

$SU(2)_X$ vector DM at the LHC

Takaaki Nomura (KIAS)

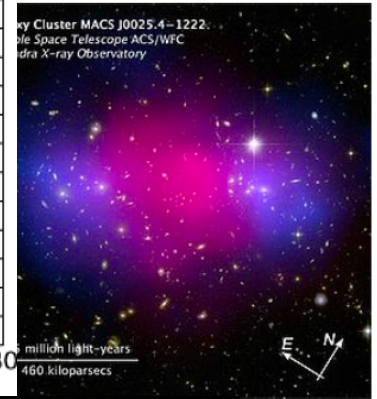
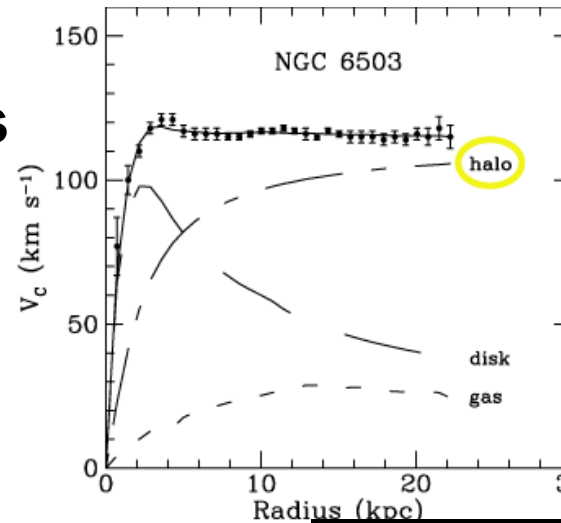
Based on the paper: C. H. Chen, T. N. arXiv:1507.00886

Many observations indicate the existence of dark matter

❖ Rotation of spiral galaxies

$$v(r) \propto \sqrt{M(r)/r}$$

$M(r) \propto r$ in outside of visible region



❖ Clusters of galaxies

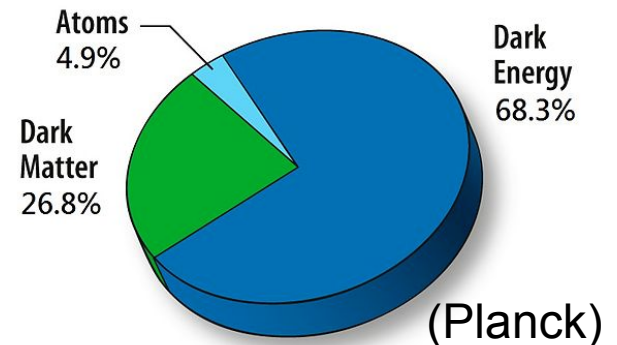
❖ Gravitational lensing

❖ Formation of Large scale structure

❖ Bullet Clusters

❖ CMB anisotropy : WMAP, Planck

Only through gravitational interaction



TODAY

Vector DM from Hidden $SU(2)_X$ gauge symmetry

❖ $SU(2)_X$ model with quadruplet scalar field

- $SU(2)_X$ is spontaneously broken to Z_3 symmetry
- Gauge boson can be Z_3 charged : DM candidate

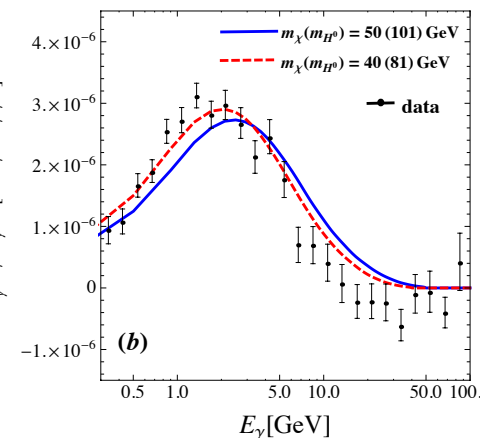
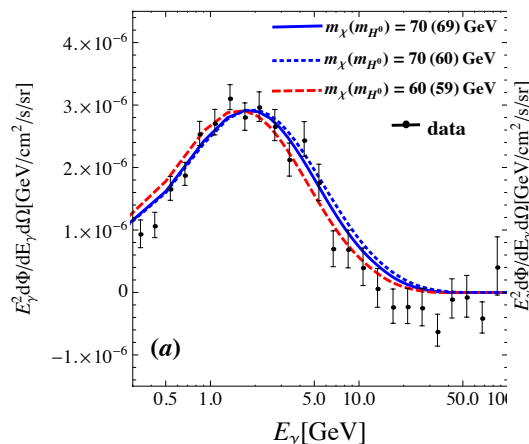
❖ $SU(2)_X$ DM phenomenology

- DM annihilate into SM particles via Higgs-dark Higgs mixing
- Explaining galactic center gamma-ray excess

(C.H.Chen, T.N. PLB 746 (2015) 351, 1501.07413)

$$m_{DM} = 40 \sim 100 \text{ GeV}$$

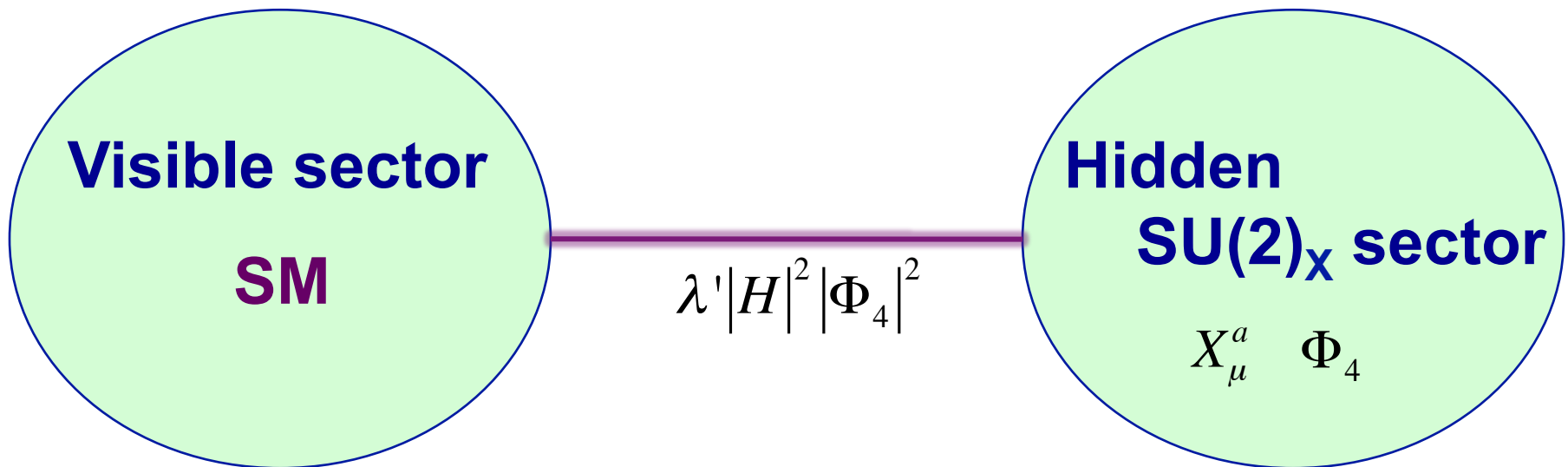
**It would be produced
at the LHC**



Structure of the model

❖ Singlet under $SU(2)_X$

❖ Singlet under G_{SM}



Gauge symmetry : $G_{SM} \times SU(2)_X$

New field contents: X_μ^a ($a = 1, 2, 3$) $SU(2)_X$ gauge fields

$$\Phi_4 = (\phi_{3/2}, \phi_{1/2}, -\phi_{-1/2}, \phi_{-3/2}) / \sqrt{2}$$

Scalar qadruplet for $U(2)_X$ breaking

Lagrangian of the model

$$L = L_{SM} + L_{new}$$

$$L_{new} = -\frac{1}{4}X_{\mu\nu}^a X^{a\mu\nu} + (D^\mu \Phi_4)(D_\mu \Phi_4) + V(H, \Phi_4)$$

$$X_{\mu\nu}^a = \partial_\mu X_\nu^a - \partial_\nu X_\mu^a + g_X \epsilon_{abc} X_\mu^b X_\nu^c$$

$$D_\mu \Phi_4 = \partial_\mu \Phi_4 - ig_X X_\mu^a T^a \Phi_4$$

$$T^1 = \frac{1}{2} \begin{pmatrix} 0 & \sqrt{3} & 0 & 0 \\ \sqrt{3} & 0 & 2 & 0 \\ 0 & 2 & 0 & \sqrt{3} \\ 0 & 0 & \sqrt{3} & 0 \end{pmatrix}, T^2 = \frac{i}{2} \begin{pmatrix} 0 & -\sqrt{3} & 0 & 0 \\ \sqrt{3} & 0 & -2 & 0 \\ 0 & 2 & 0 & -\sqrt{3} \\ 0 & 0 & \sqrt{3} & 0 \end{pmatrix}, T^3 = \begin{pmatrix} 3/2 & 0 & 0 & 0 \\ 0 & 1/2 & 0 & 0 \\ 0 & 0 & -1/2 & 0 \\ 0 & 0 & 0 & -3/2 \end{pmatrix}$$

$$V(H, \Phi_4) = \mu^2 |H|^2 + \lambda |H|^4 + \mu_\Phi^2 |\Phi_4|^2 + \lambda_\Phi |\Phi_4|^4 + \lambda' |H|^2 |\Phi_4|^2$$

➡ $\langle \Phi_4 \rangle = (v_4, 0, 0, v_4)^T / \sqrt{2}, \quad \langle H \rangle = (0, v)^T / \sqrt{2}$

❖ Gauge bosons

❖ $\chi_\mu, \bar{\chi}_\mu$ ★ **Candidate of dark matter**

From $T_3 = \pm 1$ component of $SU(2)_X$ gauge fields (Z_3 charged)

❖ X_μ^3

$T_3 = 0$ component of $SU(2)_X$ gauge fields (Z_3 non-charged)

