

# *High-scale validity of 2HDM scenarios: Study using LHC data.*

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JHEP12(2014)166: NC, Ujjal Kmar Dey, Biswarup Mukhopadhyaya  
and  
Phys. Rev. D 92, 015002 (2015): NC, Dilip Kumar Ghosh, Biswarup  
Mukhopadhyaya, Ipsita Saha

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- Dark matter and a radiative neutrino mass in a 2HDM.

# Vacuum stability: Motivating the 2HDM

- In the Standard Model (SM), the stability of the electroweak vacuum is sensitive to the values of the masses of the Higgs and the top-quark. In particular, higher  $M_t$  render the vacuum unstable well below the Planck scale ( $M_{Pl}$ ).

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- Pros: Rich phenomenology, Dark Matter (DM) candidate in special cases.
- Cons: Additional doublets  $\longrightarrow$  Additional quartic couplings  $\longrightarrow$  Fast rise of such couplings  $\longrightarrow$  threat to perturbativity.
- Our goal: To see if there is a balance between these extremes, modulo constraints from LHC and DM experiments.

## Model: Type II 2HDM

- Most general renormalizable scalar potential for two doublets  $\Phi_1$  and  $\Phi_2$ , each having hypercharge (+1)

$$\begin{aligned} V(\Phi_1, \Phi_2) = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - m_{12}^2 (\Phi_1^\dagger \Phi_2 + \Phi_2^\dagger \Phi_1) \\ & + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 \\ & + \lambda_3 \Phi_1^\dagger \Phi_1 \Phi_2^\dagger \Phi_2 + \lambda_4 \Phi_1^\dagger \Phi_2 \Phi_2^\dagger \Phi_1 + \frac{\lambda_5}{2} \left[ (\Phi_1^\dagger \Phi_2)^2 + (\Phi_2^\dagger \Phi_1)^2 \right] \\ & + \lambda_6 \Phi_1^\dagger \Phi_1 (\Phi_1^\dagger \Phi_2 + \Phi_2^\dagger \Phi_1) + \lambda_7 \Phi_2^\dagger \Phi_2 (\Phi_1^\dagger \Phi_2 + \Phi_2^\dagger \Phi_1) \end{aligned}$$

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- The doublets acquire vevs through spontaneous symmetry breaking.

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- Enlarged scalar spectrum: Mutually conjugate pair of charged scalars ( $H^\pm$ ), two neutral scalars ( $H, h$ ) and a neutral pseudoscalar ( $A$ ).

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- We illustrate our findings in context of a Type II 2HDM.

# Constraints and analysis strategy

- We demand  $m_h \sim 125$  GeV to conform with the Higgs discovery@LHC and  $m_{H^+} \geq 315$  GeV to avoid flavor constraints.

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- Higgs signal strength constraints at  $2\sigma$  further imposed.

## Results: Exact $\mathbb{Z}_2$ symmetry

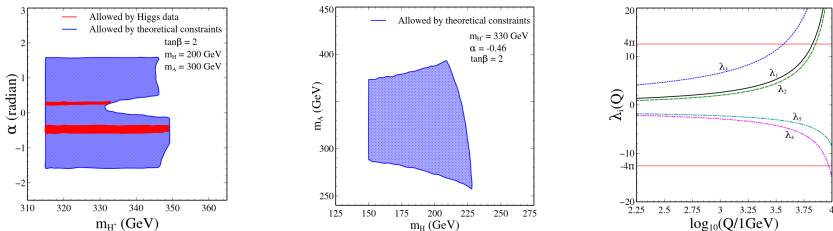
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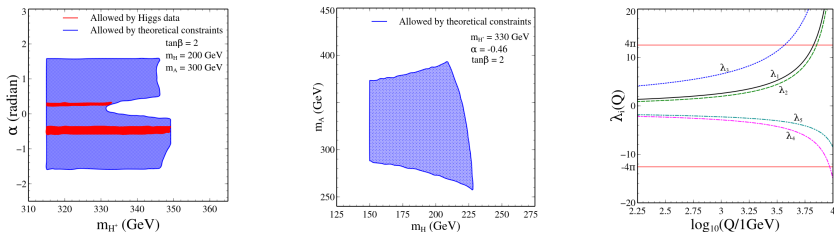
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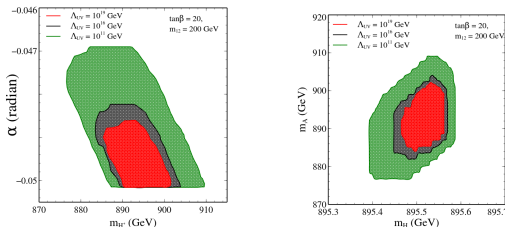
- Motivates one to look beyond exact  $\mathbb{Z}_2$  symmetry.

