

# Exotic Oscillations Searches at HK: Sterile Neutrinos and Lorentz Violation

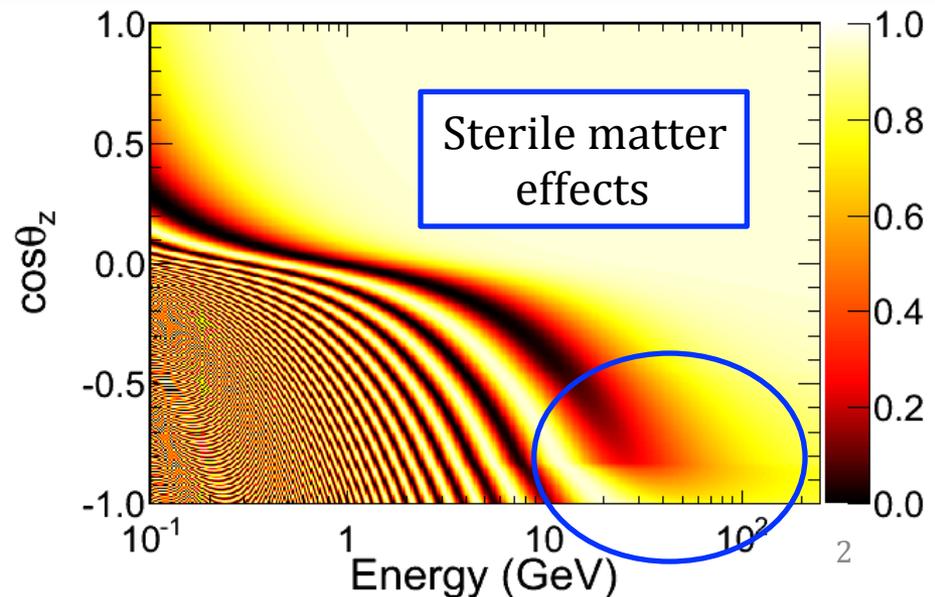
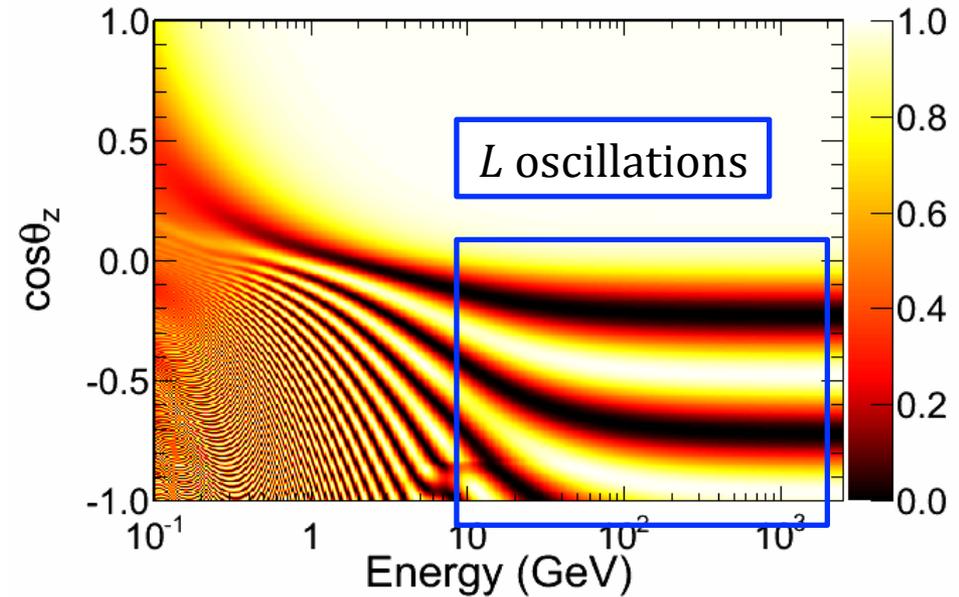
Alex Himmel, Duke

HK Collaboration Meeting

January 29<sup>th</sup>, 2015

# Lorentz Violation and Sterile Neutrinos

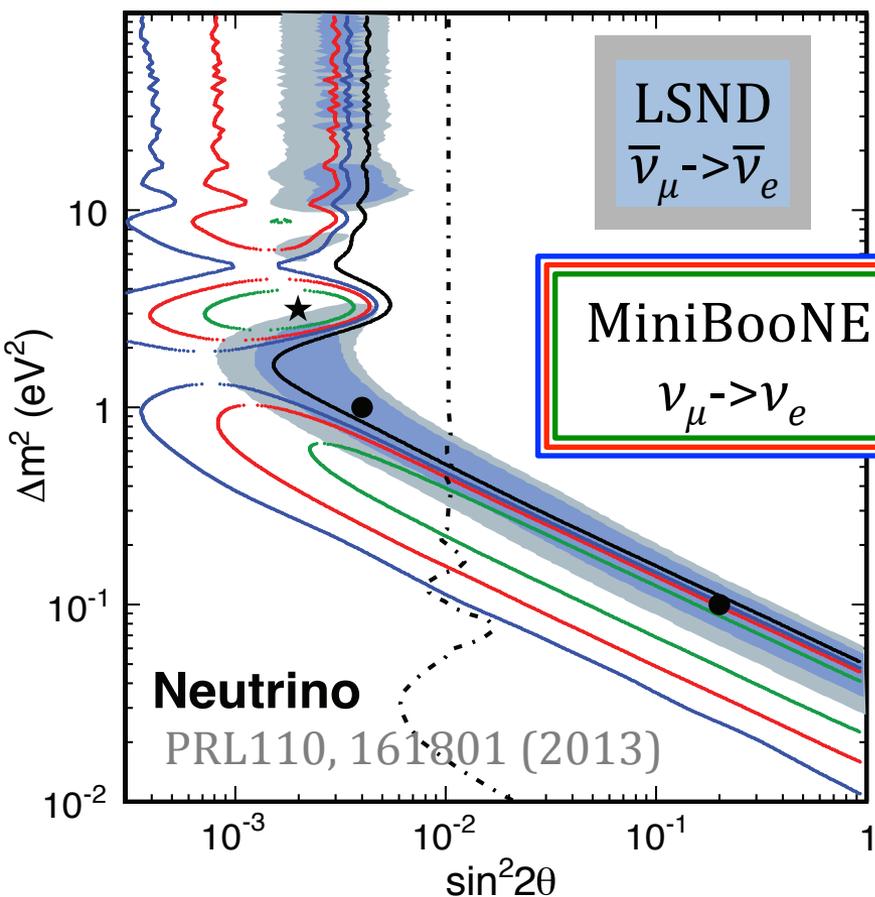
- Searches for exotic oscillations mixed with standard 3-flavor oscillations
- Lorentz violation:
  - $L$  and  $LE$  oscillations
- Sterile neutrinos:
  - Fast oscillations at short distances
  - Sterile matter effect at long distances



# Sensitivity Studies

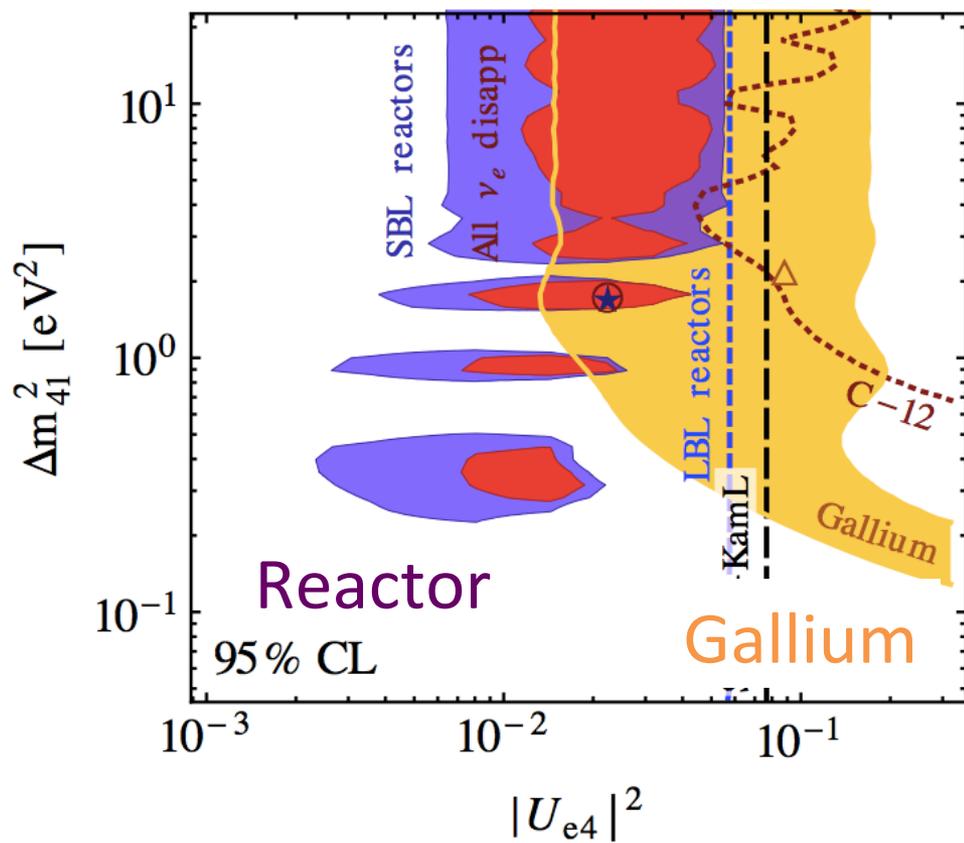
- Presenting sensitivity studies to non-standard oscillations based on analyses in SK.
- Scaling SK-II MC sensitivities to:
  - 10 years of livetime
  - 560/22.6 for FC/PC (scale by mass)
  - 14.4 for Up- $\mu$  (scale by area)
- Constrain 3-flavor oscillation parameters based on external measurements:
  - Errors included as uncertainties
  - Sources:
    - T2K 2014 PRL  $\nu_\mu$  disappearance for  $\theta_{23}, \Delta m^2_{23}$
    - SK Solar for  $\theta_{12}, \Delta m^2_{12}$
    - PDG weighted average for  $\theta_{13}$

