

Direct Detection of Dark Matter

A General Framework and Collider Connections



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Outline

Standard Approach

General Framework including non-standard interactions

Interference Effects in general

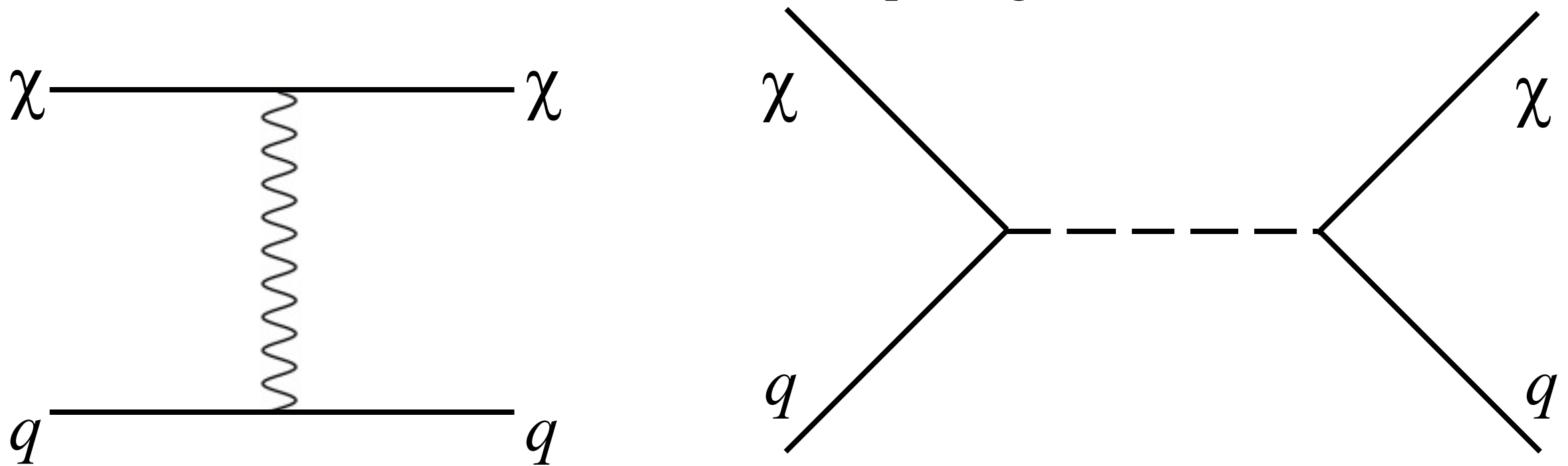
Approaches and identifications with more realistic models

The Neutrino floor(s)

A few issues for connecting collider scales to direct detection scales

Direct Detection: Standard Approach

Model WIMP-nuclear interactions as WIMP-quark/gluon interactions

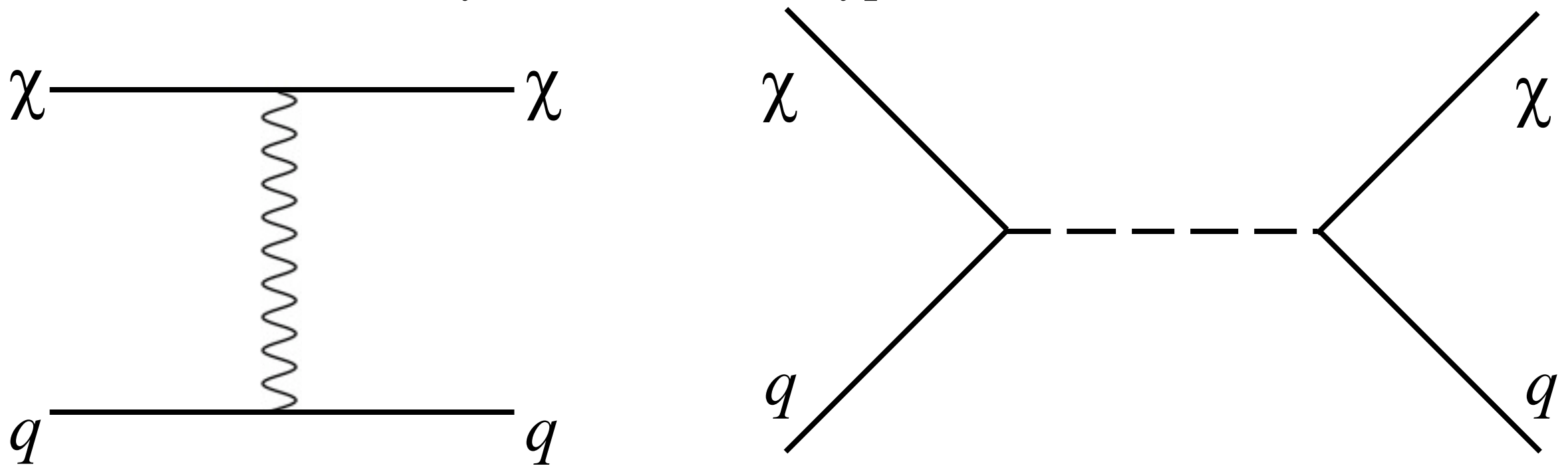


Typical momentum exchanged is $\mathcal{O}(\lesssim 100 MeV)$

With an average recoil energy of $\langle E_R \rangle = \frac{1}{2} M_\chi \langle v \rangle^2 \mathcal{O}(few \times 10 \text{keV})$
 for comparable target and dark matter masses, while more generally this is
 multiplied by an additional factor

$$\frac{4M_\chi M_A}{(M_\chi + M_A)^2}$$

As is familiar, there are myriad interaction types



Hadronic matrix elements encode nucleon interactions

$$\langle N_o | m_q \bar{q} q | N_i \rangle \longrightarrow f_{T_q}^N \bar{N} N$$

$$\langle N_o | \bar{q} \gamma^5 q | N_i \rangle \longrightarrow \Delta_q^N \bar{N} \gamma^5 N$$

$$\langle N_o | \bar{q} \gamma^\mu q | N_i \rangle \longrightarrow \mathcal{N}_q^N \bar{N} \gamma^\mu N$$

$$\langle N_o | \bar{q} \gamma^\mu \gamma^5 q | N_i \rangle \longrightarrow \Delta_q^N \bar{N} \gamma^\mu \gamma^5 N$$

$$\langle N_o | \bar{q} \sigma^{\mu\nu} q | N_i \rangle \longrightarrow \delta_q^N \bar{N} \sigma^{\mu\nu} N$$

Interaction types include coupling to nuclear charge (spin-independent) or spin (spin-dependent), which give rise to two nuclear response types

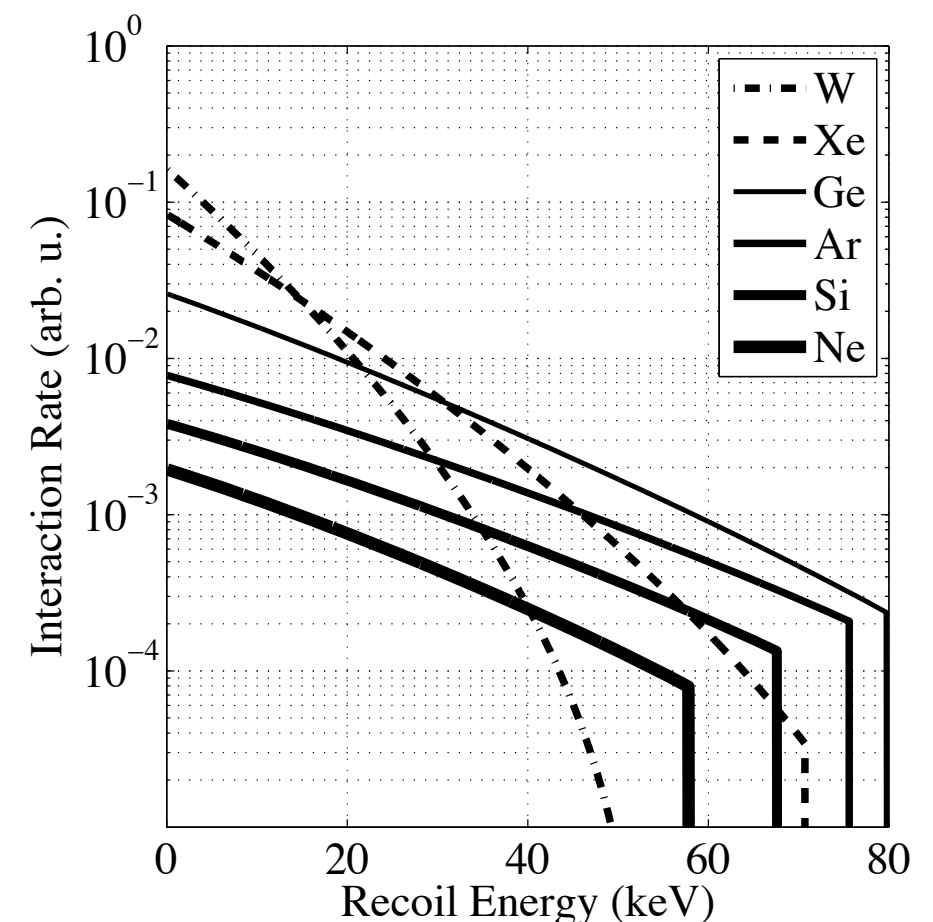
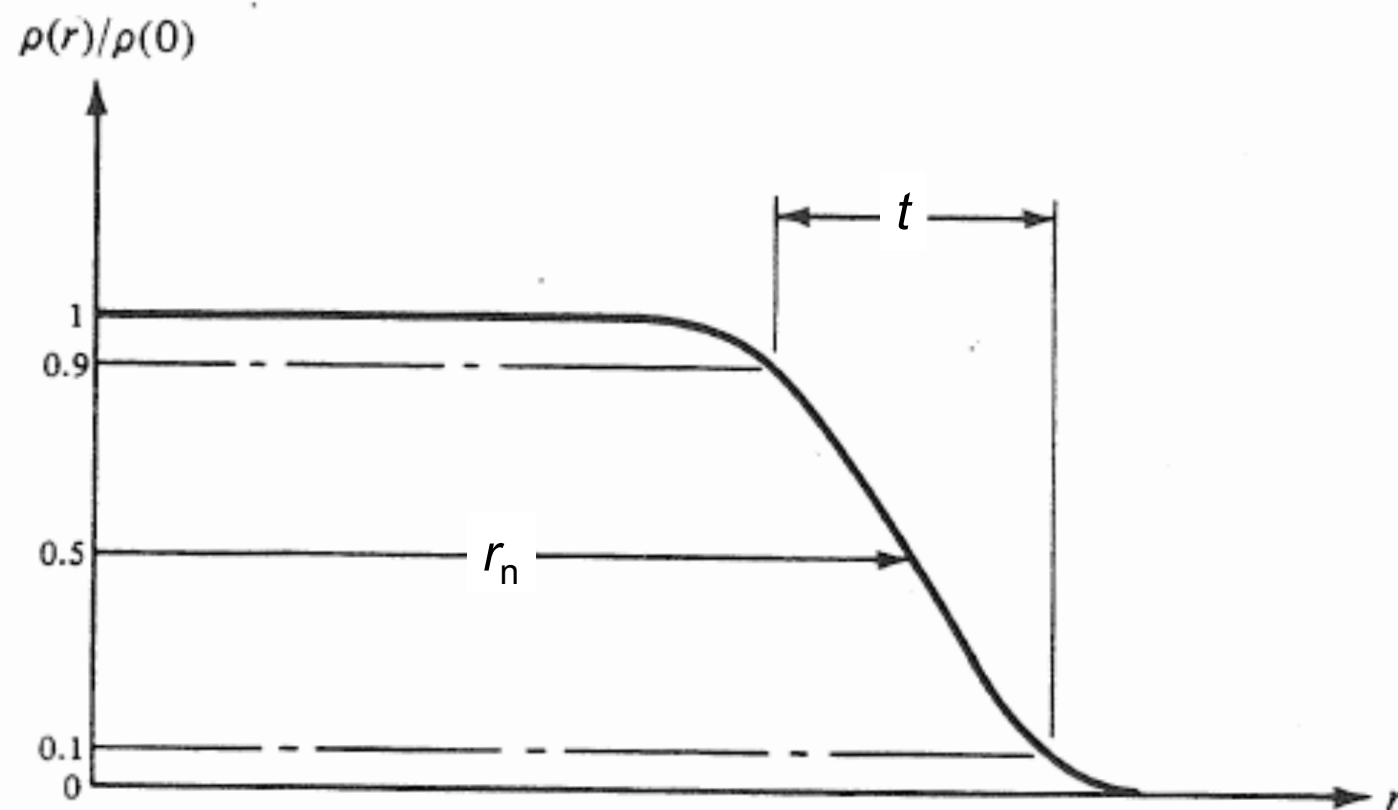
P. Agrawal, Z. Chacko, C. Kilic, and R.K. Mishra, arXiv:1003.1912

A. Crivellin, M. Hoferichter, and M. Procura, PRD 89 (2014), arXiv:1312.4951

M. Hoferichter, P. Klos, and A. Schwenk, Phys.Lett. B746 (2015) 410-416, arXiv:1503.04811

Coherent scattering occurs for $q < 1/R_{\text{Nucleus}} \simeq \text{MeV} \left(160/A_T^{1/3}\right)$

The non-zero nuclear size and momentum dependence is encoded in form factors, which can account for the loss of coherence at higher momentum transfers



Target specific nuclear physics is also taken into account

R. Schnee, arXiv:1101.5205
G.B. Gelmini, arXiv:1502.01320

The differential recoil rate is the primary quantity of interest

$$\frac{dR}{dE_R} = \frac{\rho_\chi}{m_\chi m_N} \int_{|\mathbf{v}| > v_{\min}} |\mathbf{v}| f(\mathbf{v}) \frac{d\sigma}{dE_R} d^3\mathbf{v}$$

astrophysics input

particle input

The minimum velocity which can contribute to a recoil is

$$v_{\min} = \frac{1}{\sqrt{2E_R m_N}} \left(\frac{E_R m_N}{\mu_{\chi N}} + \delta \right) \quad \text{inelastic}$$

$$\langle E_R \rangle = \frac{1}{2} M_\chi \langle v \rangle^2 \quad \mathcal{O}(\text{few} \times 10 \text{keV})$$

There is also a cut-off energy

$$E_{\max} = \frac{v_{\text{esc}}^2}{v_0^2} \langle E_R \rangle \approx 6 \langle E_R \rangle$$

The differential recoil rate is the primary quantity of interest

$$\frac{dR}{dE_R} = \frac{\rho_\chi}{m_\chi m_N} \int_{|\mathbf{v}| > v_{\min}} |\mathbf{v}| f(\mathbf{v}) \frac{d\sigma}{dE_R} d^3\mathbf{v}$$

astrophysics input

particle input

For actual detectors one must also account for the detector's efficiency and energy resolution.

WIMP-nucleon scattering is factorized

$$\frac{d\sigma_{\text{WN}}(q)}{dq^2} = \frac{1}{\pi v^2} |\mathcal{M}|^2 = \frac{\sigma_{0\text{WN}} F^2(q)}{4\mu_A^2 v^2}$$

$$\mu_A \equiv M_\chi M_A / (M_\chi + M_A)$$

With a form factor that incorporates momentum transfer

Spin-independent

Spin-dependent

$$\sigma_{0\text{WN}} = \frac{4\mu_A^2}{\pi} [Z f_p + (A - Z) f_n]^2 + \frac{32G_F^2 \mu_A^2}{\pi} \frac{J + 1}{J} (a_p \langle S_p \rangle + a_n \langle S_n \rangle)^2$$

$$\sigma_{0\text{WN,SI}} = \sigma_{\text{SI}} \frac{\mu_A^2}{\mu_n^2} A^2$$

Heavy target enhancement

$$\langle S_{p,n} \rangle = \langle N | S_{p,n} | N \rangle$$

Nucleon spin expectation values

$$\sigma_{\text{SI}} \equiv \frac{4\mu_n^2 f_n^2}{\pi}$$

Coherent scattering

V.V.Khoze's talk

Values for nucleon
properties for a
various target
materials

Nucleus	Z	Odd Nuc.	J	$\langle S_p \rangle$	$\langle S_n \rangle$	$\frac{4\langle S_p \rangle^2(J+1)}{3J}$	$\frac{4\langle S_n \rangle^2(J+1)}{3J}$
^{19}F	9	p	1/2	0.477	-0.004	9.1×10^{-1}	6.4×10^{-5}
^{23}Na	11	p	3/2	0.248	0.020	1.3×10^{-1}	8.9×10^{-4}
^{27}Al	13	p	5/2	-0.343	0.030	2.2×10^{-1}	1.7×10^{-3}
^{29}Si	14	n	1/2	-0.002	0.130	1.6×10^{-5}	6.8×10^{-2}
^{35}Cl	17	p	3/2	-0.083	0.004	1.5×10^{-2}	3.6×10^{-5}
^{39}K	19	p	3/2	-0.180	0.050	7.2×10^{-2}	5.6×10^{-3}
^{73}Ge	32	n	9/2	0.030	0.378	1.5×10^{-3}	2.3×10^{-1}
^{93}Nb	41	p	9/2	0.460	0.080	3.4×10^{-1}	1.0×10^{-2}
^{125}Te	52	n	1/2	0.001	0.287	4.0×10^{-6}	3.3×10^{-1}
^{127}I	53	p	5/2	0.309	0.075	1.8×10^{-1}	1.0×10^{-2}
^{129}Xe	54	n	1/2	0.028	0.359	3.1×10^{-3}	5.2×10^{-1}
^{131}Xe	54	n	3/2	-0.009	-0.227	1.8×10^{-4}	1.2×10^{-1}

R.W. Schnee, arXiv:1101.5205

	NA(%)	J	$\frac{ \langle S_p \rangle_{\text{th}} }{ \langle S_n \rangle_{\text{th}} }$	$\frac{\langle S_p \rangle_{\text{lit}}}{\langle S_n \rangle_{\text{lit}}}$	$\frac{ \langle L_p \rangle_{\text{th}} }{ \langle L_n \rangle_{\text{th}} }$	$\frac{\langle L_p \rangle_{\text{lit}}}{\langle L_n \rangle_{\text{lit}}}$	$ \tilde{\mu}_{\text{th}} $	$\tilde{\mu}_{\text{lit}}$	$\tilde{\mu}_{\text{exp}}$	Lit Ref.
^{19}F	100	1/2	0.475 0.009	0.4751 -0.0087	0.224 0.19	0.4751 -0.0087	2.911	2.91	2.6289	[42]
^{23}Na	100	3/2	0.248 0.02	0.2477 0.0199	0.912 0.321	0.2477 0.0199	2.219	2.22	2.2175	[42]
^{73}Ge	7.7	9/2	0.008 0.475	0.03 0.378	0.184 3.832	0.361 3.732	1.591	-0.92	-0.8795	[43]
^{127}I	100	5/2	0.264 0.066	0.309 0.075	1.515 0.655	1.338 0.779	2.74	2.775	2.8133	[40]
^{129}Xe	26.4	1/2	0.007 0.248	0.01 0.329	0.274 0.03	0.372 -0.185	0.636	-0.72	-0.778	[39], [40]
^{131}Xe	21.2	3/2	0.005 0.199	-0.009 -0.272	0.284 1.419	0.165 1.572	1.016	0.86	0.6919	[39], [40]

A More General Framework

It has been shown that the standard approach neglects a large set of possible non-relativistic operators beyond the SI/SD ones

$$1_\chi 1_N$$

Spin-independent

$$\vec{S}_\chi \cdot \vec{S}_N$$

Spin-dependent

There also exist four more nuclear responses that arise in the most general nucleus-WIMP elastic scattering

$$M, \Phi'', \Sigma', \Delta, \Sigma'', \tilde{\Phi}'$$

$$\vec{S}_\chi \cdot \vec{S}_N \equiv (\vec{S}_\chi \cdot \hat{q})(\vec{S}_N \cdot \hat{q}) + (\vec{S}_\chi \times \hat{q}) \cdot (\vec{S}_N \times \hat{q})$$

J. Fan, M. Reece, and L-T. Wang, JCAP 1011 (2010) 042, arXiv:1008.1591
A.L. Fitzpatrick, W.C. Haxton, E. Katz, N. Lubbers, and Y. Xu, JCAP 1302 (2013) 004, arXiv:1203.3542
A.L. Fitzpatrick, W.C. Haxton, E. Katz, N. Lubbers, and Y. Xu, arXiv:1211.2818
N. Anand, A.L. Fitzpatrick, and W.C. Haxton, Phys.Rev. C89, 065501 (2014)

From the general interaction

$$\mathcal{L}_{\text{int}}(\vec{x}) = c \Psi_{\chi}^*(\vec{x}) \mathcal{O}_{\chi} \Psi_{\chi}(\vec{x}) \Psi_N^*(\vec{x}) \mathcal{O}_N \Psi_N(\vec{x})$$

The scattering probability can be written as a factorized product of particle and nuclear physics responses

$$\frac{1}{2j_{\chi} + 1} \frac{1}{2j_N + 1} \sum_{\text{spins}} |\mathcal{M}|^2 \equiv \sum_k \sum_{\tau=0,1} \sum_{\tau'=0,1} \boxed{\begin{array}{|c|c|} \hline R_k \left(\vec{v}_T^{\perp 2}, \frac{\vec{q}^2}{m_N^2}, \left\{ c_i^{\tau} c_j^{\tau'} \right\} \right) & W_k^{\tau\tau'}(\vec{q}^2 b^2) \\ \hline \end{array}} \begin{array}{cc} \text{particle} & \text{nuclear} \end{array}$$

$$\langle \phi(x_1) \cdots \phi(x_k) \rangle_J \equiv e^{-iW[J]} \int \mathcal{D}\phi [\phi(x_1) \cdots \phi(x_k)] e^{iW[J]} \\
e^{iW[J]} = \int \mathcal{D}\phi \exp \left\{ i \int d^4x [\mathcal{L}[\phi] + J\phi] \right\}$$

Effective Field Theory

$$\Gamma[\varphi] \equiv W[J(\varphi)] - \int d^4x$$

Incorporating Galilean invariance, energy conservation, and Hermiticity, all non-relativistic operators will be built out of four quantities

$$\begin{array}{ccccccc}
 \boxed{\text{Exchanged momentum}} & i \frac{\vec{q}}{m_N}, & \vec{v}^\perp, & \vec{S}_\chi, & \vec{S}_N & \boxed{\text{Nucleon spin}} \\
 & & \boxed{\text{DM spin}} & & &
 \end{array}$$

Relative velocities

$$\vec{v}^\perp = \frac{1}{2} (\vec{v}_{\chi,in} - \vec{v}_{N,in} + \vec{v}_{\chi,out} - \vec{v}_{N,out}) \qquad \vec{v}^\perp \cdot \vec{q} = 0$$

There are fifteen combinations of these operators

Spin-independent

 \mathcal{O}_1

$$1_\chi 1_N$$

 \mathcal{O}_2

$$(\vec{v}^\perp)^2$$

 \mathcal{O}_3

$$i\vec{S}_N \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}^\perp\right)$$

Spin-dependent

 \mathcal{O}_4

$$\vec{S}_\chi \cdot \vec{S}_N$$

 \mathcal{O}_5

$$i\vec{S}_\chi \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}^\perp\right)$$

 \mathcal{O}_6

$$\left(\frac{\vec{q}}{m_N} \cdot \vec{S}_N\right) \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi\right)$$

 \mathcal{O}_7

$$\vec{S}_N \cdot \vec{v}^\perp$$

 \mathcal{O}_8

$$\vec{S}_\chi \cdot \vec{v}^\perp$$

 \mathcal{O}_9

$$i\vec{S}_\chi \cdot \left(\vec{S}_N \times \frac{\vec{q}}{m_N}\right)$$

 \mathcal{O}_{10}

$$i\frac{\vec{q}}{m_N} \cdot \vec{S}_N$$

 \mathcal{O}_{11}

$$i\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi$$

 \mathcal{O}_{12}

$$\vec{S}_\chi \cdot (\vec{S}_N \times \vec{v}^\perp)$$

 \mathcal{O}_{13}

$$i(\vec{S}_\chi \cdot \vec{v}^\perp) \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_N\right)$$

 \mathcal{O}_{14}

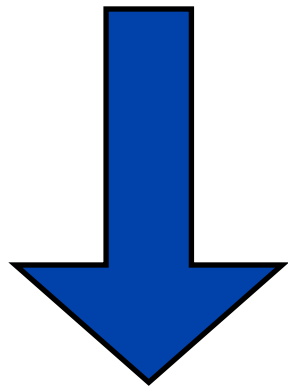
$$i(\vec{S}_N \cdot \vec{v}^\perp) \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi\right)$$

 \mathcal{O}_{15}

$$-(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N}) \left((\vec{S}_N \times \vec{v}^\perp) \cdot \frac{\vec{q}}{m_N} \right)$$

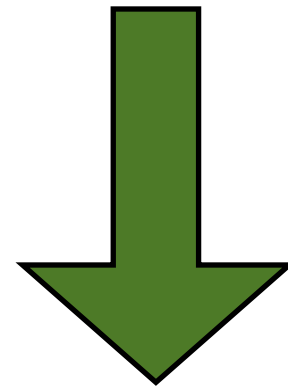
Standard practice has been to start with effective interaction terms, and then reduce in the non-relativistic limit

$$\mathcal{L}_{\text{int}}^{\text{SI}}(\vec{x}) = c_1 \bar{\Psi}_{\chi}(\vec{x}) \Psi_{\chi}(\vec{x}) \bar{\Psi}_N(\vec{x}) \Psi_N(\vec{x})$$



$$c_1 1_{\chi} 1_N$$

$$\mathcal{L}_{\text{int}}^{\text{SD}} = c_4 \bar{\chi} \gamma^{\mu} \gamma^5 \chi \bar{N} \gamma_{\mu} \gamma^5 N$$



$$-4c_4 \vec{S}_{\chi} \cdot \vec{S}_N$$

From the relativistic EFT there are 20 combinations of fermionic bilinears

From two scalar

$$\bar{\chi}\chi$$

$$\bar{\chi}\gamma^5\chi$$

$$2\times 2$$

$$\bar{\chi}\gamma^\mu\chi$$

$$\bar{\chi}\gamma^\mu\gamma^5\chi$$

and four vector terms

$$4\times 4$$

$$P^\mu\bar{\chi}\chi$$

$$P^\mu\bar{\chi}\gamma^5\chi$$

$$20$$

After performing a non-relativistic reduction, these 20 operators can be written in terms of the 15 O_i

Effective Action

Non-rel limit

Operator Matching

j	$\mathcal{L}_{\text{int}}^j$	Nonrelativistic reduction	$\sum_i c_i \mathcal{O}_i$	P/T
1	$\bar{\chi} \chi \bar{N} N$	$1_\chi 1_N$	\mathcal{O}_1	E/E
2	$i \bar{\chi} \chi \bar{N} \gamma^5 N$	$i \frac{\vec{q}}{m_N} \cdot \vec{S}_N$	\mathcal{O}_{10}	O/O
3	$i \bar{\chi} \gamma^5 \chi \bar{N} N$	$-i \frac{\vec{q}}{m_\chi} \cdot \vec{S}_\chi$	$-\frac{m_N}{m_\chi} \mathcal{O}_{11}$	O/O
4	$\bar{\chi} \gamma^5 \chi \bar{N} \gamma^5 N$	$-\frac{\vec{q}}{m_\chi} \cdot \vec{S}_\chi \frac{\vec{q}}{m_N} \cdot \vec{S}_N$	$-\frac{m_N}{m_\chi} \mathcal{O}_6$	E/E
5	$\bar{\chi} \gamma^\mu \chi \bar{N} \gamma_\mu N$	$1_\chi 1_N$	\mathcal{O}_1	E/E
6	$\bar{\chi} \gamma^\mu \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} N$	$\frac{\vec{q}^2}{2m_N m_M} 1_\chi 1_N + 2 \left(\frac{\vec{q}}{m_\chi} \times \vec{S}_\chi + i \vec{v}^\perp \right) \cdot \left(\frac{\vec{q}}{m_M} \times \vec{S}_N \right)$	$\frac{\vec{q}^2}{2m_N m_M} \mathcal{O}_1 - 2 \frac{m_N}{m_M} \mathcal{O}_3 + 2 \frac{m_N^2}{m_M m_\chi} \left(\frac{q^2}{m_N^2} \mathcal{O}_4 - \mathcal{O}_6 \right)$	E/E
7	$\bar{\chi} \gamma^\mu \chi \bar{N} \gamma_\mu \gamma^5 N$	$-2 \vec{S}_N \cdot \vec{v}^\perp + \frac{2}{m_\chi} i \vec{S}_\chi \cdot (\vec{S}_N \times \vec{q})$	$-2 \mathcal{O}_7 + 2 \frac{m_N}{m_\chi} \mathcal{O}_9$	O/E
8	$i \bar{\chi} \gamma^\mu \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} \gamma^5 N$	$2i \frac{\vec{q}}{m_M} \cdot \vec{S}_N$	$2 \frac{m_N}{m_M} \mathcal{O}_{10}$	O/O
9	$\bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \chi \bar{N} \gamma_\mu N$	$-\frac{\vec{q}^2}{2m_\chi m_M} 1_\chi 1_N - 2 \left(\frac{\vec{q}}{m_N} \times \vec{S}_N + i \vec{v}^\perp \right) \cdot \left(\frac{\vec{q}}{m_M} \times \vec{S}_\chi \right)$	$-\frac{\vec{q}^2}{2m_\chi m_M} \mathcal{O}_1 + \frac{2m_N}{m_M} \mathcal{O}_5 - 2 \frac{m_N}{m_M} \left(\frac{\vec{q}^2}{m_N^2} \mathcal{O}_4 - \mathcal{O}_6 \right)$	E/E
10	$\bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} N$	$4 \left(\frac{\vec{q}}{m_M} \times \vec{S}_\chi \right) \cdot \left(\frac{\vec{q}}{m_M} \times \vec{S}_N \right)$	$4 \left(\frac{\vec{q}^2}{m_M^2} \mathcal{O}_4 - \frac{m_N^2}{m_M^2} \mathcal{O}_6 \right)$	E/E
11	$\bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \chi \bar{N} \gamma^\mu \gamma^5 N$	$4i \left(\frac{\vec{q}}{m_M} \times \vec{S}_\chi \right) \cdot \vec{S}_N$	$4 \frac{m_N}{m_M} \mathcal{O}_9$	O/E
12	$i \bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} \gamma^5 N$	$- \left[i \frac{\vec{q}^2}{m_\chi m_M} - 4 \vec{v}^\perp \cdot \left(\frac{\vec{q}}{m_M} \times \vec{S}_\chi \right) \right] \frac{\vec{q}}{m_M} \cdot \vec{S}_N$	$-\frac{m_N}{m_\chi} \frac{\vec{q}^2}{m_M^2} \mathcal{O}_{10} - 4 \frac{\vec{q}^2}{m_M^2} \mathcal{O}_{12} - 4 \frac{m_N^2}{m_M^2} \mathcal{O}_{15}$	O/O
13	$\bar{\chi} \gamma^\mu \gamma^5 \chi \bar{N} \gamma_\mu N$	$2 \vec{v}^\perp \cdot \vec{S}_\chi + 2i \vec{S}_\chi \cdot (\vec{S}_N \times \frac{\vec{q}}{m_N})$	$2 \mathcal{O}_8 + 2 \mathcal{O}_9$	O/E
14	$\bar{\chi} \gamma^\mu \gamma^5 \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} N$	$4i \vec{S}_\chi \cdot \left(\frac{\vec{q}}{m_M} \times \vec{S}_N \right)$	$-4 \frac{m_N}{m_M} \mathcal{O}_9$	O/E
15	$\bar{\chi} \gamma^\mu \gamma^5 \chi \bar{N} \gamma^\mu \gamma^5 N$	$-4 \vec{S}_\chi \cdot \vec{S}_N$	$-4 \mathcal{O}_4$	E/E
16	$i \bar{\chi} \gamma^\mu \gamma^5 \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} \gamma^5 N$	$4i \vec{v}^\perp \cdot \vec{S}_\chi \frac{\vec{q}}{m_M} \cdot \vec{S}_N$	$4 \frac{m_N}{m_M} \mathcal{O}_{13}$	E/O
17	$i \bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \gamma^5 \chi \bar{N} \gamma_\mu N$	$2i \frac{\vec{q}}{m_M} \cdot \vec{S}_\chi$	$2 \frac{m_N}{m_M} \mathcal{O}_{11}$	O/O
18	$i \bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \gamma^5 \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} N$	$\frac{\vec{q}}{m_M} \cdot \vec{S}_\chi \left[i \frac{\vec{q}^2}{m_N m_M} - 4 \vec{v}^\perp \cdot \left(\frac{\vec{q}}{m_M} \times \vec{S}_N \right) \right]$	$\frac{\vec{q}^2}{m_M^2} \mathcal{O}_{11} + 4 \frac{m_N^2}{m_M^2} \mathcal{O}_{15}$	O/O
19	$i \bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \gamma^5 \chi \bar{N} \gamma_\mu \gamma^5 N$	$-4i \frac{\vec{q}}{m_M} \cdot \vec{S}_\chi \vec{v}^\perp \cdot \vec{S}_N$	$-4 \frac{m_N}{m_M} \mathcal{O}_{14}$	E/O
20	$i \bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \gamma^5 \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} \gamma^5 N$	$4 \frac{\vec{q}}{m_M} \cdot \vec{S}_\chi \frac{\vec{q}}{m_M} \cdot \vec{S}_N$	$4 \frac{m_N^2}{m_M^2} \mathcal{O}_6$	E/E

In general one can write down the non-relativistic Lagrangian

$$\mathcal{L}_{NR} = \sum_{\alpha=n,p} \sum_{i=1}^{15} c_i^\alpha \mathcal{O}_i^\alpha$$

General isospin (isoscalar/isovector) couplings to protons and neutrons is incorporated

$$\mathcal{L}_{NR} = \sum_{\tau=0,1} \sum_{i=1}^{15} c_i^\tau \mathcal{O}_i t^\tau \quad c_i^0 = \frac{1}{2}(c_i^p + c_i^n) \quad c_i^1 = \frac{1}{2}(c_i^p - c_i^n)$$

The total interaction can be considered as a sum over single nucleon interactions

$$\sum_{\tau=0,1} \sum_{i=1}^{15} c_i^\tau \mathcal{O}_i t^\tau \rightarrow \sum_{\tau=0,1} \sum_{i=1}^{15} c_i^\tau \sum_{j=1}^A \mathcal{O}_i(j) t^\tau(j)$$

The DM-nucleon interactions can then be written

$$\sum_{\tau=0,1} \left\{ l_0^\tau S + l_0^{A\tau} T + \vec{l}_5^\tau \cdot \vec{P} + \vec{l}_M^\tau \cdot \vec{Q} + \vec{l}_E^\tau \cdot \vec{R} \right\} t^\tau(i)$$

$$\sum_{\tau=0,1} \left\{ l_0^\tau S + l_0^{A\tau} T + \vec{l}_5^\tau \cdot \vec{P} + \vec{l}_M^\tau \cdot Q + \vec{l}_E^\tau \cdot \vec{R} \right\} t^\tau(i)$$

Nuclear

DM

$$S = \sum_{i=1}^A e^{-i\vec{q} \cdot \vec{x}_i}$$

$$T = \sum_{i=1}^A \frac{1}{2M} \left[-\frac{1}{i} \overleftarrow{\nabla}_i \cdot \vec{\sigma}(i) e^{-i\vec{q} \cdot \vec{x}_i} + e^{-i\vec{q} \cdot \vec{x}_i} \vec{\sigma}(i) \cdot \frac{1}{i} \overrightarrow{\nabla}_i \right]$$

$$\vec{P} = \sum_{i=1}^A \vec{\sigma}(i) e^{-i\vec{q} \cdot \vec{x}_i}$$

$$\vec{Q} = \sum_{i=1}^A \frac{1}{2M} \left[-\frac{1}{i} \overleftarrow{\nabla}_i e^{-i\vec{q} \cdot \vec{x}_i} + e^{-i\vec{q} \cdot \vec{x}_i} \frac{1}{i} \overrightarrow{\nabla}_i \right]$$

$$\vec{R} = \sum_{i=1}^A \frac{1}{2M} \left[\overleftarrow{\nabla}_i \times \vec{\sigma}(i) e^{-i\vec{q} \cdot \vec{x}_i} + e^{-i\vec{q} \cdot \vec{x}_i} \vec{\sigma}(i) \times \overrightarrow{\nabla}_i \right]$$

Plane waves associated with the nucleon states, which can be expanded in Bessel spherical and Bessel vector harmonics

Given a non-relativistic reduction, one can identify the dark matter operator coefficients

$$\sum_{\tau=0,1} \left\{ l_0^\tau S + l_0^{A\tau} T + \vec{l}_5^\tau \cdot \vec{P} + \vec{l}_M^\tau \cdot Q + \vec{l}_E^\tau \cdot \vec{R} \right\} t^\tau(i)$$

Nuclear

DM

$$\begin{aligned} l_0^\tau &= c_1^\tau + ic_5^\tau \vec{S}_\chi \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}_T^\perp \right) + c_8^\tau (\vec{S}_\chi \cdot \vec{v}_T^\perp) + ic_{11}^\tau \frac{\vec{q} \cdot \vec{S}_\chi}{m_N} \\ l_0^{A\tau} &= -\frac{1}{2} \left[c_7^\tau + ic_{14}^\tau \left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N} \right) \right] \\ \vec{l}_5^\tau &= \frac{1}{2} \left[c_3^\tau i \frac{(\vec{q} \times \vec{v}_T^\perp)}{m_N} + c_4^\tau \vec{S}_\chi + c_6^\tau \frac{(\vec{q} \cdot \vec{S}_\chi) \vec{q}}{m_N^2} + c_7^\tau \vec{v}_T^\perp + ic_9^\tau \frac{(\vec{q} \times \vec{S}_\chi)}{m_N} + ic_{10}^\tau \frac{\vec{q}}{m_N} \right. \\ &\quad \left. c_{12}^\tau (\vec{v}_T^\perp \times \vec{S}_\chi) + ic_{13}^\tau \frac{(\vec{S}_\chi \cdot \vec{v}_T^\perp) \vec{q}}{m_N} + ic_{14}^\tau \left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N} \right) \vec{v}_T^\perp + c_{15}^\tau \frac{(\vec{q} \cdot \vec{S}_\chi) (\vec{q} \times \vec{v}_T^\perp)}{m_N^2} \right] \\ \vec{l}_M^\tau &= c_5^\tau \left(i \frac{\vec{q}}{m_N} \times \vec{S}_\chi \right) - \vec{S}_\chi c_8^\tau \\ \vec{l}_E^\tau &= \frac{1}{2} \left[c_3^\tau \frac{\vec{q}}{m_N} + ic_{12}^\tau \vec{S}_\chi - c_{13}^\tau \frac{(\vec{q} \times \vec{S}_\chi)}{m_N} - ic_{15}^\tau \frac{(\vec{q} \cdot \vec{S}_\chi) \vec{q}}{m_N^2} \right] \end{aligned}$$

These coefficients apply to the dark matter in and out states

The dark matter-nucleus amplitude can be written as

$$\mathcal{M} = \sum_{\tau=0,1} \langle j_\chi, M_\chi; j_N, M_N | \left\{ l_0^\tau S + l_0^{A\tau} T + \vec{l}_5^\tau \cdot \vec{P} + \vec{l}_M^\tau \cdot \vec{Q} + \vec{l}_E^\tau \cdot \vec{R} \right\} t^\tau(i) | j_\chi, M_\chi; j_N, M_N \rangle$$

which can further be reduced to the standard nuclear electroweak responses

$$\begin{aligned} \mathcal{M} = & \sum_{\tau=0,1} \langle j_\chi, M_{\chi f}; j_N, M_{Nf} | \left(\sum_{J=0} \sqrt{4\pi(2J+1)} (-i)^J \left[l_0^\tau \boxed{M_{J0;\tau}} - i l_0^{A\tau} \frac{q}{m_N} \boxed{\tilde{\Omega}_{J0;\tau}(q)} \right] \right. \\ & + \sum_{J=1} \sqrt{2\pi(2J+1)} (-i)^J \sum_{\lambda \pm 1} (-1)^\lambda \left\{ l_{5\lambda}^\tau [\lambda \boxed{\Sigma_{J-\lambda;\tau}(q)} + i \boxed{\Sigma'_{J-\lambda;\tau}(q)}] \right. \\ & \left. - i \frac{q}{m_N} l_{M\lambda}^\tau [\lambda \boxed{\Delta_{J-\lambda;\tau}(q)}] - i \frac{q}{m_N} l_{E\lambda}^\tau [\lambda \boxed{\tilde{\Phi}_{J-\lambda;\tau}(q)} + i \boxed{\tilde{\Phi}'_{J-\lambda;\tau}(q)}] \right\} \\ & \left. + \sum_{J=0}^\infty \sqrt{4\pi(2J+1)} (-i)^J \left[i l_{50}^\tau \boxed{\Sigma''_{J0;\tau}(q)} + \frac{q}{m_N} l_{M0}^\tau \boxed{\tilde{\Delta}''_{J0;\tau}(q)} + \frac{q}{m_N} l_{E0}^\tau \boxed{\tilde{\Phi}''_{J0;\tau}(q)} \right] \right) | j_\chi, M_{\chi i}; j_N, M_{Ni} \rangle \end{aligned}$$

Assuming P and CP are good symmetries of the nuclear ground state leaves one with 6 responses

$$M, \Phi'', \Sigma', \Delta, \Sigma'', \tilde{\Phi}'$$

$$\Delta_{JM} \equiv \vec{M}_{JJ}^M(qx_i) \cdot \frac{1}{q} \vec{\nabla}_i$$

Spin-independent

Spin-dependent

$$\Sigma'_{JM} \equiv -i \left\{ \frac{1}{q} \vec{\nabla}_i \times \vec{M}_{JJ}^M(q\vec{x}_i) \right\} \cdot \vec{\sigma}(i)$$

$$\Sigma''_{JM} \equiv \left\{ \frac{1}{q} \vec{\nabla}_i M_{JM}(q\vec{x}_i) \right\} \cdot \vec{\sigma}(i)$$

$$\tilde{\Phi}'_{JM} \equiv \left[\frac{1}{q} \vec{\nabla}_i \times \vec{M}_{JJ}^M(q\vec{x}_i) \right] \cdot \left[\vec{\sigma}(i) \times \frac{1}{q} \vec{\nabla}_i \right] + \frac{1}{2} \vec{M}_{JJ}^M(q\vec{x}_i) \cdot \vec{\sigma}(i)$$

$$\Phi''_{JM} \equiv i \left[\frac{1}{q} \vec{\nabla}_i M_{JM}(q\vec{x}_i) \right] \cdot \left[\vec{\sigma}(i) \times \frac{1}{q} \vec{\nabla}_i \right]$$

In the long wavelength limit these correspond to various physical interpretations

$$\Delta_{JM} \equiv \vec{M}_{JJ}^M(qx_i) \cdot \frac{1}{q} \vec{\nabla}_i$$

$$\Sigma'_{JM} \equiv -i \left\{ \frac{1}{q} \vec{\nabla}_i \times \vec{M}_{JJ}^M(q\vec{x}_i) \right\} \cdot \vec{\sigma}(i)$$

$$\Sigma''_{JM} \equiv \left\{ \frac{1}{q} \vec{\nabla}_i M_{JM}(q\vec{x}_i) \right\} \cdot \vec{\sigma}(i)$$

$$\tilde{\Phi}'_{JM} \equiv \left[\frac{1}{q} \vec{\nabla}_i \times \vec{M}_{JJ}^M(q\vec{x}_i) \right] \cdot \left[\vec{\sigma}(i) \times \frac{1}{q} \vec{\nabla}_i \right] + \frac{1}{2} \vec{M}_{JJ}^M(q\vec{x}_i) \cdot \vec{\sigma}(i)$$

$$\Phi''_{JM} \equiv i \left[\frac{1}{q} \vec{\nabla}_i M_{JM}(q\vec{x}_i) \right] \cdot \left[\vec{\sigma}(i) \times \frac{1}{q} \vec{\nabla}_i \right]$$

X	$\frac{4\pi}{2J+1} W_X^{(p,p)}(0)$
M spin-independent	Z^2
Σ'' spin-dependent (longitudinal)	$4 \frac{J+1}{3J} \langle S_p \rangle^2$
Σ' spin-dependent (transverse)	$8 \frac{J+1}{3J} \langle S_p \rangle^2$
Δ angular-momentum-dependent	$\frac{1}{2} \frac{J+1}{3J} \langle L_p \rangle^2$
Φ'' angular-momentum-and-spin-dependent	$\sim \langle \vec{S}_p \cdot \vec{L}_p \rangle^{2a}$

M.I. Gresham and K.M. Zurek, PRD 89 123521 (2014) arXiv:1401.3739

Projection	Charge/current	Operator	Even J	Odd J
Charge	Vector charge	M_{JM}	E-E	O-O
Charge	Axial-vector charge	$\tilde{\Omega}_{JM}$	O-E	E-O
Longitudinal	Spin current	Σ''_{JM}	O-O	E-E
Transverse magnetic	"	Σ_{JM}	E-O	O-E
Transverse electric	"	Σ'_{JM}	O-O	E-E
Longitudinal	Convection current	$\tilde{\Delta}''_{JM}$	E-O	O-E
Transverse magnetic	"	Δ_{JM}	O-O	E-E
Transverse electric	"	Δ'_{JM}	E-O	O-E
Longitudinal	Spin-velocity current	Φ''_{JM}	E-E	O-O
Transverse magnetic	"	$\tilde{\Phi}_{JM}$	O-E	E-O
Transverse electric	"	$\tilde{\Phi}'_{JM}$	E-E	O-O

To calculate cross-sections, one needs to square the amplitude, average over initial spins and sum over final states.

$$\frac{1}{2j_\chi + 1} \frac{1}{2j_N + 1} \sum_{\text{spins}} |\mathcal{M}|^2 \equiv \sum_k \sum_{\tau=0,1} \sum_{\tau'=0,1} R_k \left(\vec{v}_T^{\perp 2}, \frac{\vec{q}^2}{m_N^2}, \left\{ c_i^\tau c_j^{\tau'} \right\} \right) W_k^{\tau\tau'}(\vec{q}^2 b^2)$$

$$\begin{aligned} R_M^{\tau\tau'}(\vec{v}_T^{\perp 2}, \frac{\vec{q}^2}{m_N^2}) &= c_1^\tau c_1^{\tau'} + \frac{j_\chi(j_\chi + 1)}{3} \left[\frac{\vec{q}^2}{m_N^2} \vec{v}_T^{\perp 2} c_5^\tau c_5^{\tau'} + \vec{v}_T^{\perp 2} c_8^\tau c_8^{\tau'} + \frac{\vec{q}^2}{m_N^2} c_{11}^\tau c_{11}^{\tau'} \right] \\ R_{\Phi''}^{\tau\tau'}(\vec{v}_T^{\perp 2}, \frac{\vec{q}^2}{m_N^2}) &= \frac{\vec{q}^2}{4m_N^2} c_3^\tau c_3^{\tau'} + \frac{j_\chi(j_\chi + 1)}{12} \left(c_{12}^\tau - \frac{\vec{q}^2}{m_N^2} c_{15}^\tau \right) \left(c_{12}^{\tau'} - \frac{\vec{q}^2}{m_N^2} c_{15}^{\tau'} \right) \\ R_{\Phi''M}^{\tau\tau'}(\vec{v}_T^{\perp 2}, \frac{\vec{q}^2}{m_N^2}) &= c_3^\tau c_1^{\tau'} + \frac{j_\chi(j_\chi + 1)}{3} \left(c_{12}^\tau - \frac{\vec{q}^2}{m_N^2} c_{15}^\tau \right) c_{11}^{\tau'} \\ R_{\tilde{\Phi}'}^{\tau\tau'}(\vec{v}_T^{\perp 2}, \frac{\vec{q}^2}{m_N^2}) &= \frac{j_\chi(j_\chi + 1)}{12} \left[c_{12}^\tau c_{12}^{\tau'} + \frac{\vec{q}^2}{m_N^2} c_{13}^\tau c_{13}^{\tau'} \right] \\ R_{\Sigma''}^{\tau\tau'}(\vec{v}_T^{\perp 2}, \frac{\vec{q}^2}{m_N^2}) &= \frac{\vec{q}^2}{4m_N^2} c_{10}^\tau c_{10}^{\tau'} + \frac{j_\chi(j_\chi + 1)}{12} \left[c_4^\tau c_4^{\tau'} + \right. \\ &\quad \left. \frac{\vec{q}^2}{m_N^2} (c_4^\tau c_6^{\tau'} + c_6^\tau c_4^{\tau'}) + \frac{\vec{q}^4}{m_N^4} c_6^\tau c_6^{\tau'} + \vec{v}_T^{\perp 2} c_{12}^\tau c_{12}^{\tau'} + \frac{\vec{q}^2}{m_N^2} \vec{v}_T^{\perp 2} c_{13}^\tau c_{13}^{\tau'} \right] \\ R_{\Sigma'}^{\tau\tau'}(\vec{v}_T^{\perp 2}, \frac{\vec{q}^2}{m_N^2}) &= \frac{1}{8} \left[\frac{\vec{q}^2}{m_N^2} \vec{v}_T^{\perp 2} c_3^\tau c_3^{\tau'} + \vec{v}_T^{\perp 2} c_7^\tau c_7^{\tau'} \right] + \frac{j_\chi(j_\chi + 1)}{12} \left[c_4^\tau c_4^{\tau'} + \right. \\ &\quad \left. \frac{\vec{q}^2}{m_N^2} c_9^\tau c_9^{\tau'} + \frac{\vec{v}_T^{\perp 2}}{2} \left(c_{12}^\tau - \frac{\vec{q}^2}{m_N^2} c_{15}^\tau \right) \left(c_{12}^{\tau'} - \frac{\vec{q}^2}{m_N^2} c_{15}^{\tau'} \right) + \frac{\vec{q}^2}{2m_N^2} \vec{v}_T^{\perp 2} c_{14}^\tau c_{14}^{\tau'} \right] \\ R_{\Delta}^{\tau\tau'}(\vec{v}_T^{\perp 2}, \frac{\vec{q}^2}{m_N^2}) &= \frac{j_\chi(j_\chi + 1)}{3} \left[\frac{\vec{q}^2}{m_N^2} c_5^\tau c_5^{\tau'} + c_8^\tau c_8^{\tau'} \right] \\ R_{\Delta\Sigma'}^{\tau\tau'}(\vec{v}_T^{\perp 2}, \frac{\vec{q}^2}{m_N^2}) &= \frac{j_\chi(j_\chi + 1)}{3} \left[c_5^\tau c_4^{\tau'} - c_8^\tau c_9^{\tau'} \right]. \end{aligned}$$

**DM
response
functions**

Operator interference is in evidence

Nuclear response functions

Response function
interference occurs

$$W_M^{\tau\tau'}(y) = \sum_{J=0,2,\dots}^{\infty} \langle j_N || M_{J;\tau}(q) || j_N \rangle \langle j_N || M_{J;\tau'}(q) || j_N \rangle$$

$$W_{\Sigma''}^{\tau\tau'}(y) = \sum_{J=1,3,\dots}^{\infty} \langle j_N || \Sigma''_{J;\tau}(q) || j_N \rangle \langle j_N || \Sigma''_{J;\tau'}(q) || j_N \rangle$$

$$W_{\Sigma'}^{\tau\tau'}(y) = \sum_{J=1,3,\dots}^{\infty} \langle j_N || \Sigma'_{J;\tau}(q) || j_N \rangle \langle j_N || \Sigma'_{J;\tau'}(q) || j_N \rangle$$

$$W_{\Phi''}^{\tau\tau'}(y) = \sum_{J=0,2,\dots}^{\infty} \langle j_N || \Phi''_{J;\tau}(q) || j_N \rangle \langle j_N || \Phi''_{J;\tau'}(q) || j_N \rangle$$

$$W_{\Phi''M}^{\tau\tau'}(y) = \sum_{J=0,2,\dots}^{\infty} \langle j_N || \Phi''_{J;\tau}(q) || j_N \rangle \langle j_N || M_{J;\tau'}(q) || j_N \rangle$$

$$W_{\tilde{\Phi}'}^{\tau\tau'}(y) = \sum_{J=2,4,\dots}^{\infty} \langle j_N || \tilde{\Phi}'_{J;\tau}(q) || j_N \rangle \langle j_N || \tilde{\Phi}'_{J;\tau'}(q) || j_N \rangle$$

$$W_{\Delta}^{\tau\tau'}(y) = \sum_{J=1,3,\dots}^{\infty} \langle j_N || \Delta_{J;\tau}(q) || j_N \rangle \langle j_N || \Delta_{J;\tau'}(q) || j_N \rangle$$

$$W_{\Delta\Sigma'}^{\tau\tau'}(y) = \sum_{J=1,3,\dots}^{\infty} \langle j_N || \Delta_{J;\tau}(q) || j_N \rangle \langle j_N || \Sigma'_{J;\tau'}(q) || j_N \rangle.$$

Within this framework

- Include general dark matter particle types
- Include general mediator particle types
- Explore possible operator degeneracies
- Determine the dominant operators
- Determine distinguishability at detectors
- Connect to models for astrophysical and collider searches

Simplified models for **tree**-level, renormalizable interactions have been examined
single dark matter particle, single mediator

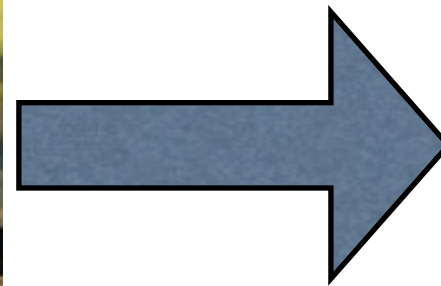
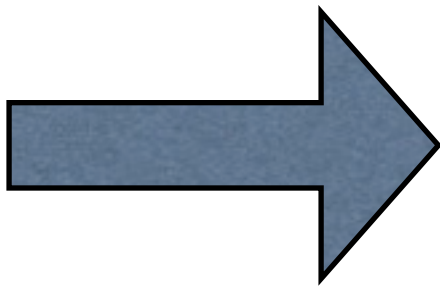
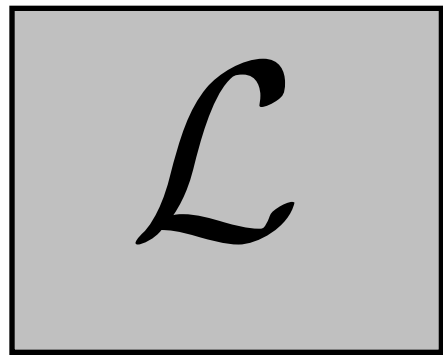
P. Agrawal, Z. Chacko, C. Kilic, and R.K. Mishra, arXiv:1003.1912