## Results: Softly broken $\mathbb{Z}_2$ symmetry

- Include  $m_{12} \neq 0$  in the scalar potential while keeping  $\lambda_6, \lambda_7 = 0$ .  
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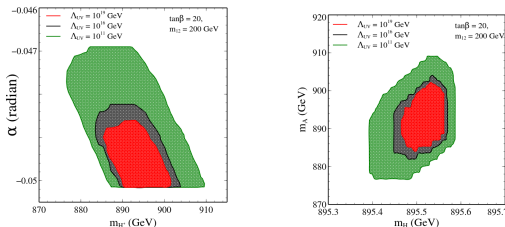
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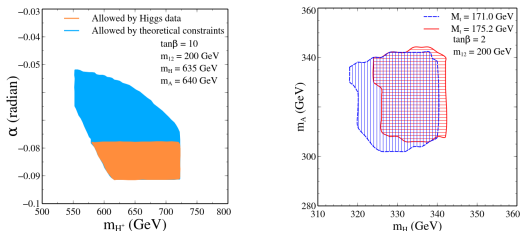


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- Fixing  $m_{12}$  induces a high degree of correlation amongst the non-standard scalar masses. They loom around the TeV scale for the benchmarks taken.

# Results: *Softly* broken $\mathbb{Z}_2$ symmetry

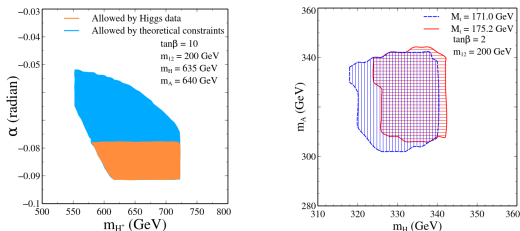
- Unlike the SM, the electroweak vacuum is rendered stable even for high values of  $M_t$ .



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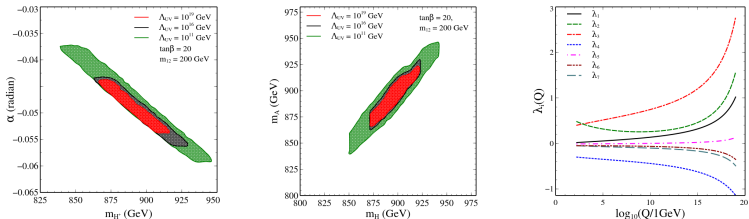


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- Higgs data from the LHC imposes  $\alpha \sim \beta - \frac{\pi}{2}$ , i.e. takes the 2HDM near the *alignment limit*.

# Results: $\mathbb{Z}_2$ symmetry broken by *hard* terms

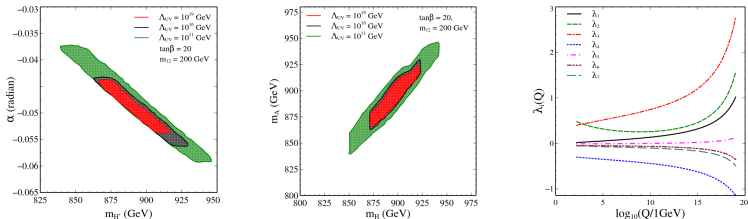
- $\lambda_6, \lambda_7 \neq 0$ .  $\lambda_1(M_t) = 0.02$  and  $\lambda_6(M_t) = \lambda_7(M_t)$  for computational convenience.



