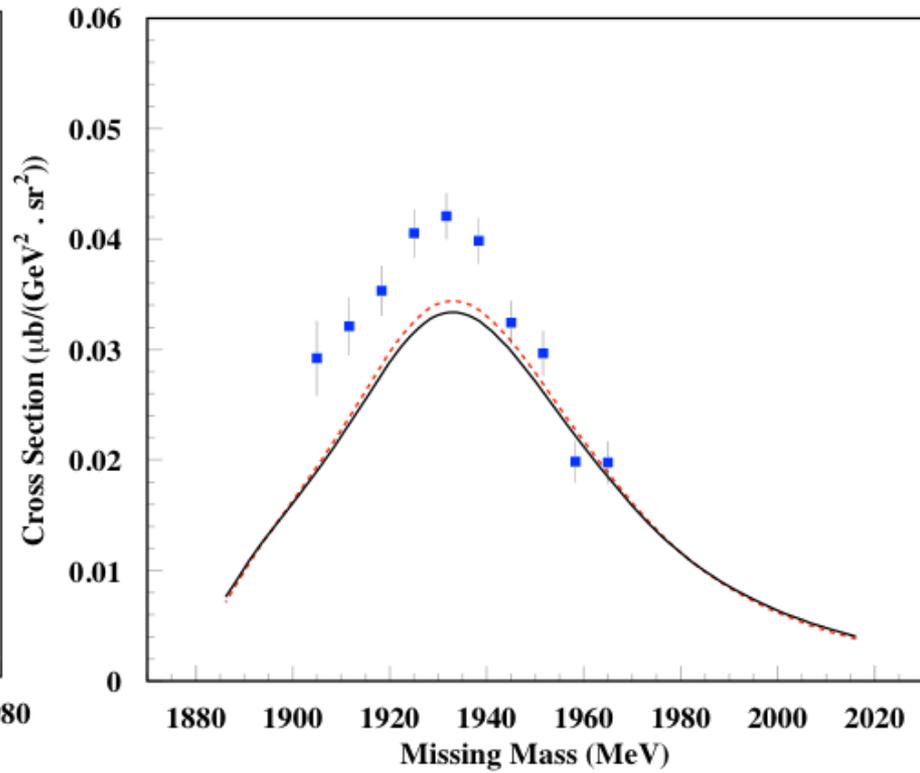
K. Hafidi, T.-S. H. Lee, Phys. Rev. C (2001)

Impulse term dominant
BB Int can be neglected



Saclay data

$Q^2=0.08 \text{ (GeV/c)}^2$
 $W=1.16 \text{ GeV}$
 $E_e=645 \text{ MeV}$



Jlab data

$Q^2=0.4 \text{ (GeV/c)}^2$
 $W=1.16 \text{ GeV}$
 $E_e=844 \text{ MeV}$

Apply the SL model to study

$$\gamma d \rightarrow \pi^- pp$$

$$\gamma d \rightarrow \pi^0 np$$

J. Wu, T. Sato, T.-S. H. Lee Phys. Rev. C91, 035203 (2014)

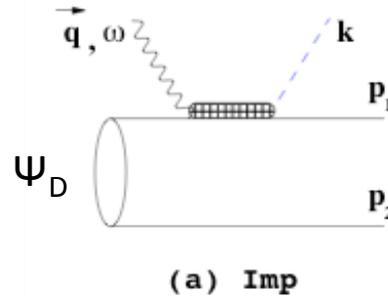
Model Hamiltonian with N, π, Δ

multiple scattering theory

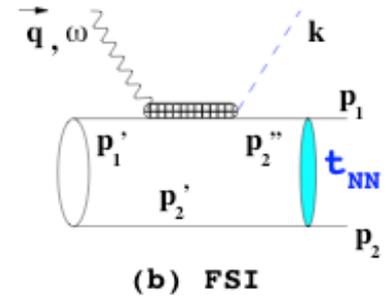
$$\langle \pi NN | T | \gamma \Psi_D \rangle$$

$\sigma (\gamma d \rightarrow \pi^- pp)$

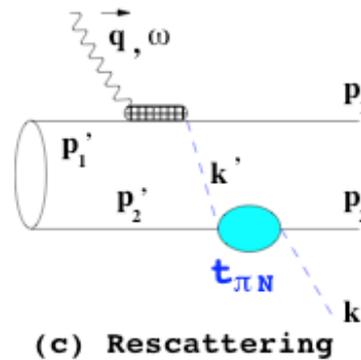
$\sigma (\gamma d \rightarrow \pi^0 np)$



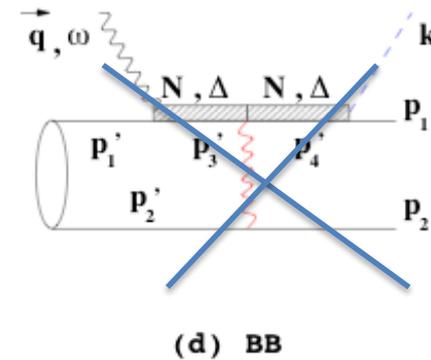
(a) Imp



(b) FSI

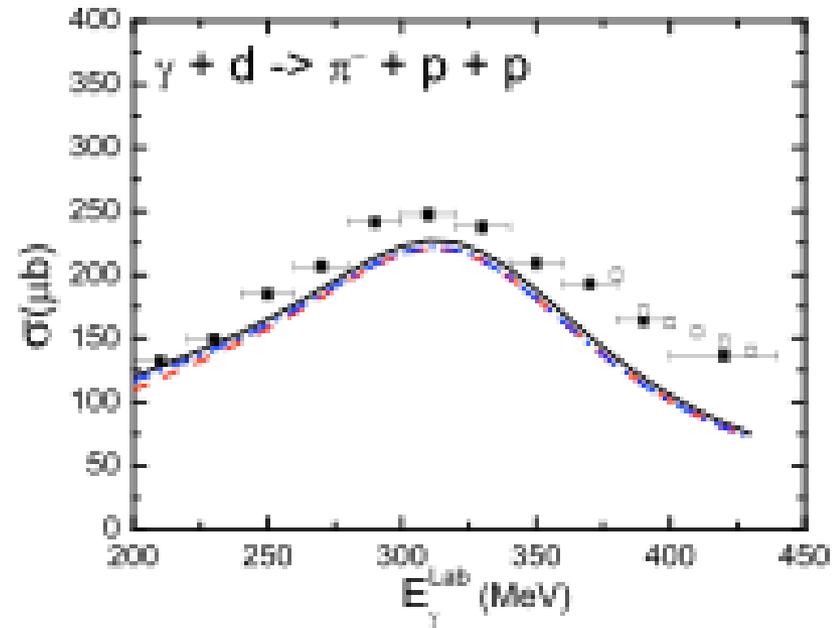
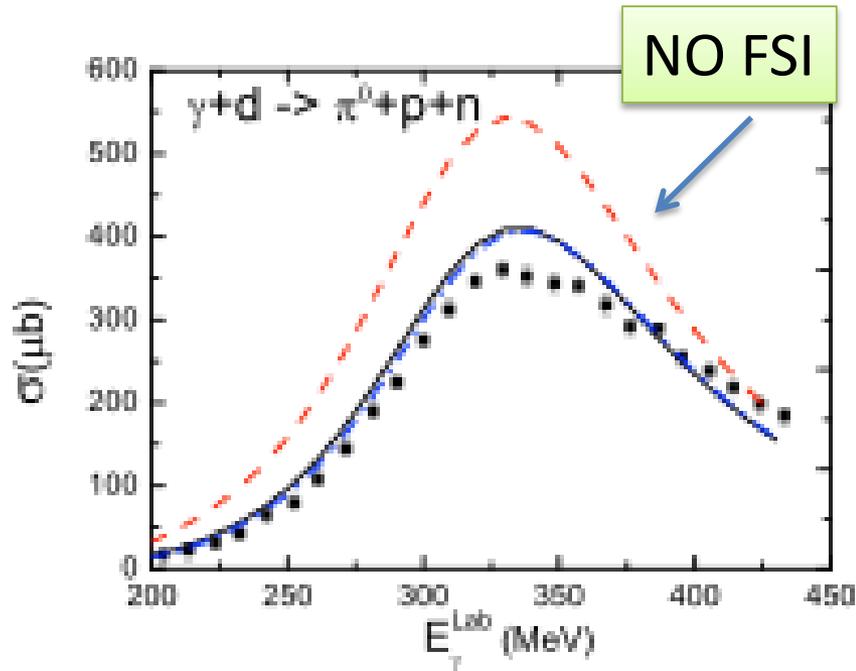


