

PhyStat-Nu, Kavli IPMU

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Neutrino Nucleus Cross Section Experiments

Morgan O. Wascko



Imperial College London & KEK

Outline

- Introduction to accelerator neutrinos
- Neutrino oscillation: the motivation for new cross section measurements
- Common analysis methods
- Model independent measurements
- Personal perspective on what else we could do
- Conclusion

Accelerator Neutrinos

- Accelerator neutrino experiments were born in the 1960s and came of age in the 1970s
- 1960s - First pion decay beam, first focussing horns
- 1970s - Development of big bubble chambers
- Important physics legacies
 - Discovery of 2nd generation of neutrinos
 - Discovery of neutral currents
 - Tests of EW theory

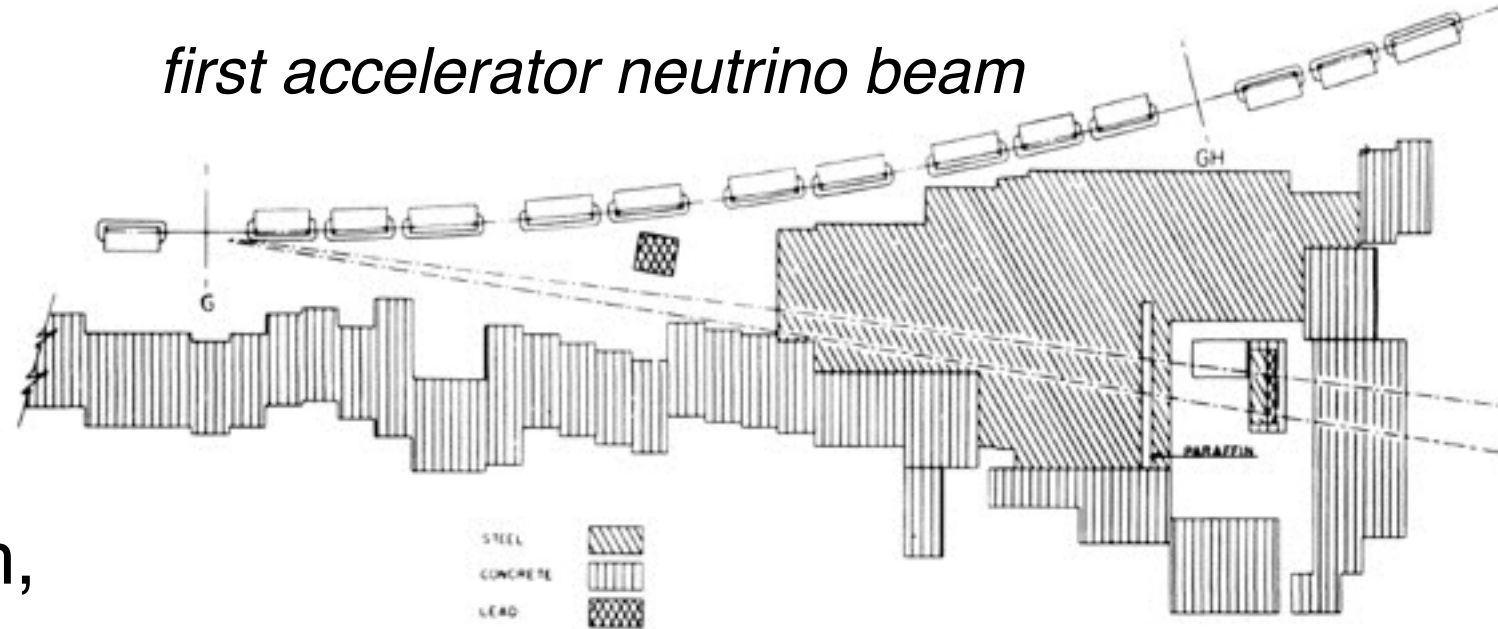
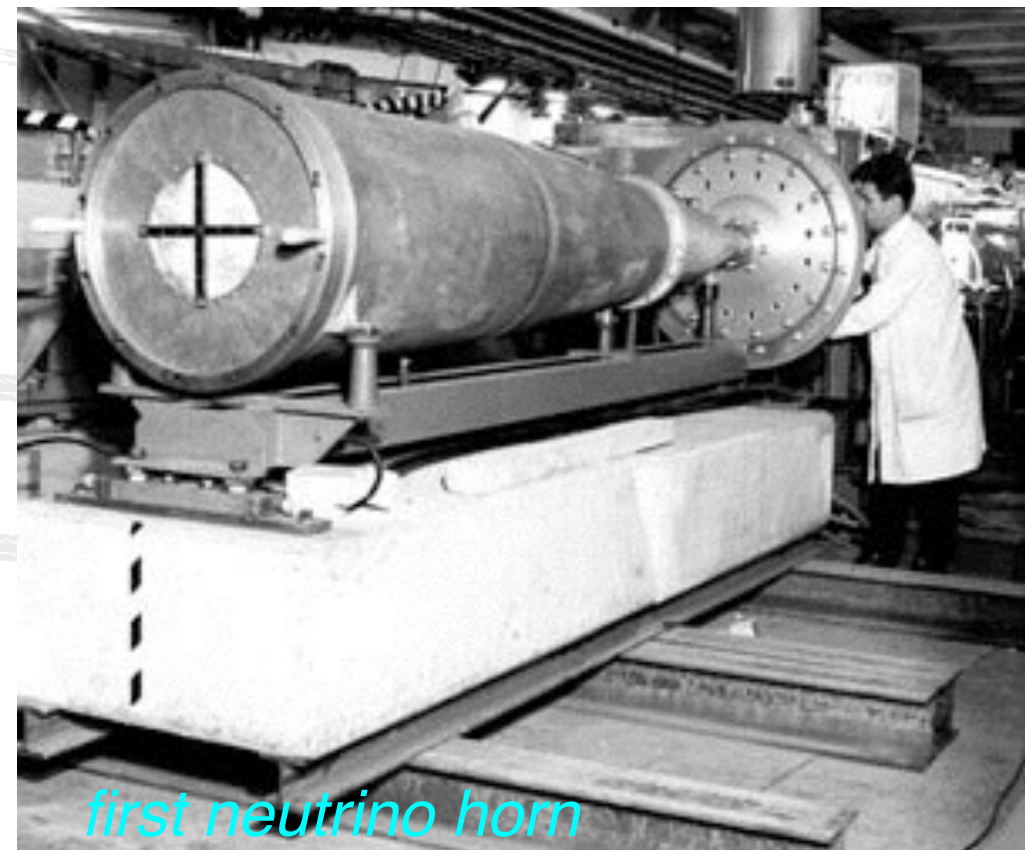
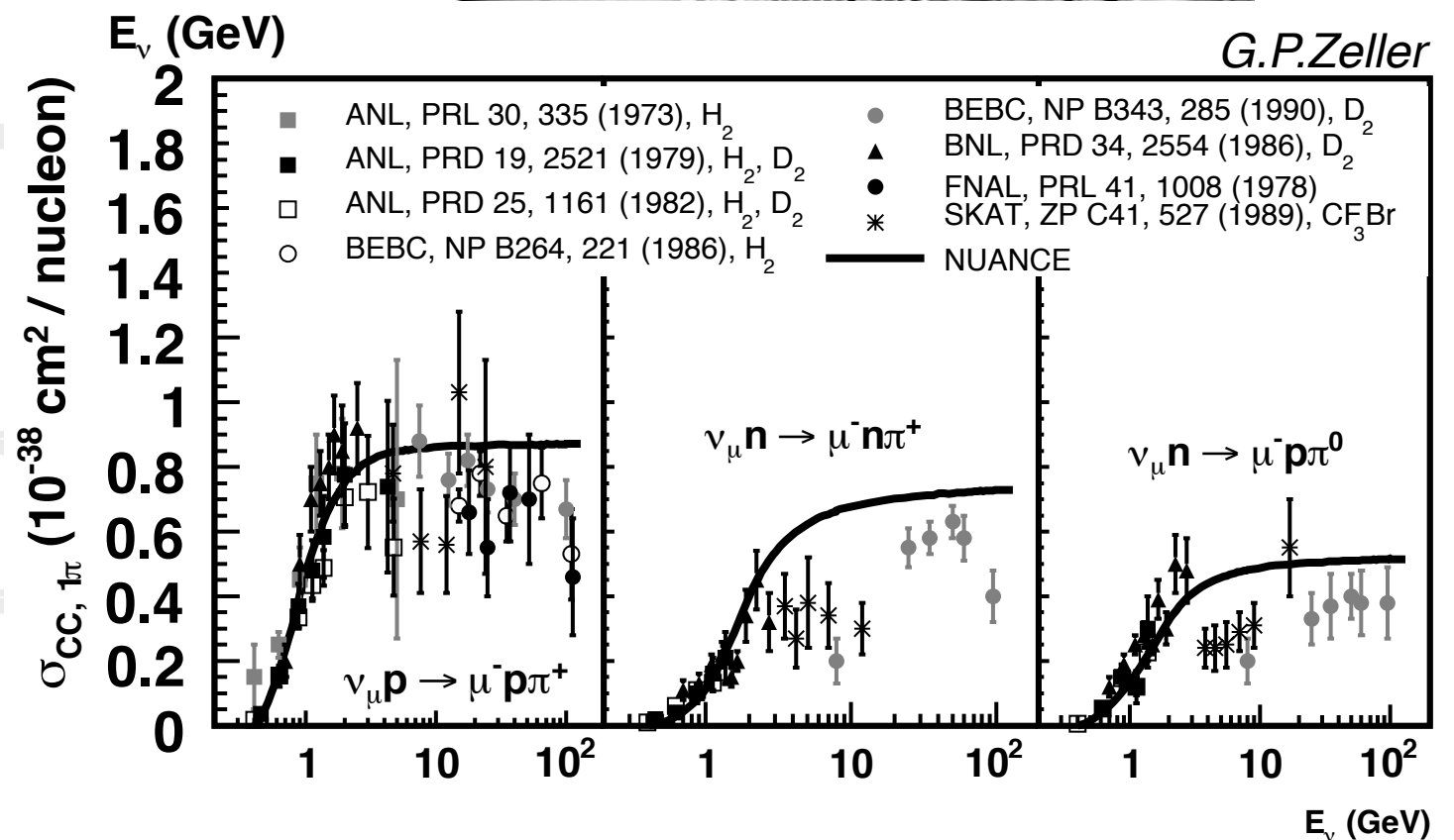
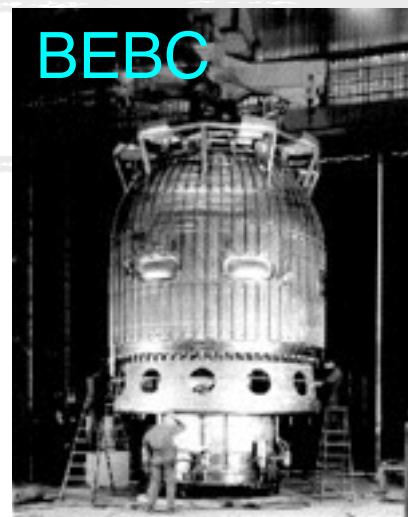
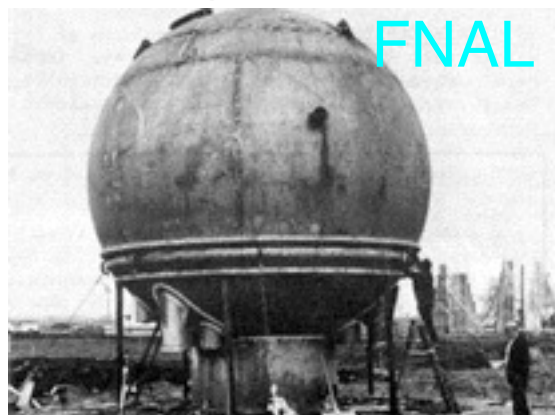
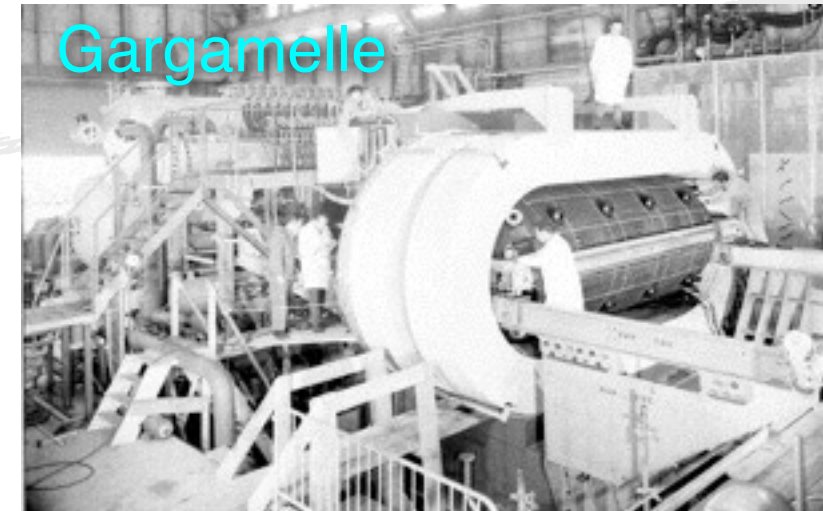
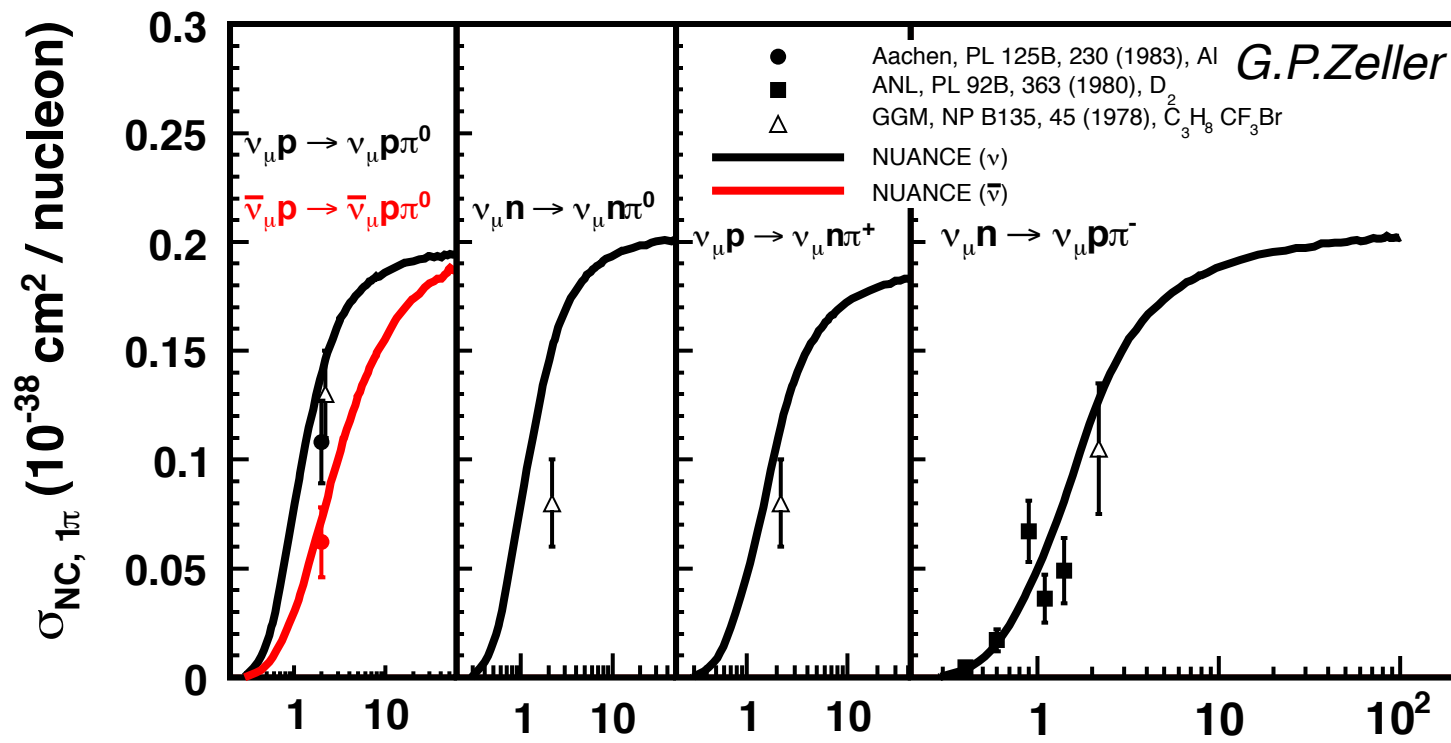


FIG. 1. Plan view of AGS neutrino experiment.



