

# Probing Higgs Boson CP Properties with $ttH$ at the LHC and the future pp collider

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New particle searches confronting the first LHC run-2 data

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In collaboration with Xiao-Gang He and Guan-Nan Li, IJMPA 30(2015)0550156

# Outline

- Motivation
- The status of Higgs measurements, Higgs CP properties
- Effective couplings for the CP-mixed Higgs state,  $ttH$
- Production of  $ttH$  at pp colliders with arbitrary CP-mixing angle
- Discrimination power from different operators for  $t\bar{t}r$  and  $t\bar{t}b\bar{b}$  process and its behaviours at pp colliders
- Summary

# Motivation



Photo: A. Mahmoud  
François Englert



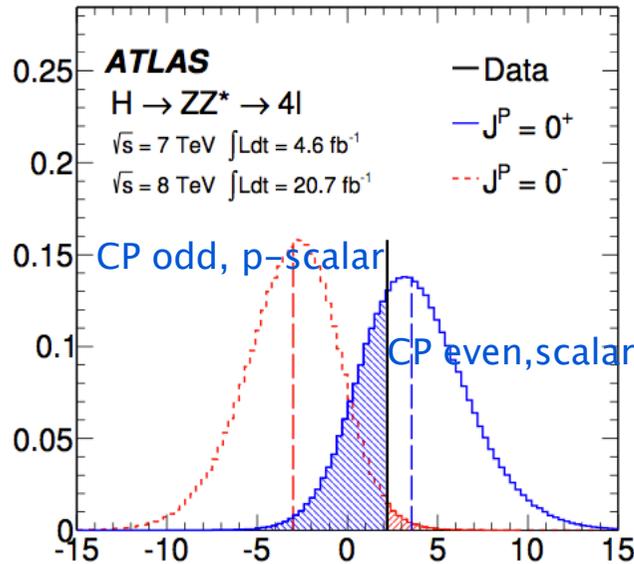
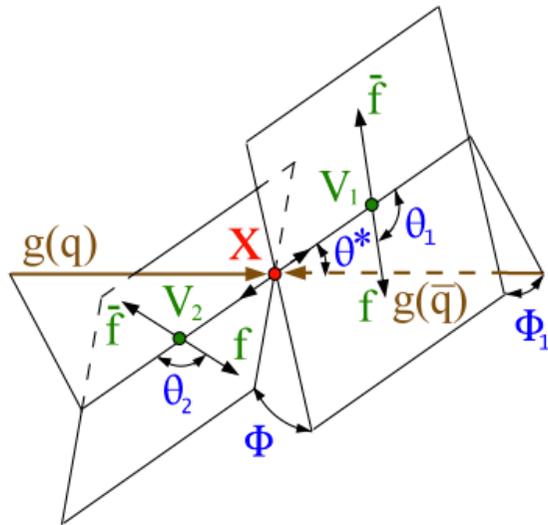
Photo: A. Mahmoud  
Peter W. Higgs

The Nobel Prize in Physics 2013 was awarded jointly to François Englert and Peter W. Higgs *"for the theoretical discovery of a mechanism that contributes to our understanding of the origin of mass of subatomic particles, and which recently was confirmed through the discovery of the predicted fundamental particle, by the ATLAS and CMS experiments at CERN's Large Hadron Collider"*

## Higgs boson

- Just the discovery of the Higgs boson is not sufficient to validate the minimal SM
- In the SM, the only fundamental neutral scalar is a  $J^{PC} = 0^{++}$  state
- Various extensions of the SM can have several Higgs with different CP properties: e.g. MSSM has two CP-even and one CP-odd states
- Therefore, should a neutral spin-0 particle be detected, a study of its CP-properties would be essential to establish it as the SM Higgs boson
- Higgs has the largest coupling to the top quark and top-Higgs interaction can be sensitive to determining Higgs properties and probing BSM physics

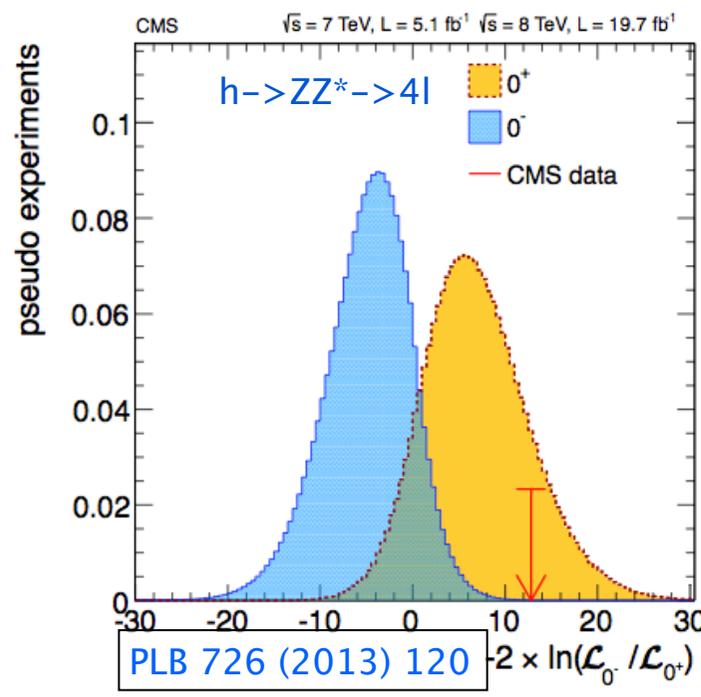
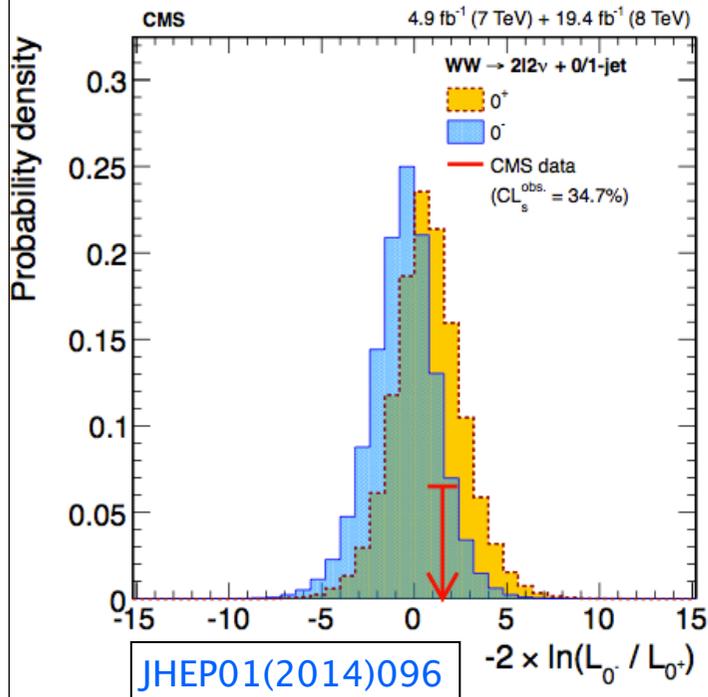
# Higgs spin and CP properties