(c) Rescattering



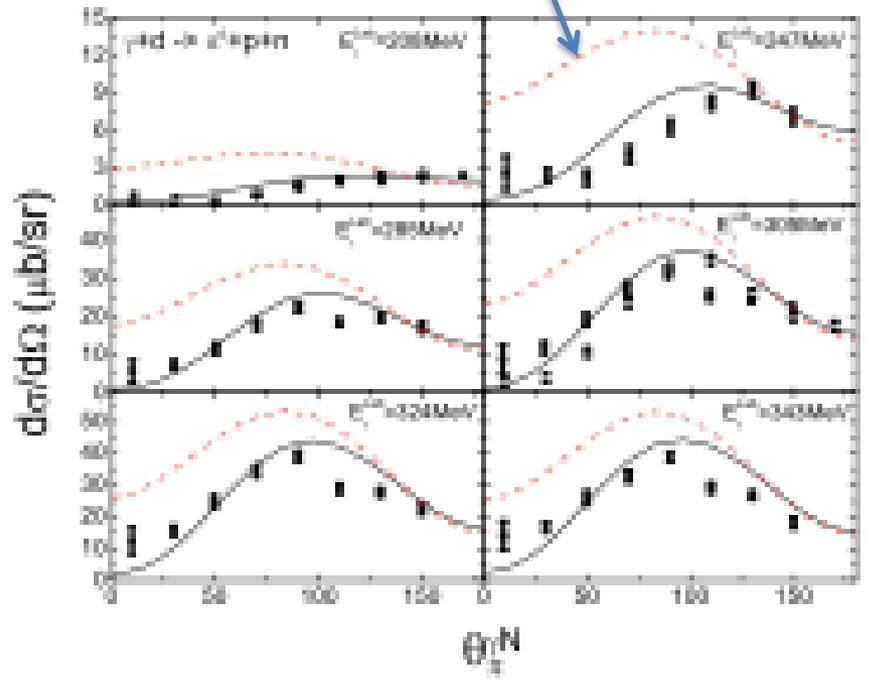
(d) BB

In the $\Delta(1232)$ region

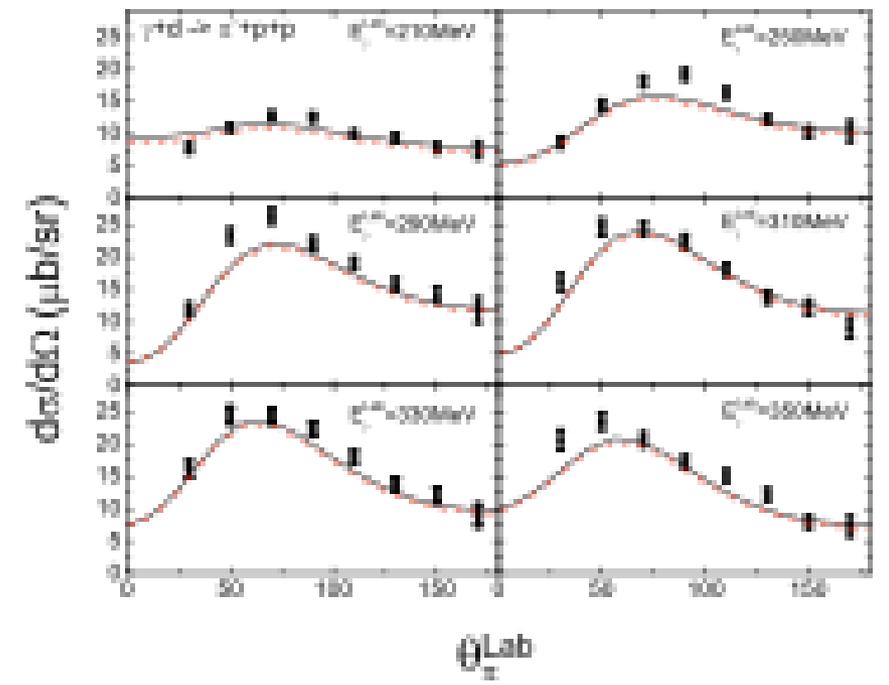


→ FSI is large for T=0 NN state
FSI is weak for T=1 NN state

NO FSI



$\gamma d \rightarrow \pi^0 np$



$\gamma d \rightarrow \pi^- nn$



FSI is large for T=0 NN state
 FSI is weak for T=1 NN state

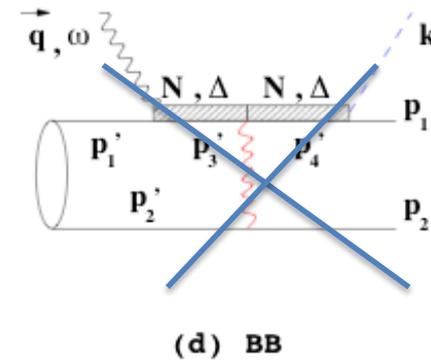
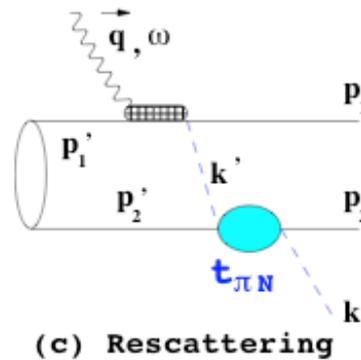
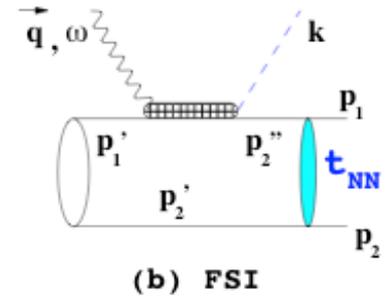
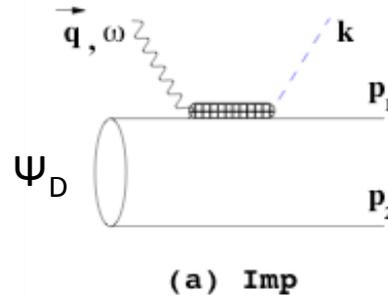
Model Hamiltonian with N, π, Δ

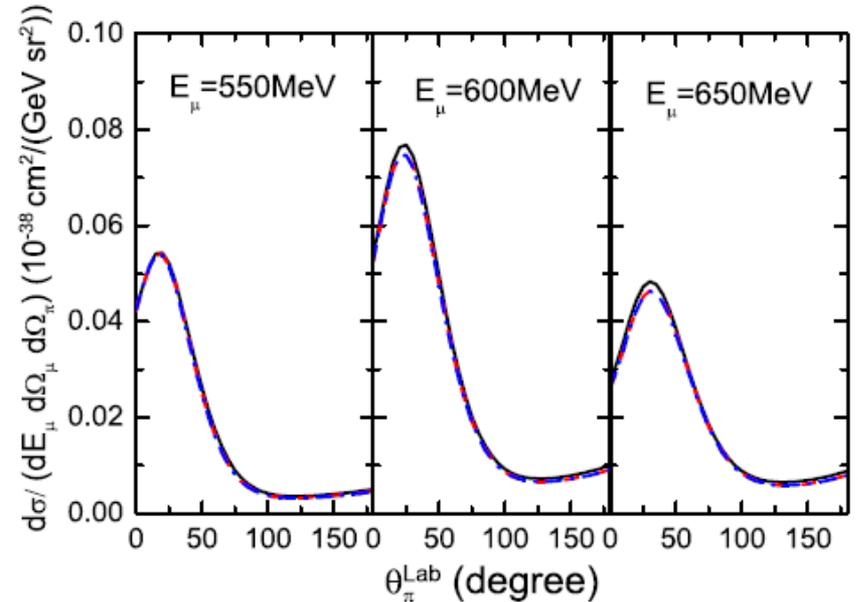
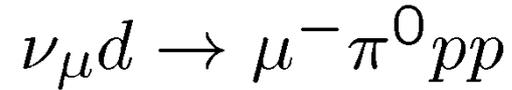
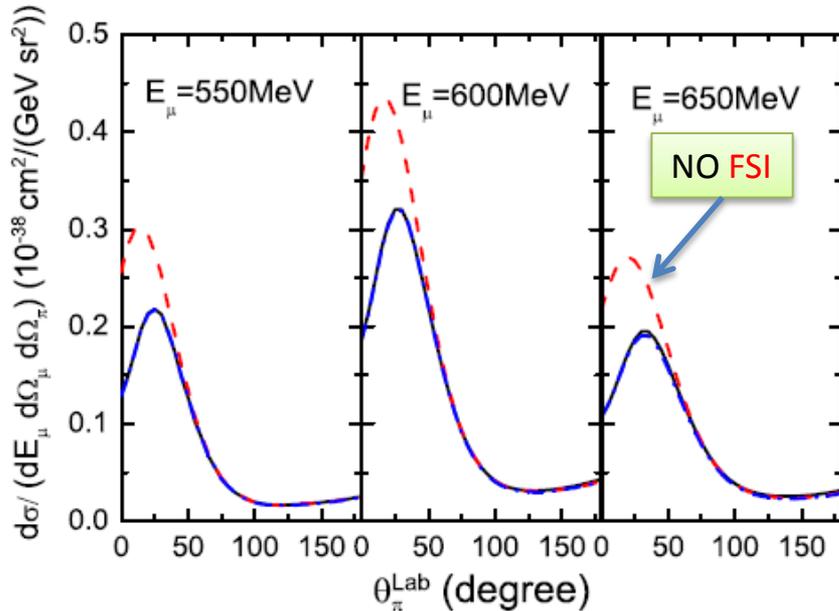
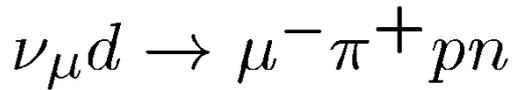
multiple scattering theory