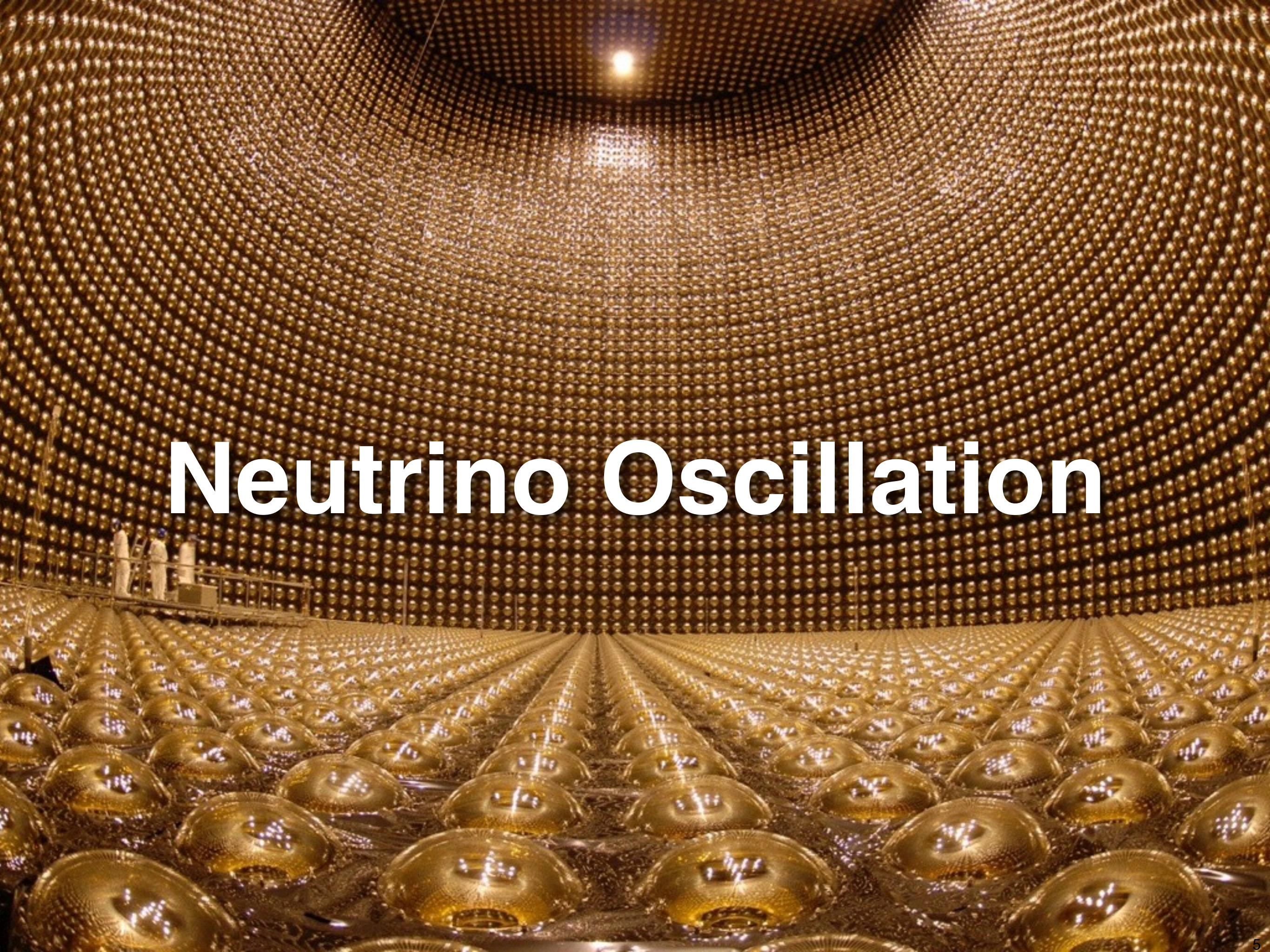
Early neutrino data

From discovery to
(precision) measurements...



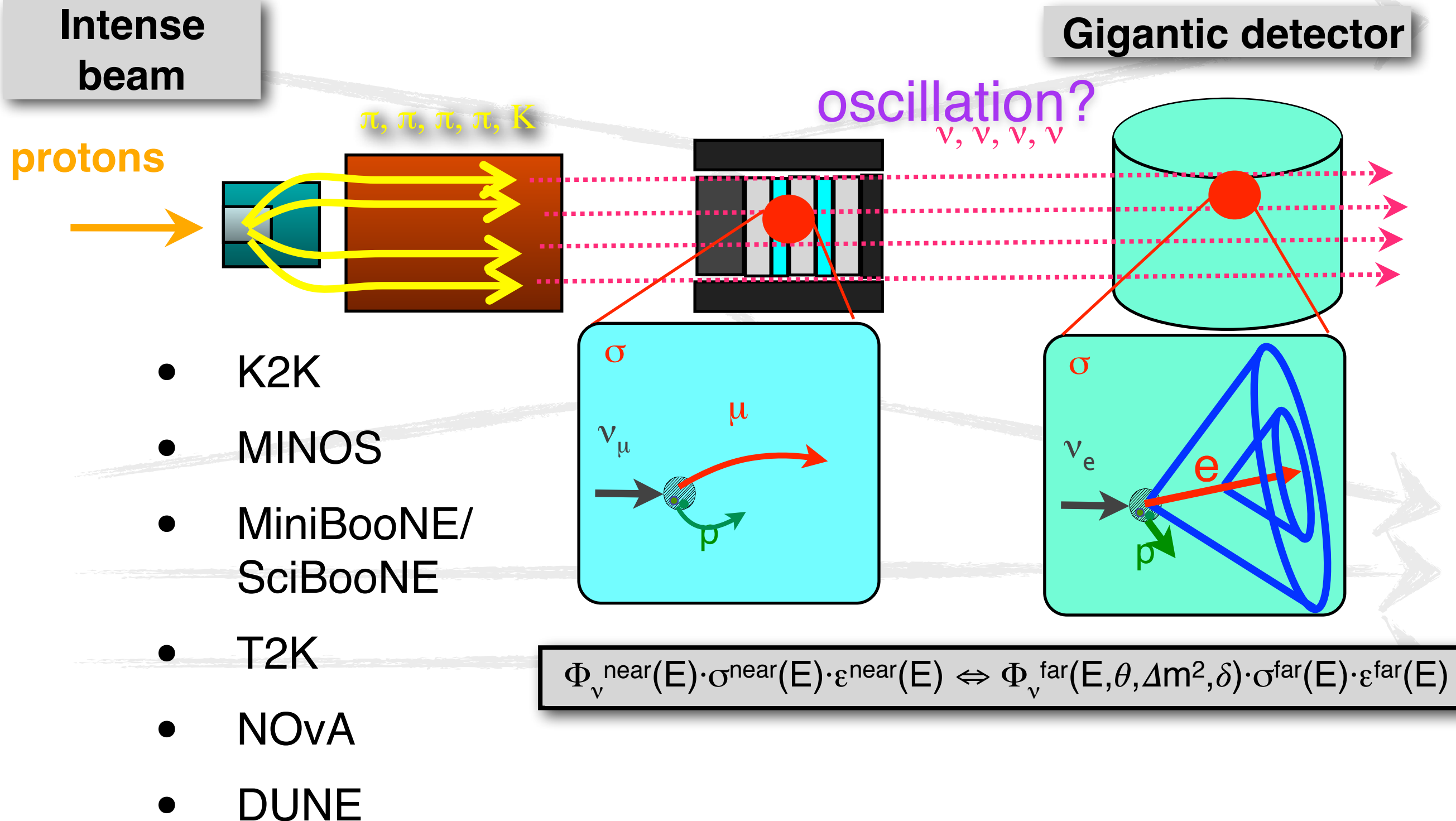
Plots from the PDG!