# Sterile Neutrinos



$\nu_e$  Appearance

$$\sin^2 2\theta_{\mu e} = 4|U_{e4}|^2|U_{\mu 4}|^2$$



$\nu_e$  Disappearance

$$\sin^2 2\theta_{ee} = 4|U_{e4}|^2(1 - |U_{e4}|^2)$$

# Not so simple...

- With only 1 sterile neutrino, should see three correlated signatures:

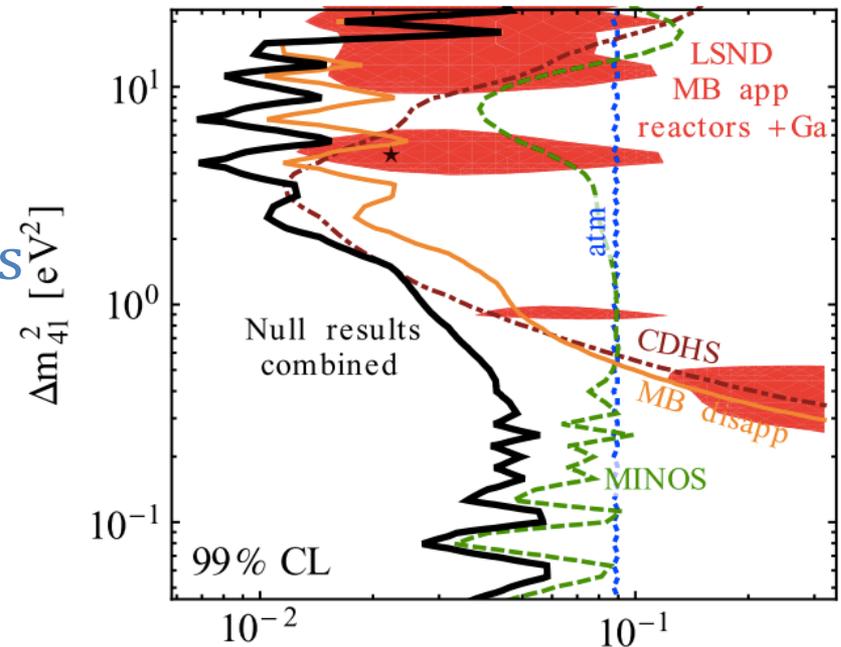
- $\nu_e$  appearance  $\sin^2 2\theta_{\mu e} = 4|U_{e4}|^2|U_{\mu4}|^2$
- $\nu_e$  disappearance  $\sin^2 2\theta_{ee} = 4|U_{e4}|^2(1 - |U_{e4}|^2)$
- $\nu_\mu$  disappearance  $\sin^2 2\theta_{\mu\mu} = 4|U_{\mu4}|^2(1 - |U_{\mu4}|^2)$

- No evidence yet of  $\nu_\mu$  disappearance

- Creates tension in global fits

- Models with additional neutrinos tried

- No consensus yet



# Super-K Sterile Model

- A fully generic sterile model **is difficult** computationally
  - Cannot calculate both active ( $\nu_e$ ) and sterile (NC) matter effects together
- So, we need to perform 2 different fits:

No- $\nu_e$ Fit	Sterile Vacuum Fit
<ul style="list-style-type: none"><li>– Fit for <math> U_{\tau 4} ^2 +  U_{\mu 4} ^2</math></li><li>– NC matter effects only</li><li>– Required for <math> U_{\tau 4} ^2</math></li><li>– Over-constrains <math> U_{\mu 4} ^2</math></li></ul>	<ul style="list-style-type: none"><li>– Fit for <math> U_{\mu 4} ^2</math> only</li><li>– <math>\nu_e</math> matter effects only</li><li>– Most accurate <math> U_{\mu 4} ^2</math> limit</li><li>– No <math> U_{\tau 4} ^2</math> limit</li></ul>

# No- $\nu_e$ Fit

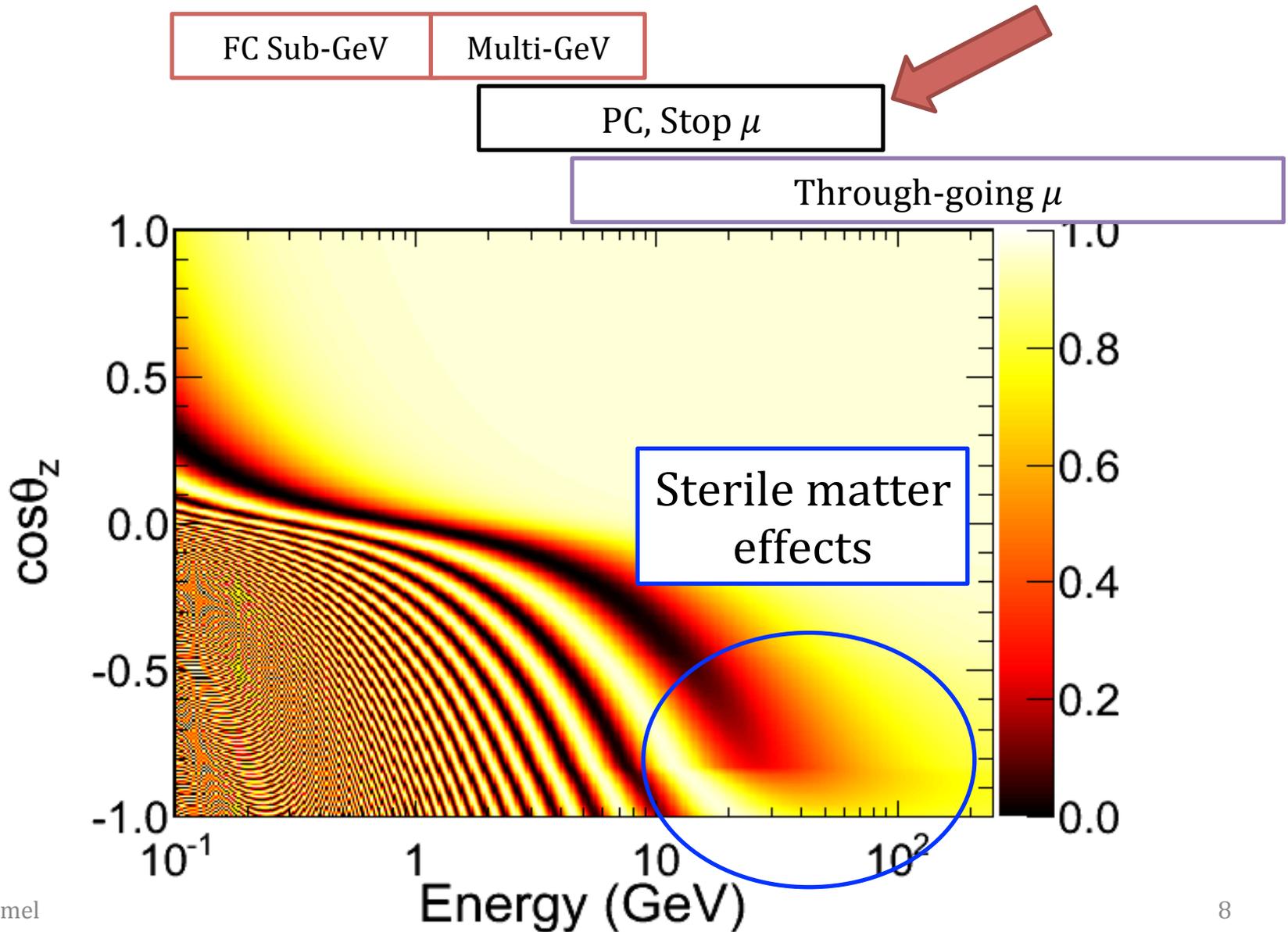
- The  $\nu_\mu$  survival probability (3+1):

$$P_{\mu\mu} = (1 - |U_{\mu 4}|^2)^2 P_{\mu\mu}^{(2)} + |U_{\mu 4}|^4$$

$$\begin{aligned}
 H^{(2)} &= H_{sm}^{(2)} + H_s^{(2)} : \\
 &= \frac{\Delta m_{31}^2}{4E} \begin{pmatrix} -\cos 2\theta_{23} & \sin 2\theta_{23} \\ \sin 2\theta_{23} & \cos 2\theta_{23} \end{pmatrix} \pm \frac{G_F N_n}{\sqrt{2}} \begin{pmatrix} |\tilde{U}_{s2}|^2 & \tilde{U}_{s2}^* \tilde{U}_{s3} \\ \tilde{U}_{s2} \tilde{U}_{s3}^* & |\tilde{U}_{s3}|^2 \end{pmatrix}
 \end{aligned}$$