❖ Higgs bosons

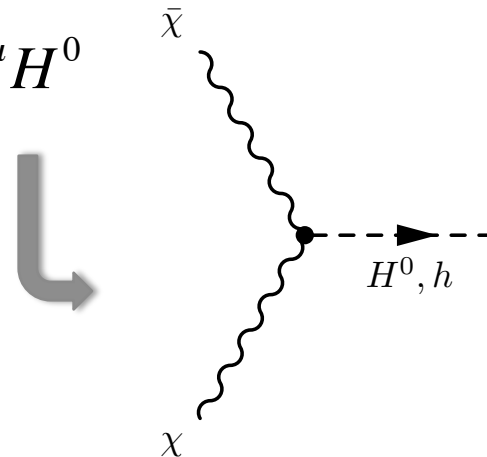
$$H \supset \phi = h \cos \theta - H^0 \sin \theta \quad \Phi_4 \supset \phi_r = h \sin \theta + H^0 \cos \theta$$

❖ Gauge interaction : DM and Higgs bosons

$$\sqrt{3}g_X m_\chi \sin \theta \chi_\mu \bar{\chi}^\mu h + \sqrt{3}g_X m_\chi \cos \theta \chi_\mu \bar{\chi}^\mu H^0$$

H^0 -SM particle interaction

➡ **SM h coupling $\times \sin \theta$**



Parameters in the model

❖ Original parameters


$$g_X, \mu, \mu_\Phi, \lambda, \lambda_\Phi, \lambda'$$

Gauge coupling &
parameters in the potential

after SSB

❖ Free parameters in our analysis

$$g_X, m_\chi, m_{H^0}, \sin \theta$$

$$(m_h = 125 \text{ GeV}, v \approx 246 \text{ GeV})$$

Gauge coupling &
new particle masses &
and mixing angle for scalar bosons

Signal of the dark matter in our model at the LHC

DMs are produced through Higgs bosons h and H^0

We consider DM mass and H^0 mass motivated by GC γ -ray excess

$\Rightarrow m_\chi = 20 \sim 80 \text{ GeV} \quad A: m_H \approx m_\chi \quad B: m_H \approx 2m_\chi$

Current constraints

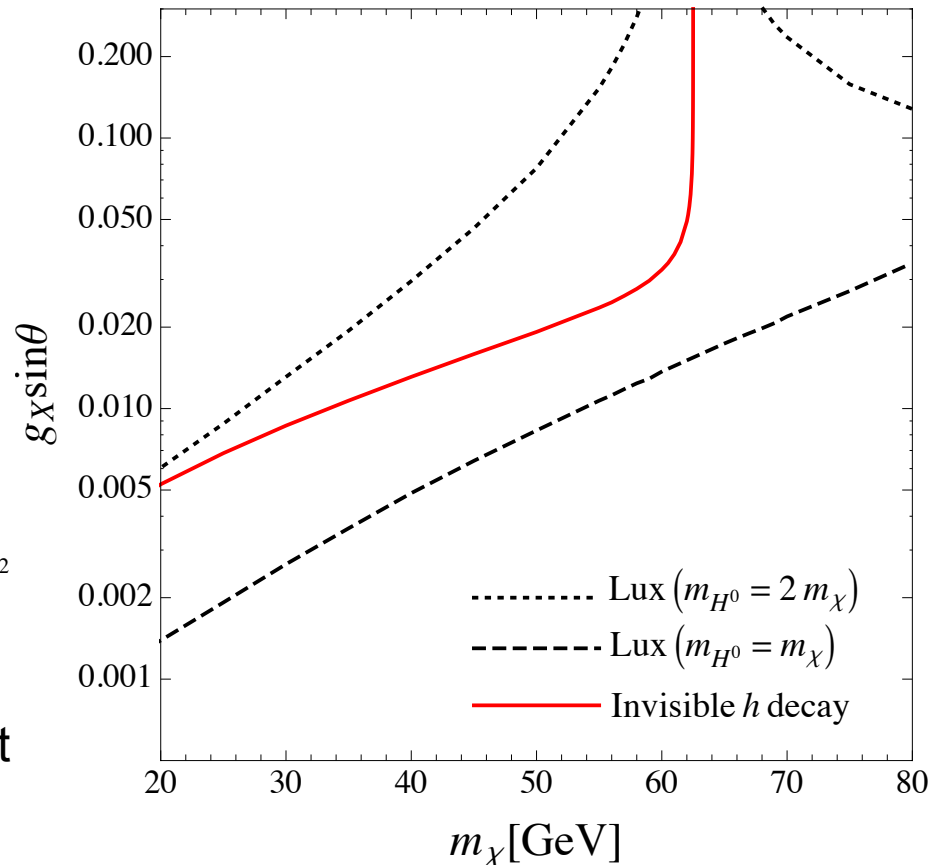
● Invisible h decay

LHC 8 TeV limit from ATLAS:
ATLAS-COM-CONF-2015-004
arXiv:1509.00672

● DM direct detection

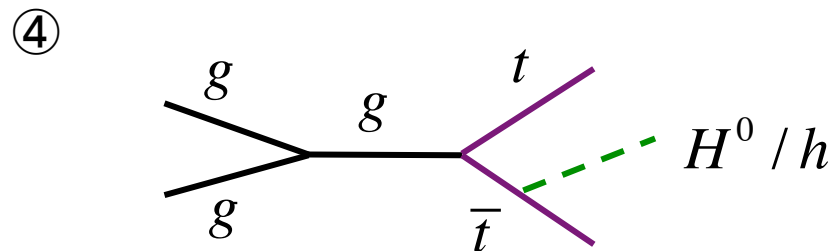
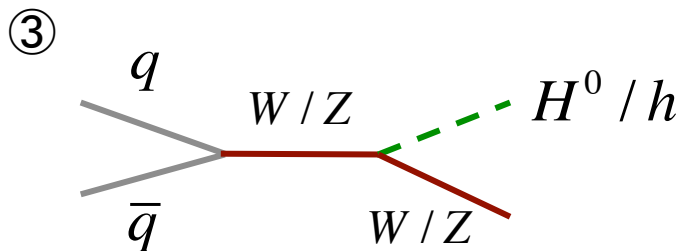
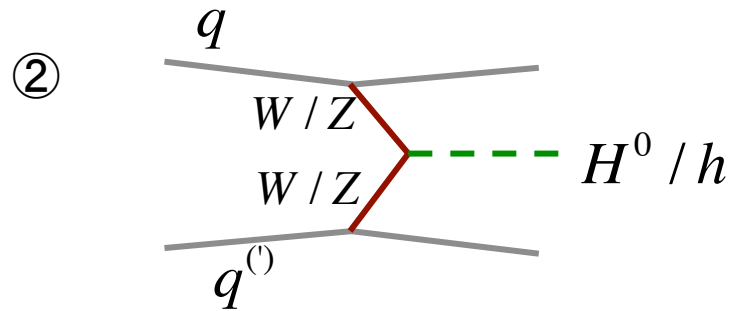
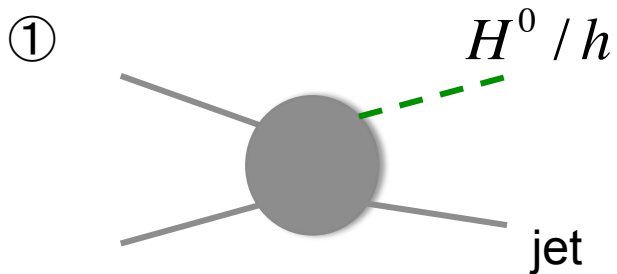
$$\sigma_{\chi N} \approx \frac{3g_X^2 f_N^2}{4\pi} (\sin\theta \cos\theta)^2 \left(\frac{m_N}{m_\chi + m_N} \right)^2 \left(\frac{m_{H^0}^2 - m_h^2}{m_h m_{H^0}} \right)^2$$

Compared with LUX constraint
(PRL 112, arXiv:1310.8214)

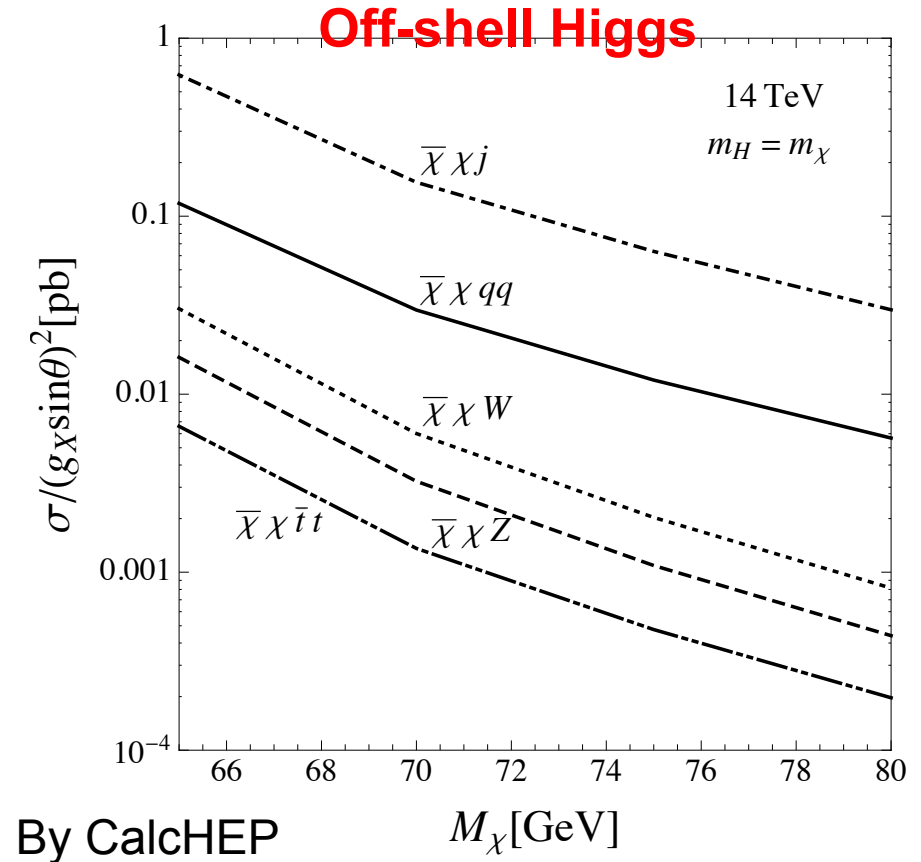
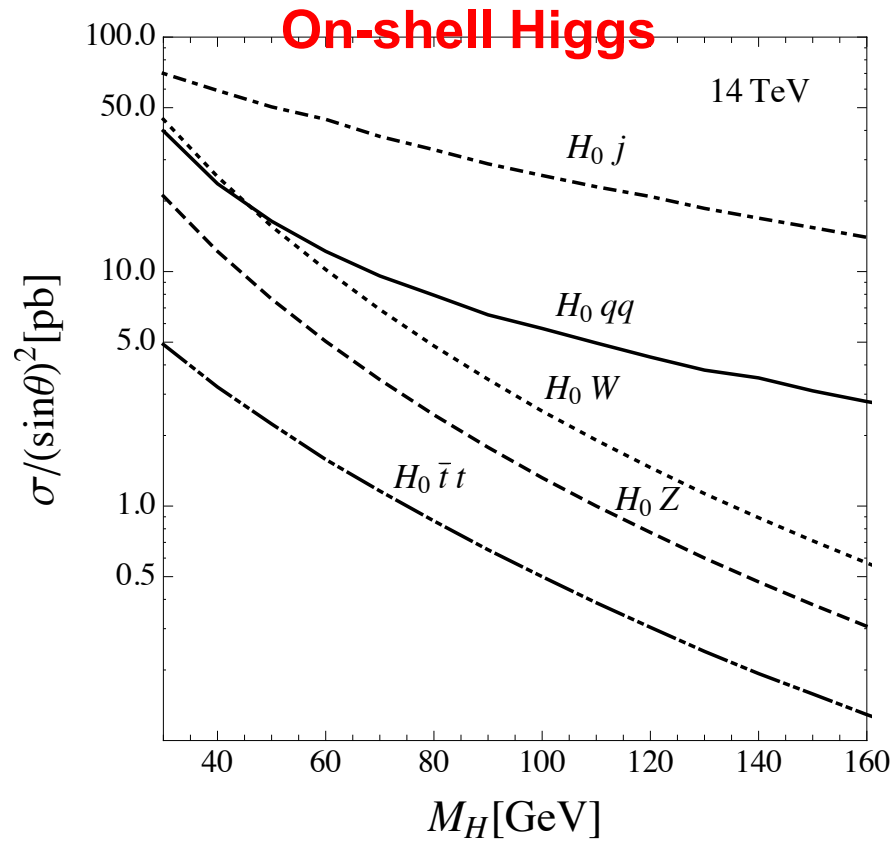