Discovery of Higgs boson in  $rr, ZZ, WW$  final state is established. The new discovered boson is “SM-like”, signal strength compatible with  $\mu=1$ .

spin=0

PRD 89 (2014) 092007



$J^P = 0^+$  is favored

but Higgs can still have a pseudoscalar component

# Global Fit

general CP mixture state:

$$\phi = \cos \alpha H + \sin \alpha A$$

even

odd

Production rate:  $R(H \rightarrow ff) = \int_{\text{exp}} L dt \cdot \sigma(pp \rightarrow H) \cdot \frac{\Gamma_f}{\Gamma_{\text{th}}}$

→ get partial decay width then  $\Gamma_f \sim g_f^2$  coupling

$$\frac{\Gamma[\phi \rightarrow WW^*]}{\Gamma_{\text{SM}}[H \rightarrow WW^*]} = \frac{\Gamma[\phi \rightarrow ZZ^*]}{\Gamma_{\text{SM}}[H \rightarrow ZZ^*]} = \cos^2 \alpha$$

$$\frac{\Gamma[\phi \rightarrow \tau^+\tau^-]}{\Gamma_{\text{SM}}[H \rightarrow \tau^+\tau^-]} = (y_d \cos \alpha)^2 + (x_d \sin \alpha)^2$$

$H \rightarrow VV, qq, rr, gg : (\cos \alpha, \sin \alpha)$

ATLAS, CMS, CDF/D0 →  $\alpha < 1.1$  (0.7) at 8 (14) TeV LHC Freitas, Schwaller, PRD(2013)

ATLAS, CMS 7+8 →  $\alpha < 0.75$  pi Djouadi, Moreau, EPJC (2013)

( $gg \rightarrow H \rightarrow VV, rr, \text{tata}, bb$ )

$gg \rightarrow H \rightarrow rr$  →  $\alpha < 0.64$  pi Kobakhidze, Wu, Yue, JHEP (2014)

if XS(ttH) error  $\pm 20\%$  →  $\alpha < 0.17$  pi Ellis, Hwang, Sakurai, Takeuchi JHEP (2014)

Cheung, Lee, Tseng PRD(2014), Bhattacharyya, Das, Pal PRD87(2013), Shu, Zhang PRL (2013), Inoue, Ramsey-Musolf, Zhang PRD89(2014), Bolognesi, Gao, Gribsan, Melnikov, Schulze, Tran, Whitbeck, PRD(2012), Englert, Goncalves-Netto, Mawatari, Plehn, JHEP(2013),

# Higgs Yukawa couplings

SM Higgs fermion coupling:  $g=m/v$   $v = 246 \text{ GeV}$

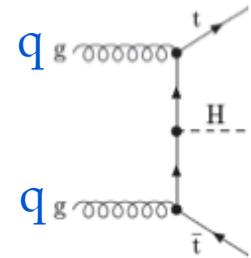
General CP mixed quark-antiquark-Higgs coupling:  $\bar{Q}(c + id\gamma_5)Qh$

For this two processes, production from pp collider:  $gg \rightarrow Q\bar{Q}h$  and  $q\bar{q} \rightarrow Q\bar{Q}h$

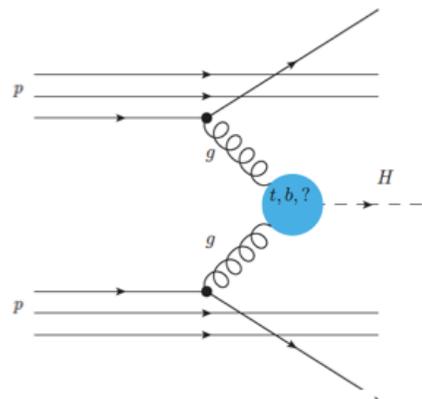
cross section proportional to  $\frac{(c^2 + d^2)}{v^2}$  and  $\frac{(c^2 - d^2) \times m_q^2}{v^2}$

Gunion, He PRL (1996)

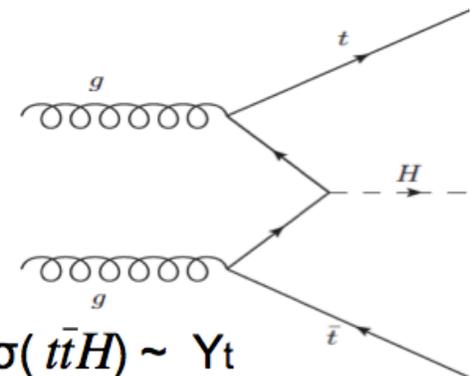
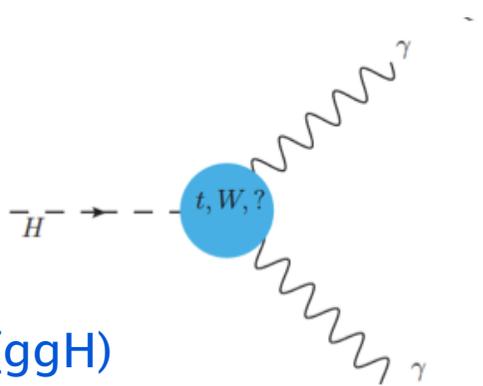
Normalized to 1      enhanced by top mass