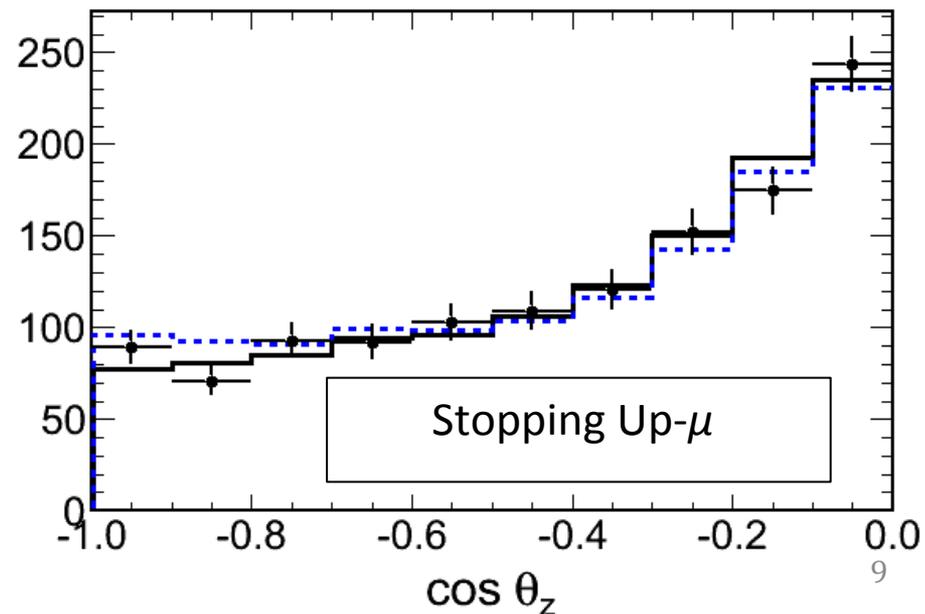
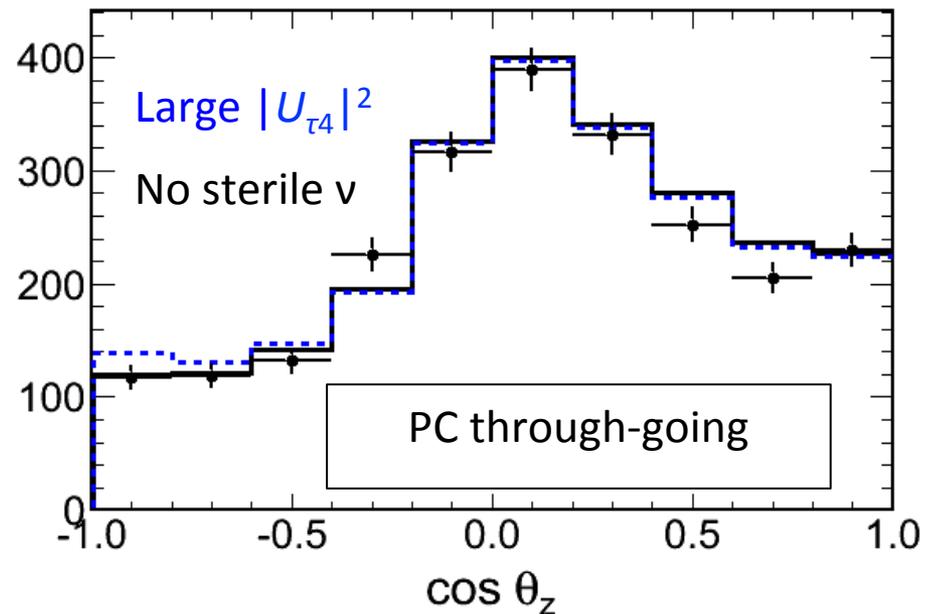
- 2-level system is the benefit of decoupling  $\nu_e$ 's from oscillations
- $\tilde{U}_{si}$  can be written in terms of  $|U_{\tau 4}|^2$  and  $|U_{\mu 4}|^2$  in a 3+1 framework

# No- $\nu_e$ Oscillogram



# Example Zenith Distributions

- Most sensitive samples
  - Energies  $\sim 10$  GeV
- Less disappearance at long path-lengths
  - Up-going events
- Systematic errors fit to both hypotheses
  - Large differences in oscillation probability reduced by systematic errors



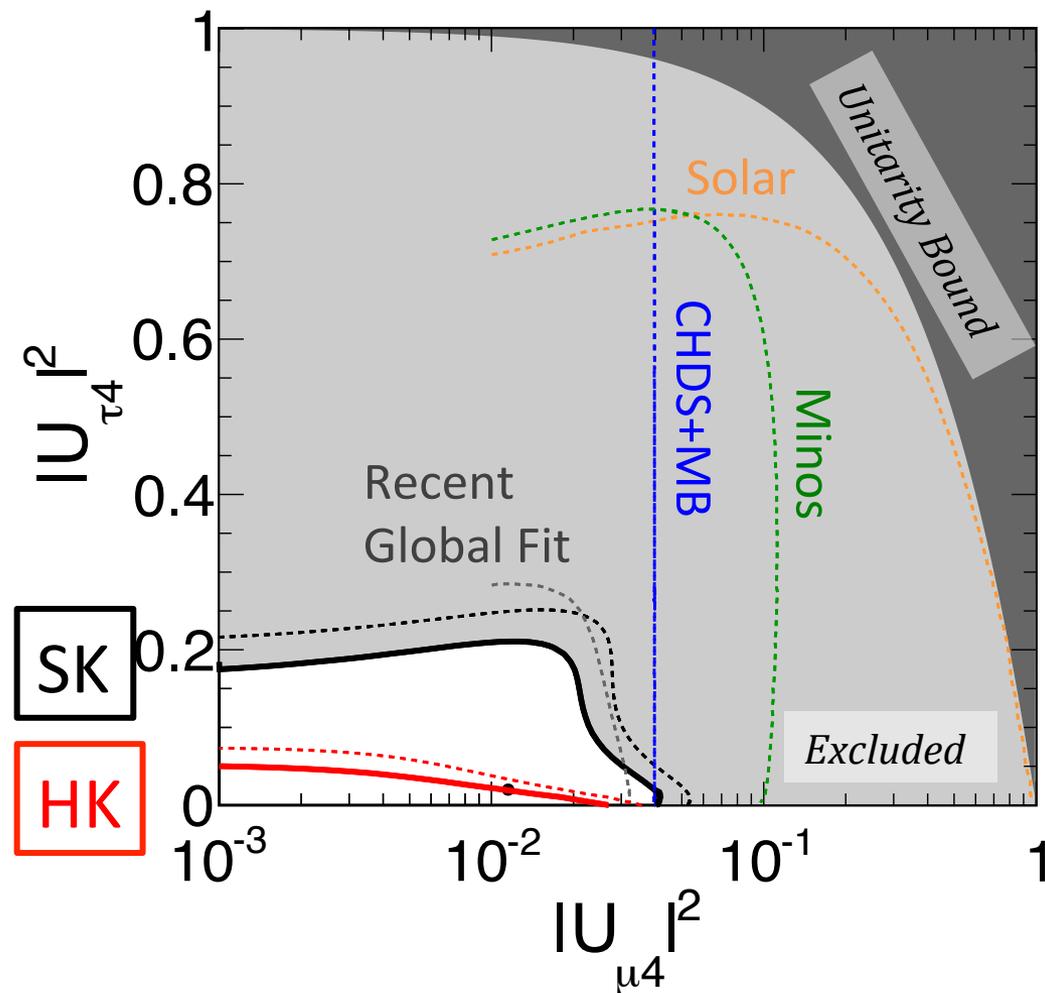
# No- $\nu_e$ Fit Results

99%  $|U_{\tau 4}|^2$  Sensitivity

SK: 0.164

HK: 0.066

Significant improvement  
with the increase in PC  
statistics.



