



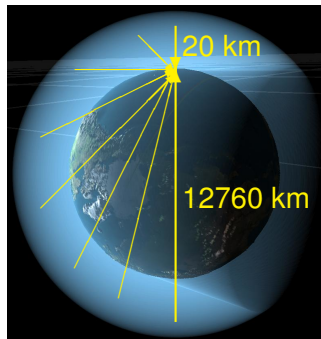
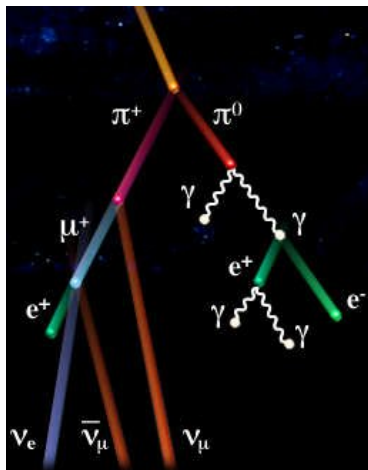
Atmospheric Neutrinos

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31 May 2016

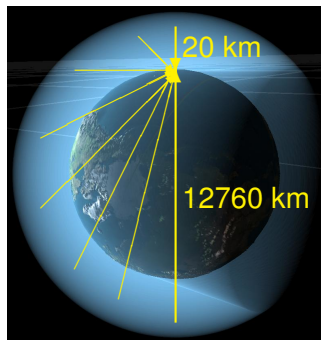
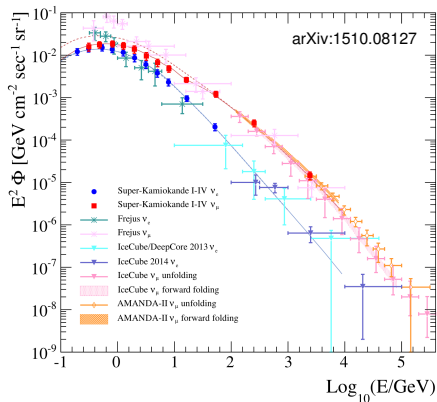
Atmospheric neutrinos



- 2:1 ratio between $\nu_\mu:\nu_e$
- similar rate of ν and $\bar{\nu}$
 - ▶ however, x-sec for $\bar{\nu}$ half of ν

- various baselines (L) available

Atmospheric neutrinos

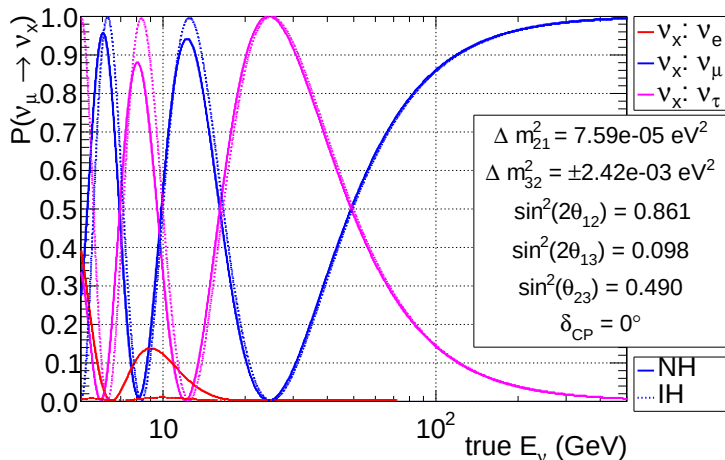


- ν energy over several orders of magnitude

- various baselines (L) available

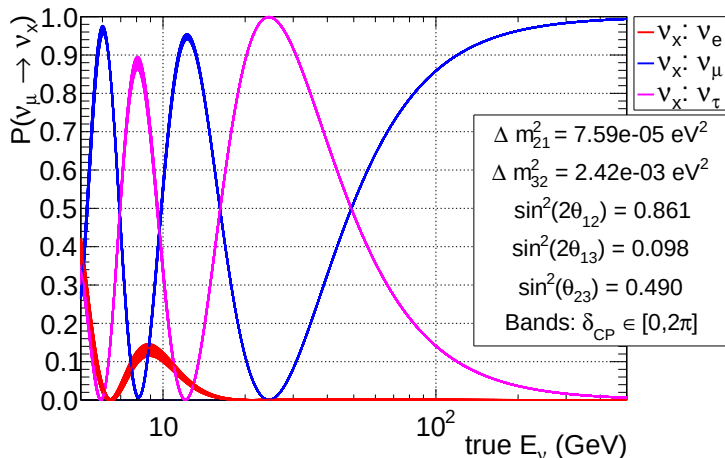
⇒ wide range of L/E available for ν oscillation measurements

Atmospheric neutrino oscillations



- Longest baseline ($L=12760 \text{ km}$, $\cos \theta_z = -1$) has:
 - ▶ First oscillation maxima at $\sim 25 \text{ GeV}$
 - ▶ Matter effects below $\sim 12 \text{ GeV}$
 - ▶ Potential for ν_e appearance at 8 GeV