H and H^0 production processes

- ① Mono-jet production : $p p \rightarrow h/H^0 + \text{jet}$
- ② Vector boson fusion (VBF) : $p p \rightarrow h/H^0 + 2 \text{ jets}$
- ③ Z/W associated production : $p p \rightarrow h/H^0 + Z/W$
- ④ Top associated production : $p p \rightarrow h/H^0 + t \bar{t}$



Production cross sections



- ❖ H^0 production $\sigma = \text{SM } h \text{ production } \sigma \times \sin^2\theta$
- ❖ Mono jet production σ is largest, however background is huge
- ❖ **VBF** is promising; we can reduce BG with kinematical cuts

Production cross sections



We consider 4 cases for VBF

$$I_A : m_h > 2m_\chi, m_{H^0} = 2m_\chi + 1 \text{ GeV}$$

$$h \rightarrow \bar{\chi}\chi$$

$$H^0 \rightarrow \bar{\chi}\chi$$

On-shell

On-shell

$$I_B : m_h > 2m_\chi, m_{H^0} = m_\chi - 1 \text{ GeV}$$

On-shell

Off-shell

$$II_A : m_h < 2m_\chi, m_{H^0} = 2m_\chi + 1 \text{ GeV}$$

Off-shell

On-shell

$$II_B : m_h < 2m_\chi, m_{H^0} = m_\chi - 1 \text{ GeV}$$

Off-shell

Off-shell

- ❖ H^0 production $\sigma = \text{SM } h \text{ production } \sigma \times \sin^2\theta$
- ❖ Mono jet production σ is largest, however background is huge
- ❖ **VBF** is promising; we can reduce BG with kinematical cuts

Kinematical cuts

Generating events:

- **Using MADGRAPH/MADEVENT package**
- **PYTHIA6 for ISR/FSR, hadronization, decay of SM particles**
- **Detector level simulation with PGS 4**

SM backgrounds:

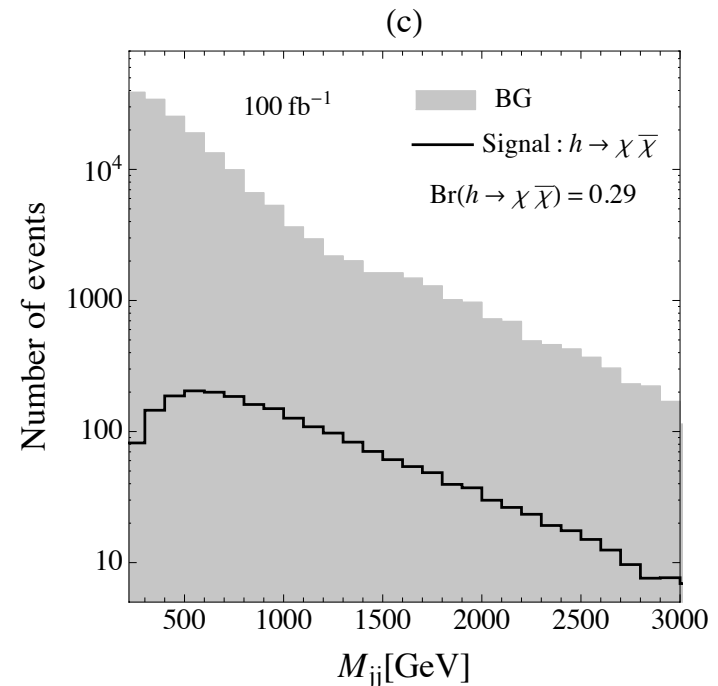
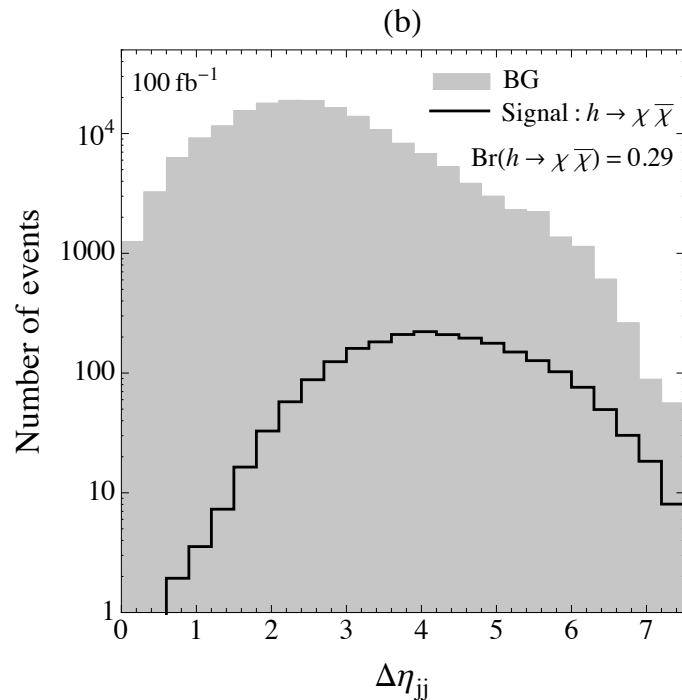
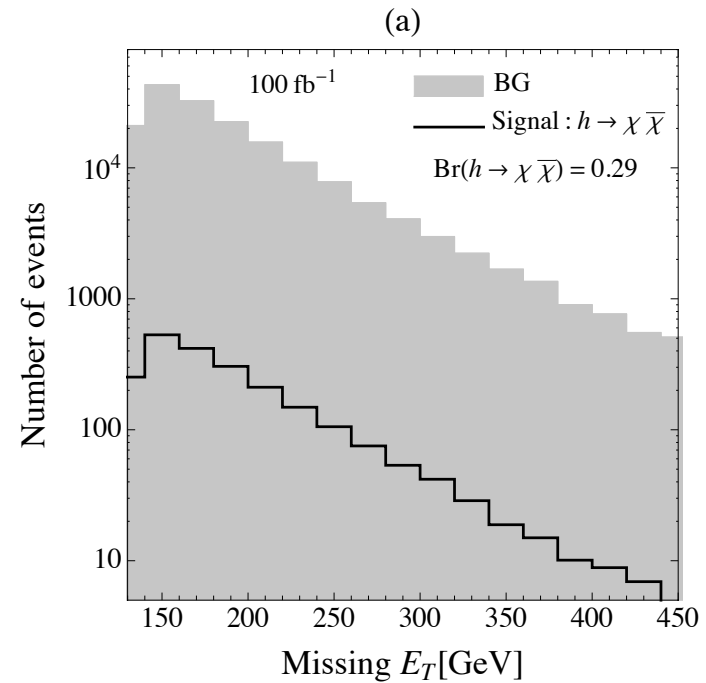
- **Z + 2jets, Z+ 3jets**
- **W+ 2jets, W+ 3jets**
- **tWb**