N. Anand, A.L. Fitzpatrick, and W.C. Haxton, Phys.Rev. C89, 065501 (2014)

JBD, L.M. Krauss, J.L. Newstead, and S. Sabharwal, PRD, arXiv: 1505.03117

$q\phi$ $\phi\chi$

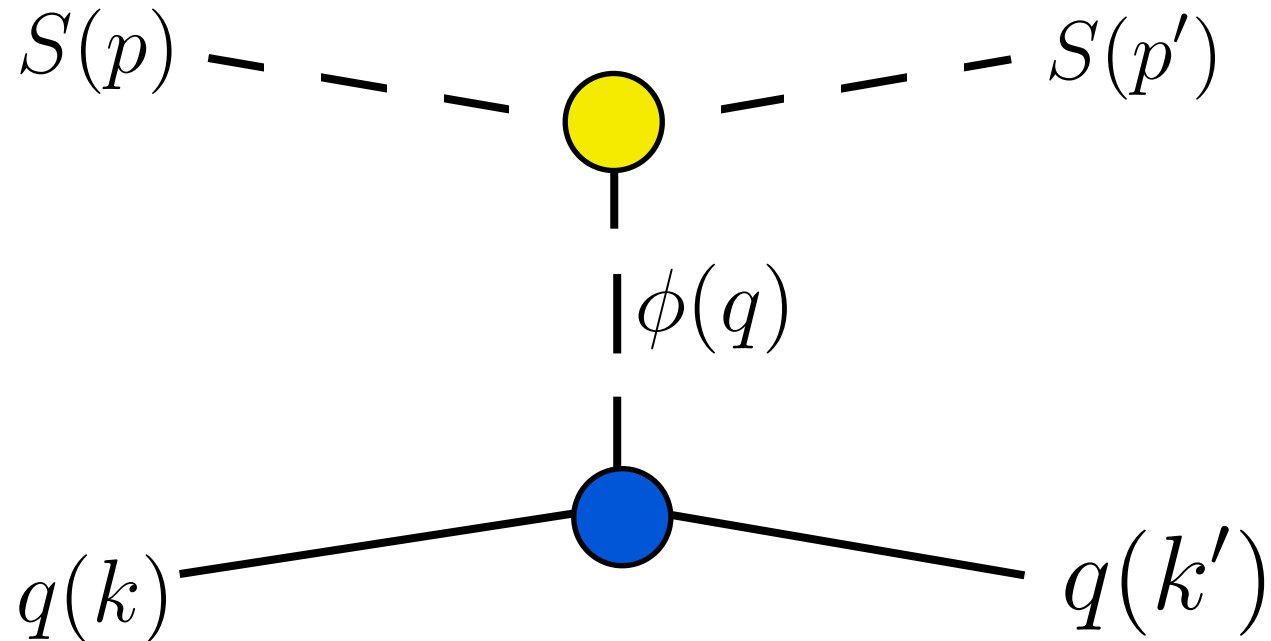
non-relativistic
reduction
match onto dark matter
and nuclear responses



$$\frac{dR}{dE_R}$$

Typically one integrates out the mediator, which amounts to assuming the mediator mass is much larger than the recoil momentum of the interaction

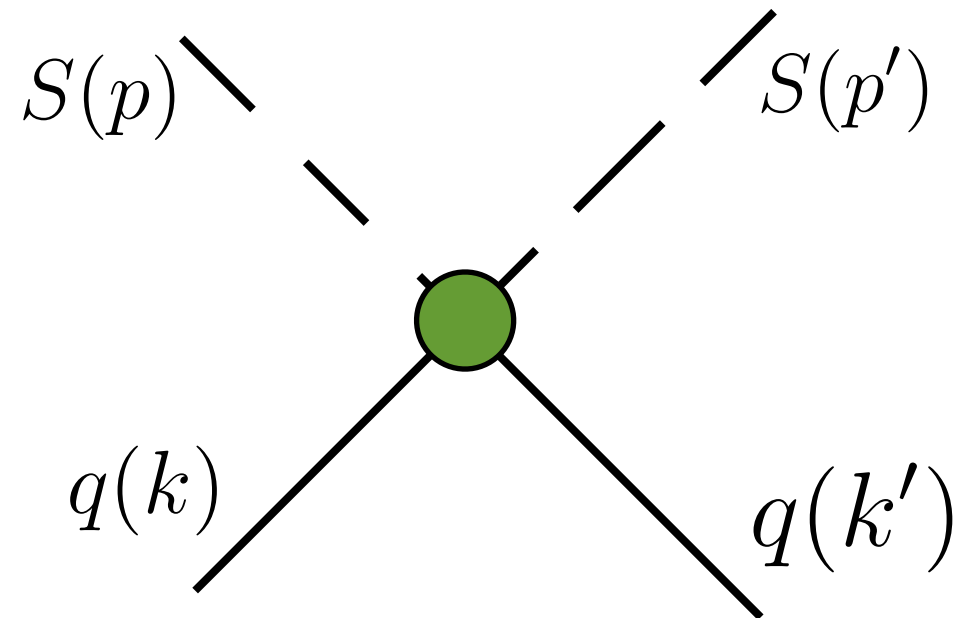
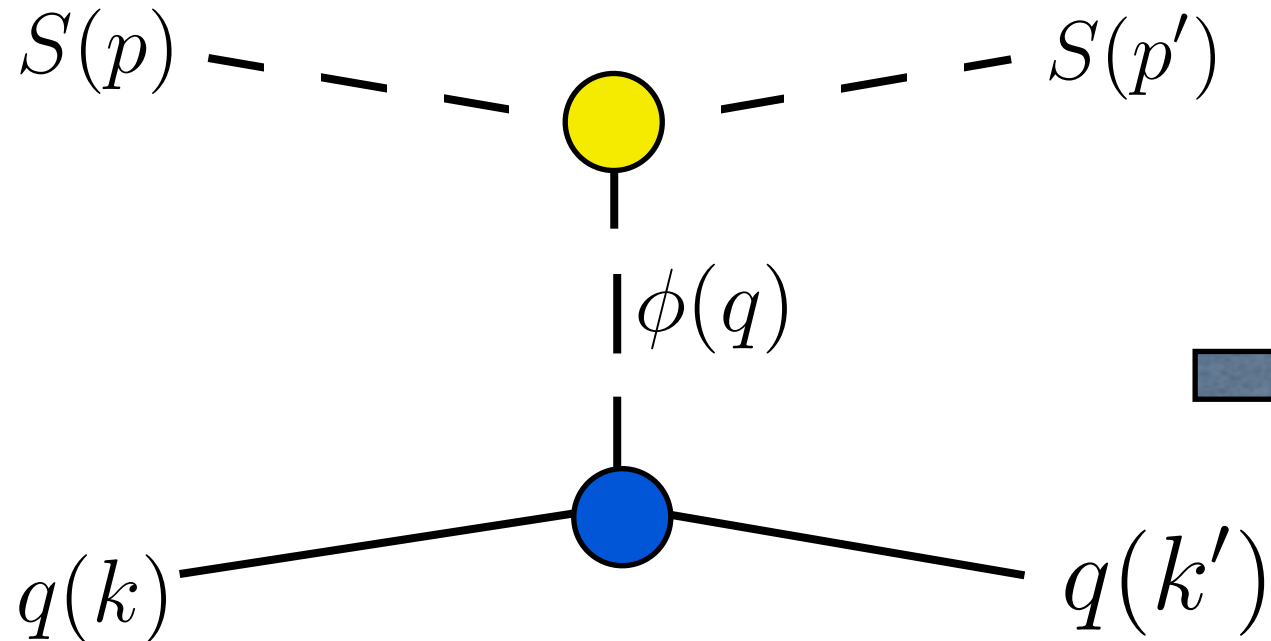
$$m_\phi^2 \gg q^2 = (p' - p)^2$$



$$\begin{aligned} \mathcal{L}_{S\phi q} = & \partial_\mu S^\dagger \partial^\mu S - m_S^2 S^\dagger S - \frac{\lambda_S}{2} (S^\dagger S)^2 \\ & + \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - \frac{1}{2} m_\phi^2 \phi^2 - \frac{m_\phi \mu_1}{3} \phi^3 - \frac{\mu_2}{4} \phi^4 \\ & + i \bar{q} \not{D} q - m_q \bar{q} q \\ & - g_1 S^\dagger S \phi - \frac{g_2}{2} S^\dagger S \phi^2 - h_1 \bar{q} q \phi - i h_2 \bar{q} \gamma^5 q \phi \end{aligned}$$

Typically one integrates out the mediator, which amounts to assuming the mediator mass is much larger than the recoil momentum of the interaction

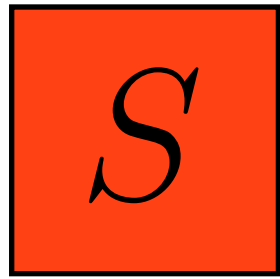
$$m_\phi^2 \gg q^2 = (p' - p)^2$$



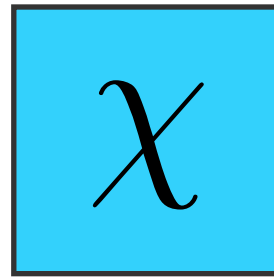
$$\begin{aligned} \mathcal{L}_{S\phi q} = & \partial_\mu S^\dagger \partial^\mu S - m_S^2 S^\dagger S - \frac{\lambda_S}{2} (S^\dagger S)^2 \\ & + \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - \frac{1}{2} m_\phi^2 \phi^2 - \frac{m_\phi \mu_1}{3} \phi^3 - \frac{\mu_2}{4} \phi^4 \\ & + i \bar{q} \not{D} q - m_q \bar{q} q \\ & - g_1 S^\dagger S \phi - \frac{g_2}{2} S^\dagger S \phi^2 - h_1 \bar{q} q \phi - i h_2 \bar{q} \gamma^5 q \phi \end{aligned}$$

$$\mathcal{L}_{eff} \supset \frac{h_1 g_1}{m_\phi^2} S^\dagger S \bar{q} q$$

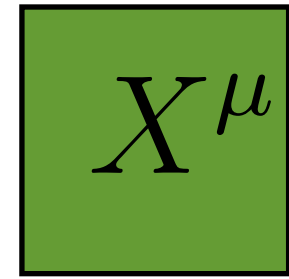
Dark Matter



spin-0

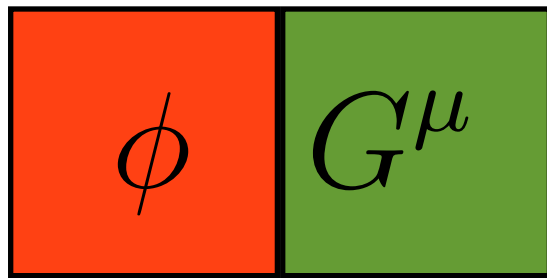


spin-1/2

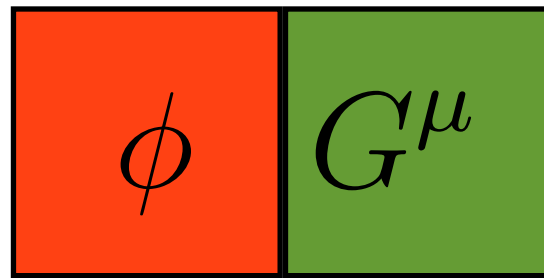


spin-1

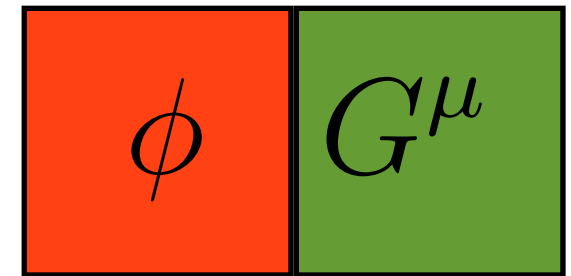
Uncharged mediators



spin-0 spin-1

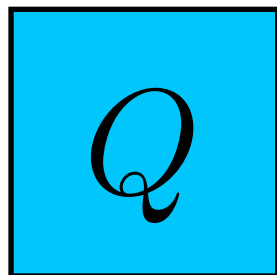


spin-0 spin-1

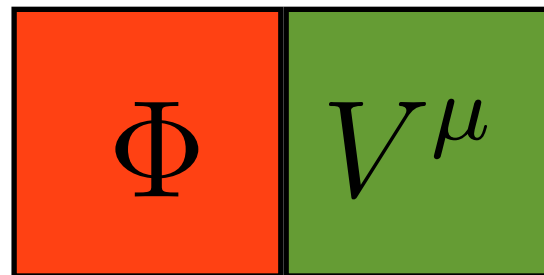


spin-0 spin-1

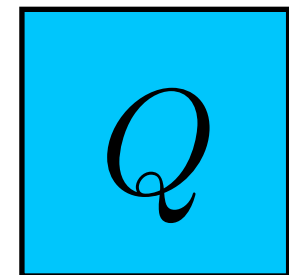
Charged mediators



spin-1/2



spin-0 spin-1



spin-1/2

- Two additional non-relativistic operators must be included in the vector dark matter case

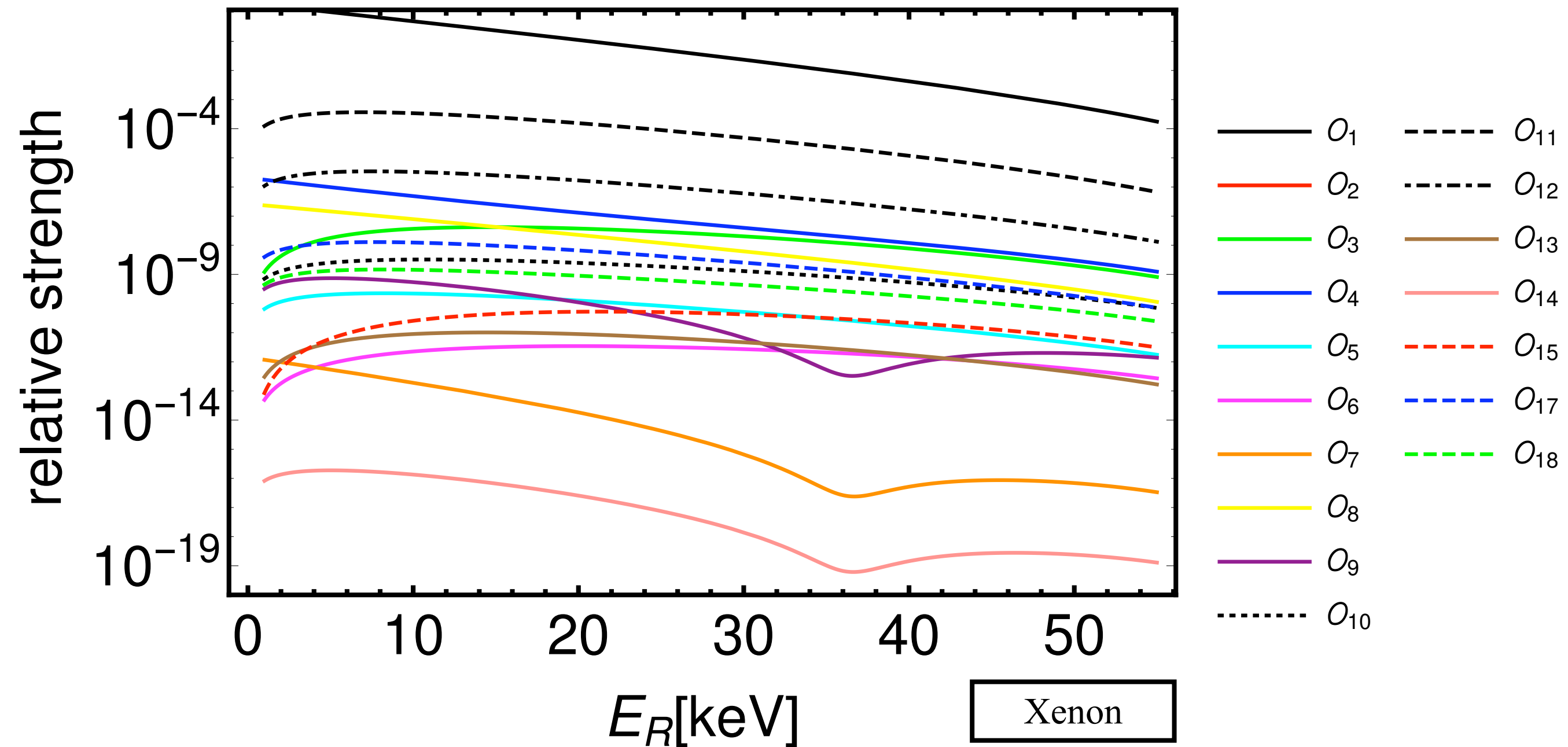
$$\begin{aligned}\mathcal{O}_{17} &\equiv \frac{i\vec{q}}{m_N} \cdot \mathcal{S} \cdot \vec{v}_\perp \\ \mathcal{O}_{18} &\equiv \frac{i\vec{q}}{m_N} \cdot \mathcal{S} \cdot \vec{S}_N\end{aligned}\qquad S_{ij} = \frac{1}{2} \left(\epsilon_i^\dagger \epsilon_j + \epsilon_j^\dagger \epsilon_i \right)$$

J. Fan, M. Reece, and L-T. Wang, JCAP 1011 (2010) 042, arXiv:1008.1591

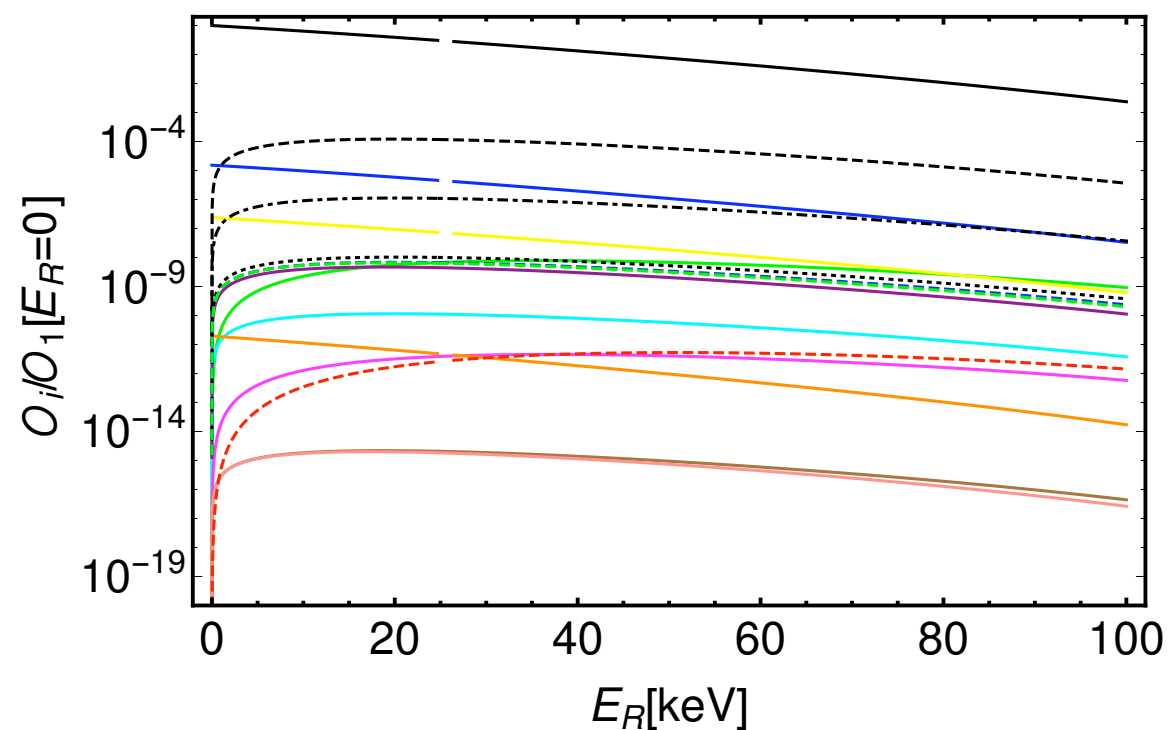
J. Hisano, K. Ishiwata, N. Nagata, M. Yamanaka, Prog.Theor.Phys. 126 (2011), arXiv:1012.5455

JBD, L.M. Krauss, J.L. Newstead, and S. Sabharwal, PRD accepted, arXiv:1505.03117

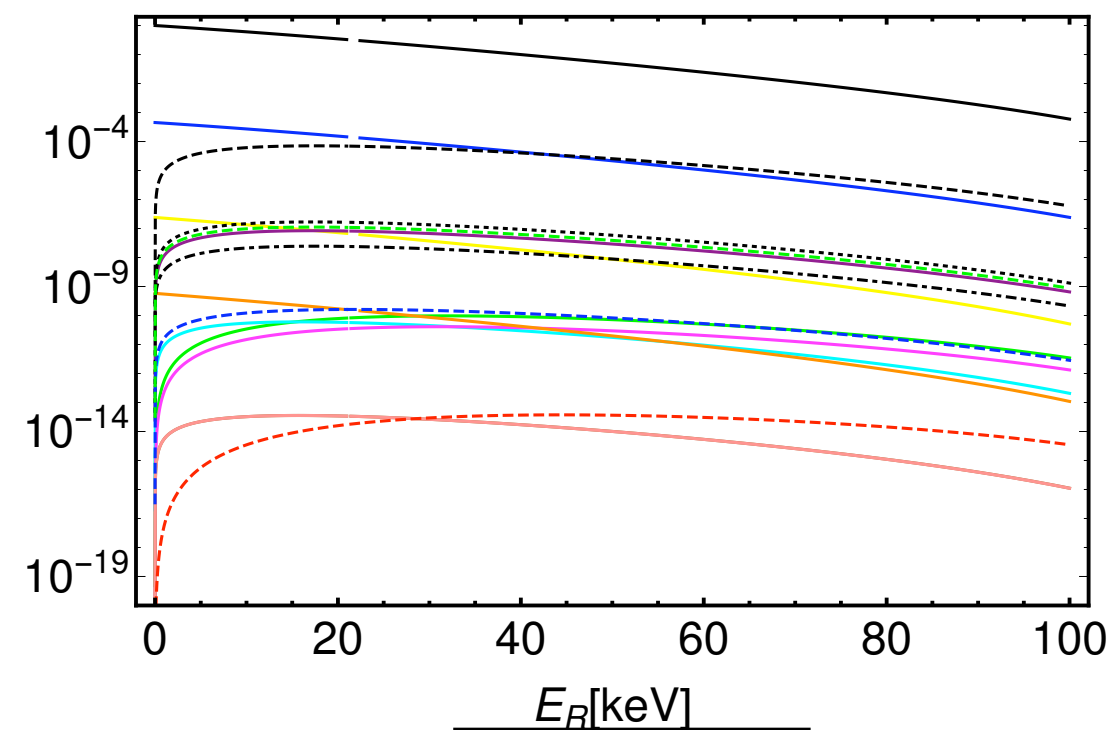
- Some EFT \mathcal{O}_i terms do not appear at leading order
- As expected/known degeneracies arise and non-standard interactions are found to dominate for certain interaction types



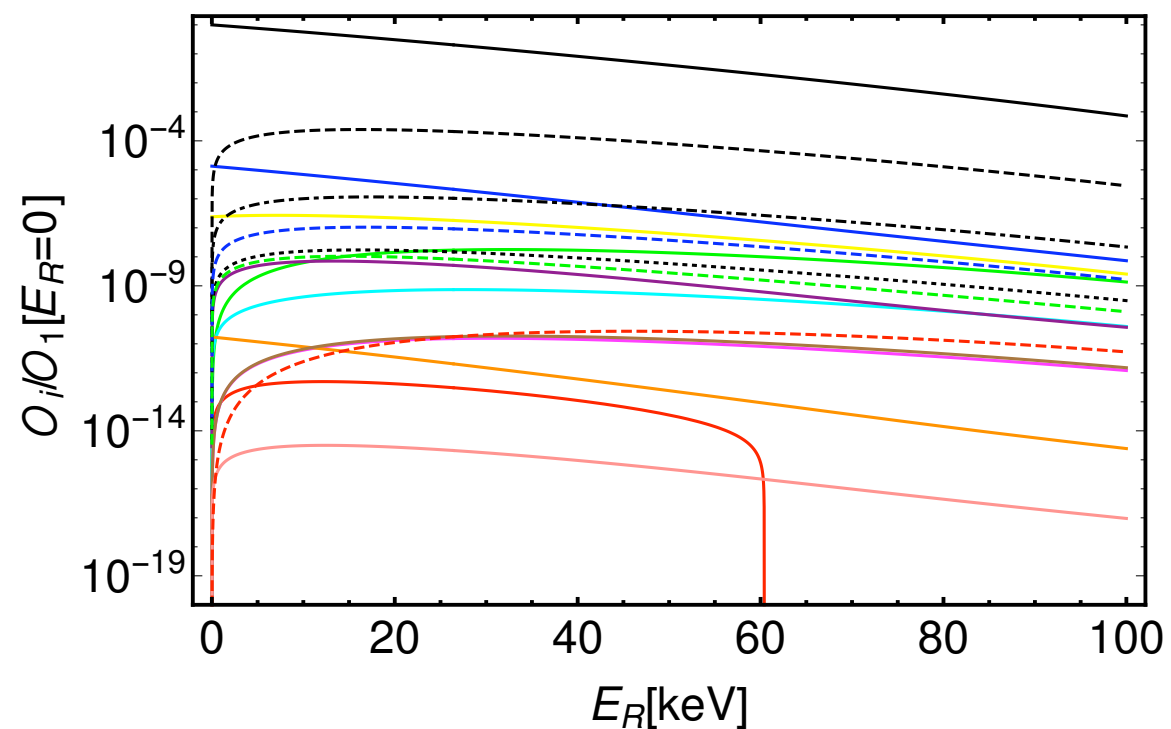
Relative strength of operators, in order to compare which operators dominate when more than one are present



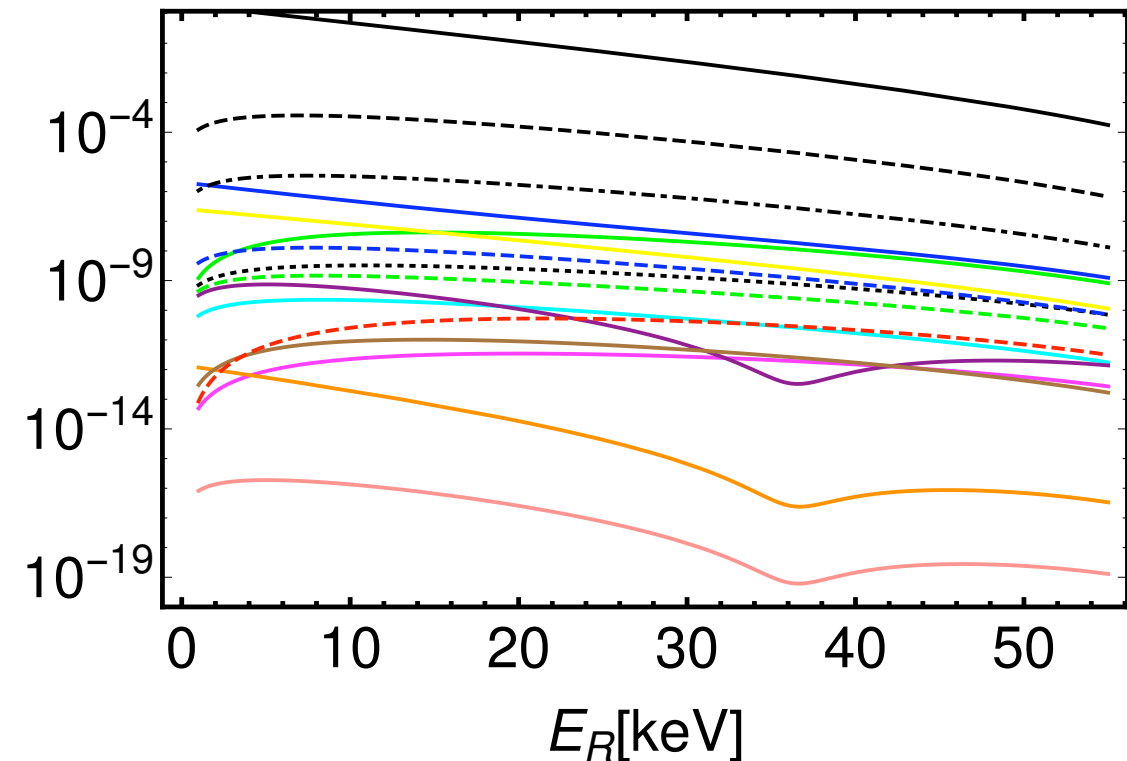
Silicon



Fluorine

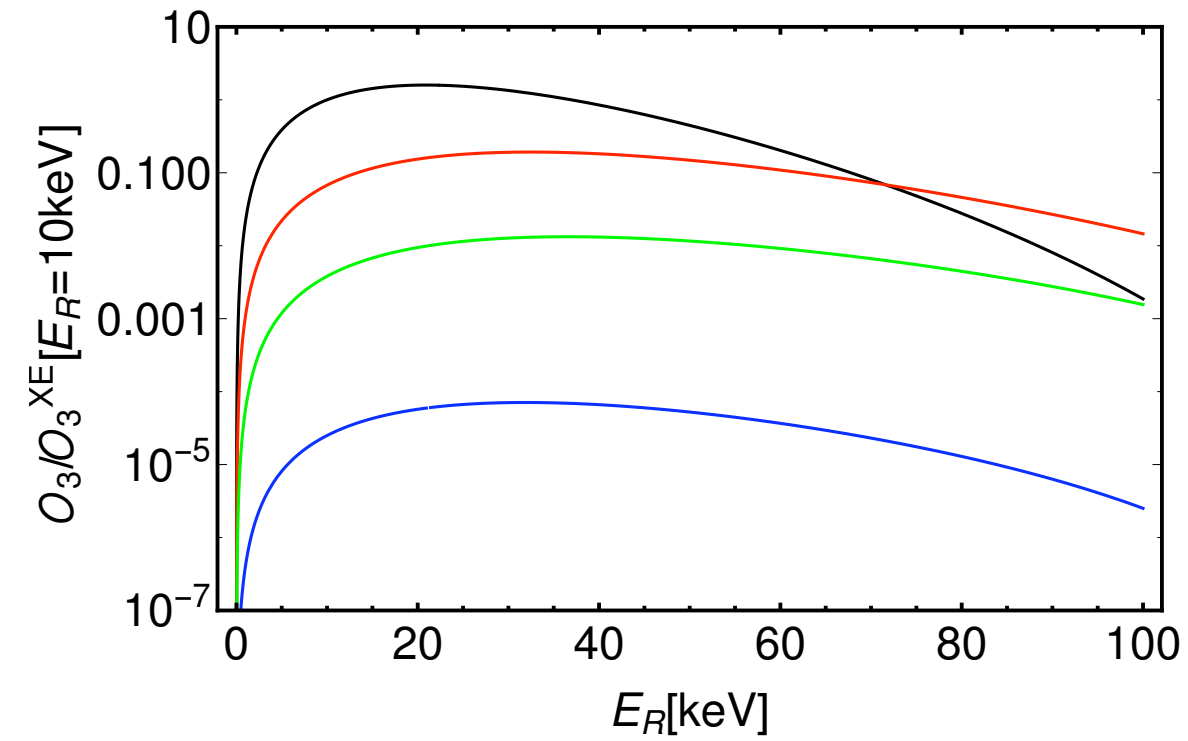


Germanium



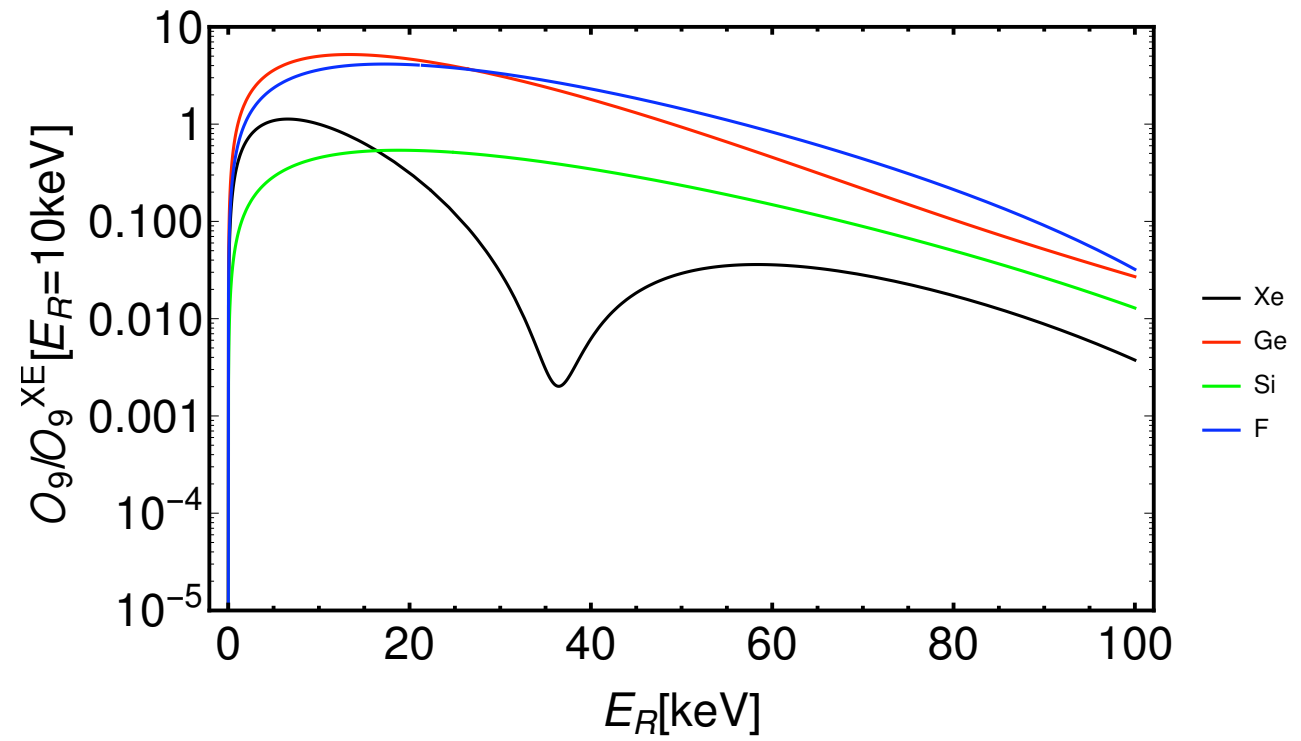
Xenon

Relative strength of operators, in order to compare which operators dominate when more than one are present



\mathcal{O}_3

$$i\vec{S}_N \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}^\perp \right)$$



\mathcal{O}_9

$$i\vec{S}_\chi \cdot \left(\vec{S}_N \times \frac{\vec{q}}{m_N} \right)$$

Response of a given operator shown for various target elements

- Aside from scalar WIMPs each particular spin produces some non-relativistic operators that are unique to that spin
- Two non-relativistic operators, O_1 and O_{10} , are ubiquitous, arising for all WIMP spins 0, 1/2, and 1

$$1_\chi 1_N \quad i \frac{\vec{q}}{m_N} \cdot \vec{S}_N$$

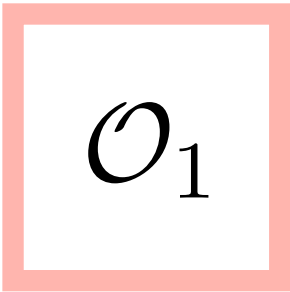
- In five scenarios for spin 0, 1/2, or 1 dark matter, relativistic operators generate unique non-relativistic operators at leading order.
- The operators can produce radically different energy dependence for scattering off different nuclear targets. Thus, a complementary use of different target materials will be helpful in order to reliably distinguish between different particle physics model possibilities for WIMP dark matter.

Spin-0 WIMP		\mathcal{O}_1	\mathcal{O}_2	\mathcal{O}_3	\mathcal{O}_4	$q^2 \mathcal{O}_4$	\mathcal{O}_5	\mathcal{O}_6	\mathcal{O}_7	\mathcal{O}_8	\mathcal{O}_9	\mathcal{O}_{10}	\mathcal{O}_{11}	\mathcal{O}_{12}	\mathcal{O}_{13}	\mathcal{O}_{14}	\mathcal{O}_{15}	\mathcal{O}_{17}	\mathcal{O}_{18}
	(h_1, g_1)	✓																	
	(h_2, g_1)											✓							
	(h_4, g_4)											✓							
	(y_1)	✓										✓							
	(y_2)	✓										✓							
	(y_1, y_2)											✓							



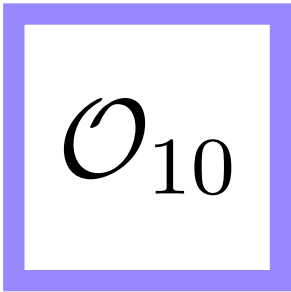
spin-0

WIMP spin	Mediator spin	\mathcal{L} terms	leading NR operator	Eqv. M_m
0	0	h_1, g_1	\mathcal{O}_1	13 TeV
0	0	h_2, g_1	\mathcal{O}_{10}	14 GeV
0	1	h_4, g_4	\mathcal{O}_{10}	8 GeV
0	$\frac{1}{2}^*$	y_1	\mathcal{O}_1	3.2 PeV
0	$\frac{1}{2}^*$	y_2	\mathcal{O}_1	3.2 PeV
0	$\frac{1}{2}^*$	y_1, y_2	\mathcal{O}_{10}	41 GeV



$$1_\chi 1_N$$

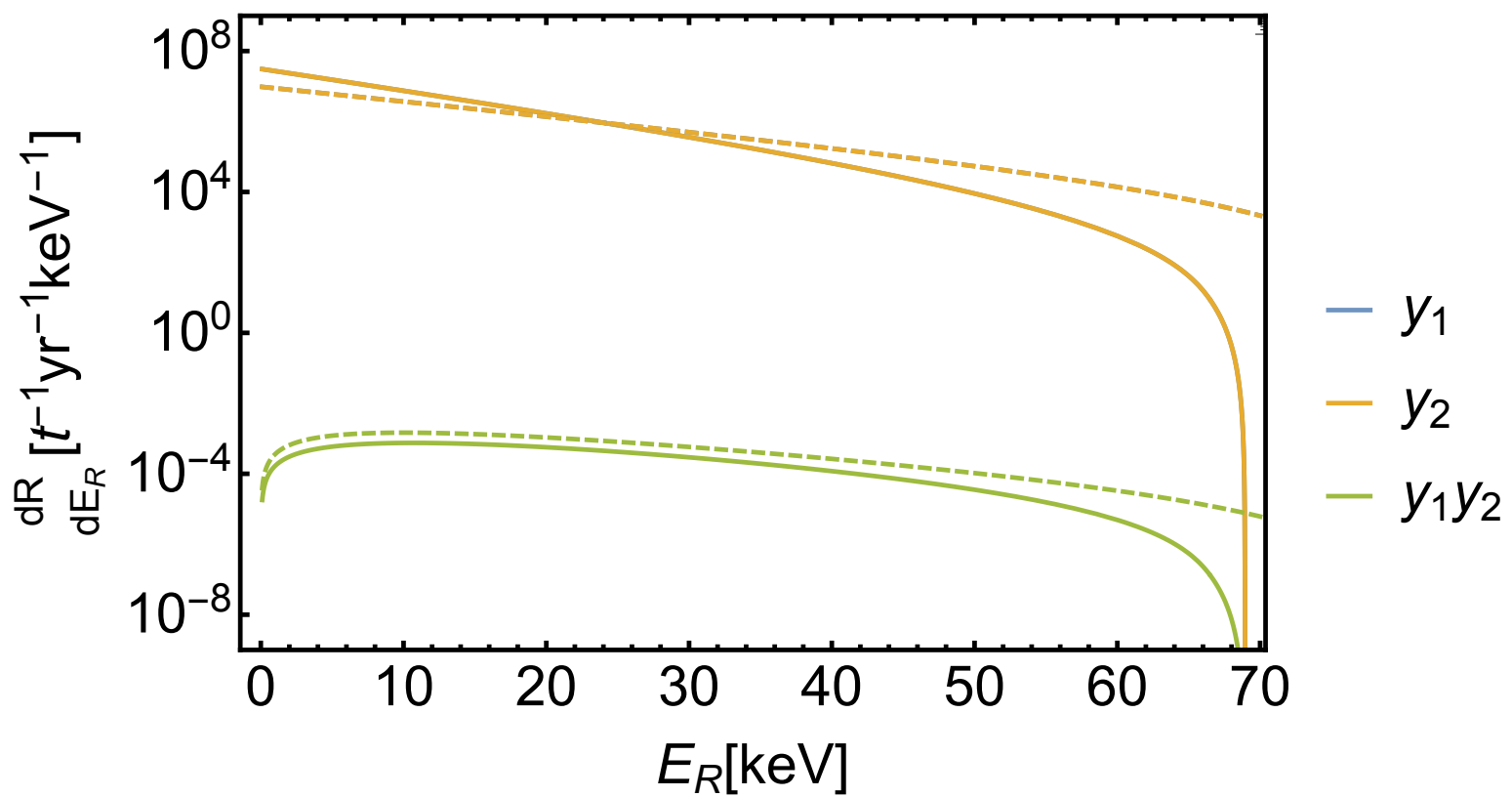
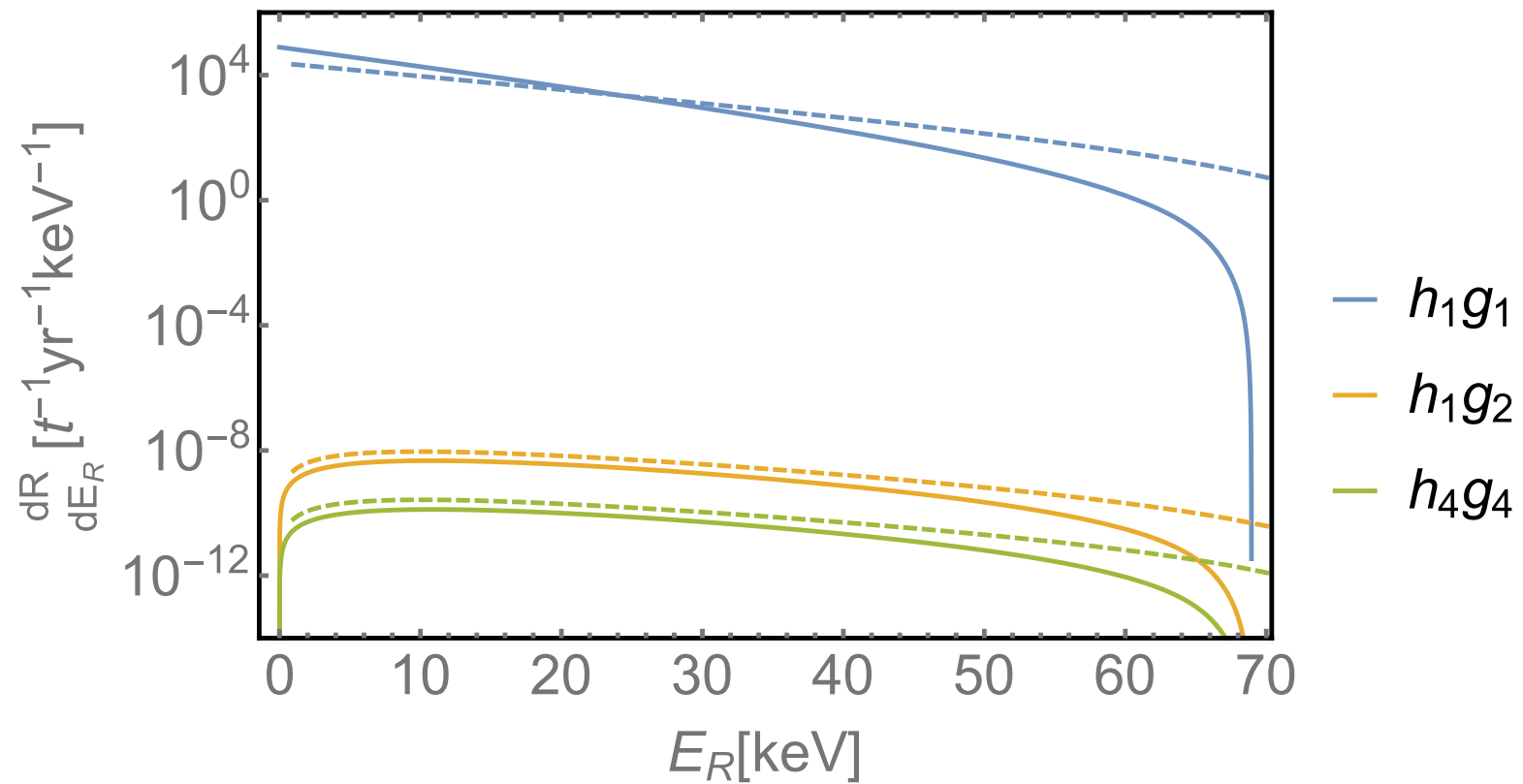
$$(S^\dagger S)(\bar q q)$$



$$i \frac{\vec q}{m_N} \cdot \vec S_N$$

$$(S^\dagger S)(\bar q \gamma^5 q)$$

$$i(S^\dagger \partial_\mu S - \partial_\mu S^\dagger S)(\bar q \gamma^\mu \gamma^5 q)$$



50 GeV spin-0 WIMP off of ⁷³Ge (dashed) and ¹³¹Xe (solid) with 1 TeV mediator

χ **spin-1/2****Scalar Mediator**

$$\begin{aligned}
\bar{\chi}\chi\bar{q}q &\longrightarrow \left(\frac{h_1^N\lambda_1}{m_\phi^2}\right)\mathcal{O}_1 \\
\bar{\chi}\chi\bar{q}\gamma^5q &\longrightarrow \left(\frac{h_2^N\lambda_1}{m_\phi^2}\right)\mathcal{O}_{10} \\
\bar{\chi}\gamma^5\chi\bar{q}q &\longrightarrow \left(-\frac{h_1^N\lambda_2m_N}{m_\phi^2m_\chi}\right)\mathcal{O}_{11} \\
\bar{\chi}\gamma^5\chi\bar{q}\gamma^5q &\longrightarrow \left(\frac{h_2^N\lambda_2m_N}{m_\phi^2m_\chi}\right)\mathcal{O}_6
\end{aligned}$$

Vector Mediator

$$\begin{aligned}
\bar{\chi}\gamma^\mu\chi\bar{q}\gamma_\mu q &\longrightarrow \left(-\frac{h_3^N\lambda_3}{m_G^2}\right)\mathcal{O}_1 \\
\bar{\chi}\gamma^\mu\chi\bar{q}\gamma_\mu\gamma^5q &\longrightarrow \left(-\frac{2h_4^N\lambda_3}{m_G^2}\right)\left(-\mathcal{O}_7 + \frac{m_N}{m_\chi}\mathcal{O}_9\right) \\
\bar{\chi}\gamma^\mu\gamma^5\chi\bar{q}\gamma_\mu q &\longrightarrow \left(-\frac{2h_3^N\lambda_4}{m_G^2}\right)(\mathcal{O}_8 + \mathcal{O}_9) \\
\bar{\chi}\gamma^\mu\gamma^5\chi\bar{q}\gamma_\mu\gamma^5q &\longrightarrow \left(\frac{4h_4^N\lambda_4}{m_G^2}\right)\mathcal{O}_4
\end{aligned}$$

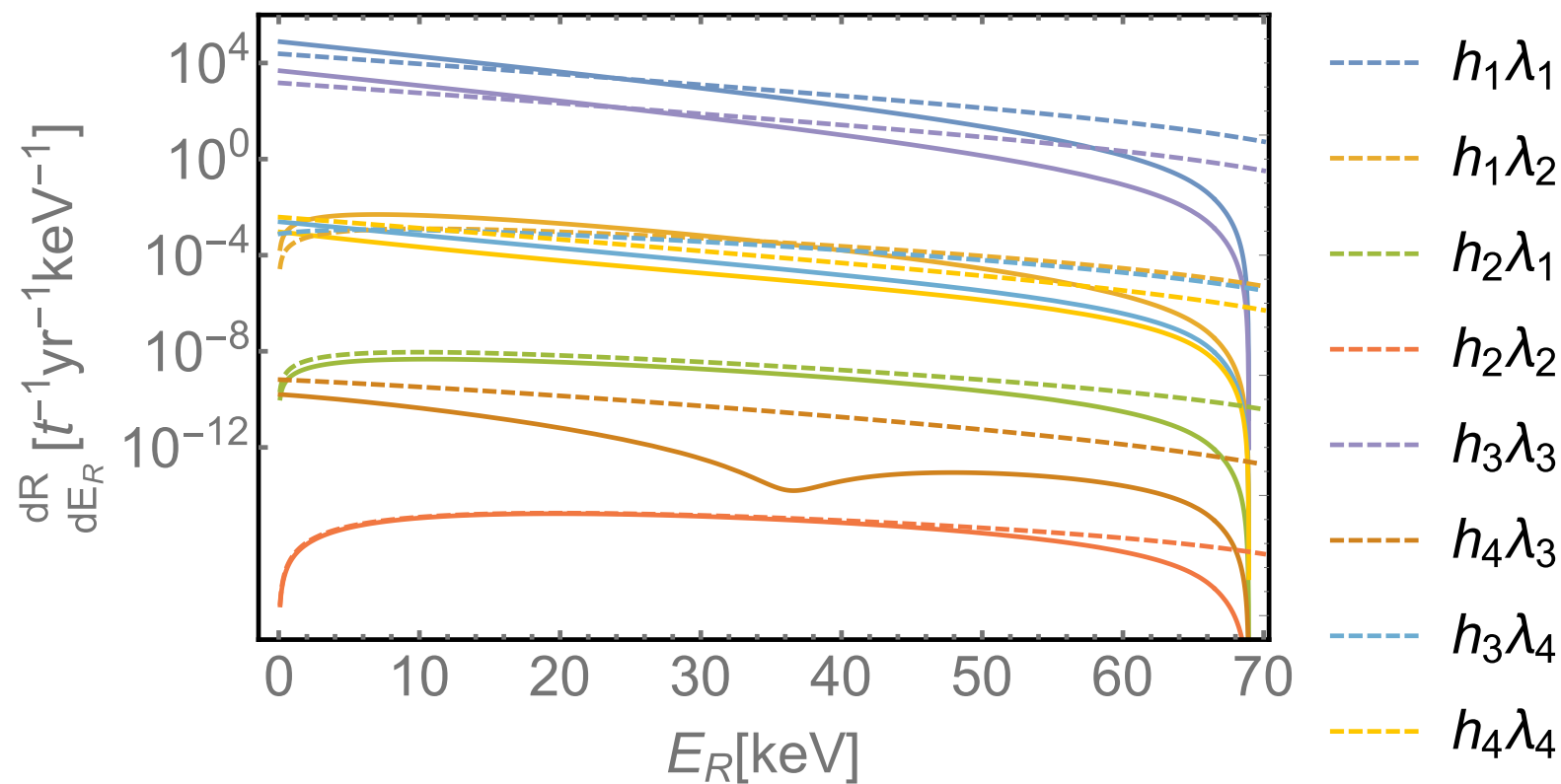
Charged Scalar Mediator

$$\begin{aligned}
\bar{\chi}\chi\bar{q}q &\longrightarrow \frac{l_2^\dagger l_2 - l_1^\dagger l_1}{4m_\Phi^2} f_{Tq}^N \mathcal{O}_1 \\
\bar{\chi}\chi\bar{q}\gamma^5q &\longrightarrow i \frac{l_1^\dagger l_2 - l_2^\dagger l_1}{4m_\Phi^2} \Delta\tilde{q}^N \mathcal{O}_{10} \\
\bar{\chi}\gamma^5\chi\bar{q}q &\longrightarrow i \frac{l_2^\dagger l_1 - l_1^\dagger l_2}{4m_\Phi^2} \frac{m_N}{m_\chi} f_{Tq}^N \mathcal{O}_{11} \\
\bar{\chi}\gamma^5\chi\bar{q}\gamma^5q &\longrightarrow \frac{l_1^\dagger l_1 - l_2^\dagger l_2}{4m_\Phi^2} \frac{m_N}{m_\chi} \Delta\tilde{q}^N \mathcal{O}_6 \\
\bar{\chi}\gamma^\mu\chi\bar{q}\gamma_\mu q &\longrightarrow -\frac{l_1^\dagger l_1 + l_2^\dagger l_2}{4m_\Phi^2} \mathcal{N}_q^N \mathcal{O}_1 \\
\bar{\chi}\gamma^\mu\gamma^5\chi\bar{q}\gamma_\mu q &\longrightarrow \frac{l_1^\dagger l_2 + l_2^\dagger l_1}{2m_\Phi^2} \mathcal{N}_q^N (\mathcal{O}_8 + \mathcal{O}_9) \\
\bar{\chi}\gamma^\mu\chi\bar{q}\gamma_\mu\gamma^5q &\longrightarrow \frac{l_1^\dagger l_2 + l_2^\dagger l_1}{2m_\Phi^2} \Delta_q^N (\mathcal{O}_7 - \frac{m_N}{m_\chi}\mathcal{O}_9) \\
\bar{\chi}\gamma^\mu\gamma^5\chi\bar{q}\gamma_\mu\gamma^5q &\longrightarrow -\frac{l_1^\dagger l_1 + l_2^\dagger l_2}{m_\Phi^2} \Delta_q^N \mathcal{O}_4 \\
\bar{\chi}\sigma^{\mu\nu}\chi\bar{q}\sigma_{\mu\nu}q &\longrightarrow \frac{l_2^\dagger l_2 - l_1^\dagger l_1}{m_\Phi^2} \delta_q^N \mathcal{O}_4 \\
\epsilon_{\mu\nu\alpha\beta}\bar{\chi}\sigma^{\mu\nu}\chi\bar{q}\sigma^{\alpha\beta}q &\longrightarrow \frac{l_2^\dagger l_1 - l_1^\dagger l_2}{m_\Phi^2} \delta_q^N (i\mathcal{O}_{10} - i\frac{m_N}{m_\chi}\mathcal{O}_{11} + 4\mathcal{O}_{12})
\end{aligned}$$

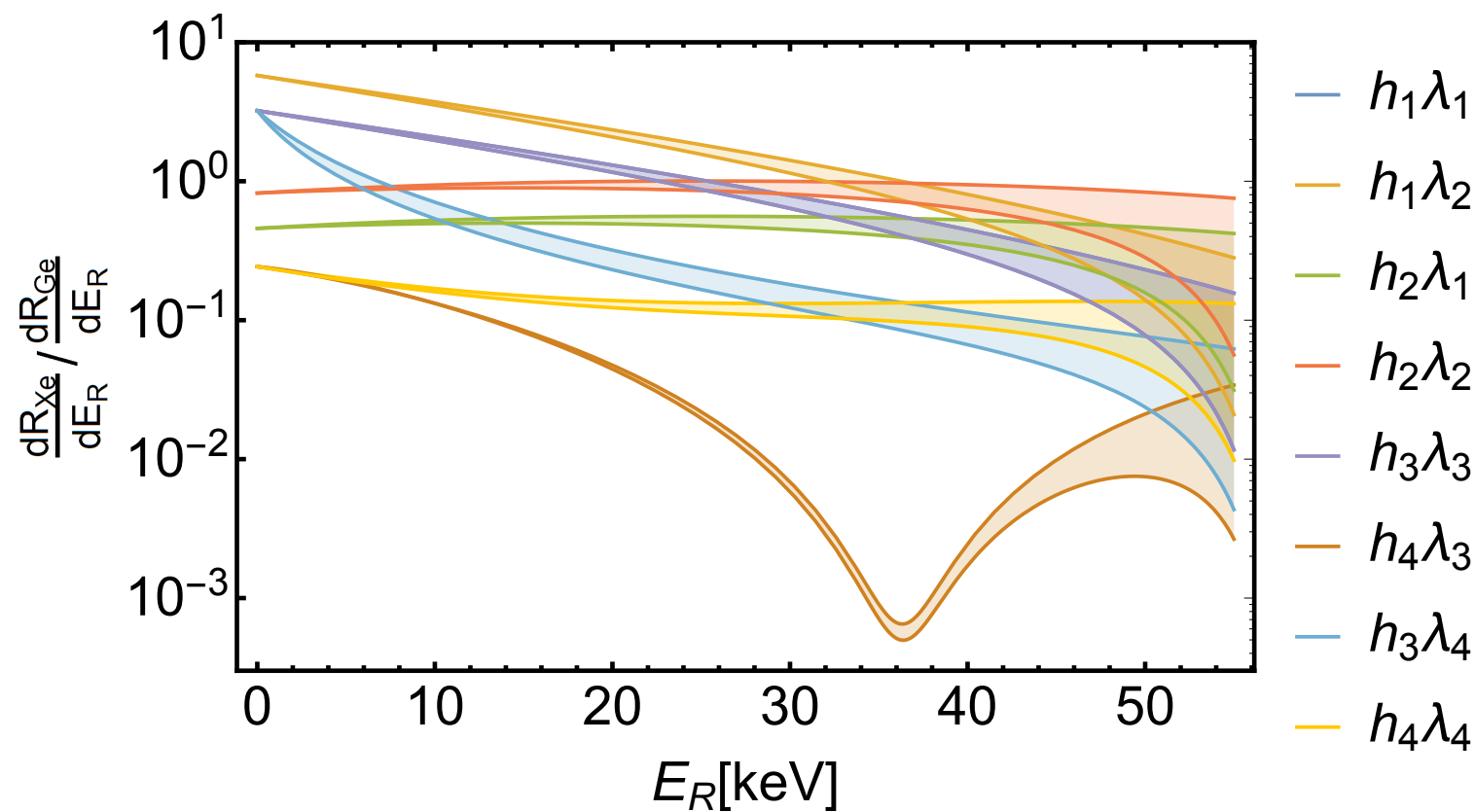
Charged Vector Mediator

$$\begin{aligned}
\bar{\chi}\chi\bar{q}q &\longrightarrow \frac{d_2^\dagger d_2 - d_1^\dagger d_1}{4m_V^2} f_{Tq}^N \mathcal{O}_1 \\
\bar{\chi}\chi\bar{q}\gamma^5q &\longrightarrow i \frac{d_2^\dagger d_1 - d_1^\dagger d_2}{4m_V^2} \Delta\tilde{q}^N \mathcal{O}_{10} \\
\bar{\chi}\gamma^5\chi\bar{q}q &\longrightarrow i \frac{d_2^\dagger d_1 - d_1^\dagger d_2}{4m_V^2} \frac{m_N}{m_\chi} f_{Tq}^N \mathcal{O}_{11} \\
\bar{\chi}\gamma^5\chi\bar{q}\gamma^5q &\longrightarrow \frac{d_2^\dagger d_2 - d_1^\dagger d_1}{4m_V^2} \frac{m_N}{m_\chi} \Delta\tilde{q}^N \mathcal{O}_6 \\
\bar{\chi}\gamma^\mu\chi\bar{q}\gamma_\mu q &\longrightarrow \frac{d_2^\dagger d_2 + d_1^\dagger d_1}{8m_V^2} \mathcal{N}_q^N \mathcal{O}_1 \\
\bar{\chi}\gamma^\mu\gamma^5\chi\bar{q}\gamma_\mu q &\longrightarrow -\frac{d_2^\dagger d_1 + d_1^\dagger d_2}{4m_V^2} \mathcal{N}_q^N (\mathcal{O}_8 + \mathcal{O}_9) \\
\bar{\chi}\gamma^\mu\chi\bar{q}\gamma_\mu\gamma^5q &\longrightarrow \frac{d_2^\dagger d_1 + d_1^\dagger d_2}{4m_V^2} \Delta_q^N (\mathcal{O}_7 - \frac{m_N}{m_\chi}\mathcal{O}_9) \\
\bar{\chi}\gamma^\mu\gamma^5\chi\bar{q}\gamma_\mu\gamma^5q &\longrightarrow -\frac{d_2^\dagger d_2 + d_1^\dagger d_1}{2m_V^2} \Delta_q^N \mathcal{O}_4
\end{aligned}$$