Atmospheric neutrinos oscillations

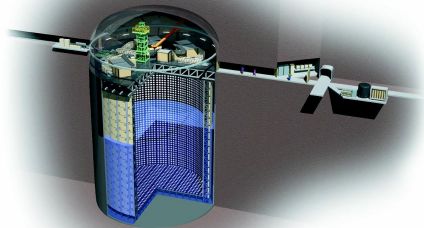


- Largest baseline ($L=12760 \text{ km}$, $\cos \theta_z = -1$) has:

- ▶ First oscillation maxima at $\sim 25 \text{ GeV}$
- ▶ δ_{CP} below $\sim 12 \text{ GeV}$
 - ★ but matter effects dominate that region
- ▶ Potential for ν_e appearance at 8 GeV

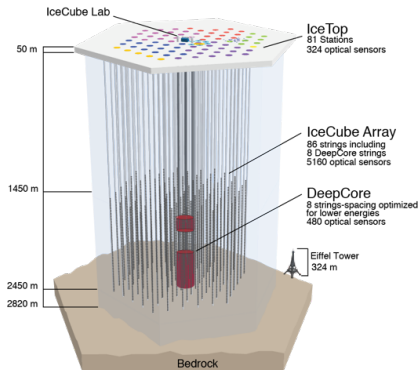
Current experiments

Super-Kamiokande



- Inner detector: 11129 PMTs
- Fiducial volume: 22.5 ktons
- Operation started in Apr. 1996

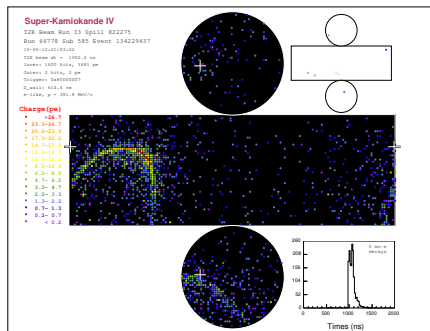
IceCube-DeepCore



- In ice: 5160 PMTs
- Sparse array: ~ 1 Gton
- Denser OM volume: ~ 6 Mtons
- Full detector: May. 2011

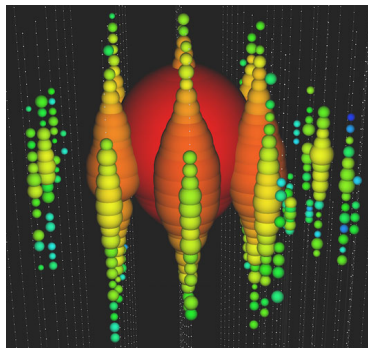
Current experiments – event displays

Super-Kamiokande



- Cherenkov rings projected in wall

IceCube-DeepCore

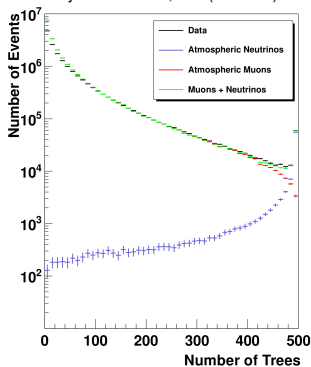


- “3D view”
- This is a high-energy event (2 PeV)
- Low-energy events (very) scaled down version of this
- Lu Lu will talk about high(er) energies

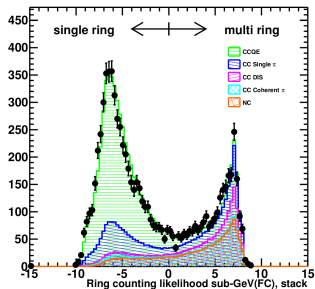
Event selection techniques

- Cuts on “raw” variables
- Combination of techniques used for “complicated” cases:
 - ▶ Likelihood calculations
 - ▶ Decision Trees
 - ▶ Neural Networks
 - ▶ . . .

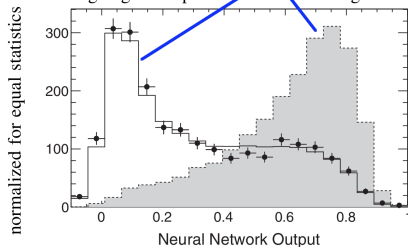
Eur.Phys.J. C75 no.3, 116 (IceCube)



Super Kamiokande I 1489.2 days



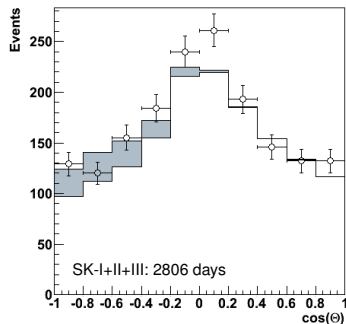
Phys.Rev.Lett. 110, 181802 (Super Kamiokande)
downward-going atmospheric τ signal MC



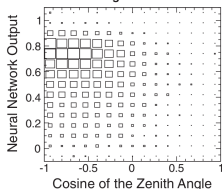
Statistical measurement of ν_τ appearance by SK

published in Phys.Rev.Lett. 110, 181802 (2013)