Some kinetic distributions

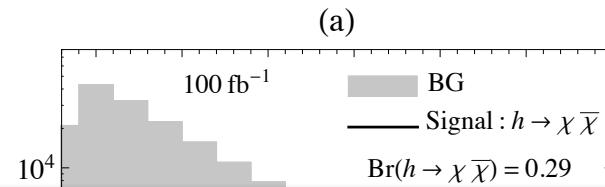
With basic cuts

$$p_T(j) > 50 \text{ GeV}, \quad |\eta(j)| < 4.7,$$

$$\eta(j_1) \cdot \eta(j_2) < 0, \quad \cancel{E}_T > 130 \text{ GeV},$$



Some kinetic distributions

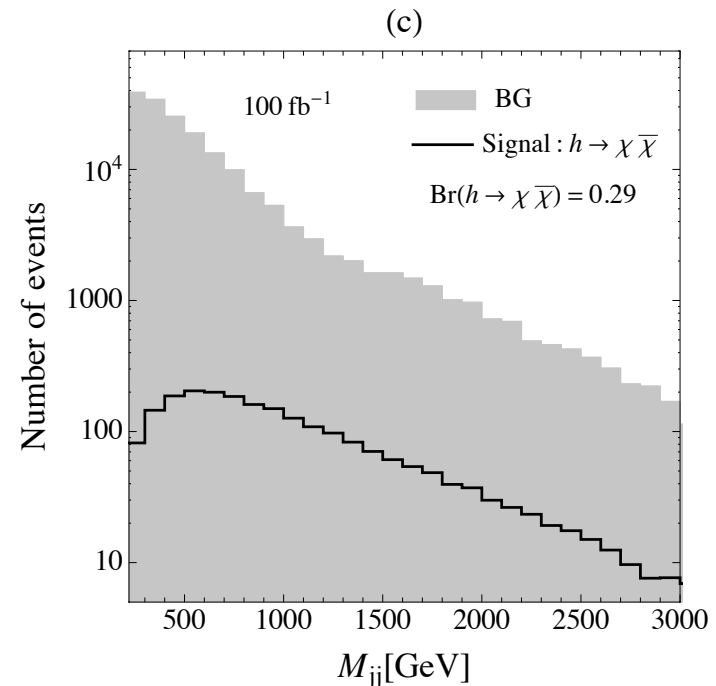
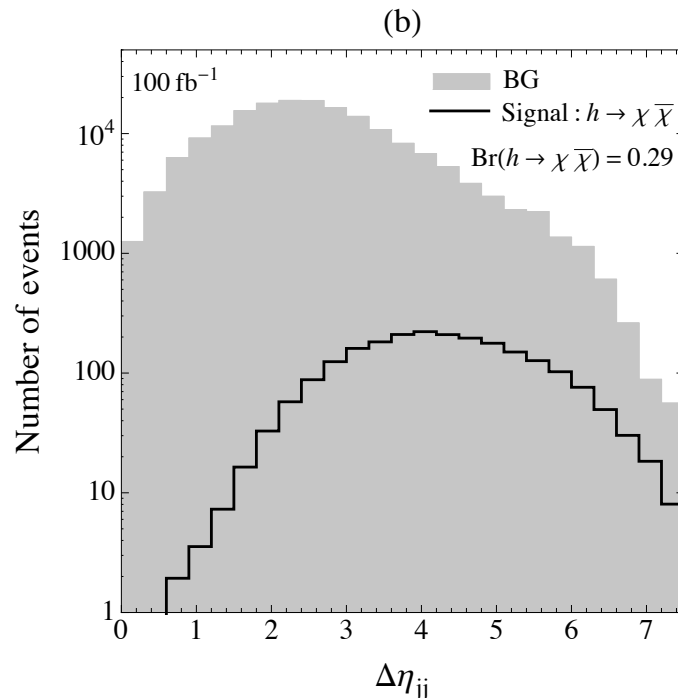


We apply kinematical cuts:

$$p_T(j) > 50 \text{ GeV}, \quad |\eta(j)| < 4.7, \quad \eta(j_1) \cdot \eta(j_2) < 0, \quad E_T^{\text{miss}} > 130 \text{ GeV},$$

$$\Delta\eta_{jj} > 4.5, \quad \Delta\phi_{jj} < 1.5, \quad M_{jj} > 1100 \text{ GeV},$$

Similar to CMS analysis : Eur. Phys. J. C 74 , 2980 (2014) [arXiv:1404.1344 [hep-ex]].



Cross sections after cuts

$\sigma_{\text{BG}}[\text{fb}]$	Zjj	Zjjj	Wjj	Wjjj
	32.9	8.54	14.2	2.20
$\sigma_{\text{signal}}[\text{fb}]$	$m_\chi[\text{GeV}]$	40	50	60
	I _A	18.6 R_{H^0} + 17.2 R_h	17.5 R_{H^0} + 17.2 R_h	17.3 R_{H^0} + 17.2 R_h
	I _B	17.2 R_h	17.2 R_h	17.2 R_h
	$m_\chi[\text{GeV}]$	65	70	75
	II _A	16.3 R_{H^0}	16.0 R_{H^0}	15.4 R_{H^0}
	II _B	0.689 R_{off}	0.211 R_{off}	0.102 R_{off}

$$R_{H^0} = \sin^2 \theta \times Br(H^0 \rightarrow \bar{\chi}\chi)$$

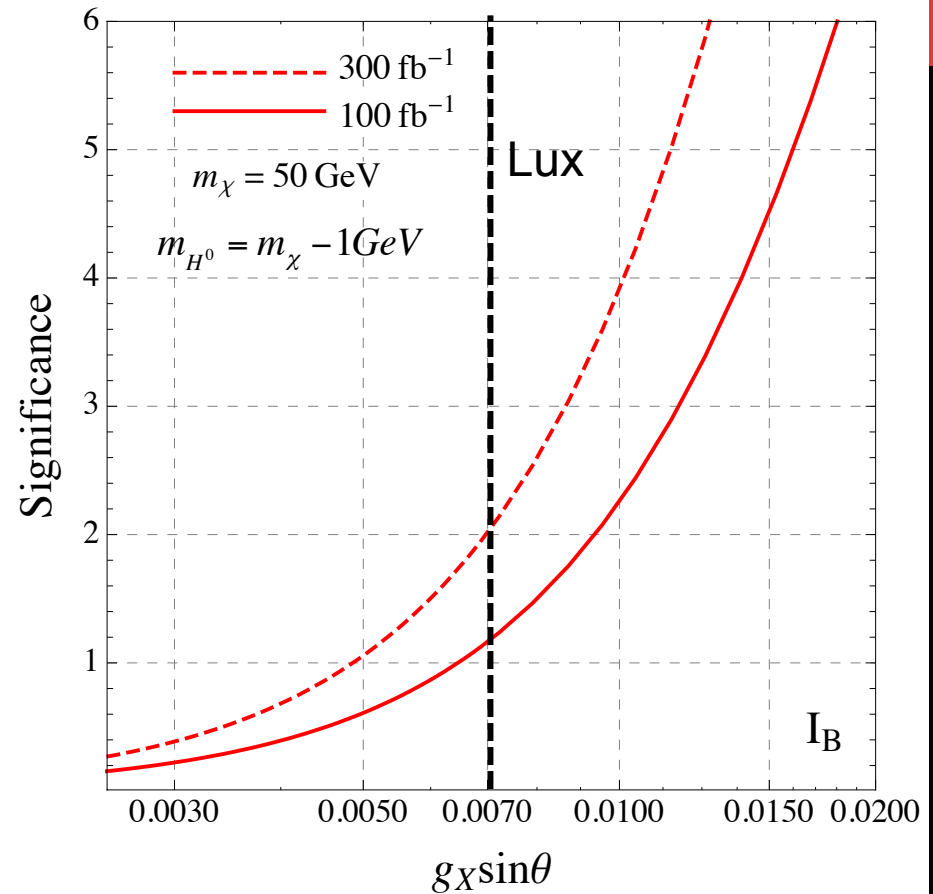
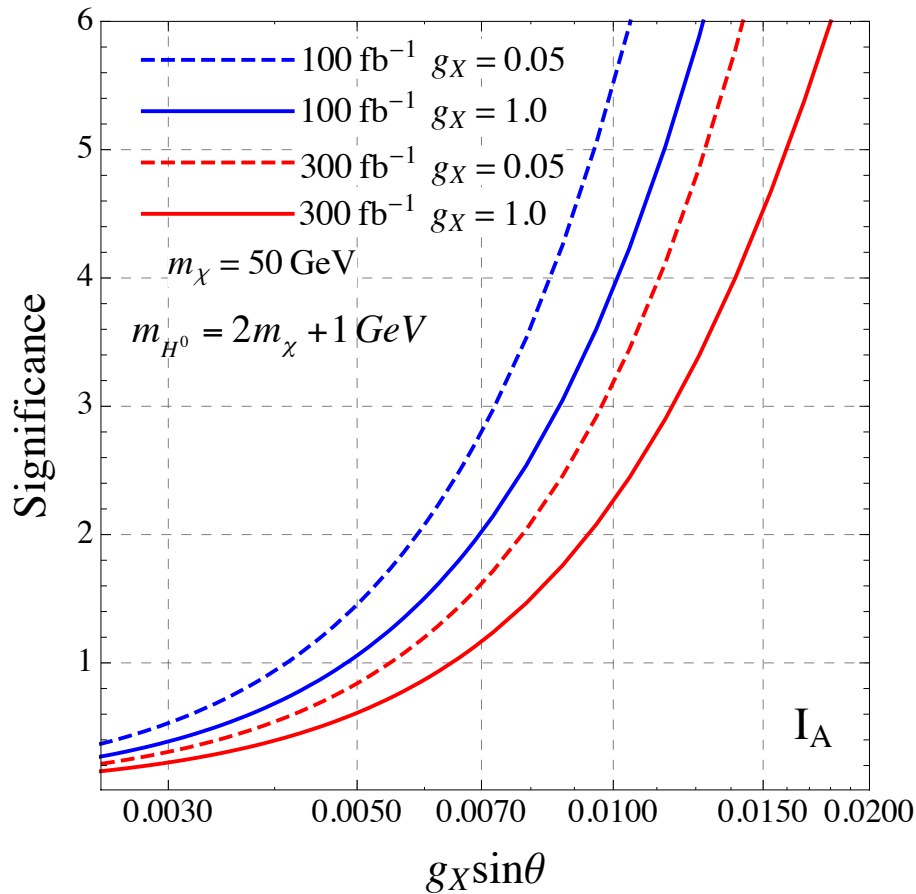
Estimate significance of the signal