50 GeV spin-1/2 WIMP off of ^{73}Ge (dashed) and ^{131}Xe (solid) for a 1TeV mediator

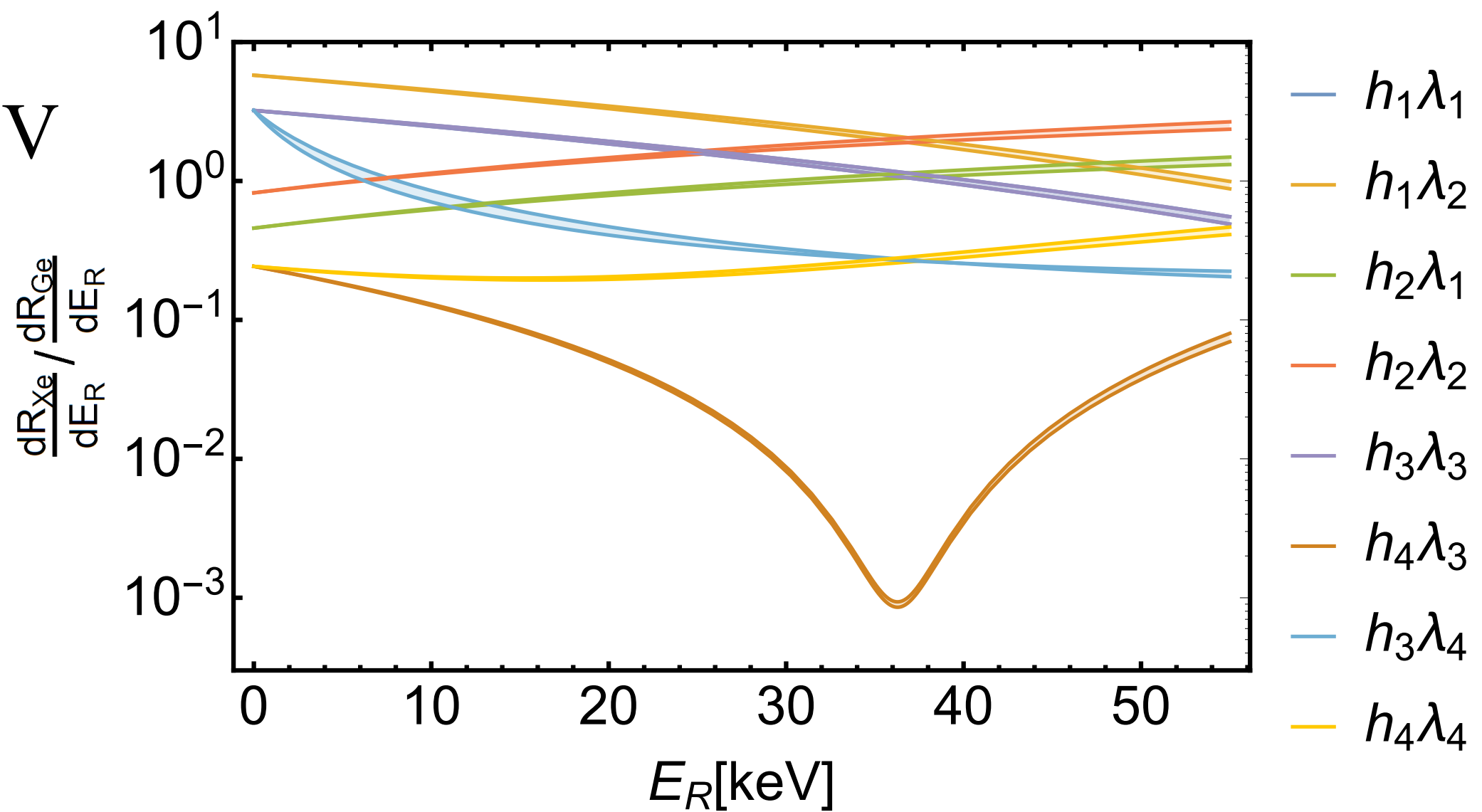


50GeV



Ratio of rates for 50GeV spin-1/2 WIMP off Xe and Ge including astrophysical uncertainties

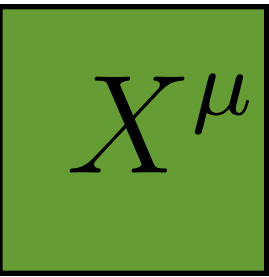
500GeV



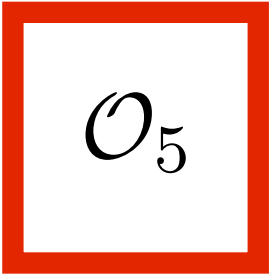
Ratio of rates for 500GeV spin-1/2 WIMP off Xe and Ge including astrophysical uncertainties

		\mathcal{O}_1	\mathcal{O}_2	\mathcal{O}_3	\mathcal{O}_4	$q^2\mathcal{O}_4$	\mathcal{O}_5	\mathcal{O}_6	\mathcal{O}_7	\mathcal{O}_8	\mathcal{O}_9	\mathcal{O}_{10}	\mathcal{O}_{11}	\mathcal{O}_{12}	\mathcal{O}_{13}	\mathcal{O}_{14}	\mathcal{O}_{15}	\mathcal{O}_{17}	\mathcal{O}_{18}
Spin-1 WIMP	(h_1, b_1)	✓																	
	(h_2, b_1)											✓							
	(h_4, b_5)											✓							
	(h_3, b_6)					✓	✓	✓										✓*	
	(h_4, b_6)										✓								✓*
	(h_3, b_7)									✓*	✓*		✓						
	(h_4, b_7)				✓*	✓		✓								✓			
	(y_3)	✓			✓							✓	✓	✓					✓
	(y_4)	✓			✓							✓	✓	✓					✓
	(y_3, y_4)											✓	✓	✓					✓

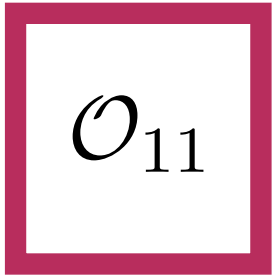
WIMP spin	Mediator spin	\mathcal{L} terms	leading NR operator	Eqv. M_m
1	0	h_1, b_1	\mathcal{O}_1	13 TeV
1	0	h_2, b_1	\mathcal{O}_{10}	10 GeV
1	1	h_4, b_5	\mathcal{O}_{10}	5.1 GeV
1	1	$h_3, b_6^{\text{Re}}(b_6^{\text{Im}})$	$\mathcal{O}_5(\mathcal{O}_{17})$	5.5 GeV(23 GeV)
1	1	$h_4, b_6^{\text{Re}}(b_6^{\text{Im}})$	$\mathcal{O}_9(\mathcal{O}_{18})$	3 GeV(4.6 GeV)
1	1	$h_3, b_7^{\text{Re}}(b_7^{\text{Im}})$	$\mathcal{O}_{11}(\mathcal{O}_8)$	186 GeV(228 GeV)
1	1	$h_4, b_7^{\text{Re}}(b_7^{\text{Im}})$	$\mathcal{O}_{14}(\mathcal{O}_4)$	65 MeV (172 GeV)
1	$\frac{1}{2}^*$	y_3	\mathcal{O}_1	3.2 PeV
1	$\frac{1}{2}^*$	y_4	\mathcal{O}_1	3.2 PeV
1	$\frac{1}{2}^*$	y_3, y_4	\mathcal{O}_{11}	120 TeV



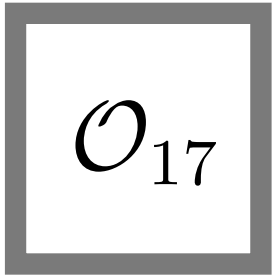
spin-1



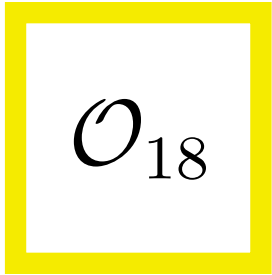
$$i\vec{S}_\chi \cdot (\frac{\vec{q}}{m_N} \times \vec{v}^\perp)$$



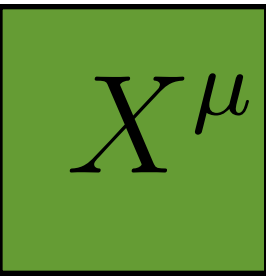
$$i\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi$$



$$i\frac{\vec{q}}{m_N} \cdot \mathcal{S} \cdot \vec{v}_\perp$$



$$i\frac{\vec{q}}{m_N} \cdot \mathcal{S} \cdot \vec{S}_N$$



spin-1

$$\partial_\nu (X^{\nu\dagger} X_\mu + X_\mu^\dagger X^\nu) (\bar{q} \gamma^\mu q)$$

$$\mathcal{O}_5$$

$$i \vec{S}_\chi \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}^\perp \right)$$

$$\epsilon_{\mu\nu\rho\sigma} \left(X^{\nu\dagger} \partial^\rho X^\sigma + X^\nu \partial^\rho X^{\sigma\dagger} \right) (\bar{q} \gamma^\mu q)$$

$$\mathcal{O}_{11}$$

$$i \frac{\vec{q}}{m_N} \cdot \vec{S}_\chi$$

$$\partial_\nu (X^{\nu\dagger} X_\mu - X_\mu^\dagger X^\nu) (\bar{q} \gamma^\mu q)$$

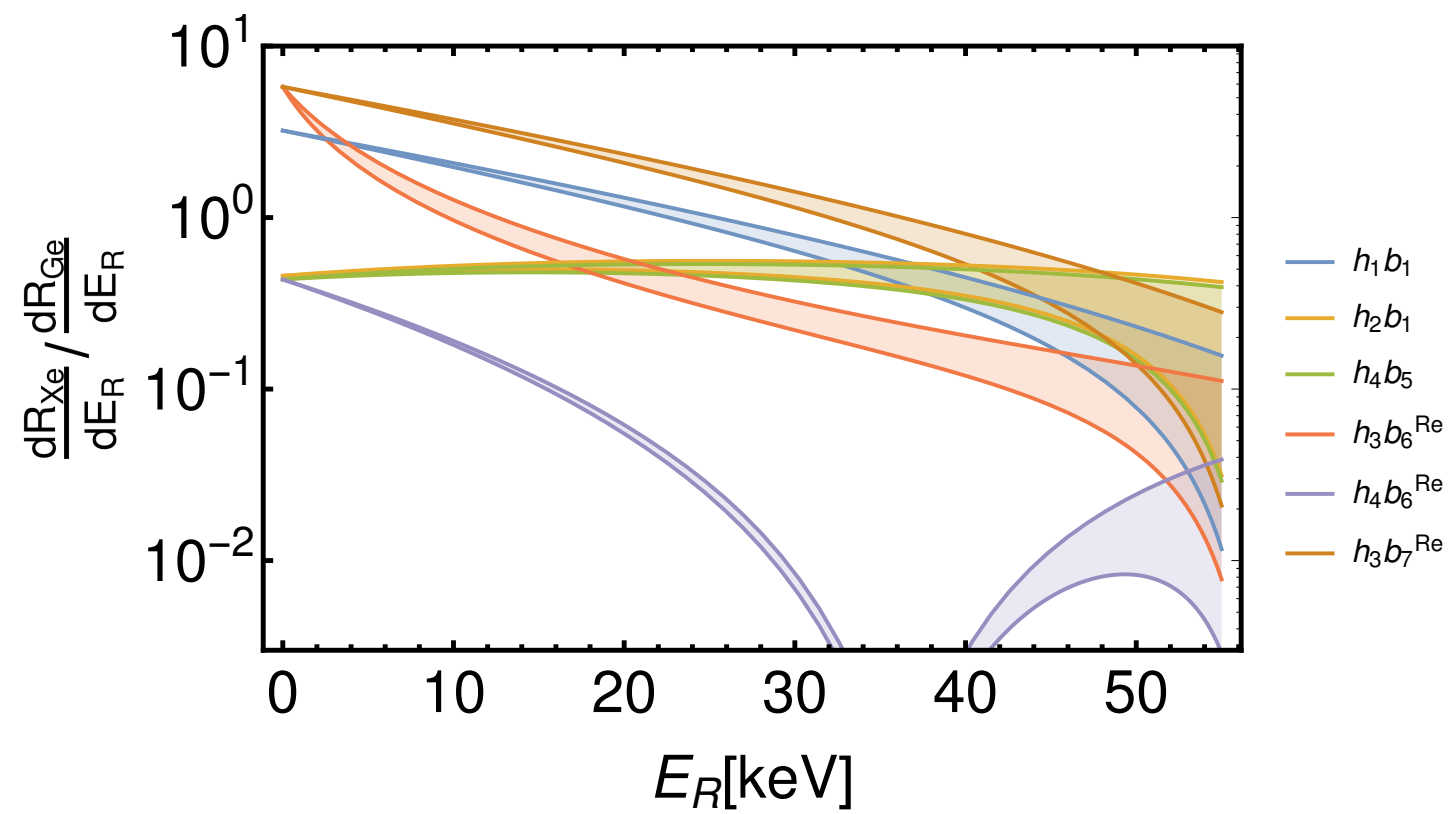
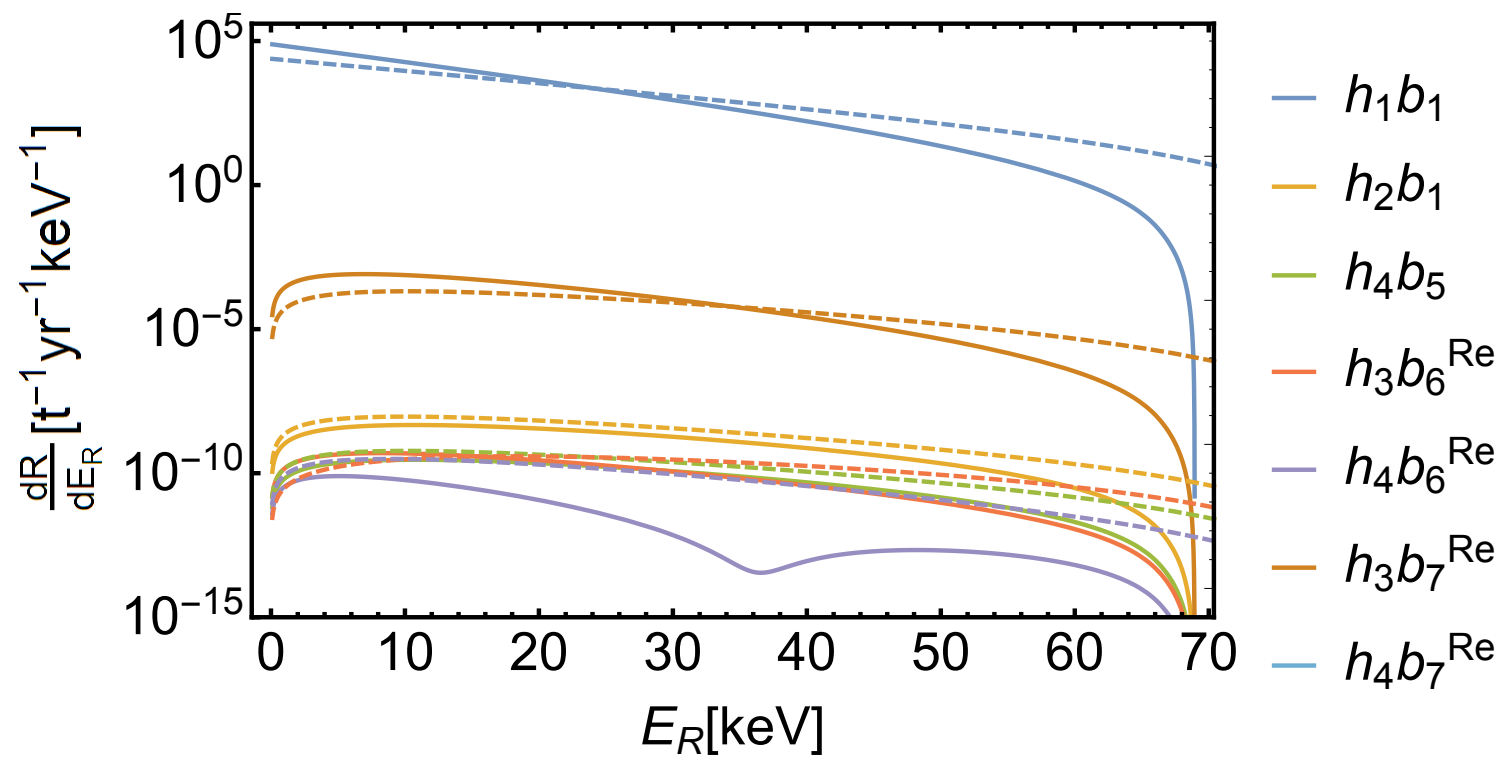
$$\mathcal{O}_{17}$$

$$i \frac{\vec{q}}{m_N} \cdot \mathcal{S} \cdot \vec{v}_\perp$$

$$\partial_\nu (X^{\nu\dagger} X_\mu - X_\mu^\dagger X^\nu) (\bar{q} \gamma^\mu \gamma^5 q)$$

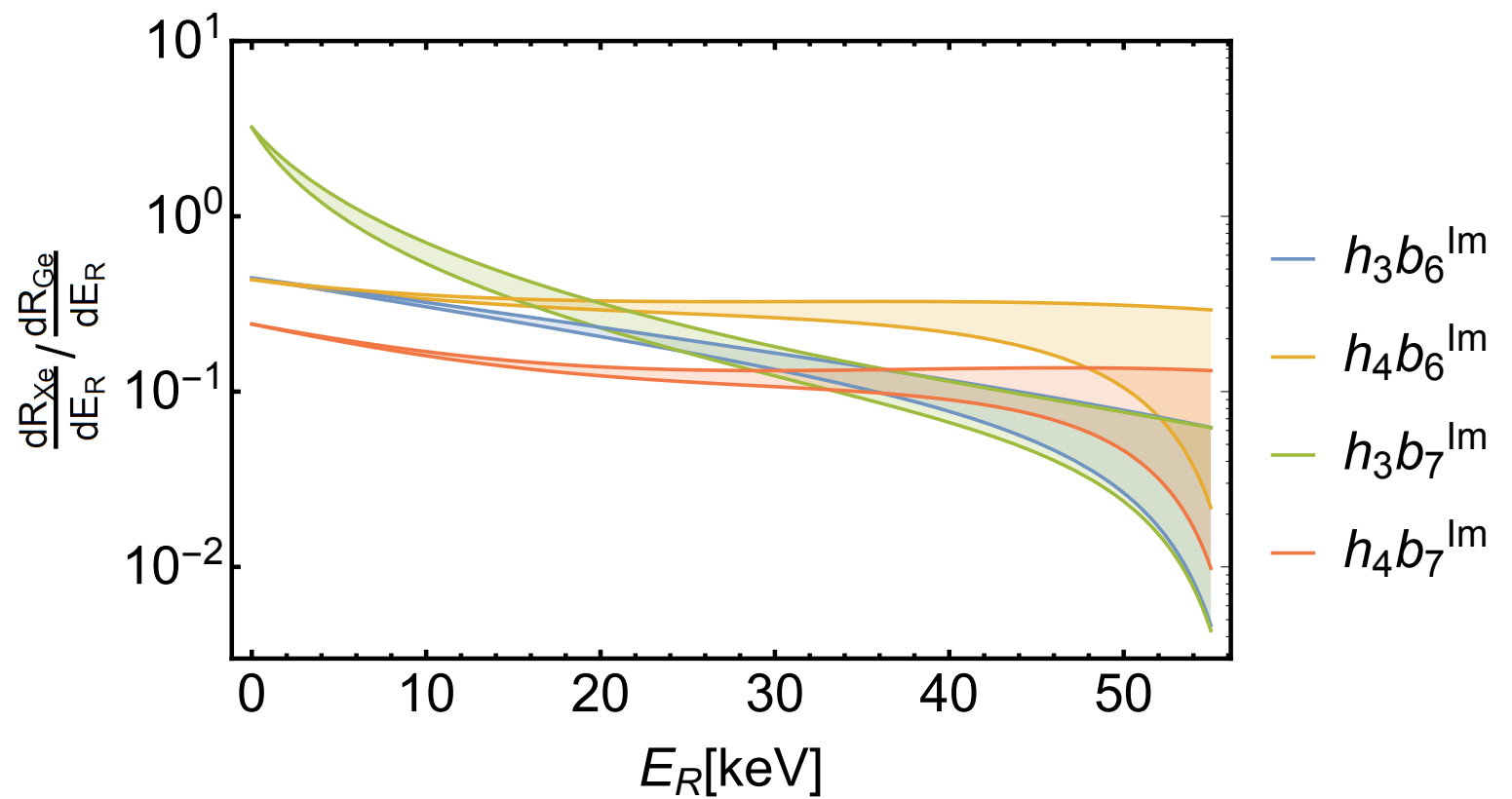
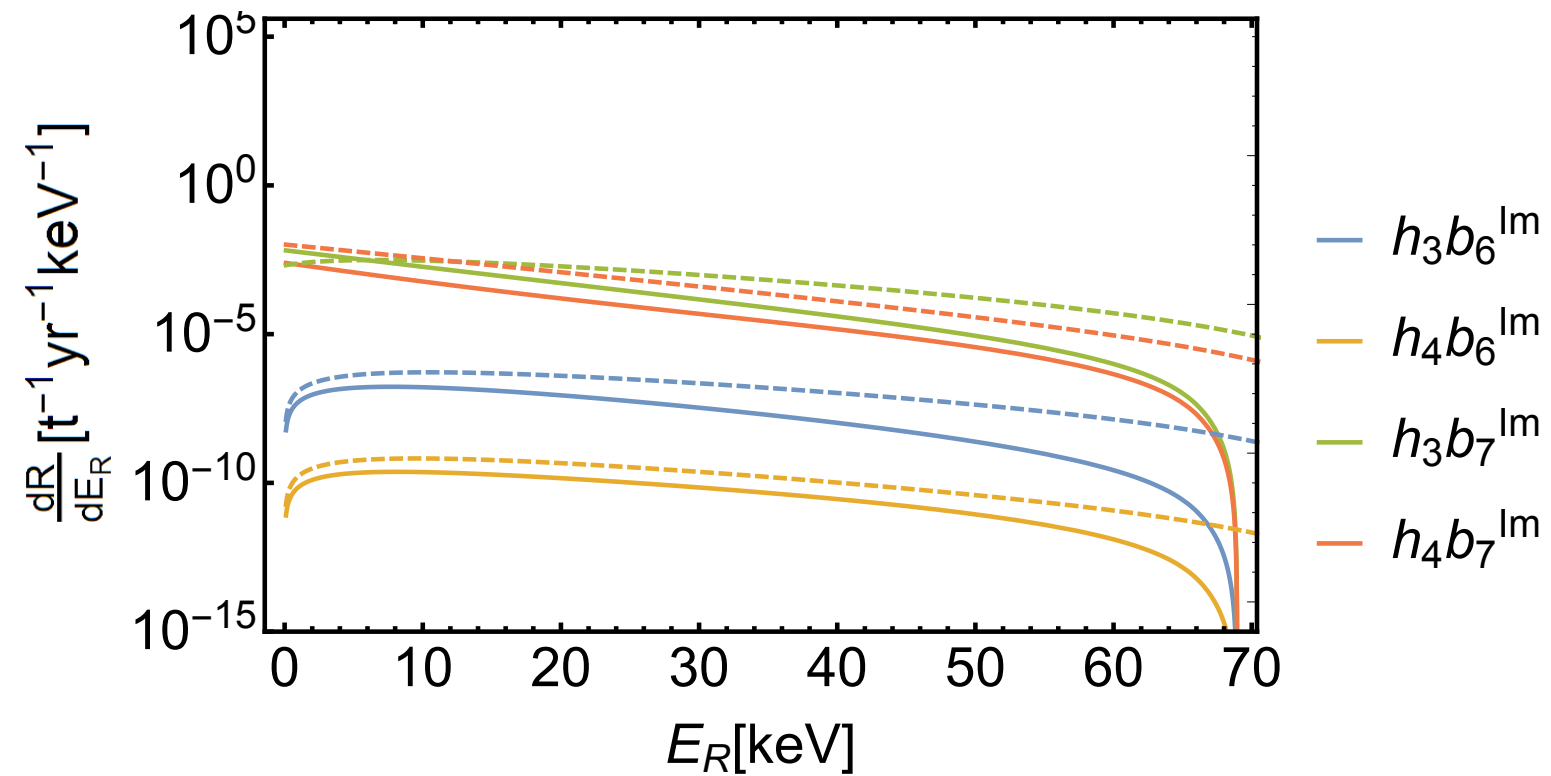
$$\mathcal{O}_{18}$$

$$i \frac{\vec{q}}{m_N} \cdot \mathcal{S} \cdot \vec{S}_N$$



50 GeV spin-1 WIMP off of ^{73}Ge (dashed) and ^{131}Xe (solid)

50 GeV spin-1 WIMP off of ^{73}Ge (dashed) and ^{131}Xe (solid)



Ratio of rates for 50GeV spin-1 WIMP off Xe and Ge including astrophysical uncertainties

Interference Effects

In the full amplitude, two types of interference effects arise

$$C_i^{\tau} C_j^{\tau'} \quad \begin{array}{l} \text{isoscalar/isovector} \\ \text{operator/operator} \end{array}$$

$$\mathcal{O}_1 / \mathcal{O}_3$$

$$\mathcal{O}_4 / \mathcal{O}_5$$

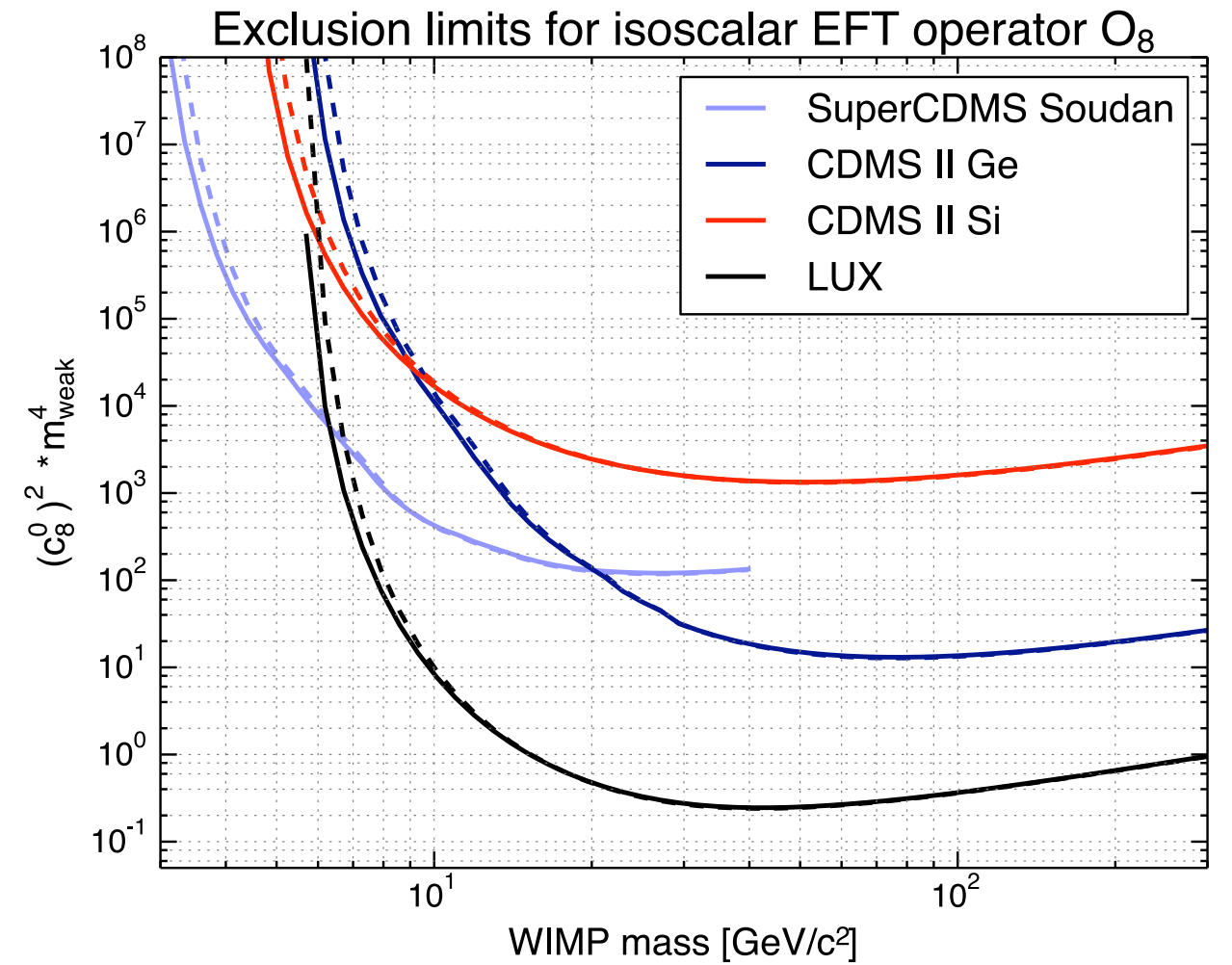
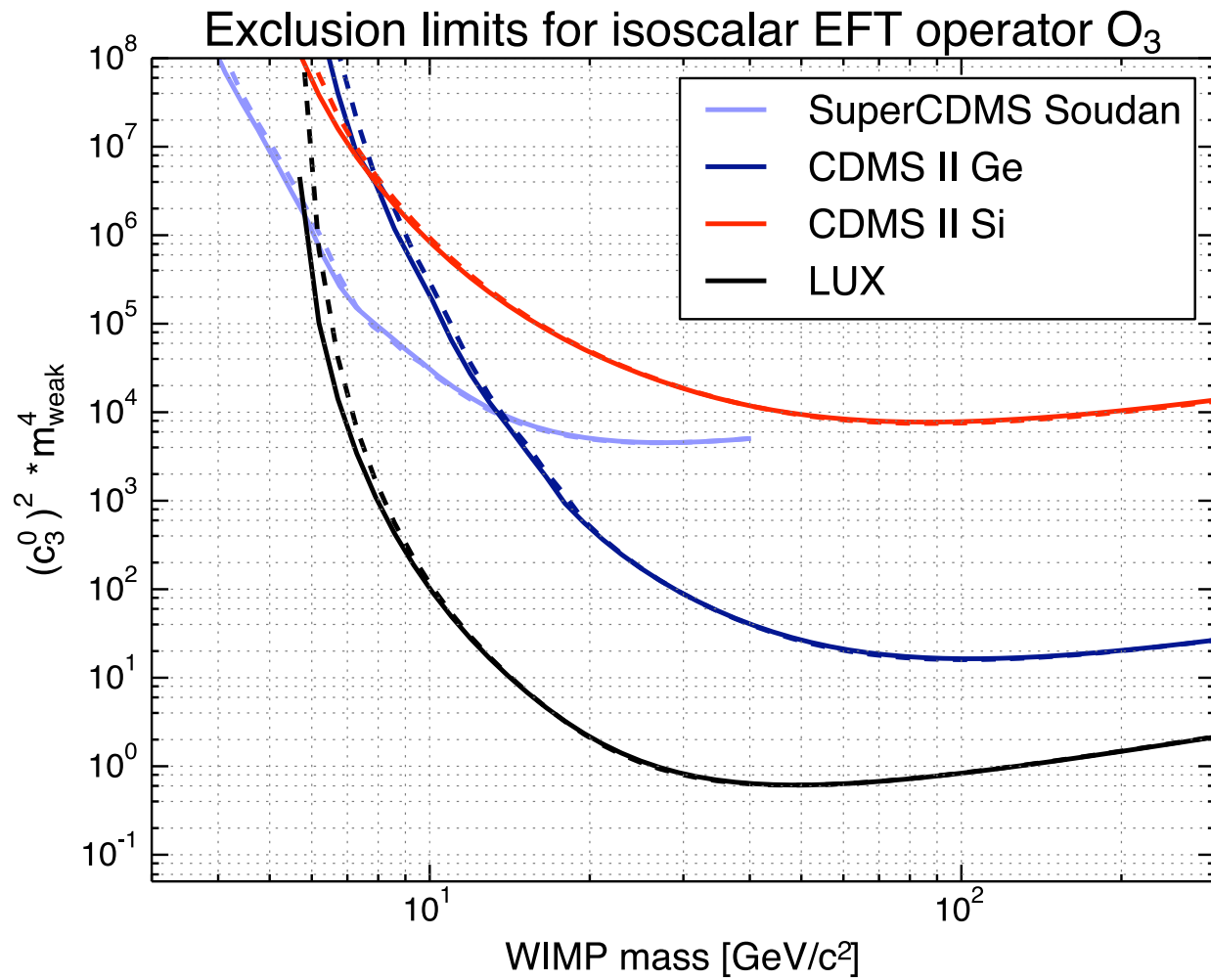
$$\mathcal{O}_4 / \mathcal{O}_6$$

$$\mathcal{O}_8 / \mathcal{O}_9$$

$$\mathcal{O}_{11} / \mathcal{O}_{12}$$

$$\mathcal{O}_{11} / \mathcal{O}_{15}$$

$$\mathcal{O}_{12} / \mathcal{O}_{15}$$

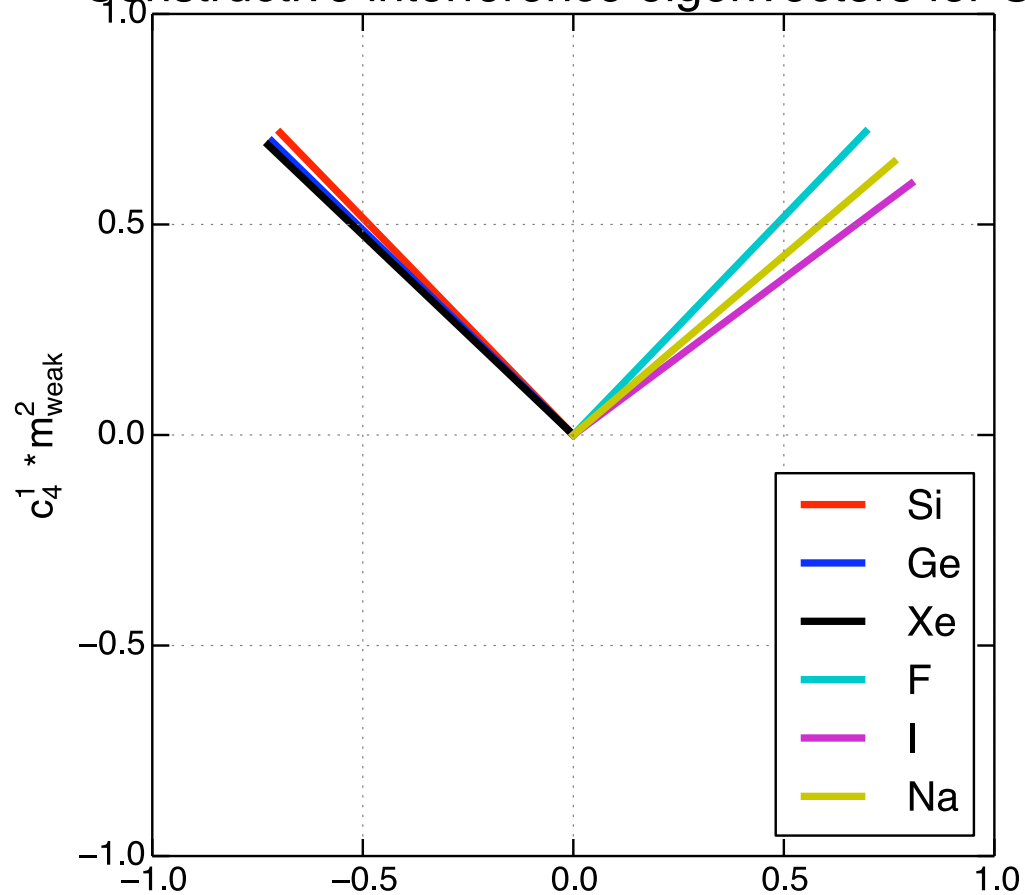


The SuperCDMS collaboration examined the sensitivity of current and upcoming experiments to non-standard operators with an eye on interference effects.

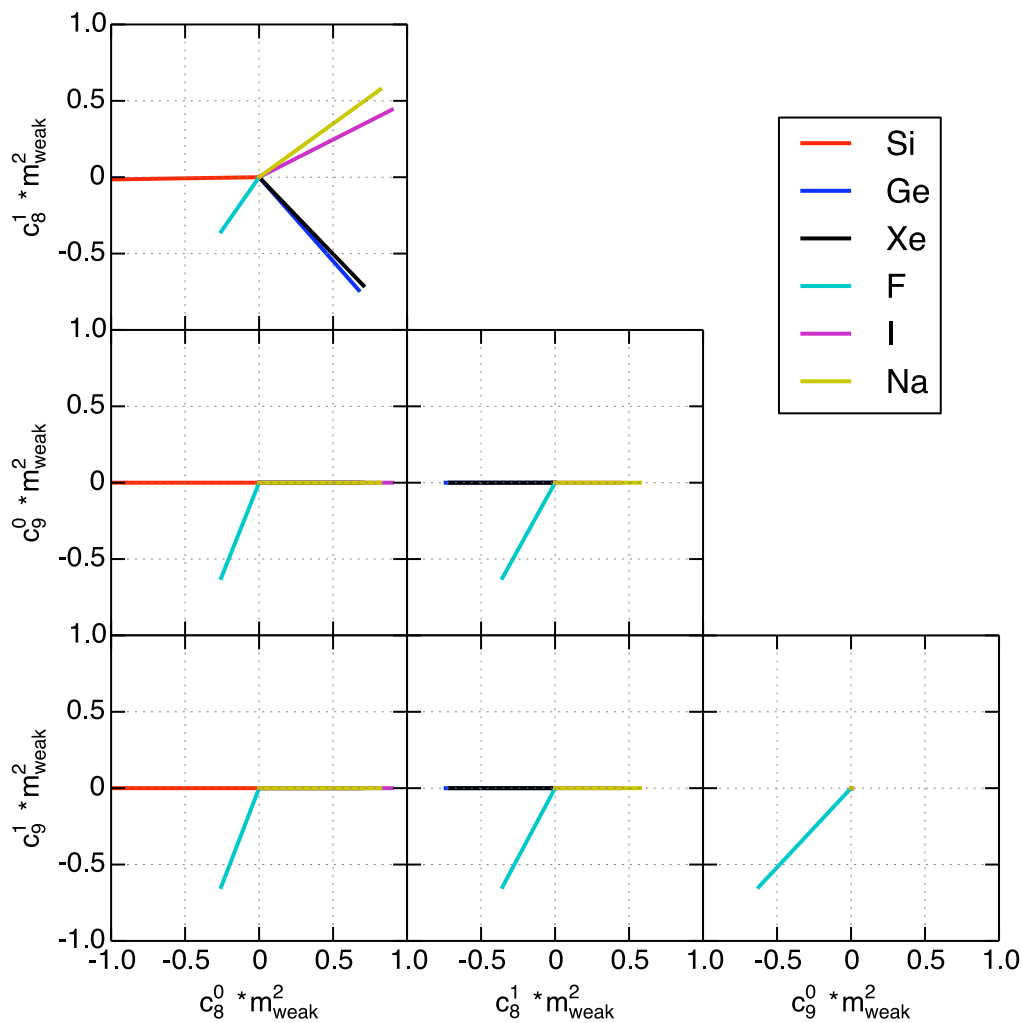
They also studied the effects of a non-SHM velocity distribution

$$f(v) = \exp \left[-\frac{v}{v_0} \right] (v_{esc}^2 - v^2)^p$$

Constructive interference eigenvectors for O_4



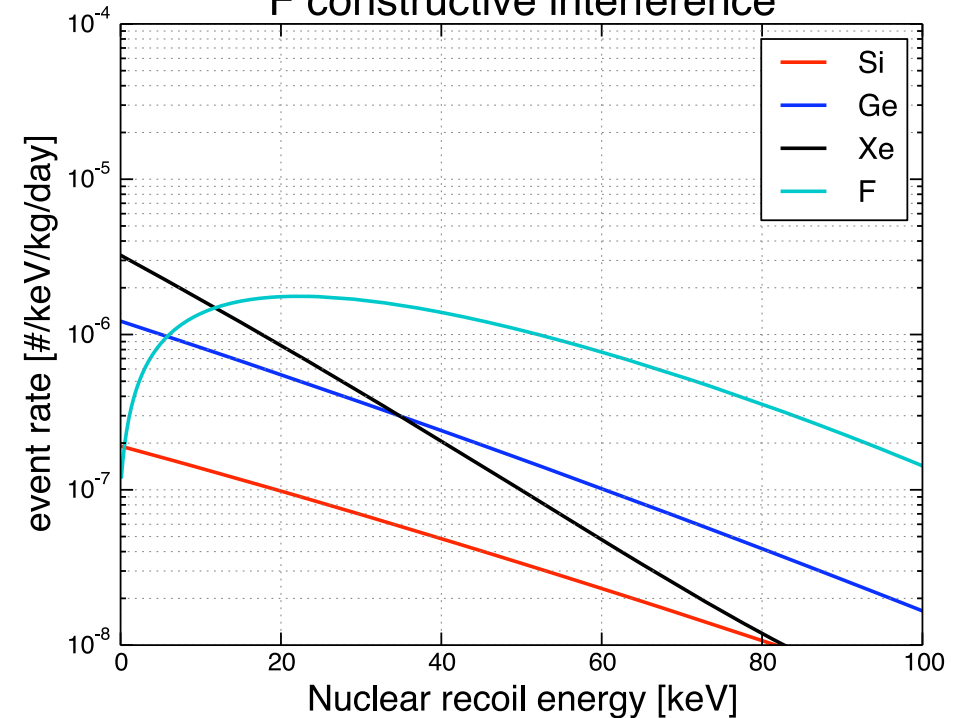
$$\begin{bmatrix} c_i^0 & c_i^1 & c_j^0 & c_j^1 \end{bmatrix} \begin{bmatrix} A_{ii}^{00} & A_{ii}^{01} & A_{ij}^{00} & A_{ij}^{01} \\ A_{ii}^{10} & A_{ii}^{11} & A_{ij}^{10} & A_{ij}^{11} \\ A_{ji}^{00} & A_{ji}^{01} & A_{jj}^{00} & A_{jj}^{01} \\ A_{ji}^{10} & A_{ji}^{11} & A_{jj}^{10} & A_{jj}^{11} \end{bmatrix} \begin{bmatrix} c_i^0 \\ c_i^1 \\ c_j^0 \\ c_j^1 \end{bmatrix}$$



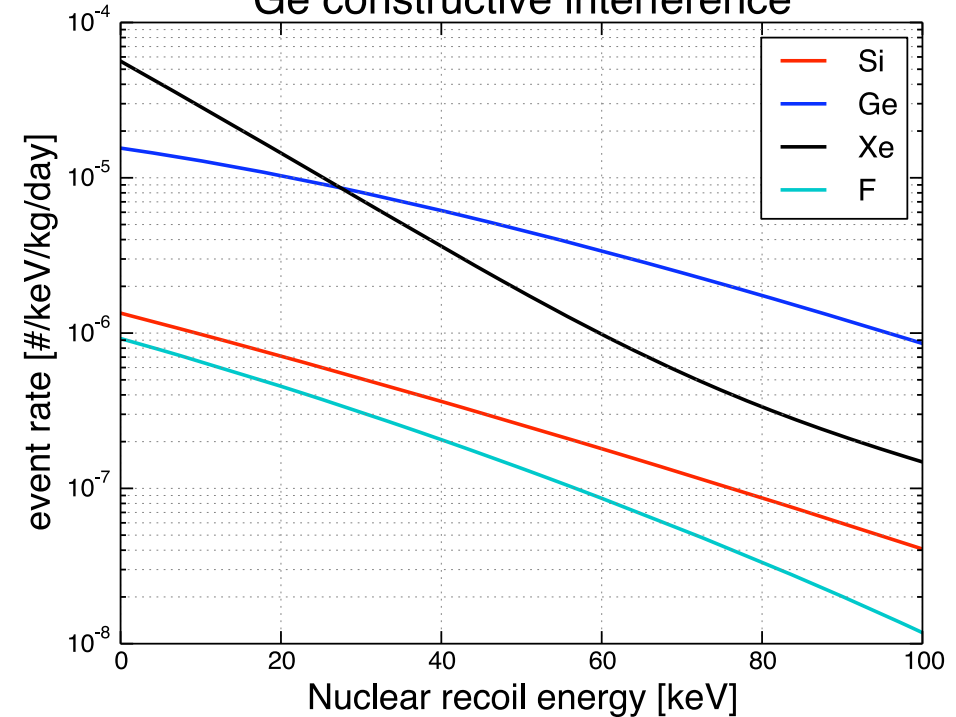
General interference

$$\mathcal{O}_8 / \mathcal{O}_9$$

F constructive interference



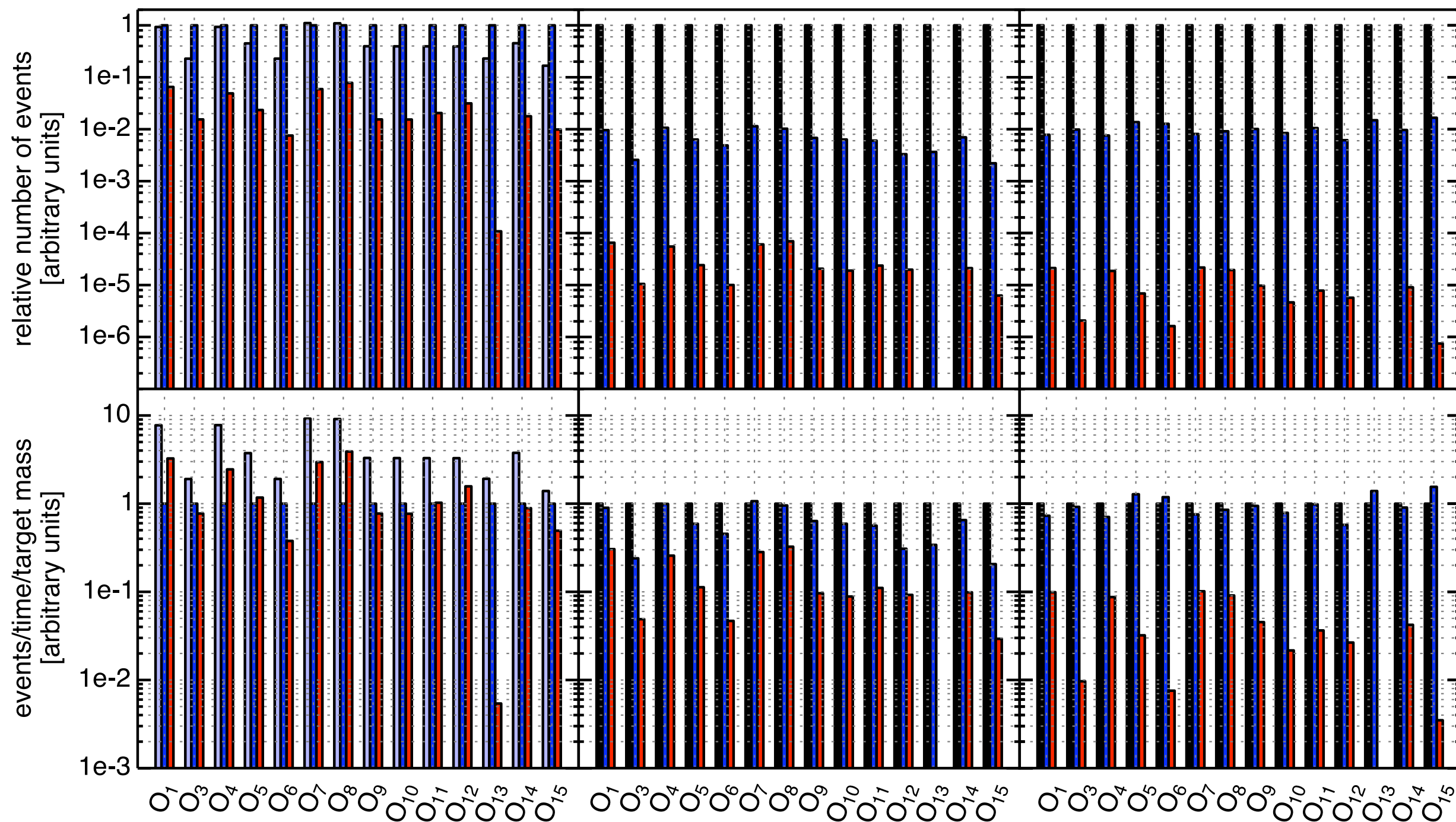
Ge constructive interference



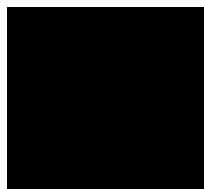
3 GeV WIMP

10 GeV WIMP

300 GeV WIMP



LZ



SuperCDMS
SNOLAB Ge
iZIP

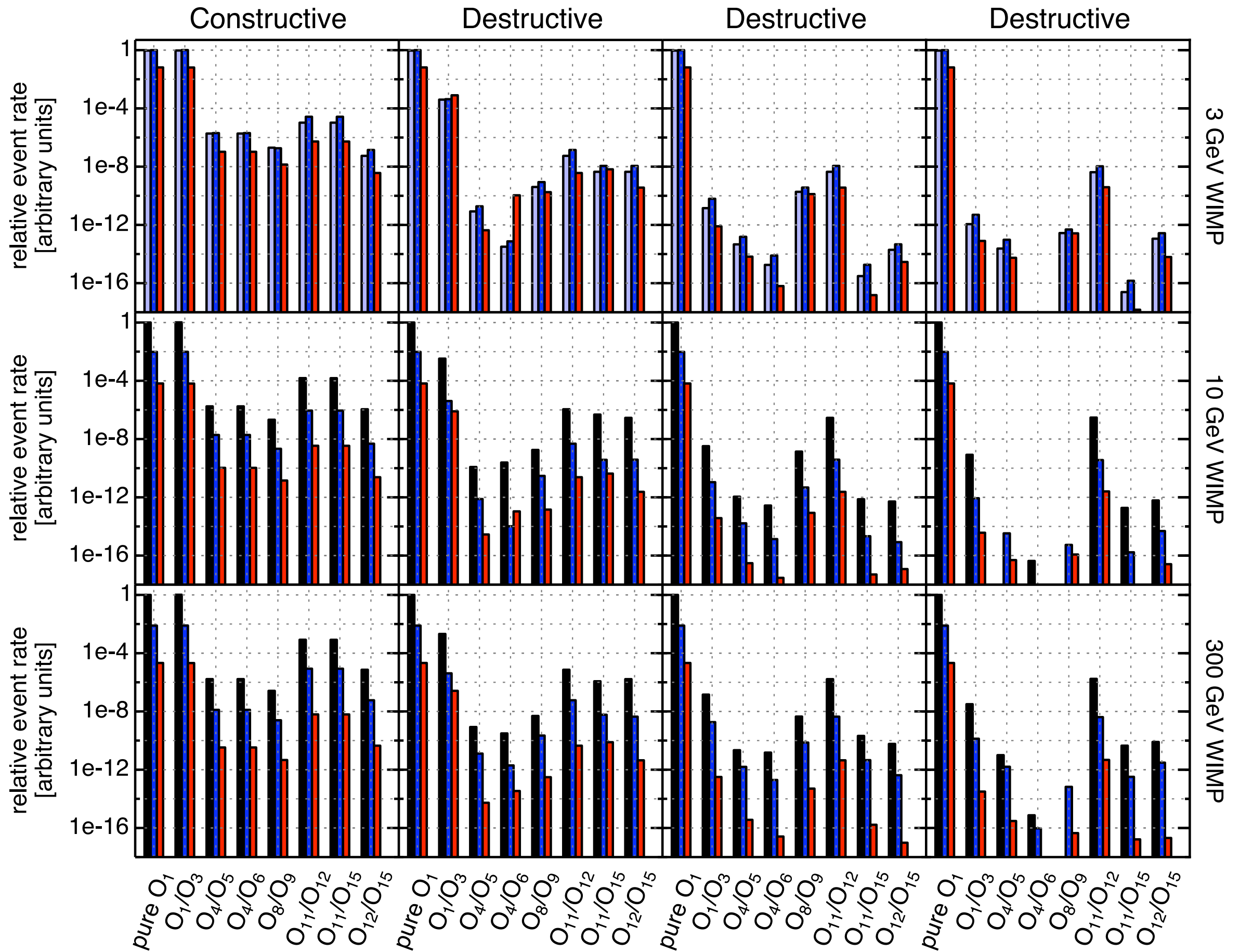


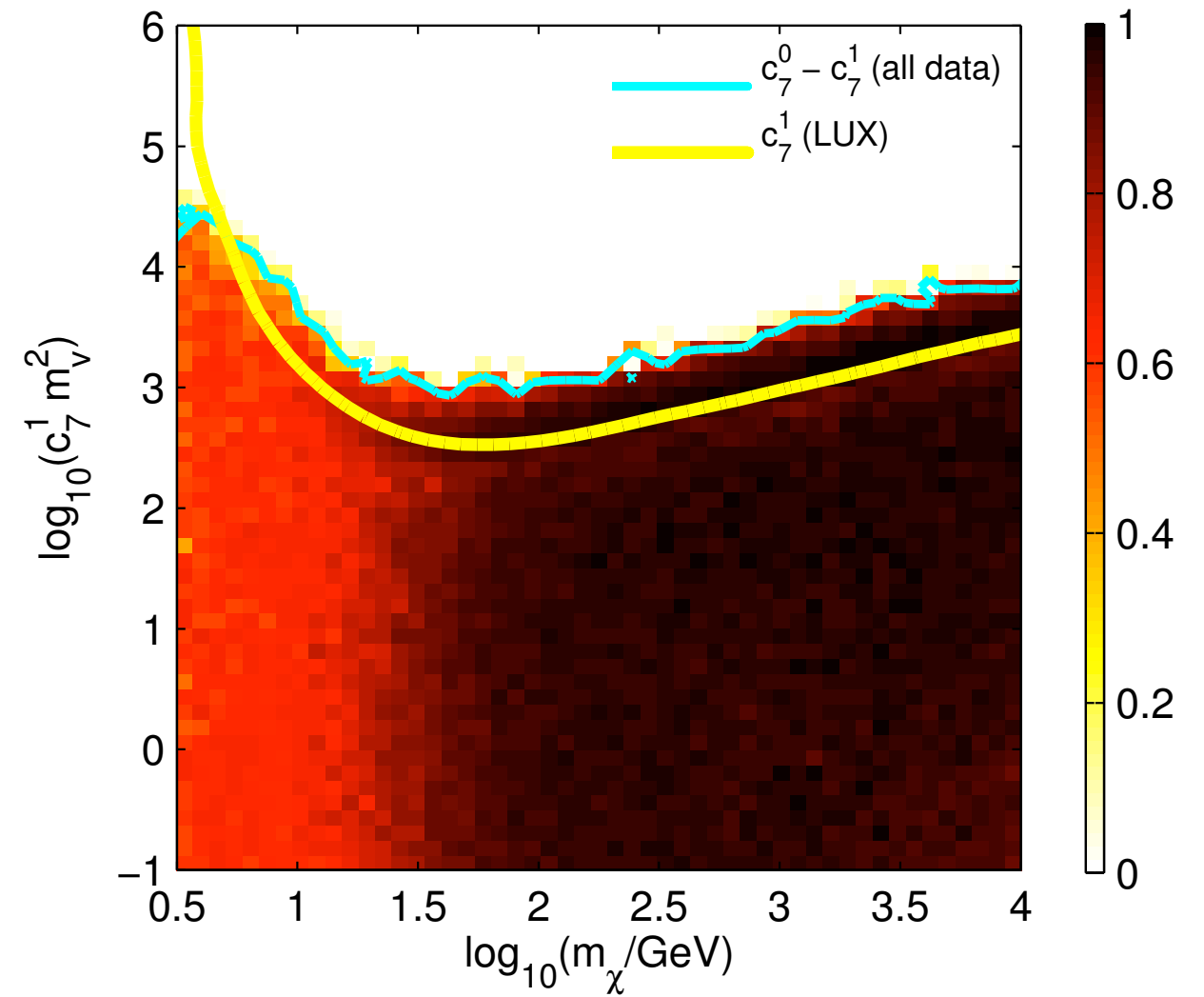
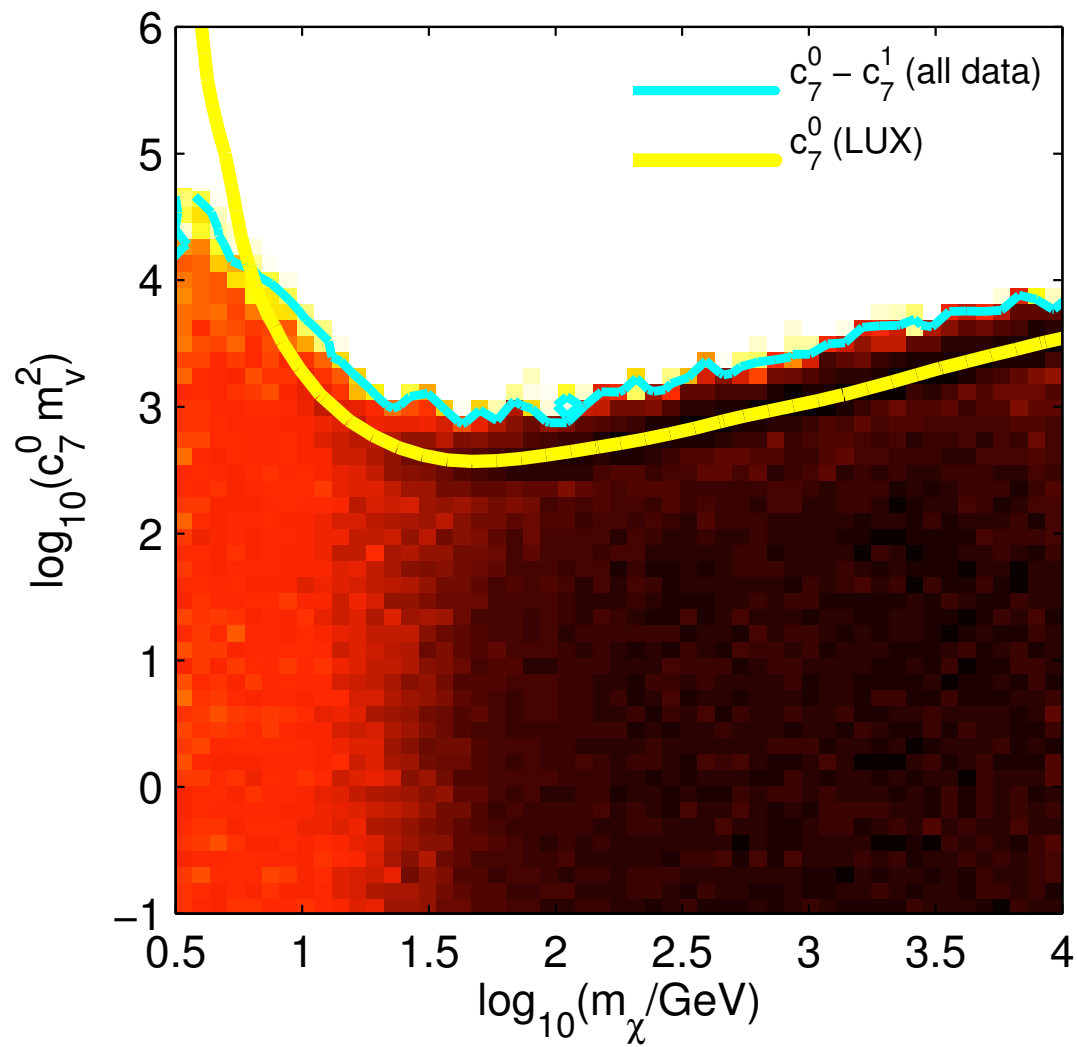
SuperCDMS
SNOLAB Si



