

Optical frequency combs and their applications

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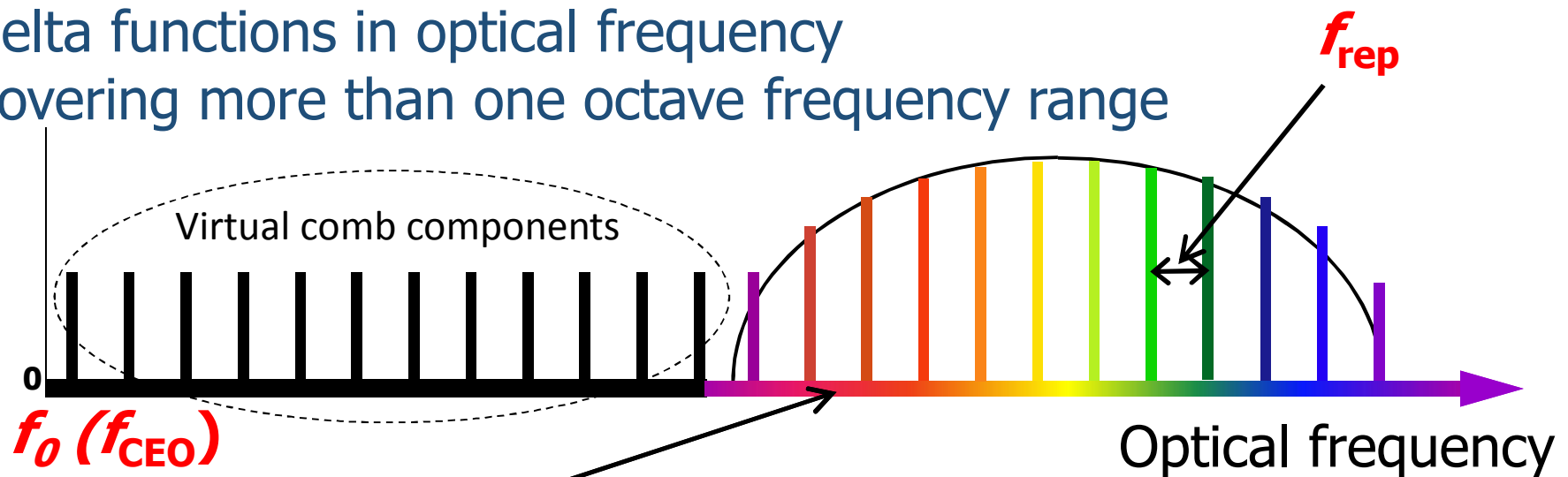
⁴ *JST, ERATO, MINOSHIMA Intelligent Optical Synthesizer Project*

What is an optical frequency comb?

Optical frequency components with equal frequency spacing

Delta functions in optical frequency

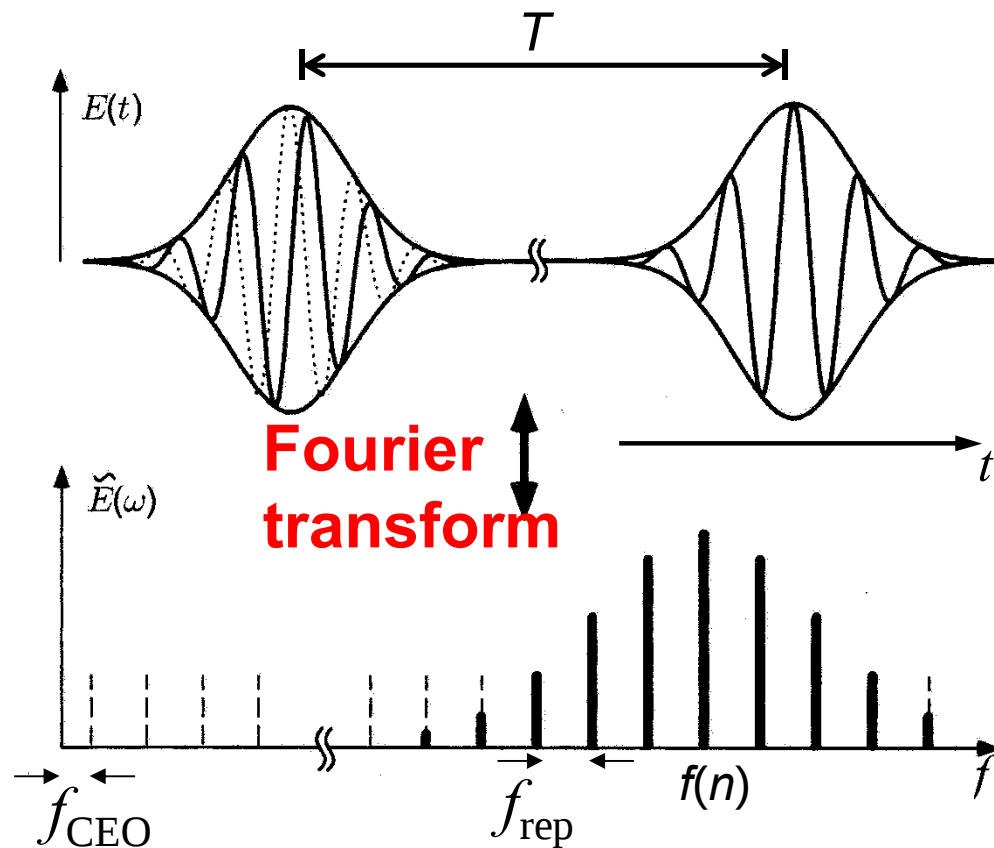
Covering more than one octave frequency range



**Precise optical
frequency ruler for
measurements**

Comb, コム (コーム)、櫛 (くし)

Optical frequency comb based on femtosecond mode-locked lasers



The Fourier transform relation between time and frequency axes:

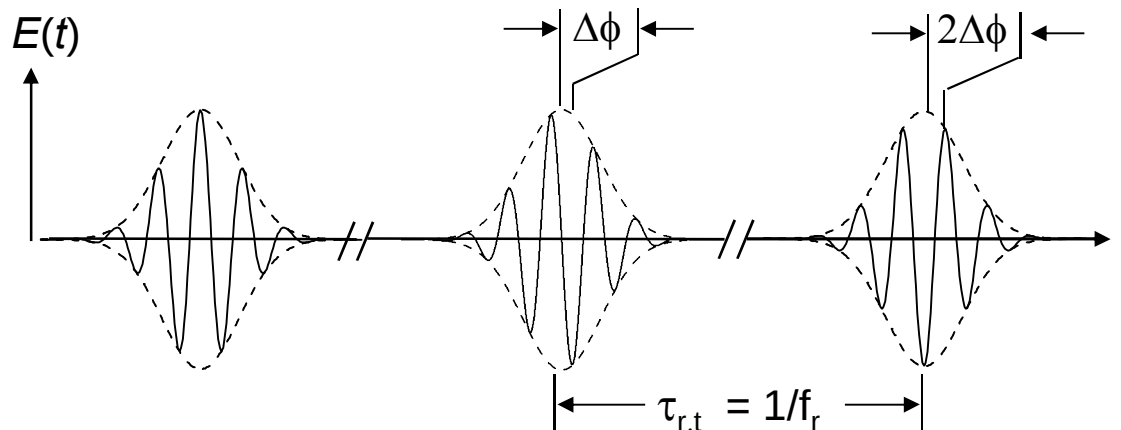
$$f_{\text{rep}} = 1/T$$

Shorter pulse width, larger frequency span

Ref.: Th. Udem *et al.*, *Phy. Rev. Lett.*, **82**, 3568 (1999).

Carrier envelope offset frequency

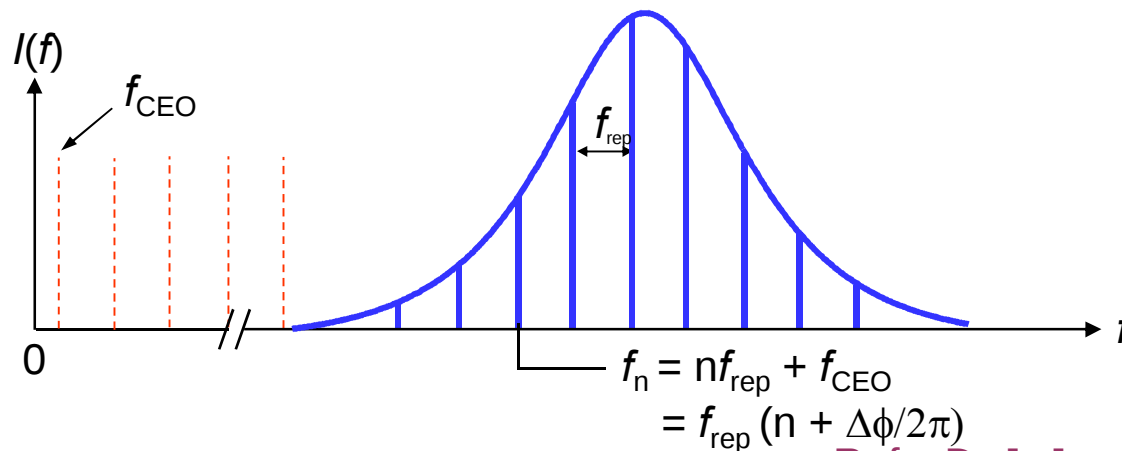
Time domain



Carrier-envelope
phase slip from pulse
to pulse because:

$$V_g \neq V_p$$

Frequency domain

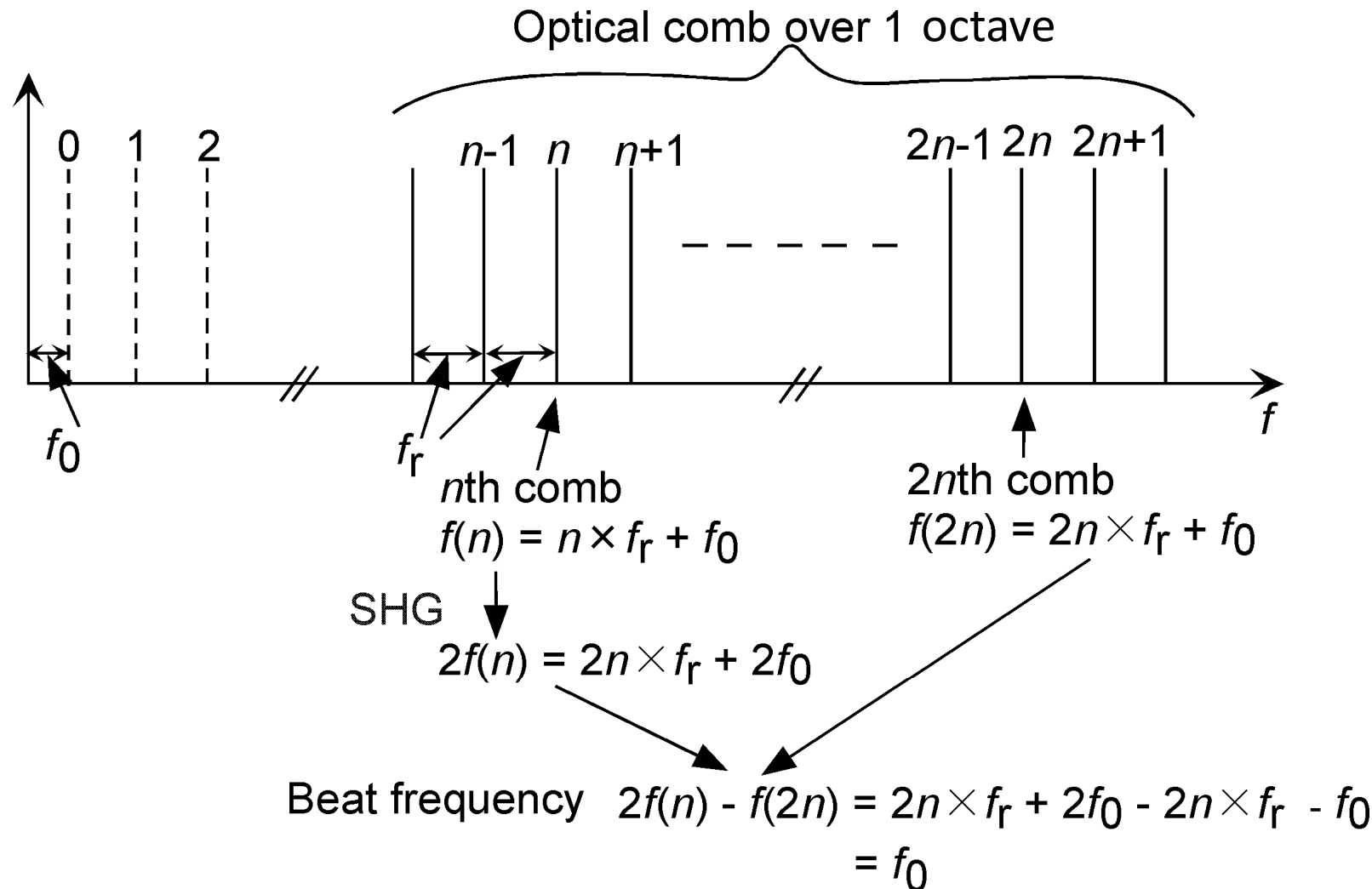


Modes are offset from
harmonics of f_r by:

$$f_{\text{CEO}} = f_{\text{rep}} \Delta\phi / 2\pi$$

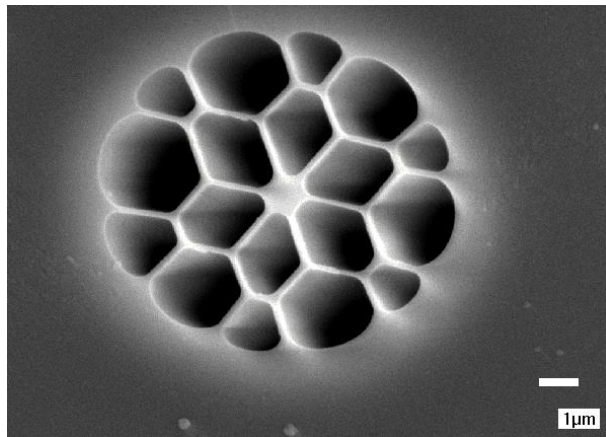
Ref.: D. J. Jones *et al.*, Science, **288**, 635 (2000).

$f/2f$ interferometer for observing f_0 (f_{CEO})



Ref.: D. J. Jones *et al.*, Science, **288**, 635 (2000).

Photonic crystal fiber (PCF)



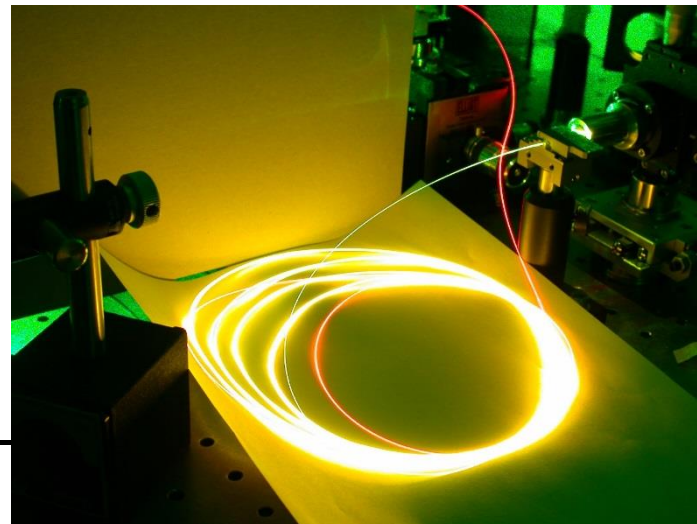
Photonic crystal fiber (PCF)

Ref.: J. C. Knight, Nature, 424, 847 (2003).

Ç Zero dispersion at 800 nm, the center wavelength of a Ti:sapphire laser

Ç Pulse remains high peak

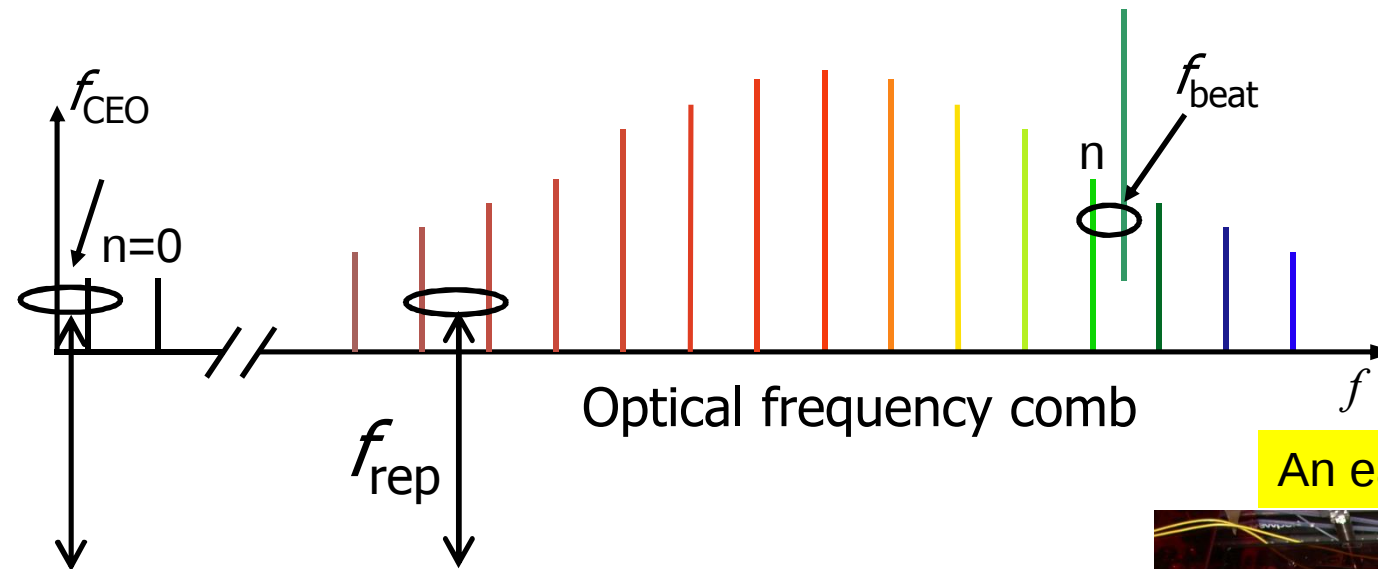
Ç Spectrum broadened by self phase modulation or four wave mixing process