The Higgs boson has the largest coupling to the top quark.  $ttH$  ★



indirect (ggH)



direct:  $\sigma(ttH) \sim Y_t$

# Effective couplings for the CP-mixed Higgs state

Fermion:

$$\mathcal{L}_{Ht\bar{t}} = -a \frac{m_t}{v} \bar{t} (\cos \xi + i \gamma_5 \sin \xi) t H,$$

even

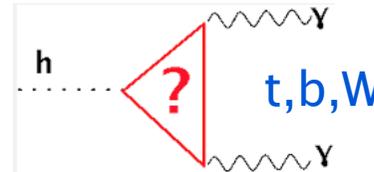
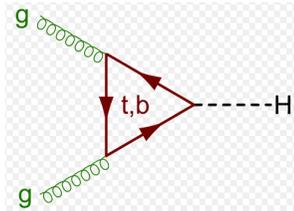
odd

$$a = 1 \quad \cos \xi = 1 \quad \longrightarrow \text{SM Higgs}$$

gauge bosons

$$\mathcal{L}_{HVV} = a \cos \xi \left( \frac{2m_W^2}{v} HW^\mu W_\mu + \frac{2m_Z^2}{v} HZ^\mu Z_\mu \right)$$

CP even component



$$\mathcal{L}_{Hgg} = \left[ I_a^g G_{\mu\nu} G^{\mu\nu} + I_b^g \tilde{G}_{\mu\nu} G^{\mu\nu} \right] H$$

$$\mathcal{L}_{H\gamma\gamma} = \left[ I_a^\gamma F_{\mu\nu} F^{\mu\nu} + I_b^\gamma \tilde{F}_{\mu\nu} F^{\mu\nu} \right] H$$

from factors:

$$I_a^g = a \cos \xi \sum_{i=b,t} F_a(\tau_i) \quad \text{scalar}$$

$$I_b^g = a \sin \xi \sum_{i=b,t} F_b(\tau_i) \quad \text{p-scalar}$$

$$F_a(\tau) = \tau^{-1} [1 + (1 - \tau^{-1})f(\tau)]$$

$$F_b(\tau) = \tau^{-1} f(\tau)$$

$$\tilde{G}_{\mu\nu}: \quad (i/2)\epsilon_{\mu\nu\alpha\beta} G^{\alpha\beta} \quad \text{The dual of } G_{\mu\nu}$$

$$I_a^\gamma = a \cos \xi [2 \sum_{i=b,t} N_C Q_i^2 F_a(\tau_i) - F_1(\tau_W)]$$

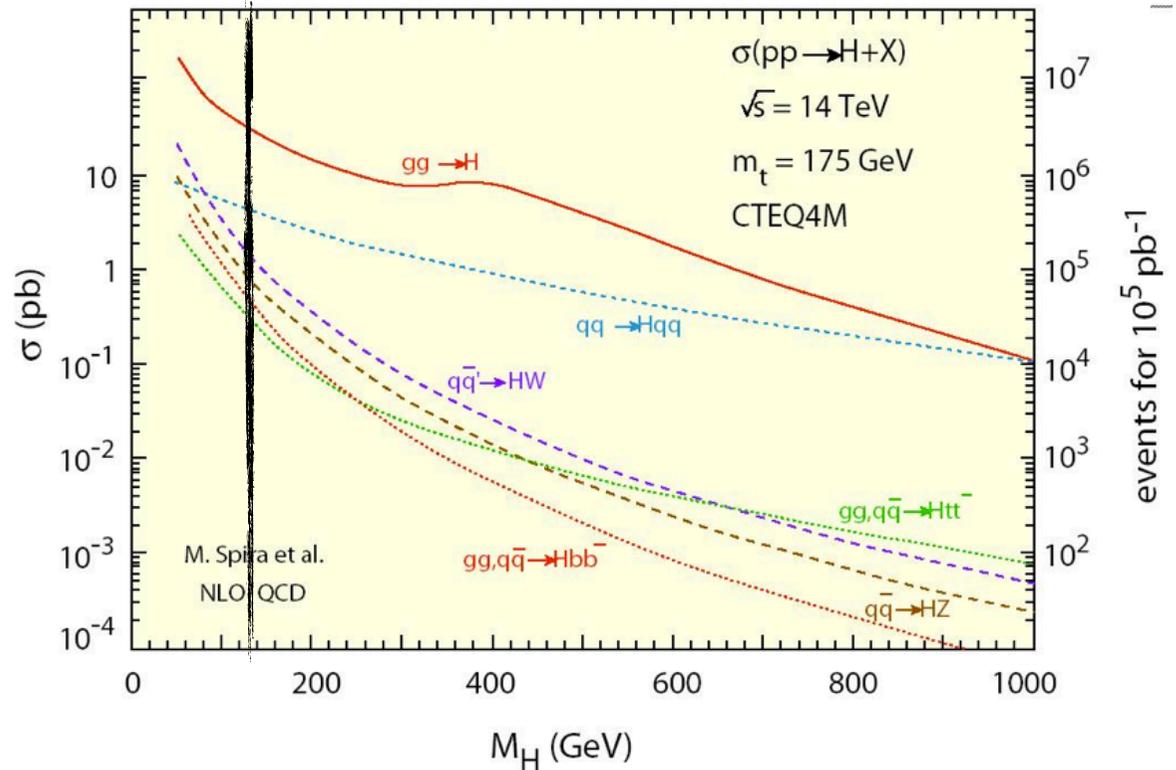
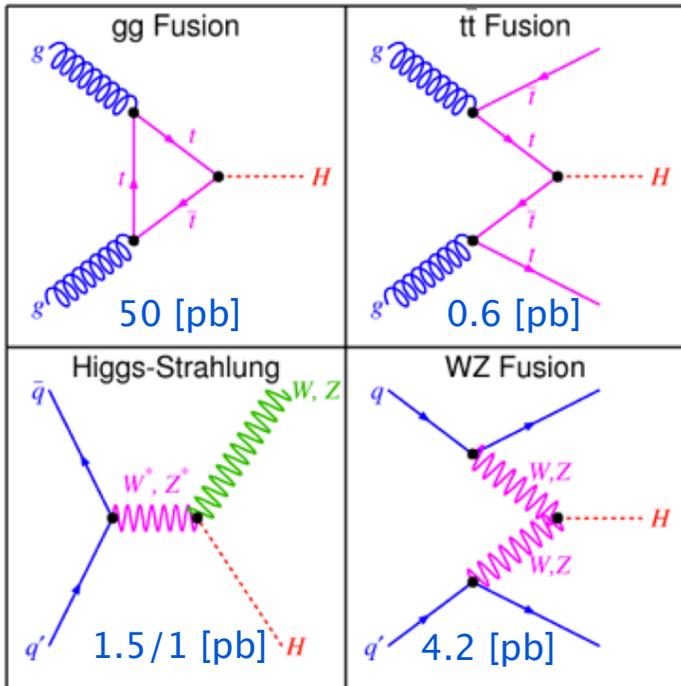
$$I_b^\gamma = 2a \sin \xi \sum_{i=b,t} N_C Q_i^2 F_b(\tau_i)$$