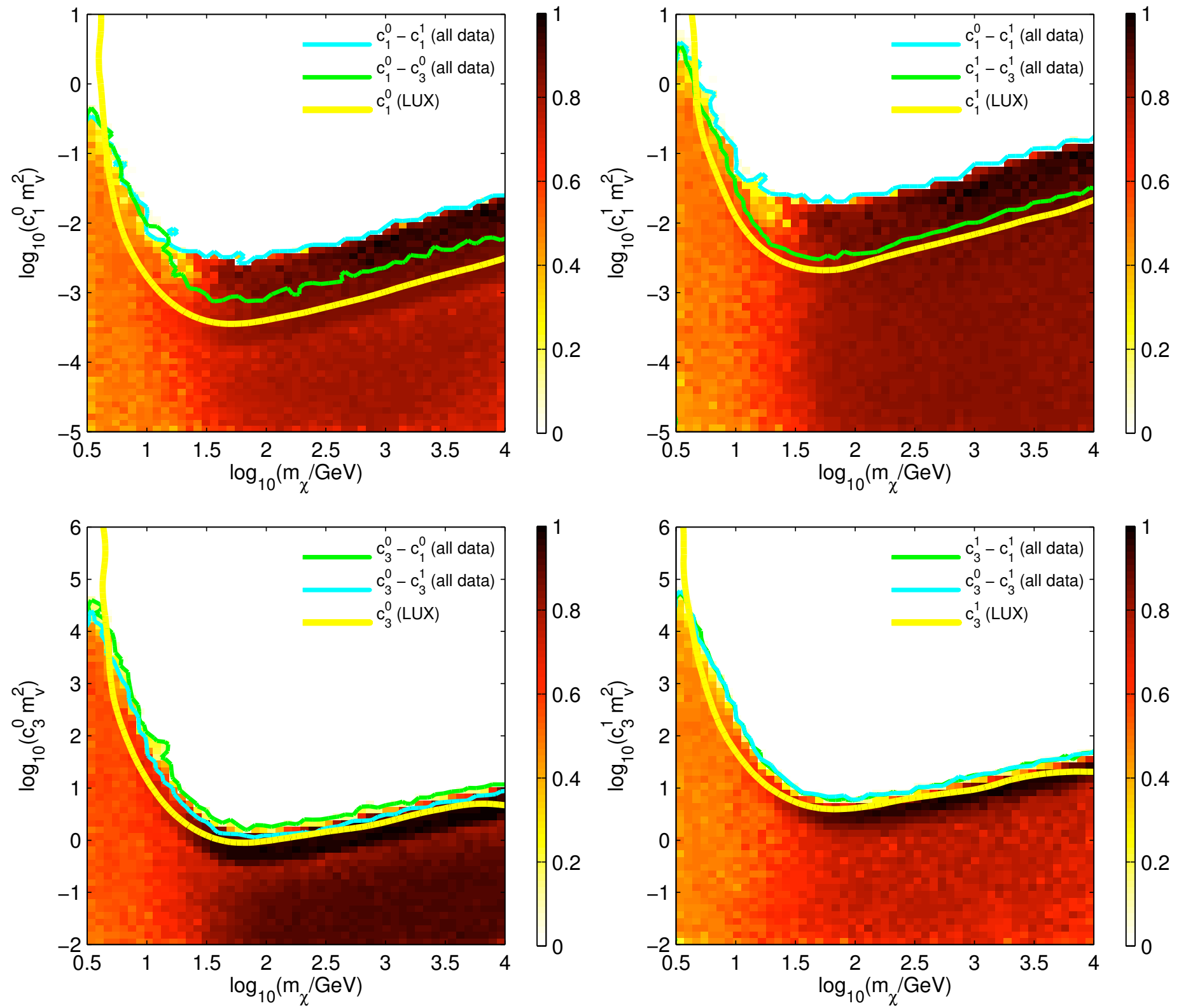
SuperCDMS
SNOLAB Ge
High Voltage





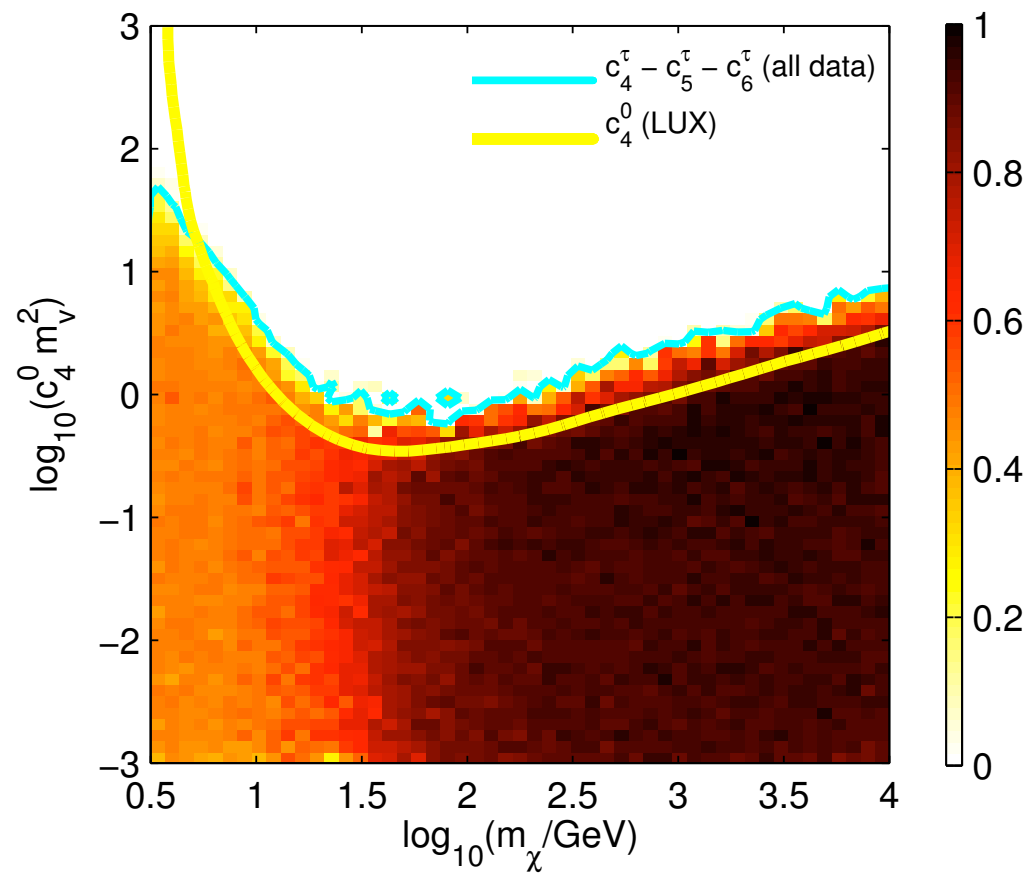


A global analysis of current data shows isoscalar/isovector interference generally makes exclusion limits weaker



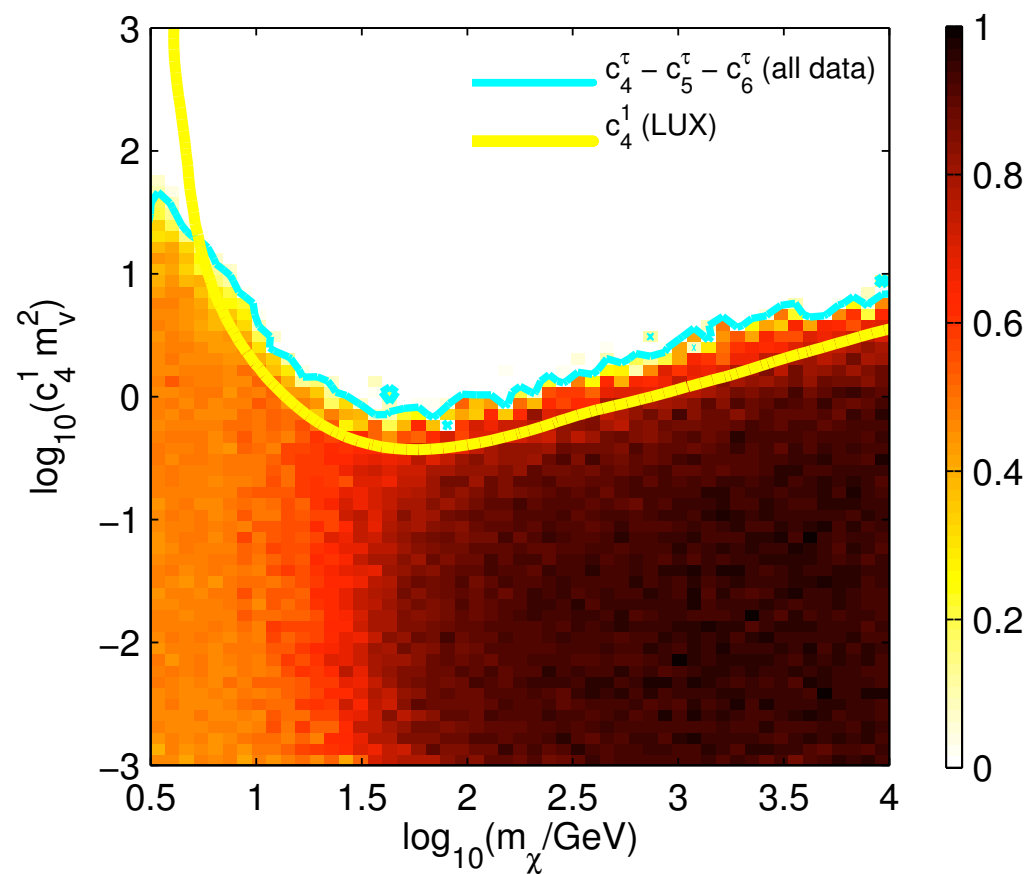
$$\mathcal{O}_1/\mathcal{O}_3$$

operator interference tends to have a smaller effect

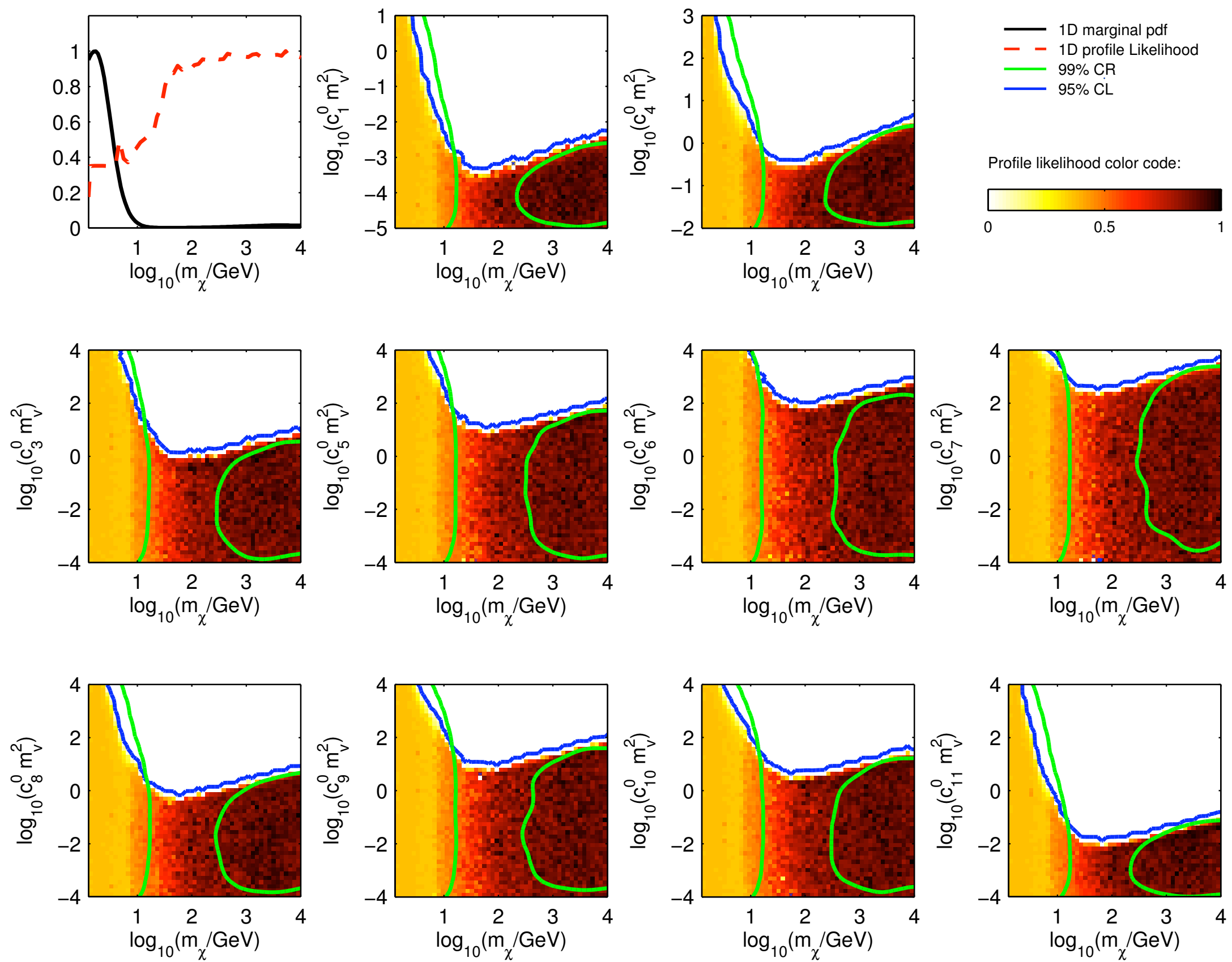


$$\mathcal{O}_4/\mathcal{O}_5$$

$$\mathcal{O}_4/\mathcal{O}_6$$



The usual spin-dependent operator suffers from less interference effects than does the spin-independent



Current experiments constrain some non-standard interactions at the same level or more than the standard spin-dependent interaction

Model reconstructions

Model reconstructions

Model reconstructions

Model reconstructions

Model reconstructions

Model reconstructions

Model reconstructions

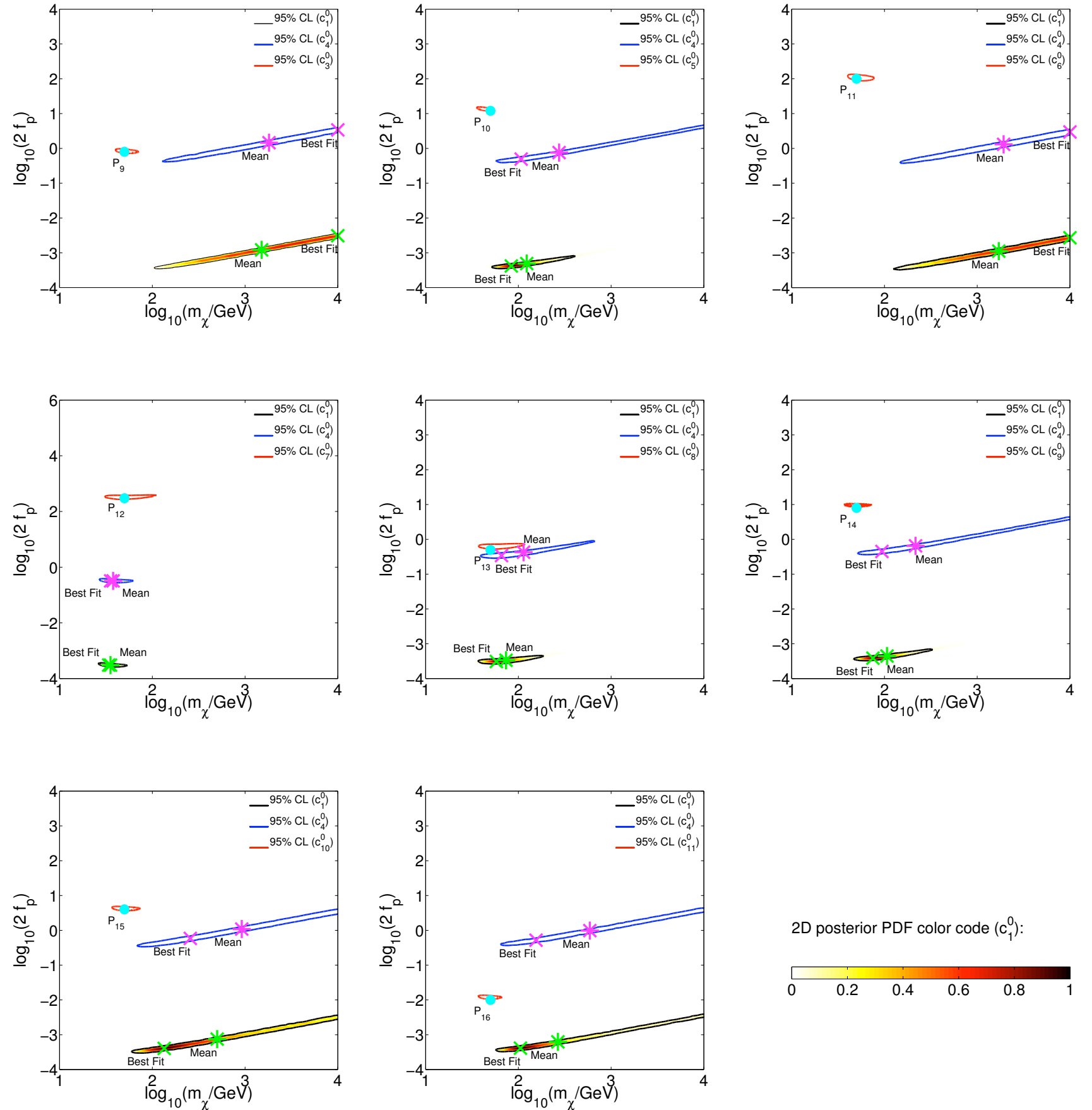
Model reconstructions

Model reconstructions

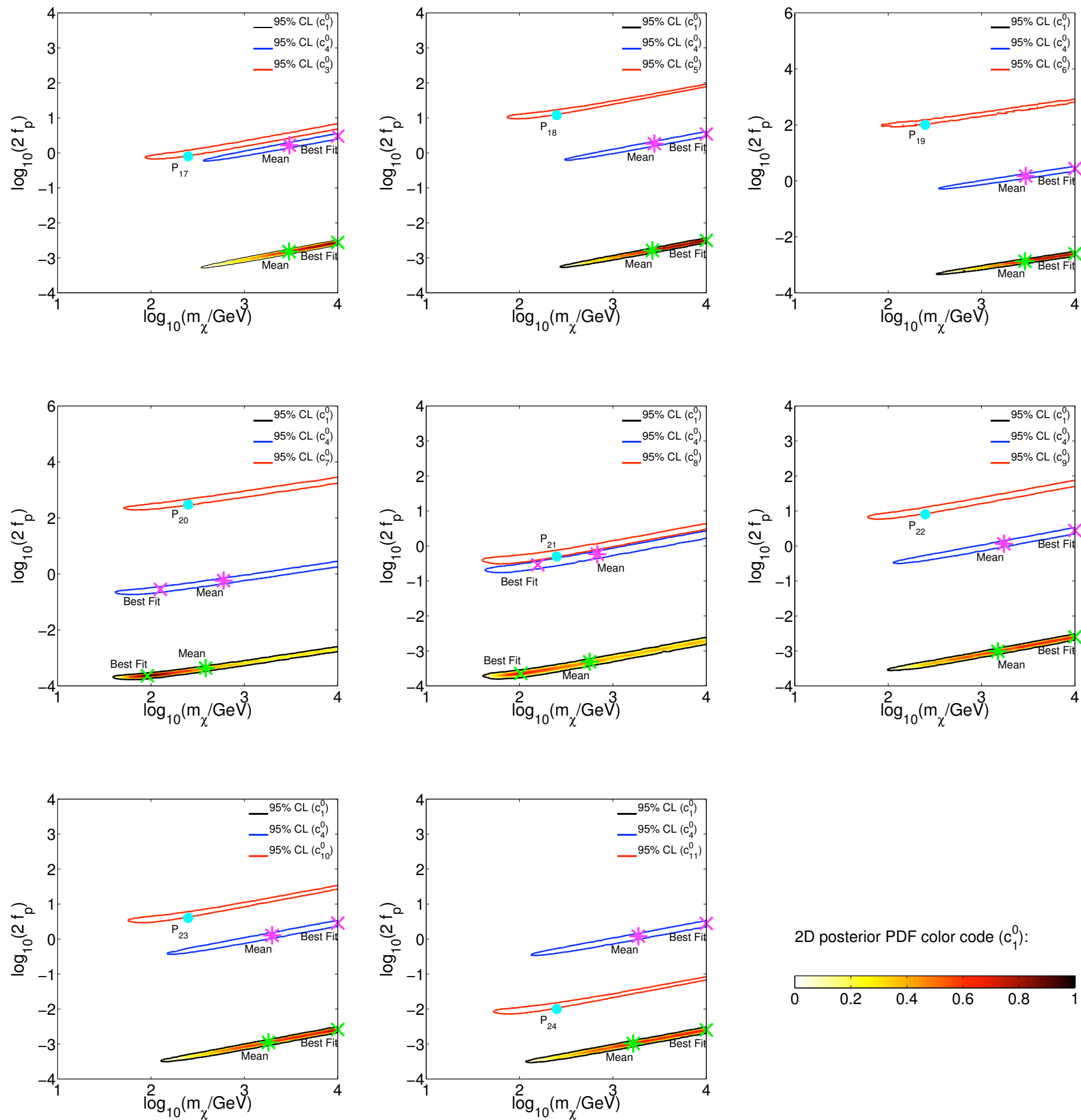
Model reconstructions

50GeV

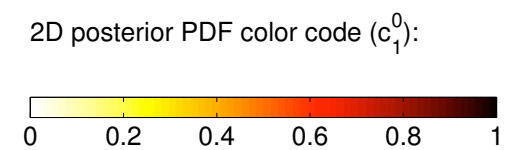
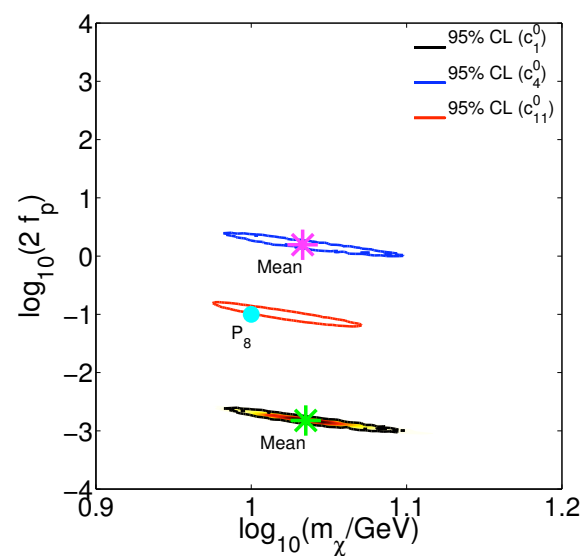
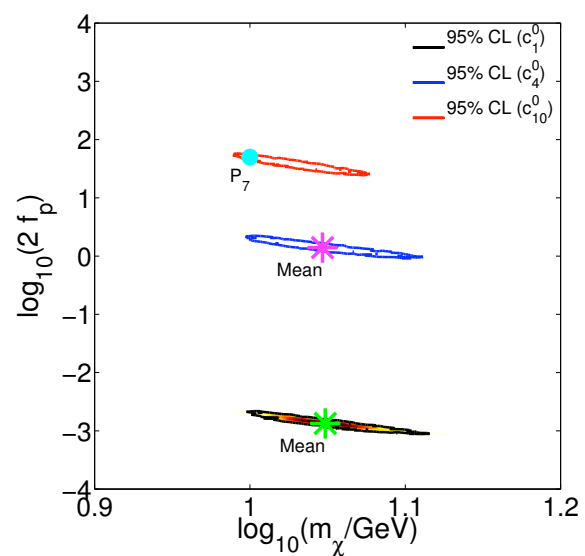
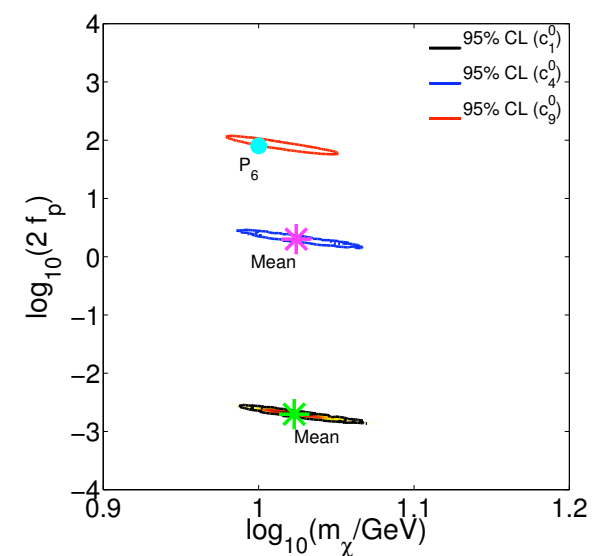
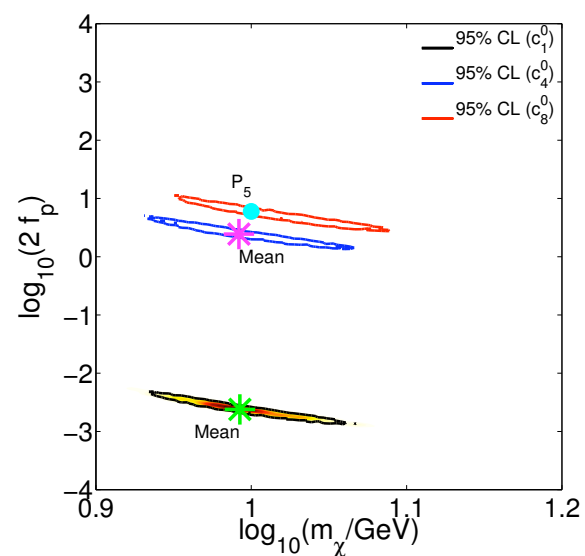
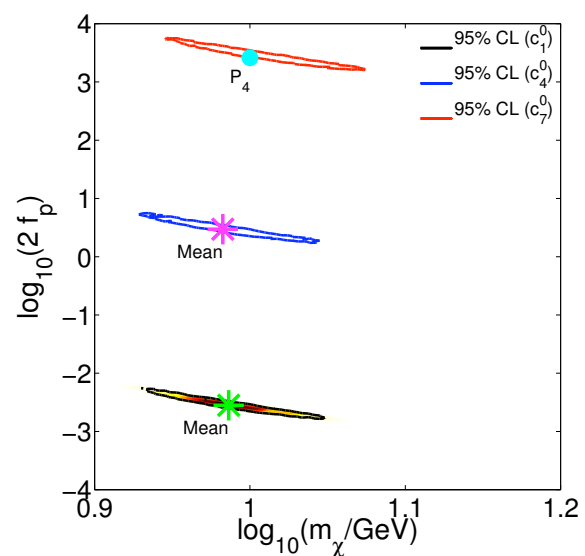
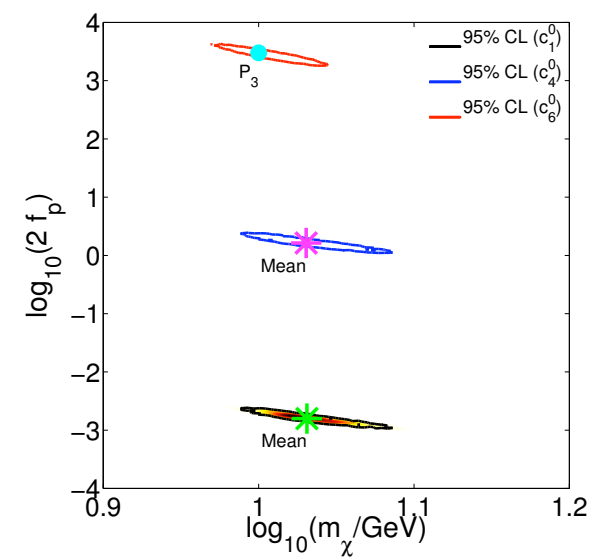
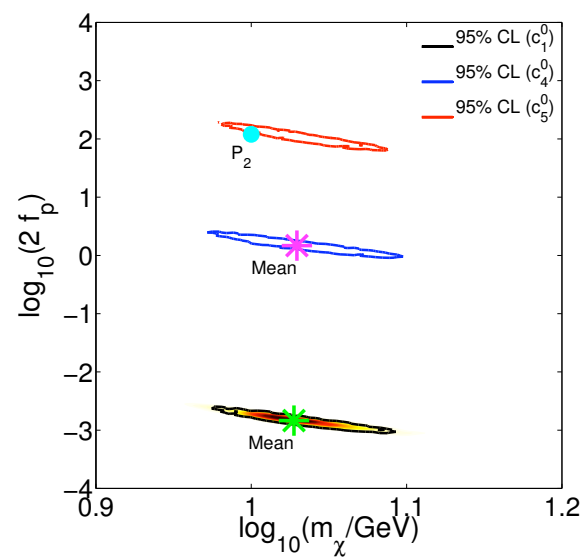
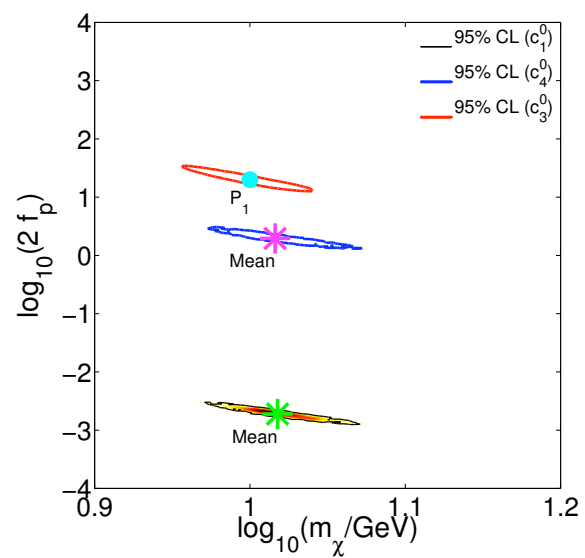
Theoretical bias in the fits for ton-scale Ge and Xe



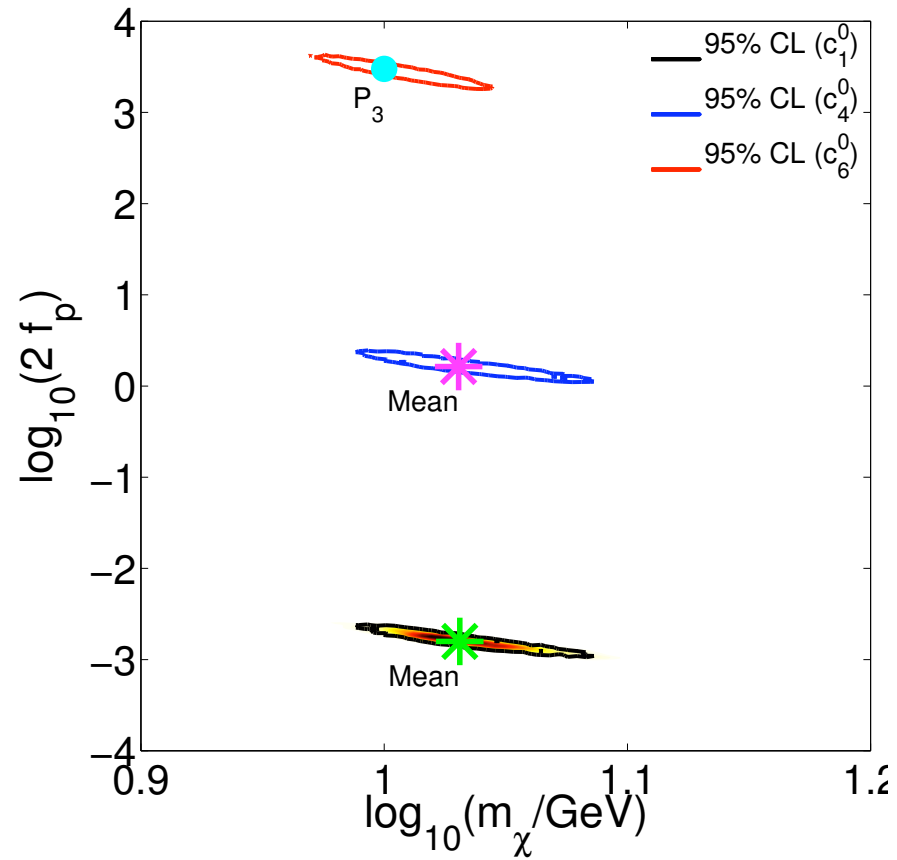
250GeV



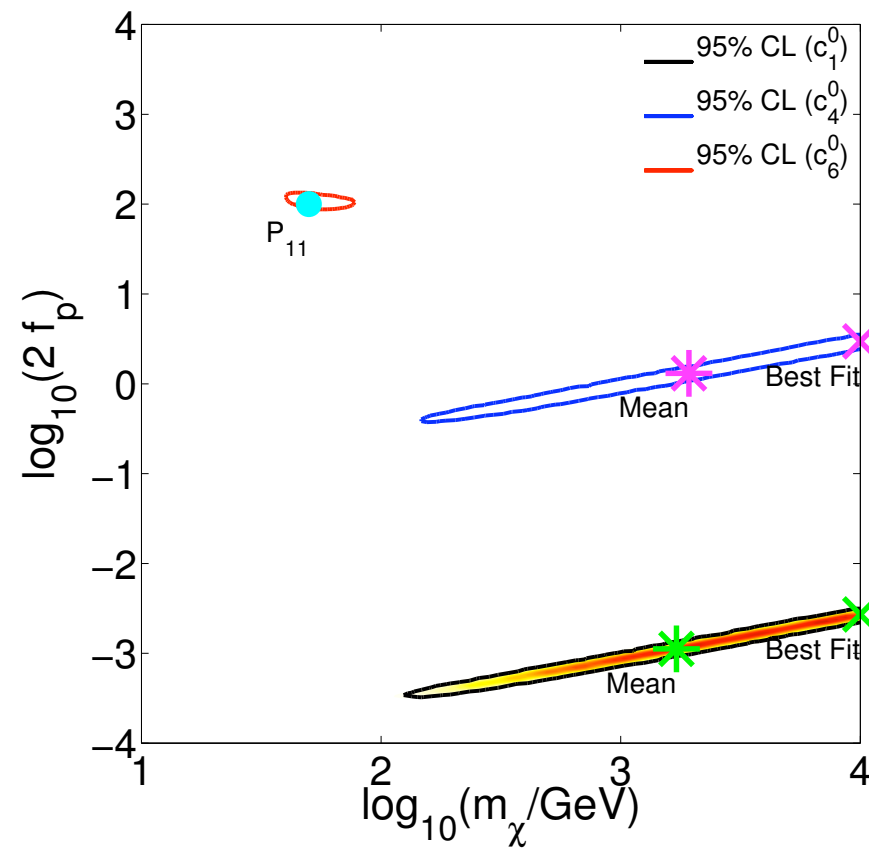
10GeV



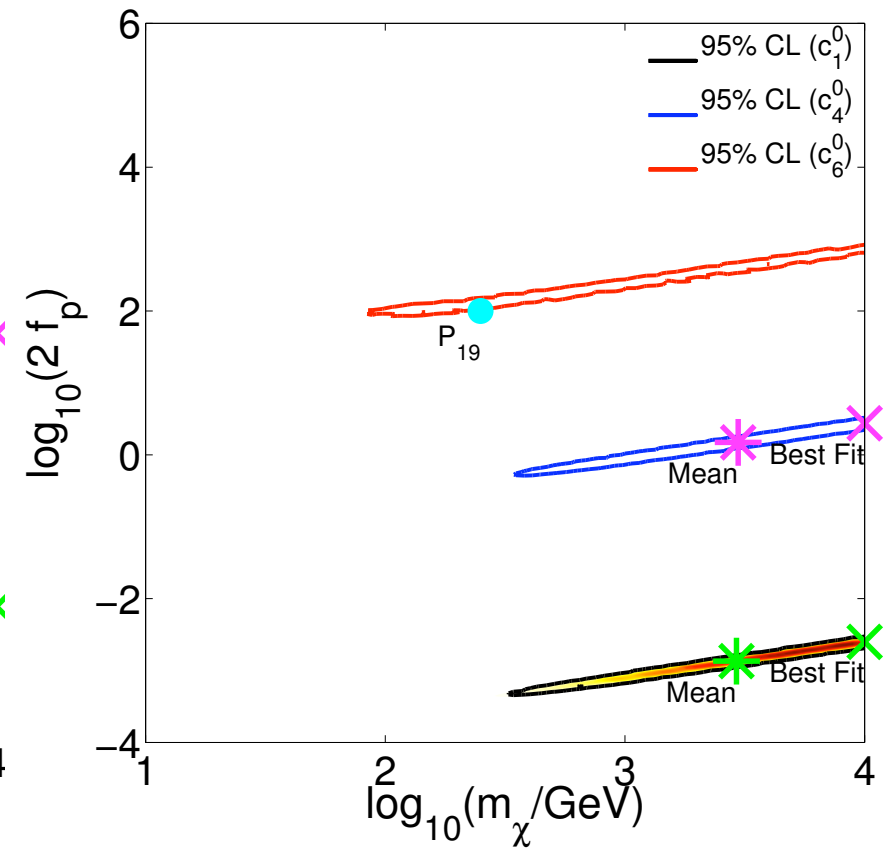
10GeV



50GeV



250GeV



Fitting a non-standard interaction with SI/SD assumptions

Anapole

$$\mathcal{L}_{\text{int}}^{\text{anapole}} = \frac{f_a}{M^2} \bar{\chi} \gamma^\mu \gamma^5 \chi \mathcal{J}_\mu^{\text{EM}} \rightarrow \frac{2f_a}{M^2} \sum_{N=n,p} (\mathcal{Q}_N \mathcal{O}_8 + \tilde{\mu}_N \mathcal{O}_9)$$

Magnetic dipole

$$\mathcal{L}_{\text{int}}^{\text{magnetic dipole}} = \frac{f_{\text{md}}}{M^2} \bar{\chi} \frac{i\sigma^{\mu\nu} q_\nu}{\Lambda} \chi \mathcal{J}_\mu^{\text{EM}} \rightarrow \frac{2f_{\text{md}}}{M^2} \sum_{N=n,p} \left(\mathcal{Q}_N \left(\frac{m_N}{\Lambda} \mathcal{O}_5 - \frac{\vec{q}^2}{4m_\chi \Lambda} \mathcal{O}_1 \right) + \tilde{\mu}_N \left(\frac{m_N}{\Lambda} \mathcal{O}_6 - \frac{\vec{q}^2}{m_N \Lambda} \mathcal{O}_4 \right) \right).$$

Electric dipole

$$\mathcal{L}_{\text{int}}^{\text{electric dipole}} = \frac{f_{\text{ed}}}{M^2} \bar{\chi} \frac{\sigma^{\mu\nu} q_\nu \gamma^5}{\Lambda} \chi \mathcal{J}_\mu^{\text{EM}} \rightarrow \frac{2f_{\text{ed}}}{M^2} \sum_{N=n,p} \left(-\mathcal{Q}_N \frac{m_N}{\Lambda} \mathcal{O}_{11} + \tilde{\mu}_N \left(\frac{m_N}{\Lambda} \mathcal{O}_{15} + \frac{m_\chi \vec{q}^2}{4m_N^2 \Lambda} \mathcal{O}_{11} \right) \right)$$

LS generating

$$\mathcal{L}_{\text{int}}^{\text{LS}} = \frac{f_{\text{LS}}}{\Lambda^2} \bar{\chi} \gamma_\mu \chi \sum_{N=n,p} \left(\kappa_1^N \frac{q_\alpha q^\alpha}{m_N^2} \bar{N} \gamma^\mu N + \kappa_2^N \bar{N} \frac{i\sigma^{\mu\nu} q_\nu}{2m_N} N \right) \rightarrow \frac{f_{\text{LS}}}{\Lambda^2} \sum_{N=n,p} \left(\left(\frac{\kappa_2^N}{4} - \kappa_1^N \right) \frac{\vec{q}^2}{m_N^2} \mathcal{O}_1 - \kappa_2^N \mathcal{O}_3 + \kappa_2^N \frac{m_N}{m_\chi} \left(\frac{\vec{q}^2}{m_N^2} \mathcal{O}_4 - \mathcal{O}_6 \right) \right)$$

Anapole

$$\mathcal{L}_{\text{int}}^{\text{anapole}} = \frac{f_a}{M^2} \bar{\chi} \gamma^\mu \gamma^5 \chi \mathcal{J}_\mu^{\text{EM}}$$

Leading vector coupling for Majorana dark matter

$$\mathcal{J}_\mu^{\text{EM}} \equiv \sum_{N=n,p} \bar{N} \left(Q_N \frac{K_\mu}{2m_N} - \tilde{\mu}_N \frac{i\sigma_{\mu\nu} q^\nu}{2m_N} \right) N$$

Electromagnetic current for nucleons

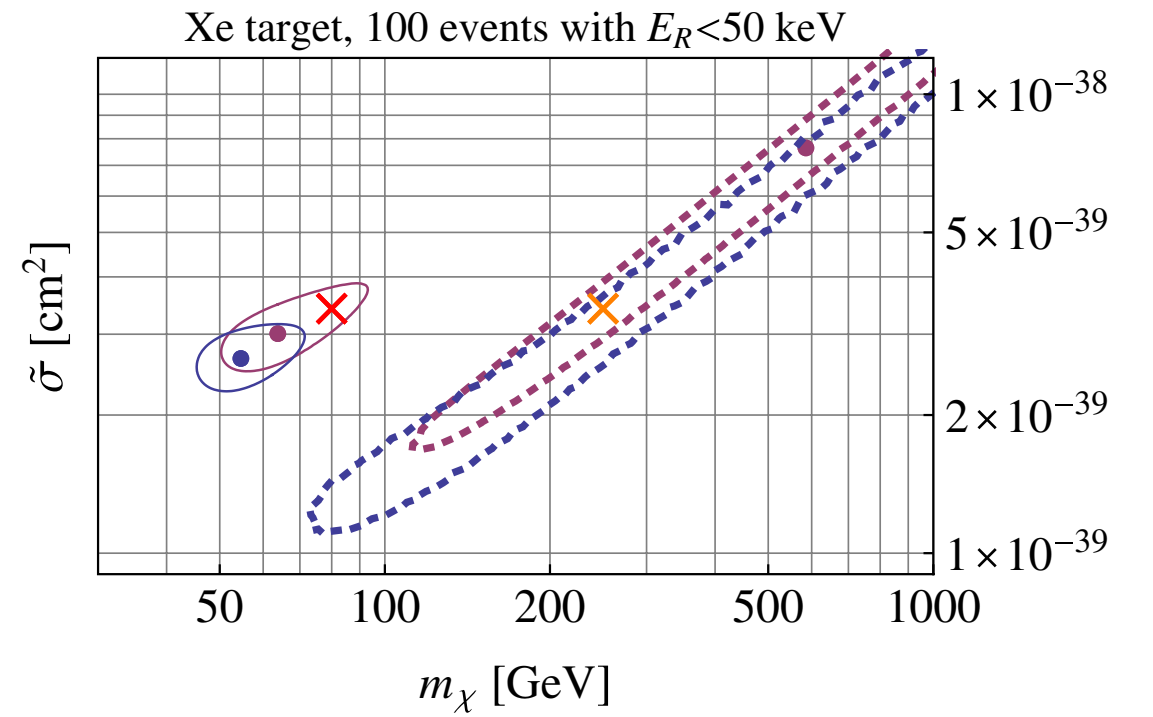
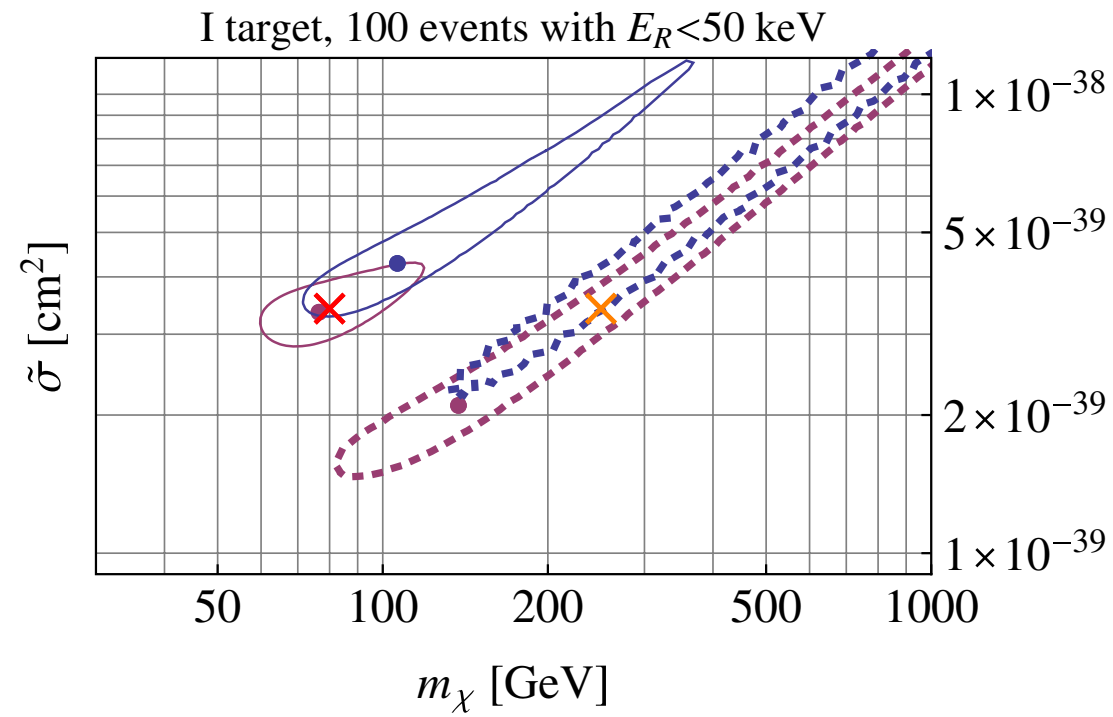
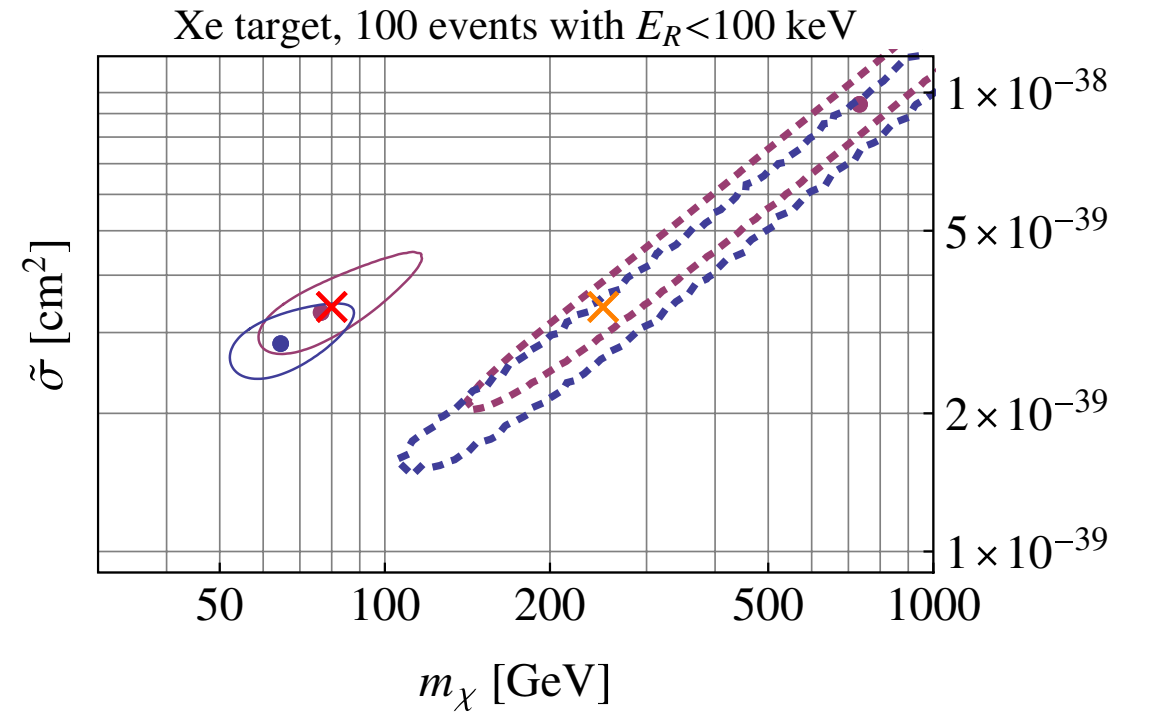
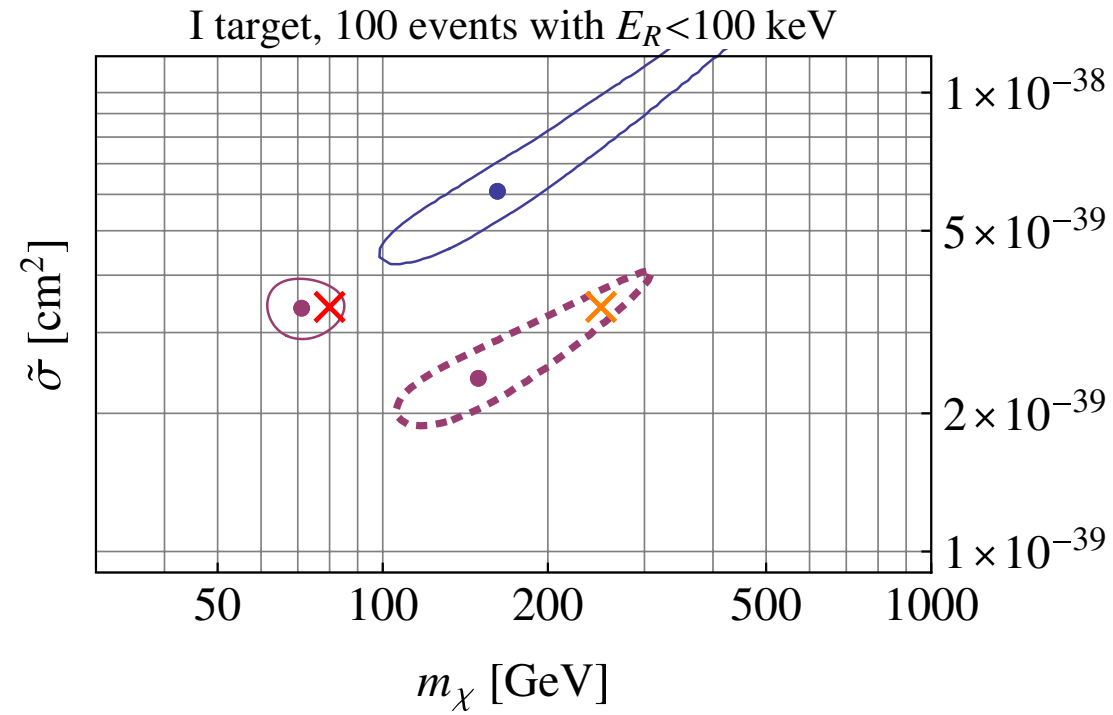
$$\mathcal{L}_{\text{int}}^{\text{anapole}} \rightarrow \frac{2f_a}{M^2} \sum_{N=n,p} (Q_N \mathcal{O}_8 + \tilde{\mu}_N \mathcal{O}_9)$$