All comparisons from:  
JHEP 1305 (2013) 050

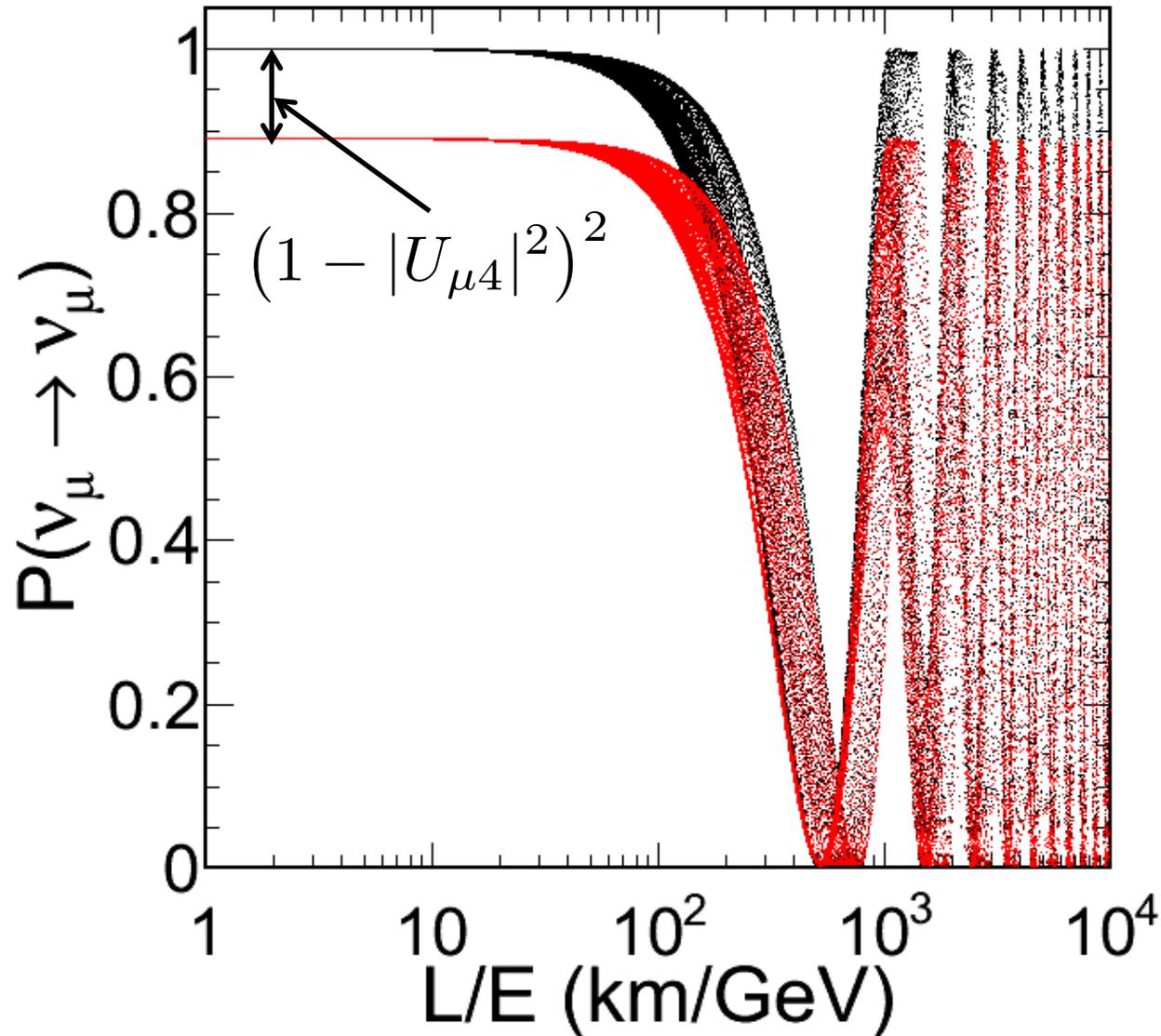
# Sterile Vacuum Fit

- The  $\nu_\mu$  survival probability in 3+1:

$$P_{\mu\mu} = (1 - |U_{\mu 4}|^2)^2 P_{\mu\mu}^{(3)} + |U_{\mu 4}|^4$$

- Here,  $P^{(3)}$  is just the standard 3-flavor oscillation probability
  - Includes  $\nu_e$  matter effects – get  $e$ -like sample normalization right
  - Does not include  $|U_{\tau 4}|^2$

# Sterile Vacuum Oscillations vs. $L/E$



# Sterile Vacuum Fit Results

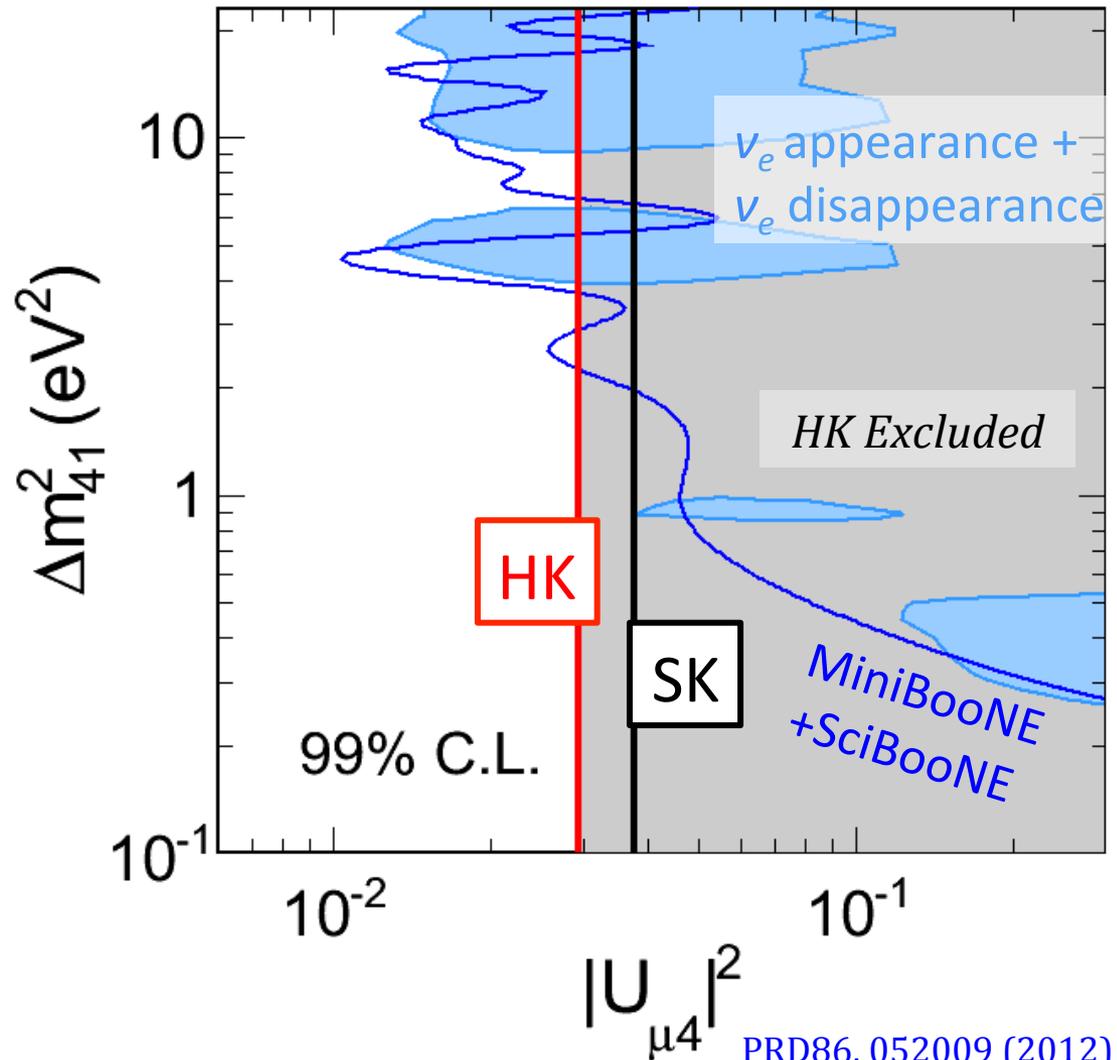
99%  $|U_{\mu 4}|^2$  Sensitivity

SK: 0.038

HK: 0.029

Improvement with HK  
is marginal.

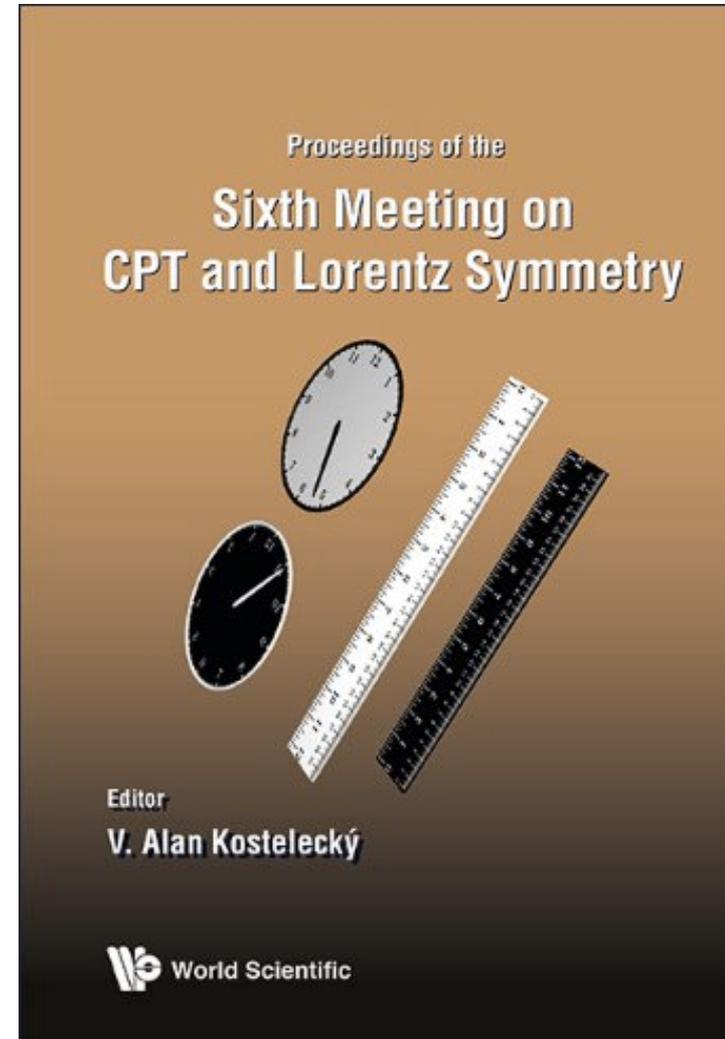
Analysis is dominated  
by systematic errors  
on flu and cross-  
section normalization.