$$F_1(\tau) = 2 + 3\tau^{-1} + 3\tau^{-1}(2 - \tau^{-1})f(\tau).$$

$$f(\tau) = \begin{cases} [\sin^{-1}(\sqrt{\tau})]^2, & \text{if } \tau \leq 1, \\ -\frac{1}{4} \left[ \ln\left(\frac{\sqrt{\tau} + \sqrt{\tau-1}}{\sqrt{\tau} - \sqrt{\tau-1}}\right) - i\pi \right]^2, & \text{if } \tau > 1. \end{cases} \quad \tau_i = m_H^2 / 4m_i^2$$

$$N_C = 3$$

# Higgs production cross section $\rightarrow$ ttH



The ttH represents the smallest XS of the Higgs production mechanisms  $\sim 1/200$

	LHC run I	LHC run II	HE-LHC/SppC/...			
$\sqrt{s}$ (TeV)	7	8	13	14	33	100
XS(ttH) [pb]	0.086	0.13	0.51	0.61	4.6	37

$\times 60$

# Production of $t\bar{t}b\bar{b}/t\bar{t}r\bar{r}$ at pp colliders

Deviations of Higgs coupling to top quark from SM one can show up in different ways.

$$pp \rightarrow t\bar{t}HX \quad \begin{array}{l} H \rightarrow b\bar{b} \\ H \rightarrow \gamma\gamma \end{array}$$

Observed upper bound:

$t\bar{t}b\bar{b}$  (LHC8)  $\rightarrow \sigma < 4.1\sigma_{\text{SM}}, 3.3\sigma_{\text{SM}}$

ATLAS-CONF-2014-011, CMS PAS HIG-14-010

$t\bar{t}r\bar{r}$  (LHC8)  $\rightarrow \sigma < 6.7\sigma_{\text{SM}}$

ATLAS-CONF-2014-061

$$\mathcal{L}_{Ht\bar{t}} = -a \frac{m_t}{v} \bar{t}(\cos \xi + i\gamma_5 \sin \xi)tH,$$

affects both  
production and  
decay

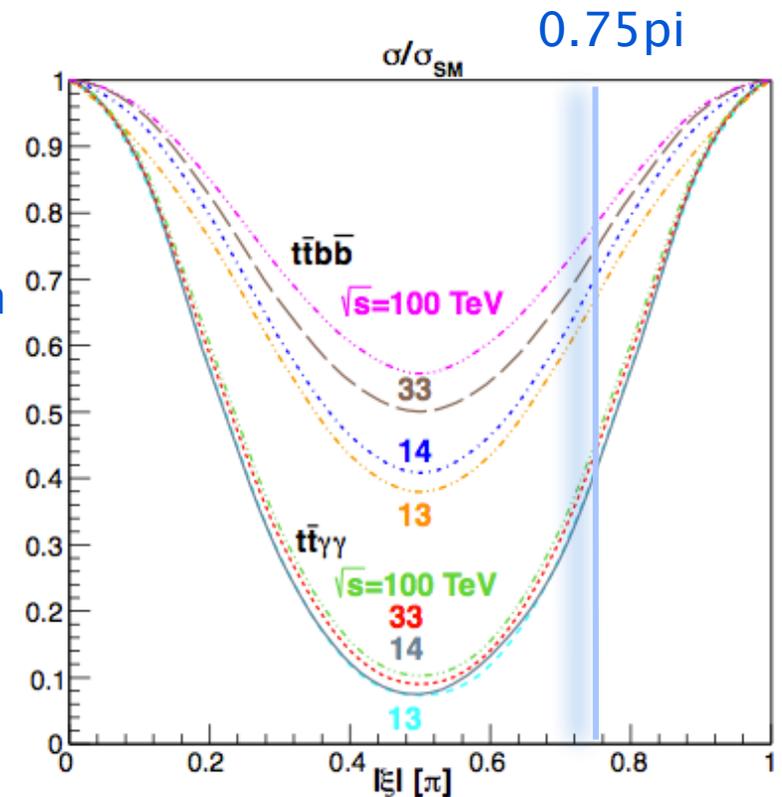
Using MadGraph5\_aMC - heft model  $\rightarrow$  Tree level cross section

Parameter set:  $a = 1$   $m_H = 125$  GeV

mild cut:  $|\eta_{t,\bar{t}}| < 4$ .