$$\langle \pi NN | T | \nu \Psi_D \rangle$$

$\sigma (\nu d \rightarrow \mu^- \pi^0 pp)$

$\sigma (\nu d \rightarrow \mu^- \pi^+ np)$





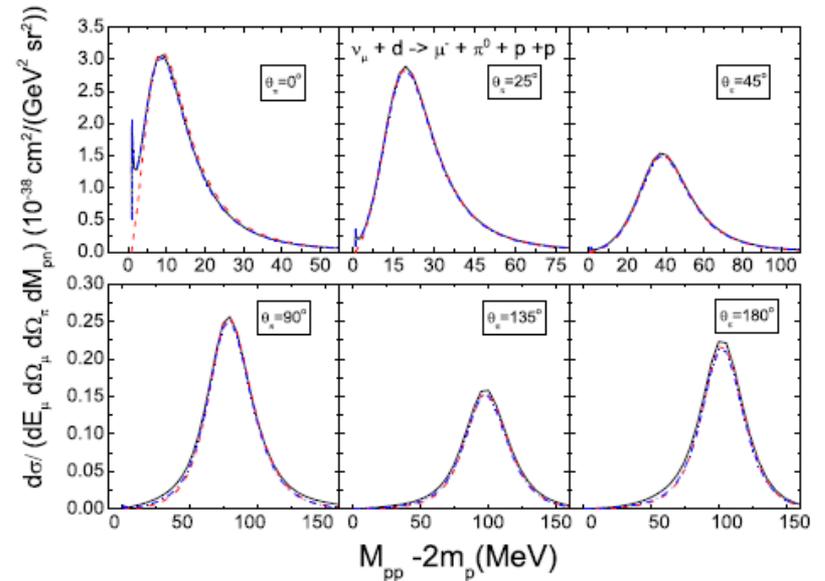
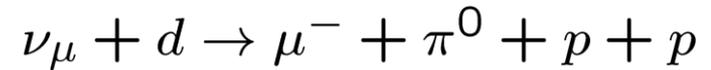
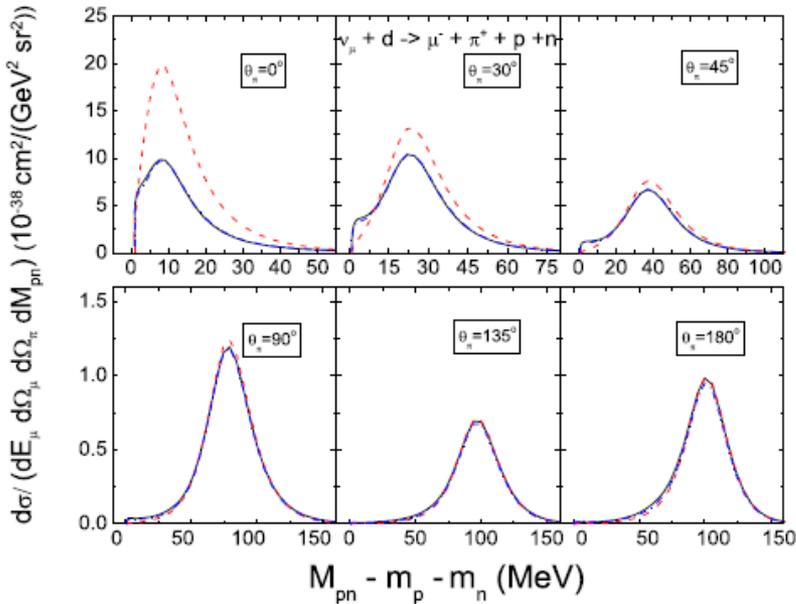
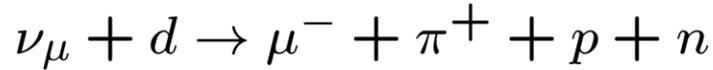
FSI is large for T=0 NN state
 FSI is weak for T=1 NN state

$$E_{\nu} = 1 \text{ GeV}$$

$$\theta_{\mu} = 25^{\circ}$$

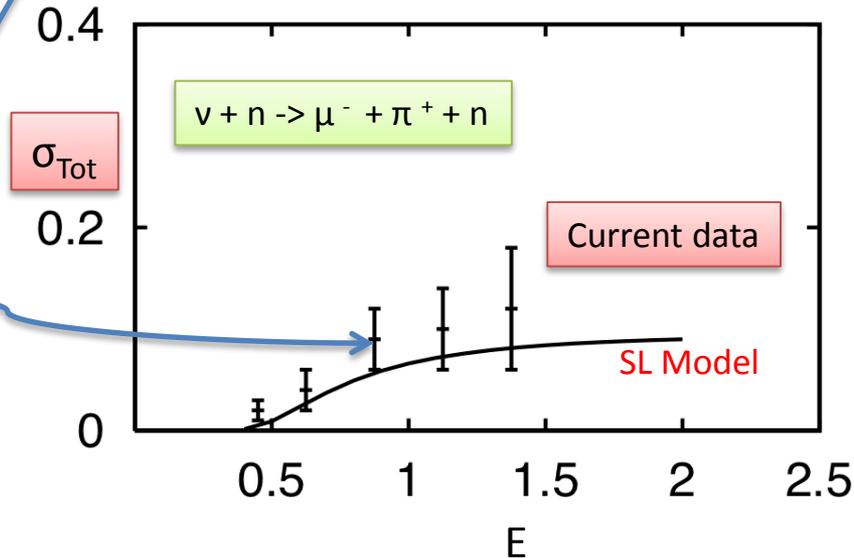
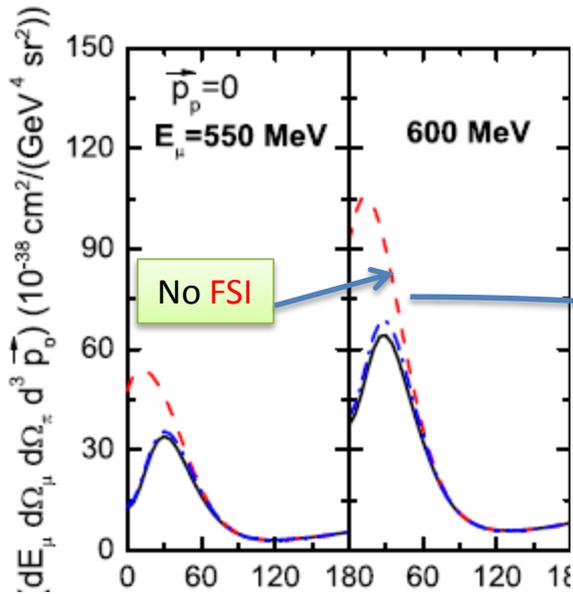
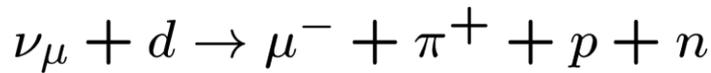
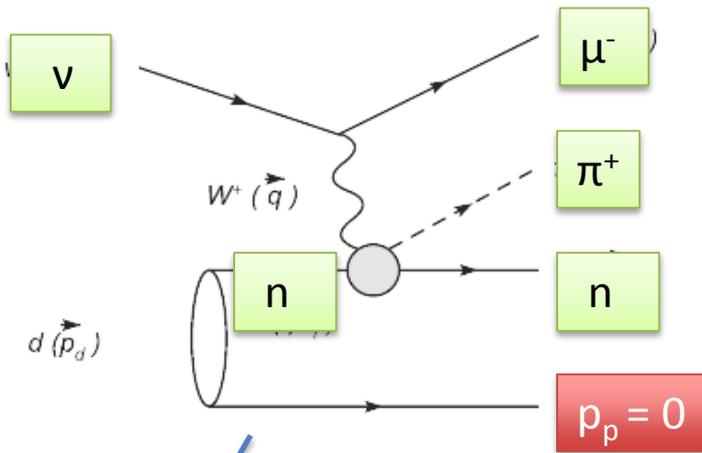
~ Delta-QF kinematics

NN invariant mass distribution



FSI is large for T=0 NN state
 FSI is weak for T=1 NN state

spectator approximation



Need to re-analyze of ANL and BNL data !

Summary

- For analyzing neutrino experiments at 1-3 GeV, it is necessary to develop theoretical models for calculating nuclear effects in the $\Delta(1232)$ region.
- The **SL Model** can describe almost all electroweak pion production data and has been applied to calculate nuclear effects by using
 - a. multiple scattering theory for deuteron target (**this talk**)
 - b. Δ -hole model for heavy nuclei
- The final state interaction effects on $\gamma d, \nu d \rightarrow \pi NN$ are very large for final $T=0$ NN state and must be included to extract the cross sections on **neutron** from data on deuteron
- Our results suggest the need for **re-analysis** of ANL and BNL data.

Back Up

Transition matrix element (radial integral) of two-nucleon wave function

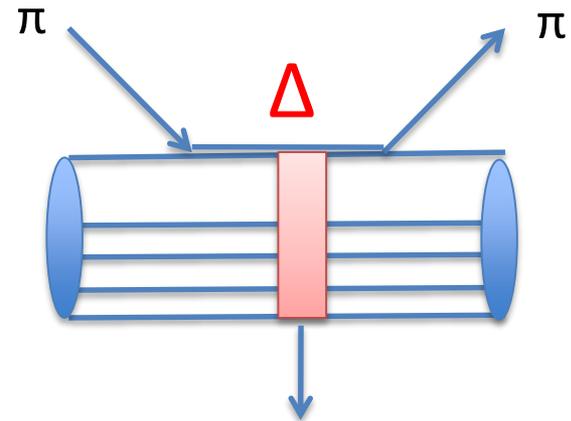
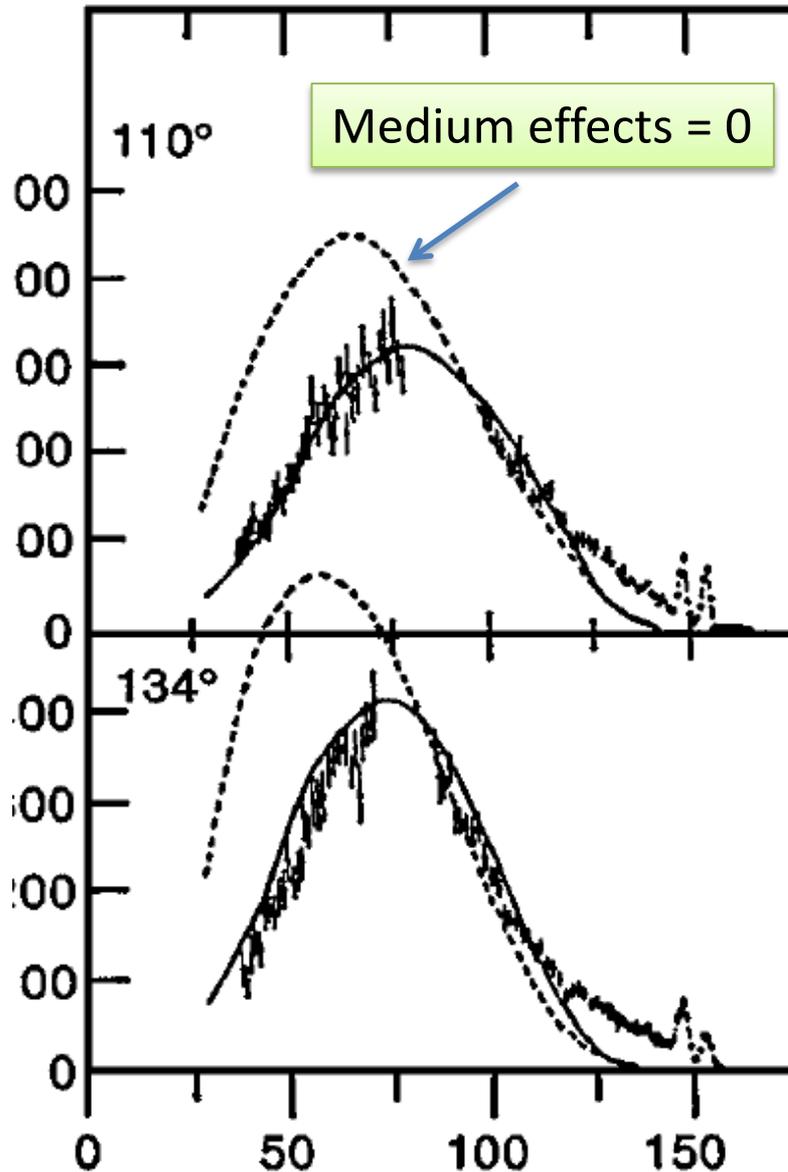
Final state	$\int_0^\infty R_{2S+1L_J}(r)R_d(r)r^2dr$
${}^3S_1(pn)$	0(orthogonality of wave function)
${}^1S_0(pn, nn, pp)$	finite