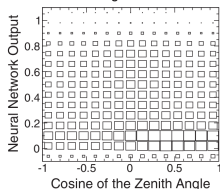
Zenith Distribution



Signal PDF



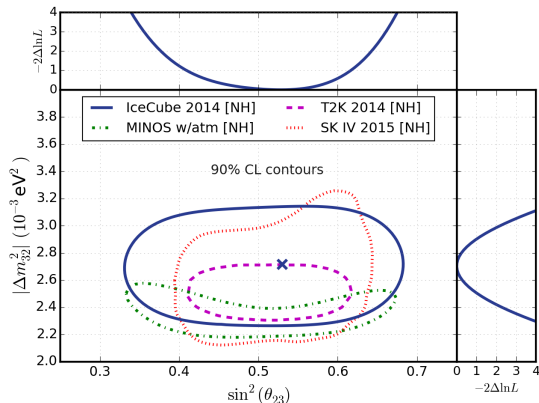
Background PDF



- Search for hadronic decays of τ in SK
- Cannot distinguish ν_τ CC individually
 - ▶ Use NN to help classification
 - ▶ Statistical measure of ν_τ appearance
- Measured ν_τ normalization 1.42 ± 0.35 (stat)
 - ▶ 3-flavour oscillation exp: 1
 - ▶ if no ν_τ appearance: 0
- 3.8σ rejection of no- ν_τ appearance

“Atmospheric mixing” parameters by IceCube and SK

IceCube: Phys.Rev. D 91, 072004 (2015); SK: AIP Conf. Proc. 1666, 100001 (2015)



- In both cases contours obtained using Wilk's theorem
 - ▶ Calculate $\Delta\ln L = \ln L - \ln L_{\text{bestfit}}$ for all points in 2D parameter space
 - ▶ $\Delta\ln L$ calculated by maximizing L over nuisance parameters
 - ▶ $-2\Delta\ln L$ is asymptotically a χ^2 distribution with 2 dof.
- Side plots: slice of $\Delta\ln L$ passing through best-fit

- IceCube: fitting to data done in 2D space (E, θ_z)
 - ▶ $\chi^2/\text{ndf} = 54.9/56$
- Super-Kamiokande: fitting done with several samples ($E, \text{PID}, \dots$) along θ_z
 - ▶ $\chi^2/\text{ndf} = 560/517$

Historical view on measuring the mixing

Looking back at the Phys.Rev.Lett. 81 (1998) 1562-1567

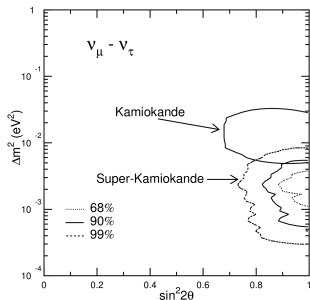


FIG. 2. The 68%, 90% and 99% confidence intervals are shown for $\sin^2 2\theta$ and Δm^2 for $\nu_\mu \leftrightarrow \nu_\tau$ two-neutrino oscillations based on 33.0 kiloton-years of Super-Kamiokande data. The 90% confidence interval obtained by the Kamiokande experiment is also shown.

rors. The global minimum occurred slightly outside the physical region at ($\sin^2 2\theta = 1.05$, $\Delta m^2 = 2.2 \times 10^{-3}$ eV², $\chi^2_{\min} = 64.8/67$ DOF). The contours of the 68%, 90% and 99% confidence intervals are located at $\chi^2_{\min} + 2.6, 5.0$, and 9.6 based on the minimum inside the physical region [19]. These contours are shown in Fig. 2. The region near χ^2 minimum is rather flat and has many local minima so that inside the 68% interval the best-fit Δm^2 is not well constrained. Outside the 99% allowed region the χ^2 increases rapidly. We obtained $\chi^2 = 135/69$ DOF, when calculated at $\sin^2 2\theta = 0$, $\Delta m^2 = 0$ (i.e. assuming no oscillations).

- As Phillip pointed out yesterday, by changing from $\sin^2 2\theta$ to $\sin^2 \theta$ we “removed” unphysical region
- However current SK contour not symmetric around $\sin^2 \theta = 0.5$
- And matter effects make the formula more complicated. . .