More than one octave spectrum

A precise optical frequency ruler

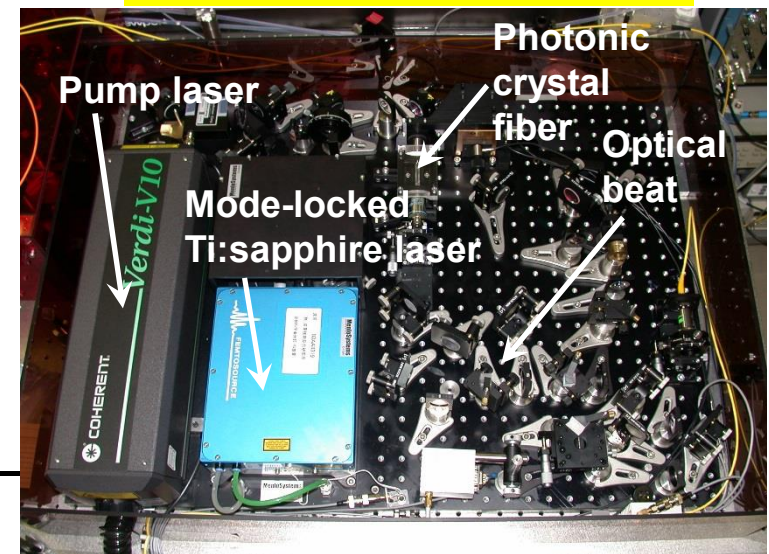
Optical frequency f_{laser}



Microwave reference frequency

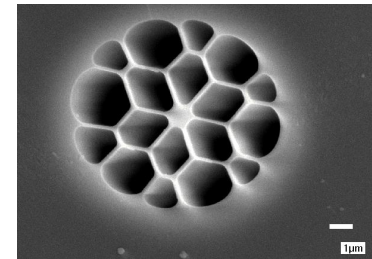
$$f_{\text{laser}} = f_{\text{CEO}} + n \cdot f_{\text{rep}} + f_{\text{beat}}$$

An early stage Ti:s comb



From Ti:sapphire combs to fiber combs

1) Coupling the laser light into the PCF is the main issue that limits the reliability of the comb.

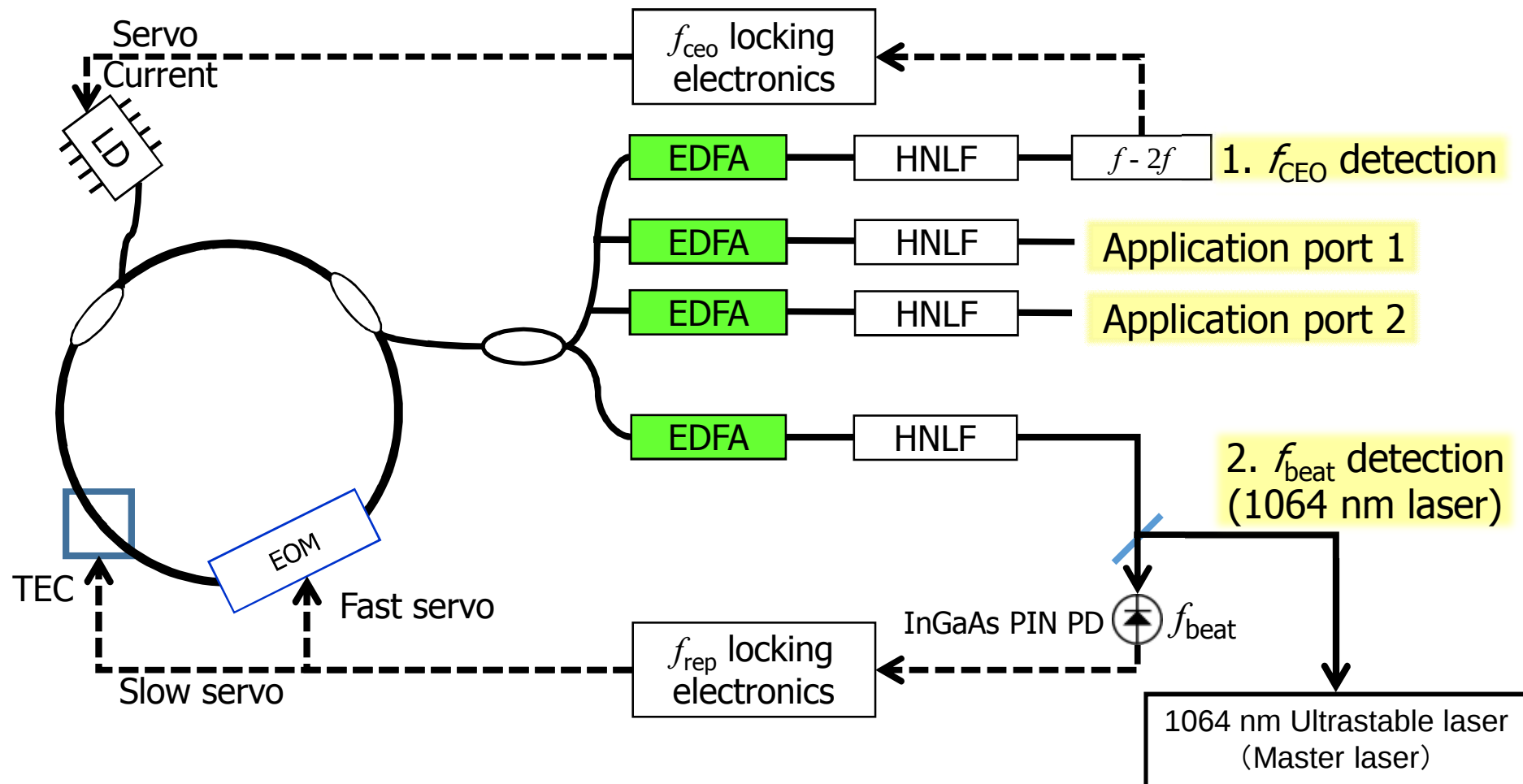


2) Pump laser is the main issue that limits the cost efficiency and also the compactness.