Nuclear effects

$$\tilde{\mu}_T = 2\tilde{\mu}_p \langle S_p \rangle + 2\tilde{\mu}_n \langle S_n \rangle + \langle L_p \rangle$$

$$\begin{aligned} \sigma_T^{\text{anapole}} = & \frac{\mu_T^2}{\pi} \left(\frac{f_a}{M^2} \right)^2 C_\chi \left\{ \vec{v}_T^{\perp 2} \tilde{W}_M^{(p,p)} \right. \\ & + \frac{\vec{q}^2}{m_N^2} \left[\tilde{W}_\Delta^{(p,p)} - \tilde{\mu}_n \tilde{W}_{\Delta\Sigma'}^{(p,n)} - \tilde{\mu}_p \tilde{W}_{\Delta\Sigma'}^{(p,p)} \right. \\ & \left. \left. + \frac{1}{4} (\tilde{\mu}_p^2 \tilde{W}_{\Sigma'}^{(p,p)} + 2\tilde{\mu}_n \tilde{\mu}_p \tilde{W}_{\Sigma'}^{(p,n)} + \tilde{\mu}_n^2 \tilde{W}_{\Sigma'}^{(n,n)}) \right] \right\} \end{aligned}$$

Nuclear responses including interference



Fits to simulated data for 80GeV and 250GeV dark matter on Iodine and Xenon targets for true and standard form factors

Future prospects for distinguishing models

V. Glusevic, M. Gresham, S.D. McDermott, A.H.G. Peter, and K. Zurek, arXiv:1506.04454

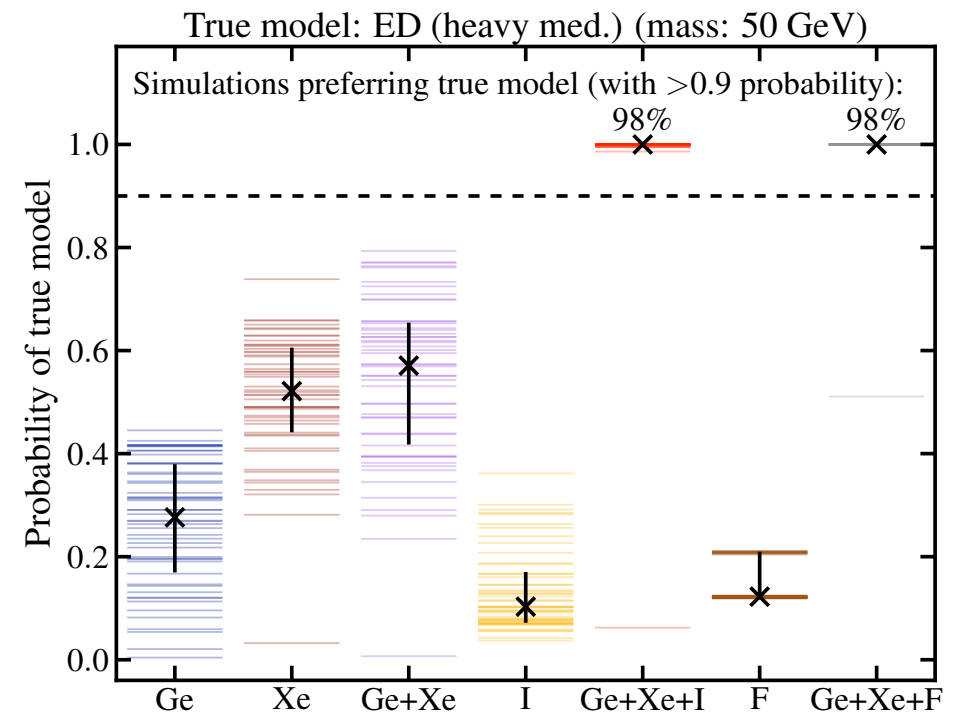
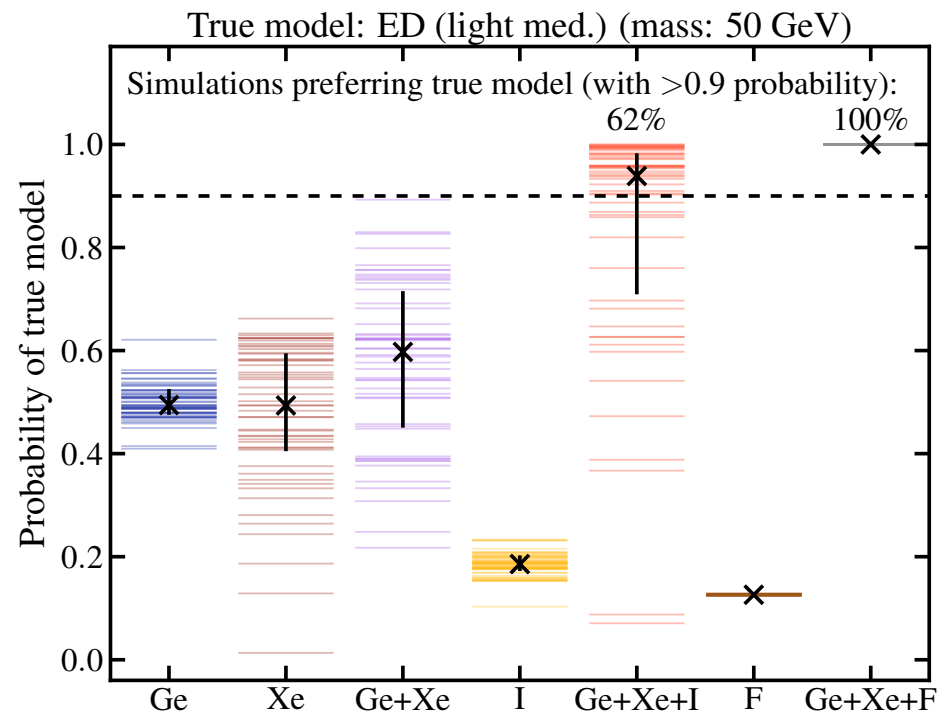
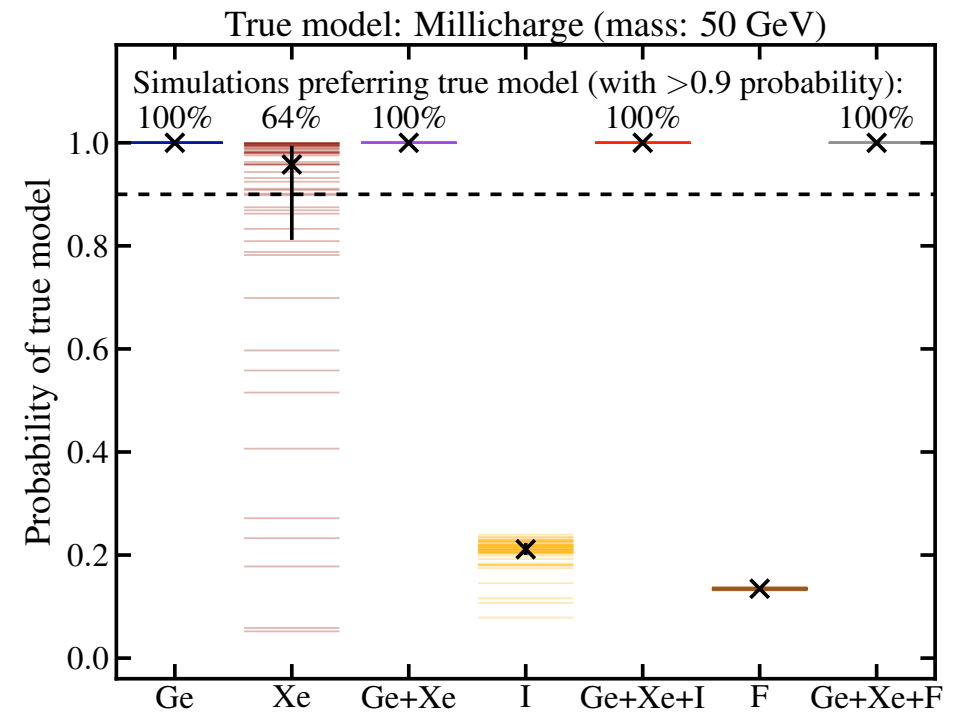
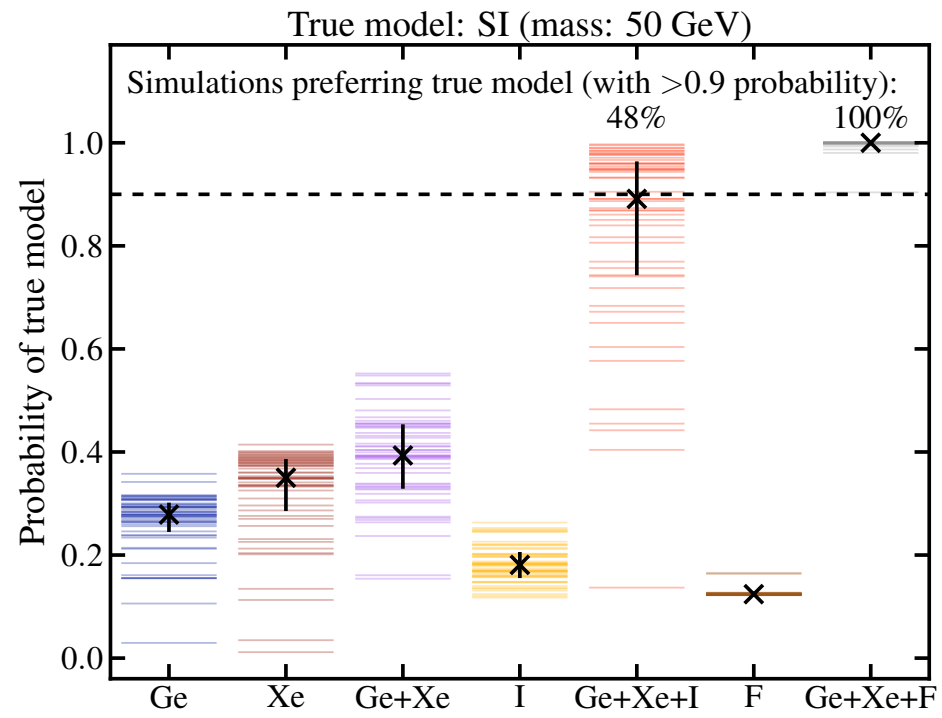
Model name	Lagrangian	\vec{q}, v Dependence	Response	f_n/f_p
SI	$\bar{\chi}\chi\bar{N}N$	1	M	+1
SD	$\bar{\chi}\gamma^\mu\gamma_5\chi\bar{N}\gamma_\mu\gamma_5N$	1	$\Sigma' + \Sigma''$	−1.1
Anapole	$\bar{\chi}\gamma^\mu\gamma_5\chi\partial^\nu F_{\mu\nu}$	$v^{\perp 2}$	M	photon-like
		\vec{q}^2/m_N^2	$\Delta + \Sigma'$	
Millicharge	$\bar{\chi}\gamma^\mu\chi A_\mu$	$m_N^2m_\chi^2/\vec{q}^4$	M	photon-like
MD (light med.)	$\bar{\chi}\sigma^{\mu\nu}\chi F_{\mu\nu}$	$1 + \frac{v^{\perp 2}m_N^2}{\vec{q}^2}$	M	photon-like
		1	$\Delta + \Sigma'$	
ED (light med.)	$\bar{\chi}\sigma^{\mu\nu}\gamma_5\chi F_{\mu\nu}$	m_N^2/\vec{q}^2	M	photon-like
MD (heavy med.)	$\bar{\chi}\sigma^{\mu\nu}\partial_\mu\chi\partial^\alpha F_{\alpha\nu}$	$\frac{\vec{q}^4}{\Lambda^4} + \frac{v^{\perp 2}m_N^2\vec{q}^2}{\Lambda^4}$	M	photon-like
		\vec{q}^4/Λ^4	$\Delta + \Sigma'$	
ED (heavy med.)	$\bar{\chi}\sigma^{\mu\nu}\gamma_5\partial_\mu\chi\partial^\alpha F_{\alpha\nu}$	$\vec{q}^2m_N^2/\Lambda^4$	M	photon-like
SI_{q^2}	$i\bar{\chi}\gamma_5\chi\bar{N}N$	\vec{q}^2/m_χ^2	M	+1
SD_{q^2} (Higgs-like/flavor-univ.)	$i\bar{\chi}\chi\bar{N}\gamma_5N$	\vec{q}^2/m_N^2	Σ''	+1/ − 0.05
SD_{q^4} (Higgs-like/flavor-univ.)	$\bar{\chi}\gamma_5\chi\bar{N}\gamma_5N$	$\vec{q}^4/m_\chi^2m_N^2$	Σ''	+1/ − 0.05
$\vec{L} \cdot \vec{S}$ -like	$\bar{\chi}\gamma_\mu\chi\frac{\partial^2\bar{N}\gamma^\mu N}{m_N^2} +$ $+ \bar{\chi}\gamma_\mu\chi\frac{\partial_\nu\bar{N}\sigma^{\mu\nu}N}{2m_N}$	\vec{q}^4/m_N^4	M	+1
		\vec{q}^4/m_N^4	Φ''	
		$\frac{\vec{q}^2v^{\perp 2}}{m_N^2} + \frac{\vec{q}^4}{m_\chi^2m_N^2}$	Σ'	

Simulated over 8000 recoil energy spectra for various models

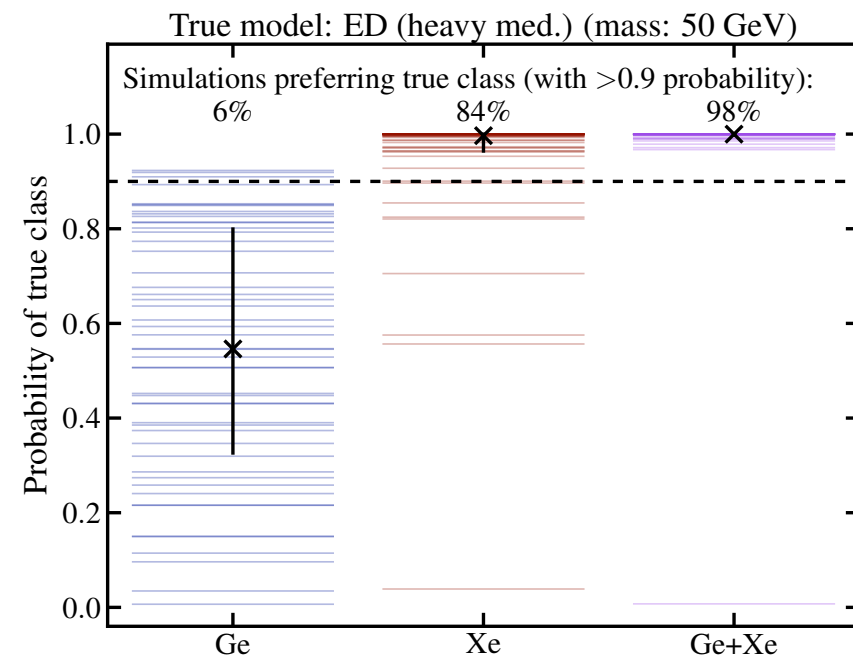
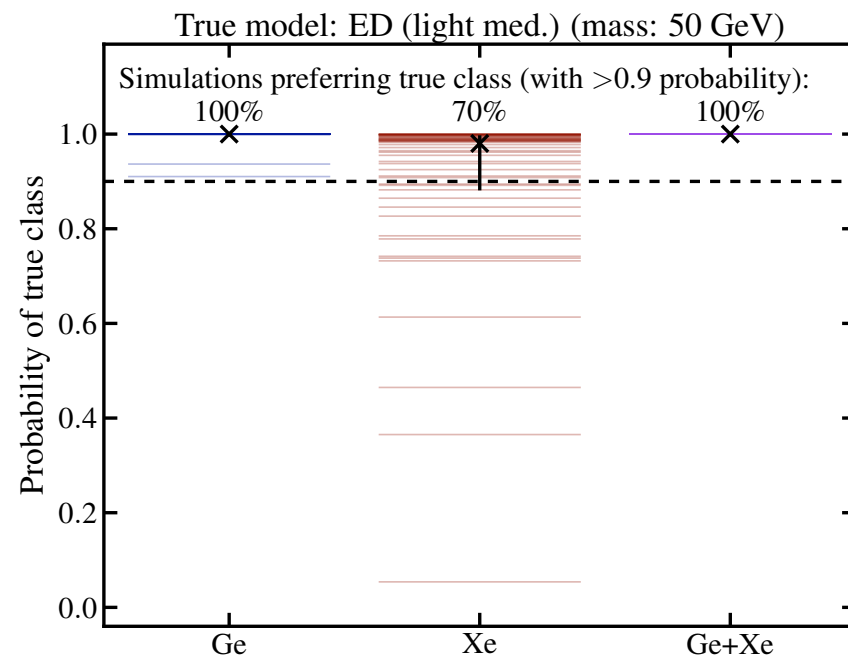
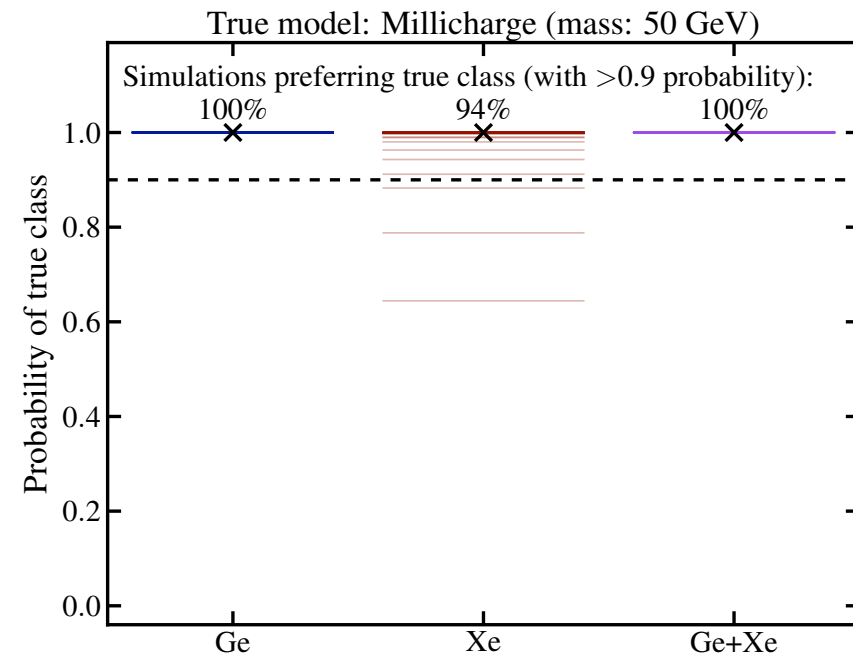
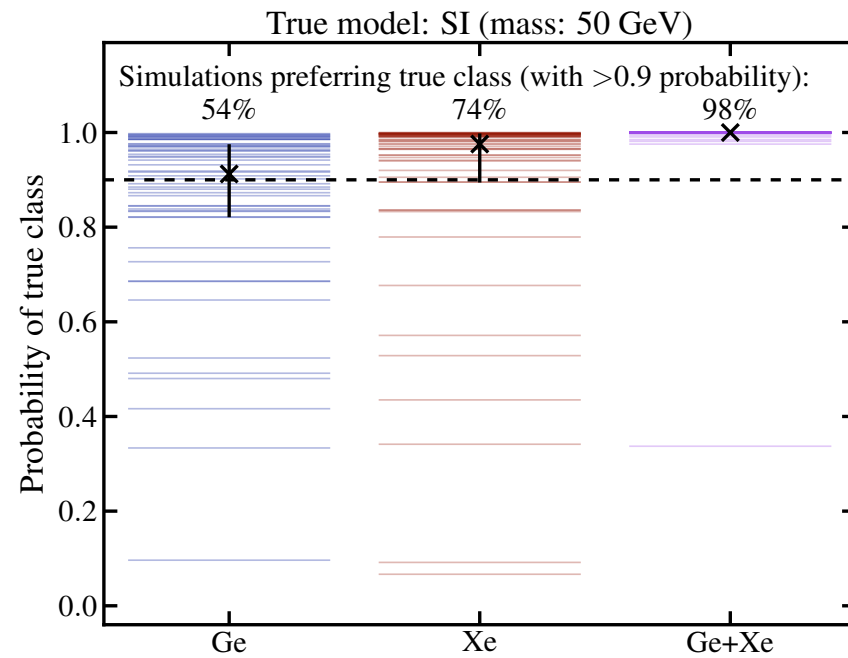
Future prospects for distinguishing models

Label	A (Z)	Energy window [keVnr]	Exposure [kg-yr]
Xe	131 (54)	5-40	2000
Ge	73 (32)	0.3-100	100
I	127 (53)	22.2-600	212
F	19 (9)	3-100	606
Na	23 (11)	6.7-200	38
Ar	40 (18)	25-200	3000
He	4 (2)	3-100	300
Xe(lo)	131 (54)	1-40	2000
Xe(hi)	131 (54)	5-100	2000
Xe(wide)	131 (54)	1-100	2000
I(lo)	127 (53)	1-600	212
XeG3	131 (54)	5-40	40 000
I+	127 (53)	1-600	424
F+	19 (9)	3-100	1200

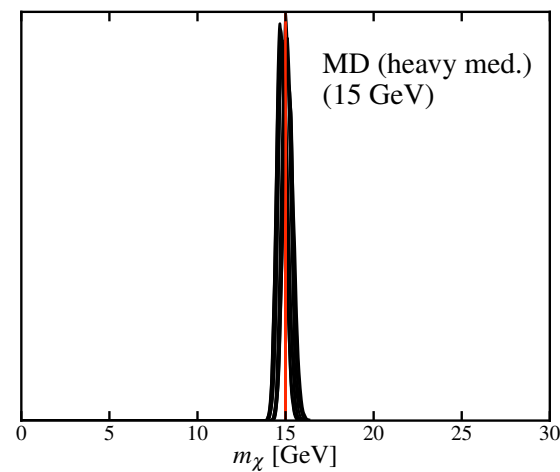
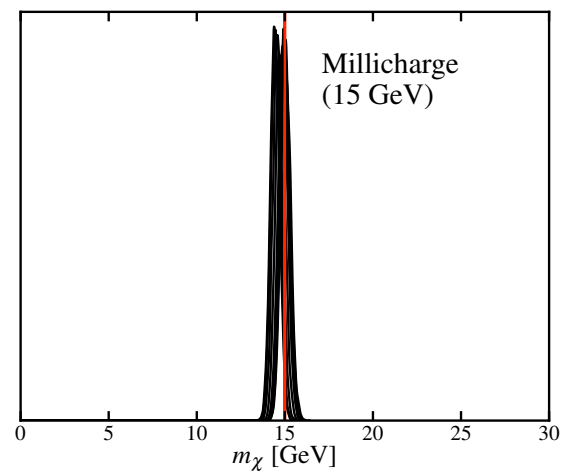
Covers the targets for the next generation of ton-scale detectors



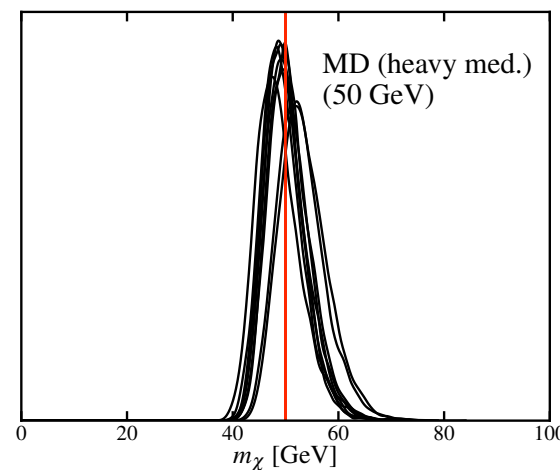
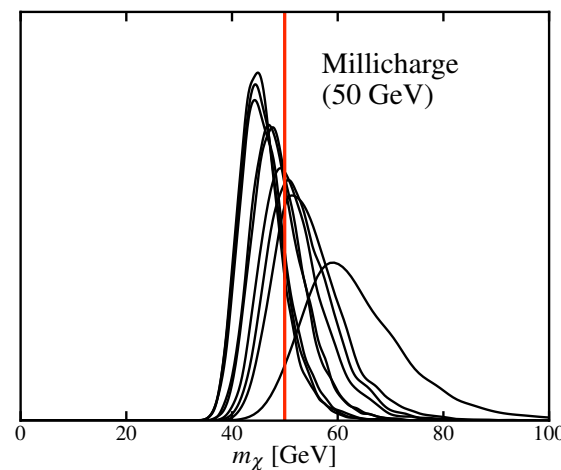
Excellent target complementarity is exhibited, and prospects of model selection are good for cross-sections just below current limits



Ge and Xe together may be able to distinguish the energy dependence class of the interactions



Mass reconstruction can be good if the correct underlying model is chosen (Ge, Xe, F)



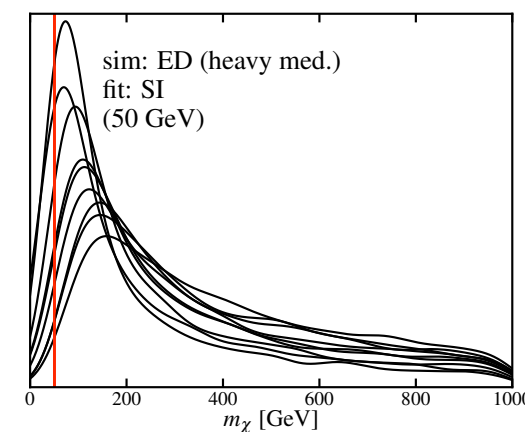
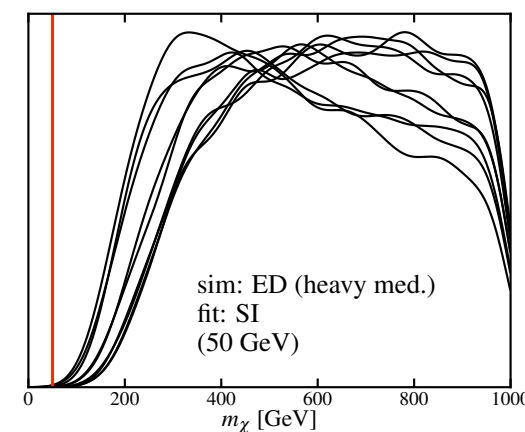
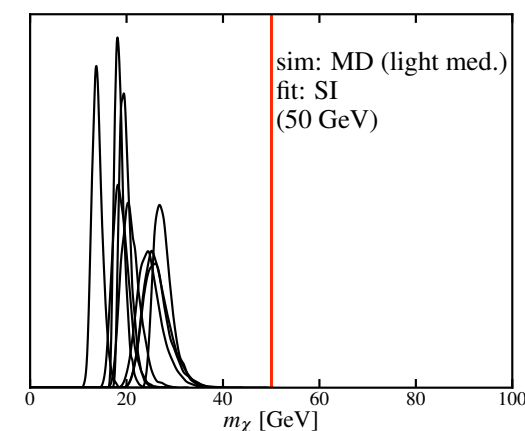
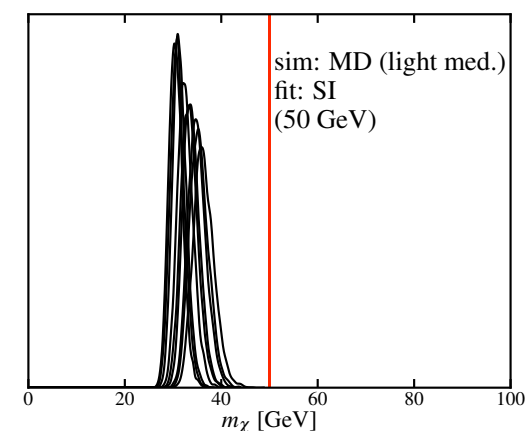
Lower mass fits are better as well

As expected, it is not as accurate if the wrong model is fit

Fit model then reconstruct mass

Xe

Ge



Annual Modulation

Annual Modulation

Annual Modulation

Annual Modulation

Annual Modulation

Annual Modulation

Annual Modulation

Annual Modulation

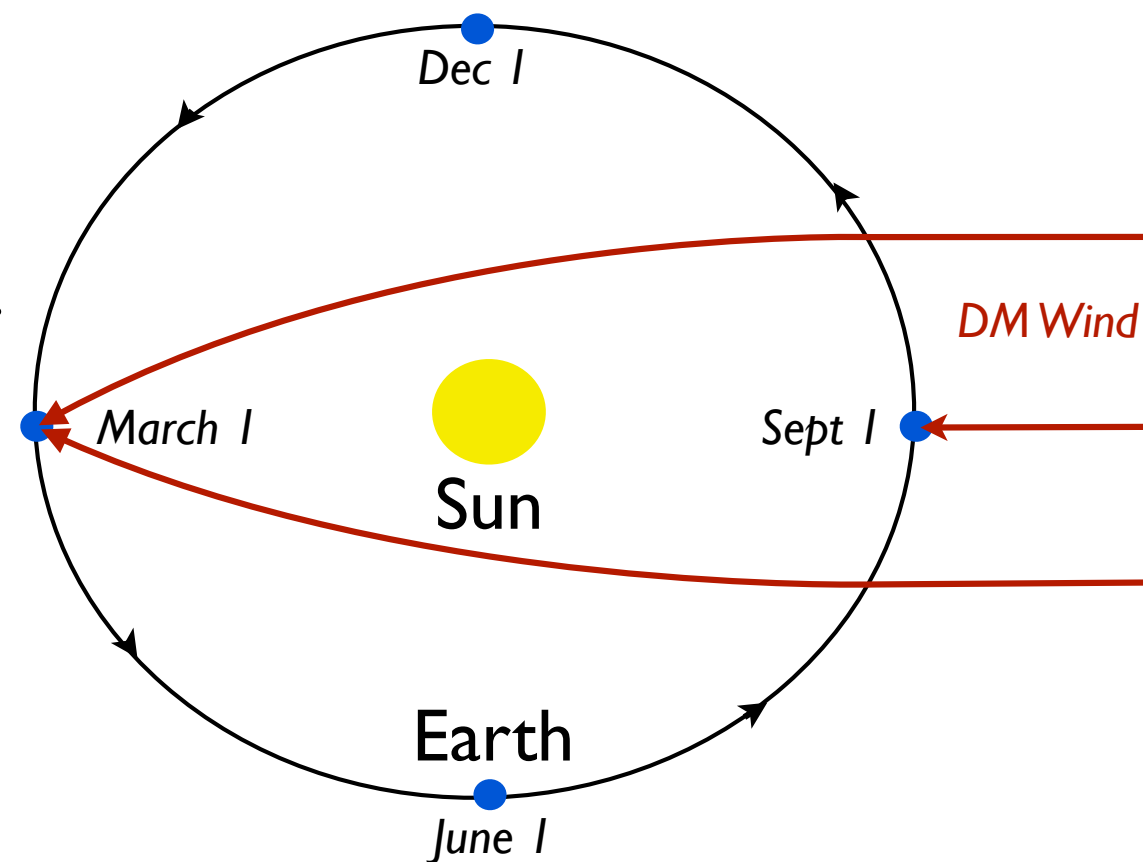
Annual Modulation

As the Earth moves around the Sun, the nuclear recoil rate due to dark matter interactions acquires a time dependence (annual modulation)

$$\frac{dR_T}{dE_R}(E_R, t) = S_0(E_R) + S_m(E_R) \cos\left(\frac{2\pi}{1 \text{ year}}(t - t_0)\right)$$

Other mechanisms such as gravitational focusing can have a significant impact on the phase of the modulation, which can vary depending on v_{min}

This can in turn create interesting effects for some velocity dependent interactions.



M.S. Alenazi and P. Gondolo, PRD **74** (2006) astro-ph/0608390

S.K. Lee, M. Lisanti, and B.R. Safdi, JCAP **1311** (2013) arXiv:1307.5323

E. Del Nobile, G.B. Gelmini, and S.J. Witte, JCAP **1508** (2015) arXiv:1505.07538

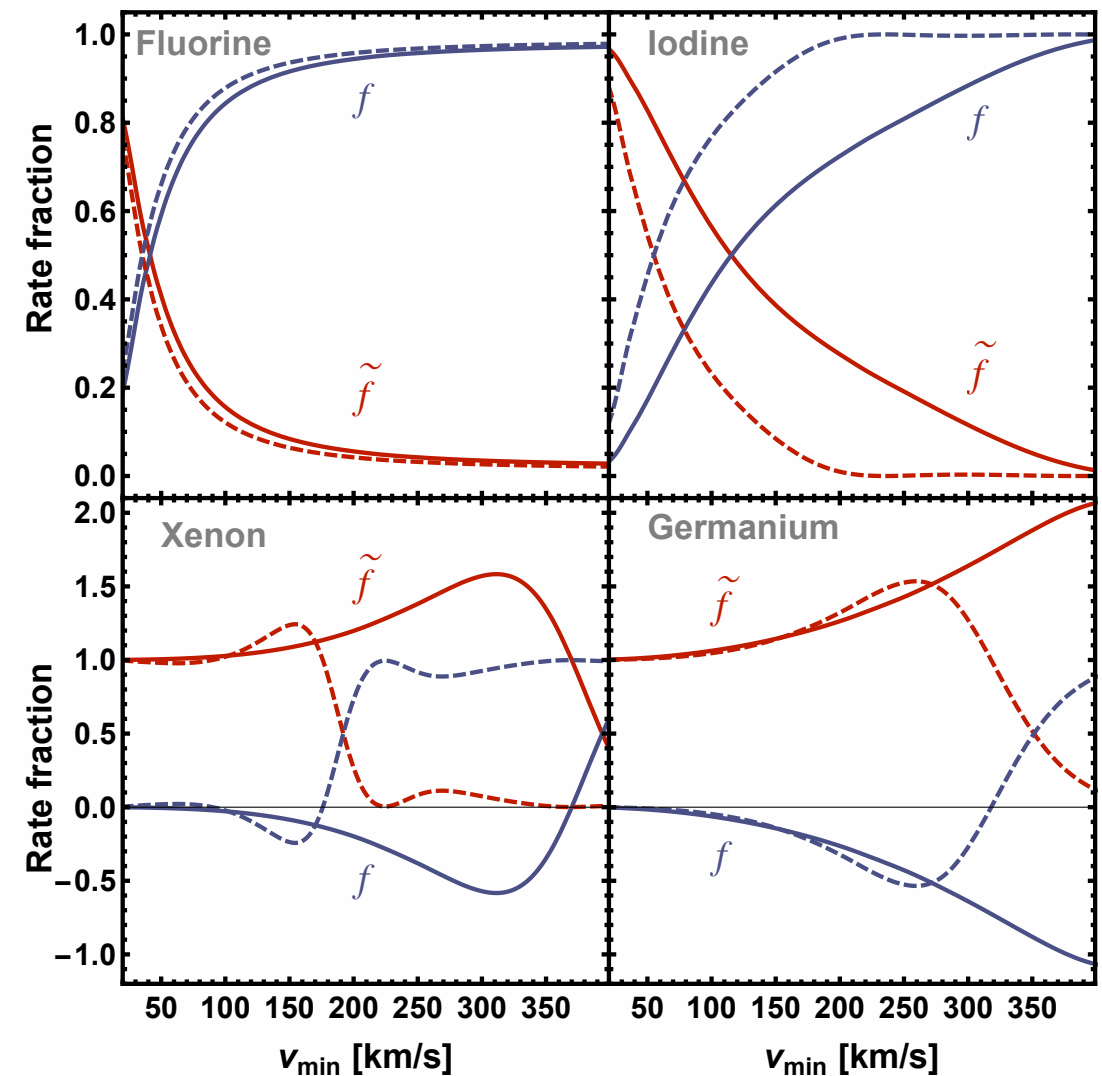
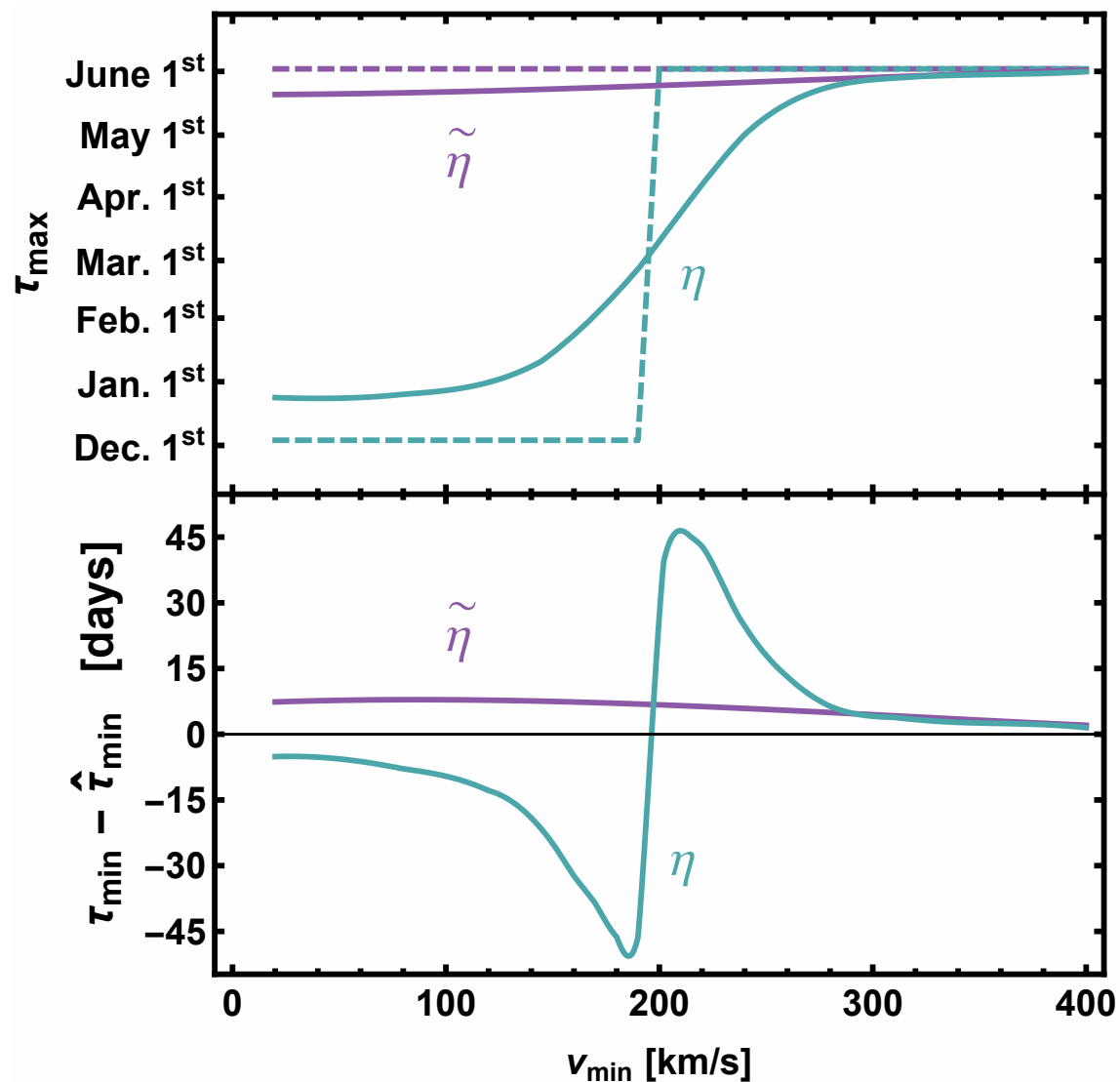
S.K. Lee, M. Lisanti, A.H.G. Peter, and B.R. Safdi, PRL **112** (2014) arXiv:1308.1953

An example $\mathcal{L} = (\lambda_\chi/2) \bar{\chi} \sigma_{\mu\nu} \chi F^{\mu\nu}$

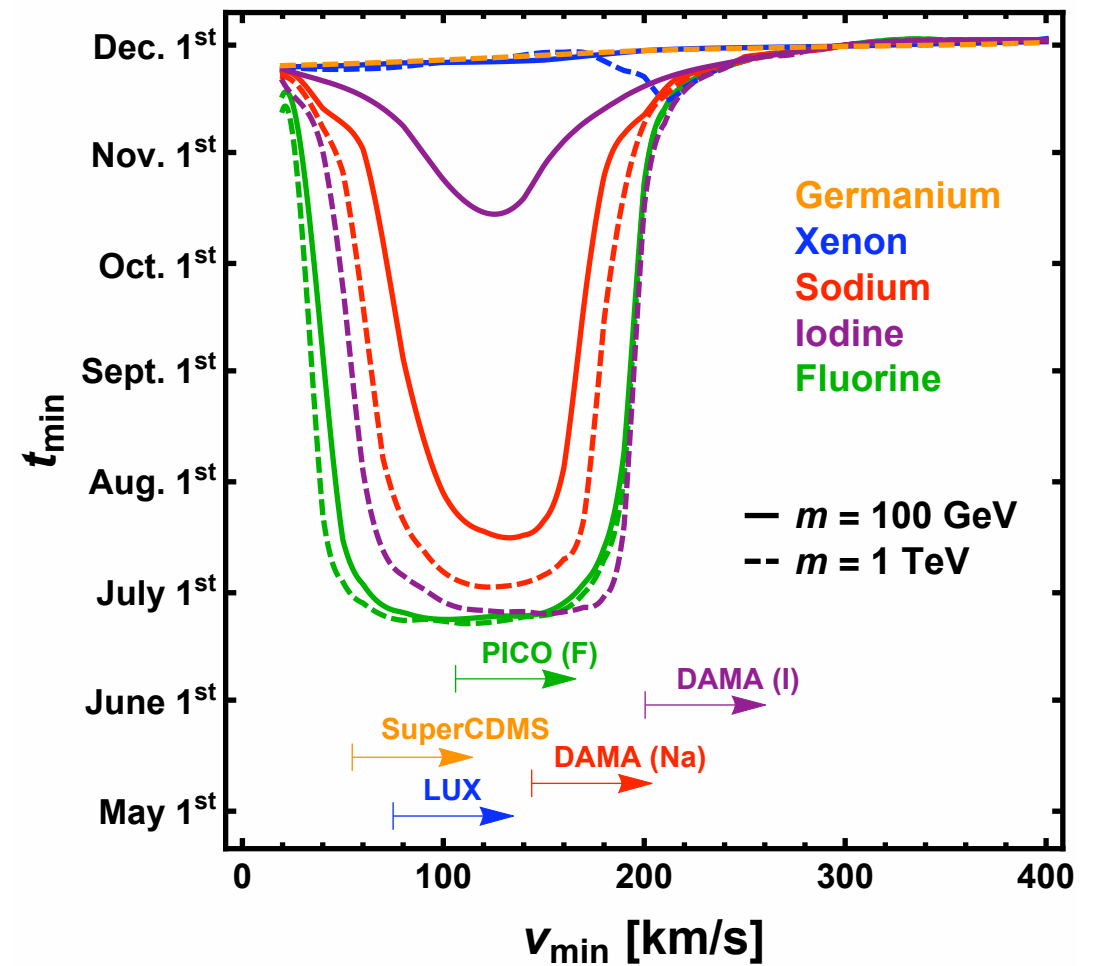
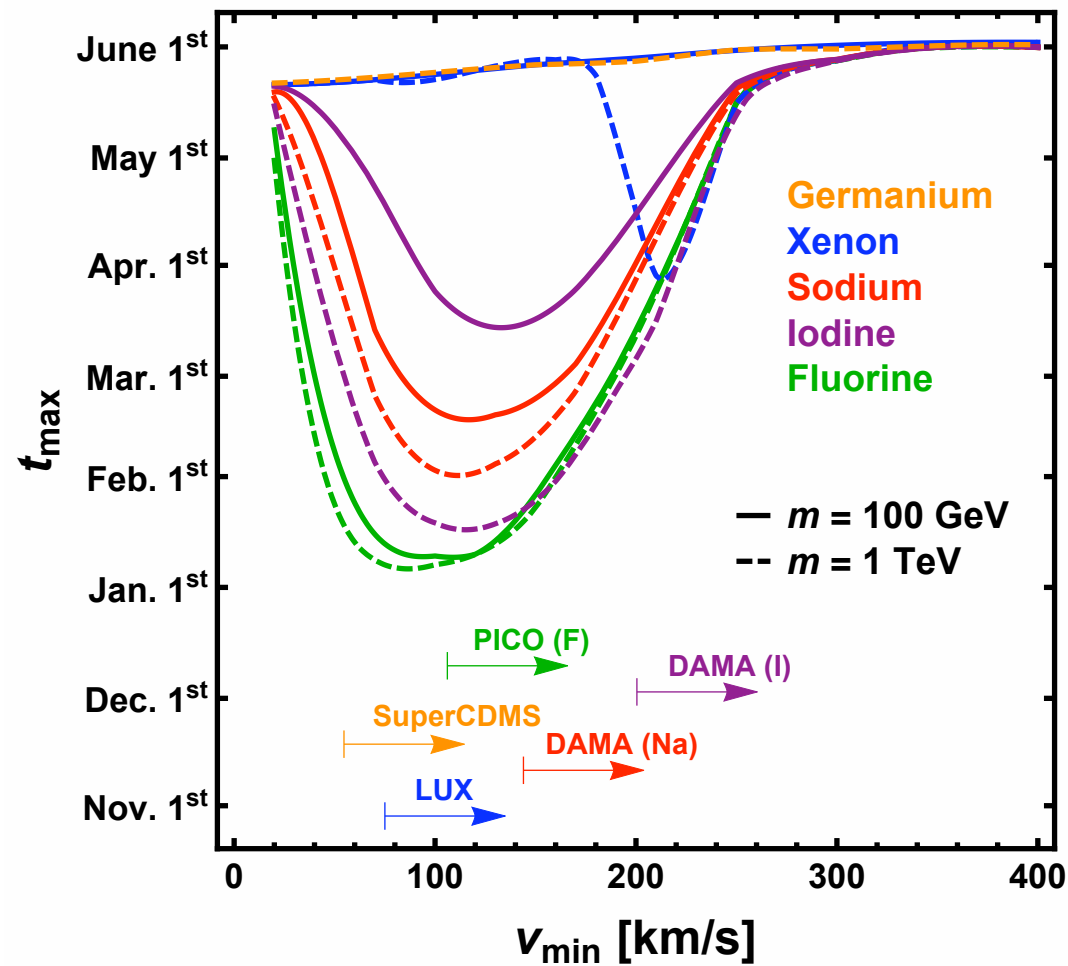
$$\frac{d\sigma_T}{dE_R}(v_{\min}, v) = \alpha \lambda_\chi^2 \left\{ Z_T^2 \frac{m_T}{2\mu_T^2} \left[\frac{1}{v_{\min}^2} - \frac{1}{v^2} \left(1 - \frac{\mu_T^2}{m^2} \right) \right] F_{\text{SI},T}^2(E_R(v_{\min})) + \frac{\hat{\lambda}_T^2}{v^2} \frac{m_T}{m_p^2} \left(\frac{S_T + 1}{3S_T} \right) F_{\text{M},T}^2(E_R(v_{\min})) \right\}$$

$$\tilde{\eta}(v_{\min}, t) \equiv \int_{v \geq v_{\min}} v f(\mathbf{v}, t) d^3v$$

$$\eta(v_{\min}, t) \equiv \int_{v \geq v_{\min}} \frac{f(\mathbf{v}, t)}{v} d^3v$$



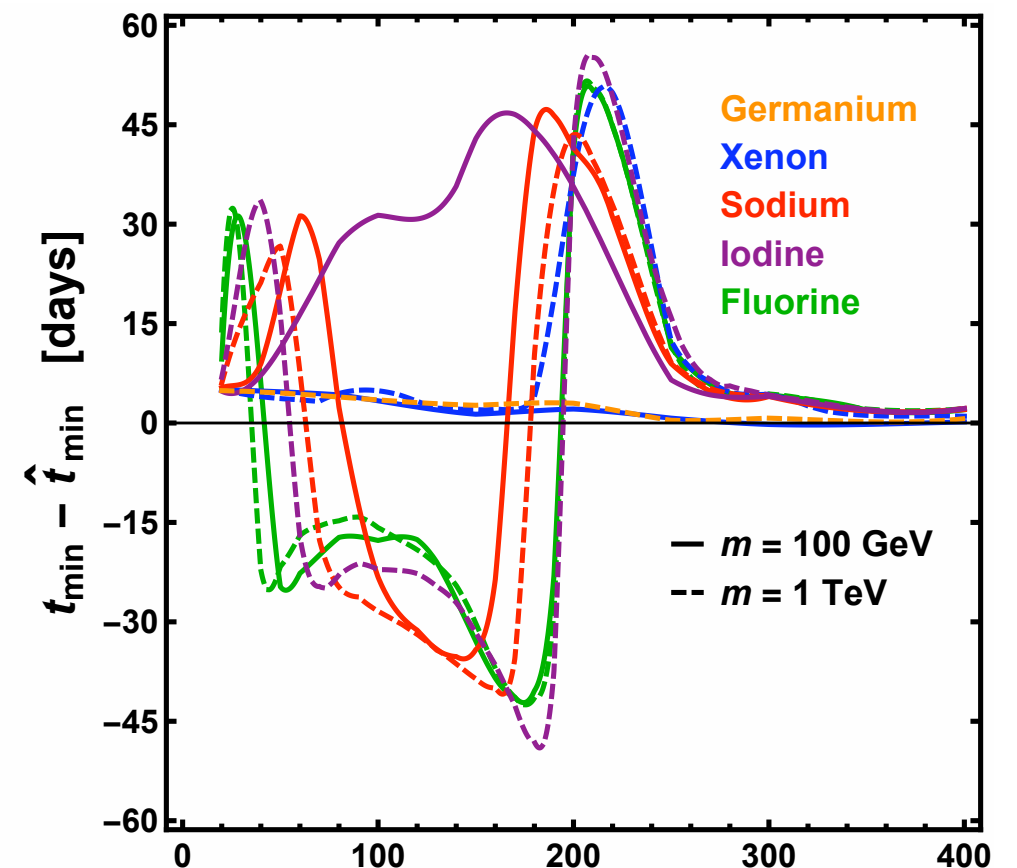
$$\tilde{f} \equiv \tilde{r}/(r + \tilde{r}) \quad f \equiv r/(r + \tilde{r})$$



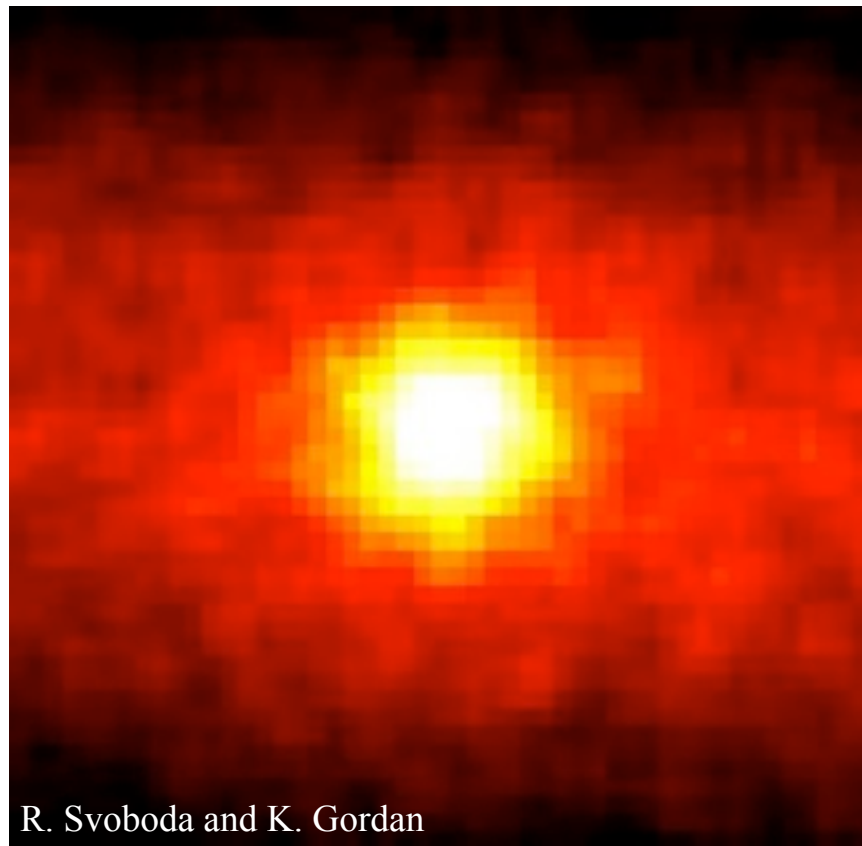
Target dependence for the time of maximum and minimum scattering rate

Difference between the time of minimum scattering rate and six months from the maximum time as a function of target element.