$$R_h = \cos^2 \theta \times Br(h \rightarrow \bar{\chi}\chi)$$

$$S = N_S / \sqrt{N_B}$$

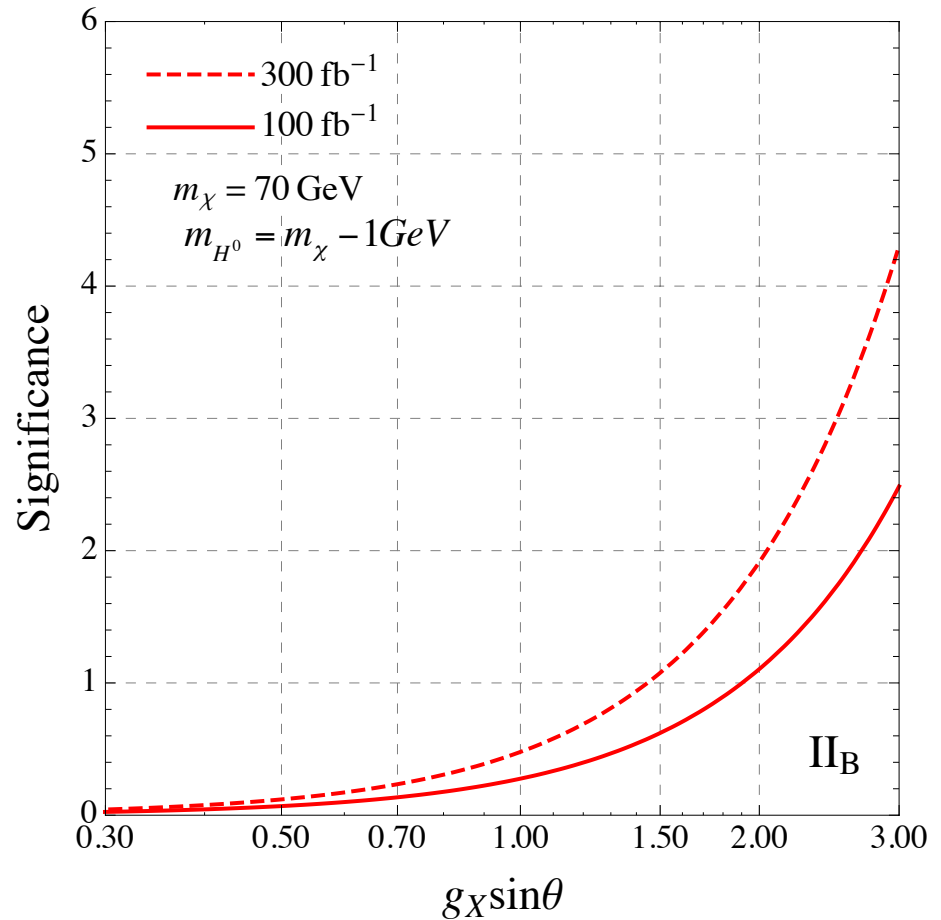
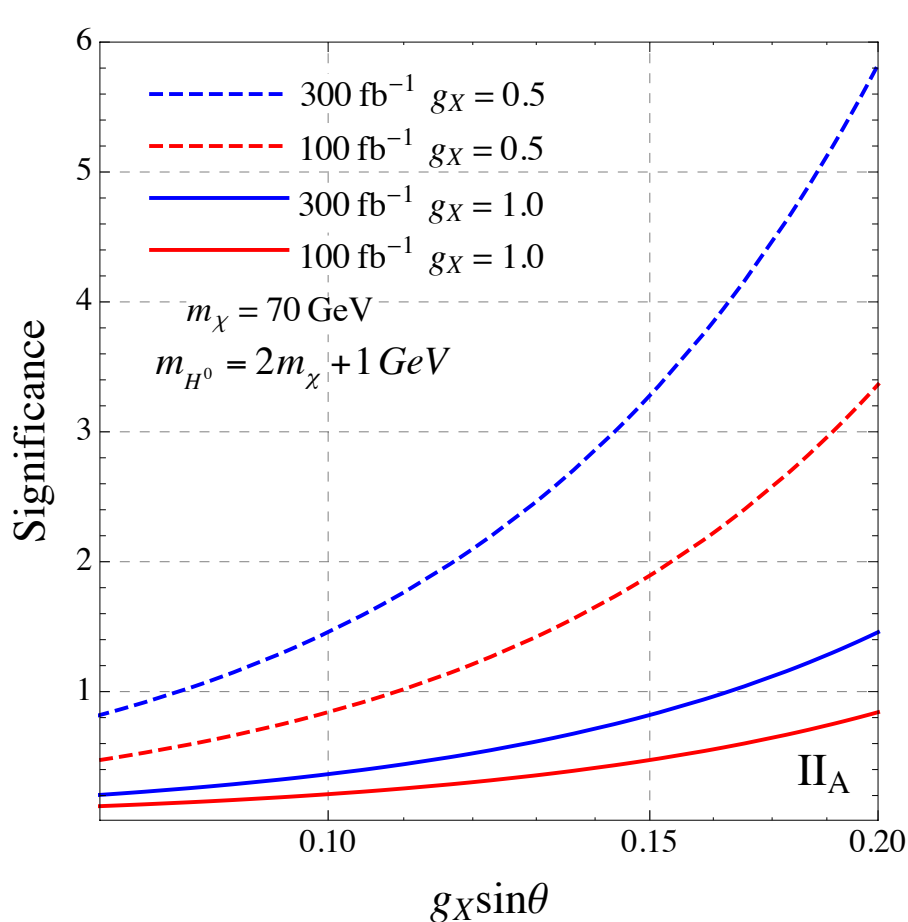
$$R_{\text{off}} = (g_X \sin \theta \cos \theta)^2$$

Significance VS coupling



- For simplicity, we took $\cos \theta = 1$ because $\sin \theta$ is small
- For I_A, $\sin \theta$ is larger for smaller $g_X \rightarrow$ more contribution from H^0

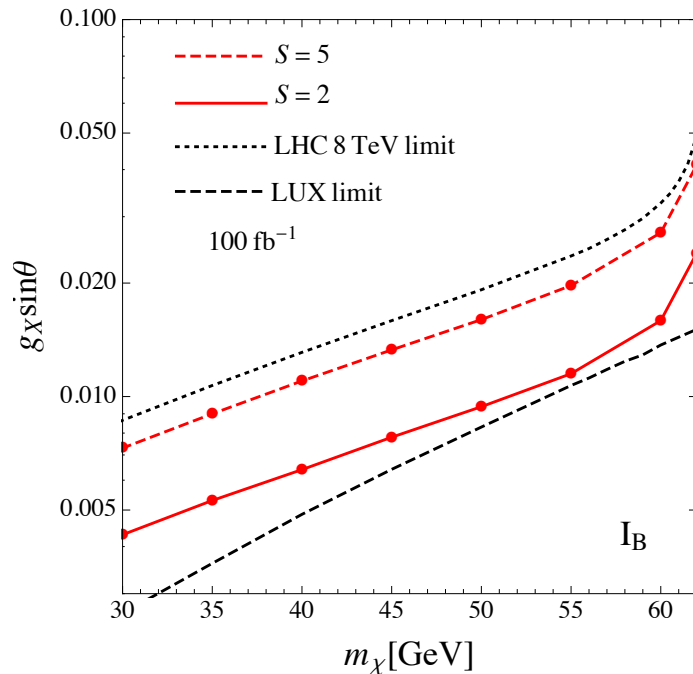
Significance VS coupling



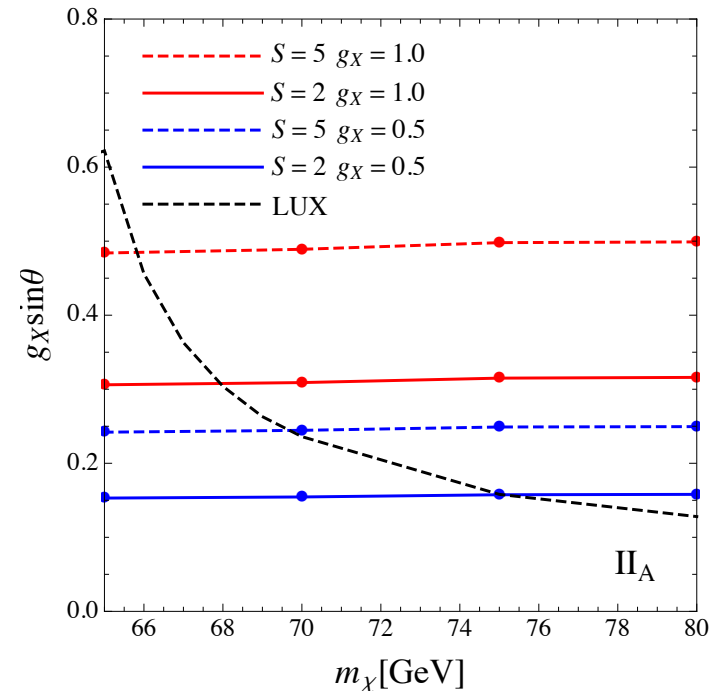
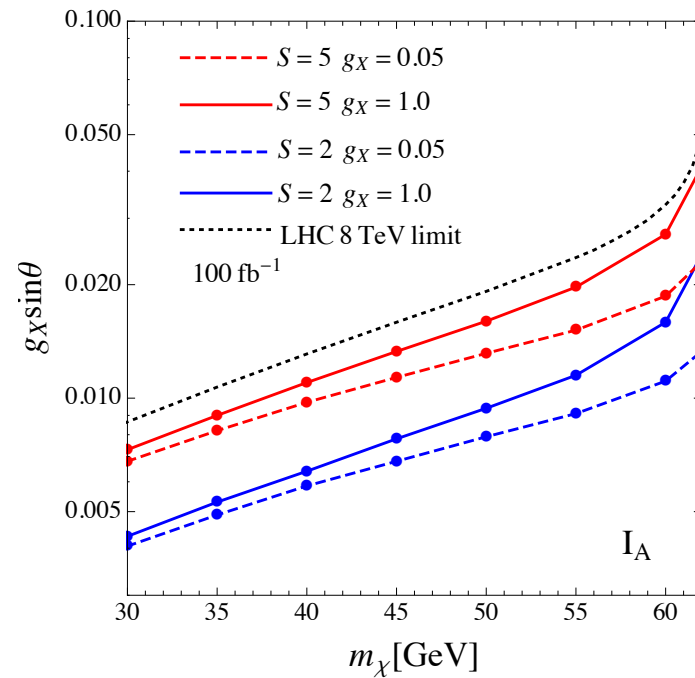
- For simplicity, we took $\cos \theta = 1$ for Π_B because we take $\sin \theta$ is small
- For Π_A , $\sin \theta$ is large for smaller g_X

Coupling-DM mass contour for fixed significance

Luminosity = 100 fb⁻¹



LHC 8 TeV limit from ATLAS:
ATLAS-COM-CONF-2015-004



Summary

Hidden SU(2) vector DM model

- ✧ Z_3 symmetry as a subgroup of SU(2)
- ✧ DM candidates are massive gauge boson
- ✧ DM interaction with SM through Higgs mixing
- ✧ Possible explanation of galactic gamma-ray excess

Search for vector DM at the LHC

- ✧ Collider signature; invisible decay of Higgs bosons
- ✧ On-shell h or H^0 case is promising
- ✧ We can test more parameter space by LHC-run2