PRD86, 052009 (2012)  
JHEP 1305 (2013) 050

# Lorentz Invariance

- A fundamental symmetry in QFT and general relativity, but small violations predicted in some models
  - Discrete spacetime structure
  - Spacetime foam
- The Standard Model Extension (SME)
  - A QFT with all the properties of the standard model which adds parameters to allow all possible LV terms
- Tested in a wide variety of contexts, including other neutrino experiments
  - MINOS, Double Chooz, LSND, MiniBooNE...



# Standard Model Extension

	Coefficient	Unit	$d$	$CPT$	Oscillation Effect
SK	<b>Isotropic</b>				
	$a_{\alpha\beta}^T$	GeV	3	odd	$\propto L$
	$c_{\alpha\beta}^{TT}$	-	4	even	$\propto LE$
Prev. Exp.	<b>Directional</b>				
	$a_{\alpha\beta}^X, a_{\alpha\beta}^Y, a_{\alpha\beta}^Z$	GeV	3	odd	sidereal variation
	$c_{\alpha\beta}^{XX}, c_{\alpha\beta}^{YZ}, \dots$	-	4	even	sidereal variation

- Focusing on the terms which just affect  $\nu \rightarrow \nu$  oscillation probabilities
  - Other terms generate  $\nu \rightarrow \text{anti-}\nu$  transitions

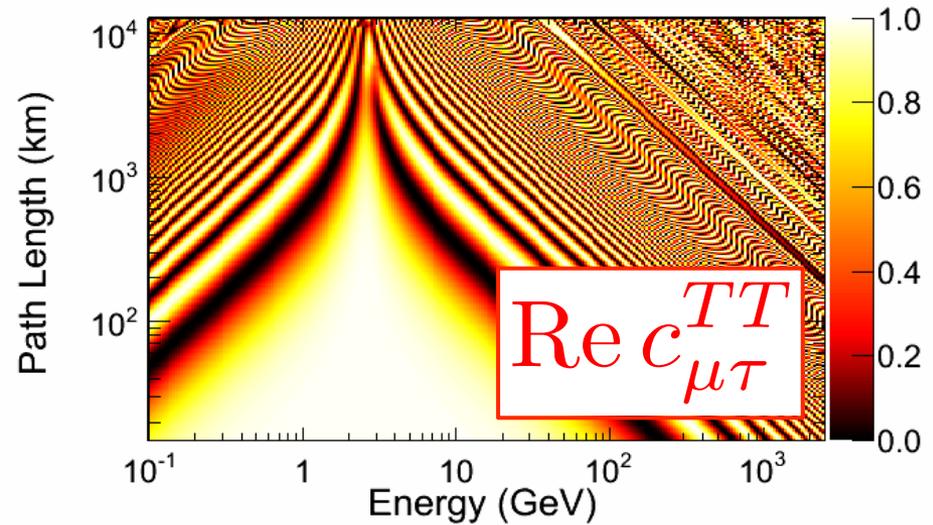
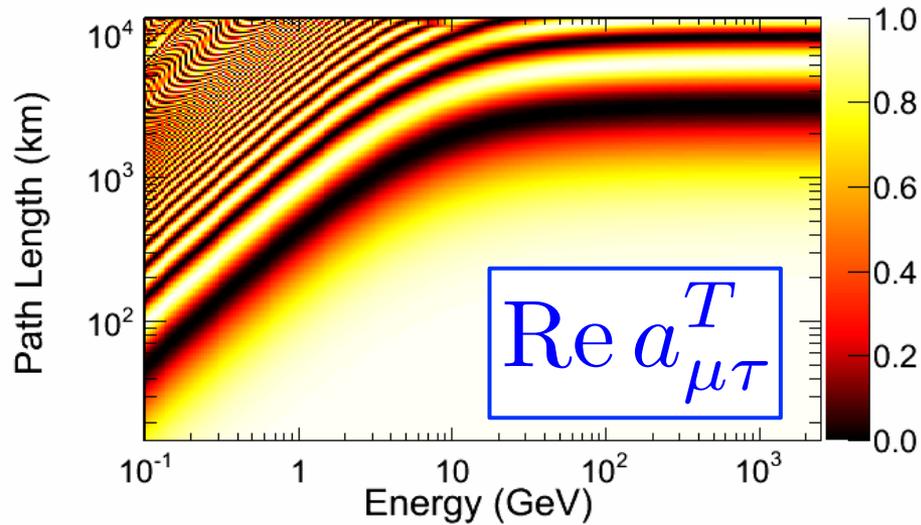
# Neutrino Oscillations with SME

$$H = U \Delta U^\dagger + V_e + H_{LV}$$

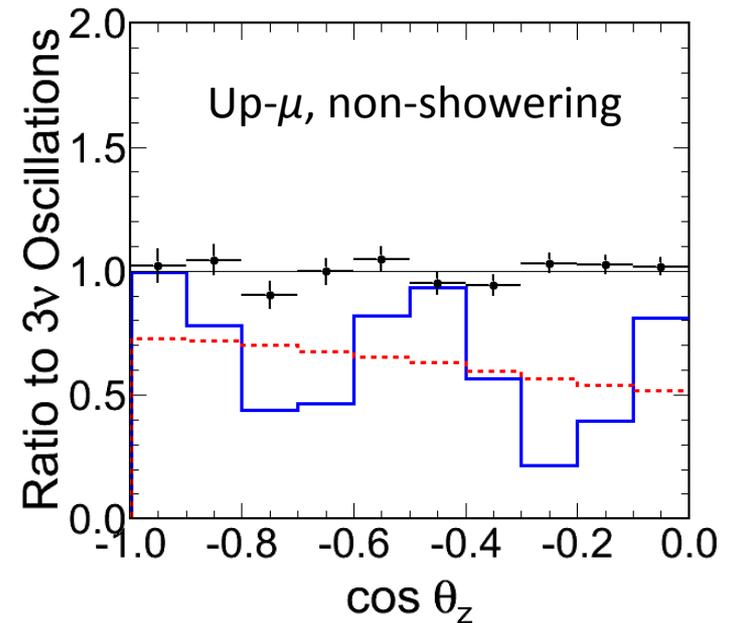
$$H_{LV} = \begin{pmatrix} 0 & a_{e\mu}^T & a_{e\tau}^T \\ (a_{e\mu}^T)^* & 0 & a_{\mu\tau}^T \\ (a_{e\tau}^T)^* & (a_{\mu\tau}^T)^* & 0 \end{pmatrix} - \frac{4E}{3} \begin{pmatrix} 0 & c_{e\mu}^{TT} & c_{e\tau}^{TT} \\ (c_{e\mu}^{TT})^* & 0 & c_{\mu\tau}^{TT} \\ (c_{e\tau}^{TT})^* & (c_{\mu\tau}^{TT})^* & 0 \end{pmatrix}$$

- Previous experiments used 1 of 2 approximations:
  - The short-baseline approximation where there are only  $LV$  oscillations
  - The perturbative approximation where  $H_{LV}$  is assumed to be small.
- Neither is appropriate for SK
  - 30% of our events fail the perturbative conditions
- We use, for the first time, the full diagonalization of the Hamiltonian to calculate oscillation probabilities.

# Lorentz Violation



- $a^T$  introduces  $L$  oscillations at high energy
- $c^{TT}$  introduces  $LE$  oscillations at high energy



# LV Sensitivity

	$e\mu$	$e\tau$	$\mu\tau$		$e\mu$	$e\tau$	$\mu\tau$
$\mathcal{K}(a^T)$ (GeV)	$4 \times 10^{-20}$ MiniBooNE	$8 \times 10^{-20}$ Double Chooz	-	$\mathcal{K}(c^{TT})$	$1 \times 10^{-19}$ MiniBooNE	$1 \times 10^{-17}$ Double Chooz	-
SK:	$2 \times 10^{-23}$	$4 \times 10^{-23}$	$6 \times 10^{-24}$		$2 \times 10^{-26}$	$1 \times 10^{-24}$	$5 \times 10^{-27}$
HK:	$7 \times 10^{-24}$	$2 \times 10^{-23}$	$2 \times 10^{-24}$		$6 \times 10^{-27}$	$7 \times 10^{-25}$	$2 \times 10^{-27}$

- Limits improve by a factor of 1.8-3.6 relative to SK sensitivity

$$- \text{sqrt}(14.4 \times 10 \text{ years} / 13 \text{ years}) = 3.3$$

- Improvements are as expected: incremental on the scale of these searches.