Initial state

${}^3S_1(\text{deuteron})$ (S=1,L=0,J=1)

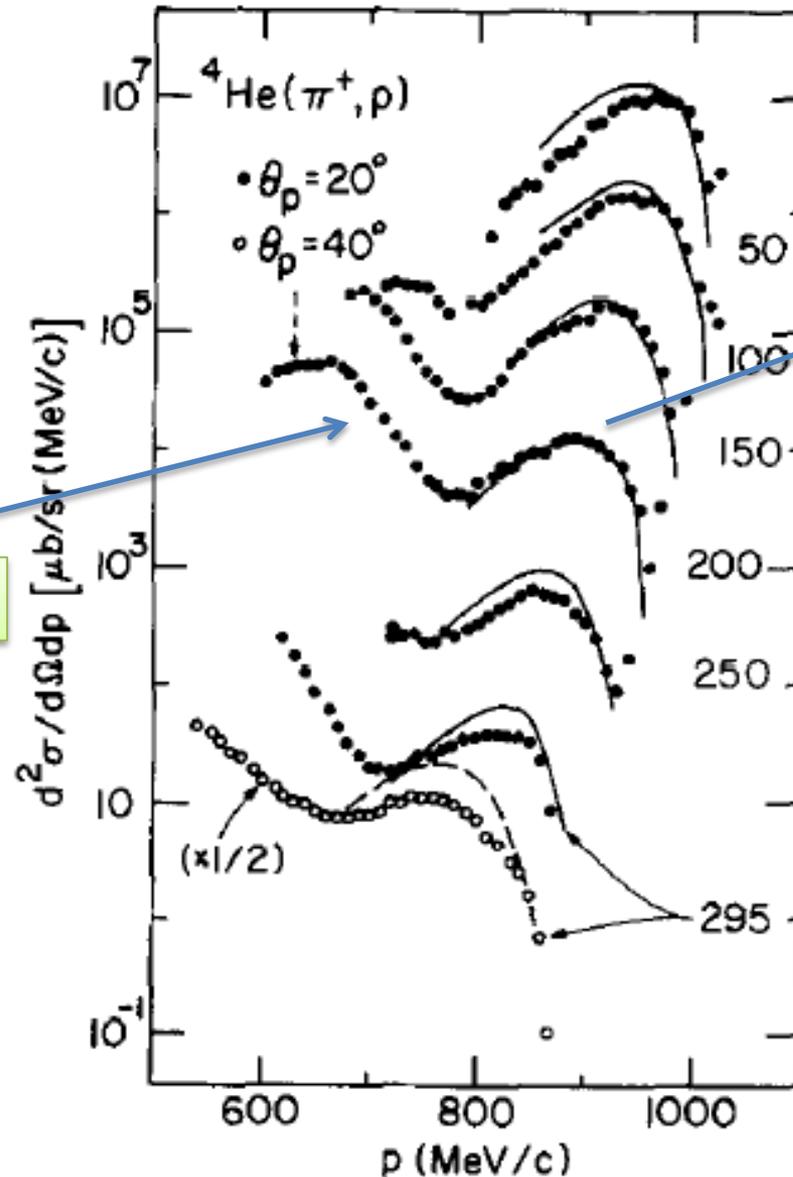
This property can be only taken into account by using distorted wave, not plane wave approximation.

Δ -Hole model calculation of $^{12}\text{C}(\pi, \pi')X$

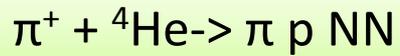


Medium effects: scattering, absorption

Δ -hole model calculation of ${}^4\text{He}(\pi^+, p)\text{NN}$



Absorption



Quasi-free scattering

Predict :

▪ Inclusive $^{12}\text{C}(\nu, \mu) X$

Szczerbinska, Sato, Kubodera, Lee et al., PLB 649 132 (2007)

▪ Coherent $^{12}\text{C}(\nu, \mu, \pi^0)^{12}\text{C}$

Nakamura, Sato, Lee, Szczerbinska, Kubodera, PR C81,035502 (2010)

Inclusive $A(v, \mu)X$

Szczerbinska, Sato, Kubodera, Lee et al., PLB 649 132 (2007)

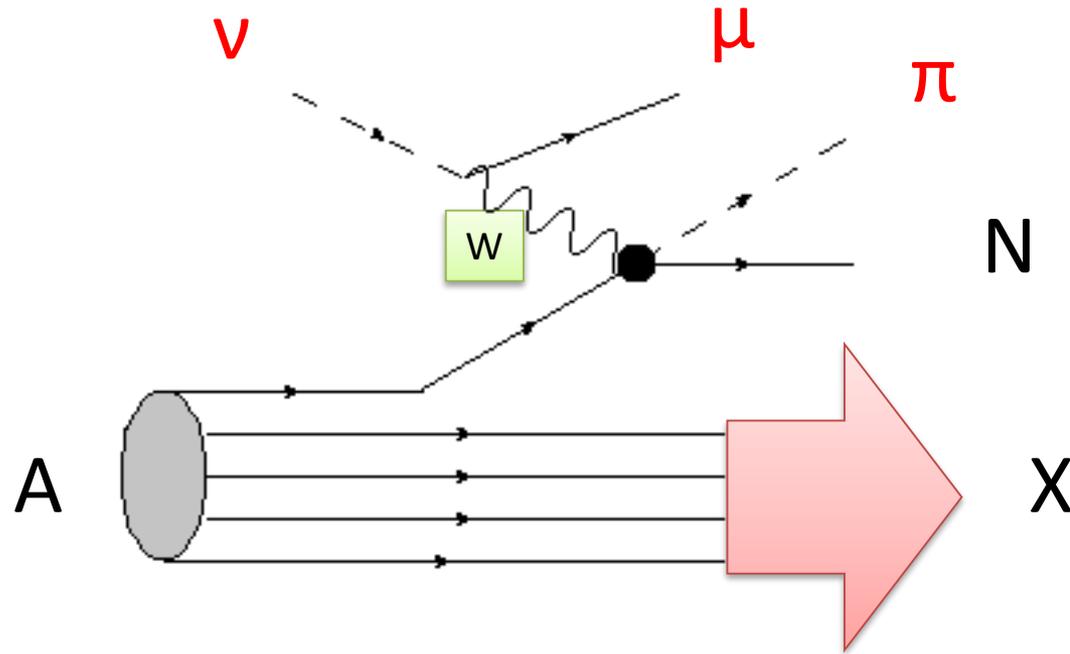
■ Impulse approximation : $T = \sum_i t(i)$

amplitude on N

■ Objectives:

a. Examine Fermi Gas Model

b. Make prediction using Spectral function



$$W^{\mu\nu} = \sum_X \langle A | J^\mu | \pi N X \rangle \langle X N \pi | J^\nu | A \rangle$$

$$\frac{d\sigma}{dE_\ell d\Omega_\ell} = \frac{p_\ell}{p_\nu} \frac{G_F^2 \cos^2 \theta_C}{8\pi^2} L_{\mu\nu} W^{\mu\nu}$$

$$\begin{aligned}
W^{\mu\nu} &\sim \int d\vec{p}' d\vec{k} d\vec{p} \theta(p_F - |\vec{p}'|) \theta(|\vec{p}| - p_F) && \Leftarrow \text{Fermi Gas} \\
&\times \Lambda^{\mu\mu'} \langle \pi N(p') | j_{\mu'} | N(p) \rangle_{\pi N - \text{cm}} && \Leftarrow \text{SL} \\
&\times \Lambda^{\nu\nu'} \langle \pi N(p') | j_{\nu'} | N(p) \rangle_{\pi N - \text{cm}}^*
\end{aligned}$$

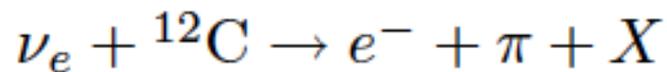
* Fermi Gas to Spectral Function

Benhar et al. NPA 579 493 (1994)