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- Larger parameter space opens up ensuring validity up to high scales. Thus, a Type-II 2HDM could be valid upto  $M_{Pl}$  only if the  $\mathbb{Z}_2$  symmetry is broken either by *soft* or *hard* terms.

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- The RH neutrinos play the role of generating a neutrino mass radiatively.

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- The relevant Yukawa and mass terms are

$$-\mathcal{L}_Y = (y_{ij}\bar{N}_i\tilde{\Phi}_2^\dagger\ell_j + h.c) + \frac{M_i}{2}(\bar{N}_i^c N_i + h.c), (i,j = 1,2,3) \quad (2)$$

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- $50 \text{ GeV} < M_H < 90 \text{ GeV}$ : s-channel DM annihilation through  $h$  exchange, and t-channel annihilation through  $A$  and  $H^\pm$  exchange (Hambye 2009, Arhrib 2013).

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- $M_H > 500 \text{ GeV}$ : Co-annihilations among  $H$ ,  $A$  and  $H^\pm$  (Arhrib 2013).

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- Benchmarks of  $M$  consistent with leptogenesis, (a)  $M = 110$  TeV and (b)  $M = 10^9$  TeV (Pilaftsis,1997; Hambye,2009).  $N_i$ - $H$  co-annihilation ruled out.

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- Effect of  $N_i$  in the beta functions only considered above the threshold  $M$ .  
 $M = 10 \text{ TeV} \rightarrow y_\nu = O(10^{-5}) \rightarrow$  No effect on RG evolution.  
 $M = 10^9 \text{ TeV} \rightarrow y_\nu = O(1) \rightarrow$  Appreciable effect on RG evolution.

$$16\pi^2 \frac{d\lambda_2}{dt} \Big|_{IDM+RH} = 16\pi^2 \frac{d\lambda_2}{dt} \Big|_{IDM} + 4\lambda_2 y_\nu^2 - 4y_\nu^4 \quad (5)$$

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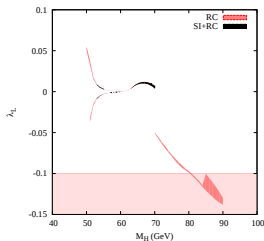
$$\Omega_{\text{DM}} h^2 = 0.1199 \pm 0.0027 \quad (6)$$

$3\sigma$  deviation from the central value permitted. Bound on nucleon-DM scattering cross section given by LUX obeyed.

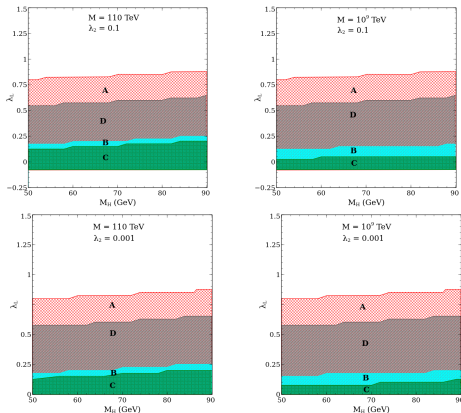
- Higgs signal strengths from ATLAS and CMS satisfied at  $2\sigma$ .

# Results

- Vary  $50 \text{ GeV} < M_H < 90 \text{ GeV}$ ,  $80 \text{ GeV} < M_{H^\pm}, M_A$ . Fix  $\lambda_2$  and  $M$  at two chosen benchmarks.
- Stability upto the Planck scale achieved, a radiative neutrino mass, relic density and direct detection cross section in the correct ballpark.