Neutrino Oscillation



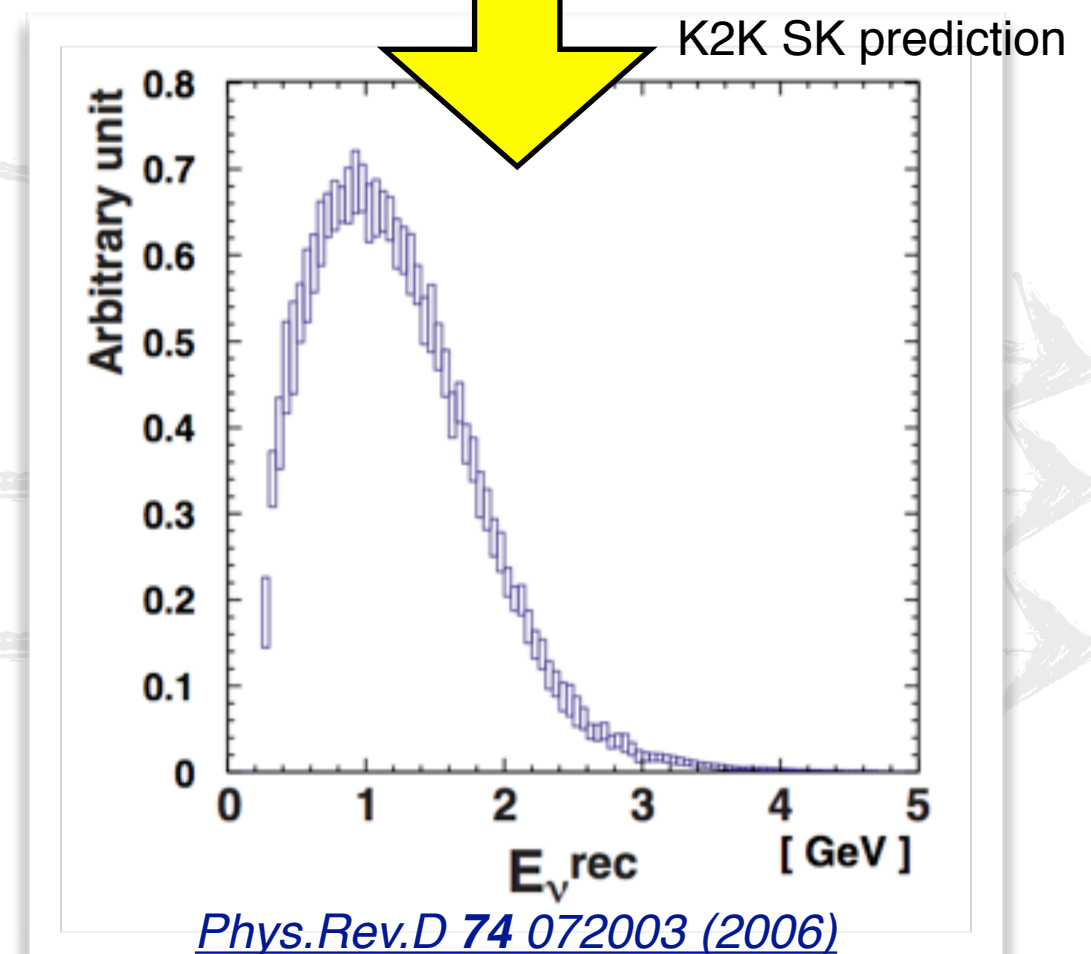
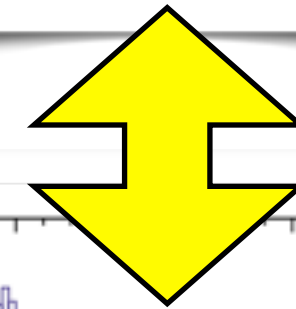
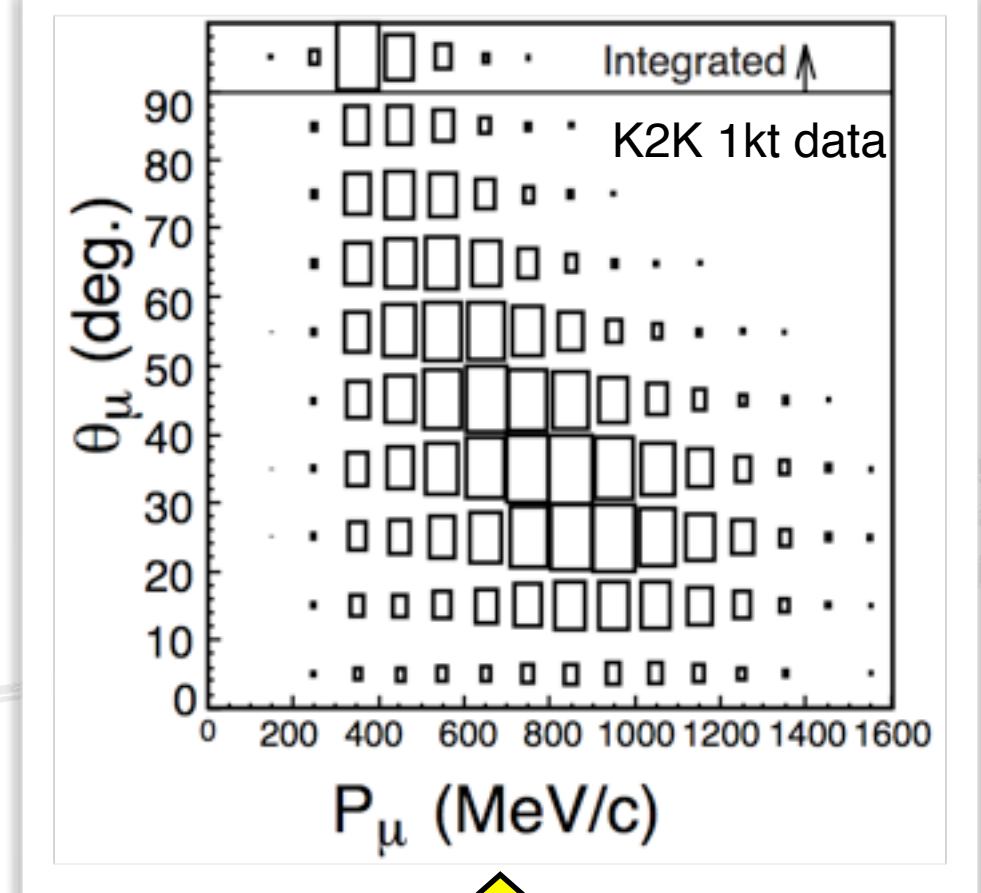
Accelerator ν Experiments

Search for δ_{CP} by comparing $\nu_{\mu} \rightarrow \nu_e$ and $\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e$.



What do we need?

- Need to predict event rates and kinematics of final state particles
 - Need to accurately calculate inferred (physics) variables from our observed variables
 - For oscillations, need to reconstruct neutrino energy
 - different ways to do this
 - all beams are relatively wideband
 - Need to accurately predict background contamination
- ➡ Need to understand neutrino-nucleus cross-sections precisely
- ➡ Need good models



Xsecs and Oscillations

- Cross section **models** used by experiments cannot describe observations by: K2K, MiniBooNE, SciBooNE, MINERvA, T2K, ...

- Leads to inflation of systematic uncertainties

- Model dependence often injected into data analysis

- Inferred variables
 - Energy, Q^2 reconstruction
 - Background subtraction

- Using these models will always give such uncertainties.

- Need to use better models!

Systematic uncertainties reported by the world's most sensitive ν_e appearance experiments vs. time

Experiment	xsec err (%)	total err (%)
MiniBooNE (2007)	12.3	17.6
T2K (2012)	7.5	10.3
T2K (2016)	4%	6%

*How are we improving the errors?
Using better models!*

A photograph of four children of diverse backgrounds gathered around a laptop. A girl with blonde braids is pointing at the screen. A boy with dark hair is looking intently. A girl with dark hair in pigtails is also looking. A boy with blonde hair is looking from the side. The text 'Analysis Methods' is overlaid in large black font.