K-factor: 1.19 - 1.40

$\sqrt{s} = 13, 14, 33, 100$  TeV,  $\xi = 0 \sim \pi$



# Discussions

- $a=1, \xi=0 \rightarrow$  SM
- $\xi$  increases, XS become considerably smaller than SM predictions  $\rightarrow$  distinguish
- if observation unequal to the prediction of SM  $a=1, \xi=0 \rightarrow$  BSM
- if observation  $\sim$  SM value, one cannot rule out the possibility of BSM ttH coupling

$$\mathcal{L}_{Ht\bar{t}} = -a \frac{m_t}{v} \bar{t} (\cos \xi + i \gamma_5 \sin \xi) t H,$$

reason:  $a$  can be adjusted

$$\xi \neq 0, a=1 \rightarrow XS(\text{ttH}) < SM(\text{ttH})$$

$$\xi \neq 0, 1/a^2 \sim \sigma/\sigma_{SM} \rightarrow XS(\text{ttH}) \sim SM(\text{ttH})$$

- just measuring cross section gives no information about Higgs CP properties, it is desirable to find ways to distinguish SM from BSM ttH coupling independent of the overall scaling parameter  $a$

# Operators in ttH process

operators from ttH final state, sensitive to Higgs CP magnitudes  $\cos^2 \xi - \sin^2 \xi$

$$\mathcal{O}_1 \equiv \frac{(\vec{p}_t \times \hat{n}) \cdot (\vec{p}_{\bar{t}} \times \hat{n})}{|(\vec{p}_t \times \hat{n}) \cdot (\vec{p}_{\bar{t}} \times \hat{n})|}, \quad \mathcal{O}_2 \equiv \frac{p_t^x p_{\bar{t}}^x}{|p_t^x p_{\bar{t}}^x|}$$

$$\mathcal{O}_3 \equiv \frac{(\vec{p}_t \times \hat{n}) \cdot (\vec{p}_{\bar{t}} \times \hat{n})}{p_t^T p_{\bar{t}}^T}, \quad \mathcal{O}_4 \equiv \frac{(\vec{p}_t \times \hat{n}) \cdot (\vec{p}_{\bar{t}} \times \hat{n})}{|\vec{p}_t| |\vec{p}_{\bar{t}}|},$$

$$\mathcal{O}_5 \equiv \frac{p_t^x p_{\bar{t}}^x}{p_t^T p_{\bar{t}}^T}, \quad \mathcal{O}_6 \equiv \frac{p_t^z p_{\bar{t}}^z}{|\vec{p}_t| |\vec{p}_{\bar{t}}|},$$

O1, O2, O3, O5:  
transverse  
momentum of t,tbar

O4, O6 needs full  
momentum of t and tbar

- $p_{t,\bar{t}}^T$  denote the magnitudes of the t and anti-t transverse momenta
- $\hat{n}$  is a unit vector in the direction of the beam line and defines the z axis
- x axis is chosen to be any fixed direction perpendicular to the beam
- There maybe other opeartors but we take the six operators as examples

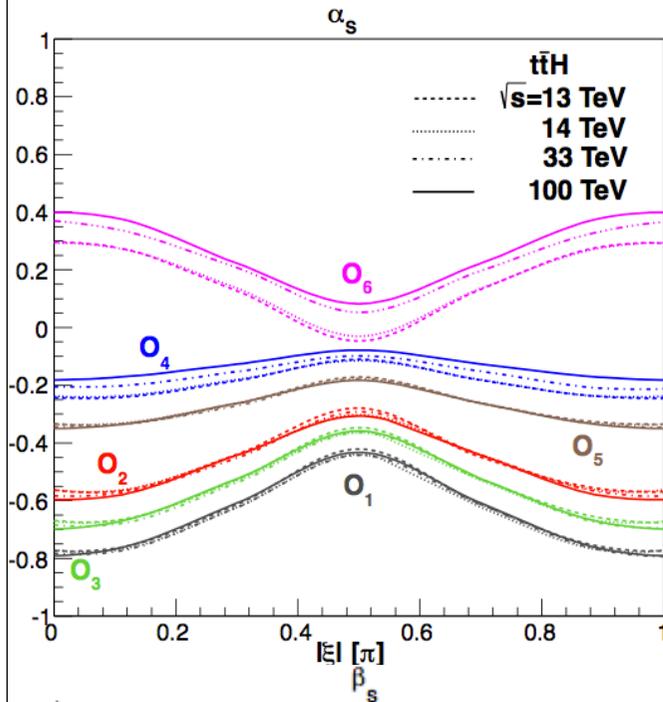
to be independent  
of scaling factor a

$$\alpha[\mathcal{O}_i] \equiv \frac{\int [\mathcal{O}_i] \{d\sigma(pp \rightarrow t\bar{t}XX)/dR\} dR}{\int \{d\sigma(pp \rightarrow t\bar{t}XX)/dR\} dR}$$

XX is the Higgs  
decay products, R  
is the phase space

weighted moments

# Weighted moments



- The changes of  $\alpha_S$  against  $\xi$  is significant providing hope to distinguish Higgs boson coupling with top quark with mixed CP component
- To what accuracy for a given  $\alpha_S$  it can be measured?

experimental errors of  $\alpha_S$ :

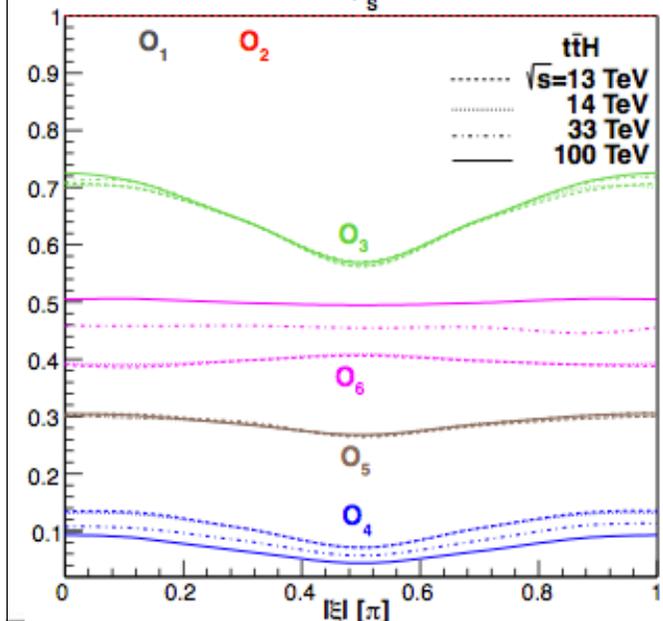
$$\delta\alpha_S = \frac{1}{\sqrt{S}} \left[ \beta_S - \alpha_S^2 + \frac{B}{S} (\beta_B - 2\alpha_B\alpha_S + \alpha_S^2) \right]^{1/2}$$