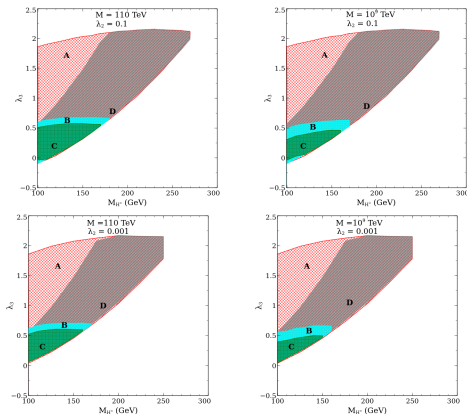


# Results: $50 \text{ GeV} < M_H < 90 \text{ GeV}$



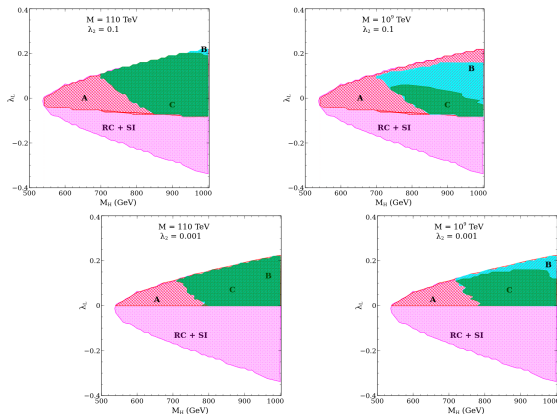
**Figure:** Regions compatible with the theoretical constraints for  $M = 110 \text{ TeV}$  (left panel) and  $10^9 \text{ TeV}$  (right panel) with three different choices of  $\Lambda_{UV}$  and two values of  $\lambda_2$ . The regions denoted by A (red), B (cyan) and C (green) obey these constraints up to  $\Lambda_{UV} = 10^6$ ,  $10^{16}$  and  $10^{19} \text{ GeV}$  respectively. The grey region denoted by D keeps the Higgs to diphoton signal strength within  $2\sigma$  limits of the current data.

# Results: $50 \text{ GeV} < M_H < 90 \text{ GeV}$



- Perturbative unitarity  $\rightarrow$  *Tight upper bound on scalar masses + upper bound on  $\lambda_2$*
- Vacuum stability  $\rightarrow$  *Affected by  $\lambda_2$*

# Results: $M_H > 500$ GeV



- $M = 10^9$  TeV  $\longrightarrow y_\nu = O(1) \rightarrow \lambda_2(\mu)$  starts approaching instability beyond the scale  $M$ .

# Conclusions

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*Thank you  
for your attention*

# Model features: Scalar sector

- $m_{11}$  and  $m_{22}$  eliminated using the tadpole conditions.
- The masses of the physical scalars,

$$\begin{aligned}m_A^2 &= \frac{m_{12}^2}{s_\beta c_\beta} - \frac{1}{2}v^2 \left( 2\lambda_5 + \frac{\lambda_6}{t_\beta} + \lambda_7 t_\beta \right), \\m_{H^\pm}^2 &= m_A^2 + \frac{1}{2}v^2 (\lambda_5 - \lambda_4), \\m_h^2 &= \frac{1}{2} \left[ (A+B) - \sqrt{(A-B)^2 + 4C^2} \right], \\m_H^2 &= \frac{1}{2} \left[ (A+B) + \sqrt{(A-B)^2 + 4C^2} \right], \\\tan 2\alpha &= \frac{2C}{A-B},\end{aligned}$$

where we have defined,

$$\begin{aligned} A &= m_A^2 s_\beta^2 + v^2 (\lambda_1 c_\beta^2 + \lambda_5 s_\beta^2 + 2\lambda_6 s_\beta c_\beta), \\ B &= m_A^2 c_\beta^2 + v^2 (\lambda_2 s_\beta^2 + \lambda_5 c_\beta^2 + 2\lambda_7 s_\beta c_\beta), \\ C &= -m_A^2 s_\beta c_\beta + v^2 [(\lambda_3 + \lambda_4) s_\beta c_\beta + \lambda_6 c_\beta^2 + \lambda_7 s_\beta^2]. \end{aligned}$$

# Constraints:Theoretical

- Vacuum stability: Stability of the electroweak vacuum is ensured up to some specified energy scale if the following conditions are satisfied for all scales  $Q$  up to that scale,

$$\text{vsc1} : \lambda_1(Q) > 0$$

$$\text{vsc2} : \lambda_2(Q) > 0$$

$$\text{vsc3} : \lambda_3(Q) + \sqrt{\lambda_1(Q)\lambda_2(Q)} > 0$$

$$\text{vsc4} : \lambda_3(Q) + \lambda_4(Q) - |\lambda_5(Q)| + \sqrt{\lambda_1(Q)\lambda_2(Q)} > 0$$