# Conclusions

- Sensitivity studies to non-standard oscillations performed by increasing SK-II lifetime for existing SK studies.
- Sterile neutrino search:
  - ➔ – Improvement in  $|U_{\tau 4}|^2$  limit thanks to increased PC statistics
  - Marginal improvement in  $|U_{\mu 4}|^2$  limit since that is systematically limited
- Lorentz violation search:
  - Improvements of a factor of 2-3
  - Consistent with increase in Up- $\mu$  statistics.

# Backups

# No- $\nu_e$ Fit in 3+N

- The 2-level system in 3+N

$$H^{(2)} = H_{\text{SM}} \pm \underbrace{\frac{G_F N_n}{\sqrt{2}} \sum_{\alpha} \begin{pmatrix} |\tilde{U}_{\alpha 2}|^2 & \tilde{U}_{\alpha 2}^* \tilde{U}_{\alpha 3} \\ \tilde{U}_{\alpha 2} \tilde{U}_{\alpha 3}^* & |\tilde{U}_{\alpha 2}|^2 \end{pmatrix}}_{H_s(A_s, \theta_s)}$$

- Extend to multiple sterile neutrinos with a sum over sterile species  $\alpha$
- Because it is a 2-level system, any number of sterile parameters reduce to 3:  $A_s, \theta_s, |U_{\mu 4}|^2$
- We also make the results of this fit available in these parameters.

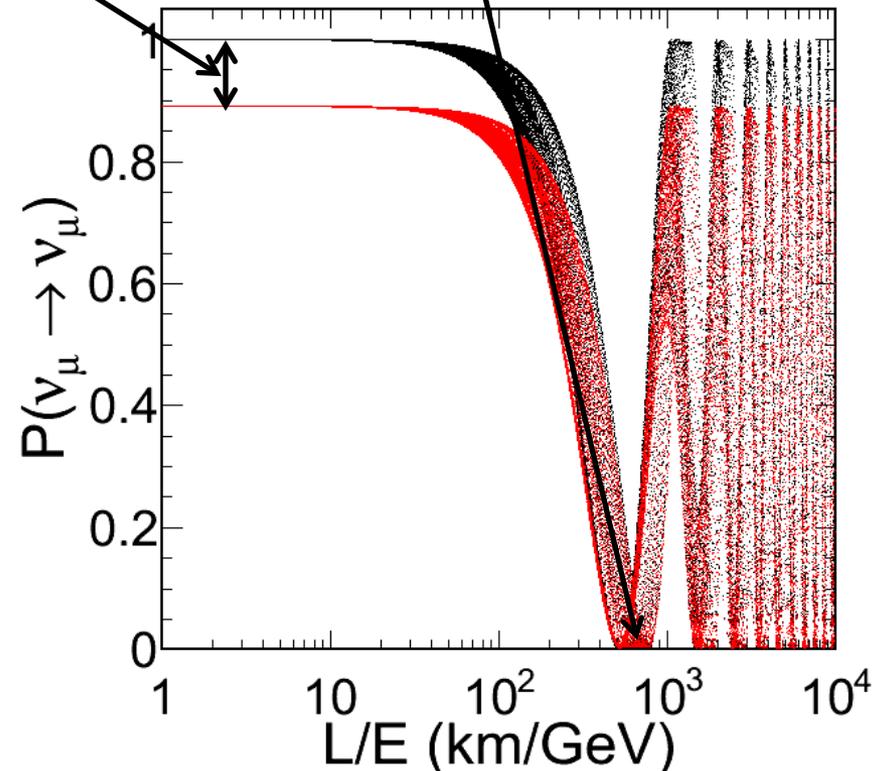
# Sterile Vacuum Fit in 3+N

- The  $\nu_\mu$  survival probability in 3+N:

$$P_{\mu\mu} = (1 - d_\mu^2)^2 P_{\mu\mu}^{(3)} + \sum_\alpha |U_{\alpha 4}|^4$$

$$d_\mu = \sum_\alpha |U_{\alpha 4}|^2$$

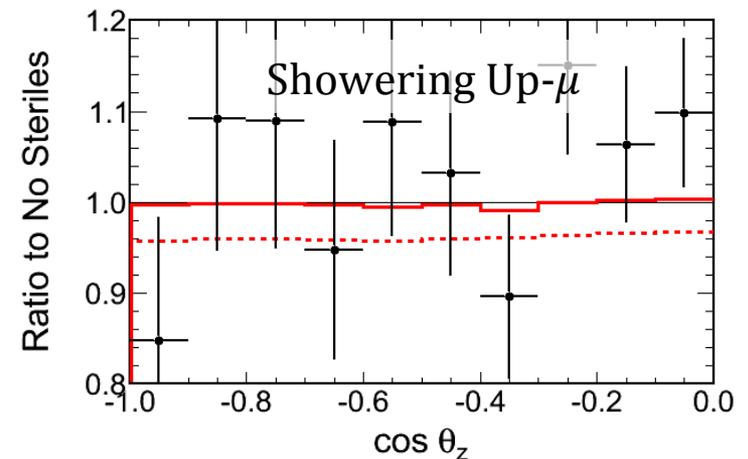
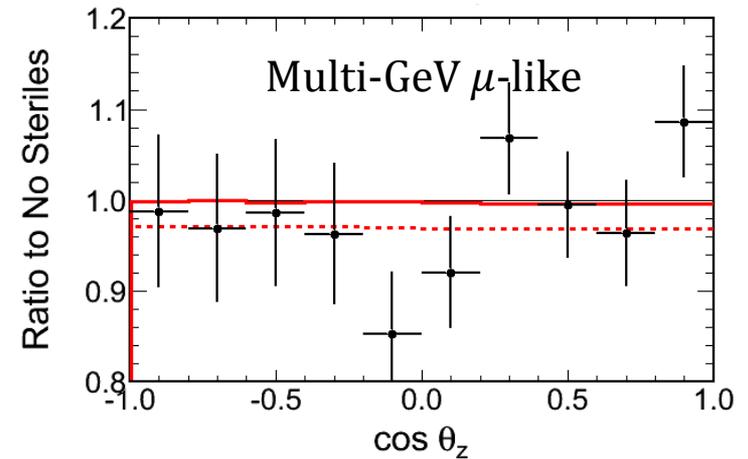
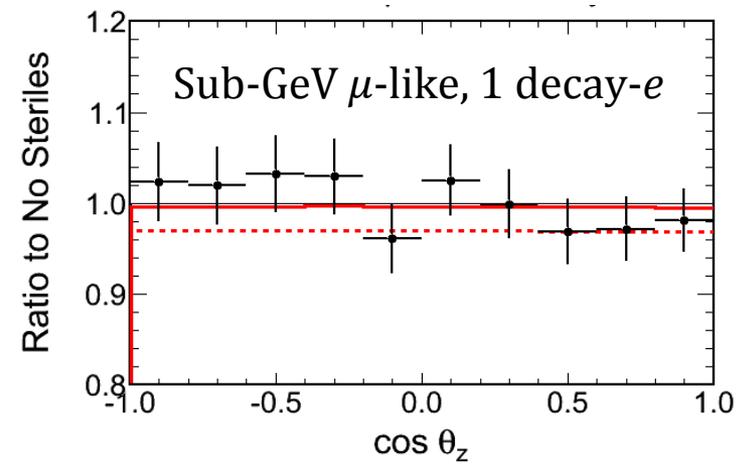
- Very similar to the 3+1 formula with  $|U_{\mu 4}|^2 \rightarrow d_\mu$
- Correspondence is not exact in constant term but that term is second-order and much harder to observe



# Sterile Vacuum Results

- Best fit:  $|U_{\mu 4}|^2 = 0.016$ 
  - Shown as solid line at right
  - Dashed line shows fit without minimizing systematics
- All of the  $\chi^2$  improvement at best fit is in systematics.
  - Fit is systematically limited

Systematic	No Steriles	Best Fit
$\nu_\mu/\nu_e$ flux, $E < 1$ GeV	$-0.52\sigma$	$-0.07\sigma$
$\nu_\mu/\nu_e$ flux, $E$ 1-10 GeV	$-0.50\sigma$	$-0.11\sigma$
CCQE $\nu_\mu/\nu_e$	$0.38\sigma$	$-0.01\sigma$