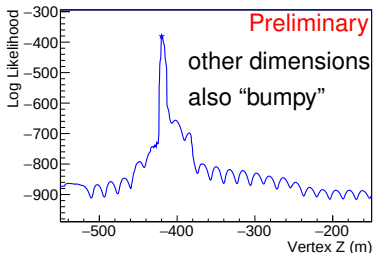
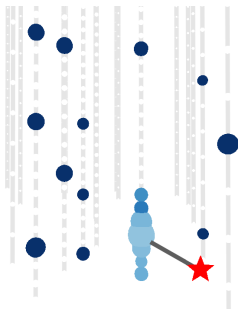
IceCube – towards future analysis

- For result two slide ago analysis focus in ν_μ CC “clean” events
 - ▶ Clear μ tracks
 - ▶ Require several non-scattered γ
 - ▶ Use only up-going events $\Rightarrow$ very small atmospheric μ contamination
 - ▶ Fits analytical formula for Cherenkov light front propagated to PMTs
- Currently working on new analysis based on new reconstruction:
 - ▶ Planning to look at full-sky
 - ★ More atmospheric μ contamination
 - ★ But would give us better handle on flux systematics
 - ▶ Use information from all hits in reconstruction
 - ★ Reconstruction more sensitive to scattering
 - ★ Unfortunately also more sensitive to noise
 - ▶ Increased presence of ν_e , ν_τ and ν NC in sample
 - ▶ And also increase significantly number of ν_μ events at final level
 - ★ significant improvement in final result expected

IceCube – new event reconstruction

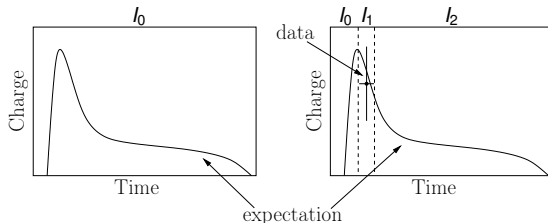
- IceCube measures Cherenkov cones in “3D”
- PMTs embedded in the parameter space creates features in their vicinity
- Natural medium also has local variations
- Low number of hits

→ “bumpy” likelihood space



- Need to fit 8 parameters corresponding to ν_μ DIS interaction
 - ▶ vertex (3), time, direction (2), energies of μ and hadronic cascade
- Usual minimizers do not work well
 - ▶ currently using “MultiNest”

The “event” likelihood space



$$L(D|H) = \prod_{i \in \{PMT\}} \prod_{j=0}^{n_i} \text{Poisson}(\int_{t \in I_j} Q^{obs} dt, \int_{t \in I_j} Q^{exp} dt)$$

- Charge expectation (Q^{exp}) distribution from spline tables
 - ▶ Spline tables account for main local/global ice properties
 - ▶ Derived from simulation
- Idea for the future: replace tables by simulated expectations
 - ▶ For every $L(D|H)$ calculation run simulation to estimate expectation
 - ▶ Can account of more detailed/evolving ice models
 - ▶ However $L(D|H)$ now only defined to given precision. . .
 - ★ Are there recommendations on how to proceed here?

The MultiNest algorithm

See full description in paper by F. Feroz et al. [arXiv:0809.3437 and arXiv:1306.2144]

- MultiNest searches for maximum in multidimensional likelihood space
 - ▶ Exploration of space via ellipsoidal nested sampling
 - ★ New trials thrown in volume defined by ellipsoids obtained from distribution of previous trials → efficient sampling
 - ★ New trials accepted/rejected depending on their LH
 - ★ Posterior distributions provided could be used as error estimates
 - ▶ Natively supports multi-modal distributions
 - ★ In our case important to avoid local minima

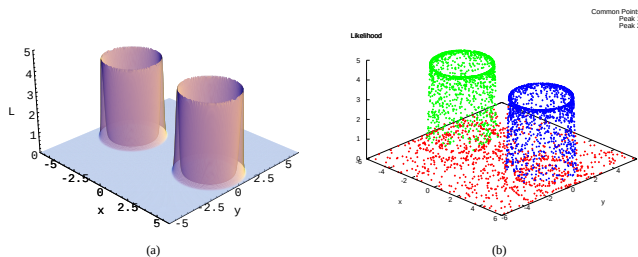
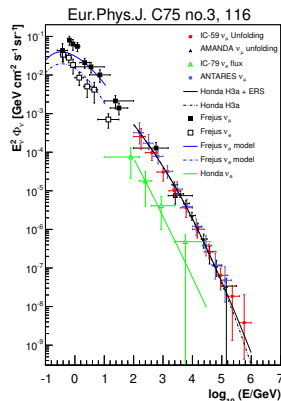
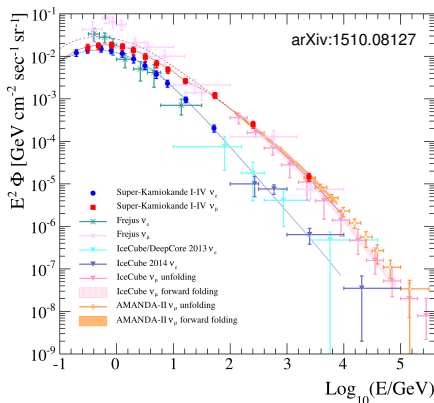


Figure 6. Toy model 2: (a) two-dimensional plot of the likelihood function defined in Eqs. (32) and (33); (b) dots denoting the points with the lowest likelihood at successive iterations of the MULTINEST algorithm. Different colours denote points assigned to different isolated modes as the algorithm progresses.