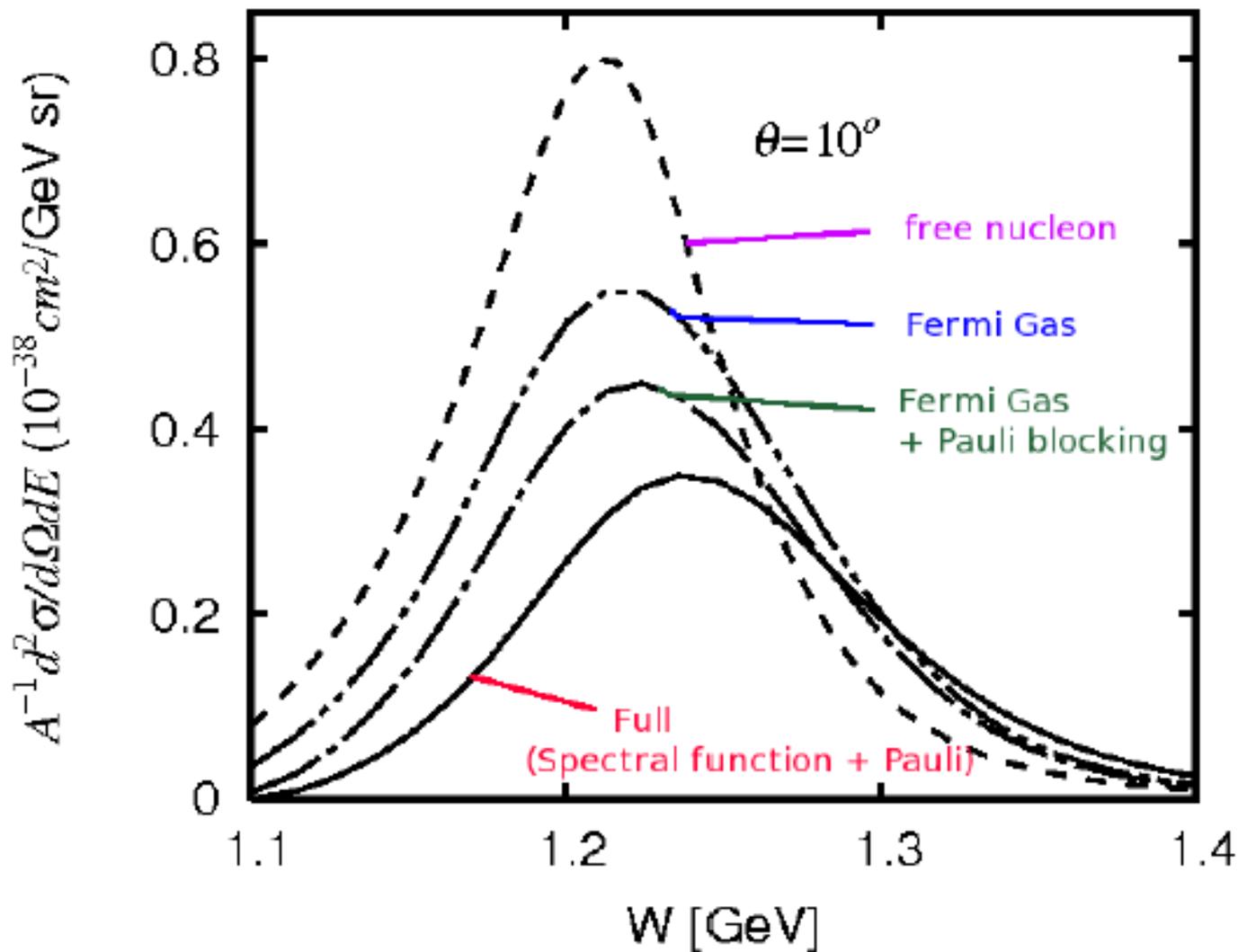
$$\frac{3}{4\pi p_F^3} \int d\vec{p} \theta(p_F - |\vec{p}|) \rightarrow \int d\vec{p} dE P(\vec{p}, E)$$

Include correlations

Nuclear Effect for 1π in Δ -region



$$E_\nu = 1 \text{ GeV}$$





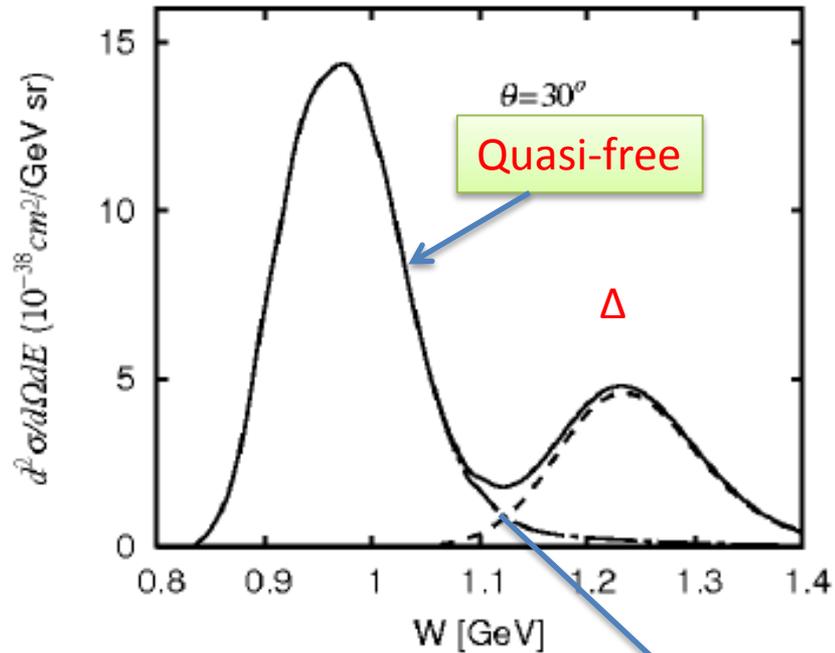
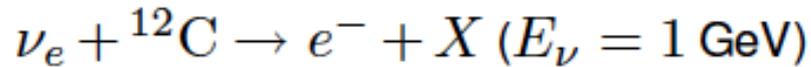
Nuclear correlation and final state interaction must be included in calculating the **nuclear effects** in analyzing experimental data

Same formula for $e + {}^{12}\text{C} \rightarrow e' + \pi + X$

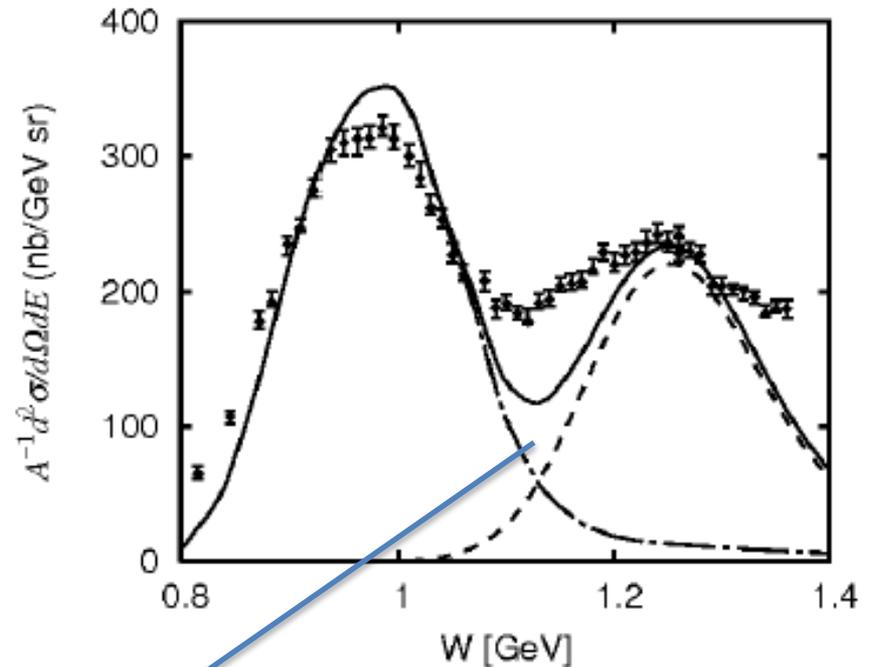
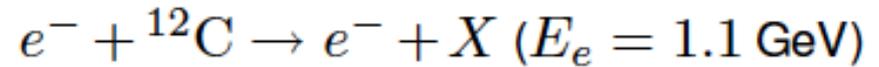


Test the model by the available **data**

Prediction



Compare with data



[Data: Sealock et al. PRL 62 1350 (1989)]

* Dip region : need to include two-body mechanisms which are beyond the impulse approximation calculations

Coherent $A(\nu, \mu\pi^0)A$ reactions

Nakamura, Sato, Lee, Szczerbinska, Kubodera, PR C81,035502 (2010)

Main motivation:

Remove π^0 which could fake
 $\nu_\mu \rightarrow \nu_e$ oscillation events

Δ-hole Model

$$\langle A | J | \pi, A \rangle = \sum_{i,j} \langle \varphi_A | j_{N,\Delta}(i) G_{\Delta-h}(E) h_{\Delta,\pi N}(j) | \pi \varphi_A \rangle$$

$$G_{\Delta-h}(E) = \frac{|\varphi_{A-1} \Delta\rangle \langle \Delta \varphi_{A-1}|}{E - M_{\Delta} - T_{\Delta} - V_{\Delta} - H_{A-1} - \sum_{\text{pauli}} - \sum_{\text{sprd}}$$

Fit π -A data

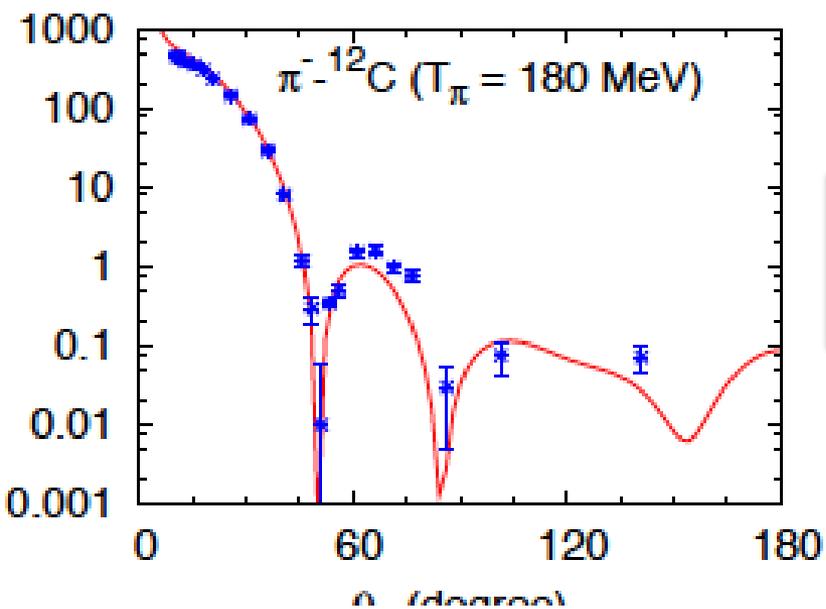
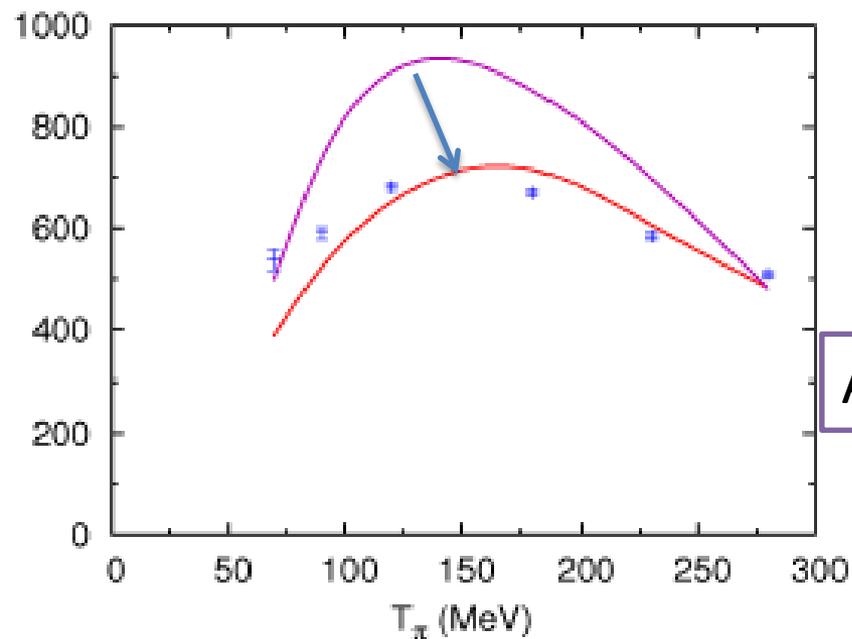
$$\sum_{\text{sprd}} = V_c(r) + V_{s.o}(r) S_{\Delta} \cdot L_{\Delta}$$