# Sterile Vacuum Fit Results

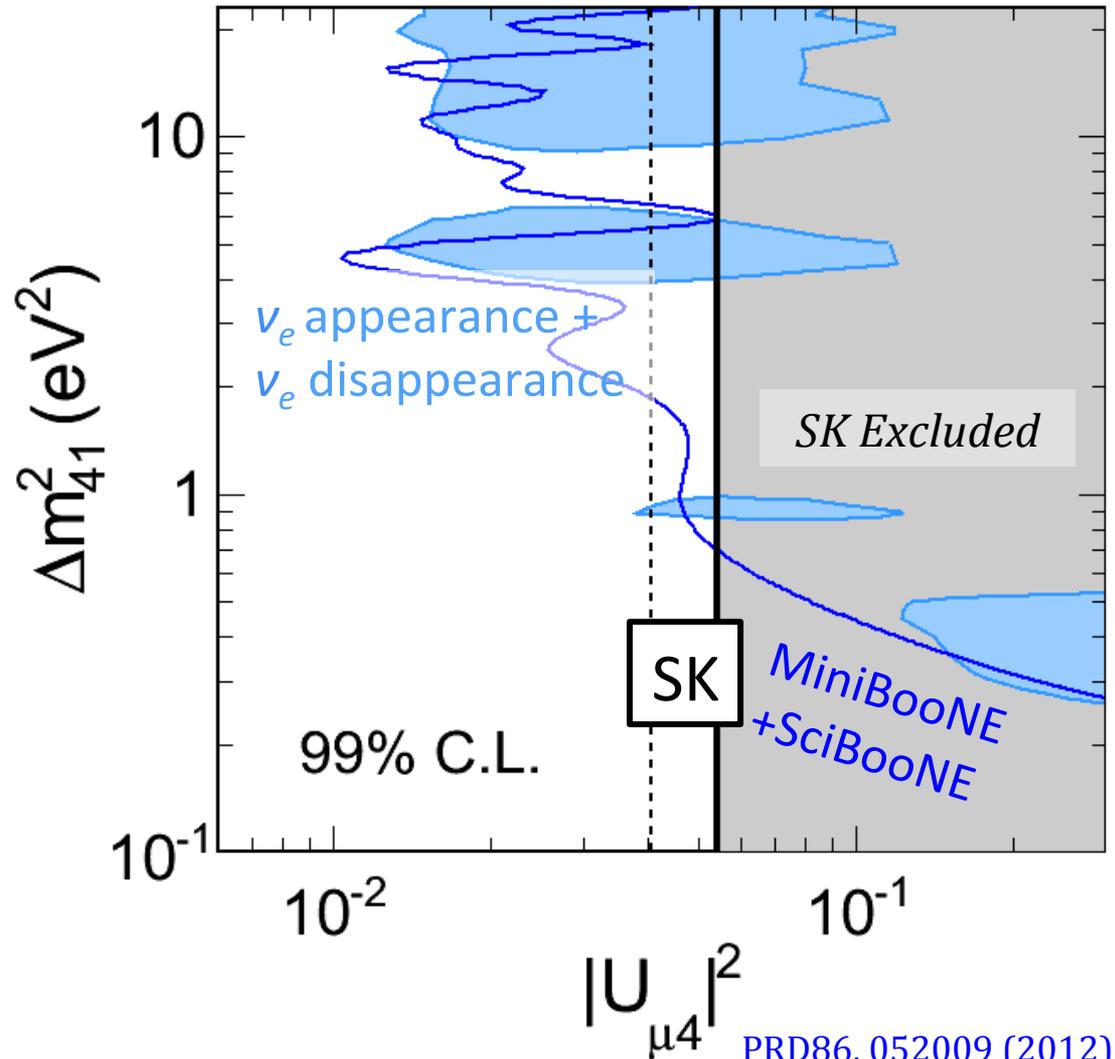
$|U_{\mu 4}|^2 < 0.041$  at 90% C.L.

$|U_{\mu 4}|^2 < 0.054$  at 99% C.L.

Sensitivity: 0.024 at 90%

As with similar experiments,  
no strong sterile-driven  $\nu_\mu$   
disappearance

- $\Delta\chi^2$  of 1.1 between the best fit and no sterile neutrinos.



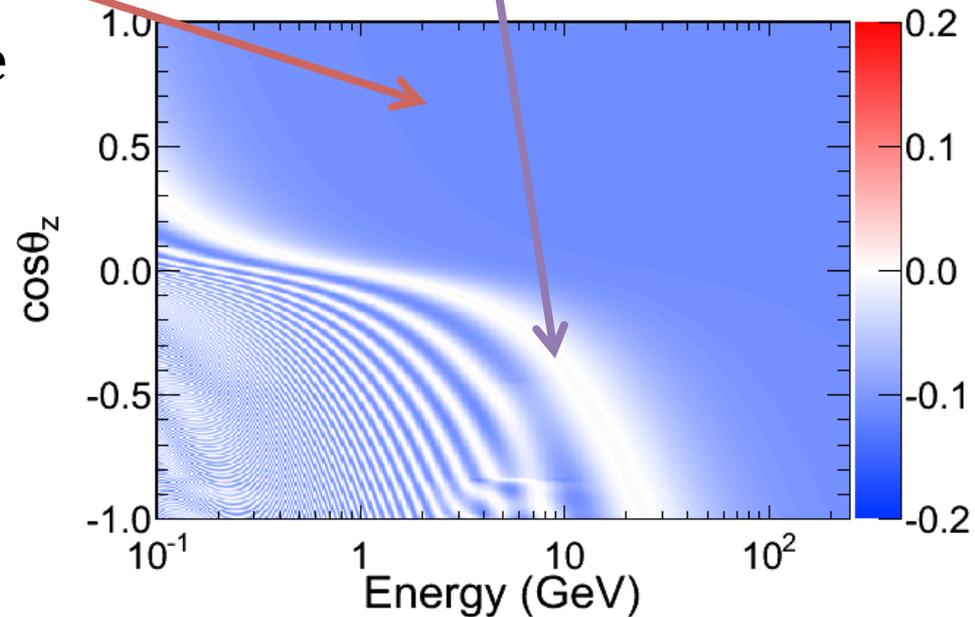
# Extending to 3+N Models: Hydrogen-Earth

$$P_{\mu\mu} = (1 - d_\mu)^2 P_{\mu\mu}^{(3)} + \sum_{i \geq 4} |U_{\mu i}|^4$$

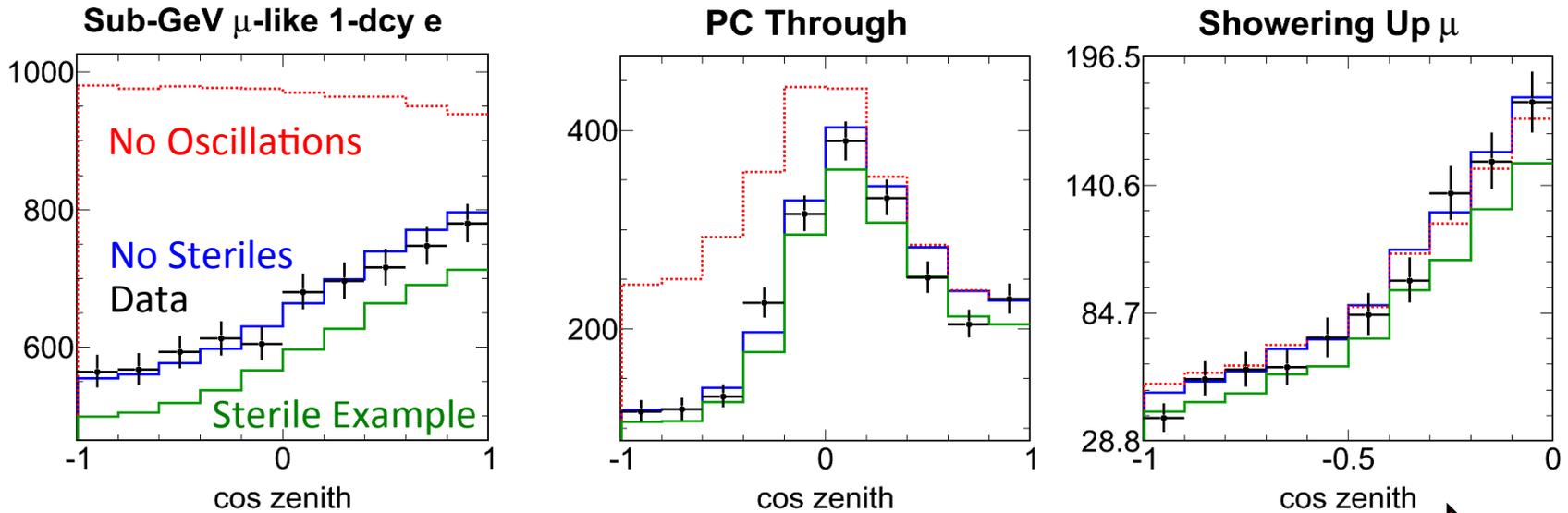
- Substitute sum for single value

$$|U_{\mu 4}|^2 \rightarrow d_\mu = \sum_{i \geq 4} |U_{\mu i}|^2$$

- **Exact in first term**,  
approximate in the second
- SK is *much* more sensitive to  
the **first term** than the **second**