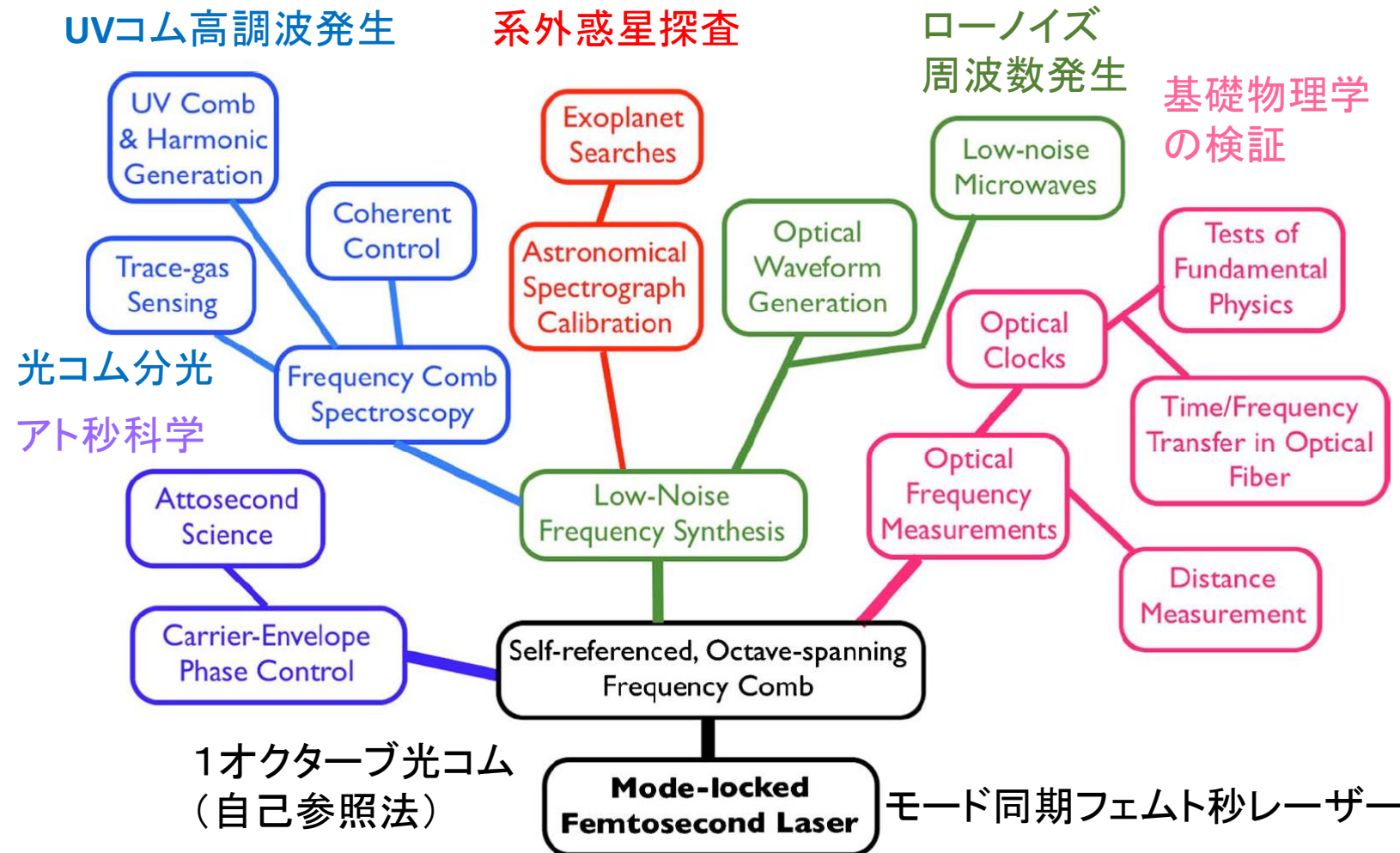
Mode-locked Er fiber laser at 1.5 μm

Multi-branch amplifiers for beat detections



K. Iwakuni *et al.*, Opt. Express 20, 13769 (2012).

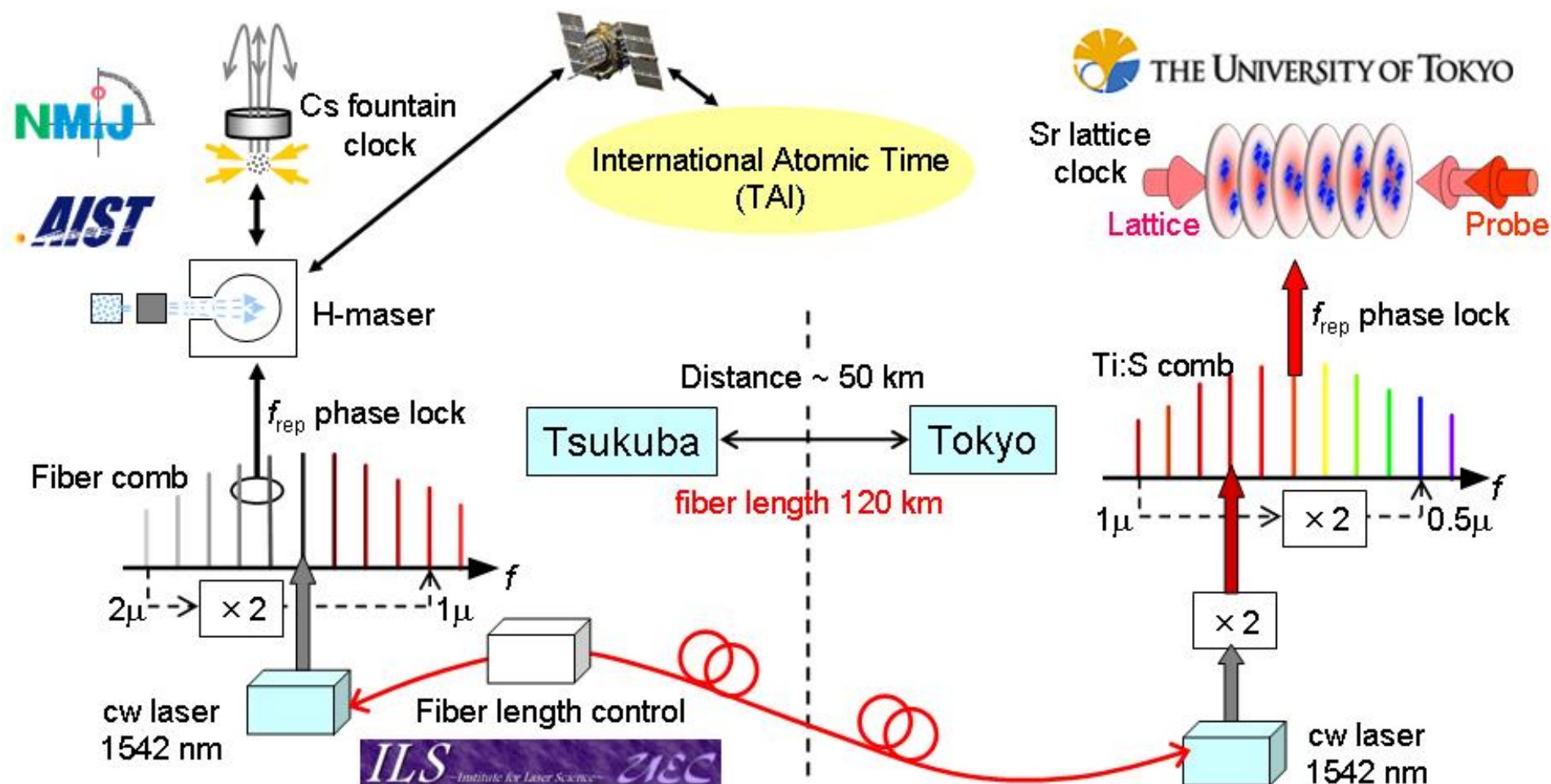
Applications of optical frequency combs



S.A. Diddams et al.: J. Opt. Soc. Am. B 27, B 51(2010).

大苗、洪: 応用物理 84, 30 (2015).

Application in precision measurement