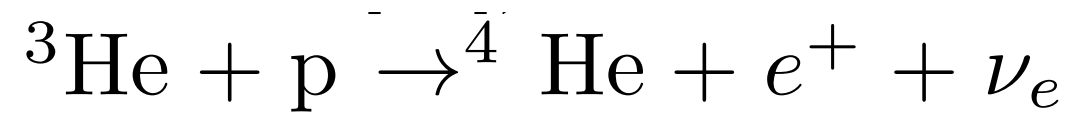
Factorizability of the velocity dependence of the cross-section could possibly be determined from multiple experiments



The Neutrino Floor



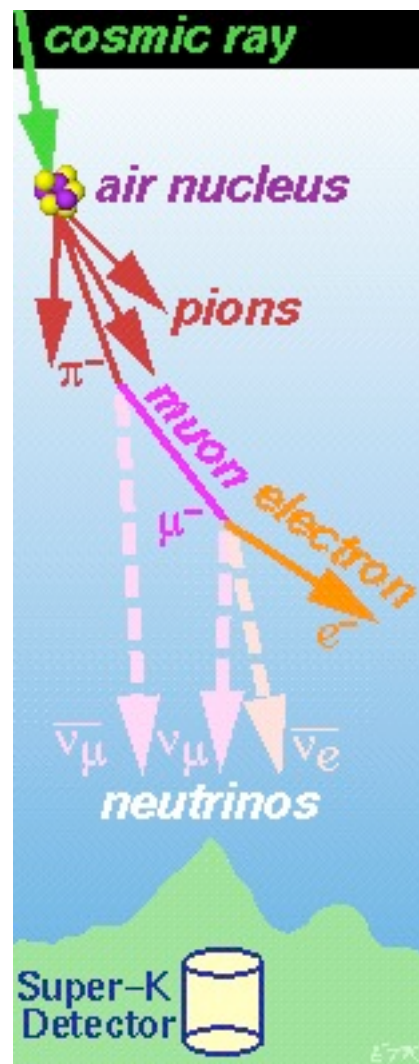
Solar neutrinos



electron capture on ${}^7\text{Be}$

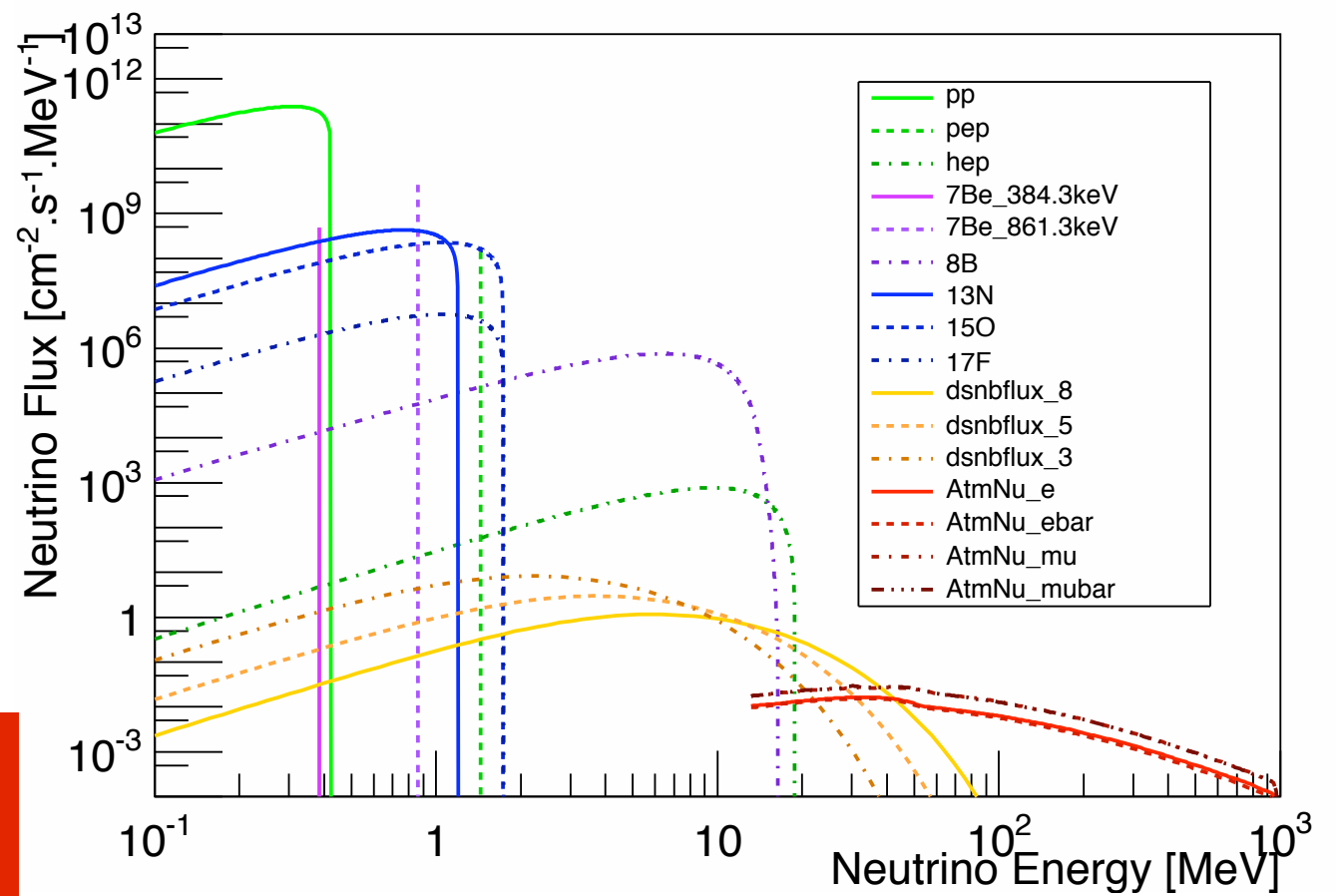
neutrinos from the CNO cycle

Solar
neutrinos

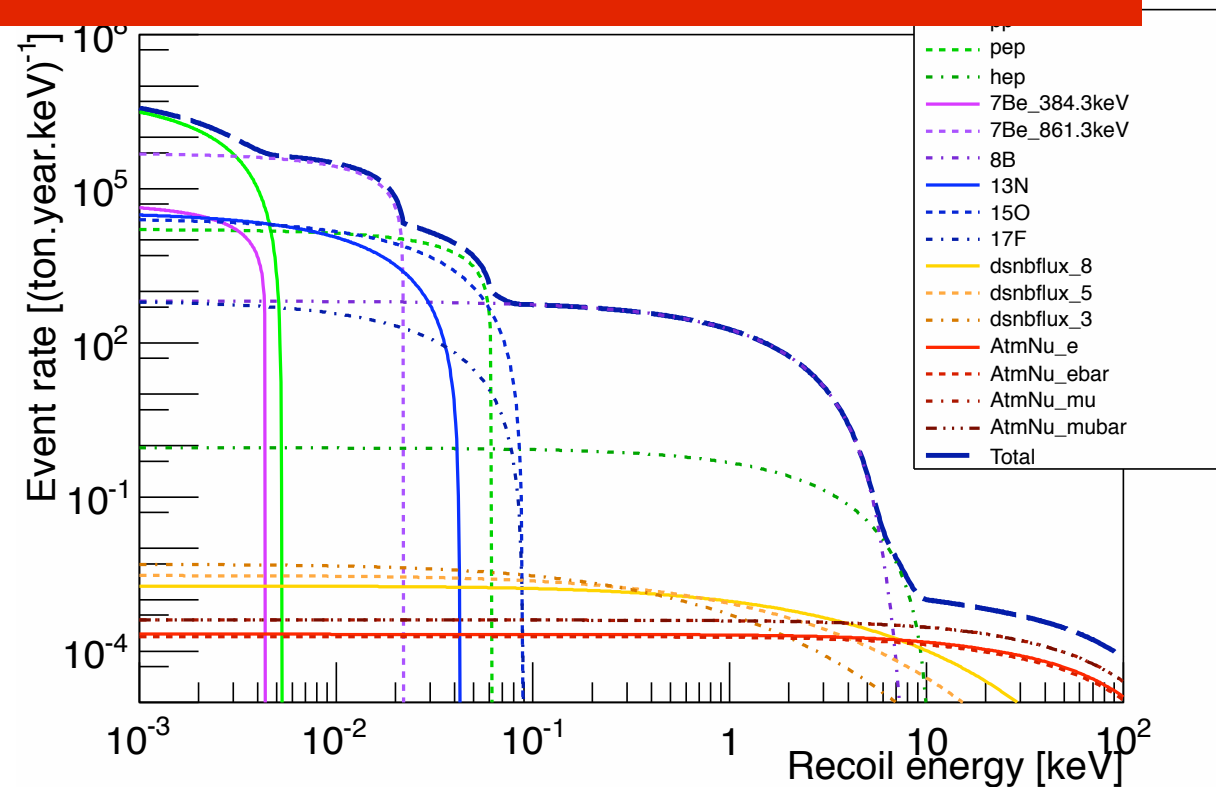


Diffuse SN background

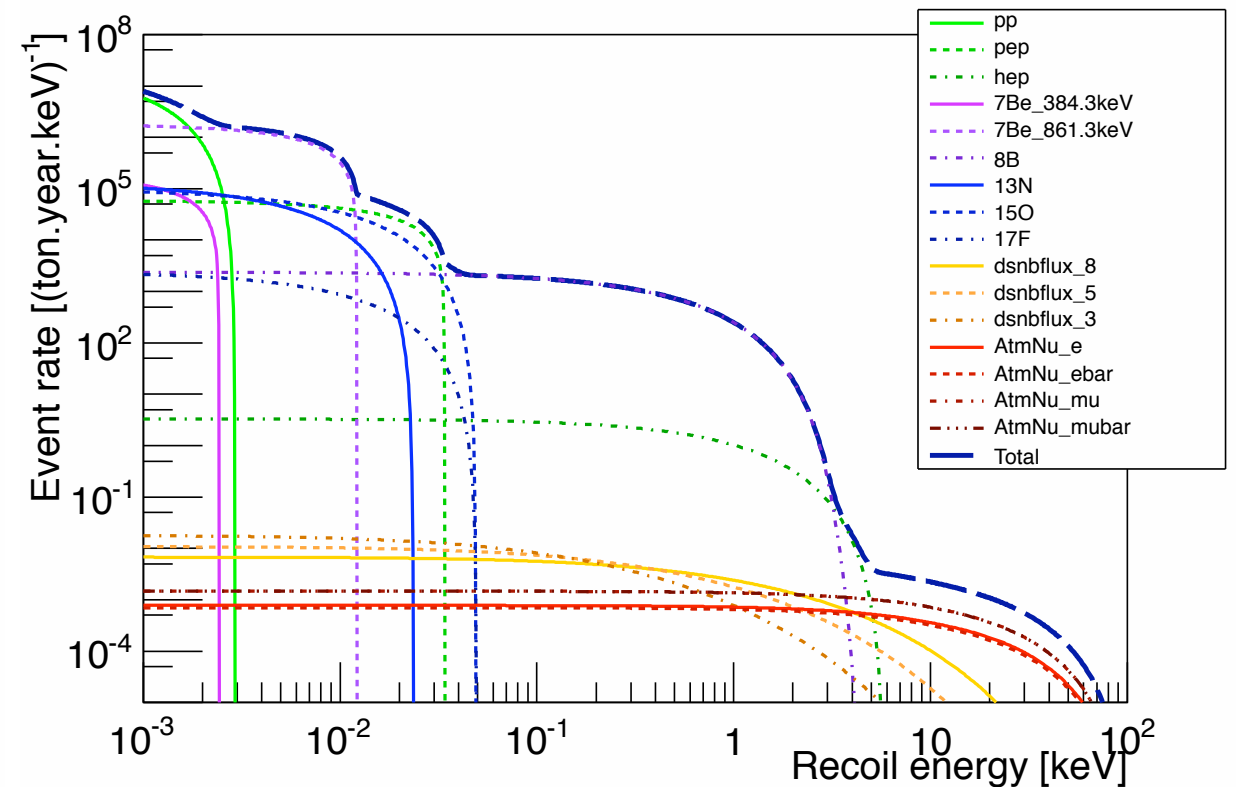
Neutrino Fluxes from each source



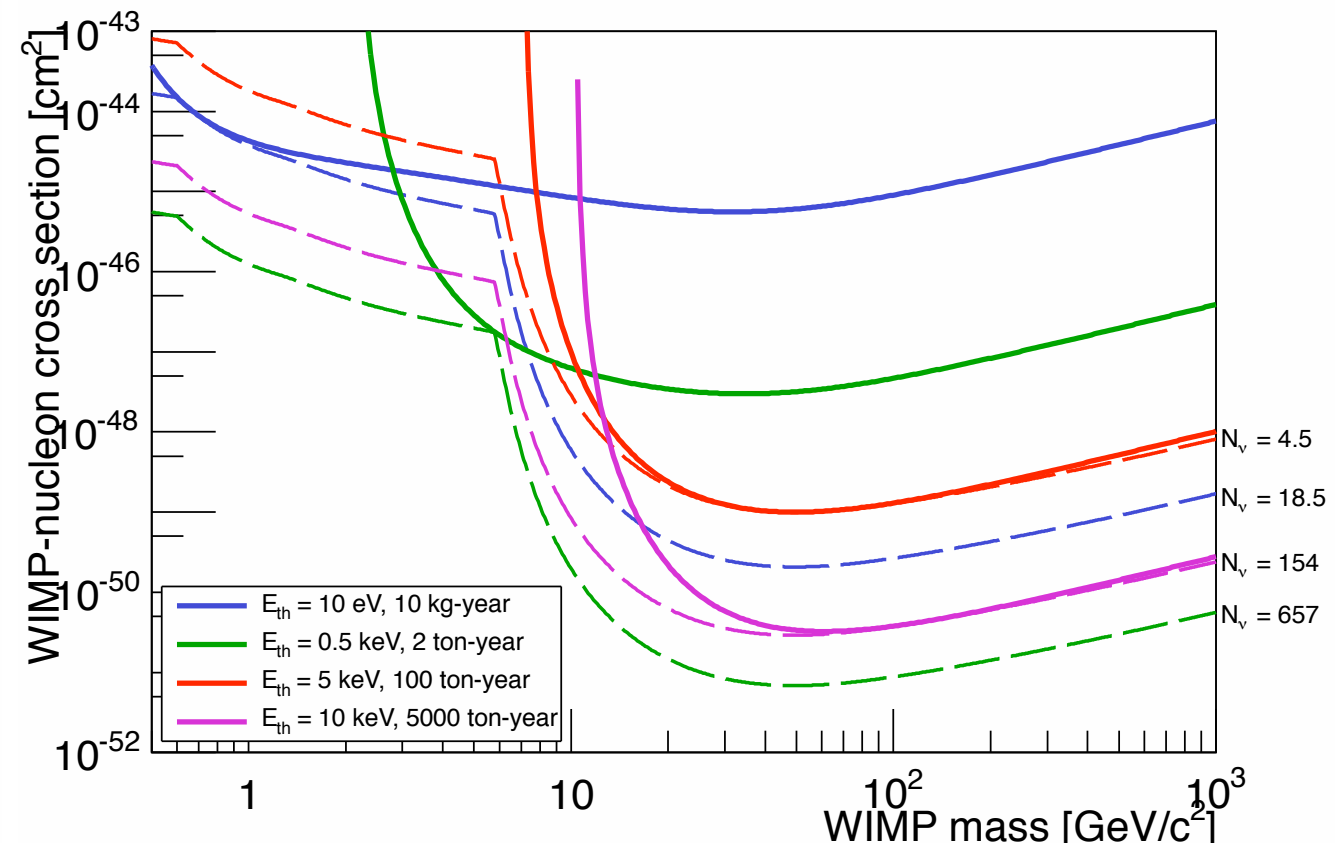
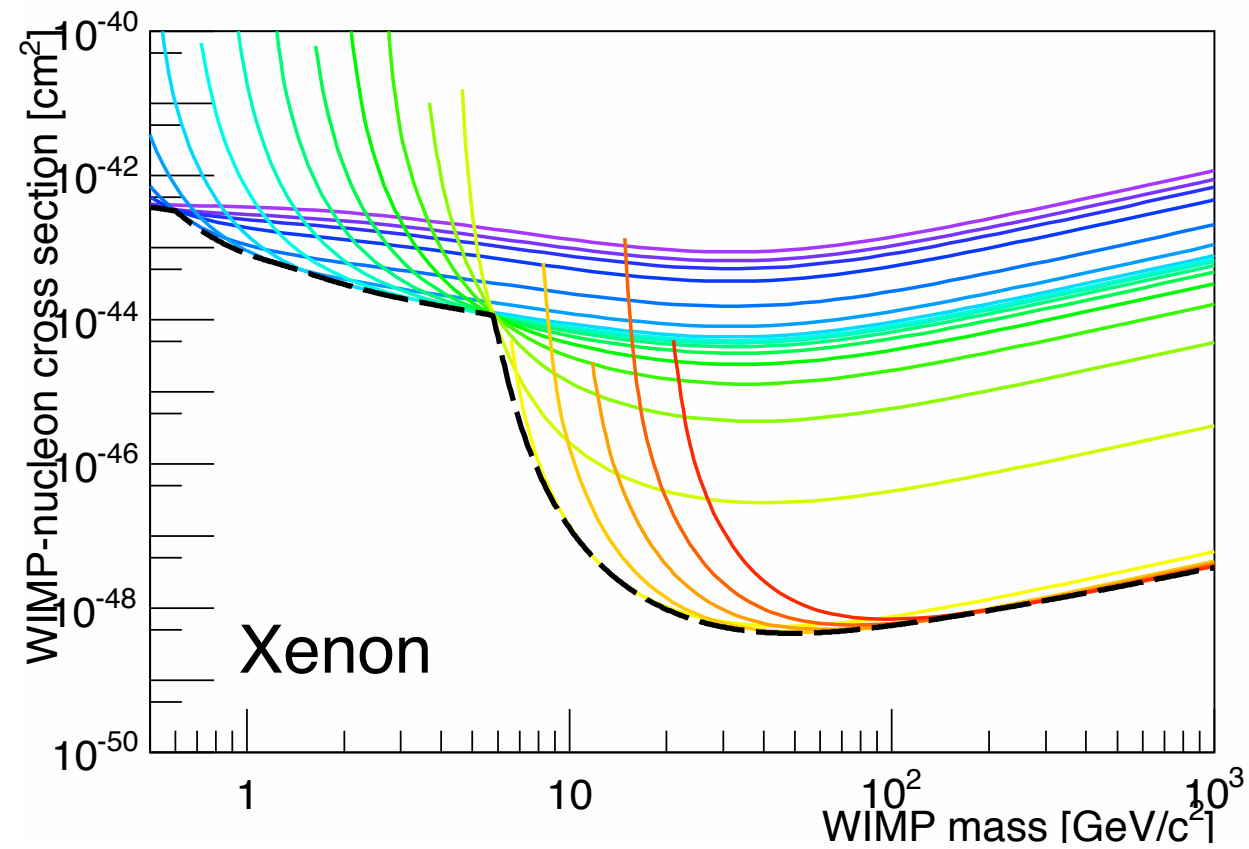
Recoil spectra due to neutrinos



Germanium

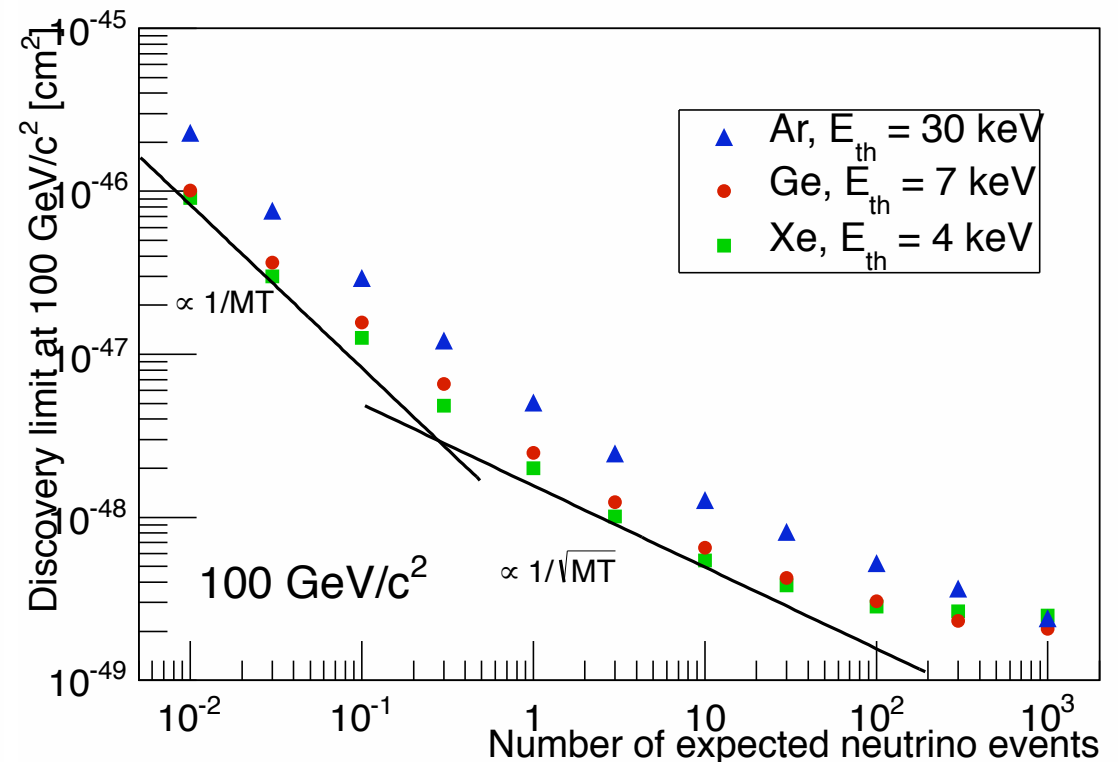
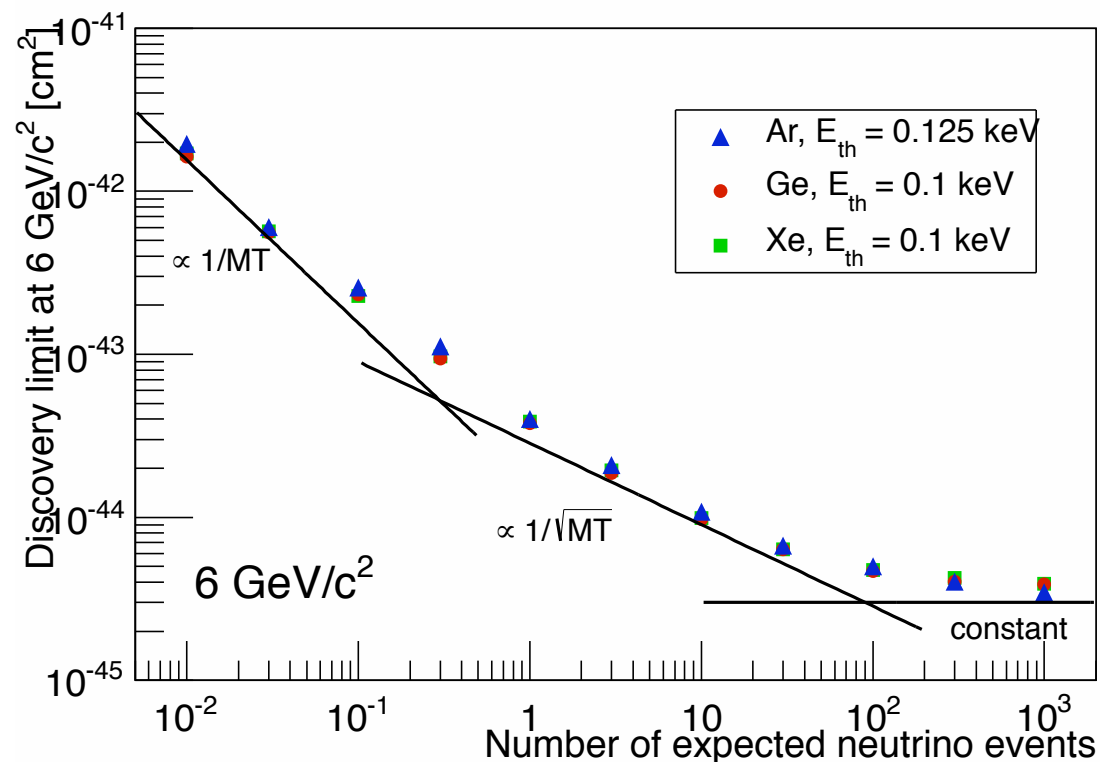


Xenon



Sensitivity curves for Xenon

Reach is a neutrino background of one event obtained for various thresholds (.001 keV-100 keV) and (background free) threshold/exposure (10 kg-yr-5,000 ton-yr) combinations

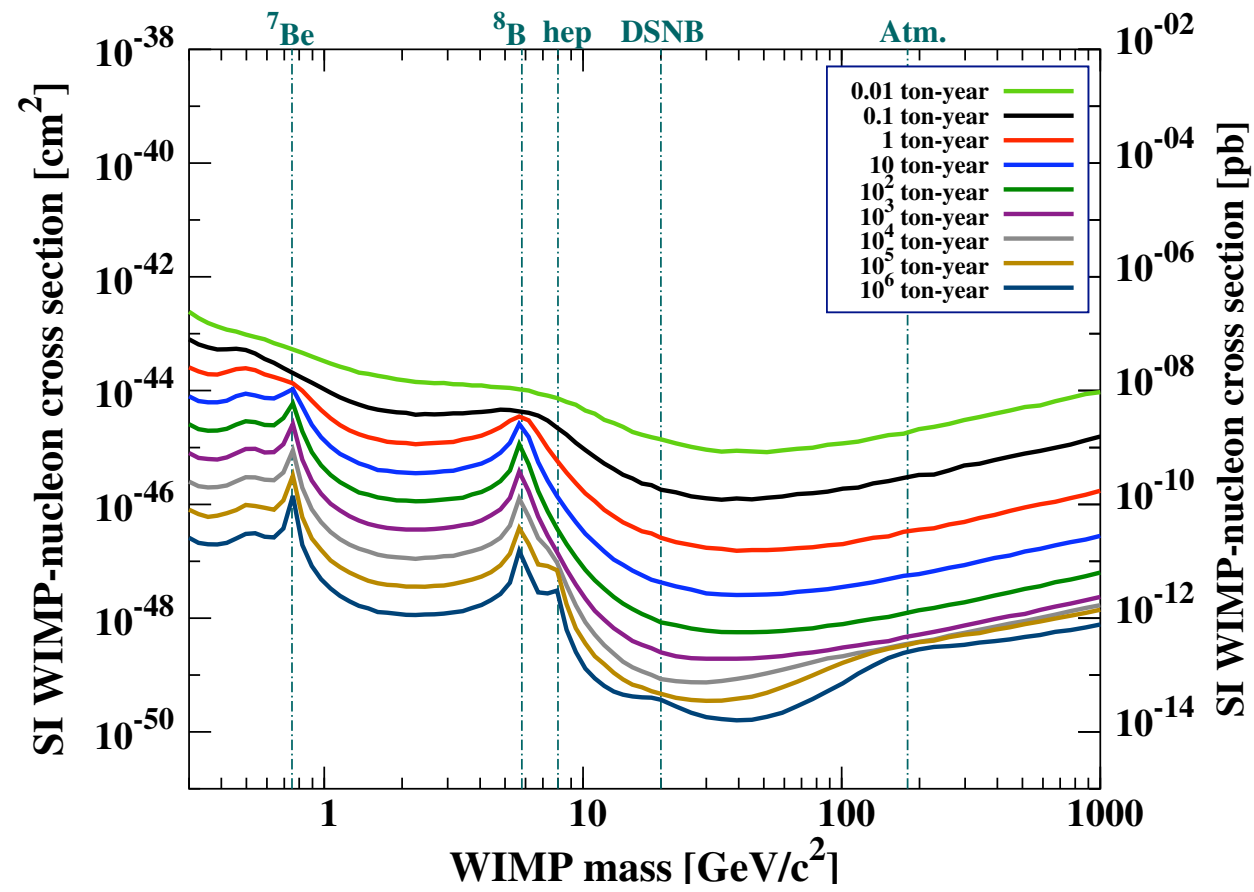
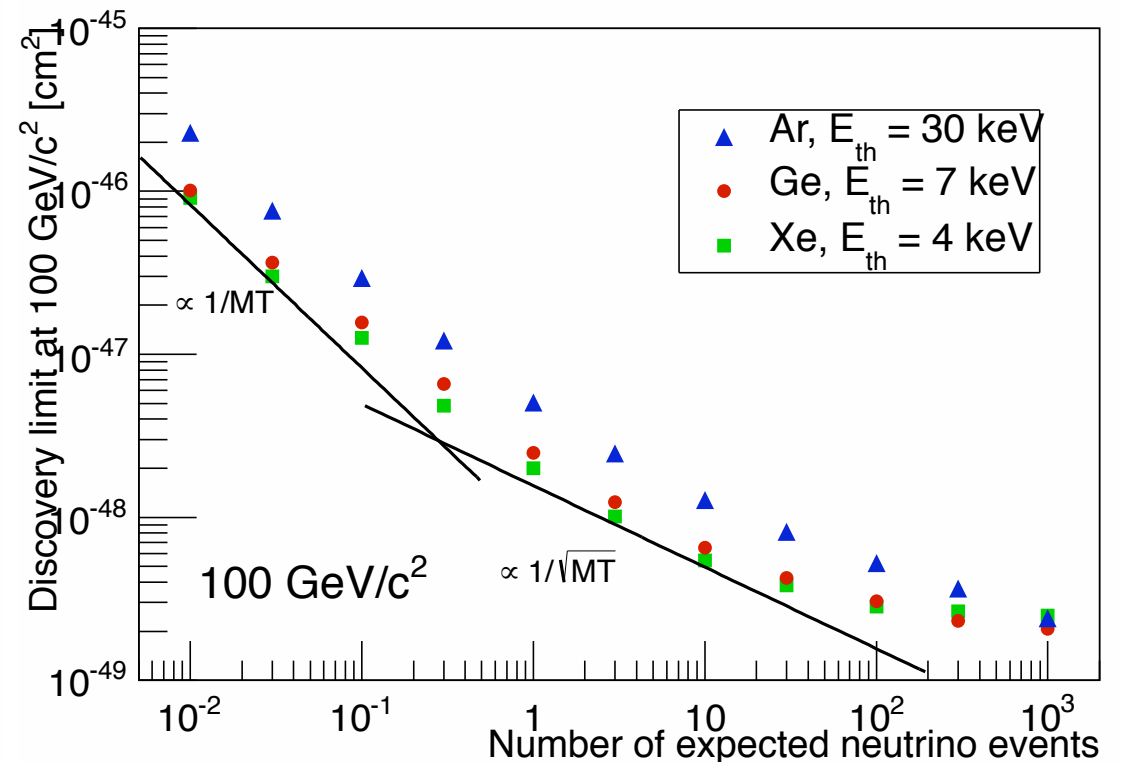
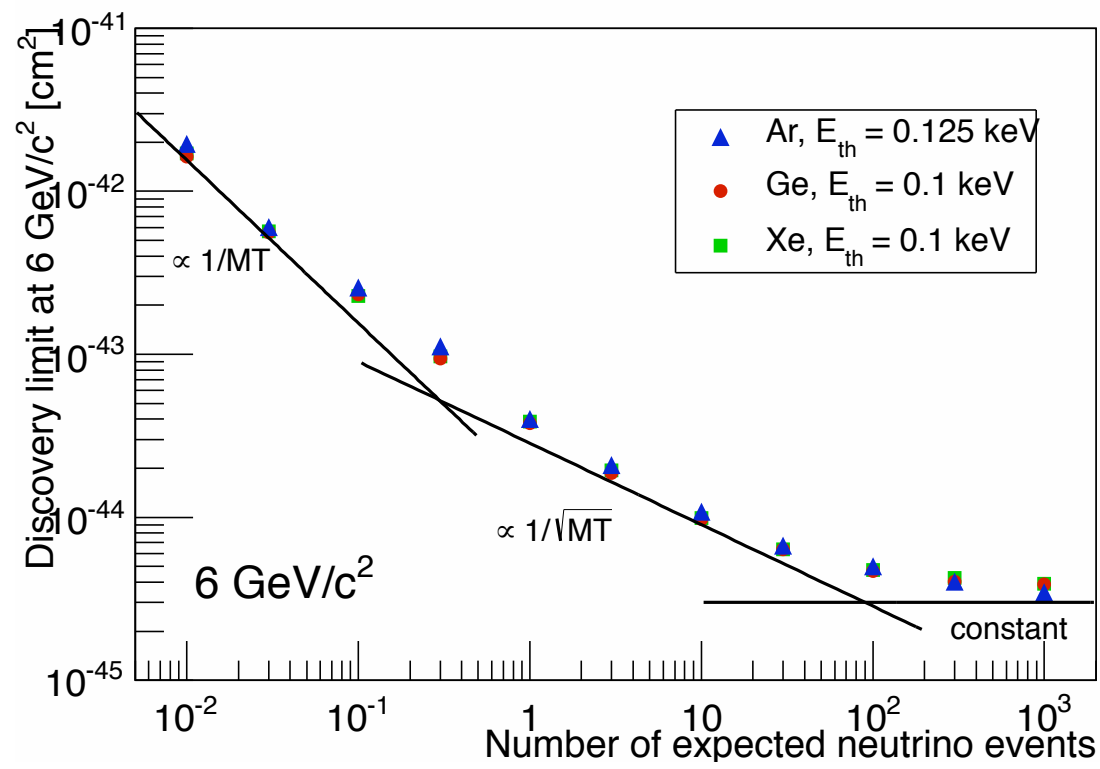


Discovery limits as a function of background neutrino events for Argon, Germanium, and Xenon.

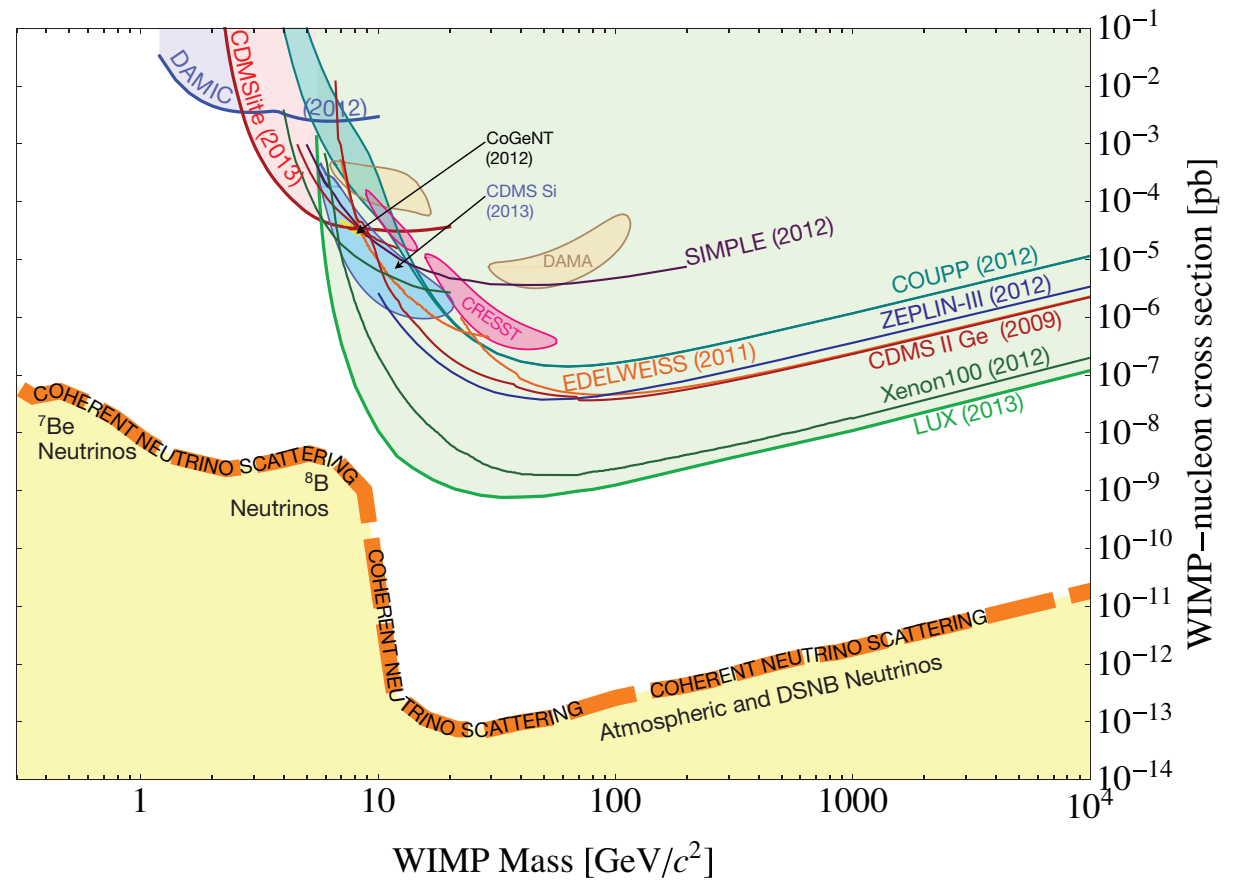
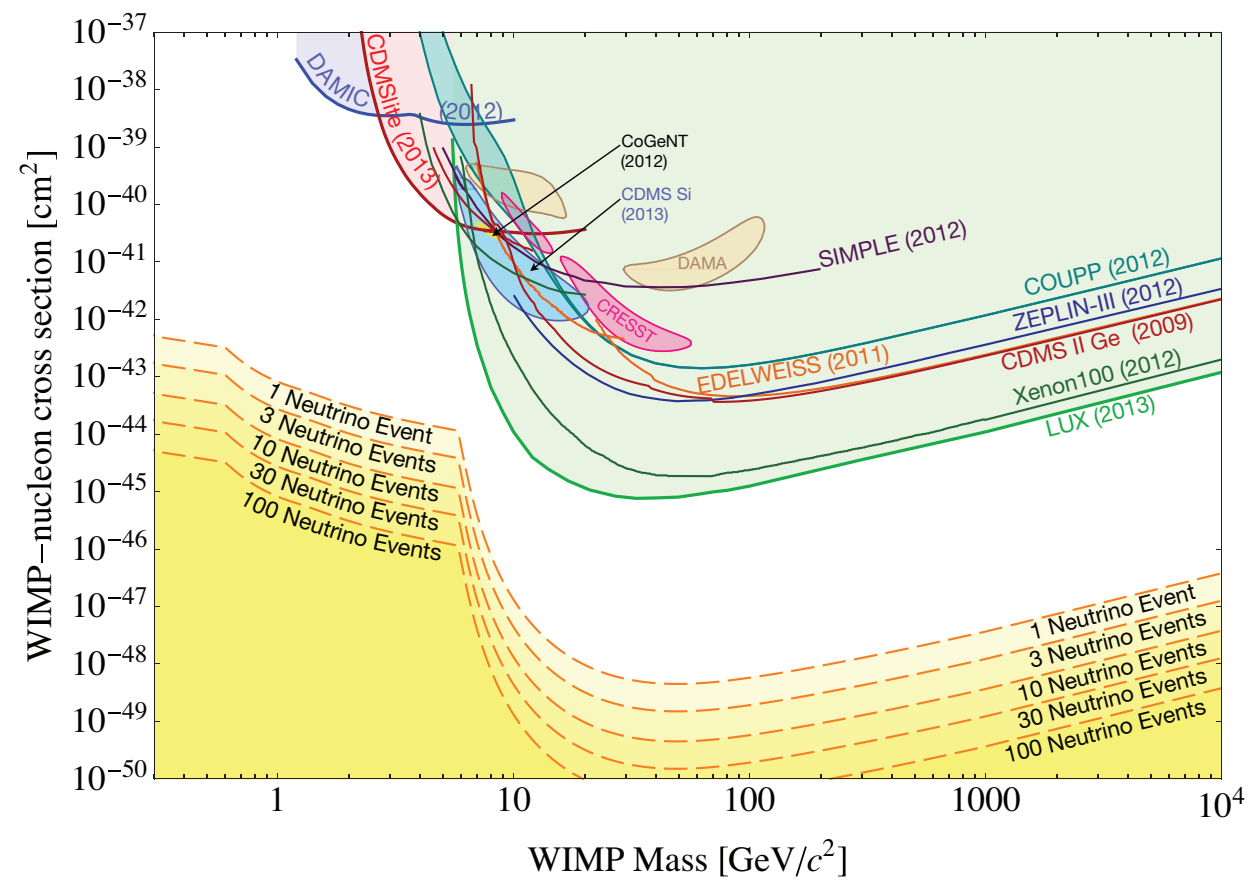
A given experiment has a 90% probability to obtain at least a 3σ detection

6GeV WIMP: Ge 240 kg-yr, Xe 130 kg-year, Ar 430 kg-yr

100GeV WIMP: Ge 32.5 ton-yr, Xe 21.5 ton-year, Ar 98 ton-yr



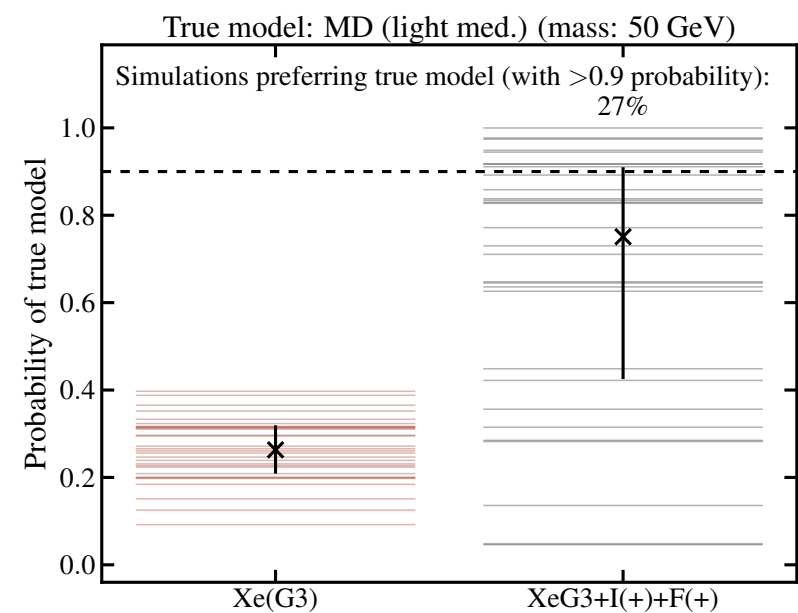
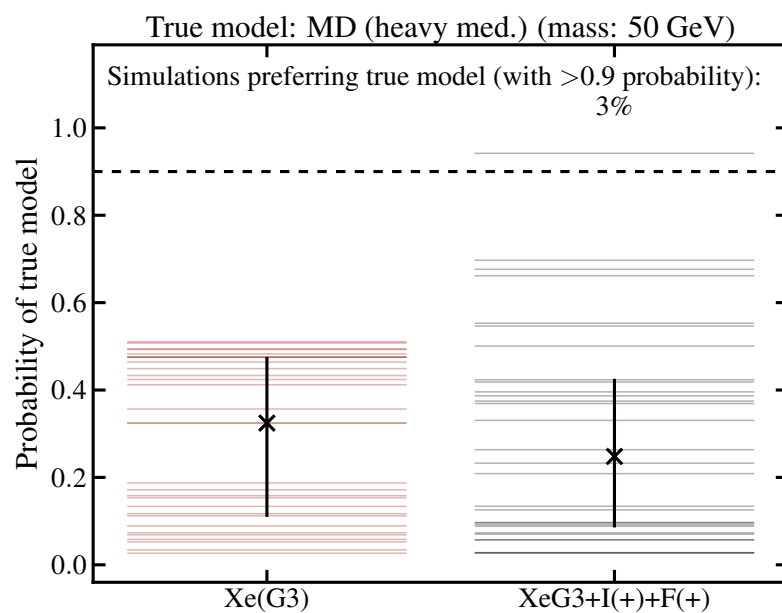
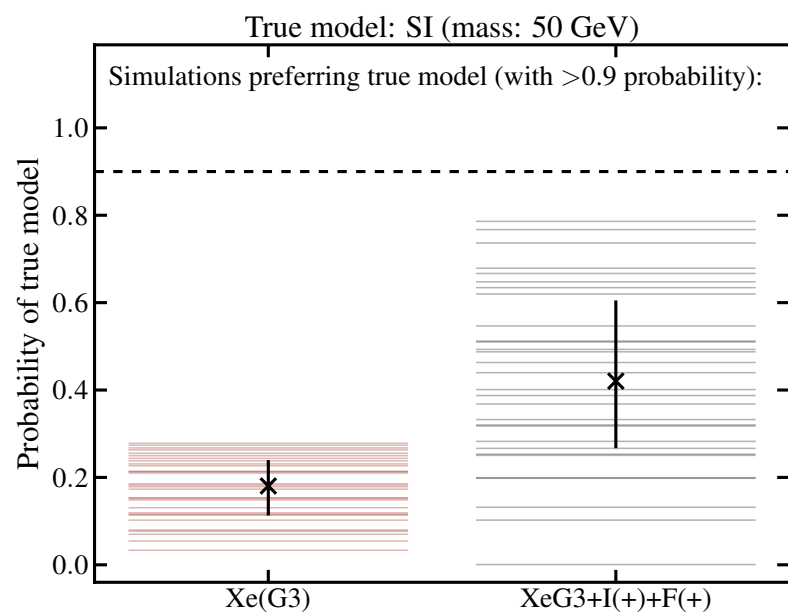
Discover limit for Xenon



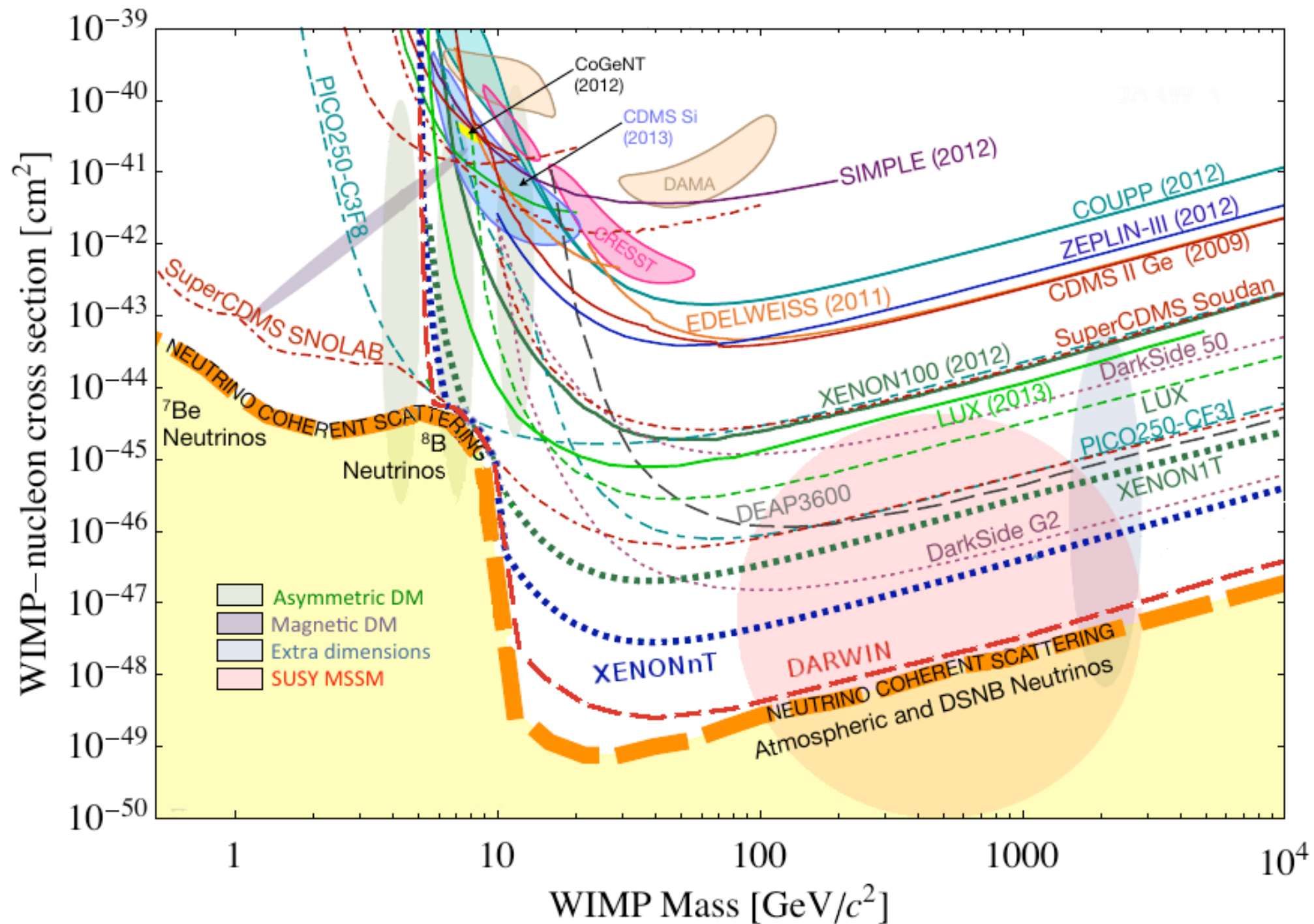
The direct detection limits after LUX along with the neutrino background

Right: combined discovery limits of two Xe-based pseudo-experiments with threshold of 3 eV and 4 keV, 500 neutrino events.

Label	A (Z)	Energy window [keVnr]	Exposure [kg-yr]
XeG3	131 (54)	5-40	40 000
I+	127 (53)	1-600	424
F+	19 (9)	3-100	1200



If a signal is not seen at the next generation of experiments, future prospects may be quite diminished



The ultimate reach and extent of direct detection experiments

...perhaps not...