Appendix

Relic density of DM

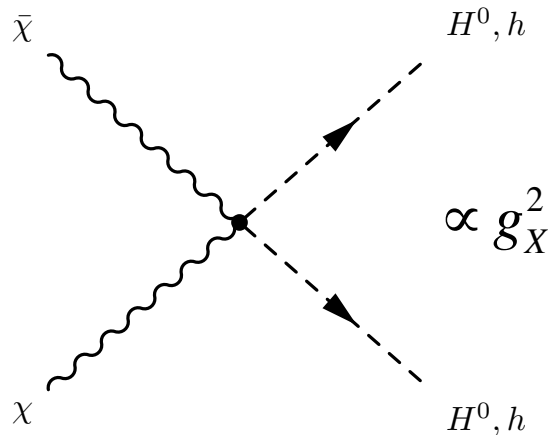
Relic density calculation

Relic density is obtained by solving Boltzmann equation :

$$\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle \sigma v_{rel} \rangle (n_\chi^2 - n_{\chi eq}^2)$$

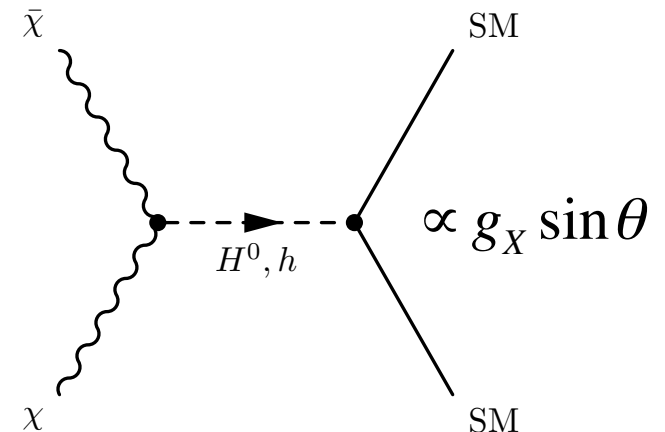
Dominant DM annihilation processes

(1) $m_\chi > m_{H^0}$



+ t(u)-channel process

(2) $m_\chi < m_{H^0}$



Suppressed by $\sin \theta$

Search for the parameter region satisfying observed relic density

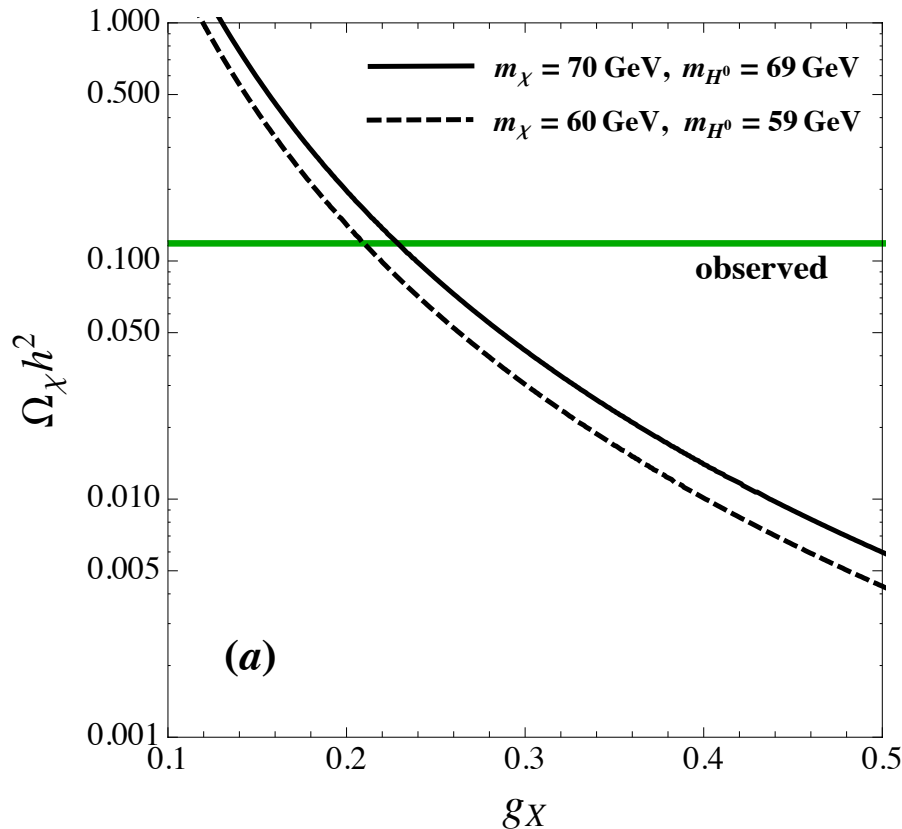
Planck data (90% C.L.) $0.1159 \leq \Omega_D h^2 \leq 0.1215$

P.A.R. Ade et al [Planck Collaboration] (2013)

Ω_D is Calculated with MicrOMEGAs

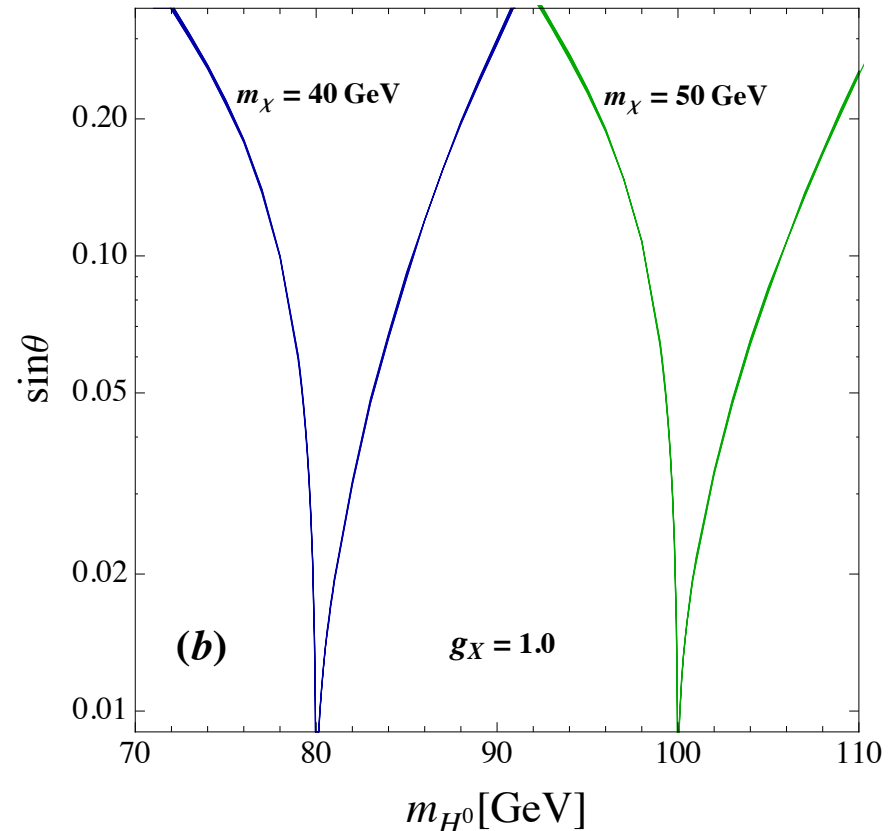
(G. Belanger, F. Boudjema, A. Pukhov and A. Semenov)

(1) $m_\chi > m_{H^0}$



Independent of $\sin\theta$

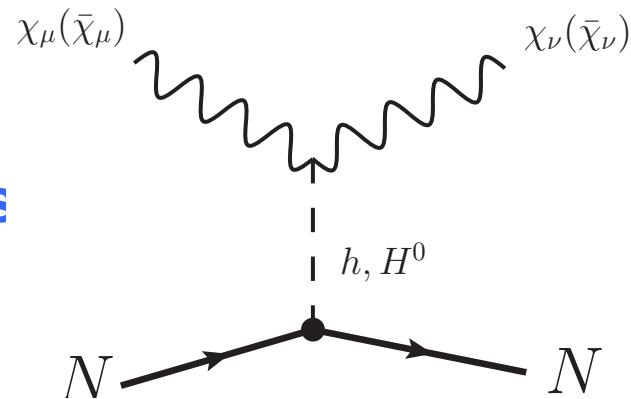
(2) $m_\chi < m_{H^0}$



$m_{H^0} \approx 2m_\chi$ is required for small $\sin\theta$

Constraint DM-Nucleon scattering

Scattering Process



DM-Nucleon scattering through H^0 and h exchanging processes

Cross section:
$$\sigma_{\chi N} \approx \frac{3g_X^2 f_N^2}{4\pi} (\sin\theta \cos\theta)^2 \left(\frac{m_N}{m_\chi + m_N} \right)^2 \left(\frac{m_{H^0}^2 - m_h^2}{m_h m_{H^0}} \right)^2$$