Analysis Methods

Method 1: template fit

Compare data to MC, within context of a model, using templates.

$$\sigma_i = f_i \langle \sigma^{pred} \rangle_i = \frac{f_i N_i^{pred} P_i}{\epsilon_i T \Phi_i}$$

i = bin of xsec variable

f_i = normalisation factor

N_i^{pred} = predicted # of events

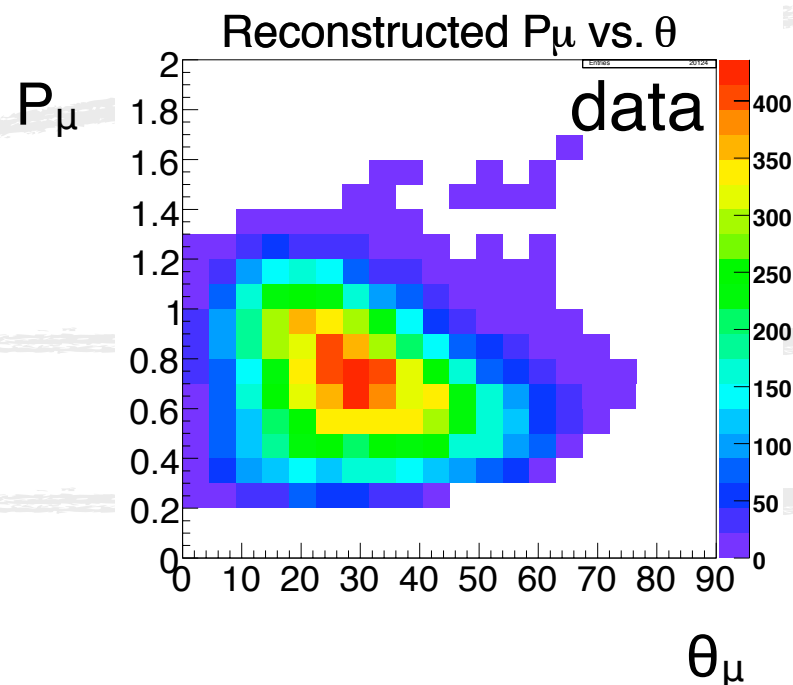
P_i = purity

ϵ_i = efficiency

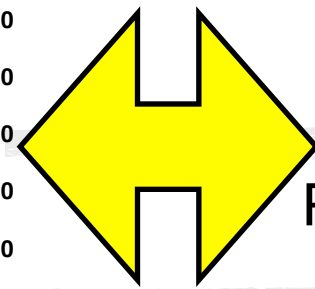
T = number of nuclear targets

Φ_i = neutrino flux per bin

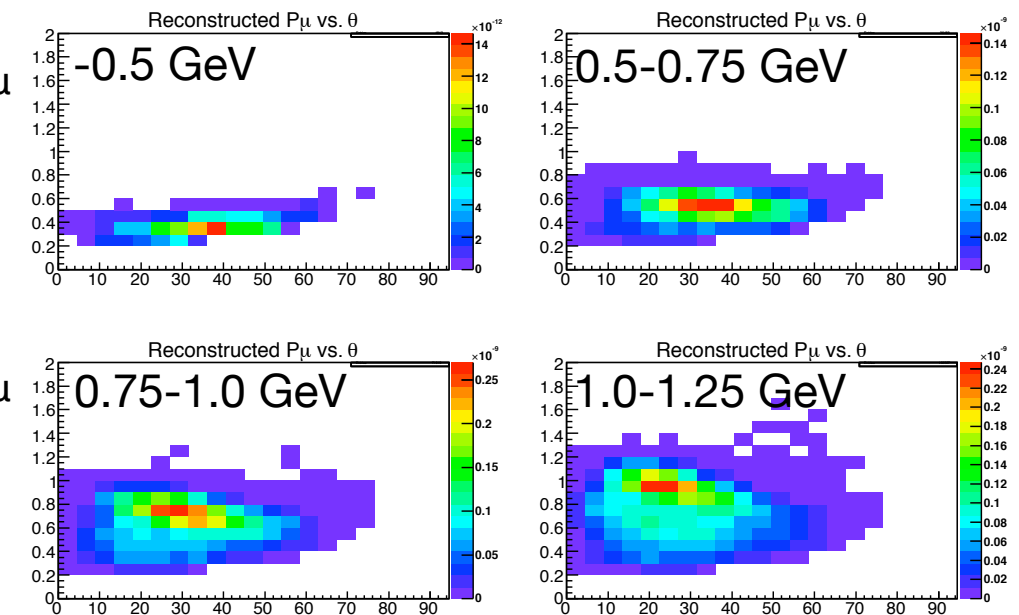
Templates can be produced in observed dynamical variables, different from xsec variable.



SciBooNE



MC template (MRD-stop)

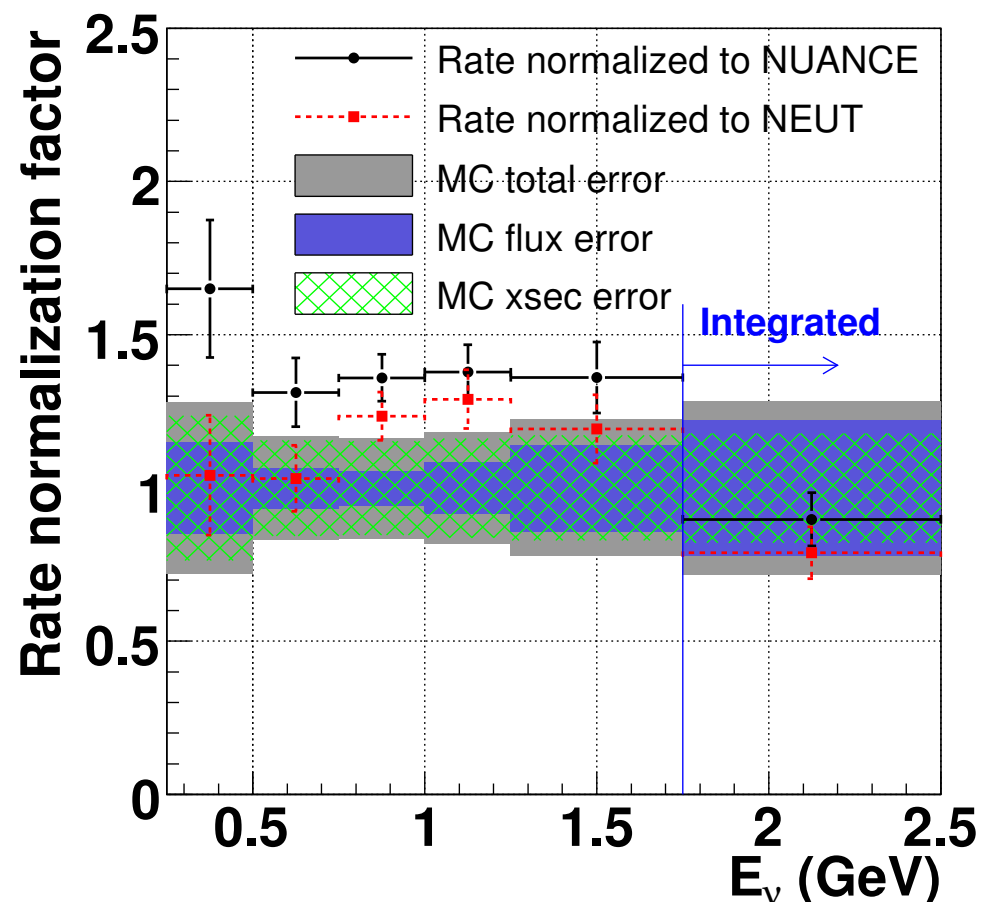


Method 1: template fit

Fit for values of f_i that minimise some GoF parameter (χ^2 , likelihood), and use MC to infer the measured value of cross section.

$$\chi^2 = \sum_{j,k}^{Nbins} (N_j^{obs} - f_j N_j^{pred}) (V^{sys} + V^{stat})_{jk}^{-1} (N_k^{obs} - f_k N_k^{pred})$$

Uncertainties: estimated with fake data studies by repeating the template fit with MC variants.