F.-L. Hong *et al.*, Opt. Lett. **34**, 692 (2009).

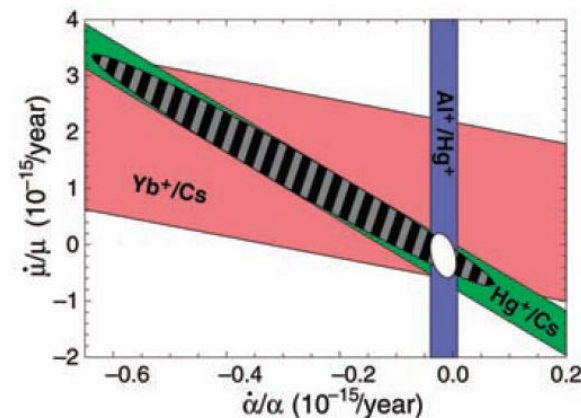
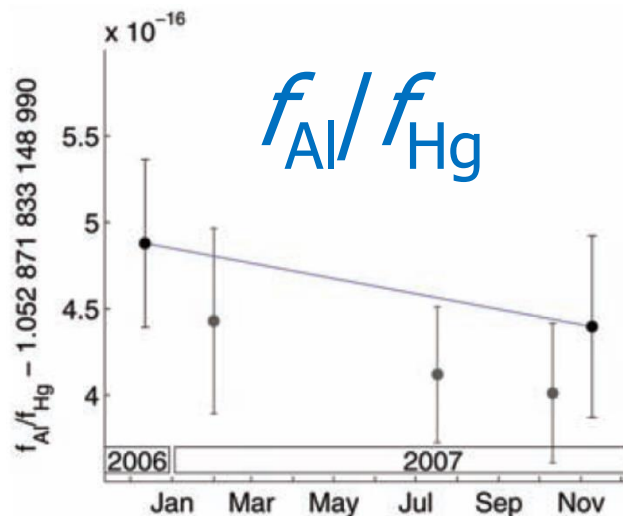
Test of the time variation of fine structure constant

$$\frac{\partial \ln \alpha}{\partial t} < 1 \cdot 10^{-17} \text{ yr}^{-1}$$

Oklo: Shlyakhter (2×10^9 yr)

$$\frac{\partial \ln \alpha}{\partial t} = (6.4 \pm 1.4) \cdot 10^{-16} \text{ yr}^{-1}$$

Quasars: J. K. Webb et al. (10^{10} yr)