Pion absorption

Δ -hole model for ^{12}C

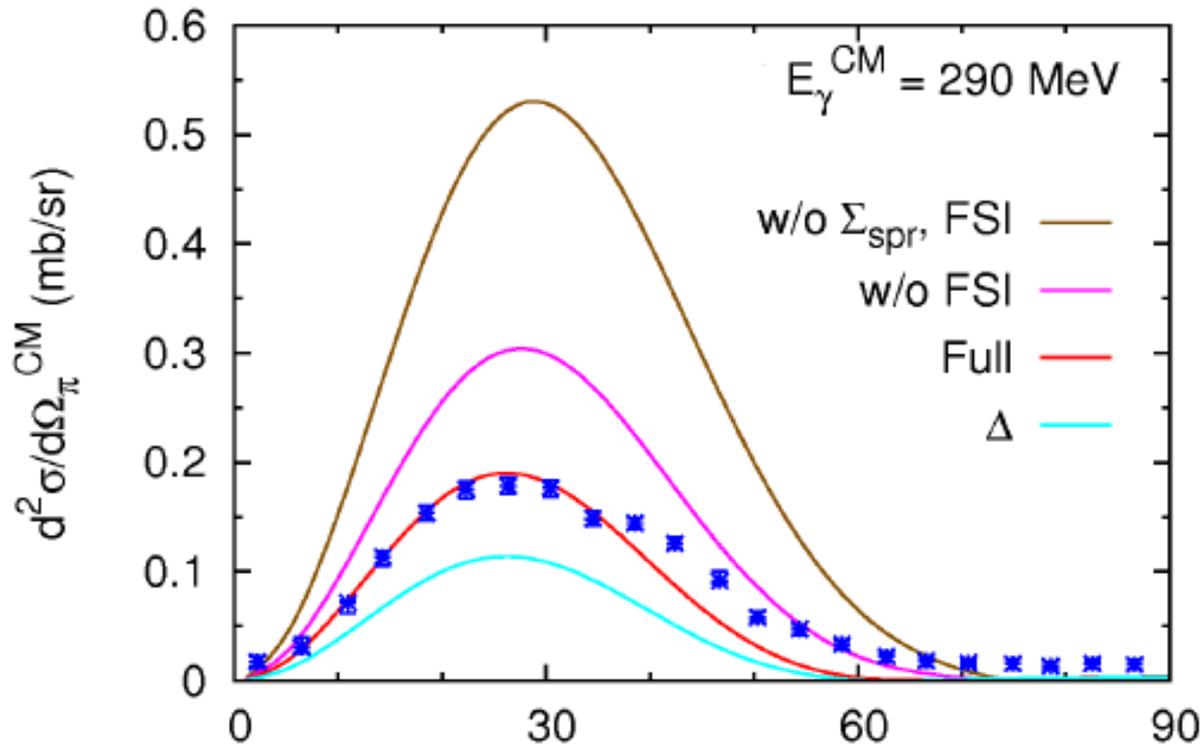
Nakamura et al., PR C81,035502 (2010)

Adjust Σ_{sprd} to fit **Total cross section data**



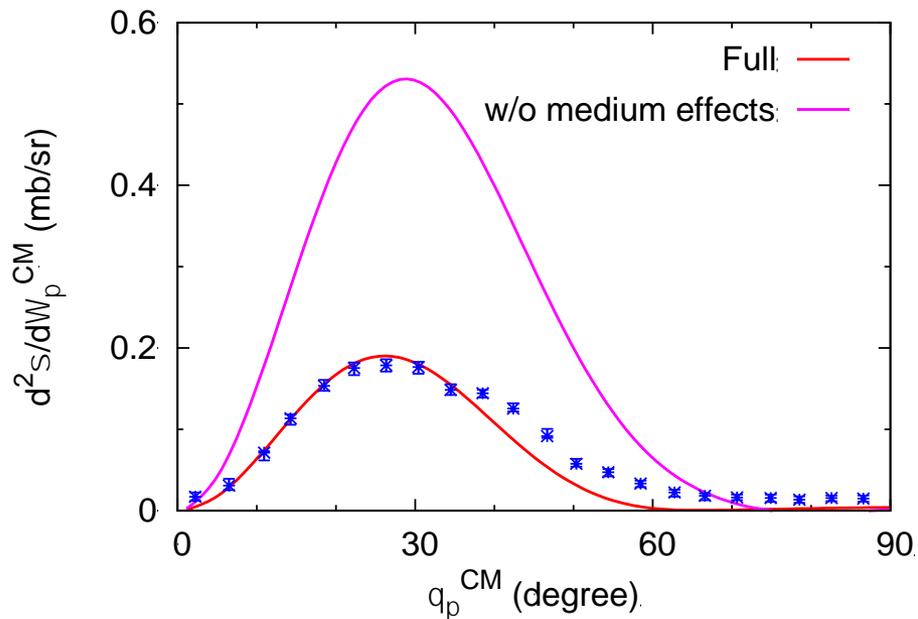
Predicted elastic scattering cross section agree well with the data

Δ -hole model prediction of $^{12}\text{C}(\gamma, \pi^0)^{12}\text{C}$

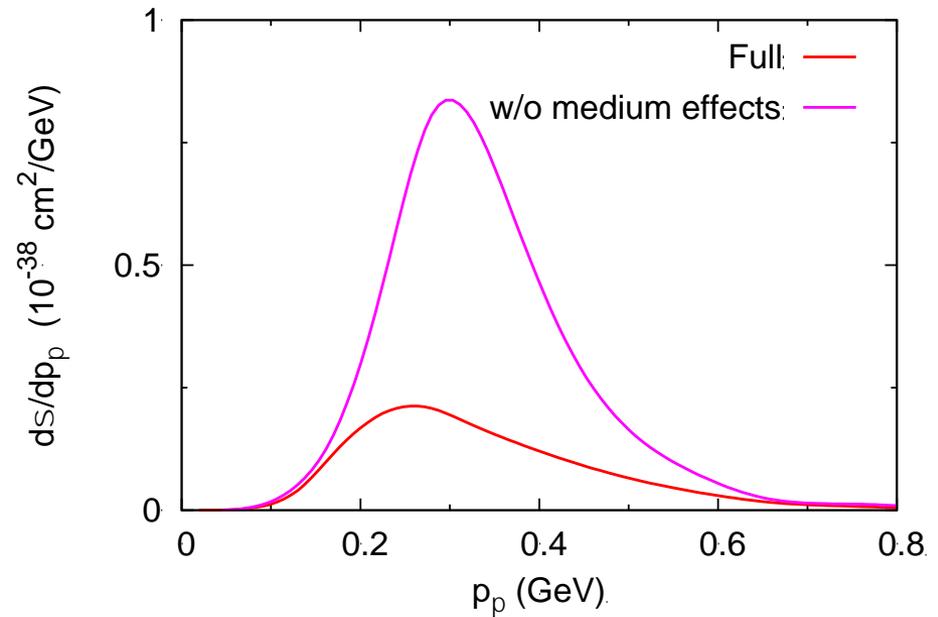
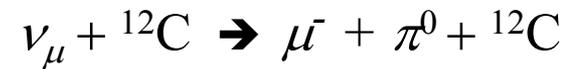


- In agreement with the data
- Medium effects on Δ is large

Compare with **data**



Prediction



Nakamura et al. (2010)

Current effort:

Extend SL model to include higher mass nucleon resonances (N^*) to predict ν -nucleus reactions



Starting point :

Hamiltonian with **excited** nucleons

Hamiltonian with **excited** nucleons

(Matsuyama, Sato, Lee, Phys. Rept, 2007)

$$H_{\text{int}} = h_{N^*, MB} + v_{MB, M'B'}$$

N^* : **Confined** quark-gluon core

MB : : $\gamma N, \pi N, 2\pi-N, \eta N, K\Lambda, K\Sigma, \omega N$

$(\pi\Delta, \rho N, \sigma N)$



ANL-Osaka Model has been developed

Kamano, Nakamura, Lee, Sato, PRC 88 (2013)

ANL-Osaka Model

Kamano, Nakamura, Lee, Sato, PRC 88 (2013)

Solve

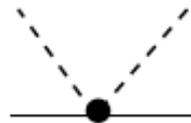
$$T_{ab}(E) = V_{ab} + \sum_c V_{ac} G_c(E) T_{cb}(E)$$