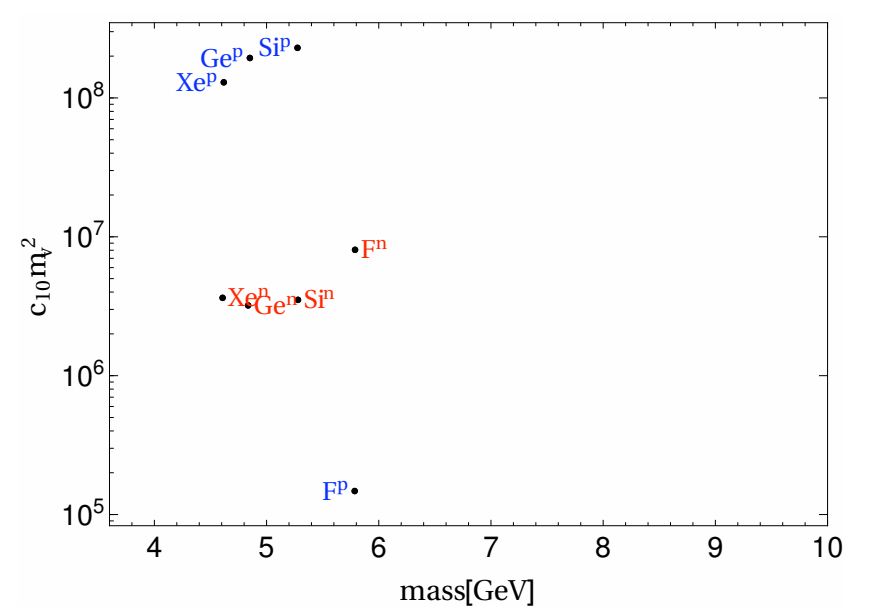
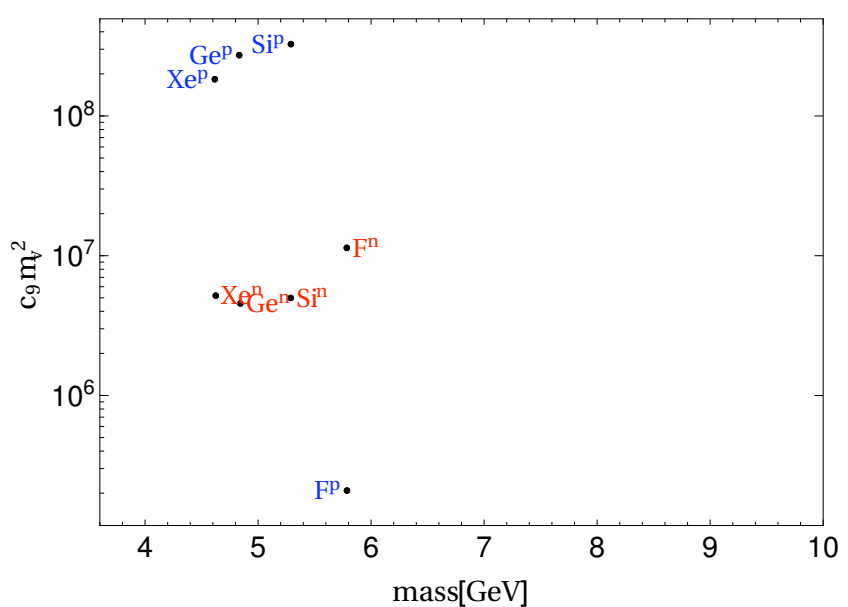
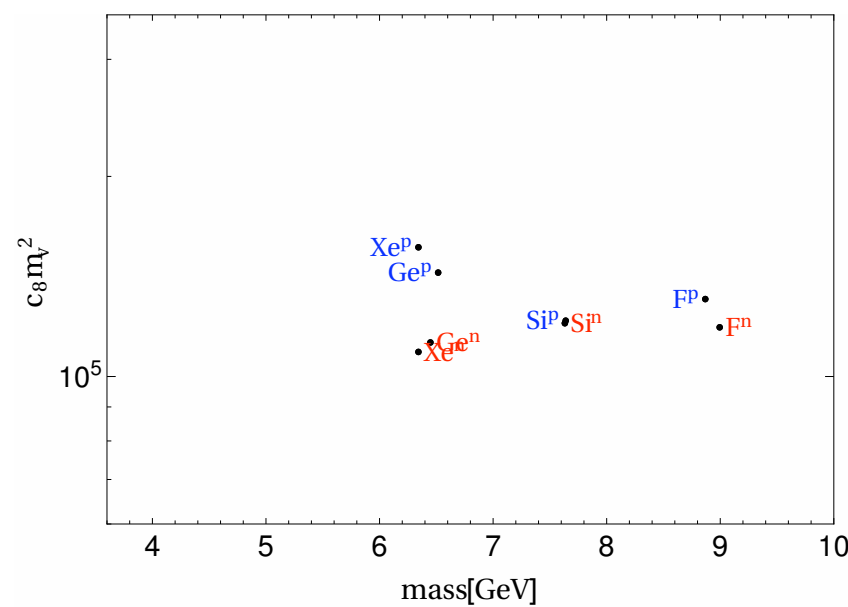
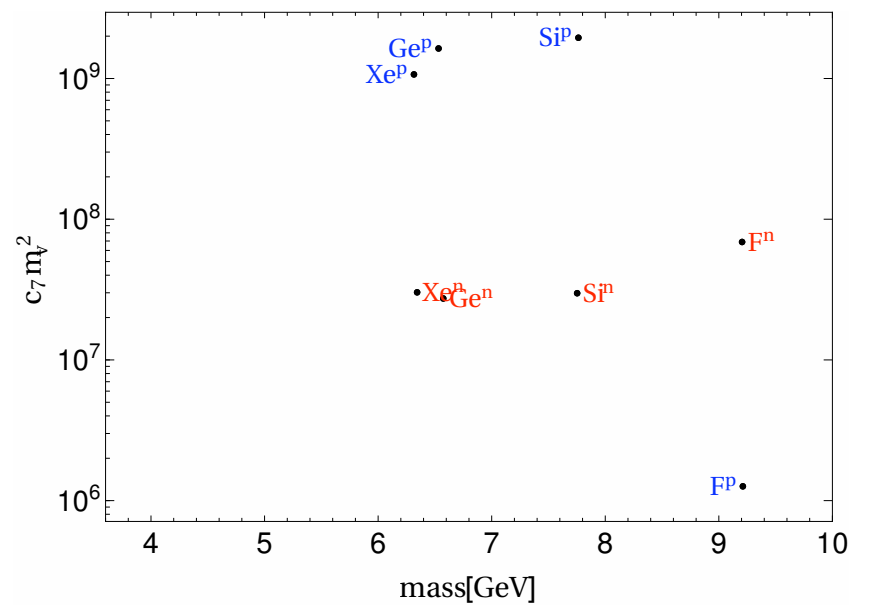
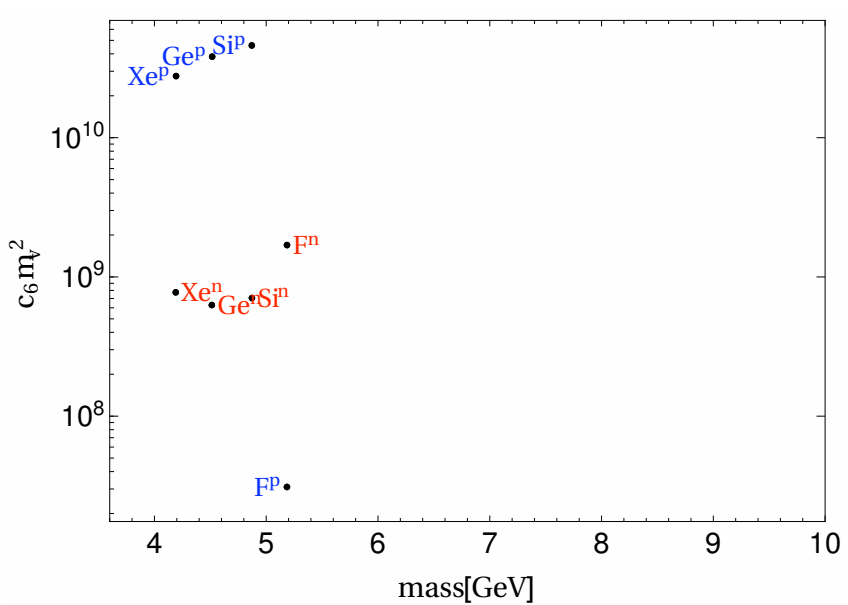
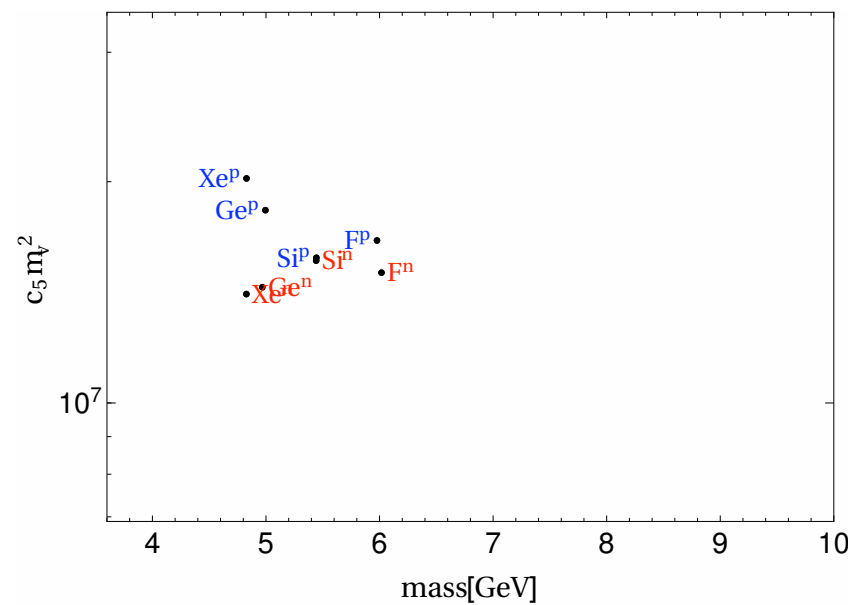
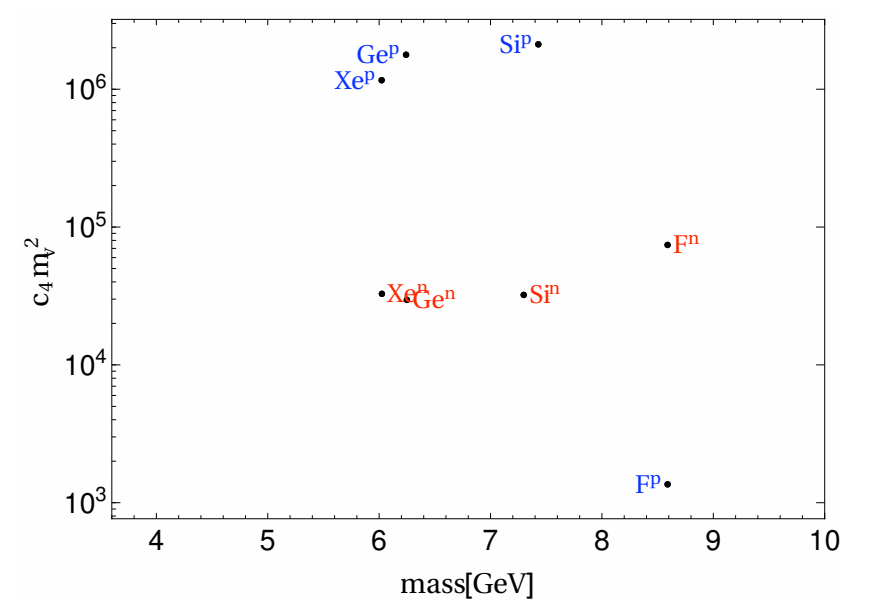
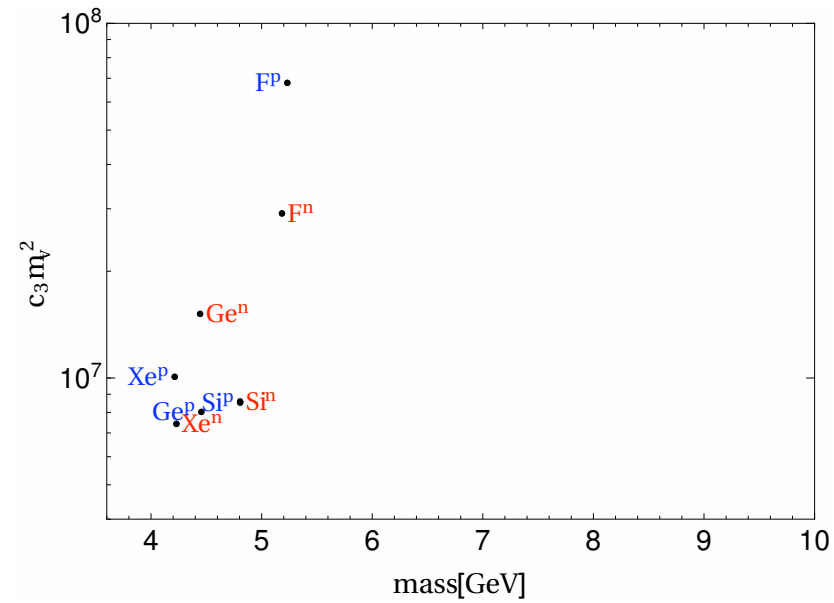
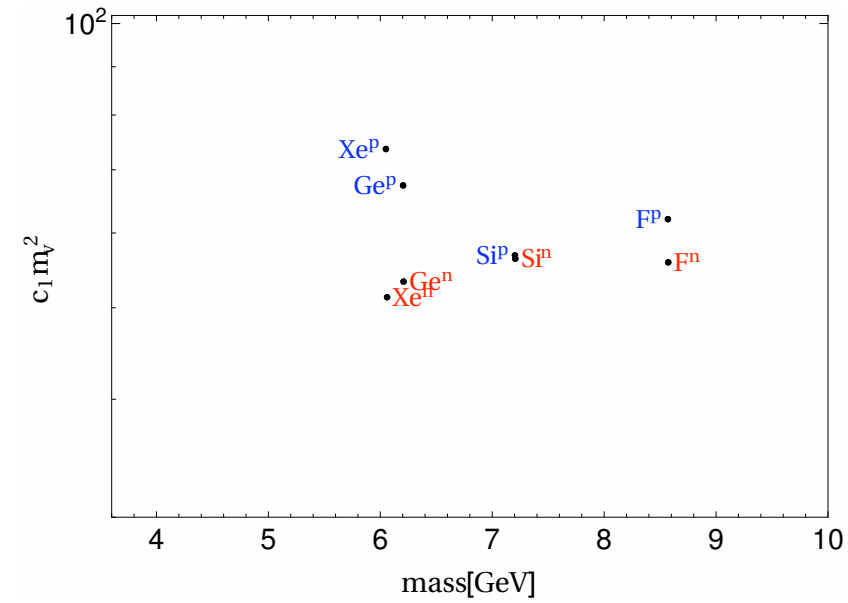
We have fit the various \mathcal{O}_i to the neutrino rate for the 8B neutrino flux, with exposures chosen to give 200 expected neutrino events

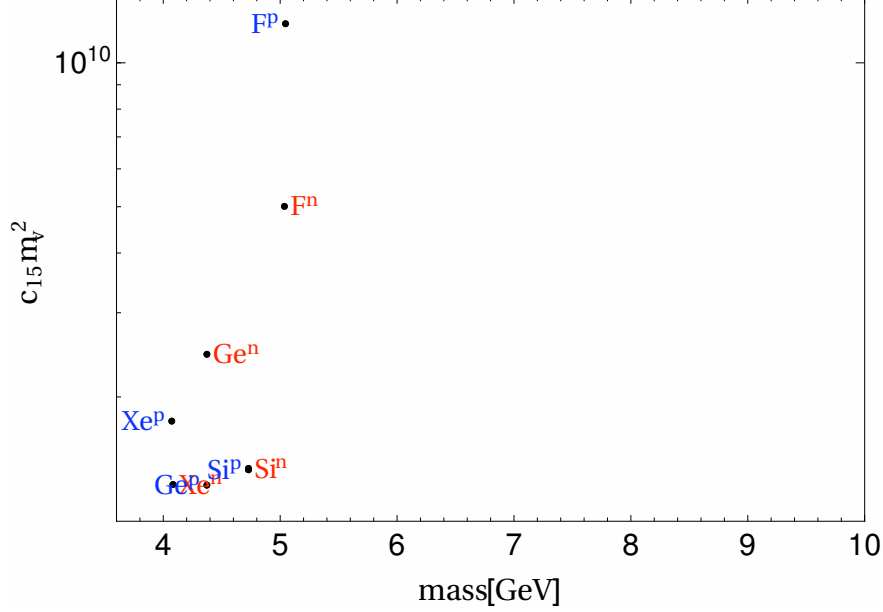
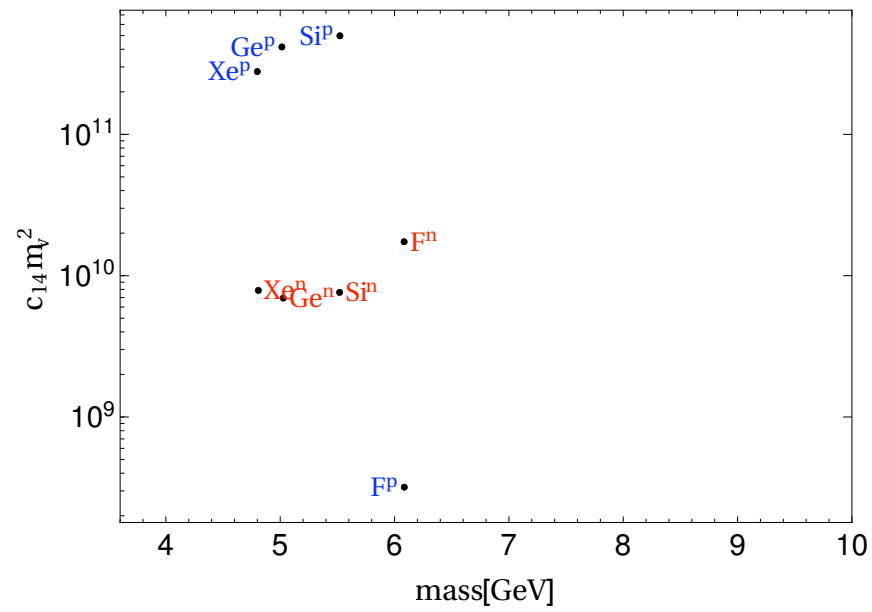
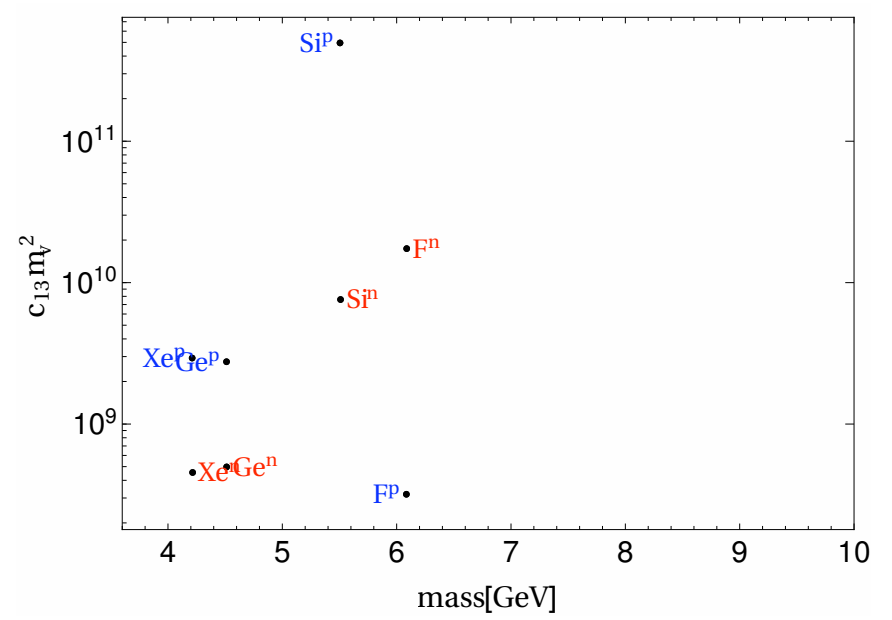
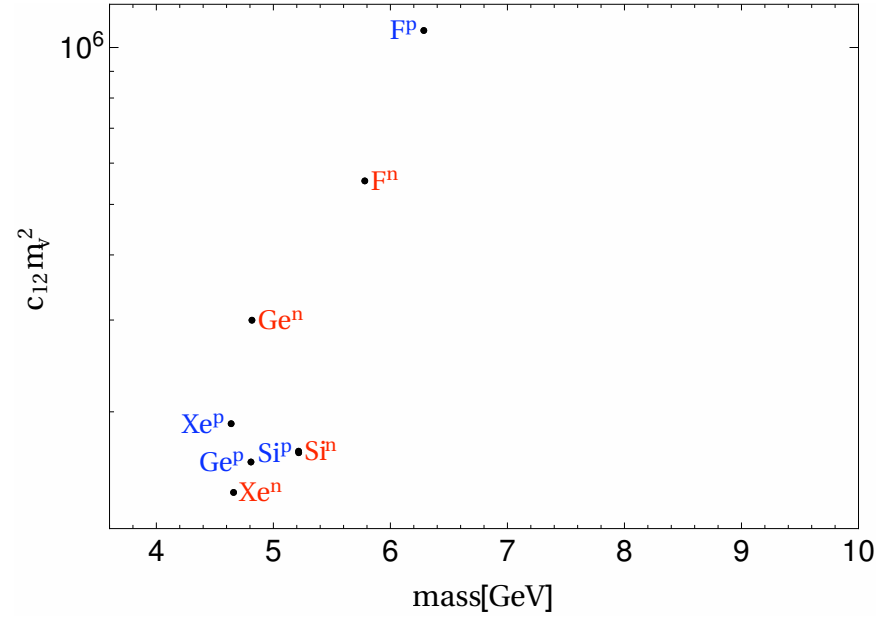
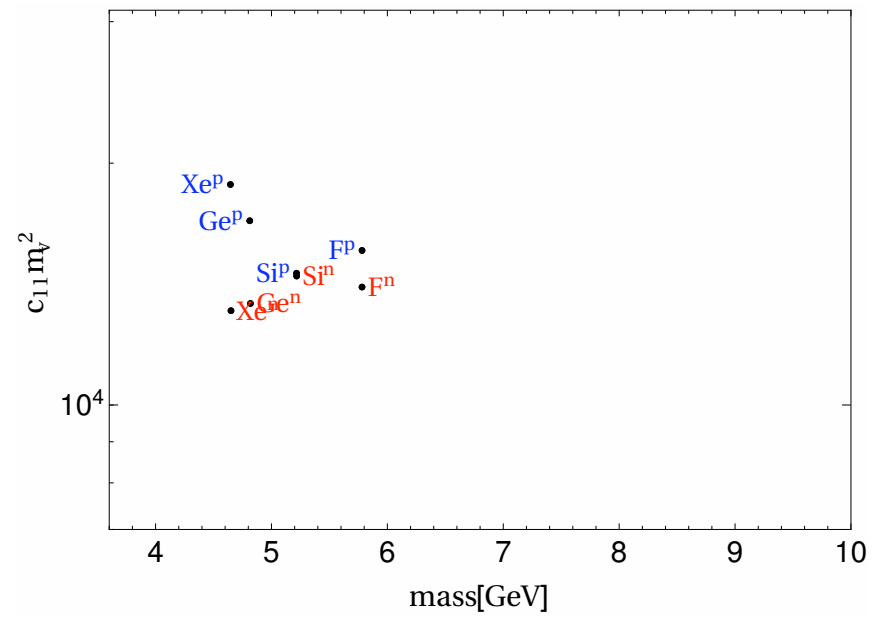
Target	threshold (low/high)
xenon	3.0 eV / 4.0 keV
germanium	5.3 eV / 7.9 keV
silicon	14 eV / 20 keV
flourine	33 eV / 28keV

Fit for Xenon

Operator	Mass (GeV)	Exp. (t.y)
\mathcal{O}_1	6	3.4
\mathcal{O}_4	6	2.8
\mathcal{O}_7	6.2	1.7
\mathcal{O}_8	6.3	3.4
q^2 and $q^2 v_T^2$		
\mathcal{O}_5	4.8	0.47
\mathcal{O}_9	4.6	0.42
\mathcal{O}_{10}	4.6	0.42
\mathcal{O}_{11}	4.6	0.51
\mathcal{O}_{12}	4.6	0.35
\mathcal{O}_{14}	4.8	0.47
$q^2 v_T^2, q^4$ and $q^4 v_T^2$		
\mathcal{O}_3	4.2	0.28
\mathcal{O}_6	4.2	0.37
\mathcal{O}_{13}	4.2	0.34
\mathcal{O}_{15}	4.1	0.27

Similarly, for Ge, Si, and F

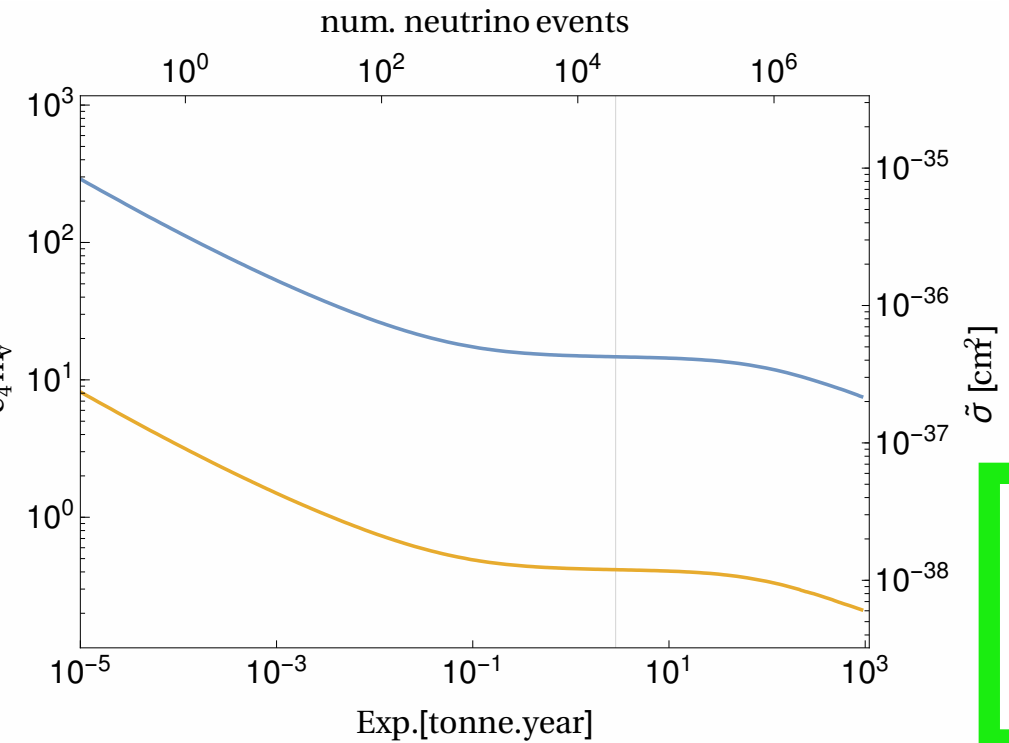
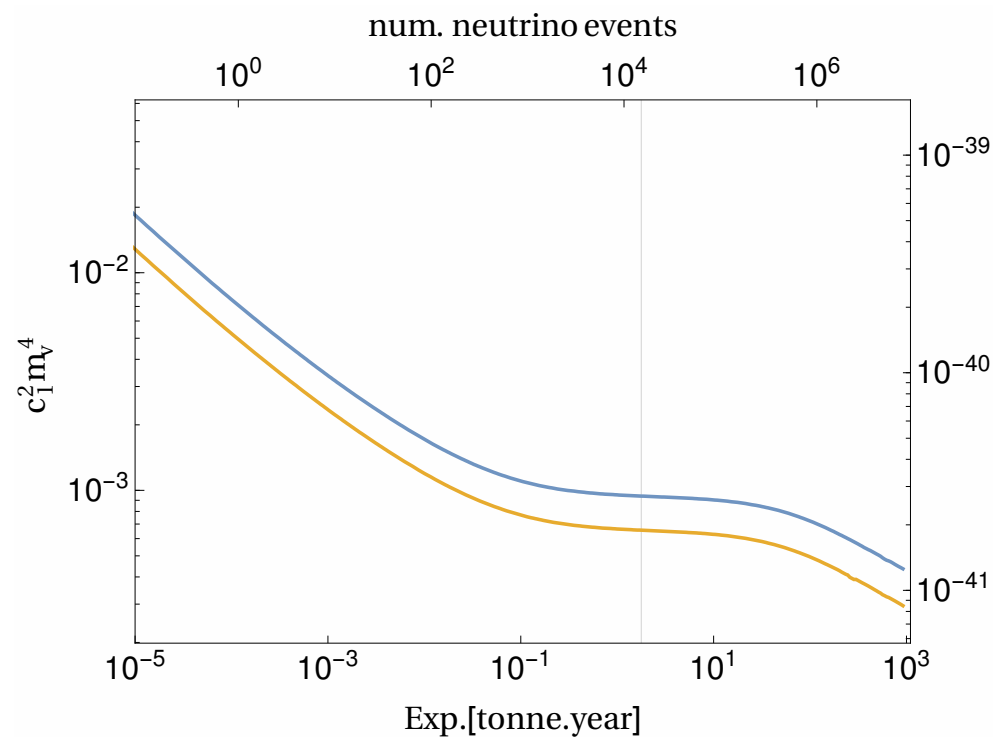




Discovery Potential

We've calculated the smallest cross-section which will produce a 3σ fluctuation above the background 90% of the time

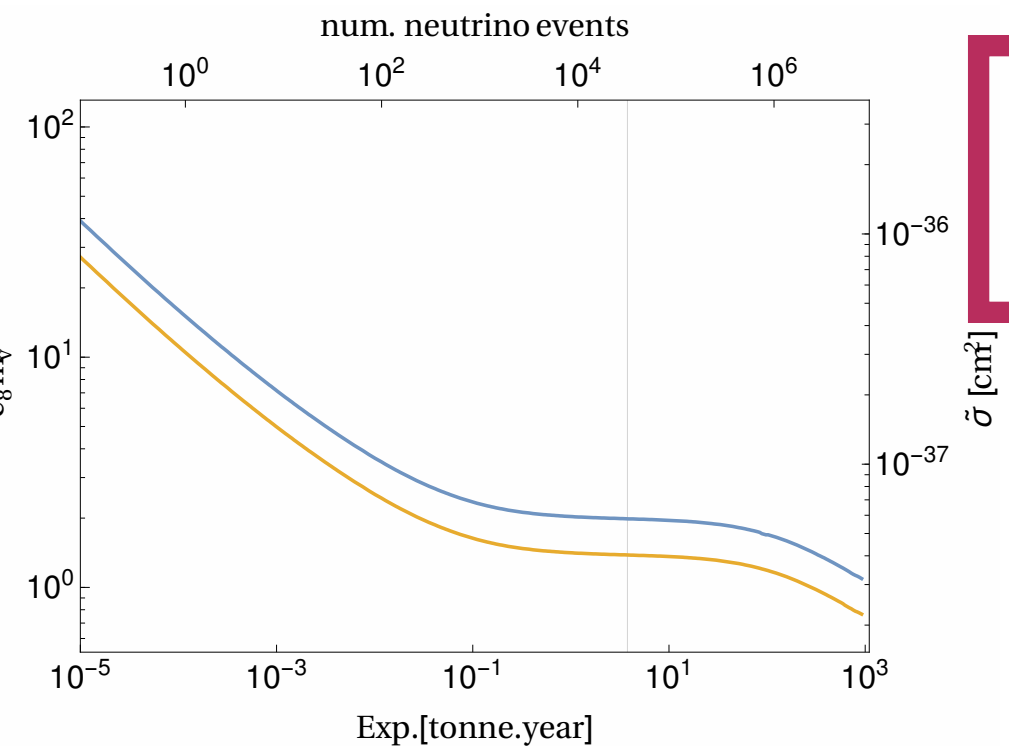
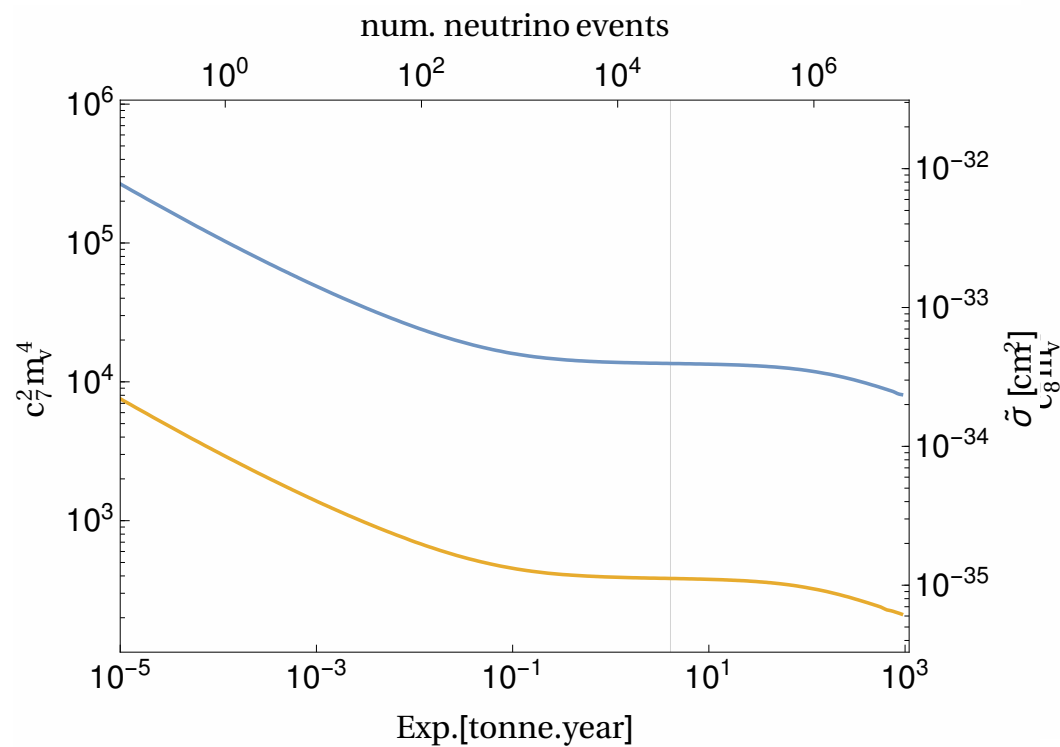
\mathcal{O}_1



\mathcal{O}_4

The standard floor is recovered for the first set of operators

\mathcal{O}_7



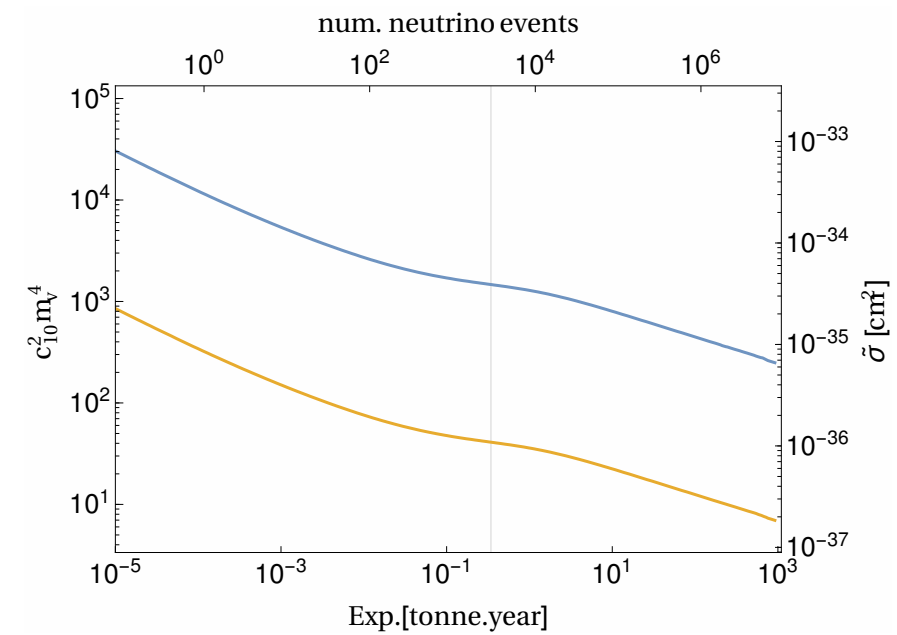
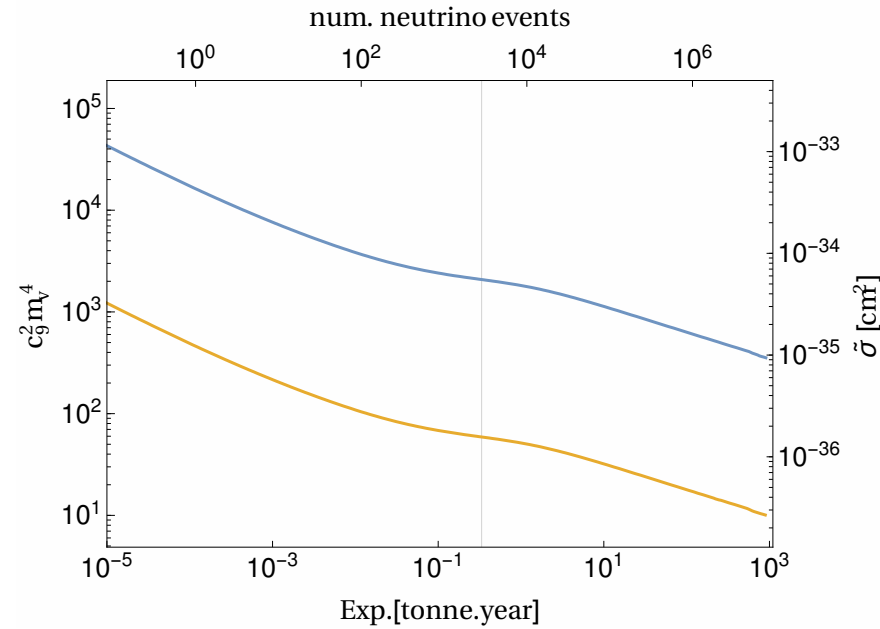
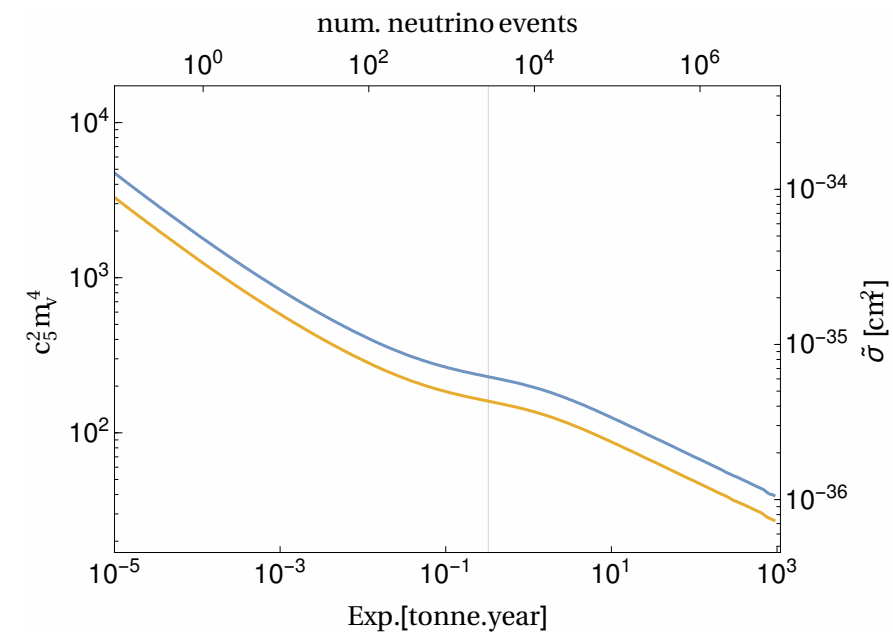
\mathcal{O}_8

q^2 and $q^2 v_T^2$

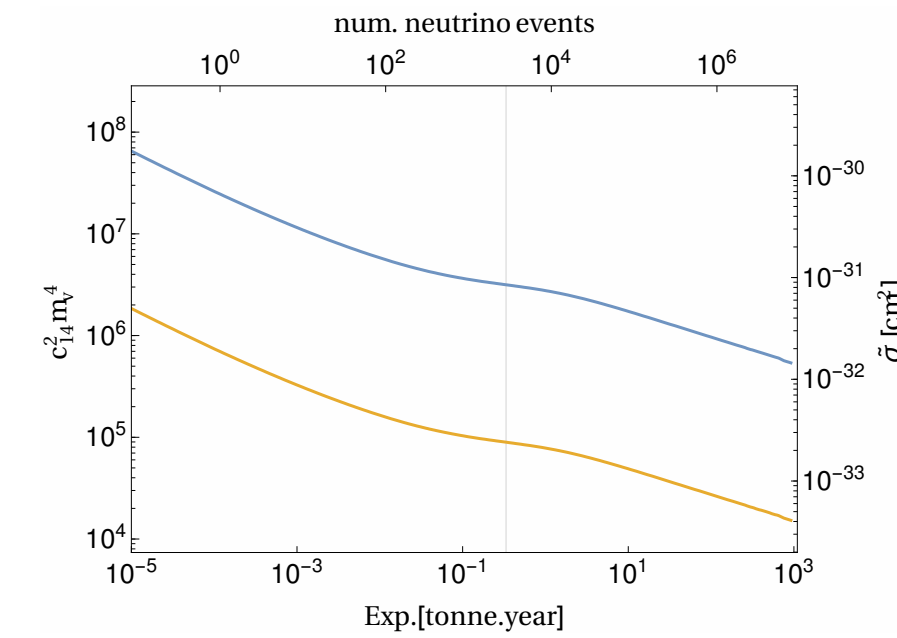
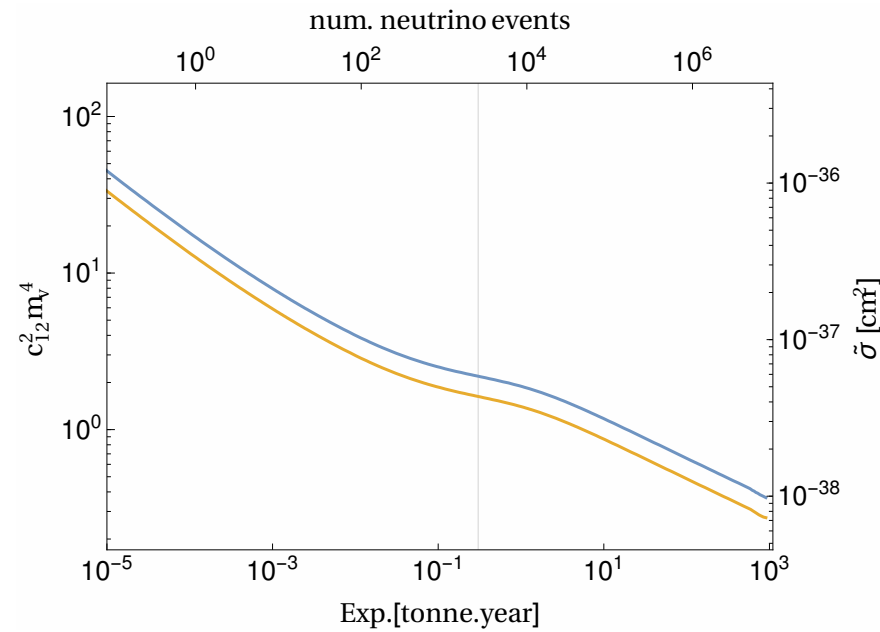
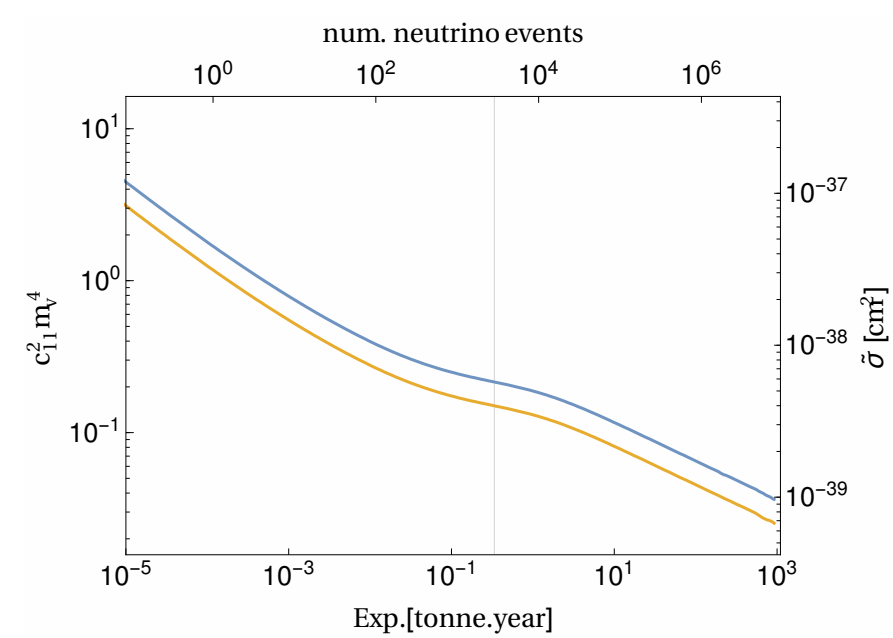
\mathcal{O}_5

\mathcal{O}_9

\mathcal{O}_{10}



but disappears for different momentum dependent operators

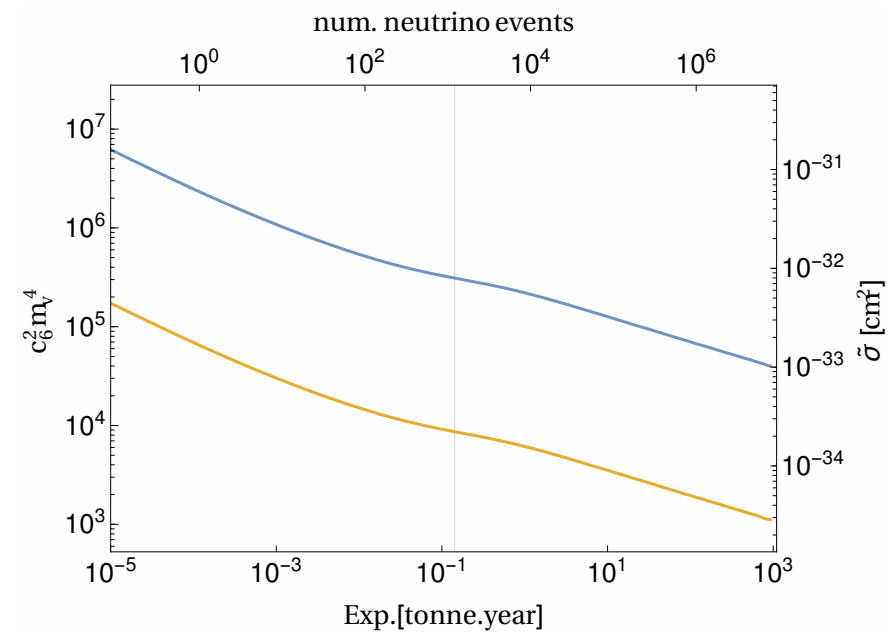
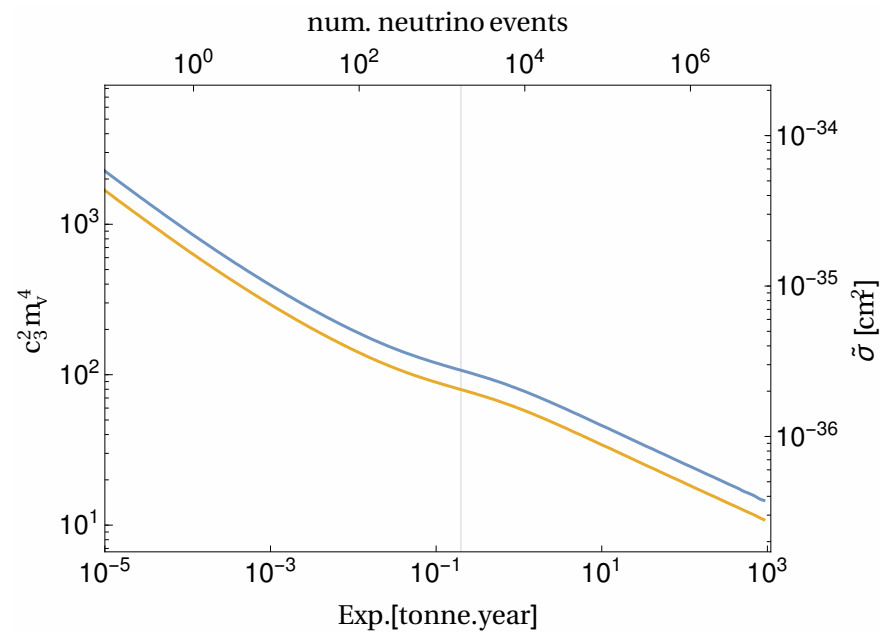


\mathcal{O}_{11}

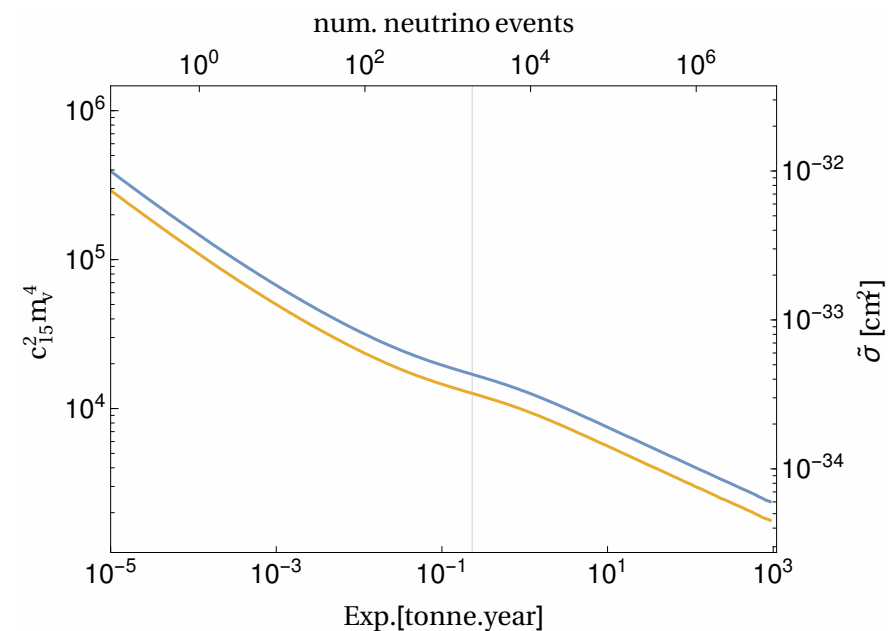
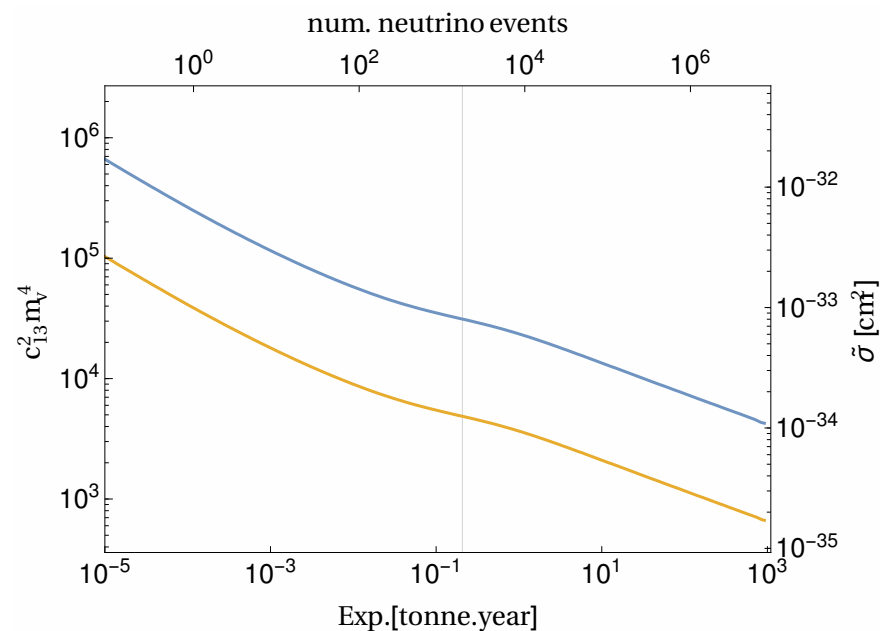
\mathcal{O}_{12}

\mathcal{O}_{14}

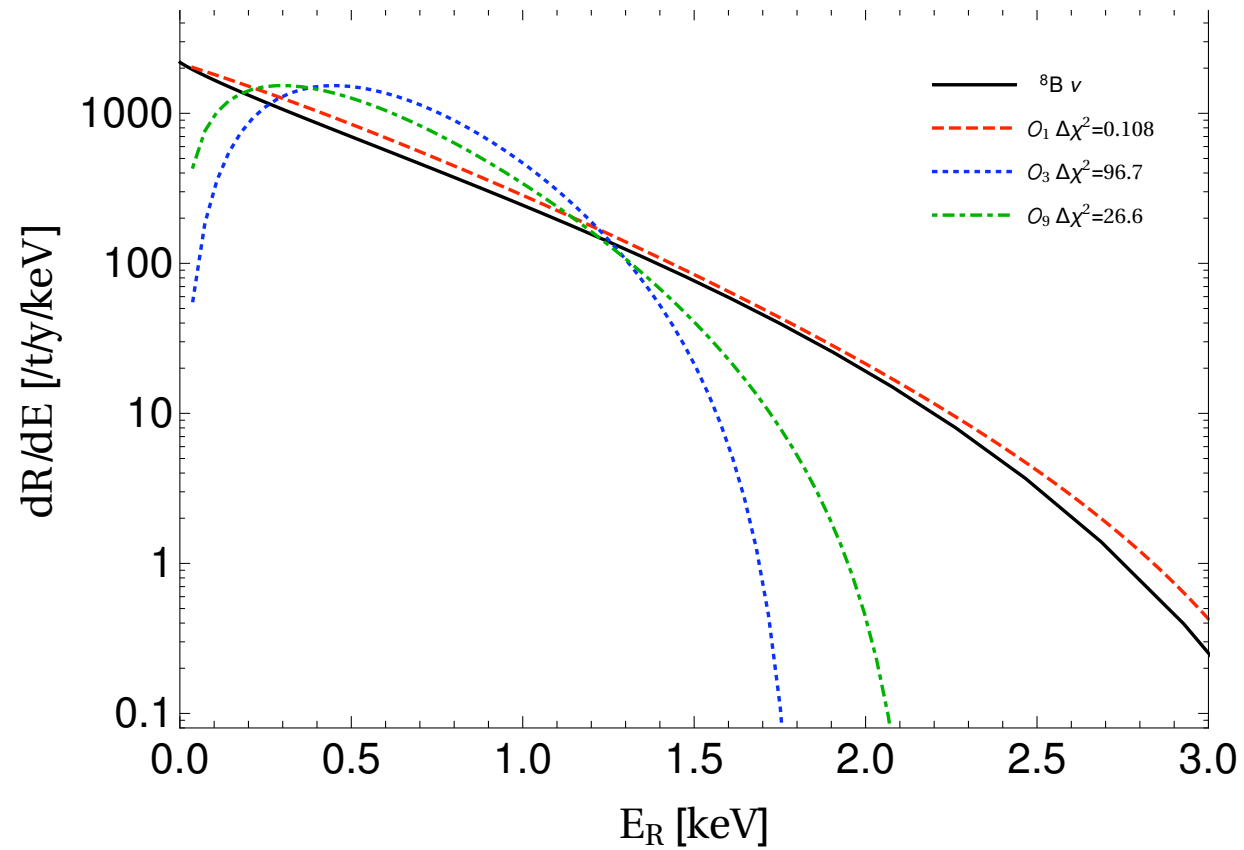
$$q^2 v_T^2, q^4 \text{ and } q^4 v_T^2$$

 \mathcal{O}_3

 \mathcal{O}_6

but disappears for different momentum dependent operators

 \mathcal{O}_{13}

 \mathcal{O}_{15}

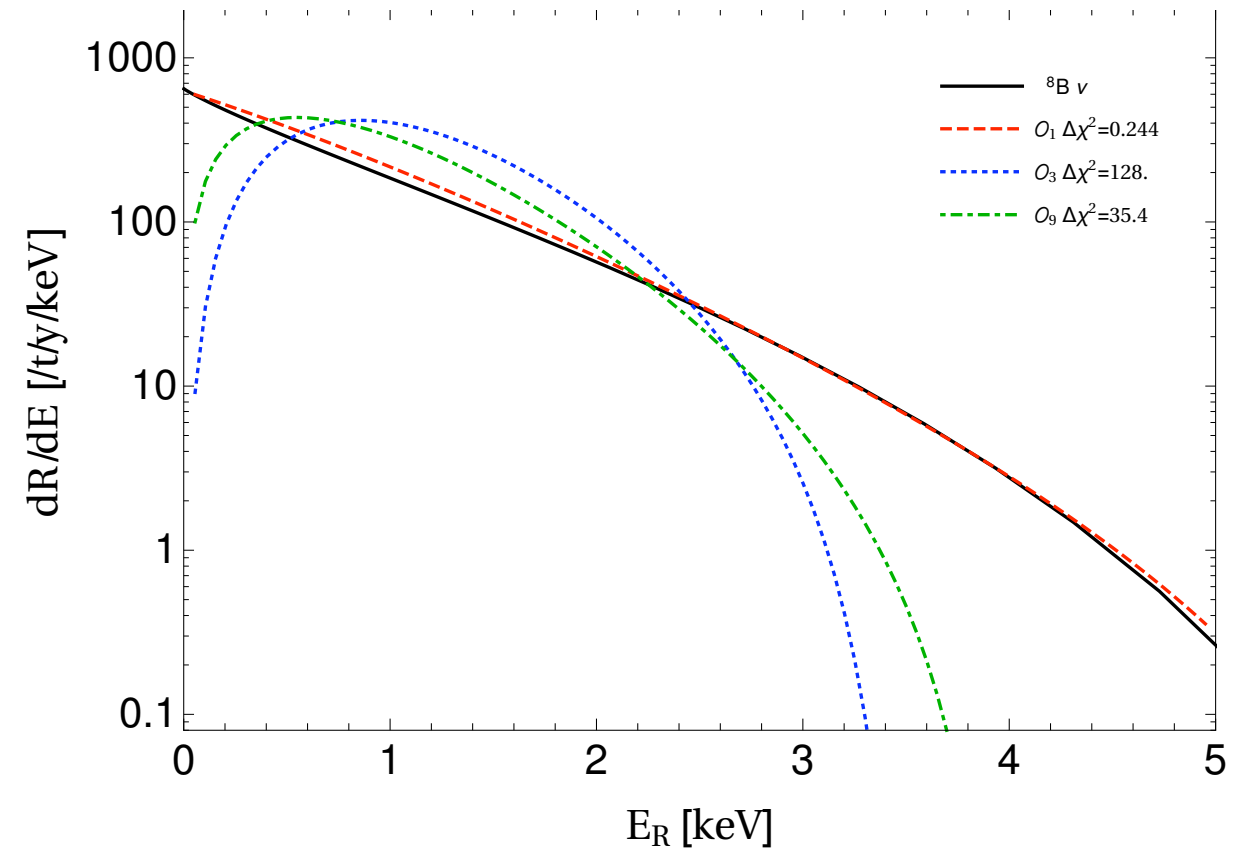
Sample max likelihood rates fit to the boron-8 neutrino rate



\mathcal{O}_3

$$i\vec{S}_N \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}^\perp \right)$$

Xenon



\mathcal{O}_9

$$i\vec{S}_\chi \cdot \left(\vec{S}_N \times \frac{\vec{q}}{m_N} \right)$$

Germanium

Connecting the Scales

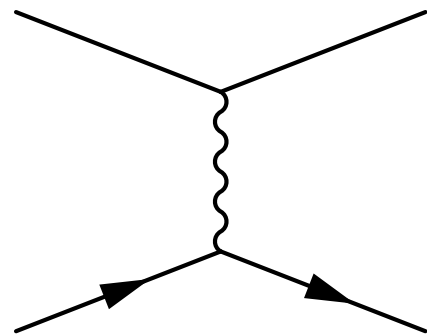
Collider

Direct Detection

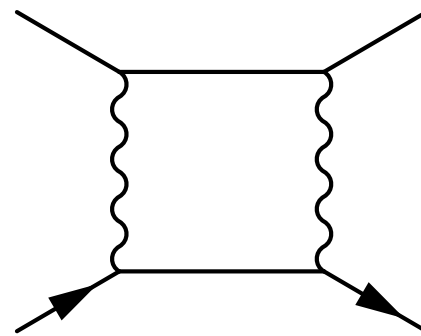


Operator Uniqueness

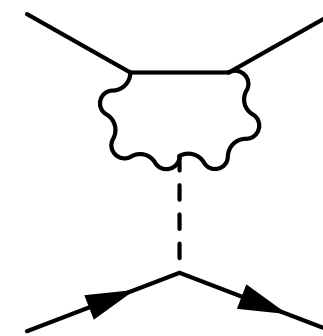
An issue that arises is whether one could begin at a high scale with one type of operator as dominant and end at a low scale with a different leading order operator.