(Figure extracted from arXiv:0809.3437)

And going back to measuring the ν flux



- While ν flux is input for oscillation analysis, we **also** measure it
- Most common techniques:
 - ▶ Forward folding
 - ★ fit model-parameters $\Rightarrow$ bands accounting for uncertainties
 - ▶ Unfolding
 - ★ model-independent method

Unfolding of the energy spectrum

- The general idea of unfolding is to obtain the true ν energy spectrum ($f(E)$) from the measured data ($g(y)$)
- Those quantities are related by a “response matrix” ($A(y, E)$):

$$g(y) = A(y, E)f(E)$$

- We would like to invert $A(y, E)$ to obtain f from g
 - ▶ However this is an ill defined problem
 - ▶ Even when we can invert A the solution might be unstable
- Different techniques about how to go about doing the unfolding
 - ▶ For invertible A , add regularisation terms to avoid instability
 - ★ Regularization term corresponds to a priori information about smoothness of true solution
 - ★ Could introduce bias in solution, weight of “regularization” needs to be determined so bias smaller than statistical errors
 - ▶ “Bayesian Unfolding”

“Bayesian Unfolding”

notation from Nucl.Instrum.Meth. A362 (1995) 487-498

- Goal: Identify the “causes” (C_i) that produced the observable effects (E_j)
- Starting point: Bayes theorem

$$P(C_i|E_j) = \frac{P(E_j|C_i)P(C_i)}{P(E_j)} = \frac{P(E_j|C_i)P(C_i)}{\sum_l P(E_j|C_l)P(C_l)}$$

- Number of events from C_i ($\hat{n}(C_i)$) given the number of events in E ($n(E_j)$)

$$\hat{n}(C_i) = \frac{1}{\epsilon_i} \sum_j n(E_j)P(C_i|E_j) = \sum_j M_{ij}n(E_j), \quad \epsilon_i \neq 0$$

($\epsilon_i = \sum_j P(C_i|E_j)$ is efficiency of detecting C_i and M_{ij} is unfolding matrix)

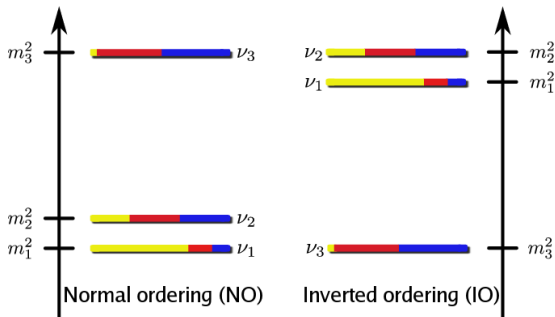
- Unfolding process:

- ① Choose initial $P_0(C)$, can be uniform
- ② Calculate $\hat{n}(C)$ and $\hat{P}(C) = P(C|n(E))$
- ③ Compare $\hat{n}(C)$ and $n_0(C) = P_0(C)N_{obs}$
- ④ Replace P_0, n_0 with $\hat{P}, \hat{n}$ and start over at ② until converged
 - ★ $\hat{P}$ can be smoothened to avoid “overfitting”
 - ★ Uncertainties calculated after final M_{ij} and $n(E_j)$

- Note [from R. Cousins]: this is not truly a Bayesian technique

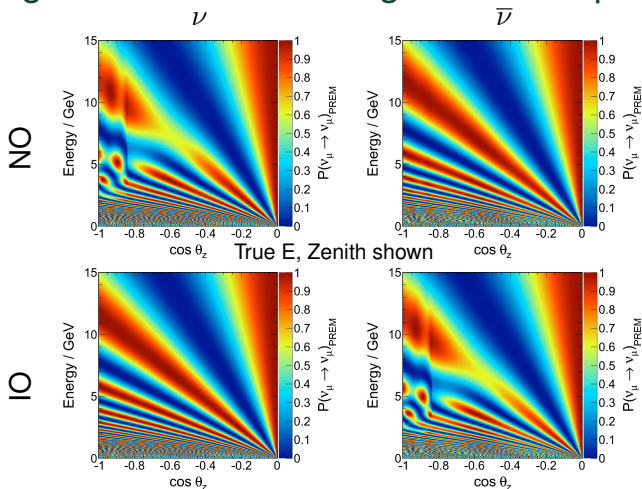
► Also called: “Expectation Maximization” or “Lucy-Richardson”

Measuring the ν Mass Ordering with atmospheric ν (future experiments)



- Figures shown for PINGU, but ORCA very similar
 - ▶ Also talk about “The KM3NeT/ORCA detector” tomorrow by Ronald Bruijn
- Most discussion would **also** apply to other experiments trying to measure the ν Mass Ordering (NMO)