$a, b, c = \gamma N, \pi N, 2\pi-N, K\Lambda, K\Sigma$

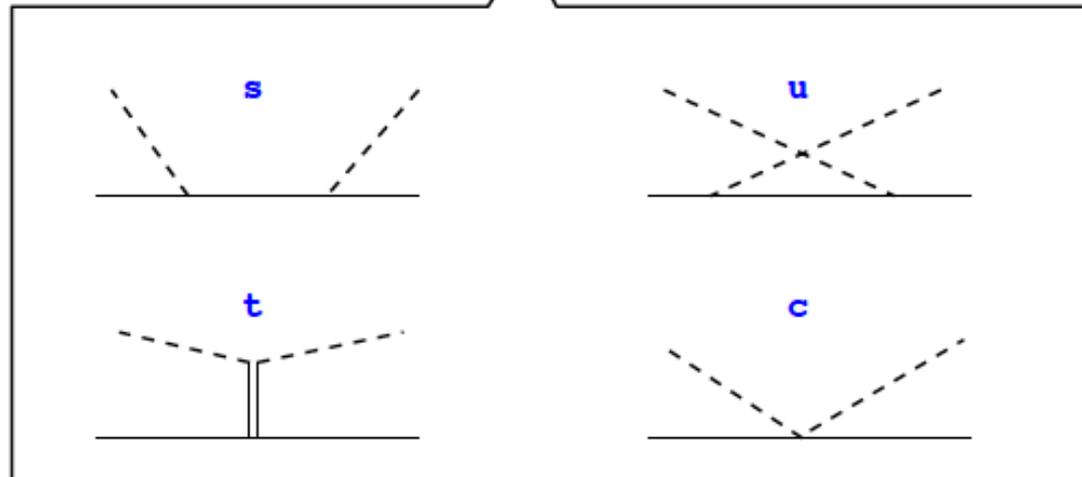
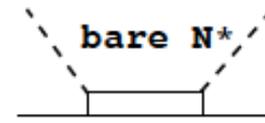
16 bare N^*

V_{ab}

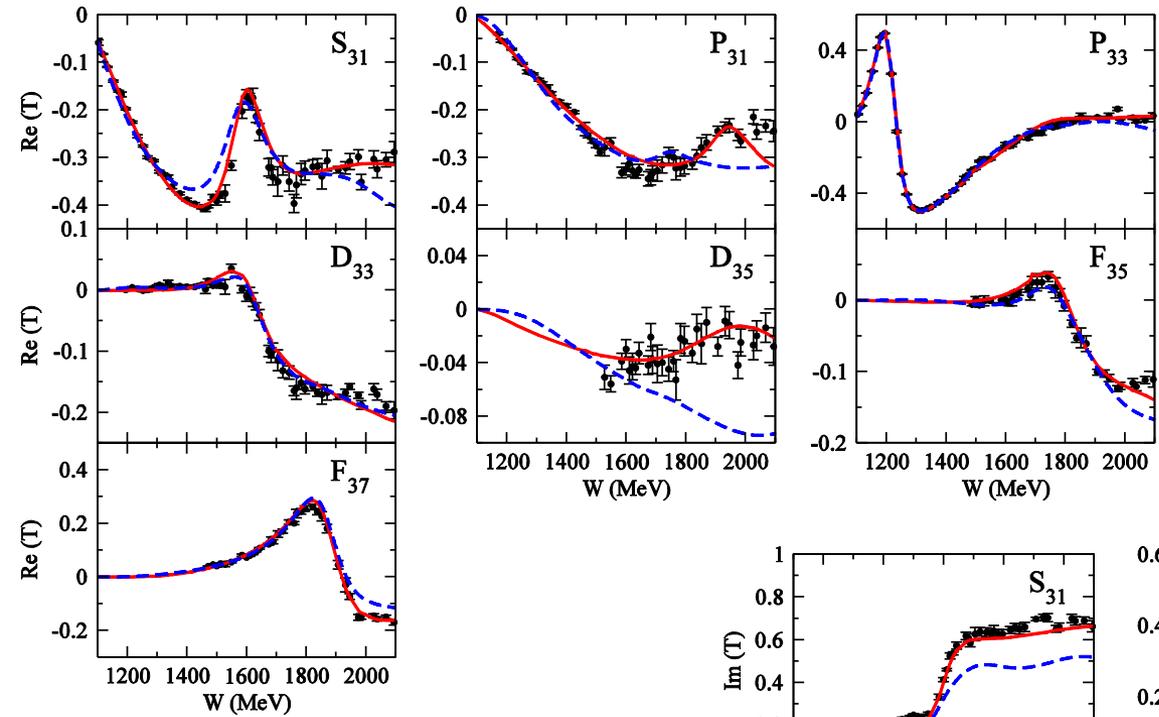
=



+



Partial wave amplitudes of pi N scattering

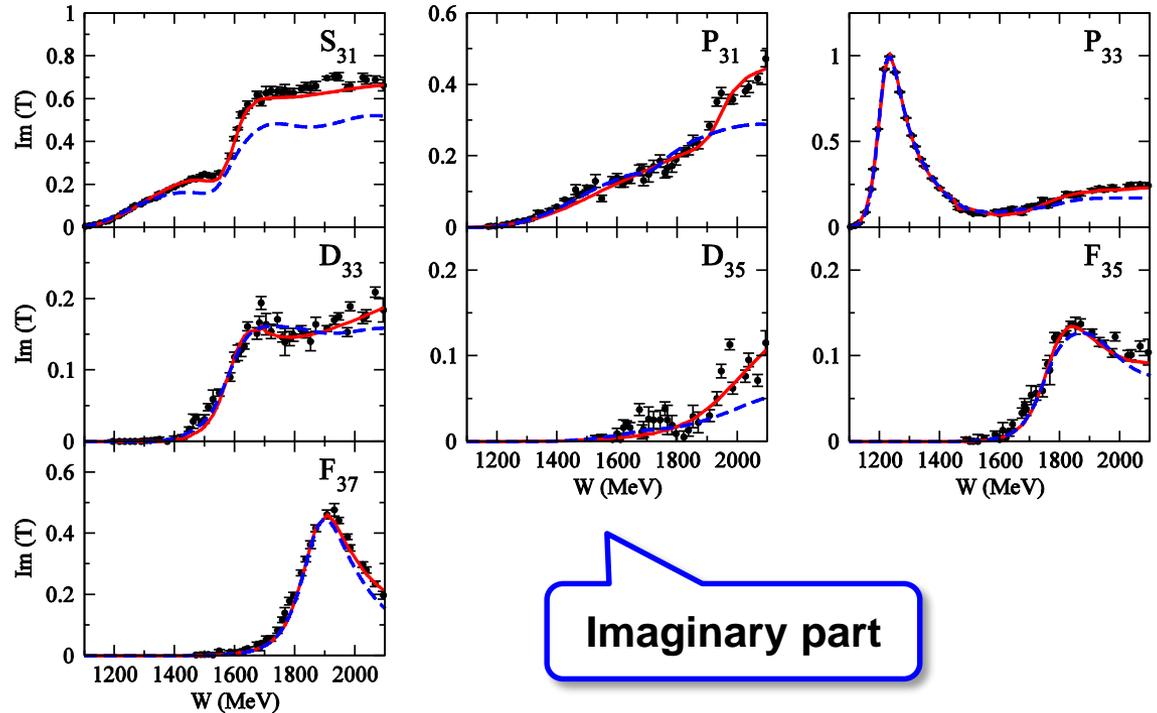


Real part

$$I = \frac{3}{2}$$

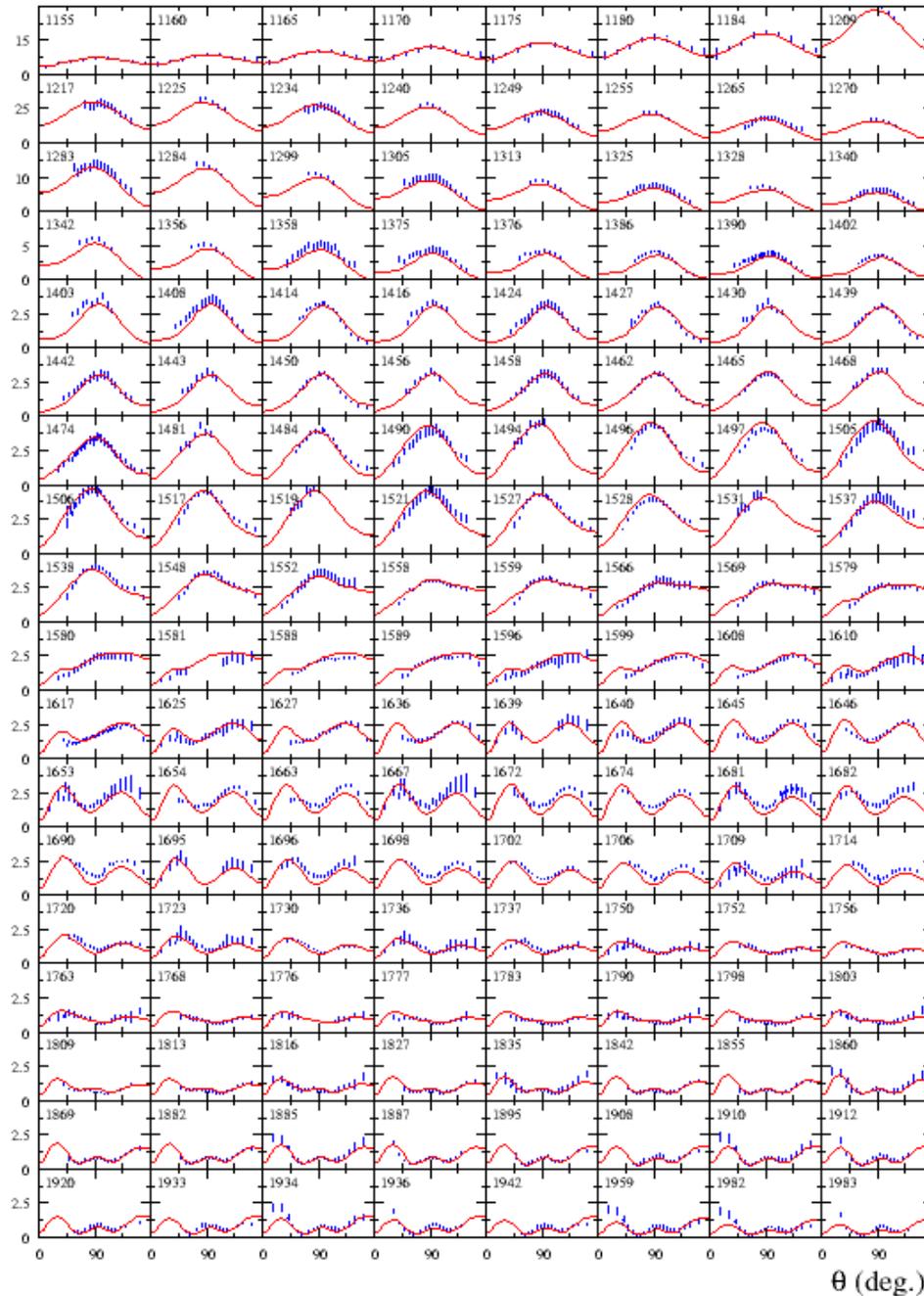
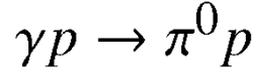
— Kamano, Nakamura, Lee, Sato, 2013