(a) Tree level



(b) Loop processes



$$\frac{g_2^2}{2 \cos^2 \theta_W} T_3^q \frac{Q}{2} \frac{1}{m_Z^2} \bar{\chi} \gamma^\mu \gamma^5 \chi \bar{q} \gamma_\mu \gamma^5 q$$

SD

$$\frac{1}{4\pi} \frac{g_2^4 Q^2}{\cos^4 \theta_W m_Z} \left[\frac{(T_3^q)^2}{2m_Z^2} + \frac{1}{4m_h^2} \right] m_q \bar{\chi} \chi \bar{q} q$$

SI

M. Freytsis and Z. Ligeti, PRD **83** (2011), arXiv:1012.5317

M.A. Fedderke, J.-Y. Chen, E.W. Kolb, and L.-T. Wang, JHEP **1408** (2014), arXiv:1404.2283

S. Matsumoto, S. Mukhopadhyay, Y.-L. Sming Tsai, JHEP **1410** (2014), arXiv:1407.1859

R.J. Hill and M.P. Solon, PRD **91** (2015) arXiv:1409.8290

Operator Uniqueness

An example was obtained for the Higgs portal interaction

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \bar{\chi} (i\not{\partial} - M_0) \chi + \Lambda^{-1} \left(\cos \theta \bar{\chi} \chi + \sin \theta \bar{\chi} i\gamma_5 \chi \right) H^\dagger H$$

After EWSB: $H^\dagger H \longrightarrow \frac{\langle v \rangle^2}{2} + \langle v \rangle h + \frac{h^2}{2}$

A chiral rotation and field redefinition is needed for a real mass

$$\chi \rightarrow \exp(i\gamma_5 \alpha/2) \chi \quad \Rightarrow \quad \bar{\chi} \rightarrow \bar{\chi} \exp(i\gamma_5 \alpha/2)$$

It is found that even for an initially pure pseudoscalar interaction $\cos \theta = 0, \sin \theta = \pm 1$ a scalar term will be generated

$$\Lambda^{-1} \left[-\frac{\langle v \rangle^2}{2\Lambda M} \bar{\chi} \chi \pm \sqrt{1 - \left(\frac{\langle v \rangle^2}{2\Lambda M} \right)^2} \bar{\chi} i\gamma_5 \chi \right] (\langle v \rangle h + h^2/2)$$

M.A. Fedderke, J.-Y. Chen, E.W. Kolb, and L.-T. Wang, JHEP **1408** (2014), arXiv:1404.2283

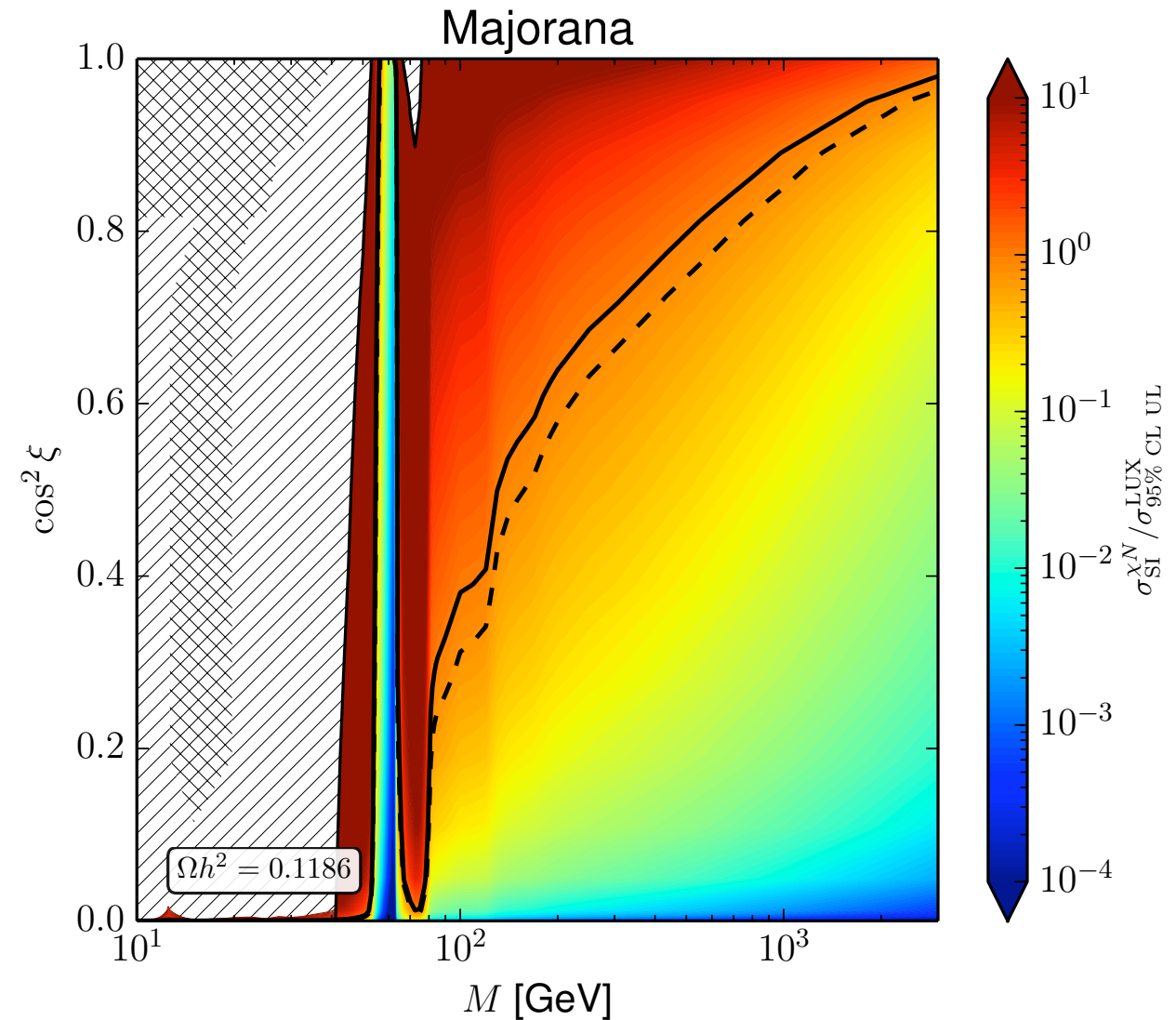
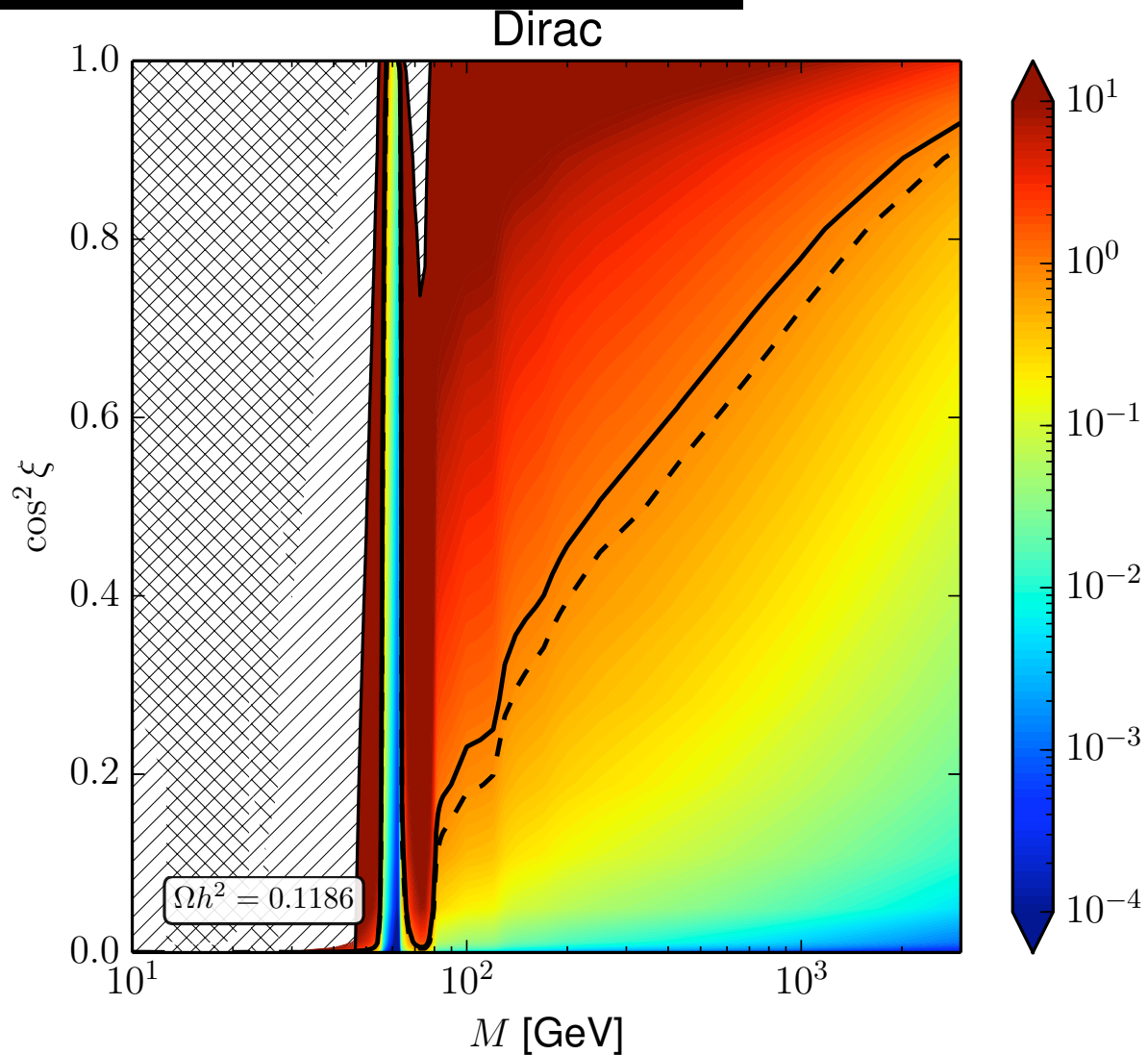
S. Matsumoto, S. Mukhopadhyay, Y.-L. Sming Tsai, JHEP **1410** (2014), arXiv:1407.1859

R.J. Hill and M.P. Solon, PRD **91** (2015) arXiv:1409.8290

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \bar{\chi} i \not{\partial} \chi - \bar{\chi} M \chi + \Lambda^{-1} \left(\langle v \rangle h + \frac{1}{2} h^2 \right) \left[\cos \xi \bar{\chi} \chi + \sin \xi \bar{\chi} i \gamma_5 \chi \right]$$

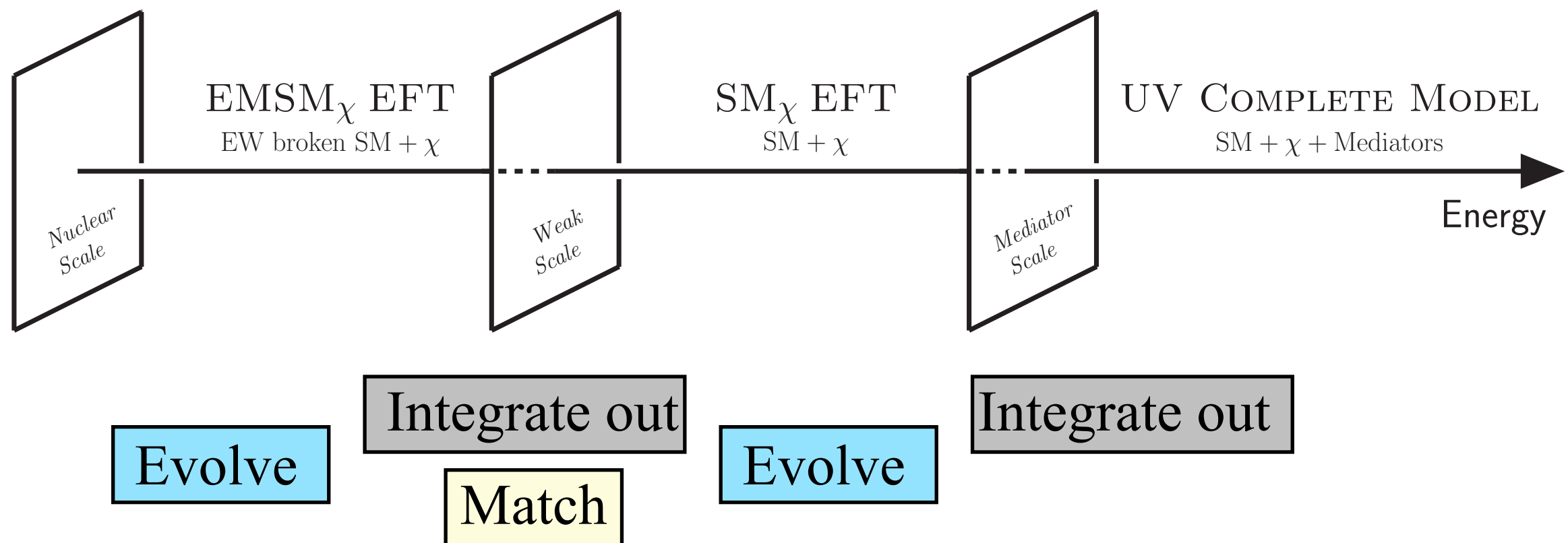
$$\cos \xi = \frac{M_0}{M} \left[\cos \theta - \frac{\langle v \rangle^2}{2\Lambda M_0} \right] \quad \text{and} \quad \sin \xi = \frac{M_0}{M} \sin \theta$$

Spin-Independent Constraints



$$\sigma_{\text{SI}}^{\chi N} = \frac{\langle |\mathcal{M}| \rangle}{16\pi(M + M_N)^2} = \frac{1}{\pi} \left(\frac{\mu_{\chi N}}{m_h^2} \right)^2 \left(\frac{f_N}{\Lambda} \right)^2 \left[\cos^2 \xi + \frac{1}{2} \left(\frac{\mu_{\chi N}}{M} \right)^2 \nu_\chi^2 \right]$$

In order to fully exploit complementarity between direct detection and collider searches, one needs to properly connect the scale of the mediator mass to the nuclear scale



$$\mathcal{L}_{\text{SM}_\chi} = \mathcal{L}_{\text{SM}} + \bar{\chi} (i\not{\partial} - m_\chi) \chi + \sum_{d>4} \sum_{\alpha} \frac{c_\alpha^{(d)}}{\Lambda^{d-4}} \mathcal{O}_\alpha^{(d)}$$

SM _χ EFT	Symbol	Operator	Symbol	Operator	Symbol	Operator
	$\mathcal{O}_{\Gamma q}^{(i)}$	$\bar{\chi} \Gamma^\mu \chi \bar{q}_L^i \gamma_\mu q_L^i$	$\mathcal{O}_{\Gamma l}^{(i)}$	$\bar{\chi} \Gamma^\mu \chi \bar{l}_L^i \gamma_\mu l_L^i$	$\mathcal{O}_{\Gamma H}^{(i)}$	$\bar{\chi} \Gamma^\mu \chi H^\dagger i \overleftrightarrow{D}_\mu H$
	$\mathcal{O}_{\Gamma u}^{(i)}$	$\bar{\chi} \Gamma^\mu \chi \bar{u}_R^i \gamma_\mu u_R^i$	$\mathcal{O}_{\Gamma e}^{(i)}$	$\bar{\chi} \Gamma^\mu \chi \bar{e}_R^i \gamma_\mu e_R^i$		
	$\mathcal{O}_{\Gamma d}^{(i)}$	$\bar{\chi} \Gamma^\mu \chi \bar{d}_R^i \gamma_\mu d_R^i$				

Wilson coefficients are evolved

$$\frac{d \mathcal{C}_{\text{SM}_\chi}}{d \ln \mu} = \gamma_{\text{SM}_\chi} \mathcal{C}_{\text{SM}_\chi}$$

Wilson coefficients are matched at the EWSB scale including effects from integrating out weak scale particles

EMSM _χ	Symbol	Operator	Symbol	Operator	Symbol	Operator
	$\mathcal{O}_{\Gamma V u}^{(i)}$	$\bar{\chi} \Gamma^\mu \chi \bar{u}^i \gamma_\mu u^i$	$\mathcal{O}_{\Gamma V d}^{(i)}$	$\bar{\chi} \Gamma^\mu \chi \bar{d}^i \gamma_\mu d^i$	$\mathcal{O}_{\Gamma V e}^{(i)}$	$\bar{\chi} \Gamma^\mu \chi \bar{e}^i \gamma_\mu e^i$
	$\mathcal{O}_{\Gamma A u}^{(i)}$	$\bar{\chi} \Gamma^\mu \chi \bar{u}^i \gamma_\mu \gamma_5 u^i$	$\mathcal{O}_{\Gamma A d}^{(i)}$	$\bar{\chi} \Gamma^\mu \chi \bar{d}^i \gamma_\mu \gamma_5 d^i$	$\mathcal{O}_{\Gamma A e}^{(i)}$	$\bar{\chi} \Gamma^\mu \chi \bar{e}^i \gamma_\mu \gamma_5 e^i$

Wilson coefficients are evolved

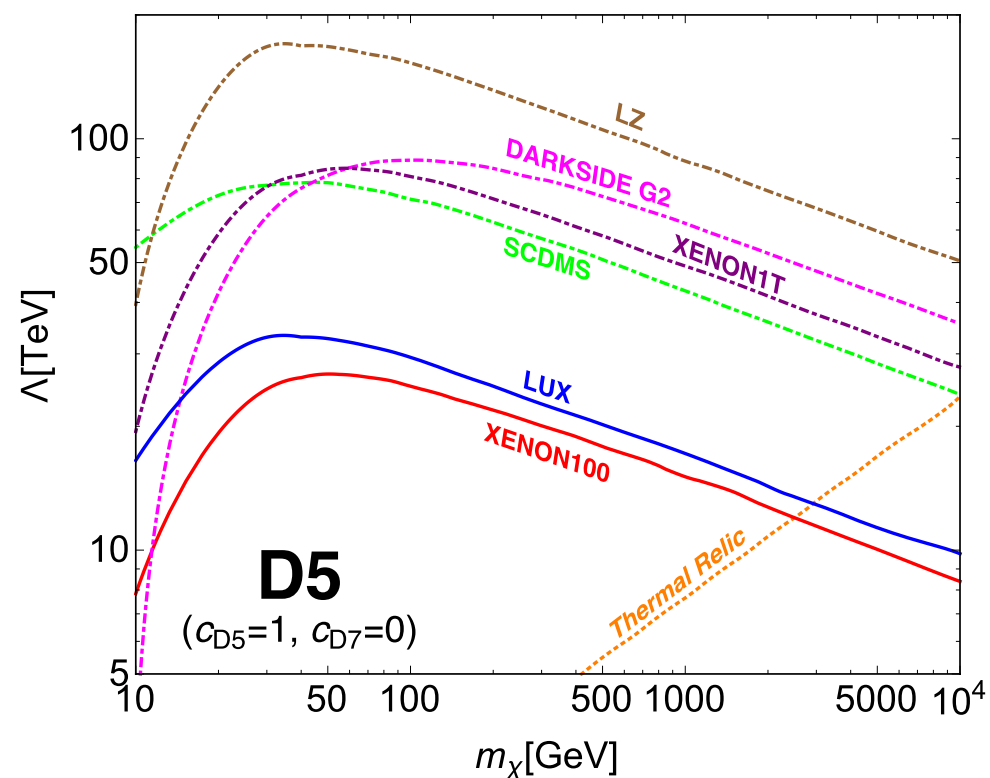
$$\frac{d \mathcal{C}_{\text{EMSM}_\chi}}{d \ln \mu} = \gamma_{\text{EMSM}_\chi} \mathcal{C}_{\text{EMSM}_\chi}$$

Arrive at Wilson coefficients at the nuclear scale

\mathcal{C}_N

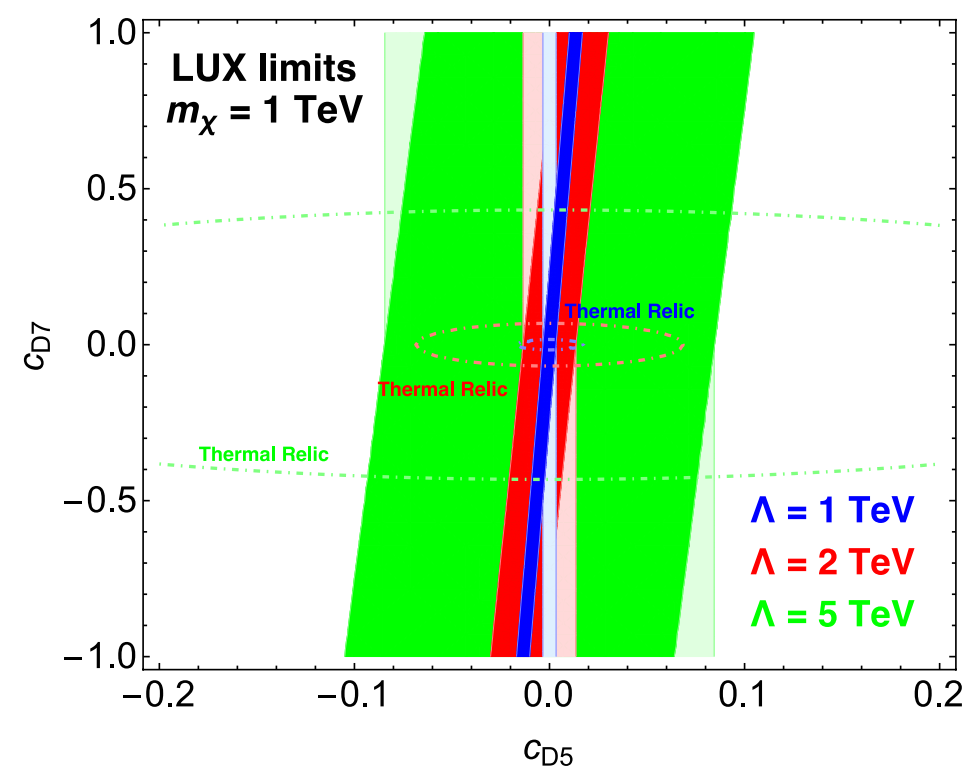
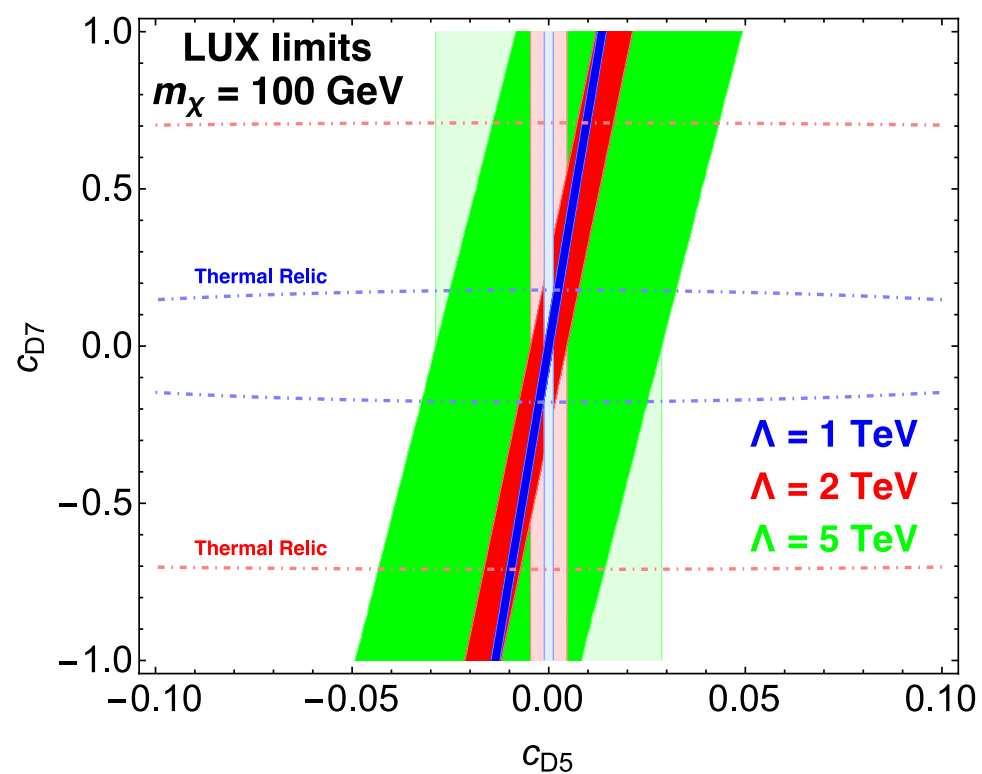
Operator Mixing

Limits can be altered when loop effects are included...



$$\mathcal{L}_{D5} = \frac{c_{D5}}{\Lambda^2} \bar{\chi} \gamma^\mu \chi \left[\sum_i \bar{u}^i \gamma_\mu u^i + \sum_i \bar{d}^i \gamma_\mu d^i \right]$$

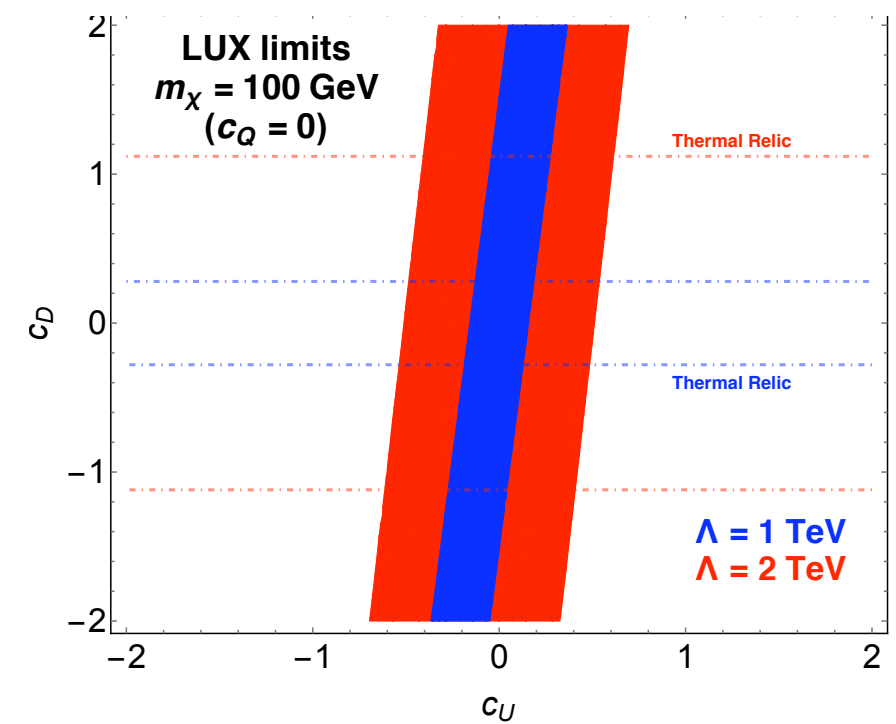
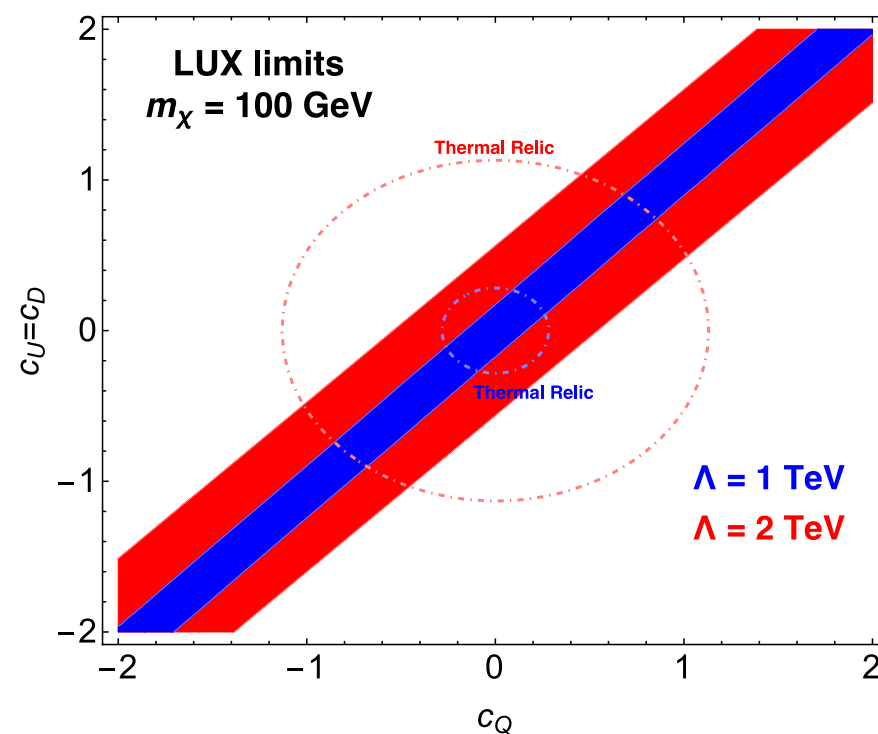
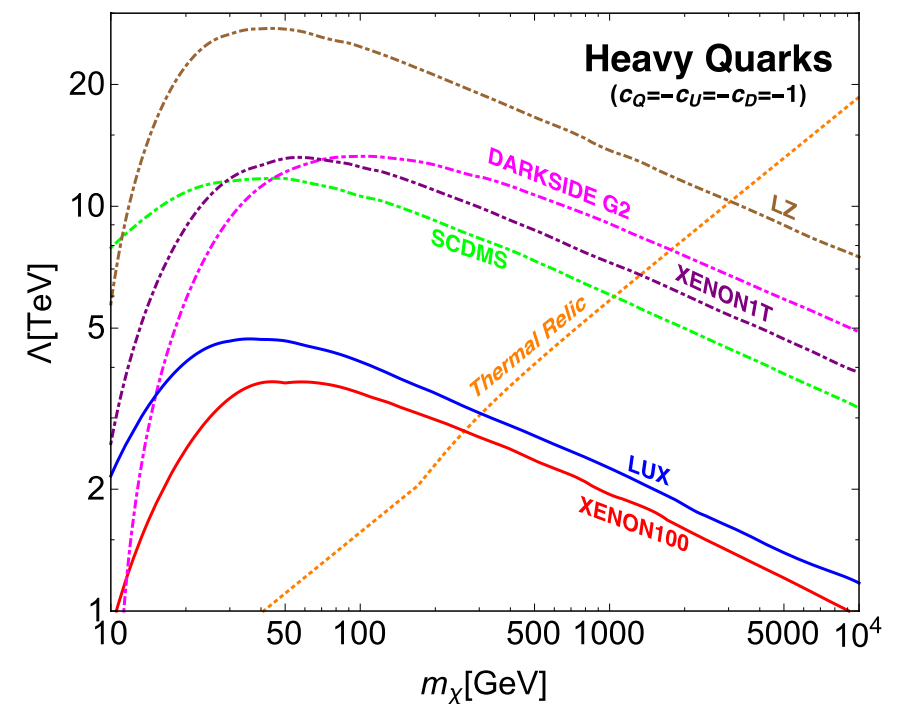
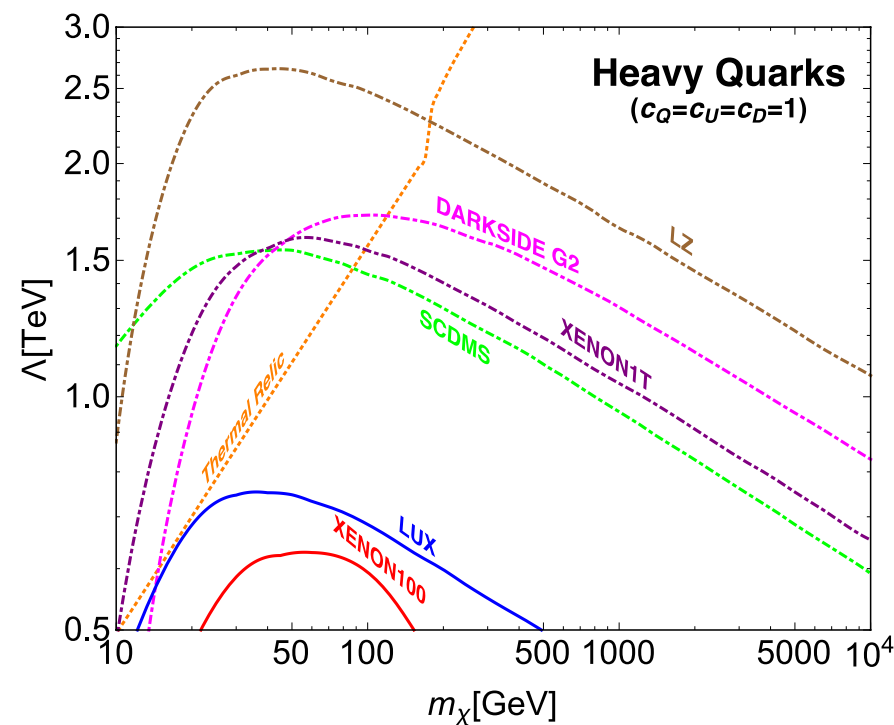
$$\mathcal{L}_{D7} = \frac{c_{D7}}{\Lambda^2} \bar{\chi} \gamma^\mu \chi \left[\sum_i \bar{u}^i \gamma_\mu \gamma_5 u^i + \sum_i \bar{d}^i \gamma_\mu \gamma_5 d^i \right]$$



Operator Mixing

Vector and axial-vector current coupling to heavy quarks

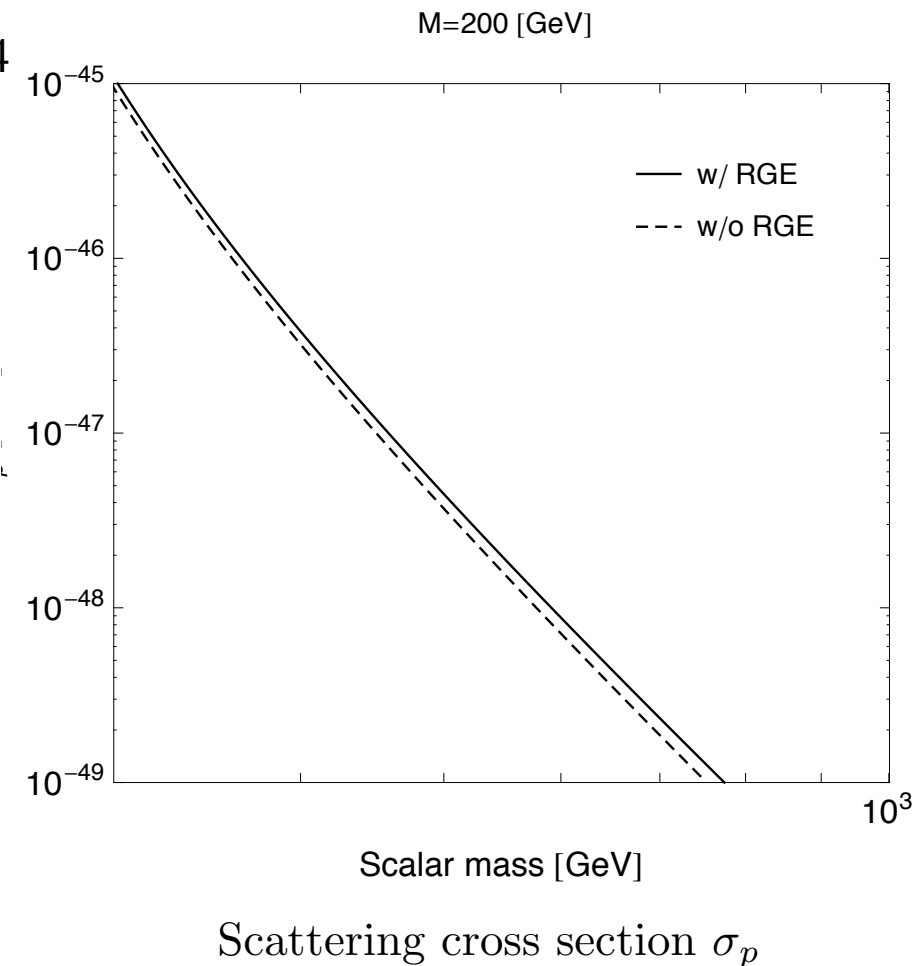
...especially when they are the leading order contribution



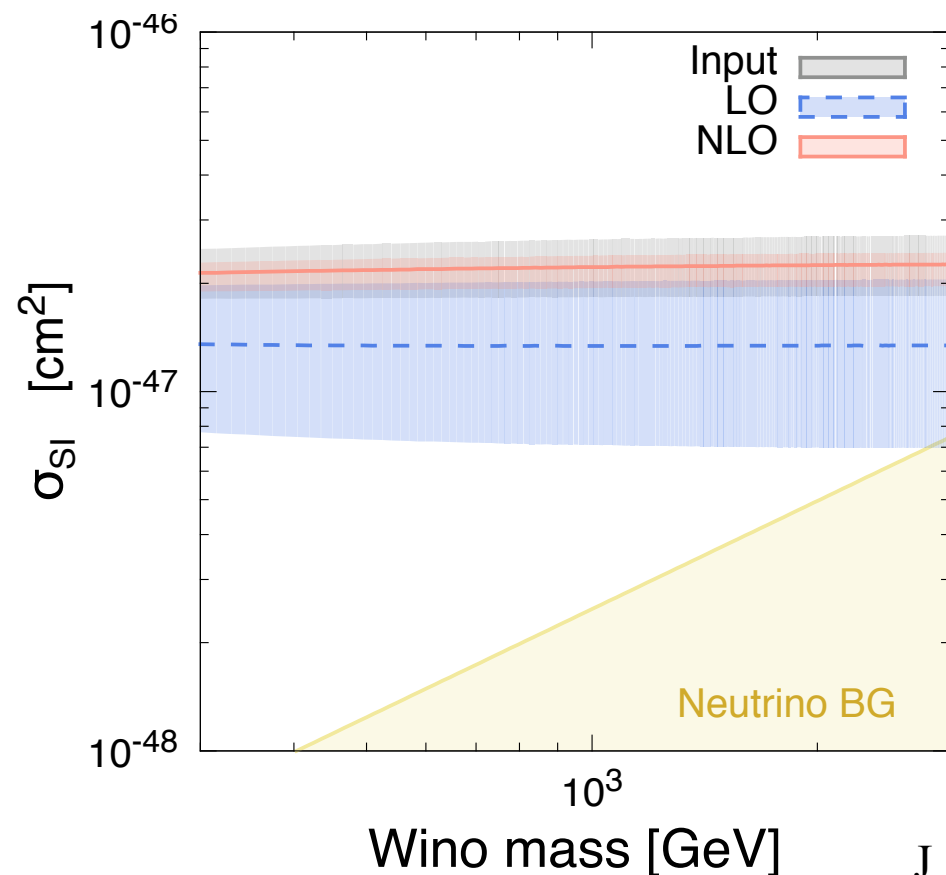
Leading order QCD loop effects on the Wilson coefficients for colored mediator exchanges have been calculated for Majorana, scalar, and real vector boson dark matter

J. Hisano, R. Nagai, and N. Nagata, JHEP **1505** (2015), arXiv:1502.02244

$\mathcal{O}(10)\%$ effects on the cross-section were found



An NLO calculation for WINO dark matter (and a generic $SU(2)_L$ dark matter) was carried out



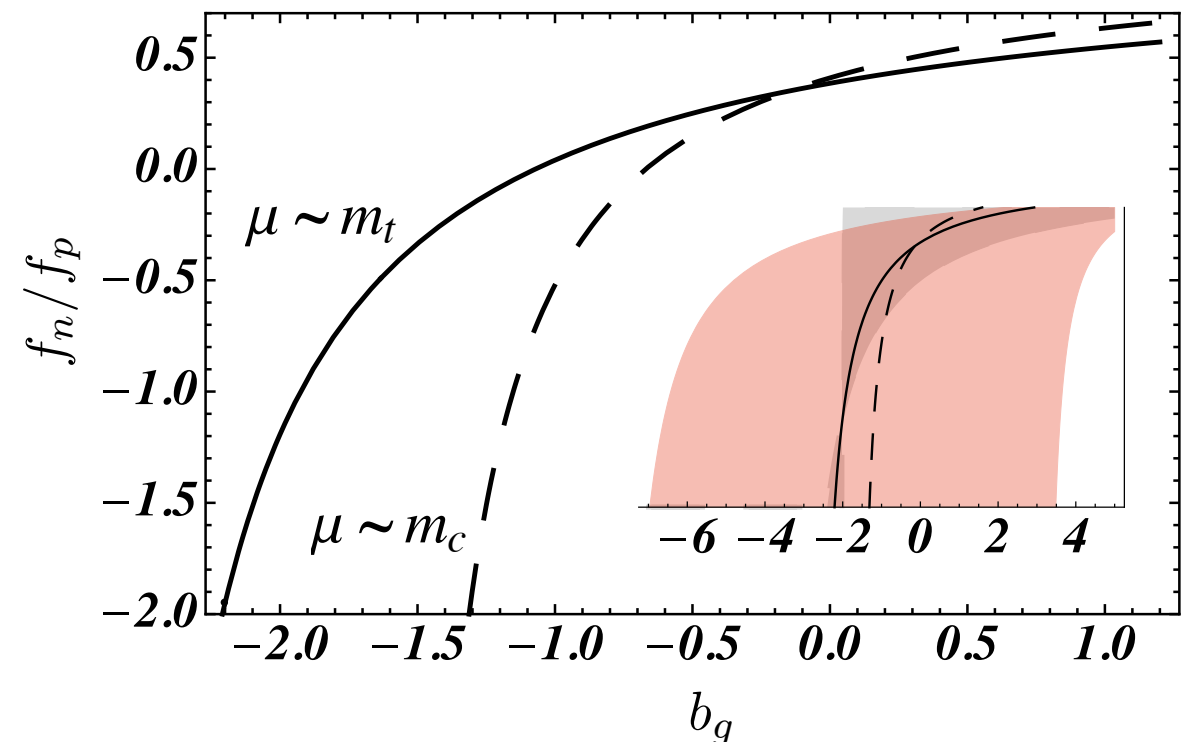
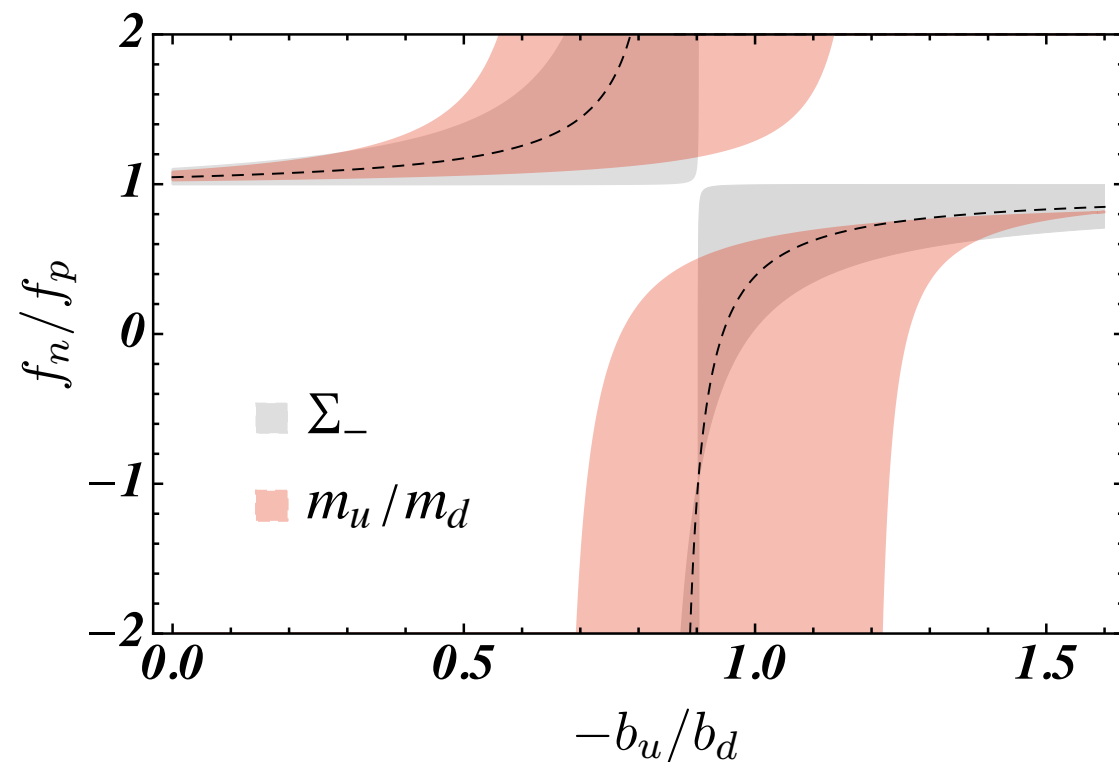
The theoretical uncertainty is much smaller and the central cross-section value is about 70% larger than for LO corrections alone.

J. Hisano, K. Ishiwata, and N. Nagata, JHEP **1506** (2015), arXiv:1504.00915

One must also account for hadronic matrix element evaluation

$$\langle p|O_u|p\rangle = \langle n|O_d|n\rangle, \quad \langle p|O_d|p\rangle = \langle n|O_u|n\rangle, \quad \langle p|O_s|p\rangle = \langle n|O_s|n\rangle$$

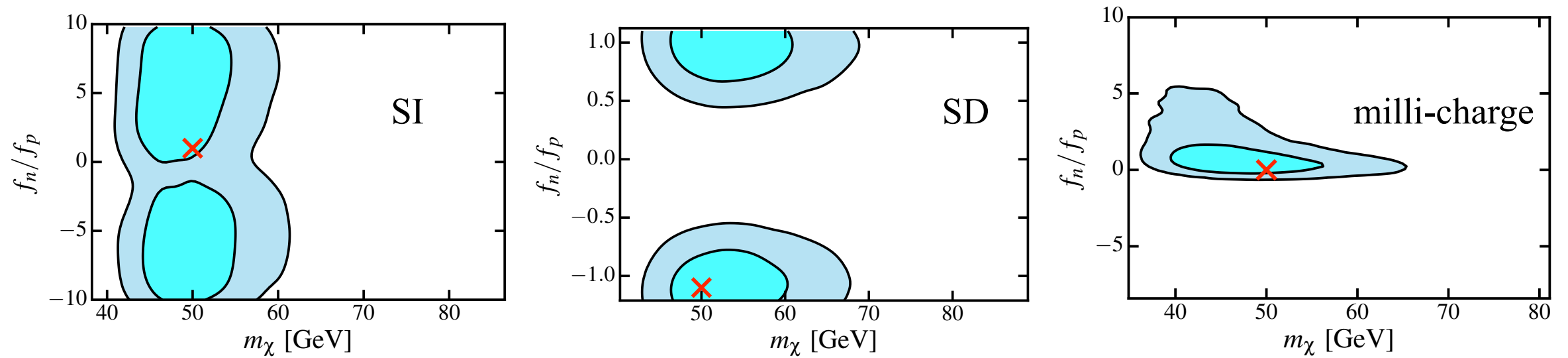
which can include important uncertainties, for example in quark mass ratios or nucleon form factors due to quark currents, renormalization scale choice



$$R_{ud} \equiv \frac{m_u}{m_d} = 0.49 \pm 0.13, \quad R_{sd} \equiv \frac{m_s}{m_d} = 19.5 \pm 2.5$$

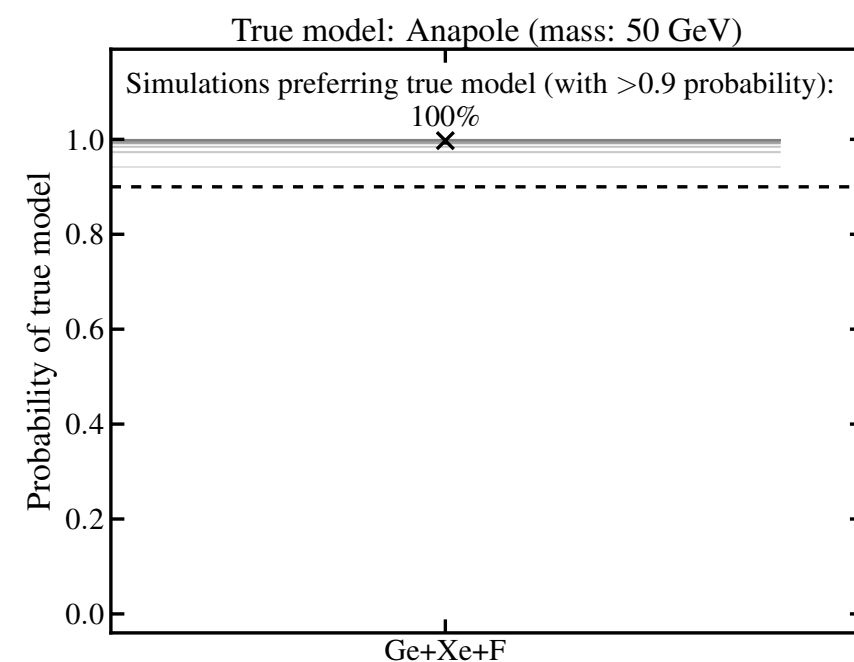
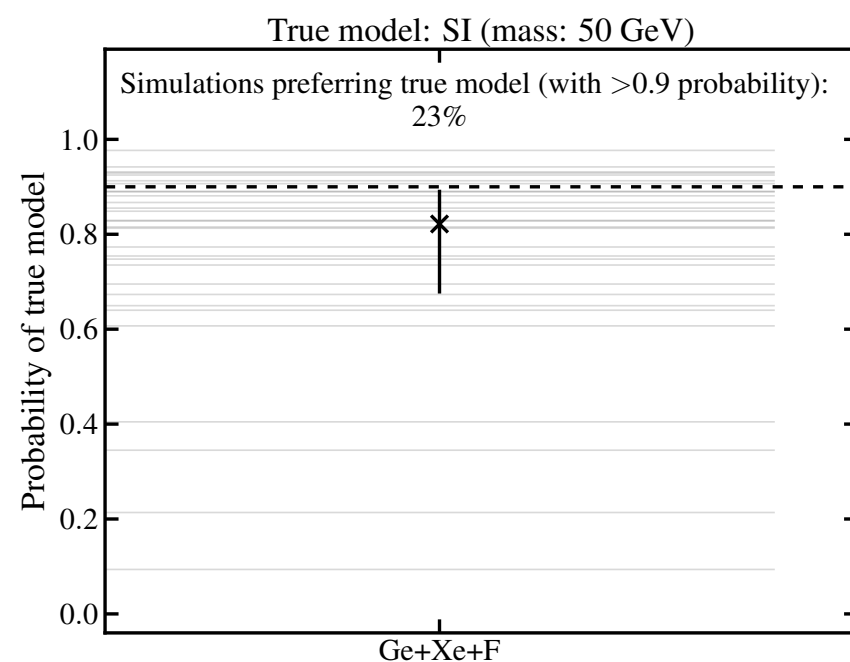
$$\Sigma_- = (m_d - m_u) \langle N | (\bar{u}u - \bar{d}d) | N \rangle = \pm 2(2) \text{ MeV}$$

$$\mathcal{L}_{\chi, SM} = \frac{1}{\Lambda^2} \bar{\chi} \chi \left[b_u \bar{u}u + b_d \bar{d}d + \frac{b_g}{\Lambda} (G_{\mu\nu}^a)^2 \right]$$



Analysis including Ge, Xe, and F with f_n/f_p a free parameter

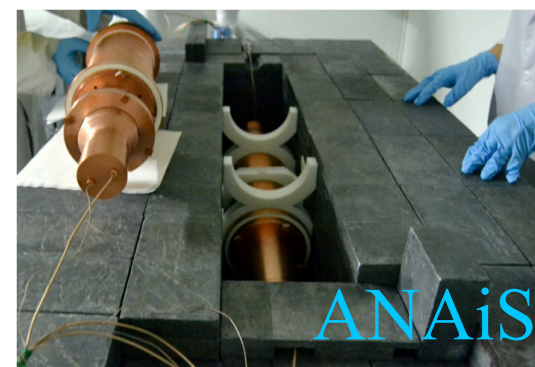
These type of uncertainties obviously can greatly effect data interpretations,



The Future and Summary



~400 kg cryogenic
Ge and Si
2019



NaI Scintillators
112.5kg
2016

KamLAND-PICO
proposed NaI



cryogenic ton scale
Ge and CaWO_4



NaI Scintillators
17kg prototype (current)
250kg future



~ 1 t liquid xenon
2015



~ 7 t liquid xenon
2018



CsI 103.4kg
future 200kg NaI,
CaMoO



20t liquid xenon
and
10t liquid argon



~ .5t (current)
1.5t (future) liquid xe



~ 1t (2015)
50t!!
(future) liquid
argon



~ 50kg (current)
3.3t (future) liquid argon



835kg liquid xenon
future ~5t
eventually ~24t

PICASSO and COUPP formed



37kg of CF_3I and 3kg of C_3F_8
future 500kg

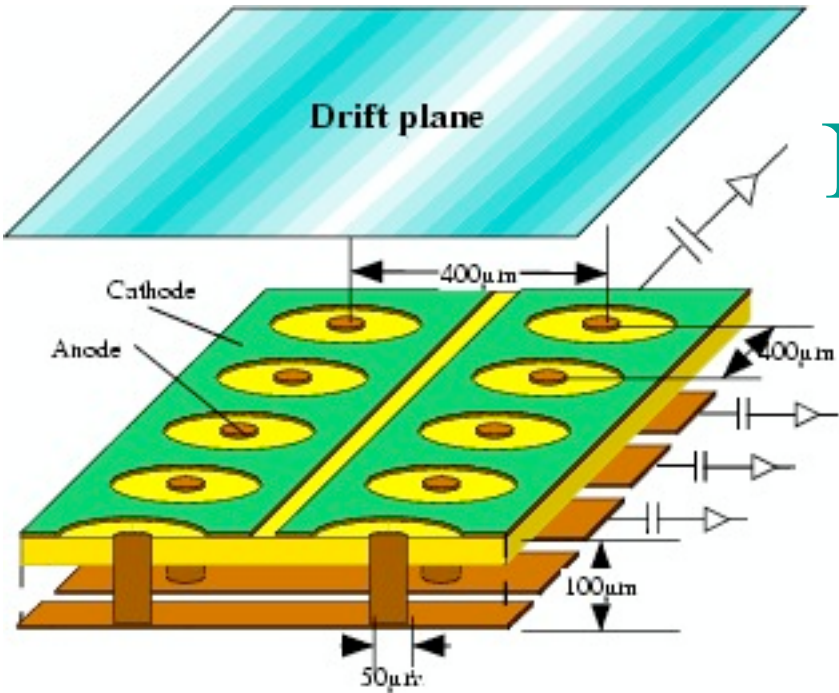


CS_2 , O_2 and CF_4 gas
future 8 m³ experiment



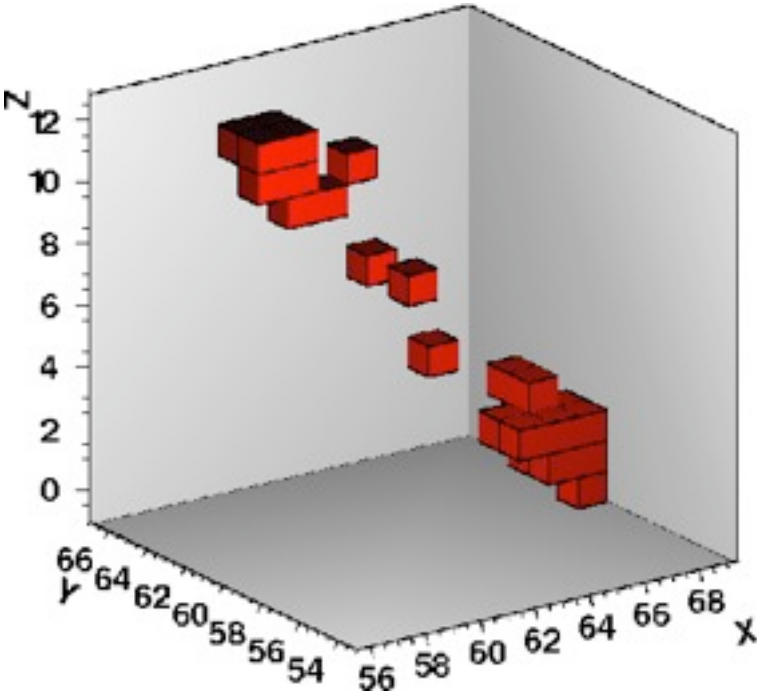
CF_4 gas
future 0(m³)

MIMAC



NEWAGE

CF_4 gas



$^4\text{He} + 5\%\text{C}_4\text{H}_{10}$

As direct detection experiments becoming increasingly sensitive, a discovery requires accurate modeling to discern particle properties

Nuclear-WIMP interactions which include responses beyond the standard ones could avoid misinterpretations of the particle nature of dark matter

A general array of single WIMP, single mediators interactions has been studied and non-standard responses arise at leading order for some interaction types

The use of a variety of detector materials can be significant for discovery and model discrimination

The neutrino background may have less of an effect on some non-standard operators

Precise model constraints will need to be carried out

Complementarity from colliders and astrophysical probes is also vital, and these should include proper handling of the scale differences and uncertainties

Thanks