Advantage: This method is especially useful for measuring cross sections as functions of inferred variables, like the input variable E_ν or internal variable Q^2 .

Drawback: This method is susceptible to model bias. If your MC model differs from nature in some important way, you can easily infer the wrong answer!

Method 2: Matrix unfolding

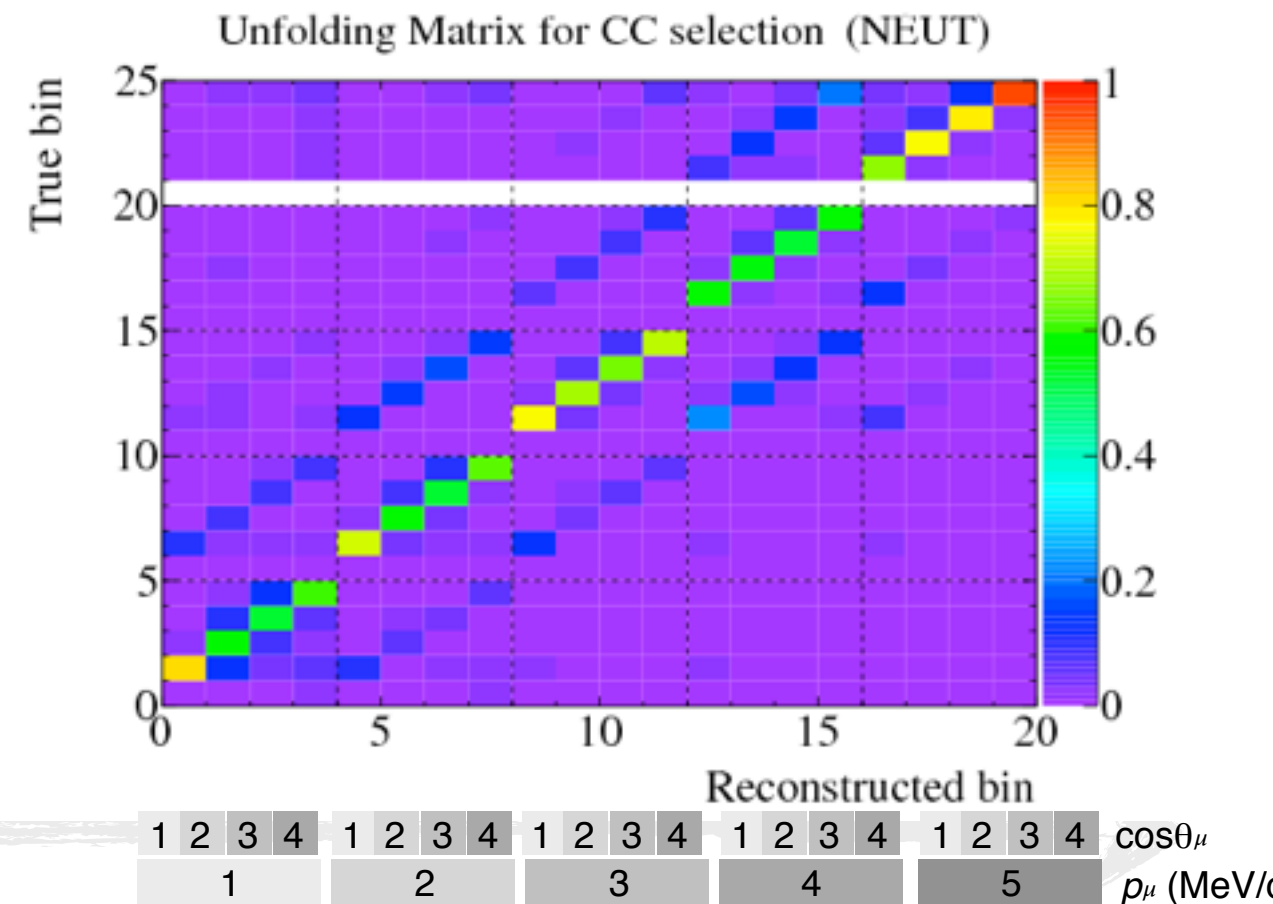
- Calculate cross section directly from number of events

$$\hat{N}_i = \frac{\sum_j U_{ij} (N_j^{obs} - B_j)}{\epsilon_i}$$

1. Apply purity correction
2. Unfold to correct detector smearing
3. Apply efficiency correction
4. Normalise with neutrino flux and number of nuclear targets to get cross section

➡ Result is flux averaged differential cross section

j = bin of reconstructed variable
i = bin of corrected ("true") variable
 N_j^{obs} = observed # of events
 B_j = background events
 U_{ij} = unfolding matrix
 ϵ_i = efficiency



$$\frac{d\sigma}{dx_i} = \frac{1}{T\Phi_\nu} \frac{\hat{N}_i}{\Delta x_i}$$

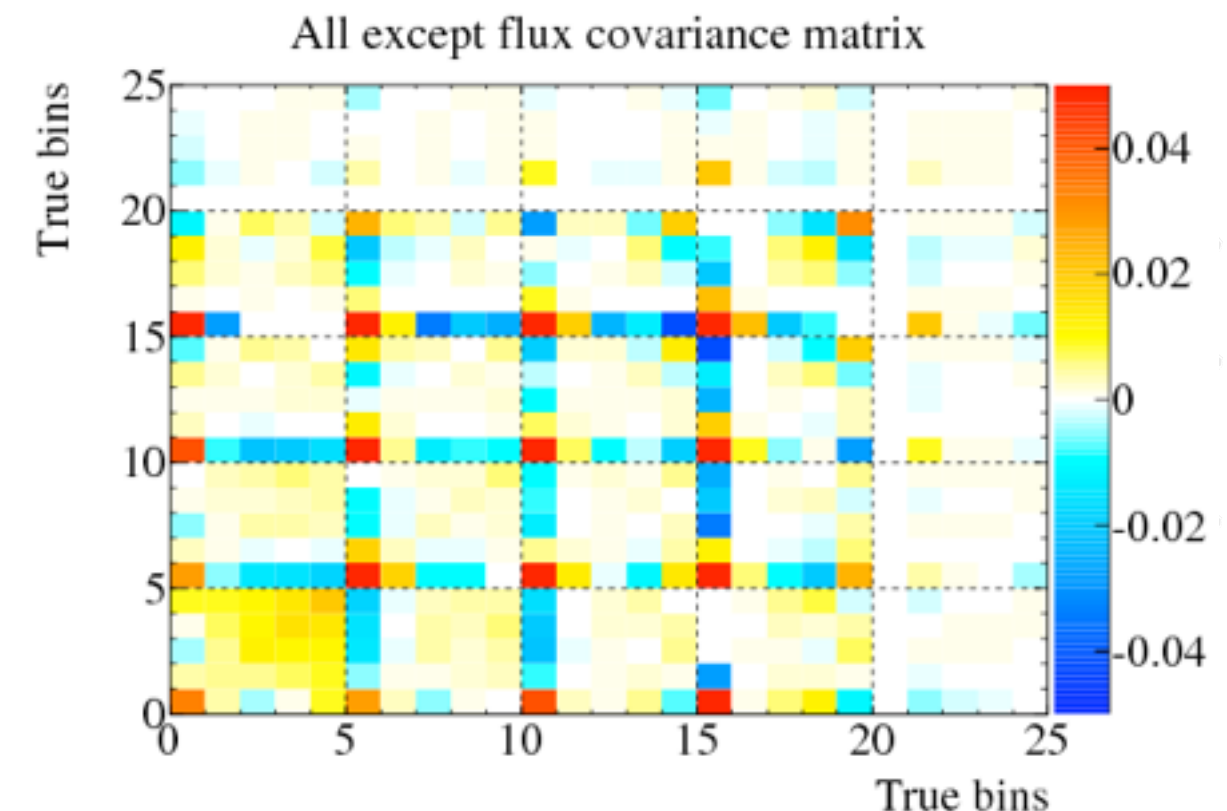
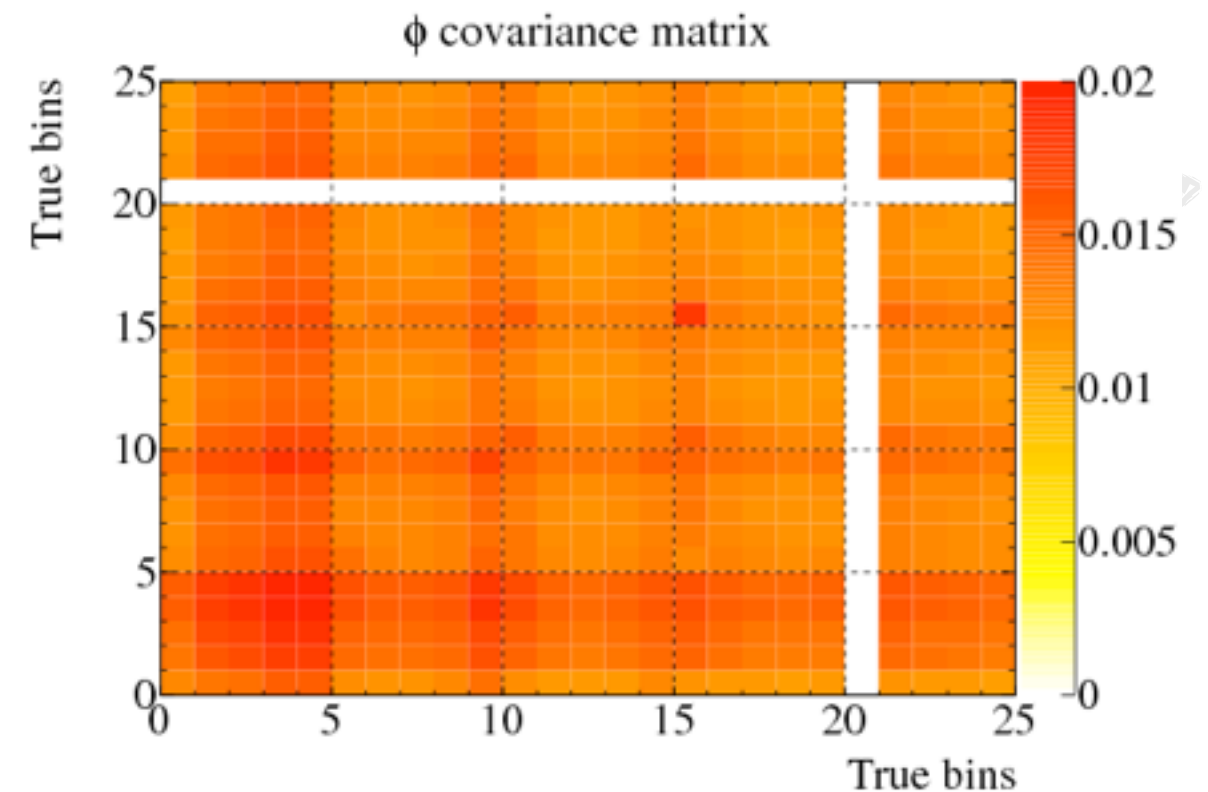
T = number of nuclear targets
 Φ_ν = total integrated neutrino flux
 Δx_i = bin width