$S$ ,  $B$  the total # of events for signal and bkg process

$$\beta[\mathcal{O}_i] \equiv \frac{\int [\mathcal{O}_i]^2 \{d\sigma(pp \rightarrow t\bar{t}XX)/dR\} dR}{\int \{d\sigma(pp \rightarrow t\bar{t}XX)/dR\} dR}$$

Note that  $\beta_S(\mathcal{O}_{1,2})$  are equal to 1

$$\mathcal{O}_1 \equiv \frac{(\vec{p}_t \times \hat{n}) \cdot (\vec{p}_{\bar{t}} \times \hat{n})}{|(\vec{p}_t \times \hat{n}) \cdot (\vec{p}_{\bar{t}} \times \hat{n})|}, \quad \mathcal{O}_2 \equiv \frac{p_t^x p_{\bar{t}}^x}{|p_t^x p_{\bar{t}}^x|}$$



# Discrimination power for ttbb and ttrr processes

To quantify the ability to distinguish the SM pure scalar case from any CP-mixed Higgs state of each operator

discrimination  
power:

$$D \equiv \frac{|\alpha_S^{\text{SM}}(\xi = 0) - \alpha_S^\xi(\xi)|}{\delta\alpha_S^{\text{SM}}(\xi = 0)} \quad \xi = 0 \sim \pi$$

for full consideration  $\rightarrow$  top and Higgs decay

Using MadGraph5\_aMC - heft model

H  $\rightarrow$  bb, H  $\rightarrow$  rr

for ttrr, adopt cuts:  $|\eta_{t,\bar{t},\gamma}| < 4$   $p_\gamma^T > 25$  GeV  $|M_{\gamma\gamma} - m_H| < 5$  GeV

for ttbb, adopt cuts:  $|\eta_{t,\bar{t},b,\bar{b}}| < 4$   $p_{b,\bar{b}}^T > 25$  GeV

top  $\rightarrow$  semileptonically, antitop  $\rightarrow$  hadronically

tt  $\rightarrow$  2b-jet + 2j +  $\ell$  +  $\cancel{E}_T \rightarrow n \equiv \mathcal{B}(t \rightarrow bW)^2 \mathcal{B}(W \rightarrow l\nu) \mathcal{B}(W \rightarrow jj) \simeq \left(\frac{9}{10}\right)^2 \times \frac{1}{3} \times \frac{2}{3}$

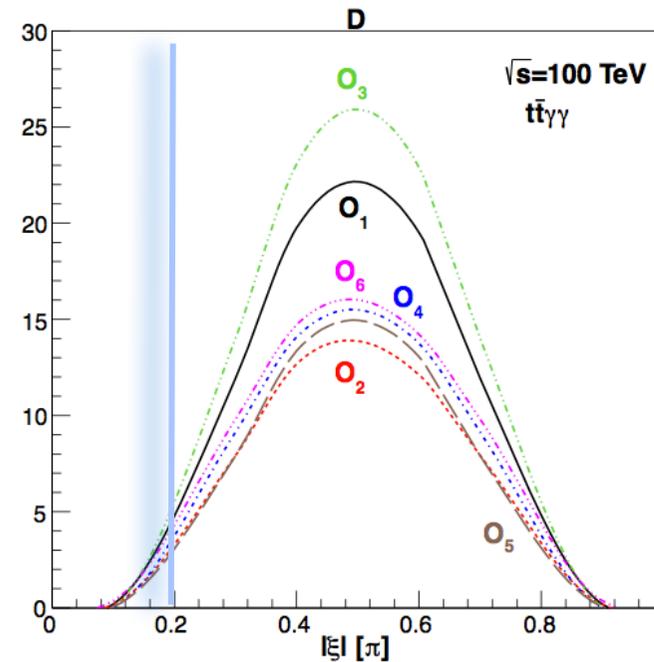
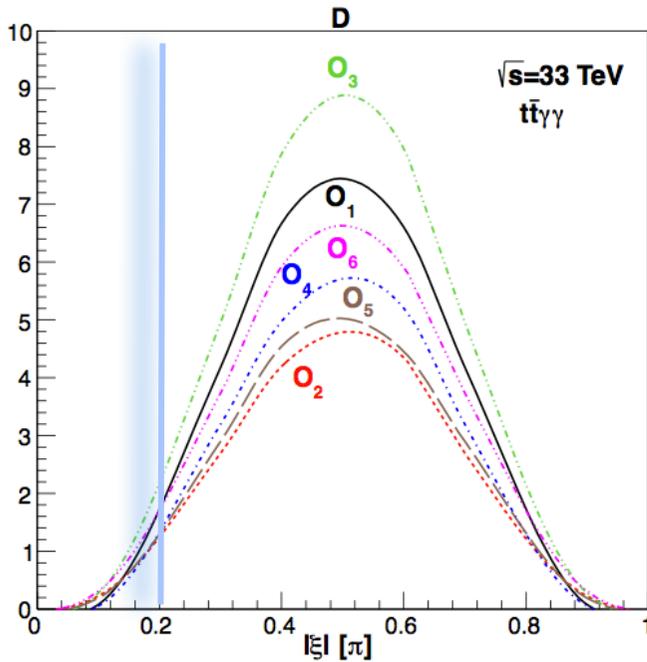
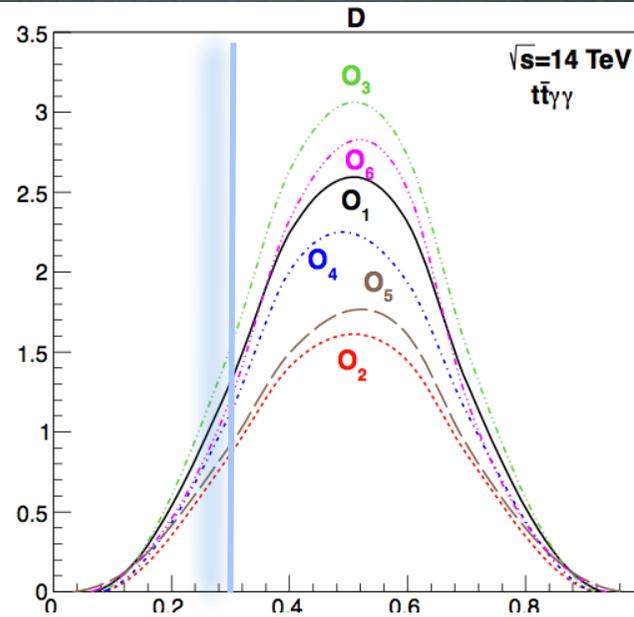
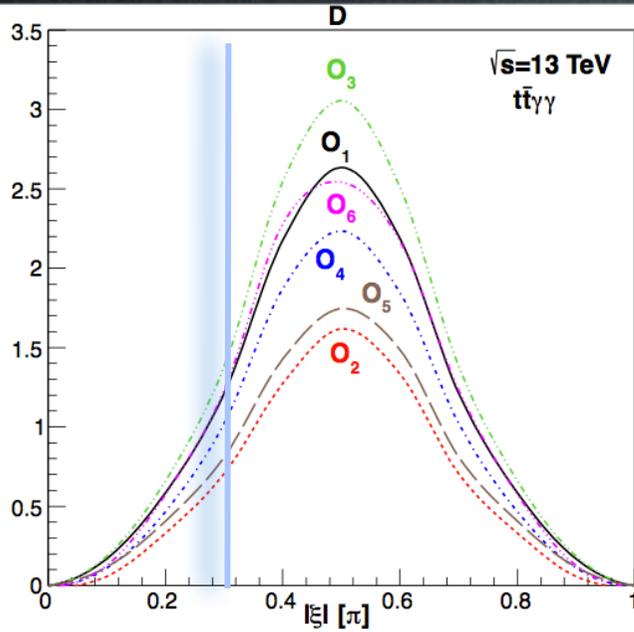
signal cross section reduced by n due to top pair decay for ttrr, n=0.18  $\rightarrow$  D  $\rightarrow$  0.42 D