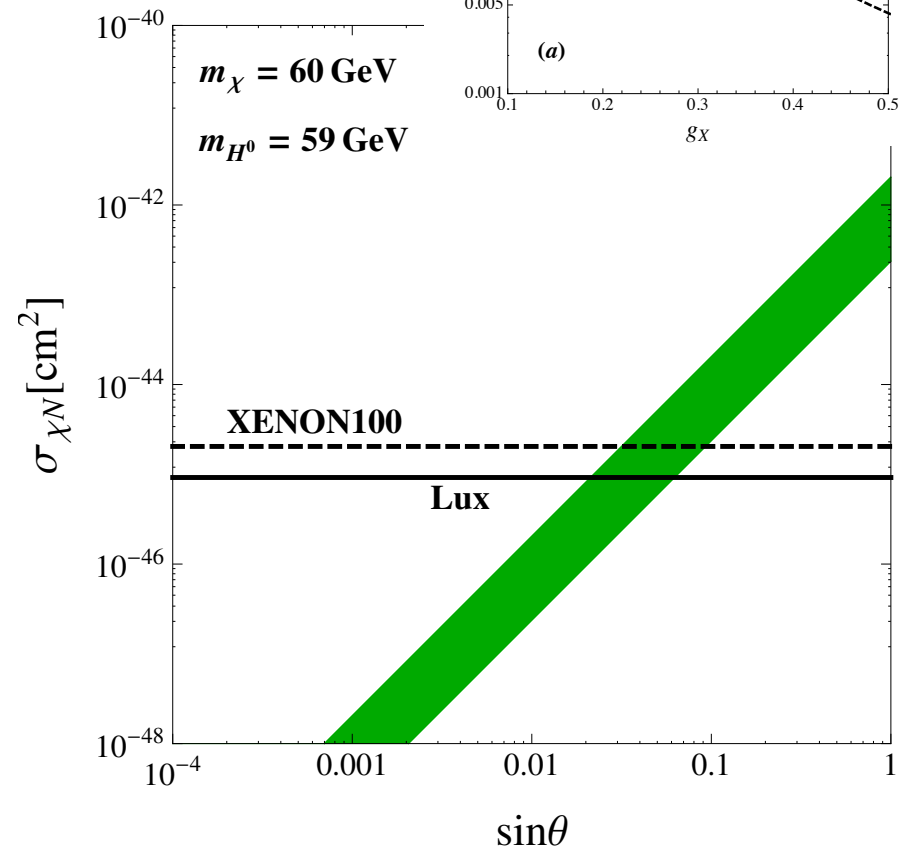
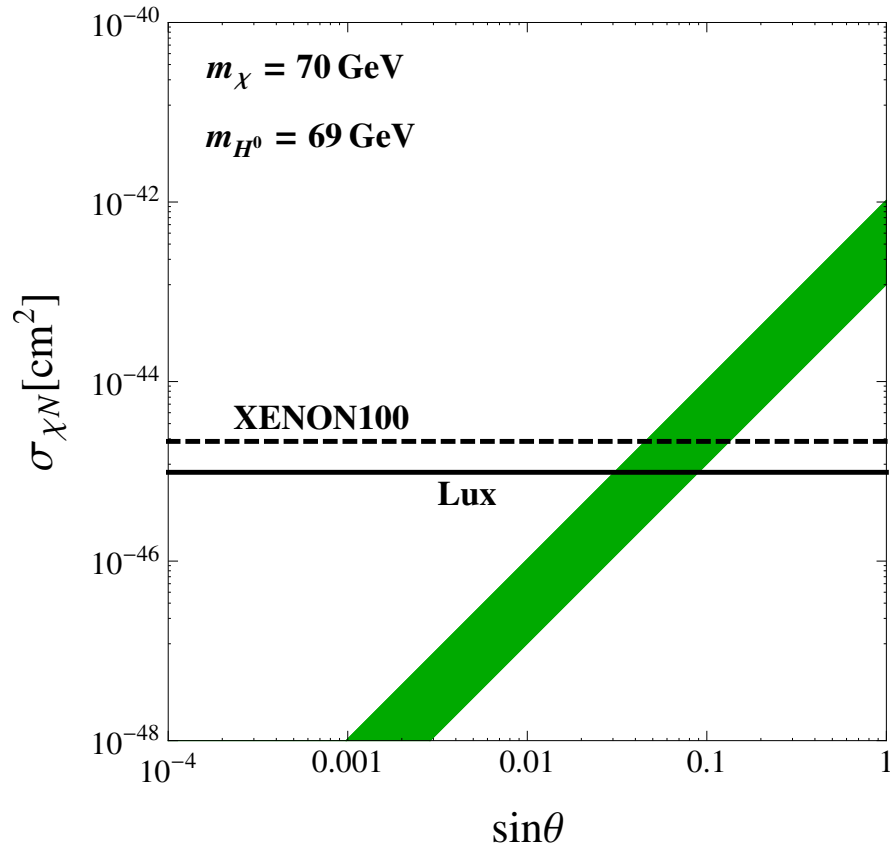
$f_N = [1.1, 3.2] \times 10^{-3}$: **Higgs-Nucleon coupling**

H.Y. Cheng, C.W.Chian (2012)

Compare the cross section with DM direct detection search

Parameter from relic density

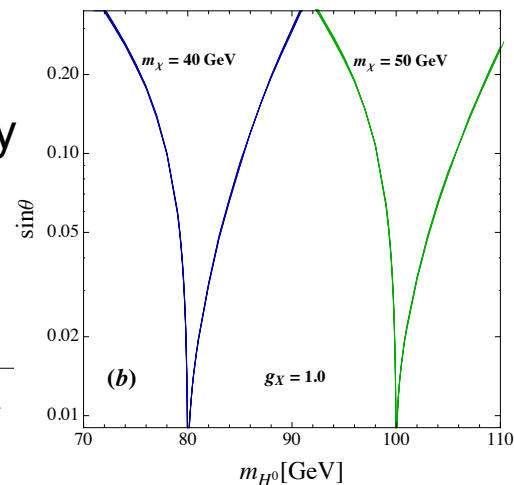
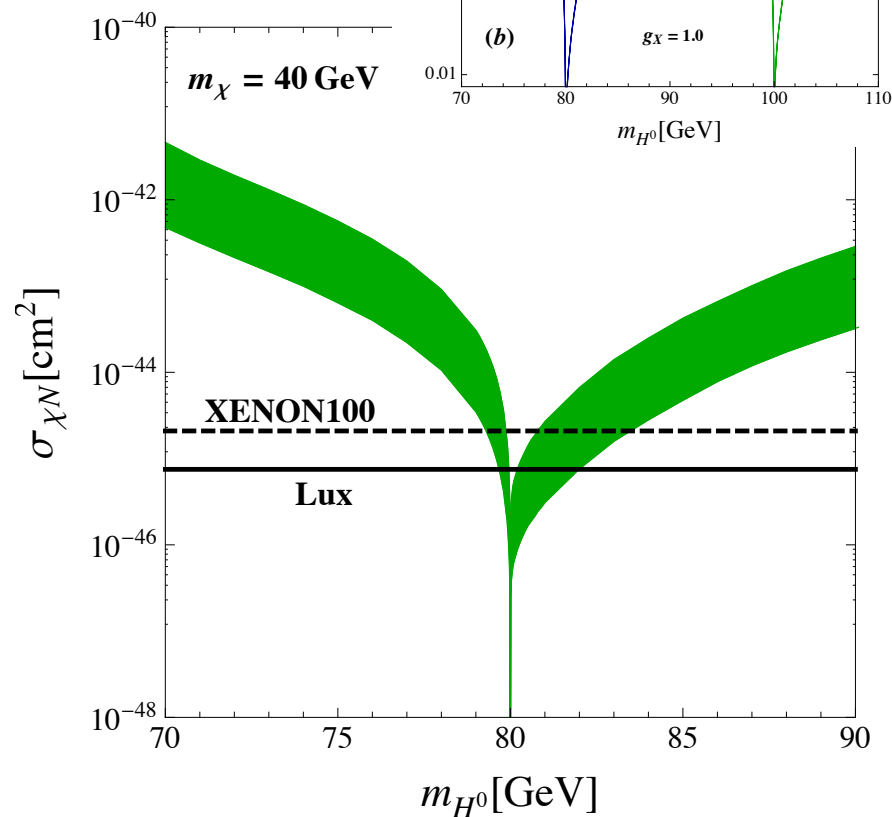
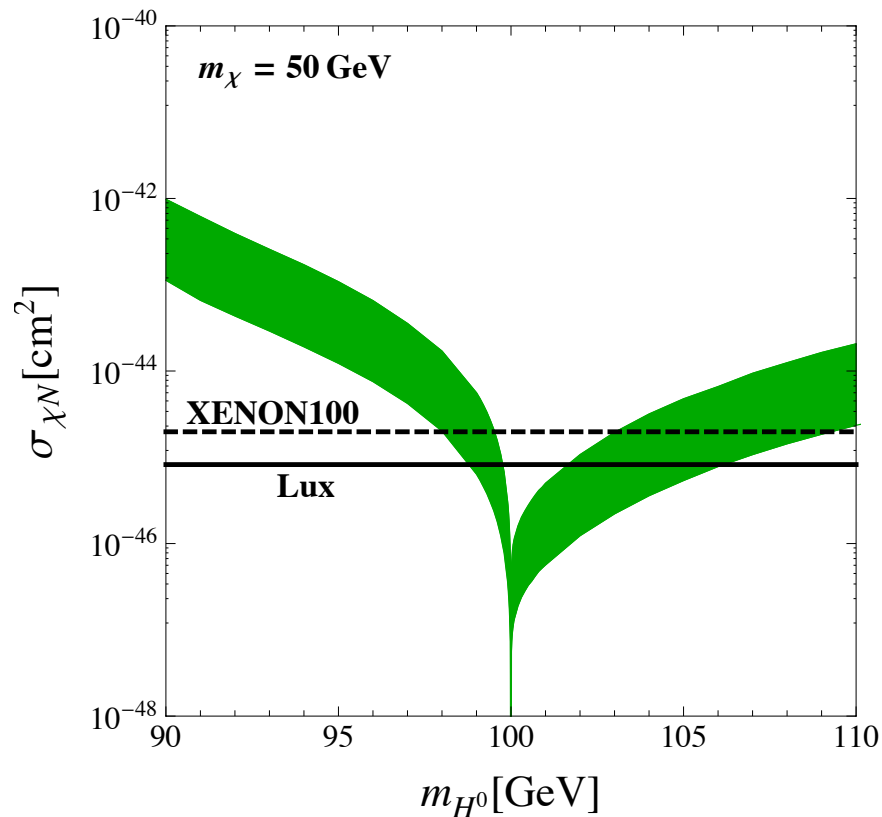
Case (1) $m_\chi > m_{H^0}$



Value of $\sin\theta$ is constrained to be smaller than ~ 0.1

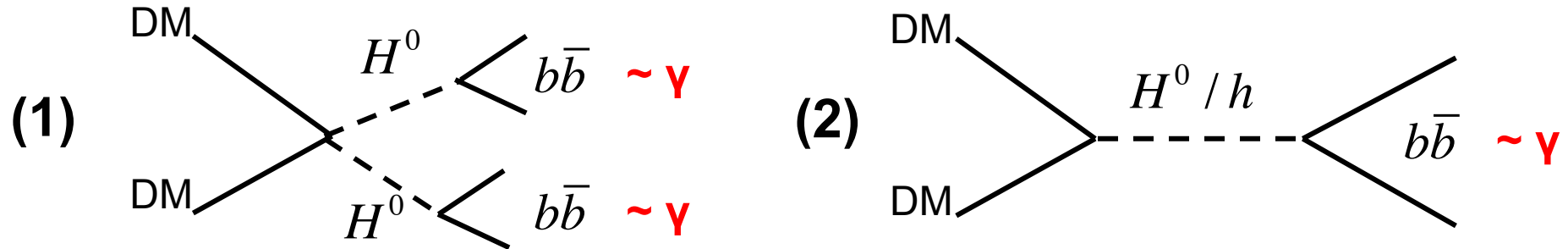
Case (2) $m_\chi < m_{H^0}$

Parameter from relic density



$m_{H^0} \approx 2m_\chi$ is required to satisfy constraints from direct detection