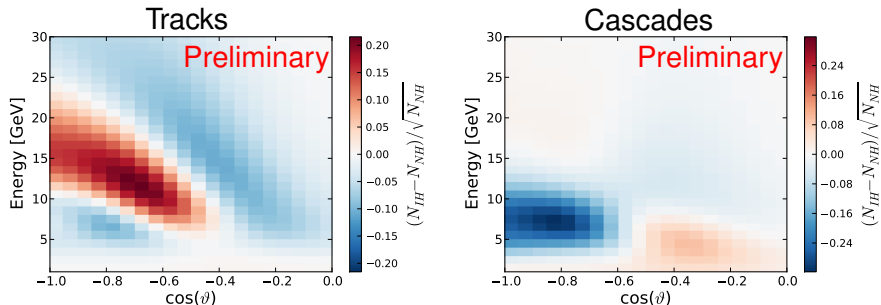
Measuring the ν Mass Ordering with atmospheric ν



- Different oscillation probabilities for ν and $\bar{\nu}$ for NO and IO
- Measure combined $\nu + \bar{\nu}$
 - ▶ different cross-section $\Rightarrow$ effect doesn't vanish
- NB: India-based Neutrino Observatory able to distinguish ν and $\bar{\nu}$

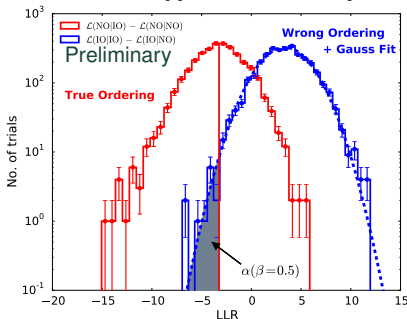
Bin-by-bin significance of mass hierarchy signature

Assuming no ν vs $\bar{\nu}$ identification, such as for PINGU



- Distinct hierarchy dependent signatures for tracks (mostly ν_{μ} CC) and cascades (mostly ν_e CC)
 - ▶ Intensity is statistical significance of each bin with 1 year data
 - ▶ Measurement is possible “statistically” by combining all bins – there is not one bin that would achieve that
 - ▶ Particular expected “distortion pattern” helps mitigate impact of systematics

Estimating sensitivity to the NMO: Log Likelihood Ratio



- 1 Generate pseudo-data trial in analysis binning
 - True physics and systematics kept fixed for generation
- 2 Fit assuming NO and IO
- 3 Calculate log likelihood ratio between IO and NO

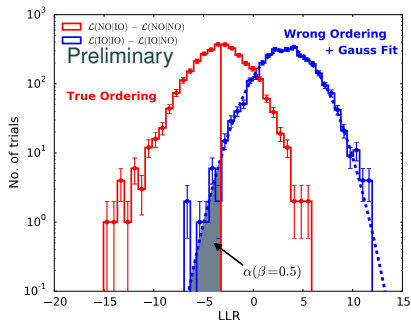
Advantages of the method:

- Can account for any systematic given
- Does not pre-suppose shape of ΔLLH distribution

Disadvantages of the method:

- The significance “limited” by number of trials
 - ★ If Gaussian can provide approximate significances
- Since each trial is a full fit (and given lots of trials needed) having large number of systematics can become prohibitively time consuming

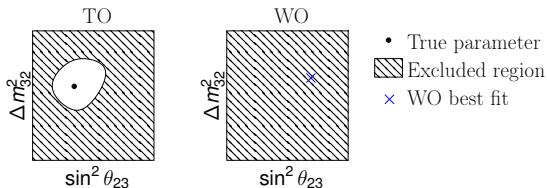
Median sensitivity



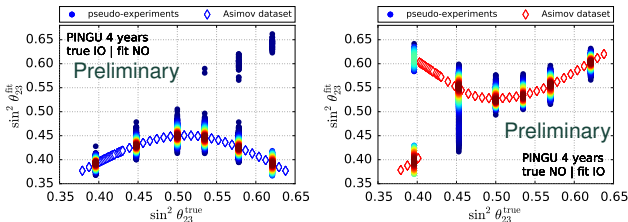
- For quantifying significance to measure ordering usually use median sensitivity
 - ▶ Widely used in literature
- “Median sensitivity” will mean that 50% of the time we can do better and 50% of the time we can do worse
- “Median sensitivity” calculated by integrating shade region under wrong ordering assumption
 - ▶ If distribution fits well Gaussian, integrate area under Gaussian curve instead of trial distribution

Excluding an ordering

- To say we measure the true ordering (TO) at a given CL we want to be able to exclude the wrong ordering (WO) for any value of the oscillation parameters



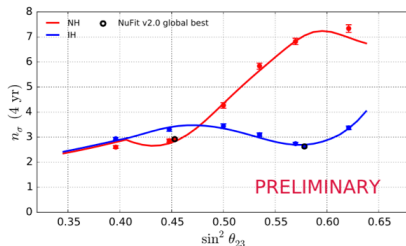
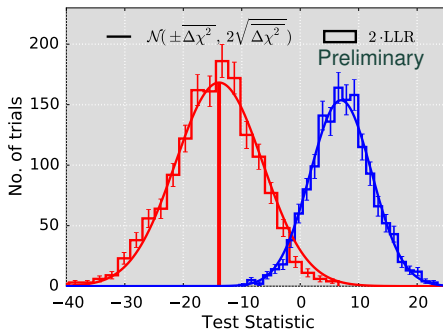
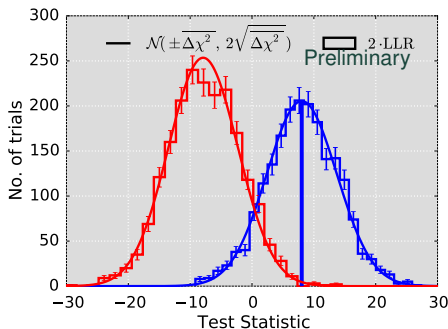
- Testing every point of the WO parameter space too costly
 - WO best-fit gives parameters of “maximum confusion” (used to get WO trial distribution)