# Fit for $|U_{\mu 4}|^2$



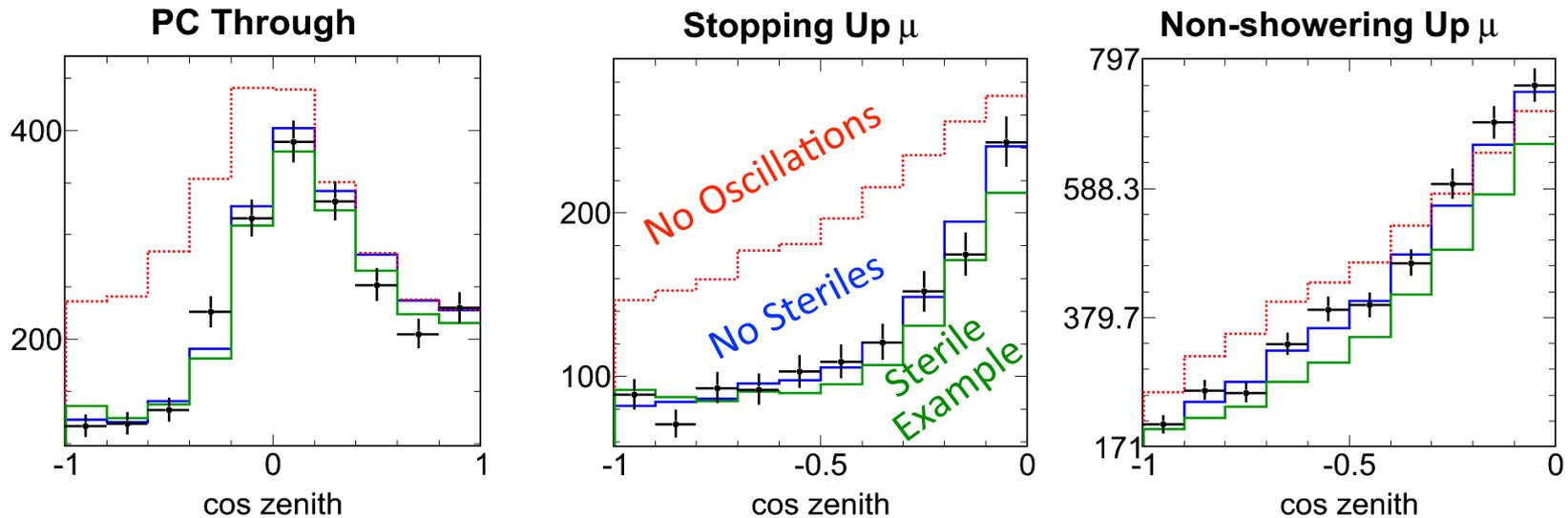
100's of MeV

Few GeV

1 TeV+

- Signature is extra disappearance in all  $\mu$  samples
  - Correlated change at all energies, all  $\cos \theta_z$
  - $\mu/e$  flux uncertainty an important systematic
- Bug was in this fit – NC events were not oscillating
  - Sensitivity improved by a few percent

# Fit for $|U_{\tau 4}|^2$ (with $|U_{\mu 4}|^2$ )



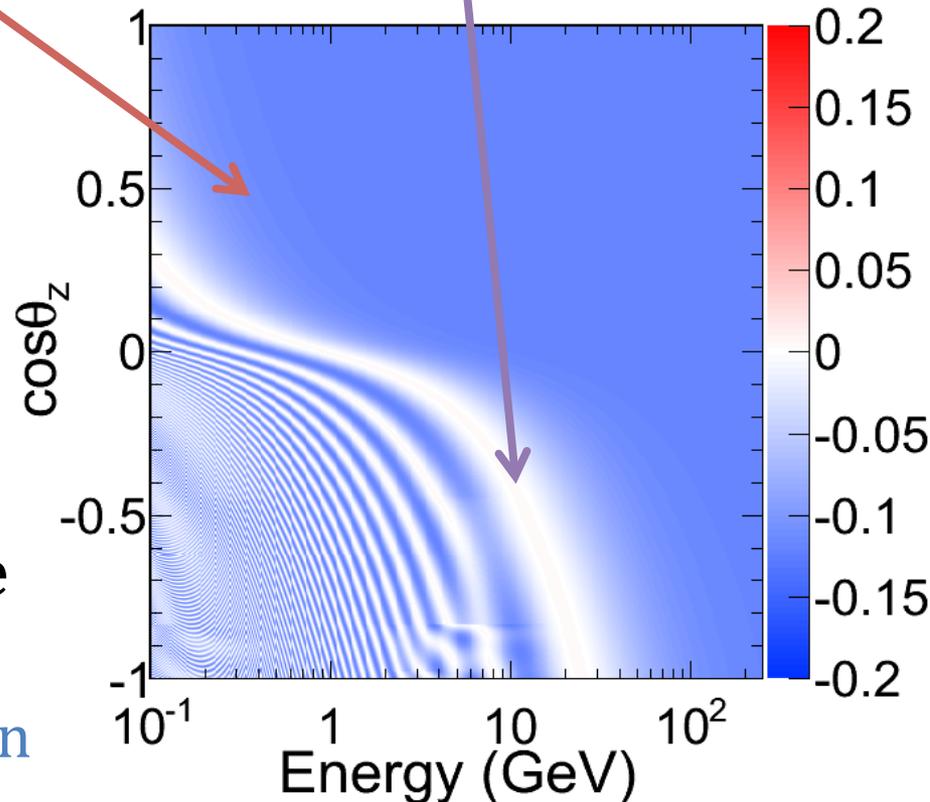
5-100 GeV

- NC Matter effects create shape distortion in PC/Up- $\mu$  zenith distribution
  - Less disappearance in most upward bins, still have extra disappearance in downward bins

# 3+N $\approx$ 3+1 for Super K

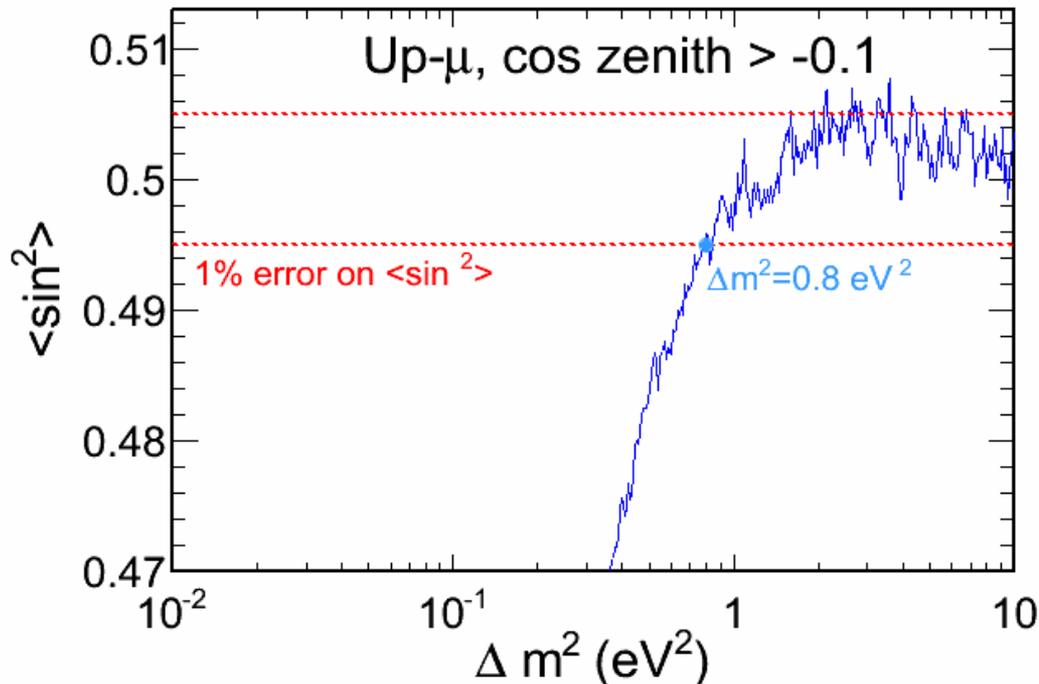
$$P_{\mu\mu} = \left(1 - |U_{\mu 4}|^2\right)^2 P_{\mu\mu}^0 + \sum_{i \geq 4} |U_{\mu i}|^4$$

- The first sterile term:
  - Controls extra disappearance
  - Is the same for any Nsterile
- The second sterile term:
  - Fills in the minima
  - Varies for Nsterile
- Our experiment is *much* more sensitive to **first term**
  - Beam experiments, focusing on the first oscillation dip, *are* sensitive to the second term.



# When is $\Delta m^2_{41}$ no longer “large”?

- When do the oscillations no longer appear fast?
  - This will be the worst at short L’s and large E’s, so lets focus on Up- $\mu$  with  $\cos \theta_z > -0.1$
  - Loop through all these events and calculate the mean of  $\sin^2(\Delta m^2 L/4E)$  for various  $\Delta m^2$
- Doing this, the approximation is valid down to  $\sim 0.8 \text{ eV}^2$



# When is $\Delta m^2_{41}$ no longer “large”?

- However, the limit on  $|U_{\mu 4}|^2$  is driven by the low  $|U_{\tau 4}|^2$  region.
  - In this region, the dominant samples are Sub-GeV muons
  - Almost no power comes from Up- $\mu$
- For these samples, the “large” assumption is  $\sim$ always valid so  $|U_{\mu 4}|^2$  limit really is a vertical line in  $\Delta m^2$  to a good approximation