Method 2: Matrix unfolding

$$V_{kl} = \frac{1}{N_{var}} \sum_s^{N_{var}} (\sigma_k^s - \sigma_k^{nom})(\sigma_l^s - \sigma_l^{nom})$$

- Use MC variants to create covariance matrix
- Neutrino flux is (usually) just a normalisation error
 - We do, of course, propagate the full shape covariance
- Very useful to separate out the flux error

➡ Potential for reducing model dependence with this method



Model independence

or, how do I get your assumptions out of my data?

What does model dependence mean?

- Distinguish between σ model and detector model
 - Any MC-derived quantity is, of course, model-dependent
- Restricting unsmearing, BG corrections, and efficiencies to detector MC quantities, not cross section processes is probably the best we can do
- This is why we should always publish final state particle cross sections first, and then proceed to process measurements, etc.
- Can we move to generator-less measurements??

Absolute flux-averaged differential cross section formula

U_{ij} : unsmearing matrix

N_j^{obs} : data

$$\hat{N}_i = \frac{\sum_j U_{ij} (N_j^{\text{obs}} - B_j)}{\epsilon_i}$$

ϵ_i : efficiency

b_j : background

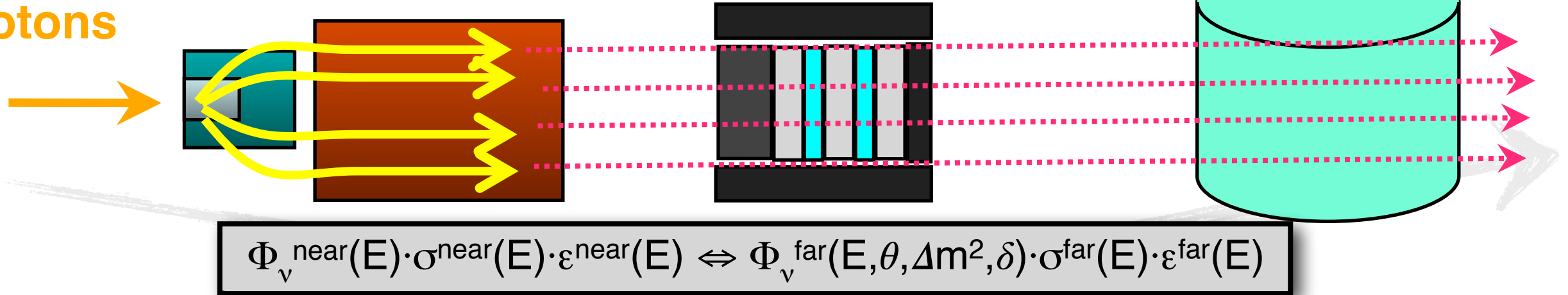
$$\frac{d\sigma}{dx_i} = \frac{1}{T\Phi_\nu} \frac{\hat{N}_i}{\Delta x_i}$$

T : integrated target number

Φ : integrated ν -flux

Is it so bad?