- Perturbativity:

$$\lambda_i(Q) < 4\pi$$

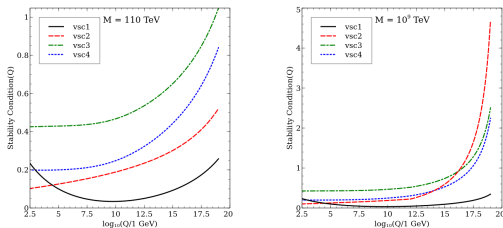
The corresponding constraints for the Yukawa and gauge interactions are,

$$y_i(Q), g_i(Q) < \sqrt{4\pi}$$

## Results: $M_H > 500$ GeV regime

| BP  | $M_H$     | $M_{H^\pm}$ | $M_A$     | $\lambda_L$ | $\lambda_2$ |
|-----|-----------|-------------|-----------|-------------|-------------|
| BP1 | 850.0 GeV | 854.0 GeV   | 858.0 GeV | 0.02        | 0.1         |
| BP2 | 710.0 GeV | 712.0 GeV   | 711.0 GeV | 0.11        | 0.1         |

**Table:** Benchmark values (BP) of parameters affecting the RG evolution of the quartic couplings. For each BP, two values of  $M$ , namely, 110 TeV and  $10^9$  TeV, have been used.

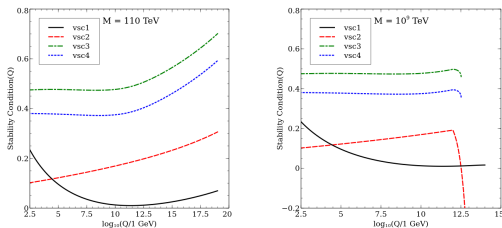


**Figure:** RG running of different scalar quartic couplings corresponding to BP1. The solid, dashed, dashed dotted and dotted lines denote the evolution curves of the stability conditions vsc1, vsc2, vsc3 and vsc4 respectively.

## Results: $M_H > 500$ GeV regime

- The theoretically allowed parameter space is fully consistent with the Higgs to diphoton LHC data in this case.
- The parameter space valid until the Planck scale and corresponding to  $M = 110$  TeV shrinks significantly for  $M = 10^9$  TeV.
- Interestingly,  $y_\nu$  becomes large  $\mathcal{O}(10^{-1})$  for  $M = 10^9$  TeV. Such a large yukawa coupling contributes to the beta function of  $\lambda_2$  through the terms  $+\lambda_2 y_\nu^2$  and  $-y_\nu^4$  that either makes  $\lambda_2$  perturbative in some cases or  $\lambda_2$  negative and the vacuum unstable in other.
- The above argument best demonstrated through a display of RG evolution of  $\lambda_2$ .

## Results: $M_H > 500$ GeV regime



**Figure:** RG running of different scalar quartic couplings corresponding to BP2. The solid, dashed, dashed dotted and dotted lines denote the evolution curves of the stability conditions vsc1, vsc2, vsc3 and vsc4 respectively.

## Constraints:Theoretical

- Unitarity: A further set of conditions come on demanding unitarity of the scattering matrix comprising all  $2 \rightarrow 2$  channels involving, by the optical theorem. Each distinct eigenvalue (shown below) of the aforementioned amplitude matrix be bounded above at  $8\pi$ .

$$a_{\pm} = \frac{3}{2}(\lambda_1 + \lambda_2) \pm \sqrt{\frac{9}{2}(\lambda_1 - \lambda_2)^2 + (2\lambda_3 + \lambda_4)^2}$$

$$b_{\pm} = \frac{1}{2}(\lambda_1 + \lambda_2) \pm \sqrt{\frac{1}{4}(\lambda_1 - \lambda_2)^2 + \lambda_5^2},$$

$$c_{\pm} = d_{\pm} = \frac{1}{2}(\lambda_1 + \lambda_2) \pm \sqrt{\frac{1}{4}(\lambda_1 - \lambda_2)^2 + \lambda_5^2},$$

$$e_1 = (\lambda_3 + 2\lambda_4 - 3\lambda_5),$$

$$e_2 = (\lambda_3 - \lambda_5),$$

$$f_1 = f_2 = (\lambda_3 + \lambda_4),$$

$$f_+ = (\lambda_3 + 2\lambda_4 + 3\lambda_5),$$

$$f_- = (\lambda_3 + \lambda_5).$$

(7)