- - - Previous model
(fitted to $\pi N \rightarrow \pi N$ data only)
[PRC76 065201 (2007)]

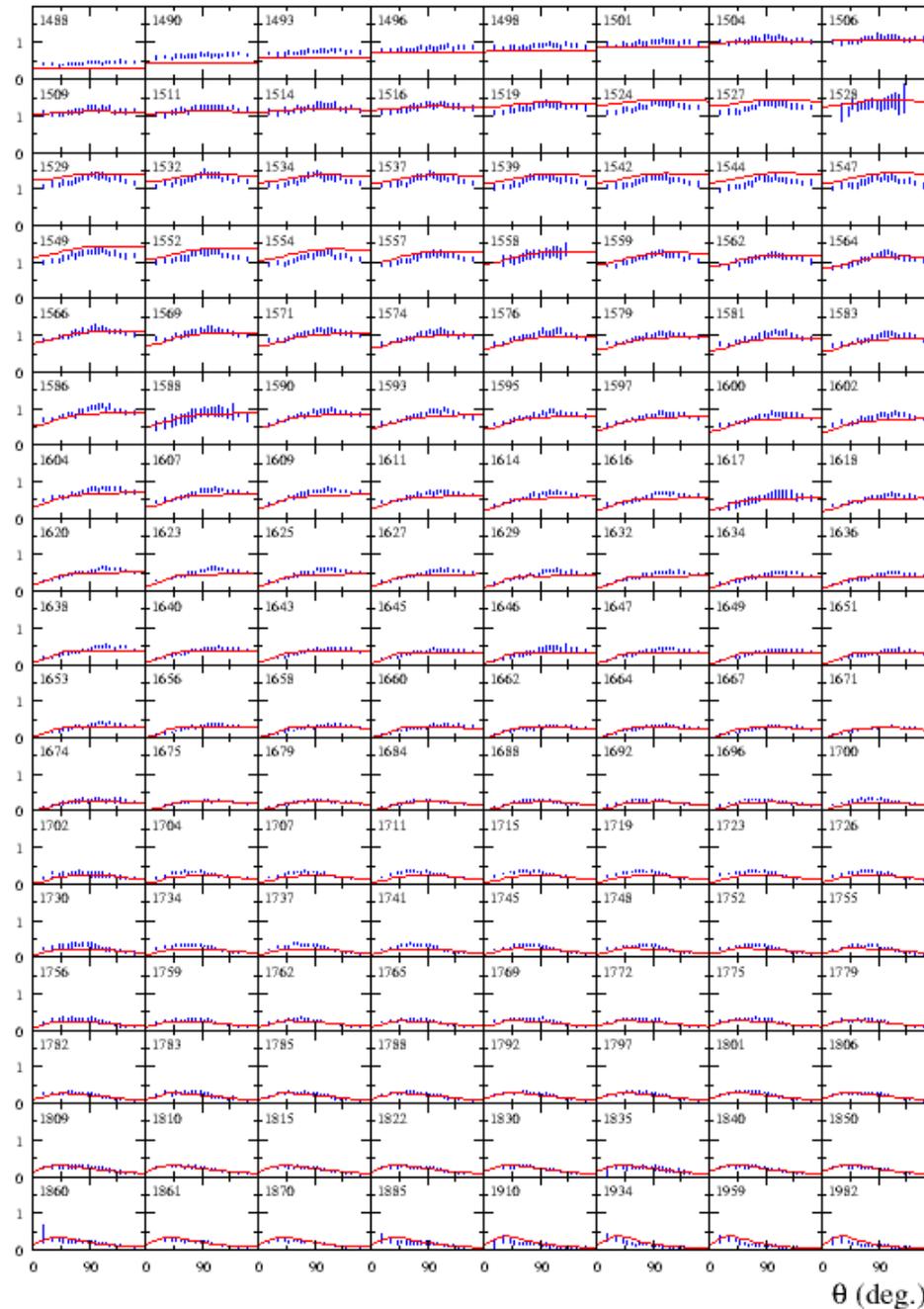


Imaginary part

$d\sigma/d\Omega$ ($\mu\text{b/sr}$)



Vector current ($Q^2=0$) for 1π
Production is well-tested by data

$d\sigma/d\Omega$ ($\mu\text{b/sr}$) $\gamma p \rightarrow \eta p$ 

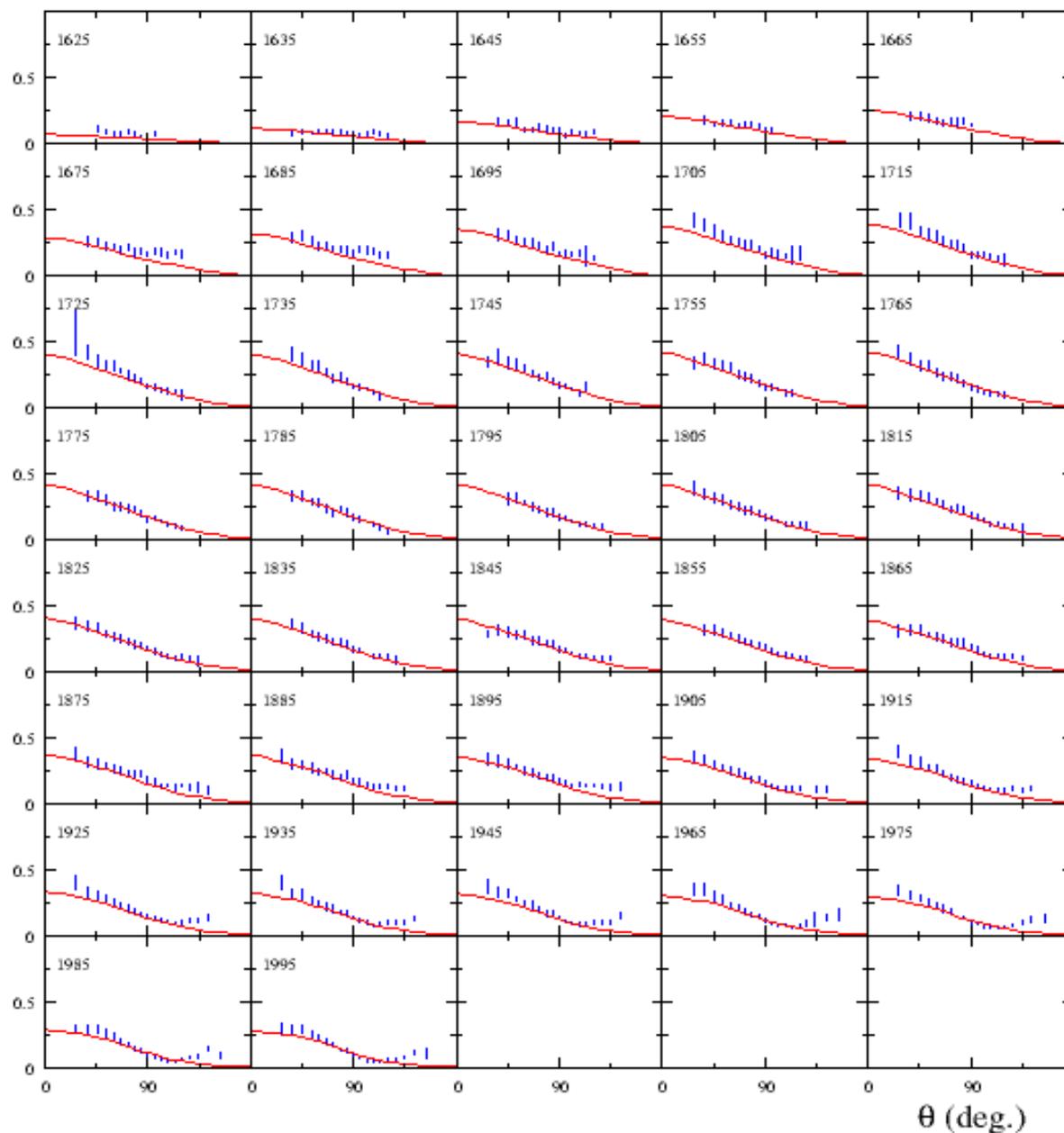
Kamano, Nakamura, Lee, Sato, 2013

Vector current ($Q^2=0$) for η
Production is well-tested by data

$d\sigma/d\Omega$ ($\mu\text{b}/\text{sr}$)

$\gamma p \rightarrow K^+ \Lambda$

Kamano, Nakamura, Lee, Sato, 2013



Vector current ($Q^2=0$) for K
Production is well-tested by data

$\pi N \rightarrow \pi\pi N$

(parameters had been fitted to $\pi N \rightarrow \pi N$)

Kamano, Julia-Diaz, Lee, Matsuyama, Sato, PRC79 025206 (2009)