Galactic center Gamma-ray from DM annihilation



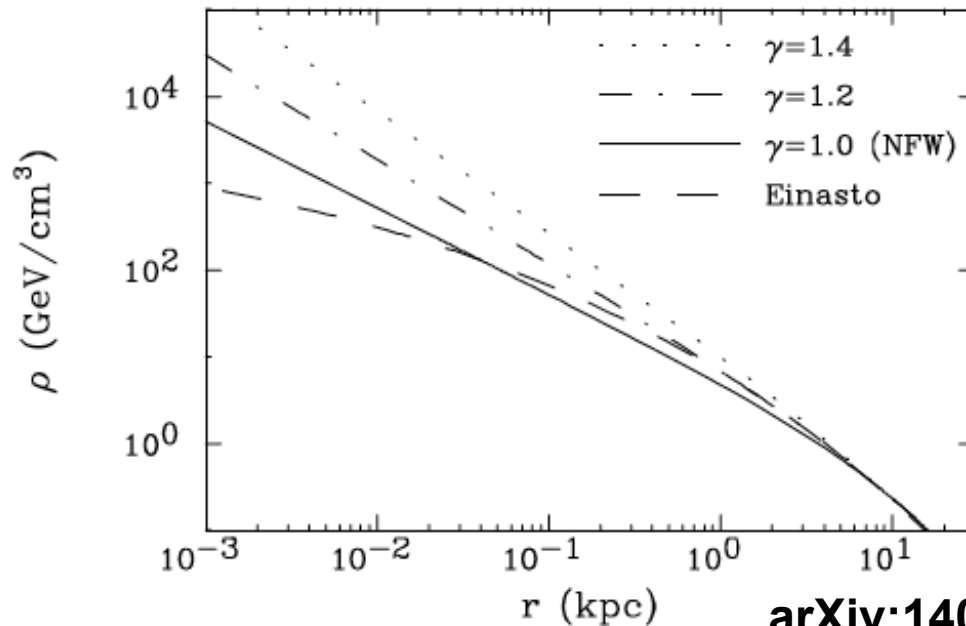
The flux of Gamma-ray from DM annihilation

$$\frac{d\Phi(E_\gamma, \psi)}{dE_\gamma d\Omega} = \frac{\langle \sigma v_{rel} \rangle}{8\pi m_\chi^2} \frac{dN_\gamma}{dE_\gamma} \int_{los} \rho^2(r) dl(\psi)$$

dN_γ/dE_γ : Gamma-ray spectrum per annihilation
 ψ : Observation angle between line-of-sight and GC
 $\rho(r)$: Density of DM

DM halo profile is parametrized by $\rho(r) = \rho_o \left(\frac{r_o}{r} \right)^\gamma \left(\frac{1 + r_o/r_s}{1 + r/r_s} \right)^{3-\gamma}$
 ($\gamma=1$ is NFW profile)

Dependence of DM density on slope factor γ



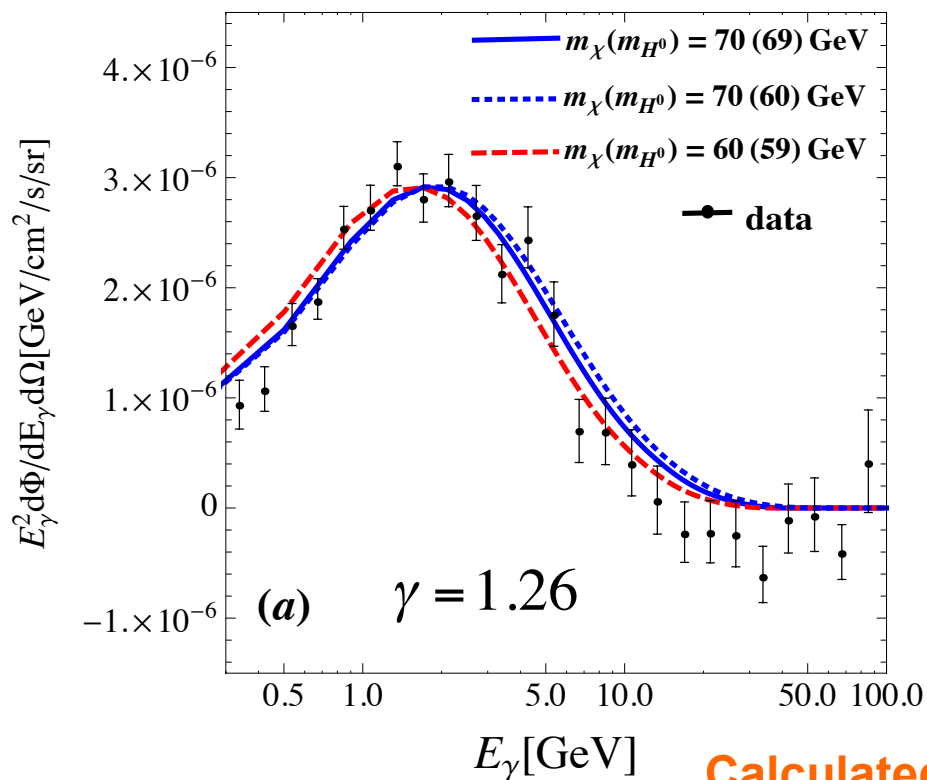
r : distance from GC

arXiv:1402.6703

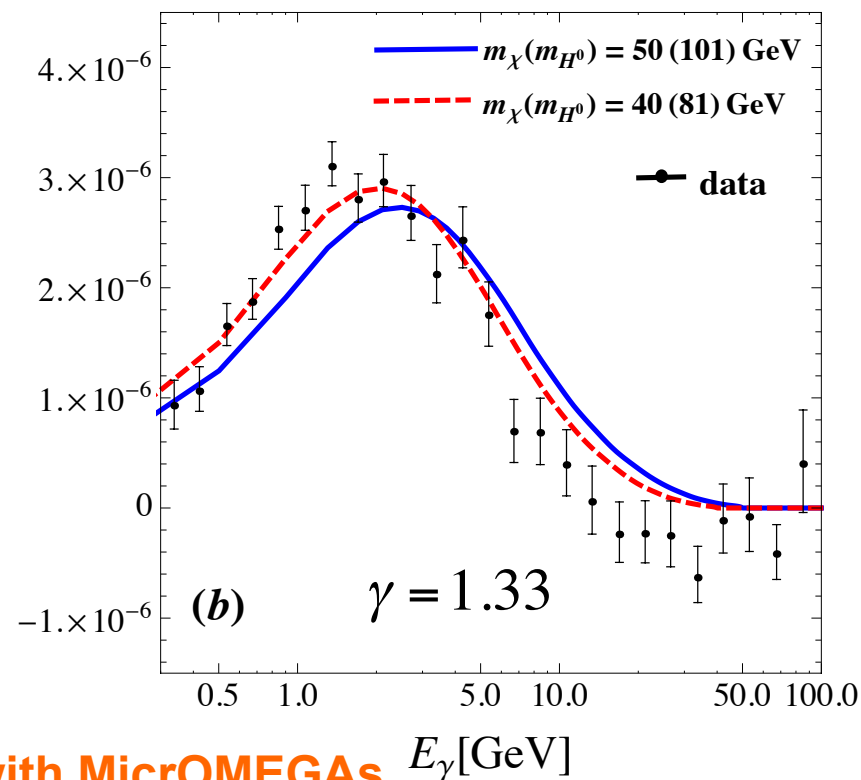
- DM is dense at galactic center for large slope factor
- Gamma-ray flux depends on the factor
- We take γ as free parameter to fit the data

Galactic center Gamma-ray from DM annihilation

(1) $m_\chi > m_{H^0}$



(2) $m_\chi < m_{H^0}$



satisfying relic density and constraints from direct detection

Branching ratio for invisible decay of Higgs bosons

Invisible decay width

$$\Gamma_{h \rightarrow \bar{\chi}\chi} = \frac{3g_X^2 \sin^2 \theta}{64\pi} \frac{m_\chi^2}{m_h} \frac{m_h^4 - 4m_h^2 m_\chi^2 + 12m_\chi^4}{m_\chi^4} \sqrt{1 - \frac{4m_\chi^2}{m_h^2}}$$

$$\Gamma_{H^0 \rightarrow \bar{\chi}\chi} = \frac{3g_X^2 \cos^2 \theta}{64\pi} \frac{m_\chi^2}{m_h} \frac{m_{H^0}^4 - 4m_{H^0}^2 m_\chi^2 + 12m_\chi^4}{m_\chi^4} \sqrt{1 - \frac{4m_\chi^2}{m_{H^0}^2}}$$

Branching ratio

$$Br(h \rightarrow \bar{\chi}\chi) = \frac{\Gamma_{h \rightarrow \bar{\chi}\chi}}{\Gamma_{h \rightarrow \bar{\chi}\chi} + \Gamma_{h \rightarrow SM} \cos^2 \theta} = \frac{\Gamma_{h \rightarrow \bar{\chi}\chi}^{g_X \sin \theta=1} (g_X \tan \theta)^2}{\Gamma_{h \rightarrow \bar{\chi}\chi}^{g_X \sin \theta=1} (g_X \tan \theta)^2 + \Gamma_{h \rightarrow SM}}$$

$$Br(H^0 \rightarrow \bar{\chi}\chi) = \frac{\Gamma_{H^0 \rightarrow \bar{\chi}\chi}}{\Gamma_{H^0 \rightarrow \bar{\chi}\chi} + \Gamma_{h \rightarrow SM}^{m_{H^0}} \cos^2 \theta} = \frac{\Gamma_{H^0 \rightarrow \bar{\chi}\chi}^{g_X \cos \theta=1} (g_X \cot \theta)^2}{\Gamma_{H^0 \rightarrow \bar{\chi}\chi}^{g_X \cos \theta=1} (g_X \cot \theta)^2 + \Gamma_{h \rightarrow SM}^{m_{H^0}}}$$