for ttbb, +b-tagging efficiency (60%), n=0.065  $\rightarrow$  D  $\rightarrow$  0.25 D

# Prediction from discrimination power

- Given  $\alpha_S, \beta_S, \alpha_B, \beta_B$  and bkg event number  $B \rightarrow S$  for certain  $D$
- e.g. to discriminate ttH coupling of  $\xi=0$  from  $\xi=0.3\pi$  at 3sigma level, predictions from ttrr and ttbb are different
  - for ttrr,  $B \sim 50$  (2300) for  $\sqrt{s}=13$  (100) TeV,  $D=3$  requires  $S=750$  (1950) from O3  
Simulated:  $S = 160$  (9900)      13 TeV  $\times$ , 100 TeV  $\checkmark$
  - for ttbb,  $B \sim 8 \cdot 10^5$  ( $8 \cdot 10^7$ ) for  $\sqrt{s}=13$  (100) TeV,  $D=3$  requires  $S = 4 \cdot 10^4$  ( $4 \cdot 10^5$ ) from O6  
Simulated:  $S = 7 \cdot 10^4$  ( $4 \cdot 10^6$ )      13 TeV  $\checkmark$ , 100 TeV  $\checkmark$
- Using ttrr channel, it is difficult to discriminate the ttH SM coupling from a 0.3pi mixed coupling at 3sigma level at 13 TeV, 100 TeV can achieve the discrimination larger than 3sigma level
- From ttbb channel, one is able to discriminate the ttH SM coupling from a 0.3pi mixed state at more than 3sigma, at any collision energy with  $\sqrt{s} > 13$  TeV.

# Discrimination power for $t\bar{t}r\bar{r}$



assume:  $\mathcal{L} = 300 \text{ fb}^{-1}$

$\mathcal{L} = 3 \text{ ab}^{-1}$   $D \rightarrow 3.2D$

$O_1, O_3, O_4, O_6$  are most useful  
balancing the sensitivity and errors

$$O_3 \equiv \frac{(\vec{p}_t \times \hat{n}) \cdot (\vec{p}_{\bar{t}} \times \hat{n})}{p_t^T p_{\bar{t}}^T}$$