Estimating sensitivity to the NMO: $\Delta\chi^2$ method

- ❶ Get expected number of events in analysis binning
 - ▶ True physics and systematics kept fixed as in LLR method
 - ▶ But, no Poisson fluctuations applied
 - ❷ Calculate minimal $\overline{\Delta\chi^2}$ for the WO
 - ▶ $\overline{\Delta\chi^2} = \min_{p \in WO} \sum_i \left(\frac{\mu_i^{TO}(p_0) - \mu_i^{WO}(p)}{\sigma_i} \right)^2$
 - ▶ $\Delta\chi^2$ is Gaussian distributed with mean $\pm \overline{\Delta\chi^2}$ and sigma $2\sqrt{\overline{\Delta\chi^2}}$
 - ❸ Evaluate distribution of $\Delta\chi^2$ for NO and IO
⇒ correspond to the LLR trial distribution
- Advantages of the method:
 - ▶ Linear systematics are extremely fast to be computed
 - ▶ Even with non-linear systematics still much faster than LLR
 - Disadvantage of the method:
 - ▶ Intrinsic assumption of gaussianity of final distribution
 - ▶ Not possible to include non-centered priors
 - ★ cannot include prior on θ_{23} due to “maximum confusion” method

Comparing Test Statistic of LLR and $\Delta\chi^2$



- Good agreement between TS
- ⇒ sensitivities in agreement
 - ▶ lines from $\Delta\chi^2$
 - ▶ points from LLR

Summary

- Various different techniques used for event selection and reconstruction
 - ▶ likelihood, decision trees, neural networks
 - ▶ sometimes different tools used as minimizers:
 - ★ MultiNest used to avoid local-minima by exploring L space
- Measurements using very different statistical techniques
 - ▶ Statistically evaluate presence of components in sample
 - ▶ From $-2\Delta\ln L$ obtain contours via Wilks theorem
 - ▶ LogLikelihood Ratio, $\Delta\chi^2$ to distinguish between hypothesis
 - ▶ Forward folding and Unfolding of ν spectra
- All these techniques used with main (physics) goal of
 - ▶ measuring ν oscillations
 - ▶ measuring the ν spectra

Backup slides

More plots from MultiNest

From arXiv:0809.3437

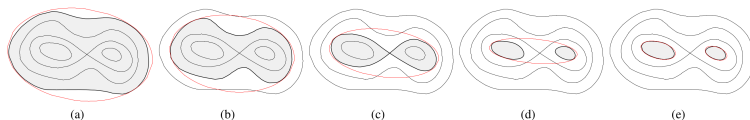


Figure 2. Cartoon of ellipsoidal nested sampling from a simple bimodal distribution. In (a) we see that the ellipsoid represents a good bound to the active region. In (b)-(d), as we nest inward we can see that the acceptance rate will rapidly decrease as the bound steadily worsens. Figure (e) illustrates the increase in efficiency obtained by sampling from each clustered region separately.

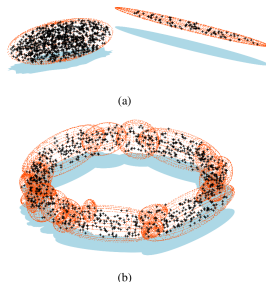


Figure 3. Illustrations of the ellipsoidal decompositions returned by Algorithm 1: the points given as input are overlaid on the resulting ellipsoids. 1000 points were sampled uniformly from: (a) two non-intersecting ellipsoids; and (b) a torus.

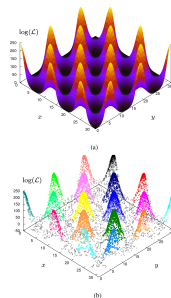


Figure 5. Toy model 1: (a) two-dimensional plot of the likelihood function defined in Eq. 31; (b) dots denoting the points with the lowest likelihood, at successive iterations of the MULTINEST algorithm. Different colours denote points assigned to different isolated modes as the algorithm progresses.