# One-loop beta functions

The RG equations for the gauge couplings, for this model, are given by [?],

$$16\pi^2 \frac{dg_s}{dt} = -7g_s^3,$$

$$16\pi^2 \frac{dg}{dt} = -3g^3,$$

$$16\pi^2 \frac{dg'}{dt} = 7g'^3.$$

Here  $g'$ ,  $g$  and  $g_s$  denote the  $U(1)$ ,  $SU(2)_L$  and  $SU(3)_c$  gauge couplings respectively.

# One-loop beta functions

$$16\pi^2 \frac{d\lambda_1}{dt} = 12\lambda_1^2 + 4\lambda_3^2 + 4\lambda_3\lambda_4 + 2\lambda_4^2 + 2\lambda_5^2 + \frac{3}{4}(3g^4 + g'^4 + 2g^2g'^2) - \lambda_1(9g^2 + 3g'^2 - 12y_t^2 - 12y_b^2 - 4y_\tau^2) - 12y_t^4,$$

$$16\pi^2 \frac{d\lambda_2}{dt} = 12\lambda_2^2 + 4\lambda_3^2 + 4\lambda_3\lambda_4 + 2\lambda_4^2 + 2\lambda_5^2 + \frac{3}{4}(3g^4 + g'^4 + 2g^2g'^2) - 3\lambda_2(3g^2 + g'^2 - \frac{4}{3}y_\nu^2) - 4y_\nu^4,$$

$$16\pi^2 \frac{d\lambda_3}{dt} = (\lambda_1 + \lambda_2)(6\lambda_3 + 2\lambda_4) + 4\lambda_3^2 + 2\lambda_4^2 + 2\lambda_5^2 + \frac{3}{4}(3g^4 + g'^4 - 2g^2g'^2) - \lambda_3(9g^2 + 3g'^2 - 6y_t^2 - 6y_b^2 - 2y_\tau^2 - 2y_\nu^2),$$

$$16\pi^2 \frac{d\lambda_4}{dt} = 2(\lambda_1 + \lambda_2)\lambda_4 + 8\lambda_3\lambda_4 + 4\lambda_4^2 + 8\lambda_5^2 + 3g^2g'^2 - \lambda_4(9g^2 + 3g'^2 - 6y_t^2 - 6y_b^2 - 2y_\tau^2 - 2y_\nu^2),$$

$$16\pi^2 \frac{d\lambda_5}{dt} = (2\lambda_1 + 2\lambda_2 + 8\lambda_3 + 12\lambda_4)\lambda_5 - \lambda_5(9g^2 + 3g'^2 - 6y_b^2 - 2y_\tau^2 - 6y_t^2 -$$

$$\begin{aligned}
16\pi^2 \frac{dy_b}{dt} &= y_b \left( -8g_s^2 - \frac{9}{4}g^2 - \frac{5}{12}g'^2 + \frac{9}{2}y_b^2 + y_\tau^2 + \frac{3}{2}y_t^2 \right), \\
16\pi^2 \frac{dy_t}{dt} &= y_t \left( -8g_s^2 - \frac{9}{4}g^2 - \frac{17}{12}g'^2 + \frac{9}{2}y_t^2 + y_\tau^2 + \frac{3}{2}y_b^2 \right), \\
16\pi^2 \frac{dy_\tau}{dt} &= y_\tau \left( -\frac{9}{4}g^2 - \frac{15}{4}g'^2 + 3y_b^2 + 3y_t^2 + \frac{1}{2}y_\nu^2 + \frac{5}{2}y_\tau^2 \right), \\
16\pi^2 \frac{dy_\nu}{dt} &= y_\tau \left( -\frac{9}{4}g^2 - \frac{3}{4}g'^2 - \frac{3}{4}y_\tau^2 + \frac{5}{2}y_\nu^2 \right).
\end{aligned}$$