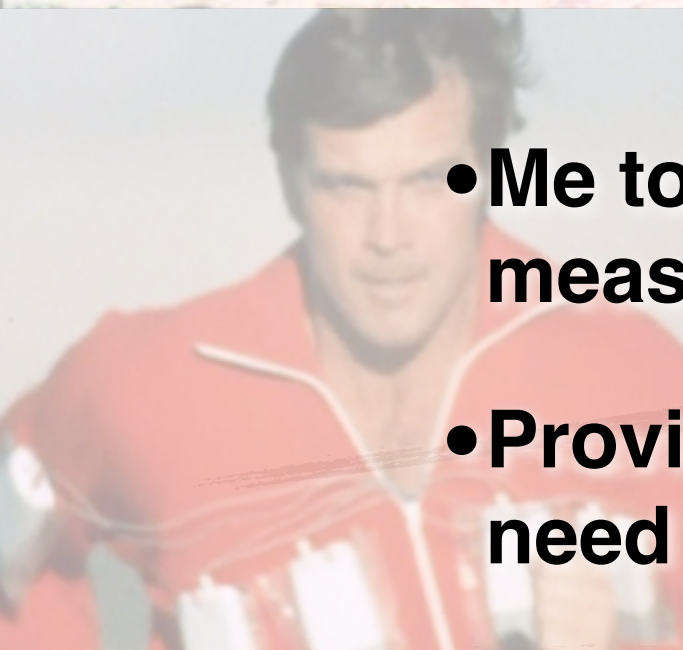
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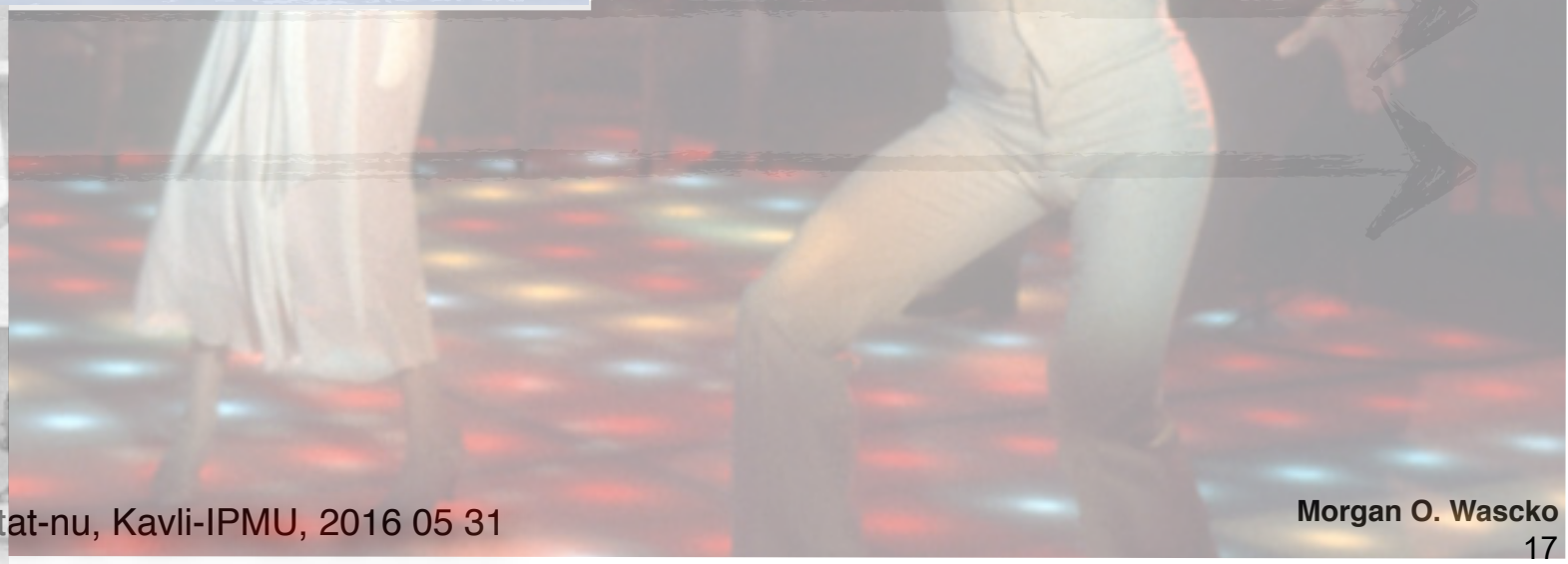
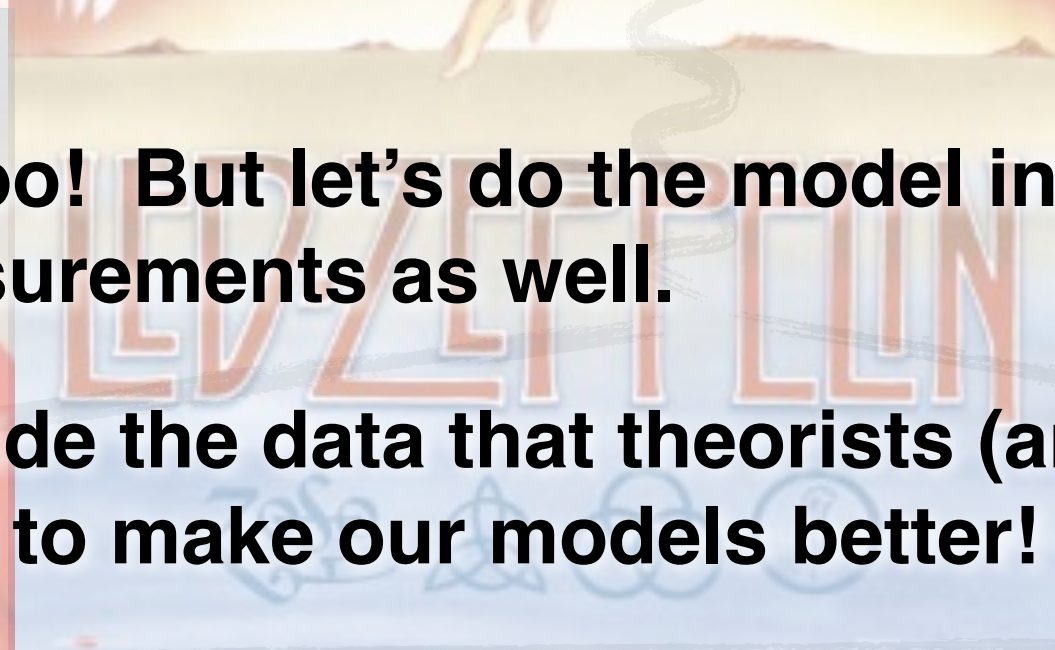
- Interaction models are useful:
 - Relate final state particles to neutrino energy, estimate systematic errors.
 - Cannot do oscillation analysis without a model, but error cancellation only works if the model matches Nature!
- Ulrich Mosel's observation, NuInt11:
 - Theorist's paradigm: "A good generator MC does not have to fit the data, provided its model is correct"
 - Experimentalist's paradigm: "A good generator MC does not have to be correct, provided it fits the data"
- We really do need model independent measurements!
 - Provide enough info for later physicists to cleanly use data with a new model.
 - Confront each model with multiple data sets



• “But I love the 70s! I want to fit for M_A !”



- Me too! But let's do the model independent measurements as well.
- Provide the data that theorists (and future you) need to make our models better!



Can we do it differently?



Best way to present data?

- *Measured quantities vs inferred quantities? How to interpret unfolded data? Generator dependencies?*
- Can we provide the tools to allow theorists to fit our data in the same way we do?
- Other fields publish data in different (and creative) ways - maybe we should consider some of these.

Best way to present data?

- To get better models, we need theorists to use our data effectively
- It's in our best interest to make that as easy as possible
- Typically, our goal is to produce cross section measurements
 - We use the detector MC to model the efficiency and smearing,
 - We then correct those effects with unfolding matrices and efficiency functions

Best way to present data?

- We could alternatively provide theorists with the tools to analyze our data *the way that we do*
- For example, when fitting for M_A , we use the detector MC to make fake data sets, and modify the fake data sets until the MC matches data
- For example, numbers of events in bins of p_μ , θ_μ
- We obviously don't want to give away the detector MC, but we could provide efficiency functions (including smearing) with systematics and our measured data
- The efficiency function could be applied to inclusive fake data samples, allowing theorists to perform analysis the way we do
- Obviously need to provide neutrino fluxes, too, but we already do that.

Show the whole story

- All neutrino data samples are rife with backgrounds.
 - MiniBooNE: $\text{CCQE} \leftrightarrow \text{CC1}\pi^+ \leftrightarrow \text{CC1}\pi^0 \rightarrow ? \text{NC1}\pi^0$
 - but really: $\mu \leftrightarrow \mu+p \leftrightarrow \mu+\pi^+ \leftrightarrow \mu+\pi^0 \rightarrow ? \pi^0$
 - Knowing what we do (about MEC) from e-A experiments, we cannot have confidence in one sample without seeing all the others.
 - We've already learned that seeing them all isn't enough!
-
- For example, to extract M_A from neutrino data:
 - Requires nuclear model & background predictions match Nature.
 - Predicated on assumption that F_A is a dipole.

Crazy idea 1

- Experimentalists use *uncorrected* data to perform parameters fits.
- We use detector MC to naturally handle efficiencies and smearing,
 - by comparing smeared MC samples after cuts to data after cuts.
- We use MC samples/reweighting techniques to adjust MC until it matches data.
- Why not publish uncorrected data along with appropriate smearing and efficiency functions?
- Turn detector MC into a lookup table.

Crazy idea 2

- Apply efficiency/smearing corrections to individual events.
 - Publish an ntuple of events: reconstructed final state particles.
 - Each event comes with a cross-section weight derived with POT numbers, flux & detector MC.
 - Allows one to make a plot giving cross sections instead of number of events.
- ➡ Gives unprecedented knowledge to future analysers since it would allow analysis of new variables

Summary

- Measuring cross sections is a tricky business
- We need to learn our own lessons!
 - When we use external data sets to constrain cross section models, we ought to take note of what works and what doesn't
 - See Callum Wilkinson's talk for that
 - And we need to remember not to inflict the same problems on the people using our own measurements
- The world has lots of good data analysis ideas
 - This workshop is a good chance to learn some!

Thank you!

ありがとうございました！