- Interesting resources:

- ▶ Presentation on unfolding in HEP: http://mkuusela.web.cern.ch/mkuusela/ETH_workshop_July_2014/slides.pdf
- ▶ V. Blobel, “Unfolding Methods in High-energy Physics Experiments” at <https://cds.cern.ch/record/157405?ln=en>
- ▶ D’Agostini, Nucl.Instrum.Meth. A362 (1995) 487-498

Unfolding instability example

From V. Blobel, “Unfolding Methods in High-energy Physics Experiments”

Example: Unfolding of a distribution of a discrete variable. The case $n = m = 20$ is assumed, with the following response matrix:

$$A = \begin{pmatrix} 0.75 & 0.25 & 0 & & \\ 0.25 & 0.50 & 0.25 & 0 & \\ 0 & 0.25 & 0.50 & 0.25 & 0 \\ & 0 & 0.25 & 0.50 & 0.25 \\ & & 0 & 0.25 & 0.50 \\ & & & \ddots & \ddots \end{pmatrix}$$

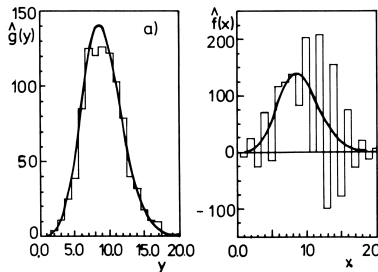


Figure 1. Distribution of the measured quantity y (a) and oscillating result of unfolding (b) using equation (1.05), shown as histograms. The original dependence is shown as a curve in both cases.

Unfolding with regularization

From V. Blobel, “Unfolding Methods in High-energy Physics Experiments”

Input pdf and data

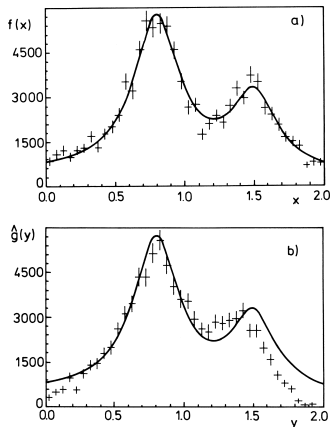


Figure 8. Histogram of the generated data (a) before and (b) after simulation of acceptance, transformation and resolution. The original function is shown as curve.

Unfolding result

- Using B-splines for regularization

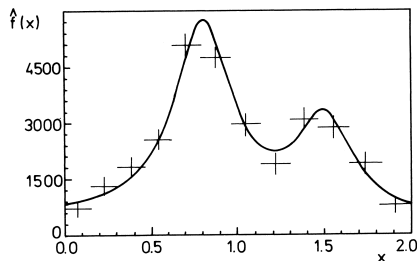


Figure 11. Result of unfolding with regularization, shown as data points together with the original function. The horizontal bar gives the range, over which the data points represents the average.

“Bayesian Unfolding” example

from Nucl.Instrum.Meth. A362 (1995) 487-498

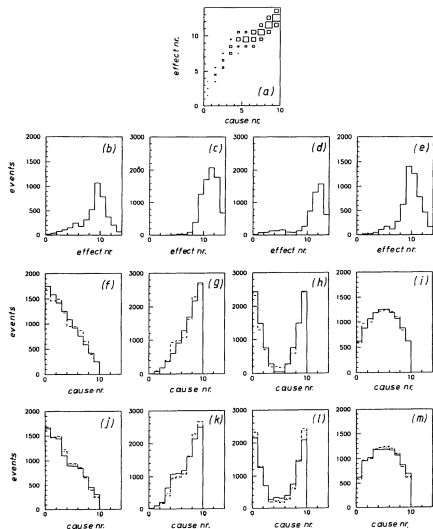


Fig. 1. (a) Visualization of the smearing matrix S_{ij} (see text): in the abscissa and the ordinate are the true and the measured quantities, respectively; the box area is proportional to the migration probability. (b-e) Smearing distributions of f_{1-4} (see text) obtained from 10000 generated events. (f-l) True distributions of f_{1-4} (solid lines) compared with the results of a 3-step unfolding (dashed lines). (j-m) Unfolded distributions after the first, second and third step (solid, dotted and dashed lines) of f_{1-4} .

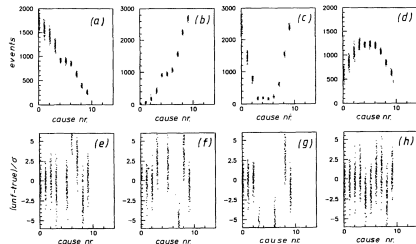


Fig. 4. Results obtained by a 3-step unfolding of 100 independent data sets, each based on 10000 generated true events smeared with S_{ij} : (a-d) distribution on the unfolded numbers for true distributions f_{1-4} ; (e-h) distribution of the difference between the unfolded and the true numbers, divided by the estimated standard deviation, for true distributions f_{1-4} .

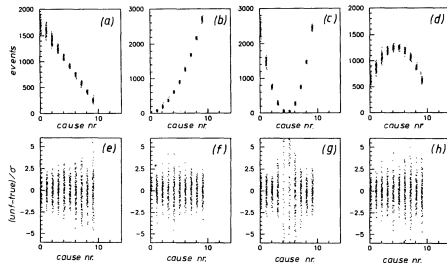


Fig. 8. Same as Fig. 4, but with a 20-step unfolding and smoothing the probability distribution between the steps.