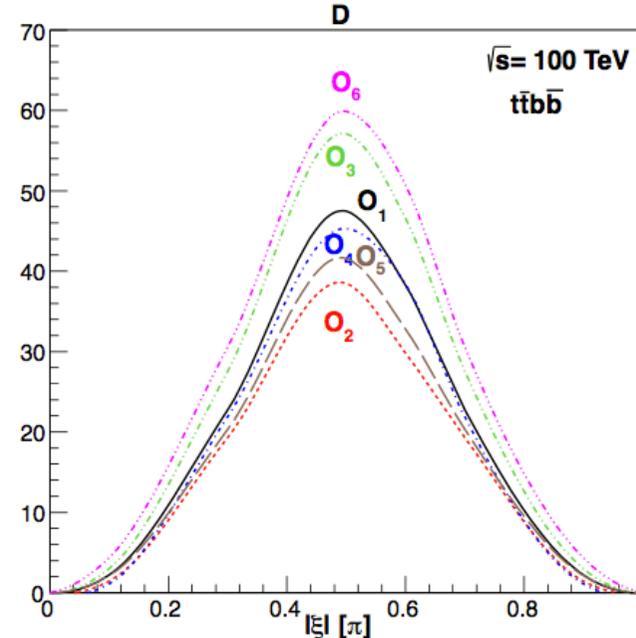
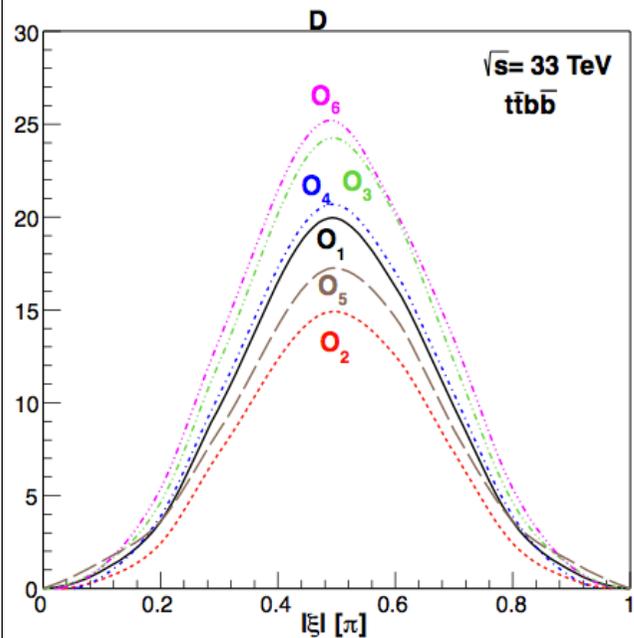
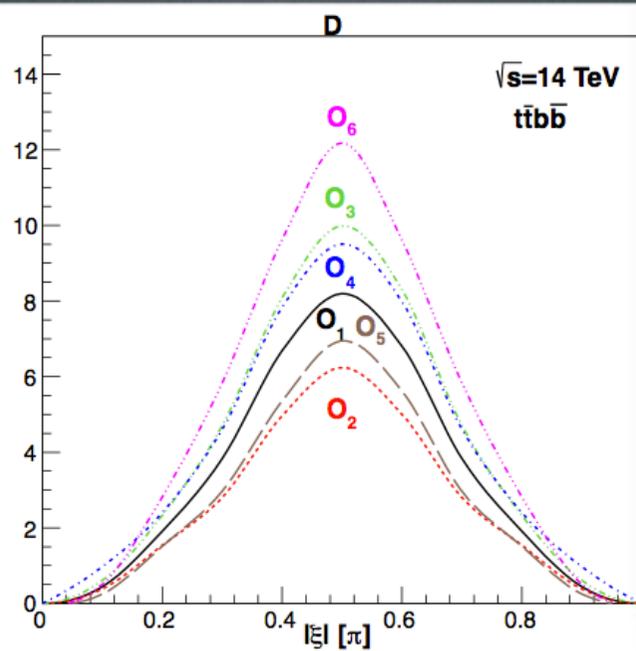
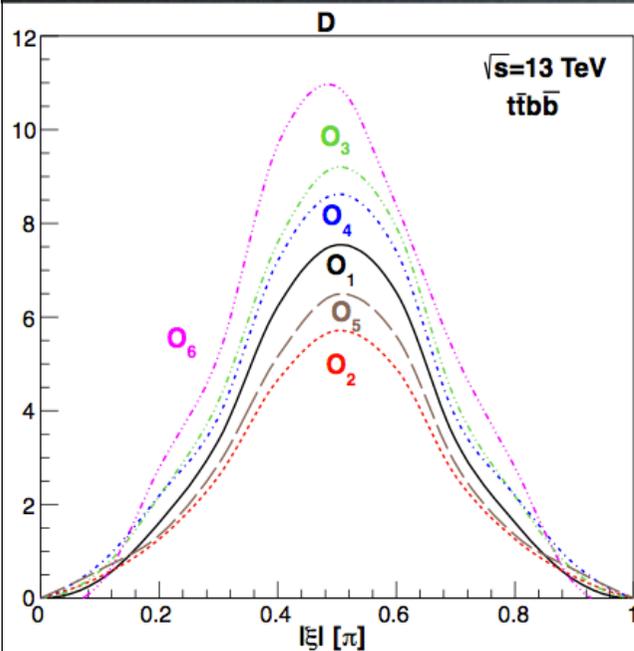
at 13,14 TeV,  $D < 3$ ;  
HL-LHC,  $\xi_i > 0.3\pi$ ,  $D > 3$

at 33, 100 TeV,  $D > 3$   
with  $\xi_i > 0.2\pi$

$O_3$  performs the best  
for all operators

at  $\xi_i = 0.5\pi$ , all the  
operators reach maximal  $D$

# Discrimination power for $t\bar{t}b\bar{b}$



$H > b\bar{b}$  decay modes show better discrimination powers due to the large event rate of the Higgs to  $b\bar{b}$  decay branching ratio

O3 and O6 give the best discrimination powers

$$O_3 \equiv \frac{(\vec{p}_t \times \hat{n}) \cdot (\vec{p}_{\bar{t}} \times \hat{n})}{p_t^T p_{\bar{t}}^T}$$

$$O_6 \equiv \frac{p_t^z p_{\bar{t}}^z}{|\vec{p}_t| |\vec{p}_{\bar{t}}|}$$

imposing further cuts on  $t\bar{t}b\bar{b}$  final state (jet multiplicities) will obtain even better discrimination power

# Summary

- The Higgs boson  $H$  has the largest coupling to the top quark  $t$ . The  $ttH$  interaction can be sensitive to the investigation of BSM.
- We studied the potential of determining Higgs boson CP properties at the LHC and future 33 TeV and 100 TeV pp colliders by analysing various operators from  $ttH$  final state.
- When the CP mixing angle increases, the cross section becomes smaller than SM one.  $\rightarrow$  distinguish the SM  $ttH$  coupling with BSM
- Weighted moments and discrimination power are defined for  $ttbb$  and  $ttrr$  process, at  $L=300/\text{fb}$ , we find that for  $ttrr$  the discrimination power is below  $3\sigma$  at the LHC, at 33 TeV and 100 TeV, more than  $3\sigma$  sensitivity can be reached.  $ttbb$  process can provide more than  $3\sigma$  discrimination power in a wide range at the LHC and 33, 100 TeV pp colliders.
- Detector simulations and more interesting phenomenologies...

Thanks for your attention!