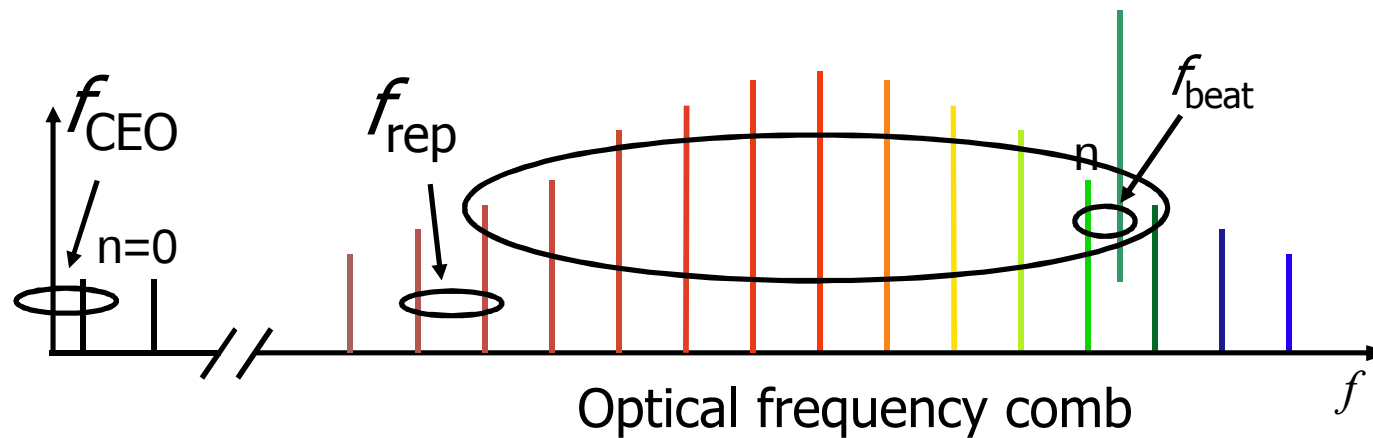


$$\dot{\alpha}/\alpha = (-1.6 \pm 2.3) \times 10^{-17} / \text{year}$$

T. Rosenband *et al.*, Science **319** (2008) 1808.

New applications of frequency combs

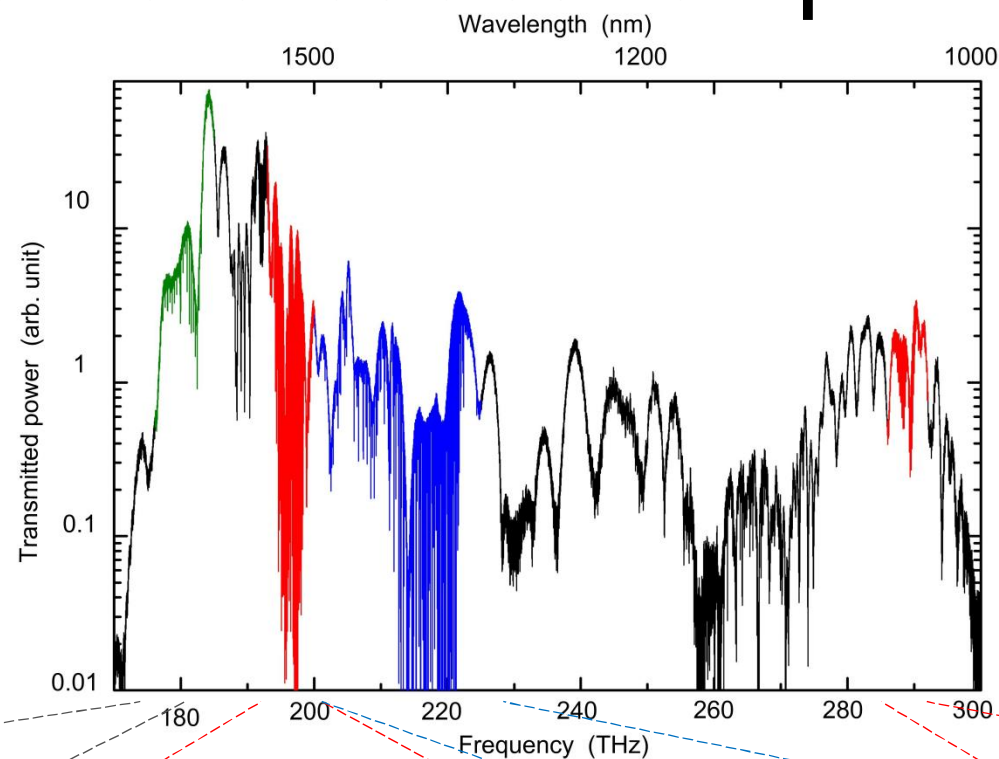
Optical frequency f_{laser}



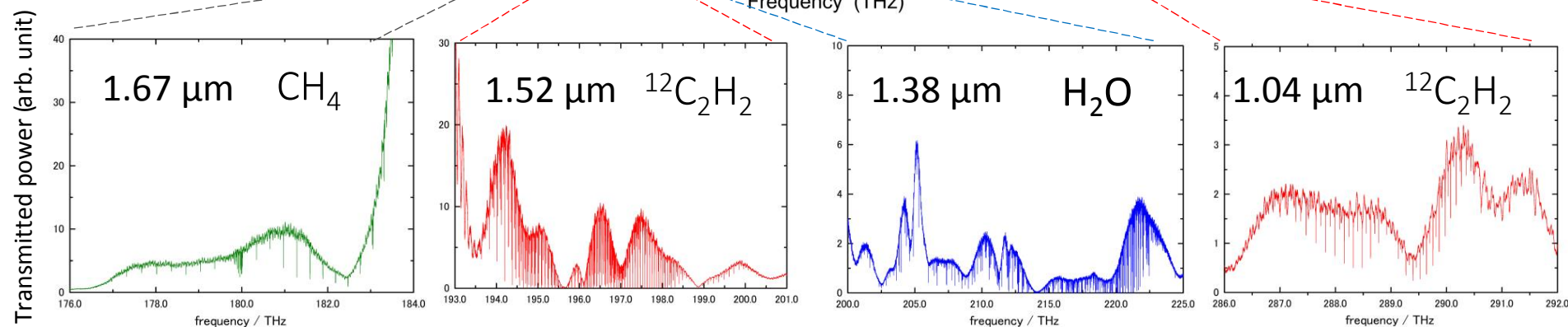
1) Dual comb spectroscopy

2) Astro comb

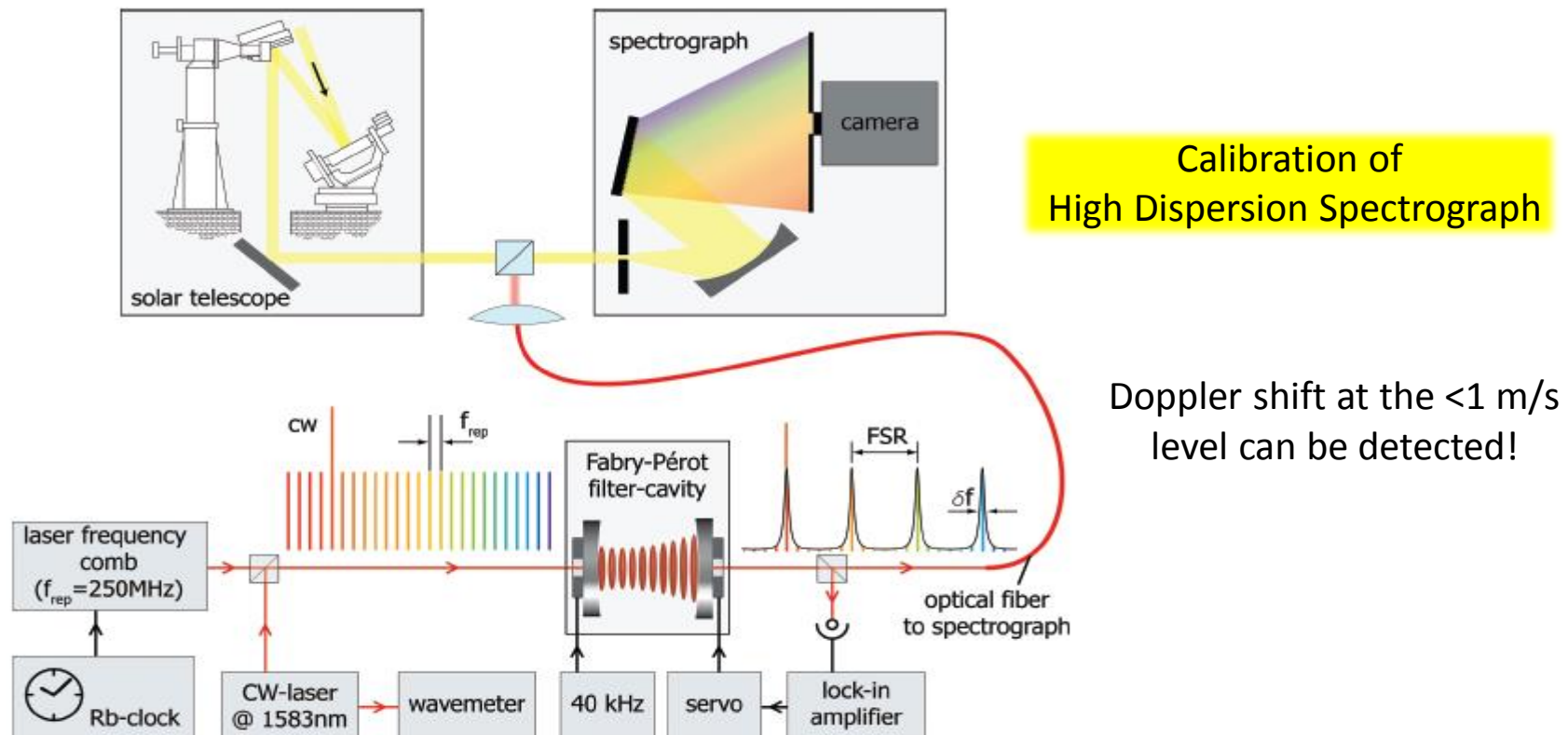
Dual comb broadband spectroscopy



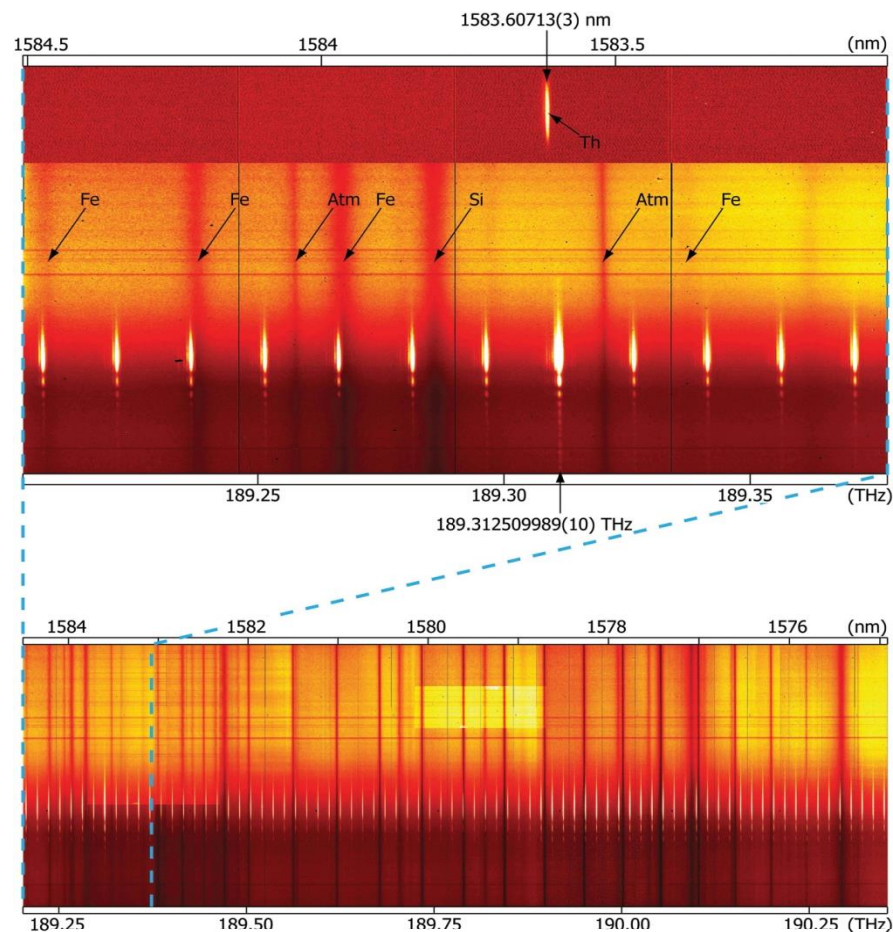
S. Okubo *et al.*, Appl. Phys. Express **8**, 082402 (2015).



Optical frequency comb for telescope



T. Steinmetz, et al., Science **321**, 1335 (2008).



Optical frequency comb
= Frequency (wavelength) ruler

T. Steinmetz, et al., Science **321**, 1335, 2008

Plan for the ERATO astro comb

The ERATO astro comb:

- Covering wavelength range from 380 ñ 540 nm with a frequency spacing of 20 GHz
- To be installed at the Okayama Astrophysical Observatory



Summary

- ÇIntroduction of frequency combs
- ÇFiber based frequency combs
- ÇApplications of frequency combs
- ÇAn astro comb for Okayama Astrophysical Observatory

Thank you for your attention!